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### Application of econometric and ecology analysis methods in physics software

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### Foreword

Due to limited time allocation, there is room only to highlight some basic concepts and to illustrate them in a few examples of application





# **Trend analysis**

• Statistical techniques to identify patterns in a series of data

- Ability to deal with noise

• Used to forecast the future (although it does not predict the future)

- But also to analyze past events

### • Tests for **statistical inference**: parametric and non parametric

- Test for randomness:  $H_0$  = random,  $H_1$  = monotonic trend/upward/downward
- Mann-Kendall test, Cox-Stuart test, Bartels test etc.

### • Related: change point detection

## Lehman laws

### M. M. Lehman, **Programs, Life Cycles, and Laws of Software Evolution,** *Proc. IEEE, vol. 68, no. 9, pp. 1060-1076, 1980*

### **1.** Continuing Change

A program that is used and that as an implementation of its specification reflects some other reality, undergoes continual change or becomes progressively less useful. The change or decay process continues until it is judged more cost effective to replace the system with a recreated version.

### 2. Increasing Complexity

- As an evolving program is continually changed, **its complexity**, *reflecting deteriorating structure*, **increases** unless work is done to maintain or reduce it.

# **Coupling between classes**

High CBO is undesirable

Excessive coupling between object classes is detrimental to modular design and prevents reuse A high coupling has been found to indicate fault-proneness

Chidamber and

Kemerer CBO



# Do I really need a statistical test to see a trend?

I can see a trend just by looking at the plot!

### What about seeing trends in 26581 plots?

How to objectively quantify what different eyes see? How to aggregate the trends observed in various plots?

processes/electromagnetic/utils

### Chidamber and Kemerer OO metrics

Abstract classes H<sub>0</sub>: random H<sub>1</sub>: upward **p-value < 0.01** 







### **Trends in software functionality** Electron backscattering simulation with Geant4



Trend of compatibility with experiment as a function of Geant4 version for different physics configurations

#### Geant4 version

Helpful guidance in algorithm development, optimization, regression testing, software maintenance...

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Geant4 version

# **Income inequality measures**

#### **Gini index** 1.0 $G = 2 \int_0^1 \left[ x - L(x) \right] dx$ Cumulative fraction of wealth 0.8 0.6 -perfect equality 0.4 1/2 Gini 0.2 Lorenz 0.0 0.0 0.2 0.6 0.8 1.0 0.4 Cumulative fraction of population

### The 62 richest people in the world are worth more than the poorest 50%



C. Gini, Variabilità e mutabilità : contributo allo studio delle distribuzioni e delle relazioni statistiche, 1912 Maria Grazia Pia, INFN Genova

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# **Pietra index**

AKA Ricci-Schutz index, Hoover index

$$\mathbf{P} = \max(L_{pe}(\mathbf{x}) - \mathcal{L}(\mathbf{x}))$$

 Used in derivative markets as a benchmark measure of statistical heterogeneity



Cumulative fraction of population

- Counterpart of Kolmogorov-Smirnov statistic
- It can be interpreted as the proportion of income that has to be transferred from those above the mean to those below the mean in order to achieve an equal distribution
  - Emphasis on individual-mean interaction

# **Other inequality measures**

**Theil index**  $T = \sum_{i=1}^{n} s_i \left[ \log s_i - \log(\frac{1}{n}) \right]$   $s_i = \text{share of the } i^{\text{th}} \text{ group in total income}$ n = total number of income groups

The same as **redundancy** in information theory: the maximum possible entropy of the data minus the observed entropy

### Atkinson index

$$I = 1 - \pi_e / \mu$$
 e = sensitivity parameter  $0 \le I \le 1$ 

Used to calculate the proportion of total income that would be required to achieve an equal level of social welfare as at present, if incomes were perfectly distributed

Theil I, Theil II, Kolm index, coefficient of variation, generalized entropy and more...13 Maria Grazia Pia, INFN Genova

# Halstead mental effort

#### geometry/solids



Geant4 version

Measure of the number of elemental mental discriminations necessary to create or understand a class



Cumulative fraction of Geant4 package





Cumulative fraction of Geant4 package ויומוום טומבומ ד ום, וו זו דע טטווטעם

processes/hadronic/models/low energy

0.37

0.8

25

0.8

1.0

1.0

Ξ

0.6

Cumulative fraction of Geant4 package

processes/scoring

Gini∠≐

Cumulative fraction of Geant4 package

0.6

0.4

geometry/solids



Geant4 9.6

- Geant4 4.0

0.2

0.4

distributed

software complexity

Geant4 10.2

Geant4 8.2

1.0

0.8

0.6

0.4

0.2

0.0

10

0.8

0.6

0.4

0.2

0.0

0.0

0.2

Cumulative fraction of CLhme

0.0

Cumulative fraction of CLhme

# **Gini and galaxies**

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#### A NEW APPROACH TO GALAXY MORPHOLOGY. I. ANALYSIS OF THE SLOAN DIGITAL SKY SURVEY EARLY DATA RELEASE

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THE ASTRONOMICAL JOURNAL, 128:163–182, 2004 July © 2004. The American Astronomical Society. All rights reserved. Printed in U.S.A.

#### A NEW NONPARAMETRIC APPROACH TO GALAXY MORPHOLOGICAL CLASSIFICATION

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#### THE GINI COEFFICIENT AS A TOOL FOR IMAGE FAMILY IDENITIFICATION IN STRONG LENSING SYSTEMS WITH MULTIPLE IMAGES

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Aggregate the capabilities of **Geant4 PhysicsLists** to reproduce experimental observables



Other econometric analysis methods: Concentration, Change point

Relation with methods used in ecology (e.g. analysis of diversity)

Information theory background

Comparative evaluation of measures and tests

**Decomposition** of inequality measures by subgroups

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Methods, applications to physics software and results will be documented in forthcoming papers

# Conclusion

- Statistical methods commonly used in other disciplines can be valuable in software and physics analysis
- Rich variety of econometric/ecology concepts and techniques
  - Trend, inequality, concentration, diversity, changepoint...
- Ongoing R&D to explore applications in physics software
  - To characterize software properties
  - To evaluate the behaviour of physics models
- A few highlights, no time for extensive presentation