

Introduction to Calorimeters



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Southampton Lecture

4 May 2016

- Introduction
- Electromagnetic Calorimetry
- Hadron Calorimetry
- Jets and Particle Flow
- Future directions in Calorimetry
- Summary

Calorimetry

One of the most important and powerful detector techniques in experimental particle physics

Two main categories of Calorimeter:

Electromagnetic calorimeters for the detection of

e^\pm and neutral particles γ

Hadron calorimeters for the detection of

π^\pm, p^\pm, K^\pm and neutral particles n, K^0_L

μ^\pm usually traverse the calorimeters losing small amounts of energy by ionisation

The 13 particle types above completely dominate the particles from high energy collisions reaching and interacting with the calorimeters

All other particles decay ~instantly, or in flight, usually within a few hundred microns from the collision, into one or more of the particles above

Neutrinos, and neutralinos, χ^0 , undetected but with **hermetic calorimetry** can be inferred from measurements of missing transverse energy in collider experiments

Introduction

Calorimeters

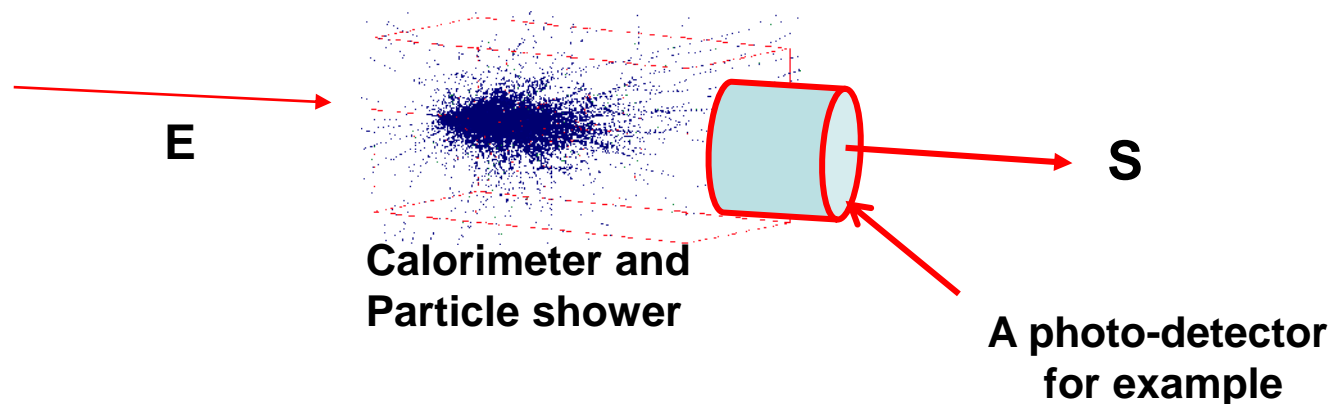
Calorimeters designed to stop and fully contain their respective particles

'End of the road' for the incoming particle

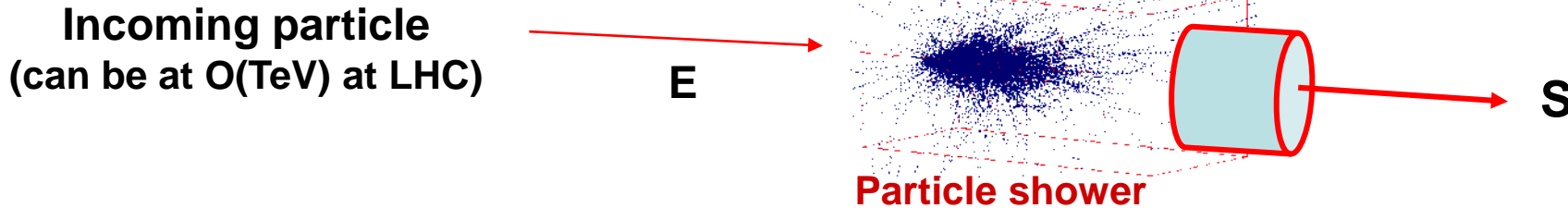
- Measure**
- **energy** of incoming particle(s) by total absorption in the calorimeter
 - **spatial location** of the energy deposit
 - (sometimes) **direction** of the incoming particle

Convert energy E of the incident particle into a detector response S

Detector response $S \propto E$



Introduction



Calorimetry: basic mechanism

Energy lost by the formation of **electromagnetic** or **hadronic** cascades /showers in the material of the calorimeter

Many charged particles in the shower

The charged particles ionize or excite the calorimeter medium

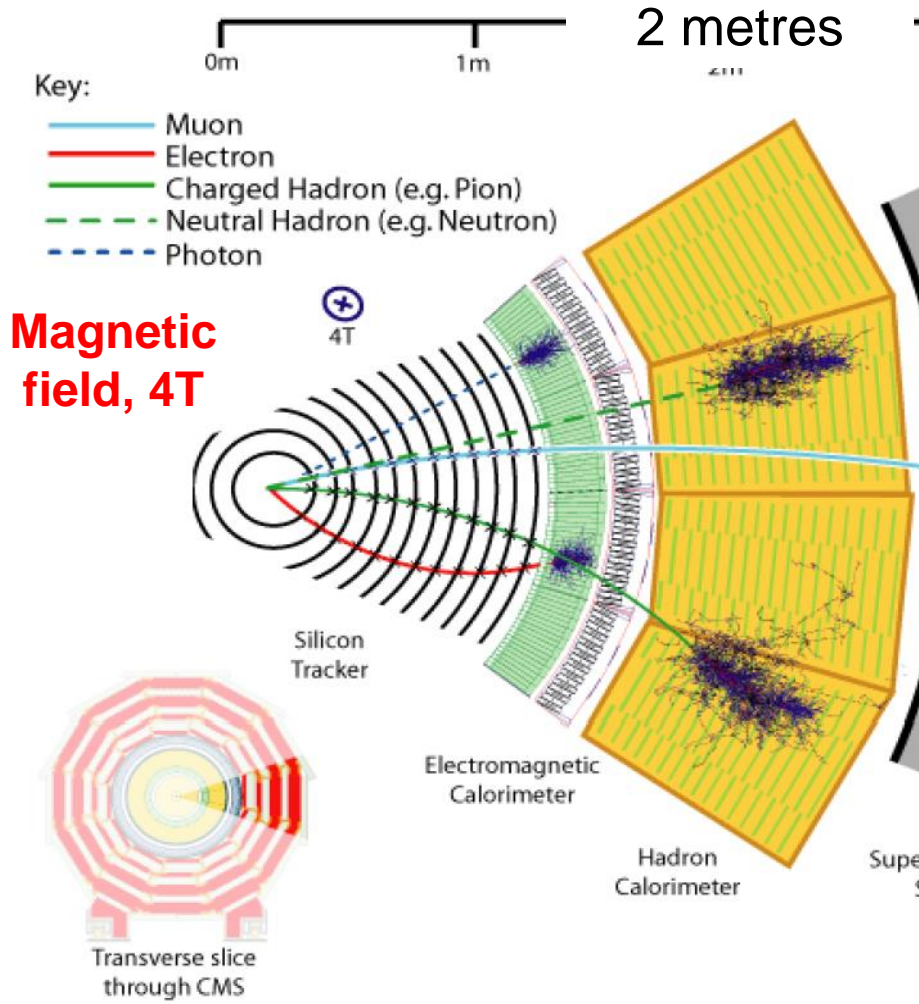
The ionisation or excitation can give rise to:

- The emission of visible photons, $O(\text{eV})$, via scintillation
- The release of ionisation electrons, $O(\text{eV})$

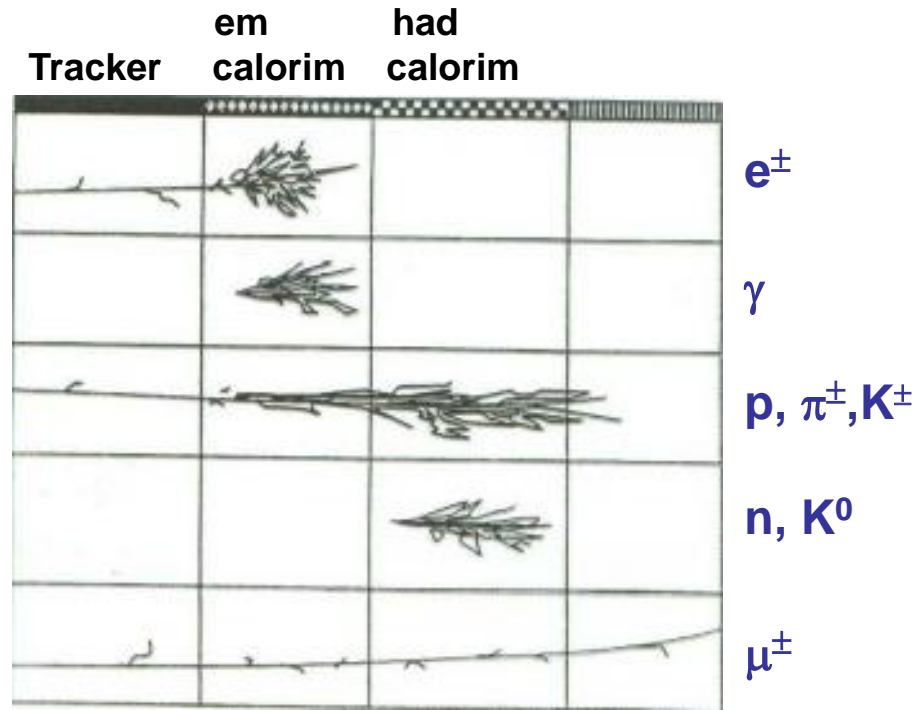
Photo-detectors or anodes/dynodes then detect these “quanta”

Introduction

Where you STOP is what you ARE !!!



A 'wedge' end on view of the CMS experiment at the LHC



Get sign of charged particles from the Tracker

Tracker to be of minimum material to avoid losing particle energy before the calorimeters.

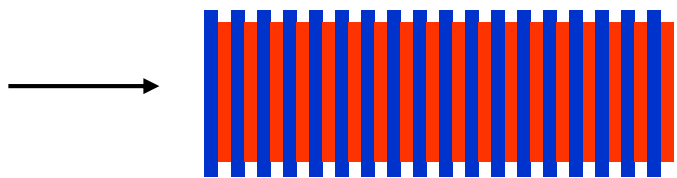
Introduction

There are two general types of calorimeter design:

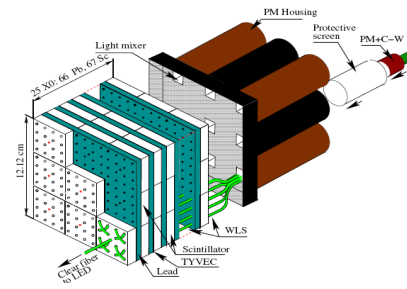
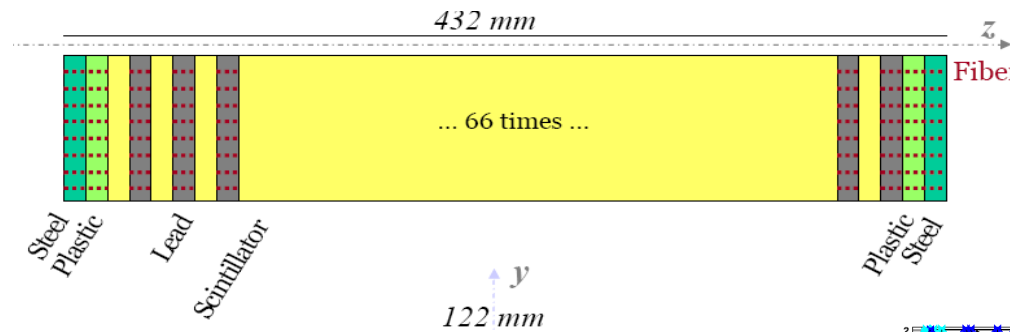
1) Sampling calorimeters

Layers of passive absorber (ie Pb or Cu) alternating with active detector layers such as plastic scintillator, liquid argon or silicon

- Only part of the energy is sampled
- Used for both electromagnetic and hadron calorimetry
- Cost effective



ATLAS ECAL & HCAL
ALICE EMCAL
CMS HCAL
LHCb ECAL

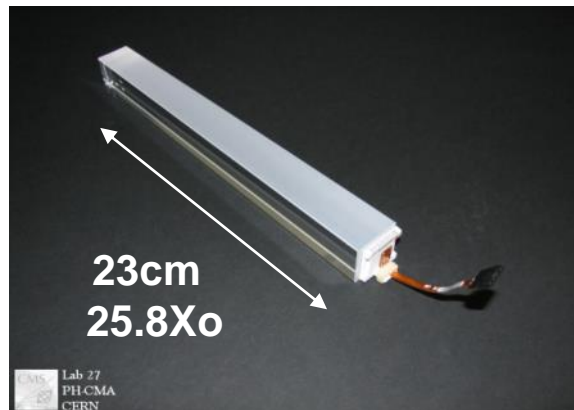
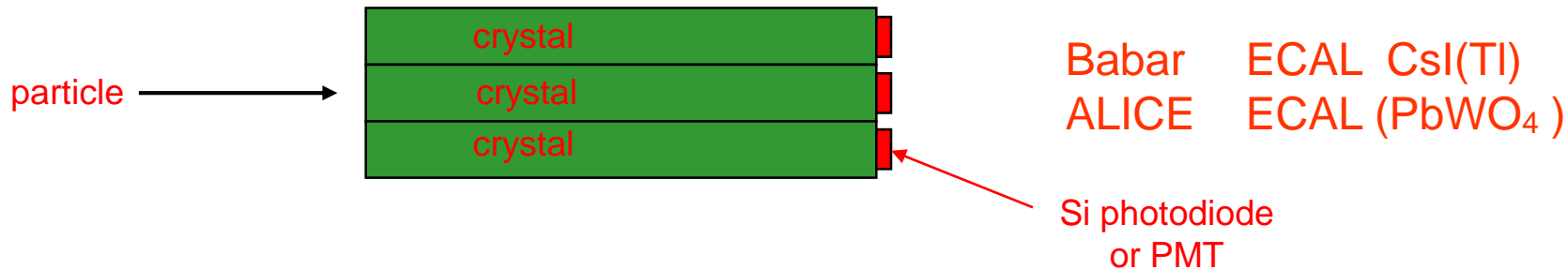


2) Homogeneous calorimeters

Single medium, both absorber and detector

- Liquified Ar/Xe/Kr
- Organic liquid scintillators, large volumes, Kamland, Borexino, Daya Bay
- Dense crystal scintillators: **PbWO₄**, CsI(Tl), BGO and many others
- Lead loaded glass

Almost entirely for electromagnetic calorimetry



CMS ECAL (PbWO₄)

Electromagnetic Calorimetry

Electromagnetic Cascades

Electromagnetic cascades

- e^\pm bremsstrahlung and photon pair production**

By far the most important processes for energy loss by electrons/positrons/photons with energies above 1 GeV
Leads to an e.m. cascade or shower of particles

- Bremsstrahlung**

Characterised by a 'radiation length', X_0 , in the absorbing medium over which an electron loses, on average, 63.2% of its energy by bremsstrahlung.

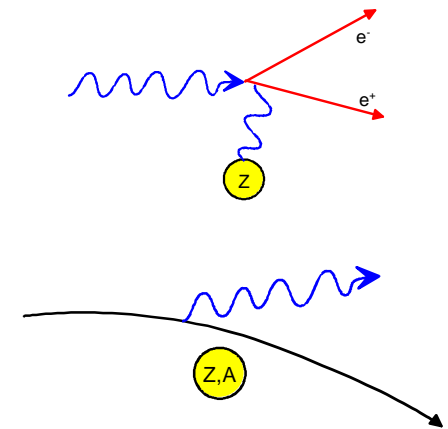
$$E = E_0 e^{-x/X_0} \quad \text{where} \quad -\frac{dE}{dx} = 4\alpha N_A \frac{Z^2}{A} r_e^2 E \ln \frac{183}{Z^{1/3}}$$

$$-\frac{dE}{dx} = \frac{E}{X_0}$$

$$X_0 = \frac{A}{4\alpha N_A Z^2 r_e^2 \ln \frac{183}{Z^{1/3}}}$$

$$X_0 \sim 180 \frac{A}{Z^2} \text{ [g cm}^{-2}\text{]}$$

In Pb (Z=82) $X_0 \sim 5.6 \text{ mm}$



$1/m_e^2$ dependence

$$-\frac{dE}{dx} \propto \frac{Z^2 E}{m_e^2}$$

Use high Z materials for compact e.m. calorimetry

Due to the $1/m^2$ dependence for bremsstrahlung, muons only emit significant bremsstrahlung above $\sim 1 \text{ TeV}$ ($m_\mu \sim 210 m_e$)

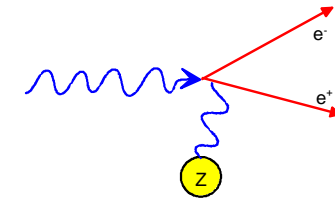
Electromagnetic Cascades

Pair production

Characteristic mean free path before pair production, $\lambda_{\text{pair}} = 9/7 X_0$

$$E_\gamma \geq 2m_e c^2$$

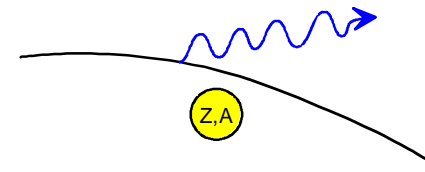
Intensity of a photon beam entering calorimeter reduced to $1/e$ of the original intensity, $I = I_0 \exp(-7/9 x/X_0)$. $\lambda_{\text{pair}} = 7.2 \text{ mm in Pb}$



Brem and pair production dominate the processes that degrade the incoming particle energy

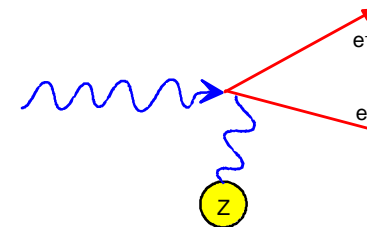
50 GeV electron

Loses 32 GeV over 1 X_0 by bremsstrahlung



50 GeV photon

Pair production to $e^+ e^-$, 25 GeV to each particle
Energy regime degraded by 25 GeV



Minimum ionising particle (m.i.p)

In Pb, over 1 X_0 , ionization loss $\sim O(10s)$ of MeV
Factor of ~ 1000 less than the above

Electromagnetic Cascades

Below a certain critical energy, E_c :

e^\pm energy losses are greater through ionisation than bremsstrahlung

The multiplication process runs out

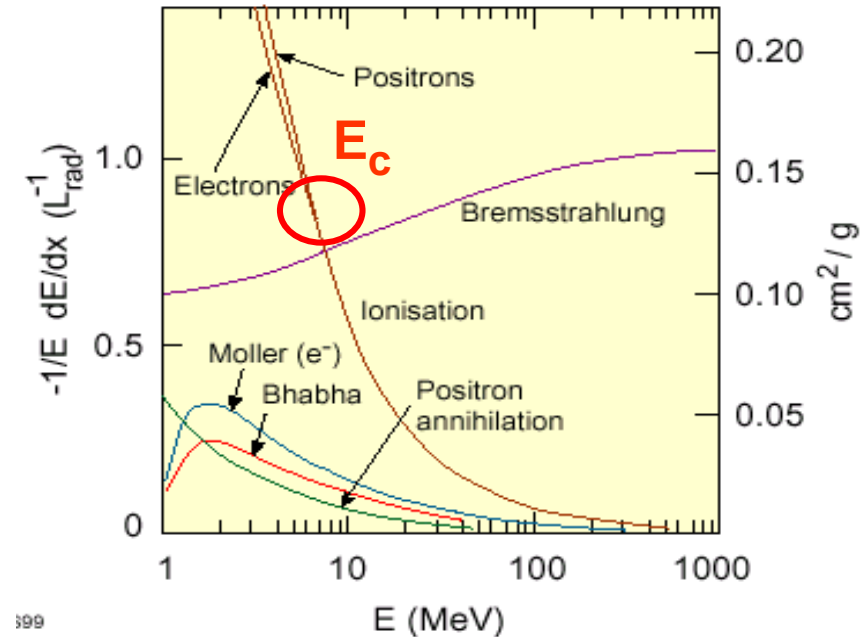
- Slow decrease in number of particles in the shower
- Electrons/positrons are stopped

Photons progressively lose energy by Compton scattering, converting to electrons via the photo-electric effect, and absorption

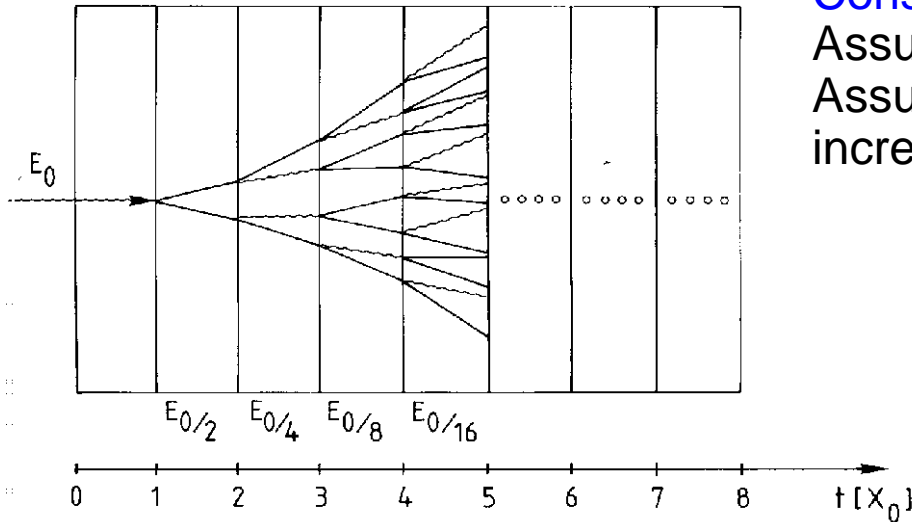
$$E_c \approx \frac{610 \text{ MeV}}{Z + 1.24} \quad \longrightarrow \quad \text{Pb (Z=82), } E_c = 7.3 \text{ MeV}$$

Liquids and solids

Fractional Energy Loss by Electrons



EM Cascades: a simple model



Consider only Bremsstrahlung and pair production
 Assume: Incident energy = E_0 , λ_{pair} and X_0 are equal
 Assume: after each X_0 , the number of particles increases by factor 2

After ' t ' layers, each of thickness X_0 :

$$\text{Number of particles} = N(t) = 2^t$$

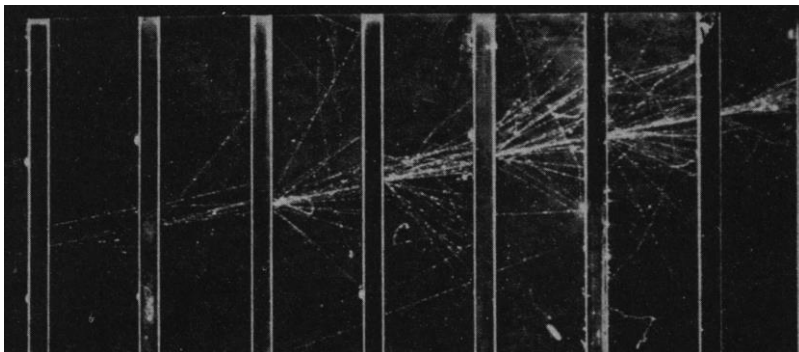
$$\text{Average energy per particle} = E(t) = E_0 / 2^t$$

Process continues until $E(t) < E_c$

This layer contains the maximum number of particles:

$$t_{\text{max}} = \frac{\ln E_0 / E_c}{\ln 2}$$

$$N^{\text{total}} = \sum_{t=0}^{t_{\text{max}}} 2^t = 2^{(t_{\text{max}} + 1)} - 1 \approx 2 \cdot 2^{t_{\text{max}}} = 2 \frac{E_0}{E_c}$$



Electron shower in a cloud chamber with lead absorbers

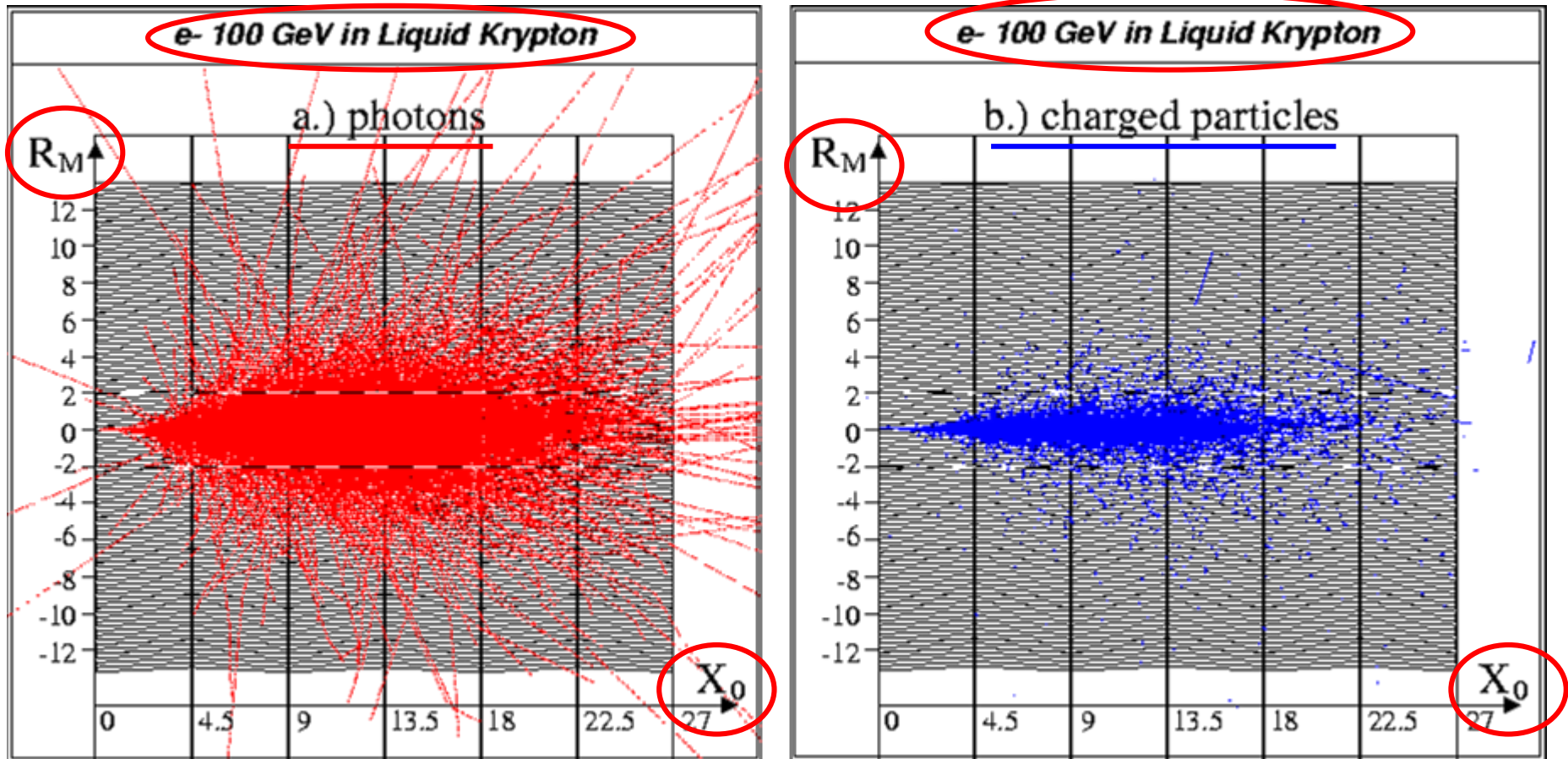
For a 50 GeV electron on Pb

$N^{\text{total}} \sim 14000$ particles

t_{max} at $\sim 13 X_0$ (an overestimate)

EM Cascade Profiles

EM shower development in Krypton ($Z=36$, $A=84$)



Photons created

Charged particles created

GEANT simulation: 100 GeV electron shower in the NA48 liquid Krypton calorimeter

EM Cascade Profiles

Longitudinal Shower Development

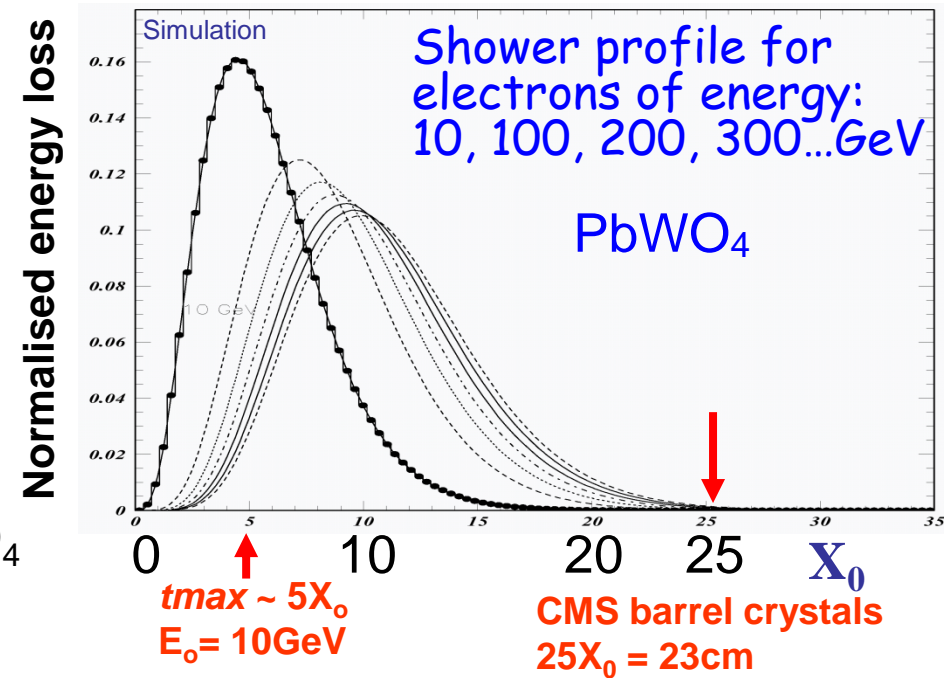
Shower only grows logarithmically with E_0

Shower maximum, where most energy deposited,

$$t_{max} \sim \ln(E_0/E_c) - 0.5 \quad \text{for } e^\pm$$

$$t_{max} \sim \ln(E_0/E_c) + 0.5 \quad \text{for } \gamma$$

$$t_{max} \sim 5 X_0 = 4.6 \text{ cm for } 10 \text{ GeV electrons in PbWO}_4$$



How many X_0 to adequately contain an em shower within a crystal?

Rule of thumb: RMS spread in shower leakage at the back

$\sim 0.5 * \text{average leakage at the back}$

CMS requires the rms spread on energy measurement to be $< 0.3\%$

Therefore require leakage $< 0.65\%$

Therefore crystals must be $25 X_0 = 23 \text{ cm}$ long

EM Cascade Profiles

Transverse Shower Development

Mainly multiple Coulomb scattering by e^\pm in shower

- 95% of shower cone located in cylinder of radius $2 R_M$ where $R_M = \text{Moliere Radius}$

$$R_M = \frac{21 \text{ MeV}}{E_c} X_0 \quad [g/cm^2]$$

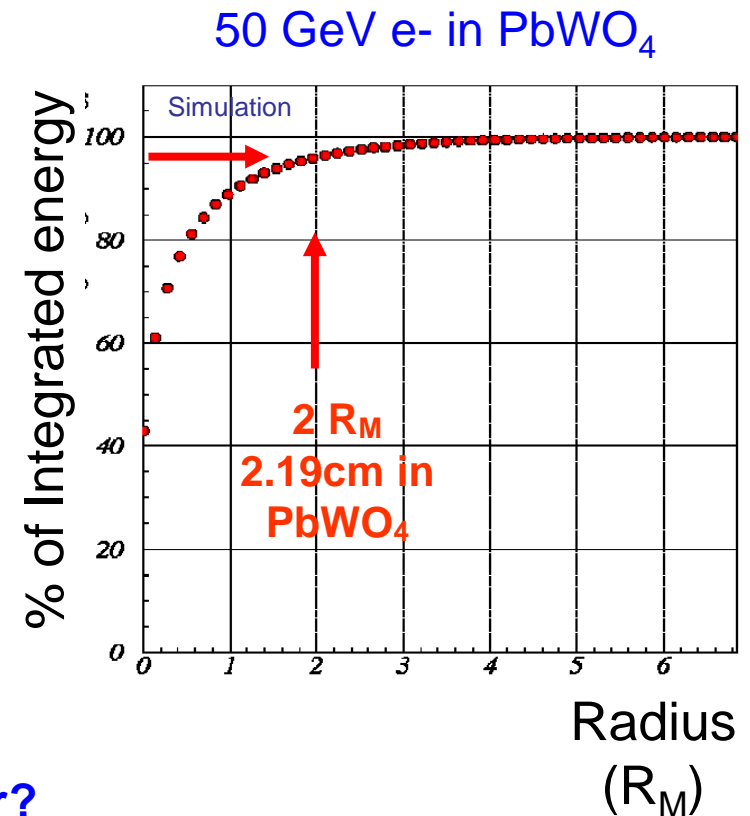
$R_M = 2.19 \text{ cm}$ in PbWO_4
using $X_0 = 0.89 \text{ cm}$ and $E_c \sim 8.5 \text{ MeV}$

How many R_M to adequately measure an em shower?

Lateral leakage degrades the energy resolution

In CMS, keep contribution to $< 2\%/\text{sqrt}(E)$

Achieved by summing energy over 3x3 (or 5x5) arrays of PbWO_4 crystals



Detectors for Electromagnetic Calorimetry

Homogeneous calorimeters

PbWO₄ crystals: CMS and ALICE

Vital properties for use at LHC:

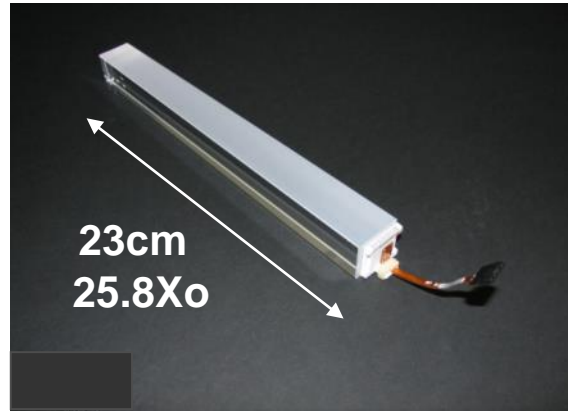
Compact and radiation tolerant

Density 8 g/cc

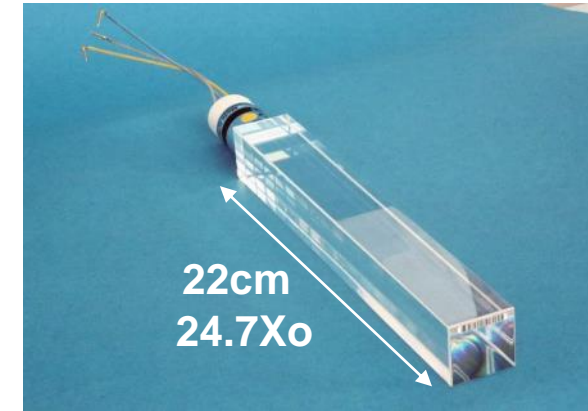
X₀ 0.89 cm

R_M 2.2 cm

Sum over 3x3 or 5x5 crystals



CMS Barrel crystal, tapered
~2.6x2.6 cm² at rear
Avalanche Photo Diode
readout, gain = 50



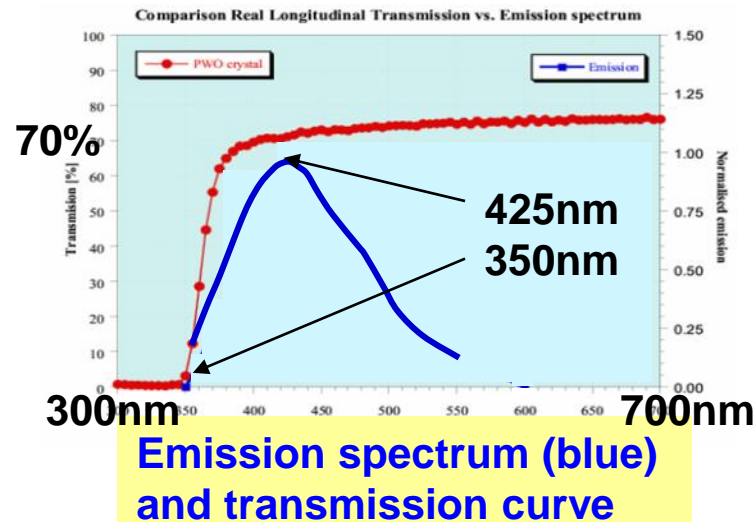
CMS Endcap crystal, tapered,
3x3 cm² at rear
Vacuum Photo Triode
readout, gain ~ 8

Fast scintillation

Emission ~80% in 25 ns

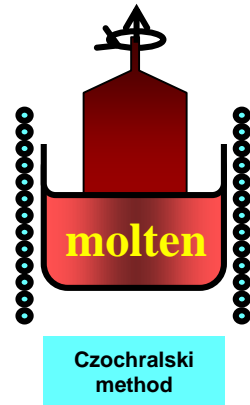
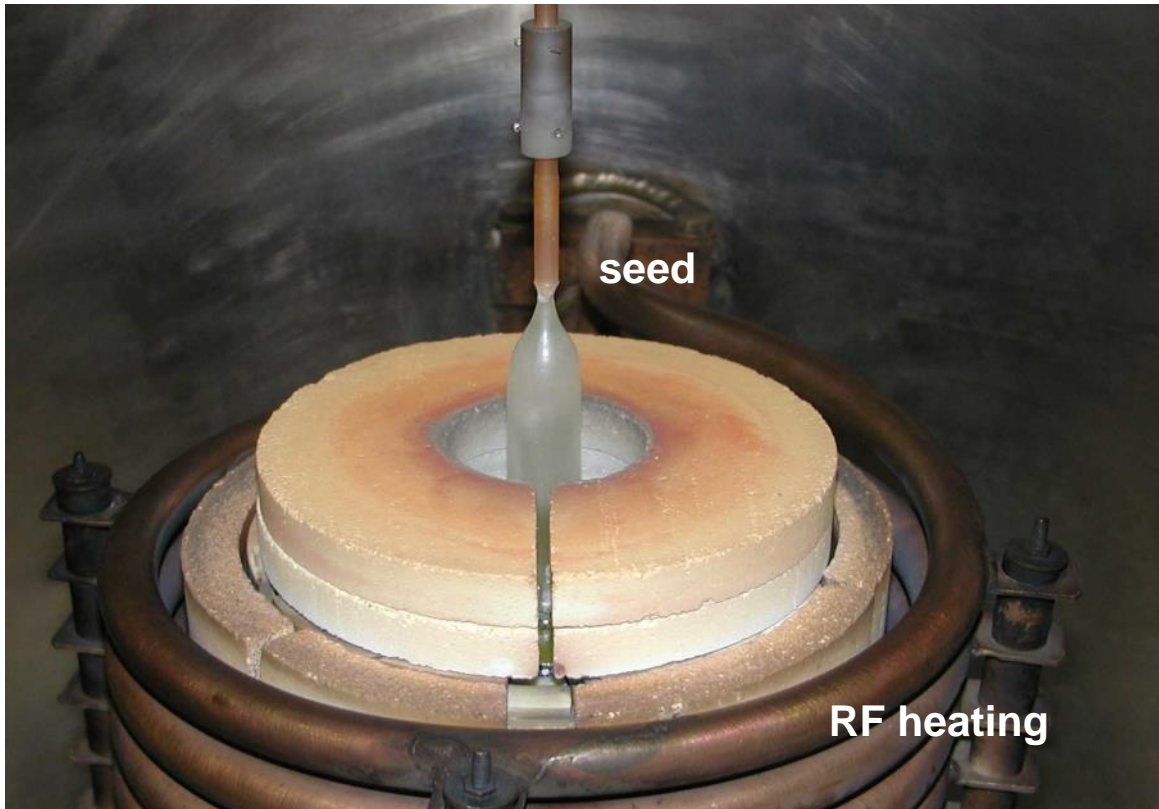
Wavelength 425 nm

Output 150 photons / MeV
(low, only 1% wrt NaI)



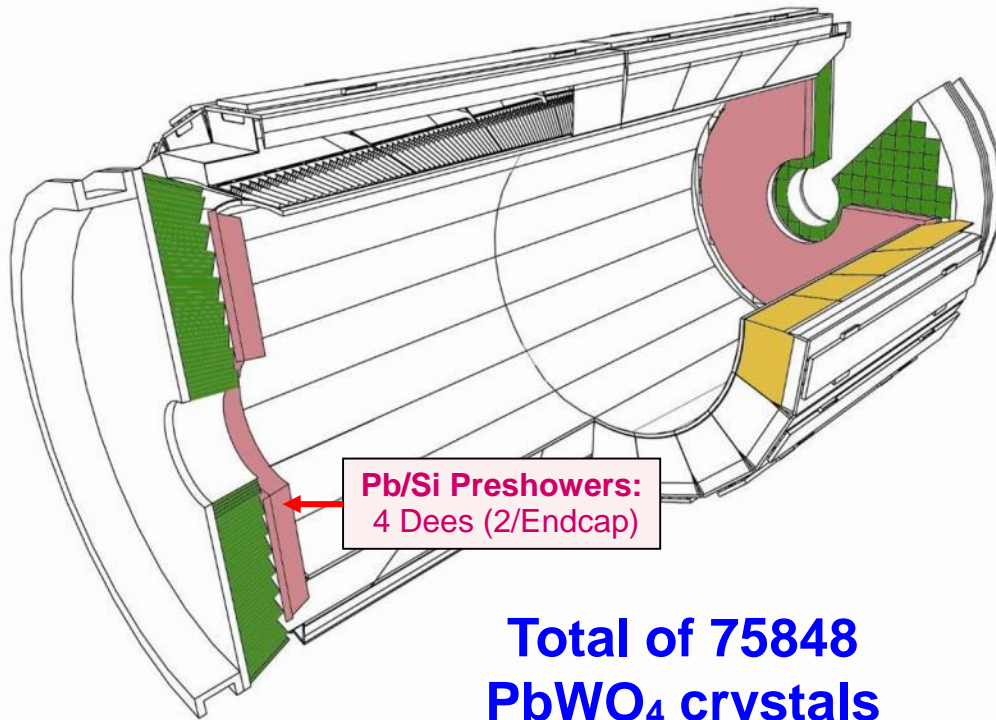
Homogeneous calorimeters

A CMS PbWO_4 crystal 'boule' emerging from its 1123°C melt



Homogeneous electromagnetic calorimeters

CMS at the LHC – scintillating PbWO_4 crystals

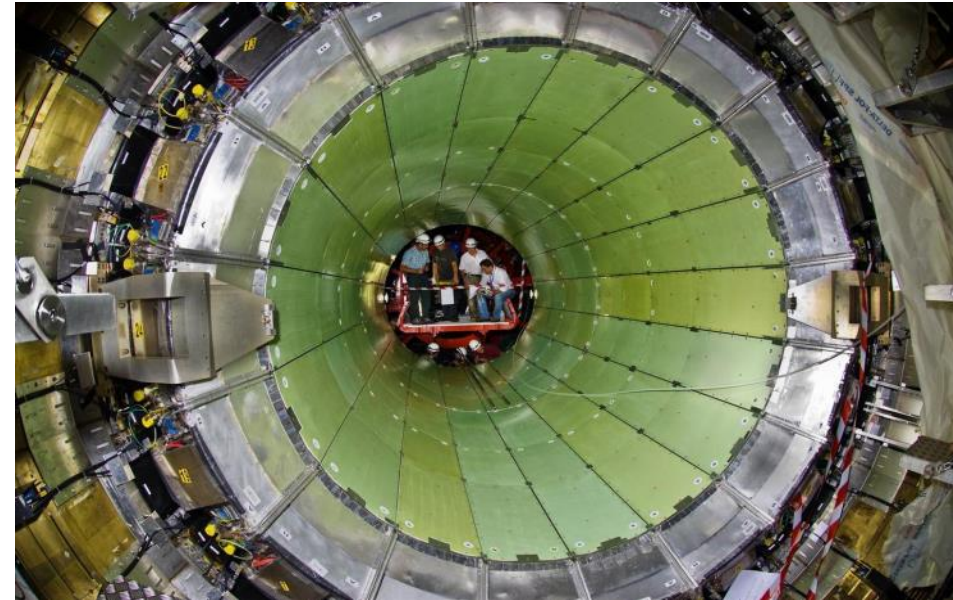


Pb/Si Preshowers:
4 Dees (2/Endcap)

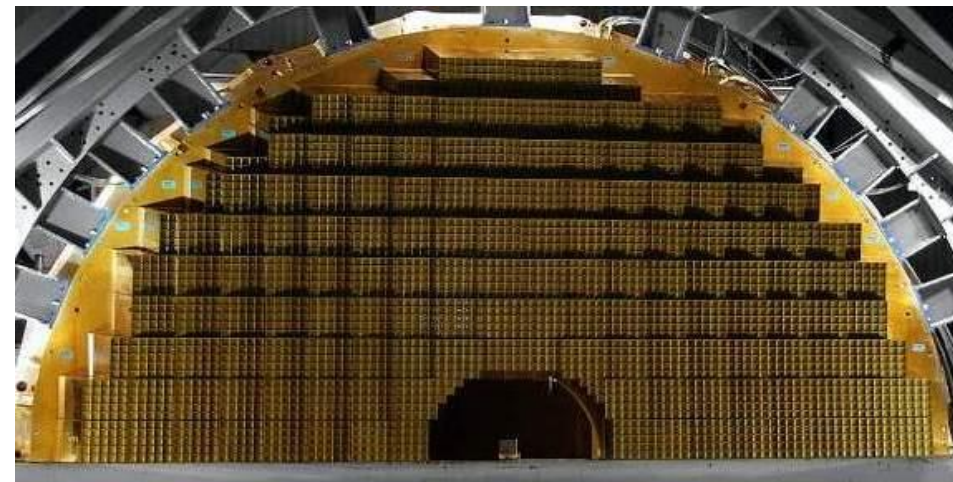
**Total of 75848
 PbWO_4 crystals**

Barrel: 36 Supermodules (18 per half-barrel)
61200 Crystals (34 types) – total mass 67.4 t

Endcaps: 4 Dees (2 per Endcap)
14648 Crystals (1 type) – total mass 22.9 t



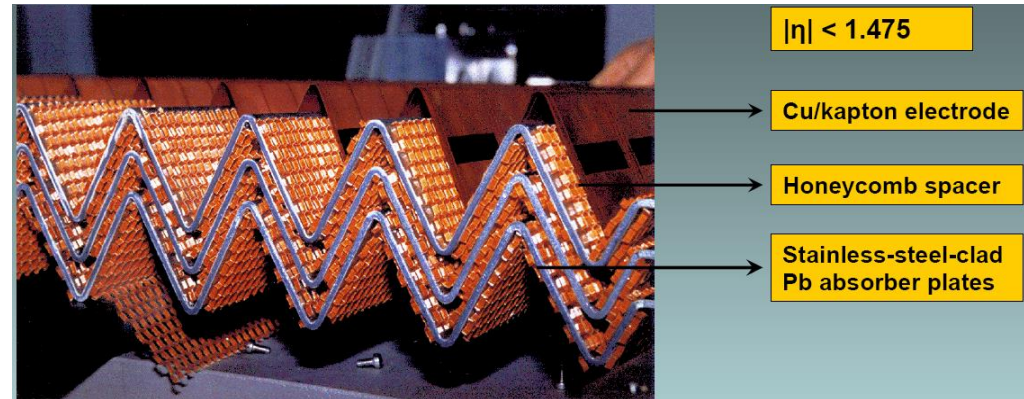
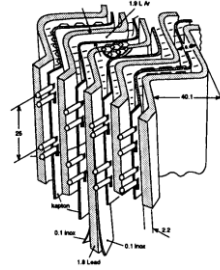
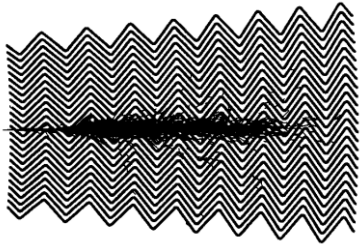
CMS Barrel



An endcap Dee, 3662 crystals awaiting transport

Sampling electromagnetic calorimeters

ATLAS 'Accordion' sampling liquid argon calorimeter at the LHC



Corrugated stainless steel clad Pb absorber sheets, 1-2 mm thick

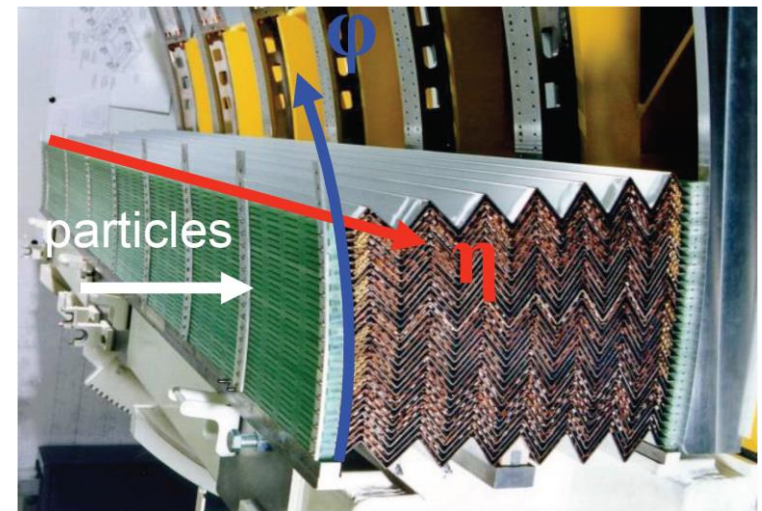
Immersed in liquid argon (90K)

Multilayer Cu-polyimide readout boards

Collect ionisation electrons with an electric field across 2.1 mm liquid Argon drift gap

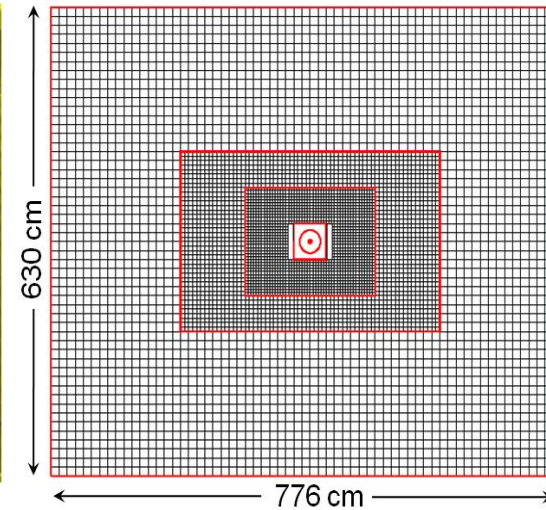
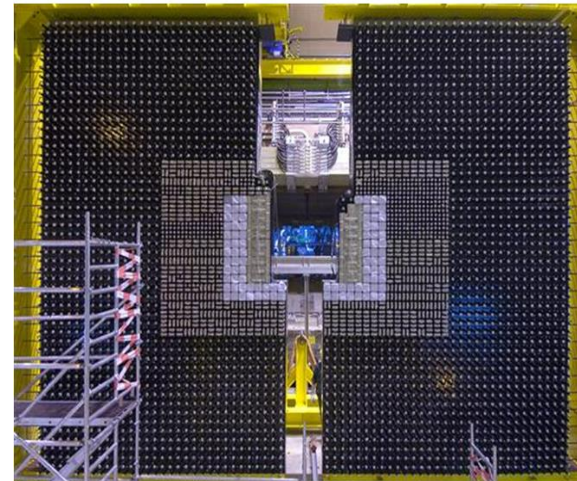
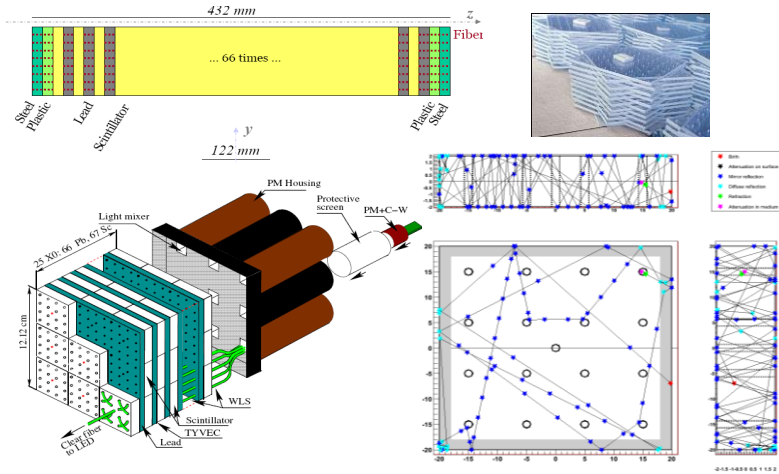
1 GeV energy deposit \rightarrow collect $5 \cdot 10^6 e^-$

Accordion geometry minimises dead zones
Liquid argon intrinsically radiation hard
Readout board allows fine segmentation
(azimuth, rapidity, longitudinal)



Sampling electromagnetic calorimeters

The LHCb sampling electromagnetic calorimeter at the LHC



Wall of 3312 modules

LHCb module

67 scintillator tiles, each 4 mm thick

Interleaved with 66 lead plates, each 2 mm thick

Readout through wavelength shifting fibres running through plates to Avalanche Photodiodes



3 types of modules

Liquid Scintillator Calorimeters

Borexino

Detect **0.862 MeV neutrinos** from ${}^7\text{Be}$ decays in the sun

300 t ultra pure organic liquid scintillator. Less than 10^{-16} g/g of ${}^{238}\text{U}$ and ${}^{232}\text{Th}$

10^4 photons / MeV at 360 nm

3 ns decay time

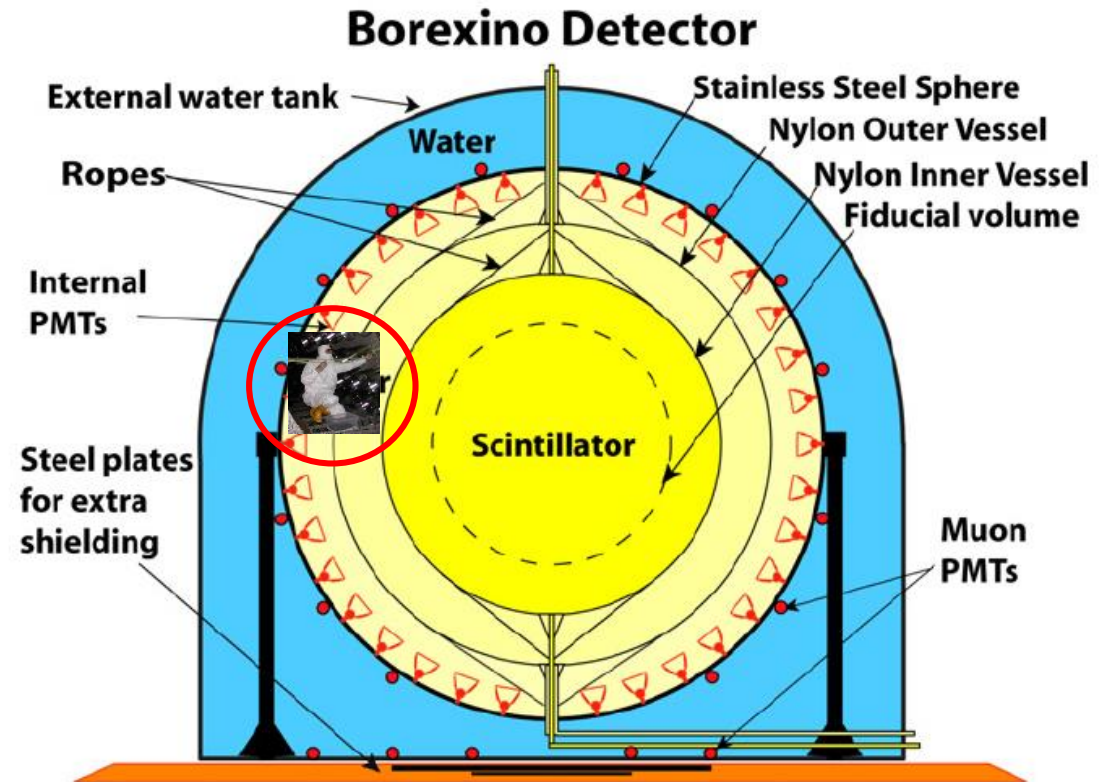
Photon mean free path 8 m

Readout

2,212 photo-multiplier 8 inch tubes

Timing 1 ns

Cluster position resolution 16 cm



Inner sphere, 4.25 m radius

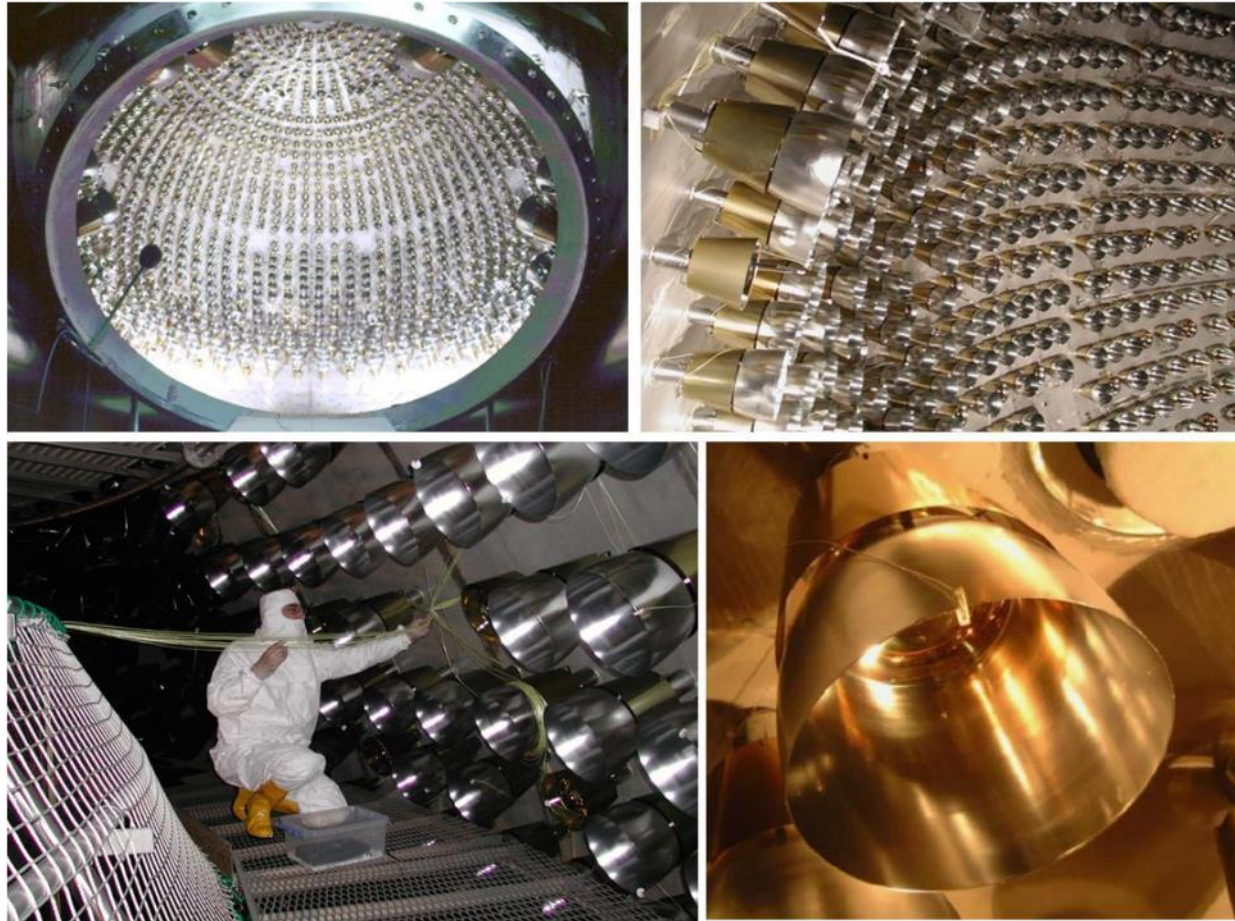
Outer vessel

5.5 m radius

Steel holding vessel

6.85 m radius

Liquid Scintillator Calorimeters



Borexino

Top: Internal surface of stainless steel support sphere + PMTs + their optical concentrators.

Bottom: Preparation of outer vessel + close-up of an optical concentrator.

Energy Resolution

Energy Resolution

Energy resolution of a calorimeter where E is energy of incoming particle:

$$\frac{\sigma}{E} = \frac{a}{\sqrt{E}} \oplus \frac{b}{E} \oplus c$$

a , stochastic term

Fluctuations in the number of signal generating processes,
ie on the number of photo-electrons generated

b , noise term

Noise in readout electronics
'pile-up' due to other particles from other collision events
arriving close in time

Energy Resolution

$$\frac{\sigma}{E} = \frac{a}{\sqrt{E}} \oplus \frac{b}{E} \oplus c$$

c , constant term

Imperfections in calorimeter construction (dimension variations)
Non-uniform detector response

Channel to channel intercalibration errors
Fluctuations in longitudinal energy containment

Energy lost in dead material, before or in detector

Crucial to have small constant term for good energy resolution at the highest particle energies

Energy Resolution

$$\frac{\sigma}{E} = \frac{a}{\sqrt{E}} \oplus \frac{b}{E} \oplus c \quad \leftarrow \text{added in quadrature !}$$

Consider a physics search for a 2 TeV $Z' \rightarrow e^+e^-$

Suppose each electron has energy $E = 1 \text{ TeV} = 1000 \text{ GeV}$

In the CMS electromagnetic calorimeter:

Stochastic term, $a = 3\%$	$3\% / \sqrt{E(\text{GeV})}$	$\sim 0.1\%$
Noise term, $b = 250 \text{ MeV}$	$0.25 \text{ GeV} / E (\text{GeV})$	$\sim 0.0\%$
Constant term, $c = 0.5\%$		0.5%

Resultant resolution, $\sigma/E = 0.1\% \oplus 0\% \oplus 0.5\% \sim 0.5\%$

Resolution at high energies dominated by the constant term

Z' mass will be measured to a precision of $\sim \sqrt{2} * 0.5\% \sim 0.7\% = 14 \text{ GeV}$

With calorimetry, the resolution, σ/E , improves with increasing particle energy

**Goal of calorimeter design - find best compromise between the three contributions
- at a price you can afford !**

Intrinsic resolution of homogeneous e.m. calorimeters

Energy released in the detector material mainly ionisation and excitation

Mean energy required to produce a 'visible' scintillation photon

in a crystal or an electron-ion pair in a noble liquid

Q

Mean number of quanta produced

$$\langle n \rangle = E_0 / Q$$

The intrinsic energy resolution is given by the fluctuations on 'n'

$$\sigma_E / E = \sqrt{n} / n = \sqrt{Q / E}$$

Typically obtain σ_E / E 1% - 3% / \sqrt{E} (GeV)

However, in certain cases:

Energy of the incident particle is **only** transferred to making quanta, and to no other energy dissipating processes, for example in Germanium.

Fluctuations much reduced:

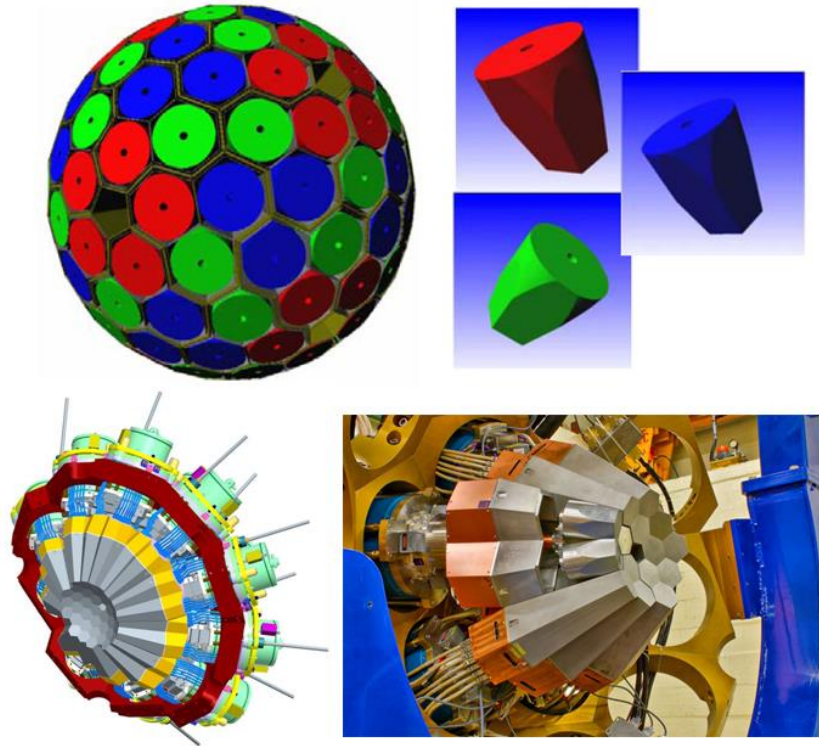
$$\sigma_E / E = \sqrt{FQ / E} \quad \text{where } F \text{ is the 'Fano' factor .}$$

F ~ 0.1 in Ge

Detector resolution in **AGATA** 0.06% (rms) for 1332 keV photons

Intrinsic em energy resolution for homogeneous calorimeters

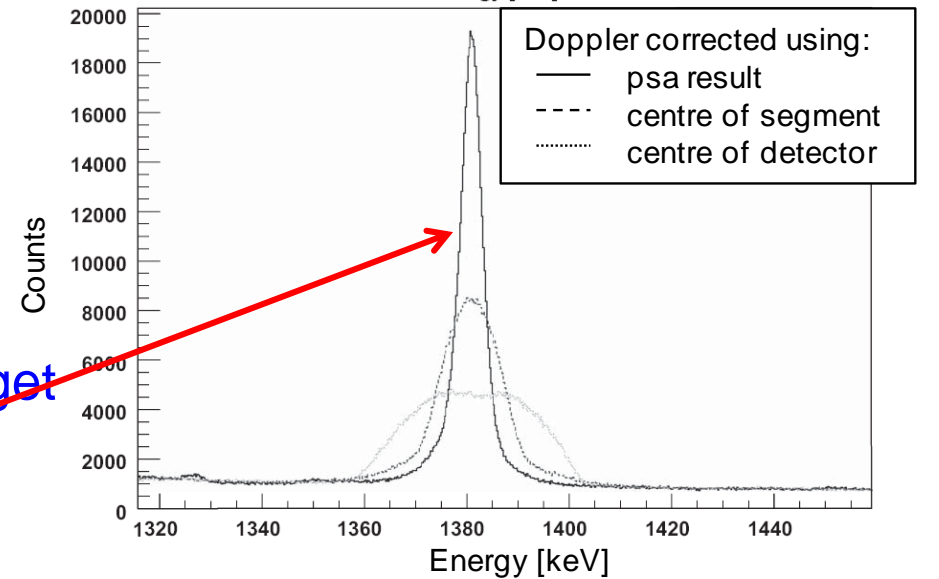
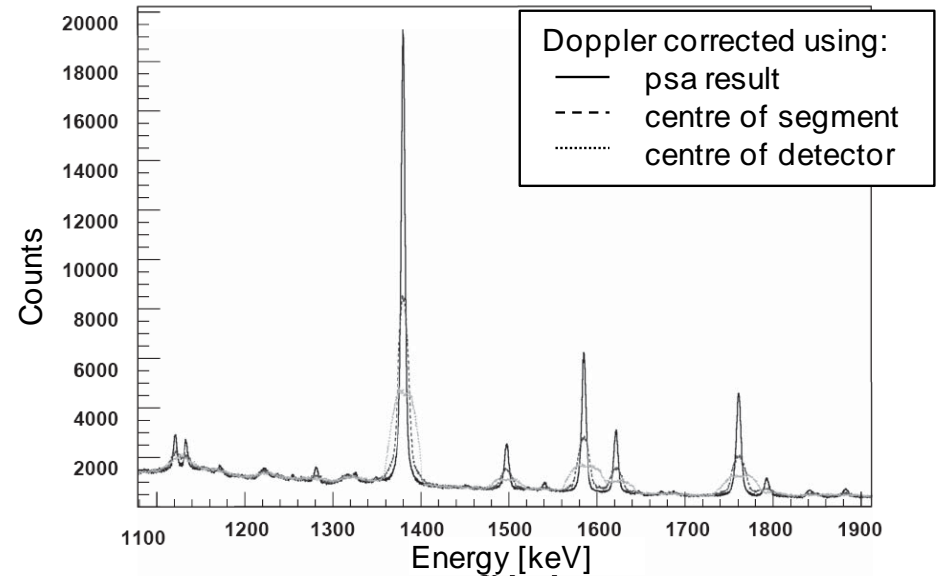
The AGATA Germanium detector



Experiment with excited nuclei from a target
1382 keV line width 4.8 keV (fwhm)

Resolution 0.15%

Resolution 0.06% with a source



Energy resolution for crystal em calorimeters

Energy resolution - the CMS PbWO₄ crystal calorimeter

Scintillation emission only small fraction of energy loss in crystal, so Fano factor, $F \sim 1$

However – get fluctuations in the avalanche process in the Avalanche Photodiodes (APDs) used for the photo-detection
- gives rise to an **excess noise factor** for the gain of the device

$F \sim 2$ for the crystal + APD combination

$N_{pe} \sim 4500$ photo-electrons released by APD, per GeV of deposited energy

Stochastic term $a_{pe} = \sqrt{F / N_{pe}} = \sqrt{(2 / 4500)} = 2.1\%$

This assumes total lateral shower containment

In practice energy summed over limited 3x3 or 5x5 arrays of crystals, to minimise added noise

Expect $a_{leak} = 2\%$ from an energy sum over a 3x3 array of crystals

Expect a stochastic term of $a = a_{pe} \oplus a_{leak} = 2.9\%$
Measured value 2.8%

Energy resolution in homogeneous em calorimeters

Energy resolution

CMS ECAL , 3x3 array of PbWO₄ crystals

Test beam electrons

a , stochastic term = 2.83%

c , constant term = 0.26%

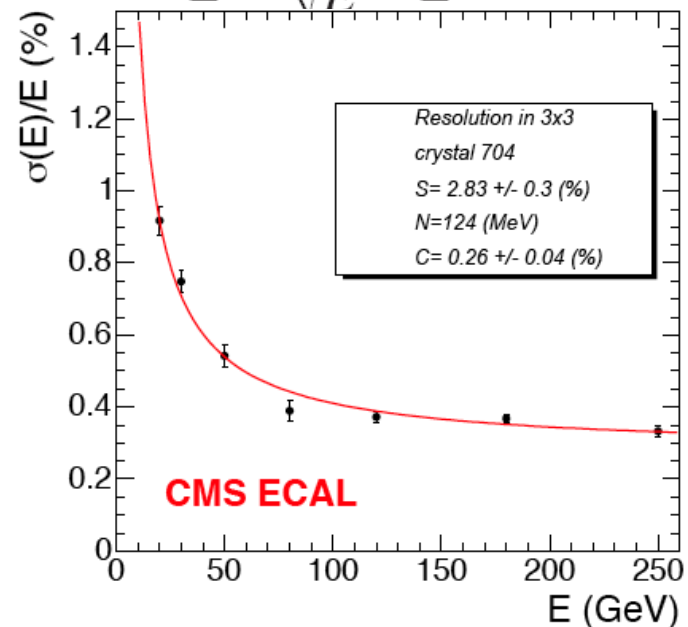
Borexino

Photoelectron yield ~500 per MeV

Expect $\sqrt{500} / 500 = 4.4\%$

Measured ~5% at 1 MeV

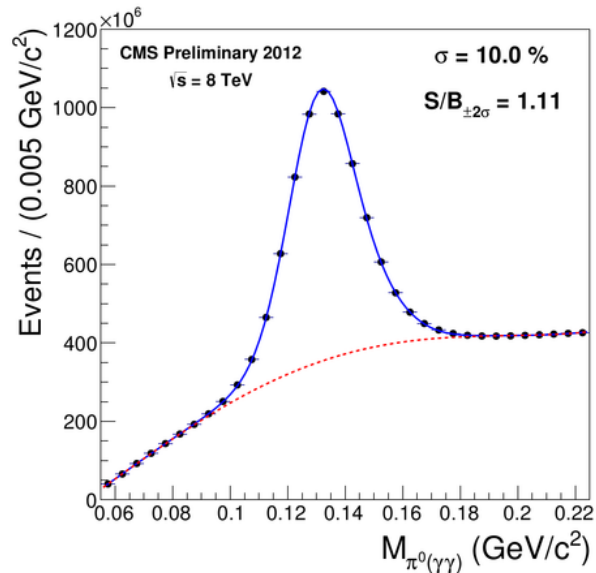
$$\frac{\sigma}{E} = \frac{a}{\sqrt{E}} \oplus \frac{b}{E} \oplus c$$



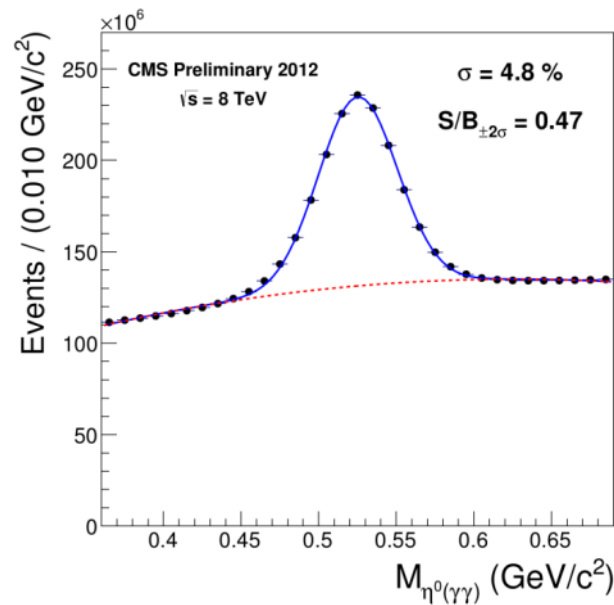
Calibration of the detector

Prior to installation: modules taken to test beams at CERN and elsewhere

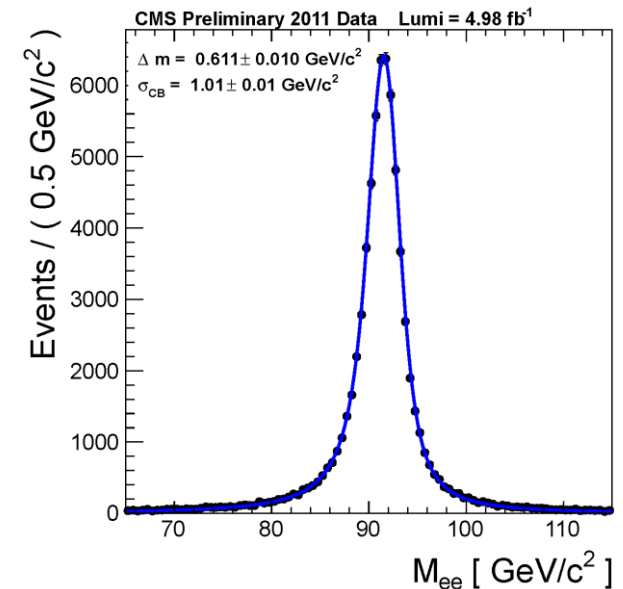
In situ in CMS: trigger, record and use known resonances to calibrate the crystals



$\pi^0 \rightarrow \gamma\gamma$



$\eta \rightarrow \gamma\gamma$



$Z \rightarrow ee$

peak at 91 GeV

width of Gaussian 1.01 GeV

Crucial input for resolution

estimates for $H \rightarrow \gamma\gamma$ at 125 GeV

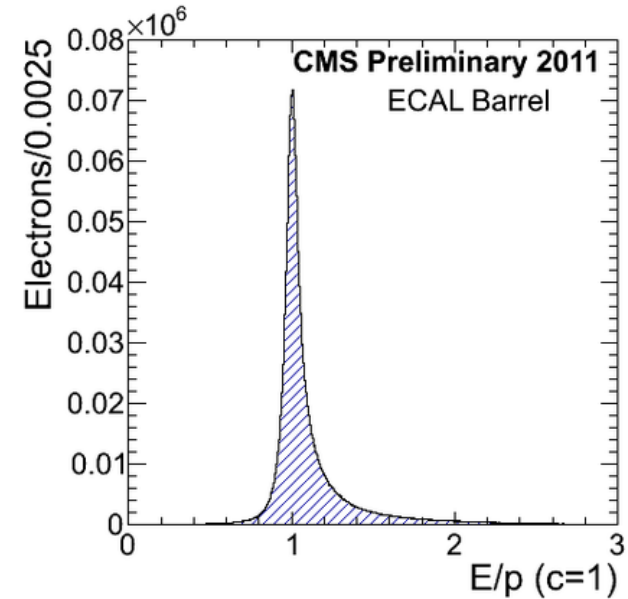
In situ in CMS also use:

W decays, $W \rightarrow e^\pm \nu$

Electron energy, E , measured in the ECAL

Electron momentum, p , measured in the Tracker

Optimize the E/p distributions ($E/p = 1$ ideally)

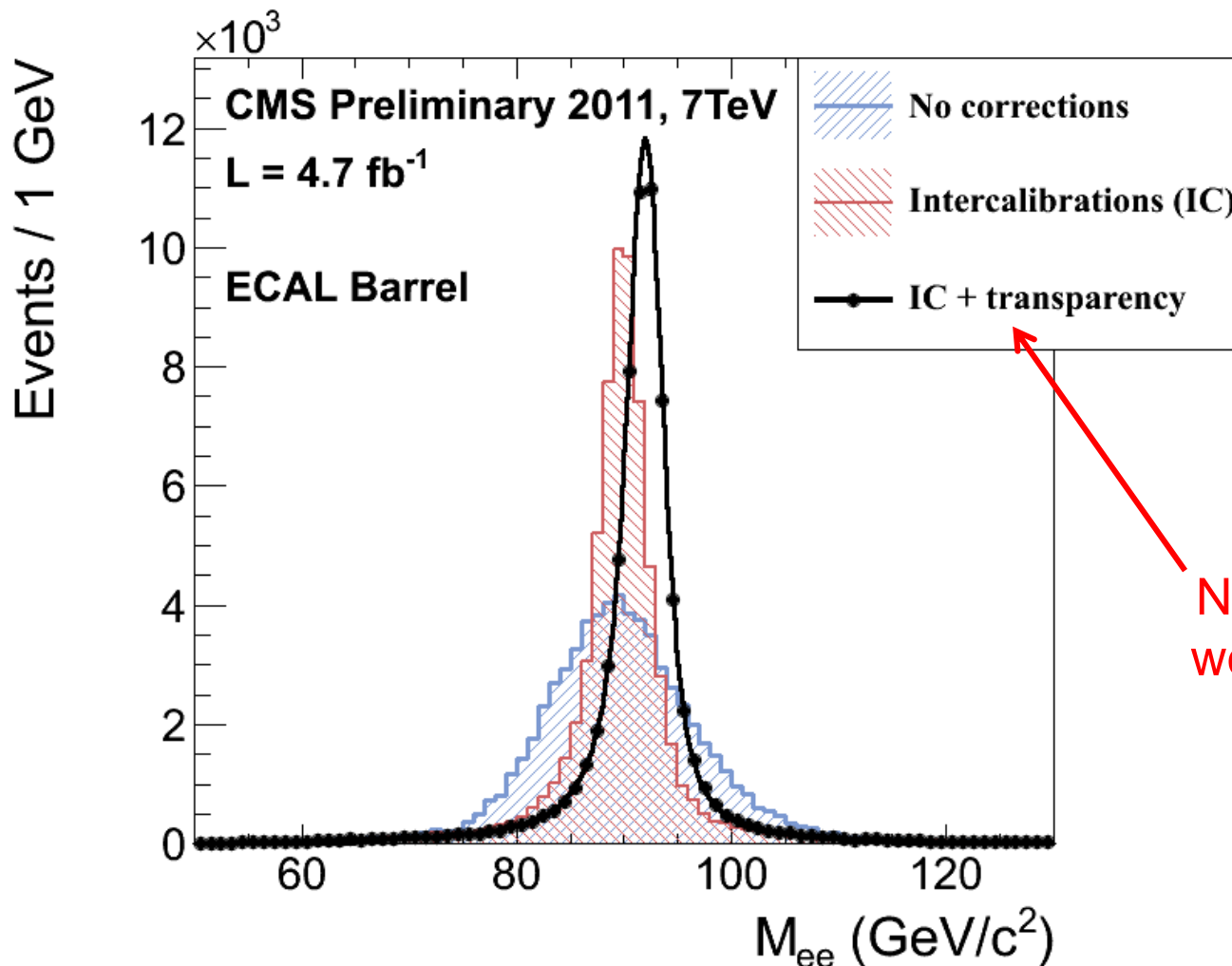


Phi symmetry (gives quick initial values)

The transverse energy flow, summed over many “minimum bias” collisions, should be the same towards any phi angle

Use this symmetry to calibrate rings of individual crystals sitting at the same pseudorapidity

Getting excellent energy resolution – in a real detector !!



Note the crucial work needed for the various corrections

Instrumental resolution of 1.01 GeV from Z \rightarrow ee decays in the CMS ECAL Barrel

Intrinsic resolution of sampling electromagnetic calorimeters

Sampling fluctuations arise due to variations in the number of charged particles crossing the active layers

$$n_{\text{charged}} \propto E_0 / t \quad (t = \text{thickness of each absorber layer})$$

If each sampling is independent $\sigma_{\text{samp}} / E = 1 / \sqrt{n_{\text{charged}}} \propto \sqrt{t / E}$

Need ~100 sampling layers to compete with homogeneous devices.

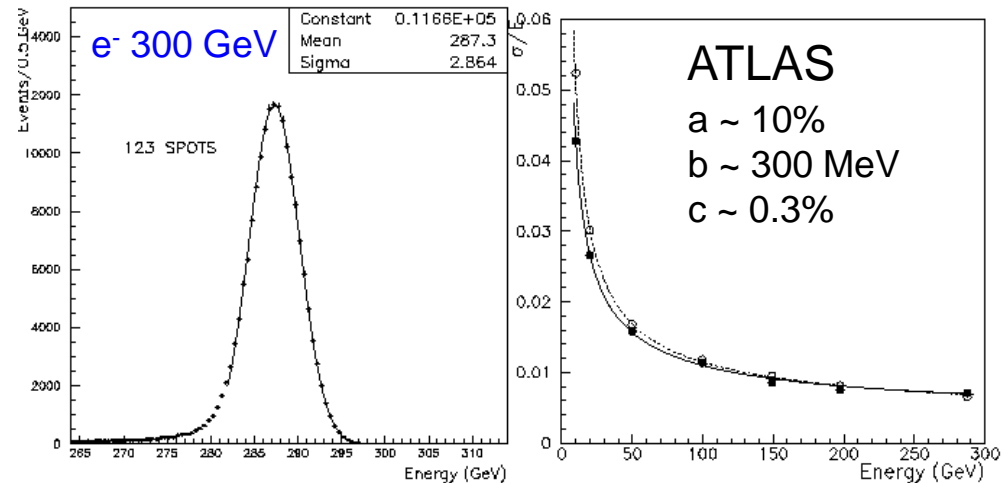
Typically $\sigma_{\text{samp}}/E \sim 10\%/\sqrt{E}$

Intrinsic energy resolution for sampling e.m. calorimeters

Intrinsic resolution of sampling electromagnetic calorimeters

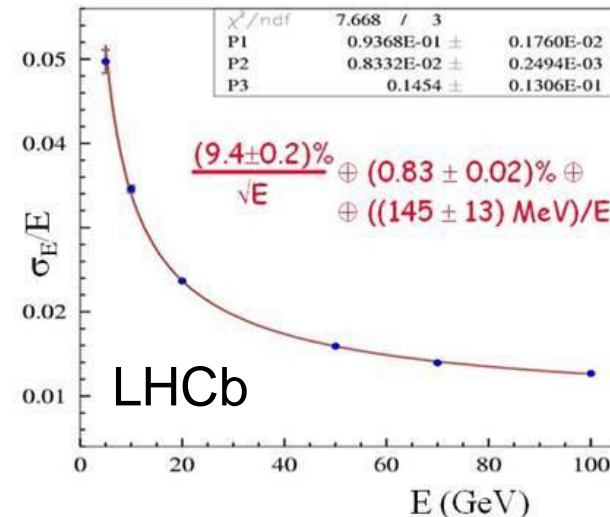
ATLAS stochastic term ~10%
 constant term 0.3%

Thickness of the 1-2 mm thick absorber sheets controlled to 6.6 μm to achieve a constant term of 0.3%



Also: ATLAS spatial resolution $\sim 5\text{mm} / \sqrt{E}$ (GeV)

LHCb stochastic term 9.4%
 constant term 0.83%



Hadronic Calorimetry

Hadronic Cascades

Hadronic cascades much more complex than e.m. cascades

Shower development determined by the mean free path, λ_I , between inelastic collisions

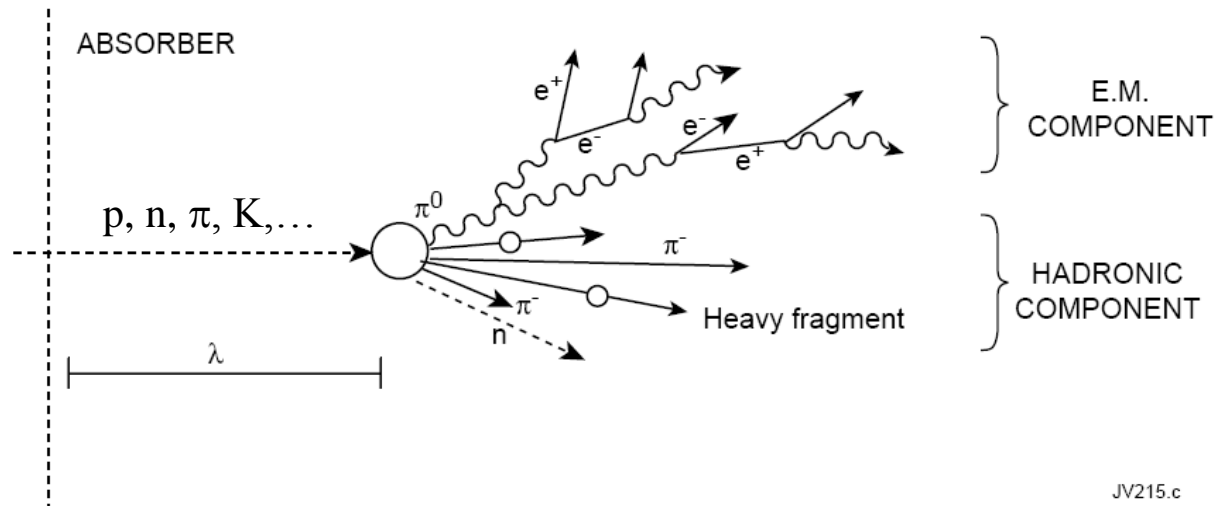
The nuclear interaction length is given by $\lambda_I = A / (N_A \cdot \sigma_{inel})$, $\sigma_{inel} \approx \sigma_0 A^{0.7}$ $\sigma_0 \approx 35 \text{ mb}$

Expect $\sigma_I \propto A^{2/3}$ and thus $\lambda_I \propto A^{1/3}$.

In practice, $\lambda_I \sim 35 A^{1/3} = 16.7 \text{ cm}$ in iron

High energy hadrons interact with nuclei producing secondary particles, mostly π^\pm and π^0

Lateral spread of shower from transverse energy of secondaries, $\langle p_T \rangle \sim 350 \text{ MeV}/c$



JV215.c

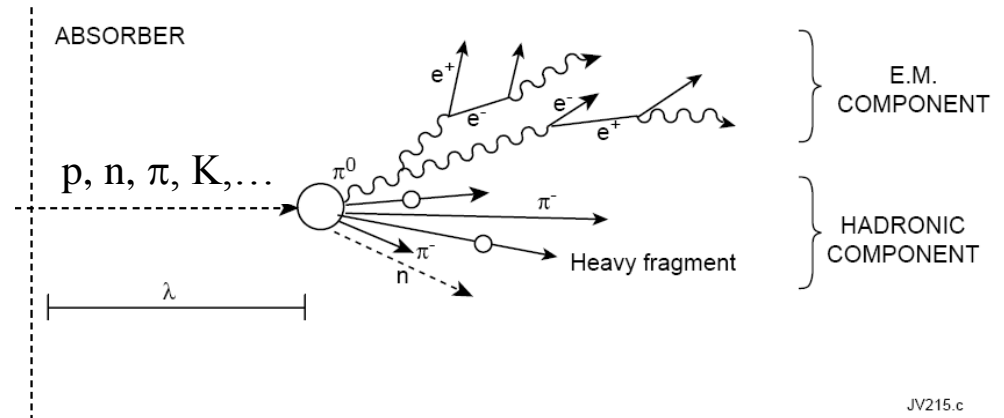
Hadronic Cascades

For a collision with a nucleus:

Multiplicity of secondary particles $\propto \ln(E)$

$\sim 1/3$ of the pions produced are neutral pions, π^0
 $n(\pi^0) \sim \ln E (\text{GeV}) - 4.6$

For a 100 GeV incoming hadron, $n(\pi^0) \approx 18$



The neutral pions quickly decay to two electromagnetic particles (2 photons)

$\pi^0 \rightarrow \gamma\gamma$ in $\sim 10^{-16}$ s

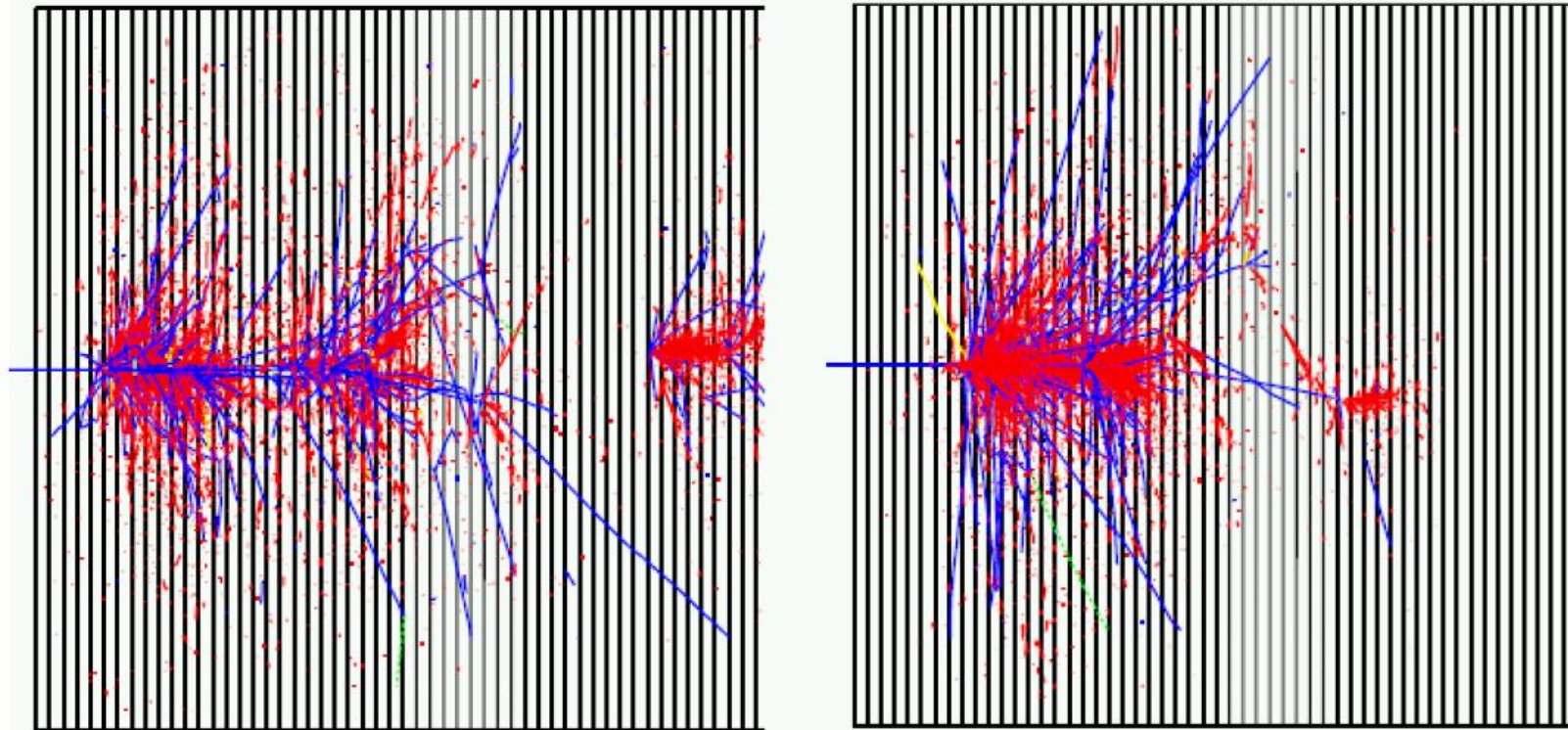
Thus hadronic cascades have two distinct components:

hadronic (largely π^+ , π^- , heavy fragments, excited nuclei) and electromagnetic ($\gamma\gamma$)

This gives rise to a much more complex cascade development which limits the ultimate resolution possible for hadronic calorimetry

Hadronic Cascades

Simulations of hadron showers



Red - e.m. component **Blue** – charged hadrons

Unlike electromagnetic showers, hadron showers do not show a uniform deposition of energy throughout the detector medium

Hadronic Cascades

Hadronic longitudinal shower development

The e.m. component more pronounced at the start of the cascade than the hadronic component

Shower profile characterised by a peak close to the first interaction, Then, an exponential fall off with scale λ_1

$$t_{\max}(\lambda_1) \approx 0.2 \ln E[\text{GeV}] + 0.7$$

$$t_{95\%}(\text{cm}) \approx a \ln E + b$$

To contain 95% of the energy in Iron:

$a = 9.4, b = 39$. For $E = 100 \text{ GeV}$, $t_{95\%} \approx 80 \text{ cm}$

For adequate containment, need $\sim 10 \lambda_1$

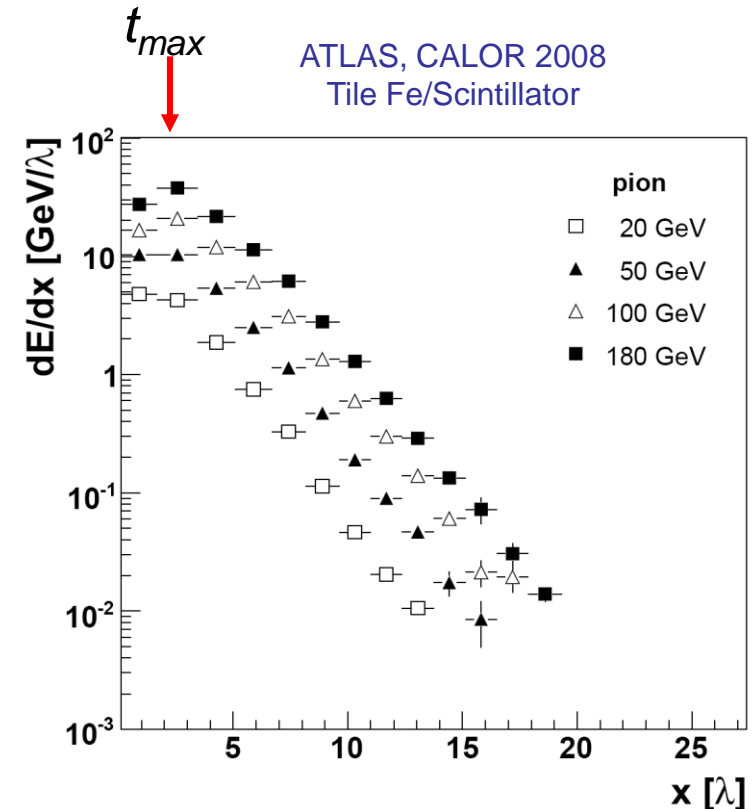
In Iron, need 1.67 m. In Copper need 1.35 m

Hadronic lateral shower development

The shower consists of core + halo

95% containment : cylinder of radius $\lambda_1 = 16.7 \text{ cm}$ in iron

Compare to a radius of **2.19 cm** for an em cascade in PbWO_4



Longitudinal profile of pion induced showers at various energies

Comparison – electromagnetic showers vs hadronic showers

Electromagnetic versus hadronic scale for calorimetry

$$X_0 \sim 180 A / Z^2 \quad \ll \quad \lambda_I \sim 35 A^{1/3}$$

E.M shower size in PbWO4 **23 cm deep x 2.19 cm radius**

Hadron shower size in Iron **80 cm deep x 16.7 cm radius**

Hadron cascades much longer and broader than electromagnetic cascades

Hadron calorimeters much larger than em calorimeters

Detectors for Hadronic Calorimetry

Hadron Sampling Calorimeters

CMS Hadron calorimeter at the LHC

Brass absorber preparation

Workers in Murmansk
sitting on brass casings of
decommissioned shells of
the Russian Northern Fleet

Explosives previously
removed!

Casings melted in St
Petersburg and turned into
raw brass plates

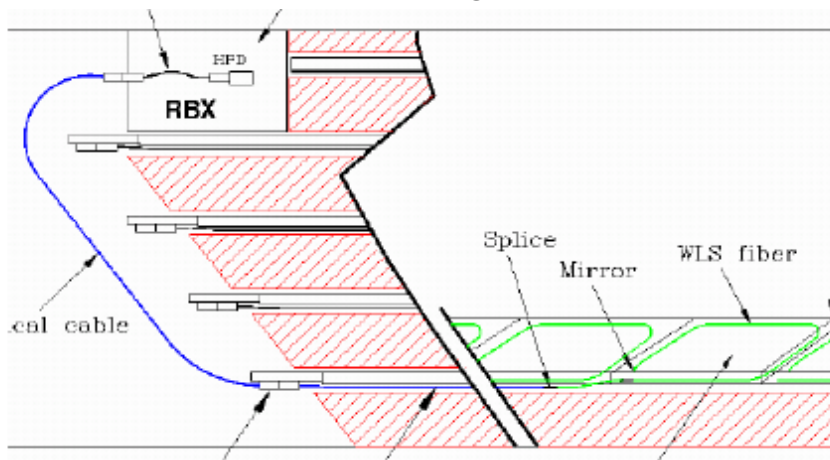
Machined in Minsk and
mounted to become
absorber plates for the CMS
Endcap Hadron Calorimeter



CMS Hadron sampling calorimetry

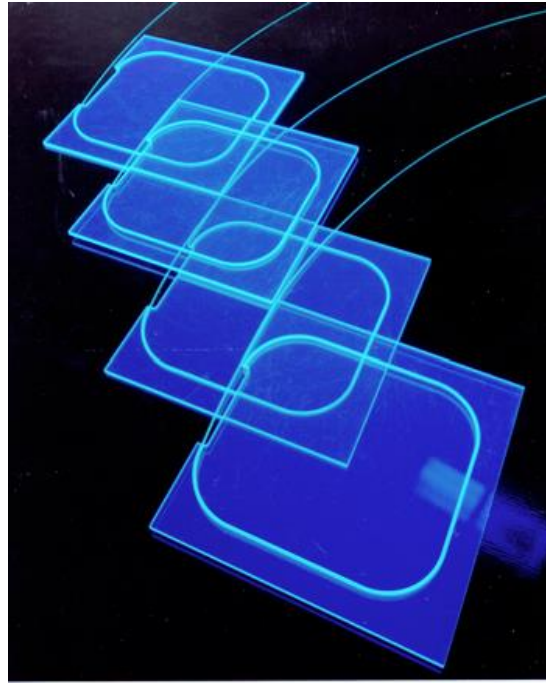
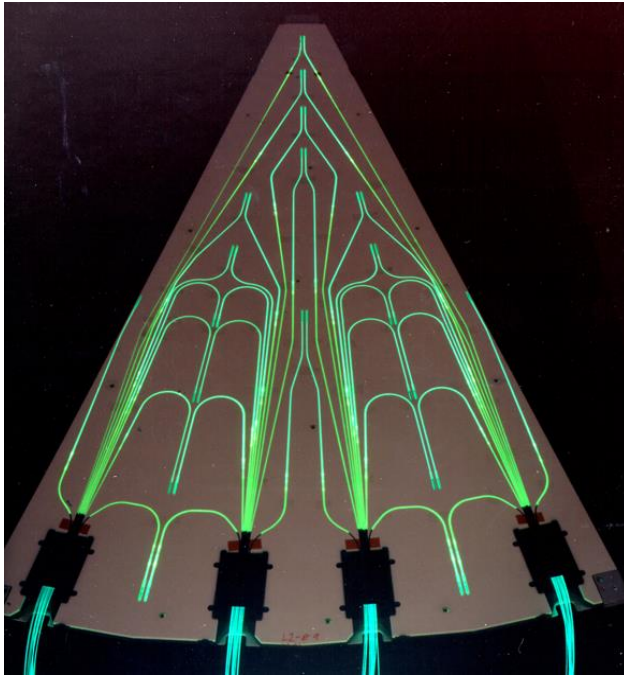


The CMS HCAL being inserted into the solenoid



Light produced in the scintillators is transported through optical fibres to Hybrid Photo Diode (HPD) detectors

CMS HCAL – fibre readout

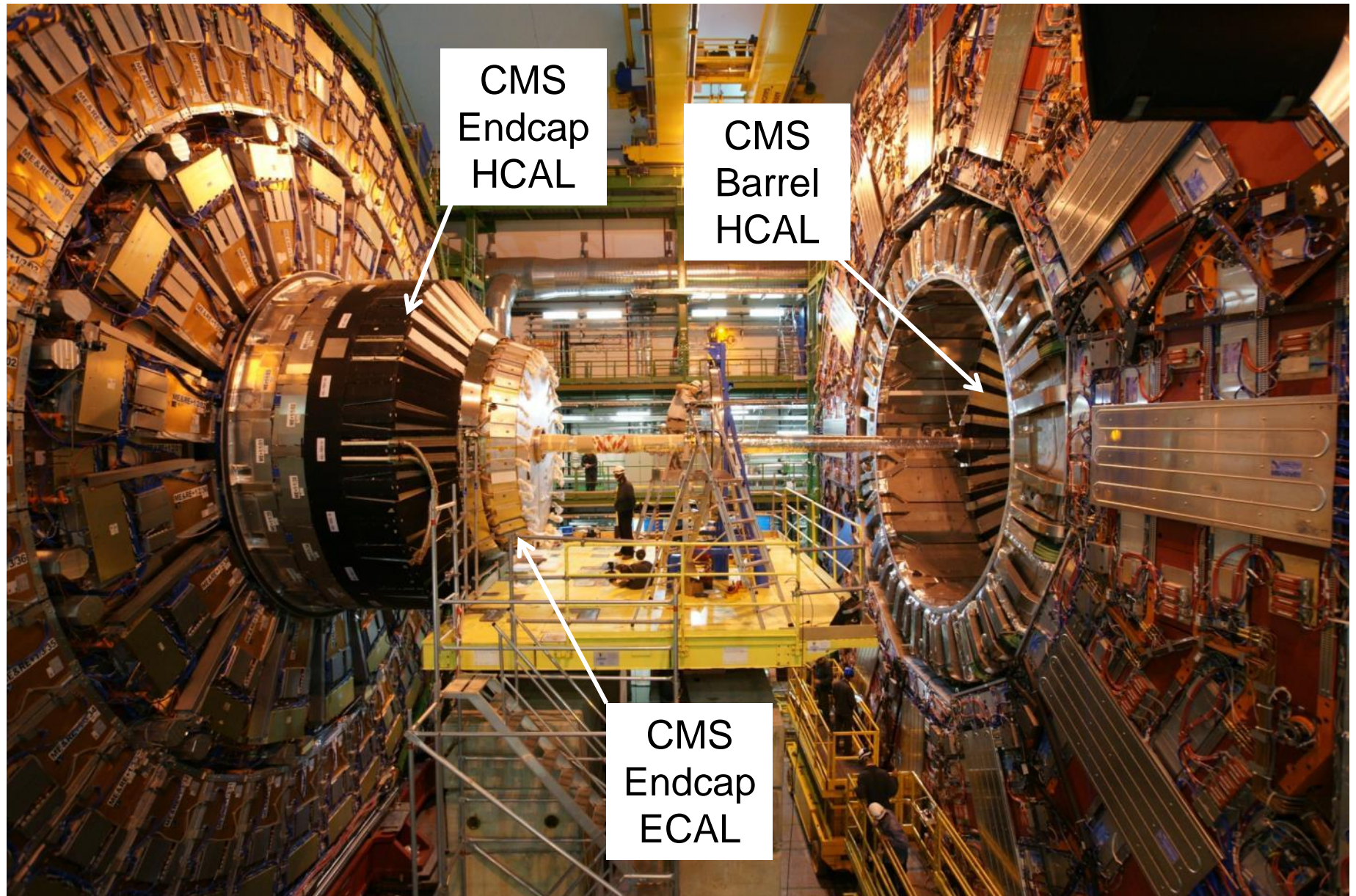


Light emission from the scintillator tiles blue-violet, $\lambda = 410\text{-}425$ nm.

This light is absorbed by wavelength shifting fibers which fluoresce in the green, $\lambda = 490$ nm.

The green light is conveyed via clear fiber waveguides to connectors at the ends of the scintillator megatiles.

CMS Hadron sampling calorimetry



Energy resolution of hadronic calorimeters

Hadron calorimetry resolution

Strongly affected by the energy lost as ‘invisible energy’:

- nuclear excitation followed by delayed photons (by up to to $\sim 1\mu\text{sec}$, so usually undetected)
- soft neutrons
- nuclear binding energy

Fluctuations in the ‘invisible energy’ play an important part in the degradation of the intrinsic energy resolution

Further degradation

If the calorimeter responds differently as a function of energy to the em component of the cascade ($\pi^0 \rightarrow \gamma\gamma$)

$F_{\pi^0} \sim 1/3$ at low energies

$F_{\pi^0} \sim a \log(E)$ (the em part increases or ‘freezes out’ with energy)

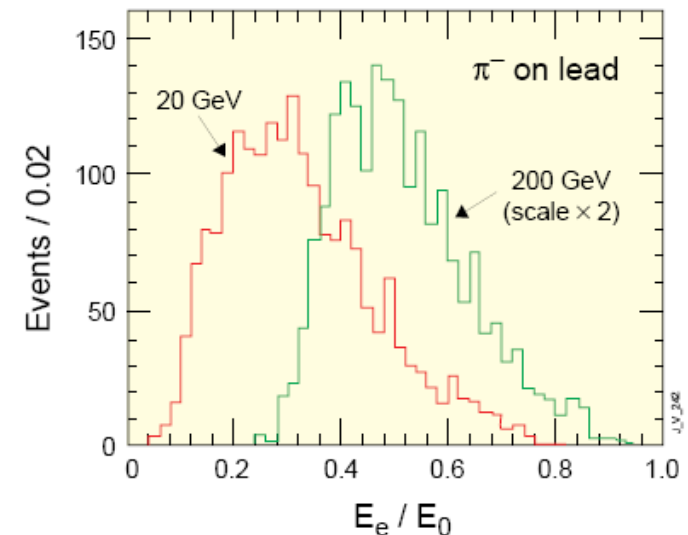
Hadron energy dissipation in Pb

Nuclear break-up (invisible) 42%

Charged particle ionisation 43%

Neutrons with $T_N \sim 1 \text{ MeV}$ 12%

Photons with $E_\gamma \sim 1 \text{ MeV}$ 3%



EM fraction for 20 GeV and 200 GeV pions on lead

In general, the **hadronic** component of a hadron shower produces a smaller signal than the em component

$$\text{so } e/h > 1$$

Consequences for $e/h \neq 1$

- response with energy is non-linear
- fluctuations of the em component of the cascade, F_{π^0} , worsen the energy resolution, σ_E/E

The fluctuations are non-Gaussian, consequently

- σ_E/E improves more slowly with energy than for an electromagnetic calorimeter
- More as $1/E$ than $1/\sqrt{E}$

‘Compensating’ sampling hadron calorimeters seek to restore $e/h = 1$ to achieve better resolution and linearity (see backup slide)

Single hadron energy resolution in CMS at the LHC

Compensated hadron calorimetry & high precision em calorimetry are usually incompatible

In CMS, hadron measurement combines **HCAL** (Brass/scint) and ECAL(PbWO₄) data

Effectively a hadron calorimeter divided in depth into two compartments

Neither compartment is 'compensating':

$e/h \sim 1.6$ for ECAL

$e/h \sim 1.4$ for HCAL

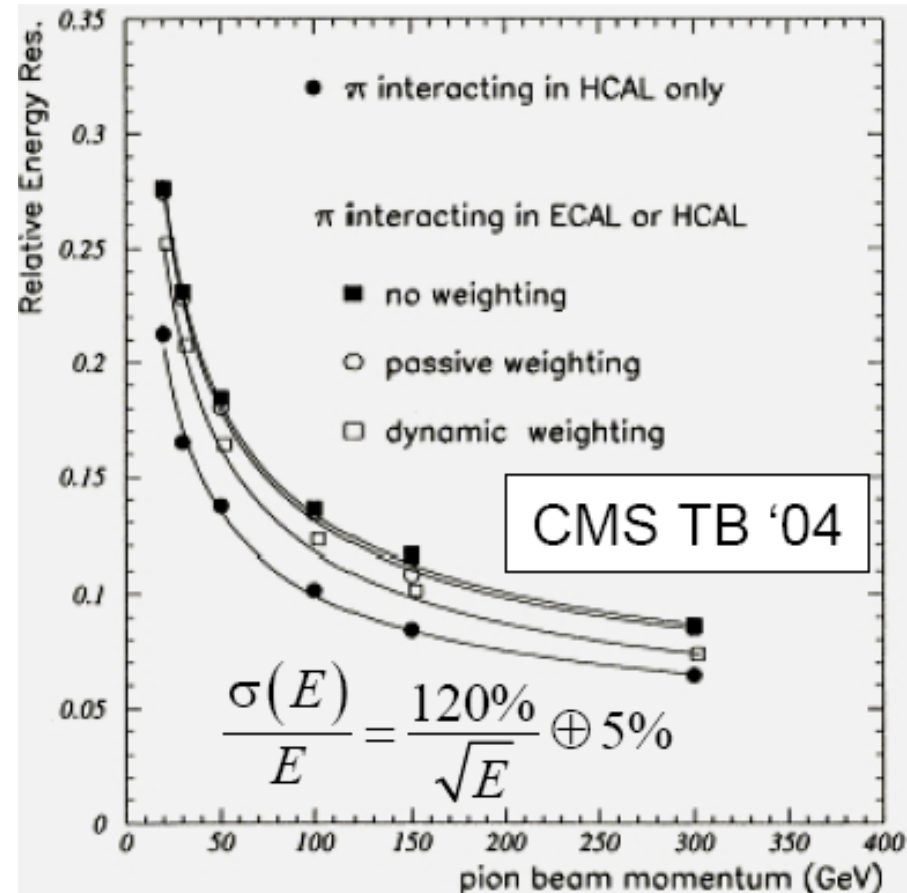
Hadron energy resolution is degraded and response is energy-dependent

Stochastic term

a = 120%

Constant term

c = 5%



CMS energy resolution for single pions up to 300GeV

Jets and Particle Flow

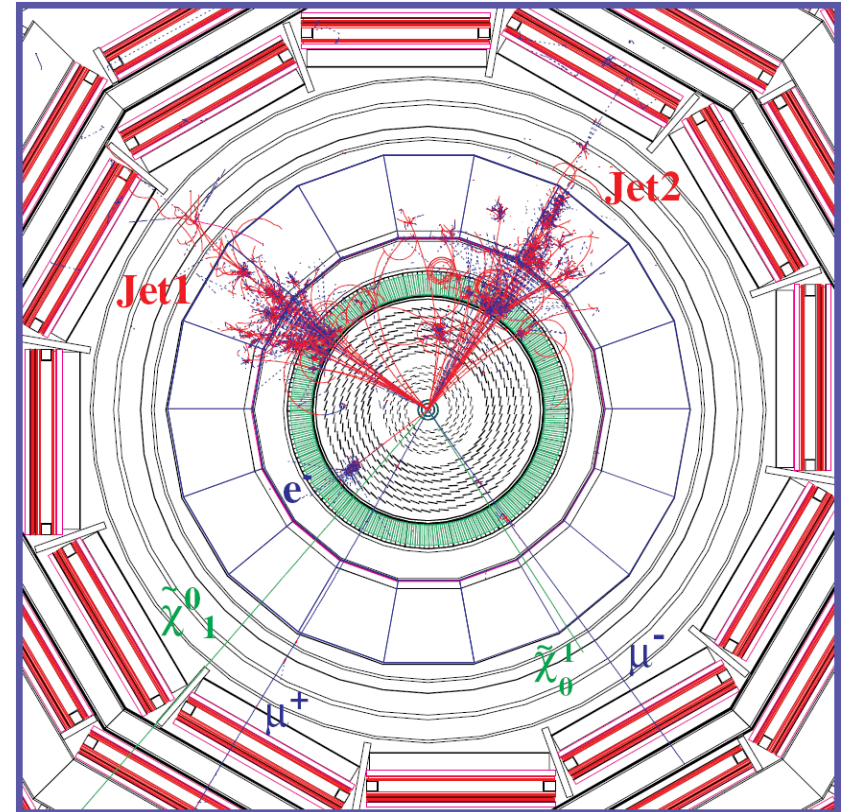
The measurement of Jets and Particle Flow

At colliders, hadron calorimeters serve primarily to measure jets and missing E_T

Single hadron response gives an indication of the level to be expected for jet energy resolution

Make combined use of

- Tracker information
- fine grained information from the ECAL and HCAL detectors



Jets from a simulated event in CMS

Traditional approach

Components of jet energy only measured in ECAL and HCAL

In a typical jet

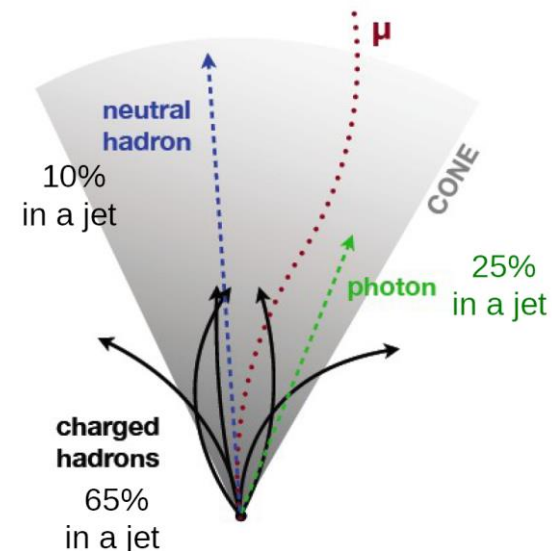
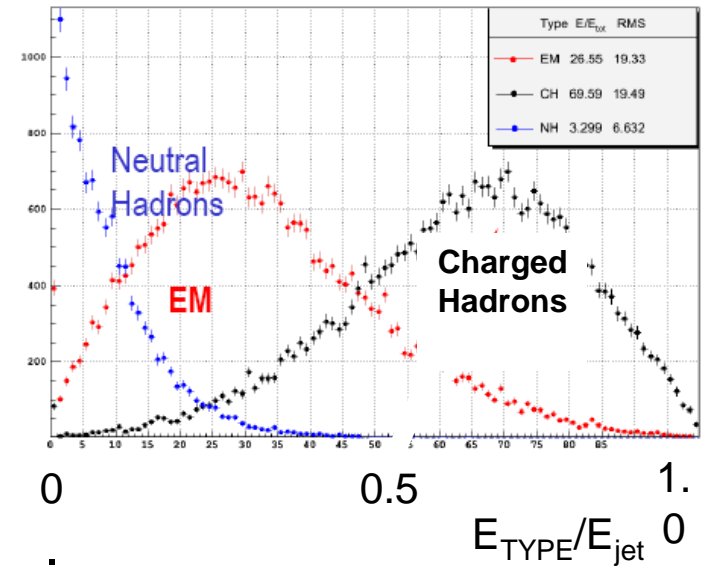
- 65% of jet energy in **charged** hadrons
- 25% in **photons** (mainly from $\pi^0 \rightarrow \gamma\gamma$)
- 10% in **neutral hadrons**

Particle Flow Calorimetry

- Charged particles measured with tracker, when better
- Photons measured in ECAL
- Leaves only neutral hadrons in HCAL (+ECAL)

Only 10% of the jet energy (the neutral hadrons) left to be measured in the poorer resolution HCAL

Dramatic improvements for overall jet energy resolution



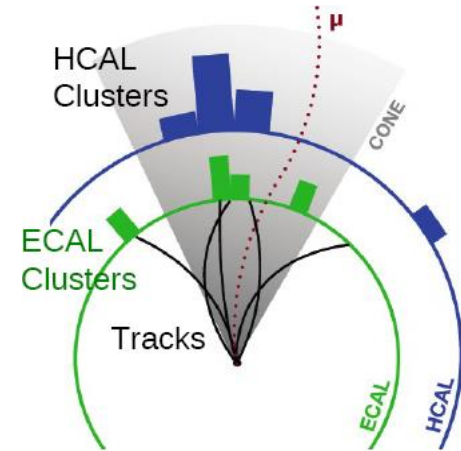
Jet measurements with Particle Flow

Momenta of particles inside a jet

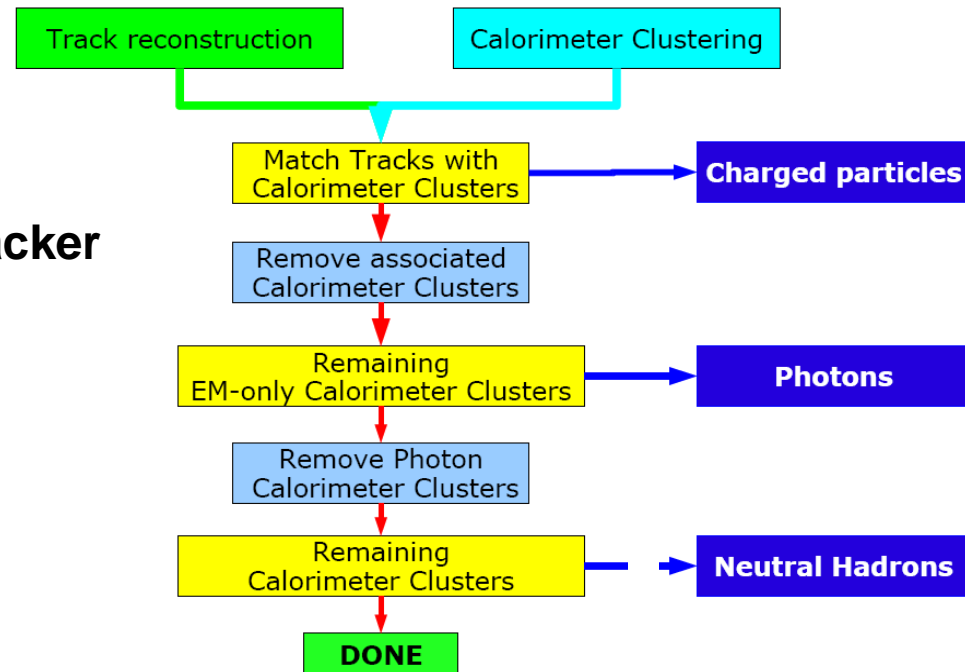
Consider a quark/gluon jet, total $p_T = 500 \text{ GeV}/c$

Average p_T carried by the stable constituent particles of the jet $\sim 10 \text{ GeV}$

Jets with $p_T < 100 \text{ GeV}$, constituents $\mathcal{O}(\text{GeV})$



For charged particles with momenta $\mathcal{O}(\text{GeV})$ better to use momentum resolution of the Tracker

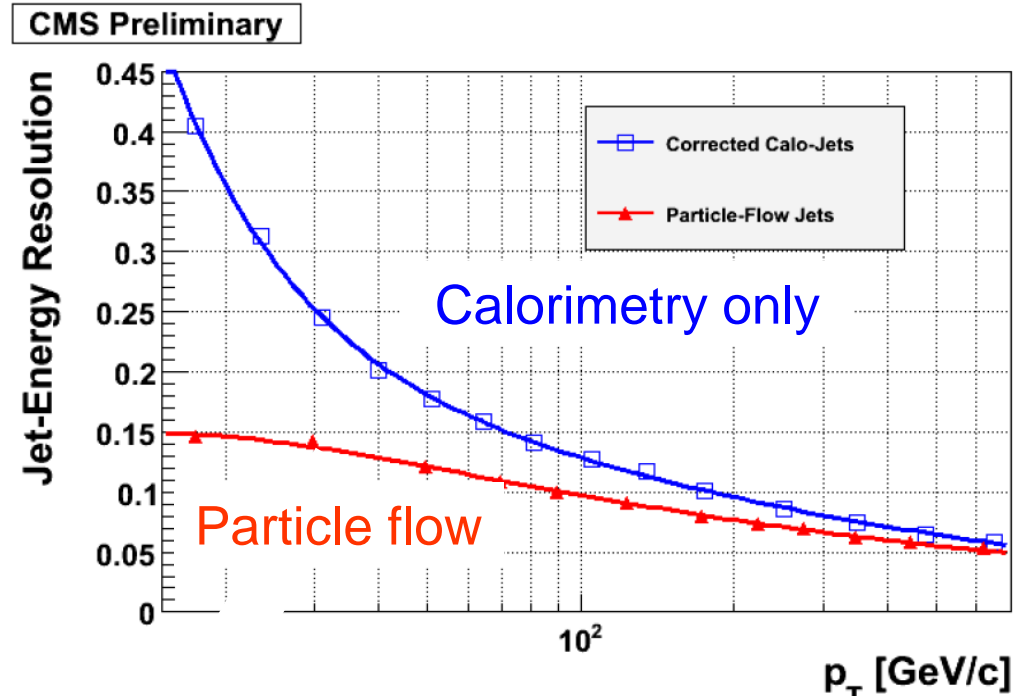


Particle Flow versus Calorimetry alone

- CMS - large central magnetic field of 4T
- Very good charged particle track momentum resolution
- Good separation of charged particle energy deposits from others in the calorimeters
- Good separation from other tracks

Large improvement in jet resolution at low P_T using the combined resolution of the Calorimetry and Tracking systems

**Simulated QCD-multijet events,
CMS barrel section: $|\eta| < 1.5$**



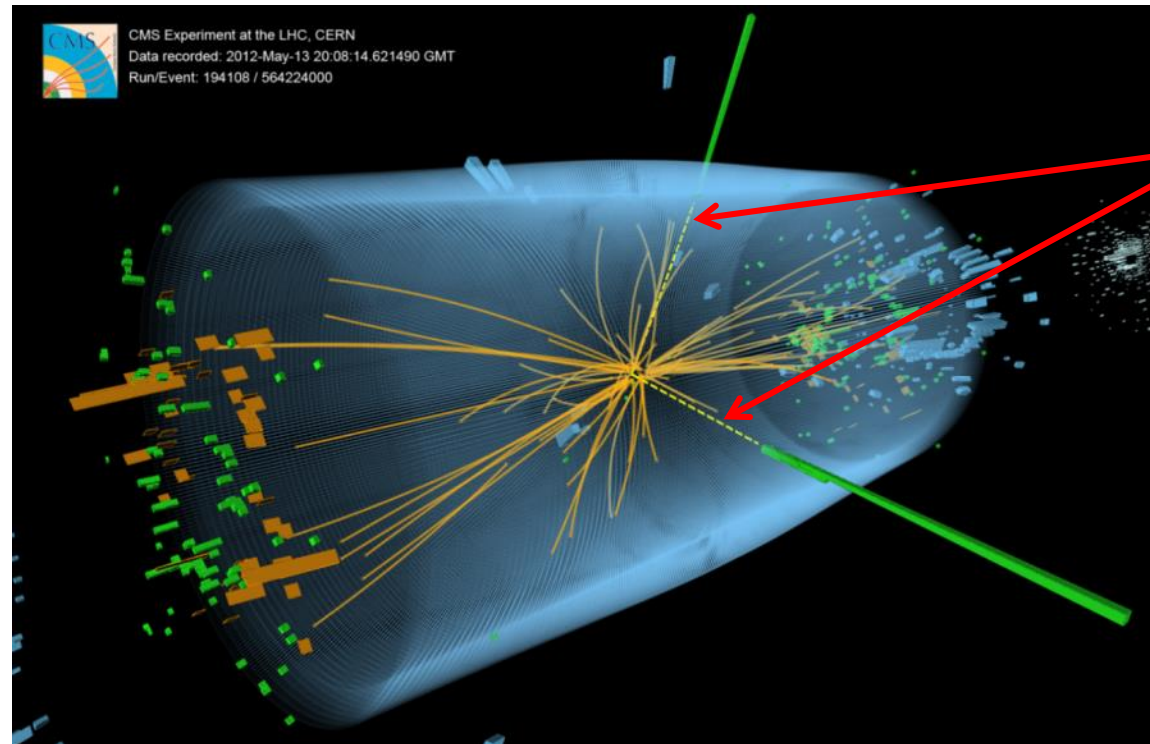
**Jet energy resolution
as a function of P_T**



Higgs and Calorimetry

The crowning glory of CMS (and ATLAS) calorimetry!

Event recorded with the CMS detector in 2012 Characteristic of Higgs boson decay to 2 photons



No charged tracks present, so must be photons

EM calorimetry

E.m. energy proportional to green tower heights

Hadronic calorimeter

Hadron energy proportional to orange tower heights

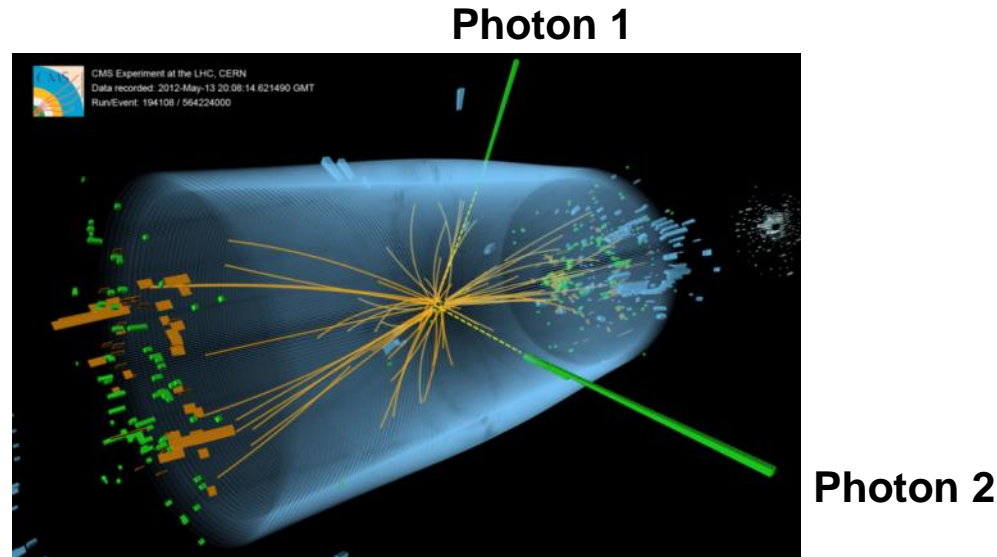
Tracker

Charged tracks
Orange curves

Muon detector

Muon detector hits
Blue towers

Can **YOU** calculate the **Effective mass** for the 2 high energy photons in the event??

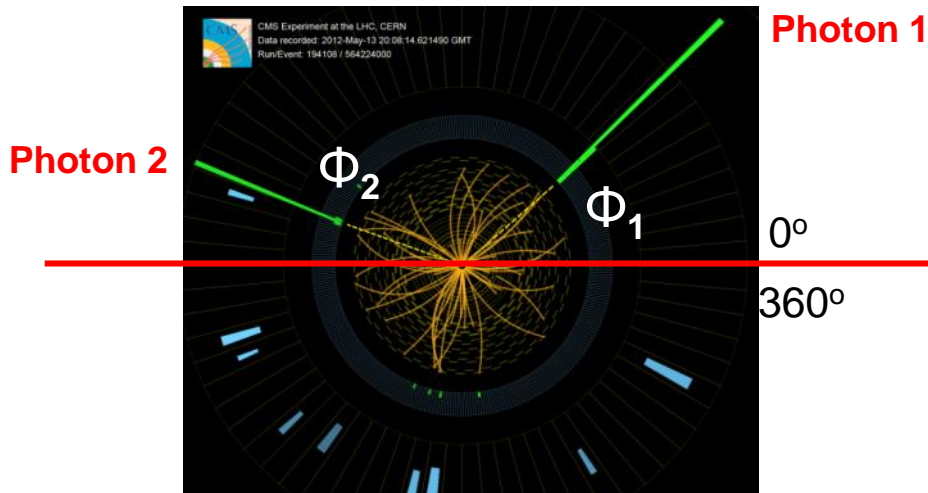


	ECAL Energy (GeV)	Angle Phi ** (radians)	Pseudo-rapidity ** (η)
Photon 1	90.0264	0.719	0.0623
Photon 2	62.3762	2.800	-0.811

** see definitions in next slide

You can also ask Professor Moretti for his estimate !

CMS Event – angle definitions

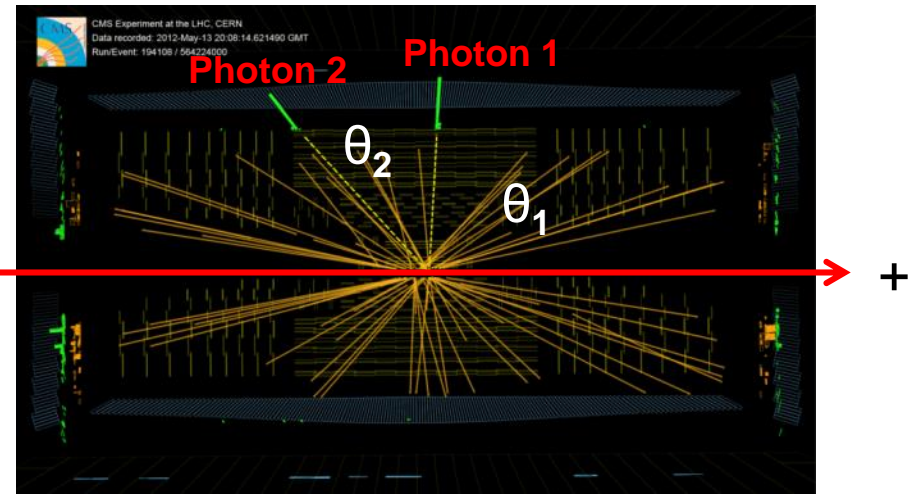


Transverse view

Angle of the photons in the r-phi plane, Φ_1 and Φ_2

$$\Phi_1 = 0.719 \text{ radians}$$

$$\Phi_2 = 2.800 \text{ radians}$$



Longitudinal view

Angle of the photons wrt the +ve direction of the beam axis, θ_1 and θ_2

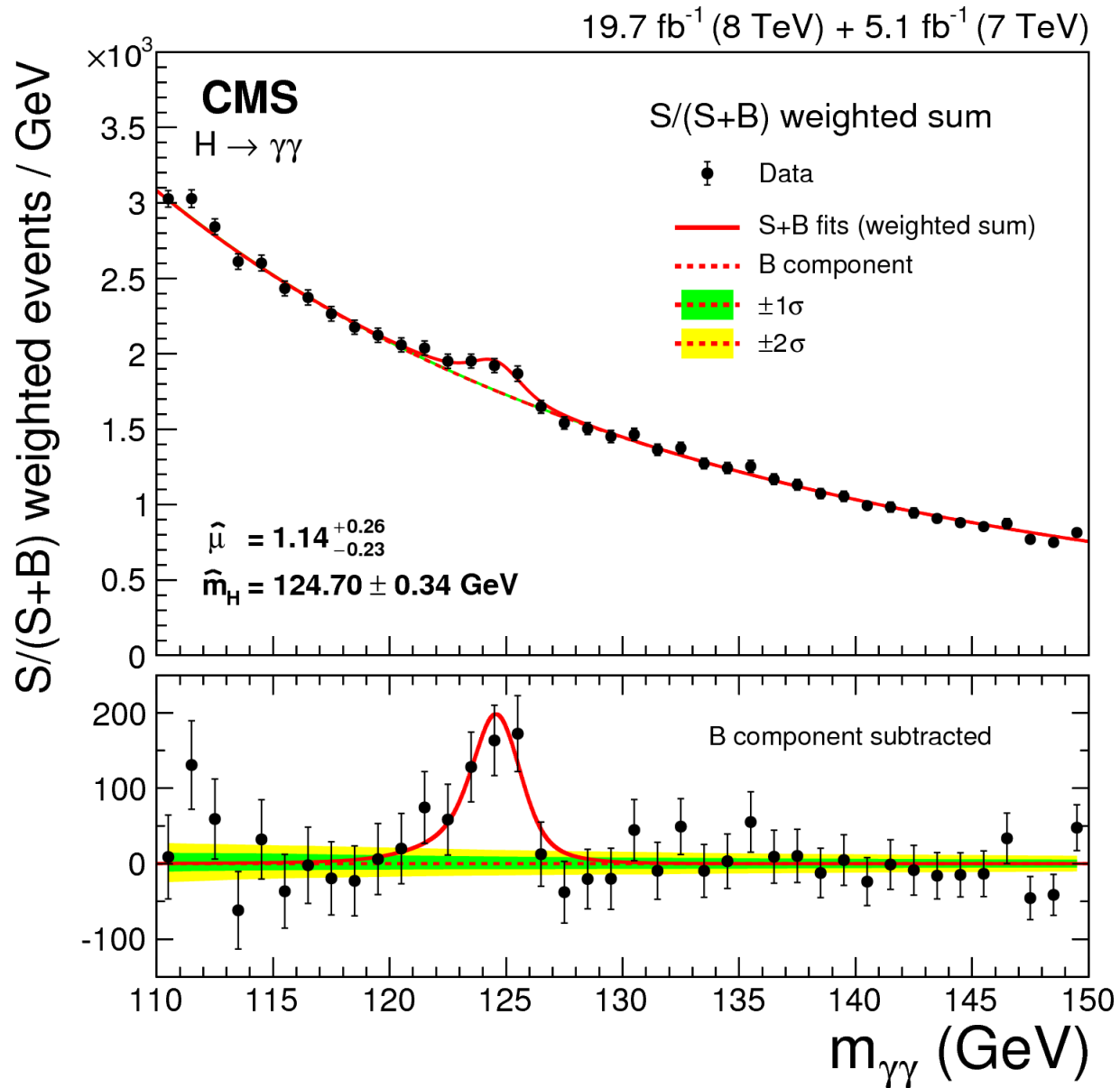
θ related to pseudo-rapidity (η) by

$$\eta = - \ln [\tan (\theta/2)]$$

$$\eta_1 = 0.0623$$

$$\eta_2 = - 0.8110$$

The crowning glory of CMS (and ATLAS) calorimetry!



Summary

Calorimetry a key detector technique for particle physics

In this talk, calorimetry for photons/electrons from ~ 1 MeV, to $O(50$ GeV) for Z decays, to $O(1$ TeV) for jets

Calorimeters playing a crucial role for physics at the LHC, eg $H \rightarrow \gamma\gamma$, $Z' \rightarrow ee$, SUSY (missing E_T)

Calorimeters indispensable for neutrino and missing E_T physics

Wide variety of technologies available. Calorimeter design is dictated by physics goals, experimental constraints and cost. Compromises necessary.

References:

Electromagnetic Calorimetry, Brown and Cockerill, NIM-A 666 (2012) 47–79

Calorimetry for particle physics, Fabian and Gianotti, Rev Mod Phys, 75, 1243 (2003)

Calorimetry, Energy measurement in particle physics, Wigmans, OUP (2000)

Backups

Future directions in Calorimetry

The International Linear Collider (ILC)

Use Particle Flow, aided by finely segmented calorimetry

Very high transverse segmentation

ECAL $\sim 1 \times 1 \text{ cm}^2$ SiW cells – CALICE

HCAL $\sim 3 \times 3 \text{ cm}^2$ Steel/scintillator

High longitudinal sampling

30 layers ECAL and 40 layers HCAL

CALICE prototype

1.4/2.8/4.2 mm thick W plates ($30X_0$)

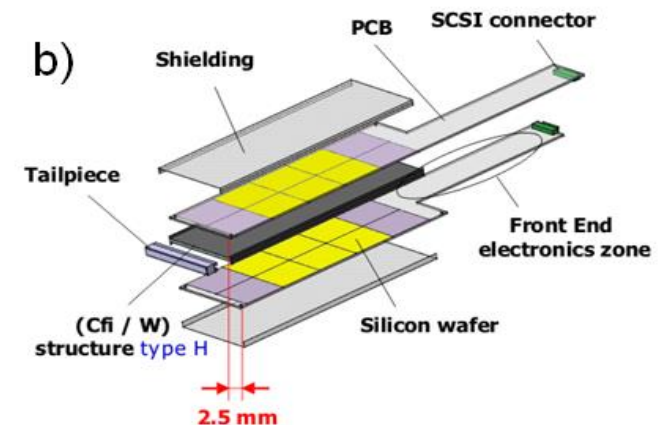
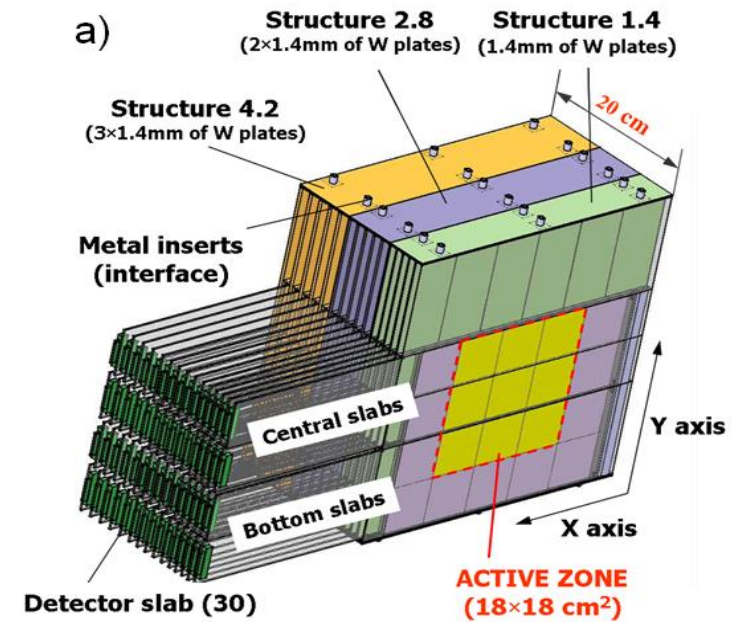
Interleaved with Silicon wafers

Read out at level of $1 \times 1 \text{ cm}^2$ pads

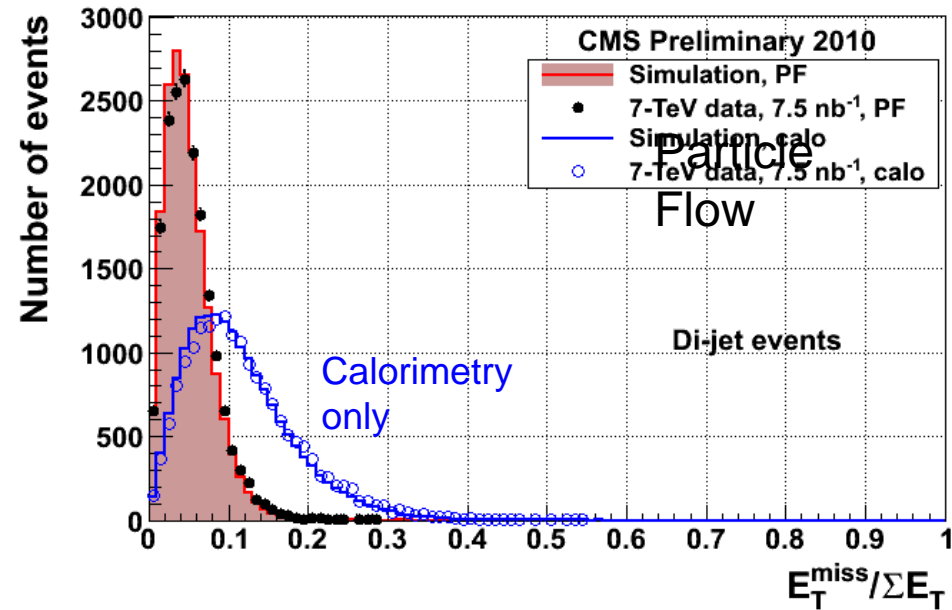
Resolution for electrons

Stochastic term $a \sim 17\%$

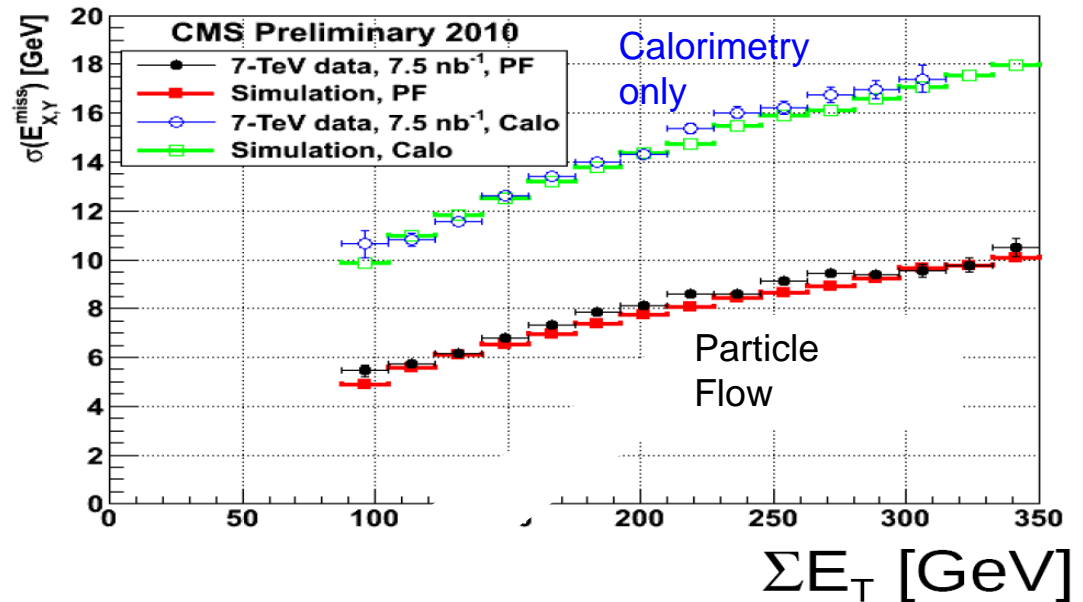
Constant term $c \sim 1.1\%$



Particle Flow Calorimetry in CMS



Missing E_T normalised to the total transverse energy for Di-jet events in CMS



Missing E_T resolution for Di-jet events

CMS missing E_T resolution < 10 GeV over whole ΣE_T range up to 350 GeV
 Factor 2 improvement on calorimetry by using Particle Flow technique

Energy resolution of hadronic calorimeters

Consequences for $e/h \neq 1$

- response with energy is non-linear
- fluctuations on F_{π^0} contribute to σ_E/E

Since the fluctuations are non-Gaussian,

- σ_E/E scales more weakly than $1/\sqrt{E}$, more as $1/E$

Deviations from $e/h = 1$ also contribute to the constant term

'Compensating' sampling hadron calorimeters

Retrieve $e/h = 1$ by compensating for the loss of invisible energy, several approaches:

- Weighting energy samples with depth
- Use large elastic cross section for MeV neutrons scattering off hydrogen in the organic scintillator
- Use ^{238}U as absorber. ^{238}U fission is exothermic. Release of additional neutrons

Neutrons liberate recoil protons in the active material

Ionising protons contribute directly to the signal

Tune absorber/scintillator thicknesses for $e/h = 1$

Example Zeus: ^{238}U plates (3.3mm)/scintillator plates (2.6mm), total depth 2m, $e/h = 1$
Stochastic term $0.35/\sqrt{E(\text{GeV})}$

Additional degradation to resolution, calorimeter imperfections :

Inter-calibration errors, response non-uniformity (laterally and in depth), energy leakage, cracks

Homogeneous electromagnetic calorimeters

ALICE at the LHC – scintillating PbWO_4 crystals

Avalanche photo diode readout



Some of the 17,920 PbWO_4 crystals for ALICE (PHOS)

Homogeneous calorimeters

Homogeneous calorimeters

Three main types: Scintillating crystals Glass blocks (Cerenkov radiation) Noble liquids

Crystals	NaI(Tl)	<u>CsI(Tl)</u>	CsI	BGO	<u>PbWO₄</u>
Density (g/cm ³)	3.67	4.53	4.53	7.13	8.28
X_0 (cm)	2.59	1.85	1.85	1.12	0.89
R_M (cm)	4.5	3.8	3.8	2.4	2.2
<u>Decay time (ns)</u>	250	<u>1000</u>	10	300	<u>5</u>
slow component			36		15
Emission peak (nm)	410	565	305	410	440
slow component			480		
<u>Light yield γ/MeV</u>	4×10^4	<u>5×10^4</u>	4×10^4	8×10^3	<u>1.5×10^2</u>
Photoelectron yield (relative to NaI)	1	0.4	0.1	0.15	0.01
Rad. hardness (Gy)	1	10	10^3	1	10^5

Lead glass, SF-6

OPAL at LEP

$X_0 = 1.69\text{cm}$,

$\rho = 5.2\text{ g/cm}^3$

**Barbar
@PEPII
10ms
inter'n rate
good light
yield, good**

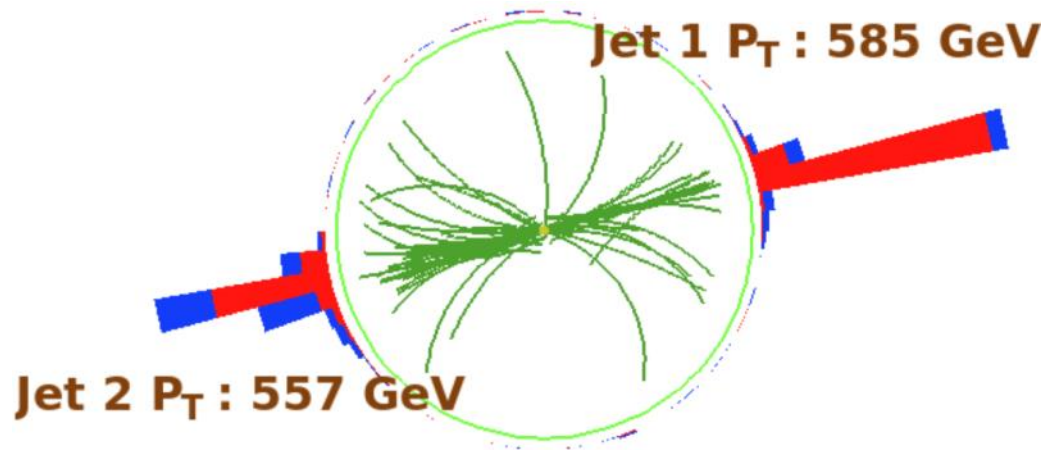
**KTeV at
Tevatron,
High rate,
Good
resolution**

**L3@LEP,
25 μ s bunch
crossing,
Low rad'n
dose**

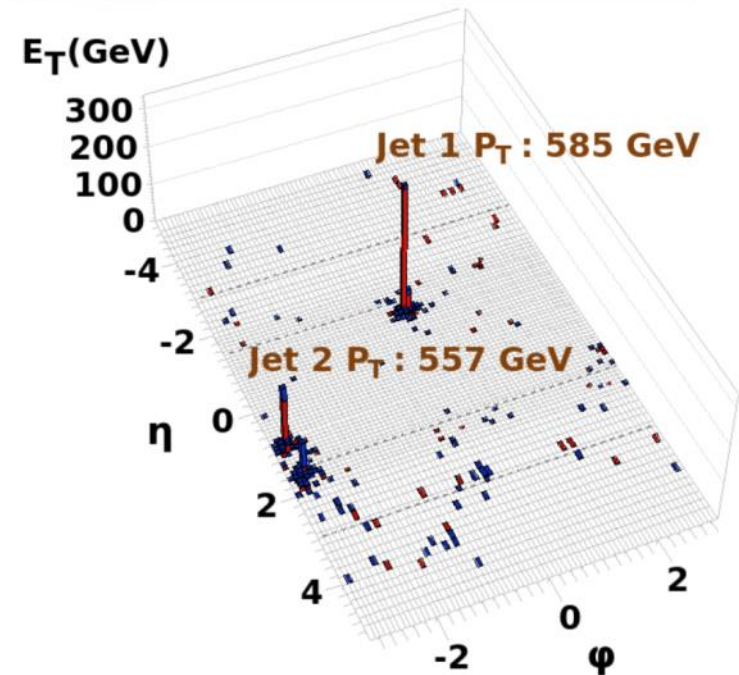
**CMS at LHC
25ns bunch
crossing,
high radiation
dose
ALICE
PANDA**

The Power of Calorimetry

A high energy DiJet event in CMS



Run : 138919
Event : 32253996
Dijet Mass : 2.130 TeV



Calorimeter energy
deposits on $\eta \times \phi$ map
ECAL red, HCAL blue

**A high mass dijet event in the first 120nb^{-1} of data, at 2.13 TeV
taken in CMS with pp collisions at 7 TeV, July 2010**

Extra info – em shower depth

How many X_0 to adequately contain an em shower?

Rule of thumb

RMS spread in shower leakage at the back ~ 0.5 * average leakage at the back

CMS - keep rms spread $< 0.3\%$ \Rightarrow leakage $< 0.65\%$ \Rightarrow crystals $25X_0$ (23cm) long

Other relations

$$\langle t_{95\%} \rangle \sim t_{max} + 0.08Z + 9.6$$

$$\langle t_{98\%} \rangle \sim 2.5 t_{max}$$

$$\langle t_{98\%} \rangle \sim t_{max} + 4 \lambda_{att}$$

Tail of cascade - photons of a few MeV \sim at the min in the mass attenuation coefficient

$\lambda_{att} \sim 3.4X_0$ \sim photon mean free path.

λ_{att} is associated with the exponential decrease of the shower after t_{max}

Comment, em longitudinal profile, Pb versus Cu:

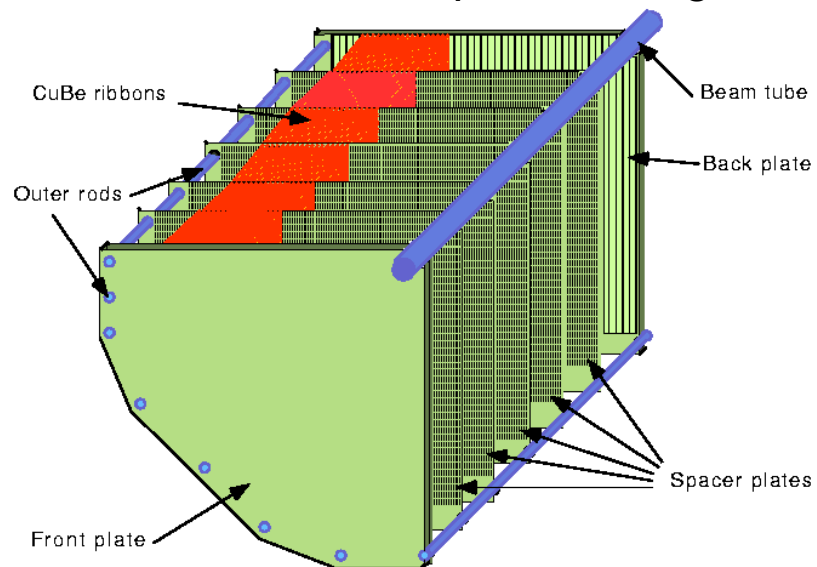
The coulomb field in Pb, $Z=82$ with $E_c = 7.3$ MeV means that bremstrahlung dominates over ionisation to much lower shower particle energies than for example in Cu, $Z=29$ with $E_c = 20.2$ MeV

As a consequence the depth (in X_0) of a shower proceeds further in Pb than in Cu.

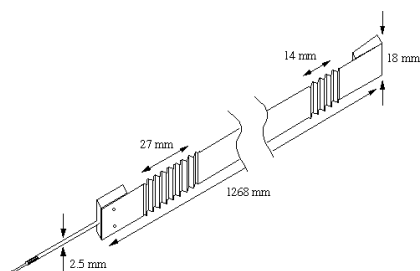
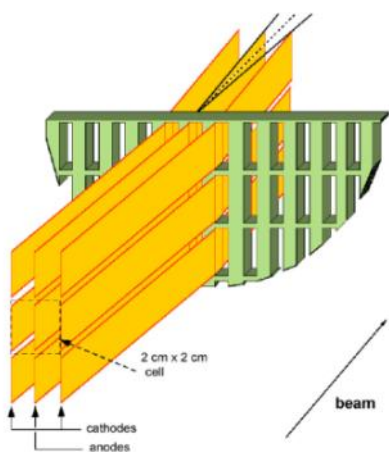
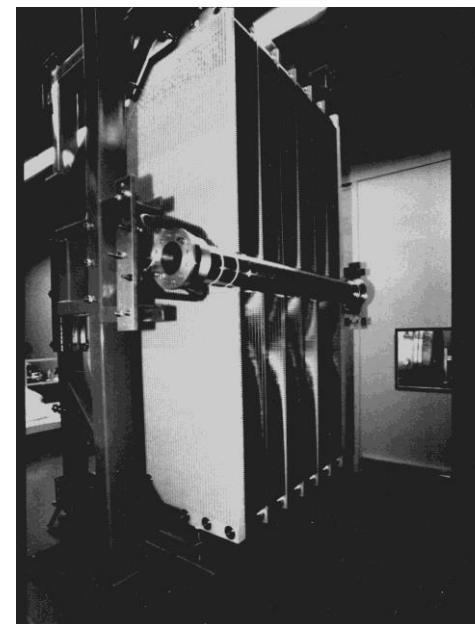
Homogeneous liquid Kr electromagnetic calorimeters

NA48 Liquid Krypton Ionisation chamber ($T = 120\text{K}$)

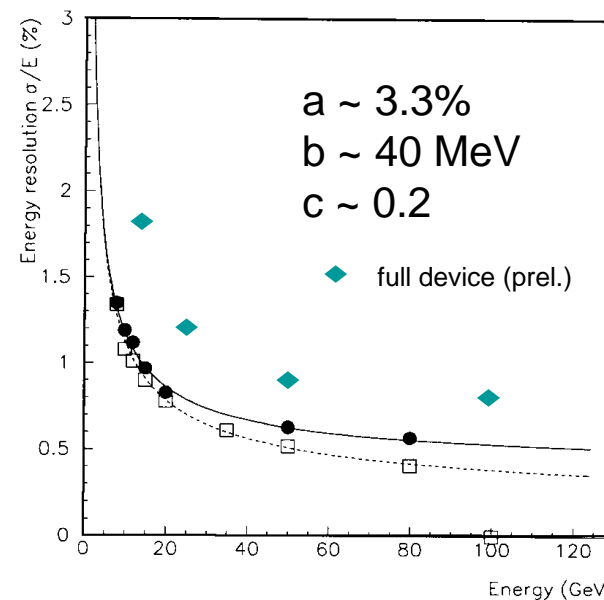
No metal absorbers: quasi homogeneous



NA48 Liquid Krypton
2cmx2cm cells
 $X_0 = 4.7\text{cm}$
125cm length ($27X_0$)
 $\rho = 5.5\text{cm}$



Cu-Be ribbon electrode



Homogeneous calorimetry

CMS PbWO₄ - photodetectors

Barrel

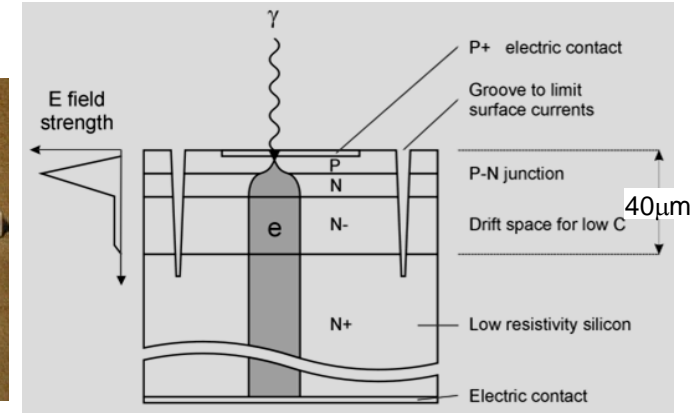
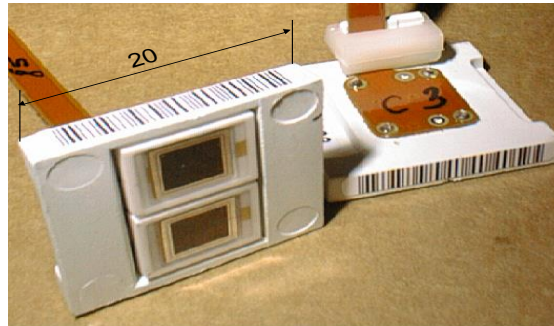
Avalanche photodiodes(APD)

Two 5x5 mm² APDs/crystal

Gain 50

QE ~75%

Temperature dependence -2.4%/°C

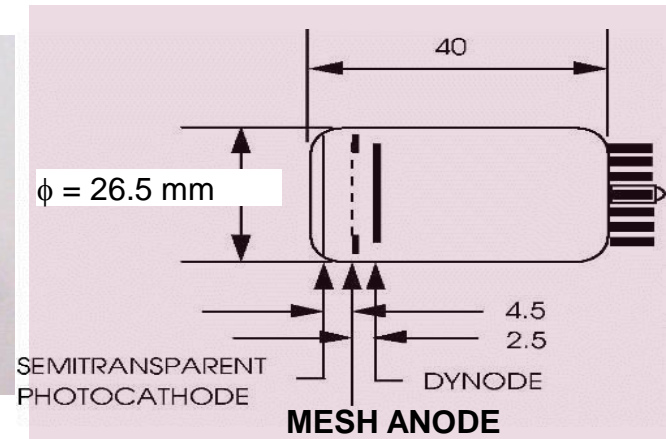


Endcaps

Vacuum phototriodes(VPT)

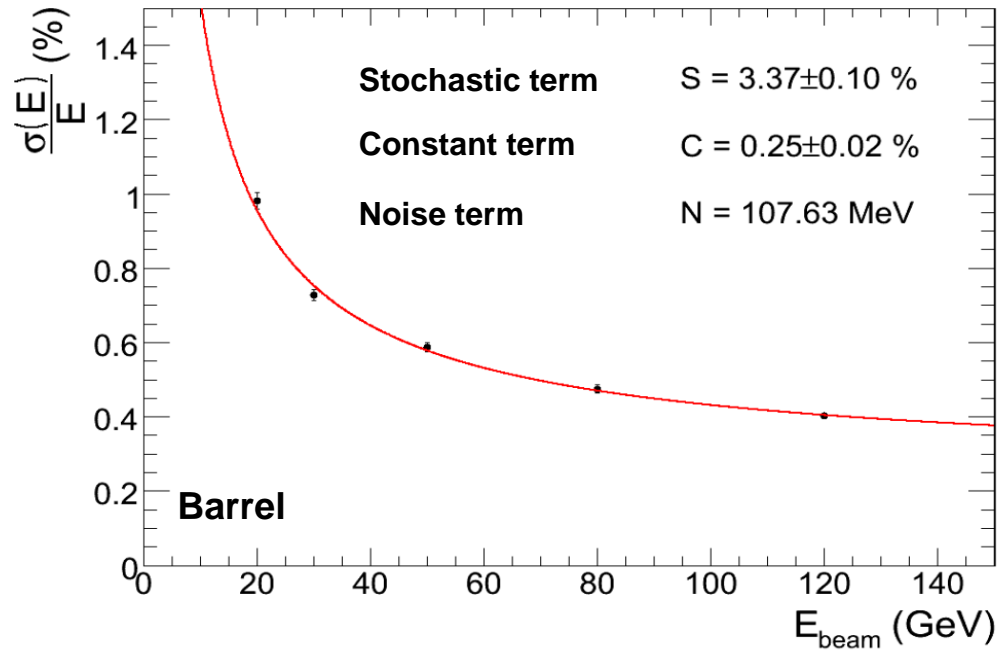
More radiation resistant than Si diodes

- UV glass window
- Active area ~ 280 mm²/crystal
- Gain 8 -10 (B=4T)
- Q.E. ~20% at 420nm



Homogeneous e.m. calorimeters

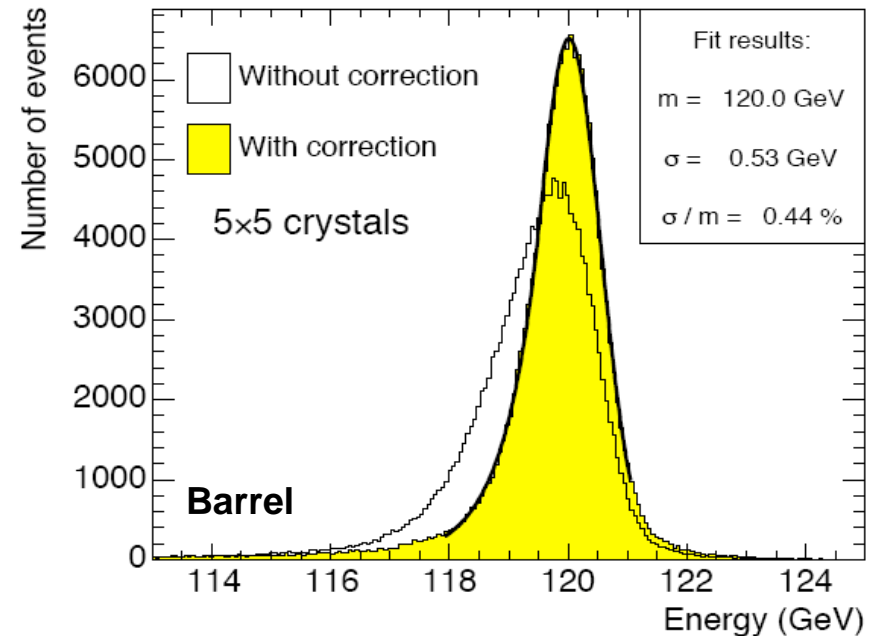
PbWO₄ - CMS ECAL energy resolution



**Electron energy resolution
as a function of energy**

**Electrons centrally (4mmx4mm)
incident on crystal**

Resolution 0.4% at 120 GeV



Energy resolution at 120 GeV

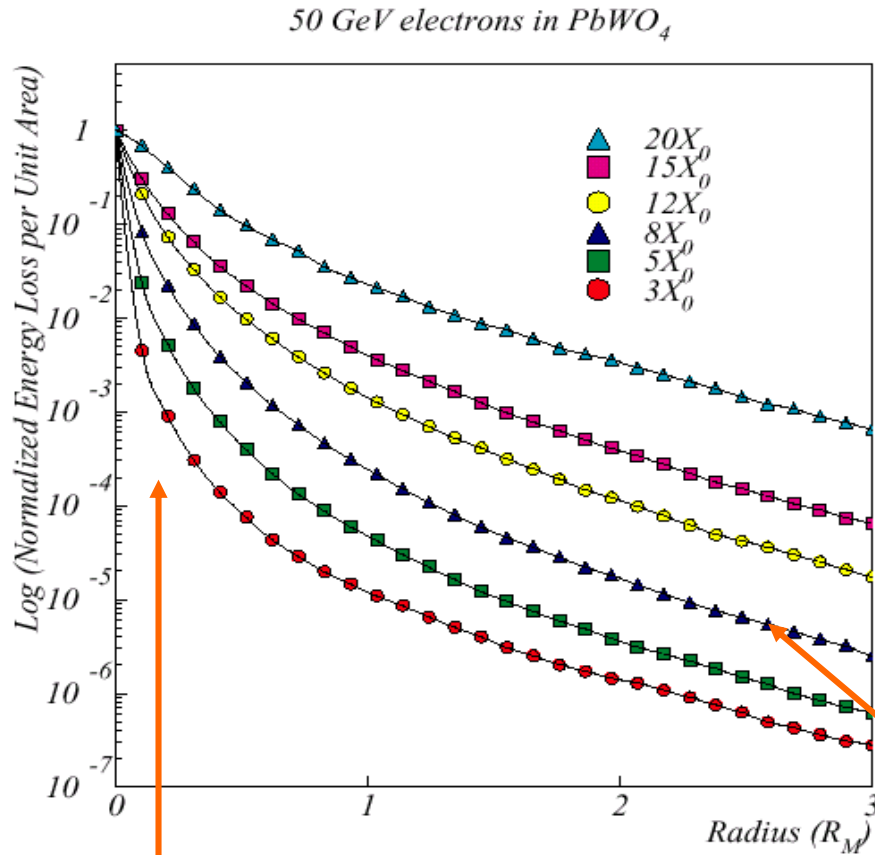
Electrons incident over full crystal face

Energy sum over 5x5 array wrt hit crystal.

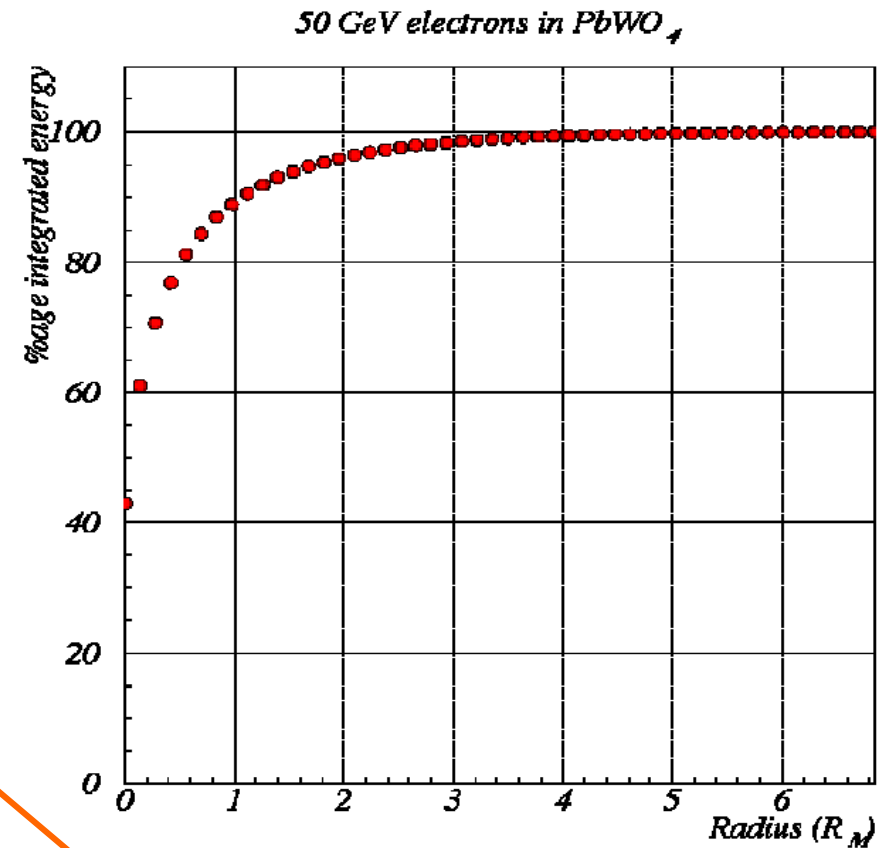
**Universal position 'correction function' for
the reconstructed energy applied**

Resolution 0.44%

EM showers: transverse profile



Central core: multiple scattering

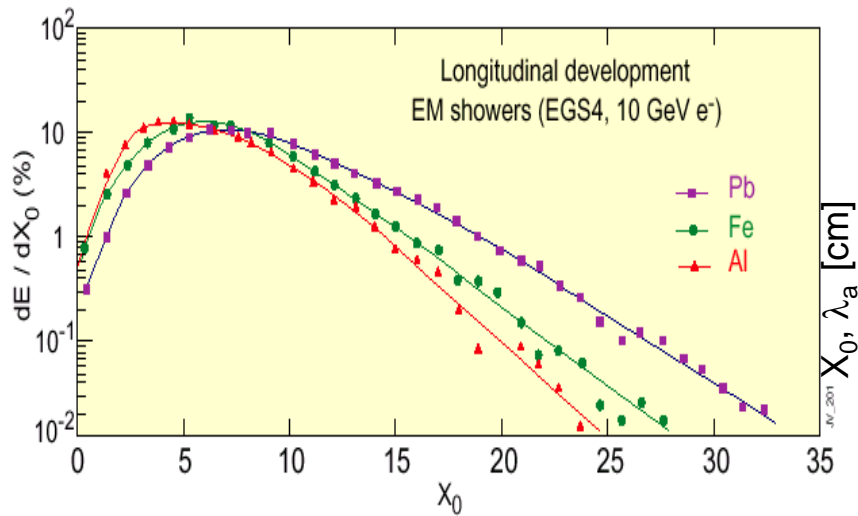


Peripheral halo: propagation of less attenuated photons, widens with depth of the shower

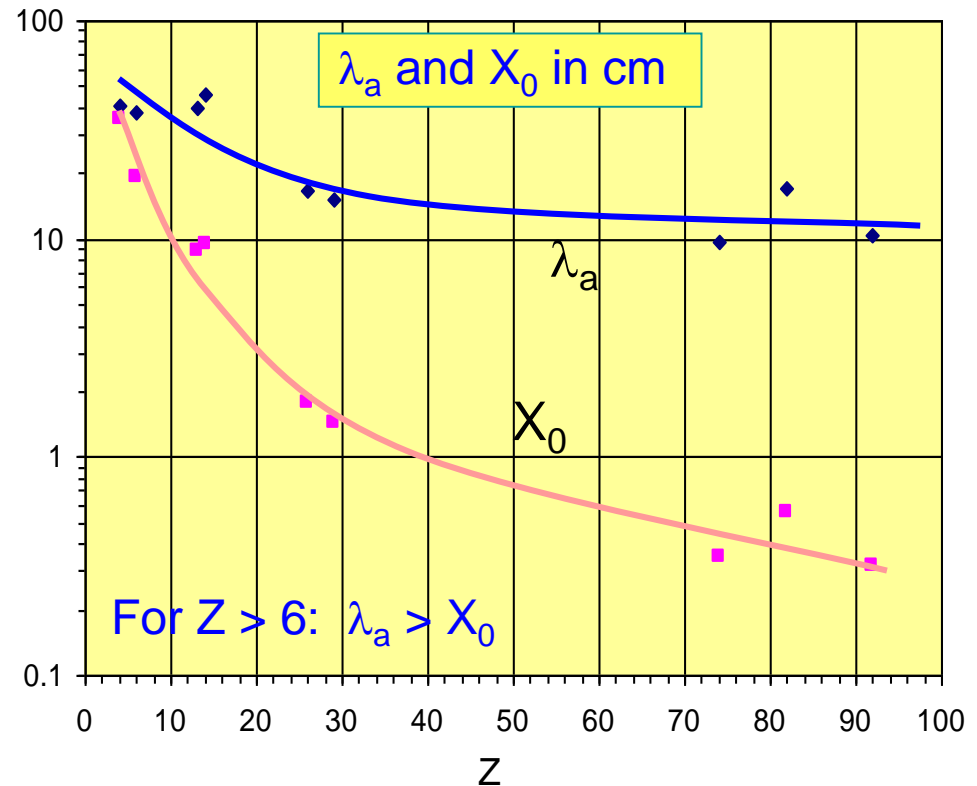
EM showers, longitudinal profile

Shower parametrization

$$\frac{dE}{dt} \propto t^\alpha e^{\beta t}$$

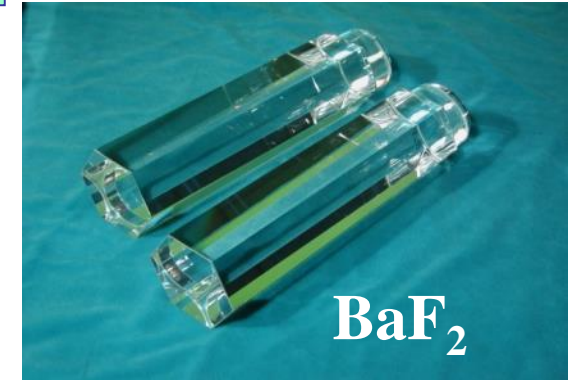
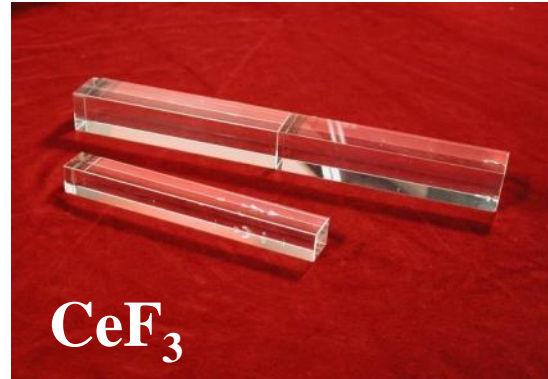
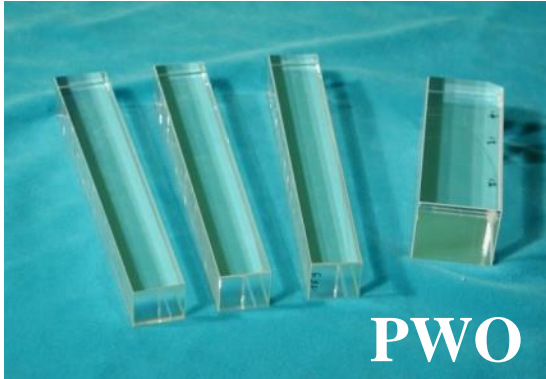


Material	Z	A	ρ [g/cm ³]	X_0 [g/cm ²]	λ_a [g/cm ²]
Hydrogen (gas)	1	1.01	0.0899 (g/l)	63	50.8
Helium (gas)	2	4.00	0.1786 (g/l)	94	65.1
Beryllium	4	9.01	1.848	65.19	75.2
Carbon	6	12.01	2.265	43	86.3
Nitrogen (gas)	7	14.01	1.25 (g/l)	38	87.8
Oxygen (gas)	8	16.00	1.428 (g/l)	34	91.0
Aluminium	13	26.98	2.7	24	106.4
Silicon	14	28.09	2.33	22	106.0
Iron	26	55.85	7.87	13.9	131.9
Copper	29	63.55	8.96	12.9	134.9
Tungsten	74	183.85	19.3	6.8	185.0



Crystals: building blocks

These crystals make light!



Crystals are basic components of electromagnetic calorimeters aiming at precision

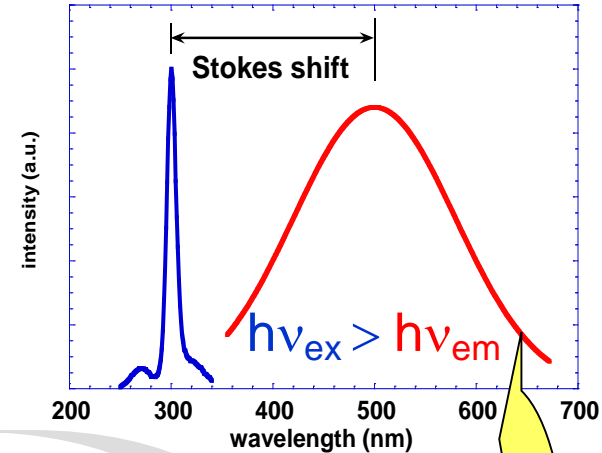


Scintillation: a three step process

Scintillator + Photo Detector = Detector

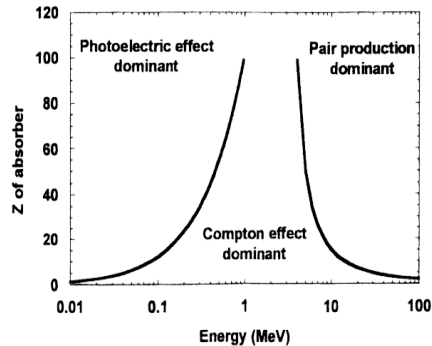
PMT, PD, APD

How does it work



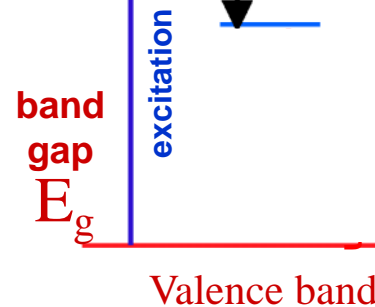
absorption e.g. γ

$$I(E) = I_0(E)e^{-\mu d}$$

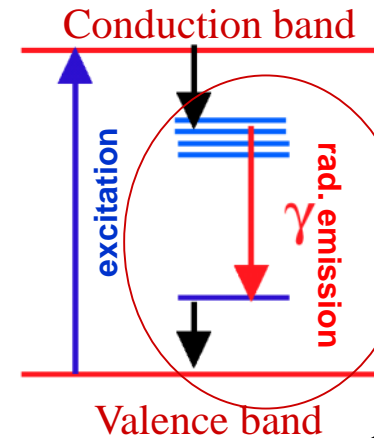


conversion

Energy \rightarrow Excitation
Conduction band



emission



Scintillating crystals

Variation in the lattice
(e.g. defects and impurities)



local electronic energy levels in the energy gap

If these levels are unoccupied electrons moving in the conduction band may enter these centres

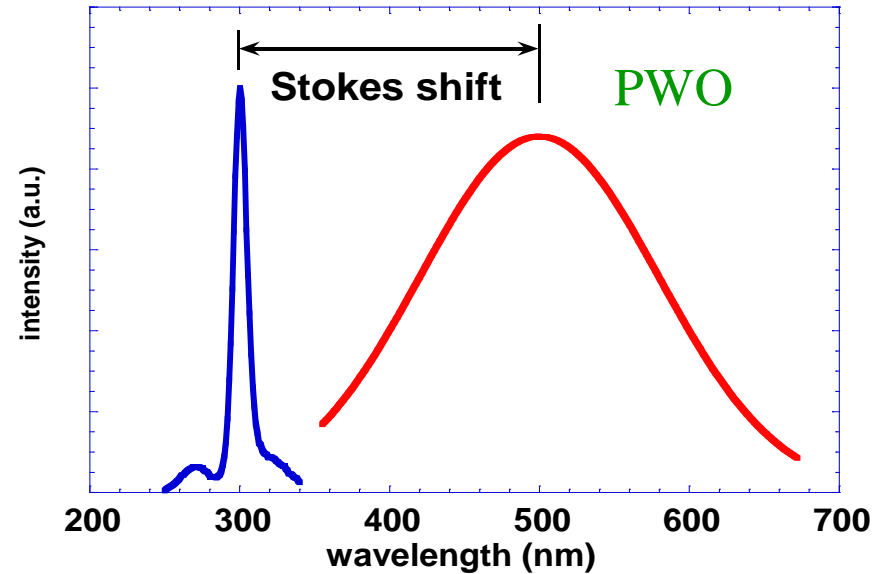
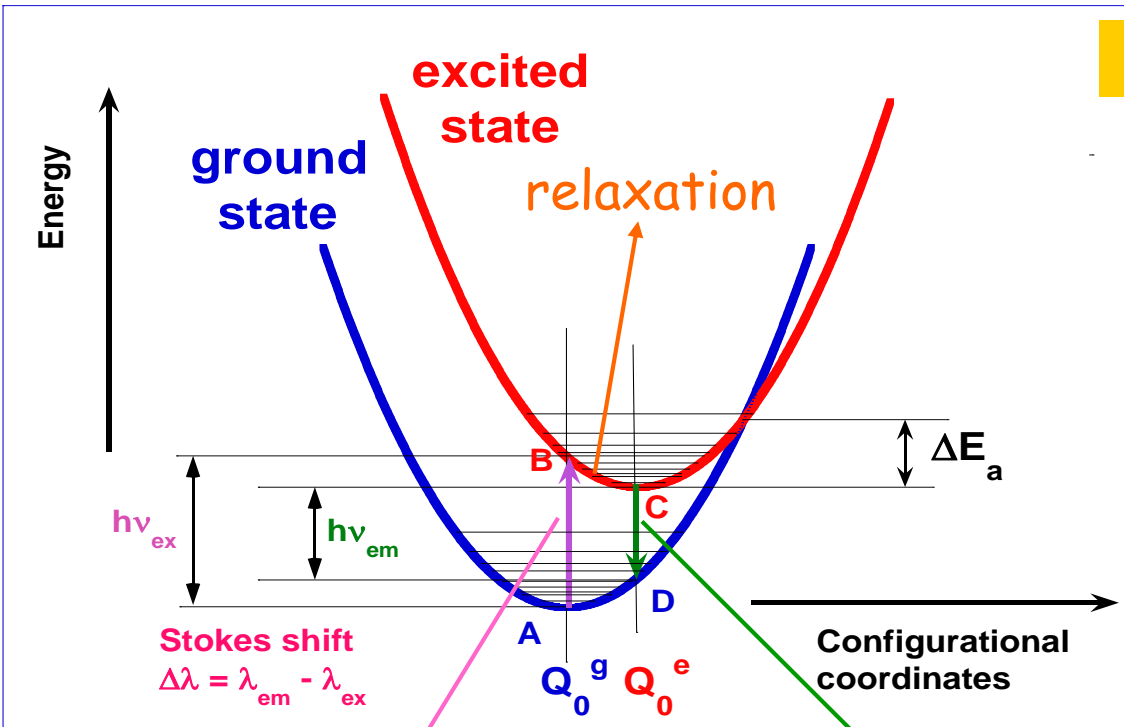
The centres are of three main types:

- **Luminescence centres** in which the transition to the ground state is accompanied by photon emission
- **Quenching centres** in which radiationless thermal dissipation of excitation energy may occur
- **Traps** which have metastable levels from which the electrons may subsequently return to the conduction band by acquiring thermal energy from the lattice vibrations or fall to the valence band by a radiationless transition

Scintillating crystals



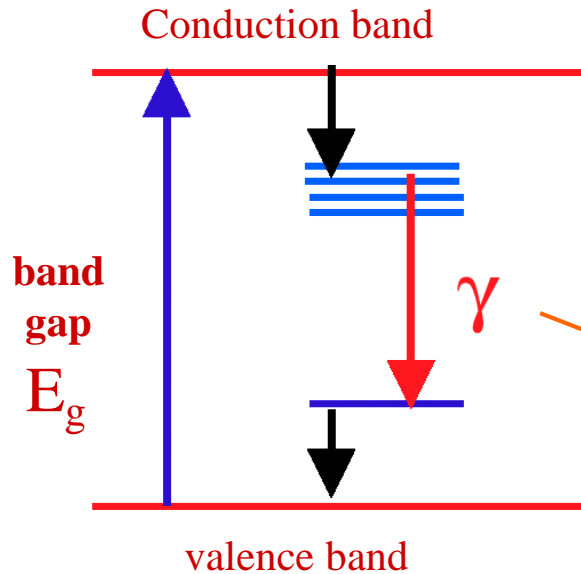
PbWO₄: $\lambda_{\text{excit}}=300\text{nm}$; $\lambda_{\text{emiss}}=500\text{nm}$



excitation

radiative emission

Scintillating crystals



$$E_{\text{dep}} \rightarrow e\text{-h}$$

$$E_s = \beta E_g \quad \beta > 1$$

$$N_{\text{eh}} = E_{\text{dep}} / \beta E_g$$

$$N_\gamma = SQ N_{\text{eh}}$$

Efficiency of transfer to luminescent centres

radiative efficiency of luminescent centres

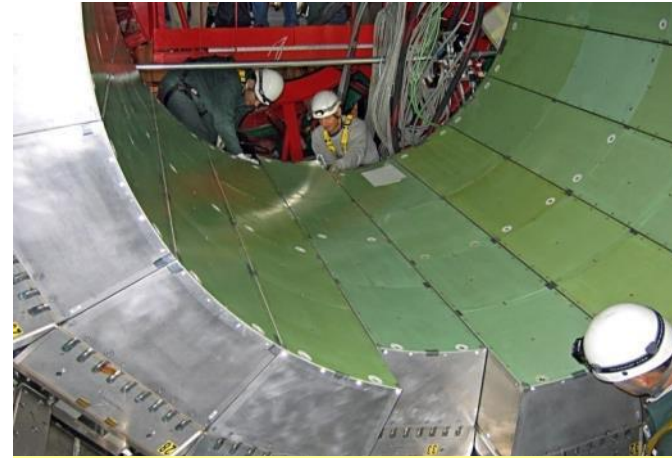
$$\eta_\gamma = N_\gamma / E_{\text{dep}} = SQ N_{\text{eh}} / E_{\text{dep}} = SQ / \beta E_g$$

- $S, Q \approx 1$, βE_g as small as possible
- medium transparent to λ_{emiss}

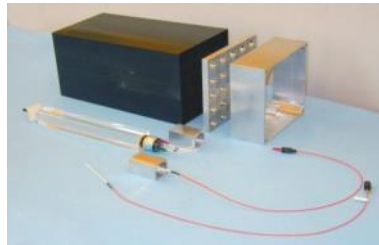
CMS Barrel and Endcap Homogeneous ECAL



A CMS Supermodule with 1700 tungstate crystals



Installation of the last SM into the first half of the barrel

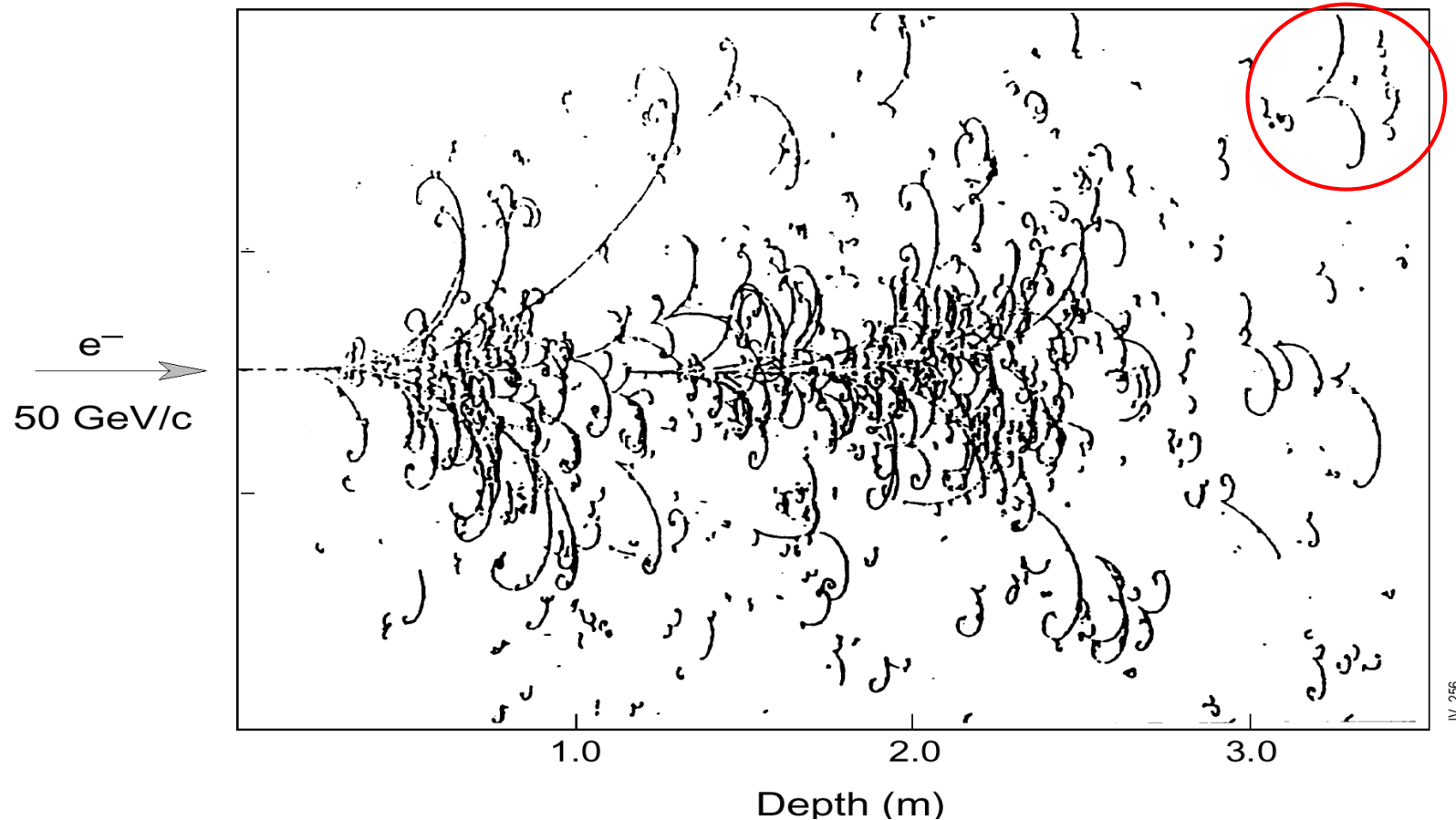


A CMS endcap 'supercrystal' 25 crystals/VPTs

Copper has been selected as the absorber material because of its density. The HB is constructed of two half-barrels each of 4.3 meter length. The HE consists of two large structures, situated at each end of the barrel detector and within the region of high magnetic field. Because the barrel HCAL inside the coil is not sufficiently thick to contain all the energy of high energy showers, additional scintillation layers (HOB) are placed just outside the magnet coil. The full depth of the combined HB and HOB detectors is approximately 11 absorption lengths.

The hadron barrel (HB) and hadron endcap (HE) calorimeters are sampling calorimeters with 50 mm thick copper absorber plates which are interleaved with 4 mm thick scintillator sheets.

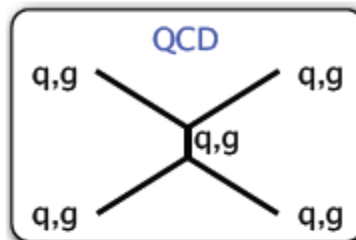
Electromagnetic shower



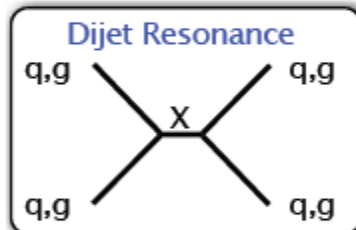
**Big European Bubble Chamber filled with Ne:H₂ = 70%:30%,
3T Field, L=3.5 m, X₀≈34 cm, 50 GeV incident electron**

Di-jets

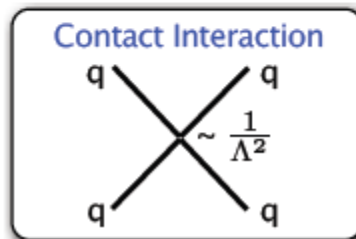
- ◆ We study the inclusive dijet final state using the **dijet mass spectrum** and the **dijet centrality ratio** observables.
- ◆ Together the Dijet Mass and Ratio provide a **test of QCD** and a **sensitive search** for new physics beyond the Standard Model.



- ▶ Dijet mass distribution is a simple check of rate vs dijet mass from QCD and PDFs.
- ▶ Dijet centrality ratio is a detailed measure of QCD dynamics from angular distribution.



- ▶ Dijet mass provides most sensitive “bump” hunt for new particles decaying to dijets.
- ▶ Dijet centrality ratio can confirm that a “bump” is not QCD fluctuation.



- ▶ Dijet centrality ratio is more sensitive than the dijet mass to contact interactions from quark compositeness.
 - when all experimental uncertainties are considered.

Jet Energy Resolution with stand alone calorimetry

For a single hadronic particle: $\sigma_E / E = a / \sqrt{E} \oplus c$ (neglect electronic noise)

Jet with low particle energies, resolution is dominated by **a**,
and at high particle energies by **c**

If the stochastic term, **a**, dominates:

- error on Jet energy \sim same as for
a single particle of the same energy

If the constant term dominates:

- error on Jet energy is less than for
a single particle of the same energy

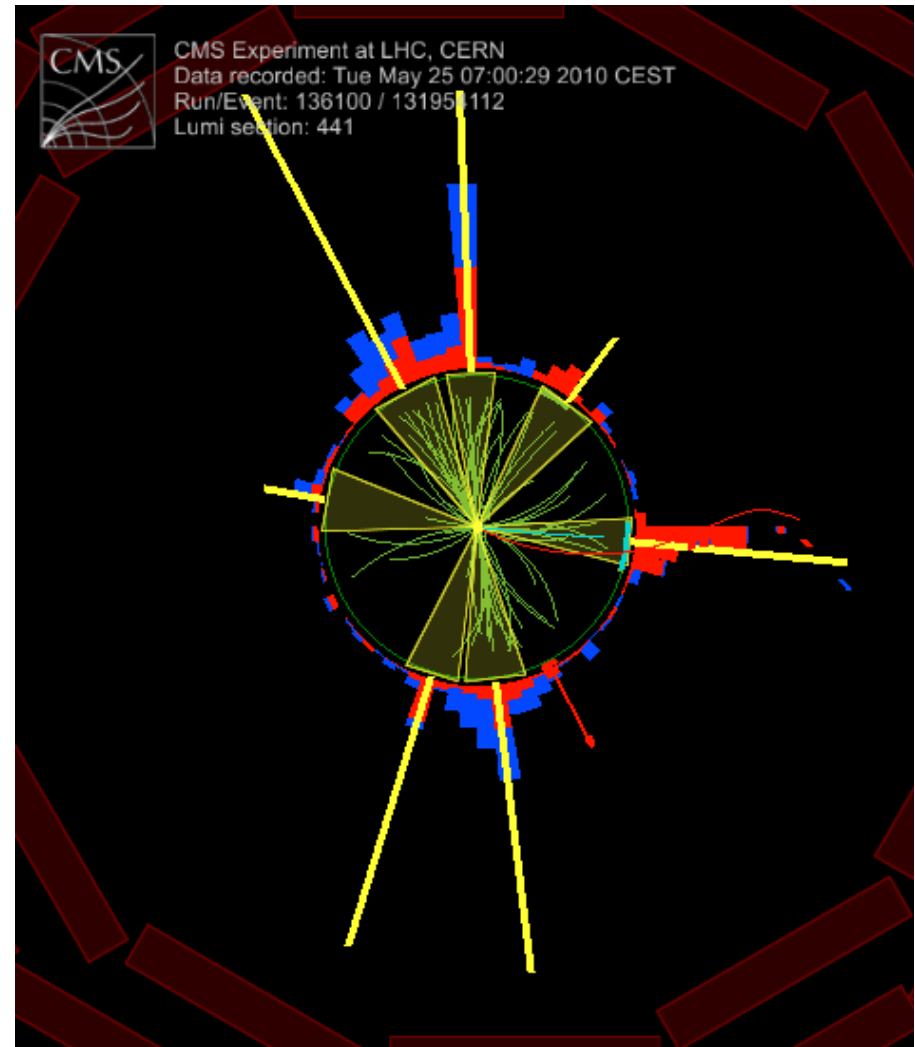
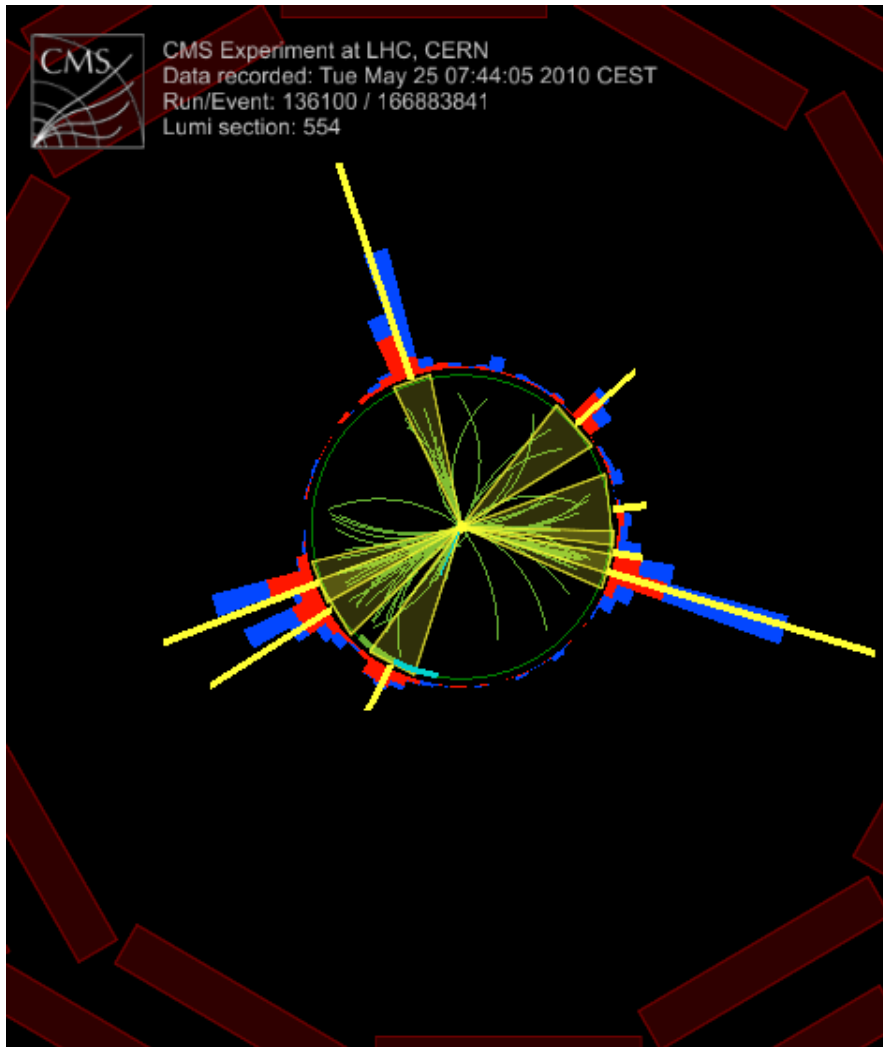
For example:

1 TeV jet composed of four hadrons of equal energy

Calorimeter with $\sigma_E / E = 0.3 / \sqrt{E} \oplus 0.05$

compared to $\delta E_{Jet} = 25 \text{ GeV}$,
 $\delta E = 50 \text{ GeV}$, for a single 1 TeV hadron

Jet s in CMS at the LHC, pp collisions at 7TeV



Red - ECAL, Blue - HCAL energy deposits
Yellow – Jet energy vectors