

Theoretical implications of dark matter (DM) constraints from the LHC and (in)direct searches

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Evolution of LHC DM models

Effective field
theory

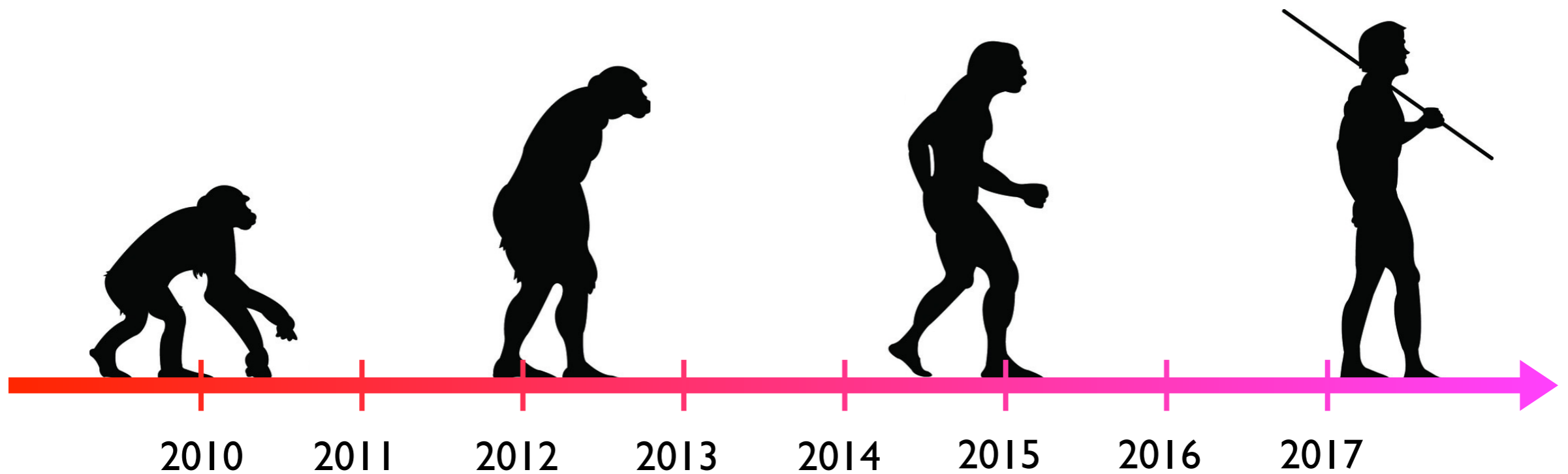
$$\frac{m_q}{\Lambda^3} \bar{\chi} \chi \bar{q} q$$

Simplified
models

$$g_\chi \bar{\chi} \chi S + \frac{g_q y_q}{\sqrt{2}} \bar{q} q S$$

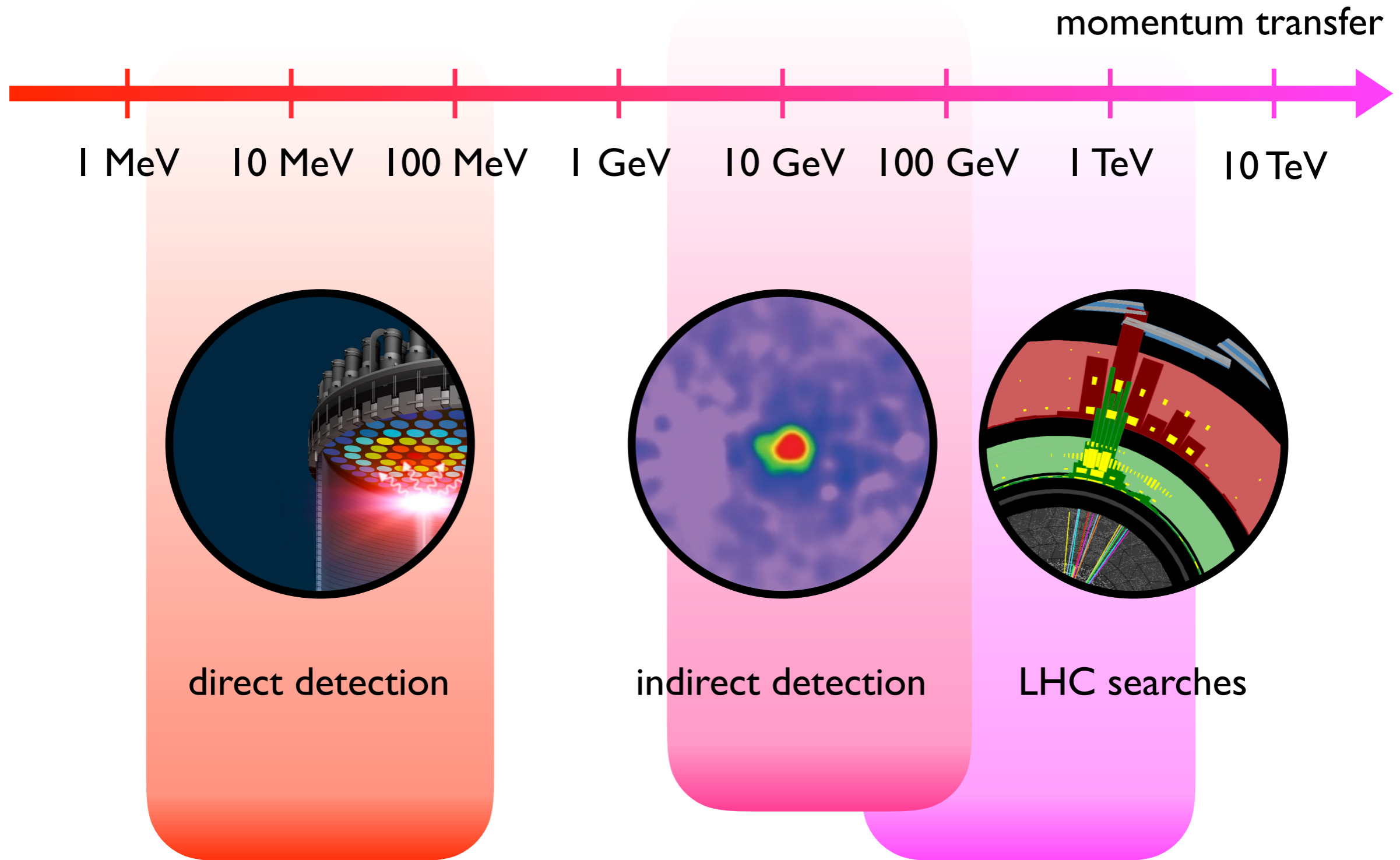
Consistent simplified
models

$$g_\chi \bar{\chi} \chi s + Y_q \bar{q} H q + \mu s |H|^2$$

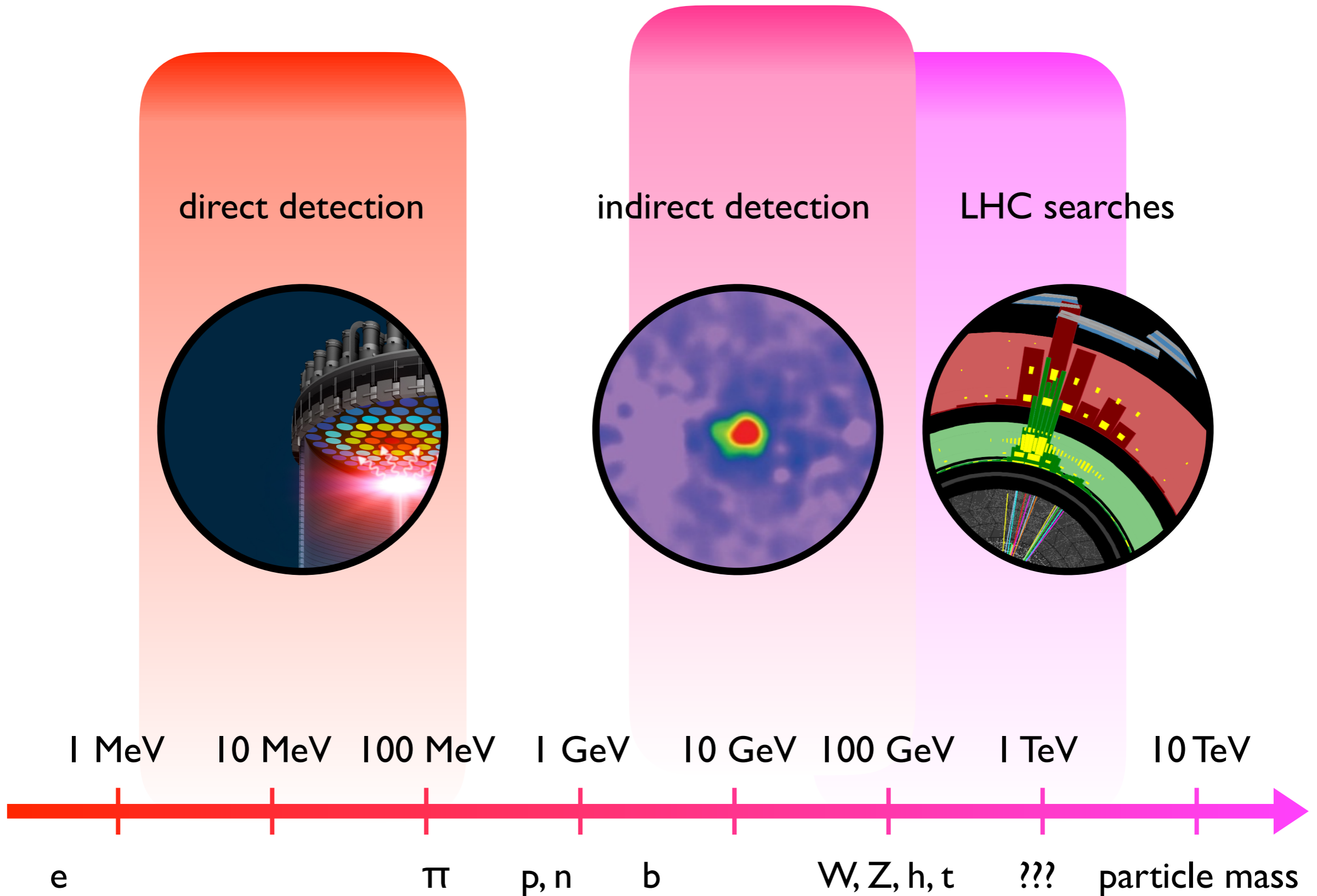


[idea & artwork adopted from Bauer]

Scales in DM searches



Scales in DM searches



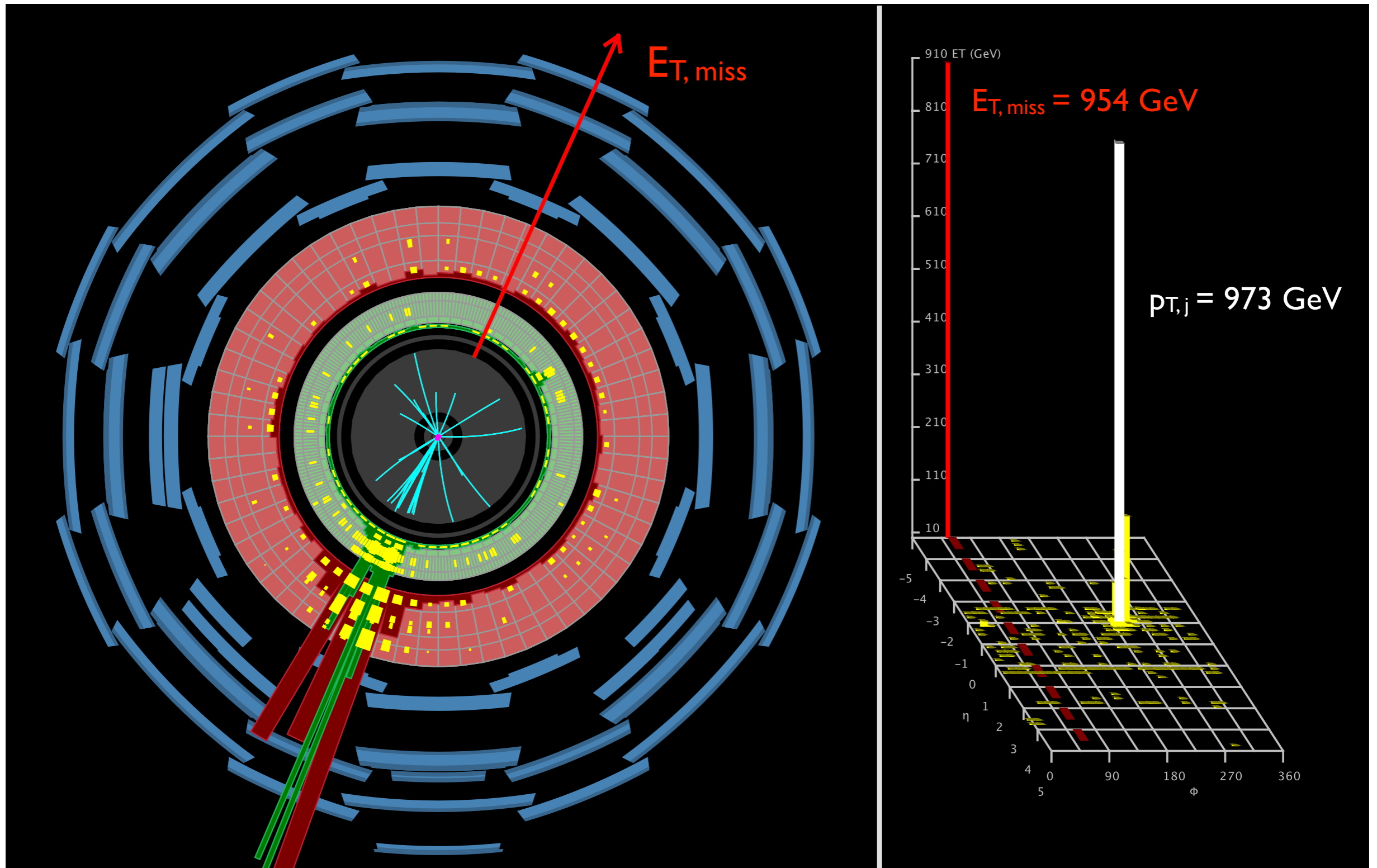
What is an effective field theory (EFT)?

[...] An effective field theory includes the appropriate degrees of freedom to describe physical phenomena occurring at a chosen length scale or energy scale, while ignoring substructure and degrees of freedom at shorter distances (or, equivalently, at higher energies) [...] Effective field theories typically work best when there is a large separation between length scale of interest and the length scale of the underlying dynamics [...]

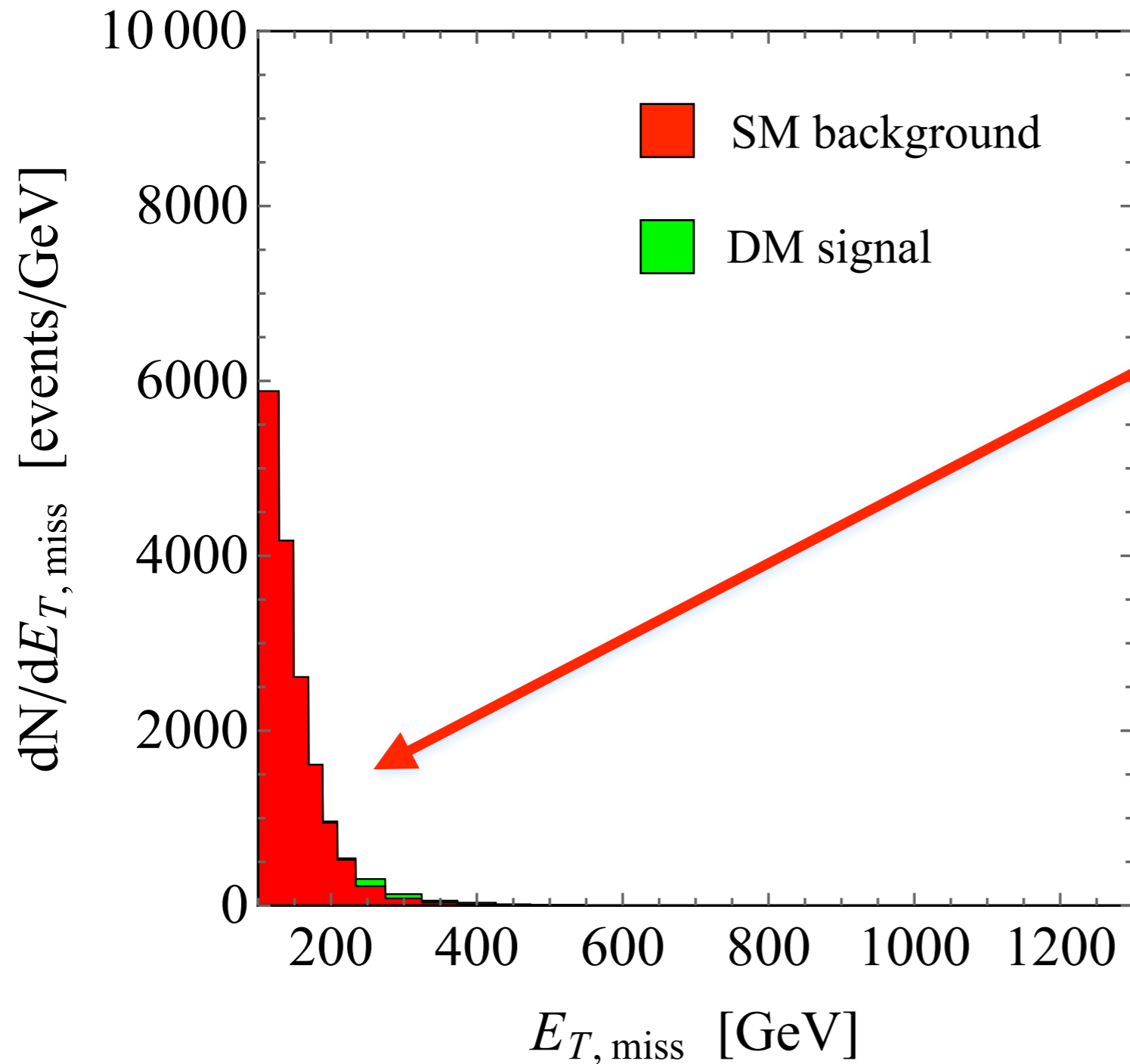
[from Wikipedia, the free encyclopedia, https://en.wikipedia.org/wiki/Effective_field_theory]

Mono-jet searches

[2015 ATLAS data (event 606734214, run 279284)]

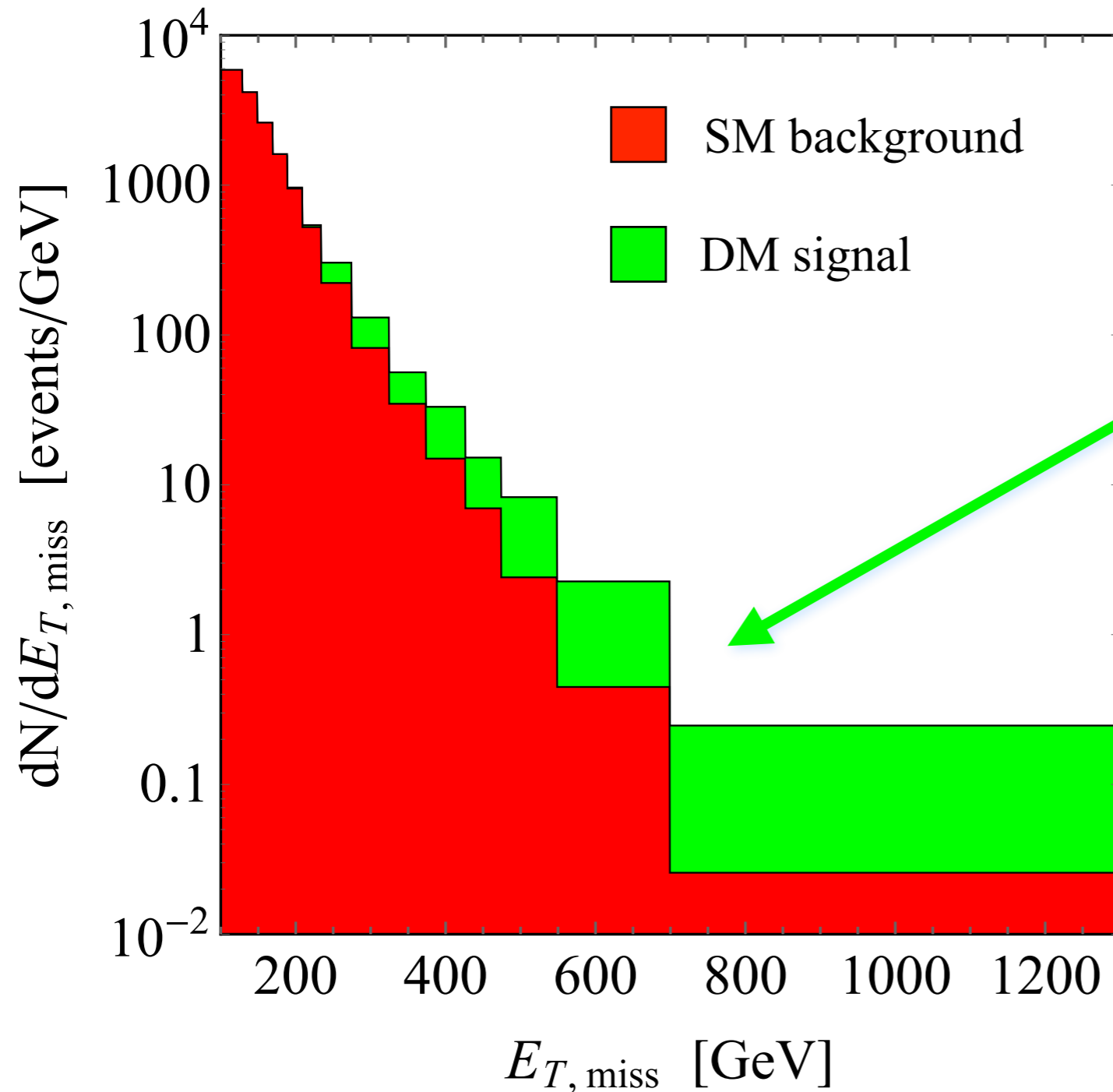


Signal vs. background



huge SM background, that arises in case of mono-jet searches from Z+jet production with Z boson decaying to neutrinos

Signal vs. background



presence of DM
manifests itself in small
enhancement in tail of
missing energy $E_{T,miss}$
distribution

[see Lindert et al., [1705.04664](#) for dedicated theory effort to improve understanding of DM backgrounds]

Does DM EFT work at LHC?

Name	Operator	Coefficient
D1	$\bar{\chi}\chi\bar{q}q$	m_q/M_*^3
D2	$\bar{\chi}\gamma^5\chi\bar{q}q$	im_q/M_*^3
D3	$\bar{\chi}\chi\bar{q}\gamma^5q$	im_q/M_*^3
D4	$\bar{\chi}\gamma^5\chi\bar{q}\gamma^5q$	m_q/M_*^3
D5	$\bar{\chi}\gamma^\mu\chi\bar{q}\gamma_\mu q$	$1/M_*^2$
D6	$\bar{\chi}\gamma^\mu\gamma^5\chi\bar{q}\gamma_\mu q$	$1/M_*^2$
D7	$\bar{\chi}\gamma^\mu\chi\bar{q}\gamma_\mu\gamma^5q$	$1/M_*^2$
D8	$\bar{\chi}\gamma^\mu\gamma^5\chi\bar{q}\gamma_\mu\gamma^5q$	$1/M_*^2$
D9	$\bar{\chi}\sigma^{\mu\nu}\chi\bar{q}\sigma_{\mu\nu}q$	$1/M_*^2$
D10	$\bar{\chi}\sigma_{\mu\nu}\gamma^5\chi\bar{q}\sigma_{\alpha\beta}q$	i/M_*^2
D11	$\bar{\chi}\chi G_{\mu\nu}G^{\mu\nu}$	$\alpha_s/4M_*^3$
D12	$\bar{\chi}\gamma^5\chi G_{\mu\nu}G^{\mu\nu}$	$i\alpha_s/4M_*^3$
D13	$\bar{\chi}\chi G_{\mu\nu}\tilde{G}^{\mu\nu}$	$i\alpha_s/4M_*^3$
D14	$\bar{\chi}\gamma^5\chi G_{\mu\nu}\tilde{G}^{\mu\nu}$	$\alpha_s/4M_*^3$

One way to check:

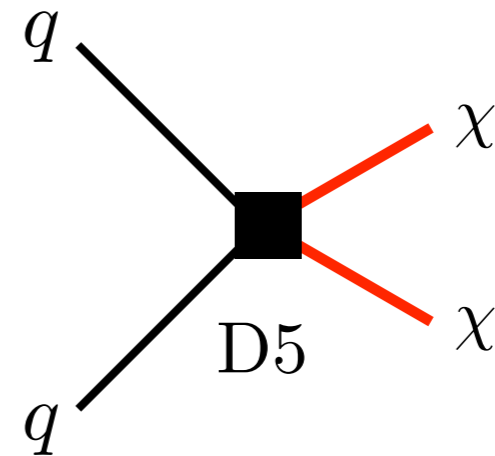
- (i) Pick one operator
- (ii) Construct simplified model that leads to operator in heavy mediator limit
- (iii) Calculate $E_{T, \text{miss}}$ & other distributions in both EFT & simplified model
- (iv) If shapes of distributions are similar, can use EFT as proxy for simplified model, otherwise not

[Zhang et al., 0912.4511; Beltran et al., 1002.4137; Goodman et al., 1005.1286, 1008.1783, 1009.0008; Bai et al., 1005.3797; Rajaraman et al., 1108.1196; Fox et al., 1109.4398; ...]

Tree-level example

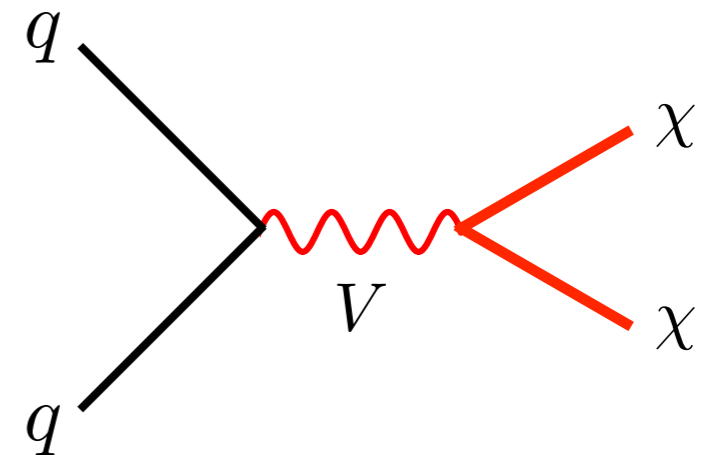
Vector operator:

$$D5 = \bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu q$$



Spin-1 simplified model:

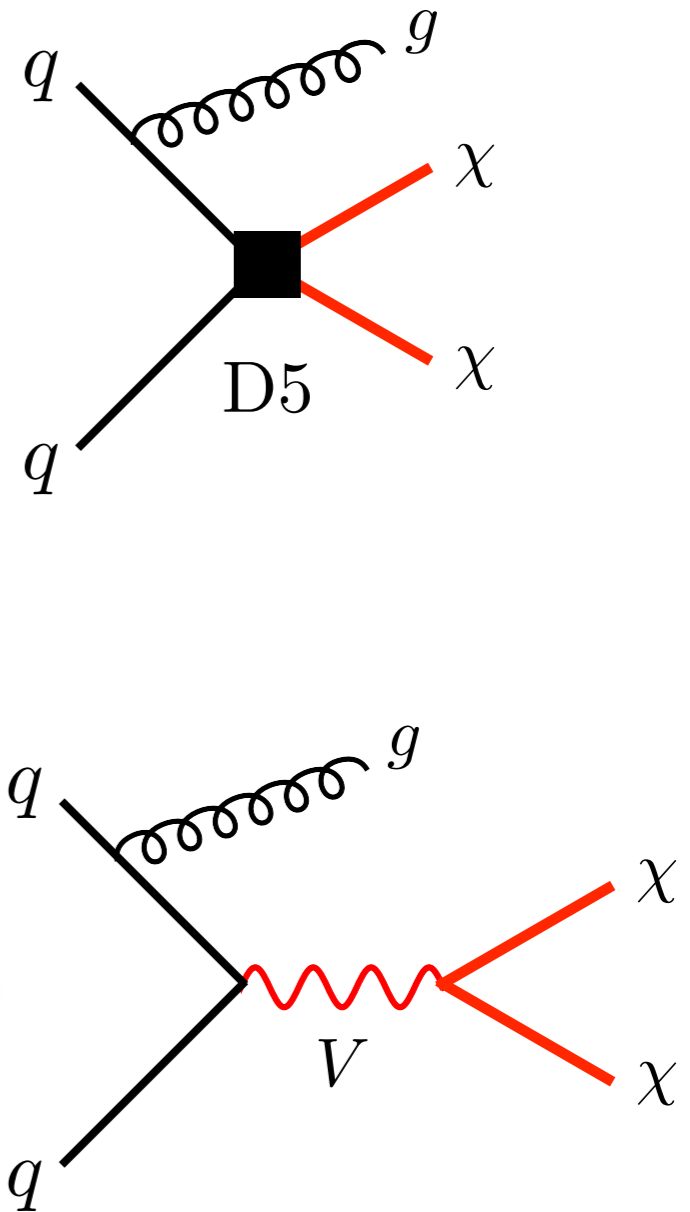
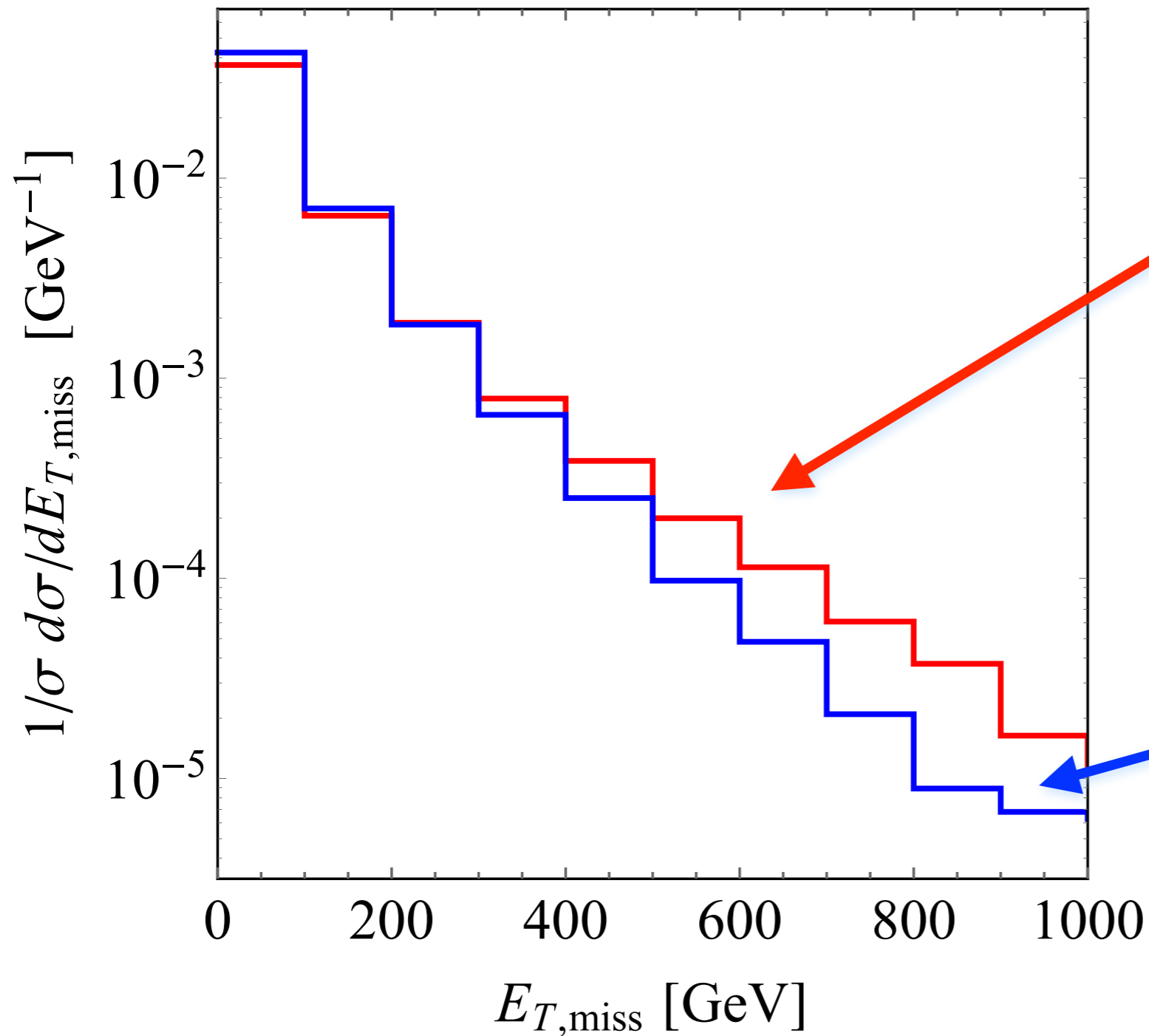
$$\mathcal{L}_V \supset g_\chi \bar{\chi} \gamma^\mu \chi V_\mu + \sum_q g_q \bar{q} \gamma^\mu q V_\mu$$



[Dudas et al., 0904.1745; Fox et al., 1104.4127; Frandsen et al., 1204.3839; ...; see also talk by Park]

D5: EFT vs. simplified model

$$M_V = 500 \text{ GeV}, \Gamma_V = 10 \text{ GeV}$$



EFT vs. simplified models: verdict

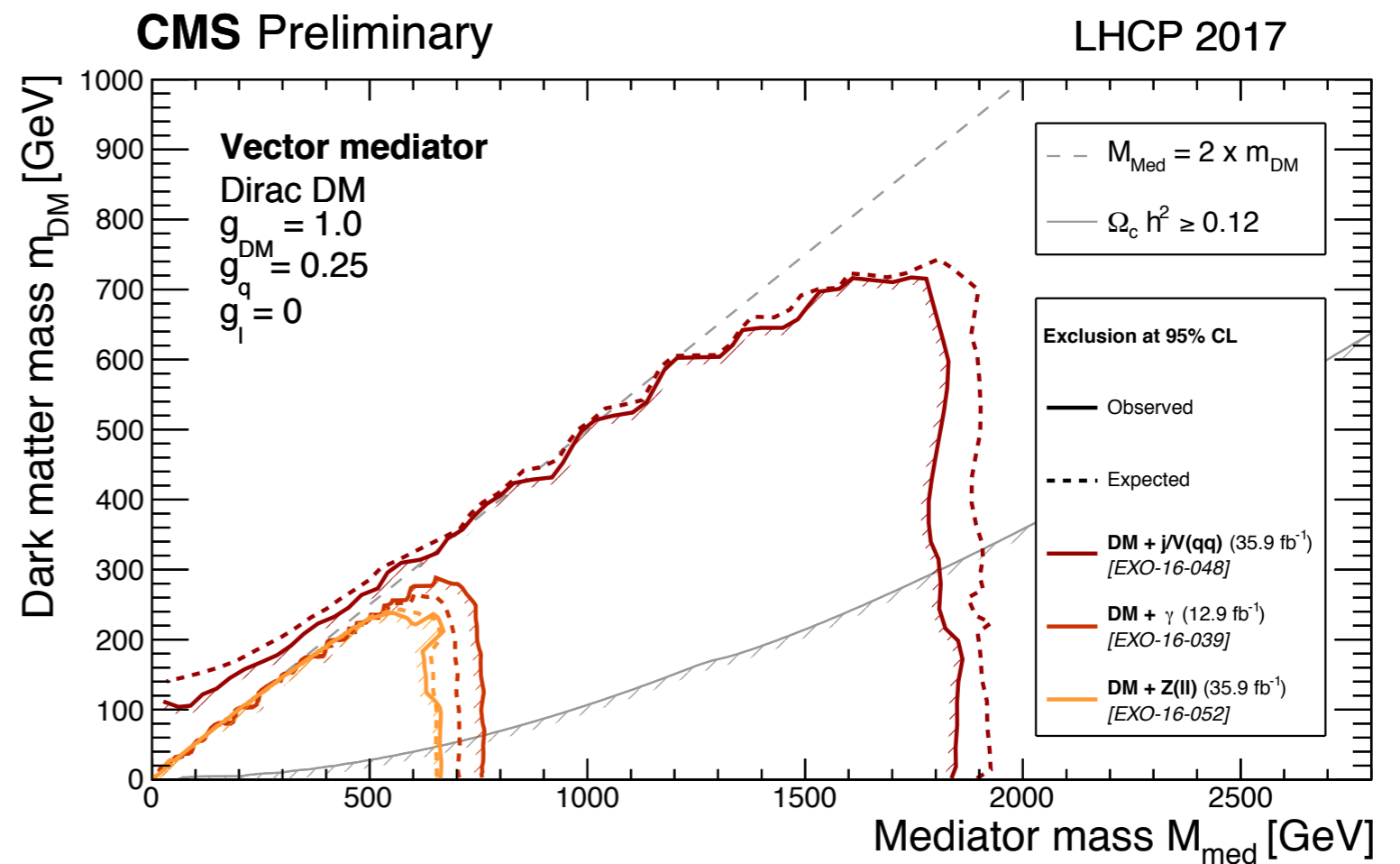
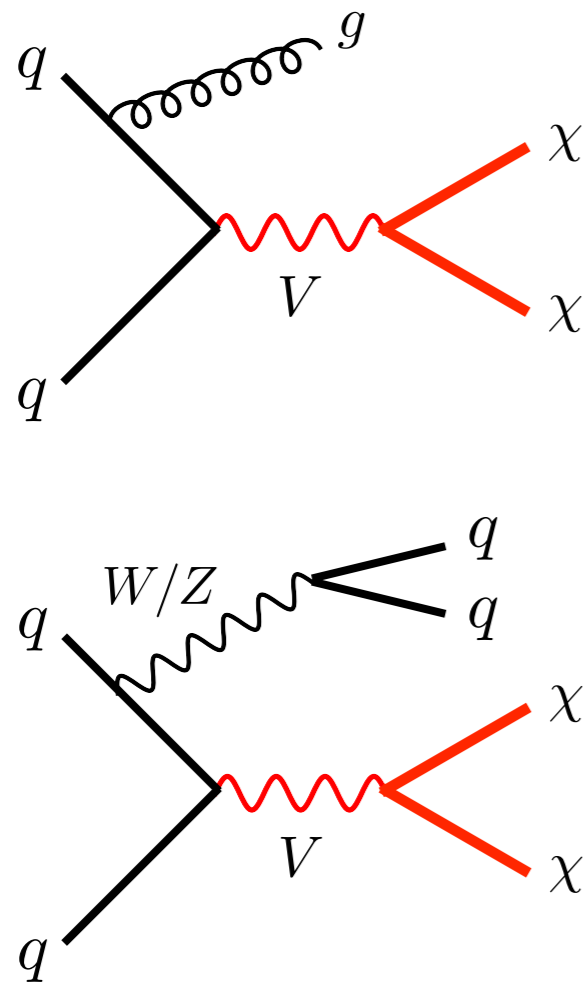
EFT often fails to correctly describe kinematical distributions of weakly-coupled simplified models with weak- or TeV-scale mediators. This flaw prompted ATLAS & CMS to move from EFT to simplified models when interpret $E_{T, \text{miss}}$ searches in LHC Run II

But in case of strongly-coupled DM candidates — composite fermions, pseudo-Nambu-Goldstone bosons, Goldstini, ... — EFT appropriate & sometimes even necessary to describe most important interactions at LHC

[see e.g. Bruggisser, Riva & Urbano, 1607.02474 & 1607.02475 for EFT discussion of strongly-coupled DM]

Spin-1 simplified models: 13 TeV limits

[<https://twiki.cern.ch/twiki/bin/view/CMSPublic/PhysicsResultsEXO>]

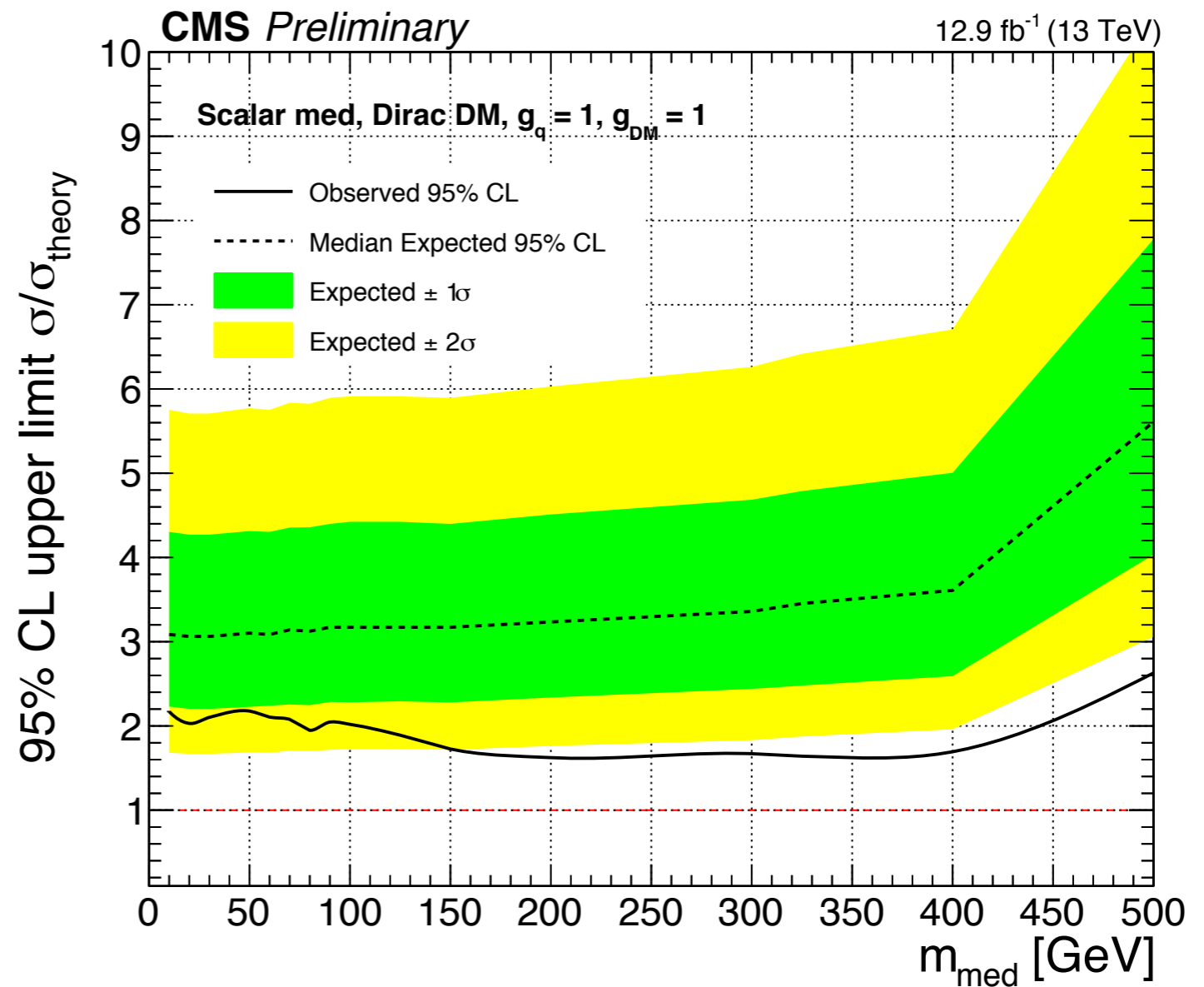
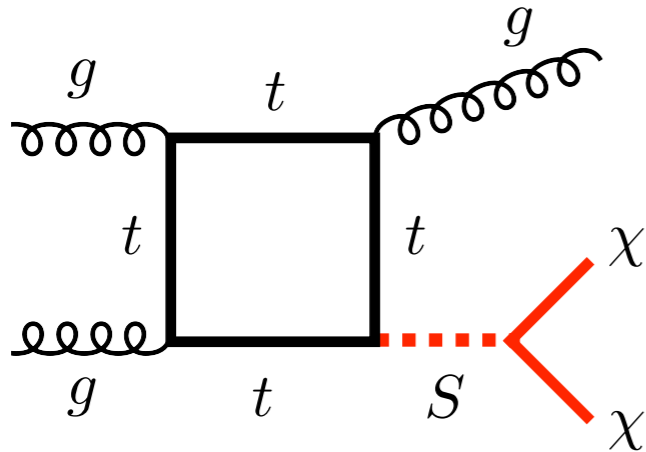


Latest $E_{\text{T,miss}} + \text{jets}$ searches exclude mediator masses up to around 1.8 TeV for both vector & axialvector exchange if $g_{\text{q}} = 0.25$, $g_{\chi} = 1$

[for more details see talks by Alpigiani, Hong & Khurana]

Spin-0 simplified models: 13 TeV limits

[CMS PAS EXO-16-037]

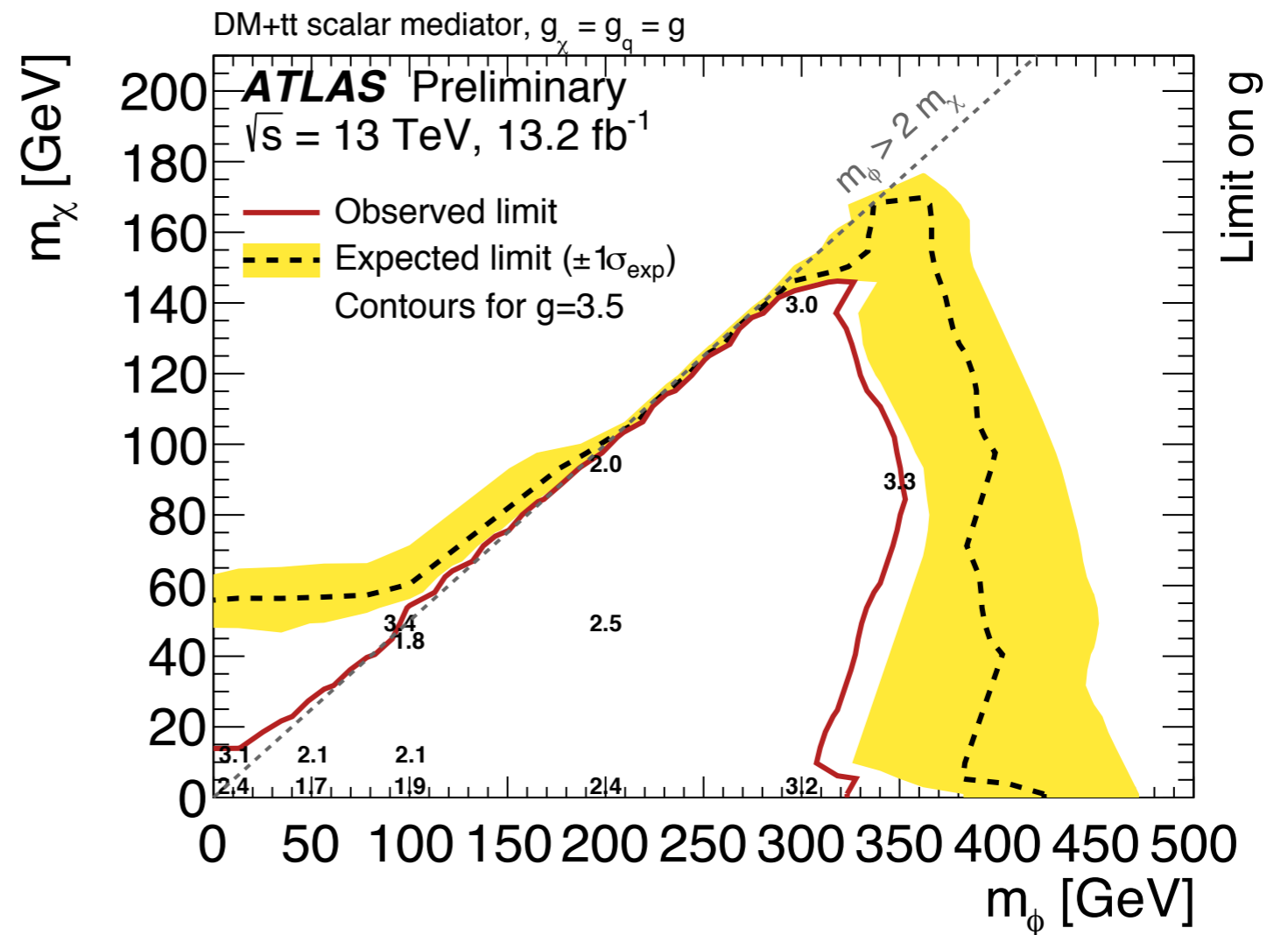
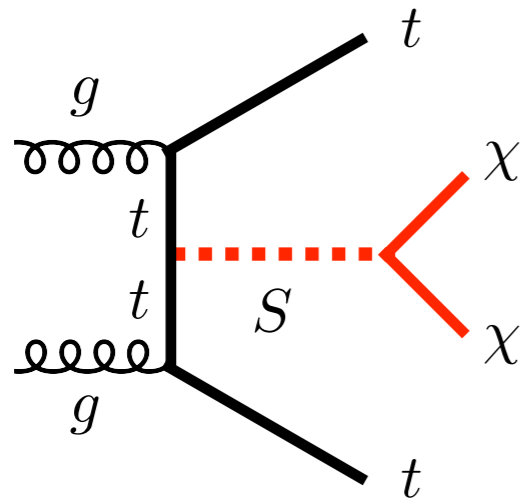


Mono-jet searches not yet sensitive to scalar models with weak couplings

[for more details see talks by Alpigiani, Hong & Khurana]

Spin-0 simplified models: 13 TeV limits

[ATLAS-CONF-2016-050]

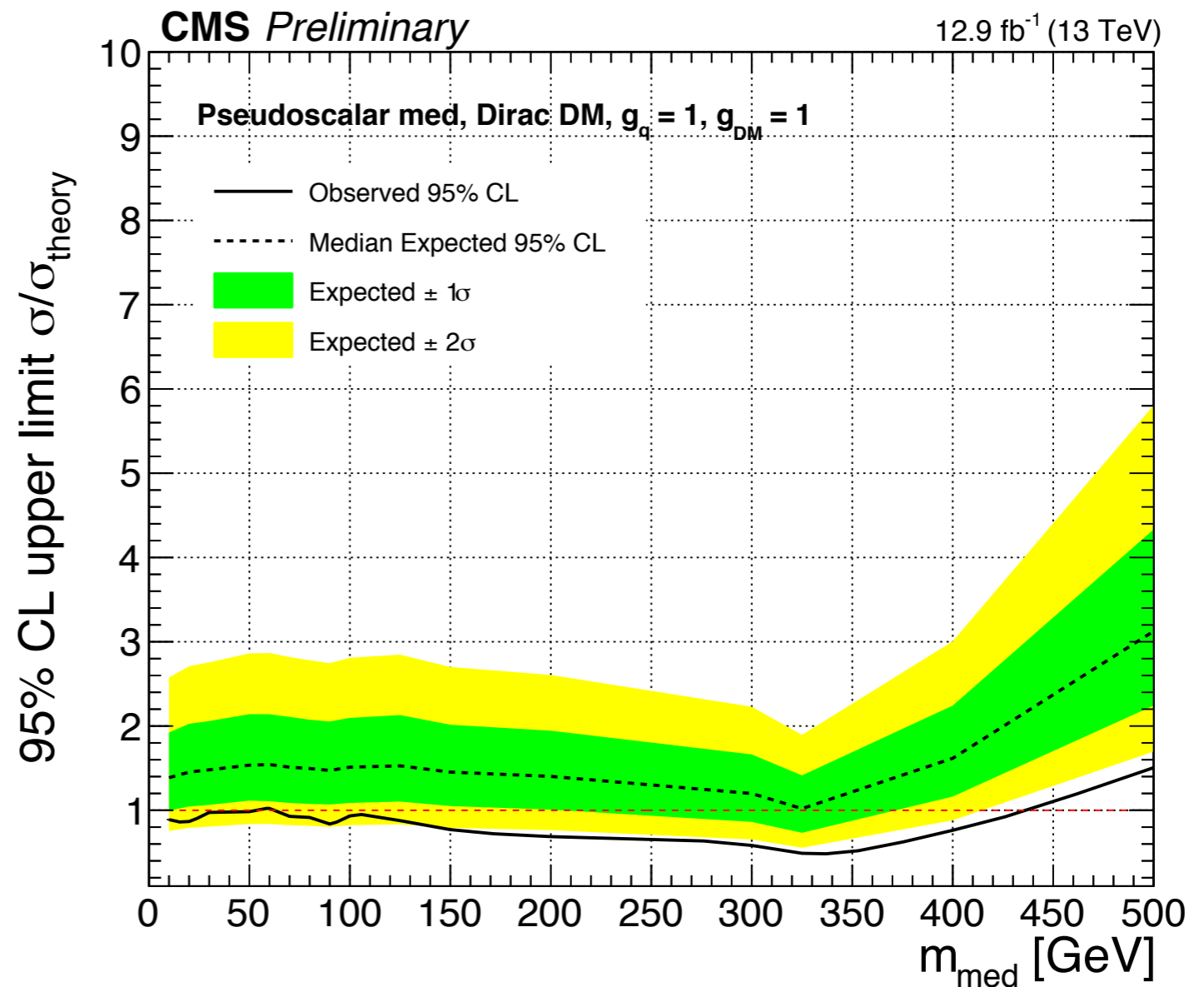
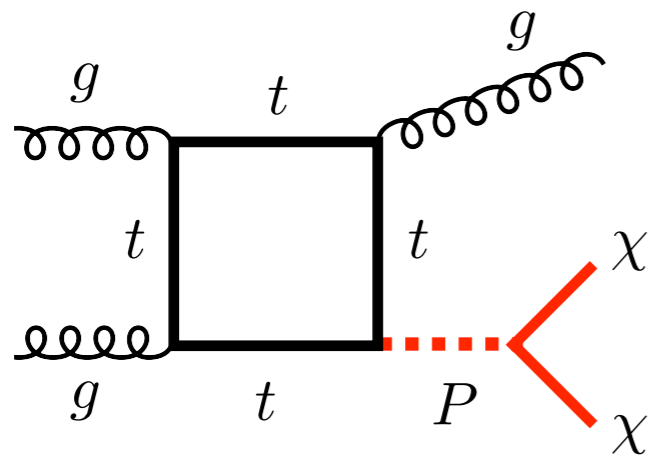


Strongly-coupled scalar models with mediator masses of 300 GeV can be tested via $E_{T,\text{miss}} + t\bar{t}$. Mediator broad in large parts of parameter space

[see backup slides for details]

Spin-0 simplified models: 13 TeV limits

[CMS PAS EXO-16-037]

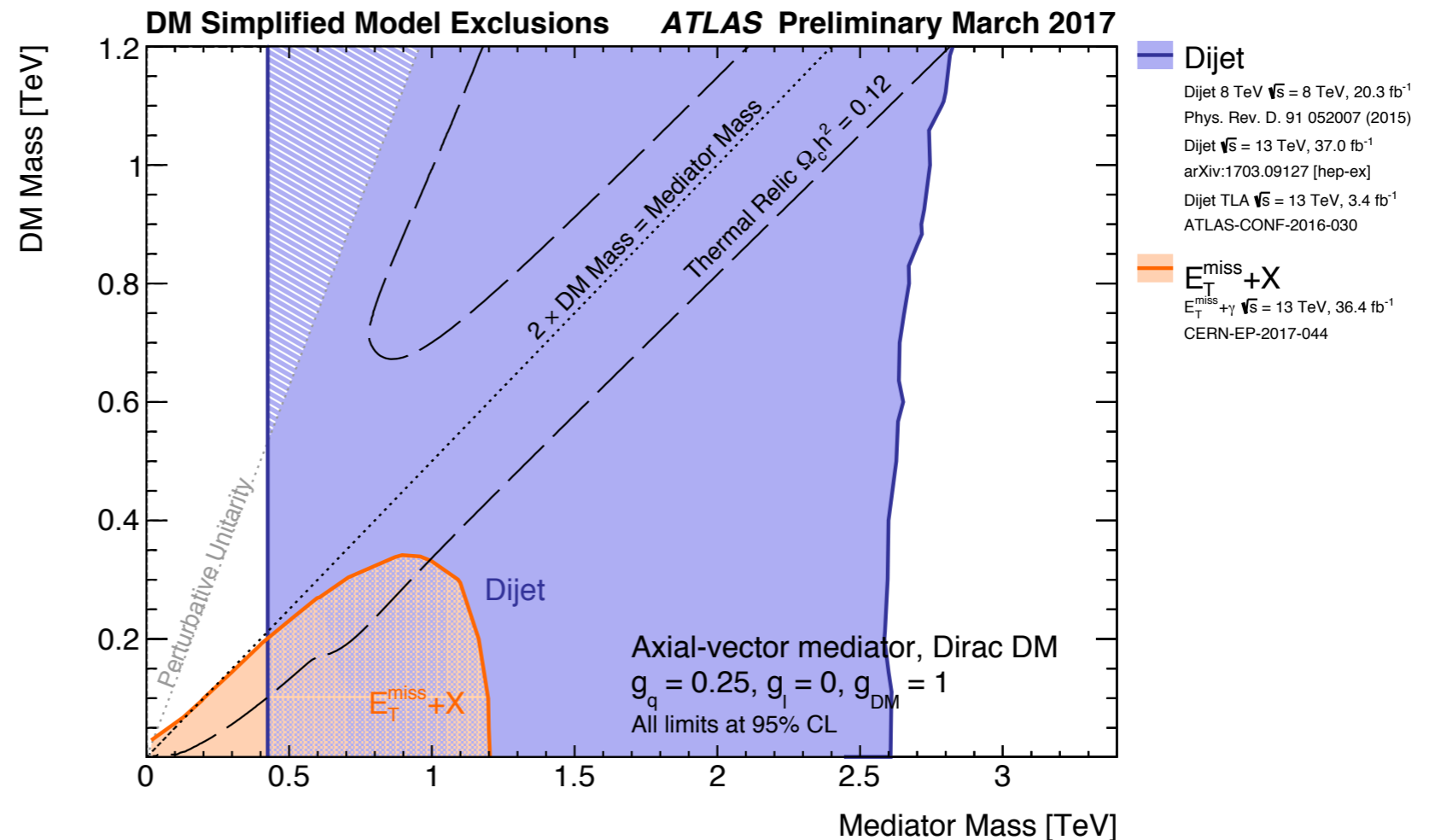
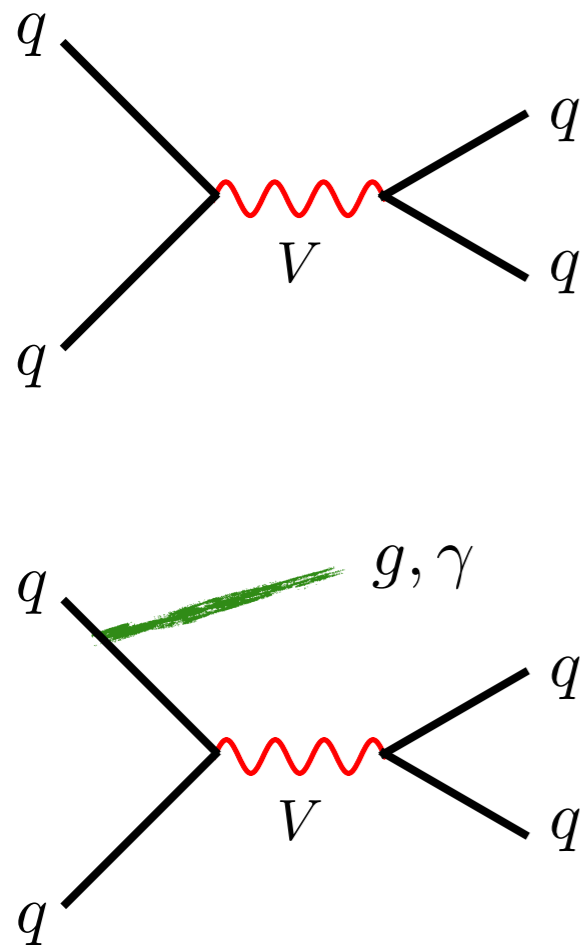


Since pseudoscalar production enhanced by a factor of more than 2,
mediator masses close to 450 GeV are excluded for $g_q = g_\chi = 1$

[for more details see talks by Alpigiani, Hong & Khurana]

Spin-1 simplified models: di-jet limits

[<https://twiki.cern.ch/twiki/bin/view/AtlasPublic/ExoticsPublicResults>]

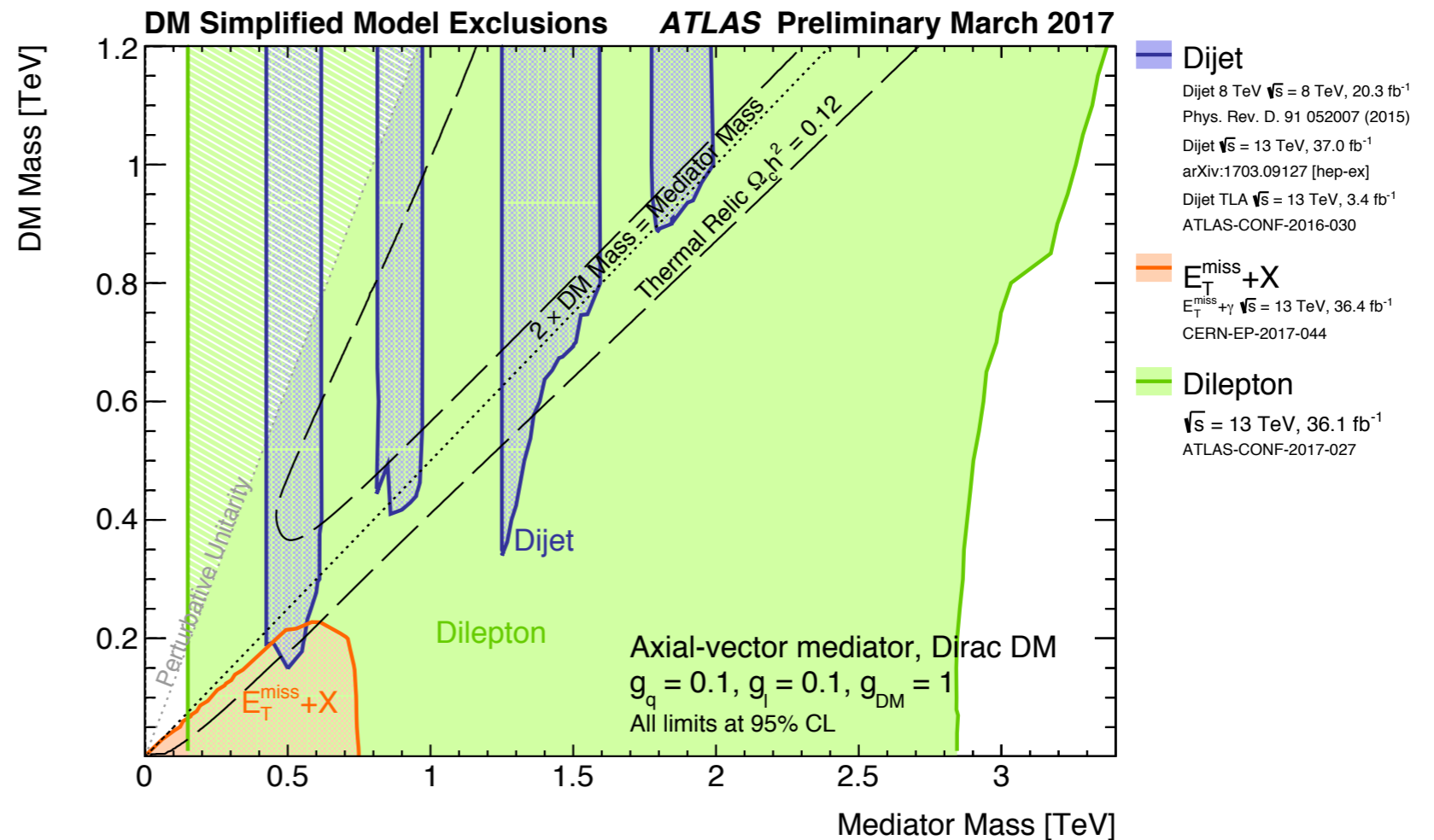
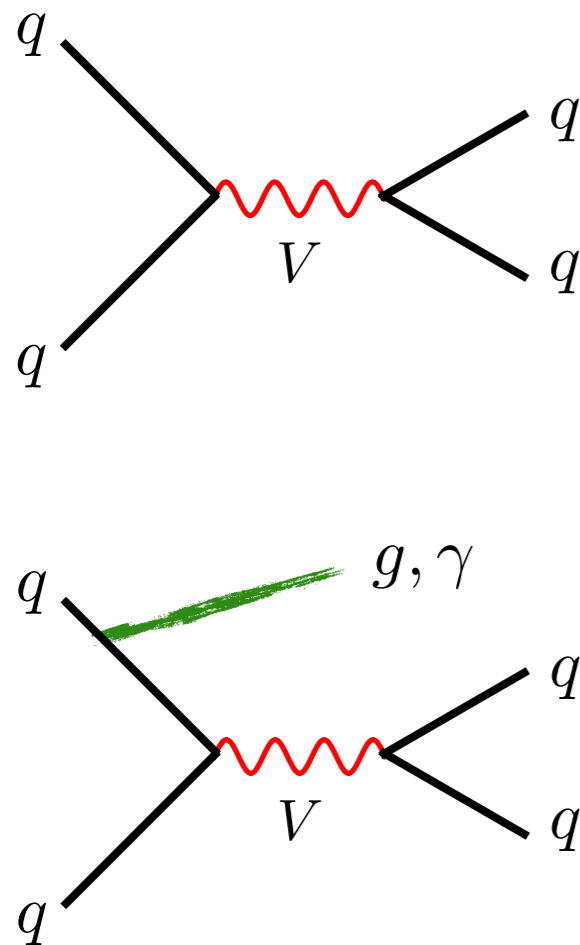


For coupling choice $g_q = 0.25, g_X = 1$ di-jet searches provide complementary constraints & exclude mediator masses from around 400 GeV to 2.8 TeV

[for more details see talks by Alpigiani, Hong & Khurana]

Spin-1 simplified models: di-jet limits

[<https://twiki.cern.ch/twiki/bin/view/AtlasPublic/ExoticsPublicResults>]



Di-jet limits can be weakened by reducing mediator-quark couplings g_q .
 If g_X kept perturbative mono-jet bounds also mitigated in such a case

[for more details see talks by Alpigiani, Hong & Khurana]

Other LHC non- $E_{T,miss}$ constraints

DM simplified models are also subject to

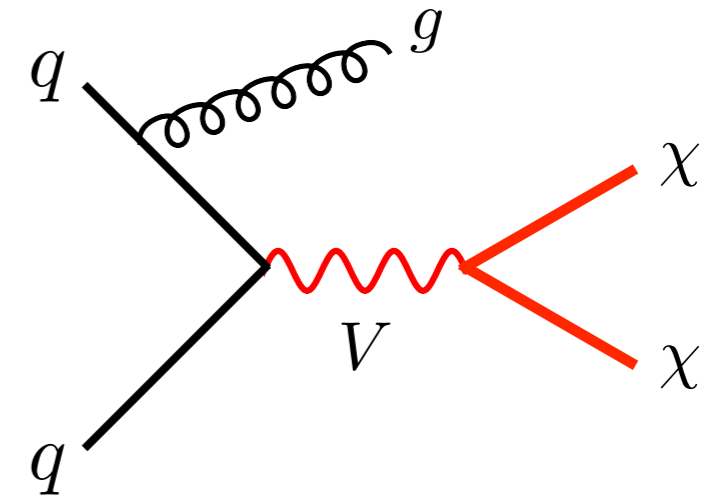
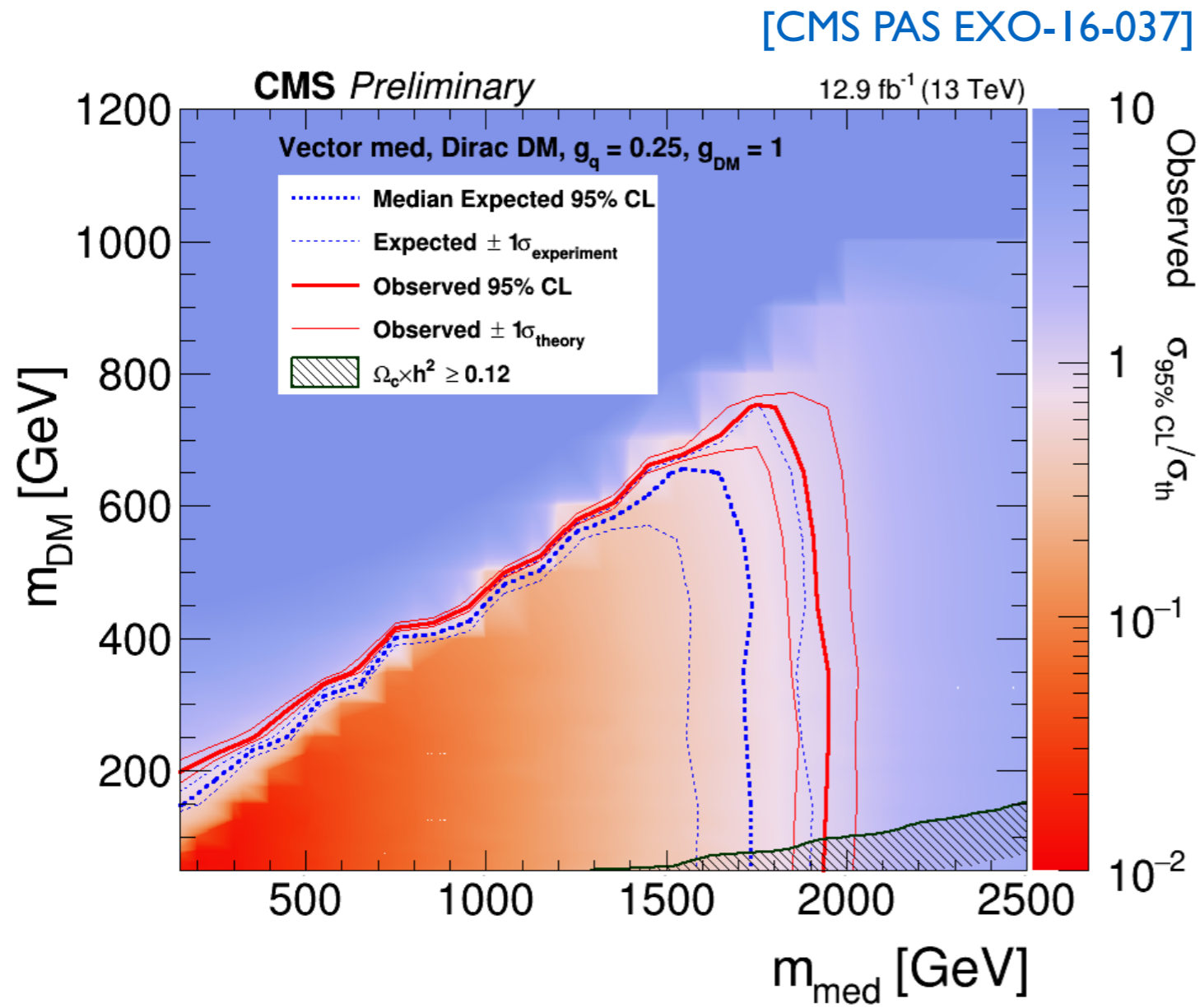
- (i) di-lepton bounds: only relevant in spin-1 case & simply avoided by setting $g_l = 0$ — unproblematic in vector case, but in simplest extension of axialvector model gauge invariance requires $g_l \neq 0$

[see Kahlhoefer et al., 1510.02110 & talks by Alpigiani, Hong & Khurana]

- (ii) di-top bounds: in spin-1 case not as stringent as di-jet limits, while in spin-0 models simple resonance searches not directly applicable due to interference of SM background with signal

[see Chala et al., 1503.05916 & backup slides]

From LHC bounds ...



... using an EFT ...

Most general EFT needed to describe χ -N interactions contains up to 14 different operators that induce 6 types of nuclear response functions:

$$\mathcal{O}_1 = 1_\chi 1_N$$

$$\mathcal{O}_3 = i\vec{S}_N \cdot \left[\frac{\vec{q}}{m_N} \times \vec{v}^\perp \right]$$

$$\mathcal{O}_4 = \vec{S}_\chi \cdot \vec{S}_N$$

$$\mathcal{O}_5 = i\vec{S}_\chi \cdot \left[\frac{\vec{q}}{m_N} \times \vec{v}^\perp \right]$$

$$\mathcal{O}_6 = \left[\vec{S}_\chi \cdot \frac{\vec{q}}{m_N} \right] \left[\vec{S}_N \cdot \frac{\vec{q}}{m_N} \right]$$

$$\mathcal{O}_7 = \vec{S}_N \cdot \vec{v}^\perp$$

$$\mathcal{O}_8 = \vec{S}_\chi \cdot \vec{v}^\perp$$

$$\mathcal{O}_9 = i\vec{S}_\chi \cdot \left[\vec{S}_N \times \frac{\vec{q}}{m_N} \right]$$

$$\mathcal{O}_{10} = i\vec{S}_N \cdot \frac{\vec{q}}{m_N}$$

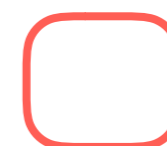
$$\mathcal{O}_{11} = i\vec{S}_\chi \cdot \frac{\vec{q}}{m_N}$$

$$\mathcal{O}_{12} = \vec{S}_\chi \cdot \left[\vec{S}_N \times \vec{v}^\perp \right]$$

$$\mathcal{O}_{13} = i \left[\vec{S}_\chi \cdot \vec{v}^\perp \right] \left[\vec{S}_N \cdot \frac{\vec{q}}{m_N} \right]$$

$$\mathcal{O}_{14} = i \left[\vec{S}_\chi \cdot \frac{\vec{q}}{m_N} \right] \left[\vec{S}_N \cdot \vec{v}^\perp \right]$$

$$\mathcal{O}_{15} = - \left[\vec{S}_\chi \cdot \frac{\vec{q}}{m_N} \right] \left[\left(\vec{S}_N \times \vec{v}^\perp \right) \cdot \frac{\vec{q}}{m_N} \right]$$



spin-independent (SI)



spin-dependent (SD)

... to DD limits ...

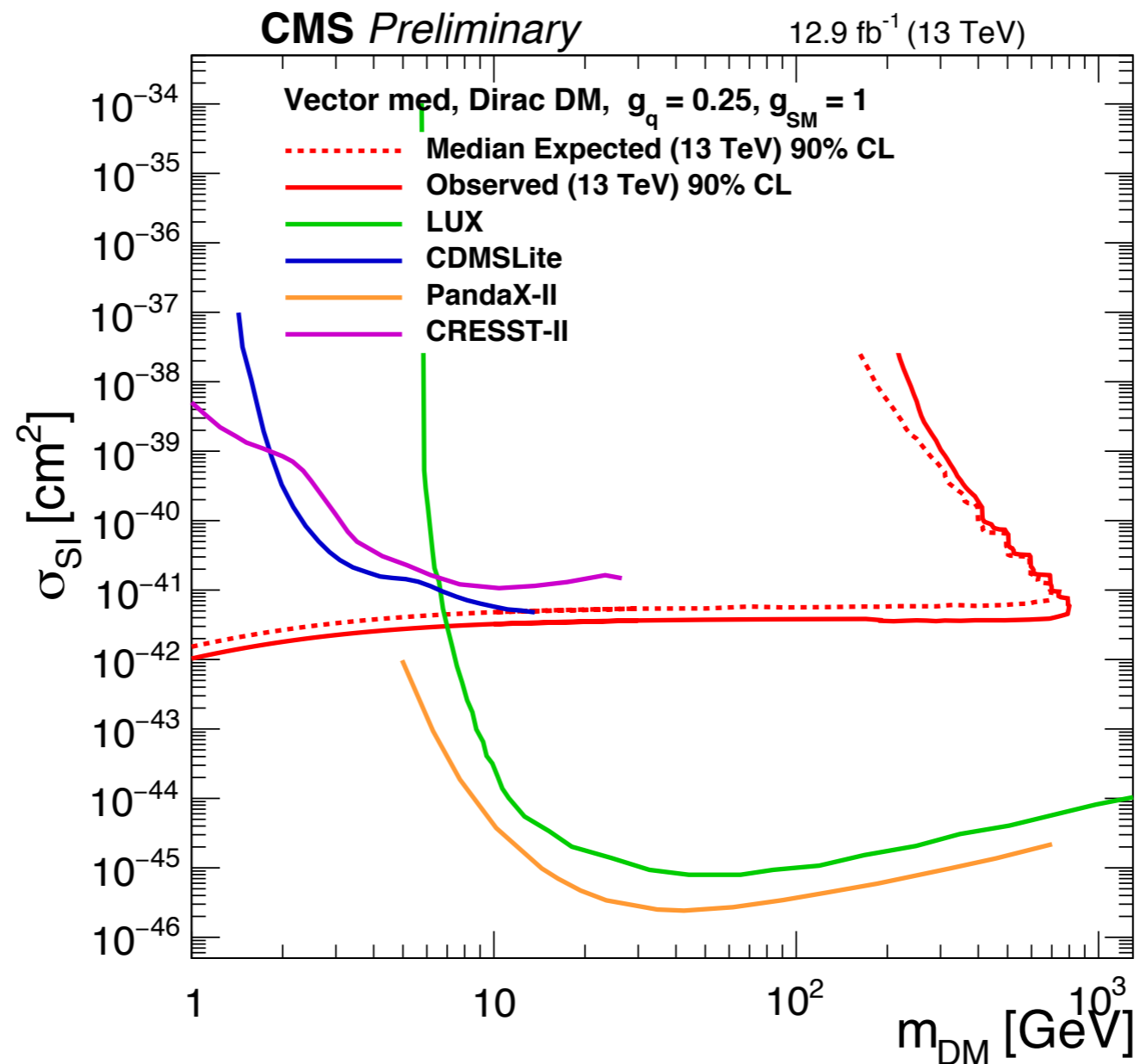
$$\begin{array}{c} \chi \\ \diagdown \\ \text{---} \\ \diagup \\ \chi \\ \text{---} \\ q^2 \downarrow \\ \text{---} \\ \text{---} \\ \diagup \\ q \\ \diagdown \\ q \end{array} \quad = \quad -\frac{g_\chi g_q}{M_V^2} \cdot \begin{array}{c} \chi \\ \diagdown \\ \text{---} \\ \text{---} \\ \diagup \\ q \\ \diagdown \\ q \end{array} \quad + \mathcal{O}(q^2/M_V^2)$$

$$\text{D5} = \bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu q \quad \longrightarrow \quad \mathcal{O}_1 = 1_\chi 1_N$$

$$\sigma_{\text{SI}} \simeq 6.9 \cdot 10^{-41} \text{ cm}^2 \left(\frac{g_\chi g_q}{0.25} \right)^2 \left(\frac{1 \text{ TeV}}{M_V} \right)^4 \left(\frac{\mu_{n\chi}}{1 \text{ GeV}} \right)^2$$

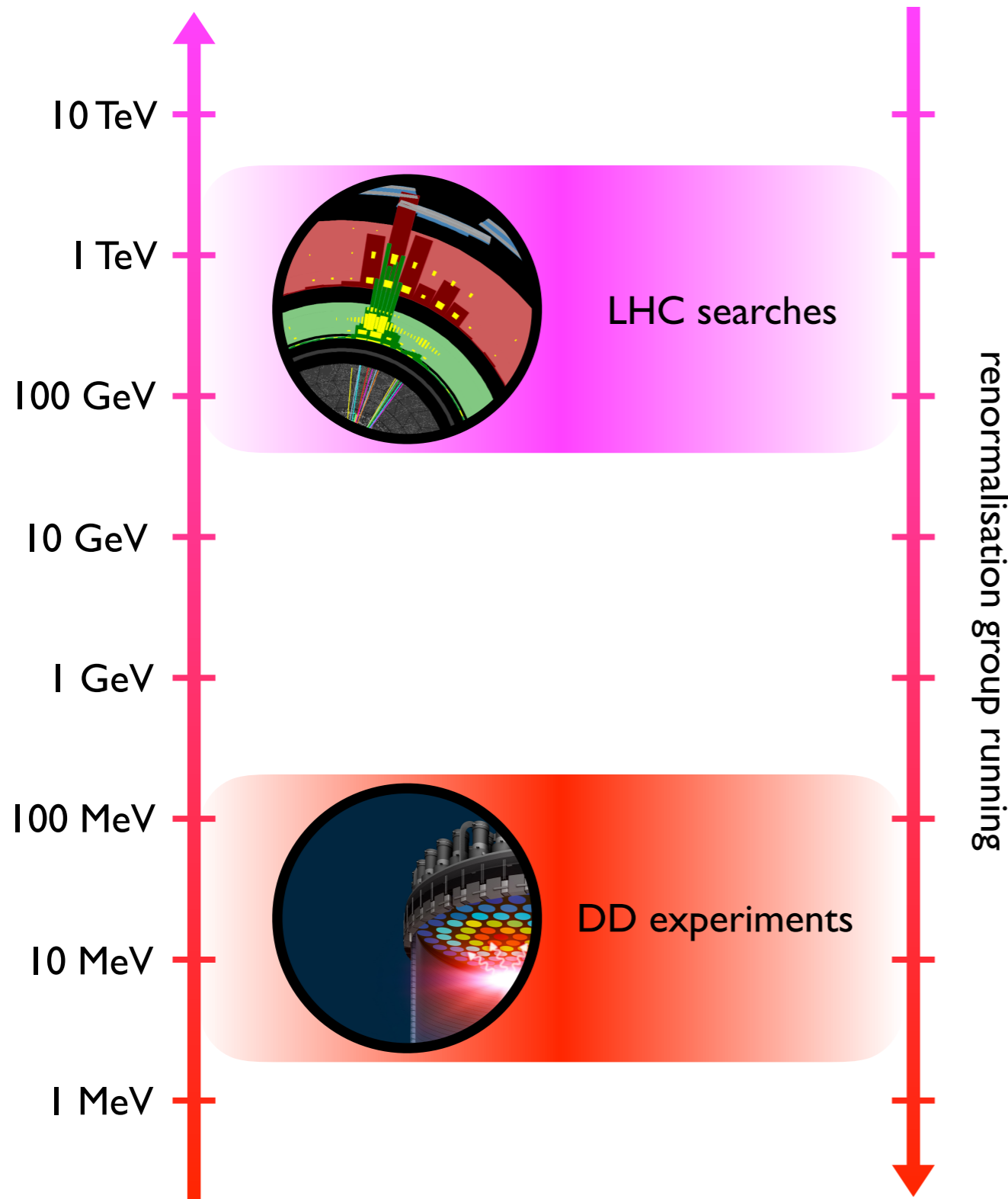
... & finally to a plot

[CMS PAS EXO-16-037]



For SI interactions LHC only competitive for low DM mass, where direct detection is challenging due to small nuclear recoil

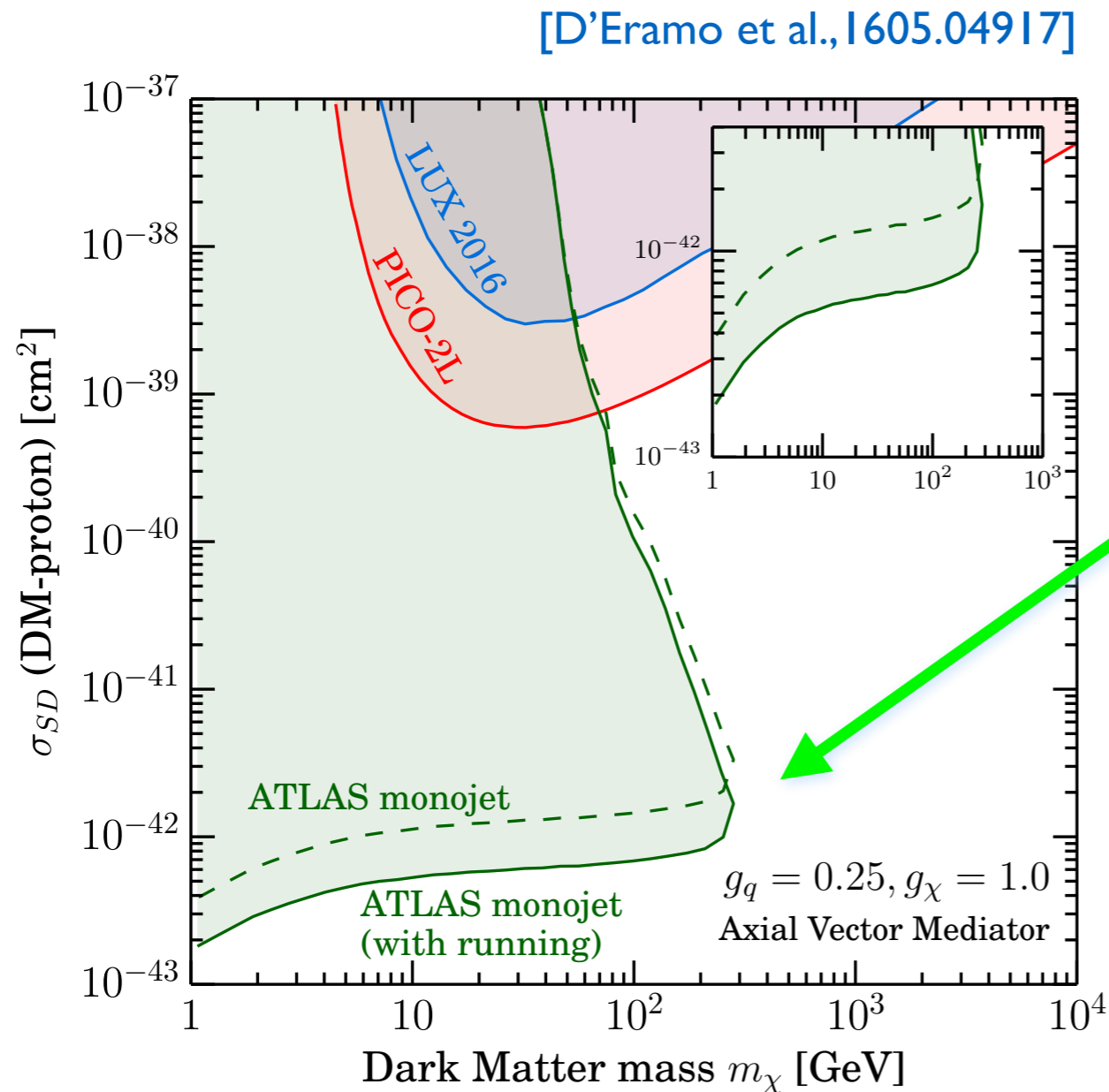
Classification of χ -N interactions



Distinction between SI & SD (or q-suppressed) χ -N couplings not stable under radiative corrections. Effects particular important for mixing of suppressed into unsuppressed operators

[Kopp et al., 0907.3159; Freytsis & Ligeti, 1012.5317; Hill & Solon, 1111.0016; UH & Kahlhoefer 1302.4454; Crivellin et al. 1402.1173, 1408.5046; D'Eramo et al. 1409.2893; ...]

Spin-1 simplified models: SD effects



in axialvector case bounds are strengthened by a factor of around 2 by renormalisation group running

While LHC limit quite similar to SI case, direct detection weakened significantly since DM-nucleon scattering is incoherent in SD case

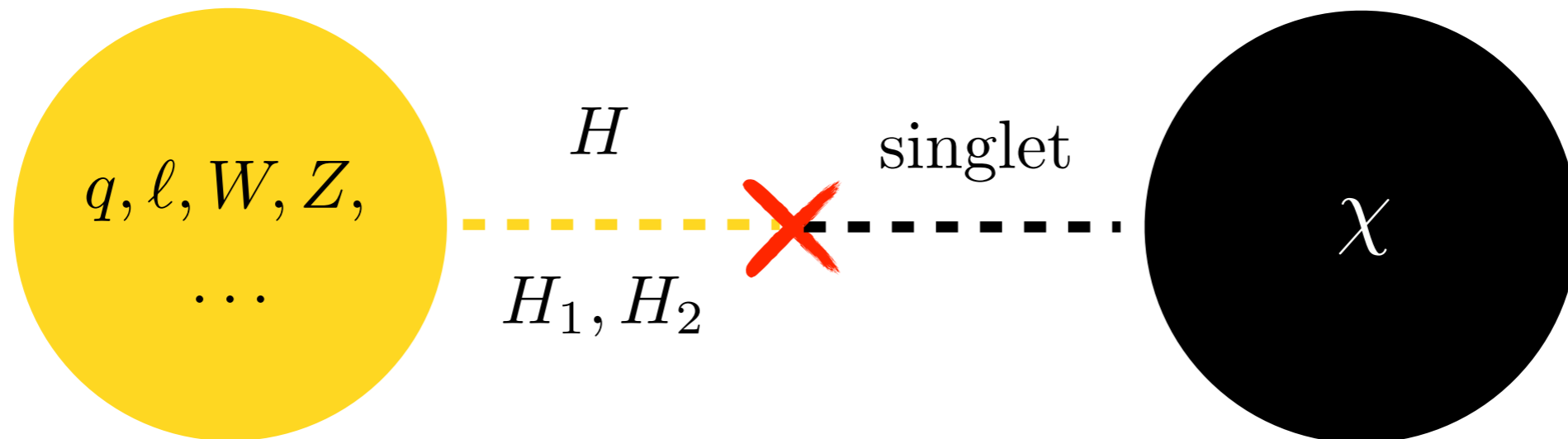
Are simplified models perfect?

Simplified models are minimal extensions of EFT that besides DM typically contain a single mediator. SM- & DM-mediator couplings are treated as free parameters & mechanism that provides mass to mediator & DM is unspecified

In ultraviolet (UV) complete model such as SM, couplings are usually not random but fixed by for example gauge invariance & anomalies. Higgs mechanism also an important ingredient in SM

To UV complete simplified models have to add more structure to them & question is whether this will change phenomenology

Consistent spin-0 simplified models



Spin-0 models with fermionic DM can be made $SU(2)_L \times U(1)_Y$ invariant by introducing a new dark Higgs that couples to visible scalar sector. If scalar sector minimal, SM Higgs is mediator & Higgs constraints are severe. But Higgs constraints avoided in decoupling or alignment limit of two-Higgs-doublet model (THDM) extensions

[Kim et al., 0803.2932; Baek et al., 1112.1847; Lopez-Honorez et al., 1203.2064; Fairbairn & Hogan, 1305.3452; Carpenter, 1312.2592; Berlin et al., 1402.7074, 1502.06000; ... ; Ko & Li, 1610.03997; Bell et al., 1612.04593; ...]

THDM plus pseudoscalar model

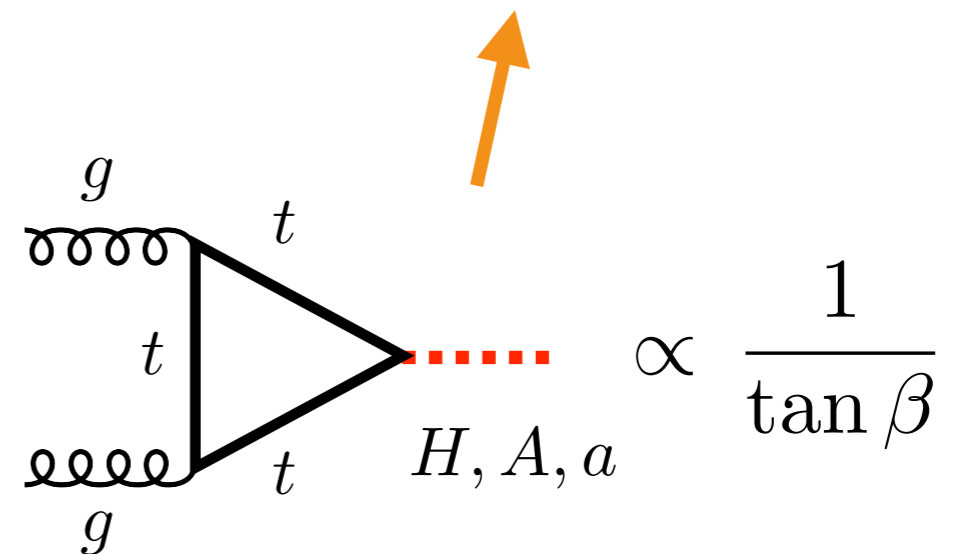
$$\mathcal{L} \supset \underbrace{-\bar{Q}Y_u\tilde{H}_2d_R + \bar{Q}Y_dH_1u_R}_{\text{yellow}} - \underbrace{ib_P P H_1^\dagger H_2}_{\text{red}} - \underbrace{iy_\chi P \bar{\chi} \gamma_5 \chi}_{\text{black}} + \text{h.c.}$$

States: h, H, A, H^\pm, a

Angles: α, β, θ

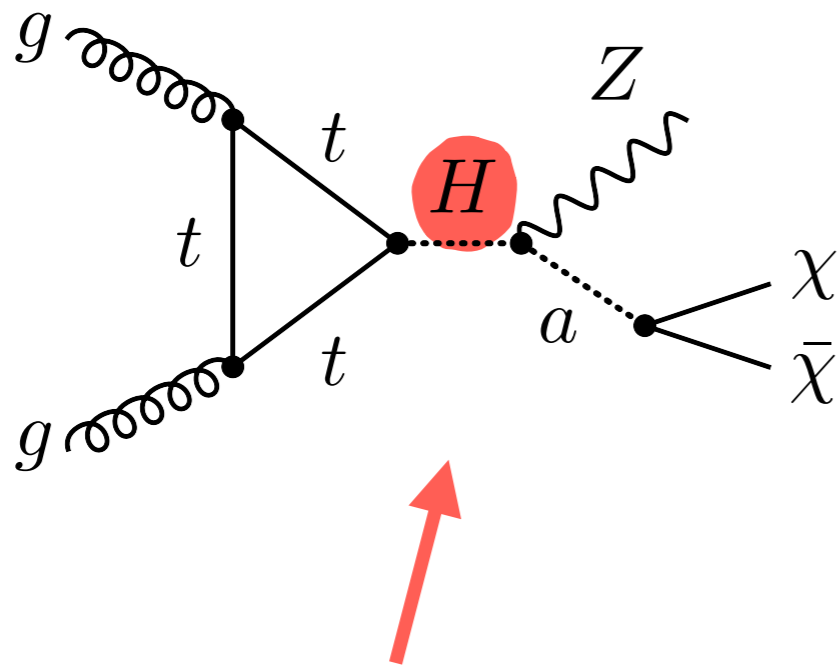
h is SM-like for
 $\cos(\beta-\alpha) \approx 0$

mostly P for
small θ

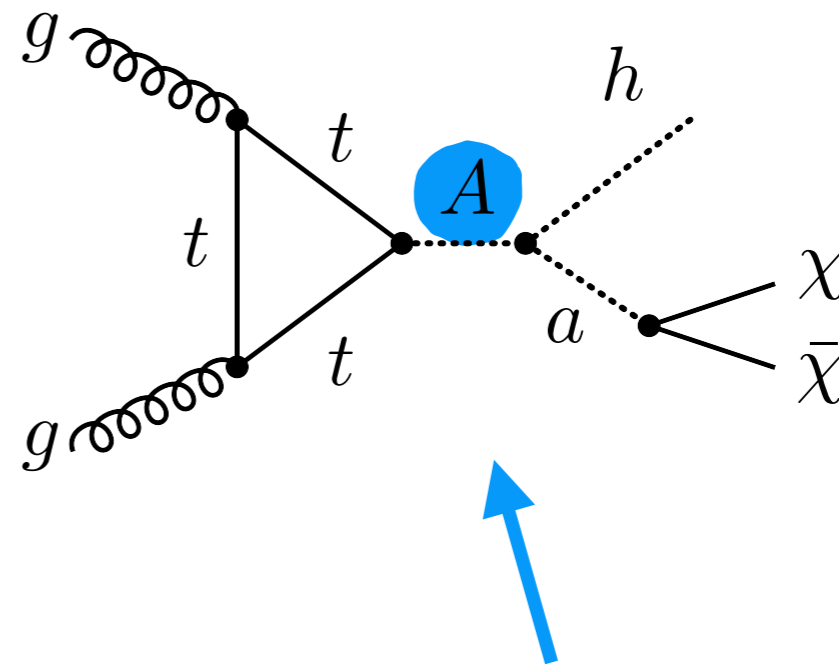


Resonant mono- X signatures

Mono- Z & mono-Higgs signals are subleading in minimal spin-0 simplified models. In THDM plus pseudoscalar (THDMP) model, presence of H & A allows for resonant mono- Z & mono-Higgs production:

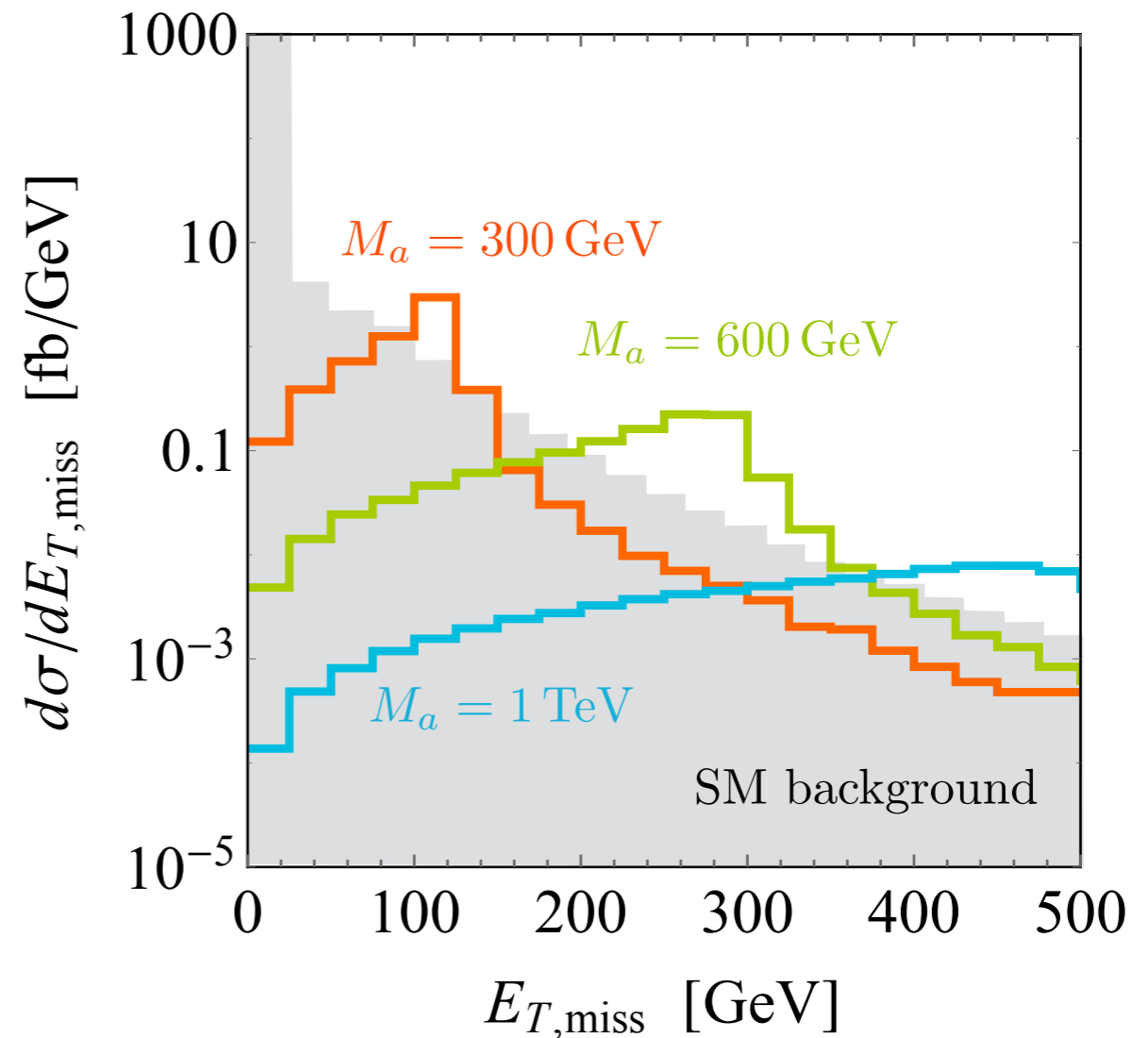
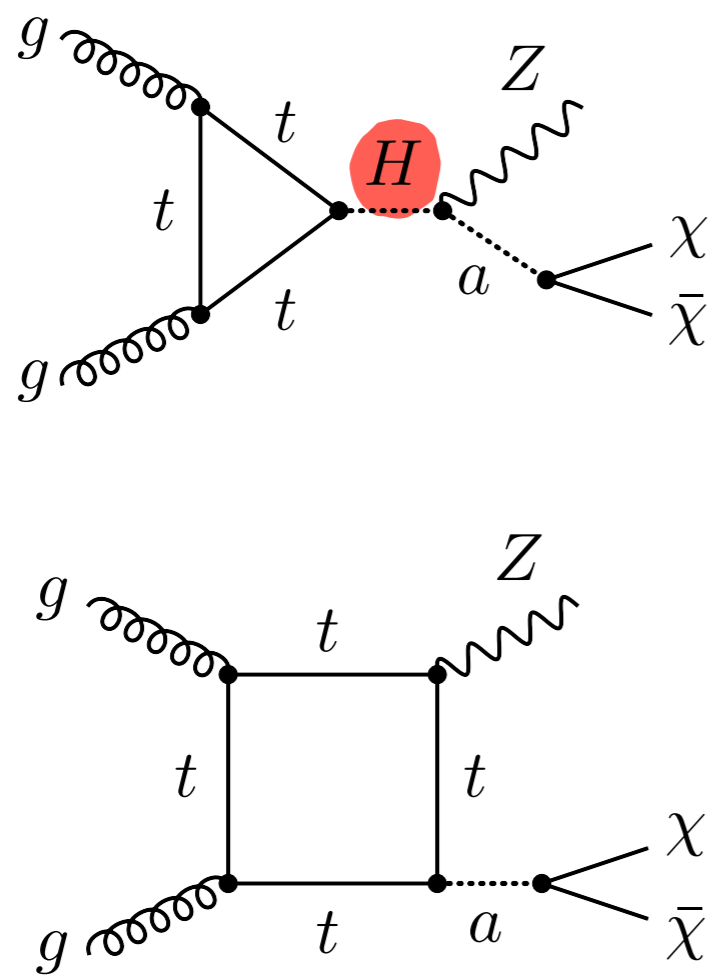


dominant for $M_H, M_a < M_A \approx M_{H^\pm}$



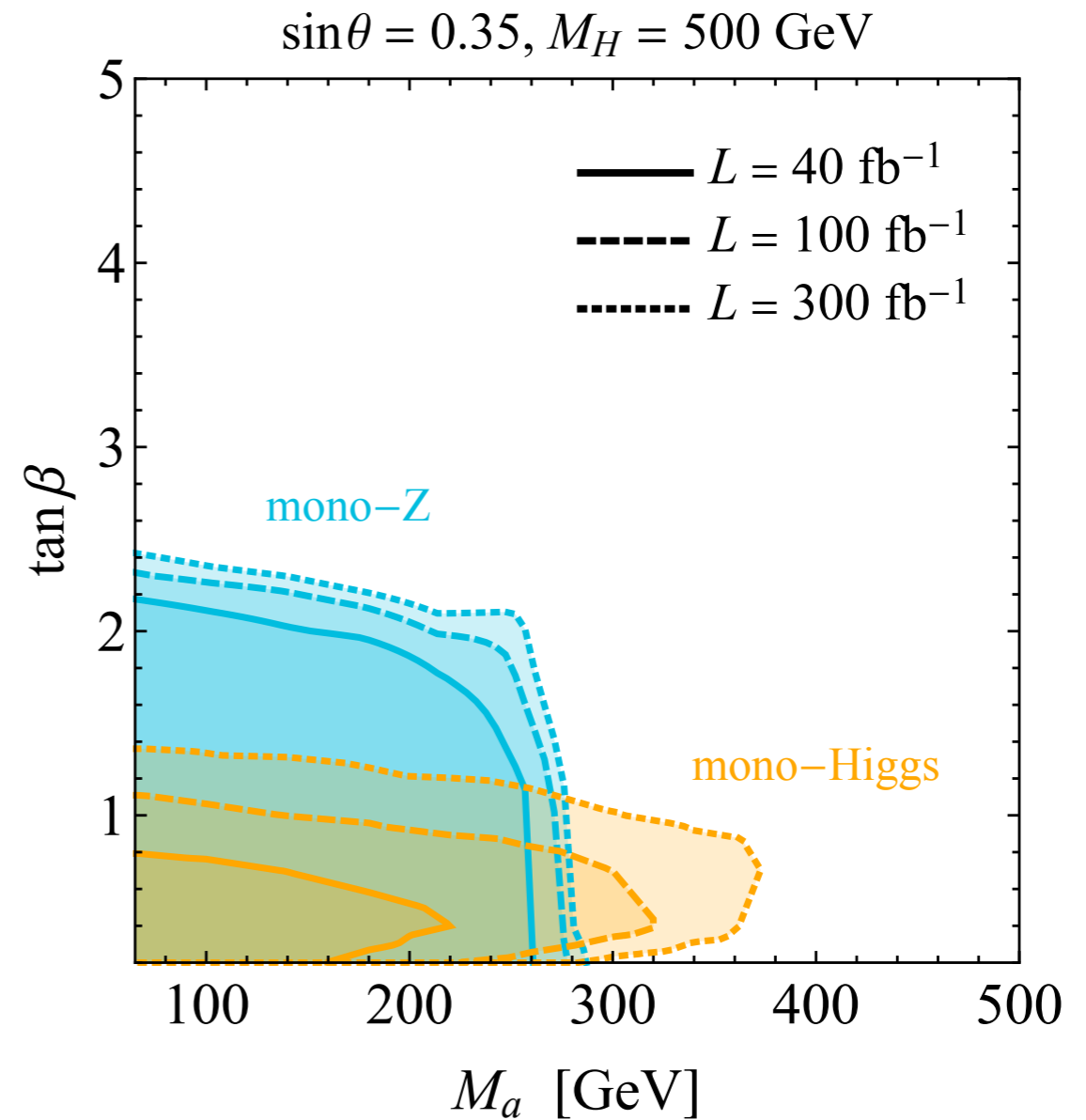
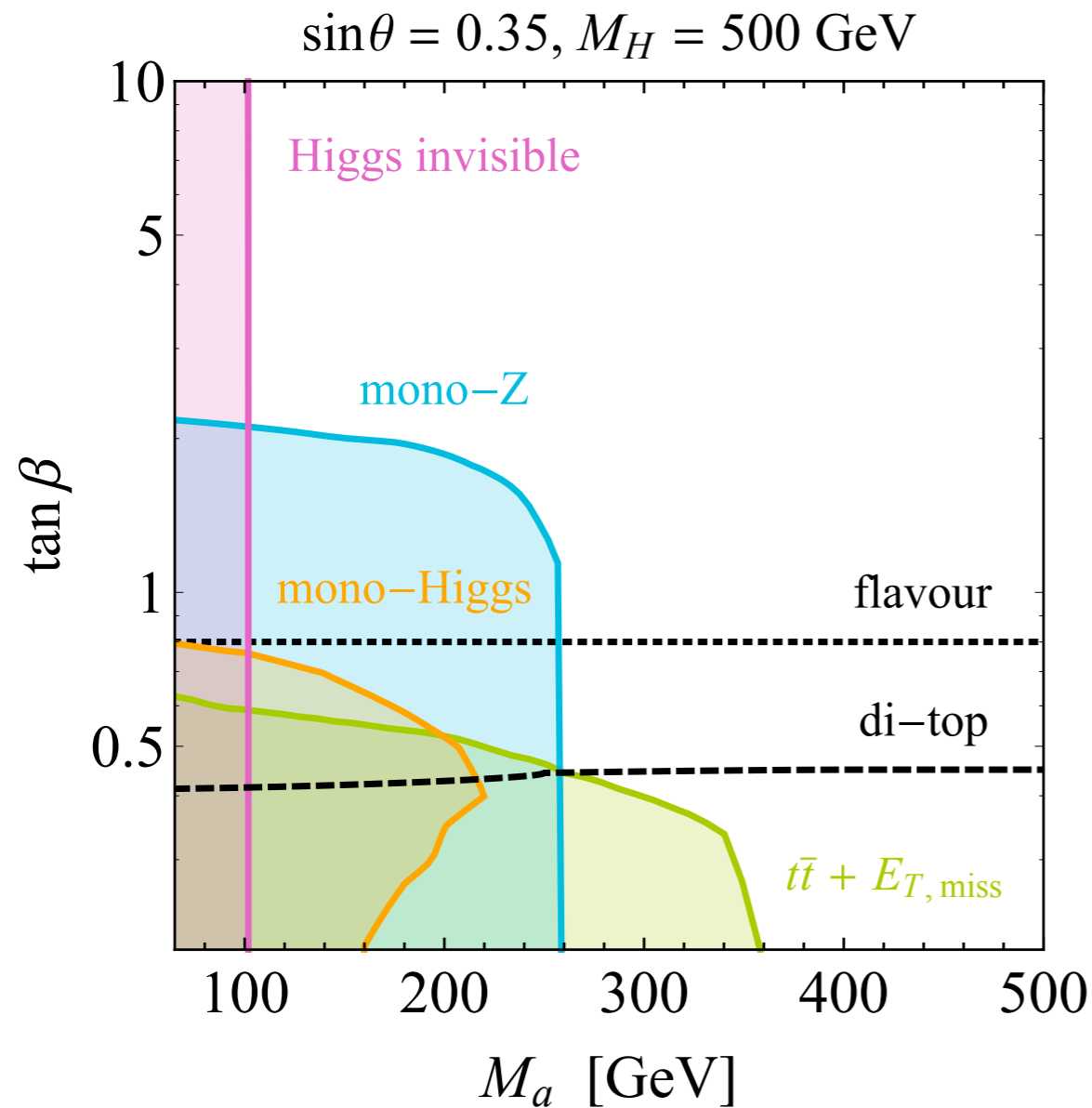
dominant for $M_A, M_a < M_H \approx M_{H^\pm}$

Resonant mono- X signatures



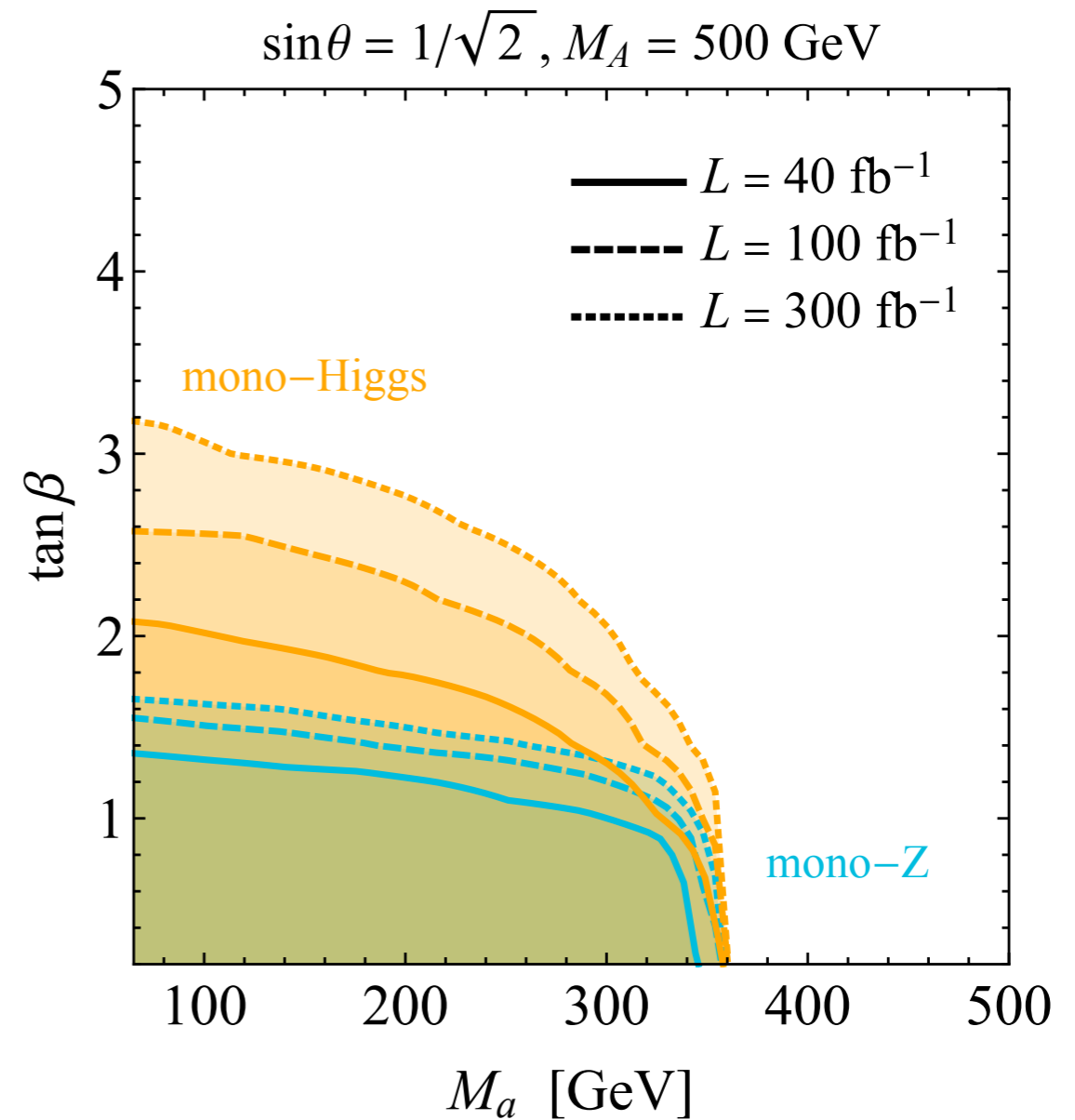
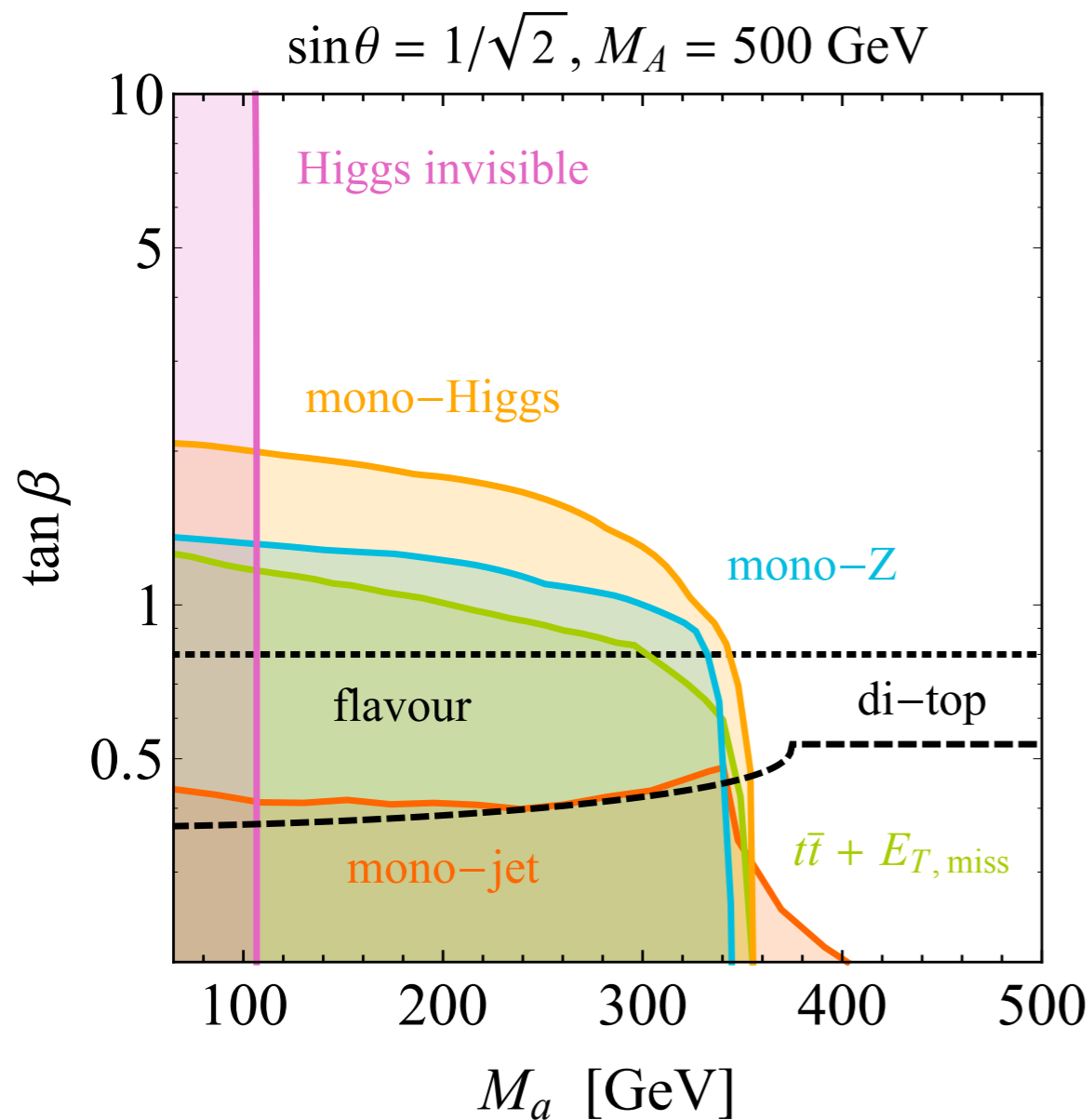
$E_{T,\text{miss}}$ distribution of mono- Z signal has Jacobean peak. Same feature appears in to mono-Higgs signature in THDMP model

THDMP benchmark: $M_H, M_a < M_A$



Depending on Higgs-mass spectrum either $E_{T,\text{miss}} + Z$ or $E_{T,\text{miss}} + h$ provides leading constraint in large parts of parameter space

THDMP benchmark: $M_A, M_a < M_H$



Depending on Higgs-mass spectrum either $E_{T,\text{miss}} + Z$ or $E_{T,\text{miss}} + h$ provides leading constraint in large parts of parameter space

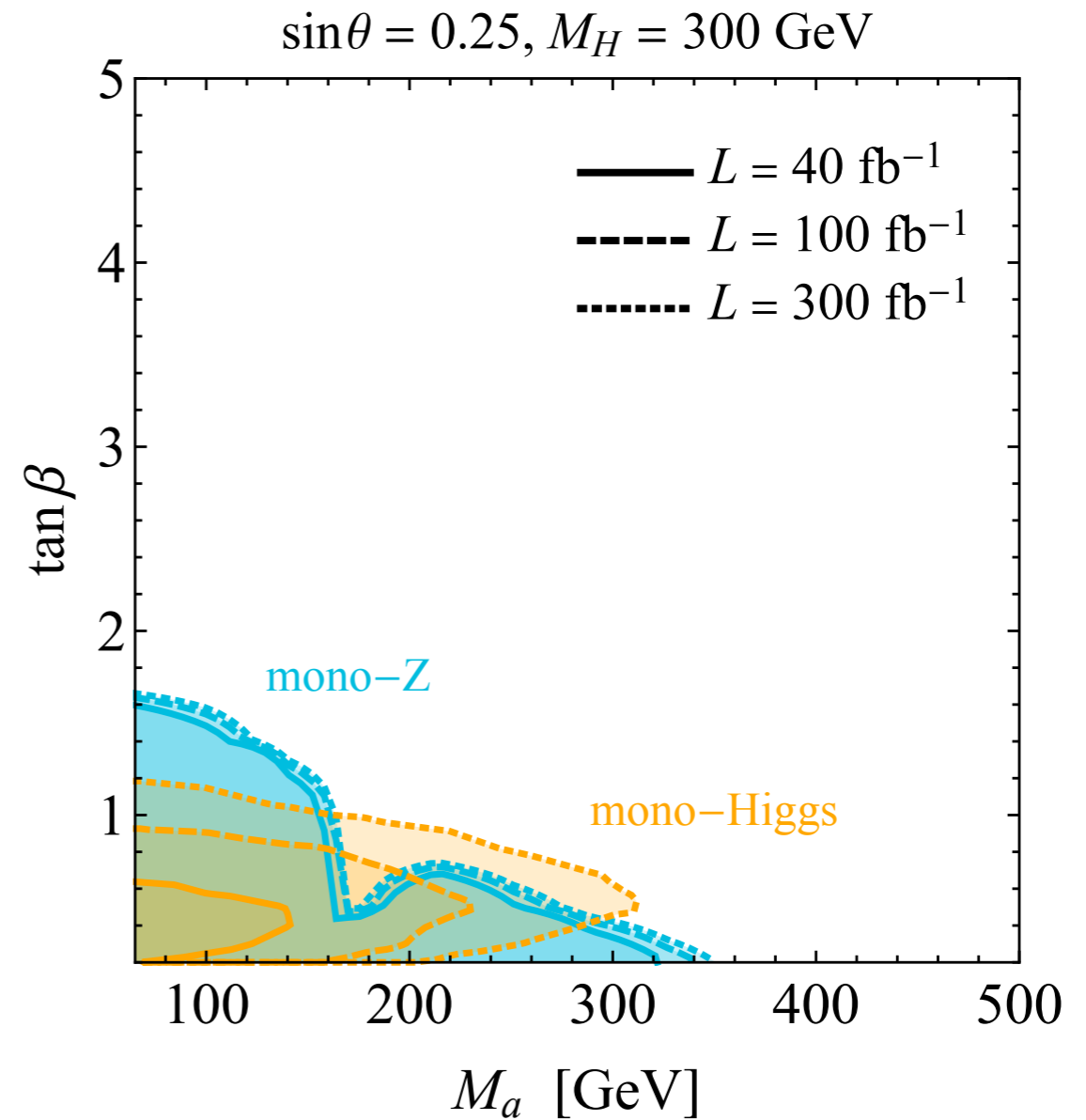
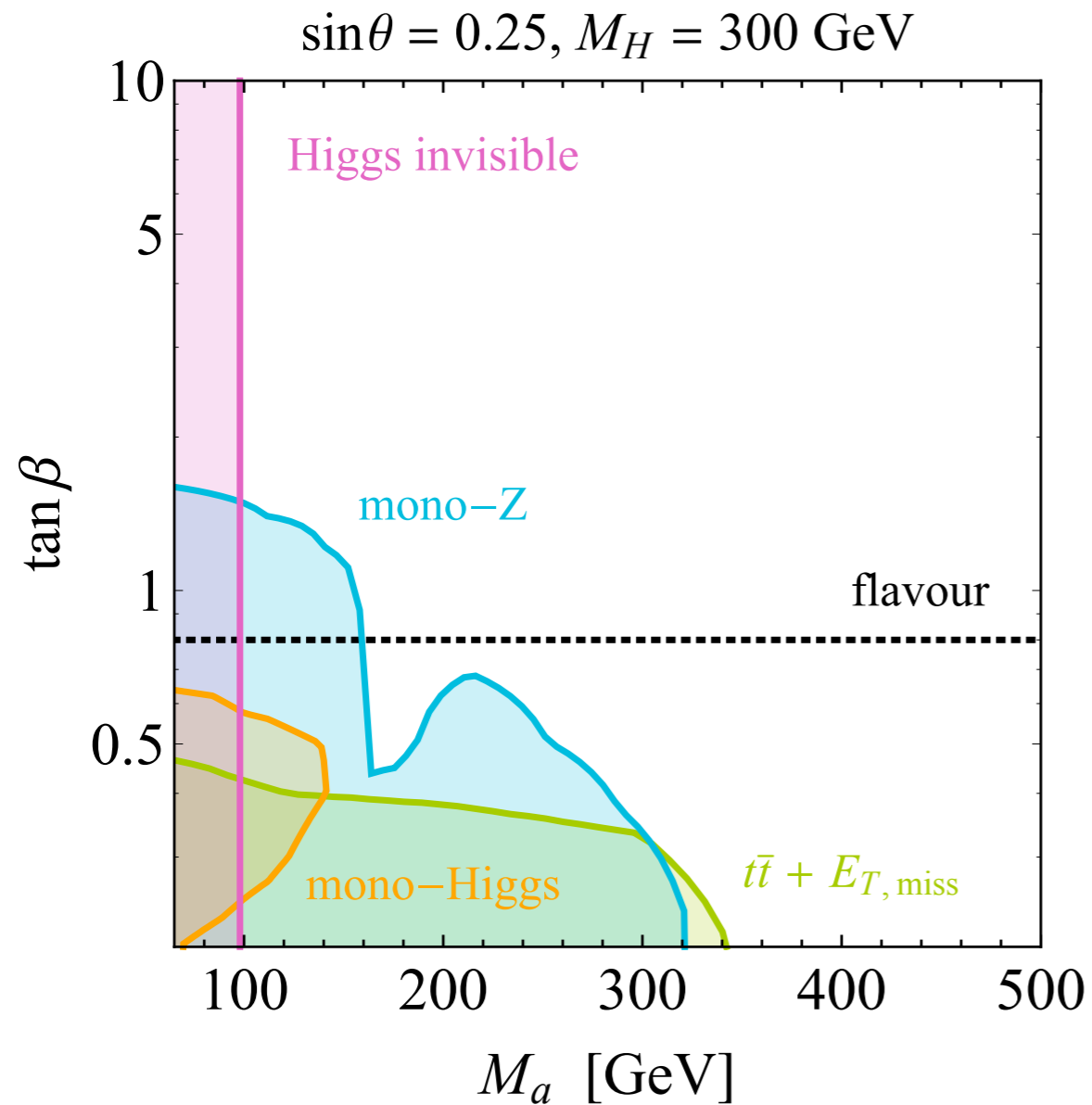
Conclusions

- Nice 13 TeV ATLAS & CMS results for a broad range of searches for DM in $E_{T,miss}+X$ with $X = j, \gamma, W, Z, h, t, t\bar{t}, b\bar{b}, \dots$ & more to come in next few years
- Interpretations of LHC searches in context of simplified models & sometimes EFTs provide information complementary to other DM searches such as (in)direct detection
- THDM plus mediator scenarios provide consistent framework that interpolates between spin-0 simplified models & well-motivated UV completions. $E_{T,miss}+Z$ or $E_{T,miss}+h$ signatures particularly interesting in such models due to possible resonance enhancement

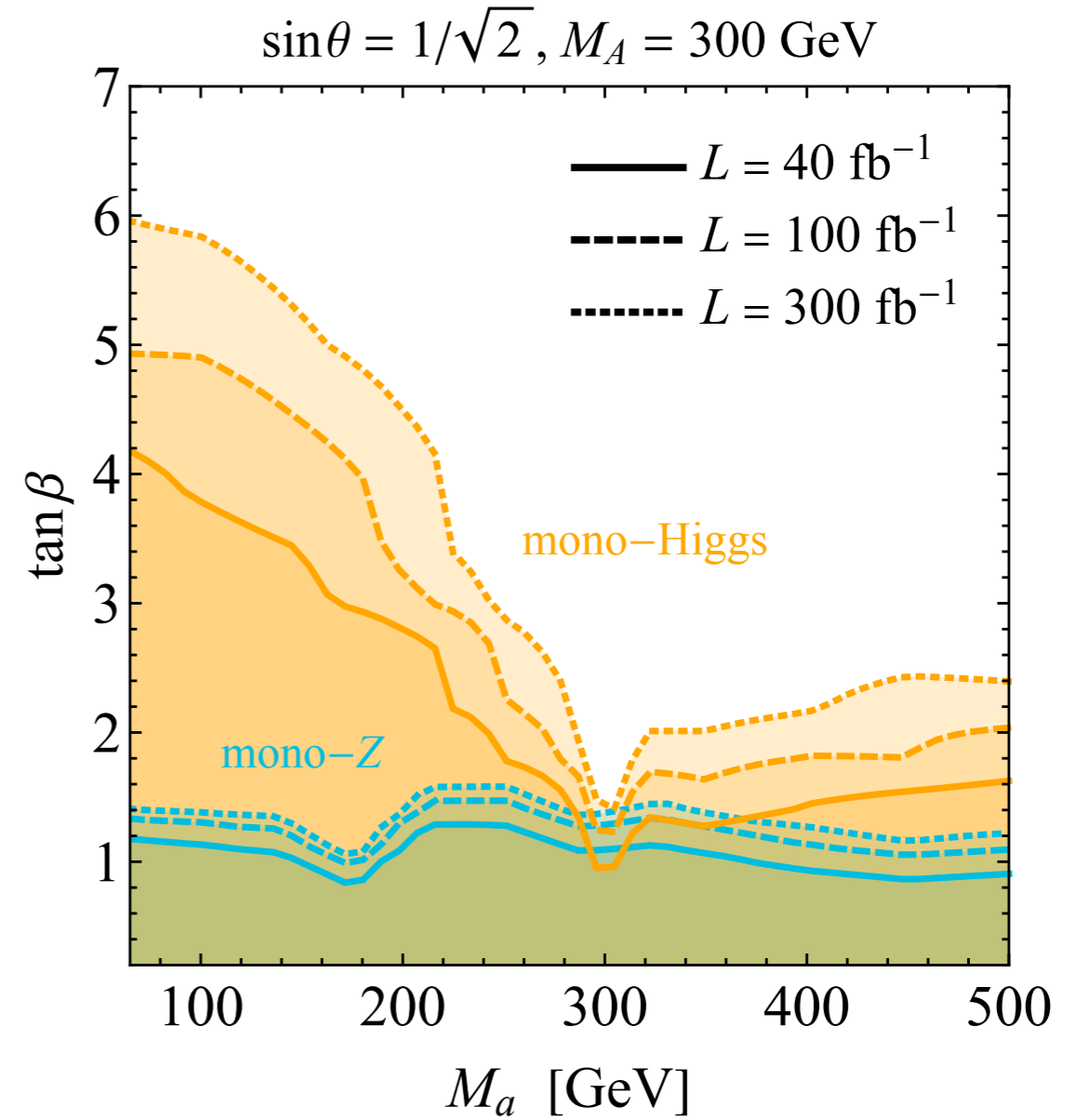
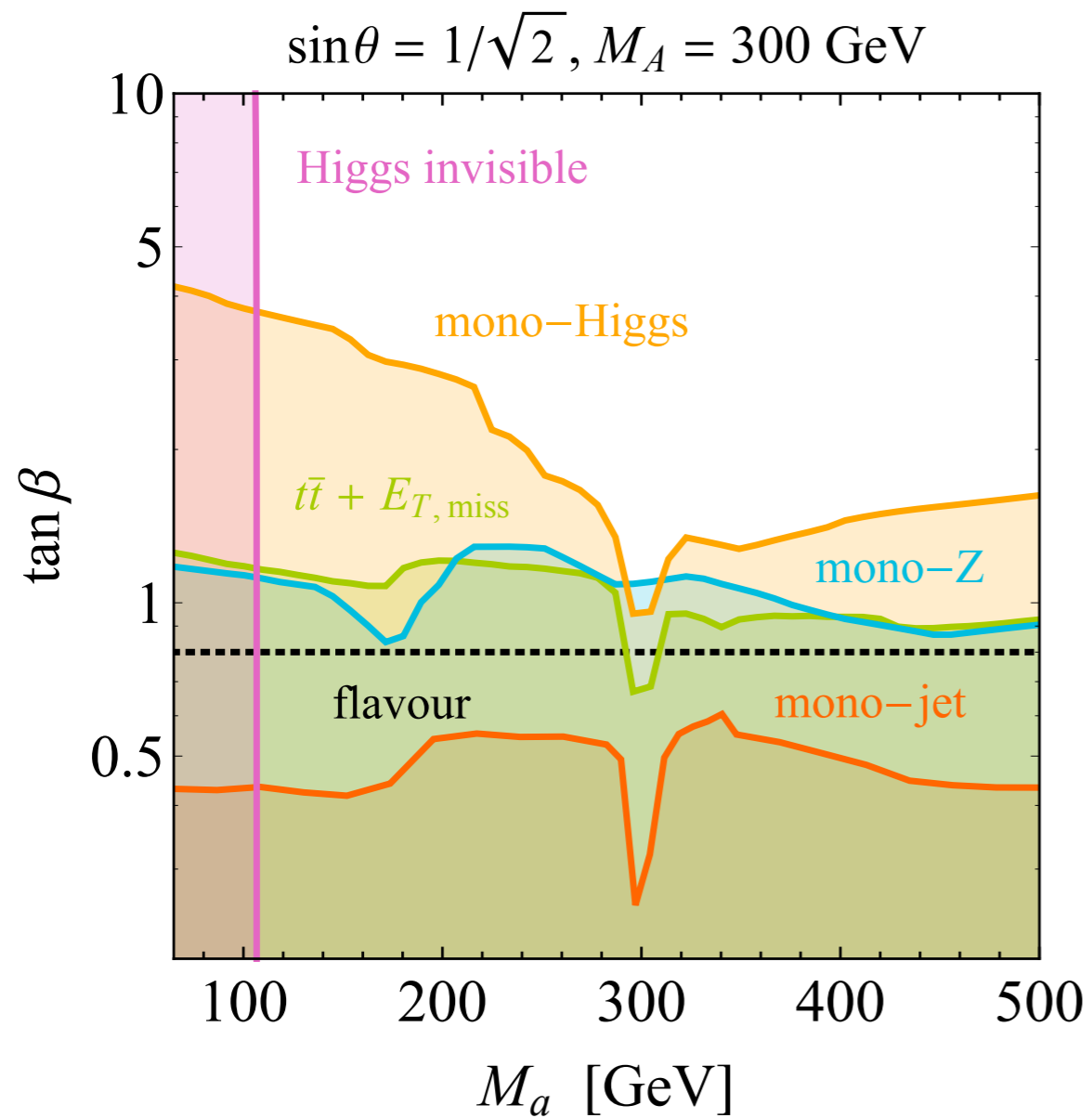
Backup



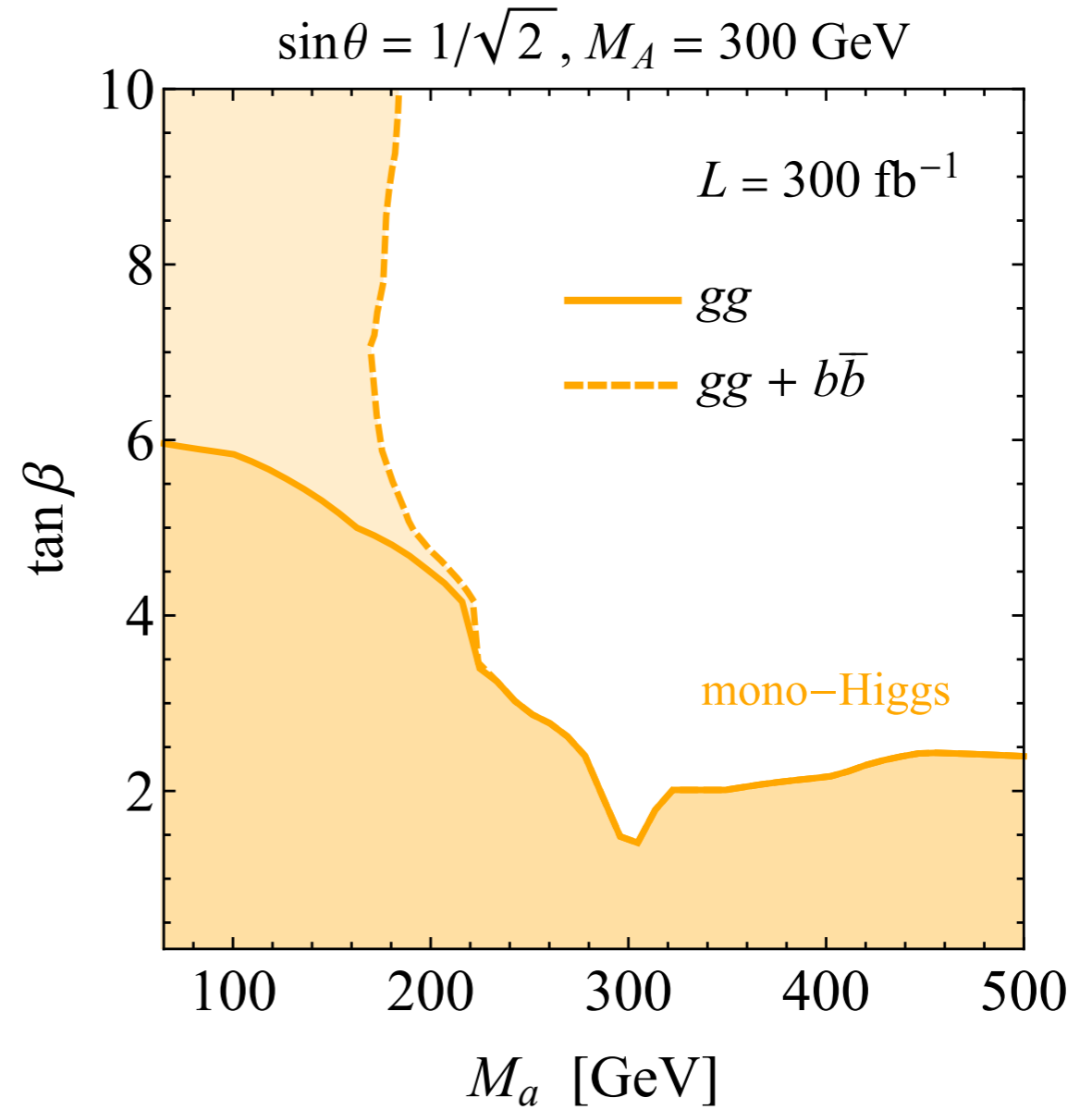
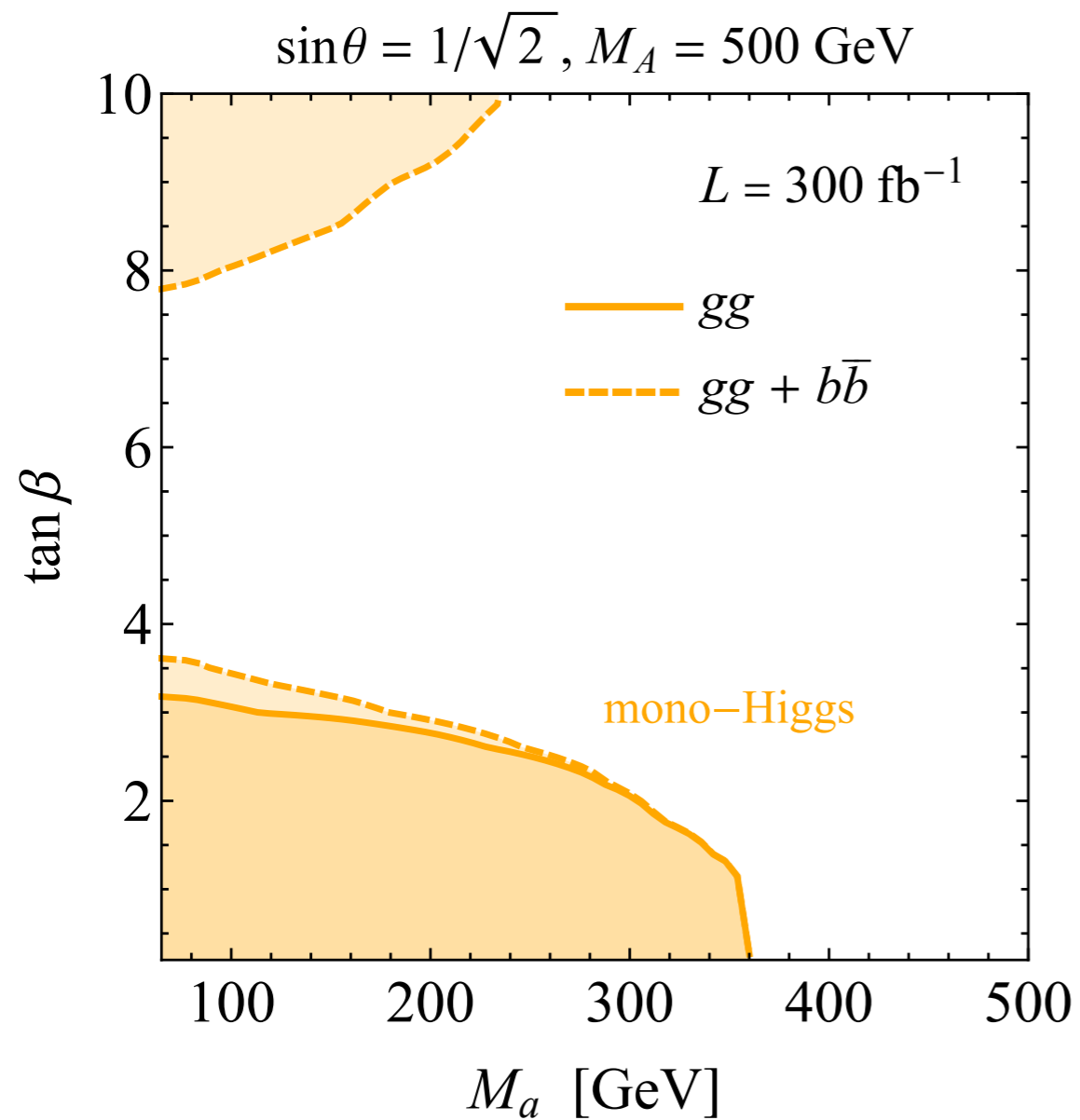
THDMP benchmark: $M_H, M_a < M_A$



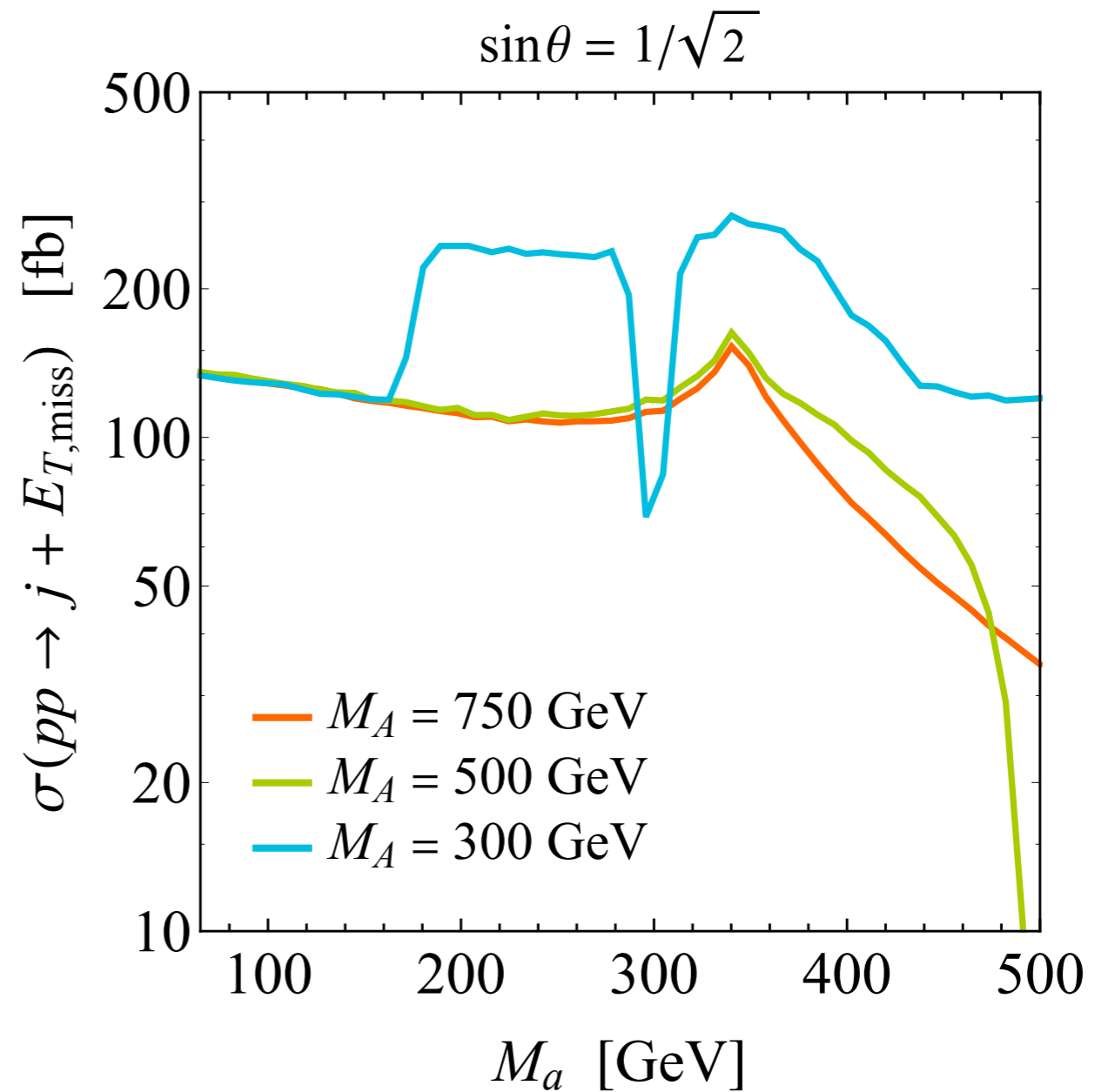
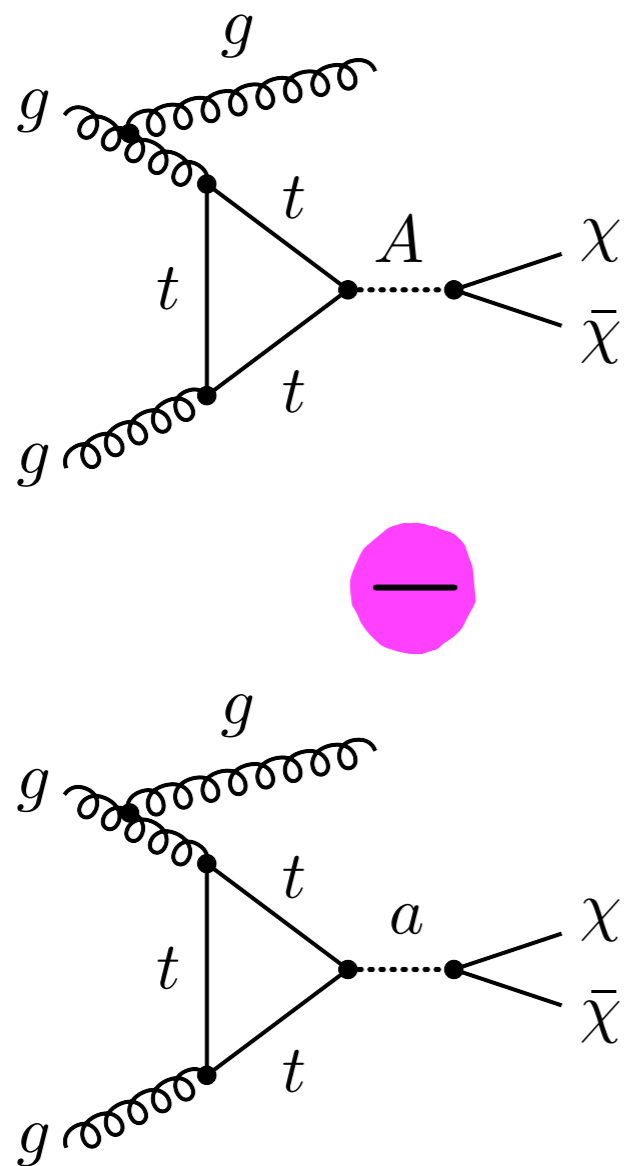
THDMP benchmark: $M_A, M_a < M_H$



THDMP: $b\bar{b}$ contributions to $h+E_{T,miss}$

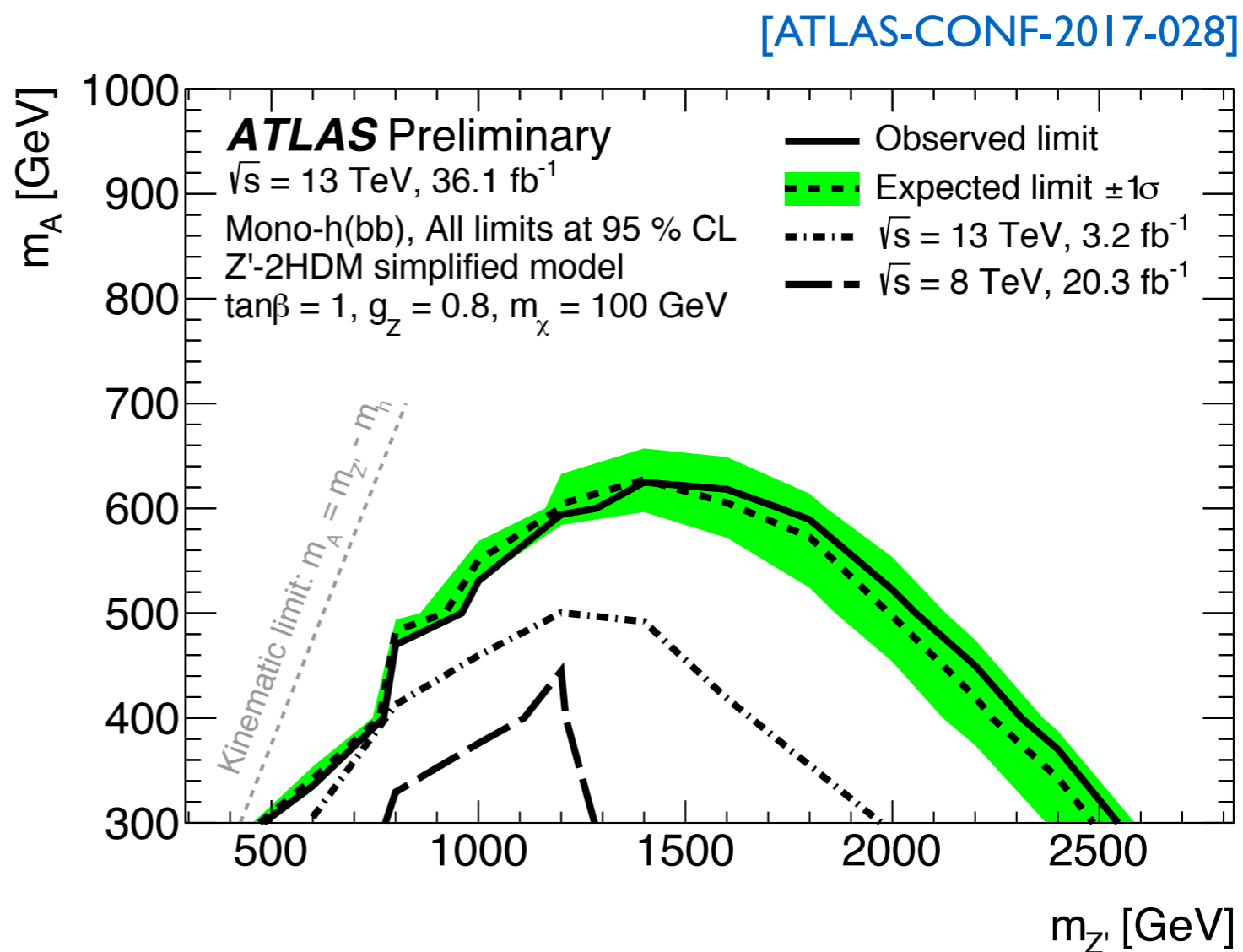
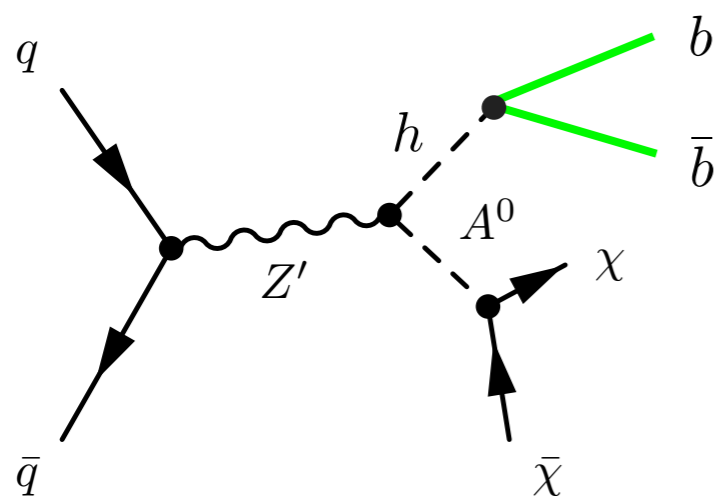


THDMP: interference effects



Contributions of A & a to mono-jet, $E_{T,\text{miss}} + t\bar{t}$, etc. interfere destructively

THDM plus Z' model: $h + E_{T, \text{miss}}$ searches



[see also talk by Piedra & poster session as well as ATLAS-CONF-2017-024 for di-photon channel]

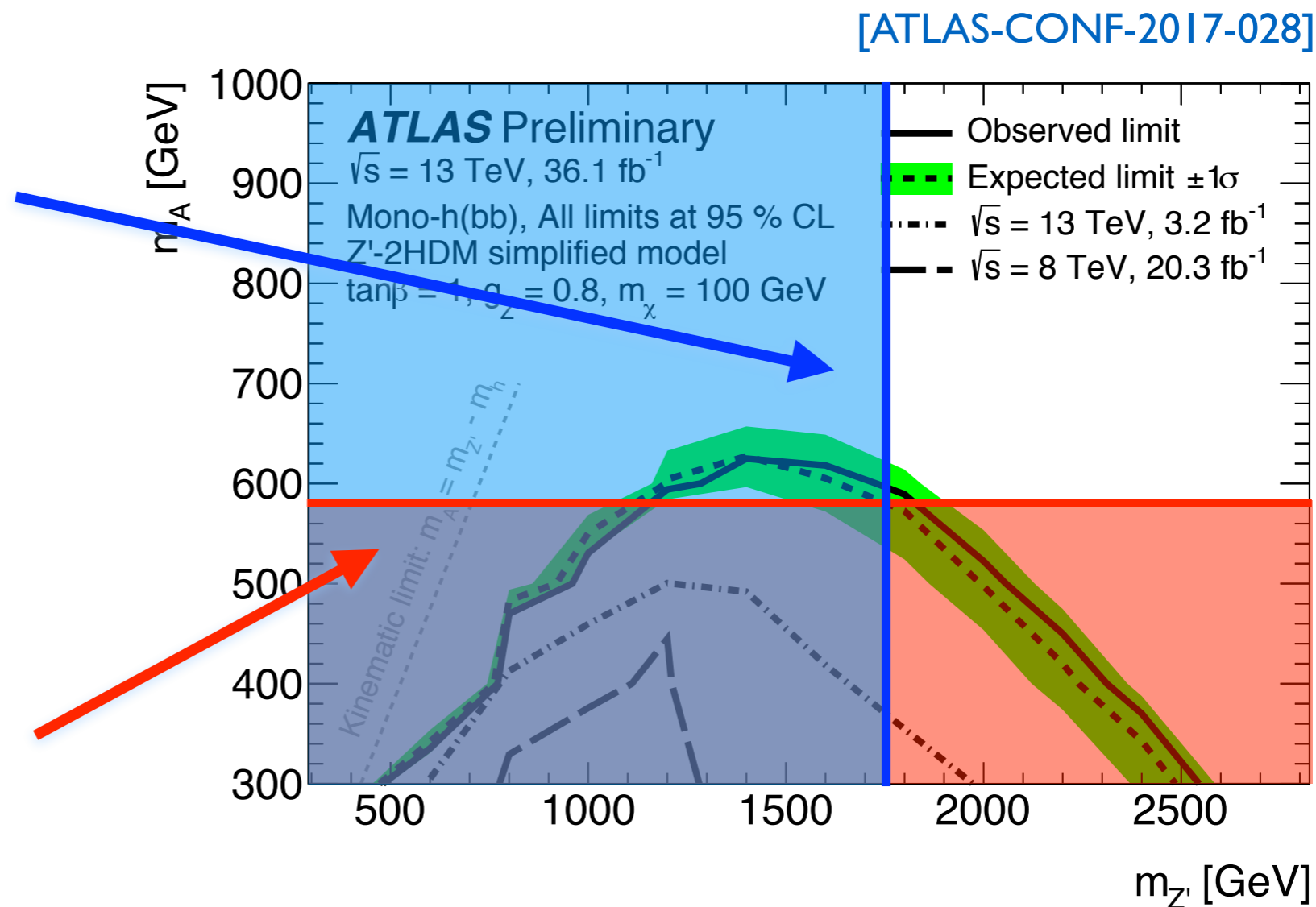
THDM plus Z' model: $h + E_{T, \text{miss}}$ searches

disfavoured at 95% CL
by ρ parameter

[Berlin et al., I402.7074]

disfavoured at 95% CL
by $B \rightarrow X_s \gamma$

[Misiak & Steinhauser, I702.04571]



[see also talk by Piedra & poster session as well as ATLAS-CONF-2017-024 for di-photon channel]

t-channel flavoured mediators

DM fermion singlet scalar flavour triplet

$$\mathcal{L}_{\text{fermion}, \tilde{u}} \supset \sum_{i=1,2,3} g \phi_i^* \bar{\chi} P_R u_i + \text{h.c.} \quad \phi_i = \{ \tilde{u}, \tilde{c}, \tilde{t} \}$$

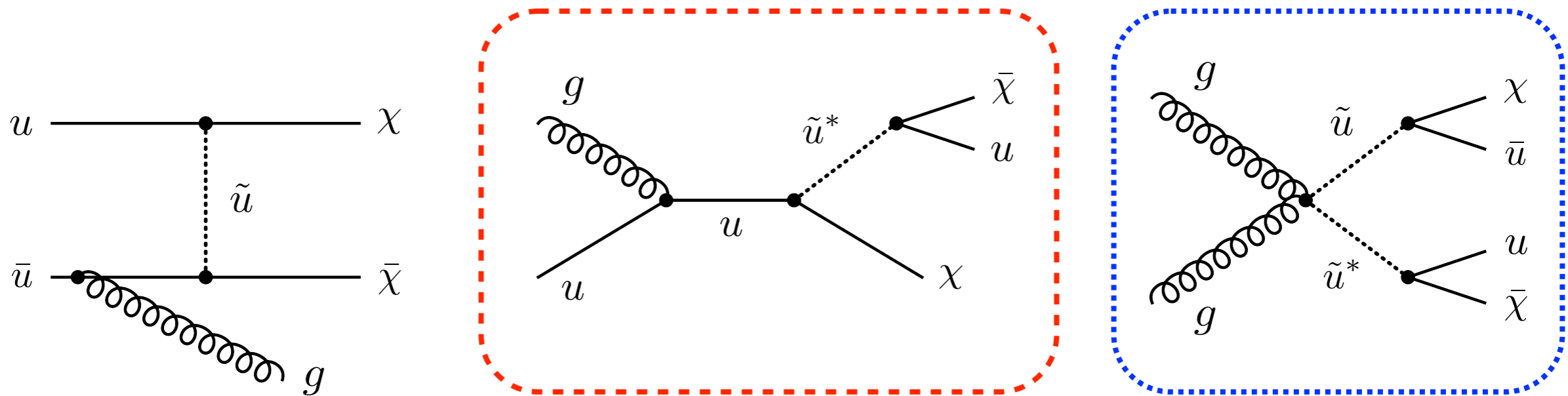
universal couplings to have minimal flavour violation (MFV),
which is needed to avoid flavour constraints

$$\{ m_\chi, M_{1,2}, M_3, g_{1,2}, g_3 \}$$

universality broken by $Y_u^\dagger Y_u$ flavour spurion (fine with MFV)

[Bell et al., I209.0231; Chang et al., I307.8120; An et al., I308.0592; Bai & Berger I308.0612; DiFranzo et al., I308.2679; Papucci et al., I402.2285; ...]

t-channel flavoured mediators

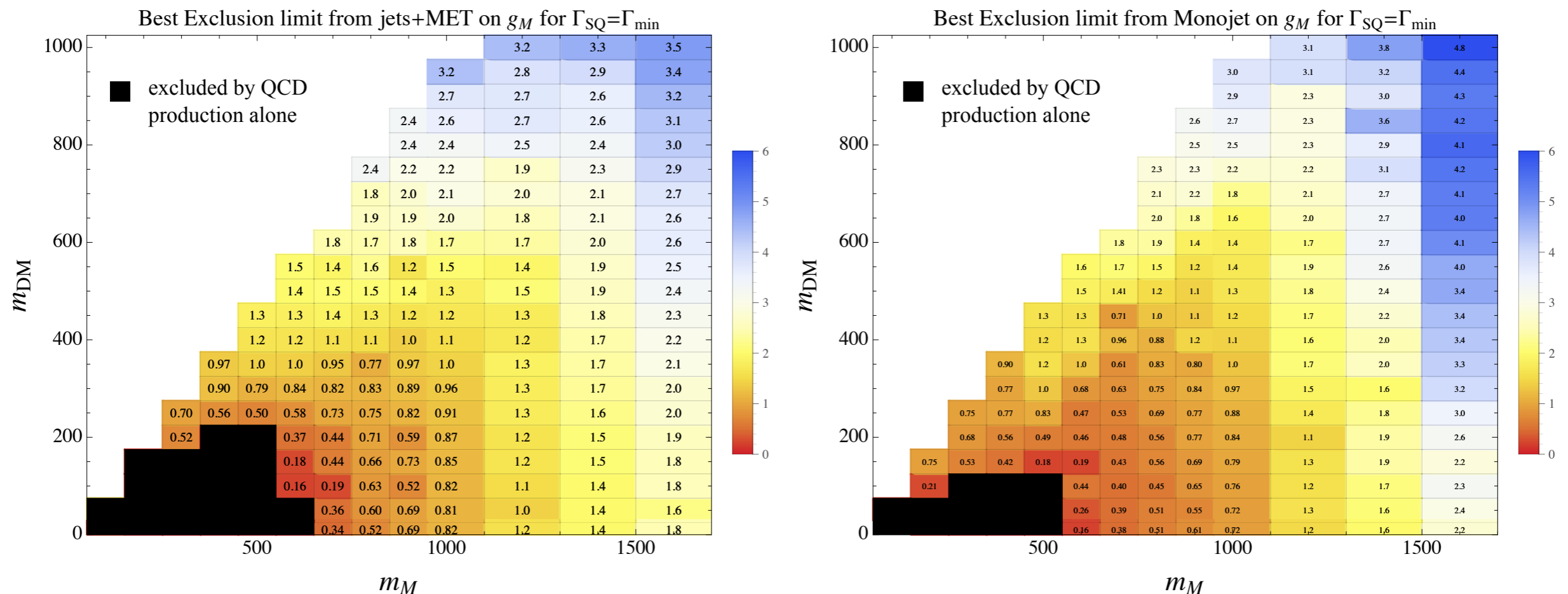


gives largest contribution to $E_{T, \text{miss}} + j$ signal, because compared to initial state radiation (ISR) diagram phase-space enhanced, profits from gluon luminosity & jet typically harder than in ISR; dominance of associated production channel is a distinct feature of t-channel models

$E_{T, \text{miss}} + 2j$ channel can dominate over $E_{T, \text{miss}} + j$ signal if $g_l \gg g_s$

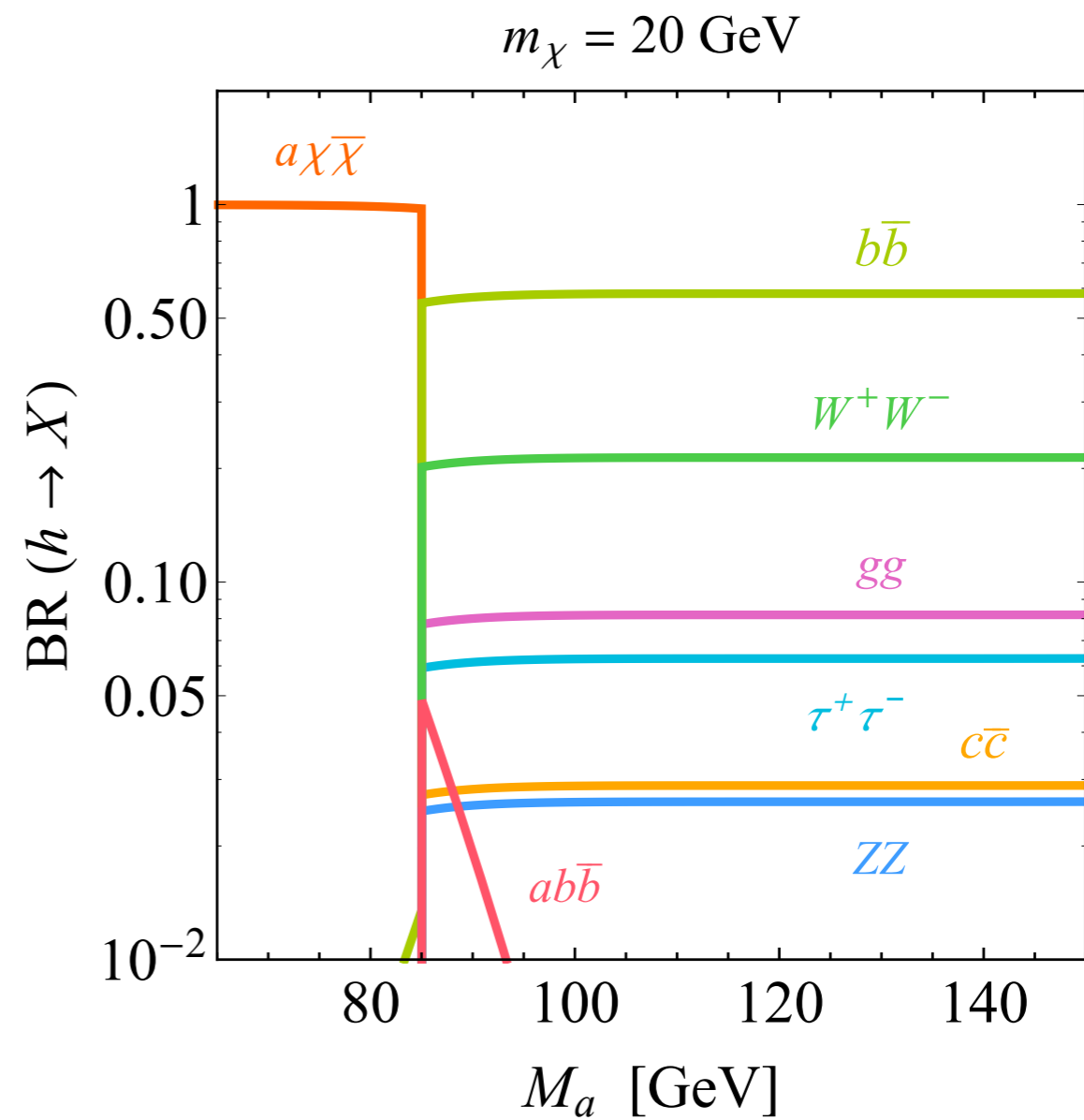
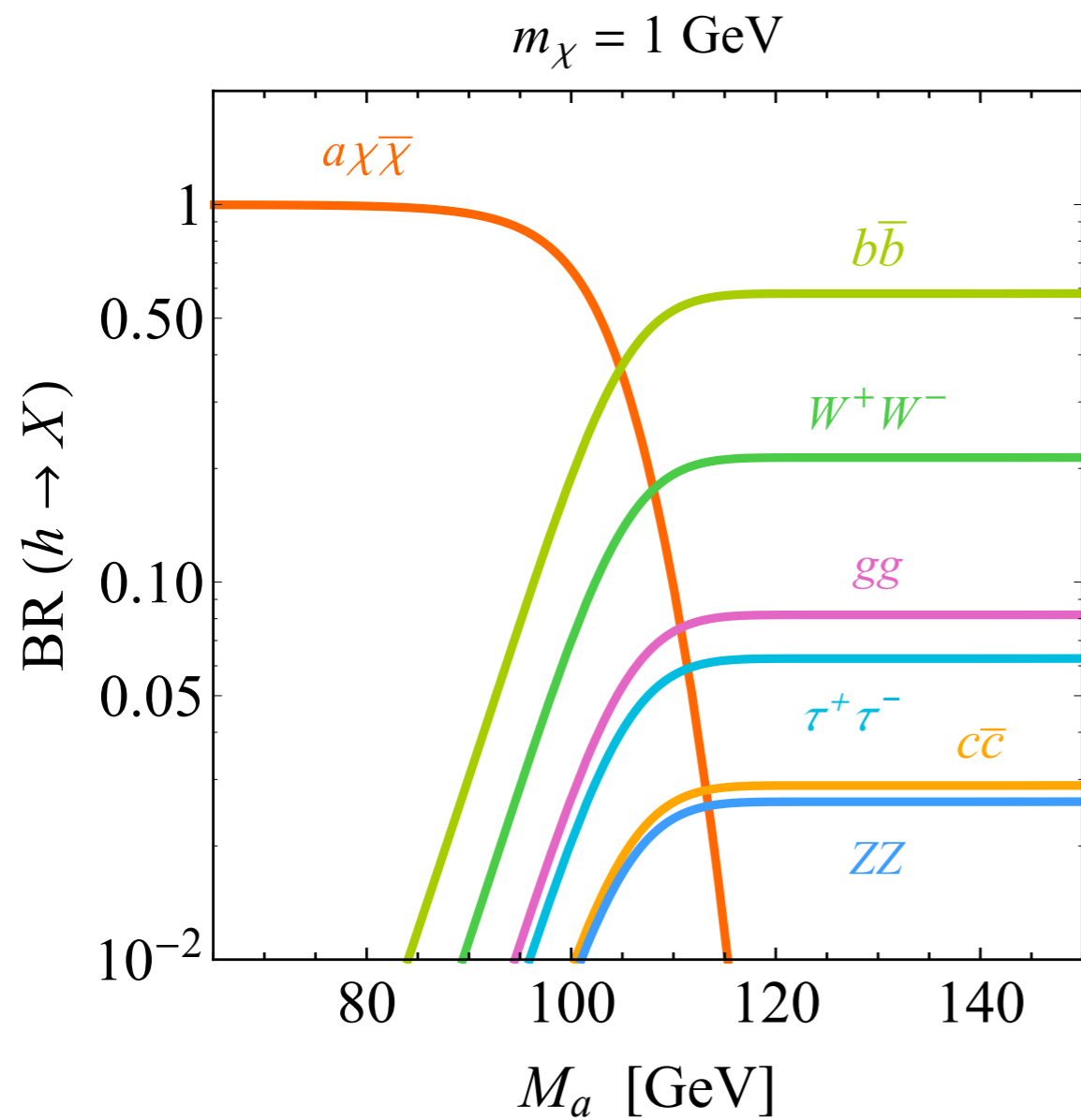
t-channel flavoured mediators

[Papucci et al., 1402.2285]

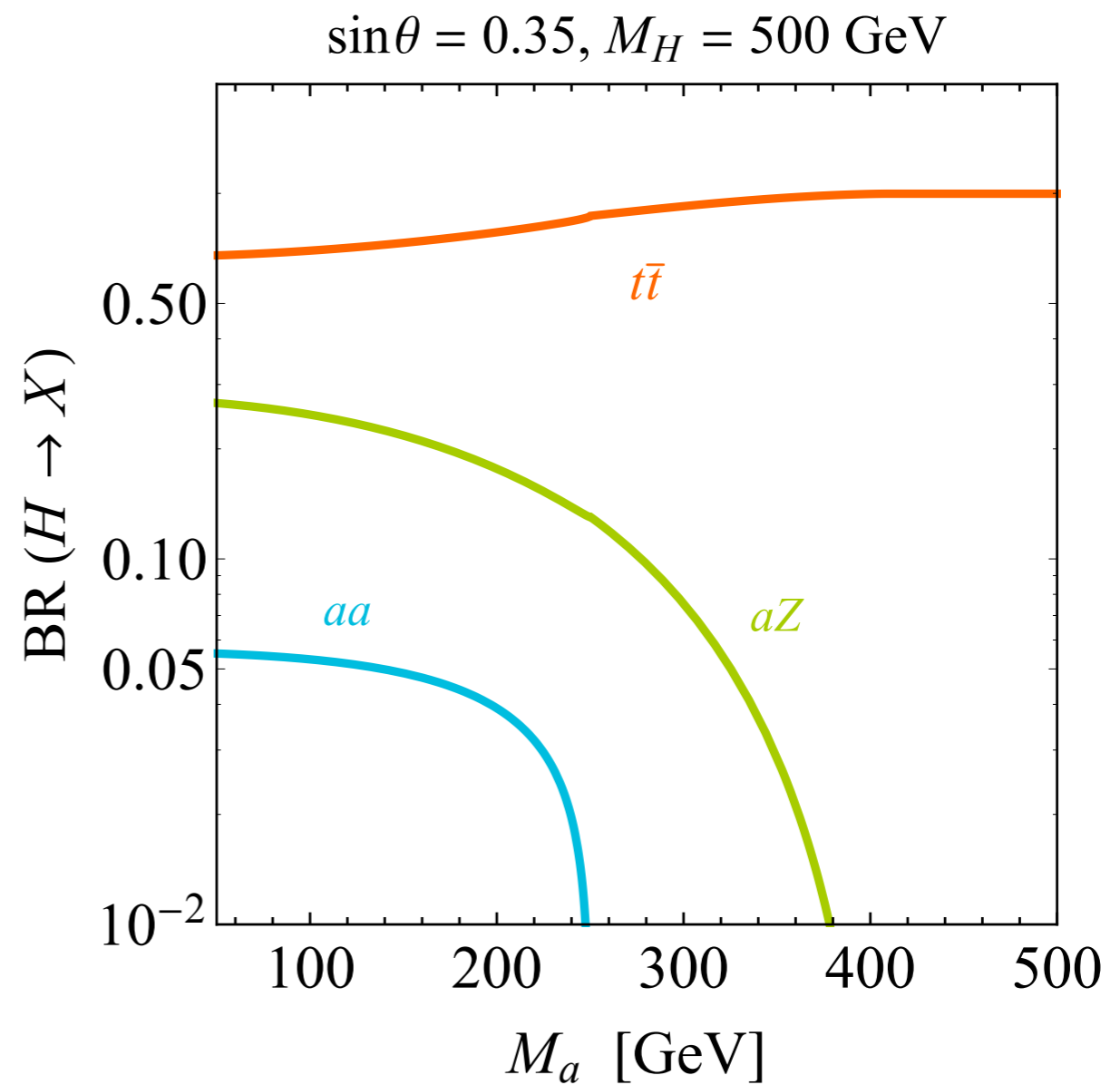
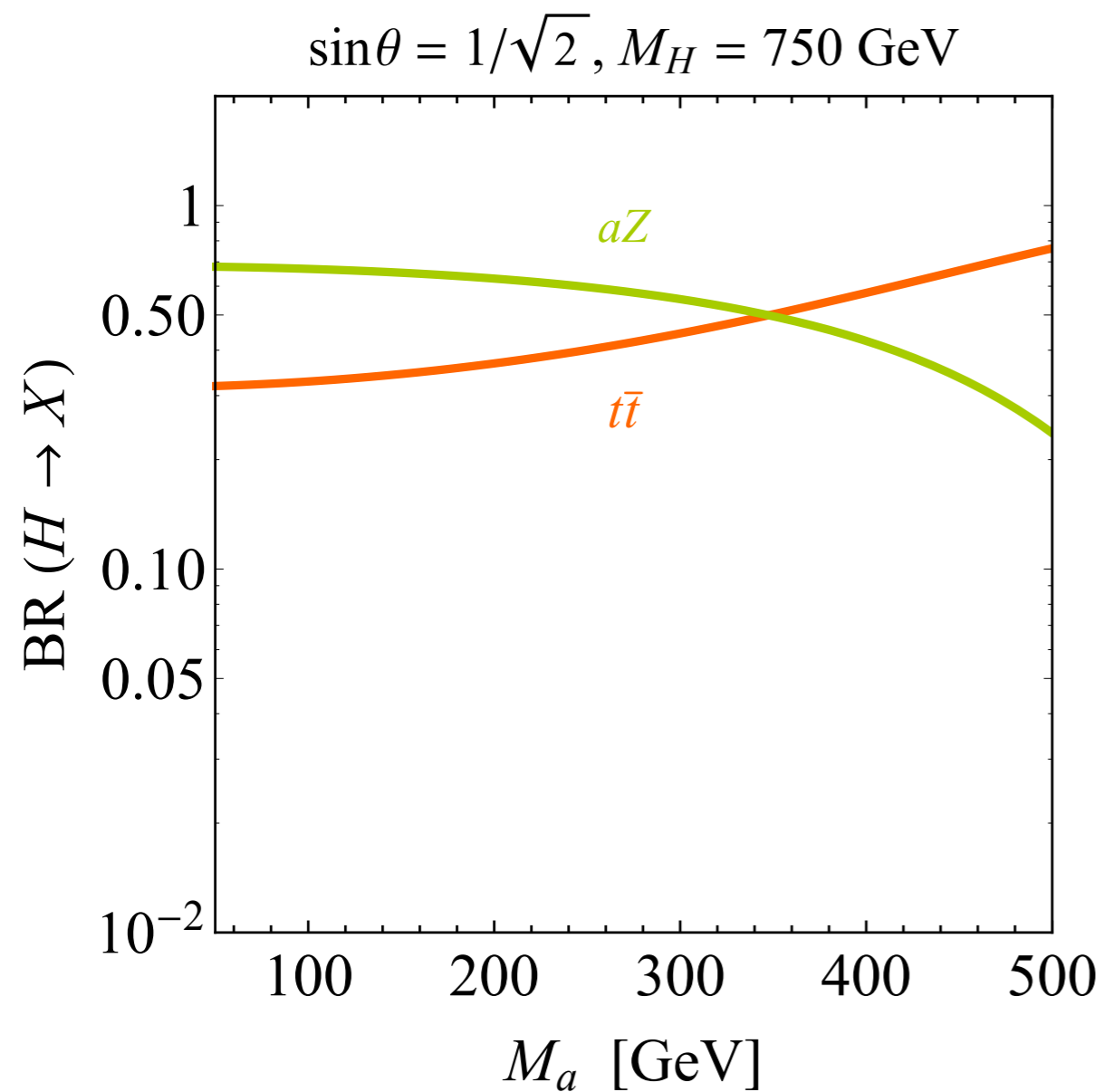


Mono-jet & supersymmetric (SUSY) searches provide comparable bounds in most of parameter space. SUSY searches often slightly better, except if mass of DM particle & mediator is degenerate

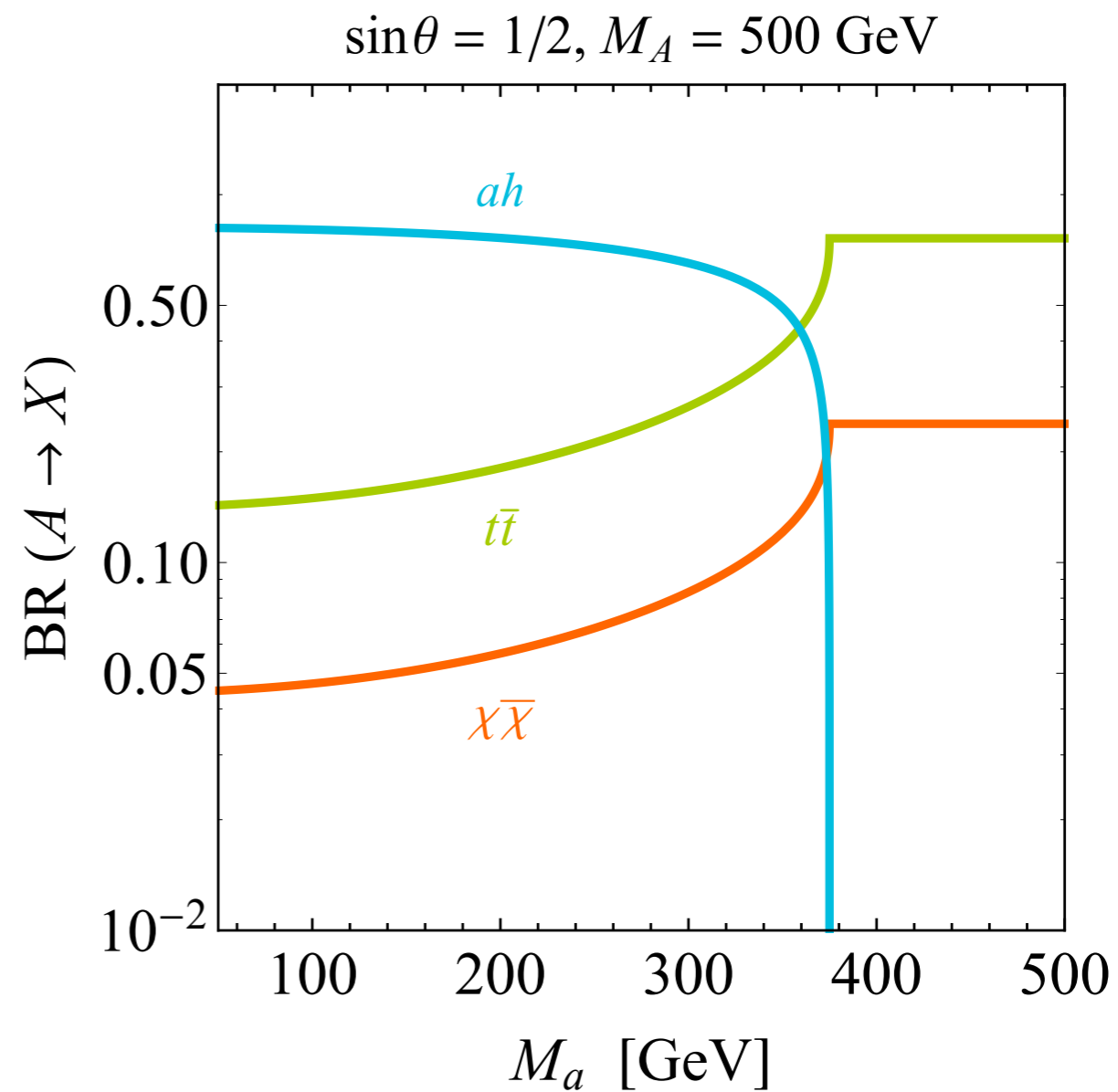
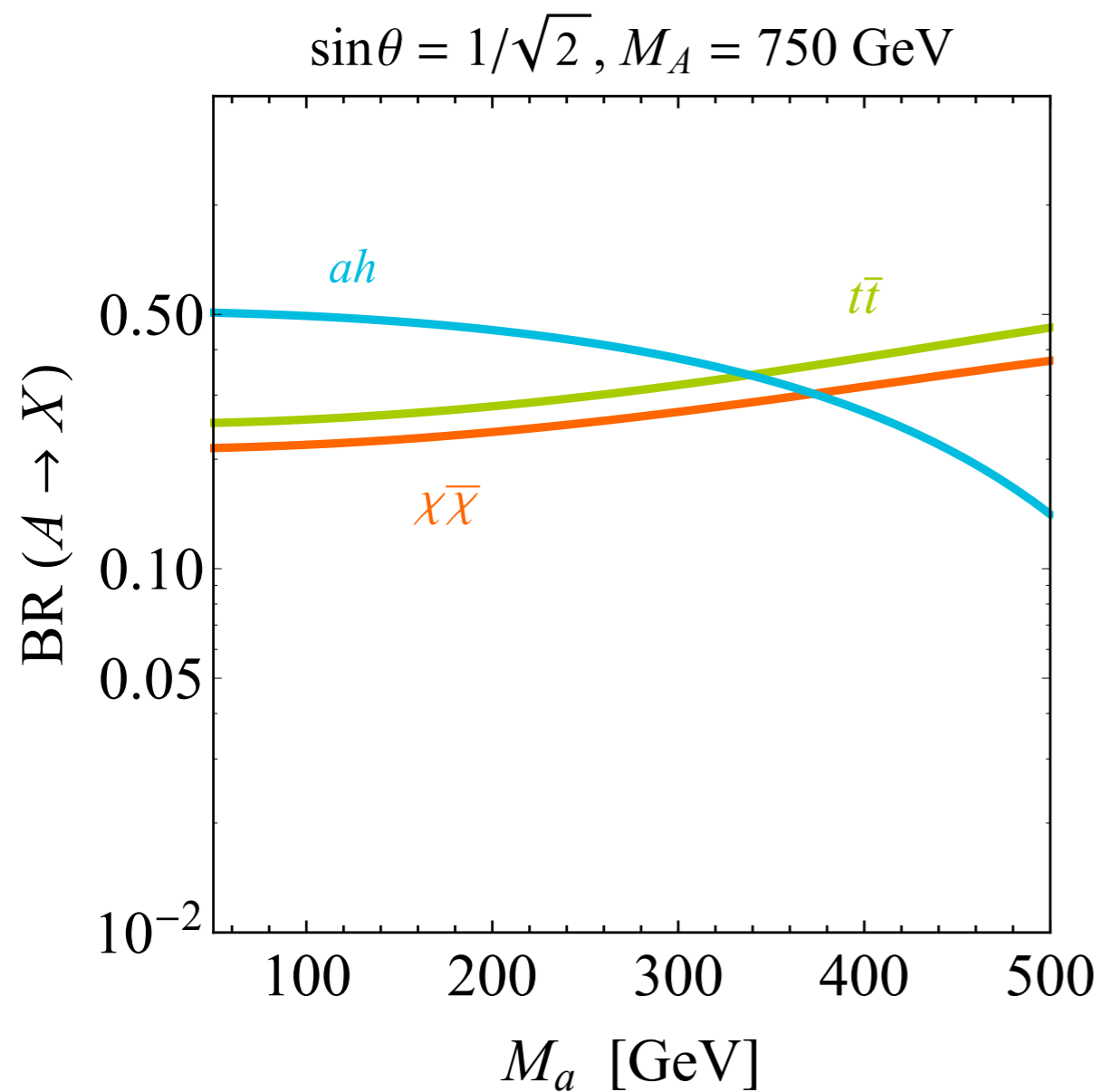
THDMP: $h \rightarrow X$ branching ratios



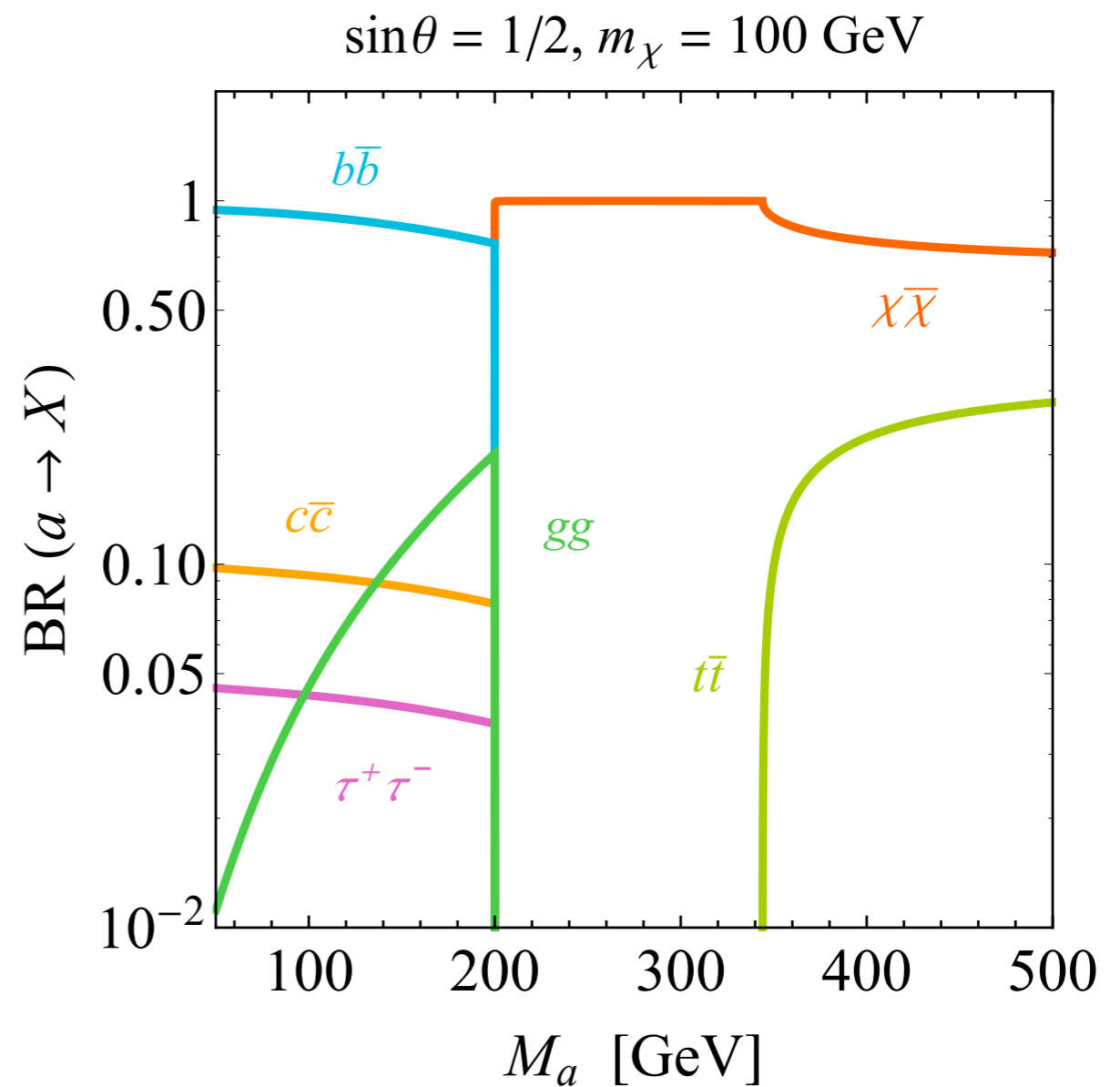
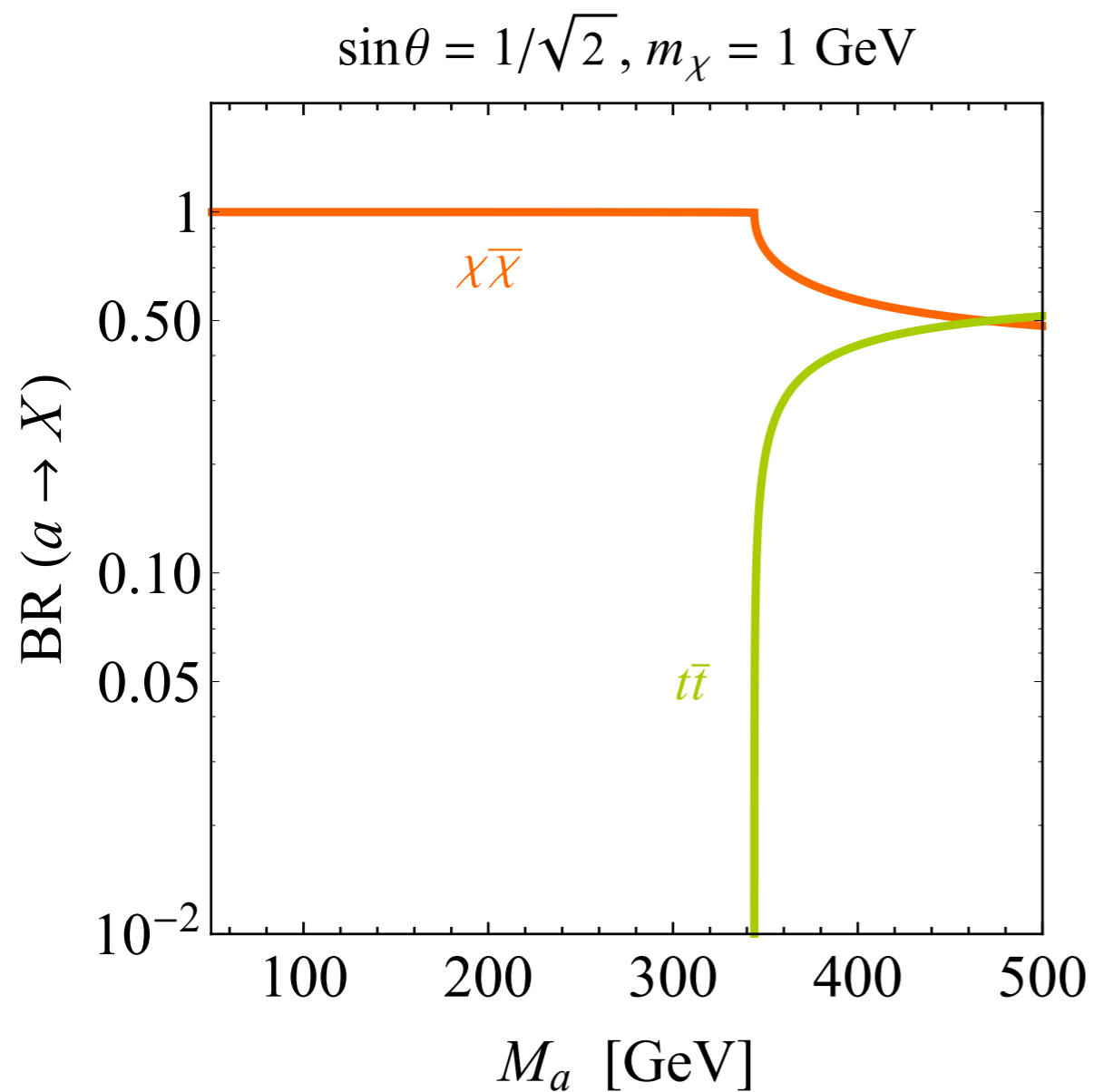
THDMP: $H \rightarrow X$ branching ratios



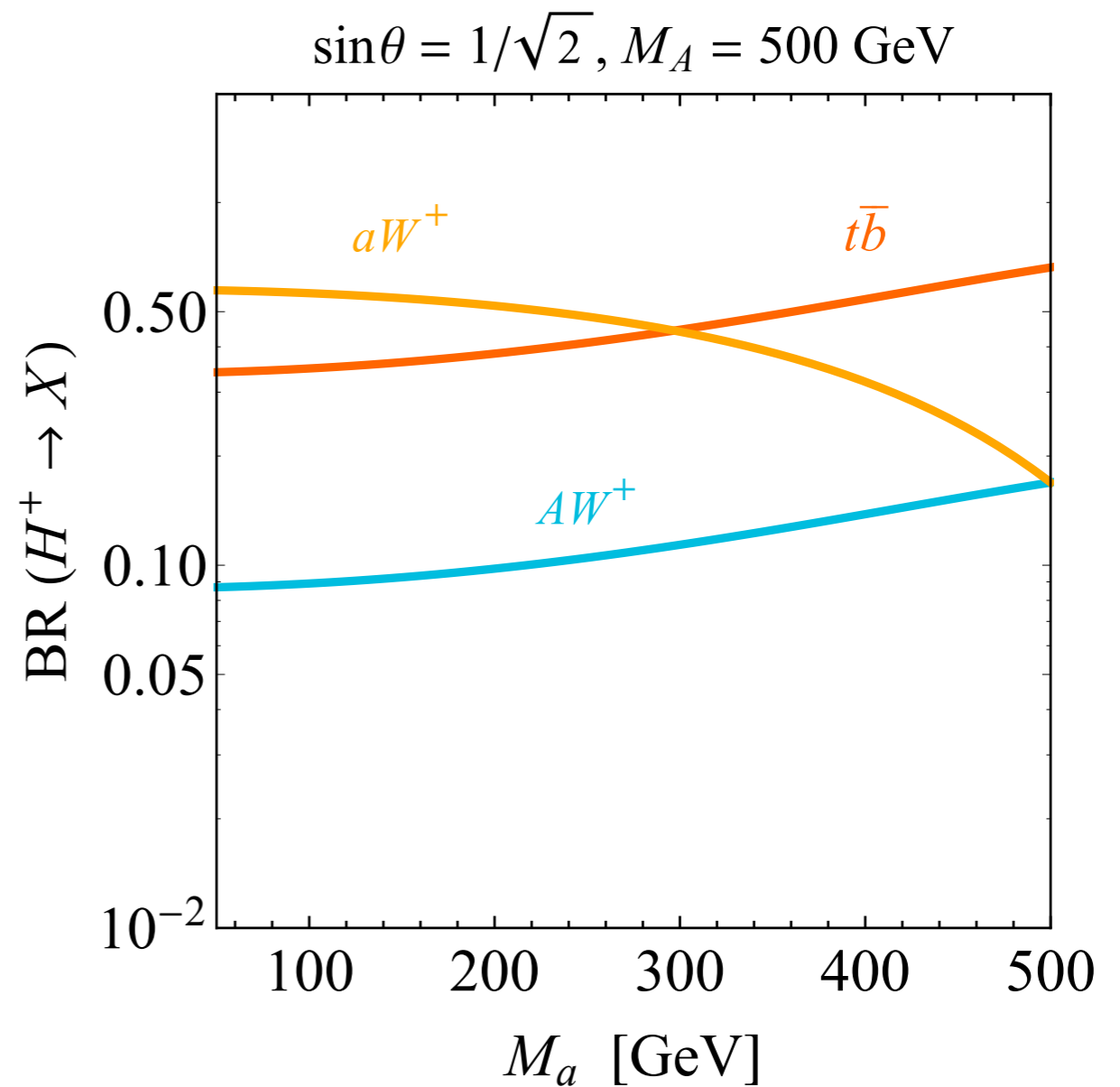
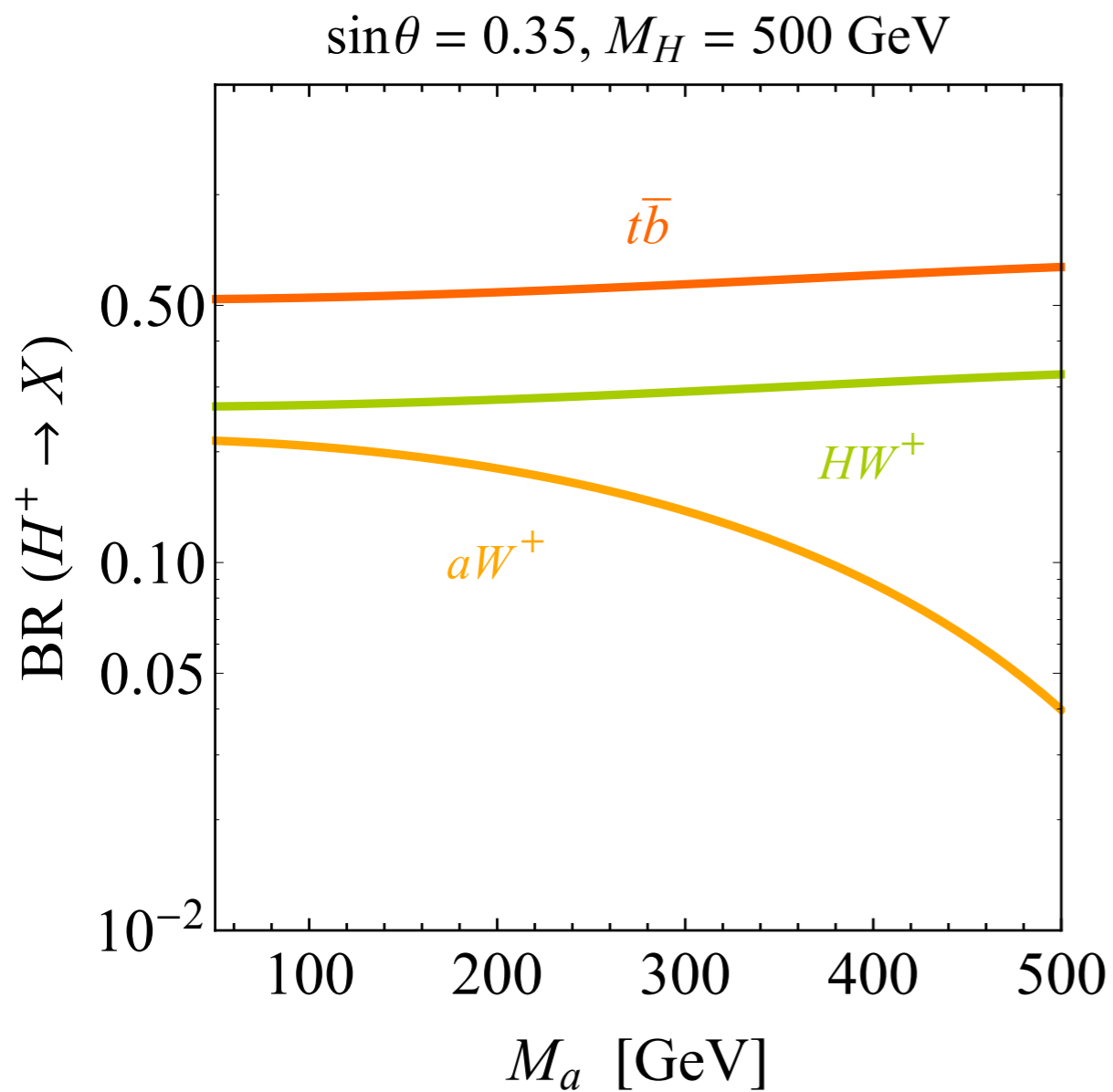
THDMP: $A \rightarrow X$ branching ratios



THDMP: $a \rightarrow X$ branching ratios



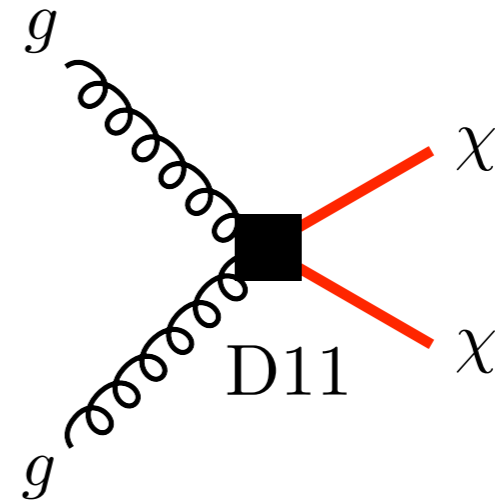
THDMP: $H^+ \rightarrow X$ branching ratios



Loop-level example

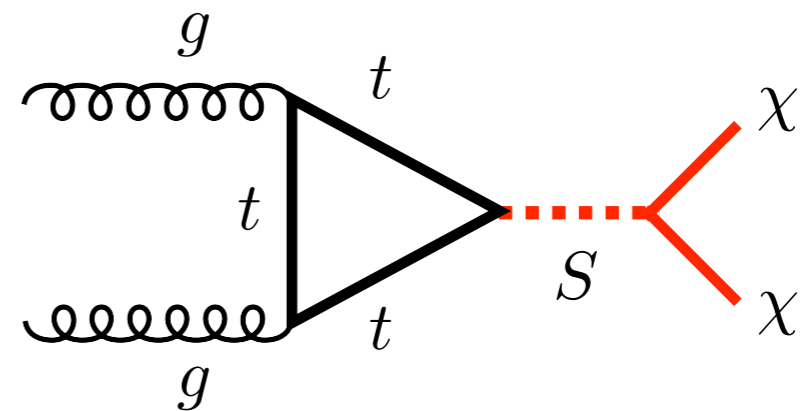
Gluonic operator:

$$D11 = \bar{\chi}\chi G_{\mu\nu}G^{\mu\nu}$$



Spin-0 simplified model:

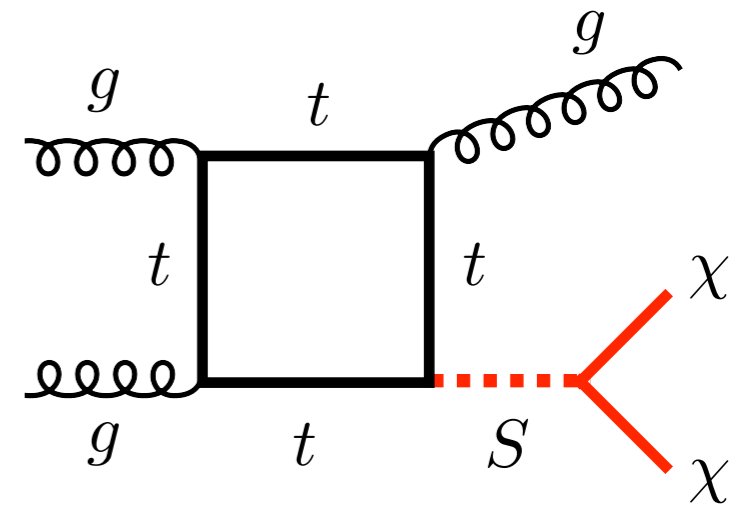
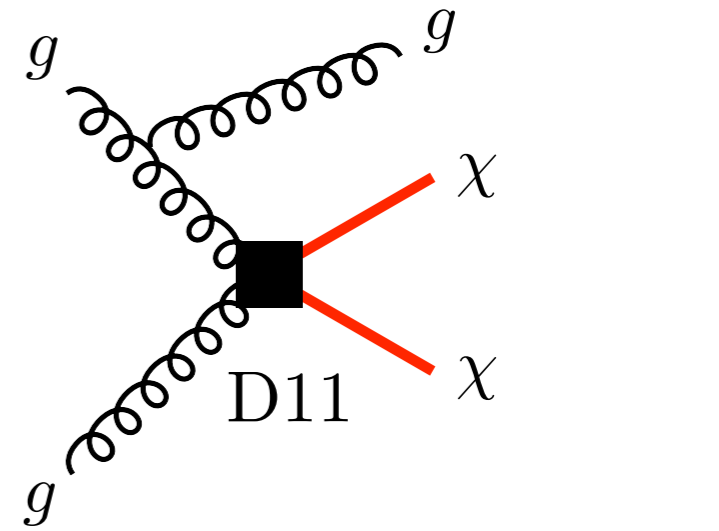
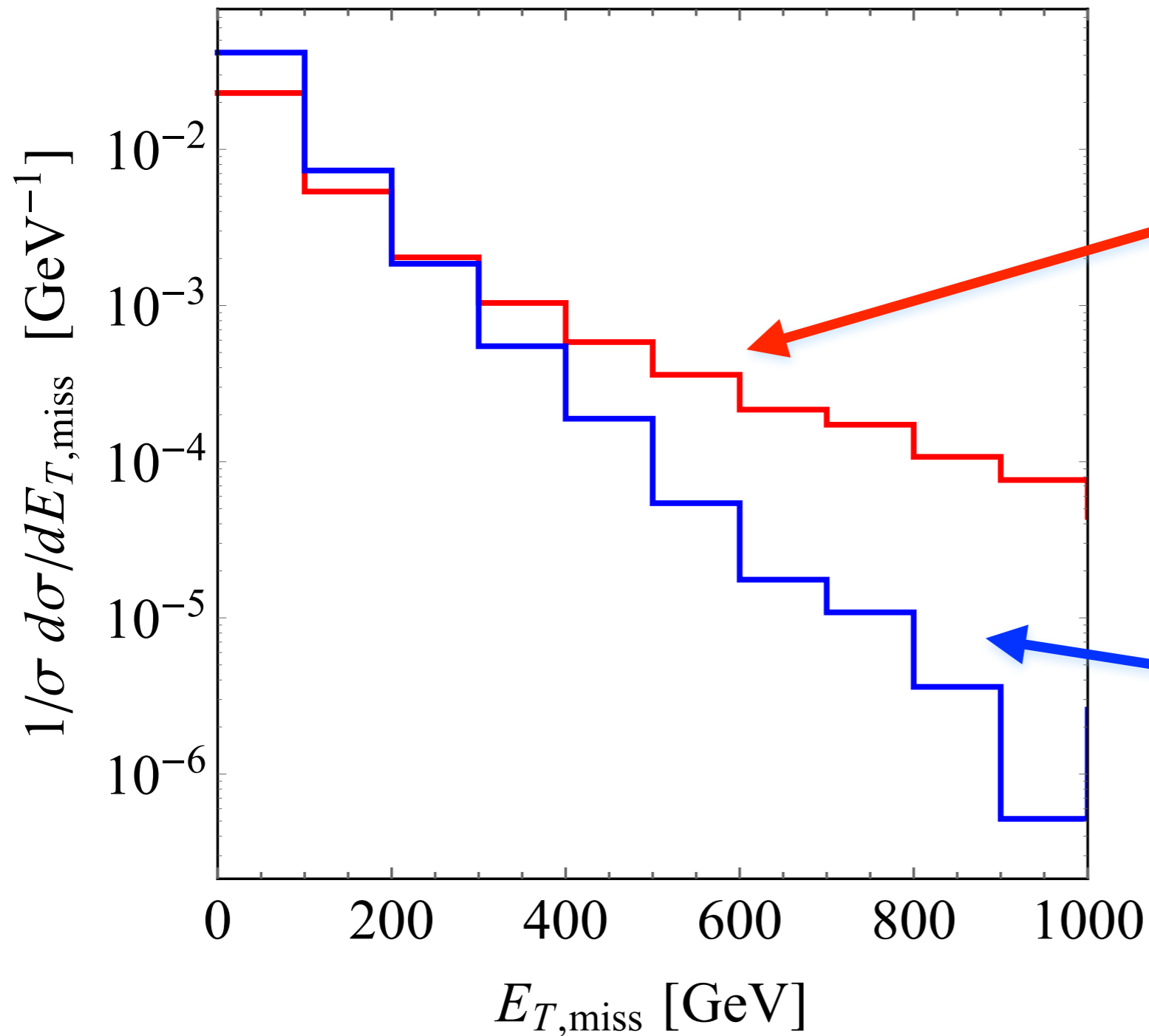
$$\mathcal{L}_S \supset g_\chi \bar{\chi}\chi S + \sum_q \frac{g_q y_q}{\sqrt{2}} \bar{q}q S$$



[UH et al., I208.4605, I311.713, I503.00691; Buckley et al., I410.6497; Harris et al., I411.0535; ...]

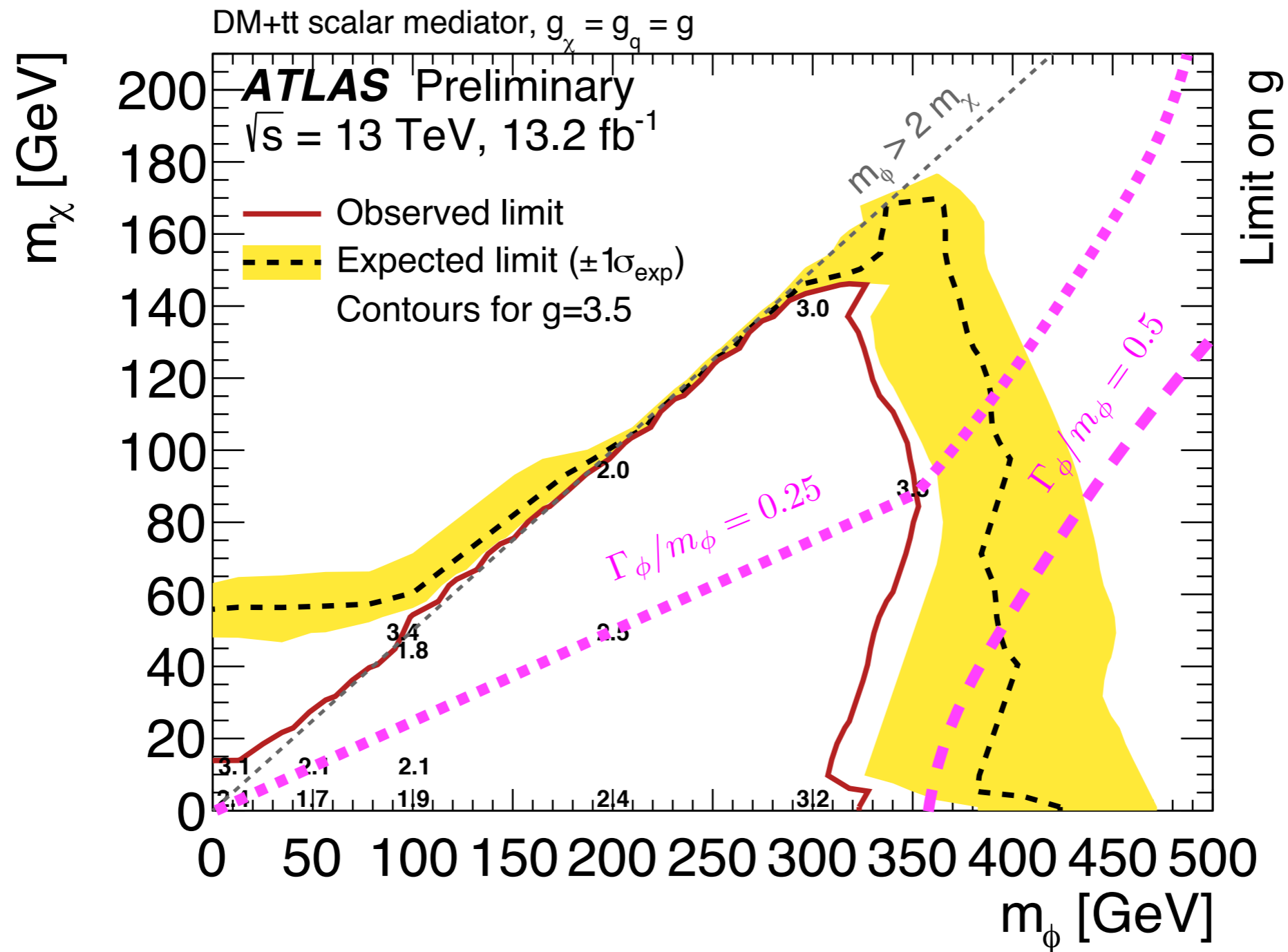
D11: EFT vs. simplified model

$$M_S = 500 \text{ GeV}, \Gamma_S = 10 \text{ GeV}$$



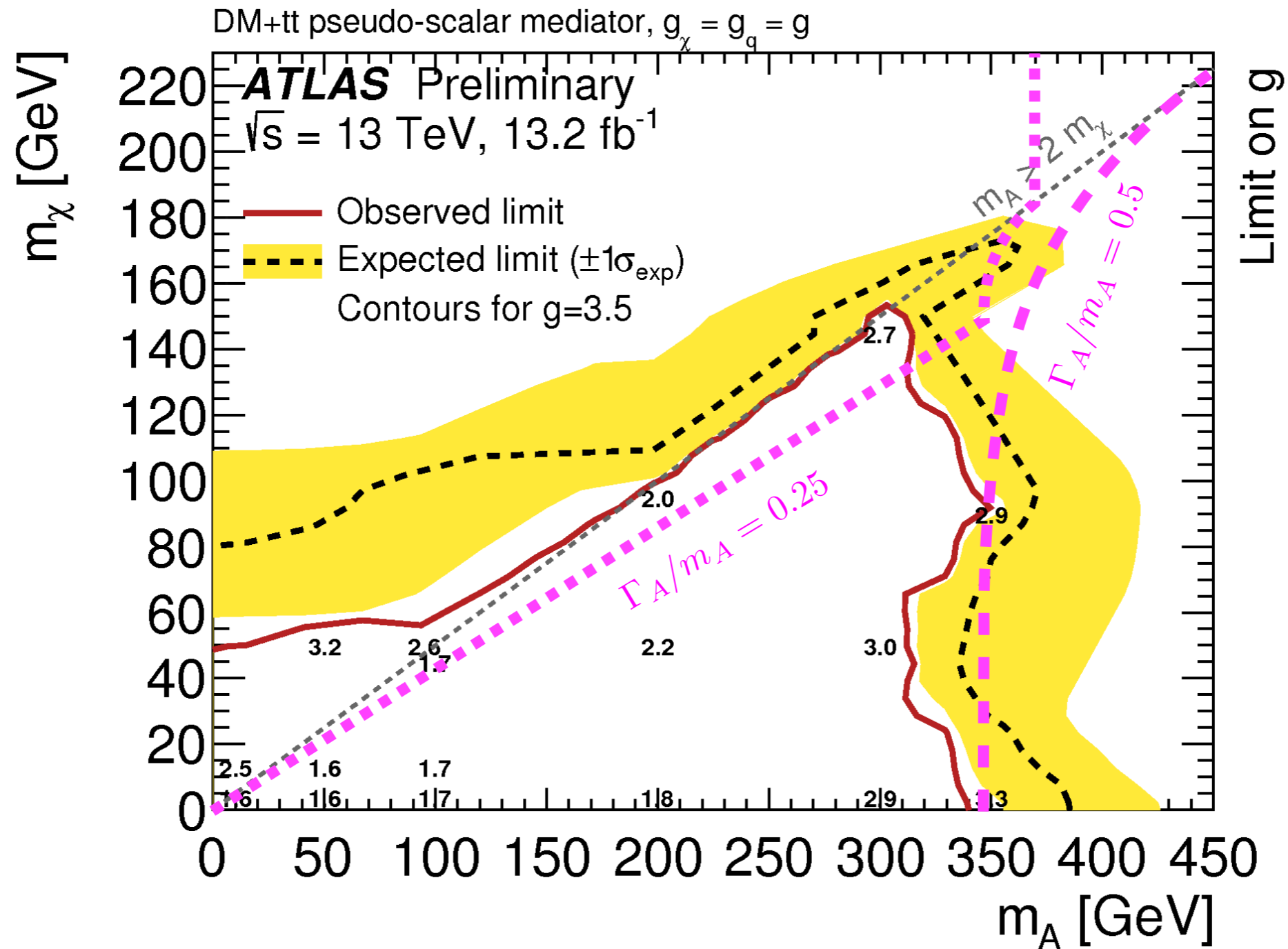
13 TeV limits on $E_{T,miss} + t\bar{t}$

[ATLAS-CONF-2016-050]



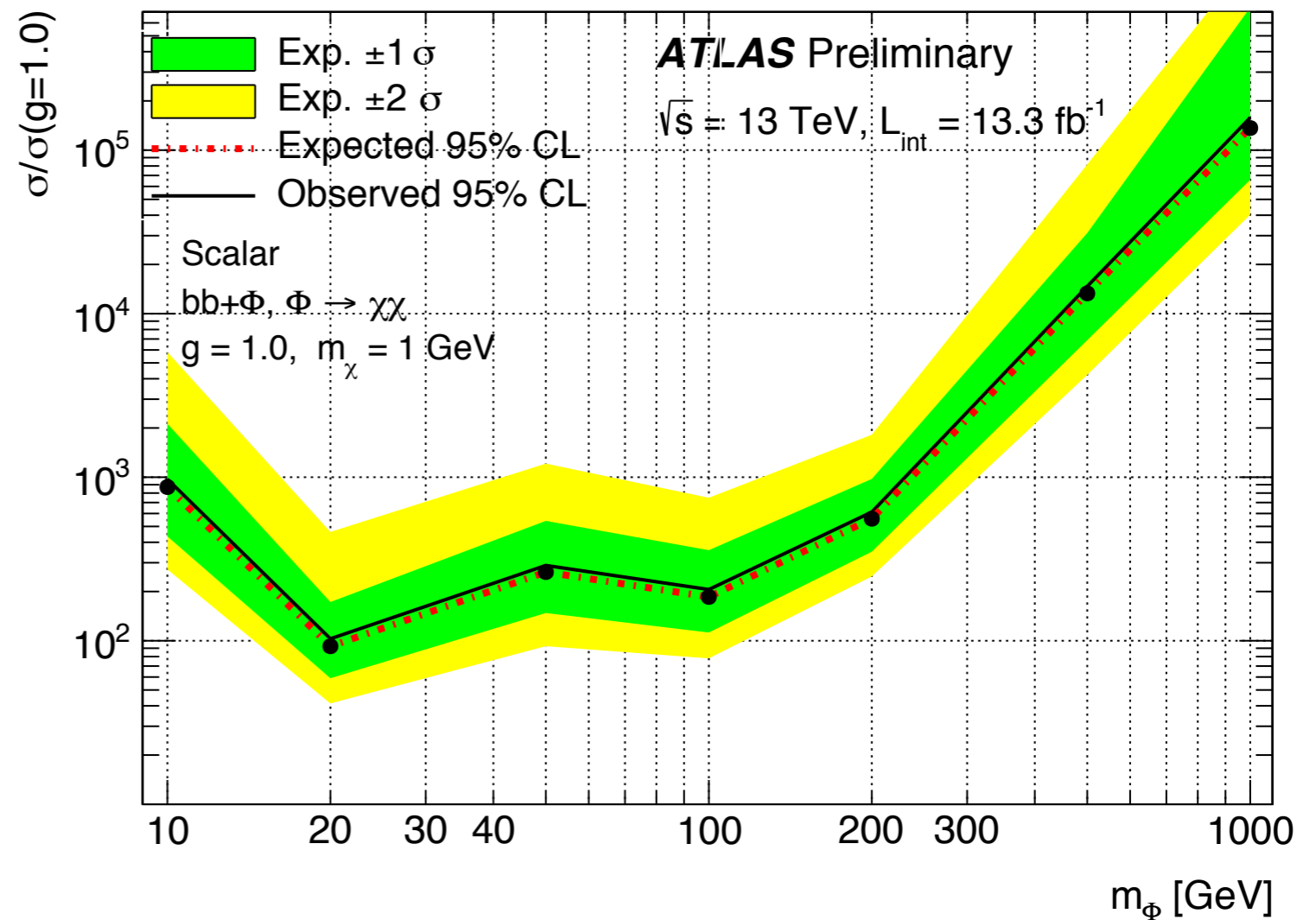
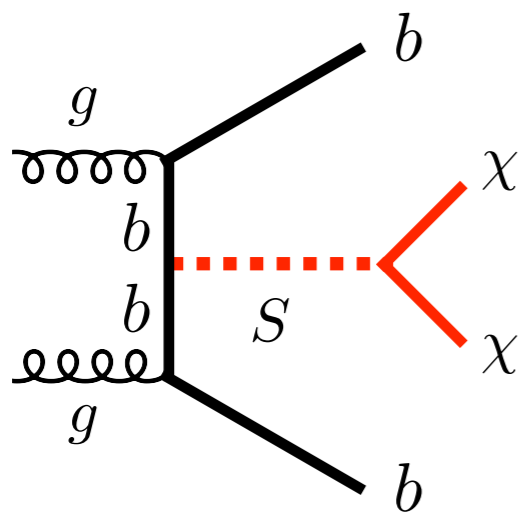
13 TeV limits on $E_{T,miss} + t\bar{t}$

[ATLAS-CONF-2016-050]



13 TeV limits on $E_{T, \text{miss}} + b\bar{b}$

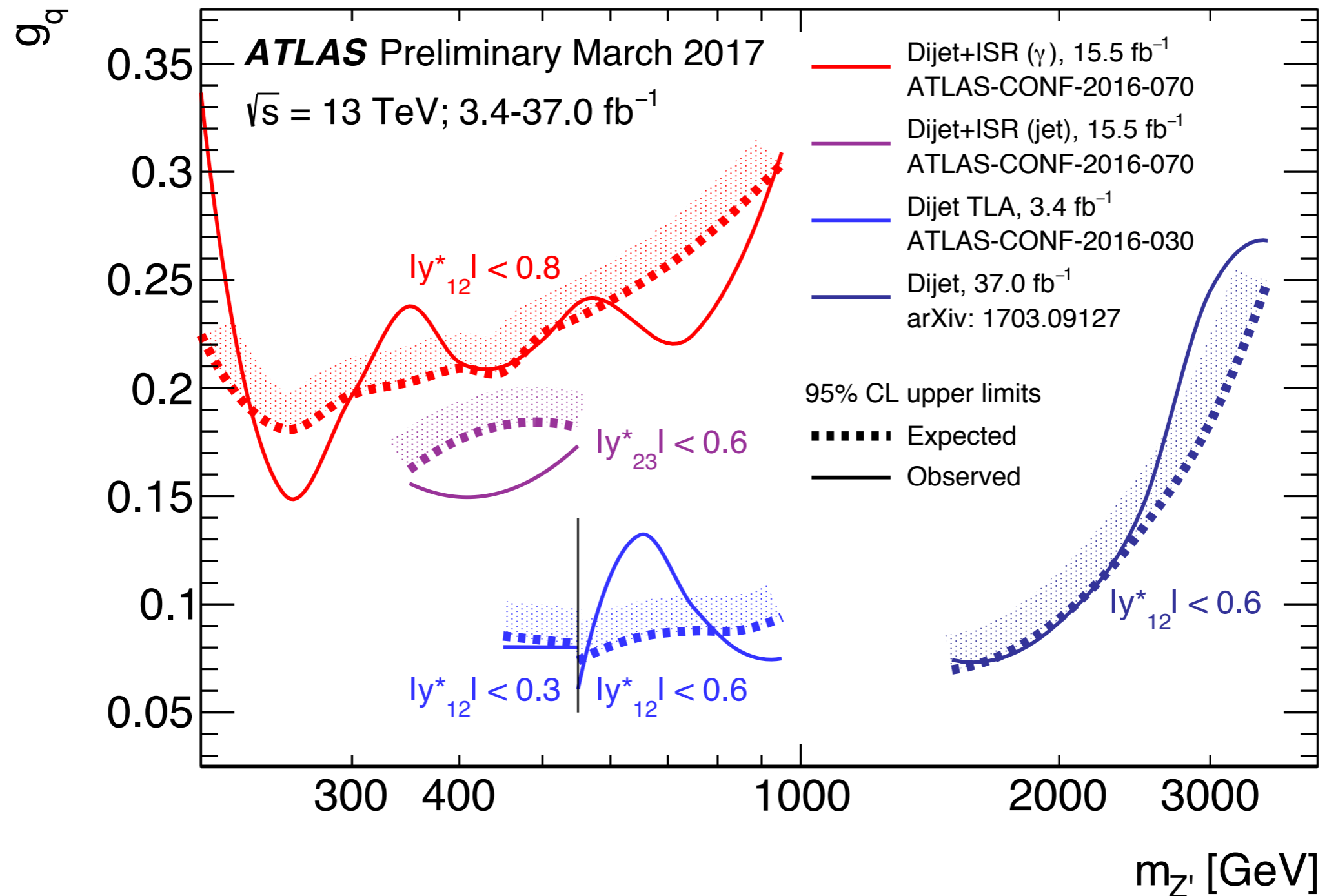
[ATLAS-CONF-2016-086]



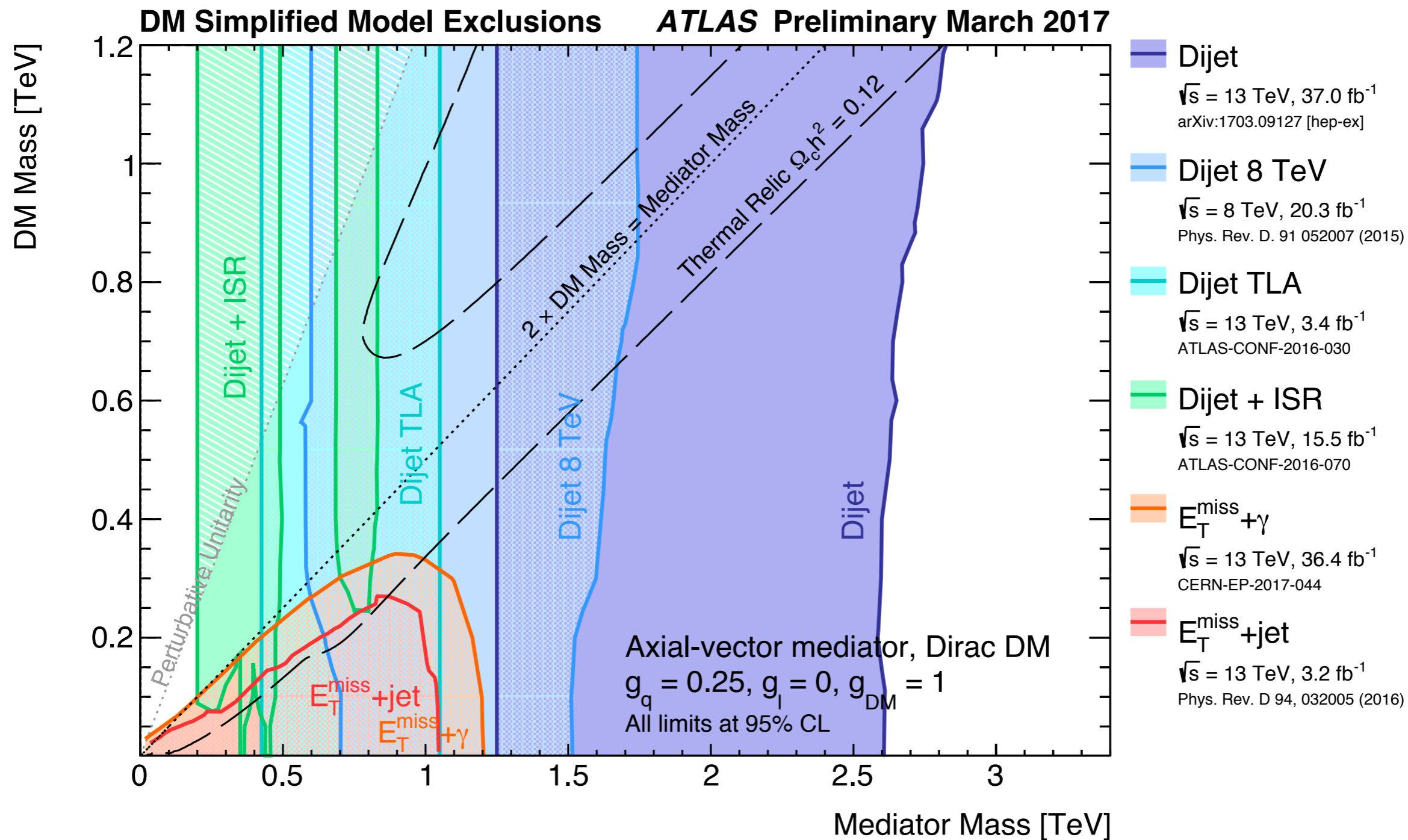
$E_{T, \text{miss}} + b\bar{b}$ searches not yet sensitive to spin-0 models with weak couplings

Di-jet limits

[<https://twiki.cern.ch/twiki/bin/view/AtlasPublic/ExoticsPublicResults>]

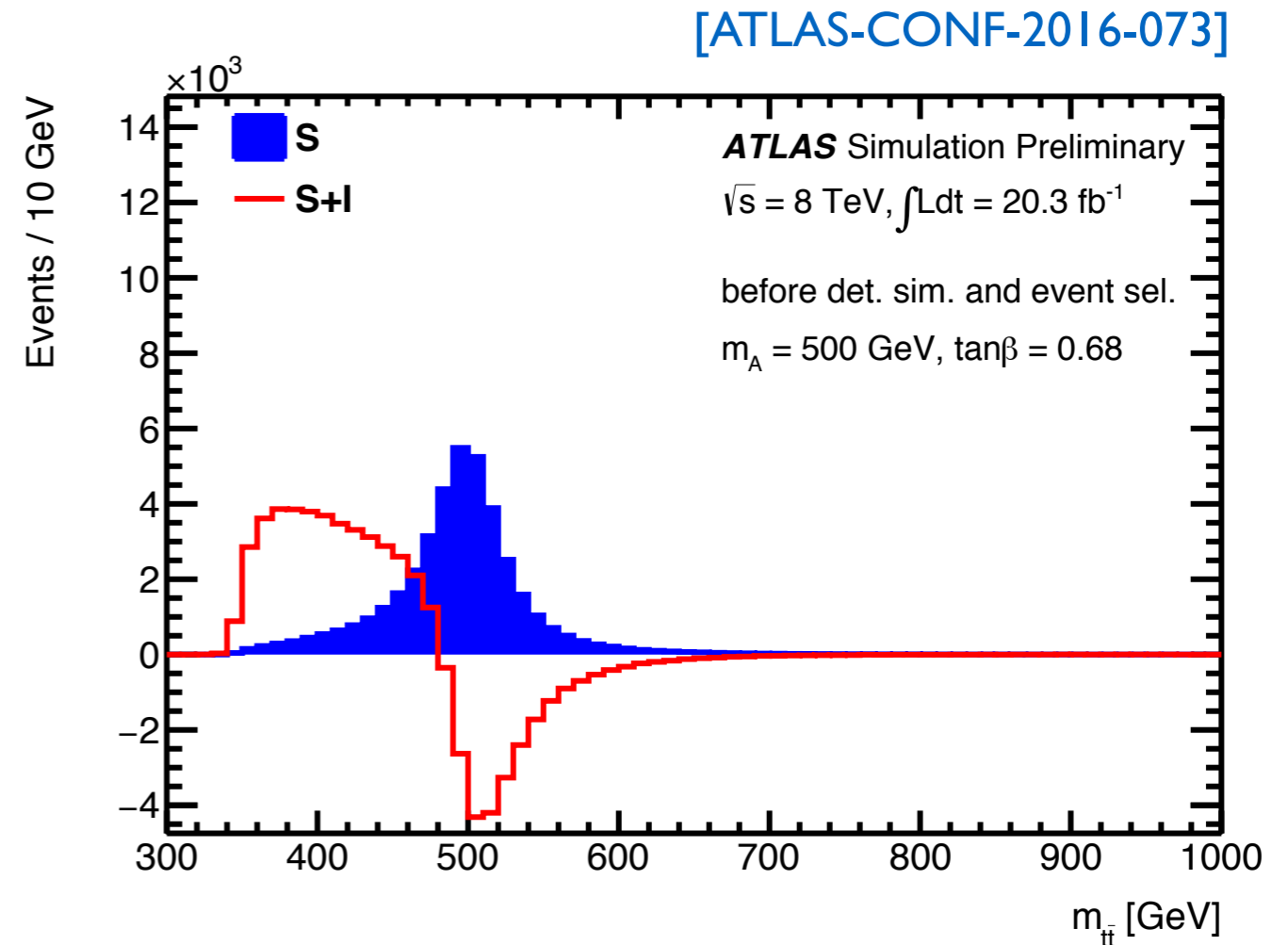
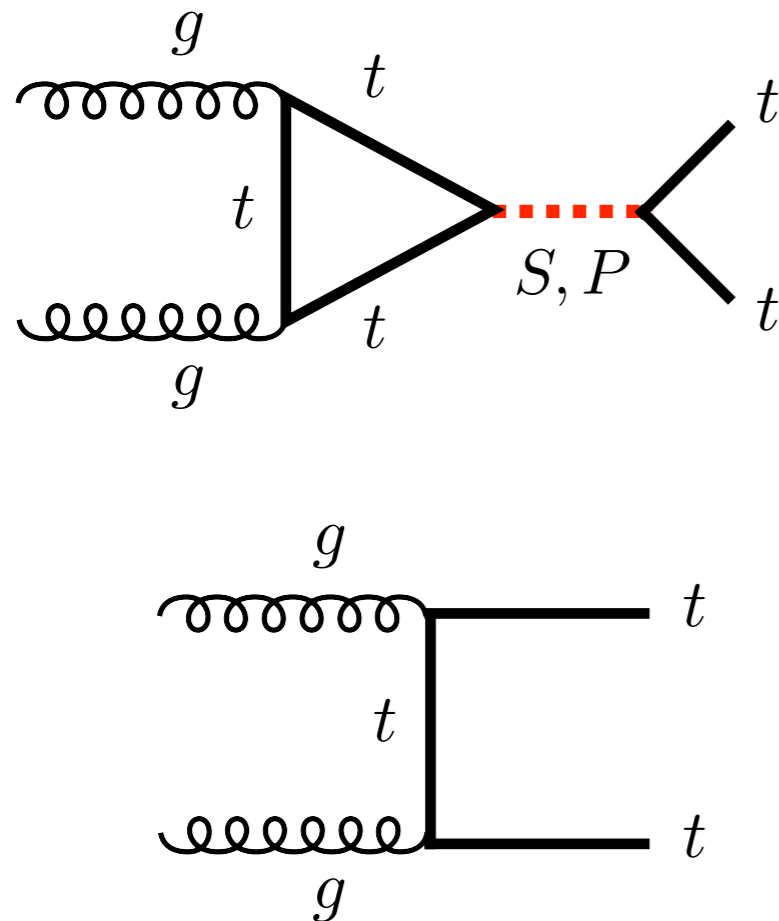


Di-jet limits



[<https://twiki.cern.ch/twiki/bin/view/AtlasPublic/ExoticsPublicResults>]

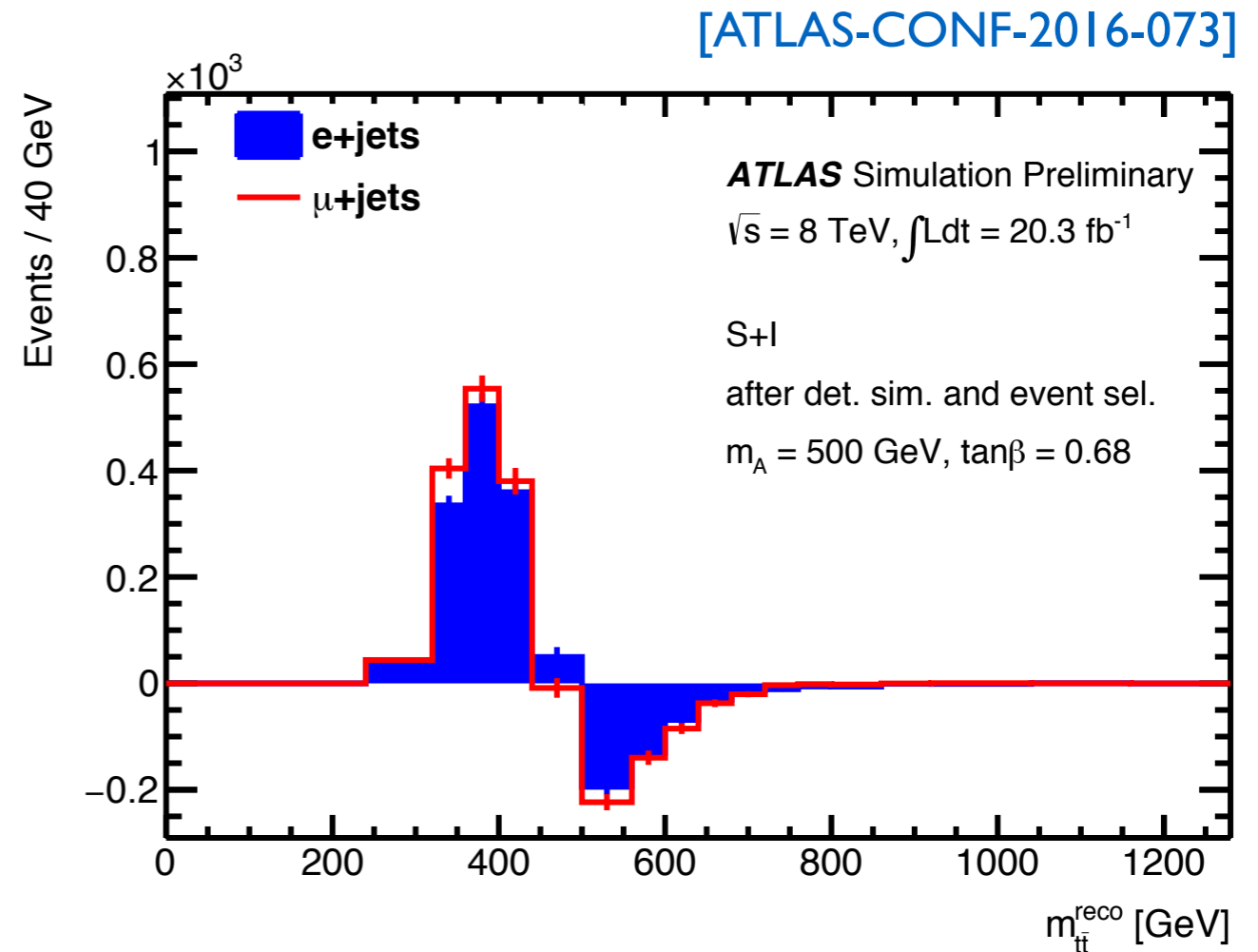
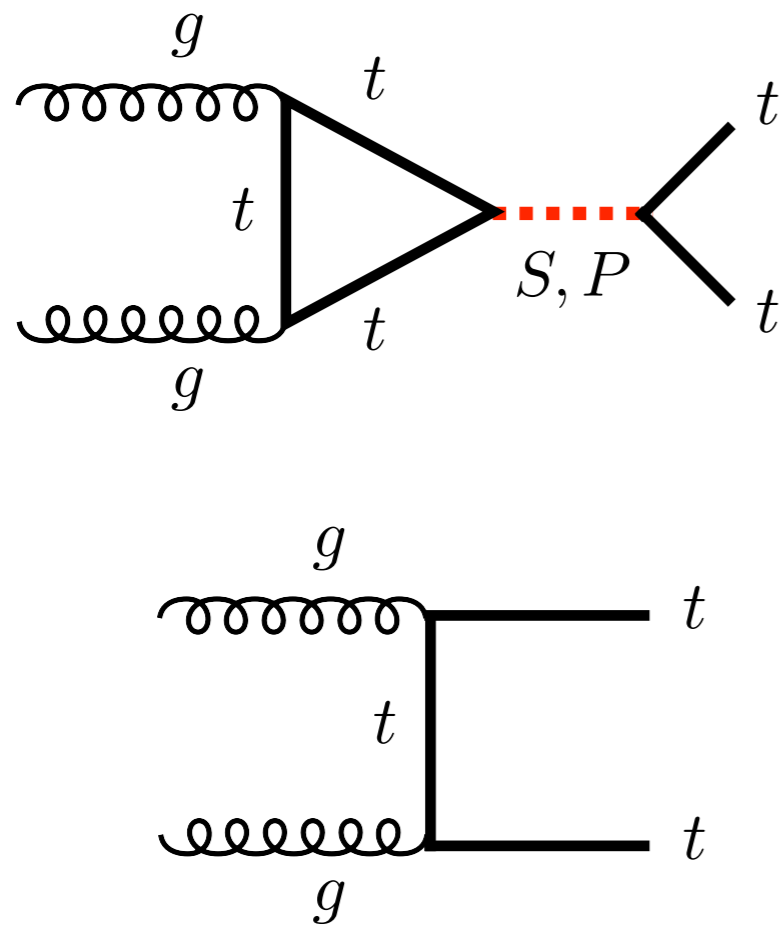
Di-top limits



Spin-0 di-top resonances interfere maximal with SM background, which leads to a peak-dip structure in $m_{t\bar{t}}$ invariant mass spectrum

[Dicus et al., 9404359; Frederix & Maltoni, 0712.2355; Craig et al., 1504.04630; Bernreuther et al., 1511.05584; ...]

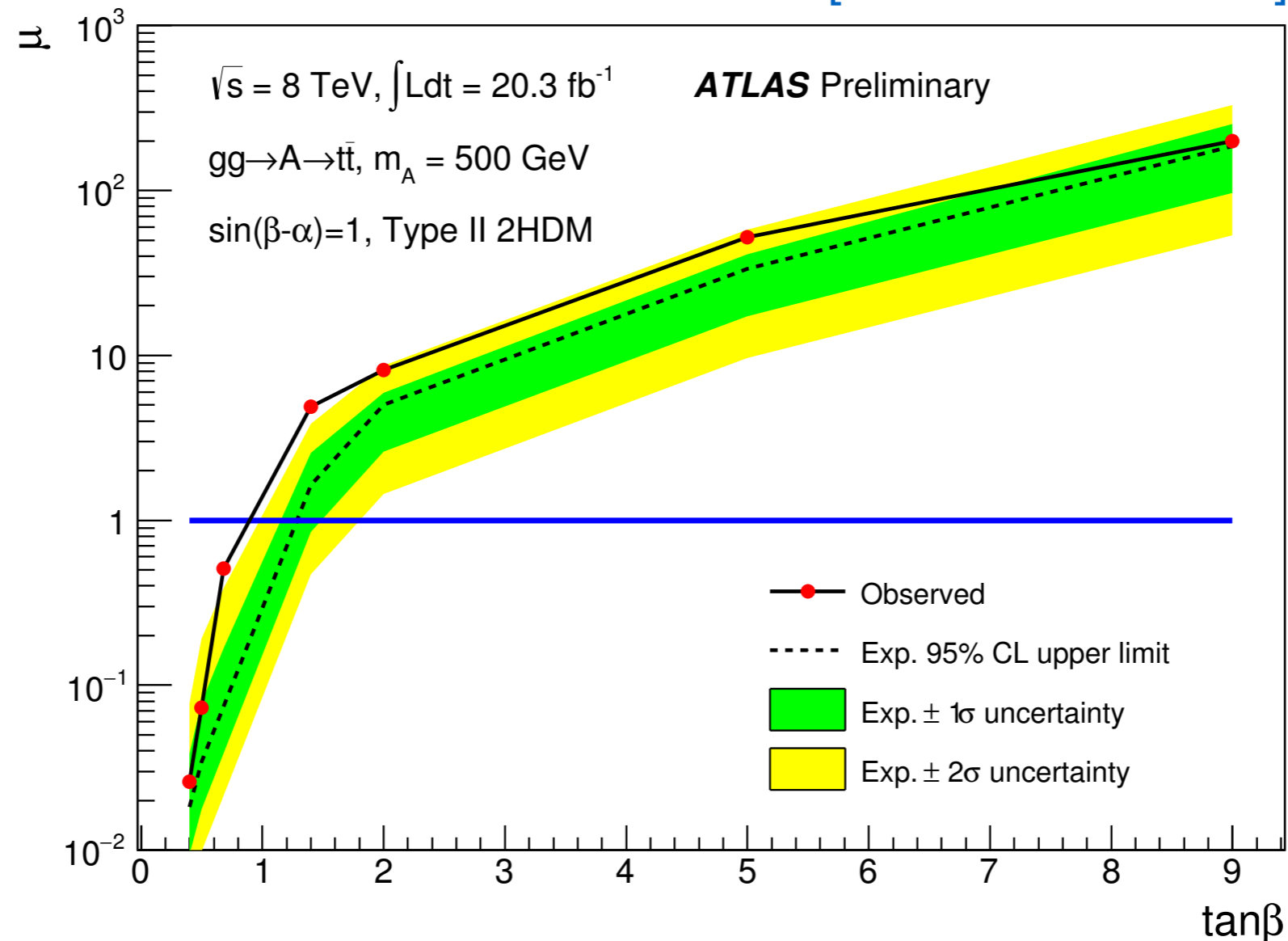
Di-top limits



Compared to parton-level spectra, reconstructed distributions with narrower resonances are more strongly distorted due detector resolution

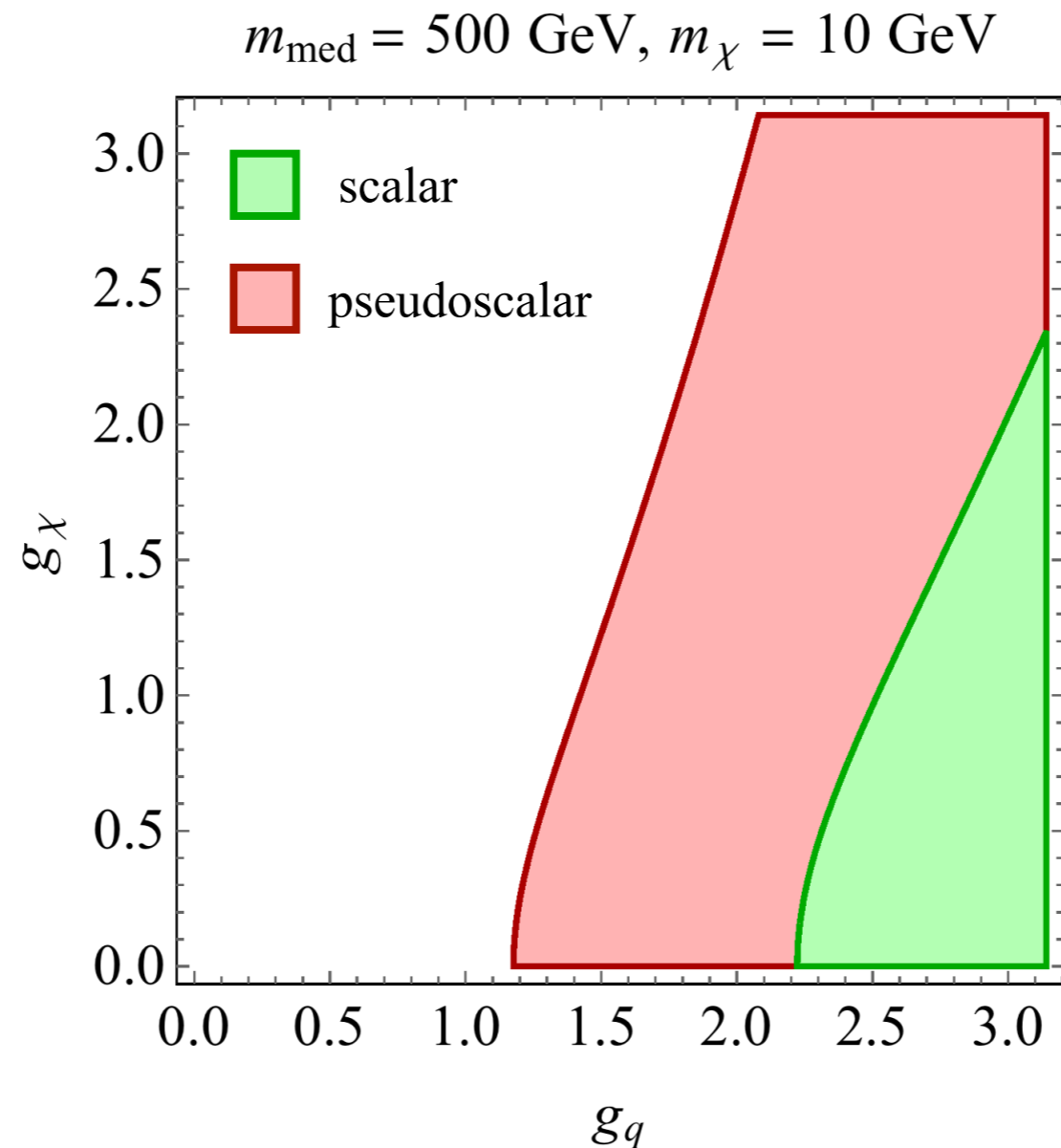
Di-top limits

[ATLAS-CONF-2016-073]



For a pseudoscalar (scalar) of 500 GeV, values of $\tan\beta < 0.85$ ($\tan\beta < 0.45$) are excluded at 95% CL in THDM of type II

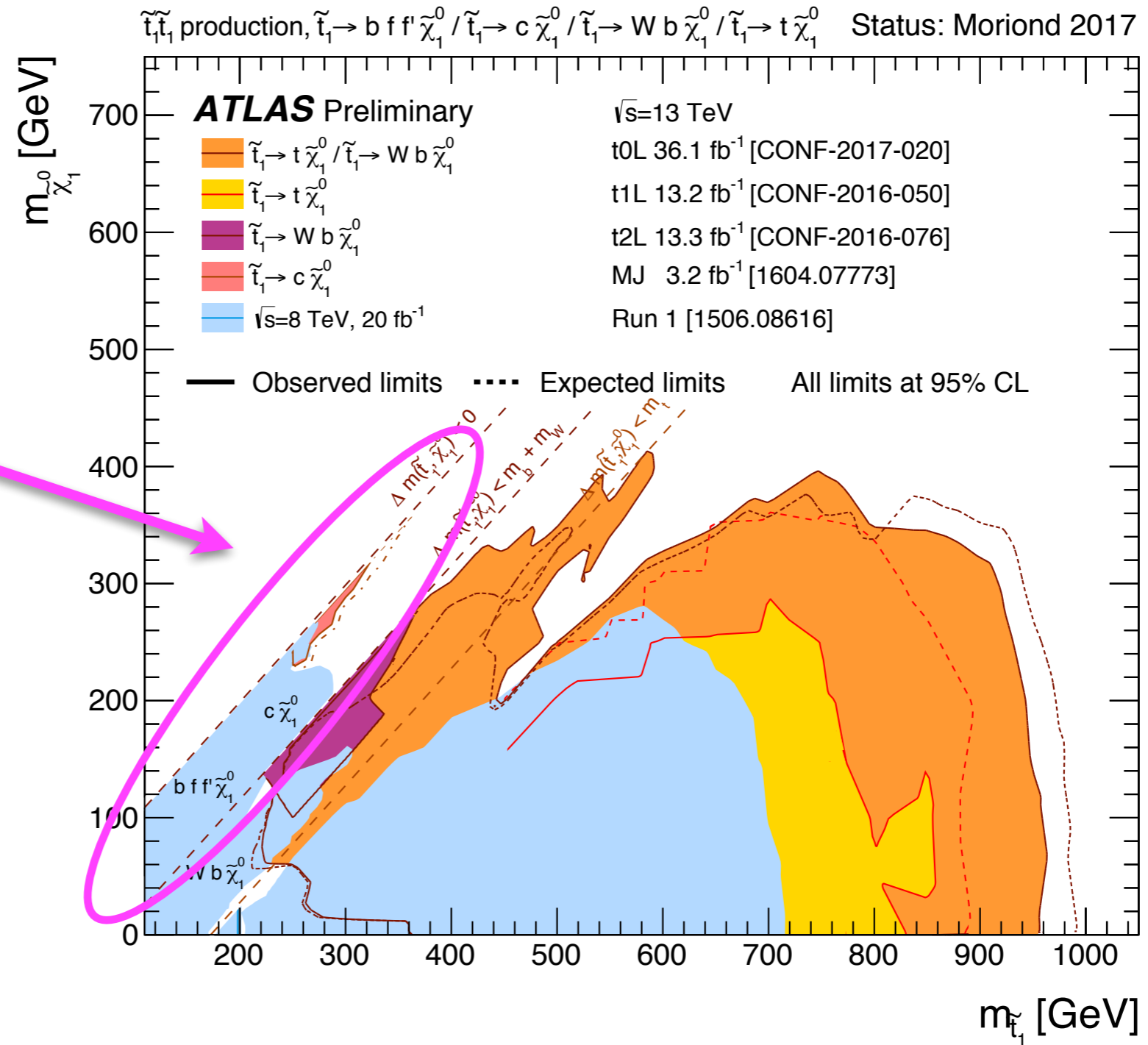
Di-top limits



Easy to recast ATLAS limits to spin-0 simplified model parameter space. For light DM & mediator masses close to $t\bar{t}$ threshold get sensitivity to couplings close to 2 (1) in scalar (pseudoscalar) case

Stop searches

parameter region
constrained by
 $E_{T,miss} + j$ searches



LHC vs. direct detection

$$\boxed{\mathcal{L}_V} \longrightarrow \bar{\chi} \gamma_\mu \chi \bar{q} \gamma^\mu q \longrightarrow \boxed{\mathcal{O}_1 = 1_\chi 1_N}$$

$$\sigma_{\text{SI}} = \frac{f^2(g_q) g_{\text{DM}}^2 \mu_{n\chi}^2}{\pi M_{\text{med}}^4}, \quad \mu_{n\chi} = \frac{m_n m_{\text{DM}}}{m_n + m_{\text{DM}}}, \quad m_n \simeq 0.939 \text{ GeV}$$

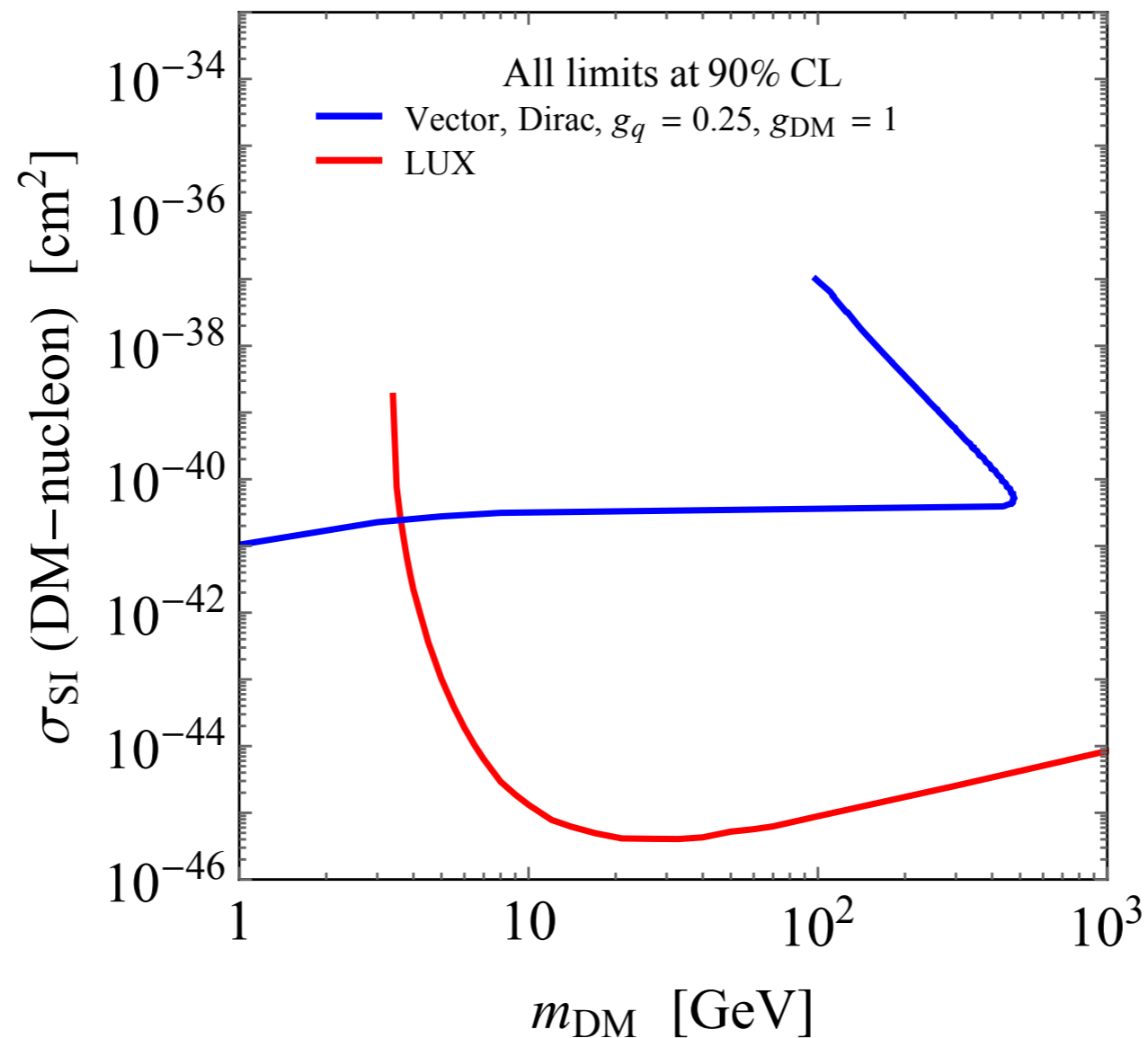
$$f(g_q) = 3g_q$$

$$\sigma_{\text{SI}} \simeq 6.9 \cdot 10^{-41} \text{ cm}^2 \left(\frac{g_q g_{\text{DM}}}{0.25} \right)^2 \left(\frac{1 \text{ TeV}}{M_{\text{med}}} \right)^4 \left(\frac{\mu_{n\chi}}{1 \text{ GeV}} \right)^2$$

† formula for $f(g_q)$ assumes universal couplings to quarks

LHC vs. direct detection

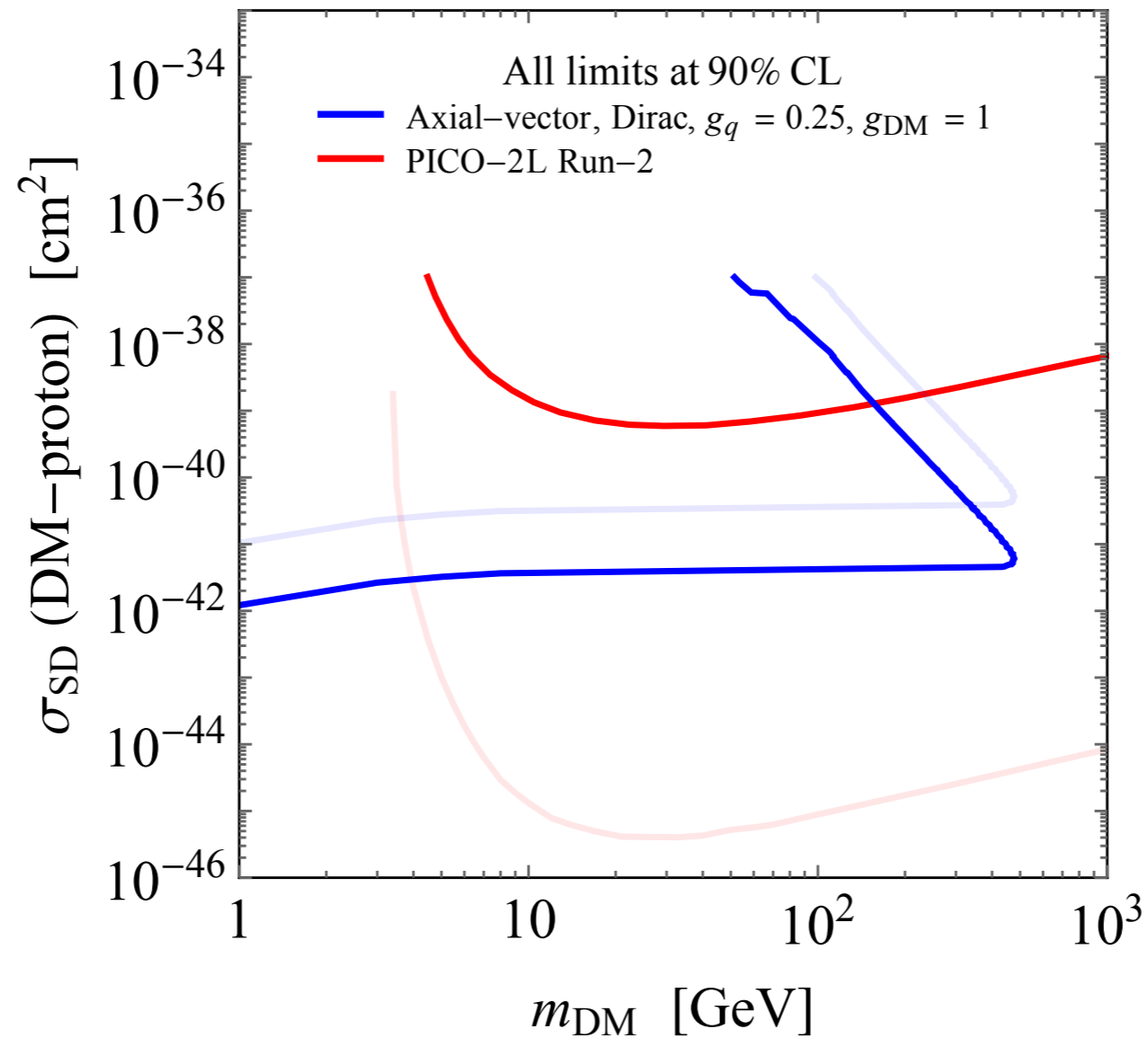
[Boveia et al., 1603.04156]



Like direct detection also mono-jet bound assumes that χ constitutes all of DM in Universe. If this is not case direct detection limit would become weaker, while LHC bound would remain unchanged

LHC vs. direct detection

[Boveia et al., 1603.04156]



$$\mathcal{L}_A$$



$$\bar{\chi} \gamma_\mu \gamma_5 \chi \bar{q} \gamma^\mu \gamma_5 q$$

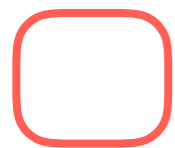


$$\mathcal{O}_4 = \vec{S}_\chi \cdot \vec{S}_N$$

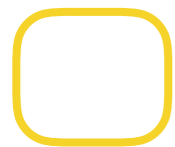
DM-N scattering for spin-0 mediators

$$\mathcal{L}_S \longrightarrow \bar{\chi}\chi\bar{q}q \longrightarrow \mathcal{O}_1 = 1_\chi 1_N$$

$$\mathcal{L}_P \longrightarrow \bar{\chi}i\gamma_5\chi\bar{q}i\gamma_5q \longrightarrow \mathcal{O}_6 = \frac{1}{m_N^2} (\vec{S}_\chi \cdot \vec{q}) (\vec{S}_N \cdot \vec{q})$$



SI



SD & momentum suppressed

Due to loss of coherence & since $q = O(0.1 \text{ GeV})$ resulting DM-N cross section $O(10^{-11})$ lower than σ_{SI} . As a result very poor direct detection limits

DM annihilation: pseudo-scalar case

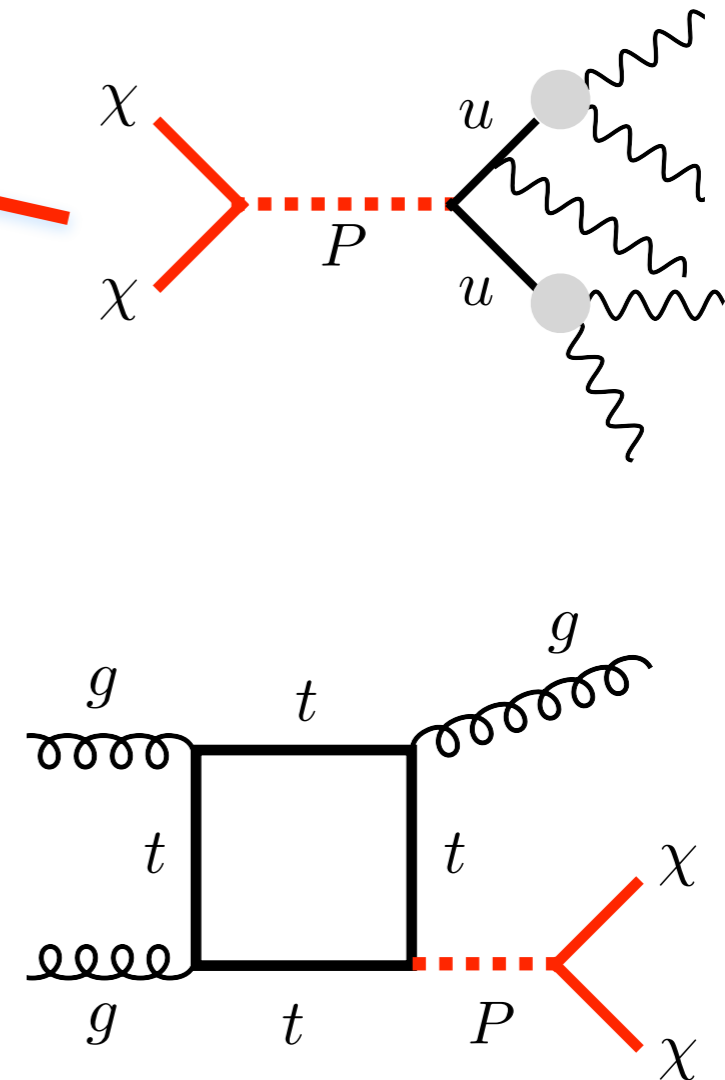
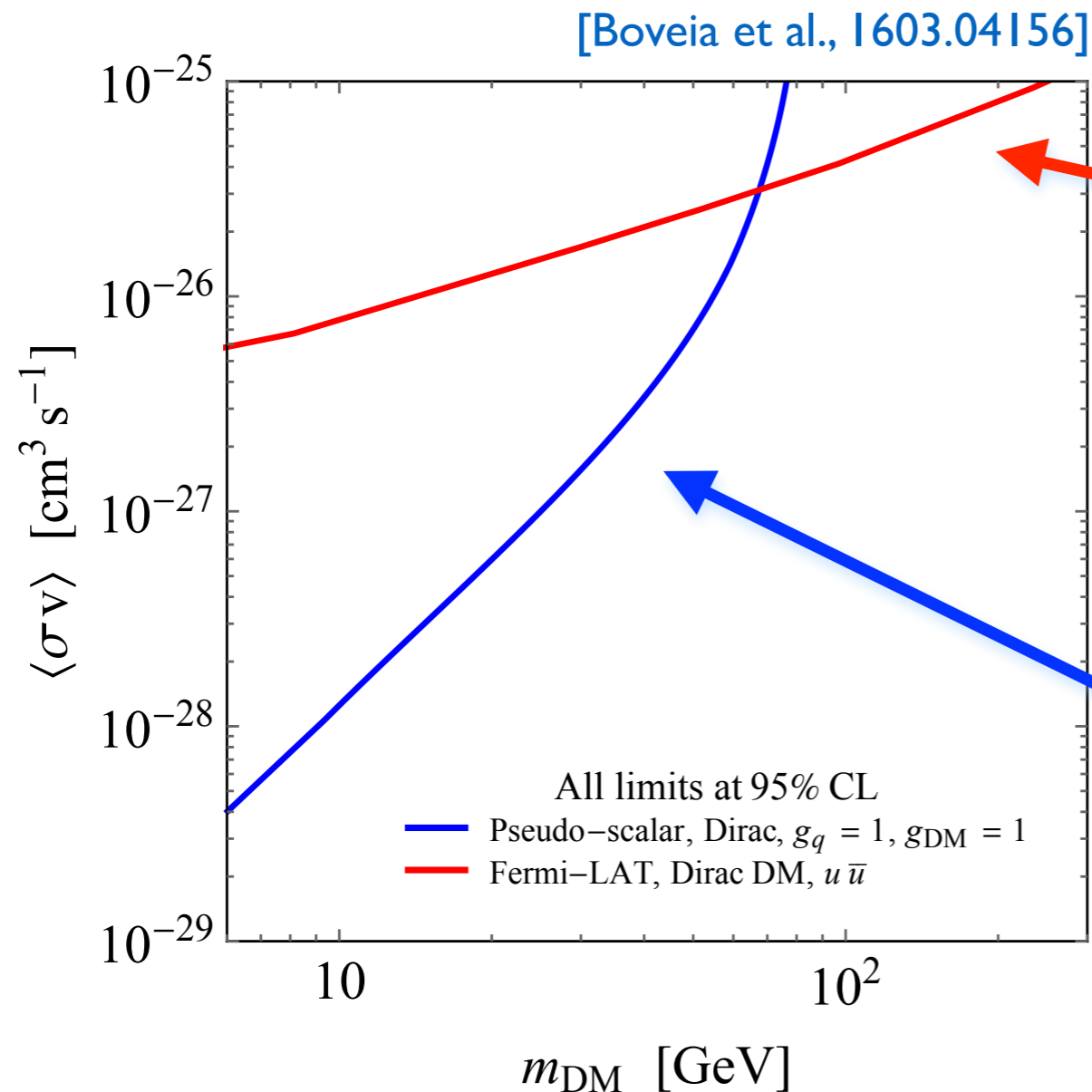
$$\langle \sigma v_{\text{rel}} \rangle_q = \frac{3m_q^2}{2\pi v^2} \frac{g_q^2 g_{\text{DM}}^2 m_{\text{DM}}^2}{(M_{\text{med}}^2 - 4m_{\text{DM}}^2)^2 + M_{\text{med}}^2 \Gamma_{\text{med}}^2} \sqrt{1 - \frac{m_q^2}{m_{\text{DM}}^2}}$$

$$\langle \sigma v_{\text{rel}} \rangle_g = \frac{\alpha_s^2}{2\pi^3 v^2} \frac{g_q^2 g_{\text{DM}}^2}{(M_{\text{med}}^2 - 4m_{\text{DM}}^2)^2 + M_{\text{med}}^2 \Gamma_{\text{med}}^2} \left| \sum_q m_q^2 f_{\text{pseudo-scalar}} \left(\frac{m_q^2}{m_\chi^2} \right) \right|^2$$

$$f_{\text{pseudo-scalar}}(\tau) = \tau \arctan^2 \left(\frac{1}{\sqrt{\tau - 1}} \right)$$

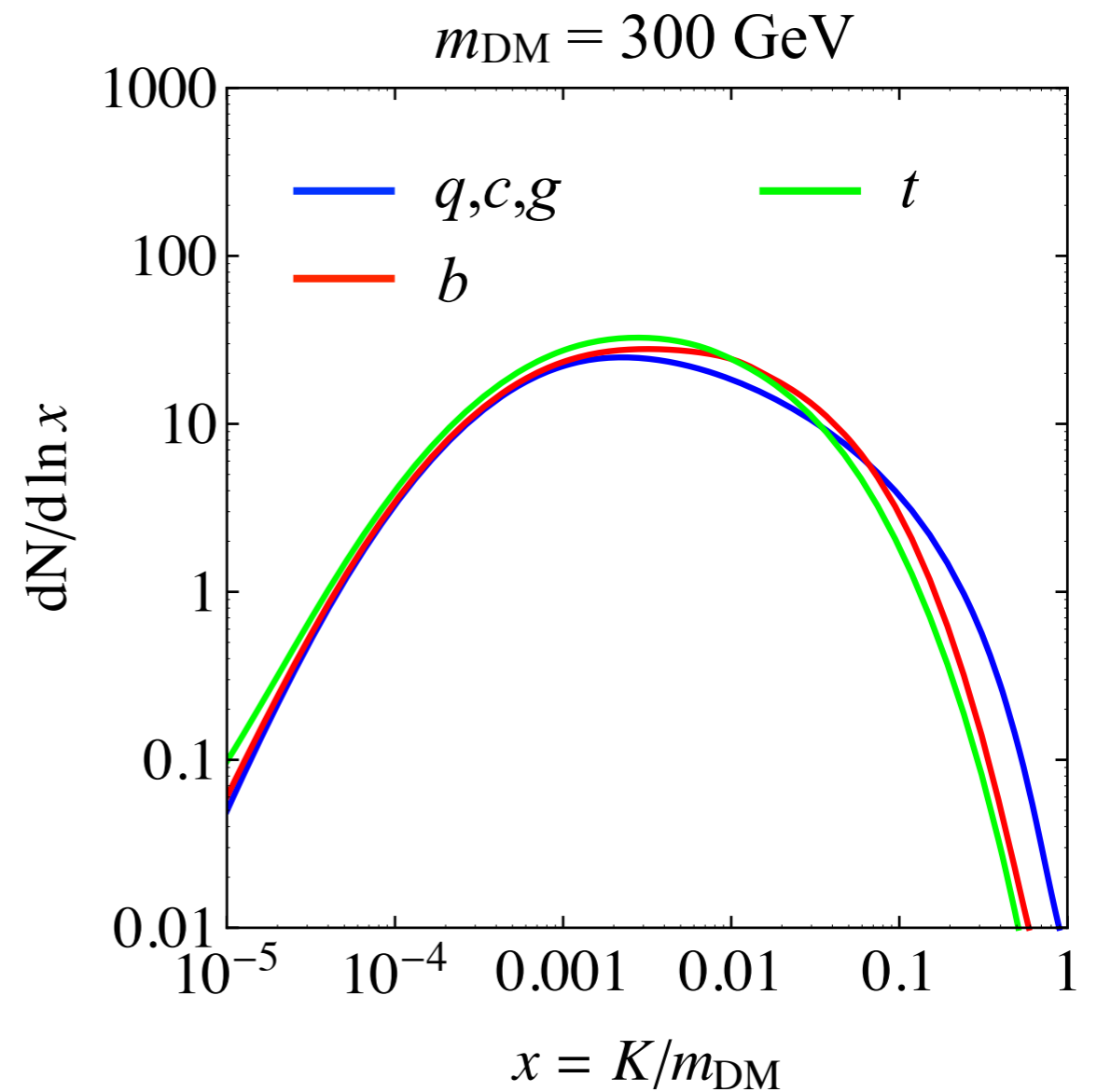
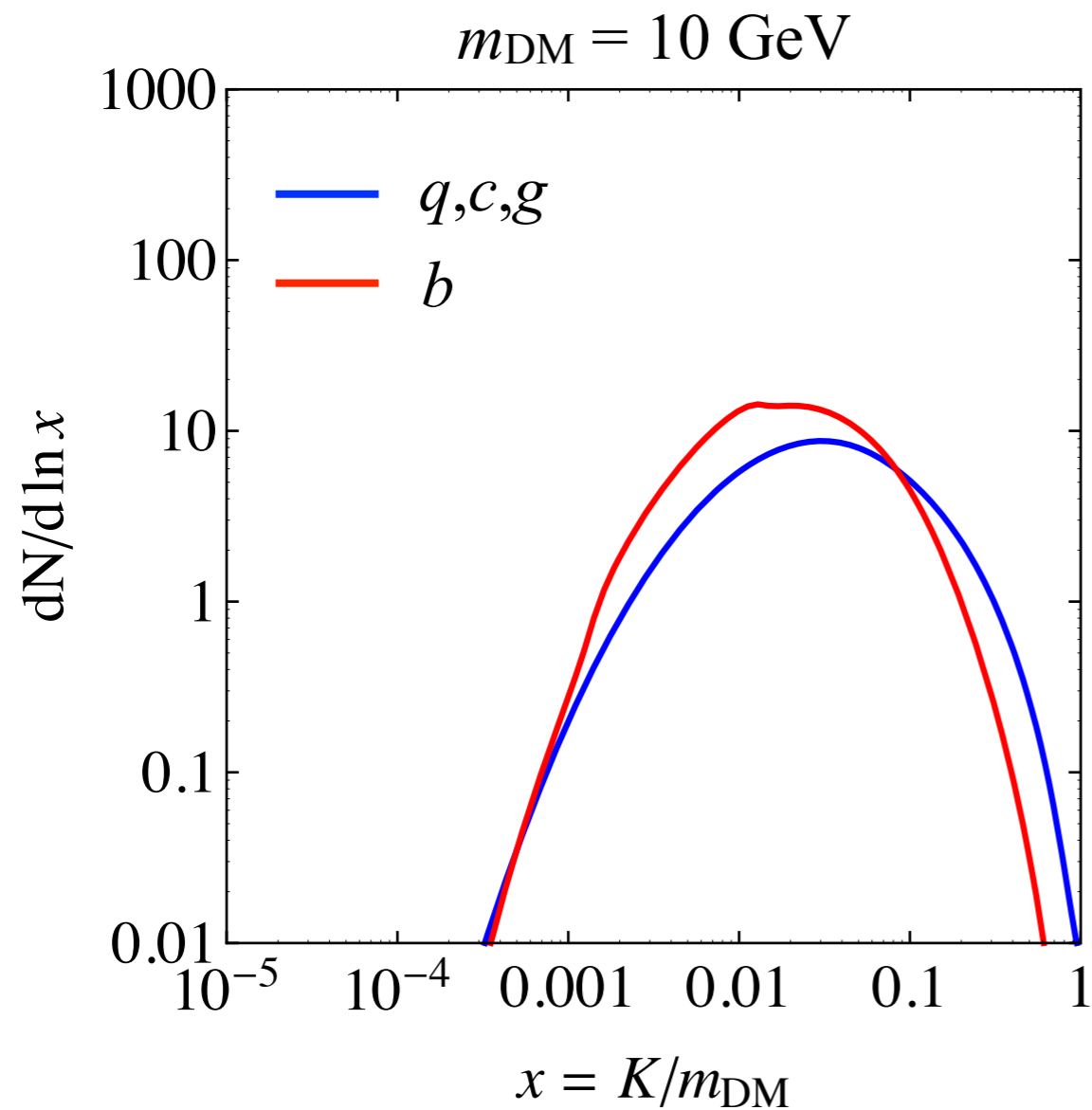
Due to m_q^2 terms annihilation to heaviest kinematically accessible quark dominates total annihilation rate

LHC vs. indirect detection



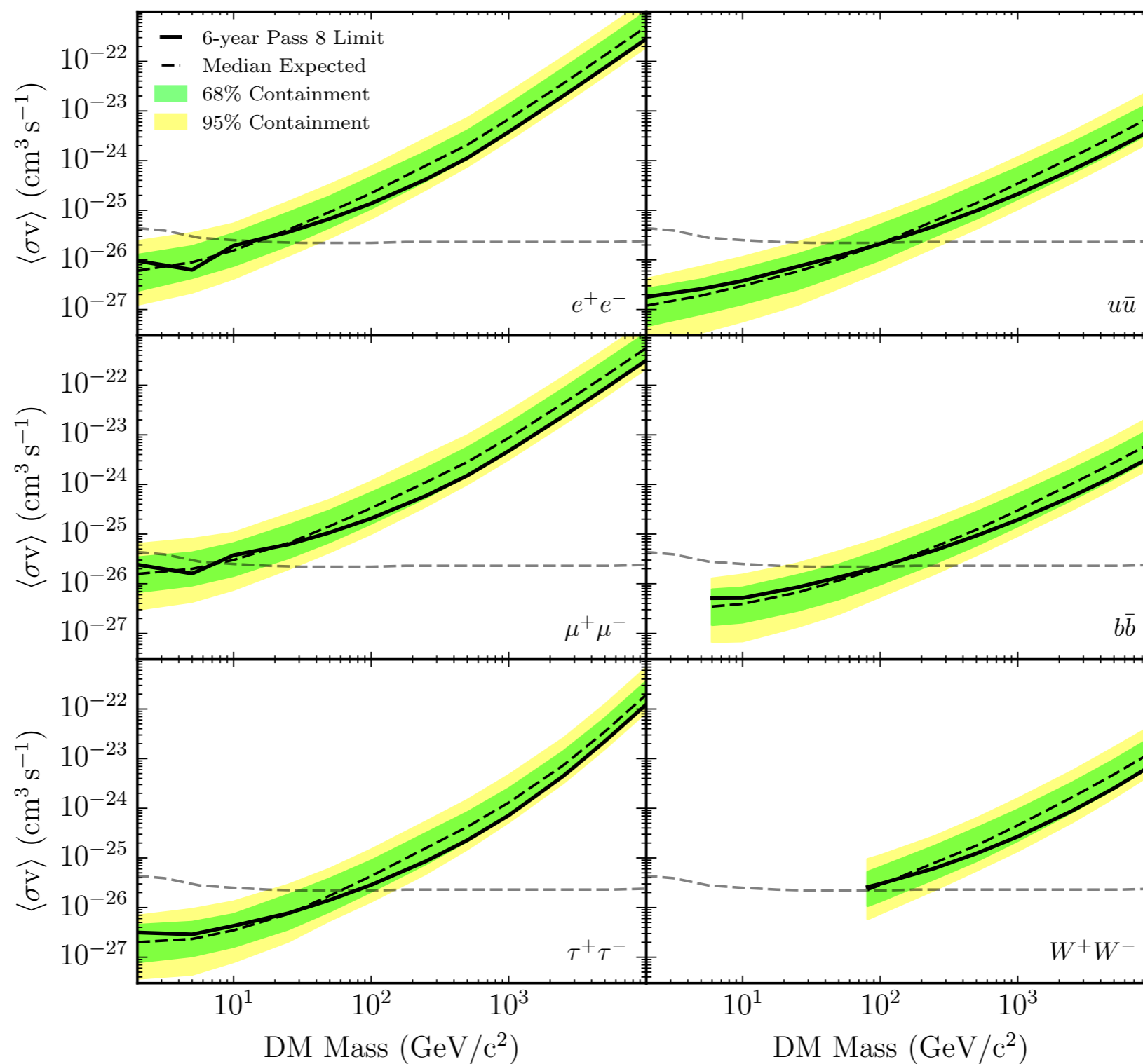
For pseudo-scalar mediator model nice complementarity between LHC mono-jet bound & indirect detection limit from Fermi-LAT

γ -ray spectra from DM annihilation



DM annihilation bounds from dwarfs

[Fermi-LAT, I503.0264I]



DM-N cross section: scalar case

$$\sigma_{\text{SI}} = \frac{f^2(g_q)g_{\text{DM}}^2\mu_{n\chi}^2}{\pi M_{\text{med}}^4}, \quad \mu_{n\chi} = \frac{m_n m_{\text{DM}}}{m_n + m_{\text{DM}}}, \quad m_n \simeq 0.939 \text{ GeV}$$

$$f(g_q) = 1.16 \cdot 10^{-3} g_q$$

$$\sigma_{\text{SI}} \simeq 6.9 \cdot 10^{-43} \text{ cm}^2 \left(\frac{g_q g_{\text{DM}}}{1} \right)^2 \left(\frac{125 \text{ GeV}}{M_{\text{med}}} \right)^4 \left(\frac{\mu_{n\chi}}{1 \text{ GeV}} \right)^2$$

† formula for $f(g_q)$ assumes universal couplings to quarks

DM-N cross section: axial-vector case

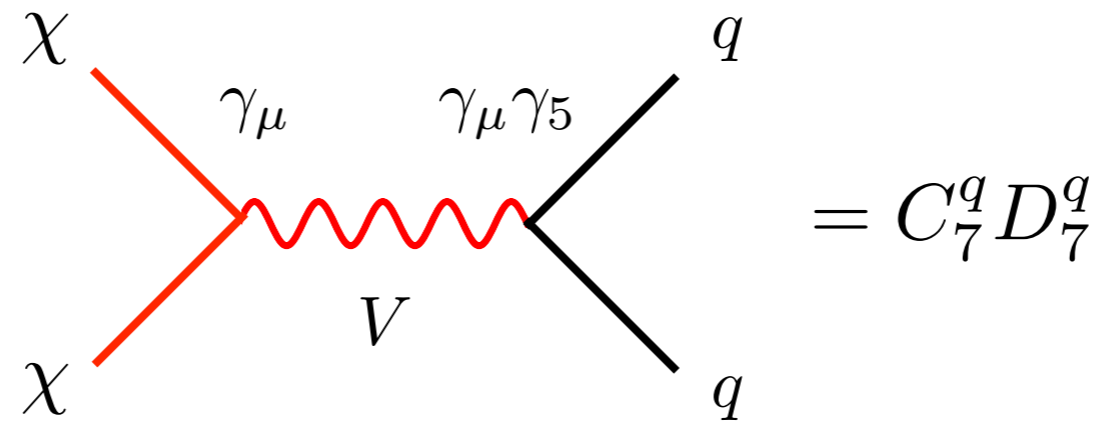
$$\sigma_{\text{SD}} = \frac{3f^2(g_q)g_{\text{DM}}^2\mu_{n\chi}^2}{\pi M_{\text{med}}^4}, \quad \mu_{n\chi} = \frac{m_n m_{\text{DM}}}{m_n + m_{\text{DM}}}, \quad m_n \simeq 0.939 \text{ GeV}$$

$$f(g_q) = 0.32 g_q$$

$$\sigma_{\text{SD}} \simeq 2.4 \cdot 10^{-42} \text{ cm}^2 \left(\frac{g_q g_{\text{DM}}}{0.25} \right)^2 \left(\frac{1 \text{ TeV}}{M_{\text{med}}} \right)^4 \left(\frac{\mu_{n\chi}}{1 \text{ GeV}} \right)^2$$

† formula for $f(g_q)$ assumes universal couplings to quarks

From suppressed to unsuppressed DD

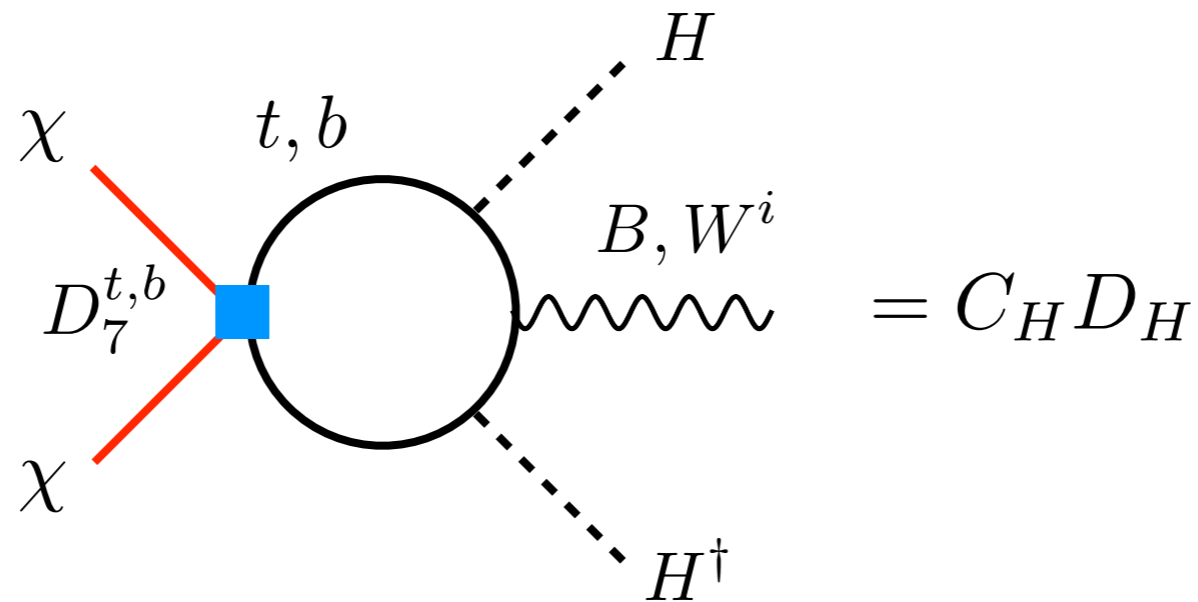


$$C_7^q = -\frac{g_\chi g_q}{M_V^2}, \quad D_7^q = \bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu \gamma_5 q$$

operator leads to SD χ -N interactions
that are both v^2 & q^2 suppressed

From suppressed to unsuppressed DD

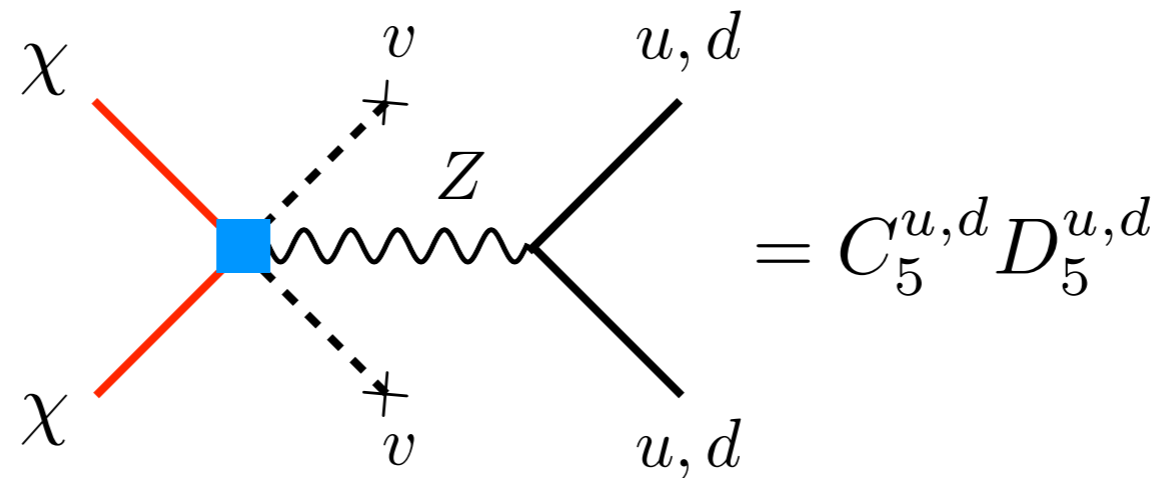
[Crivellin et al. 1402.1173]



$$C_H = - \sum_{q=t,b} \frac{3y_q^2 T_3^q C_7^q}{2\pi^2} \ln \left(\frac{v}{M_V} \right), \quad D_H = \bar{\chi} \gamma^\mu \chi (H^\dagger i \overleftrightarrow{D}_\mu H)$$

From suppressed to unsuppressed DD

[Crivellin et al. 1402.1173]



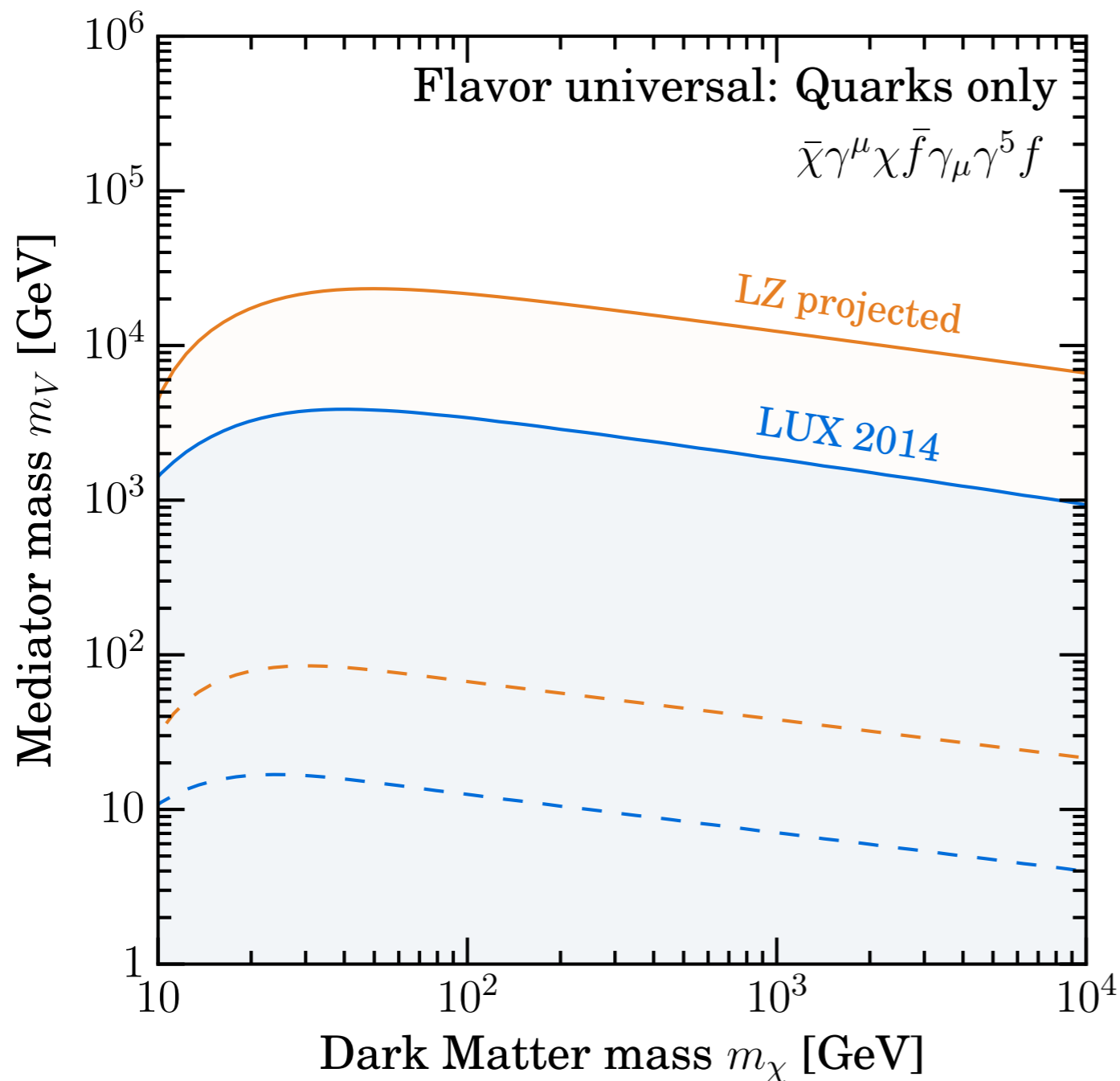
$$C_5^q = \frac{g_\chi}{M_V^2} (T_3^q - 2Q_q s_w^2) \sum_{p=t,b} \frac{3y_p^2 g_p T_3^p}{2\pi^2} \ln \left(\frac{v}{M_V} \right), \quad D_5^q = \bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu q$$



operator leads to SI χ -N interactions

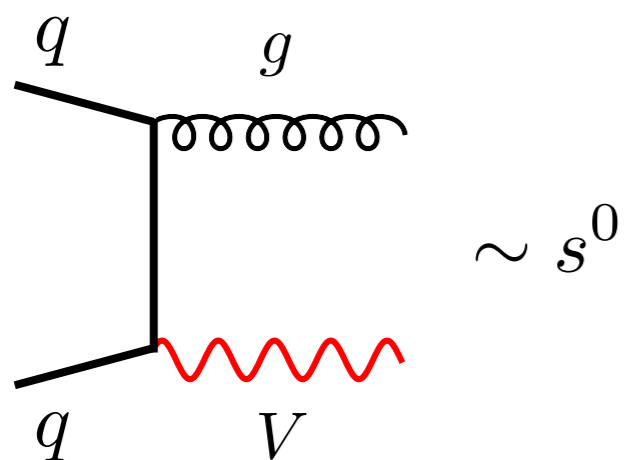
From suppressed to unsuppressed DD

[D'Eramo et al., 1605.04917]

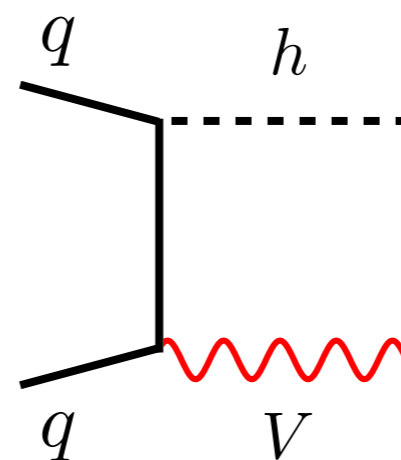


Loop suppression by far overcompensated by coherence enhancement of SI χ -N interactions

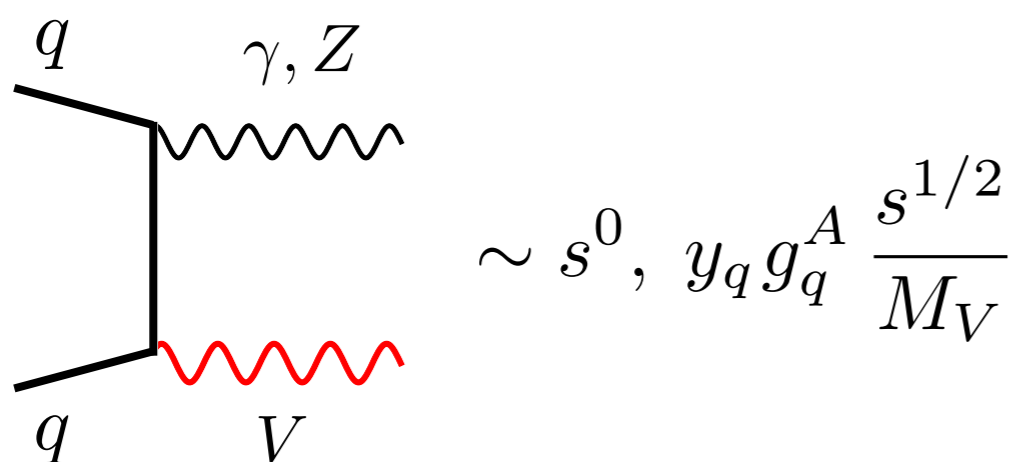
Spin-1 mono-X amplitudes



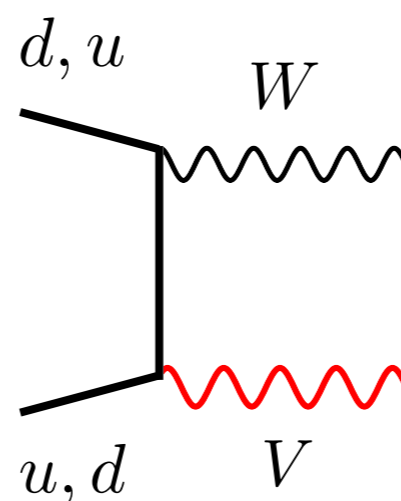
$$\sim s^0$$



$$\sim y_q g_q^A \frac{s^{1/2}}{M_V}$$

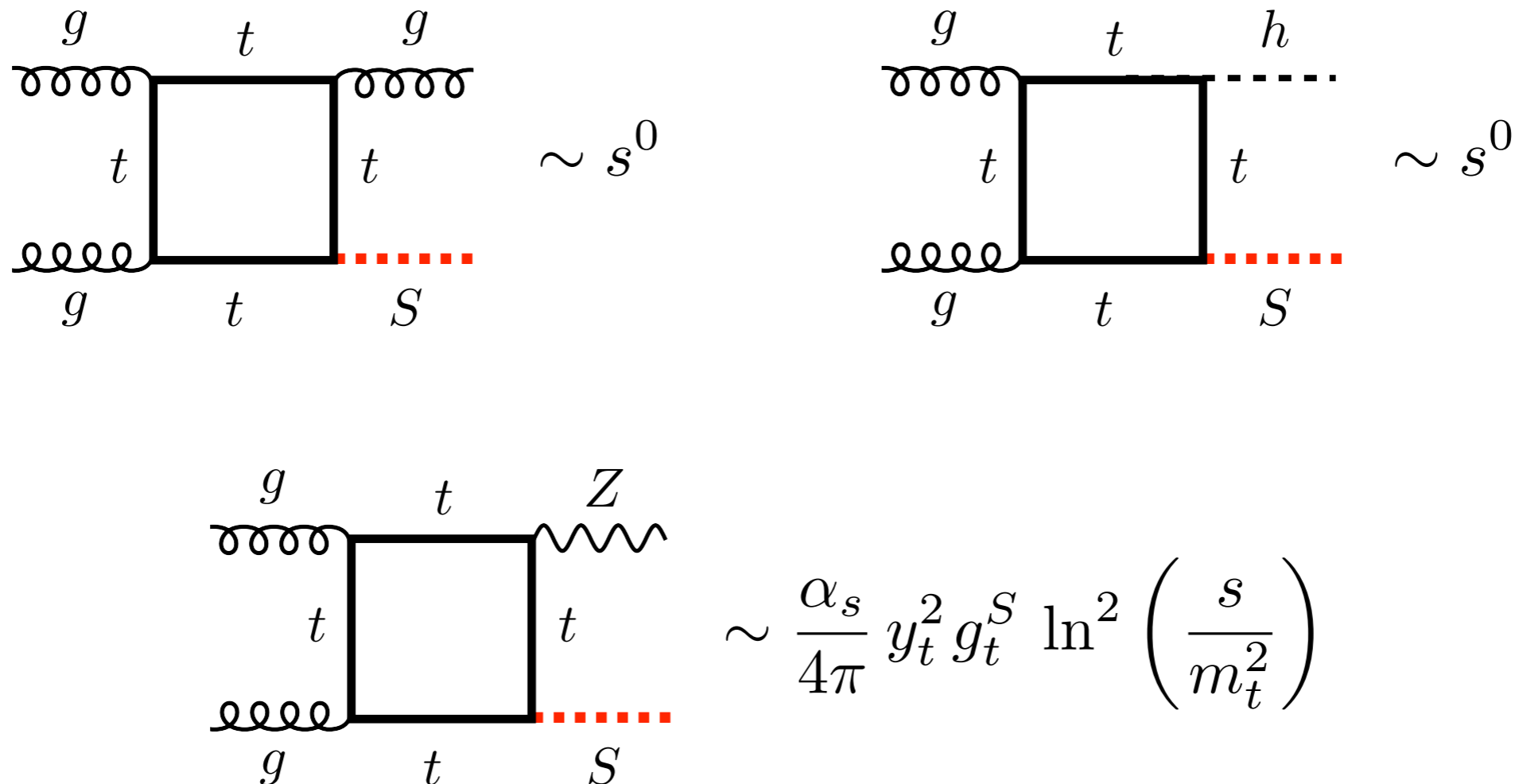


$$\sim s^0, y_q g_q^A \frac{s^{1/2}}{M_V}$$



$$\sim (g_u^L - g_d^L) \frac{s}{M_W M_V}$$

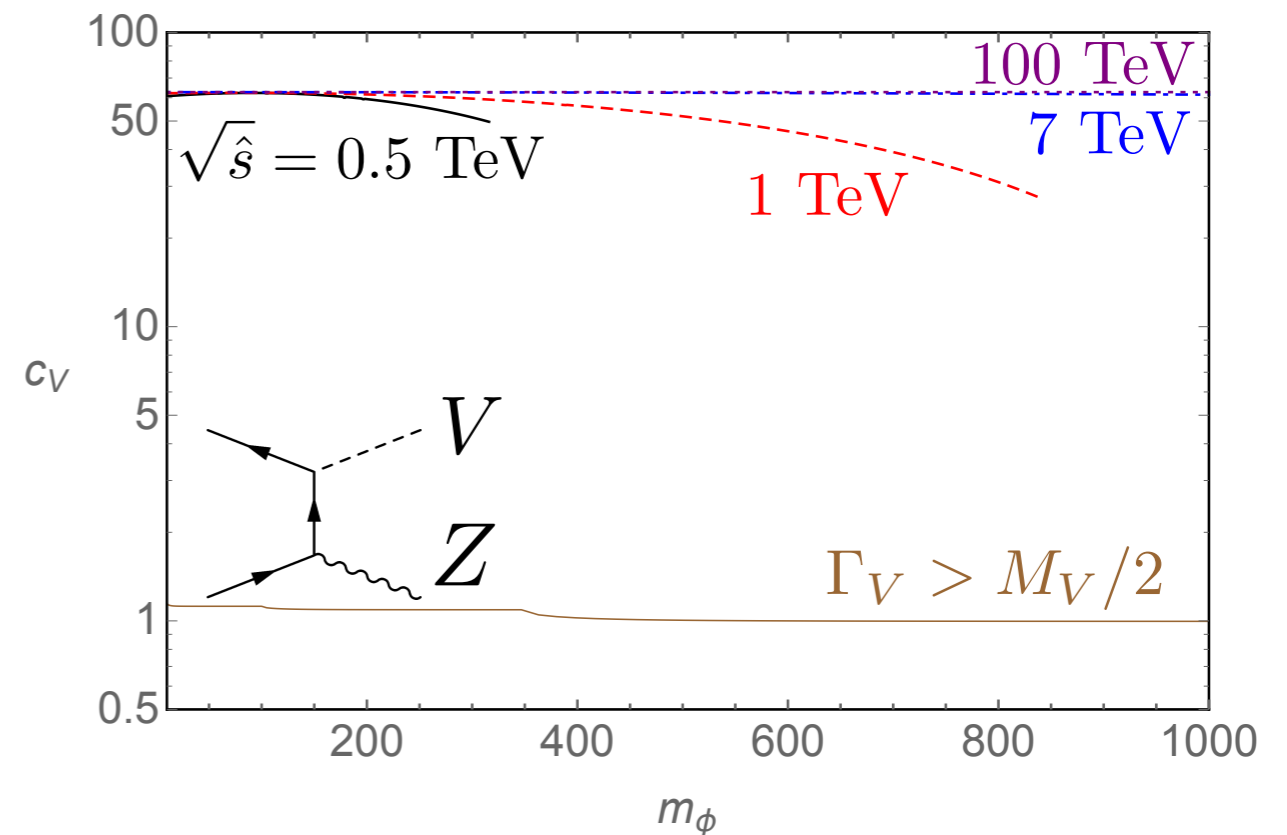
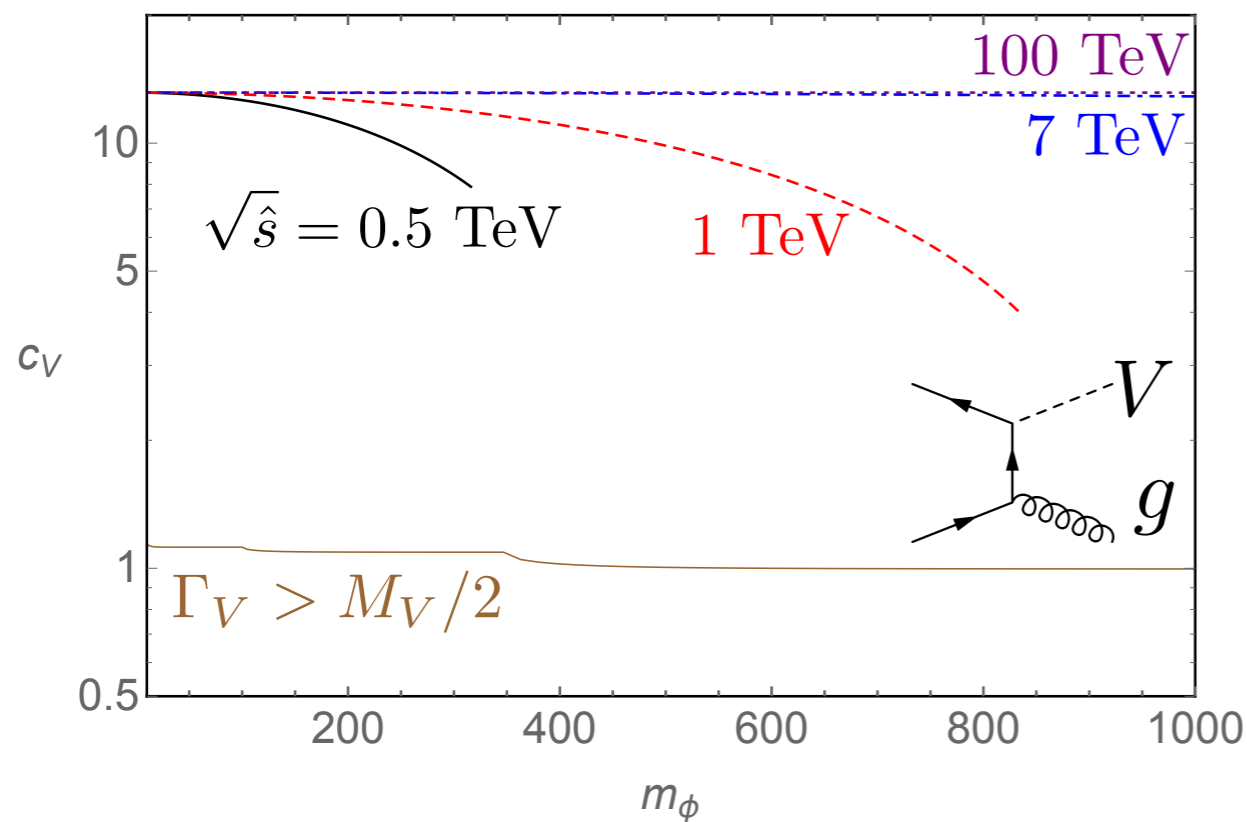
Spin-0 mono-X amplitudes



1-loop $gg \rightarrow Z+S$ amplitude diverges for $s \rightarrow \infty$. Naively, numerical effect small unless coupling g_t^S large & centre-of-mass energy $s^{1/2} \gg 13 \text{ TeV}$

Unitarity: $E_{T,\text{miss}+\text{jet}}$, Z , h searches

[Englert et al., 1604.07975]

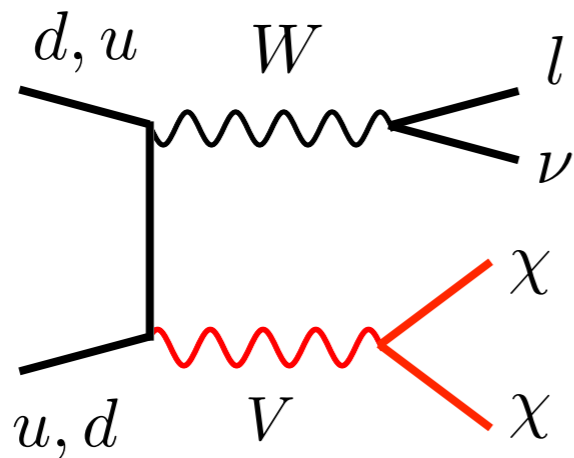


$E_{T,\text{miss}+\text{jet}}$, Z , h amplitudes in spin-1 models have no problem with unitarity at LHC energies & beyond unless DM-mediator couplings are non-perturbative†

†For such couplings, one always has $\Gamma_V > M_V$ & simple particle description breaks down

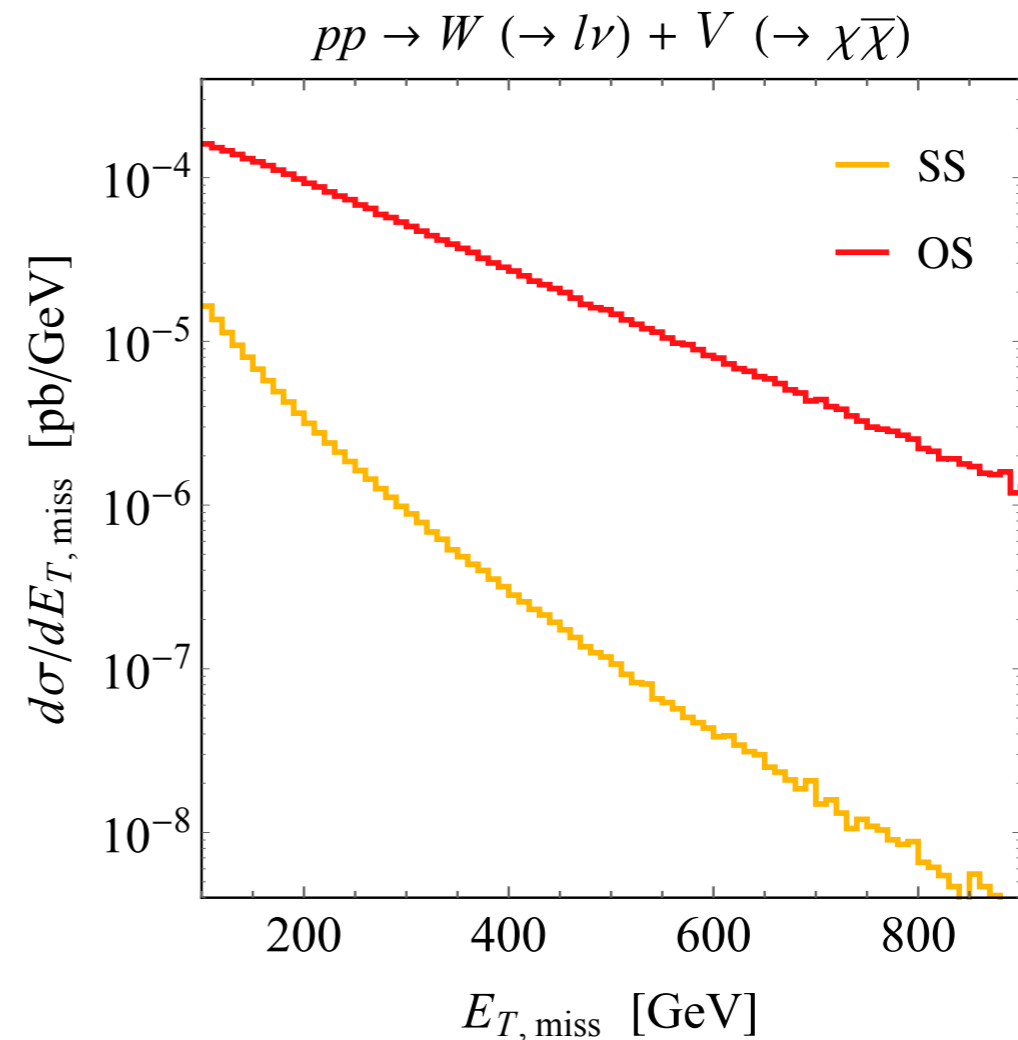
$E_{T,miss}$ spectra in mono- W sample

[UH et al., 1603.01267]



same-sign (SS): $g_u = g_d$

opposite-sign (OS): $g_u = -g_d$

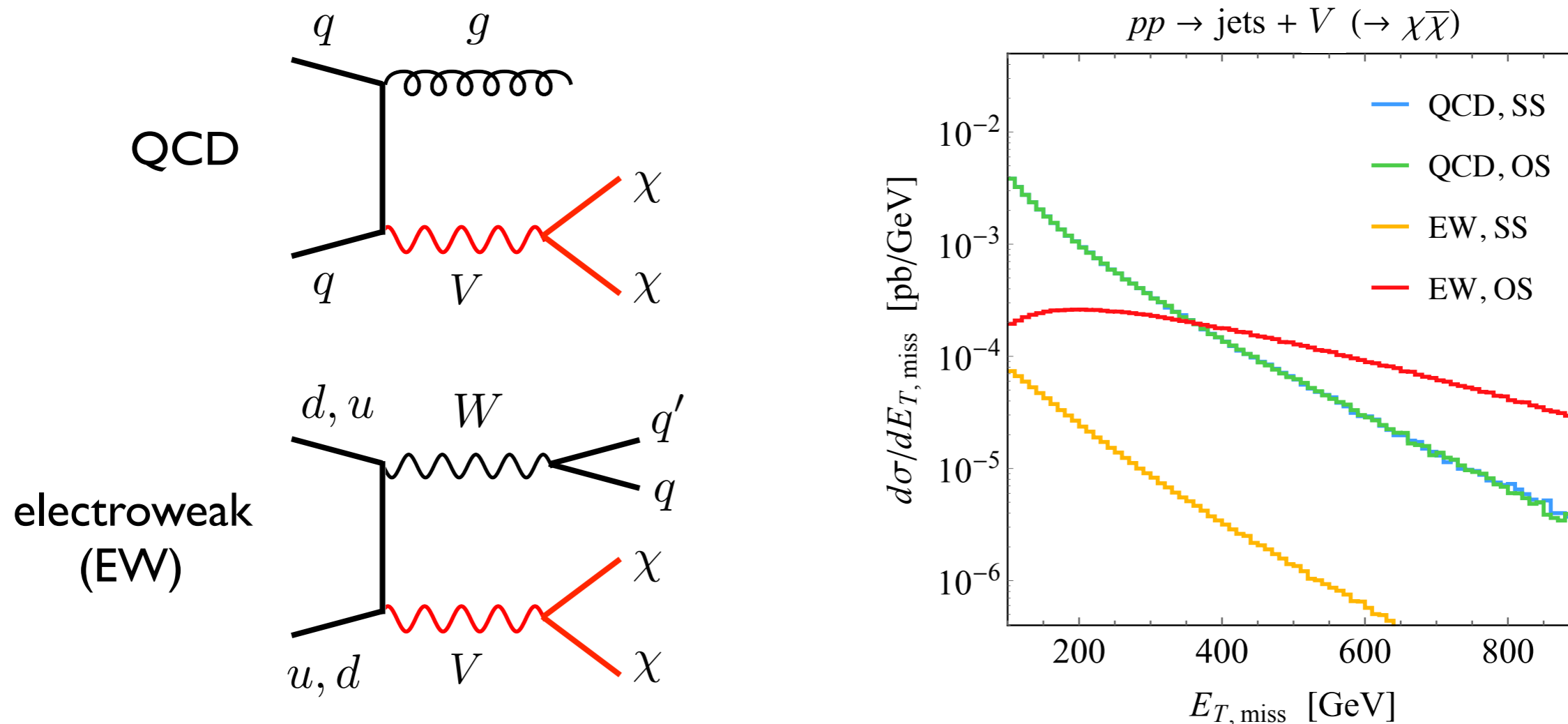


For OS couplings $E_{T,miss}$ spectrum significantly harder than in SS case. This is an artefact of unitarity violation & thus unphysical

[see also Bell et al., 1503.07874, 1512.00476]

$E_{T,miss}$ spectra in mono-jet sample

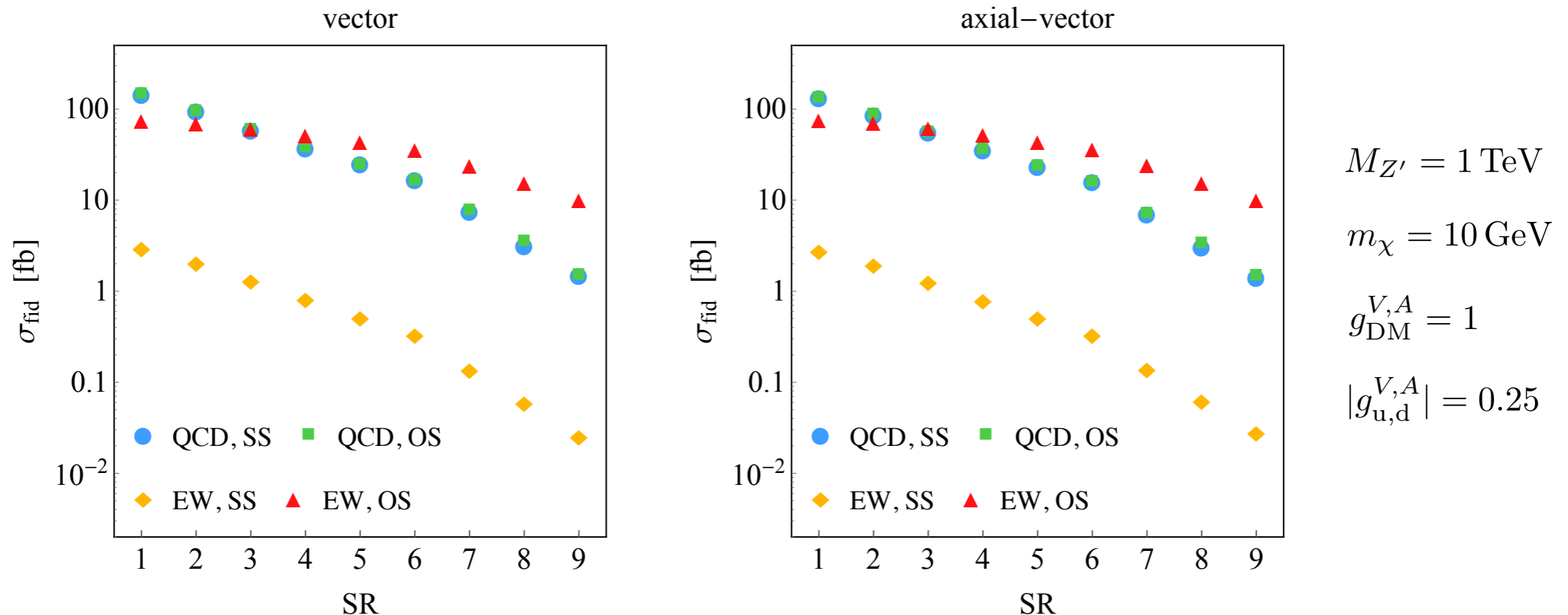
[UH et al., 1603.01267]



In fact, EW channel $pp \rightarrow W(\rightarrow q\bar{q}') + V(\rightarrow \chi\bar{\chi})$ even produces harder mono-jet events than QCD process $pp \rightarrow \text{jets} + V(\rightarrow \chi\bar{\chi})$

Mono-W problem in mono-jets

[UH et al., I603.01267]



Unitarity problem persists after parton shower, hadronisation corrections & detector effects. As a result, EW contribution gives rise to majority of events in high- $E_{T,\text{miss}}$ signal regions (SRs) of mono-jet searches[†] in OS case

[†]Plots show SRs as defined in ATLAS, I502.01518

Mono-W problem: solution I

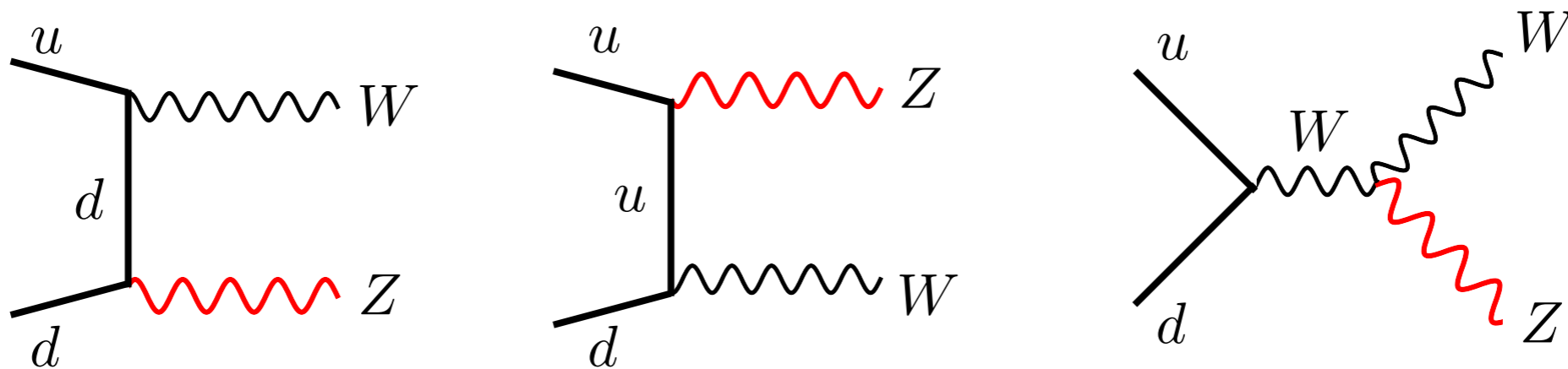
Since s-behaviour of $ud \rightarrow W+V$ amplitude proportional to $g_u^L - g_d^L$
 tree-level unitarity recovered for $g_Q = g_d^L = g_u^L$. Latter requirement
 automatically fulfilled, if quark couplings to V are written in a way
 that preserves EW symmetry:

$$\mathcal{L}_{Vq\bar{q}} = - \sum_{u,d} V_\mu (g_Q \bar{Q}_L \gamma^\mu Q_L + g_u \bar{u}_R \gamma^\mu u_R + g_d \bar{d}_R \gamma^\mu d_R)$$

$$Q_L = (u_L, d_L)^T$$

Mono-W problem: solution 2

Second solution obtained by thinking about how unitarity of $ud \rightarrow W+Z$ amplitude is realised within SM:



$$|\mathcal{M}|^2 = \frac{3g^4 c_w^2 |V_{ud}|^2}{32M_W^2} (d_1 + d_2 - 2d_3) s^2 \sin^2 \theta$$

Diagram with WWZ coupling cancels divergent s -behaviour of graphs with t -channel quark exchange. This is a result of gauge invariance

Mono-W problem: solution 2

SM result implies that even if

$$\Delta g = g_u^L - g_d^L \neq 0$$

unitarity violation avoided by adding following gauge-boson couplings to Lagrangian:

$$\Delta \mathcal{L} = i \Delta g \left\{ (\partial_\mu W_\nu^+ - \partial_\nu W_\mu^+) W^{\mu-} V^\nu - (\partial_\mu W_\nu^- - \partial_\nu W_\mu^-) W^{\mu+} V^\nu + \frac{1}{2} (\partial_\mu V_\nu - \partial_\nu V_\mu) (W^{\mu+} W^{\nu-} - W^{\mu-} W^{\nu+}) \right\}$$

Mono-W problem: solution 2

In fact, if V arises through mixing with a new vector field X , that is

$$X_\mu = N_{31} A_\mu + N_{32} Z_\mu + N_{33} V_\mu$$

& X has quark couplings of form

$$\mathcal{L}_{Xq\bar{X}} = - \sum_q X_\mu \bar{q} (f_q^V \gamma^\mu + f_q^A \gamma^\mu \gamma_5) q, \quad f_u^L \ominus f_d^L = 0$$

then relevant V couplings automatically obey

$$\Delta g = g_u^L \ominus g_d^L = g N_{23}, \quad g_{WWV} = g N_{23}$$

& modified theory unitary

Mono-W problem: solution 3

Quark-couplings of V can also be realised via dimension-6 operators:

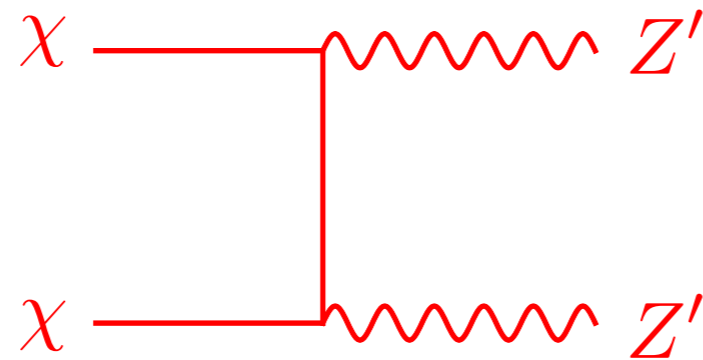
$$\mathcal{L}_{VQH} = - \sum_{u,d} V_\mu \left\{ \frac{1}{\Lambda_u^2} (\bar{Q}_L \tilde{H}) \gamma^\mu (\tilde{H}^\dagger Q_L) + \frac{1}{\Lambda_d^2} (\bar{Q}_L H) \gamma^\mu (H^\dagger Q_L) \right\}$$

In such a case $SU(2)_L$ breaking is however not $O(1)$, but given by†

$$\Delta g = g_u^L - g_d^L = \frac{v^2}{\Lambda^2}$$

In this model unitary at 13 TeV LHC requires either $|g_u^{V,A}| = |g_d^{V,A}| < 0.05$ or if $|g_u^{V,A}| = |g_d^{V,A}| = 0.25$ & $M_V = 1$ TeV is chosen, one has to employ truncation with $s^{1/2} \lesssim 6$ TeV. Both options reduce mono-W sensitivity

Unitarity violation: $\chi\bar{\chi} \rightarrow Z'Z'$



$$\sim g_{\chi}^A \frac{m_{\chi}}{M_{Z'}^2} s^{1/2}$$

$$s^{1/2} < \frac{\pi M_{Z'}^2}{(g_{\chi}^A)^2 m_{\chi}} \simeq \begin{cases} 5 \text{ TeV}, & g_{\chi}^A = 0.25, M_{Z'} = 1 \text{ TeV}, m_{\chi} = 10 \text{ GeV} \\ 0.5 \text{ TeV}, & g_{\chi}^A = 0.25, M_{Z'} = 1 \text{ TeV}, m_{\chi} = 100 \text{ GeV} \end{cases}$$

For $m_{\chi} = 10$ (100) GeV, new physics must appear before 5 (0.5) TeV to restore unitarity in DM annihilation to Z' pairs

Dark Higgs sector

Simplest way to restore unitarity is to generate mediator mass by Higgsing $U(1)'$ symmetry. Assuming that DM is Majorana particle (to avoid strong DD constraints due to vector coupling), one can write

$$\mathcal{L}_{\text{DM}} = \frac{i}{2} \bar{\psi} \not{\partial} \psi - \frac{1}{2} g_{\text{DM}}^A Z'^{\mu} \bar{\psi} \gamma_{\mu} \gamma_5 \psi - \frac{1}{2} y_{\text{DM}} \bar{\psi} (P_L S + P_R S^*) \psi$$

$$\mathcal{L}_S = \{(\partial^{\mu} + ig_S Z'^{\mu})S\}^{\dagger} \{(\partial_{\mu} + ig_S Z'_{\mu})S\} + \mu_s^2 S^{\dagger} S - \lambda_s (S^{\dagger} S)^2$$

Once S acquires vacuum expectation value (VEV) w , ψ & Z' get massive

$$m_{\text{DM}} = \frac{y_{\text{DM}} w}{\sqrt{2}}, \quad M_{Z'} \simeq 2g_{\text{DM}}^A w$$

Z' interactions

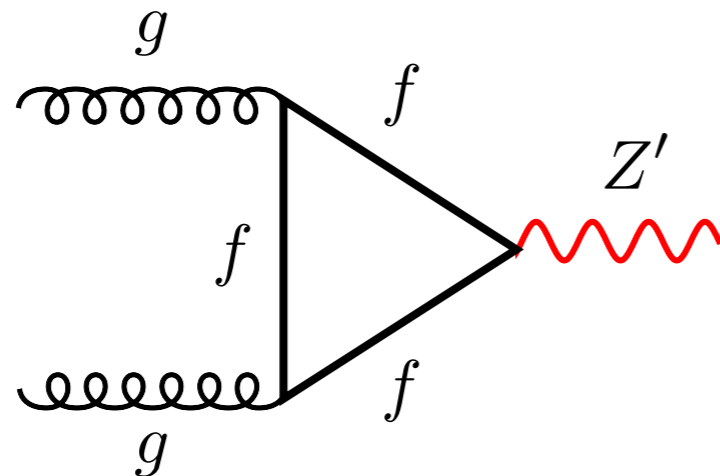
Interactions between SM states & Z' gauge boson can be written as

$$\begin{aligned} \mathcal{L}'_{\text{SM}} = & \left\{ (D^\mu H)^\dagger (-i g' q_H Z'_\mu H) + \text{h.c.} \right\} + g'^2 q_H^2 Z'^\mu Z'_\mu H^\dagger H \\ & - \sum_{f=q,\ell,\nu} g' Z'^\mu (\bar{q}_{fL} \bar{f}_L \gamma_\mu f_L + \bar{q}_{fR} \bar{f}_R \gamma_\mu f_R) \end{aligned}$$

Gauge invariance of SM Yukawa couplings requires that charges q are generation universal & must satisfy consistency conditions (CCs):

$$q_H = q_{qL} - q_{uR} = q_{dR} - q_{qL} = q_{eR} - q_{\ell L}$$

Implications of CCs



The diagram shows a triangle loop of fermions f . Two external gluon lines (g) enter from the left, and a Z' boson line exits to the right. The fermion lines are labeled f . The Z' boson line is shown as a red wavy line.

$$\sim 3 (2q_{q_L} - q_{u_R} - q_{d_R})$$

For arbitrary charge assignments consistent with CCs, theory will have anomalies, but new fermions F do not need to be coloured since ggZ' anomaly vanishes automatically. This is a nice feature because masses of new fermions bounded by unitarity:

$$m_F < \sqrt{\frac{\pi}{2}} \frac{M_{Z'}}{g_F^A}$$

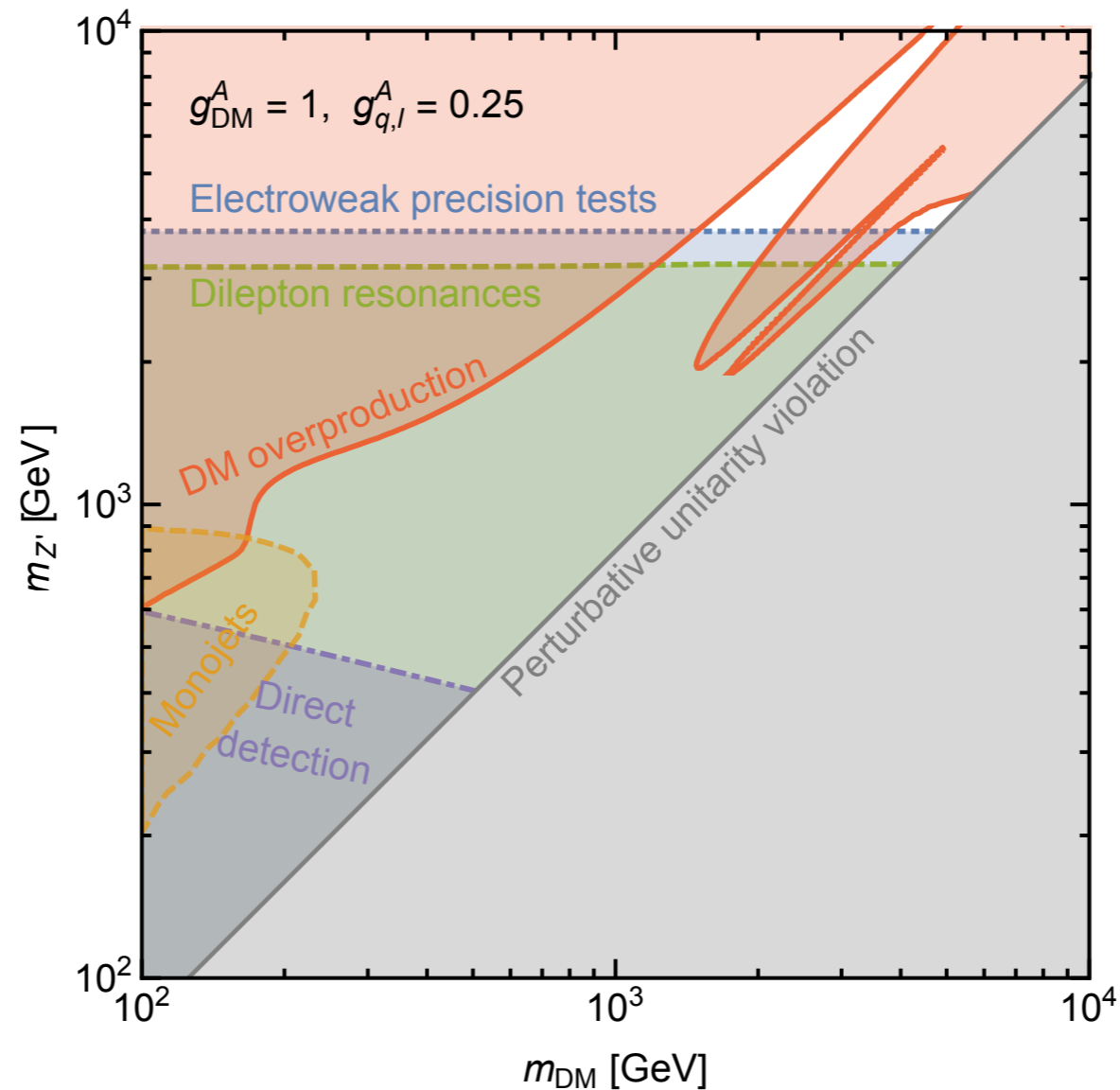
Implications of CCs

CCs also imply that for non-zero axialvector couplings to SM fermions, SM Higgs must carry $U(1)'$ charge. This has two important consequences:

- Z' must couple with same strength to quarks & leptons (assuming one Higgs doublet), resulting in stringent constraints from di-lepton resonance searches
- VEV of SM Higgs leads to $Z-Z'$ mixing, which is severely constrained by EW precision observables (EWPOs)

Axialvector Z' : constraints

[Kahlhoefer et al., 1510.02110]



In simplest UV completion of axialvector model, constraints from mono-jet & di-jet searches & DD not competitive with di-lepton searches & EWPOs

Structure of spin-0 simplified model

Since left- & right-handed SM fermions have different quantum numbers, interaction of form

$$\mathcal{L}_S \supset \sum_q \frac{g_q y_q}{\sqrt{2}} \bar{q} q S = \sum_q \frac{g_q y_q}{\sqrt{2}} (\bar{q}_L q_R + \bar{q}_R q_L) S$$

not $SU(2)_L \times U(1)_Y$ gauge invariant

Given that S is a SM singlet, terms like

$$S|H|^2, S^2|H|^2, S^3, S^4$$

not forbidden by EW symmetry. Why are such couplings not included?

Fermion singlet DM

In fact, by adding

$$\mathcal{L}_s \supset y_\chi \bar{\chi} \chi s + \mu s |H|^2$$

to SM Lagrangian both issues can be addressed

As a result of portal coupling μ , SM Higgs h & singlet s mix, giving rise to mass eigenstates $h_{1,2}$:

$$\begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h \\ s \end{pmatrix}, \quad \tan(2\theta) = \frac{2v\mu}{M_s^2 - M_h^2}$$

For small $\theta \ll 1$, h_1 (h_2) SM Higgs-like (singlet-like)

[Kim et al., 0803.2932; Baek et al., 1112.1847; Lopez-Honorez et al., 1203.2064; Fairbairn & Hogan, 1305.3452; ...]

Fermion singlet DM: vertices

$$\begin{array}{l}
 q \\
 \diagdown \\
 \{h_1, h_2\} \\
 \diagup \\
 q
 \end{array}
 = \frac{y_q}{\sqrt{2}} \{\cos \theta, -\sin \theta\}
 \qquad
 \begin{array}{l}
 W, Z \\
 \diagdown \\
 \{h_1, h_2\} \\
 \diagup \\
 W, Z
 \end{array}
 = M_{W,Z} \{\cos \theta, -\sin \theta\}$$

$$\begin{array}{l}
 \{h_1, h_2\} \\
 \diagdown \\
 \diagup \\
 \chi \\
 \chi
 \end{array}
 = y_\chi \{\sin \theta, \cos \theta\}$$

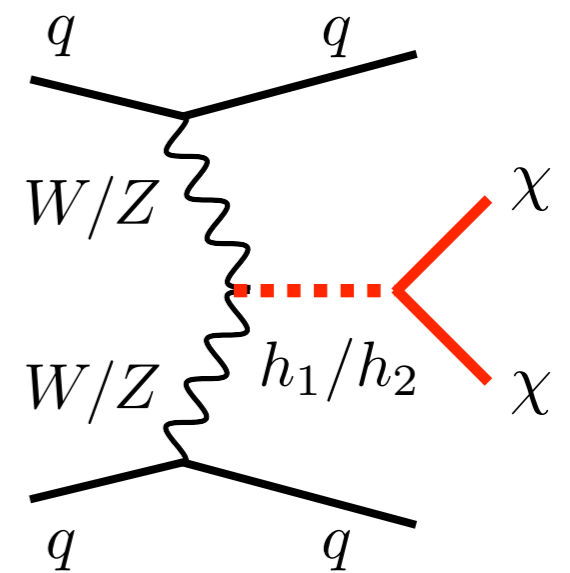
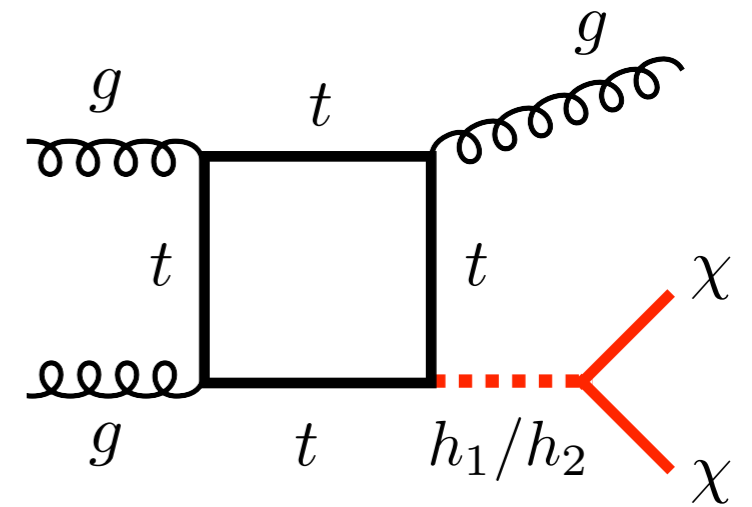
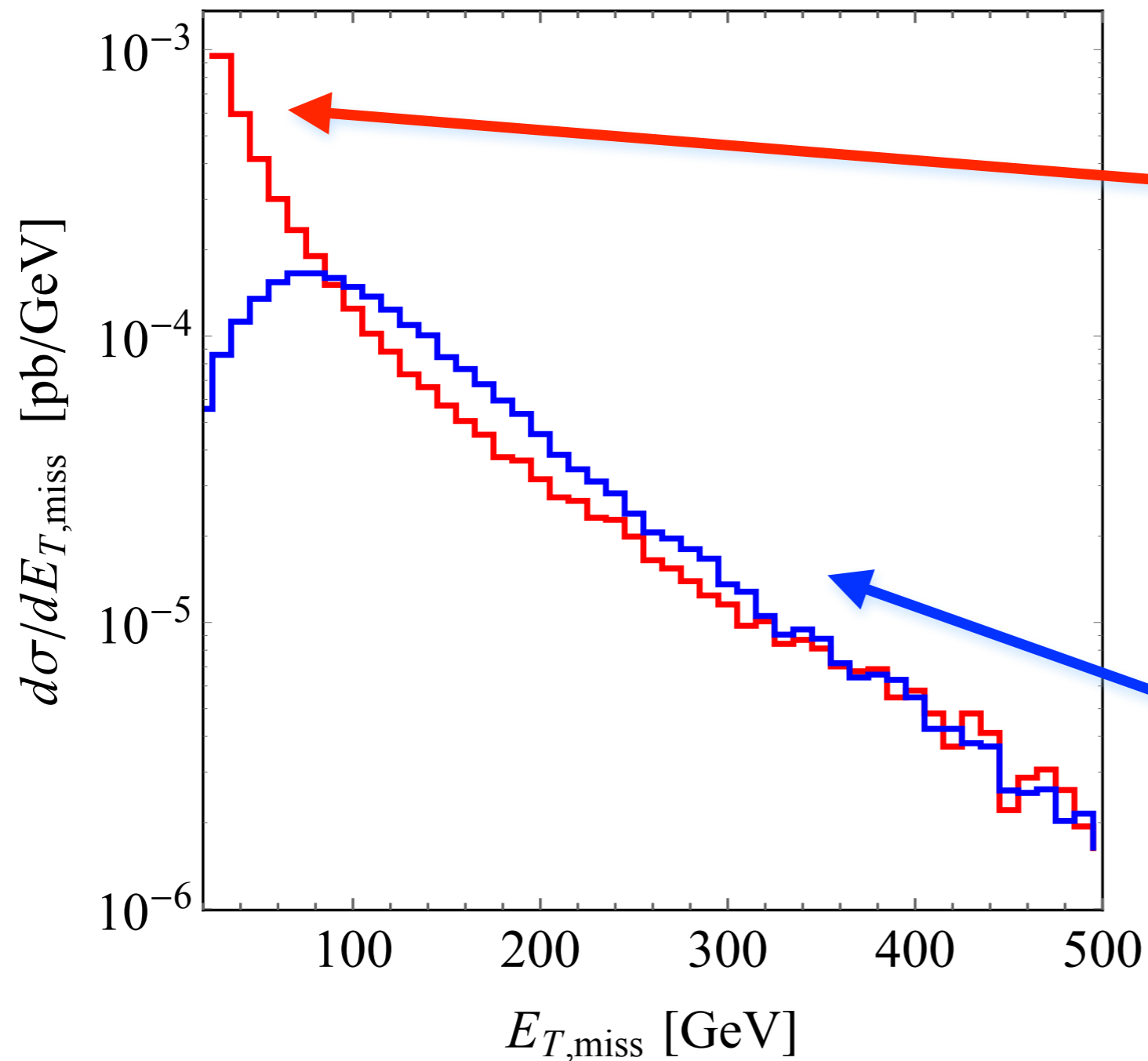
Fermion singlet DM: signatures

Compared to spin-0 simplified model LHC phenomenology is richer in fermion singlet DM scenario:

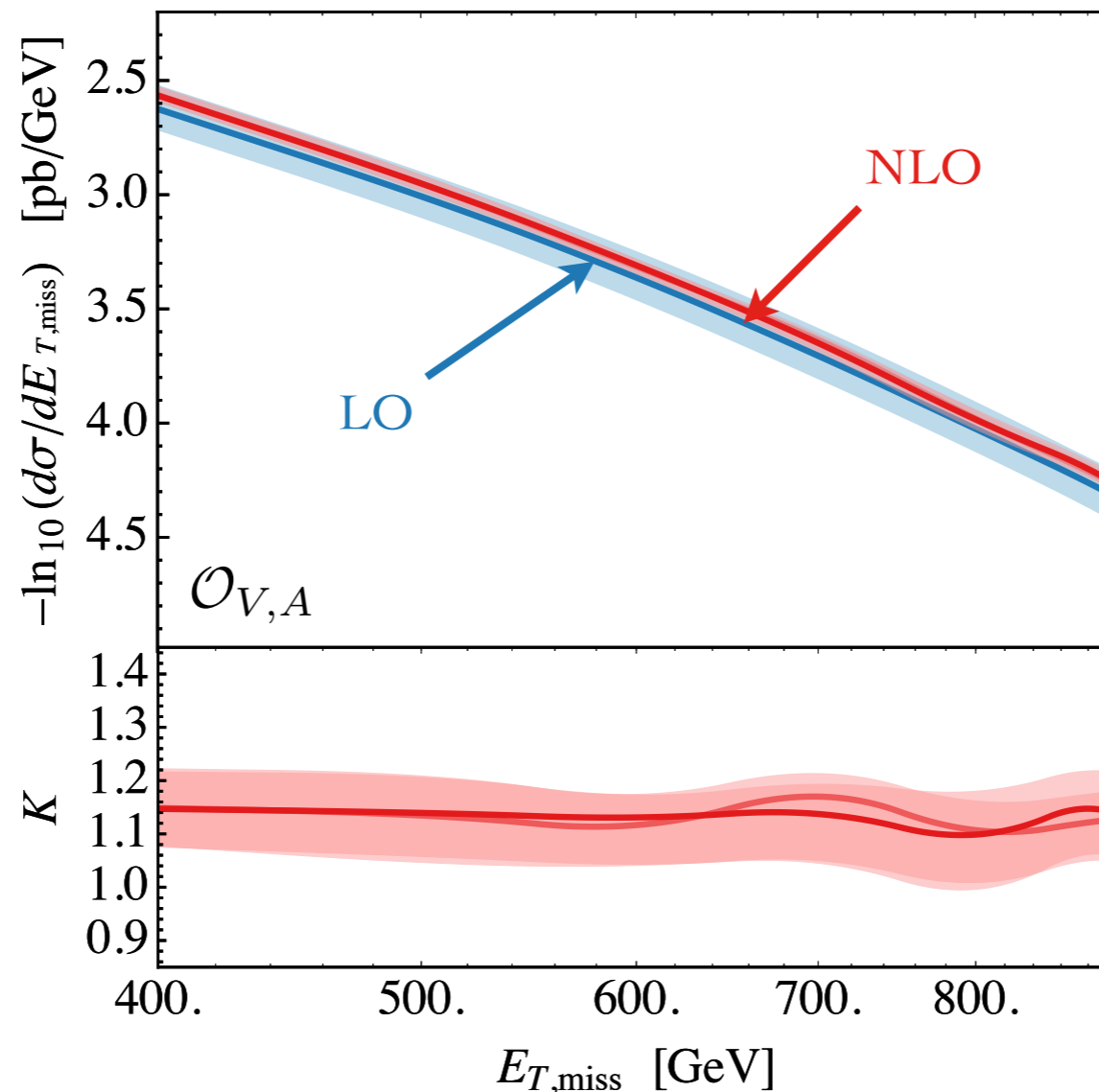
- (i) universal suppression of SM Higgs couplings by $\cos\Theta$ — LHC Run I data requires already $\sin\Theta \lesssim 0.4$
- (ii) new SM Higgs decay modes $h_1 \rightarrow \chi\bar{\chi}$ & $h_1 \rightarrow h_2 h_2$ if kinematically allowed
- (iii) $E_{T,\text{miss}}$ cross sections are changed & new signatures like $W/Z + E_{T,\text{miss}}$ & $\text{VBF} + E_{T,\text{miss}}$ arise — $E_{T,\text{miss}}$ processes involving EW bosons cannot be described consistently in spin-0 simplified model

Mono-jet vs. $W/Z, \text{VBF} + E_{T,\text{miss}}$ signal

$$M_{h_2} = 1 \text{ TeV}, m_\chi = 100 \text{ GeV}, \sin\theta = 0.1$$



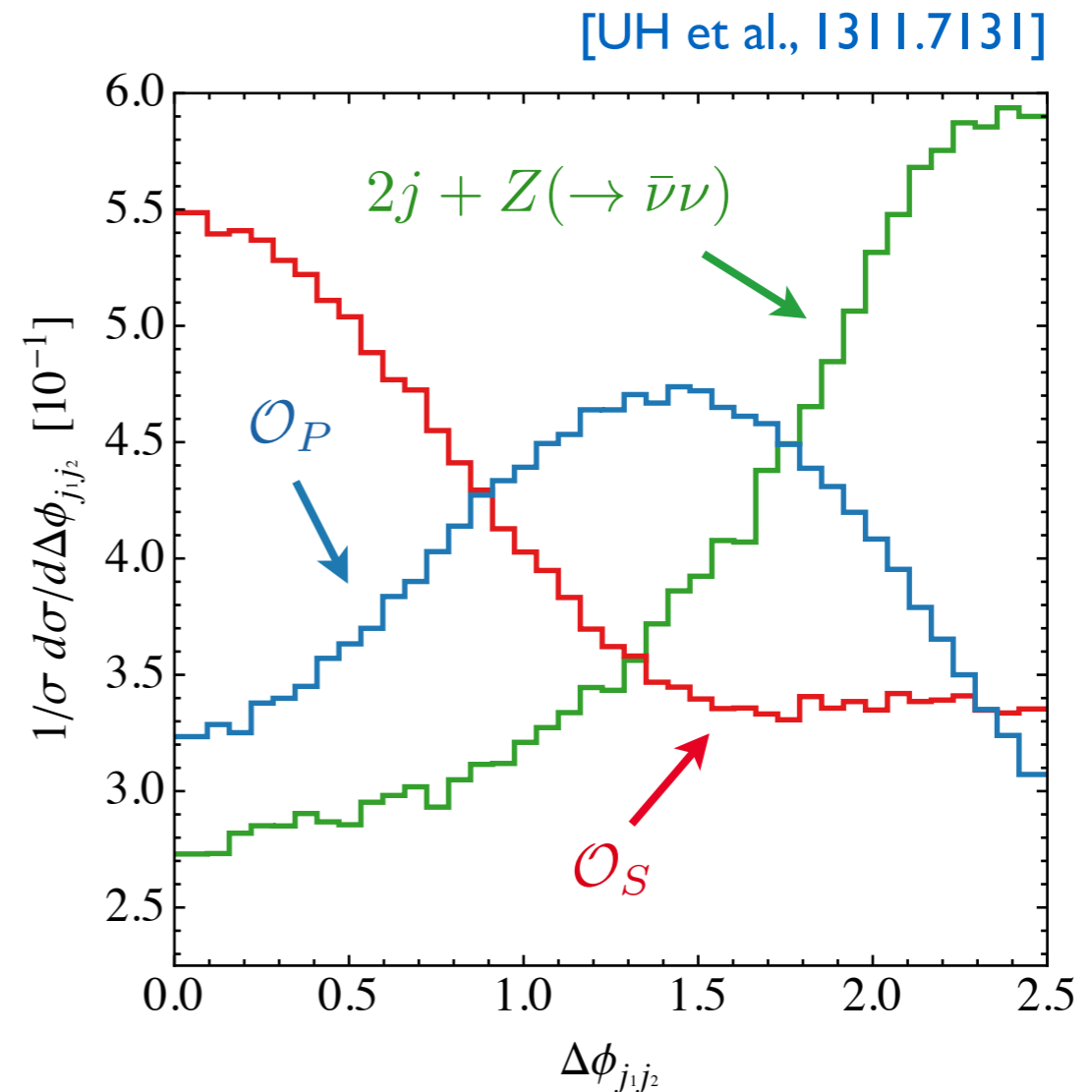
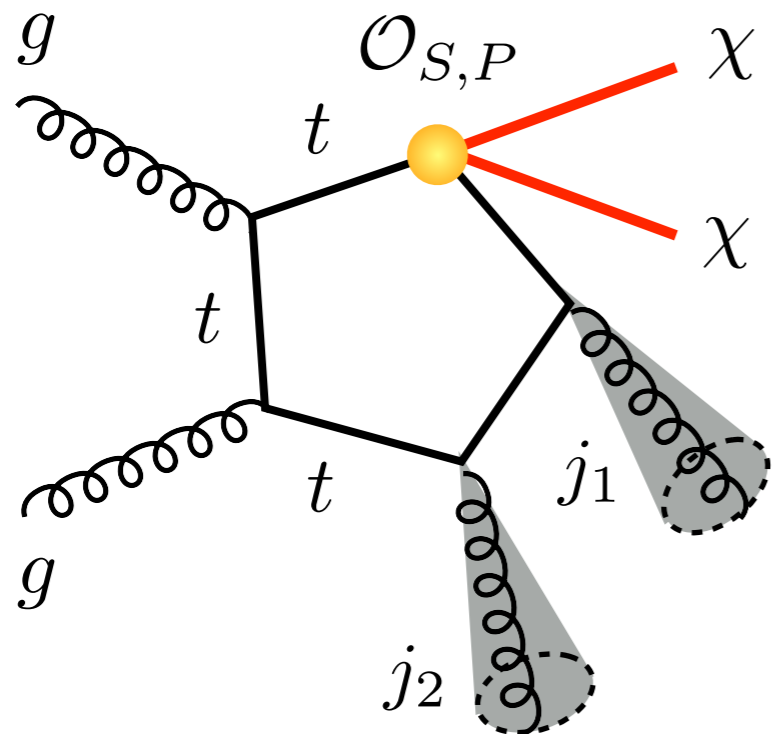
Properties beyond mass scale?



$E_{T,\text{miss}}$ & $p_{T,j1}$ spectra for vector & axialvector operators identical.

Mono-jet searches not sensitive to chirality of interactions

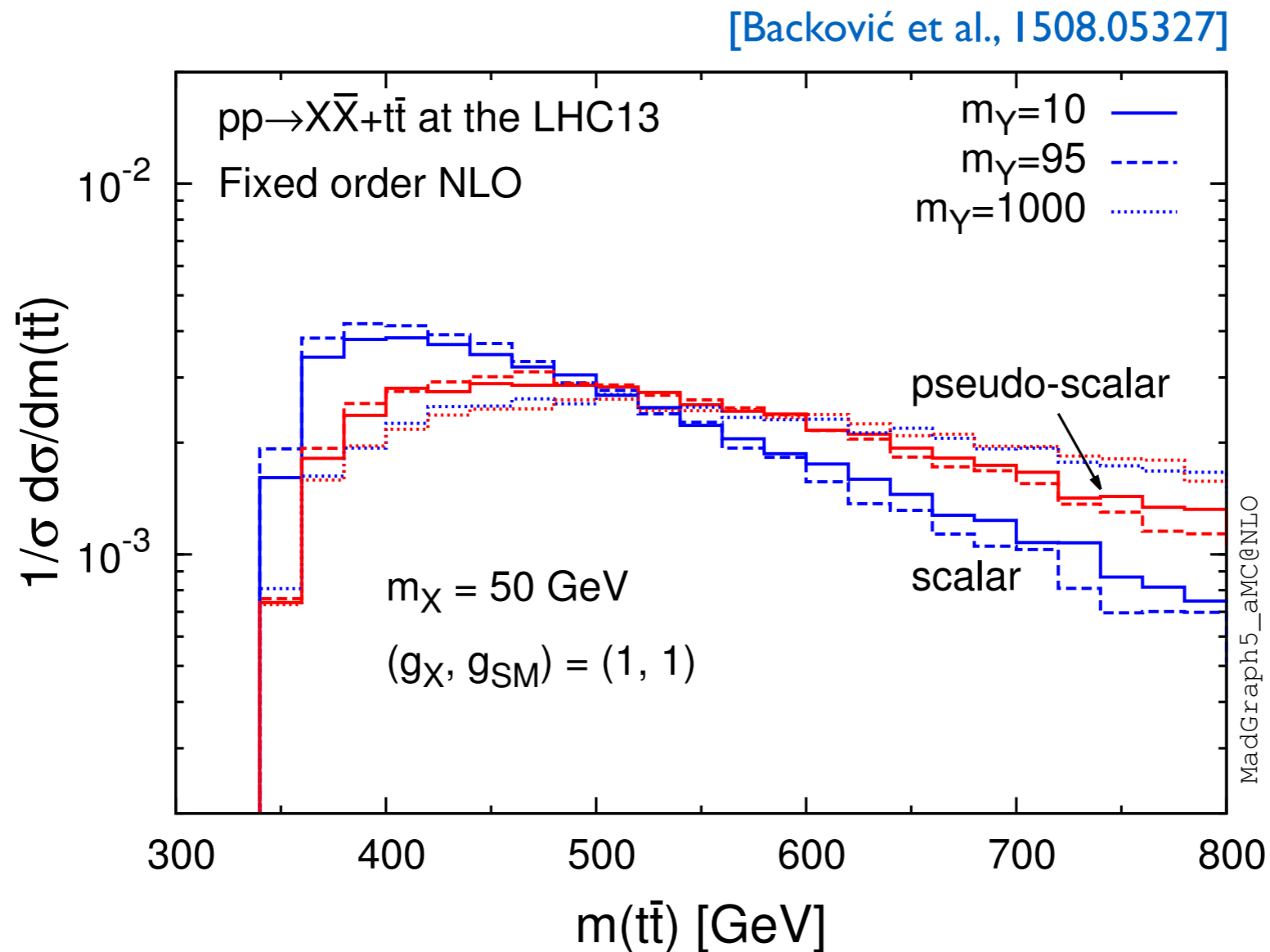
DM-pair production & 2 jets



Azimuthal angle difference $\Delta\phi_{j_1 j_2}$ in $E_{T,\text{miss}} + 2j$ events gold-plated observable to probe structure of DM-SM interactions

[see also Cotta et al., 1210.0525; Crivellin et al. 1501.00907 for related ideas]

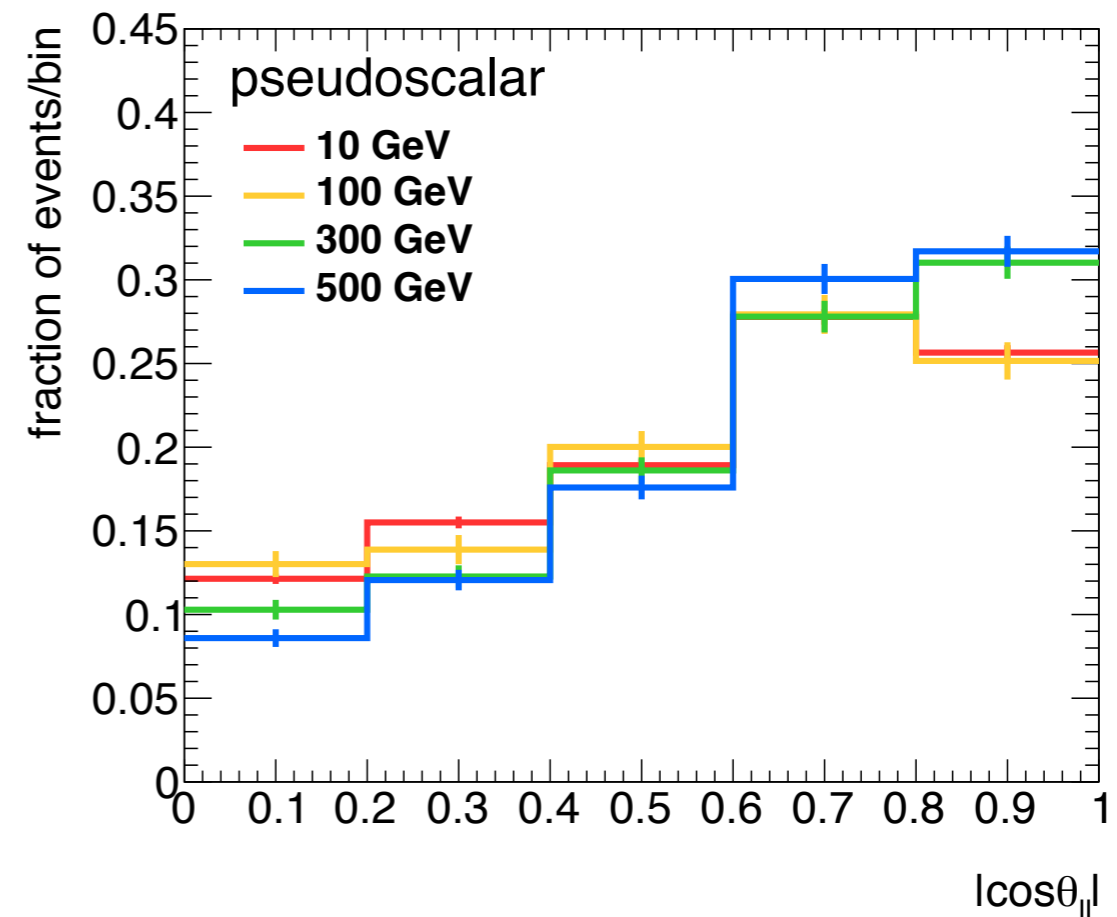
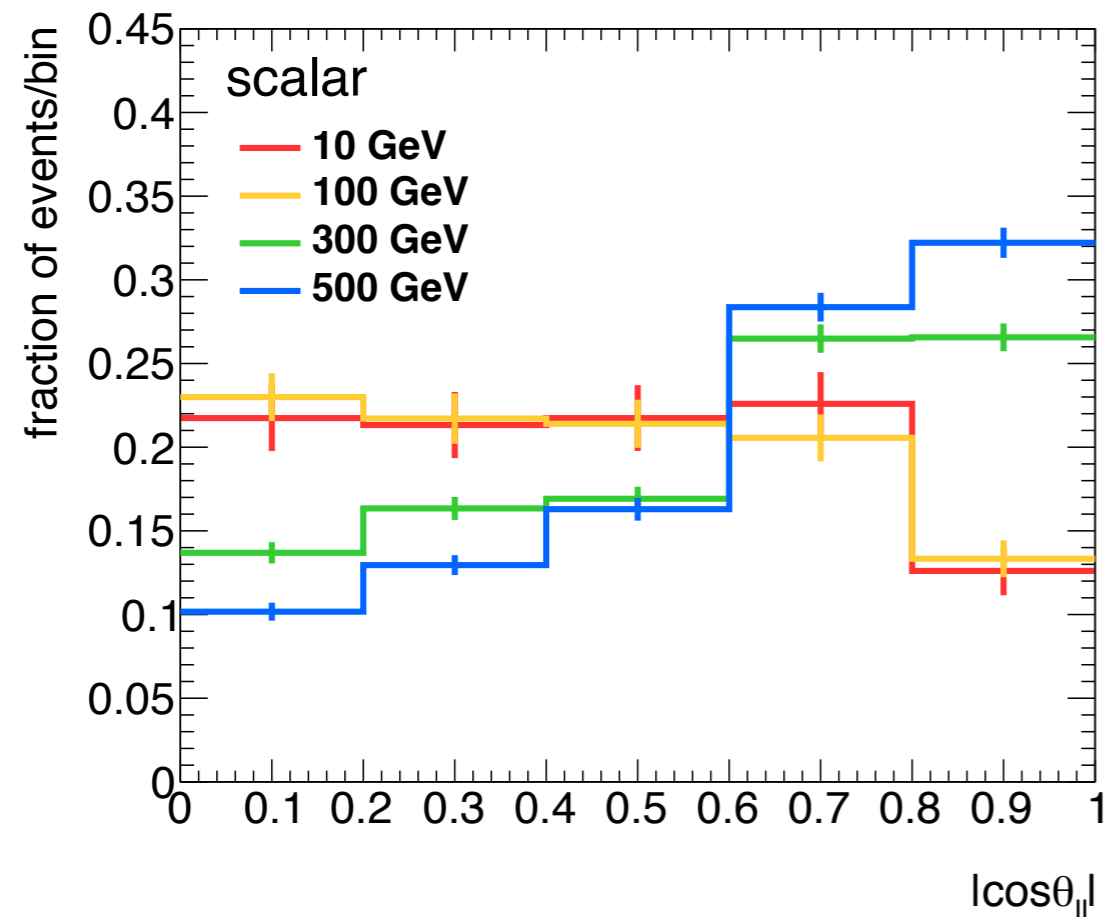
Distribution of $E_{T,miss} + t\bar{t}$ events



If mediator is light, scalar DM-top interactions may be distinguished from pseudoscalar couplings by studying invariant $t\bar{t}$ mass distribution

Distribution of $E_{T,miss} + t\bar{t}$ events

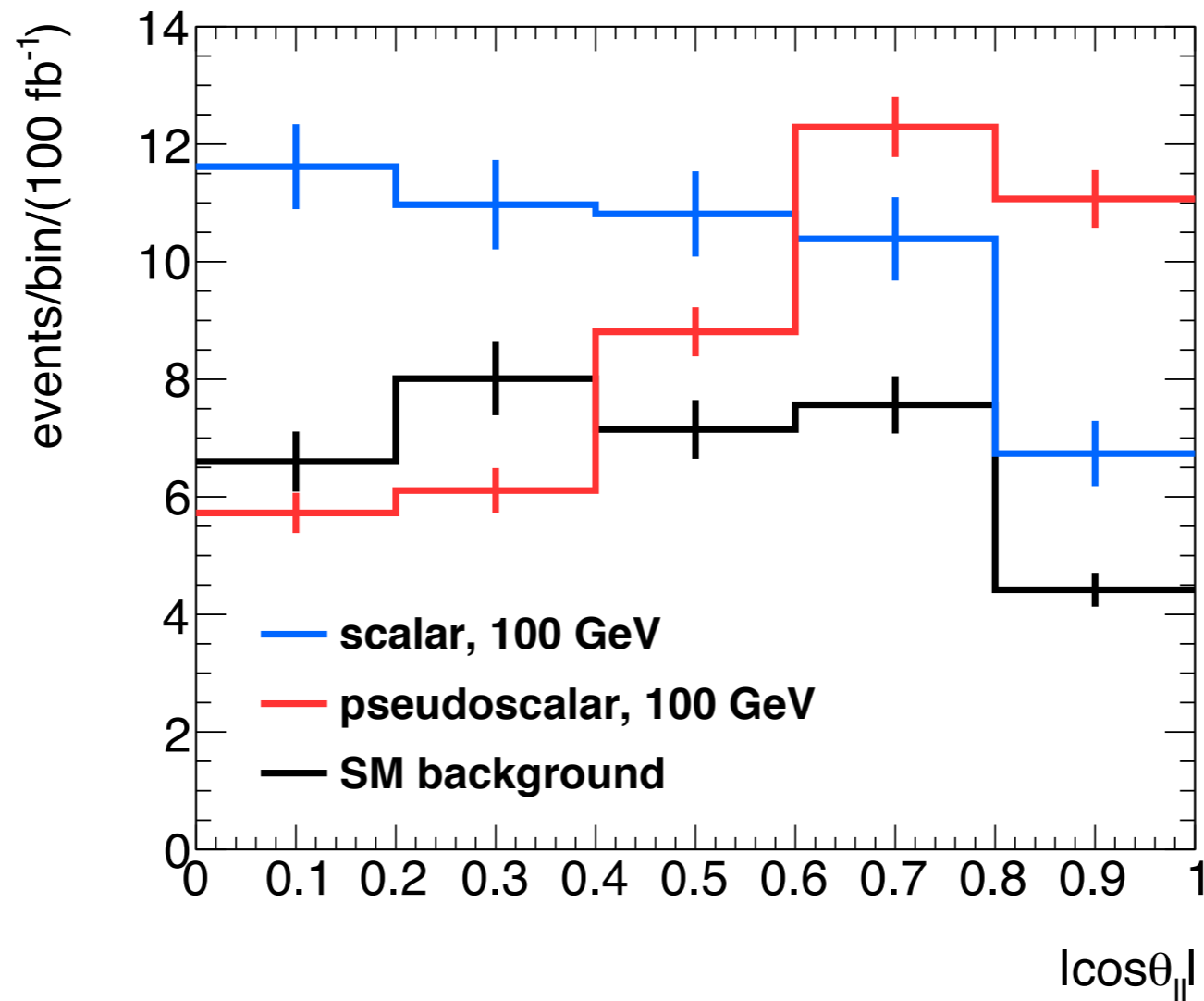
[UH, Pani & Polesello, 1611.09841]



Pseudorapidity difference of two leptons $\cos(\theta_{||}) = \tanh(\Delta\eta_{||}/2)$ in di-leptonic top decays powerful probe CP-property of spin-0 mediators

Distribution of $E_{T,miss} + t\bar{t}$ events

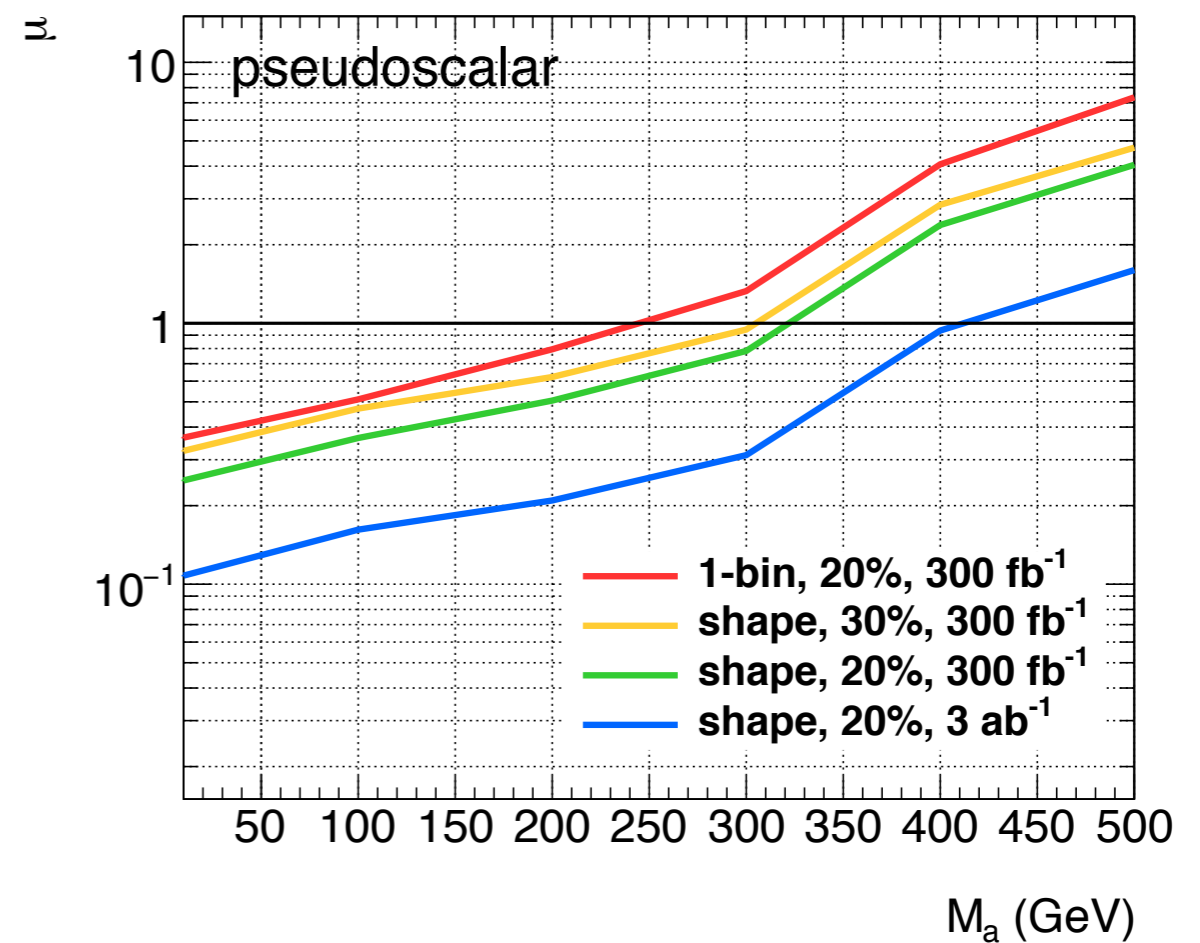
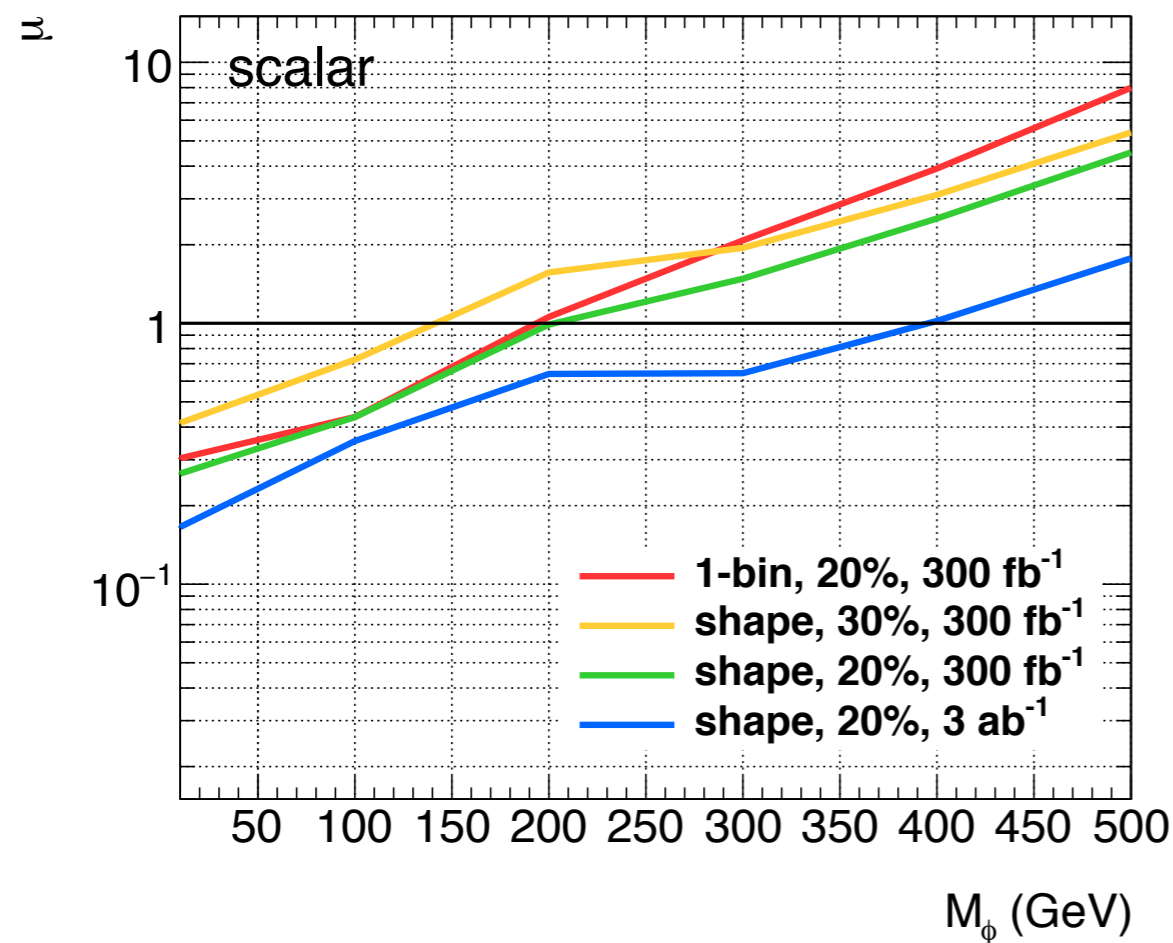
[UH, Pani & Polesello, 1611.09841]



For spin-0 mediator of 100 GeV clear separation of signal & SM background in realistic experimental setup

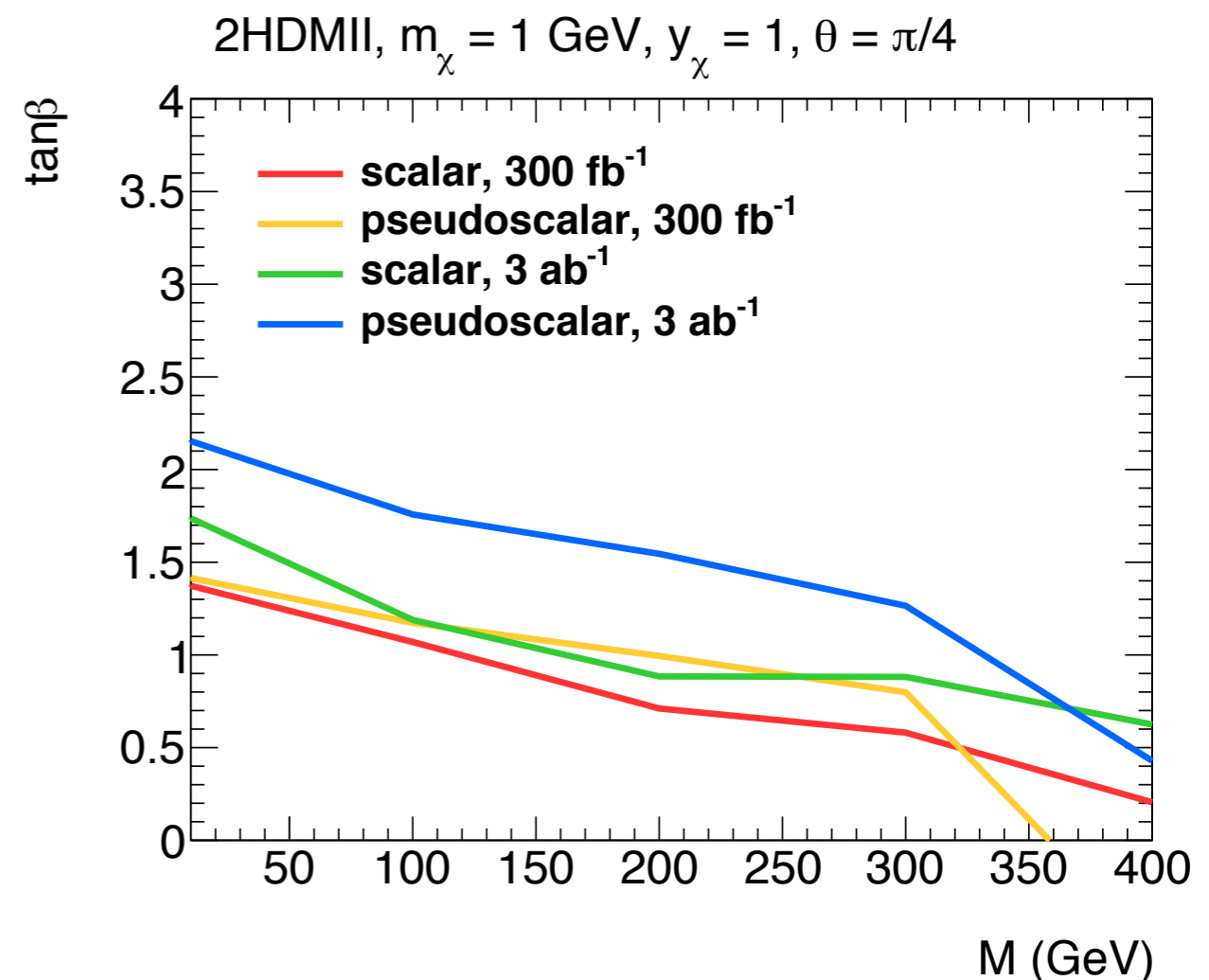
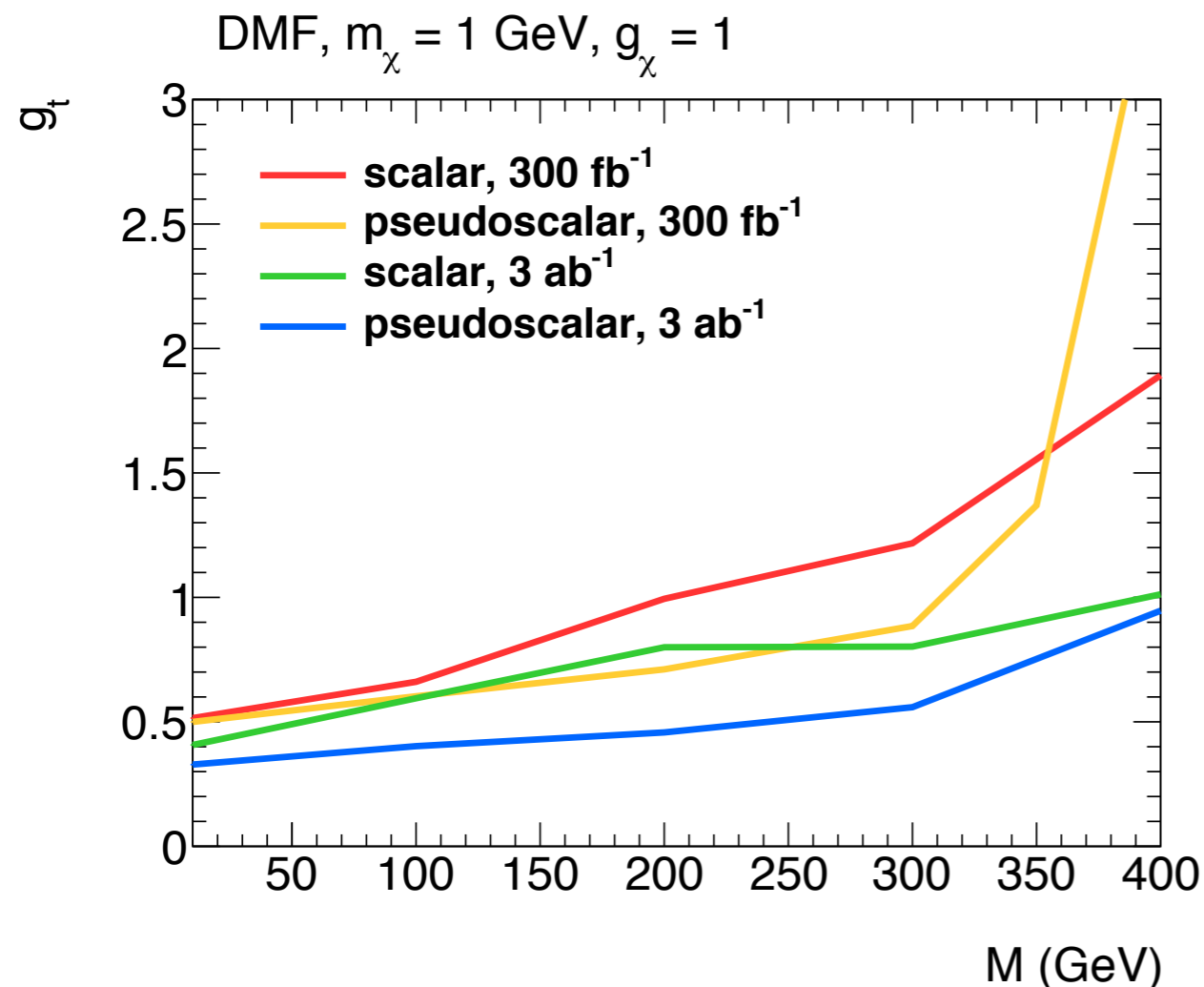
$E_{T,\text{miss}} + t\bar{t}$ searches: projections

[UH, Pani & Polesello, 1611.09841]



Likelihood shape fit provides a significant improvement over the counting experiment for high-mass mediators irrespectively of their CP nature

$E_{T,miss} + t\bar{t}$ searches: projections



Spin-0 mediators with an effective coupling strength of $O(1)$ to tops can be tested for masses up to 350 GeV (or even above) at future LHC runs

Mono-jet backgrounds at 8 TeV

[CMS, 1408.3583]

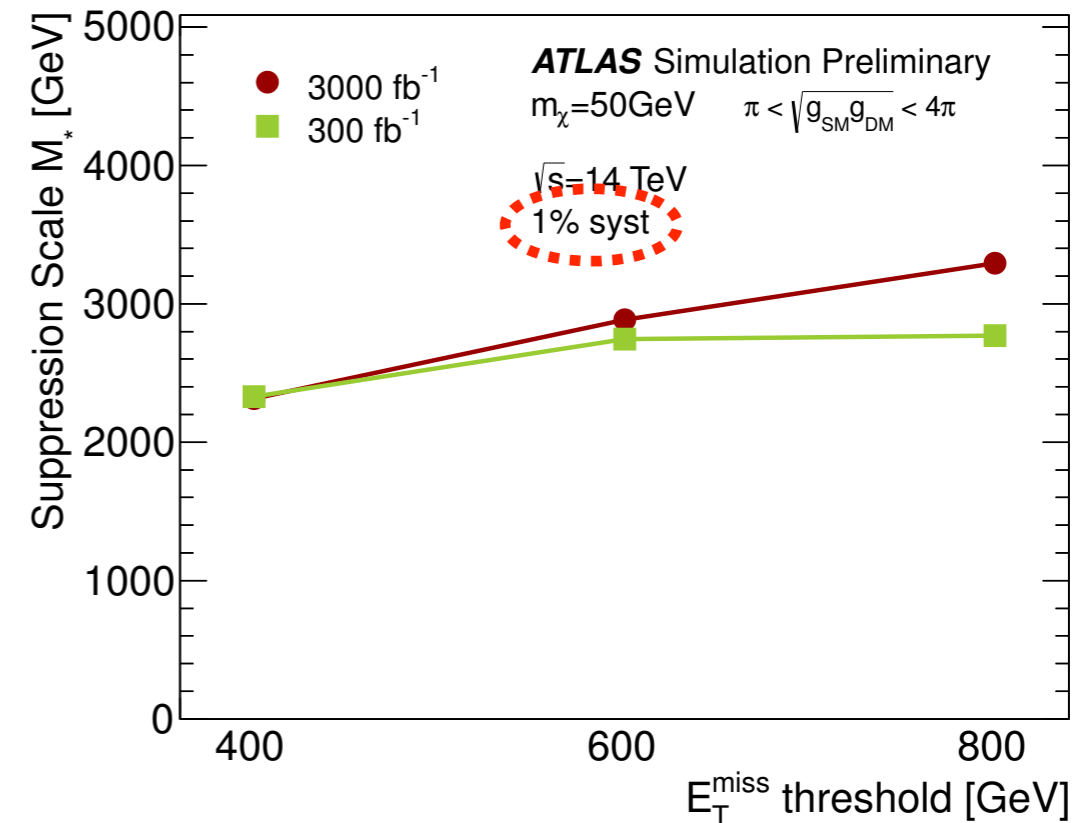
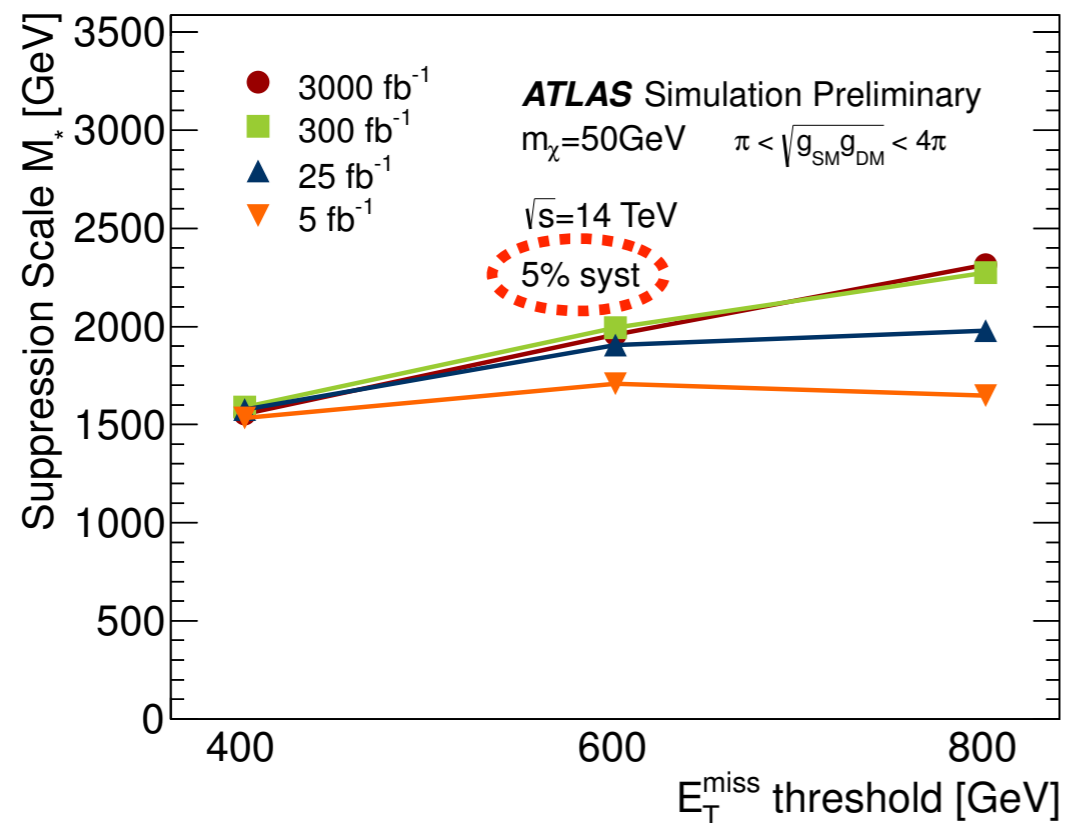
relative
uncertainty

E_T^{miss} (GeV)	>250	...	>550	
Z($\nu\nu$)+jets	32100 \pm 1600	...	362 \pm 64	13%
W+jets	17600 \pm 900	...	123 \pm 13	3%
t \bar{t}	446 \pm 220	...	2.8 \pm 1.4	
Z(ll)+jets	139 \pm 70	...	1.0 \pm 0.5	
Single t	155 \pm 77	...	—	
QCD multijets	443 \pm 270	...	0.5 \pm 0.3	
Diboson	980 \pm 490	...	20 \pm 10	2%
Total SM	51800 \pm 2000	...	509 \pm 66	
Data	52200	...	519	

At 8 TeV SM background to mono-jet searches has an error of $O(10\%)$

Mono-jet prospects at 14 TeV

[ATL-COM-PHYS-2014-549]



At high-luminosity LHC, systematic uncertainties will limit reach of mono-jet searches. How far can one push this uncertainties down?
 1% seems like a big challenge for both experiment & theory

Monte Carlo implementations

Both POWHEG BOX & MadGraph5_aMC@NLO able to simulate $E_{T,\text{miss}}+j$ signals in s-channel simplified DM models at 1-loop level including consistently parton shower (PS) effects

[UH et al., 1310.449; Backović et al., 1508.05327]

Predictions without PS can also be obtained with official MCFM release — there is also a Sherpa+OpenLoops/GoSam package which is however not public

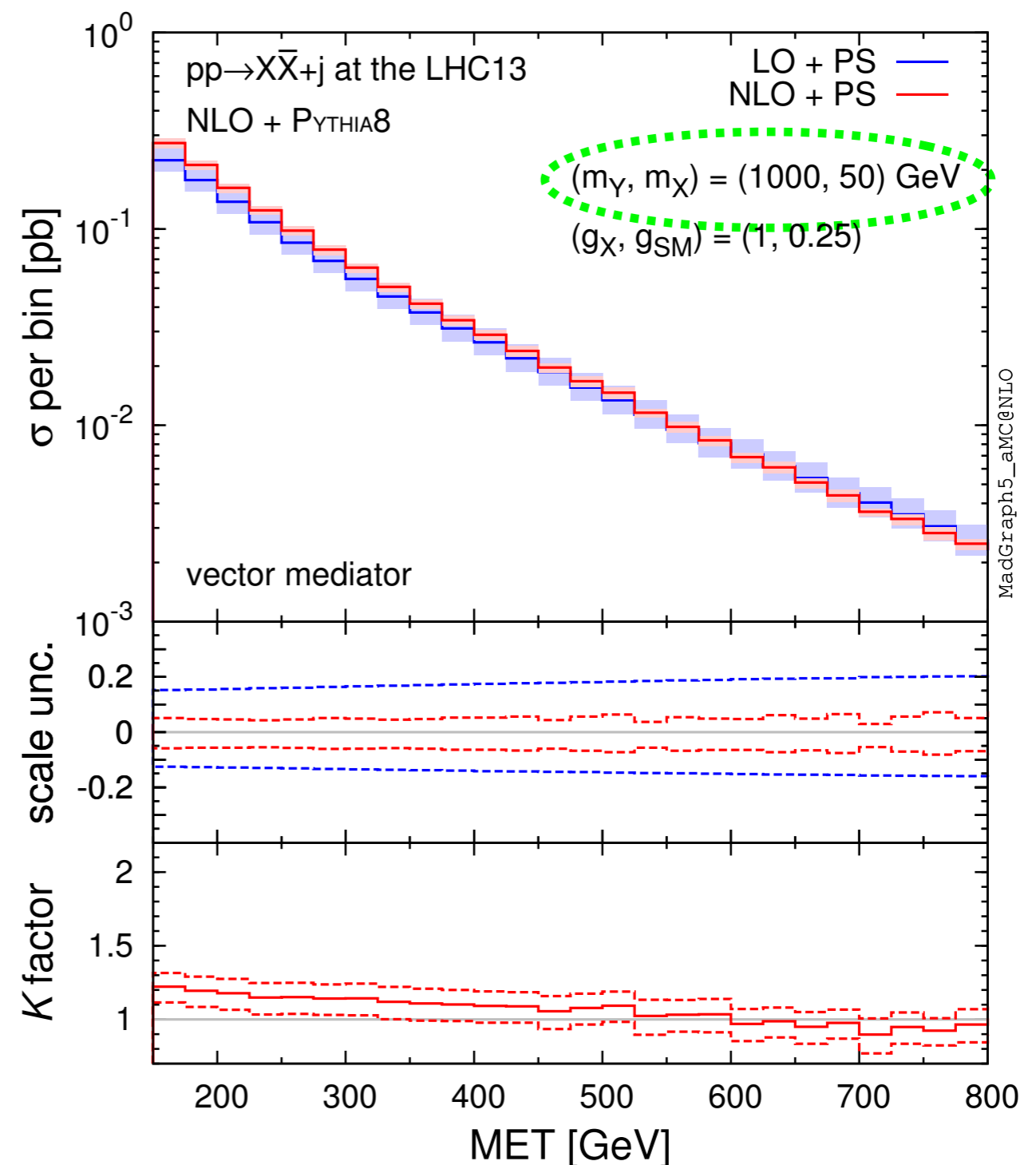
[Fox & Williams, 1211.6390]

NLOPS: spin-1 mediators

- For heavy mediators & hard $E_{T,miss}$ cuts, impact of QCD corrections small, which results in K-factors close to 1

[UH et al., 1310.4491]

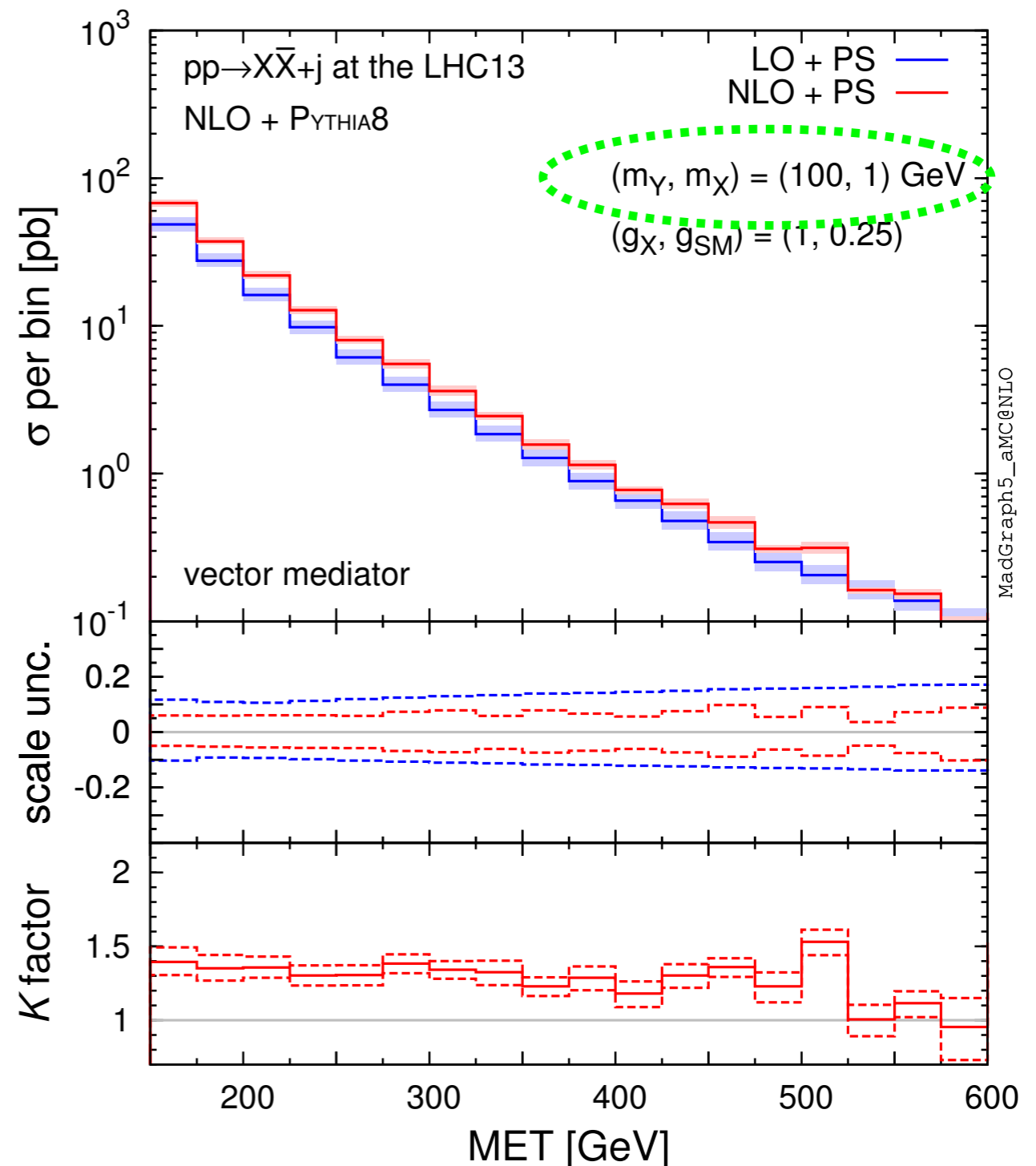
[Backović et al., 1508.05327]



NLOPS: spin-1 mediators

- For heavy mediators & hard $E_{T,miss}$ cuts, impact of QCD corrections small, which results in K-factors close to 1
- In case of very light mediators & weak $E_{T,miss}$ cuts, NLO effects are more important, leading to K-factors of $O(1.5)$

[Backović et al., 1508.05327]



Mono-jet $\neq E_{T,miss} + j$

