

CONSTRAINING COSMIC ACCELERATION (AND GRAVITY ON COSMIC SCALES)

NICO HAMAUS

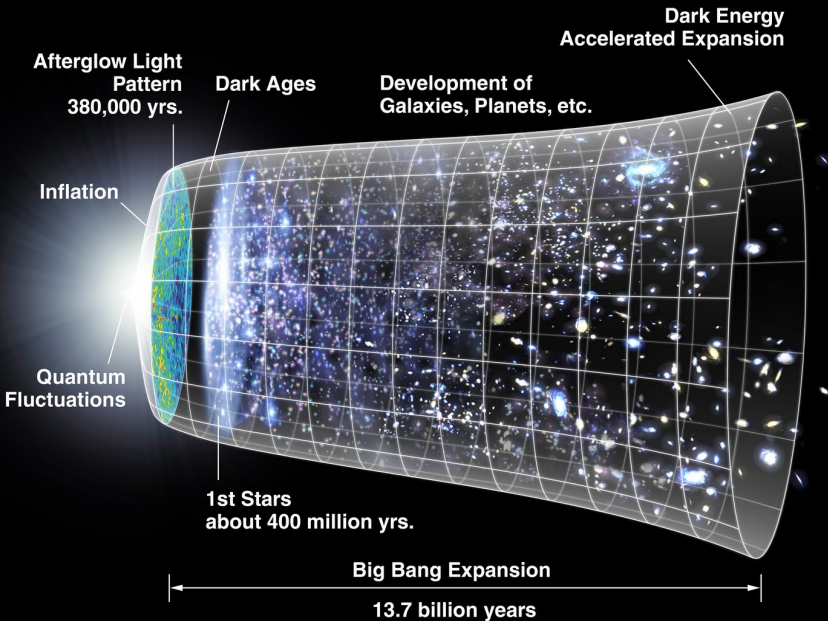
in collaboration with

**ALICE PISANI, PAUL SUTTER,
GUILHEM LAVAUX, BENJAMIN WANDEL,
STÉPHANIE ESCOFFIER, GIORGIA POLLINA,
BEN HOYLE, JOCHEN WELLER**



- 1 Introduction
- 2 Supernovae
- 3 Cosmic Microwave Background
- 4 Large-Scale Structure
- 5 Cosmic Voids
- 6 Conclusions

STANDARD MODEL OF COSMOLOGY



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Galaxies trace the expansion of cosmic spacetime, described by

FLRW-metric

$$ds^2 = c^2 dt^2 - a^2(t) \left(\frac{dr^2}{1 - kr^2} + r^2 d\Omega^2 \right)$$

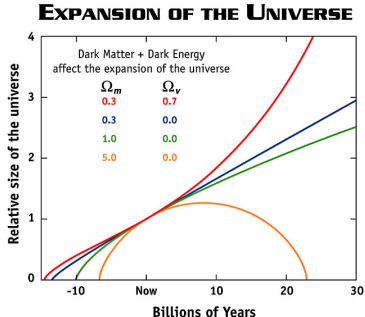
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Observational evidence for $\ddot{a} > 0 \Rightarrow \Lambda$ CDM



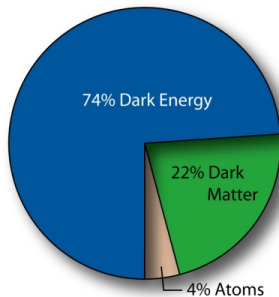
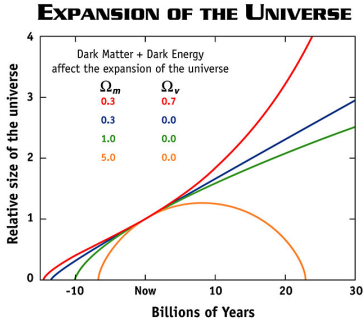
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Friedman Equations

$$\begin{aligned}\dot{a}/a \equiv H &= H_0 \sqrt{\Omega_{r,0} a^{-4} + \Omega_{m,0} a^{-3} + \Omega_{k,0} a^{-2} + \Omega_{\Lambda,0}} \\ -\ddot{a}/\dot{a}^2 \equiv q &= 1/2 \sum \Omega_i (1 + 3w_i), \quad w_i = p_i/\rho_i\end{aligned}$$

Components of the Universe: $\Omega_i = \rho_i/\rho_{\text{crit}}$ with $\sum \Omega_i + \Omega_k = 1$

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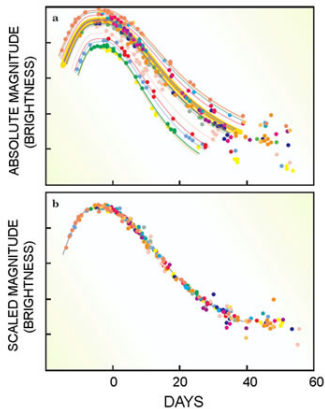
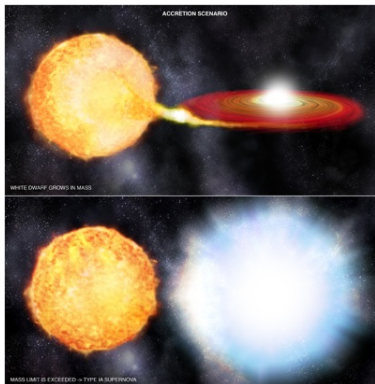
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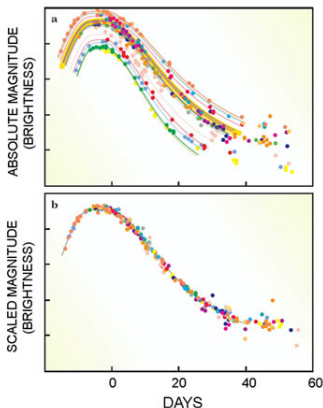
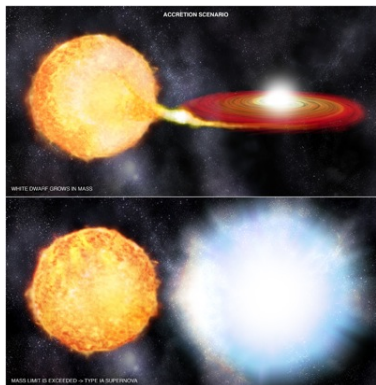
Equation of state:

- Radiation $w_r = 1/3$
- Matter $w_m = 0$
- Curvature $w_k = -1/3$
- Cosmological constant $w_\Lambda = -1$

SUPERNOVAE AS STANDARD CANDLES



SUPERNOVAE AS STANDARD CANDLES



Luminosity Distance

$$\sqrt{L/4\pi F} \equiv D_L(z) = \frac{(1+z)c}{H_0\sqrt{-\Omega_{k,0}}} \sin\left(H_0\sqrt{-\Omega_{k,0}} \int_0^z \frac{1}{H(z')} dz'\right)$$

Redshifts $z = 1/a - 1$ from spectra of host galaxies

SUPERNOVAE AS STANDARD CANDLES

Distance Modulus: apparent vs. absolute magnitude

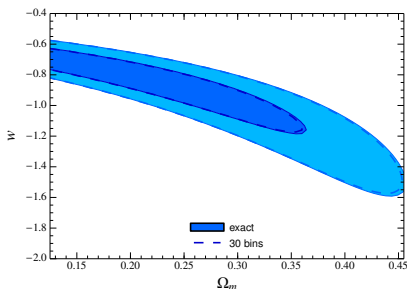
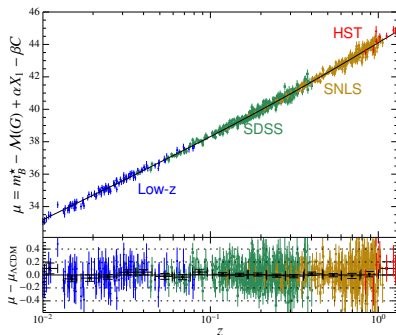
$$\begin{aligned}\mu &\equiv m(F) - M(L) = 5 \log_{10} \left(\frac{D_L(z)}{\text{Mpc}} \right) + 25 \\ &\simeq 43.17 + 5 \log_{10} z + 1.086(1 - q_0)z - 5 \log_{10} \left(\frac{H_0}{70 \text{ km/s/Mpc}} \right)\end{aligned}$$

SUPERNOVAE AS STANDARD CANDLES

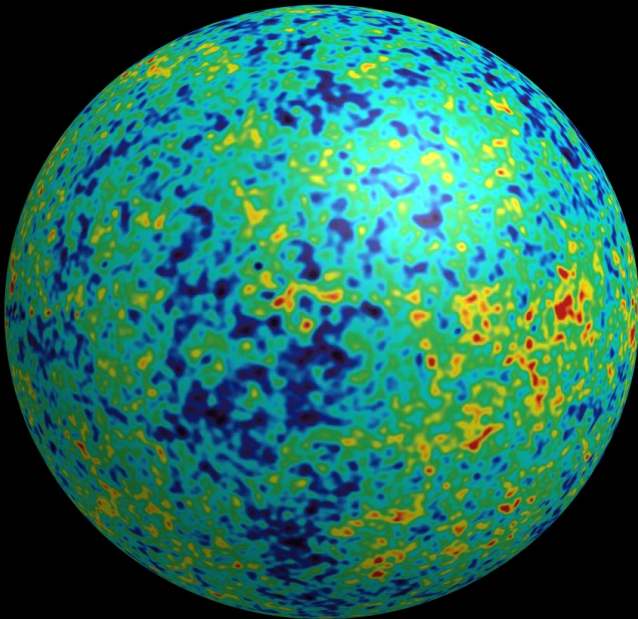
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CMB AS STANDARD RULER



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Baryon acoustic oscillations (BAO) due to sound horizon $r_s \simeq 150$ Mpc of primordial plasma at $z \sim 1100$ with apparent angular size $\theta_s \simeq 1^\circ$

Angular Diameter Distance

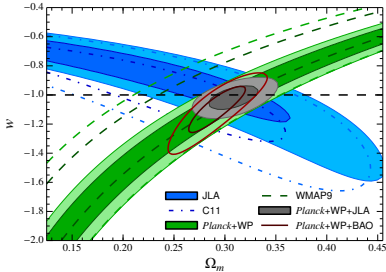
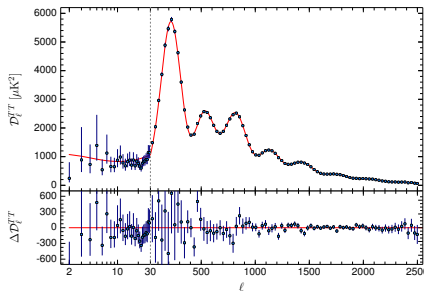
$$r_s/\theta_s \equiv D_A(z) = \frac{c}{(1+z)H_0\sqrt{-\Omega_{k,0}}} \sin \left(H_0\sqrt{-\Omega_{k,0}} \int_0^z \frac{1}{H(z')} dz' \right)$$

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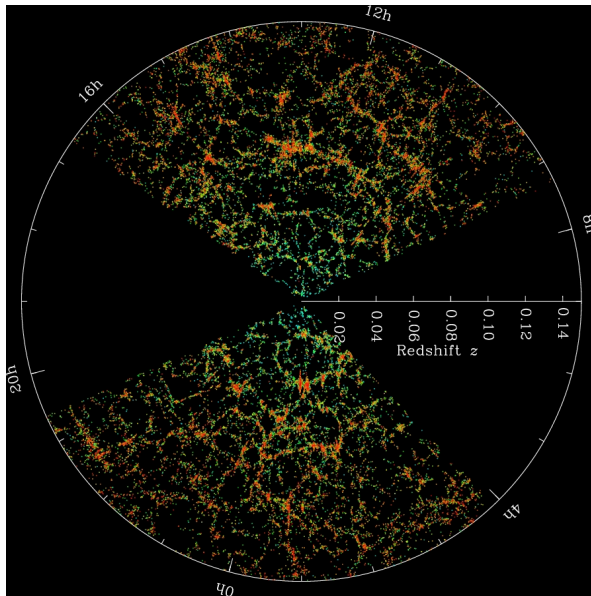
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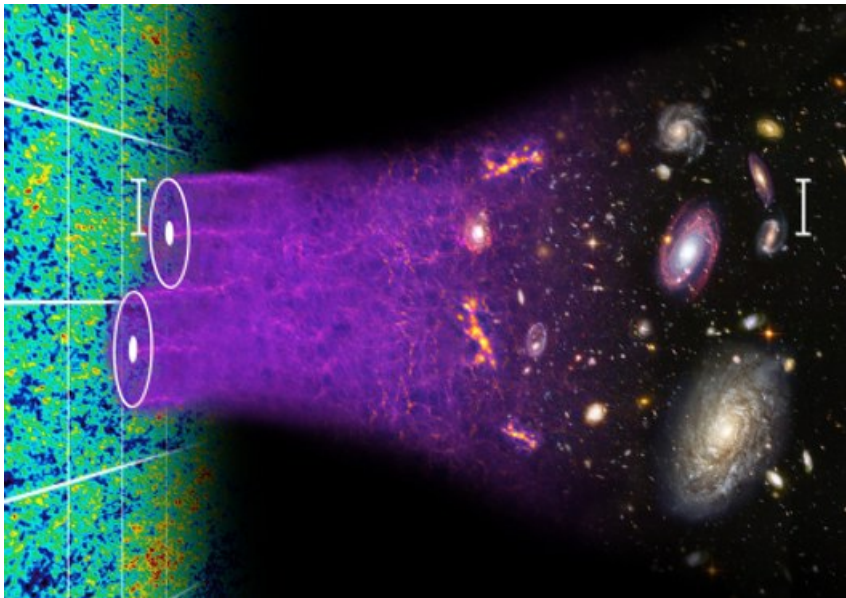
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LARGE-SCALE STRUCTURE (LSS)

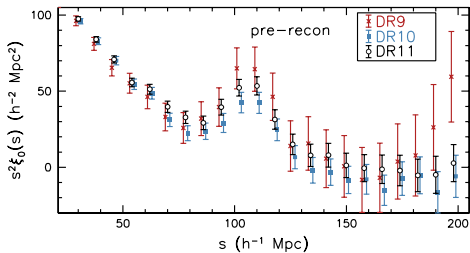
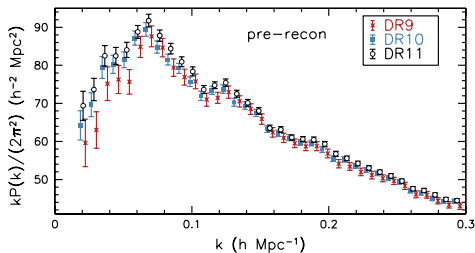


LSS AS STANDARD RULER



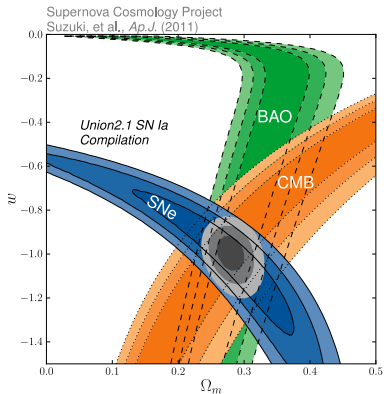
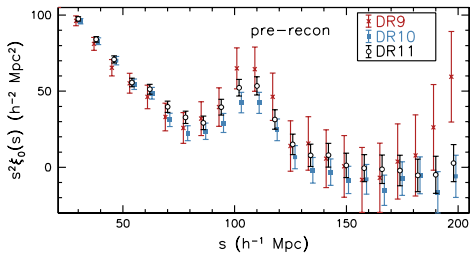
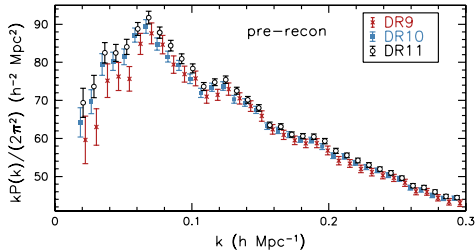
LSS AS STANDARD RULER

Anderson et al. 2014



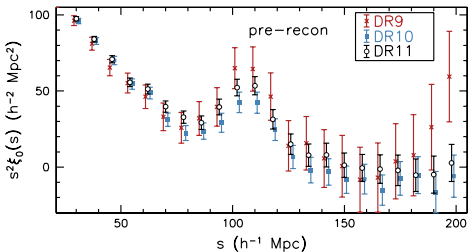
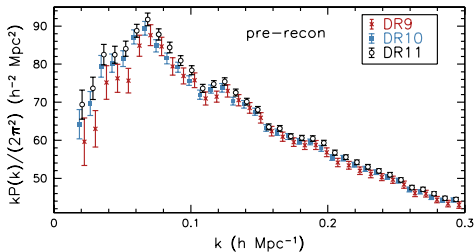
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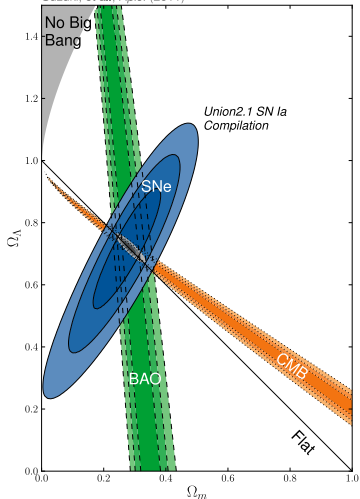


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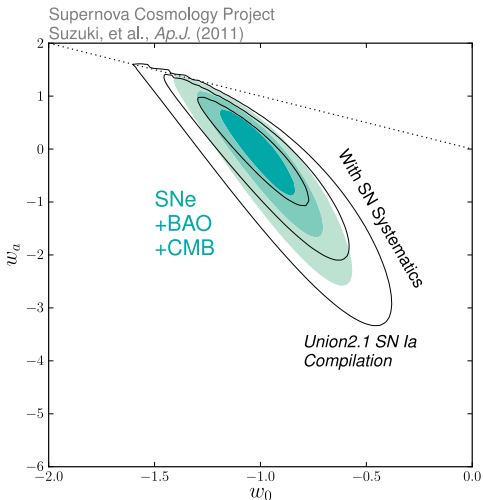


Supernova Cosmology Project
Suzuki, et al., *Ap.J.* (2011)

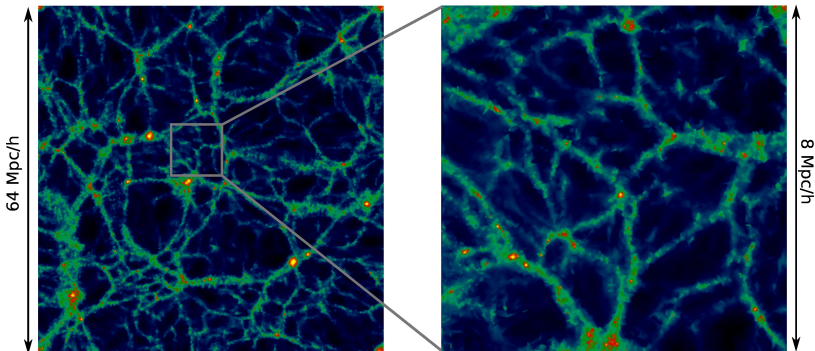


LSS AS STANDARD RULER

Evolution of dark energy: $w(z) = w_0 + w_a \frac{z}{1+z}$

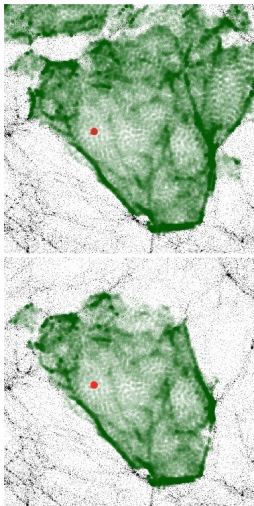


THE COSMIC WEB

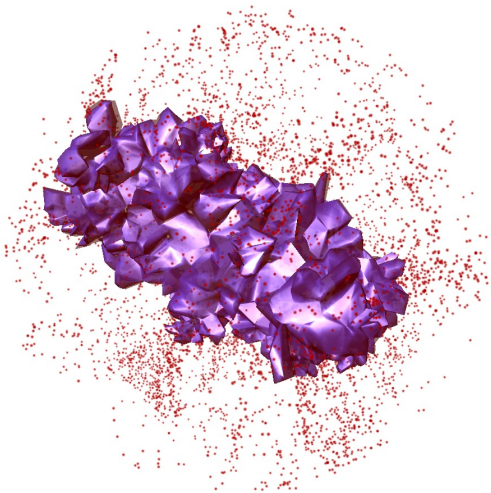


Aragon-Calvo, Szalay (2013)

COSMIC VOIDS AS STANDARD SPHERES

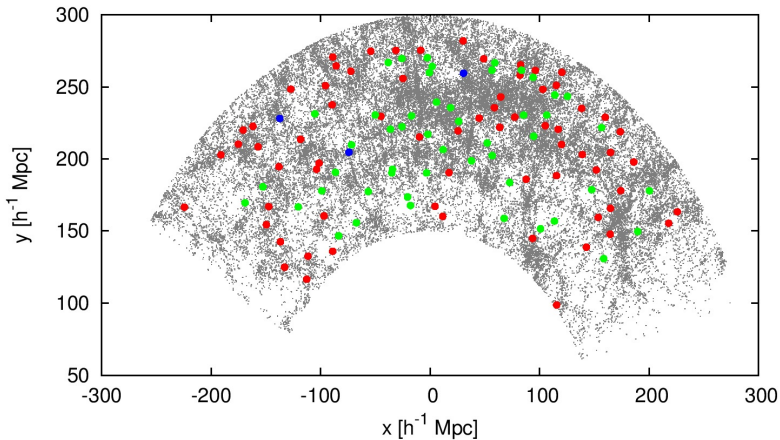


Neyrinck (2008)



Sutter, Lavaux, Wandelt, Weinberg (2012)

OBSERVED COSMIC VOIDS (SDSS)



$R = 5-15 h^{-1} \text{ Mpc}$
 $R = 15-25 h^{-1} \text{ Mpc}$

●

$R = 25-45 h^{-1} \text{ Mpc}$

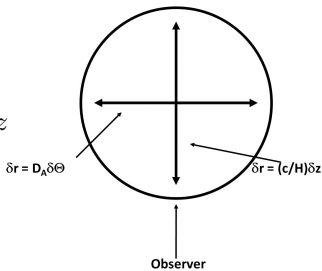
●

Sutter et al. (2012)

ALCOCK-PACZYNSKI TEST

Perform *Alcock-Paczynski test* to constrain cosmological parameters:

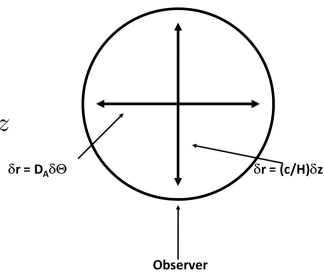
- Angular separation $\delta r_{\perp} = D_A(z) \delta\theta$
- Radial separation $\delta r_{\parallel} = cH^{-1}(z) \delta z$



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- Angular separation $\delta r_{\perp} = D_A(z) \delta\theta$
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Any deviation from the fiducial cosmology causes geometric distortions. \Rightarrow
Determine **ellipticity** ϵ via

$$\epsilon = \frac{\delta r_{\parallel}}{\delta r_{\perp}} = \frac{D_A^{\text{true}}(z) H^{\text{true}}(z)}{D_A^{\text{fid}}(z) H^{\text{fid}}(z)}$$

COSMIC VOIDS IN REDSHIFT SPACE

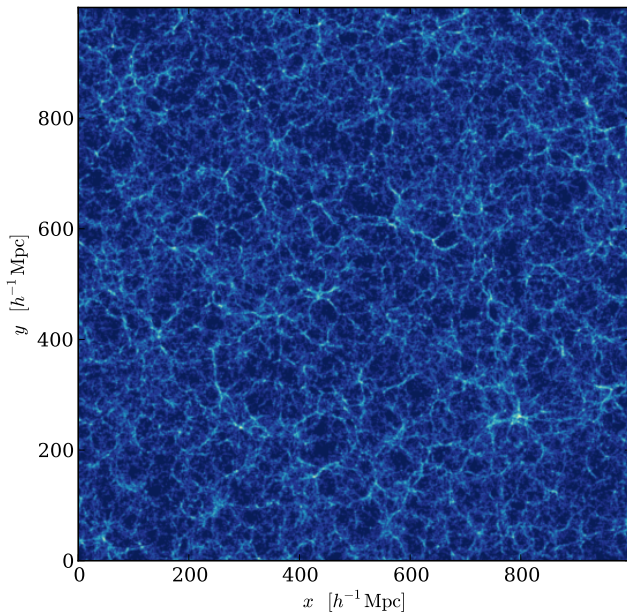
Peculiar motions of galaxies cause **redshift-space distortions**:

$$\tilde{\mathbf{r}} = \mathbf{r} + \mathbf{v}_{\parallel} H^{-1}(z)$$

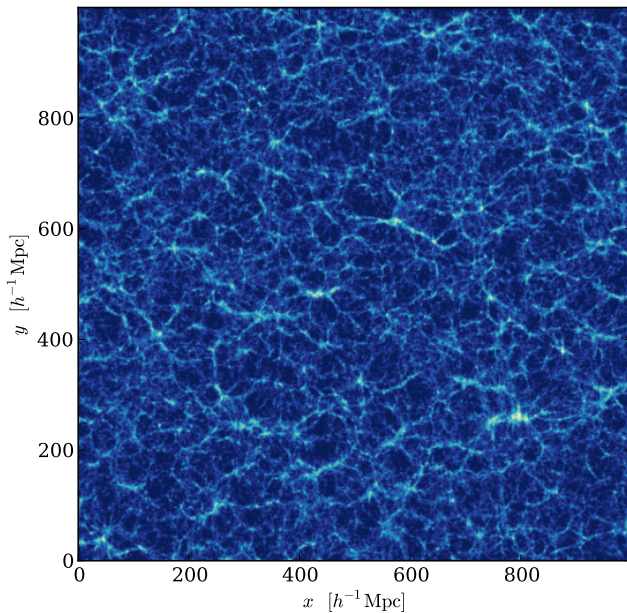
- ➡ \perp to line of sight:
Pancakes of God from linear growth
- ➡ \parallel to line of sight: *Fingers of God* from nonlinear collapse
- ➡ Galaxy correlation function no longer isotropic, what about voids?

Melott et al. (1998)

COSMIC VOIDS IN REDSHIFT SPACE



COSMIC VOIDS IN REDSHIFT SPACE



MODEL

Void-galaxy cross-correlation function in redshift space:

$$1 + \tilde{\xi}_{\text{vg}}(\tilde{\mathbf{r}}) = \int \mathcal{P}(\mathbf{v}, \mathbf{r}) [1 + \xi_{\text{vg}}(\mathbf{r})] d^3v = \int_{-\infty}^{\infty} \mathcal{P}(v_{\parallel}, \mathbf{r}) \frac{\rho_{\text{v}}(r)}{\bar{\rho}} dv_{\parallel}$$

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$$\mathcal{P}(v_{\parallel}, \mathbf{r}) = \frac{1}{\sqrt{2\pi}\sigma_v(\mathbf{r})} \exp\left[-\frac{(v_{\parallel} - v_{\text{v}}(r) \frac{r_{\parallel}}{r})^2}{2\sigma_v^2(\mathbf{r})}\right]$$

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$$\frac{\rho_{\text{v}}(r)}{\bar{\rho}} - 1 = b\delta_c \frac{1 - (r/r_s)^\alpha}{1 + (r/r_{\text{v}})^\beta}, \quad r_{\text{v}} \equiv (3V_{\text{v}}/4\pi)^{1/3}$$

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$$v_{\text{v}}(r) = -\frac{1}{3} \frac{f(z)H(z)}{1+z} r \Delta_{\text{v}}(r), \quad \Delta_{\text{v}}(r) \equiv \frac{3}{r^3} \int_0^r \left(\frac{\rho_{\text{v}}(s)}{\bar{\rho}} - 1 \right) s^2 ds$$

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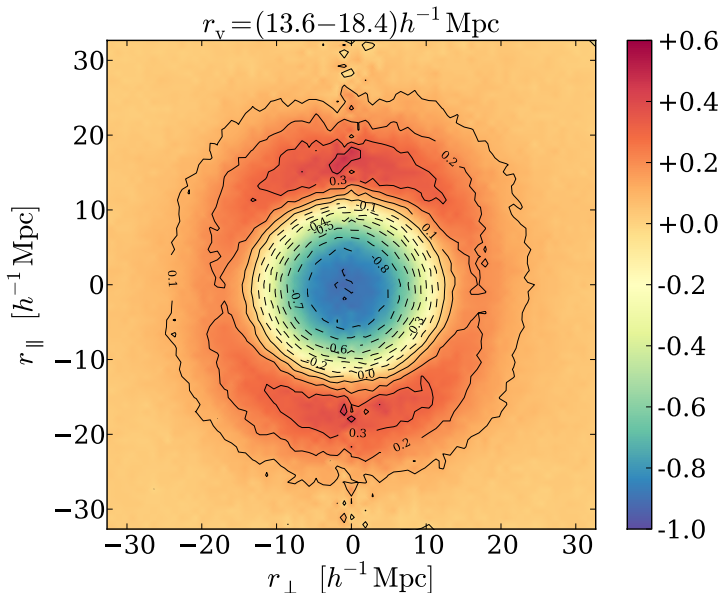
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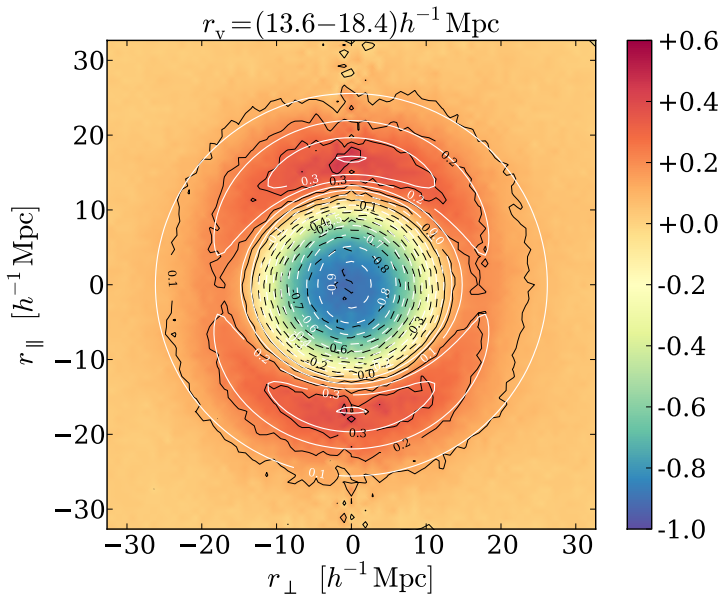
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Linear growth rate: $f(z) = \Omega_{\text{m}}^{0.55}(z)$ in General Relativity

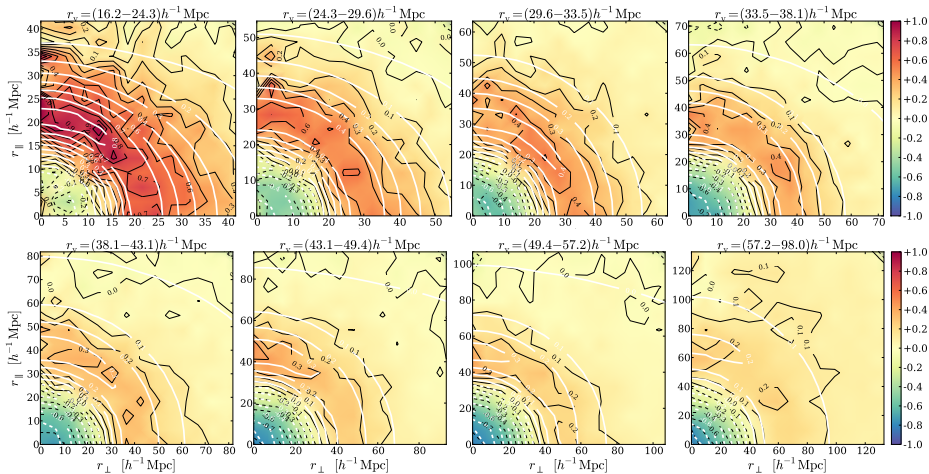
ANALYSIS: DENSE MOCK GALAXIES



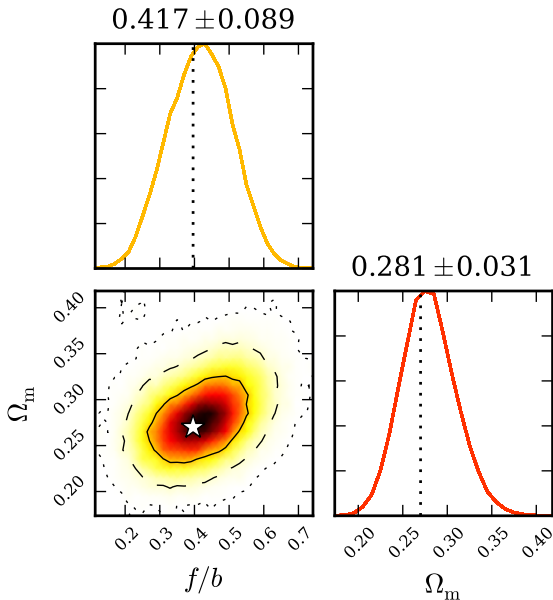
ANALYSIS: DENSE MOCK GALAXIES



ANALYSIS: SDSS CMASS DR11 GALAXIES



ANALYSIS: SDSS CMASS DR11 GALAXIES



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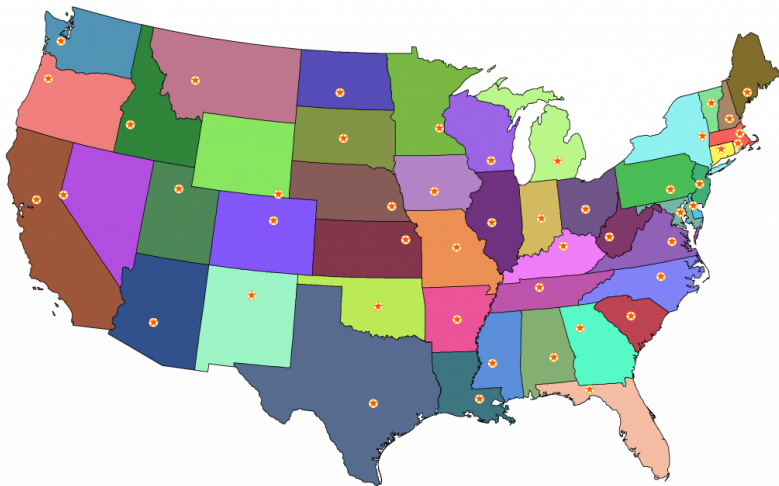
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- This can help to test modified gravity theories (alternatives for dark energy) in their unscreened regime.

QUESTIONS ?

THANK YOU !

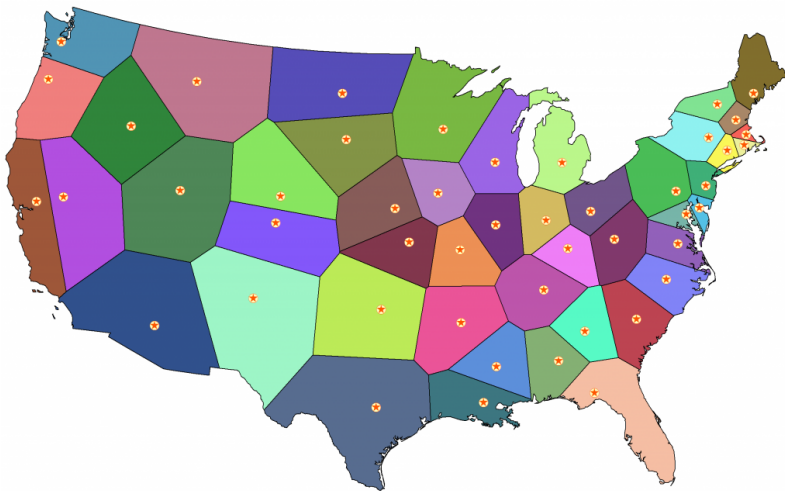
DEFINITION OF VOIDS

Define density field via **Voronoi tessellation** of tracer particles



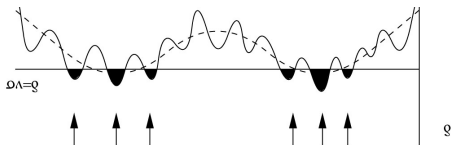
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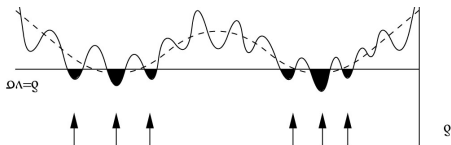
COSMIC VOIDS AS STANDARD SPHERES

Search for local minima in density field

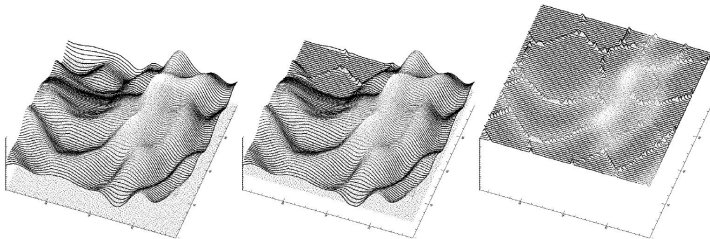


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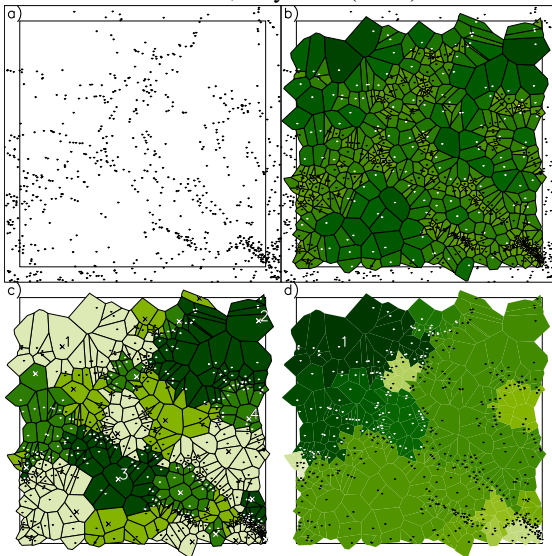
and raise a density threshold until a ridge is reached



Watershed algorithm, Platen et al. (2007)

DEFINITION OF VOIDS

ZOBOV, Neyrinck (2008)



VOID PROFILE

Estimate density and velocity profile by “stacking” tracer particles around void centers

$$\rho_v(r) = \frac{3}{4\pi} \sum_i \frac{m_i(\mathbf{r}_i)}{(r + \delta r)^3 - (r - \delta r)^3}$$

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Empirical best-fit model (4 parameters)

$$\frac{\rho_v(r)}{\bar{\rho}} - 1 = \delta_c \frac{1 - (r/r_s)^\alpha}{1 + (r/r_v)^\beta}, \quad r_v \equiv (3V_v/4\pi)^{1/3}$$

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Mass conservation to linear order

$$v_v(r) = -\frac{1}{3} \frac{f(z)H(z)}{1+z} r \Delta_v(r), \quad \Delta_v(r) \equiv \frac{3}{r^3} \int_0^r \left(\frac{\rho_v(s)}{\bar{\rho}} - 1 \right) s^2 ds$$

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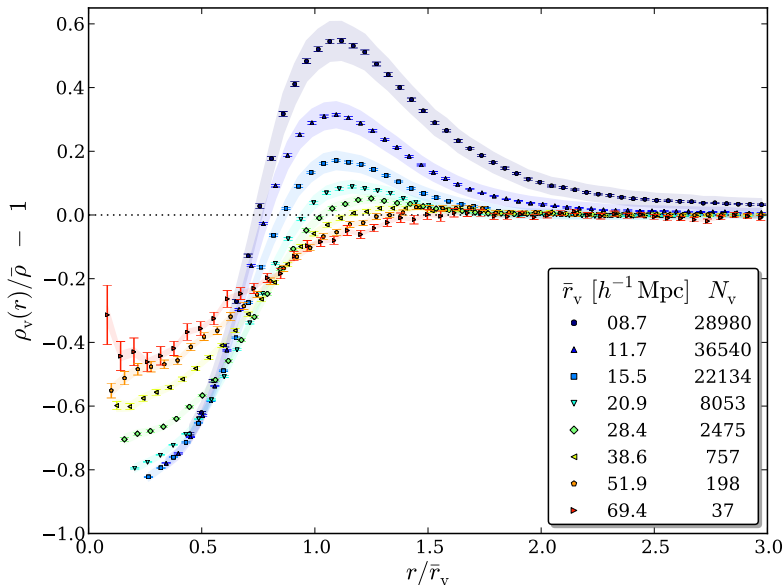
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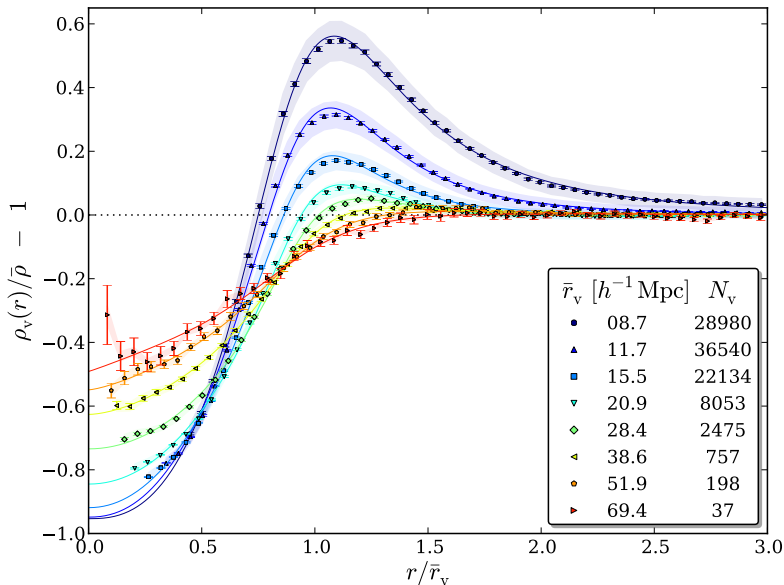
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In General Relativity: $f(z) = \Omega_m^{0.55}(z)$

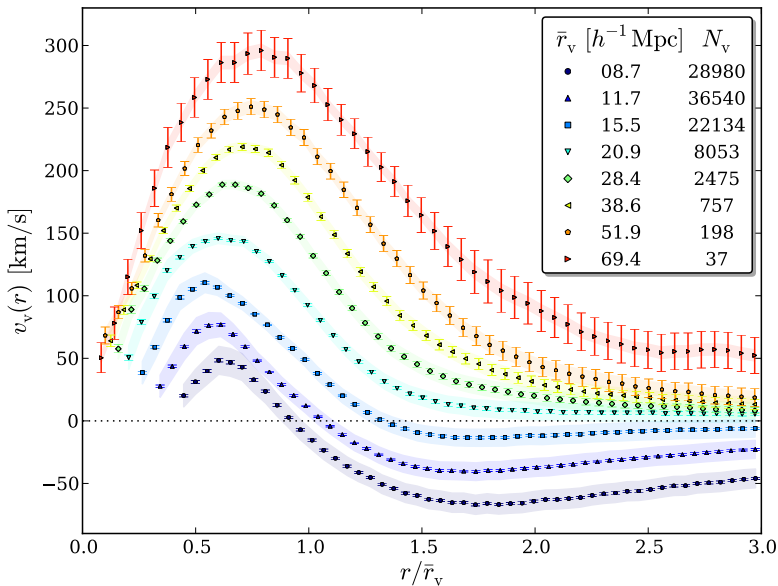
VOID PROFILE: DENSITY



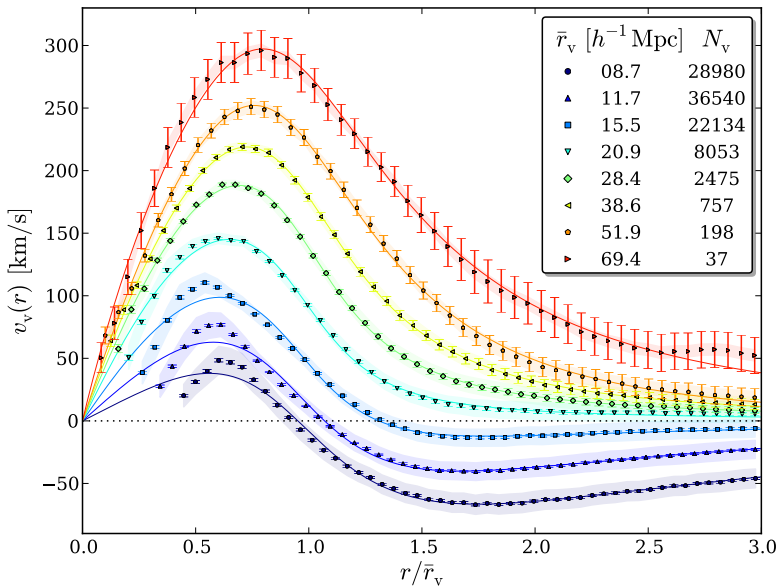
VOID PROFILE: DENSITY



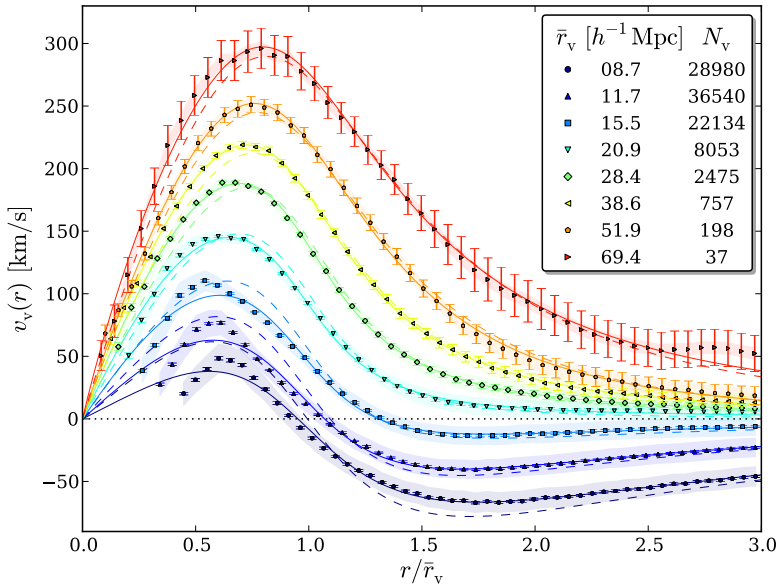
VOID PROFILE: VELOCITY



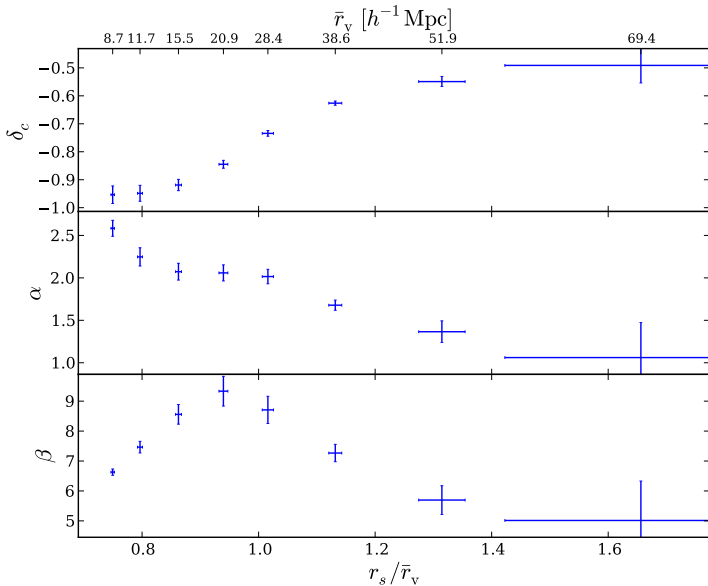
VOID PROFILE: VELOCITY



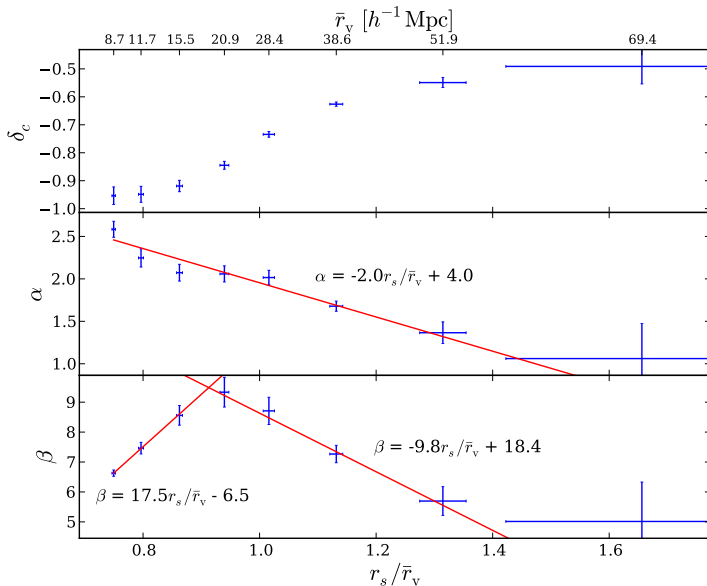
VOID PROFILE: VELOCITY



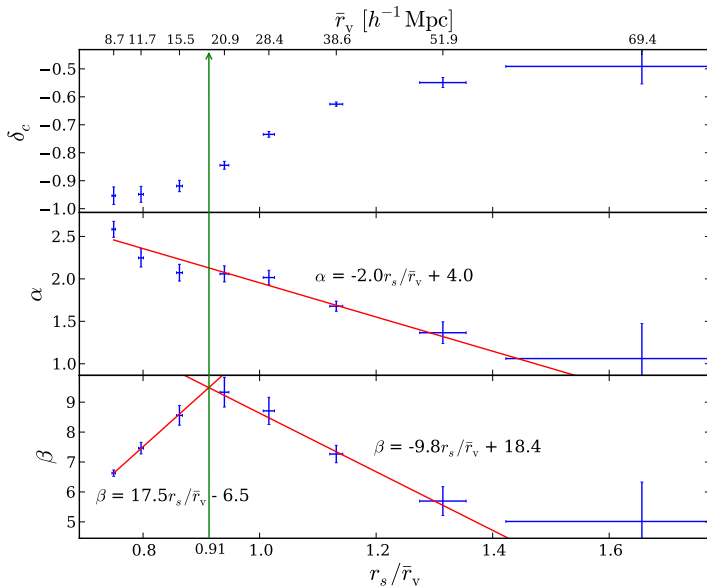
VOID PROFILE: PARAMETERS



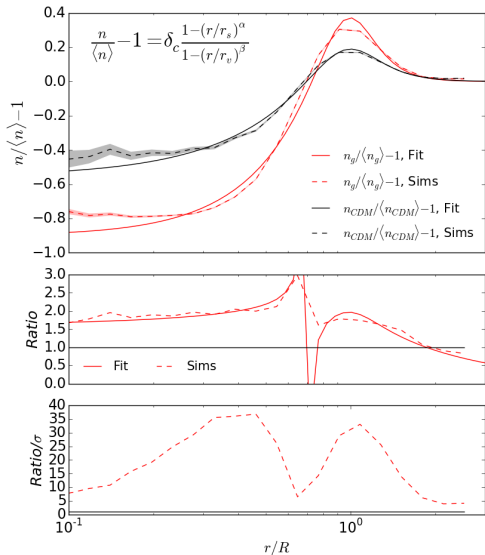
VOID PROFILE: PARAMETERS



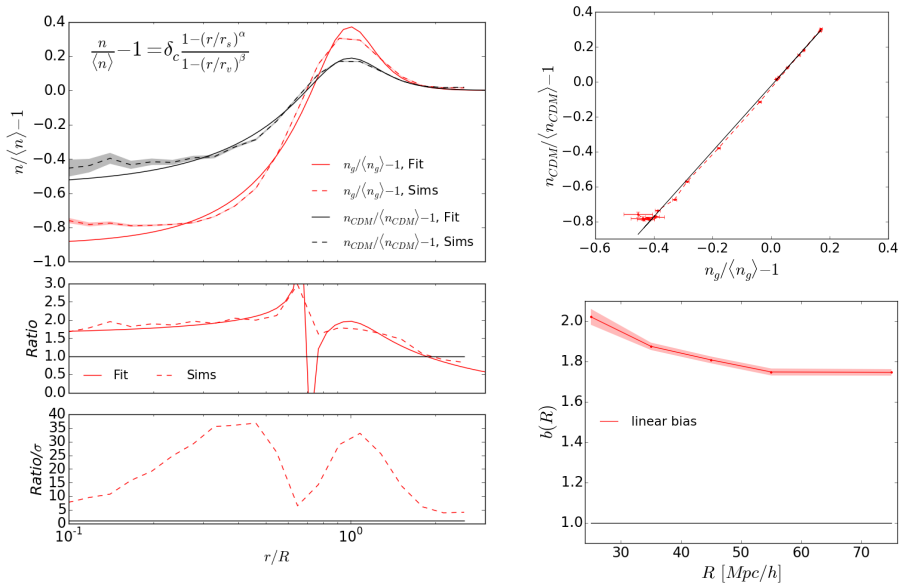
VOID PROFILE: PARAMETERS



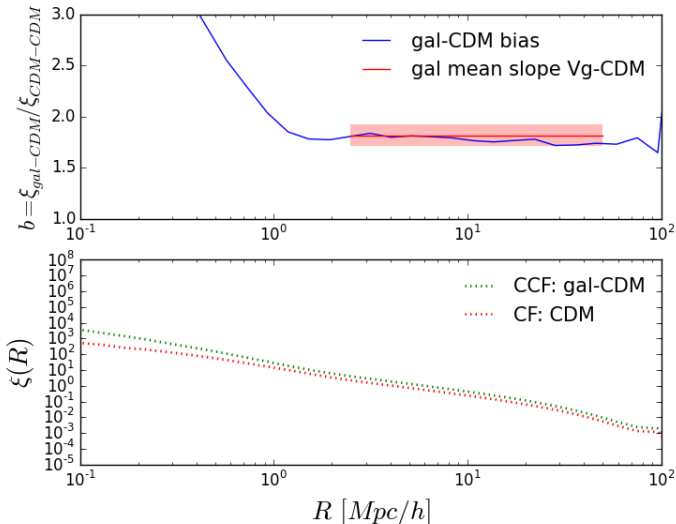
VOID PROFILE: GALAXIES VS. DARK MATTER



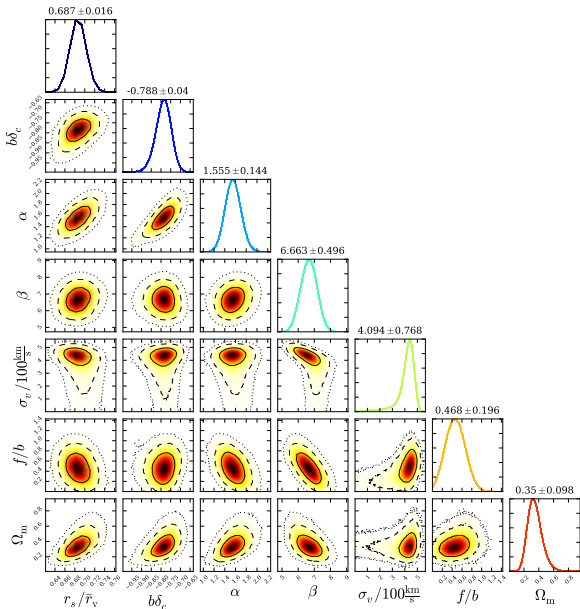
VOID PROFILE: GALAXIES VS. DARK MATTER



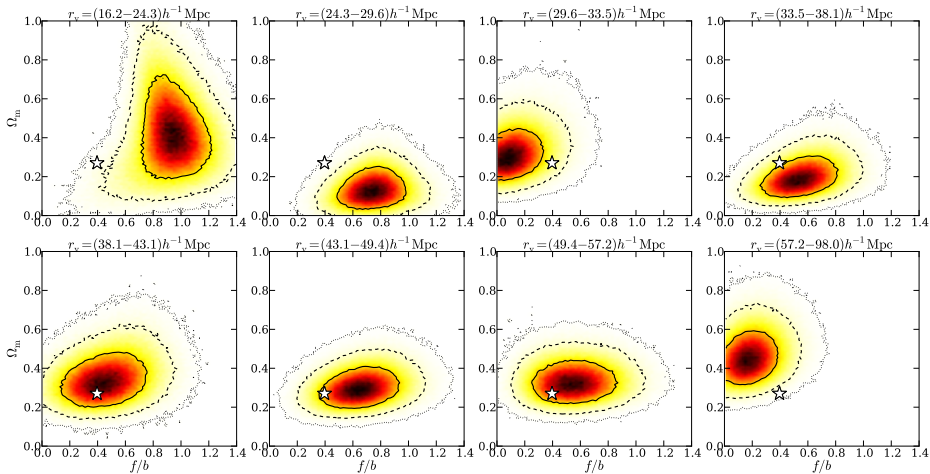
VOID PROFILE: GALAXIES VS. DARK MATTER



RSD ANALYSIS: SDSS CMASS DR11 GALAXIES



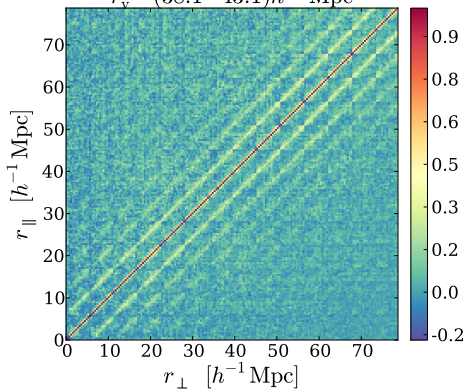
ANALYSIS: SDSS CMASS DR11 GALAXIES



RSD ANALYSIS: SDSS CMASS DR11 GALAXIES

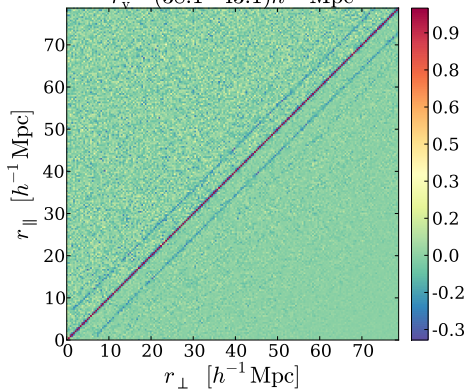
Covariance matrix

$$r_v = (38.1 - 43.1) h^{-1} \text{Mpc}$$



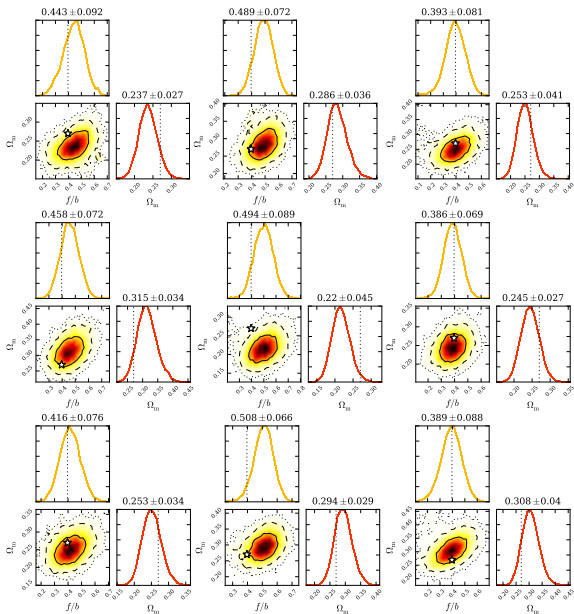
Precision matrix

$$r_v = (38.1 - 43.1) h^{-1} \text{Mpc}$$

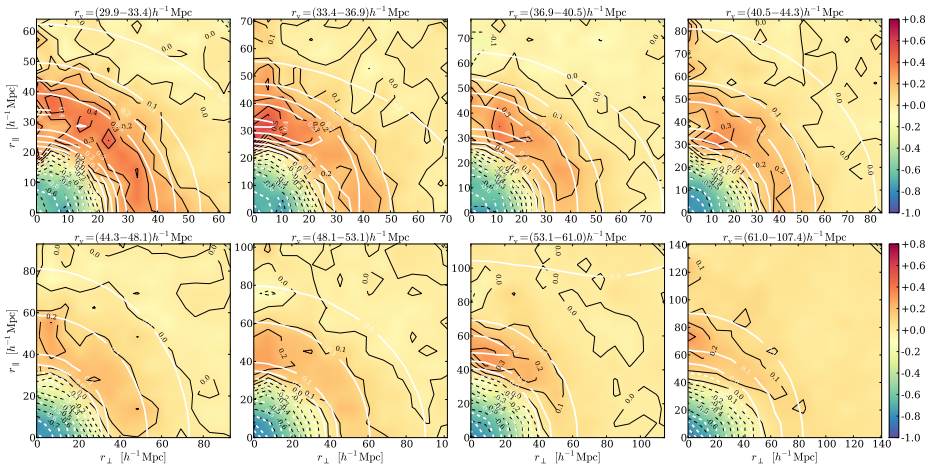


$$\mathcal{L}(\hat{\xi}_{\text{vg}}|\boldsymbol{\theta}) \propto \exp \left[-\frac{1}{2} (\hat{\xi}_{\text{vg}} - \xi_{\text{vg}})^\top \mathbf{C}^{-1} (\hat{\xi}_{\text{vg}} - \xi_{\text{vg}}) \right]$$

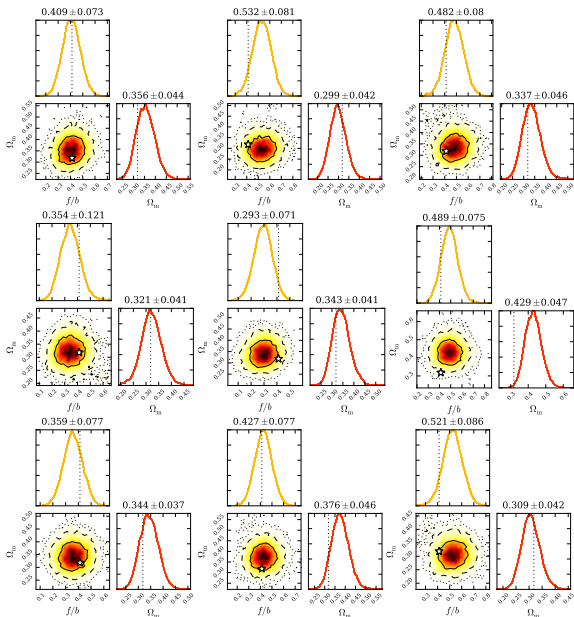
RSD ANALYSIS: SDSS CMASS DR11 BOOTSTRAPS



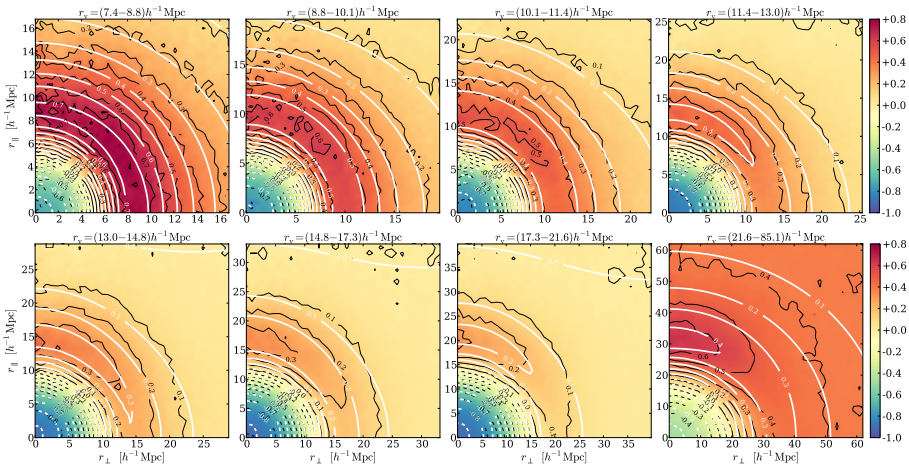
RSD ANALYSIS: SDSS CMASS DR11 MOCKS



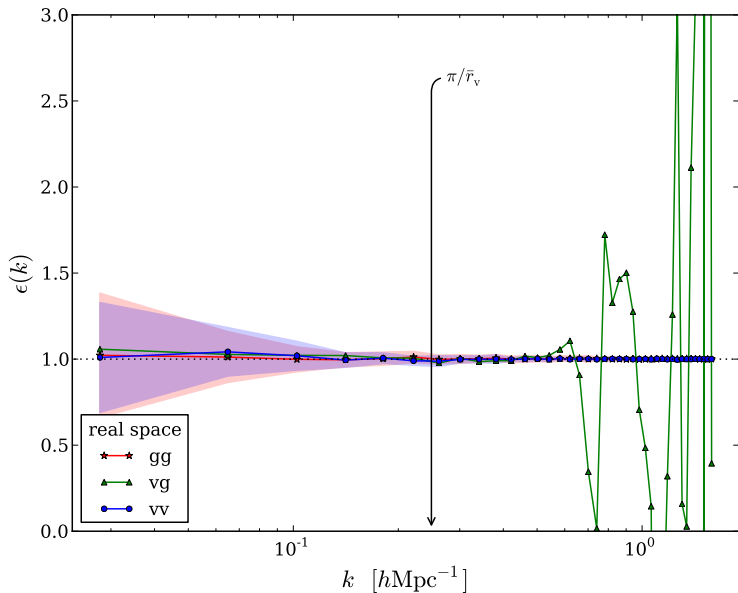
RSD ANALYSIS: SDSS CMASS DR11 MOCKS



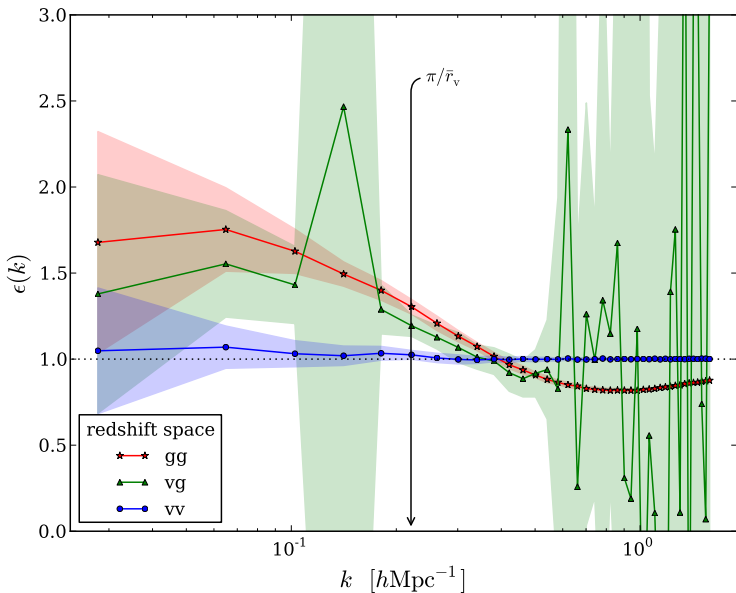
RSD ANALYSIS: SDSS MAIN MOCKS



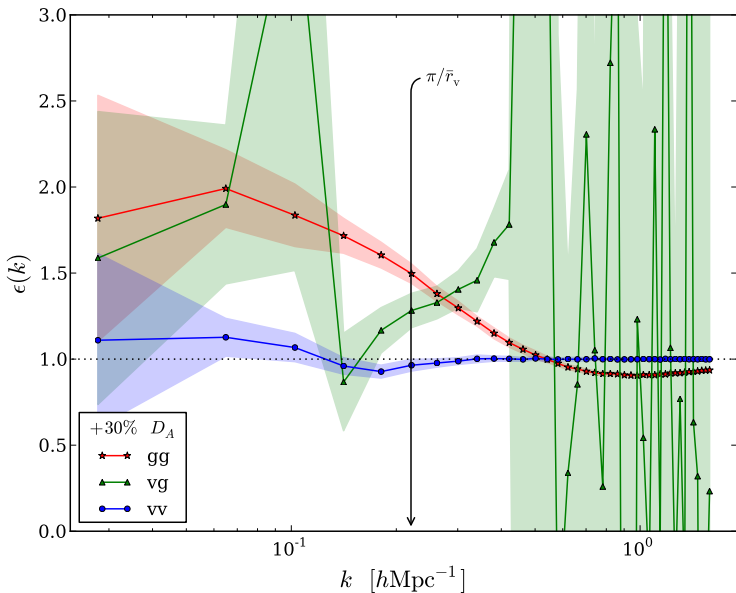
ALCOCK-PACZYNSKI TEST



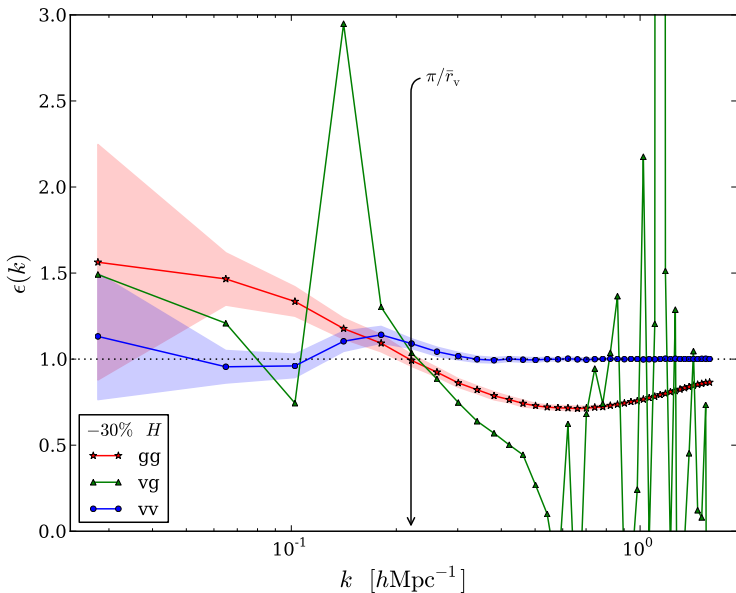
ALCOCK-PACZYNSKI TEST



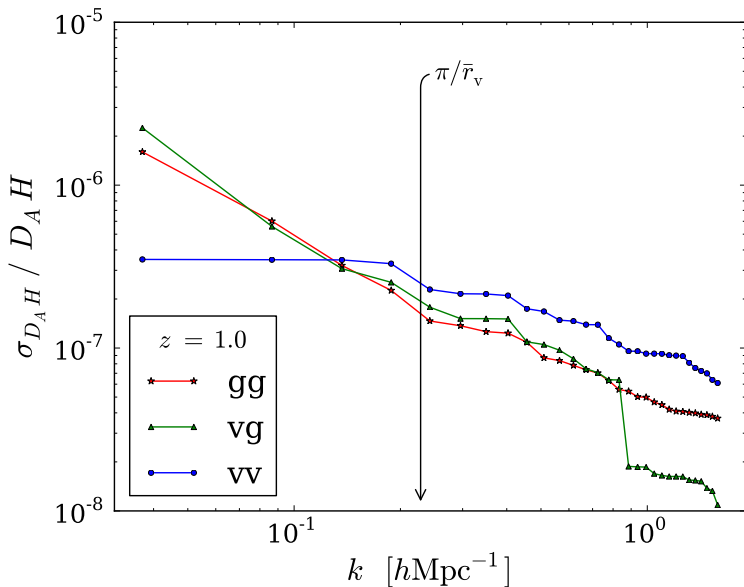
ALCOCK-PACZYNSKI TEST



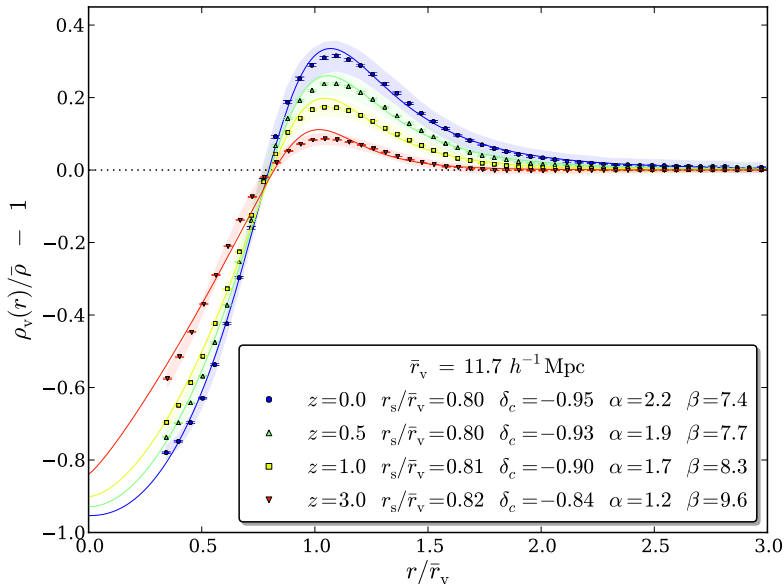
ALCOCK-PACZYNSKI TEST



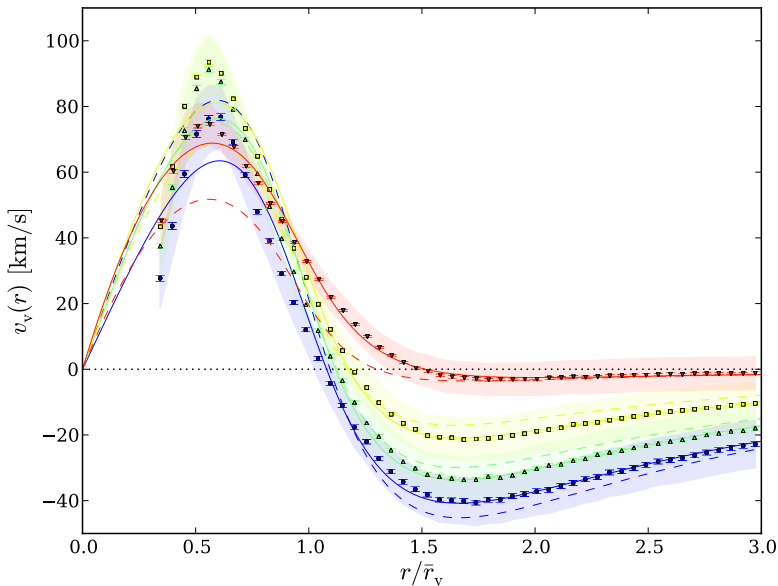
ALCOCK-PACZYNSKI TEST



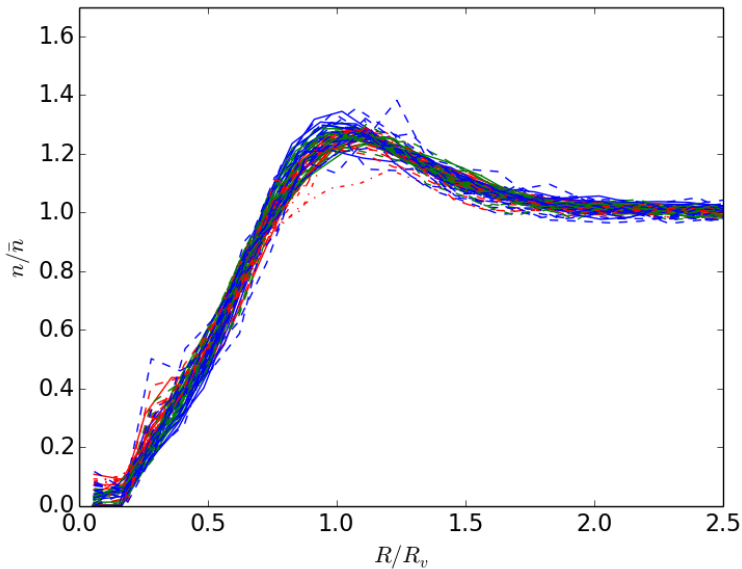
VOID PROFILE: UNIVERSALITY



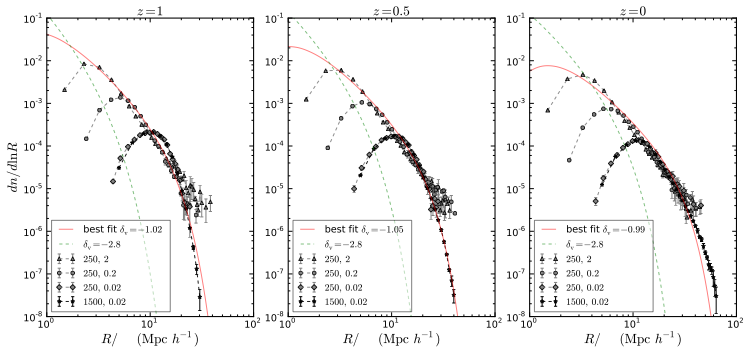
VOID PROFILE: UNIVERSALITY



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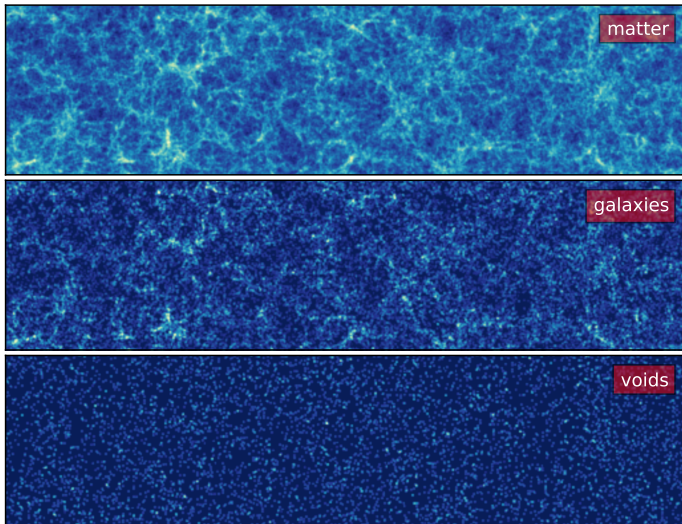


VOID ABUNDANCE

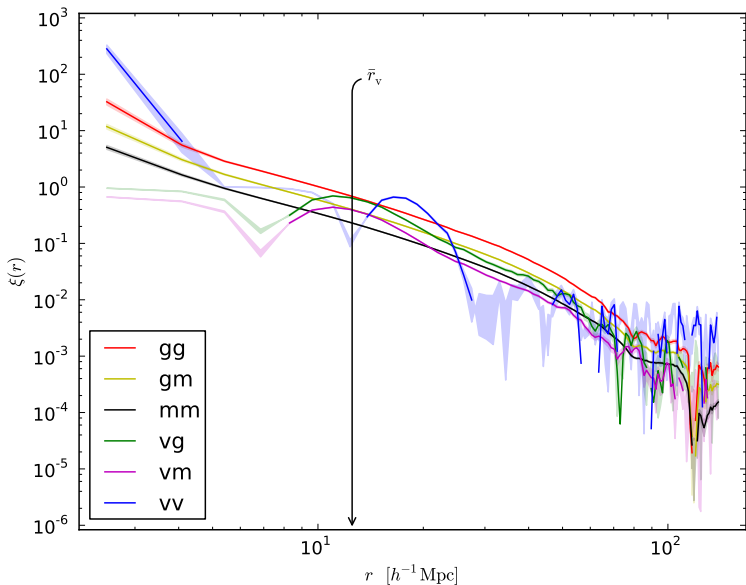


DENSITY FIELDS

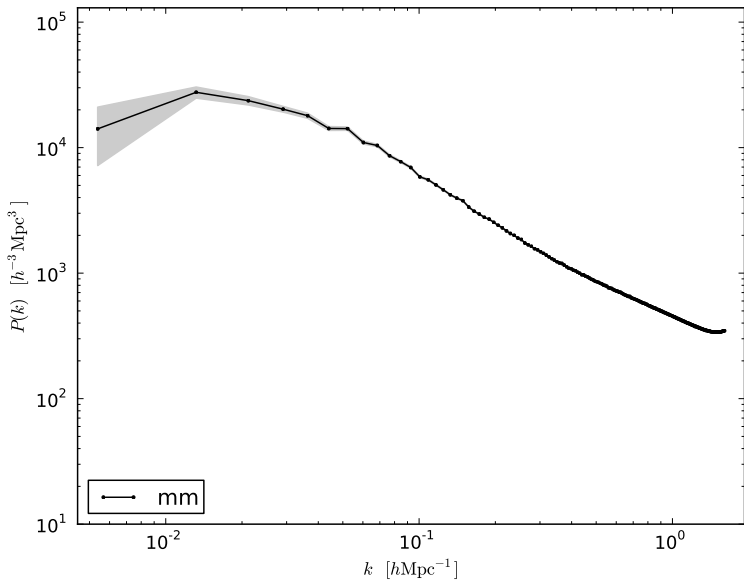
Voids are less clustered and more sparse than galaxies:



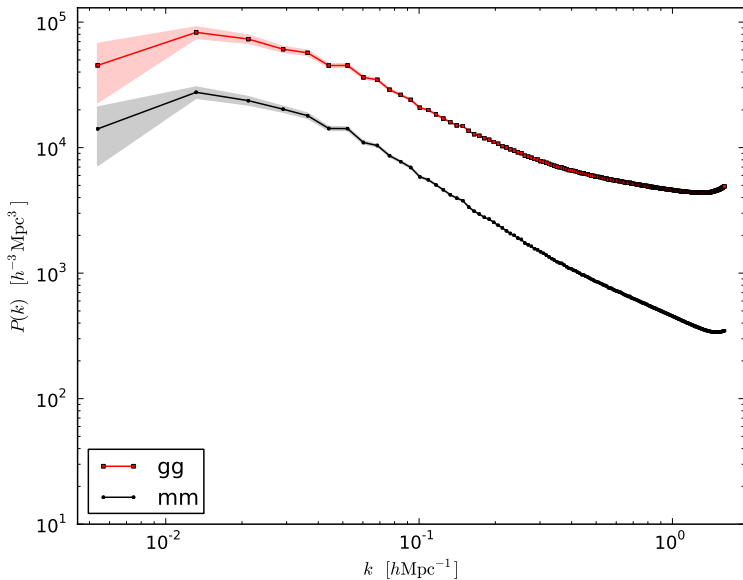
CORRELATION FUNCTION



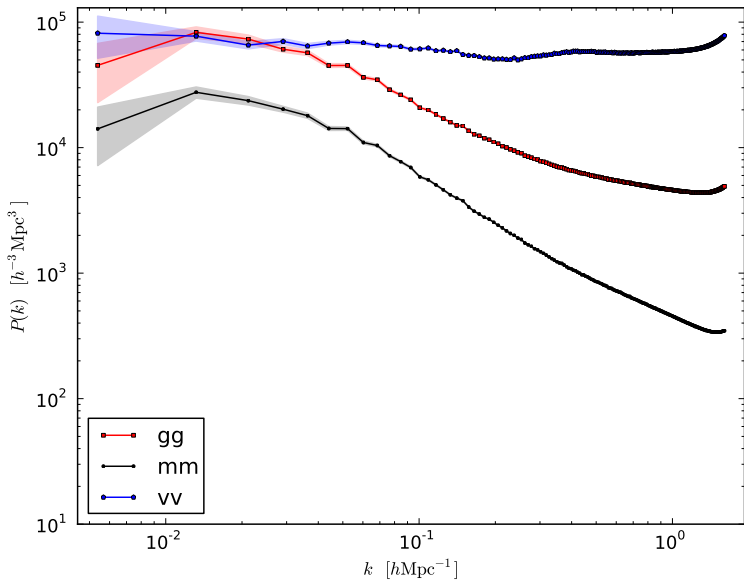
POWER SPECTRUM



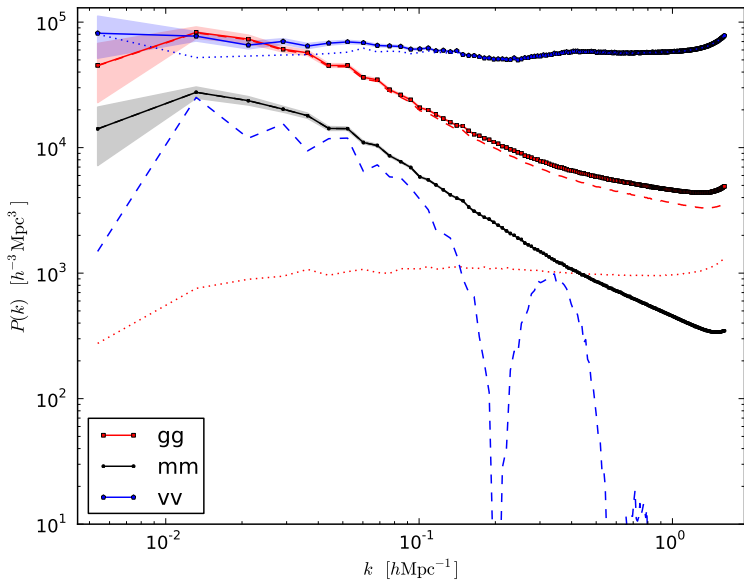
POWER SPECTRUM



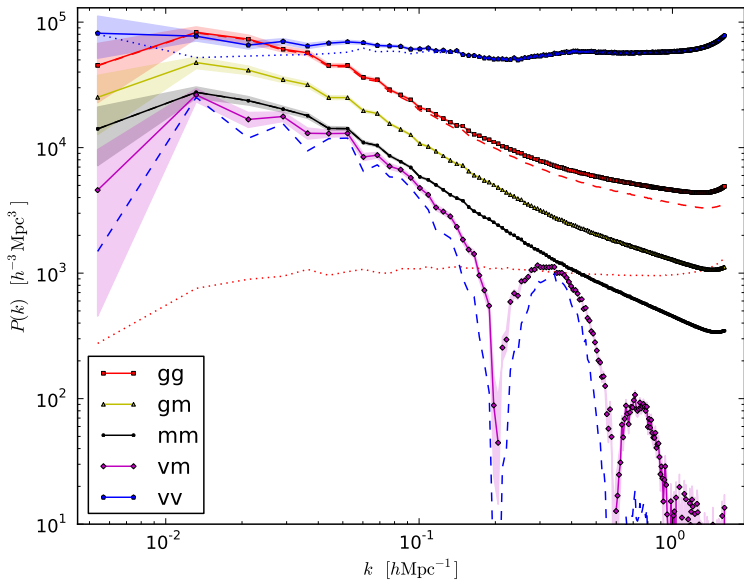
POWER SPECTRUM



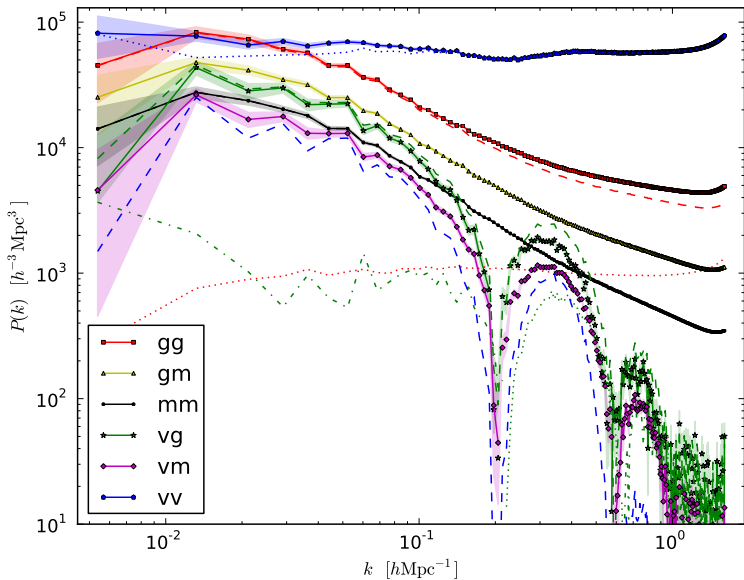
POWER SPECTRUM



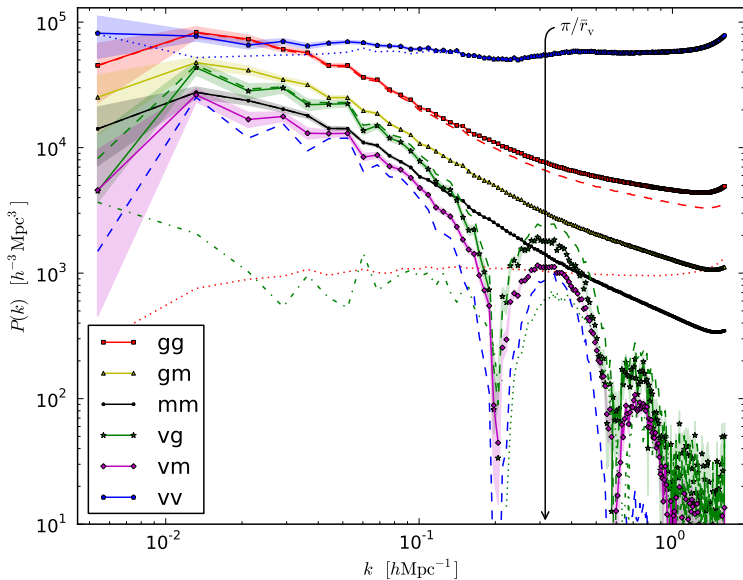
POWER SPECTRUM



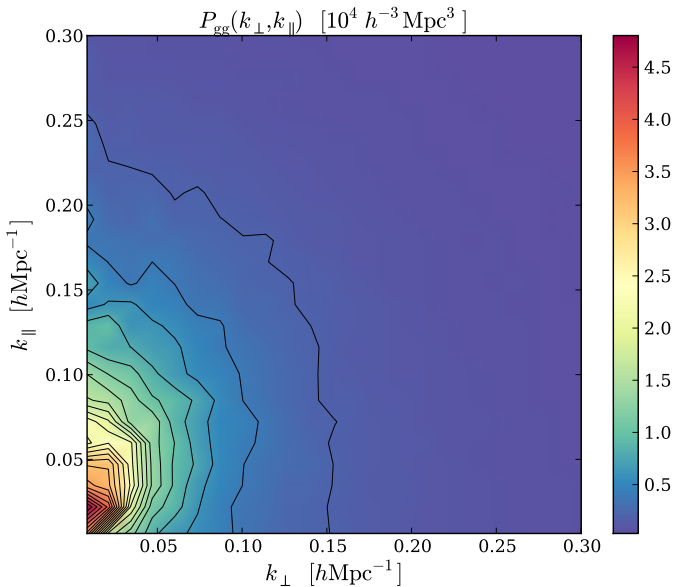
POWER SPECTRUM



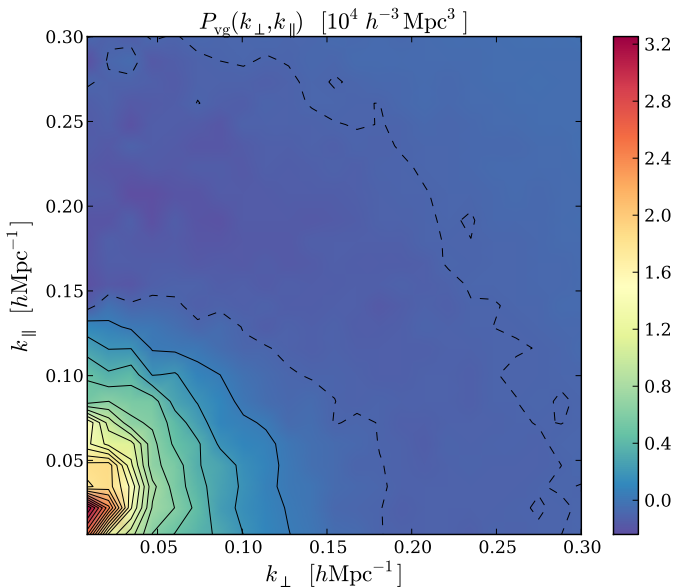
POWER SPECTRUM



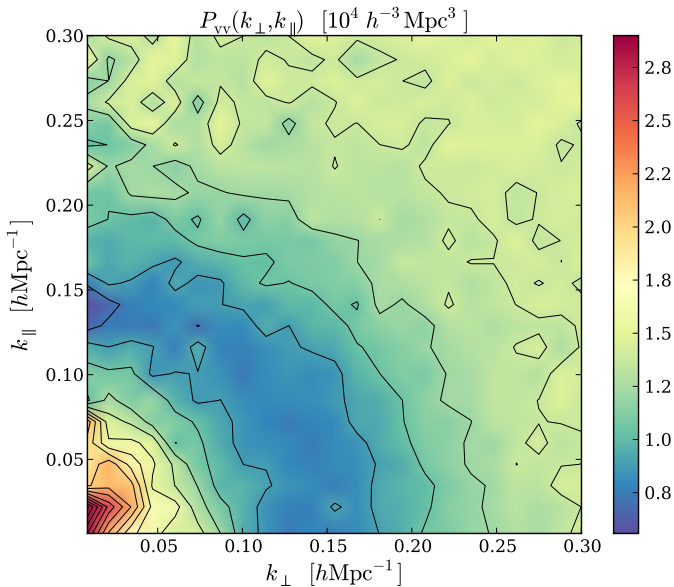
2D POWER SPECTRUM



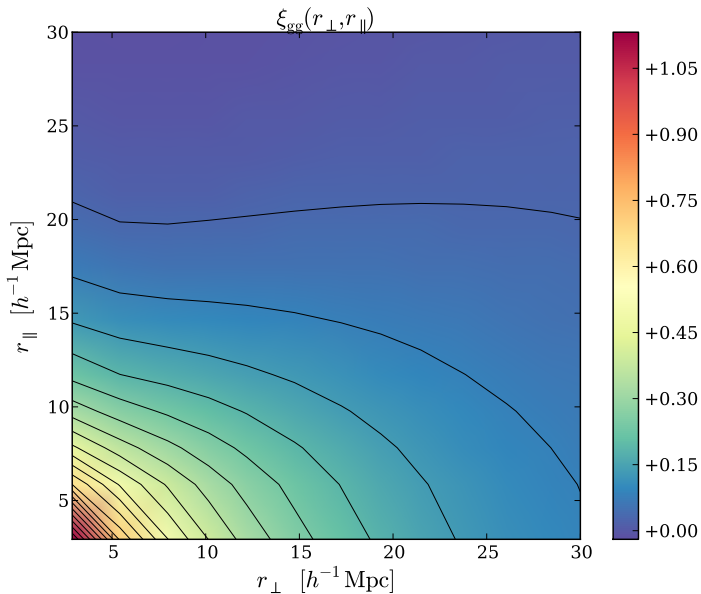
2D POWER SPECTRUM



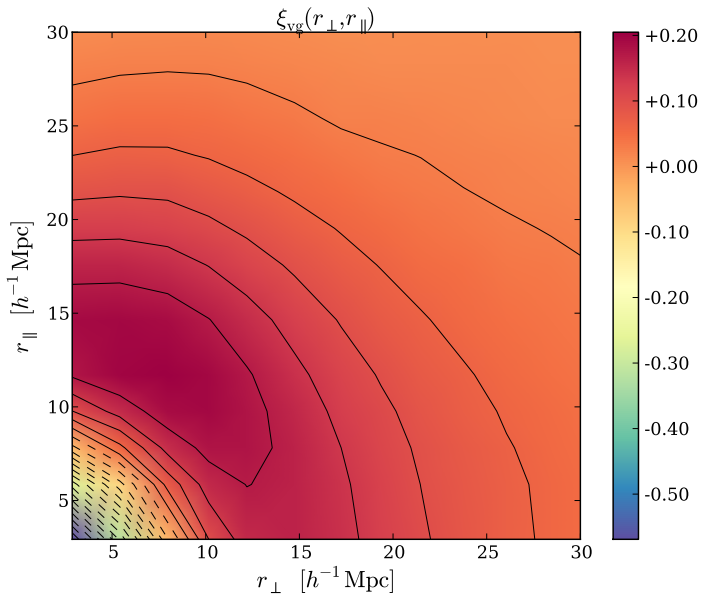
2D POWER SPECTRUM



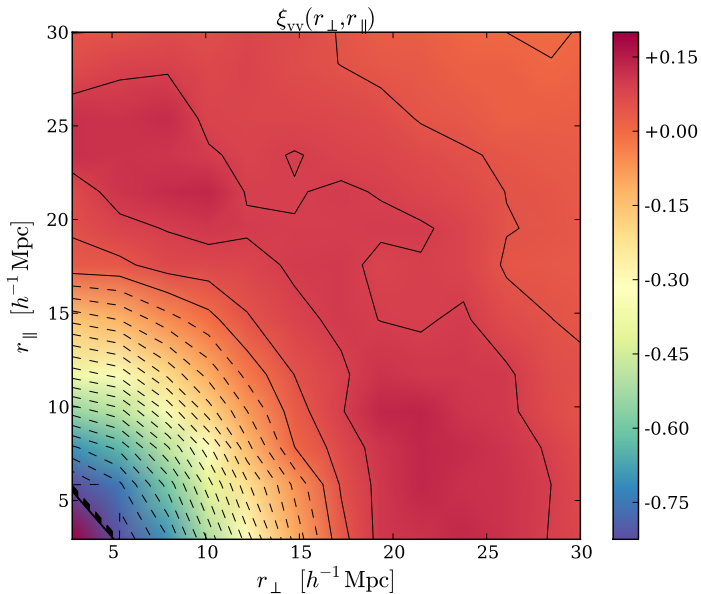
2D CORRELATION FUNCTION



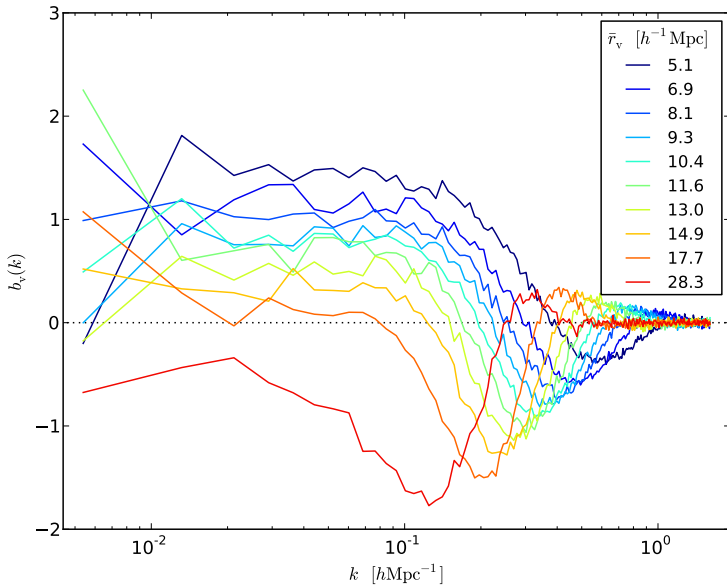
2D CORRELATION FUNCTION



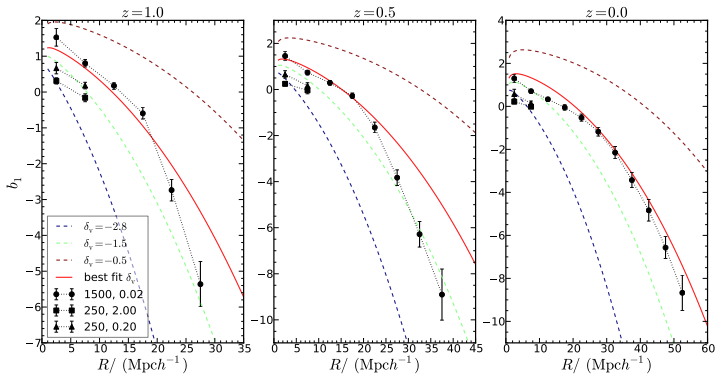
2D CORRELATION FUNCTION



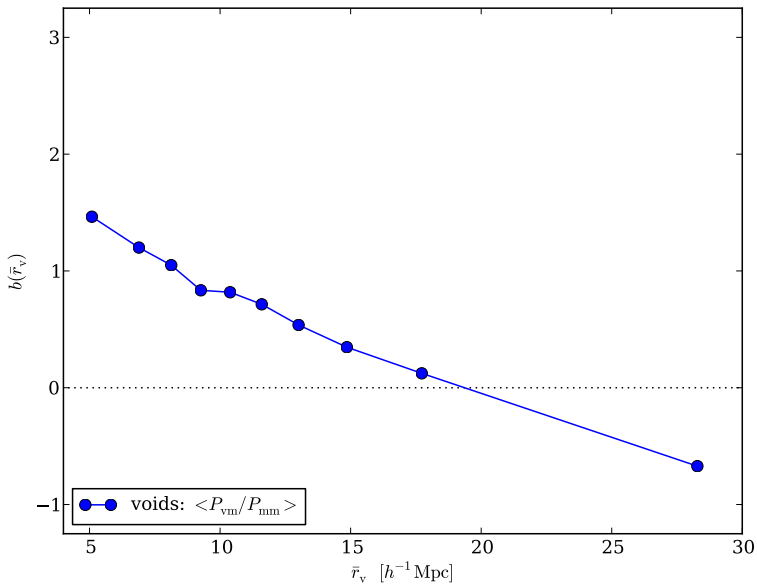
VOID BIAS



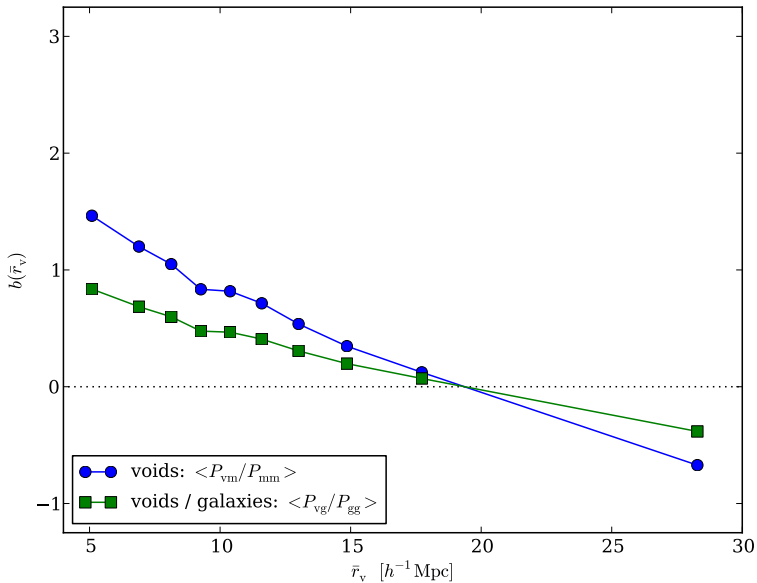
LINEAR VOID BIAS



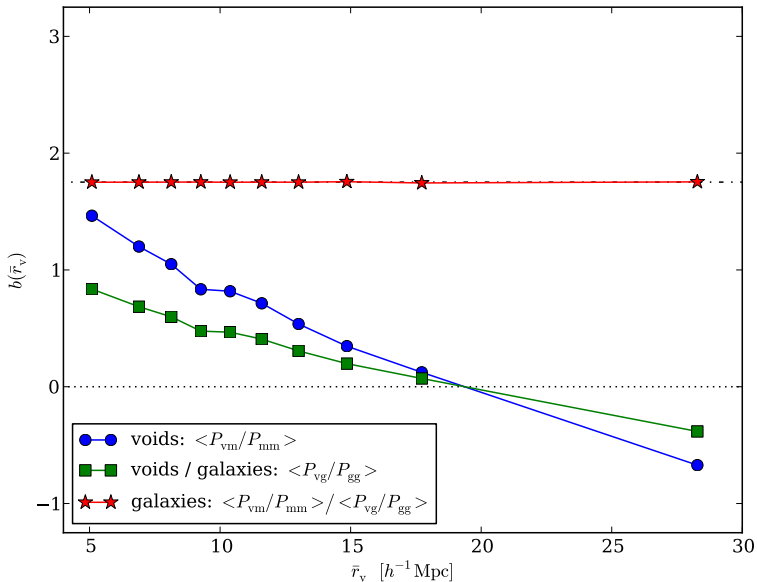
LINEAR VOID BIAS



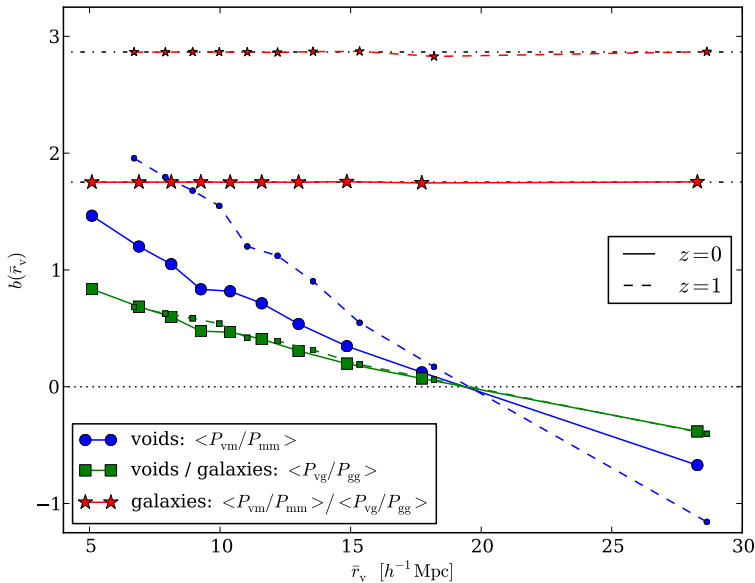
LINEAR VOID BIAS



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LINEAR VOID BIAS



LINEAR VOID BIAS

