

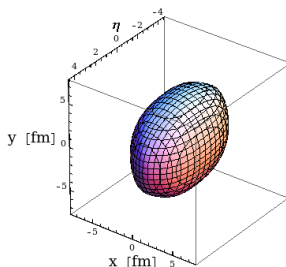
# Collective flow in relativistic nuclear collisions

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- ▶ expansion of dense matter
- ▶ close to local equilibrium
- ▶ initial conditions
- ▶ equation of state
- ▶ flow + thermal emission + decays + rescattering



## ideal hydrodynamics

- ▶ energy momentum tensor

$$T_{id}^{\mu\nu} = (\epsilon + p)g^{\mu\nu} - Pu^\mu u^\nu$$

- ▶ ideal hydro (5 functions in 3+1D),  
energy density, pressure, flow velocity

$$\epsilon(x_\mu), P(x_\mu), \vec{v}(x_\mu)$$

- ▶ 4 hydrodynamic equations

$$\partial_\mu T^{\mu\nu} = 0$$

- ▶ equation of state (zero baryon density)

$$\epsilon = \epsilon(P)$$

massless gas  $\epsilon = 3p$

## hydro equations

- ▶ using  $\epsilon + P = Ts$ ,  $d\epsilon = Tds$ ,  $dP = sdT$
- ▶ we calculate  $u_\nu \partial_\mu T^{\mu\nu}$

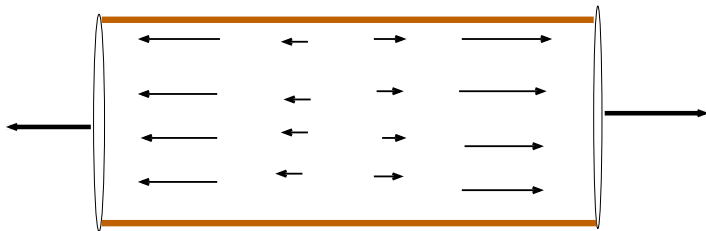
$$\partial_\mu (su^\mu) = 0$$

one equation = entropy conservation (ideal hydro)

- ▶ 3 other equations for flow velocity

$$su_\mu \partial^\mu u^\nu = (g^{\mu\nu} - u^\mu u^\nu) \partial_\mu P$$

# longitudinal expansion



## Bjorken flow

- ▶ the density depends on the proper time  $\tau = \sqrt{t^2 - z^2}$  only,  
flow velocity  $u^\mu = (t/\tau, 0, 0, z/\tau)$
- ▶ one equation

$$\frac{d\epsilon(\tau)}{d\tau} = -\frac{\epsilon(\tau) + P(\tau)}{\tau}$$

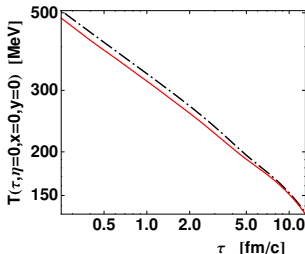
cooling from longitudinal expansion

- ▶ if  $\frac{1}{3}\epsilon \simeq P$

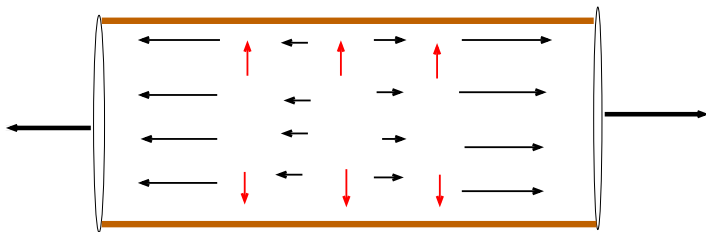
$$\epsilon(\tau) = \epsilon_0 \left(\frac{\tau_0}{\tau}\right)^{4/3}$$

- ▶ in 3+1D faster cooling when transverse expansion sets in

cooling in 2+1D and 3+1D



# longitudinal+transverse expansion



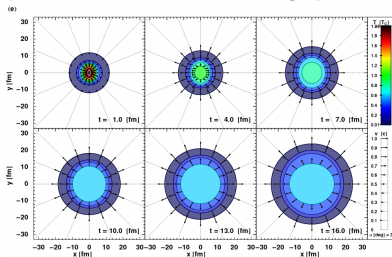
## 3+1D expansion

collective transverse expansion

$$u^\mu \partial_\mu u_x = -\frac{1 + u_x^2}{sT} \partial_x P - \frac{u_x u_y}{sT} \partial_y P + \dots$$

$$u^\mu \partial_\mu u_y = -\frac{1 + u_y^2}{sT} \partial_y P - \frac{u_x u_y}{sT} \partial_x P + \dots$$

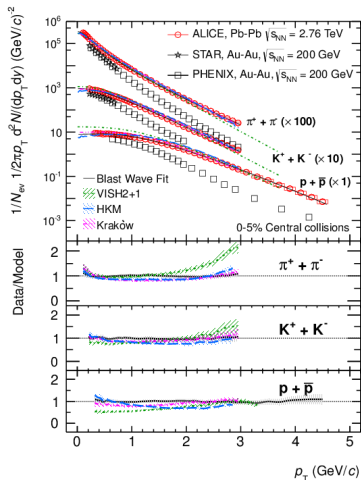
faster expansion in the direction of large pressure gradient



M. Chojnacki



# OBSERVATION 1 - transverse flow

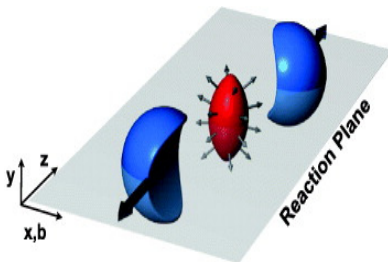


- ▶ spectra flatter due to flow
- ▶ stronger flow at the LHC
- ▶ stronger effect for heavy particles
- ▶ only soft spectra from hydro  
 $p_{\perp} < 2\text{GeV}$
- ▶ chemical ratios - normalization
- ▶ excess of soft pions?

asymmetry in the transverse plane at finite impact parameter

Glauber model, KLN model, IP-Glasma

$$\text{eccentricity} - \epsilon_2 = -\frac{\int dx dy (x^2 - y^2) \rho(x, y)}{\int dx dy (x^2 + y^2) \rho(x, y)}$$



Snellings 2011

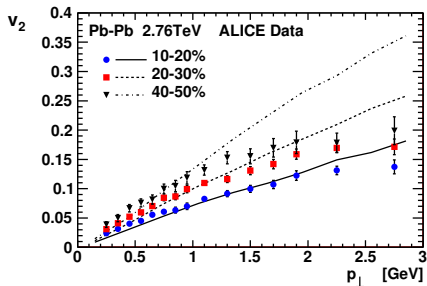
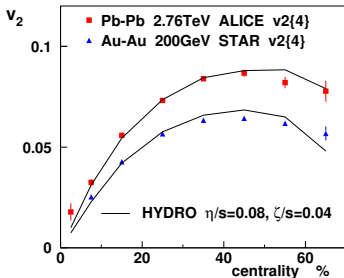
larger gradient and stronger flow in-plane -  $v_2 > 0$  - **elliptic flow**

$$\frac{dN}{d\phi} \propto 1 + 2v_2 \cos(2\phi)$$

$\epsilon_2 + \text{HYDRO RESPONSE} \longrightarrow v_2$

**Event Plane** (Reaction plane) must be reconstructed in each event

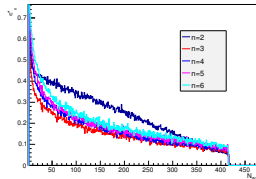
# OBSERVATION 2 - Elliptic flow



GLISSANDO ver. 2.602

208+208, 50000 events  
 $b=0.0 - 24.0$  fm  
 mixed model:  $\sigma_{\perp} = 67.7$  mb,  $\sigma_{\parallel} = 67.7$  mb,  $\alpha=0.150$   
 Gaussian wounding profile,  $A=0.92$

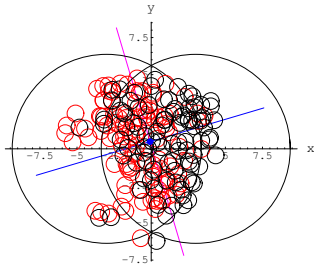
variable-axes eccentricities,  $n=2,3,4,5,6$



initial shape asymmetry transformed into flow asymmetry  
strong indication of collective behavior

smoking gun for collectivity

# fluctuating initial conditions



fluctuating initial density

→ larger eccentricity

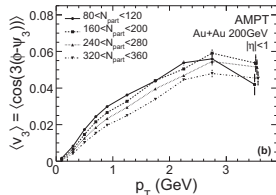
→ fluctuating eccentricity

→ **triangular deformation**  $\epsilon_3$

→ dipolar (directed) flow  $v_1$

→  $\langle p_{\perp} \rangle$  fluctuations

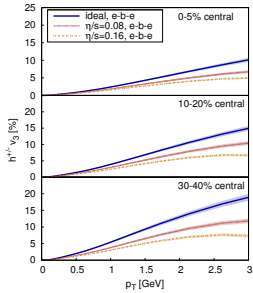
→ RP orientation, torqued fireball



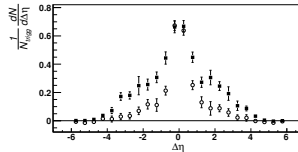
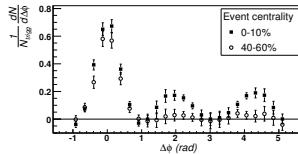
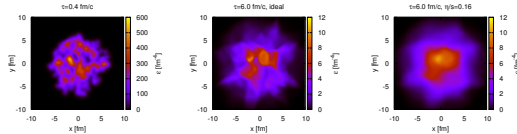
B. Alver, G. Roland

$$\frac{dN}{d\phi} \propto 1 + 2v_1 \cos(\phi - \Psi_1) + 2v_2 \cos(2(\phi - \Psi_2)) + 2v_3 \cos(3(\phi - \Psi_3)) + \dots$$

# Event by event hydro



Schenke, Jeon, Gale, Phys. Rev. 106, 042301 (2011)

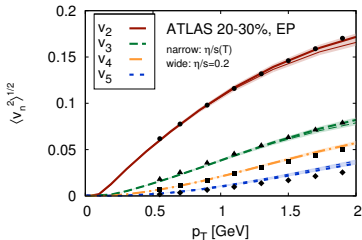
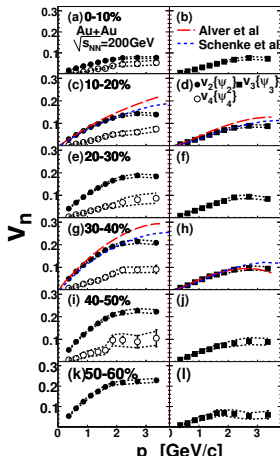


Takahashi et al., Phys. Rev. 103, 242301 (2009)

event by event ideal hydro - Andrade, Grassi, Hama, Kodama, Socolowski 2006

# OBSERVATION 3 - triangular flow

odd harmonics generated by fluctuations in initial conditions



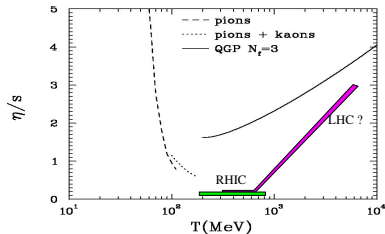
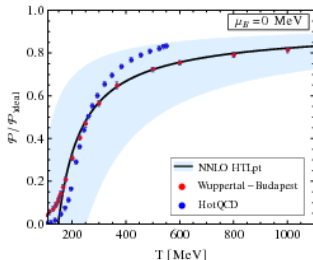
C.Gale et al. arXiv:1209.6330

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(viscous) event by event hydrodynamics

## sQGP or wQGP ?

How to see the difference?



Haque, Andersen, Mustafa, Strickland, Su, 2013

Csernai, Kapusta, McLerran, 2006

## small viscosity fluid

- ▶ strongly coupled theory  $\frac{\eta}{s} = \frac{1}{4\pi} \simeq 0.08$
- ▶ short mean-free path, large cross section

$$\eta = \frac{1}{3}npL_{mfp}$$

- ▶ for  $\eta/s = 0.08$

$$L_{mfp} = \frac{3s}{4\pi np} \simeq 0.15 - 0.3fm$$

- ▶ mean-free path comparable to wavelength

$$L_{mfp} \simeq 0.9\lambda$$

- ▶ mean-free path comparable to inter-particle distance

$$L_{mfp} \simeq 0.5n^{-1/3}$$

all of the above means no quasi-particles, no kinetic description



energy-momentum tensor

$$T^{\mu\nu} = \begin{pmatrix} \epsilon & 0 & 0 & 0 \\ 0 & p + \Pi & 0 & 0 \\ 0 & 0 & p + \Pi & 0 \\ 0 & 0 & 0 & p + \Pi \end{pmatrix} + \pi^{\mu\nu}$$

► shear viscosity

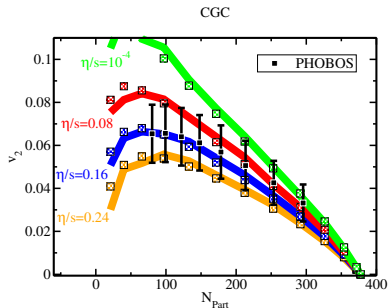
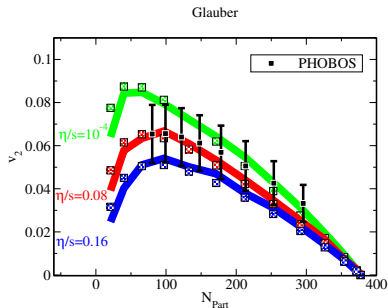
$$\Delta^{\mu\alpha} \Delta^{\nu\beta} u^\gamma \partial_\gamma \pi_{\alpha\beta} = \frac{2\eta\sigma^{\mu\nu} - \pi^{\mu\nu}}{\tau_\pi} - \frac{1}{2}\pi^{\mu\nu} \frac{\eta T}{\tau_\pi} \partial_\alpha \left( \frac{\tau_\pi u^\alpha}{\eta T} \right)$$

► bulk viscosity

$$u^\gamma \partial_\gamma \Pi = \frac{-\zeta \partial_\gamma u^\gamma - \Pi}{\tau_\Pi} - \frac{1}{2}\Pi \frac{\zeta T}{\tau_\Pi} \partial_\alpha \left( \frac{\tau_\Pi u^\alpha}{\zeta T} \right)$$

viscosity corrections from velocity gradients

## OBSERVATION 4 - small viscosity



Luzum, Romatschke, Phys. Rev. C78, 034915 (2009)

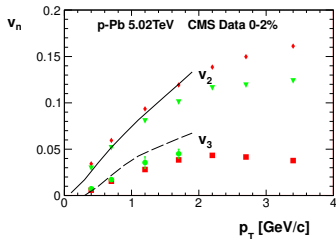
Model uncertainties

Small viscosity :  $\eta/s = 0.08 - 0.2$  - sQGP

Strongly interacting fluid

# OBSERVATION 5 - Elliptic and triangular flow observed in p-Pb

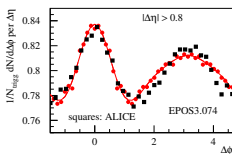
- Glauber MC initial cond. - agreement with data



PB, W.Broniowski, G. Torrieri arXiv:1306.5442; G.Y. Qin, B. Müller 1306.3439; I. Kozlov et al. 1405.3976; A. Bzdak et al. 1304.34003

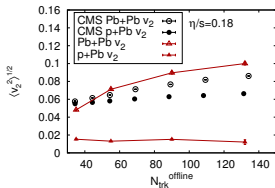
- ▶  $v_2, v_3$  consistent with hydro (Glauber MC, EPOS3)
- ▶ sensitive probe of init. cond.

- EPOS3 - agreement with data



K. Werner et al. 1307.4379

- IP-Glasma initial cond. - small  $v_2, v_3$  !

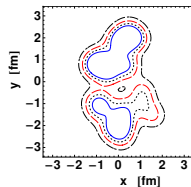


B. Schenke, R. Venugopalan 1405.3605

$v_{2,3}$  - hydro response to initial deformation !

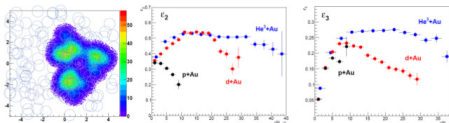
## Small system with large deformation

- ▶ deuteron projectile  
intrinsic deformation dominates over  
fluctuations  $\rightarrow$  large  $v_2$



PB 1112.0915

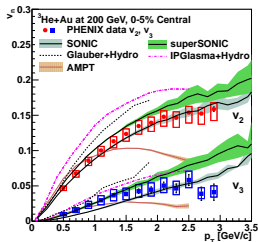
- ▶  $^3\text{He}$  projectile  
larger triangular flow



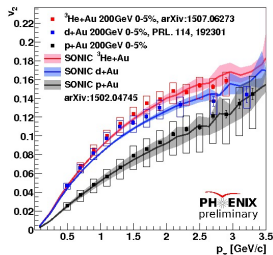
Nagle et al. arXiv:1312.4565

central collisions - deformed fireball, **control of initial geometry**

# Elliptic and triangular flow in d-Au, $^3\text{He}$ -Au and p-Au



PHENIX, arXiv:1507.06273



PHENIX

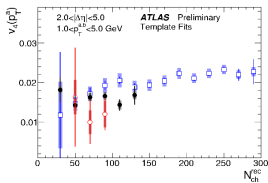
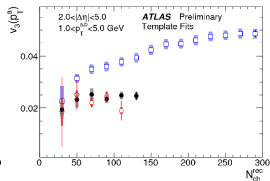
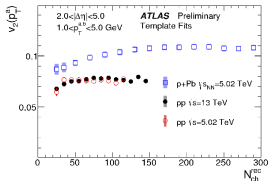
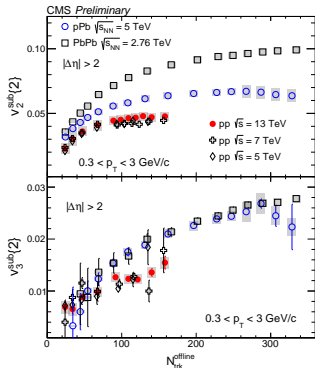
- ▶ observed  $v_3$   $\rightarrow$  collectivity
- ▶ hierarchy of  $v_2$  and  $v_3$  consistent with collective response on fireball geometry

hydrodynamic calculations reproduce the data

sensitivity to details, limits of applicability of hydro - systematic model uncertainty

large eccentricity - large flow component  
collective response to geometry

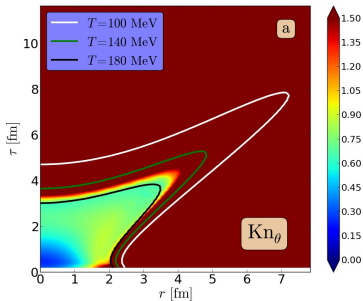
# Collective flow in pp?



Collective like correlations observed in pp

# Hydrodynamics in small systems?

## Hydrodynamics $K < 1$



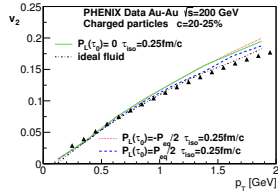
H. Niemi, G. Denicol 1404.7327

large gradients in the evolution

higher order corrections,

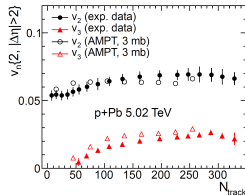
effective viscosity reduced

### 1. Early stage, pressure asymmetry $P_L \ll P_\perp$



PB, I. Wyskiel-Piekarska 1011.6210; J. Vredevoogt, S. Pratt 0810.4325  
early pressure asymmetry - irrelevant

### 2. Late stage, decoupling at freeze-out



A.Bzdak, G.L. Ma 1404.4129; L. He et al. 1502.05572  
hydrodynamics similar to AMPT cascade

## Summary

nuclear collisions - hydrodynamic expansion

- ▶ significant transverse flow generated
- ▶ elliptic flow reflecting initial asymmetry
- ▶ triangular flow - fluctuating initial conditions - flow fluctuations
- ▶ small viscosity fluid - sQGP

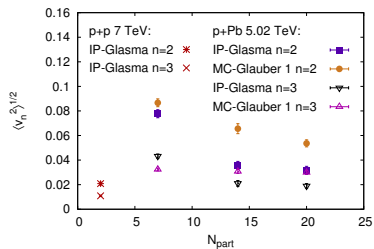
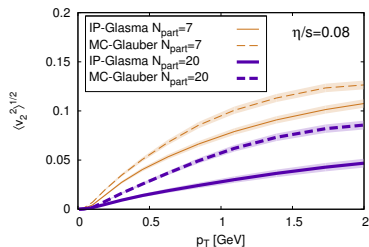
**NEW:** collectivity in small systems

- ▶ **flow in small systems observed** ( $p$ -A, ...)
  - ▶ **density driven** collective expansion
  - ▶ collectivity  $\neq$  QGP ??

**Collective expansion more general than hydrodynamic expansion**



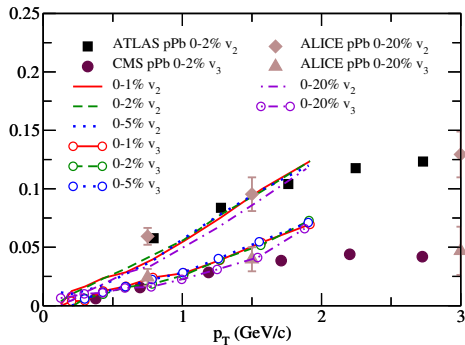
# 3+1D visc. hydro



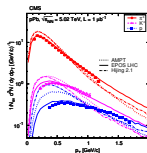
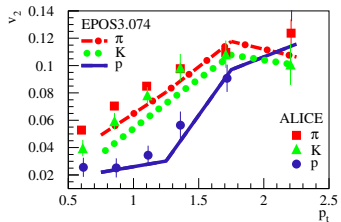
dependence on initial model,  $v_n$  small for IP-Glasma i.c.

A.Bzdak, B.Schenke, P.TribeDY, R.Venugopalan - arXiv: 1304.3403

# 3+1D hydro



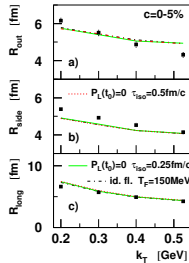
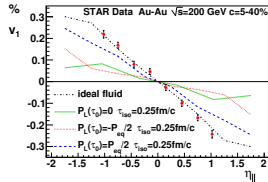
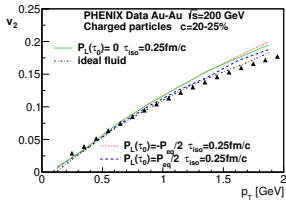
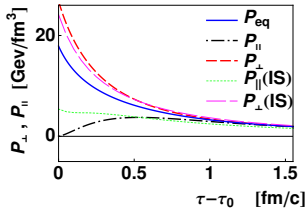
G-Y.Qin, B. Müller arXiv: 1306.3439



excellent description of spectra

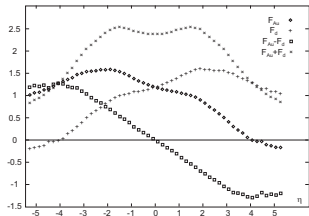
K. Werner, M. Bleicher, B. Guiot, Iu. Karpenko, T. Pierog - arXiv:1307.4379

# pressure anisotropy



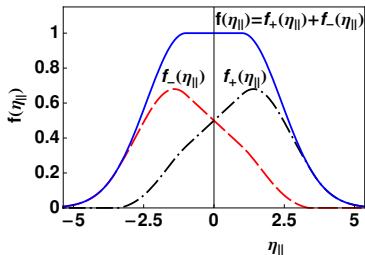
PB, I. Wykiel - arXiv:1009.0701

- early pressure anisotropy irrelevant!

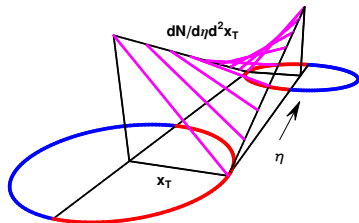


## Asymmetric emission

(Białas, Czyż, Acta Phys.Polon.B36, 905 (2005))



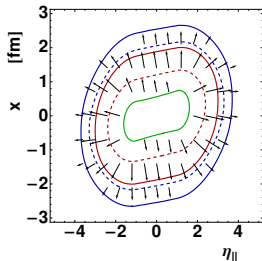
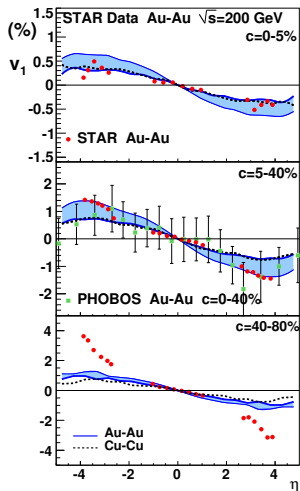
$$\rho(\eta, x, y) \propto f_{+}(\eta)N_{+}(x, y) + f_{-}(\eta)N_{-}(x, y)$$



**bremsstrahlung** (Adil Gyulassy, Phys. Rev.

C72, 034907 (2005))

# Directed flow- tilted source



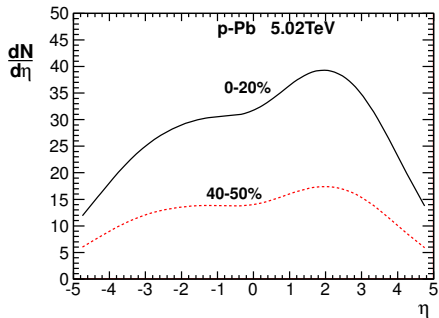
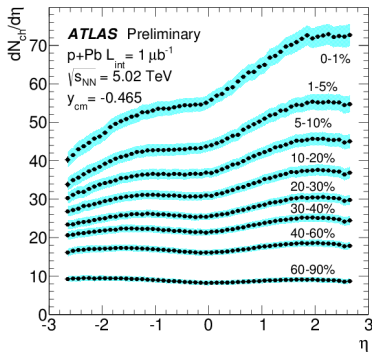
Bozek, Wyslciel, Phys. Rev. C81, 054902 (2010)

$$\partial_\tau u_x = -\frac{\partial_x p_\perp}{p + \epsilon}$$

$$\partial_\tau Y = -\frac{\partial_\eta p_\parallel}{\tau(p + \epsilon)}$$

tilted source  $\rightarrow$  transverse pressure + longitudinal pressure  
Glauber model

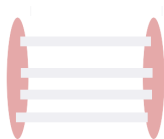
## Asymmetric distributions



# FSI scenarios

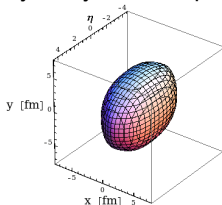
## fields+thermalization

color fields

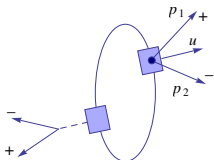


## hydrodynamics

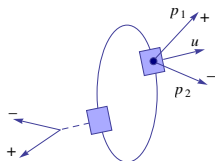
hydrodynamic expansion



local thermalization  $\rightarrow$  hadronization



hadronization, statistical emission

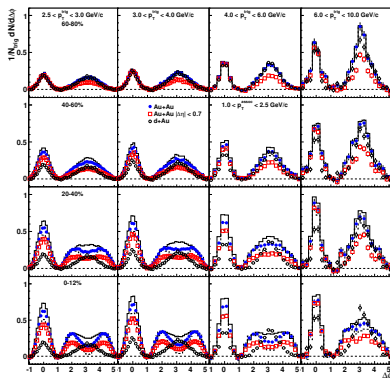


Give similar flow

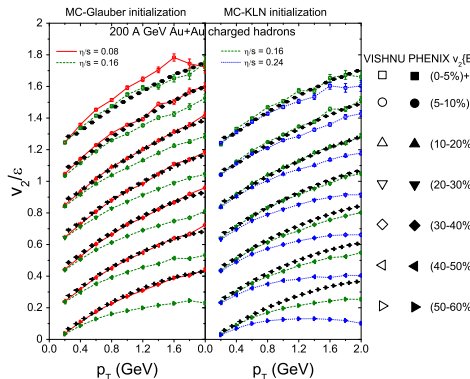




# Can we reduce uncertainties? go back to very peripheral A-A



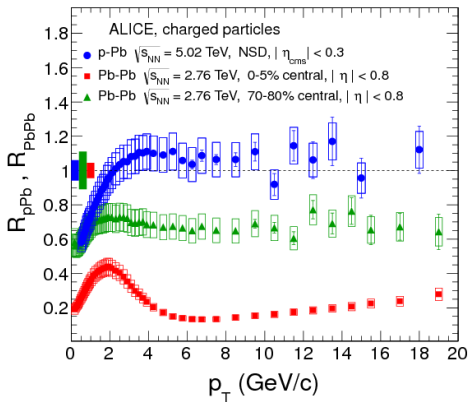
STAR-arXiv:1004.2377



Song, Bass, Heinz, Hirano, Shen-arXiv:1101.4638

also jet modification, dijet asymmetry, PID flow, HBT

# Flow without jet quenching?





## energy-momentum tensor

$$T^{\mu\nu} = \begin{pmatrix} \epsilon & 0 & 0 & 0 \\ 0 & p + \Pi & 0 & 0 \\ 0 & 0 & p + \Pi & 0 \\ 0 & 0 & 0 & p + \Pi \end{pmatrix} + \pi^{\mu\nu}$$

- ▶ shear viscosity

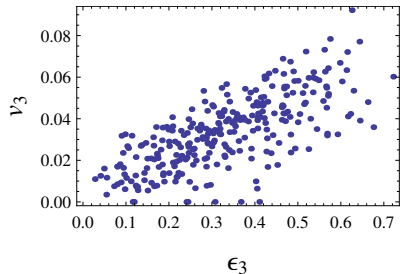
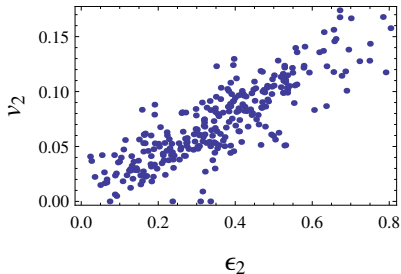
$$\Delta^{\mu\alpha} \Delta^{\nu\beta} u^\gamma \partial_\gamma \pi_{\alpha\beta} = \frac{2\eta\sigma^{\mu\nu} - \pi^{\mu\nu}}{\tau_\pi} - \frac{1}{2}\pi^{\mu\nu} \frac{\eta T}{\tau_\pi} \partial_\alpha \left( \frac{\tau_\pi u^\alpha}{\eta T} \right)$$

- ▶ bulk viscosity

$$u^\gamma \partial_\gamma \Pi = \frac{-\zeta \partial_\gamma u^\gamma - \Pi}{\tau_\Pi} - \frac{1}{2}\Pi \frac{\zeta T}{\tau_\Pi} \partial_\alpha \left( \frac{\tau_\Pi u^\alpha}{\zeta T} \right)$$

- ▶ viscosity corrections from velocity gradients
- ▶ **initial** stress tensor - pressure anisotropy
- ▶ equation of state

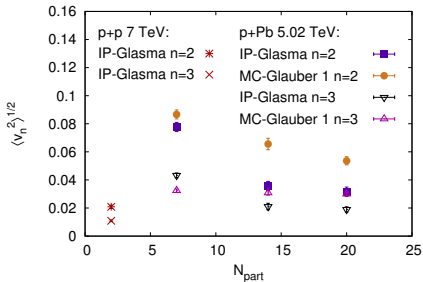
## fireball asymmetry - flow asymmetry



- Ev-by-Ev hydro response to geometry valid
- response strength depends on details

# Hydrodynamic flow in p-p?

- ▶ Humanic-nucl-th/0612098 (pythia, cascade)
- ▶ Romatschke, Luzum-arXiv:0901.4588 (overlap)
- ▶ Prasad, Roy, Chattopadhyay, Chaudhuri -arXiv: 0910.4844 (overlap)
- ▶ Bozek-arXiv: 0911.2393 (flux-tubes)
- ▶ Yan, Dong, Zhou, Li, Ma, Sa- arXiv: 0912.3342 (transport)
- ▶ Werner, Karpenko, Pierog, Bleicher, Mikhailov-arXiv: 1010.0400 (EPOS)
- ▶ Deng, Xu, Greiner-arXiv: 1112.0470 (hot-spots, transport model)
- ▶ Shuryak, Zahed-arXiv:1301.4470 (symmetric)
- ▶ Bzdak, Schenke, Tribedy, Venugopalan-arXiv: 1304.3403 (IP-Glasma)



Bzdak et al. arXiv: 1304.3403

- Is hydrodynamics valid?
- What is the initial eccentricity?

## Proton-Nucleus Collisions at the LHC: Scientific Opportunities and Requirements

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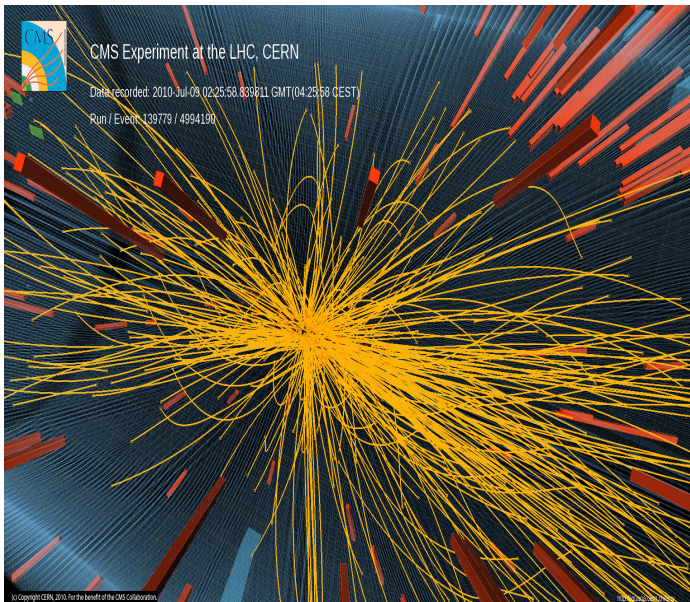
### Abstract

Proton-nucleus (p+A) collisions have long been recognized as a crucial component of the physics programme with nuclear beams at high energies, in particular for their reference role to interpret and understand nucleus-nucleus data as well as for their potential to elucidate the partonic structure of matter at low parton fractional momenta (small- $x$ ). Here, we summarize the main motivations that make a proton-nucleus run a decisive ingredient for a successful heavy-ion programme at the Large Hadron Collider (LHC) and we present unique scientific opportunities arising from these collisions. We also review the status of ongoing discussions about operation plans for the p+A mode at the LHC.

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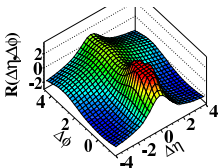
# High multiplicity events in pp



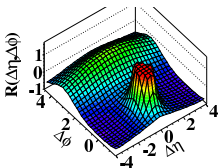


# Ridge in pp

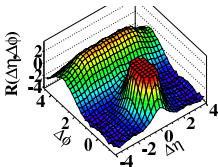
(a) CMS MinBias,  $p_T > 0.1 \text{ GeV}/c$



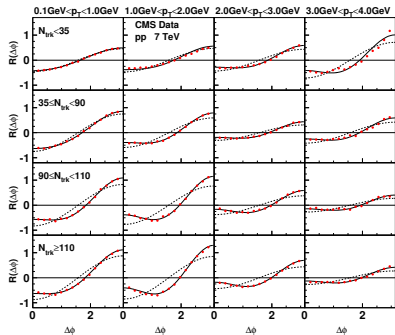
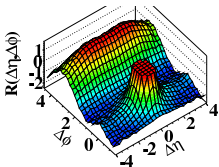
(b) CMS MinBias,  $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



(c) CMS  $N \geq 110$ ,  $p_T > 0.1 \text{ GeV}/c$



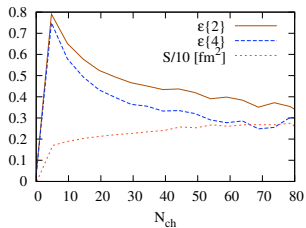
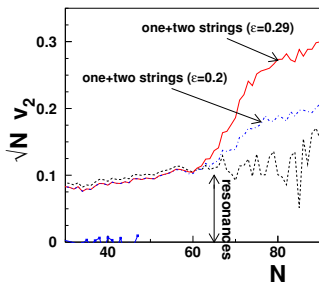
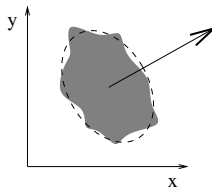
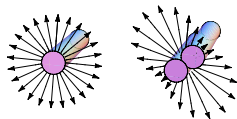
(d) CMS  $N \geq 110$ ,  $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



PB arXiv:1010.0405

can we measure (calculate)  $v_2$

# Fireball shape in pp



Bozek, 0911.2397

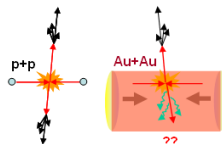
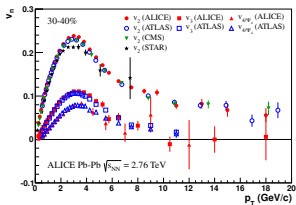
E.Asar et al., 1009.5643

Casalderrey-Solana, Wiedemann, 0911.4400

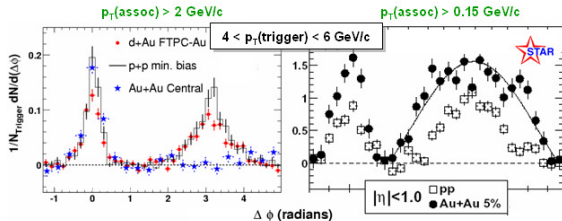
# sQGP formed in A-A collisions

## Jet quenching

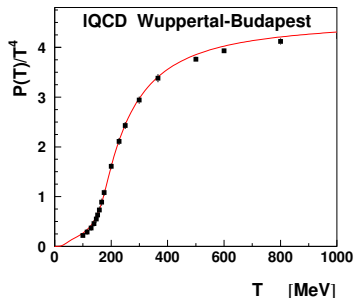
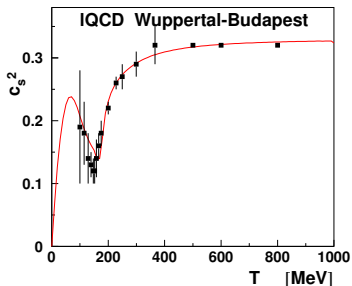
### sQGP



$$\frac{dN}{d\phi} \propto 1 + 2v_2 \cos(2(\phi - \Psi_2)) + 2v_3 \cos(3(\phi - \Psi_3)) + \dots$$



## equation of state - input



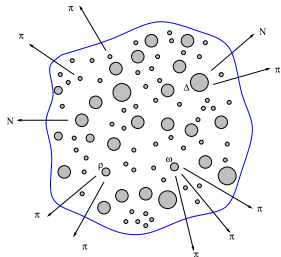
- ▶ lattice equation of state at high  $T$
- ▶ hadron gas at low temperature (know resonances from PDG)
- ▶ matching at  $T_c$  Laine, Schroder 2006, Chojnacki, Florkowski 2007, Huovinen, Petreczky 2009
- ▶ crossover - not first order phase transition

## freezeout

- ▶ density drops - hydrodynamic evolution stops
- ▶ usually surface of constant temperature
- ▶ particles emitted from fluid elements  
Cooper-Frye formula

$$E \frac{d^3 N}{dp^3} = \int d\Sigma_\mu p^\mu f[p_\mu u^\mu(x)]$$

- ▶ fluid velocity + thermal momenta
- ▶ latter - resonance decays  
and/or rescattering



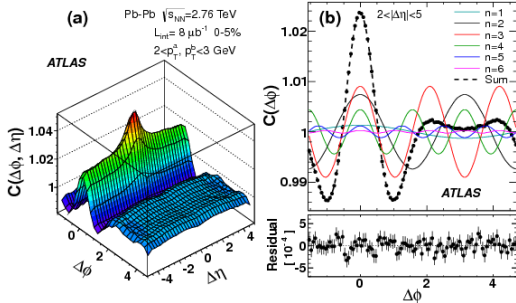
## two-particle correlations in relative azimuthal angle

$$C(\Delta\phi) \propto \int d\phi_1 d\phi_2 \delta(\phi_1 + \Delta\phi - \phi_2) \frac{dN}{d\phi_1 d\phi_2}$$

$$\propto 1 + 2v_1^2 \cos(\Delta\phi) + 2v_2^2 \cos(2\Delta\phi) + 2v_3^2 \cos(3\Delta\phi) + \dots$$

rms  $v_2$  can be measured from two-particle correlations

$$\sqrt{\langle v_2^2 \rangle} = \left\langle \frac{1}{N_{pair}} \sum_{ij} \cos(\phi_i - \phi_j) \right\rangle \text{ (cumulant method)}$$



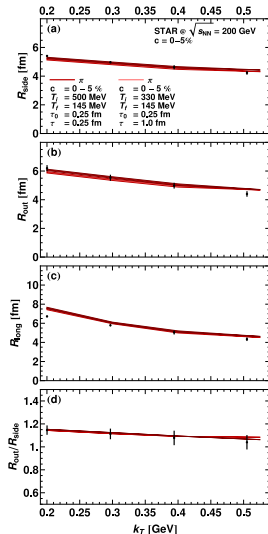
( $v_1$  - directed flow,  $v_3$  - triangular flow) odd harmonics from fluctuations - see below

# Hanbury Brown-Twiss (HBT) correlations

correlation between identical particles

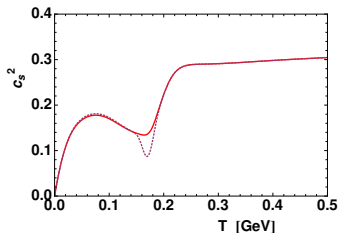
$$C(P, q) = \frac{N(p_1, p_2)}{N(p_1)N(p_2)}$$

$$C(q) = 1 + \lambda \exp[-q_S^2 R_s^2 - q_I^2 R_I^2 - q_O^2 R_O^2]$$

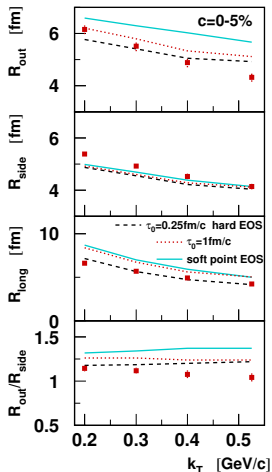


**HBT requires hard equation of state**

# OBSERVATION - hard equation of state



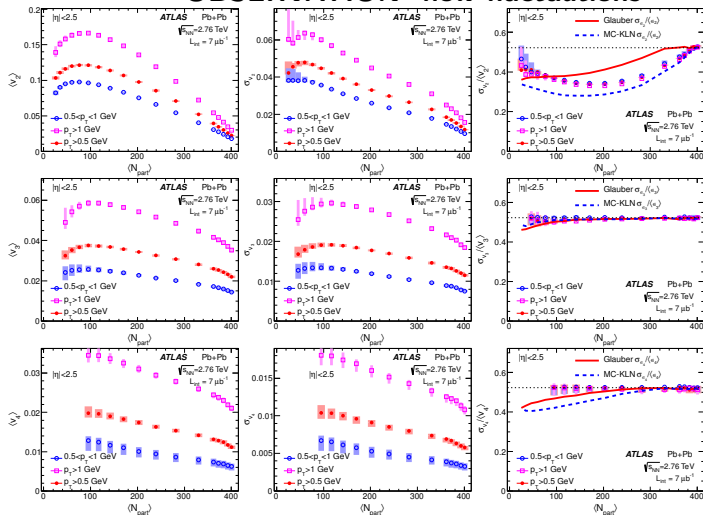
soft EOS - wrong HBT



Heavy-ion experiments consistent with lattice QCD

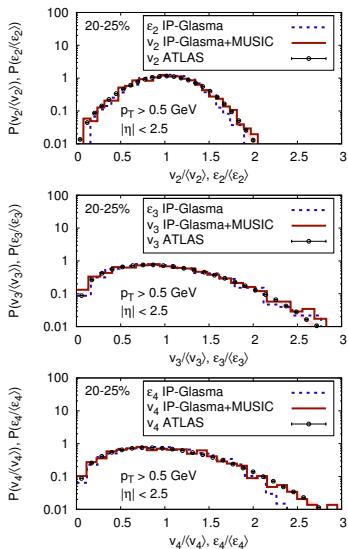


# OBSERVATION -flow fluctuations

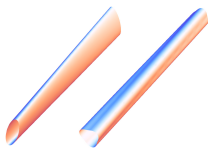


$\langle v_n \rangle$ ,  $\langle v_n^2 \rangle$  and the whole distribution of  $v_n$  can be reconstructed.

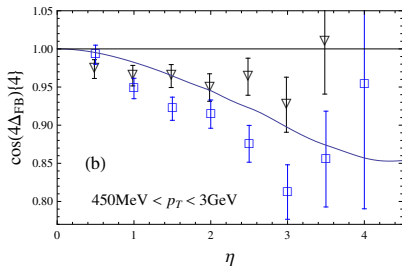
# good description of flow fluctuations with IP-glasma + hydro



event by event twist of the reaction plane



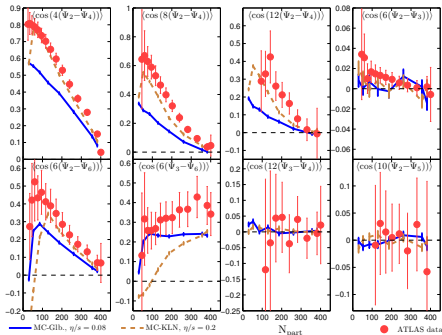
Fluctuating RP twist  
can be measured



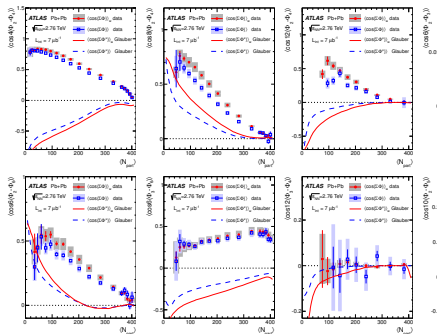
PB, Broniowski, Moreira, Phys. Rev. C83, 034911 (2011)

$$\cos(2k\Delta_{FB})\{4\} \equiv \frac{\langle e^{ik[(\phi_{F,1}+\phi_{F,2})-(\phi_{B,1}+\phi_{B,2})]} \rangle}{\langle e^{ik[(\phi_{F,1}-\phi_{F,2})-(\phi_{B,1}-\phi_{B,2})]} \rangle} = \langle \cos(2k\Delta_{FB}) \rangle_{\text{events}} + \text{nonflow}$$

# Event planes correlations



Bhalerao, Luzum, Ollitrault 2011, Qiu, Heinz 2012

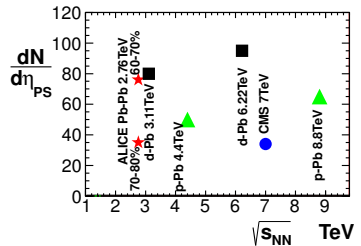


- ▶ correlations between EP  $\langle \cos(nm(\Phi_n - \Phi_m)) \rangle$ ,
- ▶ initial correlations
- ▶ nonlinearities of viscous hydrodynamics

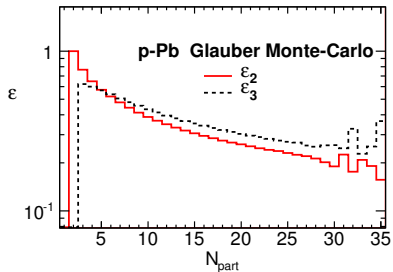
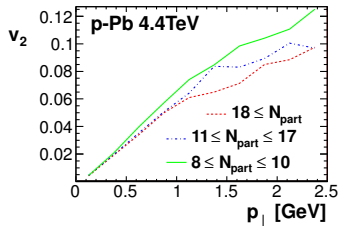
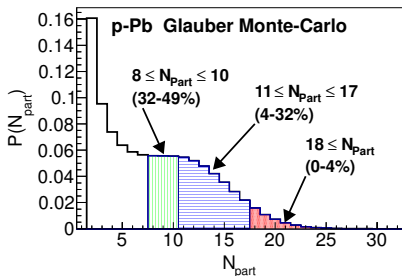


pA collision

p-Pb at 5.02TeV  
small dense fireball formed !



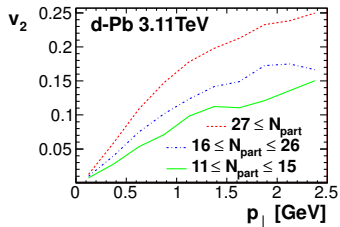
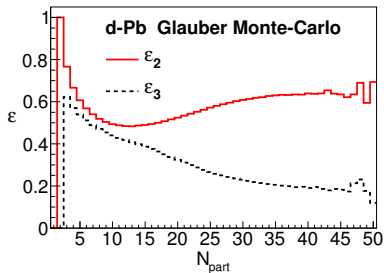
# Fireball in p-Pb



PB, arXiv:1112.0912

- ▶ collective flow effects  $\simeq$  peripheral Pb-Pb
- ▶ can be observed
- ▶ p-A (d-A) is not p-p superposition

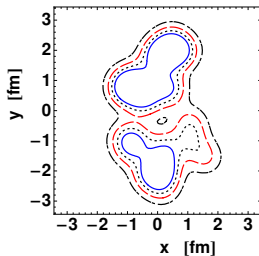
# d-Pb



large elliptic flow

PB, arXiv:1112.0912

small-on-large system  
with controlled eccentricity



# IP-glasma $\eta/s \simeq 0.2$

