

Beam-Beam Effects

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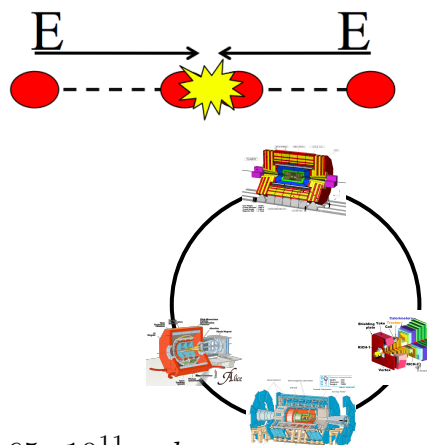
CERN Advanced Accelerator Physics School 2017
Royal Holloway University of London

Colliders

$$E^* \approx 2 \times E$$

$$N_{event/s} = L \cdot \sigma_{event}$$

$$L \propto \frac{N_p^2}{\sigma_x \sigma_y} \cdot n_b \cdot f_{rev}$$



Bunch intensity: $N_p = 1.15 - 1.65 \cdot 10^{11} \text{ ppb}$

Transverse Beam size: $\sigma_{x,y} = 16 - 30 \text{ } \mu m$

Number of bunches 1370 – 2808

Revolution frequency 11 kHz

$$L = 10^{34} \text{ cm}^{-2}\text{s}^{-1}$$

When do we have beam-beam effects?

➤ They occur when two beams get closer and collide

➤ Two types

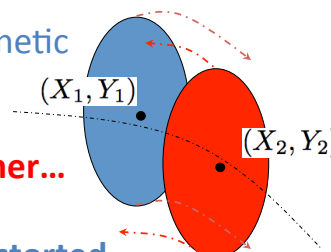
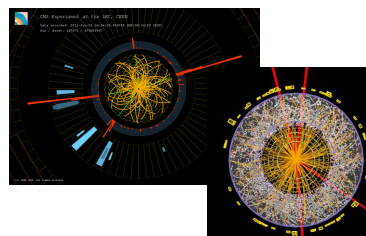
➤ High energy collisions between two particles (**wanted**)

➤ Distortions of beam by electromagnetic forces (**unwanted**)

➤ **Unfortunately: usually both go together...**

➤ **0.001% (or less) of particles collide**

➤ **99.999% (or more) of particles are distorted**



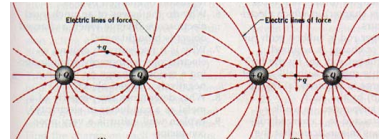
Beam-beam effects: overview

- **Circular Colliders:** interaction occurs at every turn and beams have to be preserved for hours (10-14 hours)
 - Many effects and problems
 - Try to understand some of them
 - Several Observations
- Overview of selected effects (single particle and multi-particle effects)
- Qualitative and physical picture of the effects
- Observations from colliders
- Mathematical derivations and more info in References [1,3,4] or at

Beam-beam webpage <http://lhc-beam-beam.web.cern.ch/lhc-beam-beam/>
And CAS Proceedings

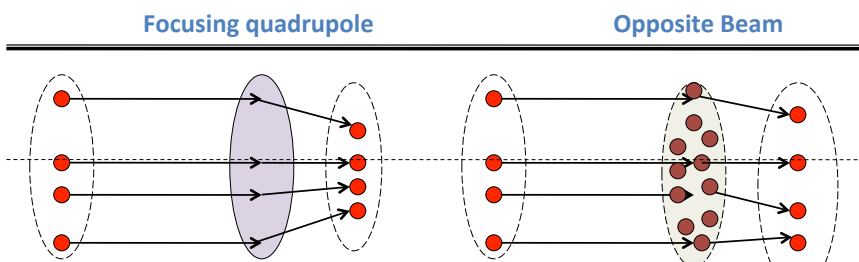
Beams EM potential

- Beam is a collection of charges
- Beam is an electromagnetic potential for other charges



Force on itself (**space charge**)
opposing beam (**beam-beam effects**)

Single particle motion and whole bunch motion **distorted**



A beam acts on particles like an electromagnetic lens, but...

Beam-Beam Mathematics

General approach in electromagnetic problems Reference[5] already applied to beam-beam interactions in Reference[1,3, 4]

$$\Delta U = -\frac{1}{\epsilon_0} \rho(x, y, z)$$

Derive potential from Poisson equation for charges with distribution ρ

Solution of Poisson equation

$$U(x, y, z, \sigma_x, \sigma_y, \sigma_z) = \frac{1}{4\pi\epsilon_0} \iiint \frac{\rho(x_0, y_0, z_0) dx_0 dy_0 dz_0}{\sqrt{(x-x_0)^2 + (y-y_0)^2 + (z-z_0)^2}}$$

$$\vec{E} = -\nabla U(x, y, z, \sigma_x, \sigma_y, \sigma_z)$$

Then compute the fields

$$\vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$$

From Lorentz force one calculates the force acting on test particle with charge q

Making some assumptions we can simplify the problem and derive analytical formula for the force...

Round Gaussian distribution:

Gaussian distribution for charges

Round beams:

Very relativistic, Force has only radial component :

$$\sigma_x = \sigma_y = \sigma$$

$$\beta \approx 1 \quad r^2 = x^2 + y^2$$

$$F \propto \frac{N_p}{\sigma} \cdot \frac{1}{r} \cdot \left[1 - e^{-\frac{r^2}{2\sigma^2}} \right]$$

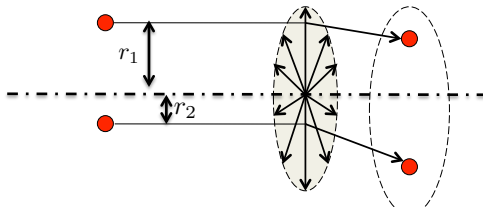
Beam-beam Force

$$\Delta r' = \frac{1}{mc\beta\gamma} \int F_r(r, s, t) dt$$

Beam-beam kick obtained
integrating the force over the
collision (i.e. time of passage)

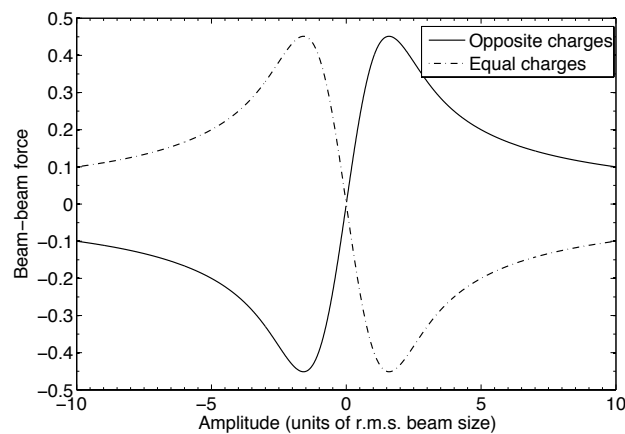
$$\Delta r' = -\frac{N_p r_0}{r} \cdot \frac{r}{r^2} \left[1 - e^{-\frac{r^2}{2\sigma^2}} \right]$$

Only radial component in
relativistic case



How does this force looks
like?

Beam-beam Force



$$F_r(r) = \pm \frac{ne^2(1 + \beta_{rel}^2)}{2\pi\epsilon_0} \frac{1}{r} \left[1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right]$$

Why do we care?

Pushing for luminosity means stronger beam-beam effects

$$\mathcal{L} \propto \frac{N_p^2}{\sigma_x \sigma_y} \cdot n_b$$

$$F \propto \frac{N_p}{\sigma} \cdot \frac{1}{r} \cdot \left[1 - e^{-\frac{r^2}{2\sigma^2}} \right]$$

Strongest non-linearity in a collider YOU CANNOT AVOID!

Physics fill lasts for many hours 10h – 24h



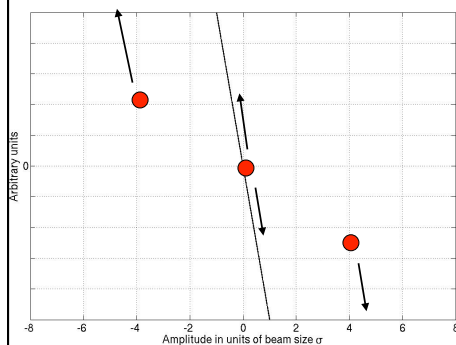
Two main questions:

What happens to a single particle?

What happens to the whole beam?

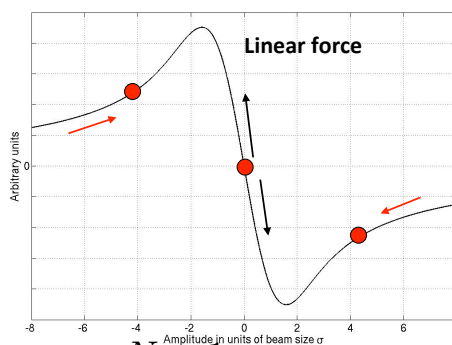
Beam-Beam Force: single particle...

Lattice defocusing quadrupole



$$F = -k \cdot r$$

Beam-beam force



$$F \propto \frac{N_p}{\sigma} \cdot \frac{1}{r} \cdot \left[1 - e^{-\frac{r^2}{2\sigma^2}} \right]$$

For small amplitudes: linear force

For larger amplitudes (x > 1 σ): very non-linear!

The beam will act as a strong non-linear electromagnetic lens!

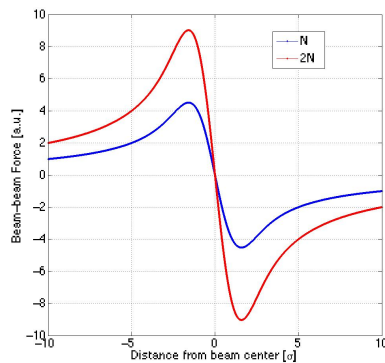
Beam-Beam parameter

Quantifies the strength of the force
but does NOT reflect the nonlinear
nature of the force

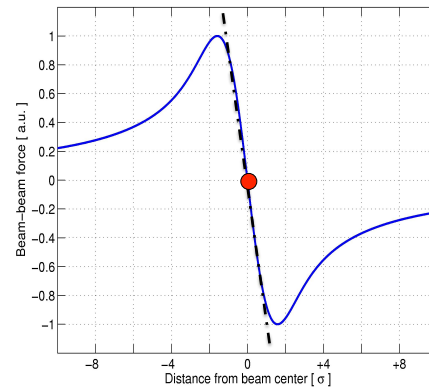
For small amplitudes $r \rightarrow 0$

$$F \propto -\xi \cdot r$$

The slope of the force gives you
the **beam-beam parameter** ξ



Beam-beam force



$$\Delta r' = -\frac{N_p r_0}{r} \cdot \frac{r}{r^2} \cdot \left[1 - e^{-\frac{r^2}{2\sigma^2}} \right]$$

$$\Delta r' = \frac{2N_p r_0}{\gamma} \cdot \frac{1}{r} \cdot \left[1 - \left(1 - \frac{r^2}{2\sigma^2} + \dots \right) \right]$$

Beam-Beam parameter:

For round beams:

$$\xi = \frac{\beta^*}{4\pi} \cdot \frac{\delta(\Delta r')}{\delta r} = \frac{N r_0 \beta^*}{4\pi \gamma \sigma^2}$$

For non-round beams:

$$\xi_{x,y} = \frac{N r_0 \beta_{x,y}^*}{2\pi \gamma \sigma_{x,y} (\sigma_x + \sigma_y)}$$

Examples:

Parameters	LEP (e ⁺ e ⁻)	LHC(pp)	LHC 2015	HL-LHC
Intensity N _{p,e} /bunch	4 10 ¹¹	1.15 10 ¹¹	1.7 10 ¹¹	2.2 10 ¹¹
Energy GeV	100	7000	6500	7000
Beam size H	160-200 μm	16.6 μm	18 μm	10 μm
Beam size V	2-4 μm	16.6 μm	18 μm	10 μm
β _{x,y} * m	1.25-0.05	0.55-0.55	0.4-0.4	0.15-0.15
Crossing angle μrad	0	285	290	590
$\xi_{bb/IP}$	0.08	0.0037	0.009	0.01

B-factory maximum beam-beam parameter of 0.16

1 turn map with linearized BB

For small amplitudes beam-beam can be approximated as linear force as a quadrupole

$$F \propto -\xi \cdot r$$

Focal length:
$$\frac{1}{f} = \frac{\Delta x'}{x} = \frac{Nr_0}{\gamma\sigma^2} = \frac{\xi \cdot 4\pi}{\beta^*}$$

Beam-beam matrix:
$$\begin{pmatrix} 1 & 0 \\ -\frac{\xi \cdot 4\pi}{\beta^*} & 1 \end{pmatrix}$$

Perturbed one turn matrix with perturbed tune ΔQ and beta function at the IP β^* :

$$\begin{pmatrix} \cos(2\pi(Q + \Delta Q)) & \beta^* \sin(2\pi(Q + \Delta Q)) \\ -\frac{1}{\beta^*} \sin(2\pi(Q + \Delta Q)) & \cos(2\pi(Q + \Delta Q)) \end{pmatrix} \\ = \begin{pmatrix} 1 & 0 \\ -\frac{1}{2f} & 1 \end{pmatrix} \cdot \begin{pmatrix} \cos(2\pi Q) & \beta_0^* \sin(2\pi Q) \\ -\frac{1}{\beta_0^*} \sin(2\pi Q) & \cos(2\pi Q) \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 \\ -\frac{1}{2f} & 1 \end{pmatrix}$$

Linear tune shift and beta beating

Solving the one turn matrix one can derive the tune shift ΔQ and the perturbed beta function at the IP β^* :

Tune is changed

$$\cos(2\pi(Q + \Delta Q)) = \cos(2\pi Q) - \frac{\beta_0^* \cdot 4\pi\xi}{\beta^*} \sin(2\pi Q)$$

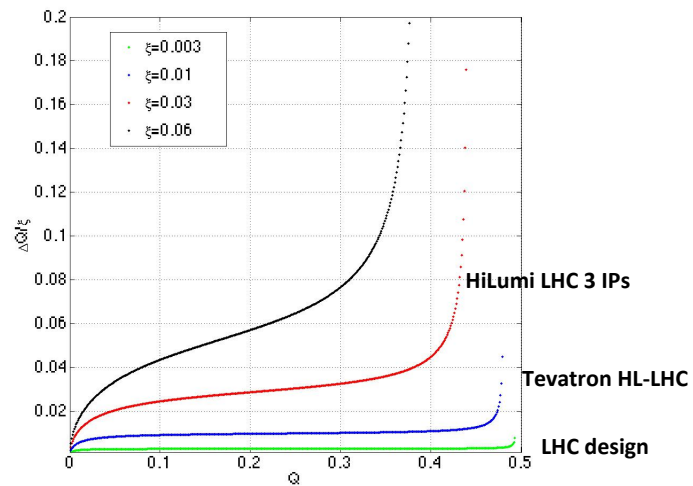
β -function is changed:

$$\frac{\beta^*}{\beta_0^*} = \frac{\sin(2\pi Q)}{\sin(2\pi(Q + \Delta Q))}$$

...how do they change?

Tune dependence of tune shift and dynamic beta

Tune shift as a function of tune

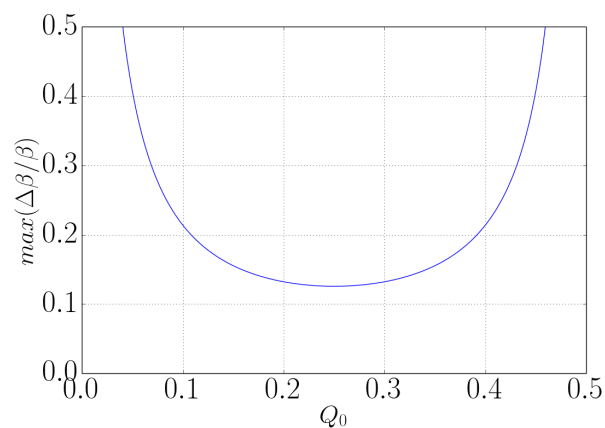


Larger ξ ➔ Strongest variation with Q

Dynamic beta-beating due to beam-beam effects

Maximum beta change as a function of unperturbed tune

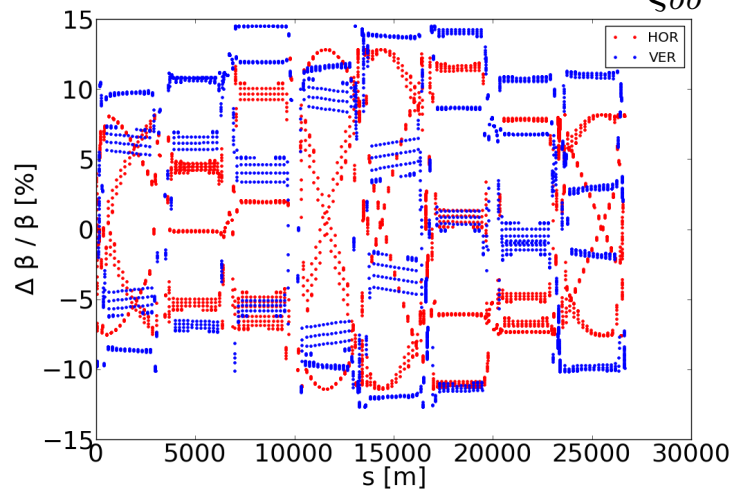
$$\max \left(\frac{\Delta\beta}{\beta} \right) = \frac{2\pi\xi}{\sin(2\pi Q_0)} \quad \xi_{bb} = 0.02$$



Maximum beating as a function of tune

Dynamic beta-beating due to beam-beam effects

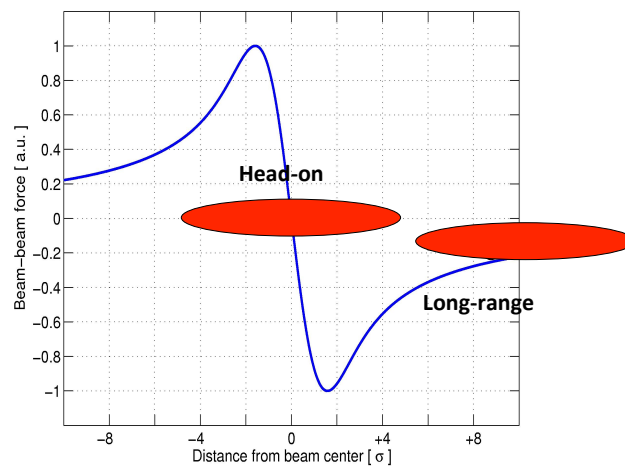
$$\xi_{bb} = 0.02$$



From optics codes beating along the accelerator

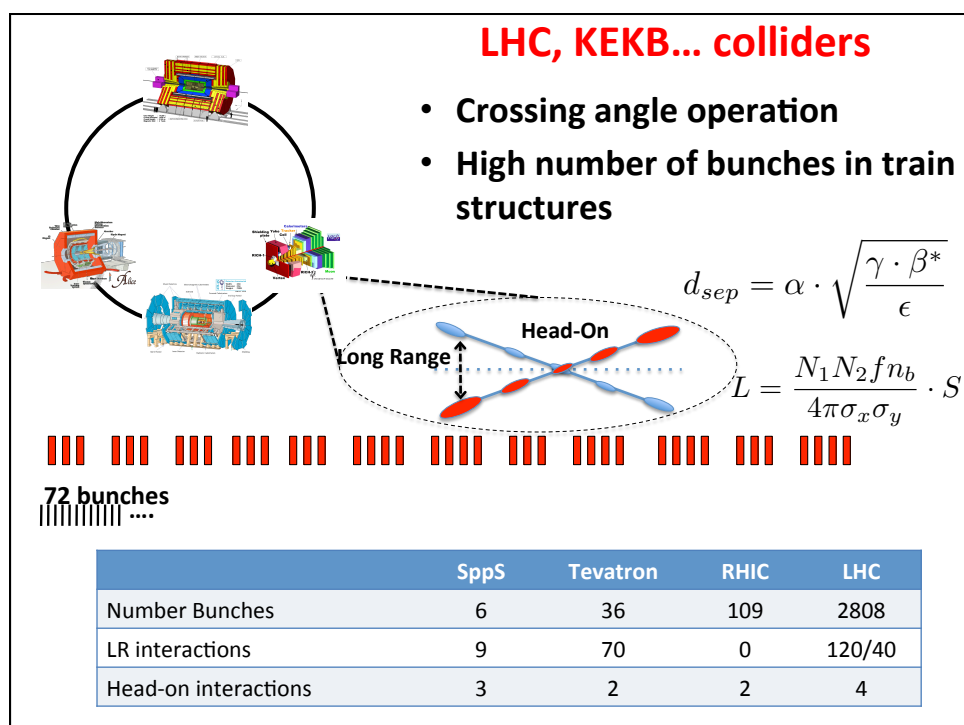
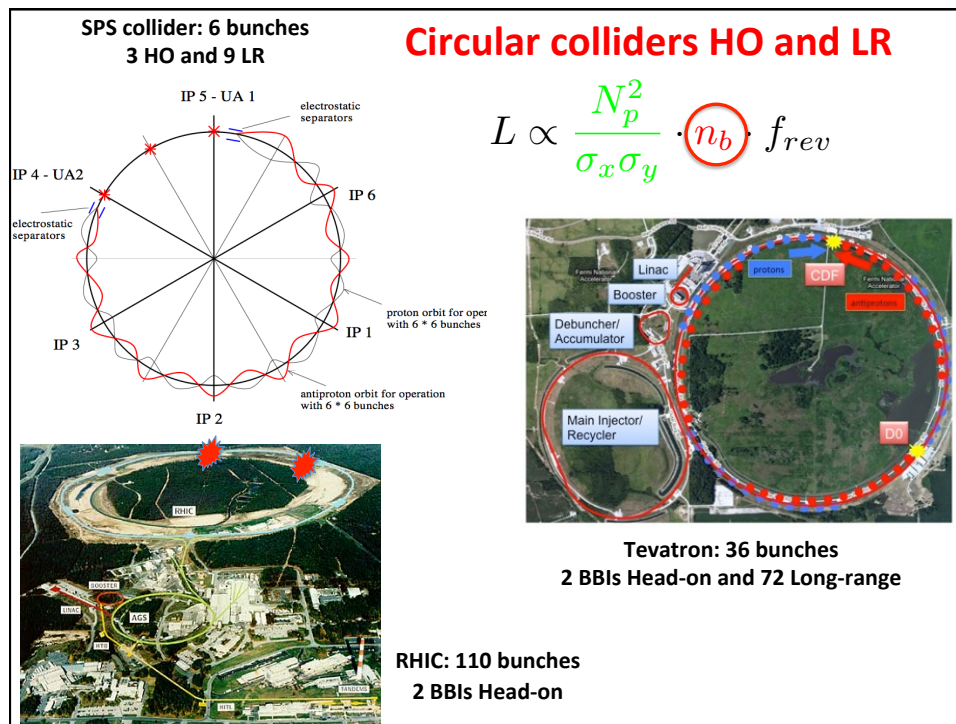
Head-on and Long-range interactions

Beam-beam force

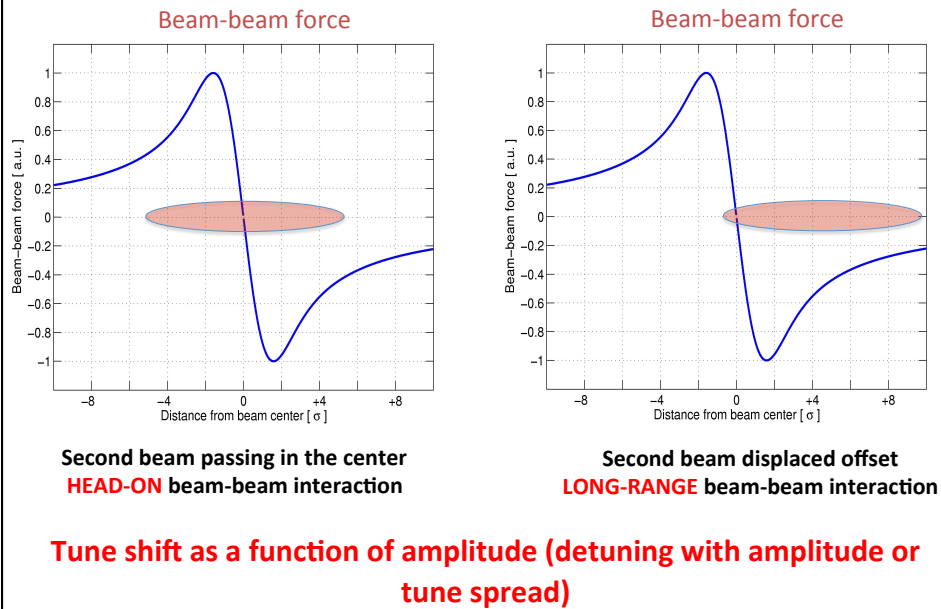


Other beam passing in the center force: **HEAD-ON** beam-beam interaction

Other beam passing at an offset of the force: **LONG-RANGE** beam-beam interaction

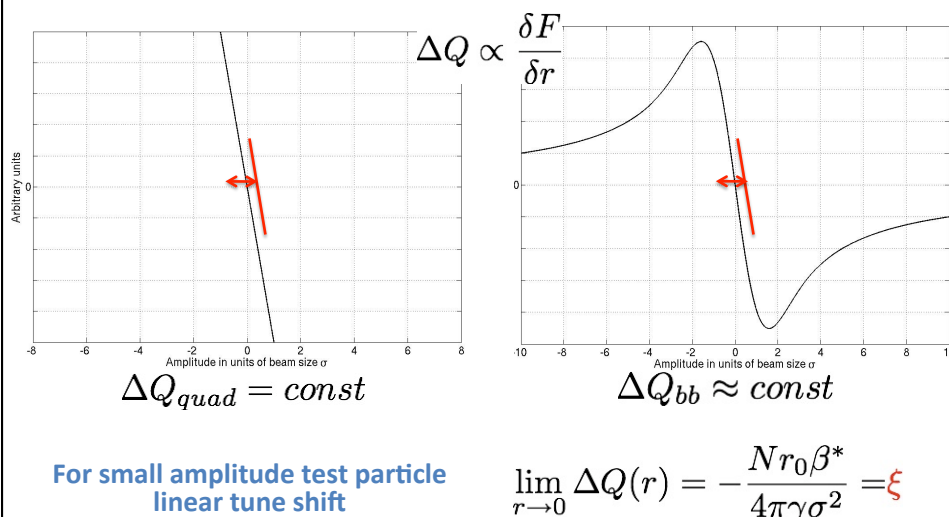


A beam will experience all the force range



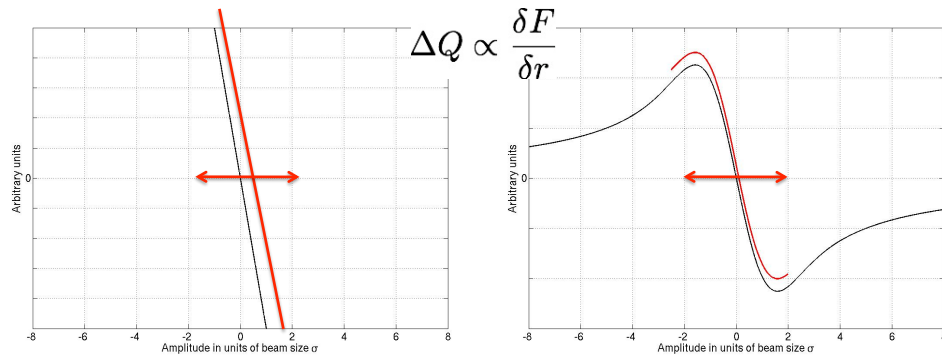
Detuning with Amplitude for head-on

Instantaneous tune shift of test particle when it crosses the other beam is related to the derivative of the force with respect to the amplitude



Detuning with Amplitude for head-on

Beam with many particles this results in a tune spread



$$\Delta Q_{quad} = const$$

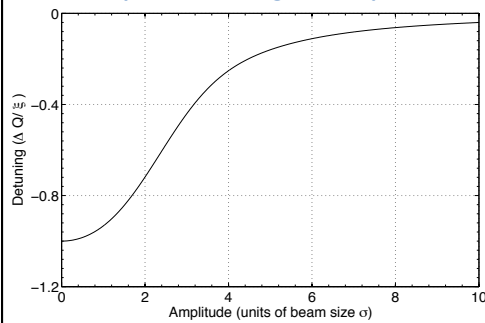
$$\Delta Q_{bb} \neq const$$

$$\Delta Q(x) = \frac{Nr_0\beta}{4\pi\gamma\sigma^2} \cdot \frac{1}{(\frac{x}{2})^2} \cdot (\exp -(\frac{x}{2})^2 I_0(\frac{x}{2})^2 - 1)$$

Mathematical derivation in Ref [3] using Hamiltonian formalism and in
Ref [4] using Lie Algebra

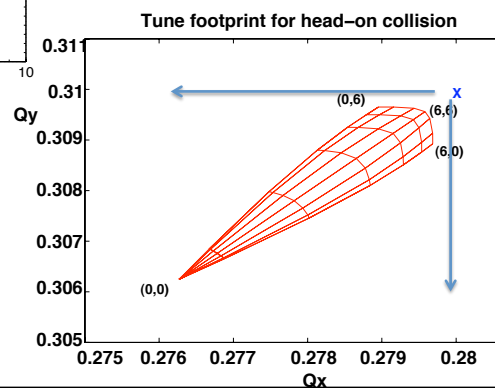
Head-on detuning with amplitude and footprints

1-D plot of detuning with amplitude

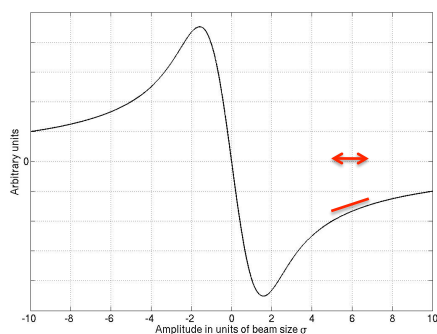


And in the other plane?
THE SAME DERIVATION
same tune spread

FOOTPRINT
2-D mapping of the detuning with
amplitude of particles



And for long-range interactions?

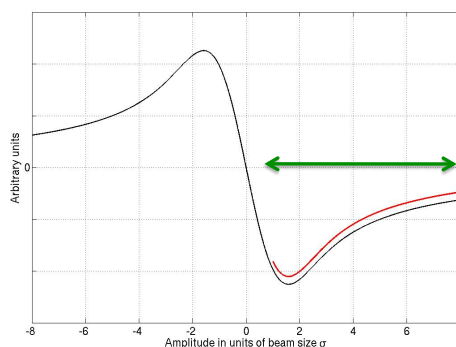


Second beam centered at d (i.e. 6σ)

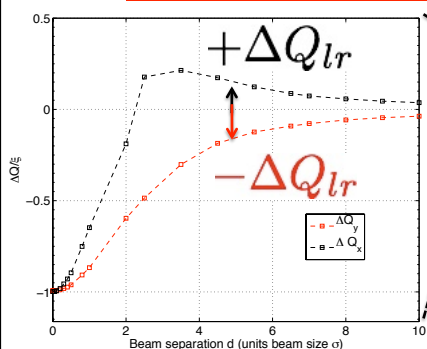
- Small amplitude particles **positive** tune shifts
- Large amplitude can go to **negative** tune shifts

Long range tune shift scaling for distances $d > 6\sigma$

$$\Delta Q_{lr} \propto -\frac{N}{d^2}$$

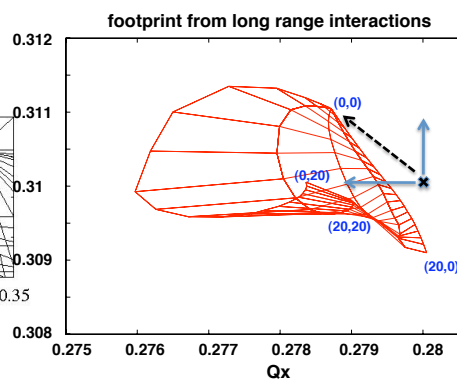
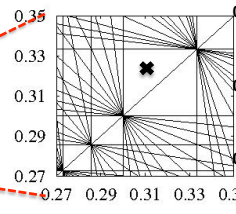
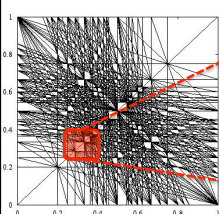


Beam-beam tune shift and speed: LRs

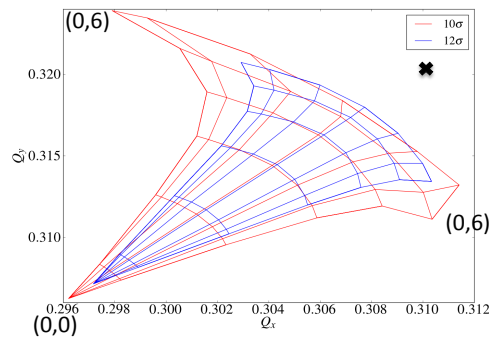


Tune shift as a function of separation in horizontal plane

- In the horizontal plane long range tune shift
- In the vertical plane opposite sign!



Beam-beam tune shift and spread: HO + LRs

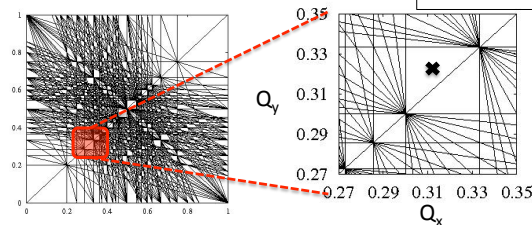


Footprints depend on:

- number of interactions (124 per turn)
- Type (Head-on and long-range)
- Separation
- Plane of interaction

Very complicated depending on collision scheme

Pushing luminosity increases this area while we need to keep it small to avoid resonances and preserve the stability of particles



Difficult to avoid resonances!

Complications

PACMAN and SUPER PACMAN bunches

$$L \propto \frac{N_p^2}{\sigma_x \sigma_y} \cdot n_b \cdot f_{rev}$$



72 bunches

|||||

Pacman:

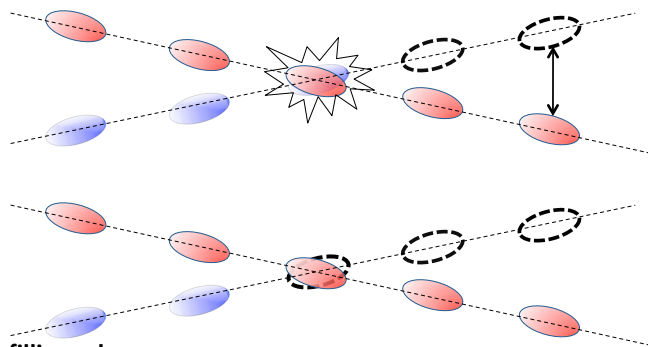
miss long range BBI

(120-40 LR interactions)

Super Pacman:

miss head-on BBI

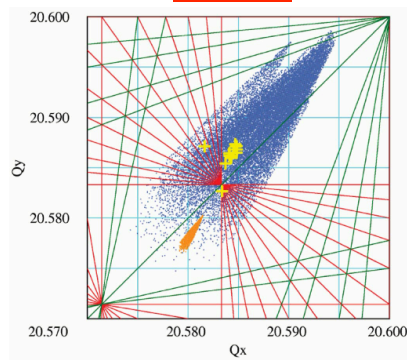
IP2 and IP8 depending on filling scheme



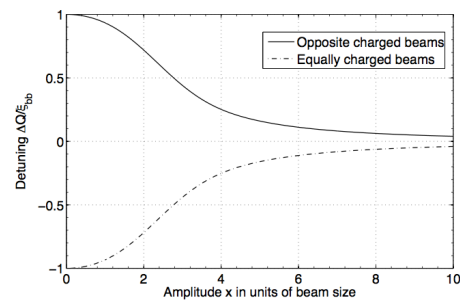
Different bunch families: Pacman and Super Pacman

Pacman and Super-pacman

Tevatron



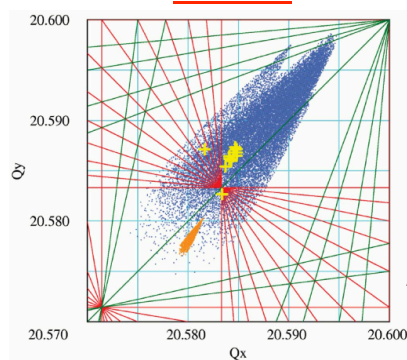
Antiproton bunches footprint (blue)
Proton bunches footprint (orange)



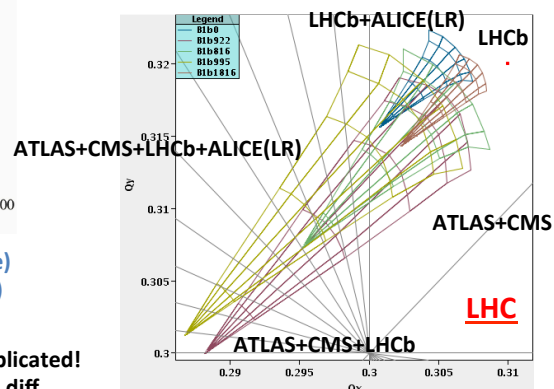
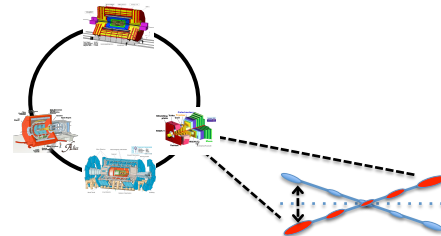
...operationally it is even more complicated!
...intensities differences, emittances diff...

Pacman and Super-pacman

Tevatron



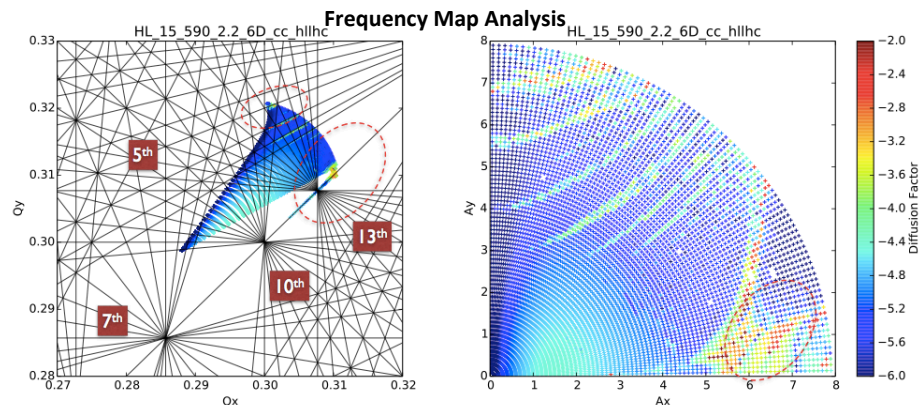
Antiproton bunches footprint (blue)
Proton bunches footprint (orange)



...operationally it is even more complicated!
...intensities differences, emittances diff...

Non-linear dynamics and Particle Losses

Dynamic Aperture: area in amplitude space with stable motion
 Stable area of particles depends on beam intensity and crossing angle



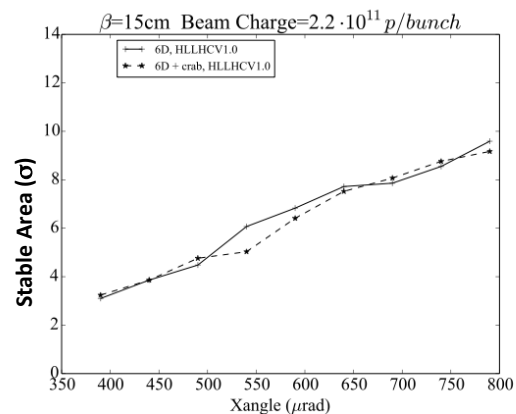
Stable area depends on beam-beam interactions therefore the choice of running parameters (crossing angles, β^* , intensity) is the result of careful study of different effects!

Ref [6]

Non-linear dynamics and Particle Losses

Dynamic Aperture: area in amplitude space with stable motion
 Stable area of particles depends on beam intensity and crossing angle

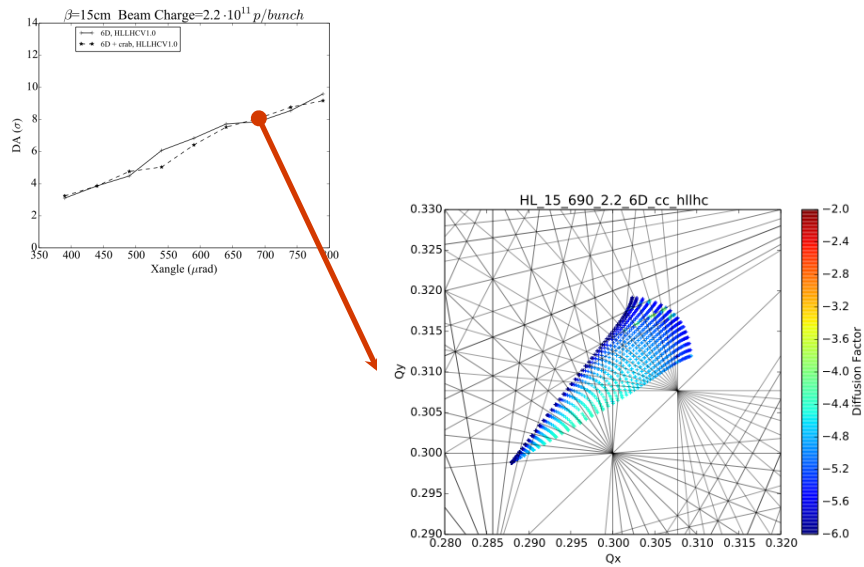
$$d_{sep} = \alpha \cdot \sqrt{\frac{\gamma \cdot \beta^*}{\epsilon}}$$



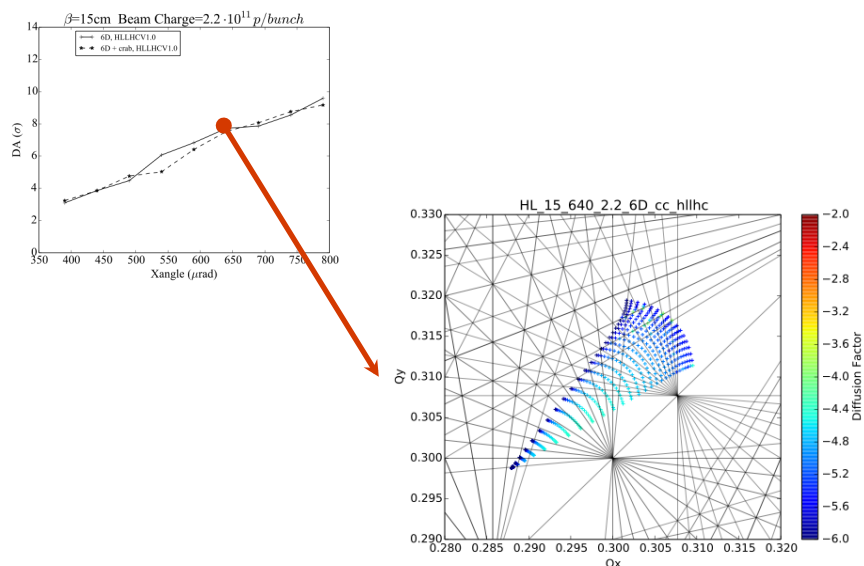
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Ref [6]

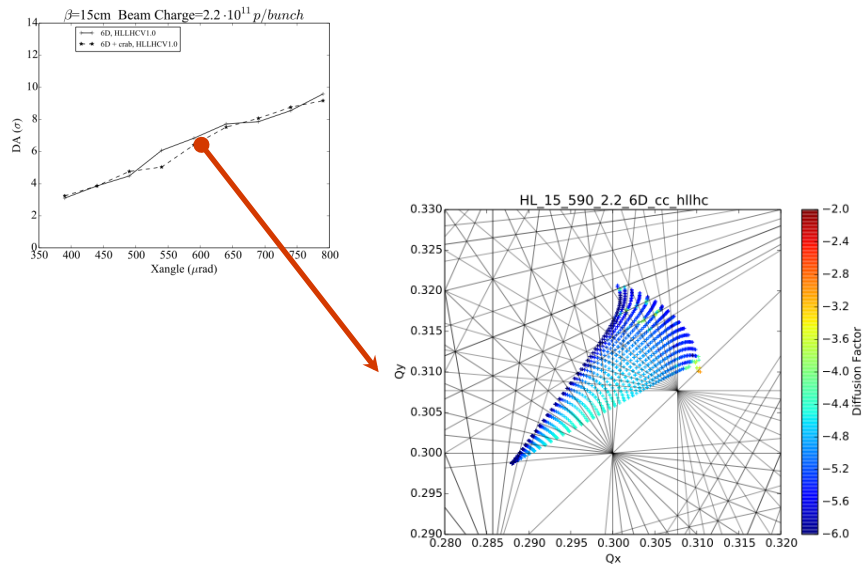
Non-linear dynamics and Particle Losses



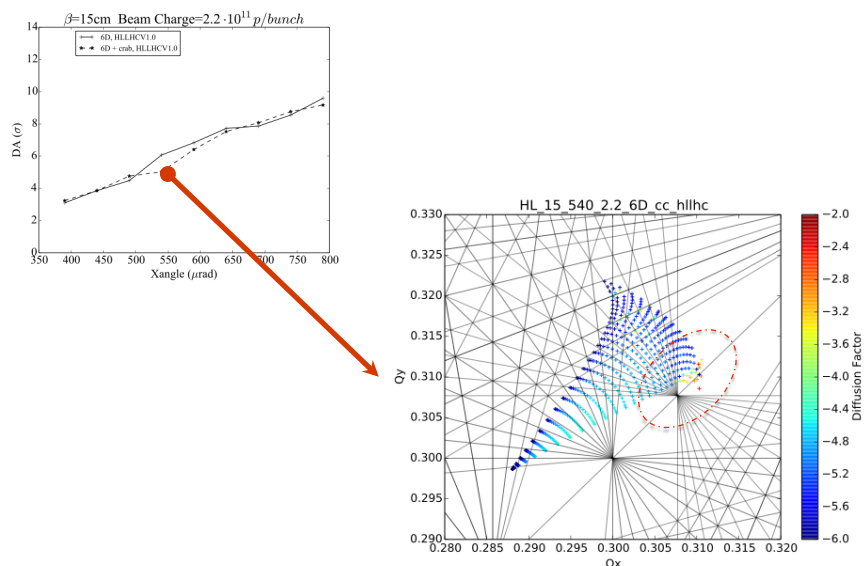
Non-linear dynamics and Particle Losses



Non-linear dynamics and Particle Losses

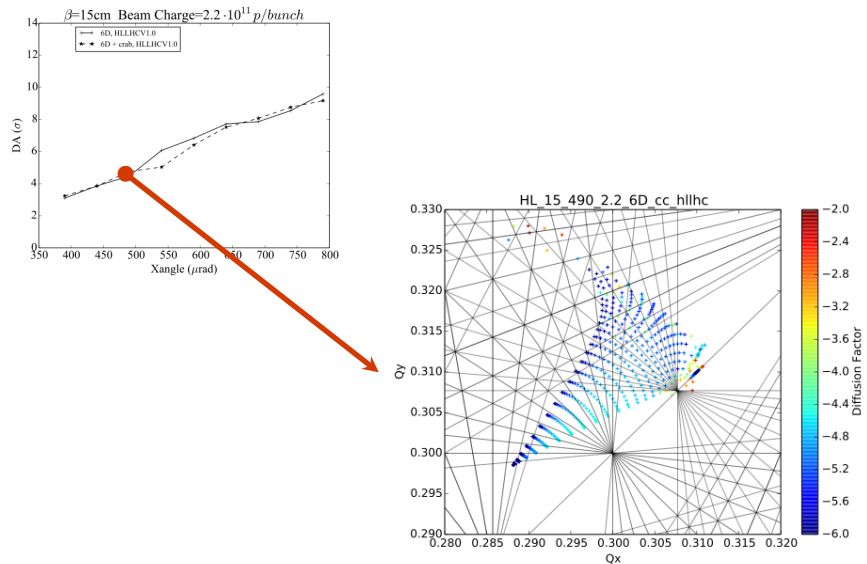


Non-linear dynamics and Particle Losses



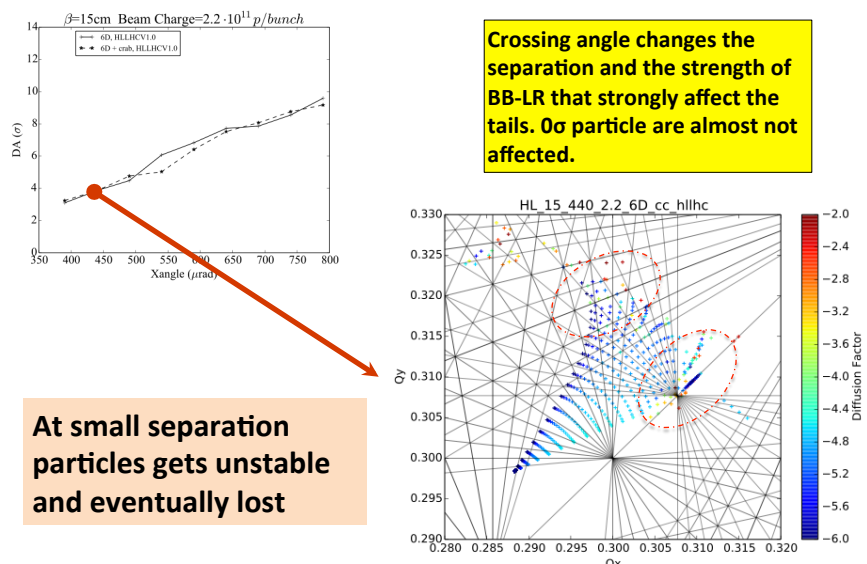
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Non-linear dynamics and Particle Losses



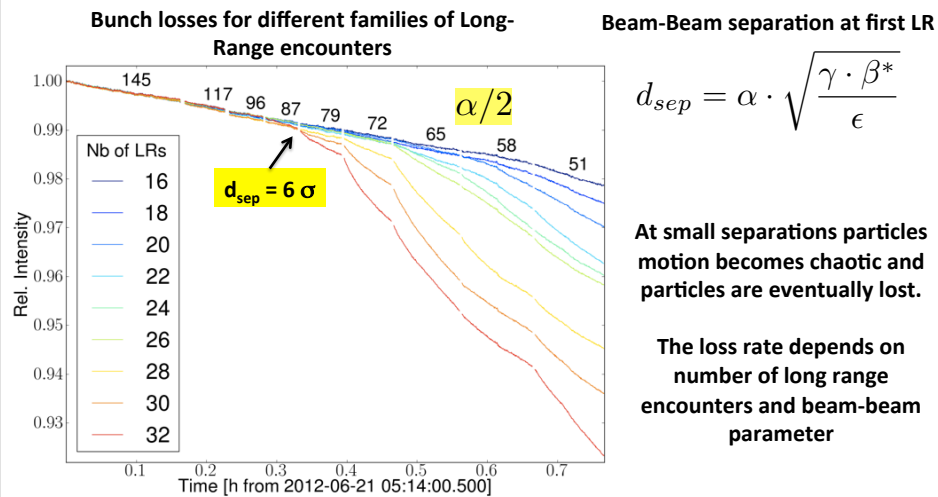
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Non-linear dynamics and Particle Losses



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Non-linear dynamics and Particle Losses



The on-set of losses and the loss rates can be related to dynamic aperture

Long-range BB and Orbit Effects

Long Range Beam-beam interactions lead to orbit effects

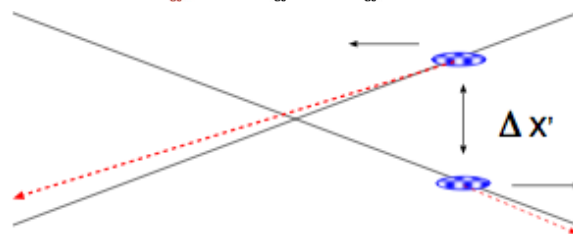
Long range kick

$$\Delta x'(x+d, y, r) = -\frac{2Nr_0}{\gamma} \frac{(x+d)}{r^2} [1 - \exp(-\frac{r^2}{2\sigma^2})]$$

For well separated beams $d \gg \sigma$

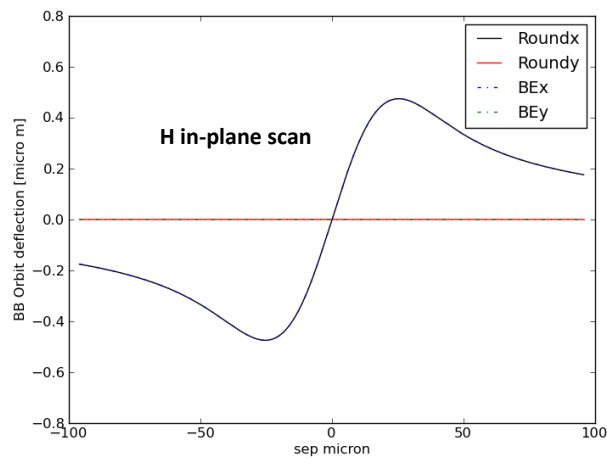
The force has an amplitude independent contribution: **ORBIT KICK**

$$\Delta x' = \frac{const}{d} [1 - \frac{x}{d} + O(\frac{x^2}{d^2}) + \dots]$$



Orbit can be corrected but we should remember PACMAN effects

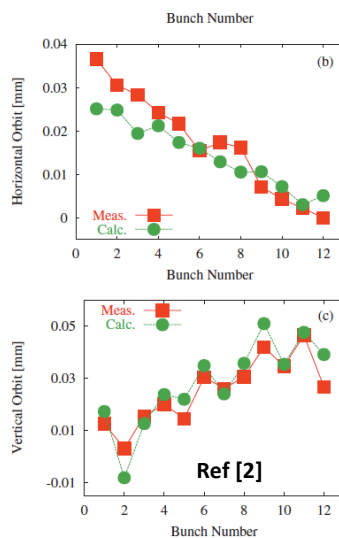
Orbit effect as a function of separation



Angular Deflections:
$$\theta_y + i\theta_x = \frac{2r_p}{\gamma} N_p F_0(x, y, \Sigma)$$

Closed Orbit effect:
$$Orb_{x,y} = \theta_{x,y} \cdot \beta_{x,y} \cdot \frac{1}{2 \tan(\pi \cdot Q_{x,y})}$$

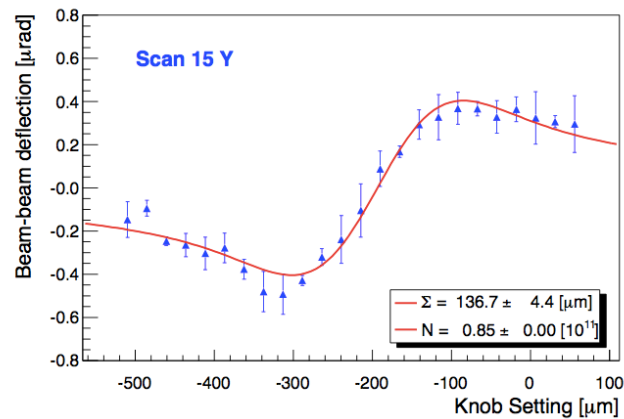
Tevatron orbit effects



Beam-beam single bunch orbit
can be well reproduced and
measured also in LEP

Effects can become important
(1 σ offset not impossible)

Orbit effect as a function of separation



Angular Deflections:
$$\theta_y + i\theta_x = \frac{2r_p}{\gamma} N_p F_0(x, y, \Sigma)$$

Closed Orbit effect:
$$Orb_{x,y} = \theta_{x,y} \cdot \beta_{x,y} \cdot \frac{1}{2 \tan(\pi \cdot Q_{x,y})}$$

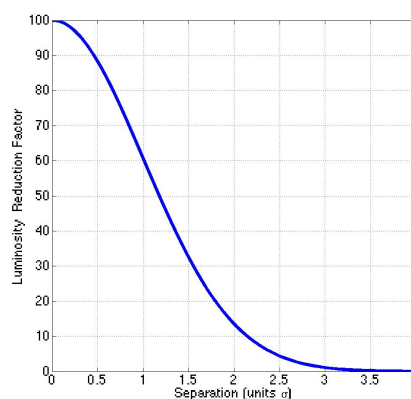
Orbit can be corrected but we should remember PACMAN effects

LHC observations

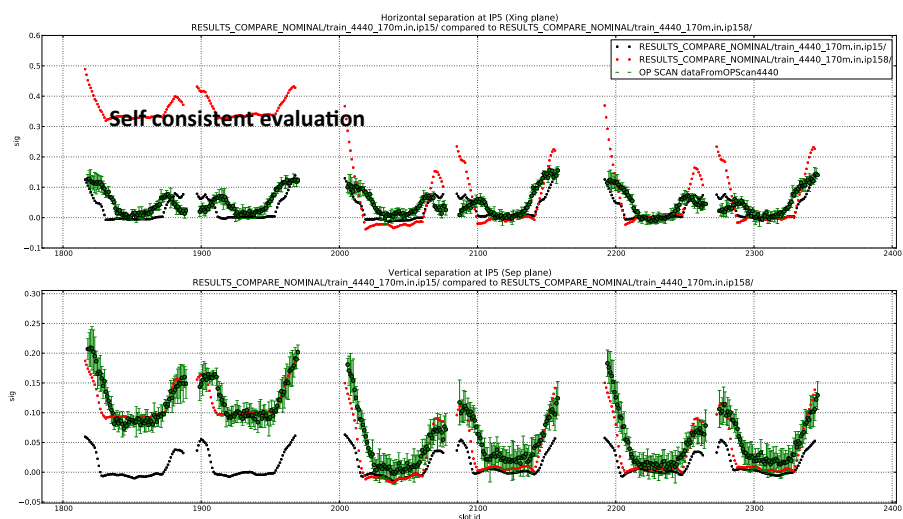
Many long range interactions could become important effect!
Holes in bunch structure leads to PACMAN effects this cannot be corrected!

$$L = L_0 \cdot e^{-\frac{d^2}{4\sigma_x^2}}$$

Orbit Effects due to long-range beam-beam effects should be kept SMALL to avoid loss of luminosity!

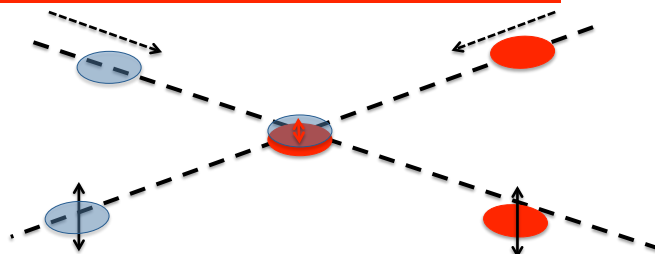


LHC observations vs simul



LUMINOSITY Deterioration

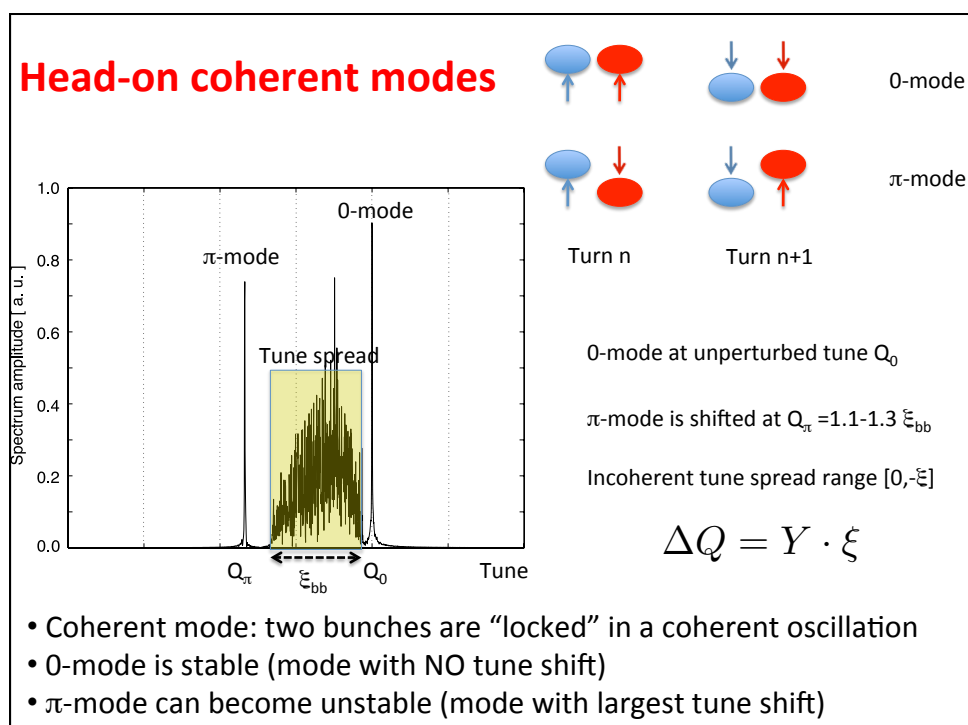
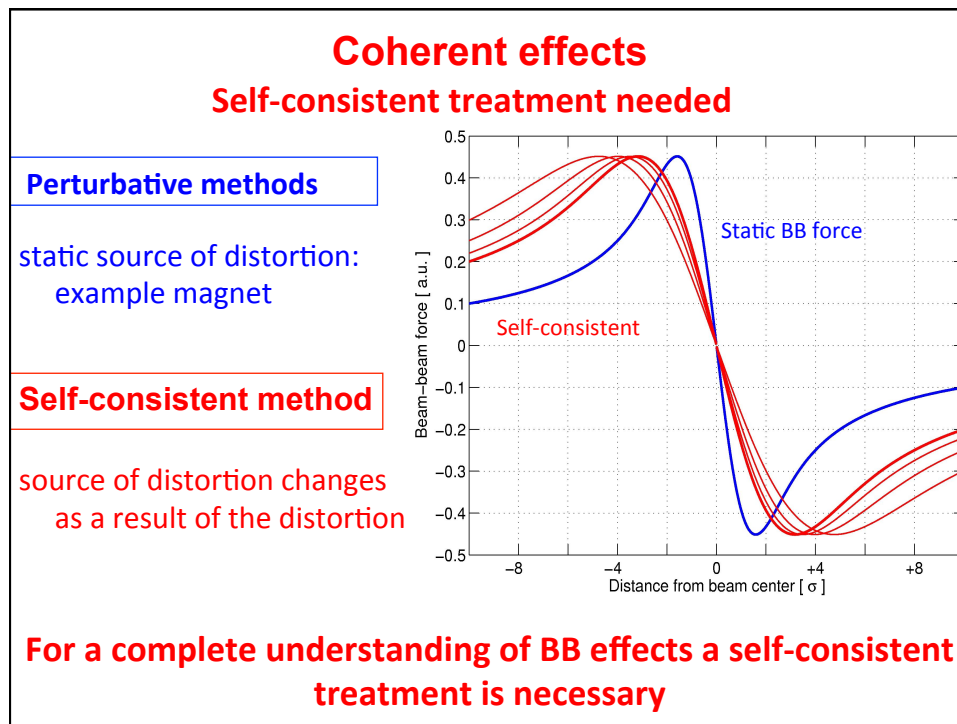
Coherent beam-beam effects



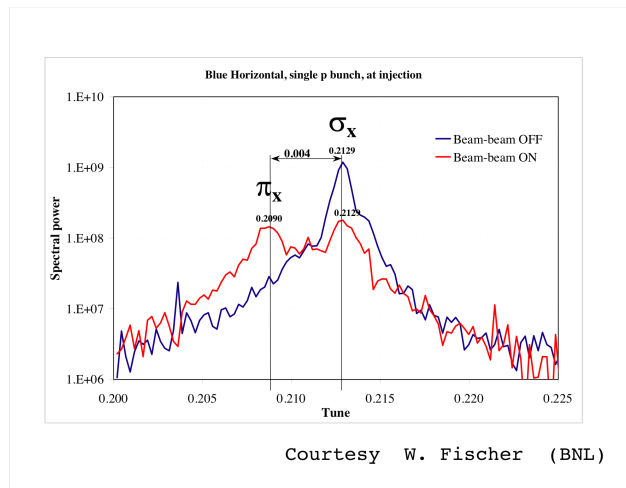
- Whole bunch sees a kick as an entity (**coherent kick**)
- Coherent **kick seen by full bunch** different from single particle kick
- Requires **integration** of individual kick over particle distribution

$$\Delta r' = -\frac{N_p r_0}{r} \cdot \frac{r}{r^2} \cdot \left[1 - e^{-\frac{r^2}{4\sigma^2}} \right]$$

- Coherent kick of separated beams can excite coherent **dipolar oscillations**
- All bunches couple because each bunch “sees” many opposing bunches(LR): **many coherent modes** possible!



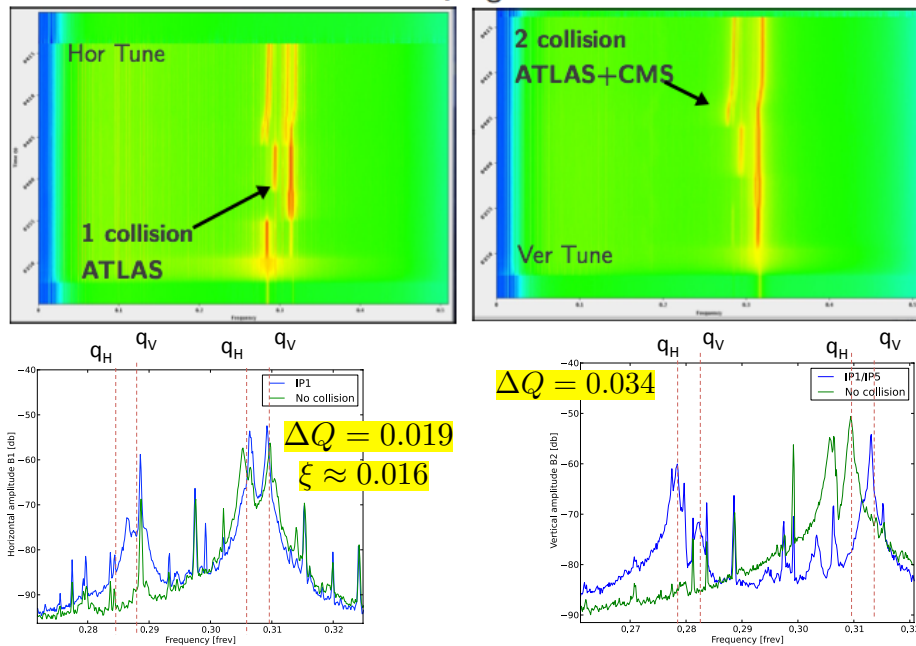
Coherent modes at RHIC



Tune spectra before collision and in collision two modes visible

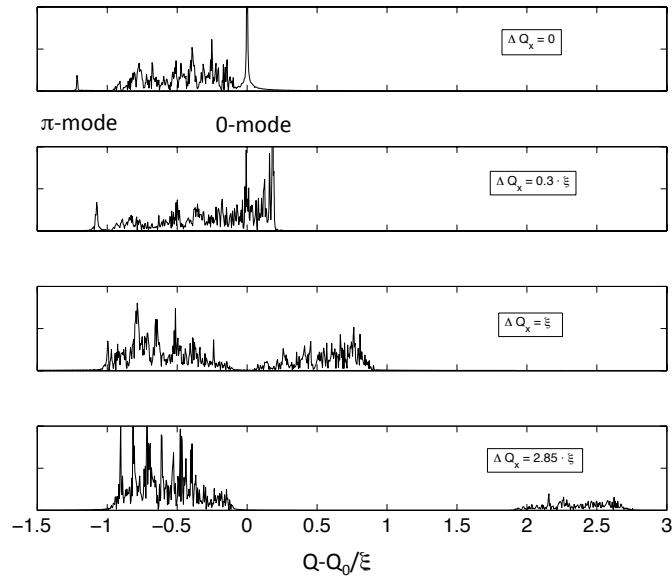
Head-on beam-beam coherent modes in the LHC

BBQ Signals



Breaking of coherent motion: Tune split

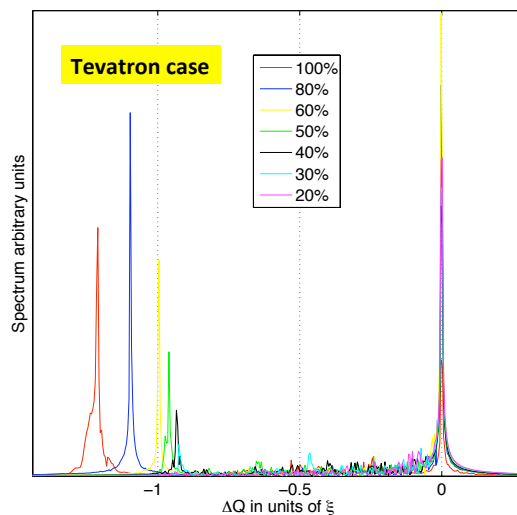
RHIC case



Tune split breaks symmetry and coherent modes disappear

Analytical calculations in Reference [8]

Breaking of coherent motion: Intensity ratio



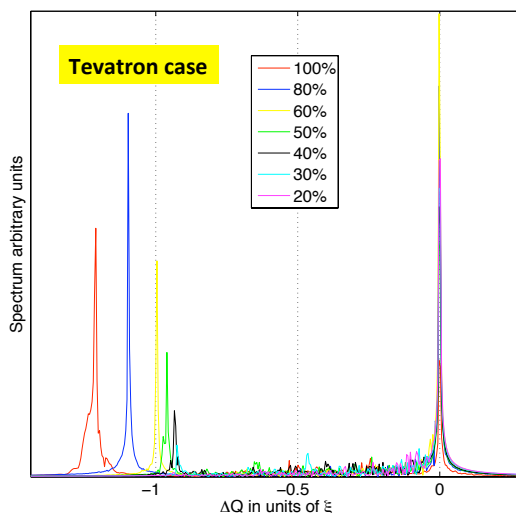
For two bunches colliding head-on in one IP the coherent mode disappears if intensity ratio between bunches is 55% Reference[9]

We assumed:

- equal emittances
- equal tunes
- NO PACMAN effects
(bunches will have different tunes)

For coherent modes the key is to break the symmetry in your coupled system...(tunes, intensities, collision patterns, ...)!

Breaking of coherent motion: Intensity ratio



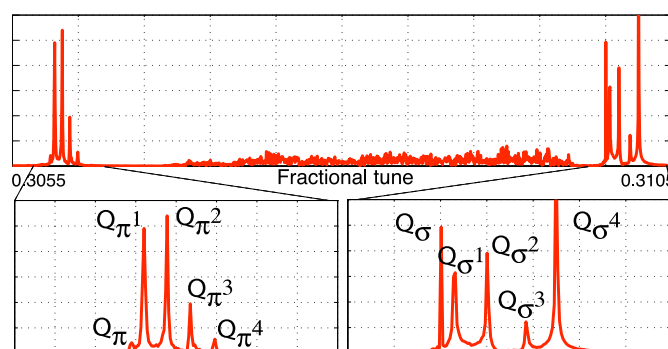
For two bunches colliding head-on in one IP the coherent mode disappears if intensity ratio between bunches is 55% Reference[9]

We assumed:

- equal emittances
- equal tunes
- NO PACMAN effects
(bunches will have different tunes)

or to merge the modes into the incoherent spread!

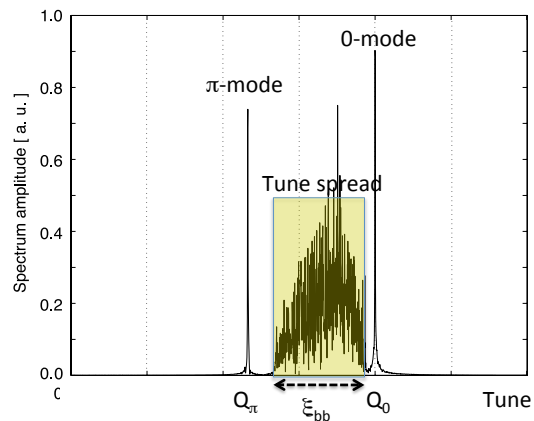
Long-range coherent modes



Pacman bunch will have different number of modes
Could drive instabilities if coupled to impedance driven modes...

Cannot be damped by incoherent spread...!

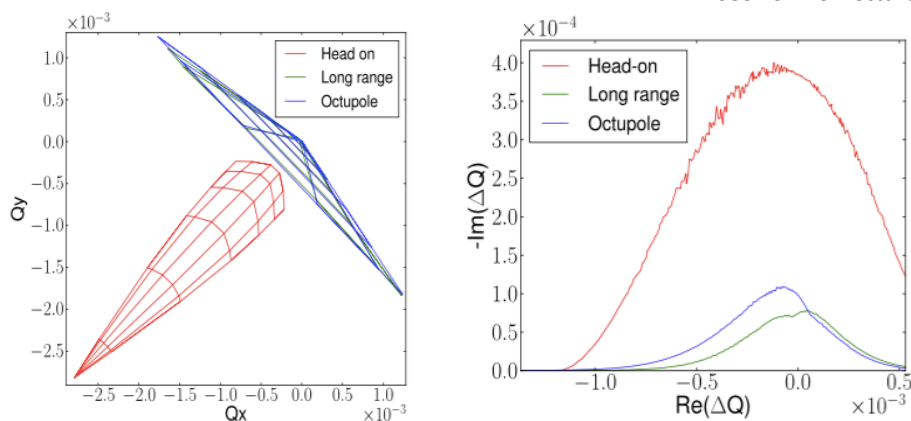
Landau damping



Incoherent tune spread is the Landau damping region any mode with frequency laying in this range should not develop

Tune spread positive effects: Landau damping

See Kornilov lecture

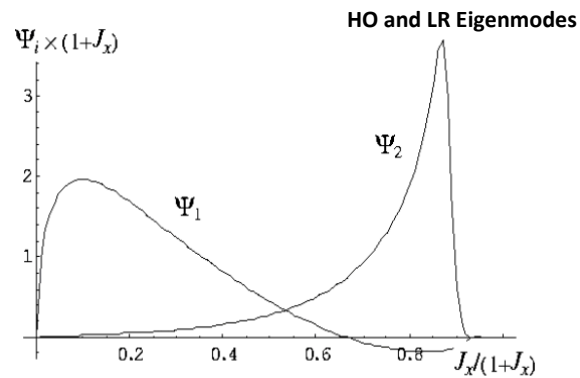


Head-on spread and Landau damping most effective if compared to octupoles or long-range spreads.

Effective to damp impedance and head-on beam-beam modes!

Cannot damp long-range modes!

Tune spread positive effects: Landau damping



Different particles are involved in the coherent motion and in the Landau damping...

HO modes are due to core particle oscillation as the spread → Landau damping effective!

LR modes are due to bunch tails oscillations → NO Landau damping!

Special observation in Leptons

From our known formulas:

$$L = \frac{N_1 N_2 f n_b}{4\pi\sigma_x\sigma_y} \quad \xi_{x,y} = \frac{Nr_0\beta_{x,y}^*}{2\pi\gamma\sigma_{x,y}(\sigma_x + \sigma_y)}$$

Increasing bunch population N_1 and N_2 :

- luminosity should increase N_2
- beam-beam parameter linearly

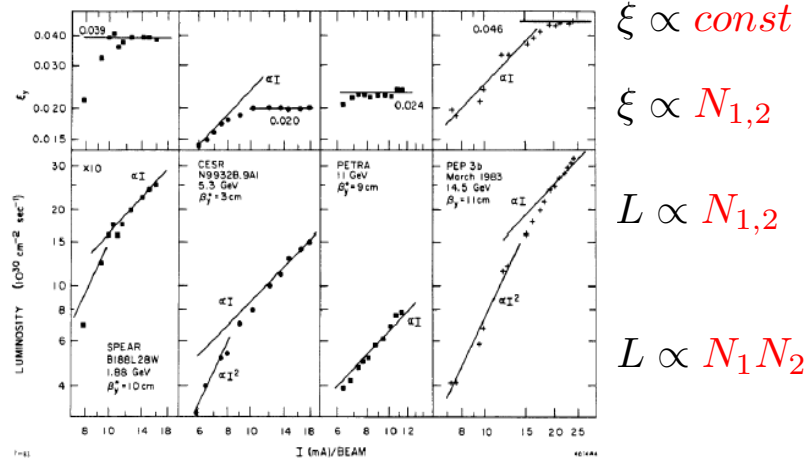
$$L \propto N_1 N_2$$

$$\xi \propto N_{1,2}$$

But...

Leptons beam-beam limit

First beam-beam limit (J. Seeman, 1983)



Luminosity and vertical tune shift parameter vs. beam current for SPEAR, CESR, PETRA & PEP.

What is happening?

$$\xi_{x,y} = \frac{N r_0 \beta_{x,y}^*}{2\pi \gamma \sigma_{x,y} (\sigma_x + \sigma_y)}$$

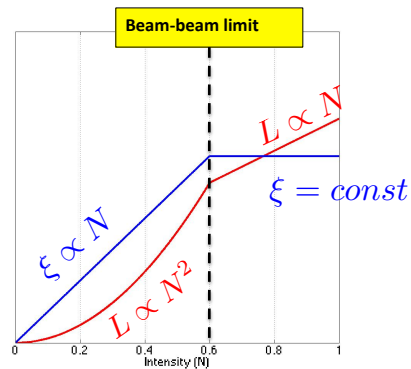
Lepton colliders $\sigma_x \gg \sigma_y$

$$\xi_y \approx \frac{r_0 \beta_y^*}{2\pi \gamma \sigma_x} \left(\frac{N}{\sigma_y} \right)$$

$$L = \frac{N f n_b}{4\pi \sigma_x} \left(\frac{N}{\sigma_y} \right)$$

As to be constant!

$$L = \frac{N^2 f n_b}{4\pi \sigma_x \sigma_y}$$



Above beam-beam limit:

σ_y increases when N increases to keep ξ constant

Equilibrium emittance

1. Synchrotron radiation: vertical plane damped, horizontal plane excited!
2. Horizontal beam size normally much larger than vertical (LEP 200 - 4 μm)
3. Vertical beam-beam effect depends on horizontal (larger) amplitude
4. Coupling from horizontal to vertical plane

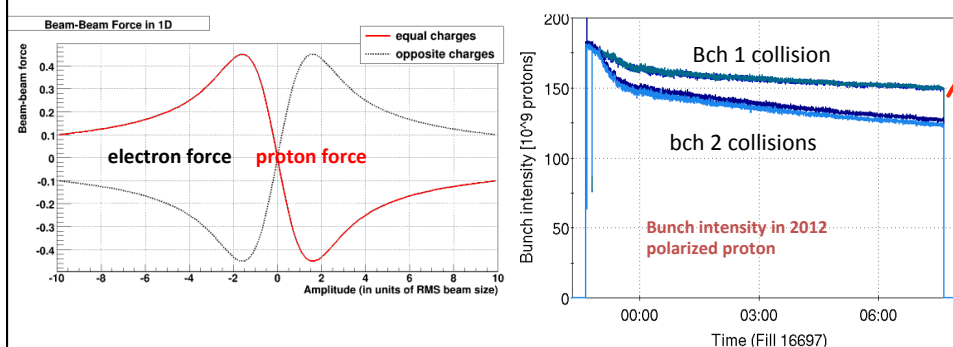
$$\xi_{x,y} = \frac{Nr_0\beta_{x,y}^*}{2\pi\gamma\sigma_{x,y}(\sigma_x + \sigma_y)}$$

Equilibrium between horizontal excitation and vertical damping
determines ξ_{limit}

Beam-beam compensation: Head-on

Head-on

- Linear e-lens, suppress shift
- Non-linear e-lens, suppress tune spread

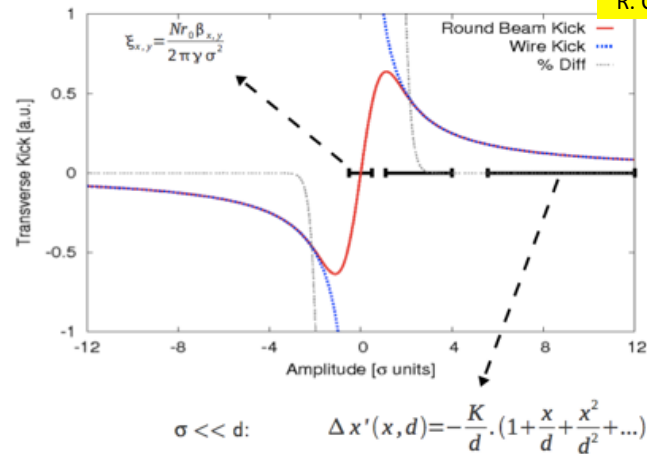


Past experience: at Tevatron linear and non-linear e-lenses, also hollow....
Recently proved and operationally used in RHIC! → 91% peak lumi increase!

Beam-beam compensations: long-range

Beam-beam wire compensation

R. Calaga



- Past experiences: at RHIC several tests till 2009...
- **Present: prove of principle studies on-going for possible use in HL-LHC...**

...not covered here...

- *Linear colliders special issues*
- *Asymmetric beams effects*
- *Coasting beams*
- *Beamstrahlung*
- *Synchrotron coupling*
- *Beam-beam and impedance mode coupling*
- ...

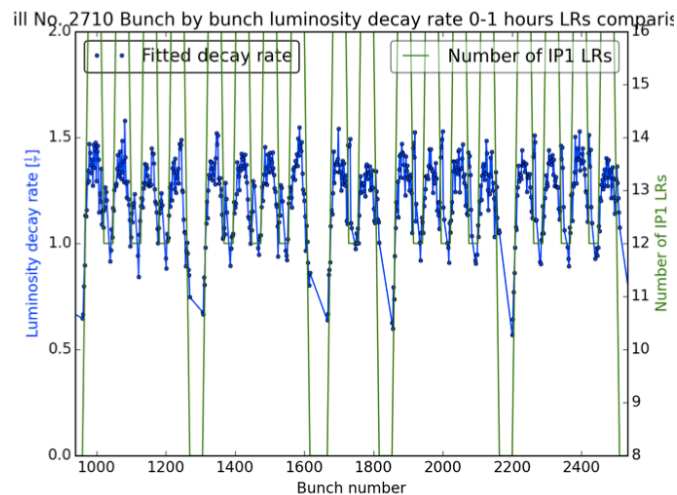
References:

- [1] http://cern.ch/Werner.Herr/CAS2009/proceedings/bb_proc.pdf
- [2] V. Shiltsev et al, "Beam beam effects in the Tevatron", *Phys. Rev. ST Accel. Beams* 8, 101001 (2005)
- [3] Lyn Evans "The beam-beam interaction", CERN 84-15 (1984)
- [4] Alex Chao "Lie Algebra Techniques for Nonlinear Dynamics" SLAC-PUB-9574 (2002)
- [5] J. D. Jackson, "Classical Electrodynamics", John Wiley & Sons, NY, 1962.
- [6] H. Grote, F. Schmidt, L. H. A. Leunissen, "LHC Dynamic Aperture at Collision", LHC-Project-Note 197, (1999).
- [7] W. Herr, "Features and implications of different LHC crossing schemes", LHC-Project-Note 628, (2003).
- [8] A. Hofmann, "Beam-beam modes for two beams with unequal tunes", CERN-SL-99-039 (AP) (1999) p. 56.
- [9] Y. Alexahin, "On the Landau damping and decoherence of transverse dipole oscillations in colliding beams", *Part. Acc.* 59, 43 (1996).
- [10] R. Assmann et al., "Results of long-range beam-beam studies - scaling with beam separation and intensity "

...much more on the LHC Beam-beam webpage:

<http://lhc-beam-beam.web.cern.ch/lhc-beam-beam/>

Beam-beam Observations 2012 (I)



Strong Long-range effects →

Intensity lifetimes reduction → Higher losses

Emittance effects → increase of the transverse emittances and/or scraping

→ Lumi lifetime reduction!