

Heavy Flavors on The Lattice

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ABSTRACT

The lattice QCD results on the hadron spectrum and weak transitions between hadrons are briefly reviewed. Hadrons containing heavy quarks c or b are considered. The focus is on the recent simulations and some older results which are particularly relevant in view of the recent experimental discoveries.

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1 Introduction

The study of hadron properties requires a non-perturbative method since the strong coupling constant at hadronic energy is not small. Lattice QCD is an ab-initio non-perturbative method based directly on the QCD Lagrangian with parameters m_{q_i} and g_s . An expectation value of a desired quantity C is obtained via numerical path integration $\langle C \rangle \propto \int \mathcal{D}U \mathcal{D}q_i \mathcal{D}\bar{q}_i e^{-S_{QCD}} C$ formulated on a discretized and finite Euclidian space-time.

Here I focus on the lattice results reported between the summer 2016 and the LHCP conference held in mid-May 2017. Some older lattice results are also reported which are particularly relevant in view of the very recent experimental discoveries.

2 Spectroscopy and two-hadron scattering

Excited charmonia, charmed and charmed-strange mesons: The most extensive spectra of the excited charmonia, D and D_s have been calculated Hadron Spectrum Collaboration. Several complete quark-antiquark multiplets nL were found in a recent simulation with $m_\pi \simeq 240$ MeV: see Figs. 3, 4, and 5 in [1]. Multiplets of hybrid states were also found and some of them carry exotic J^{PC} . Light-quark mass dependence of charmonia in comparison to earlier results at $m_\pi \simeq 400$ MeV is found to be mild. Most of these states, particularly those with $J = 3, 4$ or exotic $J^{PC} = 1^{-+}, 0^{+-}, 2^{+-}, \dots$ have yet to be discovered experimentally. The main caveat of this calculation is that it disregards strong decays of resonances and threshold effects, which is remedied for some states in what follows.

Strongly decaying hadron resonances and hadron-hadron scattering: The hadronic resonances with masses above threshold strongly decay to a pair of hadrons $H_1 H_2$. In the recent years, the main effort was to simulate $H_1 H_2$ scattering channels on the lattice and extract the underlying scattering matrix $T(E)$ as a function of energy. This is possible thanks to the rigorous Lüscher's formalism [2] (see [3] for introduction on the topic). The scattering matrix $T(E)$ renders the $H_1 H_2$ cross-section $\sigma(E) \propto |T(E)|^2$, which in principle allows lattice QCD determination of the resonance masses and decay widths from the peaks in the cross-section.

Charmed resonances from $D\pi - D\eta - D_s \bar{K}$ coupled channel scattering: Hadron Spectrum Collaboration extracted 3×3 scattering matrix for three coupled channels at $m_\pi \simeq 400$ MeV and searched for poles in the scattering matrix [4]. The resonance pole was found in d -wave scattering, which closely resembles experimental D_2 with $J^P = 2^+$. The scalar D_0^* state was found as a bound-state pole on the real-axes almost on $D\pi$ threshold due to the heavy m_π employed in the simulation [4]. Experimentally scalar $D_0^*(2400)$ meson is a wide resonance above $D\pi$ threshold; it emerged as a wide resonance in a less detailed lattice simulation of $D\pi$ scattering in the one-channel approximation at $m_\pi \simeq 266$ MeV [5].

$Z_c(3900)$ from coupled channel $J/\psi\pi - D\bar{D}^* - \eta_c\rho$ scattering: In order to search for the exotic $Z_c(3900)$ state with flavor $\bar{c}cd\bar{u}$, the HALQCD collaboration extracted 3×3 scattering matrix for three coupled channels with $J^P = 1^+$ [6]. Less rigorous HALQCD approach was applied, which has not been verified on conventional resonances. The resulting differential ratios as a function of $J/\psi\pi$ and $D\bar{D}^*$ invariant masses indeed show a peak around 3.9 GeV, resembling experimental peak. If the coupling between $J/\psi\pi - D\bar{D}^*$ channels is set to zero by hand, the peak disappears. The HALQCD results therefore indicate that $Z_c(3900)$ peak is possibly a coupled channel effect rather than a genuine resonance.

Search for $X(5568)$ in $B_s\pi^+$ scattering: The $X(5568)$ state with exotic content $\bar{b}s\bar{d}u$ was recently claimed by D0 collaboration [7]. If this state with $J^P = 0^+$ exists, it can strongly decay only to $B_s\pi^+$ and lies significantly below all other thresholds, which makes a lattice search for $X(5568)$ cleaner and simpler than for other exotic candidates. The simulation of $B_s\pi^+$ scattering did not find $X(5568)$ [8], in agreement with the LHCb [9] and CMS [10] results.

Doubly bottom BB^* and B_sB^* bound states: Several lattice simulations provide a growing evidence for a strongly-stable state with flavor $\overline{bb}ud$, $J^P = 1^+$, $I = 0$ and mass $m < m_B + m_{B^*}$. The simulation [11, 12] was based on the static b -quark, while [13] employed NRQCD for b -quark. Such a state, if bound by $m_B + m_{B^*} - m = 189 \pm 10$ MeV [13], decays only weakly to $ud\overline{bb} \rightarrow B^+\overline{D}^0$, $J/\psi B^+K^0$. The indication for a strongly-state strange partner B_sB^* with $m < m_{B_s} + m_{B^*}$ was also found [13], with expected weak decays to $B^+D_s^-$, $J/\psi B_sK^0$, $B_s\overline{D}^0$, $J/\psi B^0\phi$.

Excited Ω_c^* : The extensive excited Ω_c^* spectrum with css valence content was predicted on lattice in 2013 [14, 15], disregarding their strong decays. Five states were found in the energy region 3.0 – 3.2 GeV, in agreement with LHCb discovery this year. The lattice calculation predicts their quantum numbers: two carry $J^P = 1/2^-$, two carry $3/2^-$ and one $5/2^-$.

Charmonium scalar resonance $\chi_{c0}(2P)$: This year Belle reported on an alternative candidate for a scalar resonance $\chi_{c0}(2P)$ with $m = 3862_{-32}^{+26}{}_{-13}^{+40}$ MeV and $\Gamma = 201_{-67}^{+154}{}_{-82}^{+88}$ MeV which favors $J^{PC} = 0^{++}$ [16]. A slightly heavier and narrower resonance with $m = 3966 \pm 20$ MeV and $\Gamma = 67 \pm 18$ MeV emerged from exploratory simulation of $D\overline{D}$ scattering in s-wave [17] and a Breit-Wigner-type fit in the resonance region (scenario (i) from [17]). The uncertainty on the width is large in both cases, and more work is needed to understand the physics in this channel.

Hadro-quarkonium: A system of a quarkonium $\overline{Q}Q$ and a light hadron (meson or baryon) was studied [18]. The modifications on $\overline{Q}(r)Q(0)$ binding potential $V(r)$ was found to be at most few MeV. Consequently also $\overline{Q}Q$ binding energies modify by at most few MeV in presence of a light hadron.

3 Weak transitions

Exclusive $b \rightarrow cl\overline{\nu}$ decays: Most recent calculations investigate this transition in view of the tension between V_{cb} obtained from exclusive and inclusive decays.

The new preliminary results for $B \rightarrow D^*$ at zero D^* recoil have been obtained by HPQCD, based on relativistic HISQ charm quark and NRQCD bottom quark [19]. The resulting form factor $h_{A_1}(1)$ leads to the preliminary value of $V_{cb} = 41.5(17) \cdot 10^{-3}$ [19] that is closer to inclusive V_{cb} than previous exclusive V_{cb} from FNAL/MILC [20]. The updated final results from this HPQCD simulation are expected soon.

The preliminary status of the first on-going $B \rightarrow D^*$ simulation at non-zero D^* recoil was presented at the Lattice 2017 (held after LHCP 2017) by Alejandro Vaquero on behalf of the Fermilab/MILC collaborations. This will be very valuable to verify the Standard Model prediction for $R(D^*) = Br(B \rightarrow D^*\tau\overline{\nu}_\tau)/Br(B \rightarrow D^*\mu\overline{\nu}_\mu)$ [21], which shows intriguing tension with the experiment.

The f_0 and f_+ form factors for $B_s \rightarrow D_s$ were extracted in the whole q^2 region by HPQCD [22]. Relativistic HISQ c -quark and NRQCD b -quark were employed. These are valuable also since $f_0^{B_s \rightarrow D_s}(m_\pi^2)/f_0^{B \rightarrow D}(m_K^2)$ allows determination of fragmentation-function ratio f_s/f_d needed for LHC measurement of $B(B_s \rightarrow \mu^+\mu^-)$ due to the normalization modes. The HPQCD determined f_s/f_d using experimental $B(\overline{B}_s \rightarrow D_s^+\pi^-)/B(\overline{B}^0 \rightarrow D^+K^-)$ and the above form-factor ratio via the factorization hypothesis as proposed in [23].

Two methods of treating b quarks were shown to give consistent results for $B_c \rightarrow \eta_c$ and $B_c \rightarrow J/\psi$ form factors in HPQCD study [24]. First method considers relativistic HISQ b -quark on a range of masses $m_Q \leq m_b$, while NRQCD is used in the second method: agreement at $m_Q = m_b$ gives credibility in the results.

Towards inclusive semileptonic decays: The formalism and first exploratory lattice results for inclusive semileptonic decays $B \rightarrow X_c l \overline{\nu}$ were presented by S. Hashimoto [25]. The squared amplitude $|\mathcal{M}|^2 = |V_{cb}|^2 G_F^2 M_B l^{\mu\nu} W_{\mu\nu}$ based on $H = V_{cb} \frac{G_F}{\sqrt{2}} \overline{l} \gamma_\mu (1 - \gamma_5) \nu J^\mu$ ($J^\mu \equiv \overline{c} \gamma^\mu (1 - \gamma_5) b = V^\mu - A^\mu$)

contains trivial leptonic part $l^{\mu\nu}$, while the hadronic part

$$W_{\mu\nu} = \sum_X (2\pi)^3 \delta^4(p_B - q - p_x) \frac{1}{2M_B} \langle B(p_B) | J_\mu^\dagger(0) | X \rangle \langle X | J_\nu(0) | B(p_B) \rangle$$

contains a sum over all on-shell final states $X_c = D, D^*, \dots$. Instead of summing those explicitly, one can obtain the sum directly by considering forward scattering matrix element

$$T^{\mu\nu} = i \int d^4x e^{-iqx} \frac{1}{2M_B} \langle B | T \{ J_\mu^\dagger(x) J_\nu(0) \} | B \rangle$$

which is related to desired W via the optical theorem $2 \text{Im}M(B \rightarrow B) = \sum_X \int d\Pi_X |M(B \rightarrow X)|^2$ (see for example Section 18.5 of Peskin) as $W = -\frac{1}{\pi} \text{Im}T$. The T can be computed on the lattice from the four-point function [25]

$$T_{\mu\nu}^{JJ}(\omega, \vec{q}) \propto \int_0^\infty dt e^{\omega t} \int d\vec{x} e^{i\vec{q}\vec{x}} \langle 0 | B(\vec{p}_B = \vec{0}, t_{snk}) J_\mu^\dagger(\vec{x}, t_2) J_\nu(0, t_1) B^\dagger(\vec{0}, t_{src}) | 0 \rangle$$

where ω denotes the energy of the final state X , J contains V or A parts and various normalizations factors have been omitted for simplicity.

The exploratory numerical simulation has been done on JLQCD configurations for the spectator s quark $B_s \rightarrow X_c l \bar{\nu}$ at zero recoil $\vec{q} = \vec{p}_B - \vec{p}_X = \vec{0}$ and for b -quark mass smaller than physical. The resulting $T_{\mu\nu}(\omega, \vec{q} = \vec{0})$ as a function of ω is shown in Fig. 10 of [25]. The $V_0 V_0$ part is found to be dominated by D_s pole (dashed lines) and represents another way to extract of HQET form factor $h_+(1)$ via $T_{00}^{VV} = \frac{|h_+(1)|^2}{M_{D_s} - \omega}$.

The $T_{11}^{AA}(\omega, \vec{0}) = \frac{|h_{A_1}(1)|^2}{M_{D_s^*} - \omega}$ is dominated by D_s^* pole. The HQET form factors determined in this way are consistent with direct calculation but have currently larger errors. The $V_1 V_1$ and $A_0 A_0$ contain contribution from X_c final states with other quantum numbers.

New exclusive $q \rightarrow q' l \bar{\nu}$ and $q \rightarrow q' l^+ l^-$ baryon decays: Six $\Lambda_c \rightarrow \Lambda l \bar{\nu}$ form factors were determined [26] for the first time in view of the BESIII 2015 measurement of this decay rate. Taking V_{cs} from global CKM fit, these form factors lead to the rate that is consistent, and twice more precise as BESIII rate. This gives confidence in lattice treatment of this and analogous electroweak baryon transitions. Alternatively, the form factors lead to the value of V_{cs} , which is currently less precise, but consistent with the one from $D_s \rightarrow l \bar{\nu}$.

The $b \rightarrow s l^+ l^-$ transition and their ratios (relevant for the lepton flavor violation) have attracted large attention recently in view of few tensions between Standard model predictions and experiment. On this front, there is only one new lattice result available since summer 2016. This is a report on the ongoing simulation of $\Lambda_b \rightarrow \Lambda^*(1520) l^+ l^-$ form factors [27]. The $\Lambda_b \rightarrow \Lambda^* l^+ l^-$ has namely certain advantages with respect to the more standard $\Lambda_b \rightarrow \Lambda l^+ l^-$ decay where Λ is neutral and long-lived, which is not favorable for the accurate experimental study. The unstable Λ^* resonances, one the other hand, immediately decay into charged particles and produce tracks that originate from b -decay vertex, which motivates exploring decays also through unstable Λ^* in experiment.

4 Conclusions

Lattice QCD is a reliable ab-initio non-perturbative method that is based directly on the fundamental theory of strong interactions - QCD.

Spectra of strongly stable hadrons (B, D, \dots) are well under control and in agreement with experiment. Variety of exclusive electro-weak transitions between them are being studied with increasing precision. The formalism and the first exploratory lattice results for the inclusive weak transitions $B \rightarrow X_c l \bar{\nu}_l$ have been presented during the last year.

Experiments provided lots of interesting and puzzling hadrons in the recent years. The five excited $\Omega_c^* \simeq c s s$ states, discovered by LHCb this year, have been predicted by lattice QCD around 2013. There is a

growing evidence for a strongly-stable state with flavor \overline{bbud} , $J^P = 1^+$, $I = 0$ and mass $m < m_B + m_{B^*}$ from the lattice. Most of the experimentally discovered exotic hadrons are actually strongly decaying resonances that decay to a single or to multiple-channels. They have to be inferred from the one-channel or multiple-channel scattering matrix. It is encouraging that scattering matrices for single-channel scattering have been reliably extracted for certain channels in the recent years. Scattering matrices for two-channel and three-channel scattering have also been extracted in some cases. One study along these lines indicates that the experimental $Z_c^+(3900)$ peak arises due to the large coupling between the $D\overline{D}^*$ and $J/\psi\pi^+$ channels. Lots of exciting and challenging problems along these lines still remain to be attacked.

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