

Calcolo della sezione d'urto di produzione di bosoni W ad LHC, da scattering singolo e doppio

Federico Alberto Ceccopieri

Università & INFN Perugia

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♡ ♡ Bruxelles ♡ ♡

Outlook

- W production in hadronic collisions : theory, briefly
- Benchmarks of the code for single W production vs other codes
 - How well does it work the LO approx vs data
 - How predictions based on Hadronic Model pdfs compare with MSTW08 ones
- First estimate of same-sign W 's production cross section
- Perspectives and other channels

Decay kinematics in W rest frame

- $pp \rightarrow W^\pm (\rightarrow l^\pm (\bar{\nu})) X$
- W rest frame \equiv partonic centre of mass ($x_a = x_b = 1$)
- D-type = d,s,b; U-type = u,c,t
- θ_{lD}^* is the angle between the charged lepton and D-type quark
- partonic subprocesses : $U\bar{D} \rightarrow l^+ \nu$ and $D\bar{U} \rightarrow l^- \bar{\nu}$

$$\frac{1}{\sigma_{U\bar{D}}} \frac{d\sigma_{U\bar{D}}}{d \cos \theta_{lD}^*} = \frac{1}{\sigma_{D\bar{U}}} \frac{d\sigma_{D\bar{U}}}{d \cos \theta_{lD}^*} = \frac{3}{8} (1 + \cos \theta_{lD}^*)^2$$

- helicity conservation:
 l^+ follows the direct \bar{D} direction, l^- follows the direct D direction

$$E_T^* = E^* \sin \theta_{lD}^* = \frac{M_W}{2} \sin \theta_{lD}^*, \quad E_T^{max} = \frac{M_W}{2}$$

- E_T invariant for longitudinal boost: $E_T = E_T^*$

kinematics detail

- W rapidity $y_W = \frac{1}{2} \ln \frac{x_a}{x_b}$
- neutrino unobserved \rightarrow W rapidity under-determined
- $A = M_W/(2E_T)$, $B = \sqrt{1 - 1/A^2}$

$$\eta_l = y_W + \frac{1}{2} \ln \frac{1 \pm B}{1 \mp B}$$

- twofold ambiguity in the determination of W rapidity and hence in x_a and x_b
- Motivation : for a given E_T and η , 2 possible y_W 's

$$x_a = e^{\eta} \frac{M_W}{\sqrt{s}} (A \pm \sqrt{A^2 - 1}) \quad x_b = e^{-\eta} \frac{M_W}{\sqrt{s}} (A \mp \sqrt{A^2 - 1})$$

- Lorentz invariants u, t read in terms of η and E_T

$$t = (p_a - p_l)^2 = -x_a \sqrt{s} E_T e^{-\eta}, \quad u = (p_b - p_l)^2 = -x_b \sqrt{s} E_T e^{\eta}$$

Cross sections

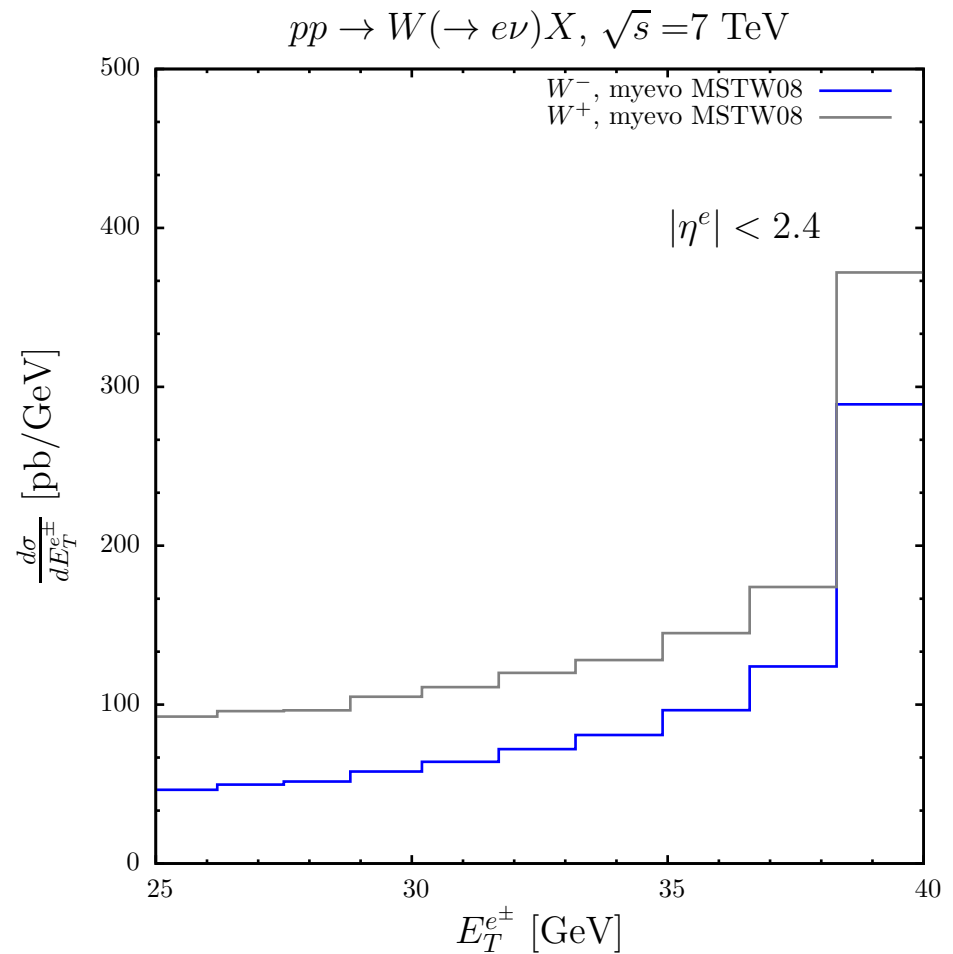
- Neglect here Cabibbo suppressed contributions
- narrow width approx (NWA): $\hat{s} = M_W$
- $A = M_W / (2E_T)$
- $D = d,s,b$; $U = u,c,t$
- EW currents: partonic subprocesses not P invariant, but hadronic initial state (pp) is \rightarrow final distribution (summed over partonic channels) is symmetric in rapidity
- σ differential in lepton rapidity and transverse momentum (neutrino unobserved)

$$\frac{d^2 \sigma^{pp \rightarrow W^- (\rightarrow l^- \bar{\nu}) X}}{d\eta dE_T} = \frac{G_F^2}{6s\Gamma_W} \frac{1}{\sqrt{A^2 - 1}} V_{D\bar{U}}^2 \left[f_D(x_a) f_{\bar{U}}(x_b) u^2 + f_{\bar{U}}(x_a) f_D(x_b) t^2 \right]$$

$$\frac{d^2 \sigma^{pp \rightarrow W^+ (\rightarrow l^+ \nu) X}}{d\eta dE_T} = \frac{G_F^2}{6s\Gamma_W} \frac{1}{\sqrt{A^2 - 1}} V_{U\bar{D}}^2 \left[f_U(x_a) f_{\bar{D}}(x_b) t^2 + f_{\bar{D}}(x_a) f_U(x_b) u^2 \right]$$

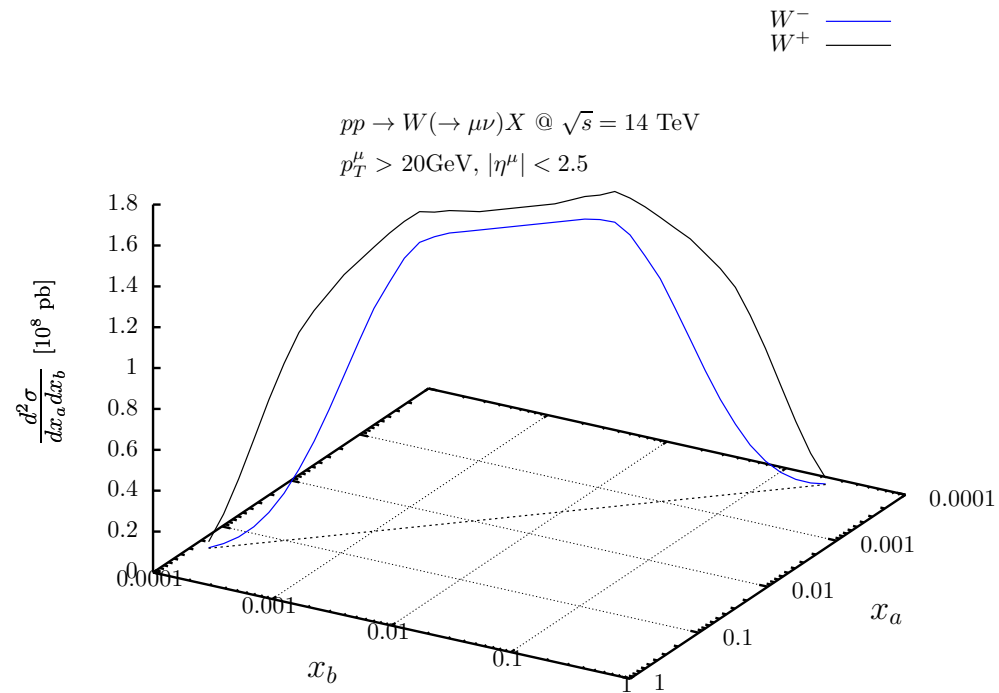
E_T distribution, jacobian peak

- change from $(x_a, x_b) \rightarrow (\eta, E_T)$
- $A = M_W/(2E_T)$
- $E_T^{max} = M_W/2$
- $d\sigma \propto \frac{1}{\sqrt{A^2-1}}$



(x_a, x_b) coverage

- Useful input for x-grids for double parton distributions
- NWA $\rightarrow \hat{s} = M_W^2 \rightarrow x_a x_b = M_W^2 / s$



Benchmark with DYNNLO

- DYNNLO code (Catani & al.) vs mycode for SPS $pp \rightarrow W(\rightarrow l\nu)X$ production
- Basic settings and cuts:
 - $\sqrt{s} = 7$ TeV, $E_T^l > 25$ GeV, $|\eta^l| < 2.4$
 - $\mu_F = M_W$, LO, NWA, MSTW08LO PDFs, $n_f = 5$ active flavours
 - No lepton isolation cut, No \cancel{E}_T cut (both redundant at LO)
 - EW parameters from PDG'12 (as in DYNNLO).

cross section (fiducial)	DYNNLO [pb]	Mycode [pb]
$\sigma^{W^+(\rightarrow l^+\nu)}$	2536.9 ± 0.3	2524
$\sigma^{W^-(\rightarrow l^-\bar{\nu})}$	1668.8 ± 0.2	1658

- Agreement at the level of 1% top

Accuracy and grids

- Study η (linear) and E_T (power) grids size
- $\sigma(W^+)$ cross section as case study

nET neta	10	10^2	10^3	10^4	10^5
10	2404	2498	2526	2535	2538
10^2	2402	2495	2524	2532	*
10^3	2402	2495	2524	*	*

- η dependence flat (c.f.r. distributions)
- $\sigma(10 \times 10^4)$ in agreement with DYNNLO at 0.1%

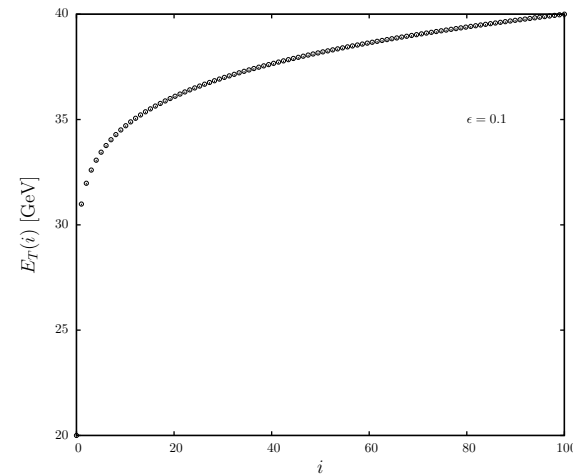
E_T -integration grid optimisation

- set : neta=10, nET=10³, $\sigma^{W^+}(\epsilon = 0.33) = 2526$ [pb]

$$E_T(i) = E_T^{min} \left[\frac{E_T^{max}}{E_T^{min}} \right]^{(i/nET)^\epsilon}$$

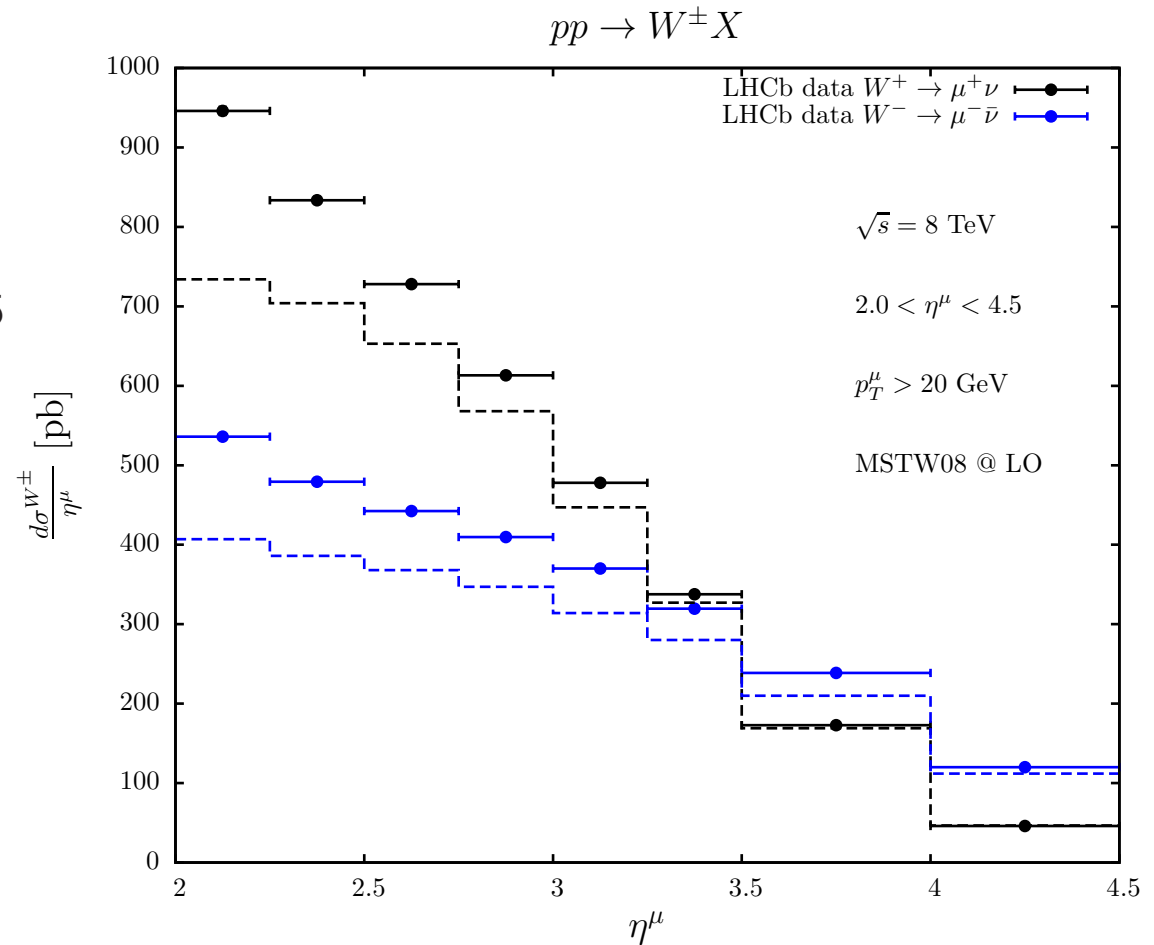
- $\epsilon < 1 \rightarrow$ more points around E_T^{max} (Jaco peak)

ϵ	σ^{W^+} [pb]
1.00	2516
0.50	2523
0.33	2526
0.25	2528
0.10	2530
0.05	2517



Charged lepton distributions, LHCb

- LHCb, JHEP01 (2016) 155
- Missing strength at mid-rapidity
- 25% in the first bin

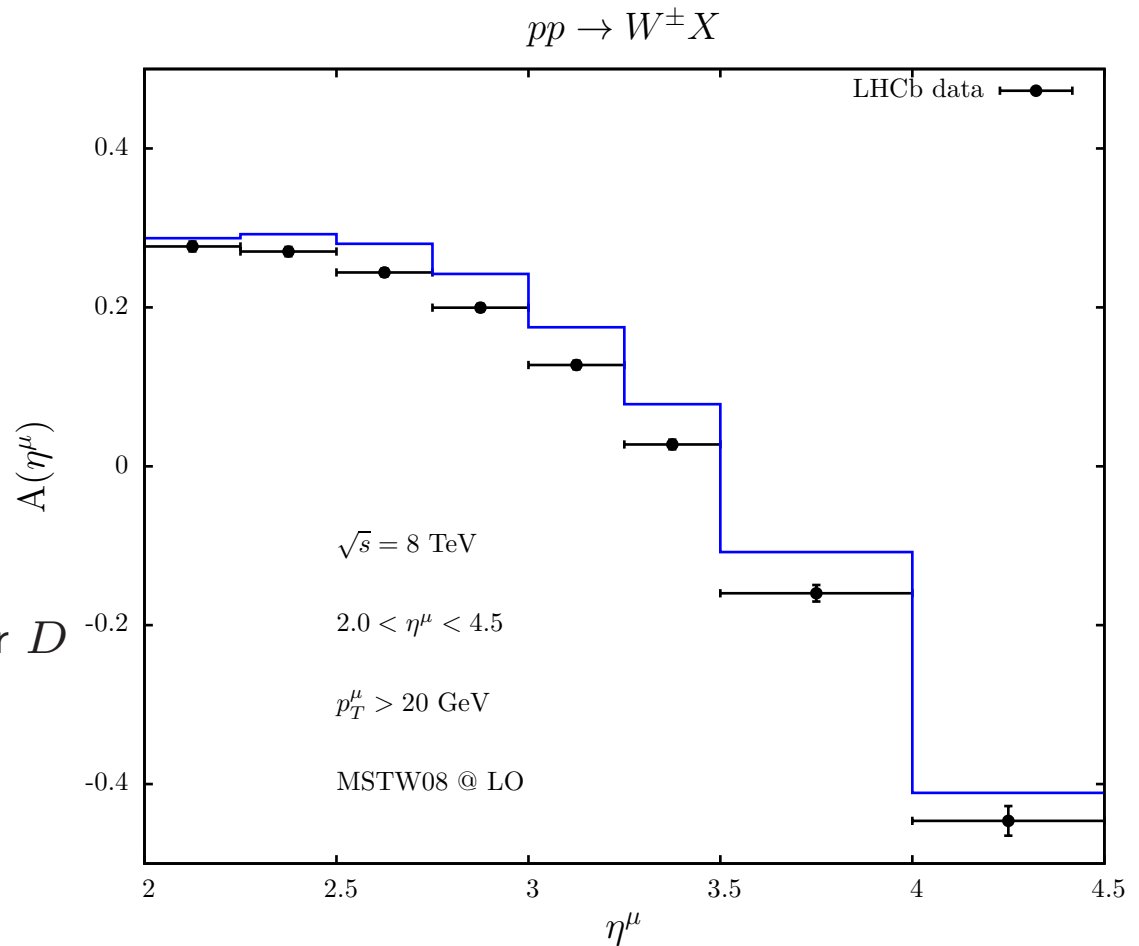


Charged lepton asymmetry, LHCb

- LHCb, JHEP01 (2016) 155

- $$A(\eta^l) = \frac{\frac{d\sigma^{l^+}}{d\eta^l} - \frac{d\sigma^{l^-}}{d\eta^l}}{\frac{d\sigma^{l^+}}{d\eta^l} + \frac{d\sigma^{l^-}}{d\eta^l}}$$

- Significant excess of U over D

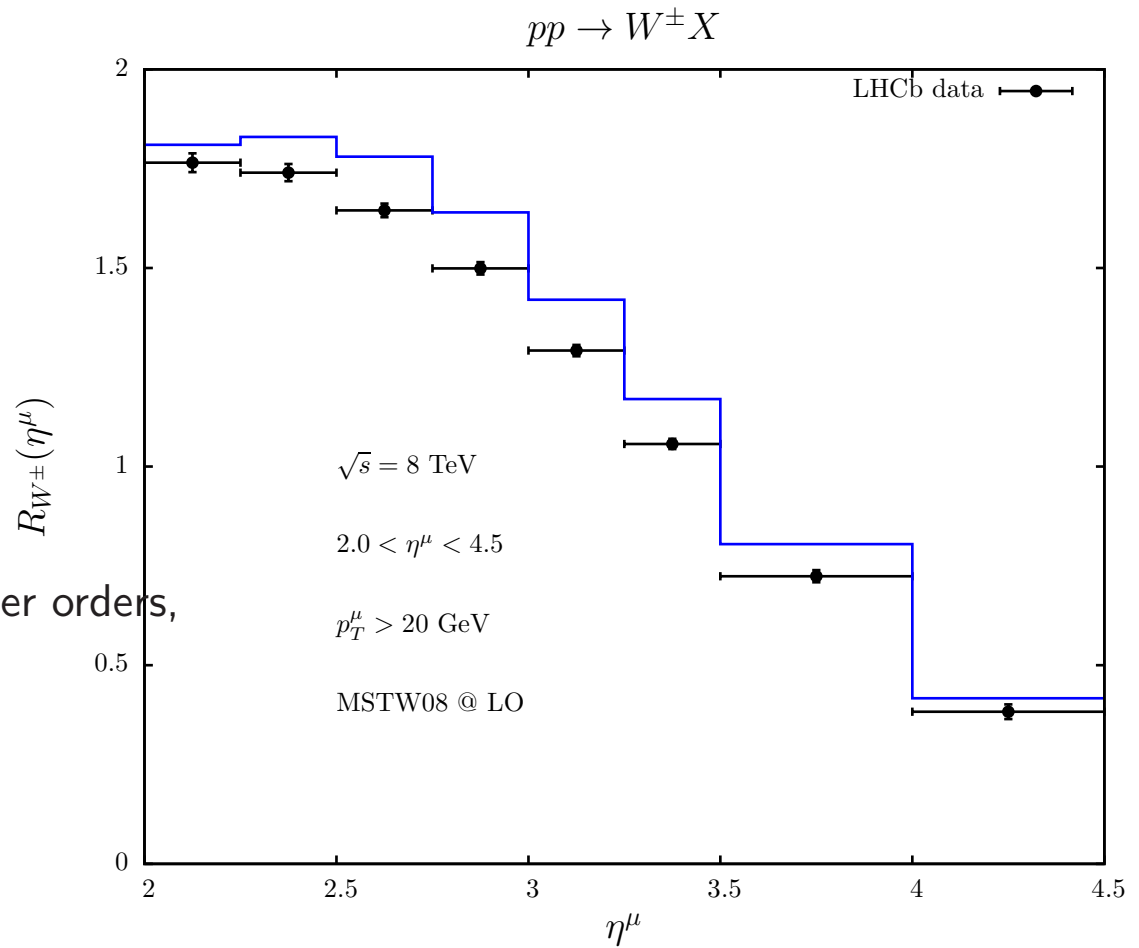


W^+/W^- ratio, LHCb

- LHCb, JHEP01 (2016) 155

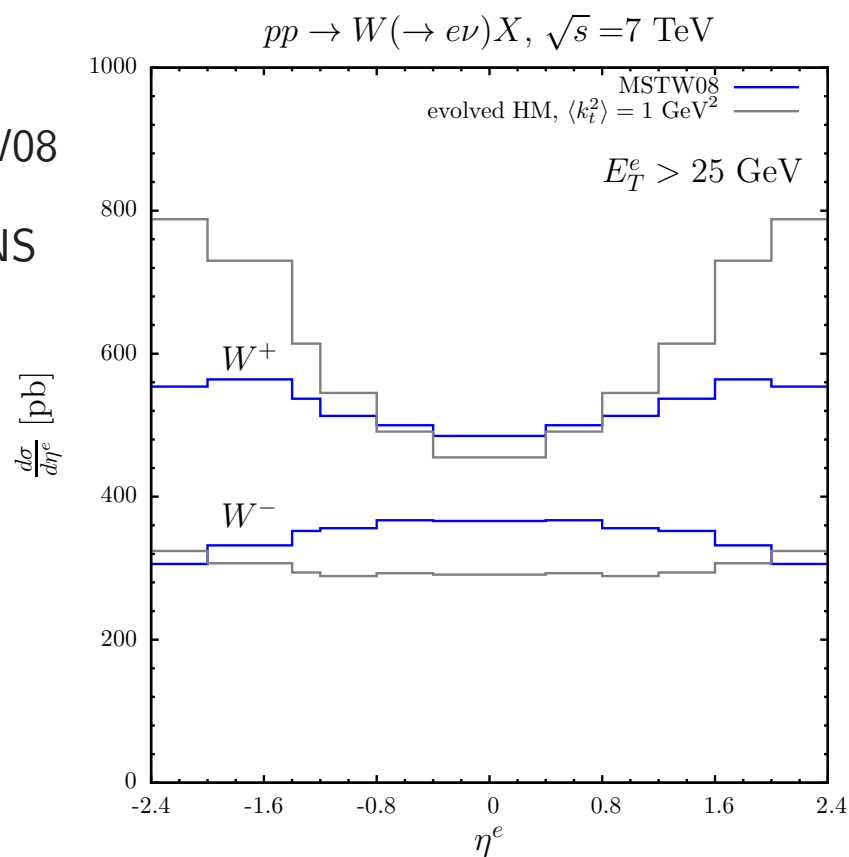
- $R_W(\eta^l) = \frac{d\sigma^{l^+}}{d\eta^l} / \frac{d\sigma^{l^-}}{d\eta^l}$

- Despite we are missing higher orders, the agreement is fair



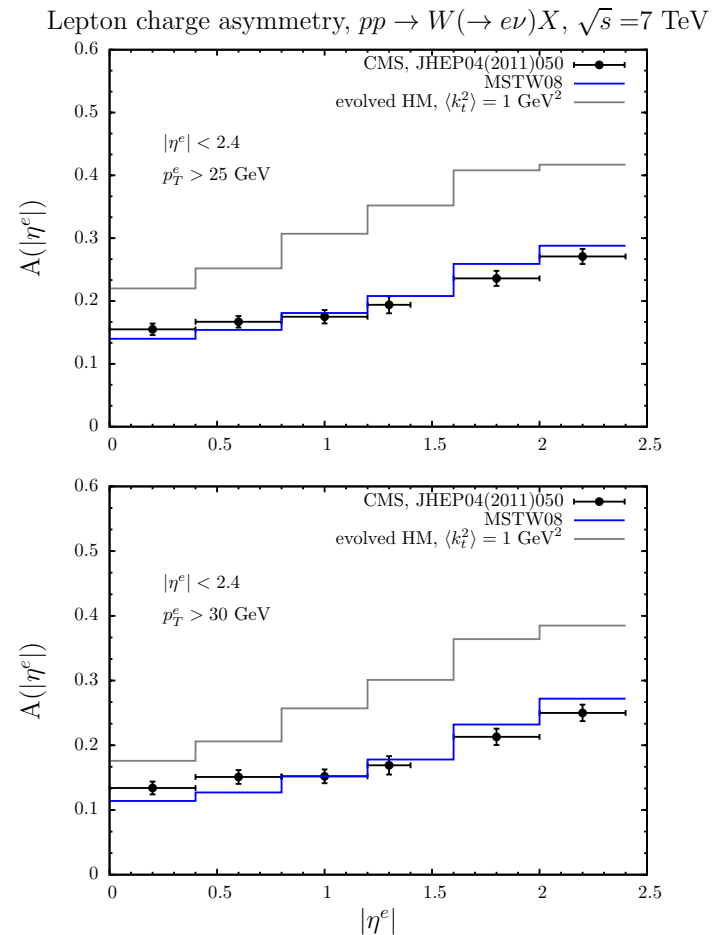
Charged lepton distributions: eHM vs MSTW08

- Evolved Hadronic Model (eHM) vs MSTW08
- private evo code, $\alpha_s(M_Z) = 0.139$, VFNS
- $m_c = 1.4$, $m_b = 4.76$ GeV
- infrared sensitivity : $\alpha_s(Q^2 + \langle k_t^2 \rangle)$
- $\langle k_t^2 \rangle = 1$ GeV²
- $\mu_0^2 < Q^2 < M_W^2$, $\mu_0^2 = 0.08$ GeV²
- Normalisation almost ok, shape different



Lepton charge asymmetry, CMS

- Observable : $A(\eta^l) = \frac{\frac{d\sigma^{l^+}}{d\eta^l} - \frac{d\sigma^{l^-}}{d\eta^l}}{\frac{d\sigma^{l^+}}{d\eta^l} + \frac{d\sigma^{l^-}}{d\eta^l}}$
- Observable is pdf-shape sensitive
- Hadronic model (HM) evolved to $Q = M_W$
- infrared sensitivity : $\alpha_s(Q^2 + \langle k_t^2 \rangle)$
- $\langle k_t^2 \rangle = 1 \text{ GeV}^2$
- MSTW08 : shape ok
- HM : higher than observed asymmetry
 $\rightarrow u(x) = 2d(x)$ not supported by data



$\sigma(WW)$ with GS09 double PDFs

- Compare with results presented in the paper of Gaunt & al., EPJ C69 (2010) 53
- Basic settings and cuts:
 - $\sqrt{s} = 14$ TeV, $E_T^l > 20$ GeV, $|\eta^l| < 2.5$, no inv. mass cut
 - $\mu_F = M_W$, LO, NWA, GS09 double PDFs, $n_f = 5$
 - $\sigma_{eff} = 14.5$ mb
 - $\sigma(W^\pm W^\pm) = 1/2[\sigma(W^\pm)]^2$ (NB: at differential level)
 - neta=10, nET=100, $\epsilon = 0.1$, run time: 5 hours (locally)

σ fiducial	EPJ C69 (2010) 53 [fb]	Mycode [fb]
$\sigma^{W^-W^-}$	0.46	0.58
$\sigma^{W^+W^+}$	0.82	1.05

- $\sim 20\%$ disagreement, $\sigma_{LO} > \sigma_{NLL}$, under study
- however σ 's calculated under different approximations

Muons invariant mass cut

- CMS : $20 < M_{ll} < 70$ GeV, $M_{ll} > 105$ GeV
the cut suppresses WZ and ZZ backgrounds
- $l_i^\mu = E_{T,i}(\cosh \eta_i, \sin \phi_i, \cos \phi_i, \sinh \eta_i) \quad i = 1, 2$
- $M_{ll}^2 = 2E_{T,1}E_{T,2}(\cosh \Delta\eta - \cos \Delta\phi) \quad \Delta\eta = \eta_2 - \eta_1, \quad \Delta\phi = \phi_2 - \phi_1$
- ME does not depend upon ϕ_i 's, unfold the integrals

$$\frac{d^4\sigma^{pp \rightarrow WWX}}{d\eta_1 dE_{T,1} d\eta_2 dE_{T,2}} = \frac{1}{2\sigma_{eff}} D_{ij}(x_1, x_2, M_W) D_{kl}(x_3, x_4, M_W) \frac{d^2\sigma_{ik}^{pp \rightarrow WX}}{d\eta_1 dE_{T,1}} \frac{d^2\sigma_{jl}^{pp \rightarrow WX}}{d\eta_2 dE_{T,2}} \mathcal{I}$$

- The function \mathcal{I} provides the necessary reweighting

$$\mathcal{I}(\eta_i, E_{T,i}) = (2\pi)^{-1} \int_0^{2\pi} d\Delta\phi \prod_n \Theta_n(M_{ll}(E_{T,i}, \Delta\eta, \Delta\phi), M_n^{cut})$$

Factorised dPDFs and impact of mass cut

- **Preliminar simulations** ($n_f = 4$, $n_{\text{eta}}=10$, $n_{\text{ET}}=10$, $\epsilon = 0.33$, run time: few minutes)
 - $\sqrt{s} = 13$ TeV, $E_T^l > 25$ GeV, $|\eta^l| < 2.4$
 - Mass cut: $20 < M_{\mu\mu} < 70$ GeV, $M_{\mu\mu} > 105$ GeV
 - $\sigma_{\text{eff}} = 14.5$ mb
 - $f_{ij}(x_a, x_b, M_W) = f_i(x_a, M_W) f_j(x_b, M_W) (1 - x_a - x_b)^n$

Mass cut on	$n = 0$ [fb]	$n = 1$ [fb]	$n = 2$ [fb]
$\sigma^{W^- W^-}$	0.41	0.39	0.37
$\sigma^{W^+ W^+}$	0.75	0.69	0.64
Mass cut off	$n = 0$ [fb]	$n = 1$ [fb]	$n = 2$ [fb]
$\sigma^{W^- W^-}$	0.61	0.57	0.54
$\sigma^{W^+ W^+}$	1.08	1.00	0.93

- Mass cut impact **30-33%**, n -impact (large x) **10-15 %**

Next step

- use evolved our own double PDFs
- no need to plug σ_{eff}

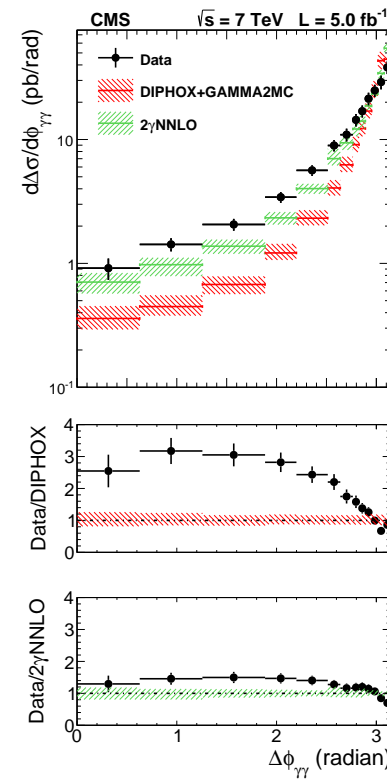
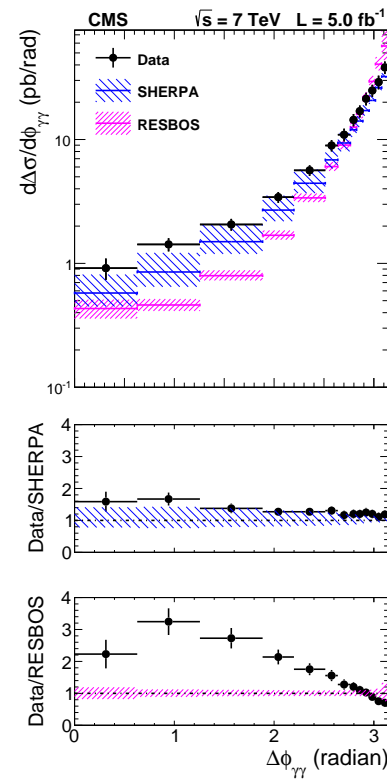
$$\frac{d^4\sigma^{pp\rightarrow WWX}}{d\eta_1 dE_{T,1} d\eta_2 dE_{T,2}} = \sum_{i,k,j,l} \frac{1}{2} \int d^2\mathbf{b} D_{ij}(x_1, x_2, \mathbf{b}, M_W) D_{kl}(x_3, x_4, \mathbf{b}, M_W).$$

$$\cdot \frac{d^2\sigma_{ik}^{pp\rightarrow WX}}{d\eta_1 dE_{T,1}} \frac{d^2\sigma_{jl}^{pp\rightarrow WX}}{d\eta_2 dE_{T,2}} \mathcal{I}(\eta_i, E_{T,i})$$

- we should
 - tackle computational issue related to additional \mathbf{b} integration
 - handle large-index matrices (x_i 's, flavours, etc.)

Diphoton channel

- Consider $pp \rightarrow \gamma\gamma X$
- Higgs, 750 GeV candidate etc.
- cross sections known at NNLO + resummations.
- CMS measurement: EPJ C74 (2014) 3129
- $\sqrt{s} = 7 \text{ TeV}$, $|\eta^\gamma| < 2.5$,
 $E_T^\gamma > 25, 40 \text{ GeV}$,
 $\Delta R(\gamma_1, \gamma_2) > 0.45$,
 $\sigma \sim 17 \text{ pb}$
- theory low at low $\Delta\Phi_{\gamma\gamma}$:
 possible DPS contribution?



Diphoton channel: data-driven DPS estimate

- Consider $pp \rightarrow \gamma X$, CMS measurement: PRD84 (2011) 052011
- $\sqrt{s} = 7$ TeV, $|\eta^\gamma| < 2.5$
- from published $d^2\sigma/dE_T d|\eta|$:
 $\sigma(E_T^\gamma > 25 \text{ GeV}) \sim 28 \text{ nb}$, $\sigma(E_T^\gamma > 40 \text{ GeV}) \sim 4 \text{ nb}$
- Assume $\sigma_{eff} = 14.5 \text{ mb}$
- $\sigma^{DPS} = \sigma(ij \rightarrow \gamma_1 X) \otimes \sigma(lk \rightarrow \gamma_2 X) / \sigma_{eff}$
 $\sigma^{DPS}(E_{T,1} > 25 \text{ GeV}, E_{T,2} > 40 \text{ GeV}) = 8 \text{ fb}$
- $\sigma^{SPS}(exp) \simeq 17 \text{ pb}$, but for $0 < \Delta\Phi_{\gamma\gamma} < \pi/5 \rightarrow \sigma^{SPS}(exp) \simeq \mathbf{0.57 \text{ pb}}$
- Assuming flat behaviour of DPS vs $\Delta\Phi_{\gamma\gamma}$:
 - $\sigma^{DPS}(E_{T,1} > 25 \text{ GeV}, E_{T,2} > 40 \text{ GeV}, 0 < \Delta\Phi_{\gamma\gamma} < \pi/5) = \mathbf{8/5 \text{ fb}}$
 - Assume integrated lumi $10 \text{ fb}^{-1} \rightarrow \mathbf{S/\sqrt{B}} \sim 0.2$
- DPS alone is too small to fill the gap since (theory-exp) $\sim 0.3 \text{ pb}$

Conclusions

- First benchmarks with other codes: OK
- LO reasonable, as a first crude approx
- Code optimisation underway
- Almost ready to implement our own double PDFs:
model dependent but σ_{eff} -free estimate of same sign Ws cross section
- Looking for DPS in other channels :
 - $\gamma\gamma$ (not feasible for now)
 - $Wb\bar{b}$ (within reach given tools at our disposal)
 - UE in DY (one hard/one soft), connection DPS vs UE
 - photoproduction of 4 jets in pA and eP to pin down the $3 \rightarrow 4$ contribution