

Observations and Diagnostics in High Brightness Beams

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CAS - Advanced Accelerator Physics, 3-15 September 2017, Egham, UK



Lecture on yellow report

- Observations and Diagnostics in High Brightness Beams
- Proceedings of the CAS-CERN Accelerator School: Intensity Limitations in Particle Beams, Geneva, Switzerland, 2–11 November 2015, edited by W. Herr, CERN Yellow Reports: School Proceedings, Vol. 3/2017, CERN-2017-006-SP (CERN, Geneva, 2017)
- https://publishing.cern.ch/index.php/CYR SP/article/download/253/272



Outline

- · Brightness and its meaning
- Fundamental parameters
- Transverse and longitudinal measurements
- Intercepting and non intercepting diagnostics
- This lecture is about general principles without so many technical details

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Some references

- C. Lejeune and J. Aubert, "Emittance and Brightness, definitions and measurements", Adv. Electron. Electron Phys., Suppl. A 13, 159 (1980).
- A. Wu Chao, M. Tigner "Handbook of Accelerator Physics and Engineering" World Scientific, pag 255
- C. A. Brau "What Brightness means" in The Physics and Applications of High Brightness Electron Beam", World Scientific, pag 20
- M. Reiser, "Theory and design of charged particle beams", Wiley-VCH, pag 61
- Shyh-Yuan Lee, "Accelerator Physics", World Scientific, pag 419
- J. Clarke "The Science and Technology of Undulators and Wiggles" Oxford Science Publications, pag 73



Brightness and Brilliance

- Several authors give different definitions
- Brilliance is sometimes used, especially in Europe, instead of brightness
- There is also confusion because the same words apply both to particle beams and photon beams
- The best way is to look to units, which should be unambiguous

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The source of the name

 In 1939 Von Borries and Ruska, who got the Nobel Prize in 1986 for the invention of the electronic microscope, introduced the concept of beam brightness

$$B_{microscope} = \frac{I}{A\Omega} = \frac{Ne}{\pi r^2 \pi \alpha^2 \Delta t}$$

- This quantity is practically constant in the microscope column
- This quantity is extremely important because it defines the quality of the source and determines the kind of experiments which can be done



Definitions of Brightness

$$B = \frac{dI}{dSd\Omega}$$

For particle distribution whose boundary in 4D trace space is defined by an hyperellipsoid

$$\overline{B} = \frac{2I}{\pi^2 \varepsilon_x \varepsilon_y}$$
 [A/(m-rad)²]

$$\overline{B}_n = \frac{2\overline{I}}{\pi^2 \varepsilon_{nx} \varepsilon_{ny}}$$

Normalized Brightness

From diagnostics point of view what does it mean high brightness?

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Sometimes 6D brightness

$$B_{6D} \propto \frac{Ne}{\varepsilon_{nx}\varepsilon_{ny}\sigma_t\sigma_\gamma}$$

- In numbers, for typical electron beams parameters:
 - N≈109
 - σ_ν ≈10⁻³
 - ε_ṅ≈1 mm mrad
 - $-\sigma_t$ < 1 ps
 - 6D brightness is of the order of 10¹⁵ A/m².

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Some example of HB beams

- Linacs driving a radiation source (FEL, Compton, THz...)
- Linacs for ILC
- · Plasma accelerated beams

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Brilliance

$$B = \frac{d^4N}{dt d\Omega dS d\lambda / \lambda}$$

Photons/ (s mm² mrad² 0.1% of bandwidth)

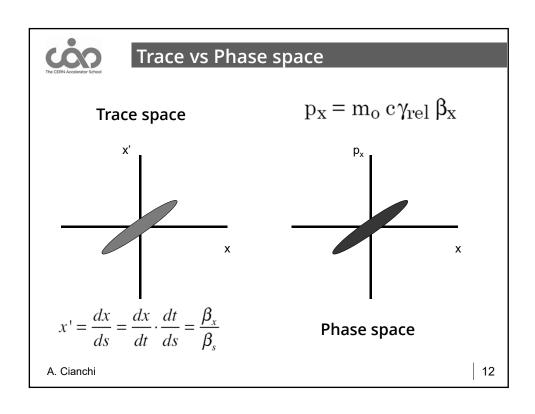
 $\mbox{H.}$ Wiedeman uses the name "spectral brightness" for $\mbox{ photons}$

- Report of the Working Group on Synchrotron Radiation Nomenclature – brightness, spectral brightness or brilliance?
- The conclusion reached is that the term spectral brightness best describes this quantity. Brightness maintains the generally accepted concept of intensity per unit source size and divergence, while the adjective spectral conveys the scientific importance of the number of photons in a given bandwidth, particularly for experiments such as inelastic and/or number resolutions.
- J. Synchrotron Rad. (2005). 12, 385

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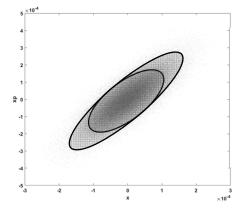


Transverse Diagnostics





RMS emittance



$$\sigma_x^2(z) = \langle x^2 \rangle = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} x^2 f(x, x', z) dx dx'$$

$$\sigma_{x'}^{2}(z) = \left\langle x'^{2} \right\rangle = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} x'^{2} f(x, x', z) dx dx'$$

$$\sigma_{xx'}(z) = \langle xx' \rangle = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} xx' f(x, x', z) dx dx'$$

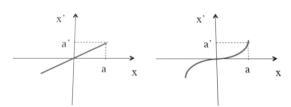
$$\varepsilon_{rms} = \sqrt{\sigma_{x}^{2} \sigma_{x'}^{2} - \sigma_{xx'}^{2}} = \sqrt{\left(\left\langle x^{2} \right\rangle \left\langle x'^{2} \right\rangle - \left\langle xx' \right\rangle^{2}\right)}$$

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Importance of RMS emittance



$$x' = Cx^n$$

$$\varepsilon_{rms} = C\sqrt{\langle x^2 \rangle \langle x^{2n} \rangle - \langle x^{n+1} \rangle^2} \qquad \begin{cases} n = 1 \Rightarrow \varepsilon_{rms} = 0 \\ n > 1 \Rightarrow \varepsilon_{rms} \neq 0 \end{cases}$$

Even when the phase-space area is zero, if the distribution lies on a curved line its rms emittance is not zero.

RMS emittance is not an invariant for Hamiltonian with non linear terms.

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Geometrical vs Normalized

$$\varepsilon_n^2 = \langle x^2 \rangle \langle \beta^2 \gamma^2 x'^2 \rangle - \langle x \beta \gamma x' \rangle$$

$$\sigma_E^2 = \frac{\left\langle \beta^2 \gamma^2 \right\rangle - \left\langle \beta \gamma \right\rangle^2}{\left\langle \gamma \right\rangle^2}$$

$$\varepsilon_n^2 = \langle \gamma \rangle^2 \sigma_\varepsilon^2 \langle x^2 \rangle \langle x'^2 \rangle + + \langle \beta \gamma \rangle^2 \left(\langle x^2 \rangle \langle x'^2 \rangle - \langle x x' \rangle^2 \right)$$

M. Migliorati et al, Physical Review Special Topics, Accelerators and Beams 16, 011302 (2013)

K. Floettmann, PRSTAB,6, 034202 (2003)

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Fundamental issue

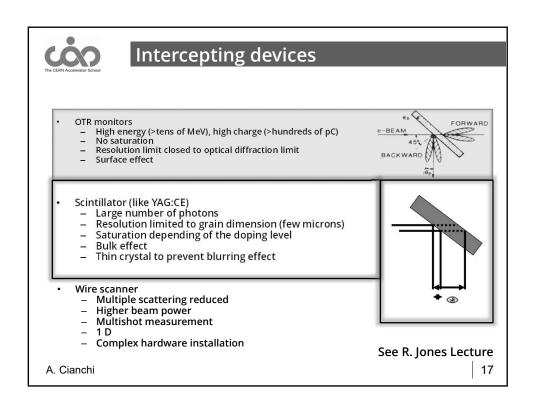
$$\varepsilon_n^2 = \langle \gamma \rangle^2 \left(\sigma_\varepsilon^2 \sigma_x^2 \sigma_{x'}^2 + \varepsilon^2 \right) \qquad \sigma_x(s) \approx \sigma_{x'} s$$

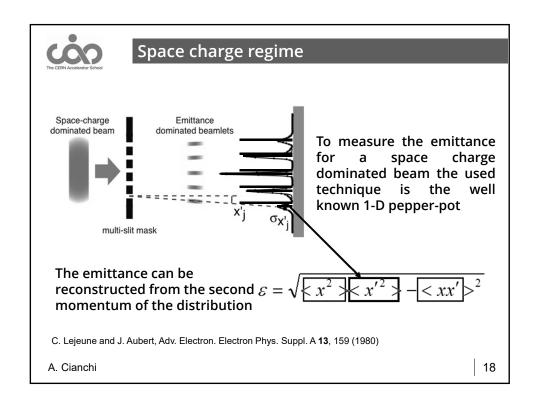
$$\sigma_{x}(s) \approx \sigma_{x'}s$$

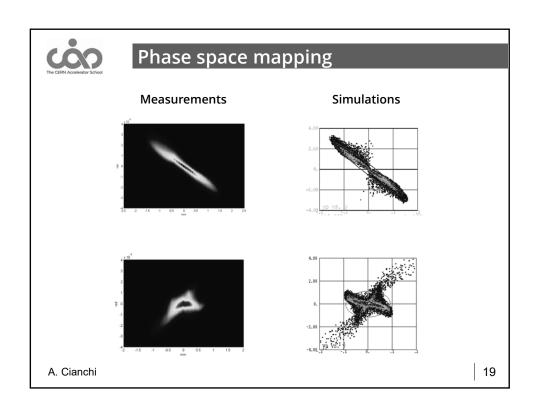
$$\varepsilon_n^2 = <\gamma>^2 \left(s^2 \sigma_\varepsilon^2 \sigma_{x'}^4 + \varepsilon^2\right)$$

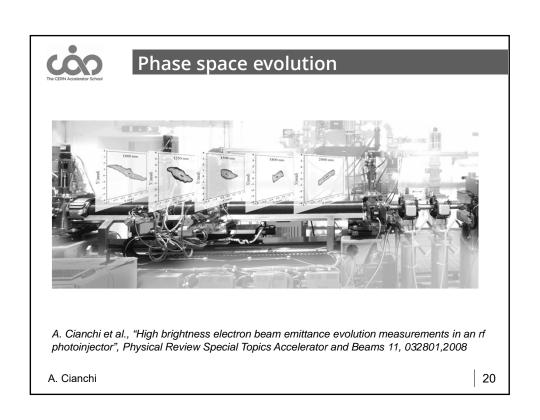
- · For the accelerator community the normalized emittance is one of the main parameter because is constant
- For plasma accelerated beams, due to the large energy spread and huge angular divergence, it is not true anymore

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Emittance without space charge

 The most used techniques for emittance measurements are quadrupole scan and multiple monitors

$$\gamma x^{2} + 2\alpha x x' + \beta x'^{2} = \varepsilon = \gamma_{0} x_{0}^{2} + 2\alpha_{0} x_{0} x'_{0} + \beta_{0} x'_{0}^{2}$$

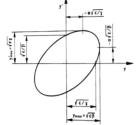
$$M(s_1s_2) = \begin{pmatrix} C & S \\ C' & S' \end{pmatrix} \qquad \begin{pmatrix} \beta \\ \alpha \\ \gamma \end{pmatrix} = \begin{pmatrix} C^2 & -2SC & S^2 \\ -CC' & S'C + SC' & -SS' \\ C'^2 & -2S'C' & S'^2 \end{pmatrix} \begin{pmatrix} \beta_0 \\ \alpha_0 \\ \gamma_0 \end{pmatrix}$$

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Beam Matrix

$$\sigma = \begin{pmatrix} \sigma_{11} & \sigma_{12} \\ \sigma_{12} & \sigma_{22} \end{pmatrix} = \varepsilon \begin{pmatrix} \beta & -\alpha \\ -\alpha & \gamma \end{pmatrix}$$



$$\sigma_{11}x^2 + 2\sigma_{12}xx' + \sigma_{22}x'^2 = 1$$

$$\sigma_1 = M\sigma_0 M^T$$

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Multiple screens

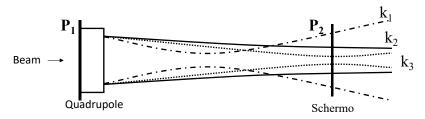
$$\sigma_{i,11} = C_i^2 \sigma_{11} + 2S_i C_i \sigma_{12} + S_i^2 \sigma_{22}$$

- There are 3 unknown quantities
- $\sigma_{i,11}$ is the RMS beam size
- C_i and S_i are the element of the transport matrix
- We need 3 measurements in 3 different positions to evaluate the emittance

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Quadrupole scan



$$\sigma_{11} = C^2(k)\sigma_{11} + 2C(k)S(k)\sigma_{12} + S^2(k)\sigma_{22}$$

- It is possible to measure in the same position changing the optical functions
- The main difference respect to the multi screen measurements is in the beam trajectory control and in the number of measurements

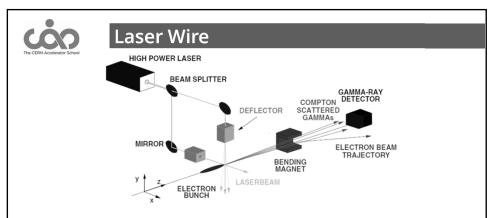
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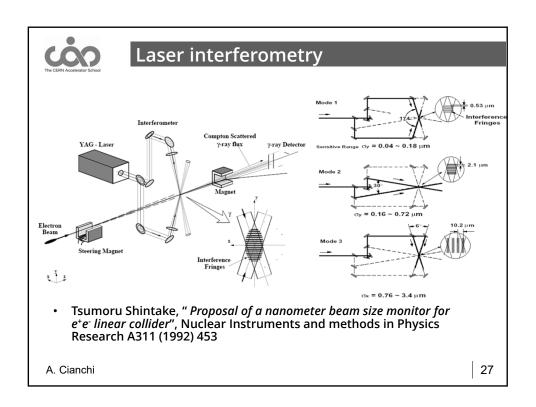
Intercepting diagnostics

- · High charge or high repetition rate machines
- Small beam dimension (between 50 μm down to tens of nm)
- All the intercepting devices are damaged or destroyed from these kind of beams
- No wire scanners, no OTR screens, no scintillators
- There are good candidates for longitudinal diagnostic
- It is difficult to replace intercepting devices for transverse dimensions
- There are a lot of ideas in testing

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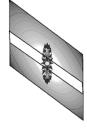
- Not intercepting device
- Multi shot measurement (bunch to bunch position jitter, laser pointing jitter, uncertainty in the laser light distribution at IP)
- Setup non easy
- Resolution limited from the laser wavelength
- · Several effects to take into account
- I. Agapov, G. A. Blair, M. Woodley, Physical review special topicsaccelerators and beams 10, 112801 (2007)





Diffraction Radiation

- The charge goes into the hole without touching the screen
- The electromagnetic field of the moving charge interacts with the metallic screen
- No power is deposited on the screen
- The angular distribution of the emerging radiation is affected by the beam transverse size, the angular spread and the position inside the slit
 - M. Castellano 1997 Nucl. Instrum. Methods Phys. Res., Sect. A 394, 275.
- Rectangular slit



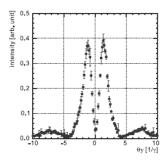
 $I \propto e^{-\frac{2\pi a}{\gamma \lambda}}$

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First experiment @ KEK

P. Karataev et al., "Beam-Size Measurement with Optical Diffraction Radiation at KEK Accelerator Test Facility", Phys. Rev. Lett. 93, 244802 (2004)



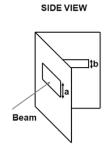
- Weak signal vs strong background, coming mainly from Synchrotron Radiation
- Precise control of the beam position inside the slit needs a complementary diagnostics

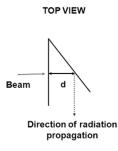
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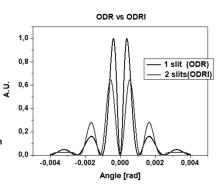


Introducing ODRI

Optical Diffraction Radiation Interference

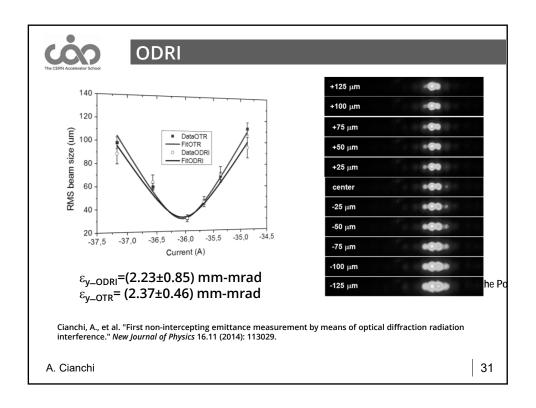






A. Cianchi et al. "Nonintercepting electron beam size monitor using optical diffraction radiation interference", PRSTAB 14, 102803

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Emittance recap

- Space charge dominated beams
 - Pepper pot like
- Non space charge dominated beams
 - Quadrupole scan mainly
- Problems with intercepting diagnostics for high brightness/repetition rate machines
 - Several instruments are still developing



Longitudinal Diagnostics

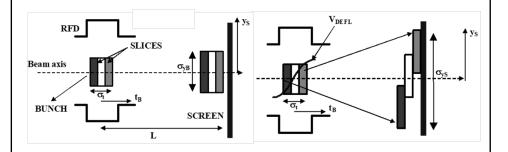


Longitudinal parameters

- Fundamental parameter for the brightness
- Bunch lengths can be on ps (uncompressed) or sub-ps time scale, down to fs scale!
- Several methods
 - Coherent radiations
 - RFD
 - EOS
 - Others?
- T. Watanabe et al, "Overall comparison of subpicosecond electron beam diagnostics by the polychromator, the interferometer and the femtosecond streak camera", Nuclear Instruments and Methods in Physics Research A 480 (2002) 315-327



RF deflector



Paul Emma, Josef Frisch, Patrick Krejcik, A Transverse RF Deflecting Structure for Bunch Length and Phase Space Diagnostics, LCLS-TN-00-12 Christopher Behrens, Measurement and Control of the Longitudinal Phase Space at High-Gain Free-Electron Lasers , FEL 2011, Shanghai

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RFD

$$\Delta y' = \frac{qV_0}{pc} \left[kz \cos(\varphi) + \sin(\varphi) \right]$$
 Betatron phase advance
$$y(z) = \left(\sqrt{\beta \beta_0} \sin \Delta \right) y_0' \pm \frac{qV_0}{pc} kz \left(\sqrt{\beta \beta_0} \sin \Delta \right)$$

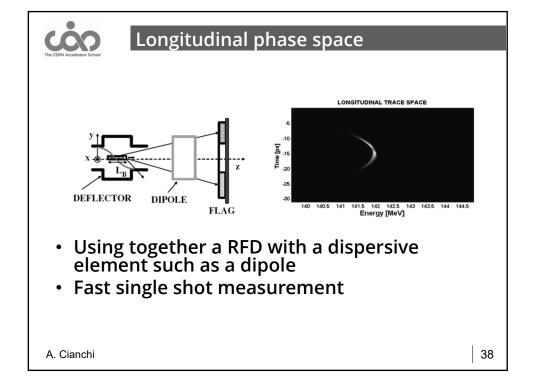
$$\begin{split} \left\langle \left(y - \left\langle y \right\rangle \right)^2 \right\rangle^{\pm} &= \beta \beta_0 \sin^2 \Delta \left\langle y_0'^2 \right\rangle + \beta \beta_0 \sin^2 \Delta \left(\frac{qV_0}{pc} k \right)^2 \left\langle z^2 \right\rangle + \\ -\beta \beta_0 \sin^2 \Delta \left\langle y_0' \right\rangle^2 - \sigma &= \sqrt{\sigma_0^2 + \sigma_z^2} \quad z \right\rangle^2 + \\ &\pm 2\beta \beta_0 \sin^2 \Delta \left(\frac{qV_0}{pc} k \right) \left\langle y_0 z \right\rangle + 2\beta \beta_0 \sin^2 \Delta \left(\frac{qV_0}{pc} k \right) \left\langle y_0' \right\rangle \left\langle z \right\rangle \end{split}$$

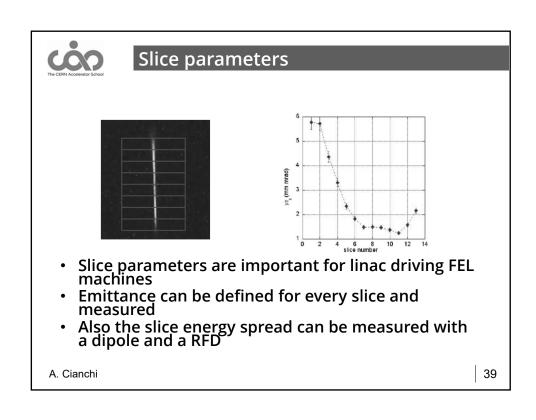


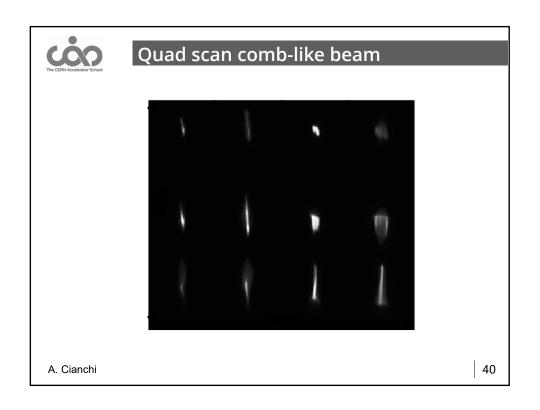
RFD summay

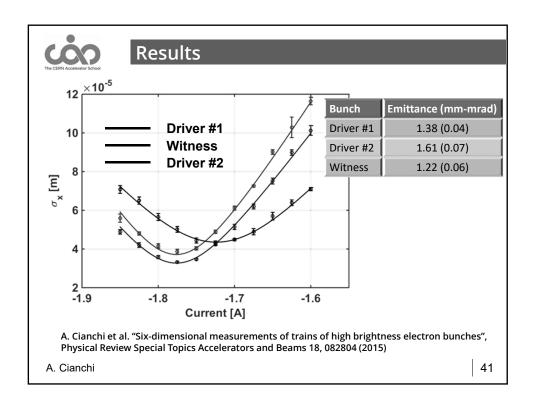
- · Easy to implement
- Single shot
- Resolution down to fs
- Intercepting device
- As energy increases some parameter must be increased:
 - Frequency
 - Voltage or length







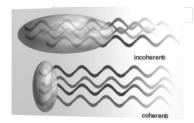






Coherent radiation

- Any kind of radiation can be coherent and usable for beam diagnostics
 - Transition radiation
 - Diffraction radiation
 - Synchrotron radiation
 - Undulator radiation
 - Smith-Purcell radiation
 - Cherenkov radiation



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Power Spectrum

$$I_{tot}(\omega) = I_{sp}(\omega)[N+N^*(N-1) F(\omega)]$$

$$F(\omega) = \left| \int_{-\infty}^{\infty} dz \rho(z) e^{i(\omega/c)z} \right|^{2} \qquad \rho(z) = \frac{1}{\pi c} \int_{0}^{\infty} d\omega \sqrt{F(\omega)} \cos\left(\frac{\omega z}{c}\right)$$

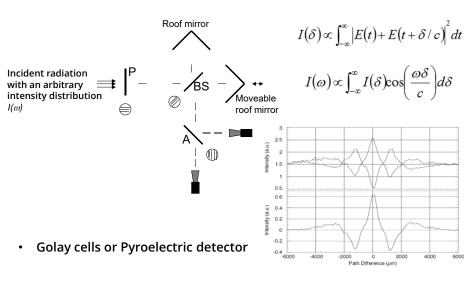
- From the knowledge of the power spectrum is possible to retrieve the form factor
- The charge distribution is obtained from the form factor via Fourier transform
- The phase terms can be reconstructed with Kramers-Kronig analysis (see R. Lai, A.J. Sievers, NIM A 397 (1997) 221-231)

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Martin-Puplett Interferometer





Experimental considerations

- Spectrum cuts at low and high frequencies can affect the beam reconstruction
 - Detectors
 - Windows
 - Transport line
 - Finite target size
- For this reason the approach is to test the power spectrum with the Fourier transform of a guess distribution
- Coherent synchrotron radiation or diffraction radiation can be generated by totally not intercepting devices and so they are eligible for high brightness beams diagnostic
- <u>Multishots measurements. Single shot devices are still under developing</u>

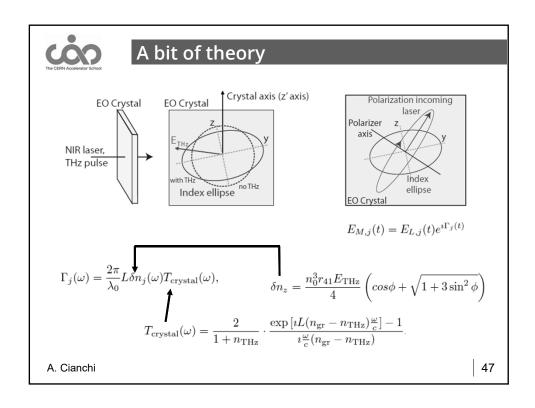
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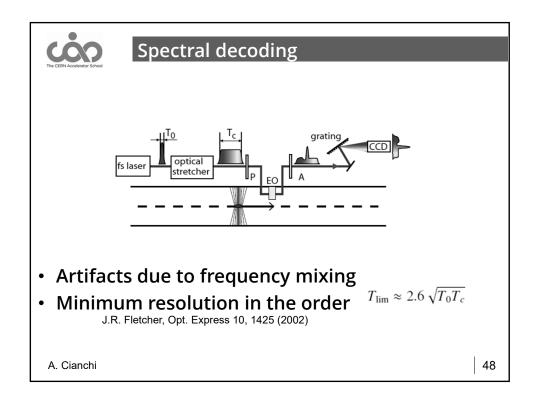


Electro Optical Sample (EOS)

- Totally non intercepting device and not disturbing device
- It is based on the change of the optical properties of a non linear crystal in the interaction with the Coulomb field of the moving charges
- Several schemes have been proposed and tested
 - I.Wilke et al., "single-Shot electron beam bunch length measurements" PRL, v.88, 12(2002)
 - G. Berden et al., "Electo-Optic Technique with improved time resolution for real time, non destructive, single shot measurements of femtosecond electron bunch profiles, PRL v93, 11 (2004)
 - B. Steffen, "Electro-optic time profile monitors for femtosecond electron bunches at the soft x-ray free-electron laser FLASH", Phys. Rev. ST Accel. Beams 12, 032802 (2009)

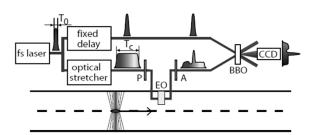
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Temporal decoding

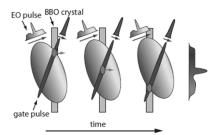


- Resolution: duration of the gate beam, thickness of the SHG crystal
- 50 fs or slightly better
- low efficiency SHG process, approx. 1mJ laser pulse energy necessary

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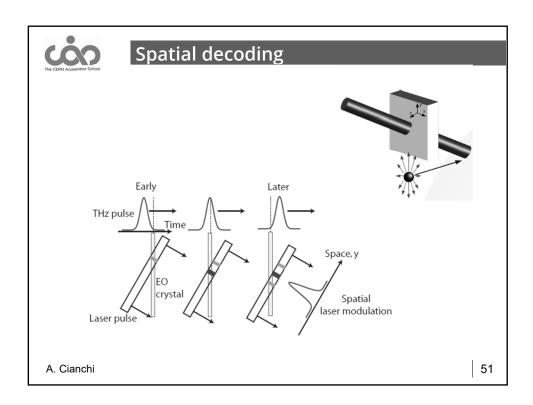


Temporal cont.



 The short gate pulse overlaps with different temporal slices of the EO pulse at different spatial positions of the BBO crystal. Thus the temporal modulation of the EO pulse is transferred to spatial distribution of the SHG light.

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Longitudinal diagnostics recap

- RFD
 - Single shot
 - Resolution down to few fs
 - Intercepting
- Coherent radiation
 - Both intercepting and not intercepting
 - Resolution not limited in principle
 - Single shot device still developing
 - Indirect reconstruction from spectrum
- EOS
 - Not intercepting
 - Single shot
 - Resolution limited to about 40 fs
 - Time of arrival monitor

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Conclusions

- High brightness beam demands particular diagnostic techniques in order to measure very small transverse emittance (<1 mmmrad) and very short bunch length (< 1 ps)
- Intercepting or not intercepting diagnostics are recommended in some cases
- Some diagnostics are already state of the art
- · Some others are still developing
- New ideas are daily tested, so if you want your part of glory start to think about today!

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Finally it's over

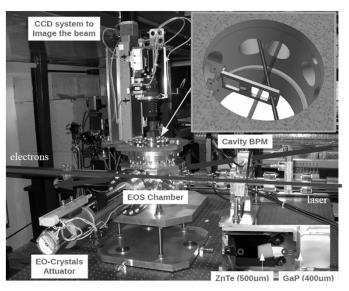
Thank you for your attention, if you are still alive...



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EOS setup



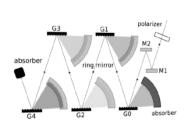
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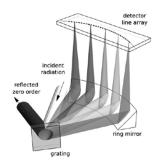
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Single shot CTR measurements I

 S. Wesch, B. Schmidt, C. Behrens, H. Delsim-Hashemi, P. Schmuser, A multichannel THz and infrared spectrometer for femtosecond electron bunch diagnostics by single-shot spectroscopy of coherent radiation Nuclear Instruments and Methods in Physics Research A 665 (2011) 40–47





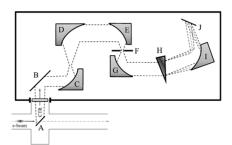
Pyro-electric line detector 30 channels @ room temperature no window, works in vacuum fast read out sensitivity

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Single shot CTR measurements II

 T. J. Maxwell et al. "Coherent-radiation spectroscopy of few-femtosecond electron bunches using a middle-infrared prism spectrometer." *Physical review letters* 111.18 (2013)



KRS-5 (thallium bromoiodide) prism based spectrometer developed

Images OTR from foil onto 128 lead zirconate titanate pyroelectric elements with 100 μm spacing line array

Also double prism (ZnSe), S. Wunderlich et al., Proceedings of IBIC2014

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Quantum limit

 Due to the Pauli exclusion principle, there is a maximum brightness theoretically achievable by an electron beam, as the 6D phase space density is limited by Heisenberg uncertainty principle

$$B_{quantum} = \frac{2e}{h^3} (m_0 c^2)^3 = \frac{2e}{\lambda_c^3} \approx 10^{25} \frac{A}{m^2}$$

- · We have 10 orders of magnitude less.
- Electron emission mechanisms and Coulomb interactions play a crucial role

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Parameters to measure

- High brightness can be achieved with small emittance, high current or both
- <u>Longitudinal</u> and <u>transverse</u> parameters must be measured
- High charge and small emittance -> high power density beam
- · Low charge, very short bunch length
- We focus our attention on linac or transfer line where it is possible to use intercepting diagnostic

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Design issue

 The beamlets must be emittance dominated

$$\sigma_x'' = \frac{\varepsilon_n^2}{\gamma^2 \sigma_x^3} + \frac{I}{\gamma^3 I_0(\sigma_x + \sigma_y)}$$

Martin Reiser, Theory and Design of Charged Particle Beams (Wiley, New York, 1994)

Assuming a round beam

$$R_0 = \frac{I\sigma_0^2}{2\gamma I_0 \varepsilon_n^2} \qquad \sigma_x = \frac{d}{\sqrt{12}}$$

d must be chosen to obtain R₀<<1, in order to have a emittance dominated beam

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Design issues 2

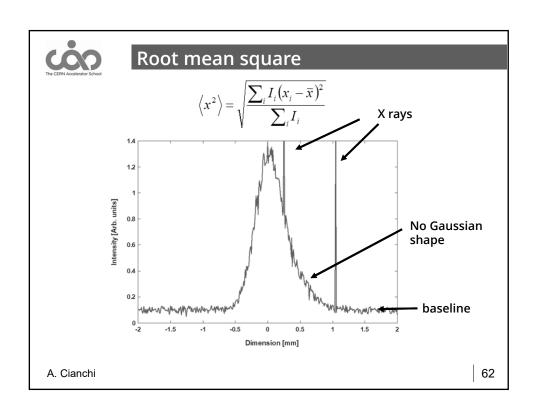
- The contribution of the slit width to the size of the beamlet profile should be negligible
- The material thickness (usually tungsten) must be long enough to stop or heavily scatter beam at large angle (critical issue at high energy)
- The angular acceptance of the slit cannot be smaller of the expected angular divergence of the beam

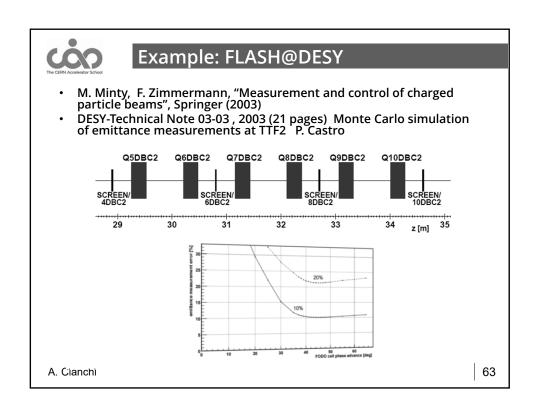
$$\sigma = \sqrt{\left(\mathbf{L} \cdot \sigma'\right)^2 + \left(\frac{\mathbf{d}^2}{12}\right)}$$

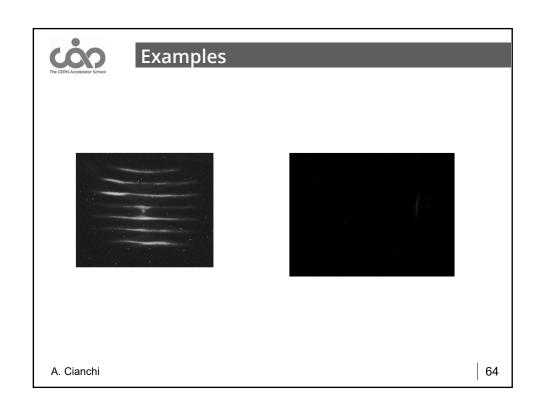
$$L >> \frac{d}{\sigma' \cdot \sqrt{12}}$$

$$l < \frac{d}{2\sigma'}$$

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Transverse parameters

- The most important parameter is the emittance
- To obtain high brightness beam it is of paramount importance to keep emittance growth under control
- Different methods apply for beams with or without space charge contribution
- Mainly the space charge is relevant at the exit of the RF GUN (few MeV)