

# INSTRUMENTATION & DETECTORS for HIGH ENERGY PHYSICS IV

# DETECTOR: LECTURE III QUIZZ

**Gas vs solid state ionisation detector ?**

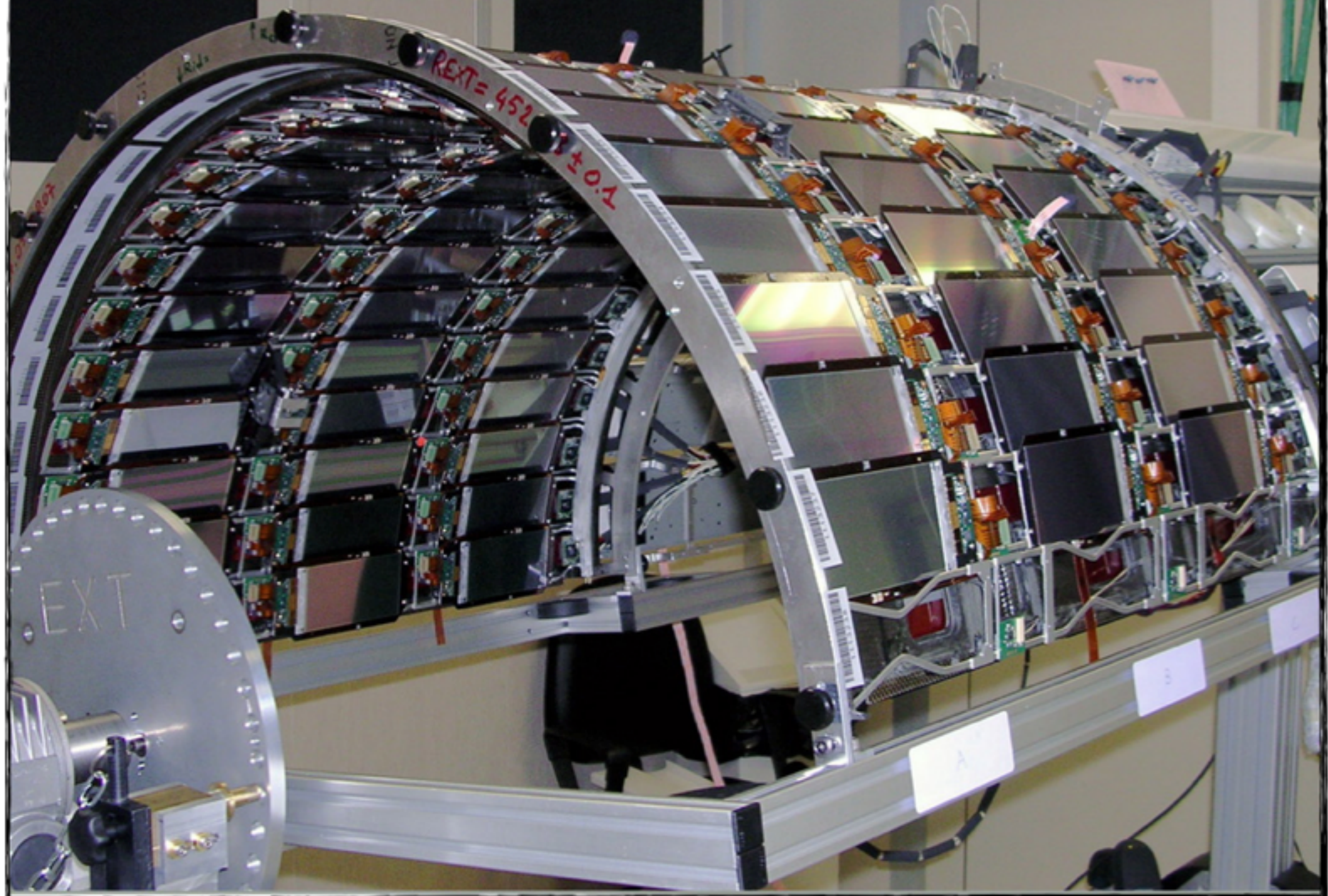
**Typical size of a cell in a silicium detector**

**Why do experimentalists like small cell size ?**

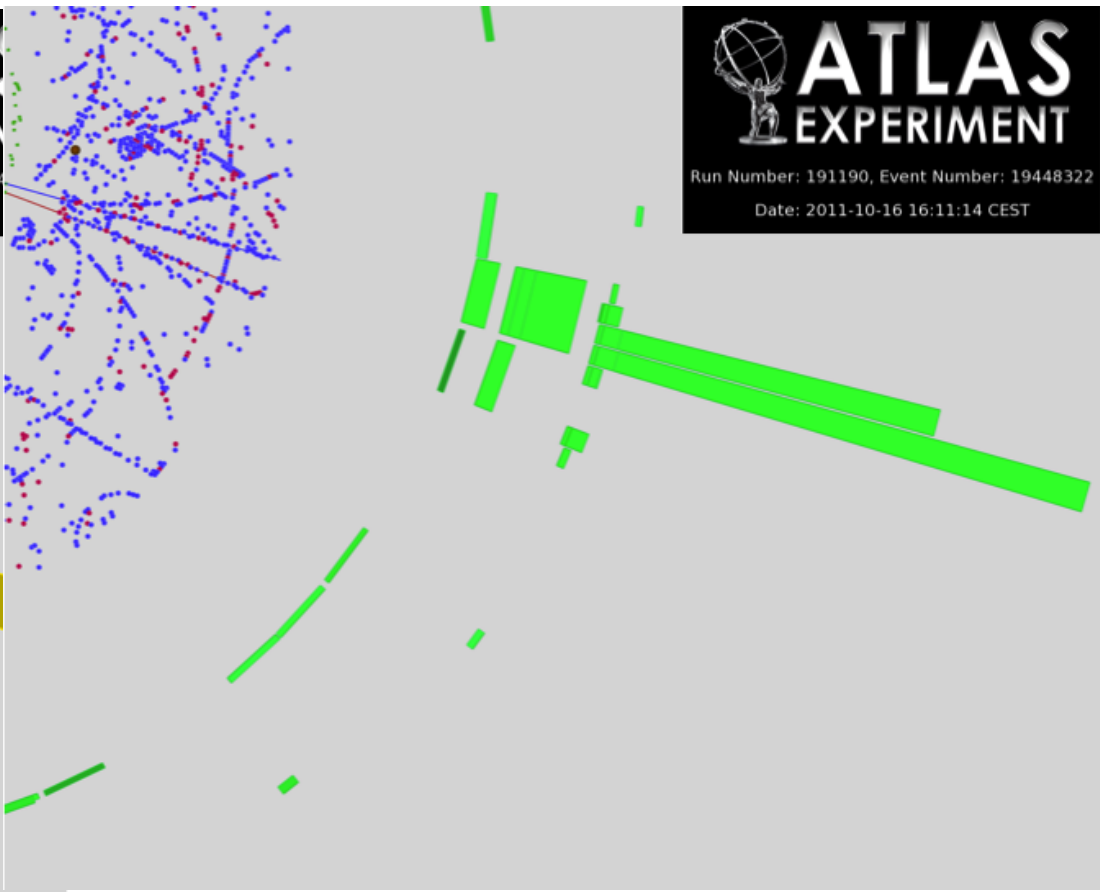
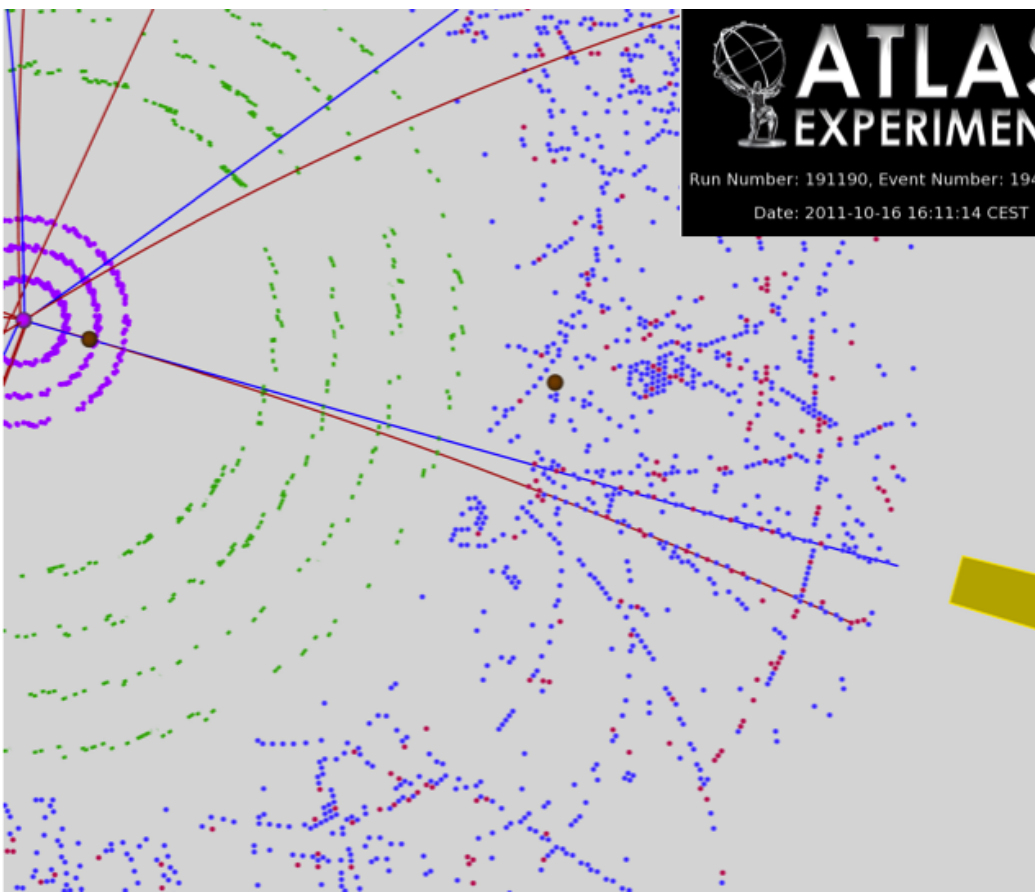
**What is the consequence of small cell size ?**



# CMS Inner Barrel



# PHOTON CONVERSION





# ATLAS MUON SYSTEM

Atlas Muon Spectrometer, 44m long, from r=5 to 11m.

1200 Chambers

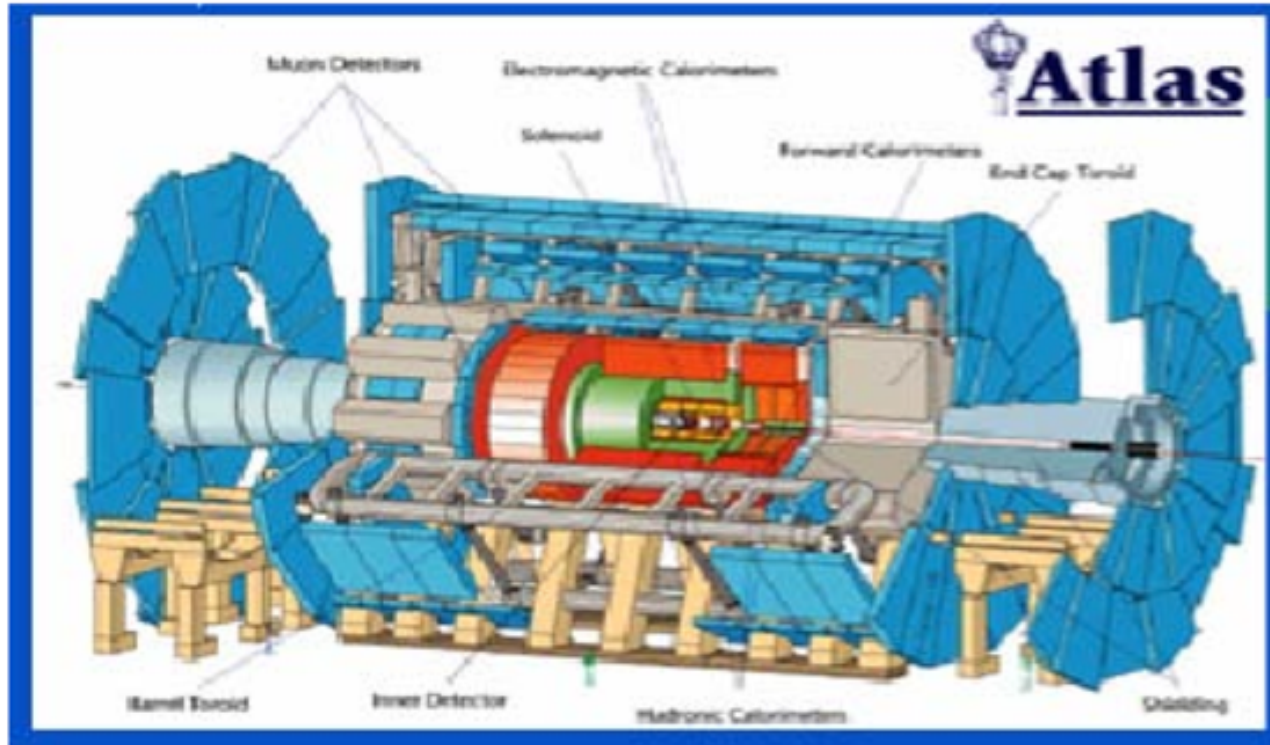
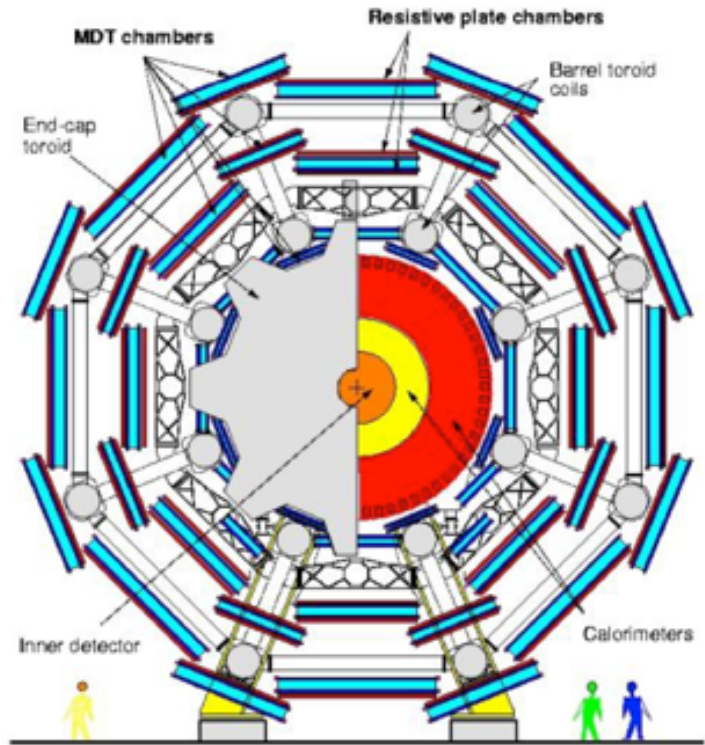
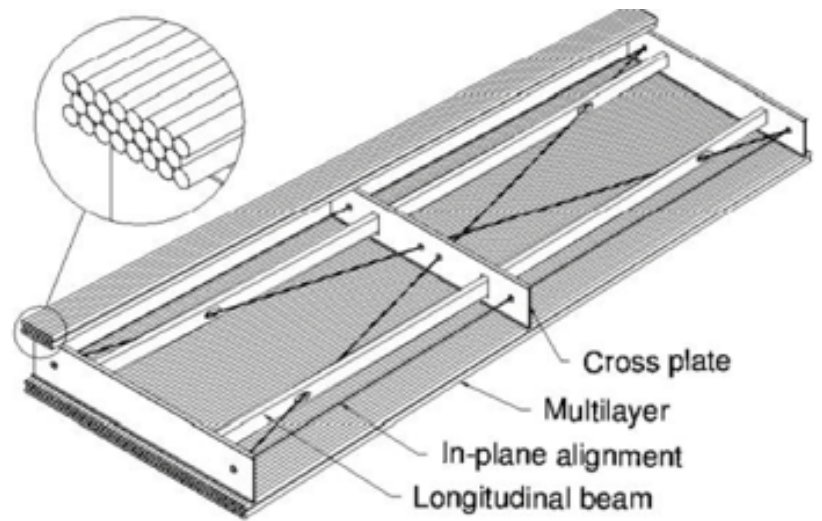
6 layers of 3cm tubes per chamber.

Length of the chambers 1-6m !

Position resolution: 80 $\mu$ m/tube, <50 $\mu$ m/chamber (3 bar)

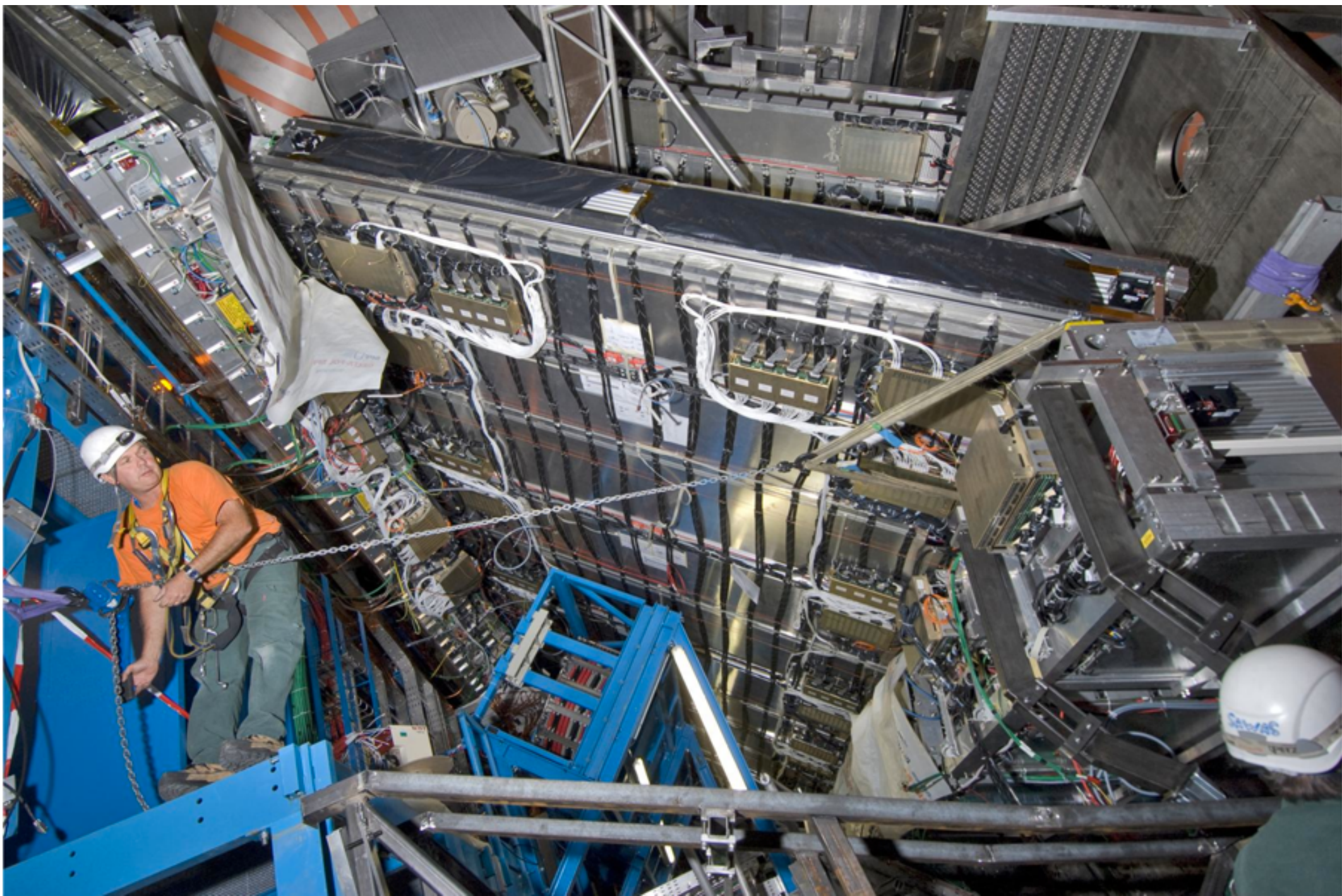
Maximum drift time  $\approx$ 700ns

Gas Ar/CO<sub>2</sub> 93/7





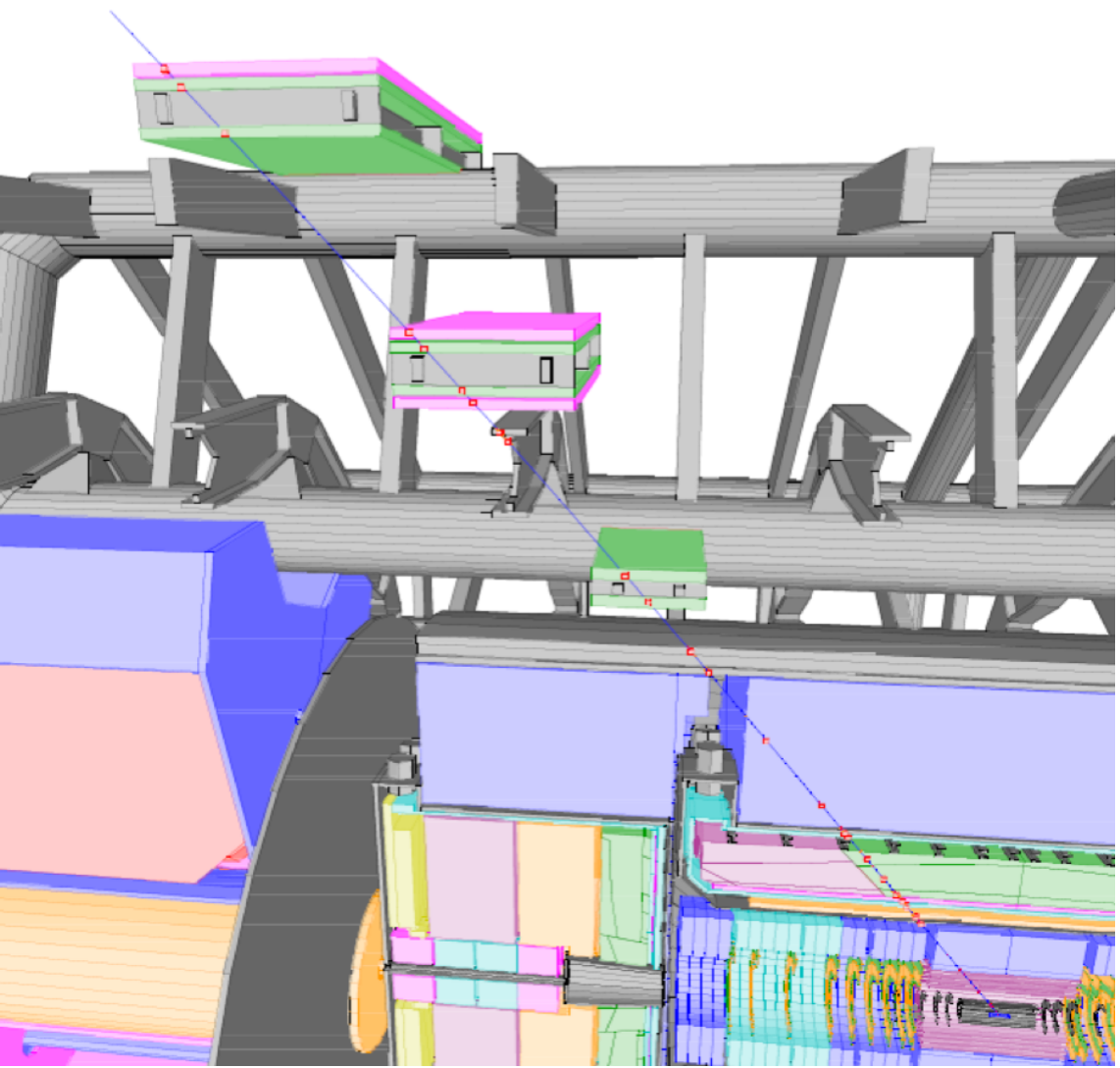
# ATLAS RPC



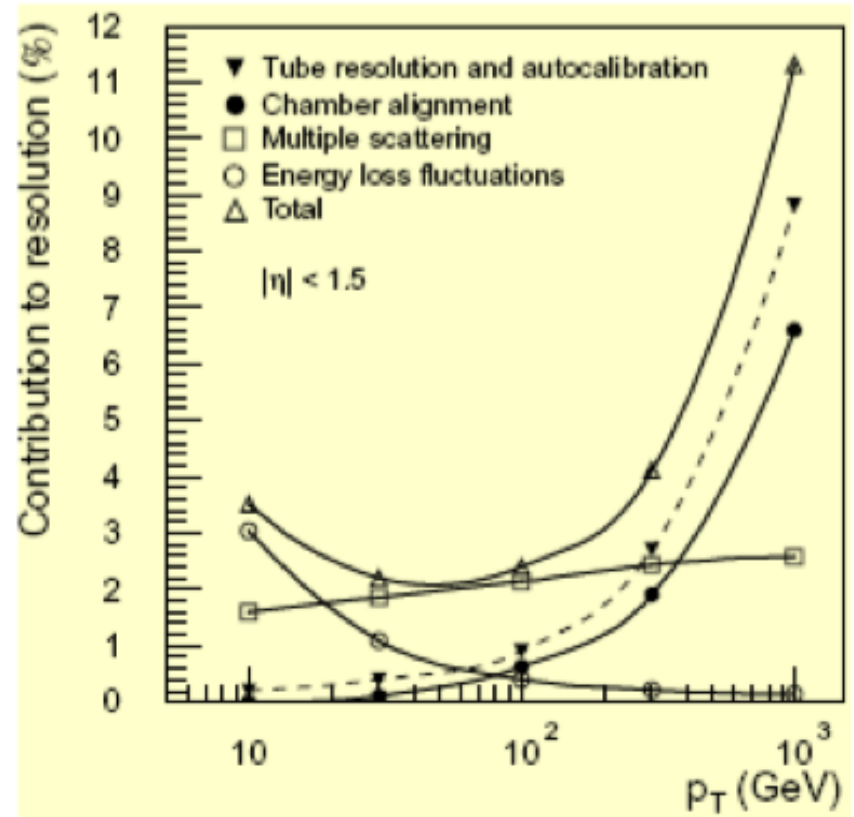


# MUON MOMENTUM RESOLUTION

COMBINE Measurement from the tracker and the muon chambers



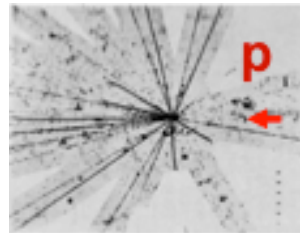
•  $\delta p_T/p_T$  vs  $p_T$



Contributions:    mesure  $\propto p$   
                          diffusion  $\sim cte$   
                           $\delta E/loss \propto 1/p$

# FROM INTERACTIONS to DETECTOR

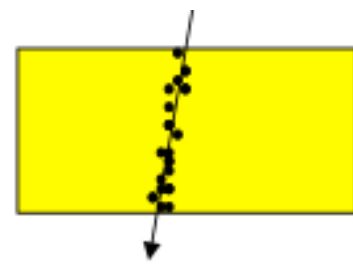
1. Particles interact with matter  
depends on particle and material



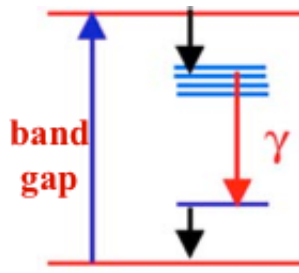
2. Energy loss transfer to detectable signal  
depends on the material

Detecting emitted light

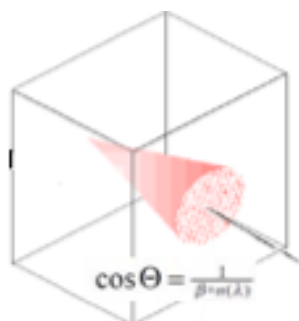
Detecting ionisation current



Ionisation

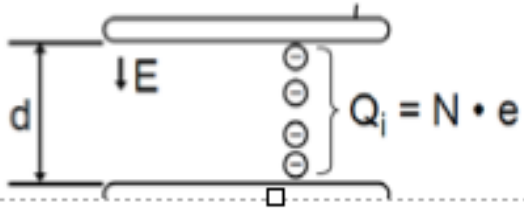


Scintillation light



Cerenkov light

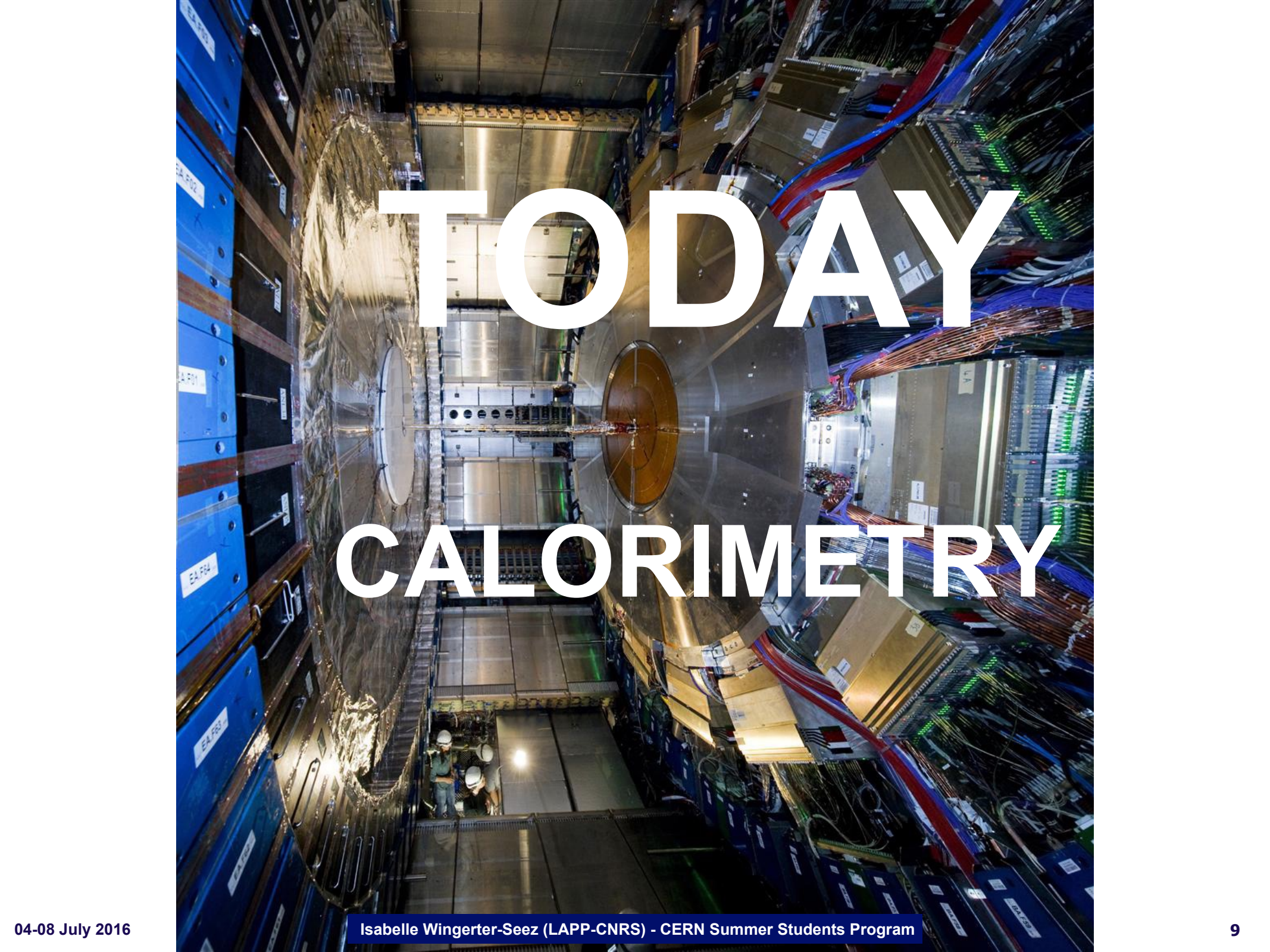
3. Signal collection  
depends on signal and type of detection



4. BUILD a SYSTEM  
depends on physics, experimental conditions,....



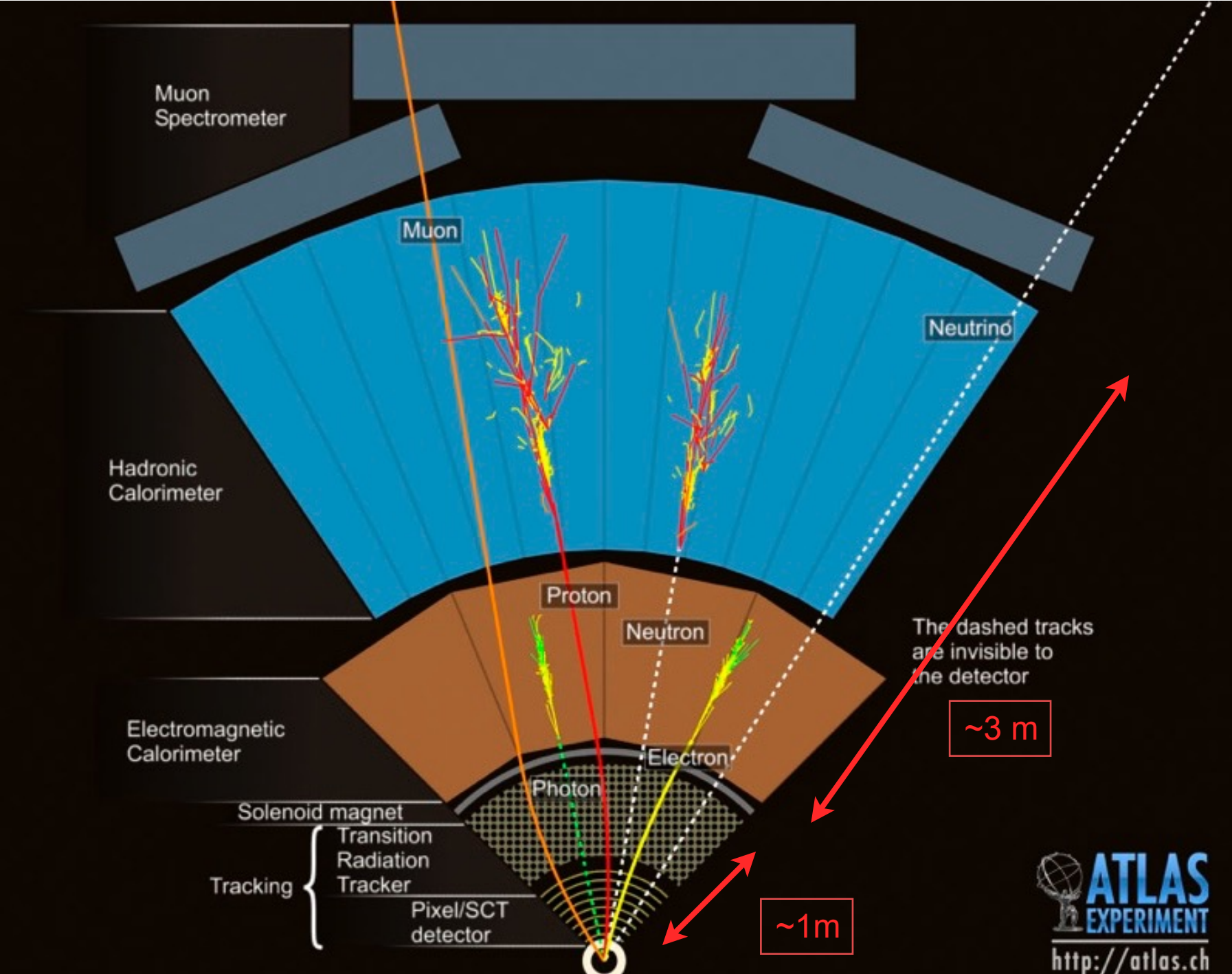


A photograph of a large particle detector, likely the ATLAS calorimeter, showing a complex structure of metal and electronics. The detector is surrounded by a dense network of cables and components. The text "TODAY CALORIMETRY" is overlaid in large white letters across the center of the image.

# TODAY CALORIMETRY



# CALORIMETERS





# Calorimetry: energy measurement by total absorption; often with spatial information



Latin: *calor* = heat

But: calorimetry in particle physics  $\neq \Delta T^*$

E.g.  $\Delta T$  for 1 litre of water at 20°C from energy deposition of:

- 1 GeV particle =  $3.8 \times 10^{-14}$  K
- All 13 TeV from 1 LHC pp collision =  $5.5 \times 10^{-10}$  K

Even if **all protons** in the LHC ( $\sim 10^{14}$ ;  $\sim 10^8$  joules) were dumped into the CMS ECAL and transferred their energy to heat, it would only **heat the CMS ECAL by about 5.5°C**

\*There are some exceptions...

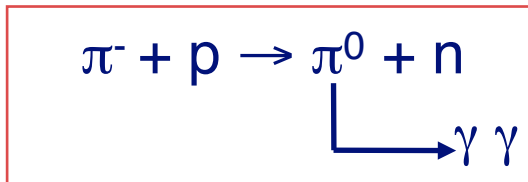
$$[ C_{\text{water}} = 4.18 \text{ J g}^{-1} \text{ K}^{-1}; m = \Delta E / (C_{\text{water}} \Delta T) ]$$

# WHY CALORIMETERS ?

First calorimeters appeared in the 70's:  
need to measure the energy of all particles, charged and **neutral**.

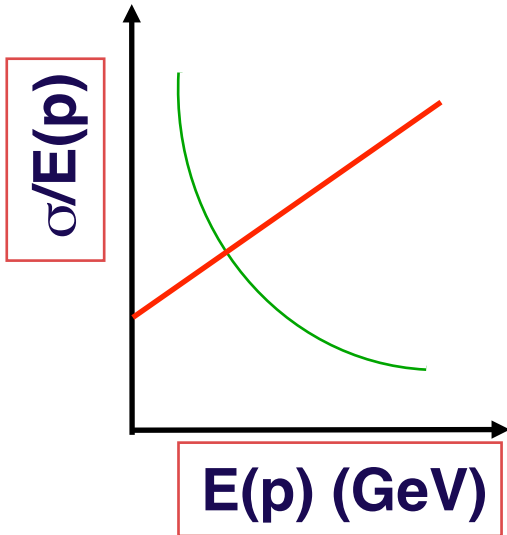
Until then, only the momentum of **charged particles** was measured using **magnetic analysis**.

The measurement with a calorimeter is destructive e.g.



Magnetic analysis

$$\frac{\sigma(p)}{p} = ap \oplus b$$



$$\frac{\sigma(E)}{E} \approx \frac{a}{\sqrt{E}}$$

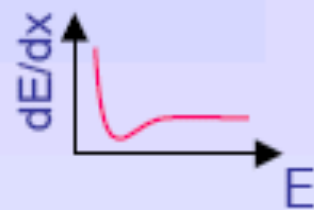
Calorimetry

Particles (but  $\mu$  and  $\nu$ ) do not come out alive of a calorimeter



$e^+ / e^-$

■ Ionisation



■ Bremsstrahlung



$\gamma$

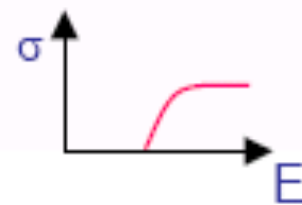
■ Photoelectric effect



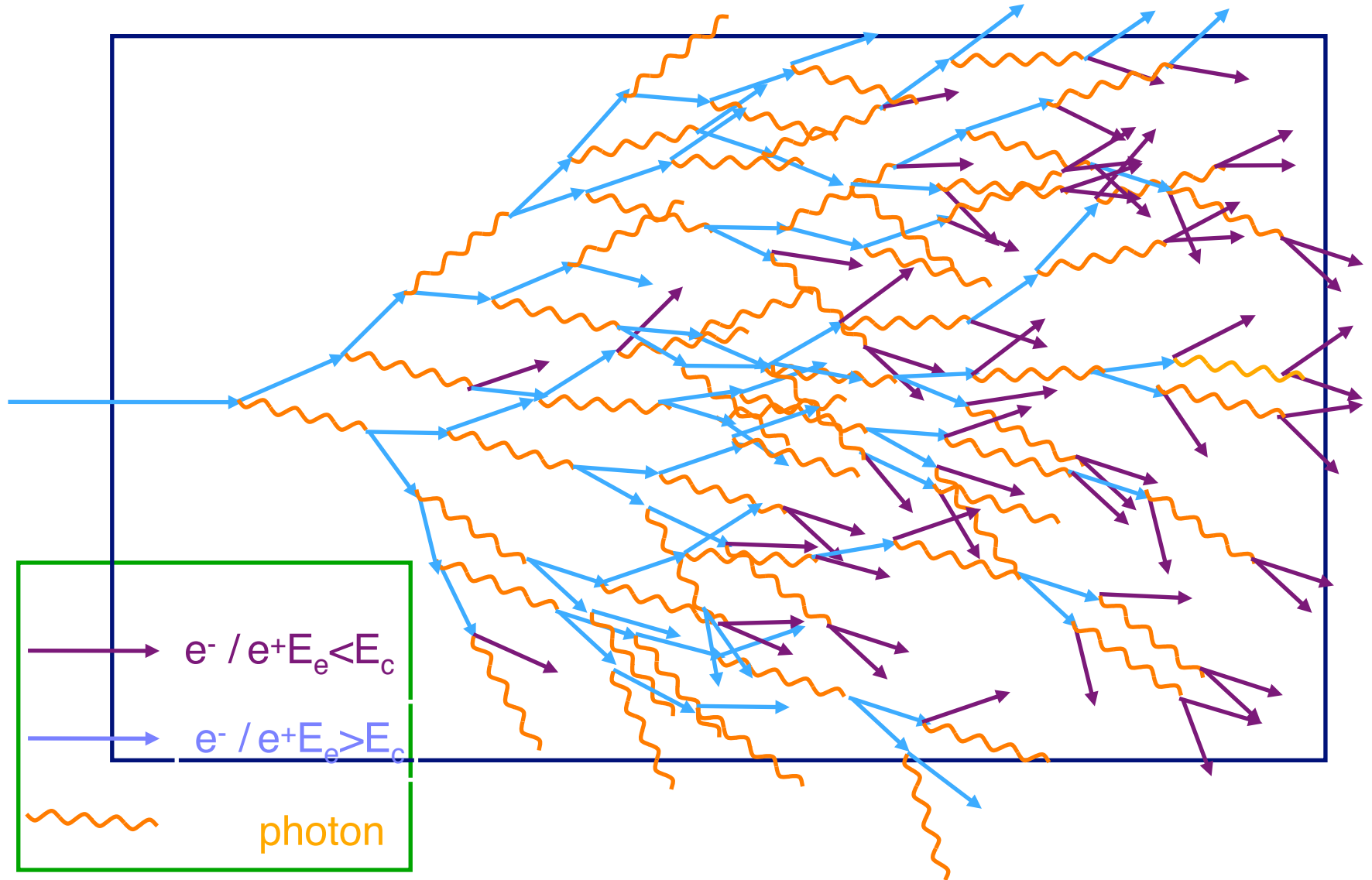
■ Compton effect



■ Pair production



# ELECTROMAGNETIC SHOWER





# ELECTROMAGNETIC SHOWER DEVELOPMENT

The shower develops as a **cascade** by **energy transfer** from the incident particle to a **multitude of particles** ( $e^\pm$  and  $\gamma$ ).

The **number of cascade particles** is **proportional** to the **energy deposited** by the incident particle

The role of the calorimeter is to **count** these cascade particles

The relative occurrence of the various processes briefly described is a function of the material ( $Z$ )

The radiation length ( $X_0$ ) allows to universally describe the shower development

# CRITICAL ENERGY

Critical energy:

$$\left(\frac{dE}{dx}\right)_{\text{Tot}} = \left(\frac{dE}{dx}\right)_{\text{Ion}} + \left(\frac{dE}{dx}\right)_{\text{Brems}}$$

$$\left.\frac{dE}{dx}(E_c)\right|_{\text{Brems}} = \left.\frac{dE}{dx}(E_c)\right|_{\text{Ion}}$$

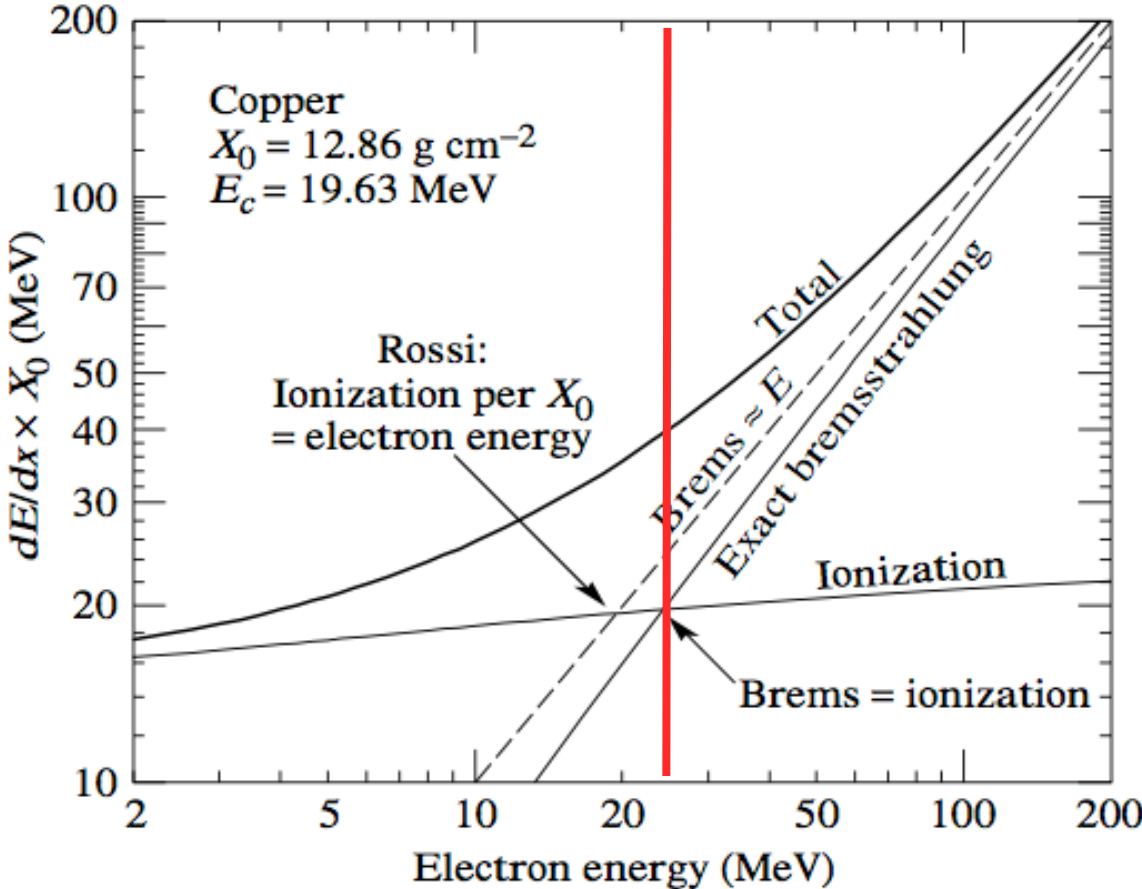
Approximation:

$$E_c^{\text{Gas}} = \frac{710 \text{ MeV}}{Z + 0.92}$$

$$E_c^{\text{Sol/Liq}} = \frac{610 \text{ MeV}}{Z + 1.24}$$

Example Copper:

$$E_c \approx 610/30 \text{ MeV} \approx 20 \text{ MeV}$$





# EM SHOWER DEVELOPMENT: SIMPLE MODEL

The multiplication of the shower continues until the energies fall below the critical energy,  $E_c$

A simple model of the shower uses variables scaled to  $X_0$  and  $E_c$

$$t = \frac{x}{X_0}, y = \frac{E}{E_c}$$

Electrons lose about 2/3 of their energy in  $1X_0$ , and the photons have a probability of 7/9 for conversion:  $X_0 \sim$  generation length

After distance  $t$ :

$$\begin{aligned} \text{number of particles, } & n(t) = 2^t \\ \text{energy of particles, } & E(t) \approx \frac{E}{2^t} \end{aligned}$$

When  $E \sim E_c$  shower maximum:

$$\begin{aligned} n(t_{\max}) &\approx \frac{E}{E_c} = y \\ t_{\max} &\approx \ln \left( \frac{E}{E_c} \right) = \ln y \end{aligned}$$

# EM LONGITUDINAL DEVELOPMENT

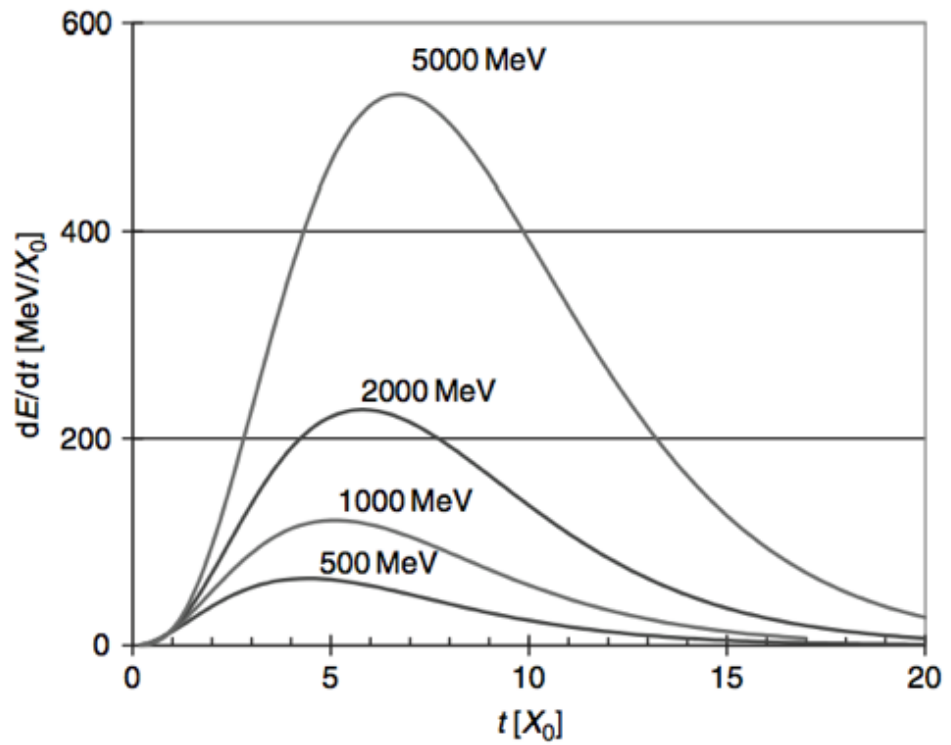
## Longitudinal profile

Parametrization:  
[Longo 1975]

$$\frac{dE}{dt} = E_0 t^\alpha e^{-\beta t}$$

- $\alpha, \beta$  : free parameters
- $t^\alpha$  : at small depth number of secondaries increases ...
- $e^{-\beta t}$  : at larger depth absorption dominates ...

Numbers for  $E = 2$  GeV (approximate):  
 $\alpha = 2, \beta = 0.5, t_{\max} = \alpha/\beta$



More exact  
[Longo 1985]

$$\frac{dE}{dt} = E_0 \cdot \beta \cdot \frac{(\beta t)^{\alpha-1} e^{-\beta t}}{\Gamma(\alpha)}$$

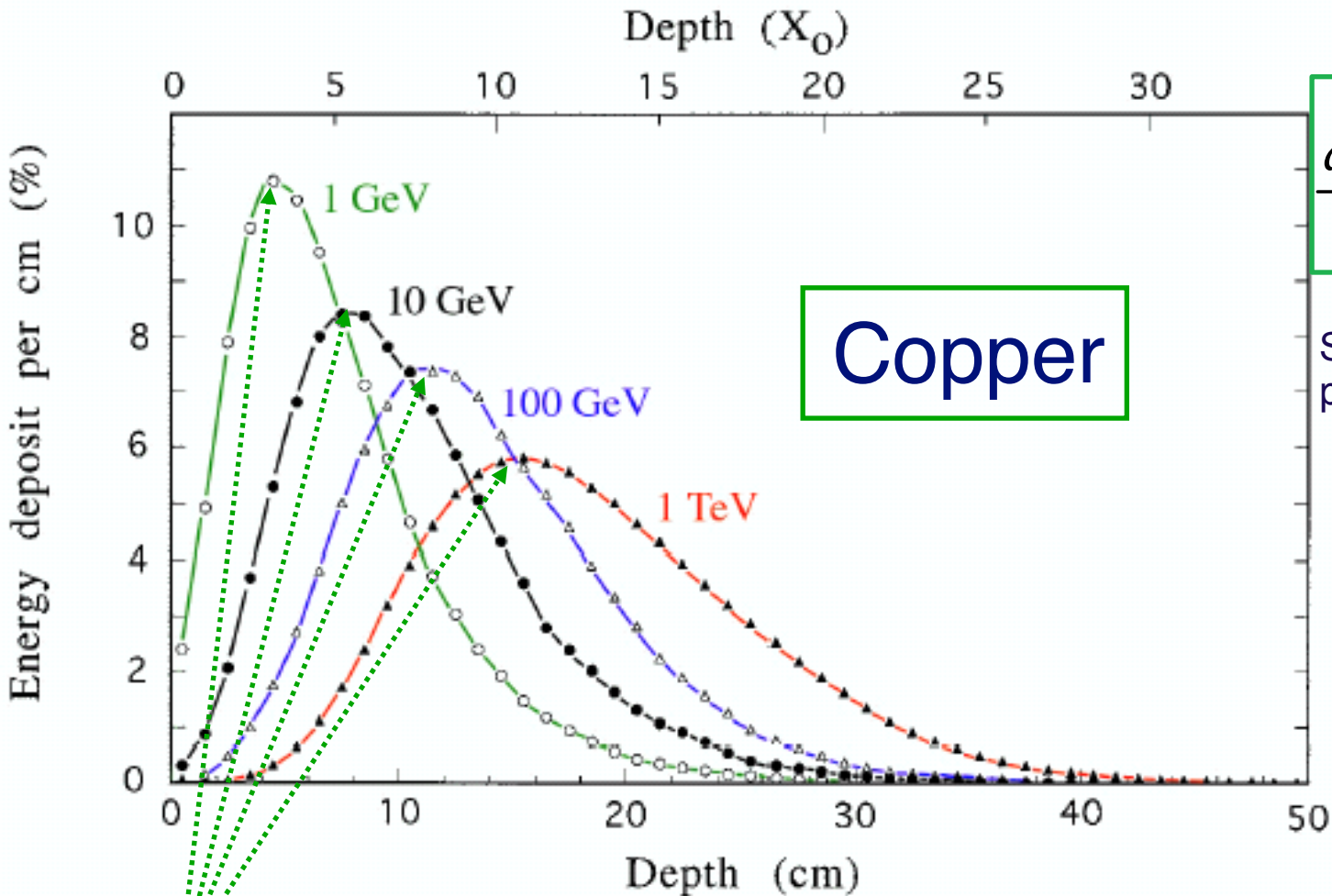
[ $\Gamma$ : Gamma function]

$$\rightarrow t_{\max} = \frac{\alpha - 1}{\beta} = \ln \left( \frac{E_0}{E_c} \right) + C_{e\gamma}$$

with:  
 $C_{e\gamma} = -0.5$  [ $\gamma$ -induced]  
 $C_{e\gamma} = -1.0$  [e-induced]



# EM SHOWERS LONGITUDINAL DEVELOPMENT



$$\frac{dE}{dt} \propto E_0 b \frac{(bt)^{a-1} e^{-bt}}{\Gamma(a)}$$

Copper

Shower energy development parametrization

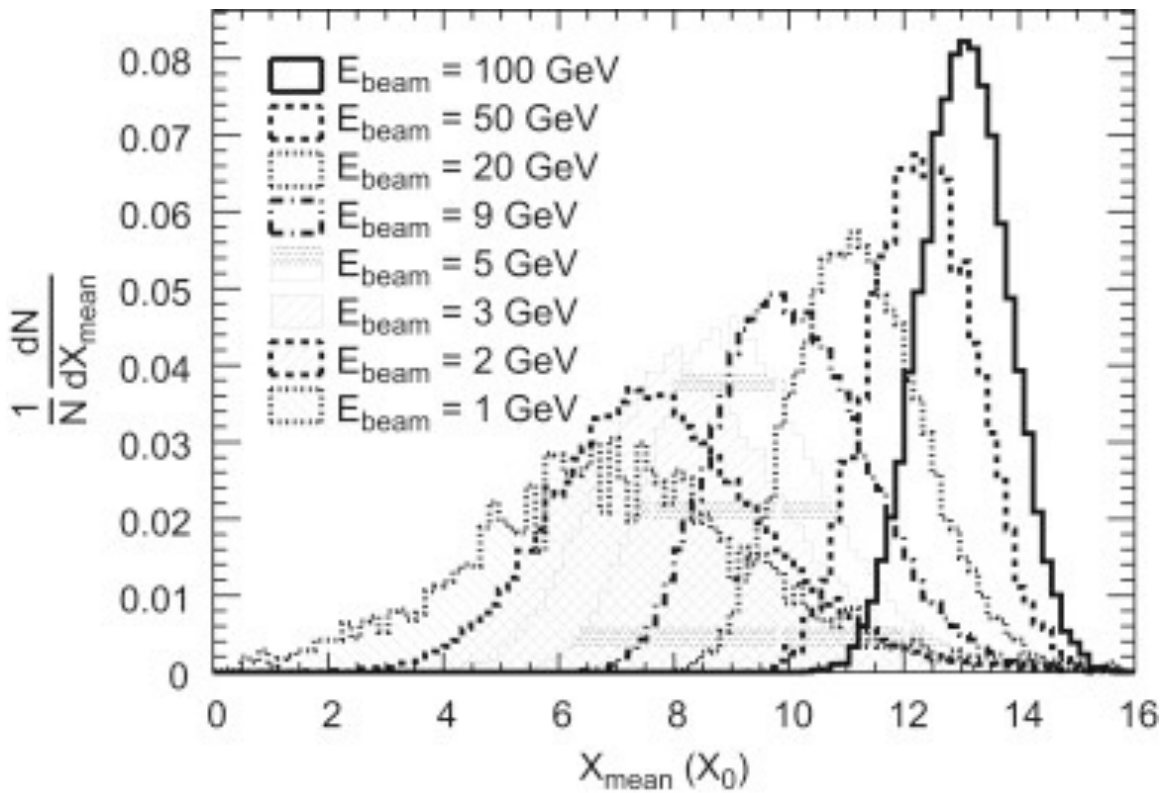
b: material

E.Longo & I.Sestili  
(NIM128-1975)

$$X_{\max} = X_0 \ln\left(\frac{E}{E_c} + t_0\right)$$

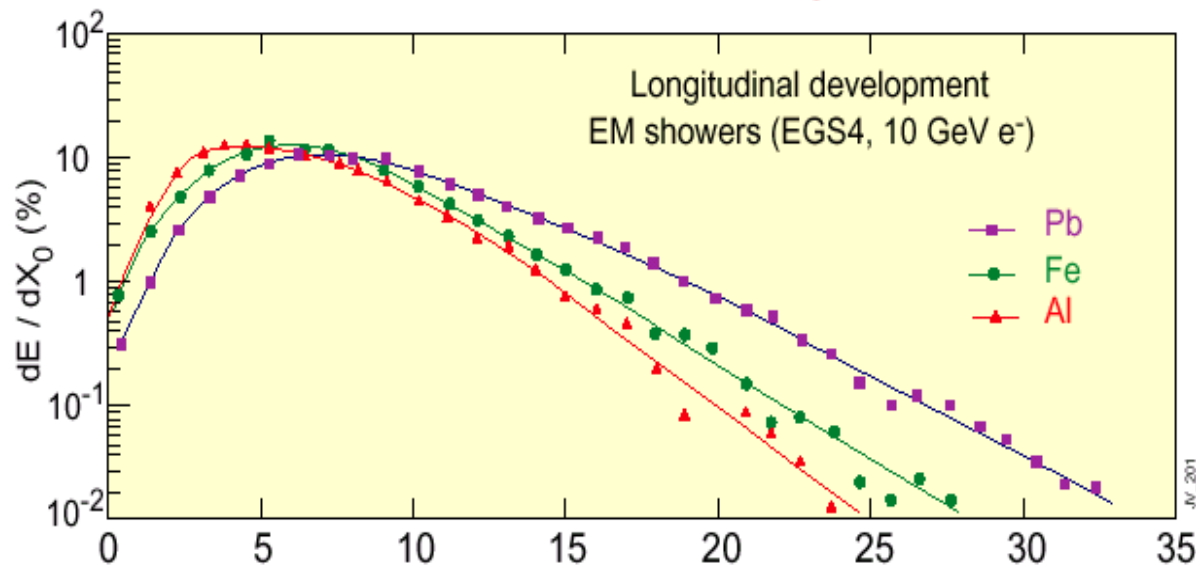
$$t_0 = \begin{matrix} -0.5 \text{ electrons} \\ +0.5 \text{ photons} \end{matrix}$$

# EM SHOWERS LONGITUDINAL DEVELOPMENT



ATLAS combined testbeam  
2004 setup

Electrons shower mean  
depth in  $X_0$  (MC)  
1,2,3,5,9,20,50, 100 GeV



$E_c \propto 1/Z$

- Shower maximum
- Shower tails

$t_{95\%} = t_{\text{max}} + 0.08Z + 9.6$



# SEARCH FOR DECAYS OF THE $Z^0$ INTO A PHOTON AND A PSEUDOSCALAR MESON

ALEPH Collaboration

D. DECAMP, B. DESCHIZEAUX, C. GOY, J.-P. LEES, M.-N. MINARD

Laboratoire de Physique des Particules (LAPP), IN2P3-CNRS, F-74019 Annecy-le-Vieux Cedex, France

.....

Measurement made by ALEPH

$$e^+e^- \rightarrow e^+e^-$$

$$e^+e^- \rightarrow \gamma\gamma$$

Electron/Photon longitudinal development: different

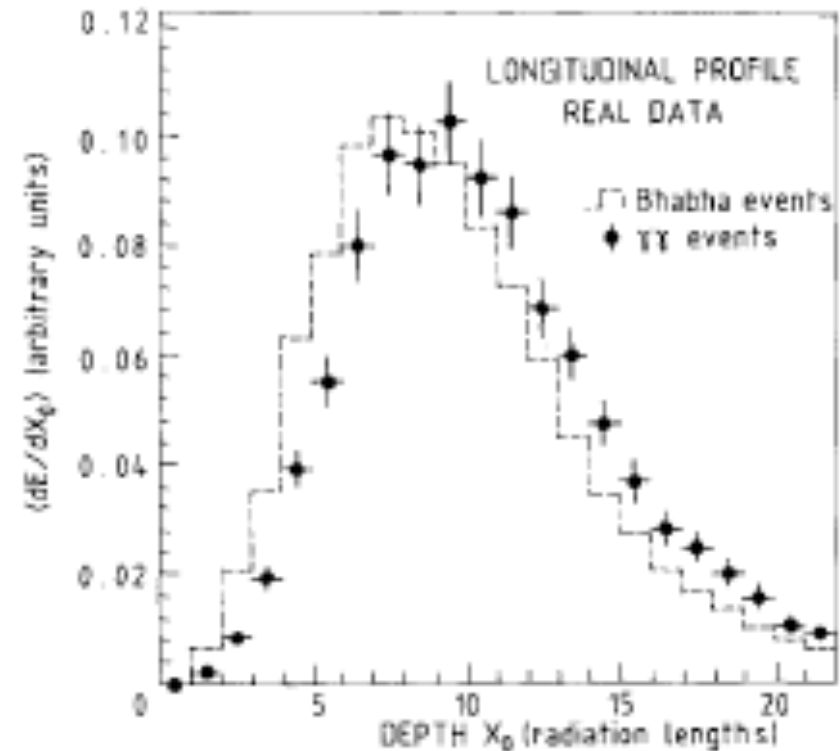


Fig. 1. Longitudinal profile of electromagnetic showers, both for electrons from  $e^+e^- \rightarrow e^+e^-$  and for the  $\gamma\gamma$  candidates. Both samples are real data. There is a clear shift by about 1 radiation length of the photon showers with respect to electron showers, as expected.

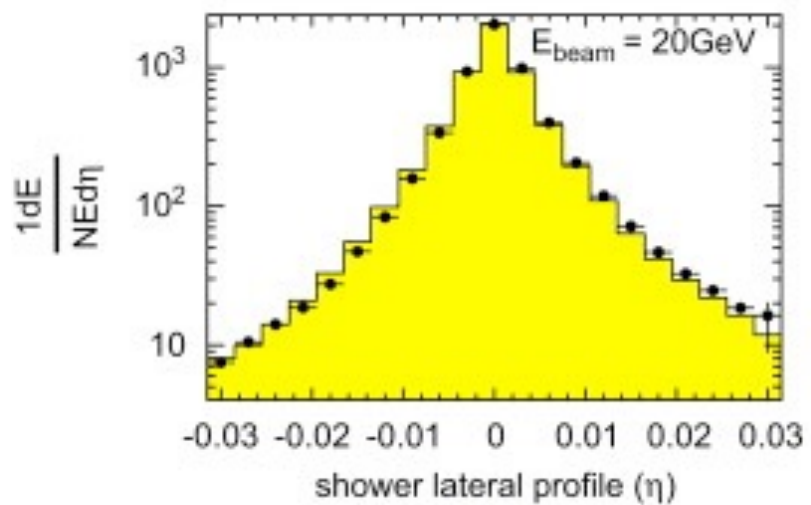
# EM shower lateral development

Molière radius,  $R_m$ , scaling factor for lateral extent, defined by:

$$R_M = \frac{21\text{MeV} \times X_0}{E_c} \approx \frac{7A}{Z} g \times \text{cm}^{-2}$$

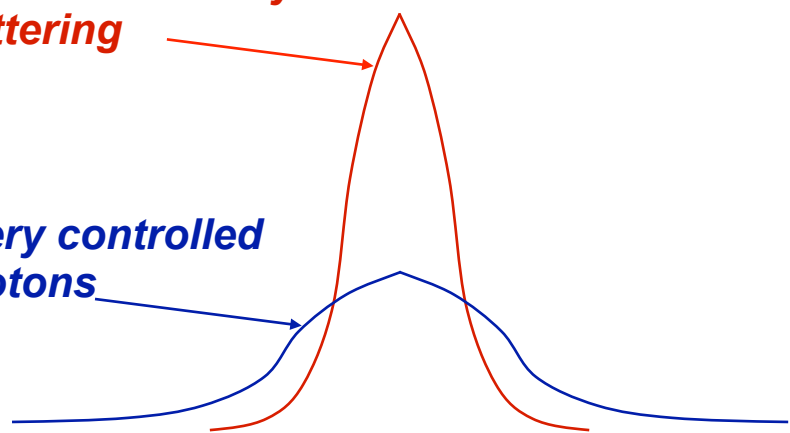
Gives the average lateral deflection of electrons of critical energy after  $1X_0$

- 90% of shower energy contained in a cylinder of  $1R_m$
- 95% of shower energy contained in a cylinder of  $2R_m$
- 99% of shower energy contained in a cylinder of  $3.5R_m$



*Width of core controlled by multiple scattering of  $e^\pm$*

*Width of periphery controlled by Compton photons*

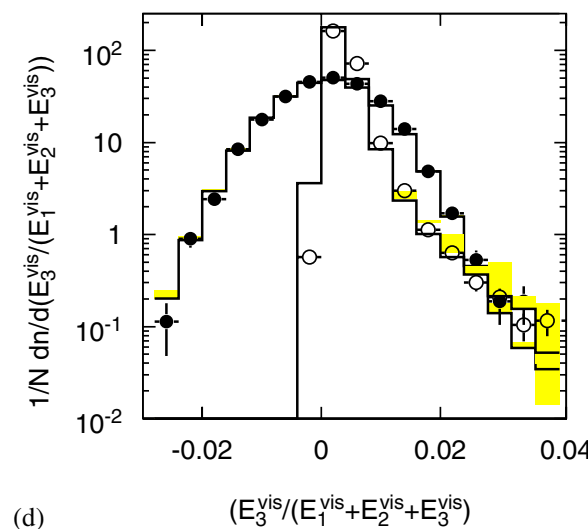
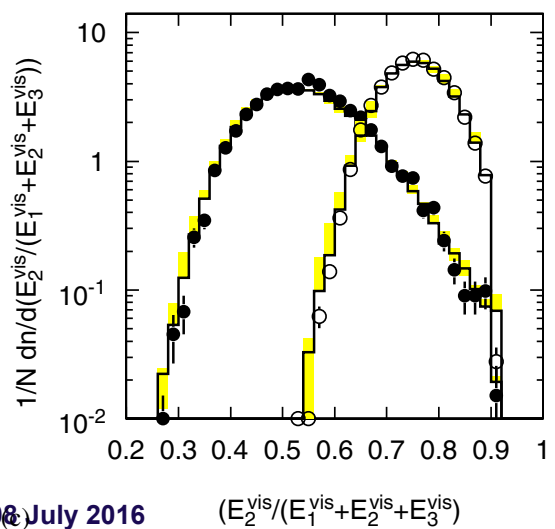
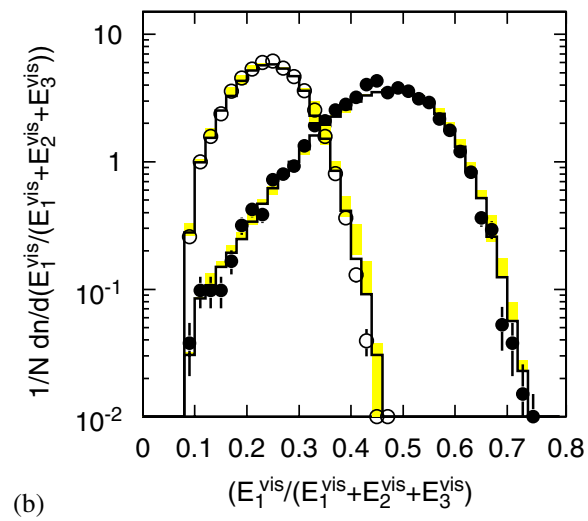
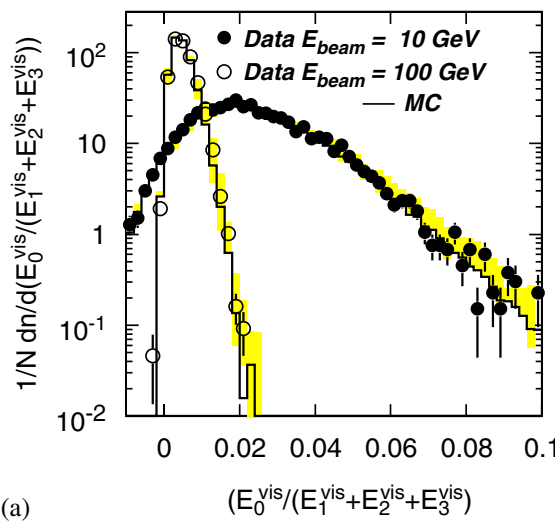




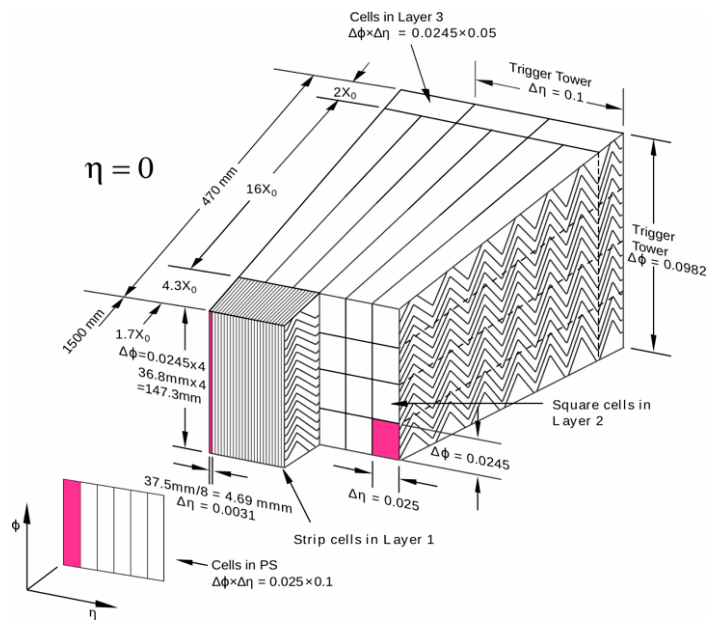
# EM shower simulations

Electromagnetic processes are well understood and can be very well reproduced by MC simulation:

A key element in understanding detector performance



## ATLAS EM calorimeter testbeam



# PROPERTIES of ELECTROMAGNETIC CALORIMETERS

Material	Z	Density [g cm <sup>-3</sup> ]	E <sub>c</sub> [MeV]	X <sub>0</sub> [mm]	ρ <sub>M</sub> [mm]	λ <sub>int</sub> [mm]	(dE/dx) <sub>mip</sub> [MeV cm <sup>-1</sup> ]
C	6	2.27	83	188	48	381	3.95
Al	13	2.70	43	89	44	390	4.36
Fe	26	7.87	22	17.6	16.9	168	11.4
Cu	29	8.96	20	14.3	15.2	151	12.6
Sn	50	7.31	12	12.1	21.6	223	9.24
W	74	19.3	8.0	3.5	9.3	96	22.1
Pb	82	11.3	7.4	5.6	16.0	170	12.7
<sup>238</sup> U	92	18.95	6.8	3.2	10.0	105	20.5
Concrete	-	2.5	55	107	41	400	4.28
Glass	-	2.23	51	127	53	438	3.78
Marble	-	2.93	56	96	36	362	4.77
Si	14	2.33	41	93.6	48	455	3.88
Ge	32	5.32	17	23	29	264	7.29
Ar (liquid)	18	1.40	37	140	80	837	2.13
Kr (liquid)	36	2.41	18	47	55	607	3.23
Polystyrene	-	1.032	94	424	96	795	2.00
Plexiglas	-	1.18	86	344	85	708	2.28
Quartz	-	2.32	51	117	49	428	3.94
Lead-glass	-	4.06	15	25.1	35	330	5.45
Air 20°, 1 atm	-	0.0012	87	304 m	74 m	747 m	0.0022
Water	-	1.00	83	361	92	849	1.99



# TOWARDS ELECTROMAGNETIC CALORIMETERS

Detectable signal is proportional to the number of potentially detectable particles in the shower  $N_{\text{tot}} \propto E_0/E_c$

Total track length  $T_0 = N_{\text{tot}} \cdot X_0 \sim E_0/E_c \cdot X_0$

$$\frac{\sigma(E)}{E} \propto \frac{1}{\sqrt{T_0}} \propto \frac{1}{\sqrt{E}}$$

Detectable track length  $T_r = f_s \cdot T_0$  where  $f_s$  is the fraction of  $N_{\text{tot}}$  which can be detected by the involved detection process (Cerenkov light, scintillation light, ionization)  $E_{\text{kin}} > E_{\text{th}}$

$$\frac{\sigma(E)}{E} \propto \frac{1}{\sqrt{E}} \frac{1}{\sqrt{f_s}}$$

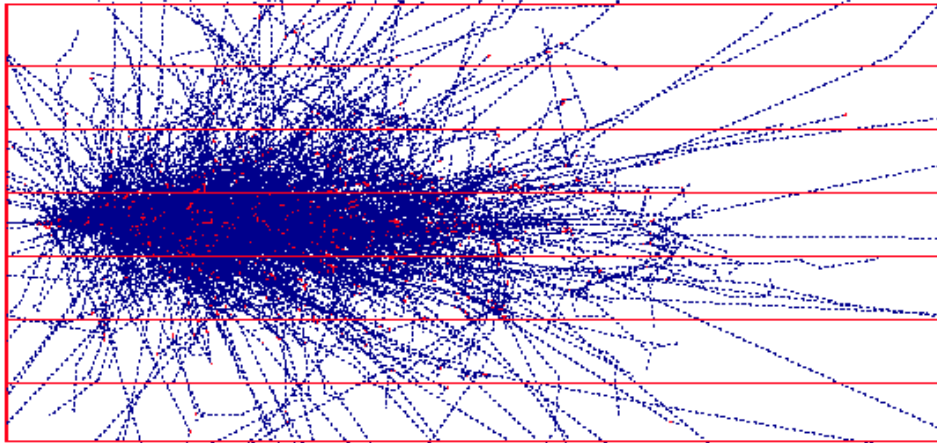
Converting back to materials ( $X_0 \propto A/Z^2$ ,  $E_c \propto 1/Z$ ) and fixing  $E$

Maximize detection  $f_s$

Minimize  $Z/A$

$$\frac{\sigma(E)}{E} \propto \frac{1}{\sqrt{f_s}} \sqrt{\frac{E_c}{X_0}} \propto \frac{1}{\sqrt{f_s}} \sqrt{\frac{Z}{A}}$$

# HOMOGENOUS CALORIMETERS



All the energy is deposited in the active medium

Excellent energy resolution

No longitudinal segmentation

All  $e^\pm$  with  $E_{\text{kin}} > E_{\text{th}}$  produce a signal

Scintillating crystals

$$E_{\text{th}} \approx \beta \cdot E_{\text{gap}} \sim \text{eV}$$

$$\rightarrow 10^2 \div 10^4 \gamma/\text{MeV}$$

$$\sigma/E \sim (1 \div 3)\% / \sqrt{E} \text{ (GeV)}$$

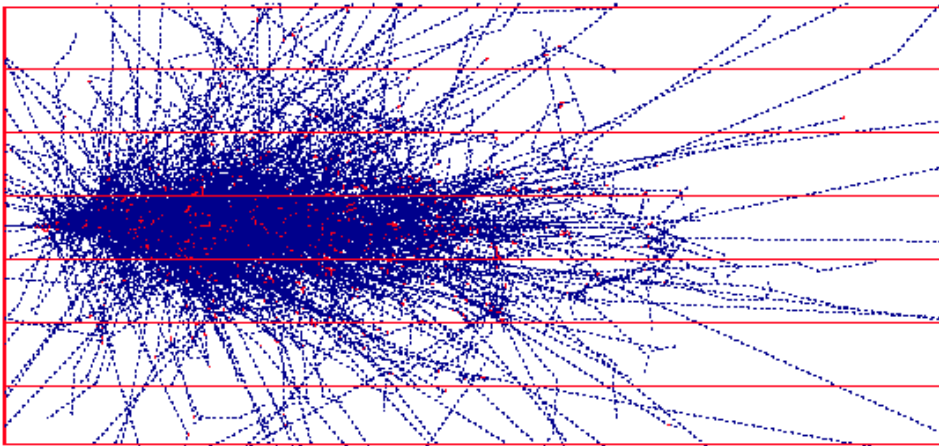
Cerenkov radiators

$$\beta > 1/n \rightarrow E_{\text{th}} \approx 0.7 \text{ MeV}$$

$$\rightarrow 10 \div 30 \gamma/\text{MeV}$$

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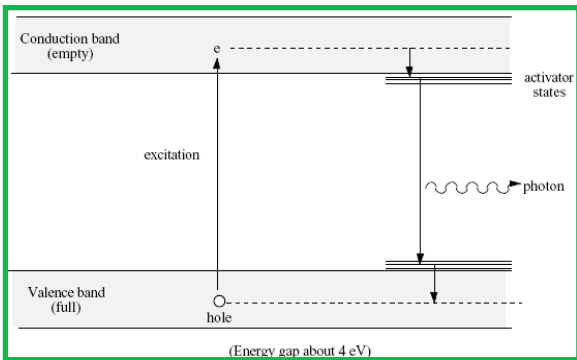
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Cerenkov radiators

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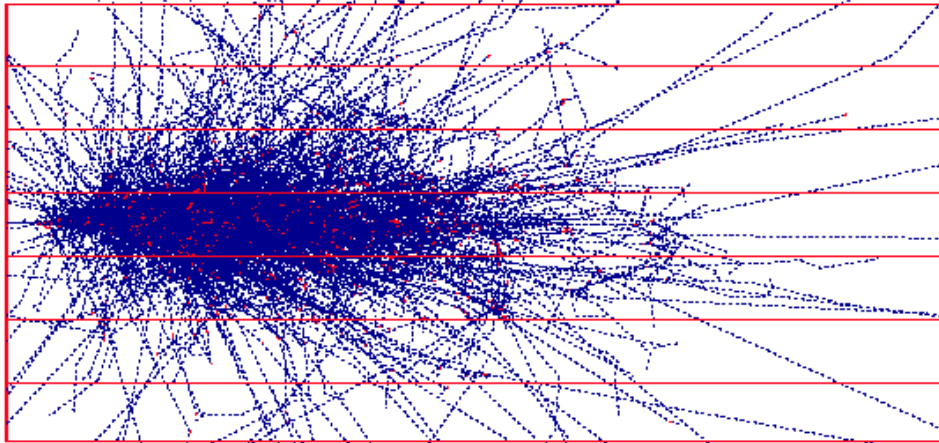
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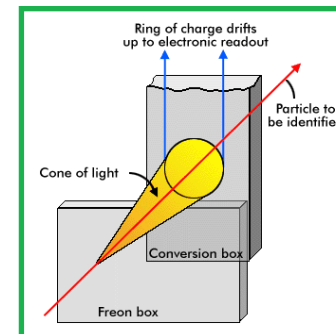
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Cerenkov radiators

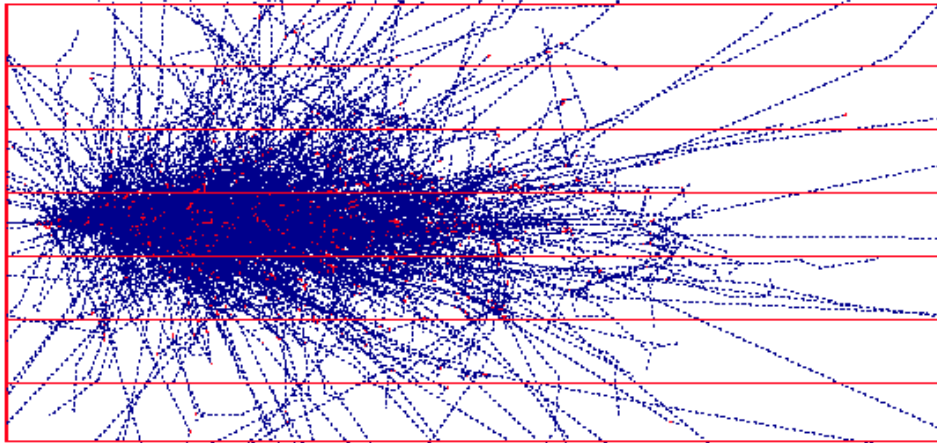
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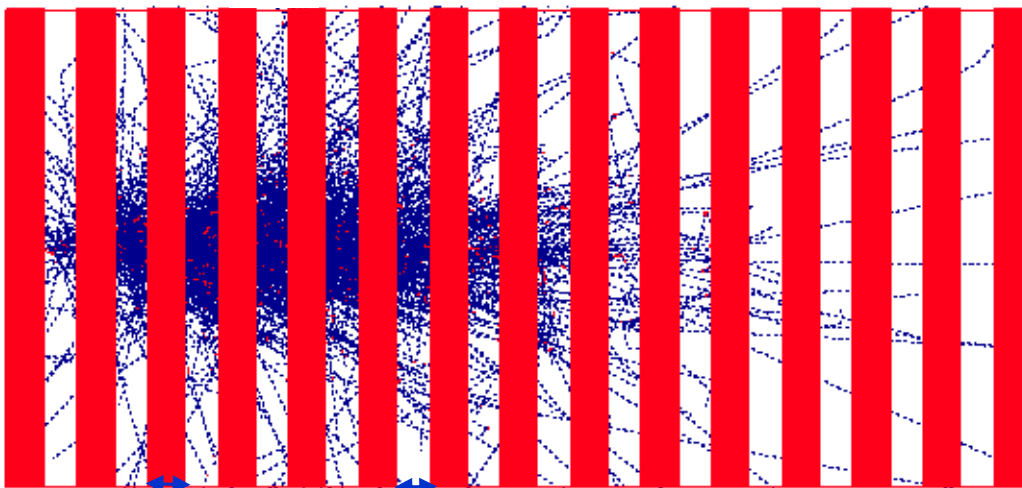
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$$\rightarrow 10 \div 30 \text{ } \gamma/\text{MeV}$$

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# SAMPLING CALORIMETERS



Shower is sampled by layers of an active medium and dense radiator

Limited energy resolution

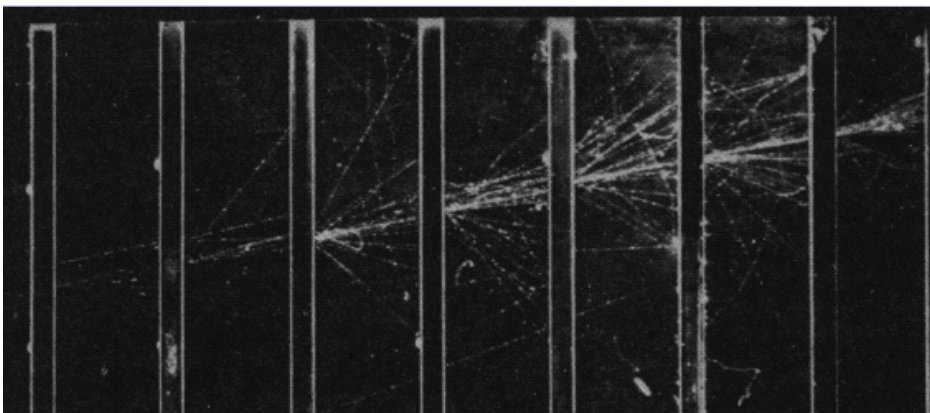
Longitudinal segmentation

Only  $e^\pm$  with  $E_{\text{kin}} > E_{\text{th}}$  of the active layer produce a signal

Absorber (high Z): typically Lead, Uranium

Active medium (low Z): typically Scintillators, Liquid Argon, Wire chamber

Energy resolution of sampling calorimeter dominated by fluctuations in energy deposited in the active layers



$$\sigma(E)/E \sim (10 \div 20)\% / \sqrt{E \text{ (GeV)}}$$



# SAMPLING FLUCTUATIONS



Most of detectable particles are produced in the absorber layers

Need to enter the active material to be counted/measured

Using the model of the track length

$$T_r = f_s T_0 \sim f_s \cdot E/E_c^{abs} \cdot X_0^{abs}$$

$f_s$ : sampling fraction

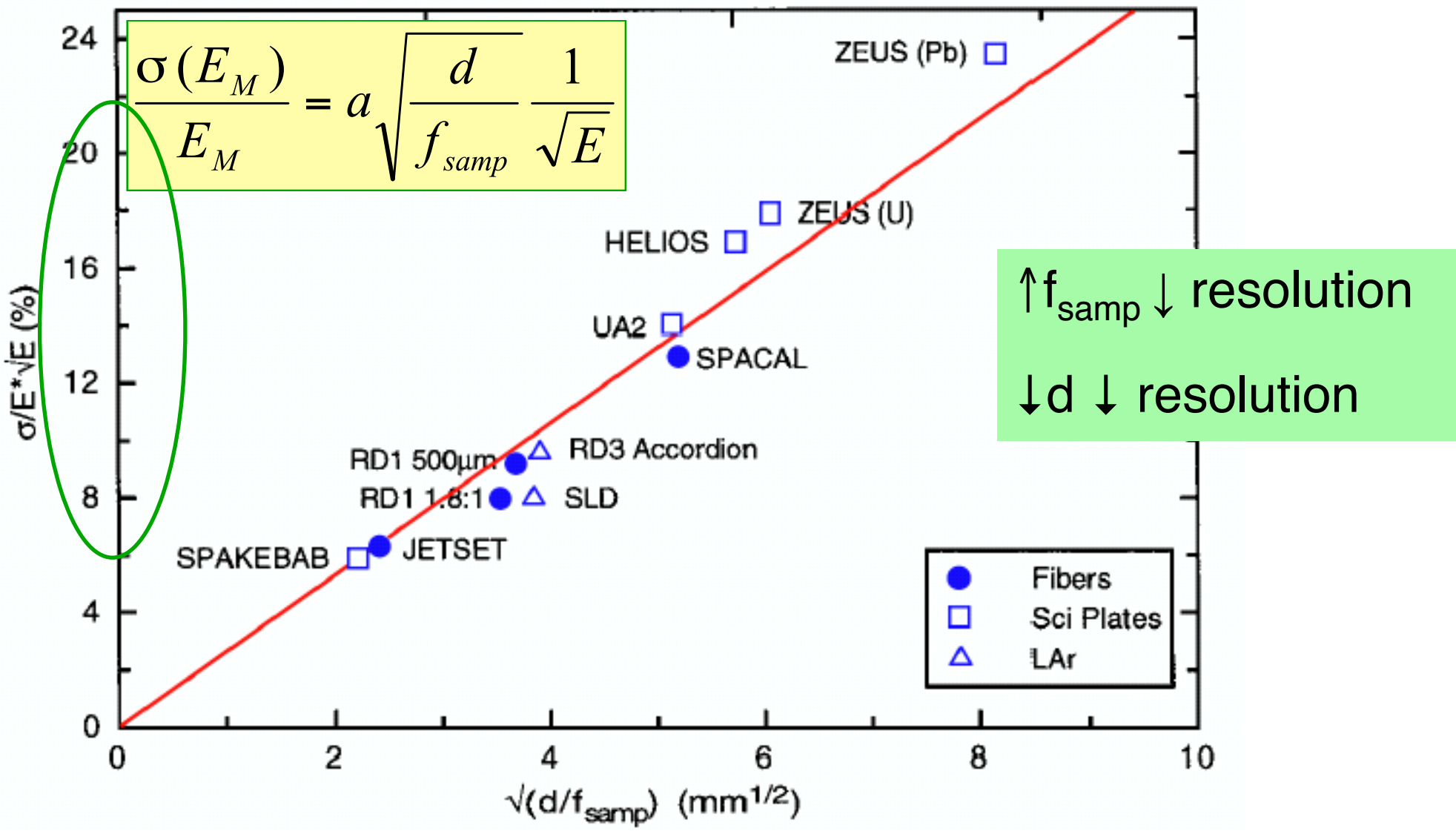
Number of detectable particles in active layer

$$N_r = T_r/d = f_s \cdot E/E_c^{abs} \cdot X_0^{abs}/d$$

Resolution scales like

$$\frac{\sigma(E_M)}{E_M} = a \sqrt{\frac{d}{f_{samp}}} \frac{1}{\sqrt{E}}$$

# RESOLUTION FOR SAMPLING CALORIMETERS



# ENERGY RESOLUTION

$$\frac{\sigma}{E} = \frac{a}{\sqrt{E}} \oplus \frac{b}{E} \oplus c$$

**a** the **stochastic term** accounts for Poisson-like fluctuations

naturally small for homogeneous calorimeters

takes into account sampling fluctuations for sampling calorimeters

**b** the **noise term** (hits at low energy)

mainly the energy equivalent of the electronics noise

at LHC in particular: includes fluctuation from non primary interaction (pile-up noise)

**c** the **constant term** (hits at high energy)

Essentially detector non homogeneities like intrinsic geometry, calibration but also energy leakage



# EXAMPLE

Take a Lead Glass crystal

$$E_c = 15 \text{ MeV}$$

produces Cerenkov light

Cerenkov radiation is produced par  $e^\pm$  with  $\beta > 1/n$ , i.e  $E > 0.7\text{MeV}$

Take a 1 GeV electron

At maximum 1000 MeV/0.7 MeV  $e^\pm$  will produce light

Fluctuation  $1/\sqrt{1400} = 3\%$

One then has to take into account the photon detection efficiency which is typically 1000 photo-electrons/GeV:  $1/\sqrt{1000} \sim 3\%$

Final resolution  $\sigma/E \sim 5\%/\sqrt{E}$

# CMS crystals: $\text{PbWO}_4$



Excellent energy resolution

$X_0 = 0.89\text{cm} \rightarrow$  compact calorimeter (23cm for 26  $X_0$ )

$R_M = 2.2\text{ cm} \rightarrow$  compact shower development

Fast light emission (80% in less than 15 ns)

Radiation hard ( $10^5\text{Gy}$ )

But

Low light yield (150  $\gamma/\text{MeV}$ )

Response varies with dose

Response temperature dependance

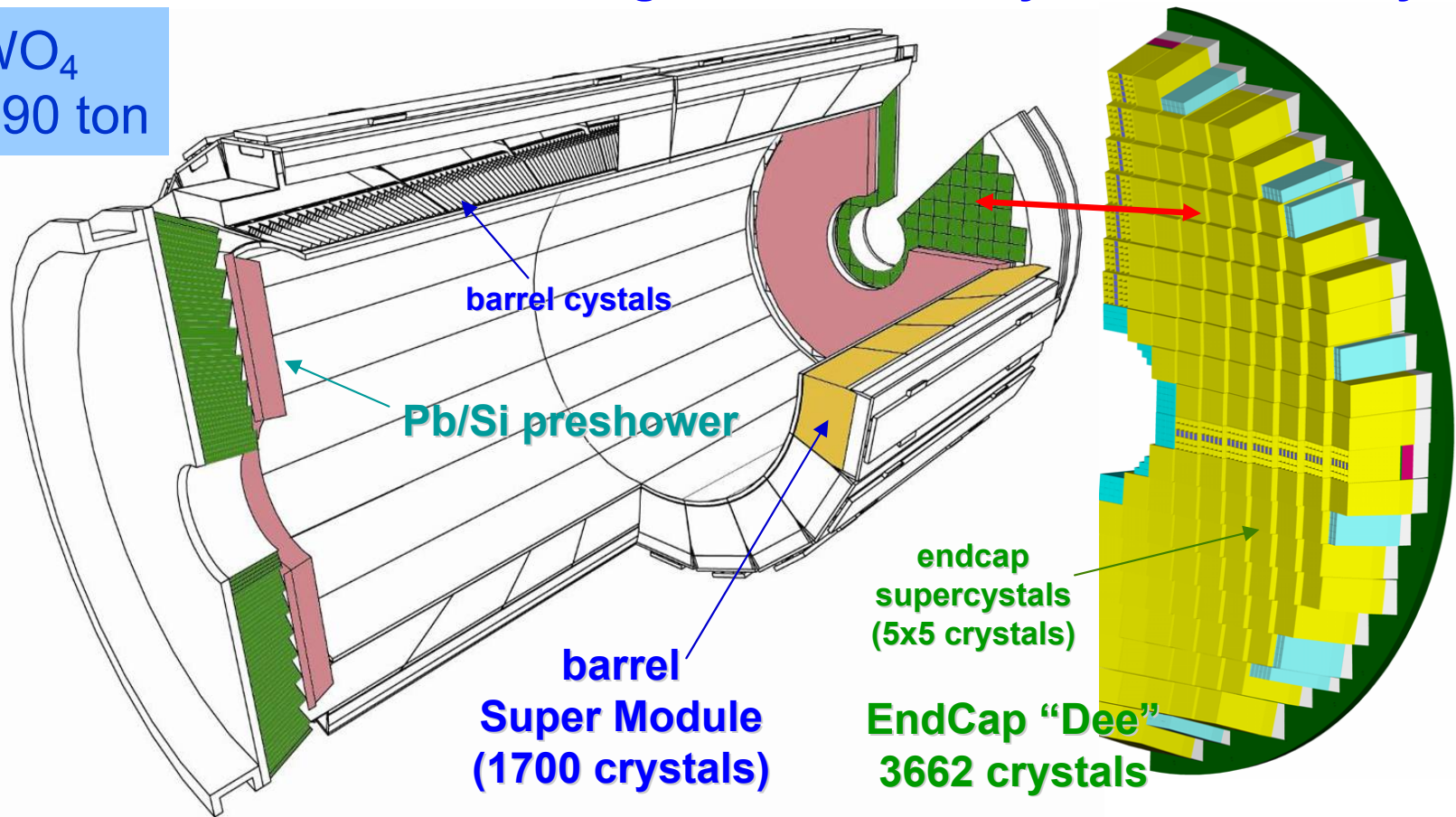


# ECAL @ CMS

Precision electromagnetic calorimetry: 75848 PWO crystals

PWO:  $\text{PbWO}_4$   
about 10 m<sup>3</sup>, 90 ton

Previous  
Crystal  
calorimeters:  
max 1m<sup>3</sup>



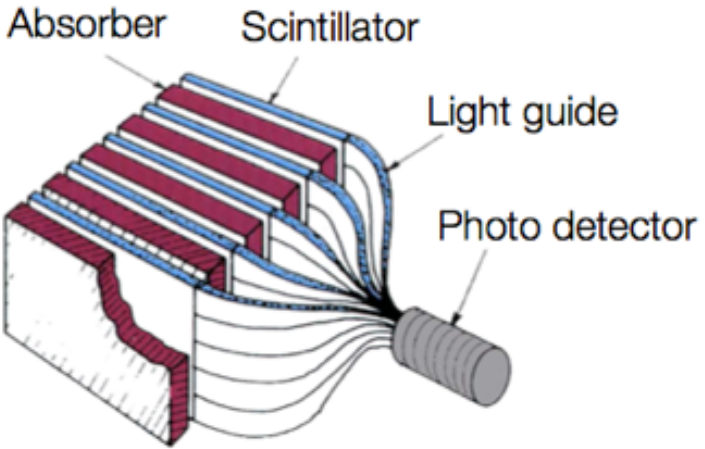
**Barrel:  $|\eta| < 1.48$**   
**36 Super Modules**  
**61200 crystals (2x2x23cm<sup>3</sup>)**

**EndCaps:  $1.48 < |\eta| < 3.0$**   
**4 Dees**  
**14648 crystals (3x3x22cm<sup>3</sup>)**



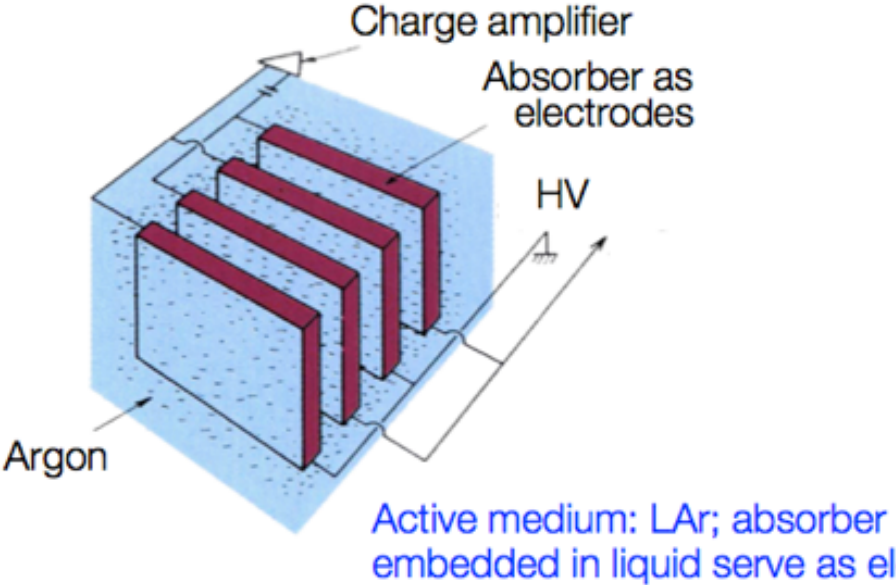
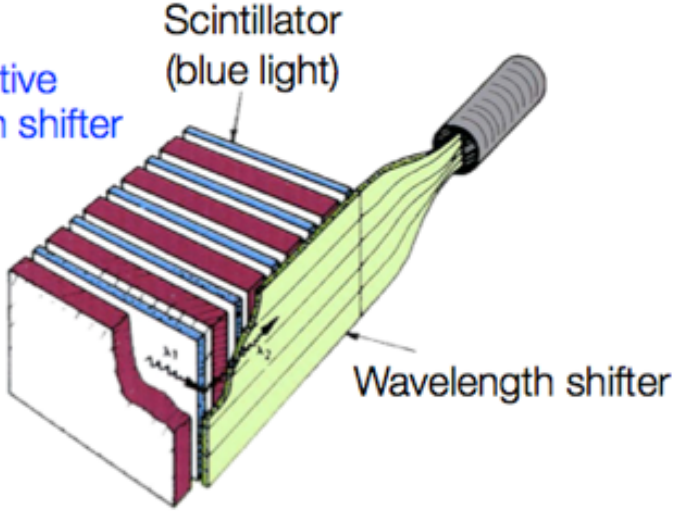
# SAMPLING CALORIMETER

Scintillators as active layer;  
signal readout via photo multipliers

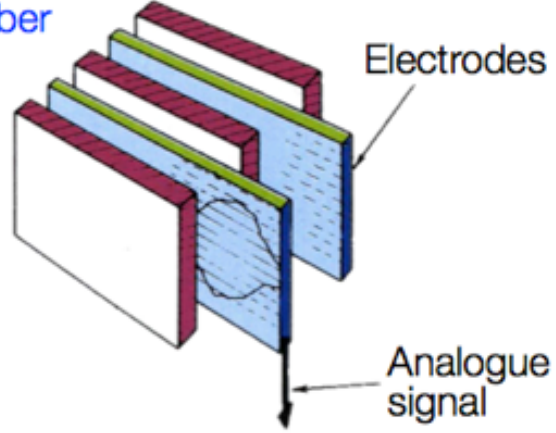


## Possible setups

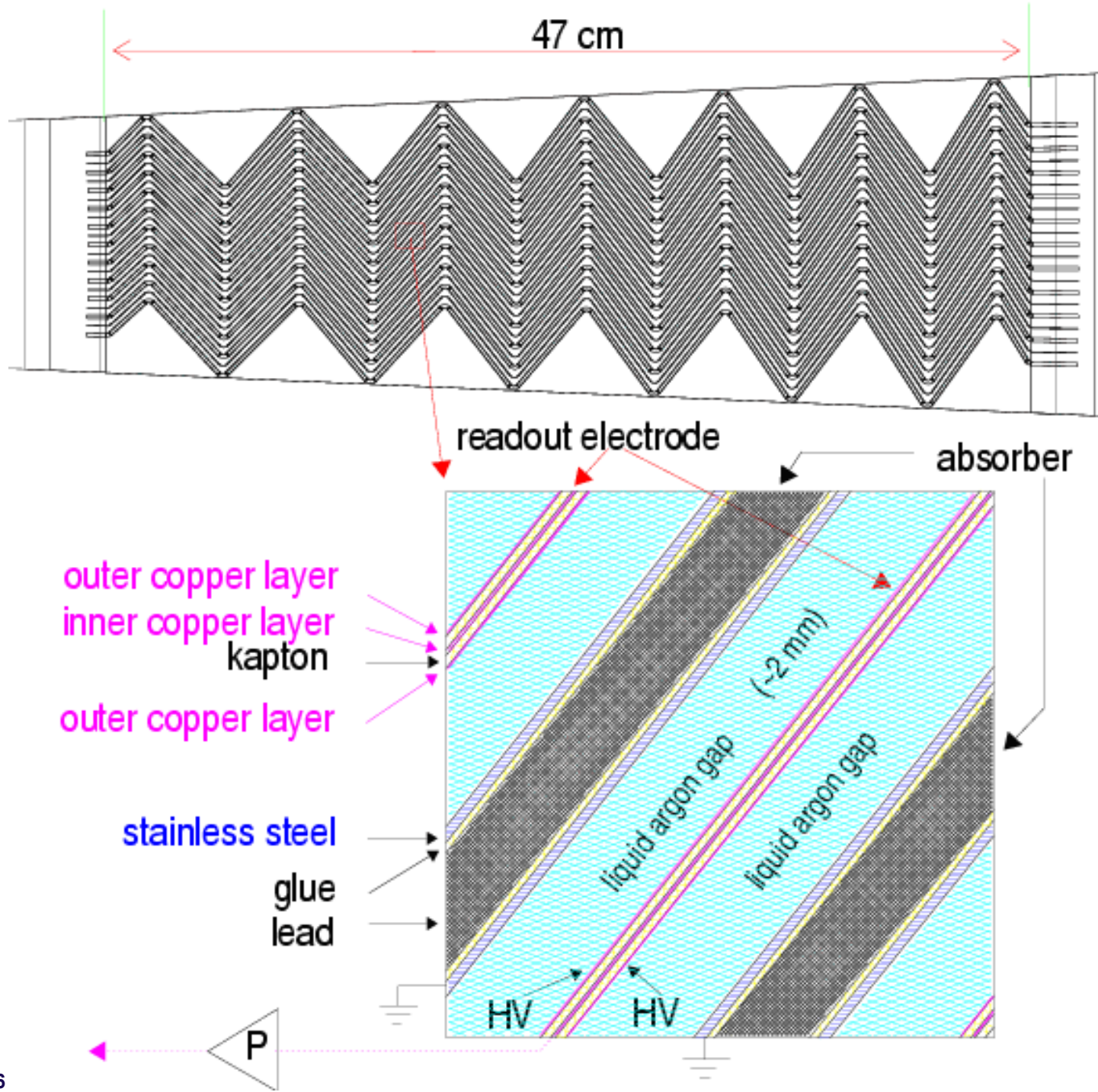
Scintillators as active layer; wave length shifter to convert light



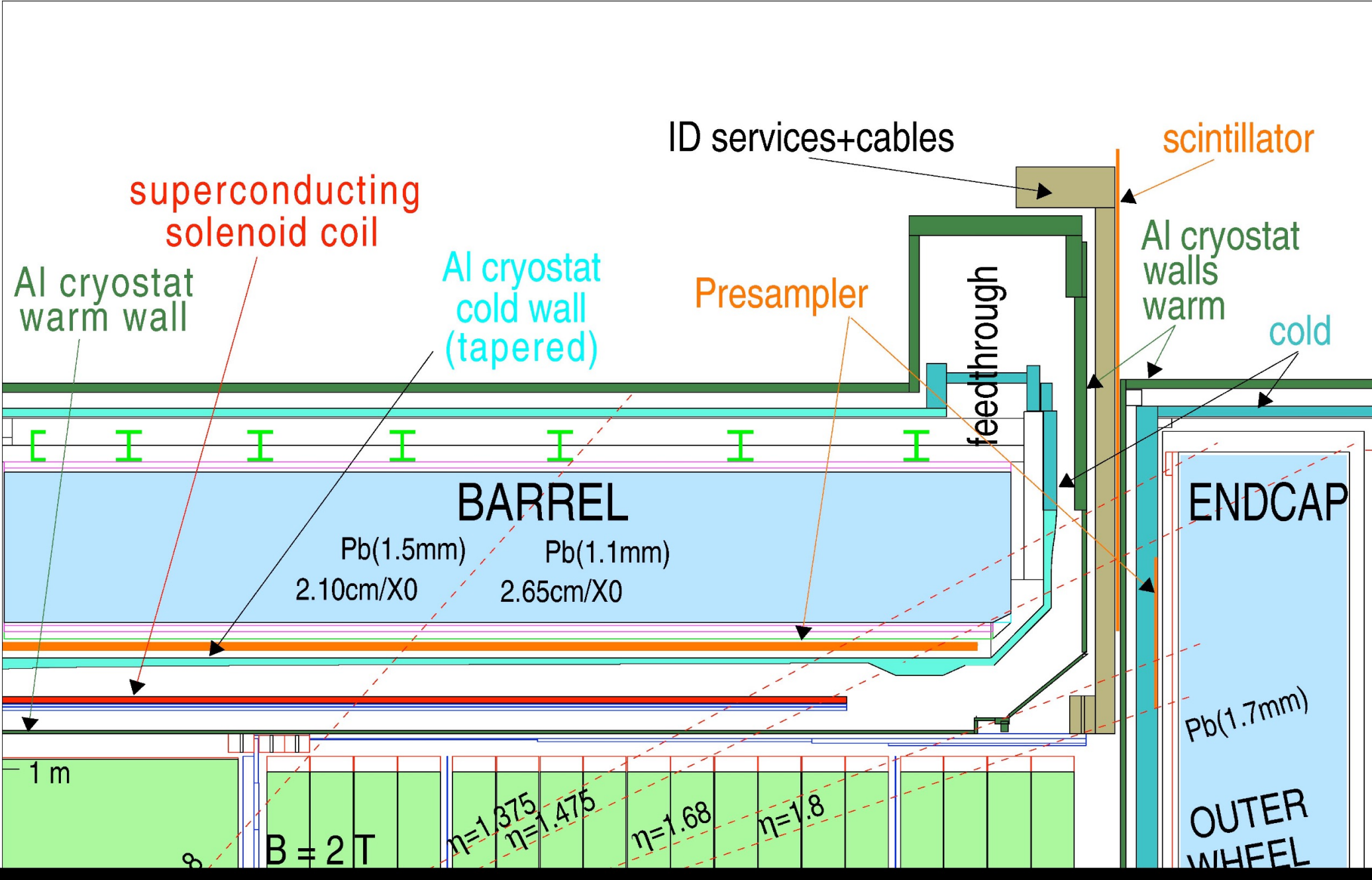
Ionization chambers between absorber plates



# ATLAS LIQUID ARGON EM CALORIMETER



# THE ATLAS CALORIMETER STRUCTURE





# ATLAS ELECTROMAGNETIC CALORIMETER

**Accordion Pb/LAr  $|\eta| < 3.2$  ~170k channels**

Precision measurement  $|\eta| < 2.5$

3 layers up to  $|\eta| = 2.5$  + presampler  $|\eta| < 1.8$

2 layers  $2.5 < |\eta| < 3.2$

Layer 1 ( $\gamma/\pi^0$  rej. + angular meas.)

$$\Delta\eta \cdot \Delta\phi = 0.003 \times 0.1$$

Layer 2 (shower max)

$$\Delta\eta \cdot \Delta\phi = 0.025 \times 0.025$$

Layer 3 (Hadronic leakage)

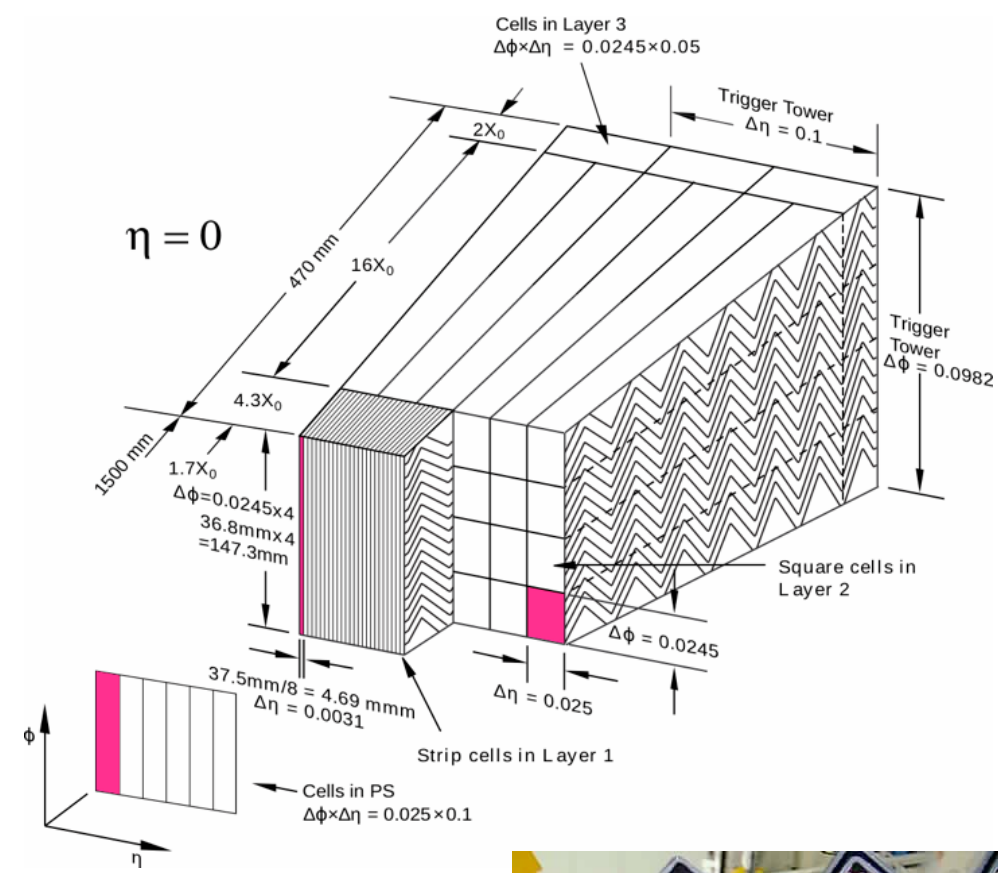
$$\Delta\eta \cdot \Delta\phi = 0.05 \times 0.025$$

**Energy Resolution: design for  $\eta \sim 0$**

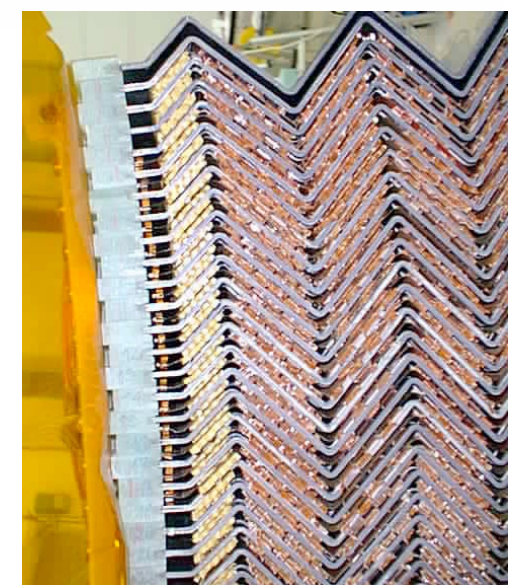
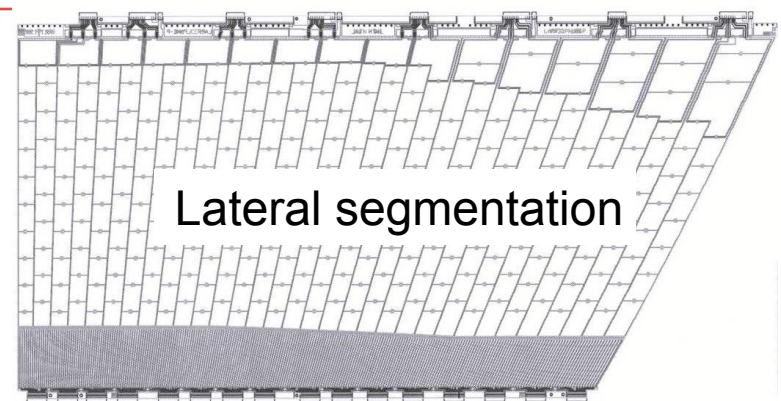
$$\Delta E/E \sim 10\%/\sqrt{E} \oplus 150 \text{ MeV}/E \oplus 0.7\%$$

**Angular Resolution**

$$50 \text{ mrad}/\sqrt{E(\text{GeV})}$$



origin:27. dwg du 02/07/1999



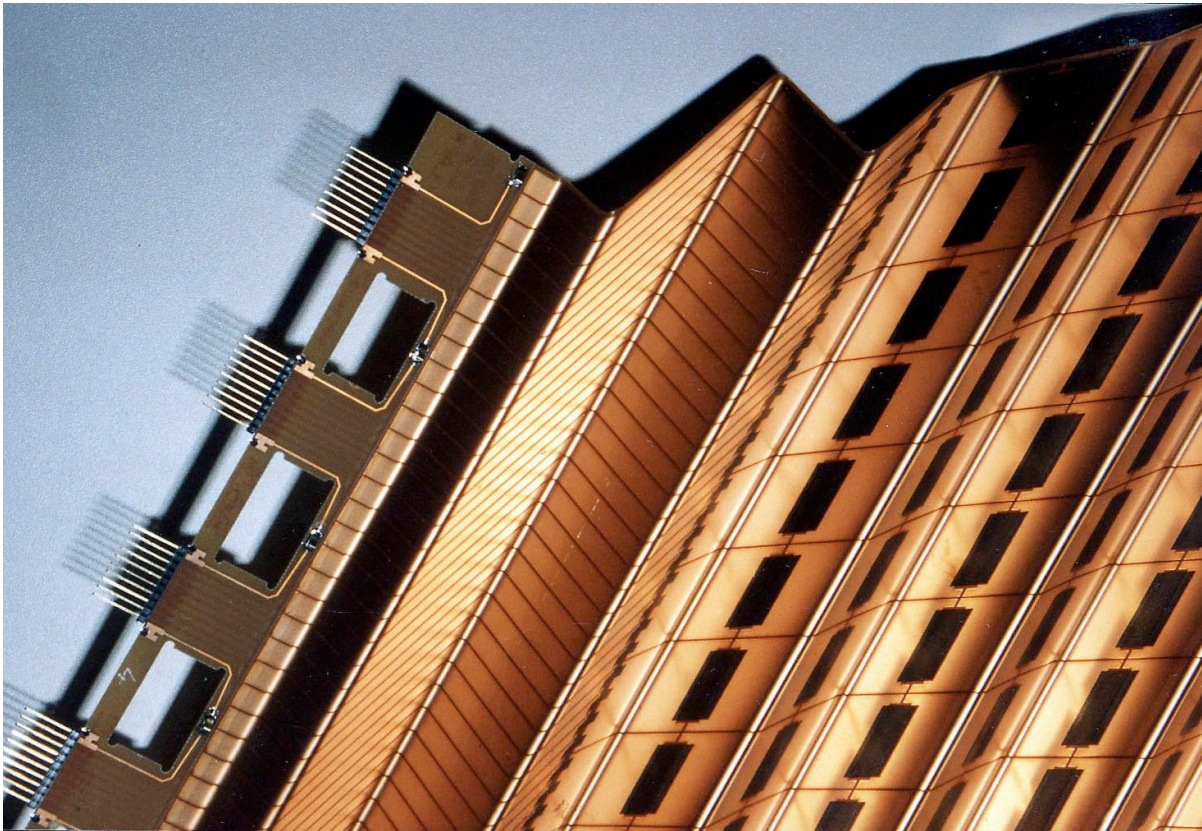
170k channels

# POSITION-ANGULAR RESOLUTION

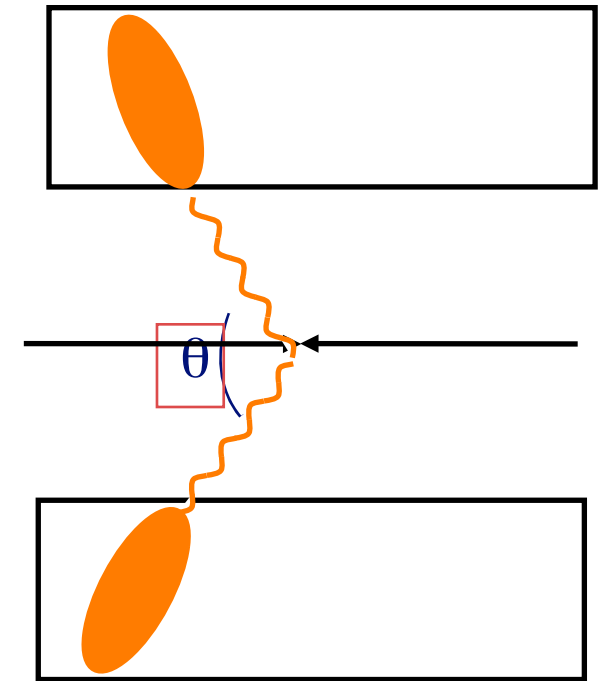
## Higgs Boson in ATLAS

For  $M_H \sim 120$  GeV, in the channel  $H \rightarrow \gamma\gamma$

$$\sigma(M_H) / M_H = \frac{1}{2} [\sigma(E_{\gamma 1})/E_{\gamma 1} \oplus \sigma(E_{\gamma 2})/E_{\gamma 2} \oplus \cot(\theta/2) \sigma(\theta)]$$



04-08 July 2016

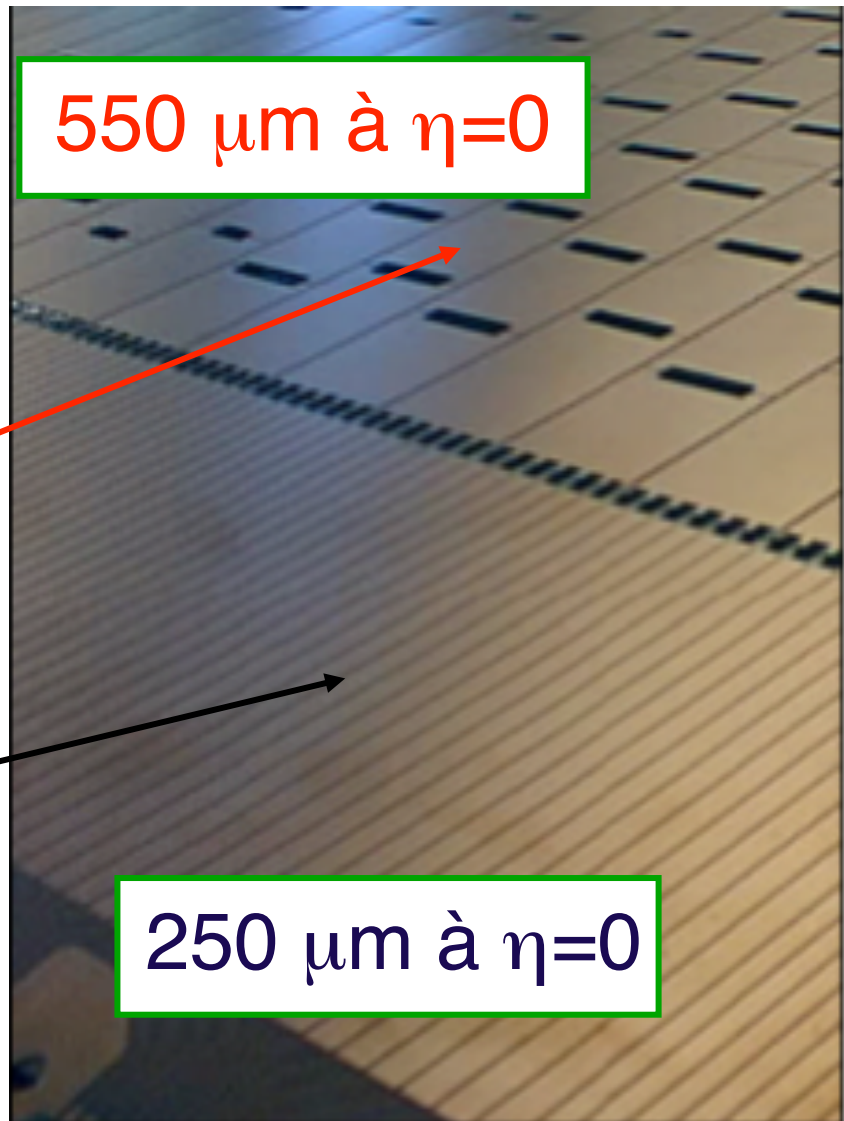
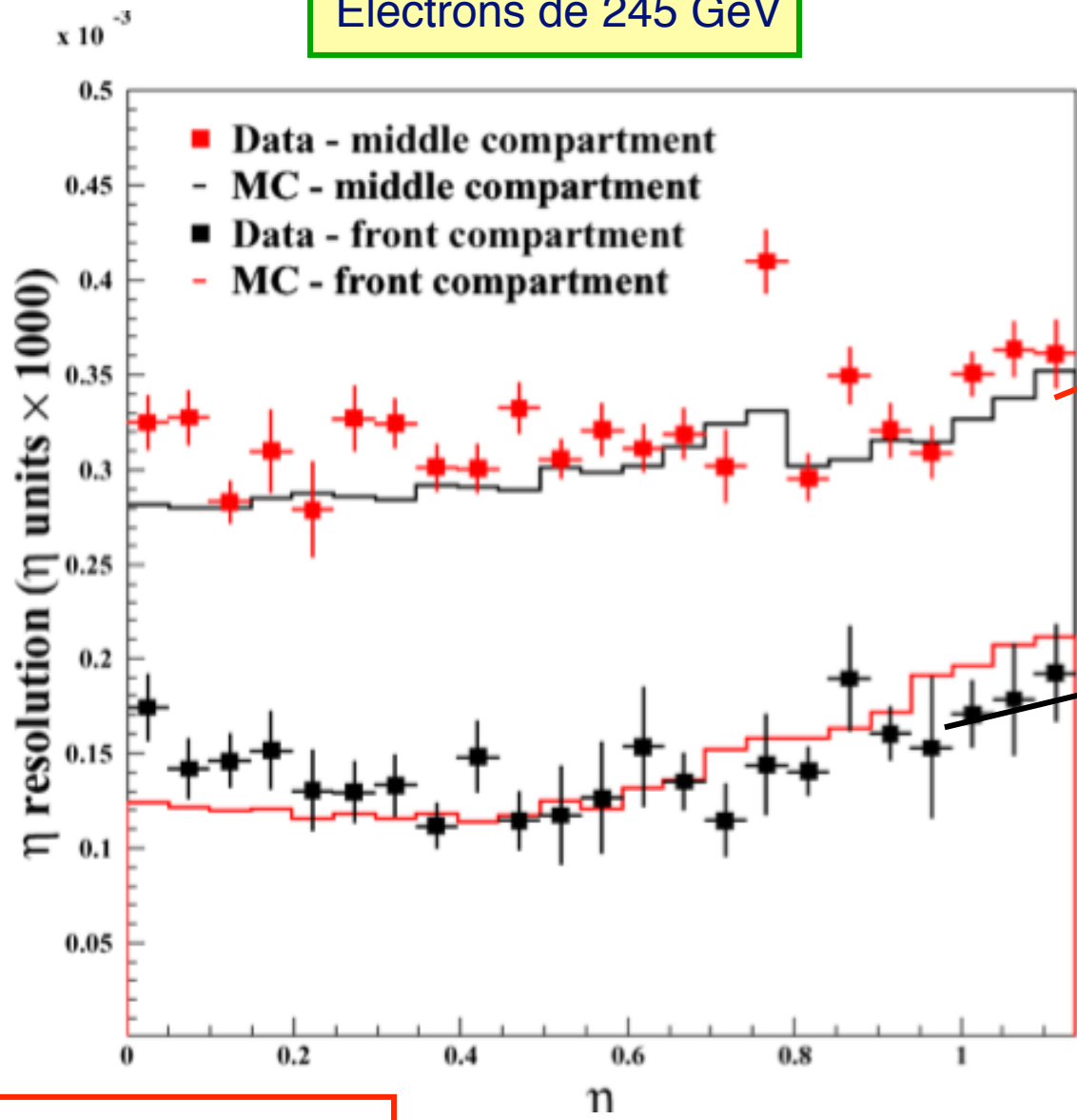


$$pp \rightarrow H + x \rightarrow \gamma\gamma + x$$



# SPATIAL RESOLUTION

Electrons de 245 GeV



NIM A550 96-115 (2005)

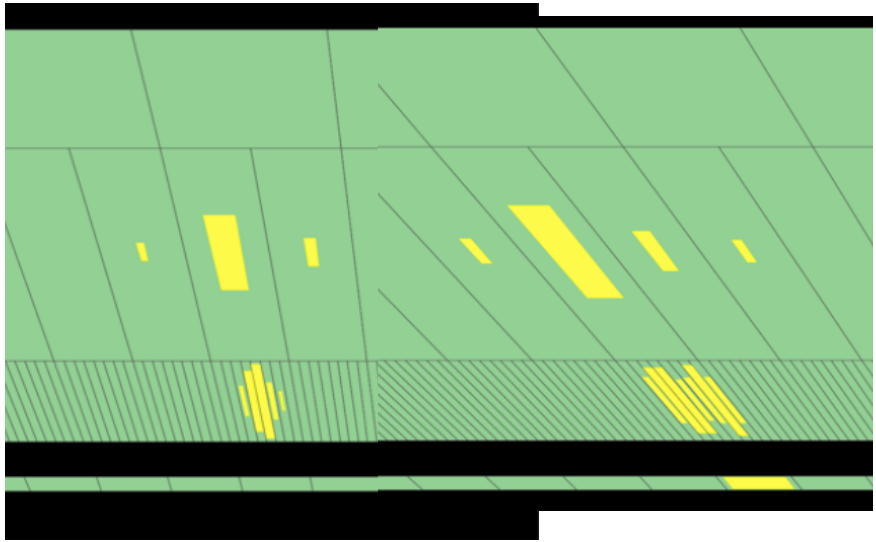
04-08 July 2016

# PIONS REJECTION

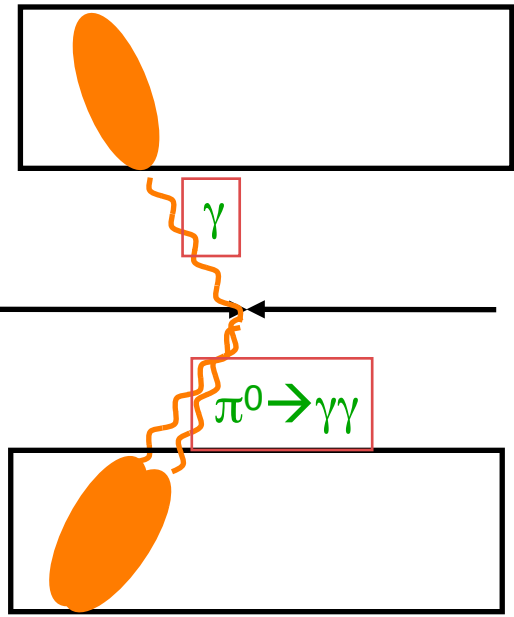
Higgs boson in ATLAS

With  $M_H \sim 125$  GeV in the channel  $H \rightarrow \gamma\gamma$

Background:  $\pi^0$  looking like a  $\gamma$



$\gamma/\pi^0$  rejection



$pp \rightarrow \gamma\text{-jet} \rightarrow \gamma + \pi^0 + X$



# HOMOGENEOUS vs SAMPLING CALORIMETERS

Technology (Experiment)	Depth	Energy resolution	Date
NaI(Tl) (Crystal Ball)	$20X_0$	$2.7\%/E^{1/4}$	1983
Bi <sub>4</sub> Ge <sub>3</sub> O <sub>12</sub> (BGO) (L3)	$22X_0$	$2\%/\sqrt{E} \oplus 0.7\%$	1993
CsI (KTcV)	$27X_0$	$2\%/\sqrt{E} \oplus 0.45\%$	1996
CsI(Tl) (BaBar)	$16\text{--}18X_0$	$2.3\%/E^{1/4} \oplus 1.4\%$	1999
CsI(Tl) (BELLE)	$16X_0$	1.7% for $E_\gamma > 3.5$ GeV	1998
PbWO <sub>4</sub> (PWO) (CMS)	$25X_0$	$3\%/\sqrt{E} \oplus 0.5\% \oplus 0.2/E$	1997
Lead glass (OPAL)	$20.5X_0$	$5\%/\sqrt{E}$	1990
Liquid Kr (NA48)	$27X_0$	$3.2\%/\sqrt{E} \oplus 0.42\% \oplus 0.09/E$	1998
Scintillator/depleted U (ZEUS)	$20\text{--}30X_0$	$18\%/\sqrt{E}$	1988
Scintillator/Pb (CDF)	$18X_0$	$13.5\%/\sqrt{E}$	1988
Scintillator fiber/Pb spaghetti (KLOE)	$15X_0$	$5.7\%/\sqrt{E} \oplus 0.6\%$	1995
Liquid Ar/Pb (NA31)	$27X_0$	$7.5\%/\sqrt{E} \oplus 0.5\% \oplus 0.1/E$	1988
Liquid Ar/Pb (SLD)	$21X_0$	$8\%/\sqrt{E}$	1993
Liquid Ar/Pb (H1)	$20\text{--}30X_0$	$12\%/\sqrt{E} \oplus 1\%$	1998
Liquid Ar/depl. U (DØ)	$20.5X_0$	$16\%/\sqrt{E} \oplus 0.3\% \oplus 0.3/E$	1993
Liquid Ar/Pb accordion (ATLAS)	$25X_0$	$10\%/\sqrt{E} \oplus 0.4\% \oplus 0.3/E$	1996

Homogeneous

Resolution of typical  
electromagnetic calorimeter  
[E is in GeV]

Sampling

# HADRONIC SHOWERS

Hadronic cascades develop in an analogous way to e.m. showers

Strong interaction controls overall development

High energy hadron interacts with material, leading to multi-particle production of more hadrons

These in turn interact with further nuclei

Nuclear breakup and spallation neutrons

Multiplication continues down to the pion production threshold

$$E \sim 2m_{\pi} = 0.28 \text{ GeV}/c^2$$

Neutral pions result in an electromagnetic component (immediate decay:  $\pi^0 \rightarrow \gamma\gamma$ )  
(also:  $\eta \rightarrow \gamma\gamma$ )

Energy deposited by:

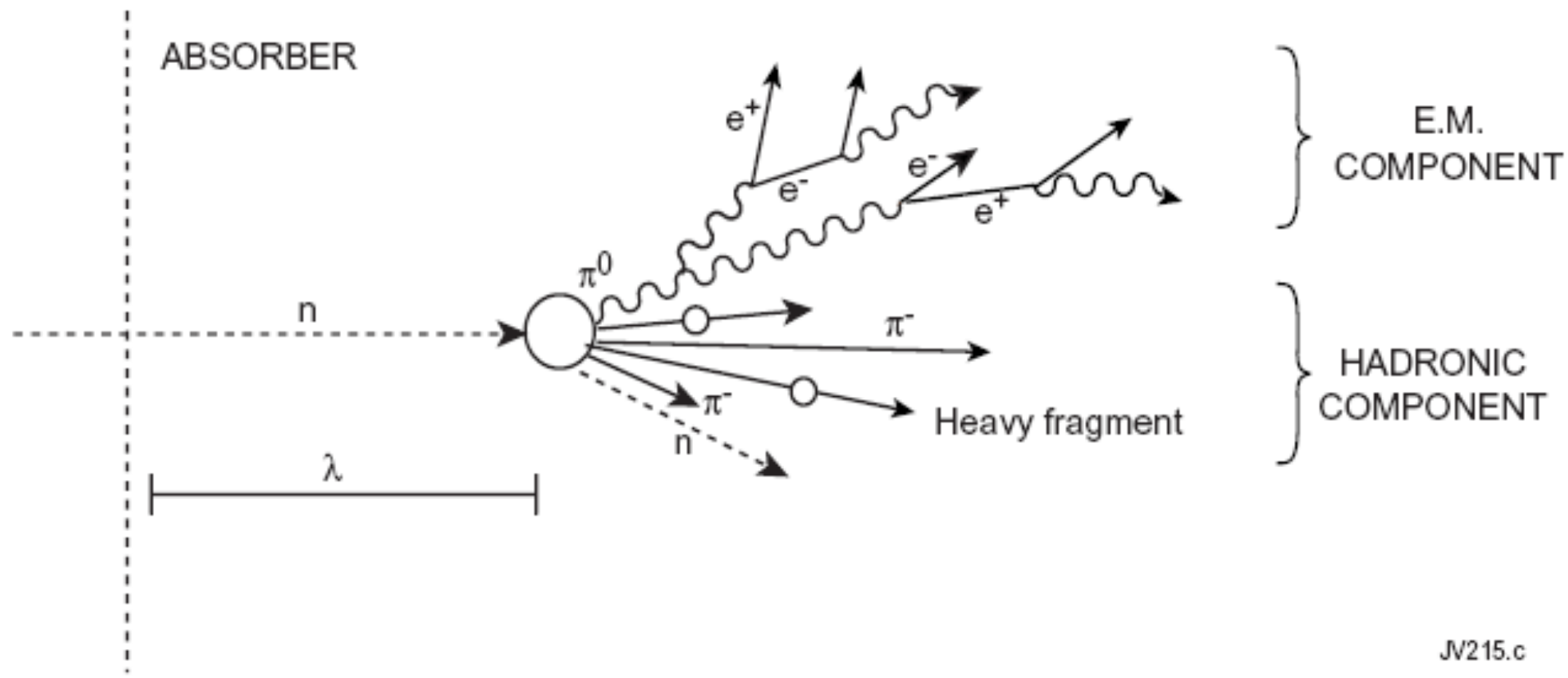
Electromagnetic component (i.e. as for e.m. showers)

Charged pions or protons

Low energy neutrons

Energy lost in breaking nuclei (nuclear binding energy)

# HADRONIC CASCADE



JV215.c

As compared to electromagnetic showers, hadron showers are:

- Larger/more penetrating
- Subject to larger fluctuations – more erratic and varied

# HADRONIC SHOWERS: WHERE DOES THE ENERGY GO ?

	<i>Lead</i>	<i>Iron</i>
<b>Ionization by pions</b>	<b>19%</b>	<b>21%</b>
<b>Ionization by protons</b>	<b>37%</b>	<b>53%</b>
<i>Total ionization</i>	56%	74%
<b>Nuclear binding energy loss</b>	<b>32%</b>	<b>16%</b>
Target recoil	2%	5%
<i>Total invisible energy</i>	34%	21%
<b>Kinetic energy evaporation neutrons</b>	<b>10%</b>	<b>5%</b>
Number of charged pions	0.77	1.4
Number of protons	3.5	8
Number of cascade neutrons	5.4	5
Number of evaporation neutrons	31.5	5
<b>Total number of neutrons</b>	<b>36.9</b>	<b>10</b>
<b>Neutrons/protons</b>	<b>10.5/1</b>	<b>1.3/1</b>



# HADRONIC INTERACTION

Simple model of interaction on a disk of radius R:  $\sigma_{\text{int}} = \pi R^2 \propto A^{2/3}$

$$\sigma_{\text{inel}} \approx \sigma_0 A^{0.7}, \sigma_0 = 35 \text{ mb}$$

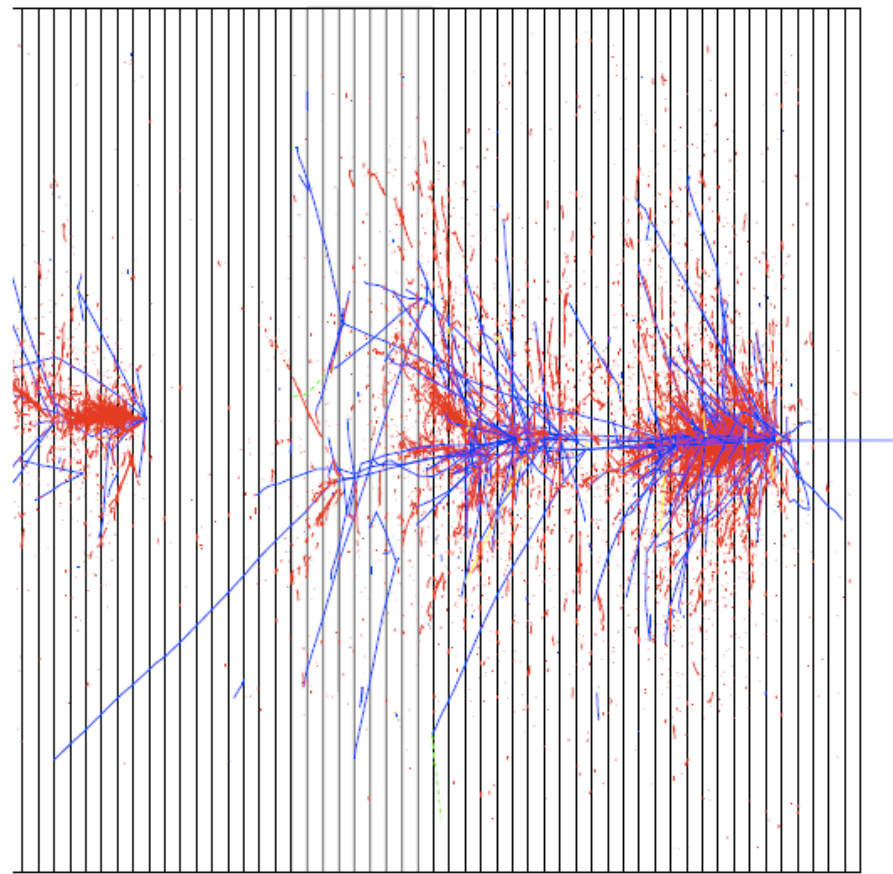
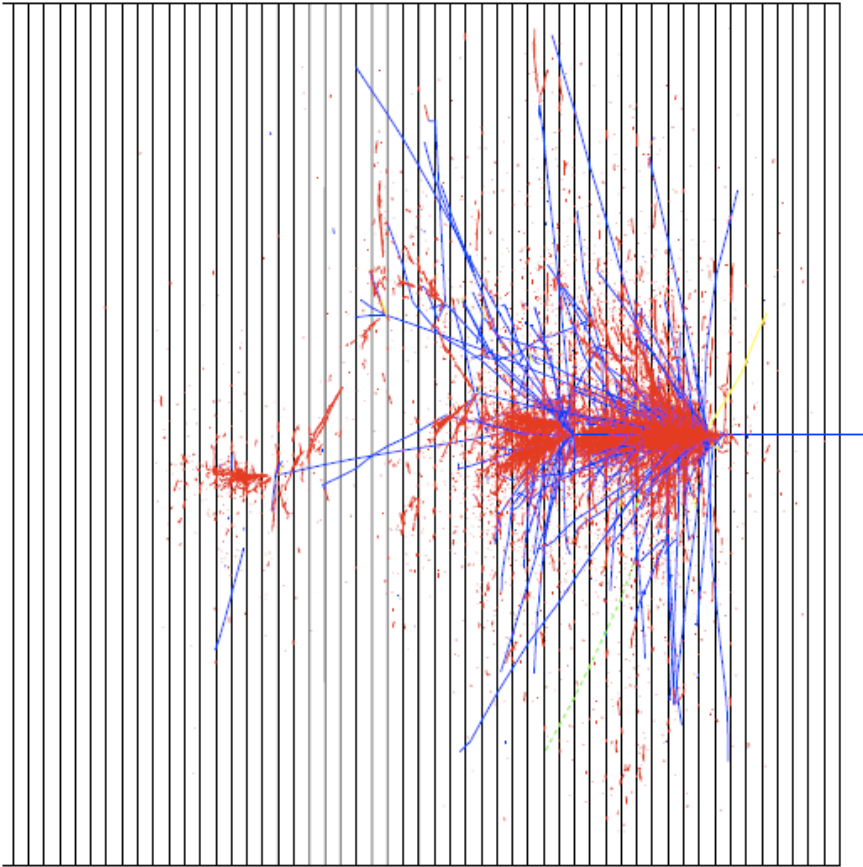
**Nuclear interaction length:** mean free path before inelastic interaction

$$\lambda_{\text{int}} \approx \frac{A}{N_A \sigma_{\text{int}}} \approx 35 A^{1/3} \text{ g cm}^{-2}$$

	Z	$\rho$ (g.cm <sup>-3</sup> )	$E_c$ (MeV)	$X_0$ (cm)	$\lambda_{\text{int}}$ (cm)
Air				30 420	~70 000
Water				36	84
PbWO <sub>4</sub>		8.28		0.89	22.4
C	6	2.3	103	18.8	38.1
Al	13	2.7	47	8.9	39.4
L Ar	18	1.4		14	84
Fe	26	7.9	24	1.76	16.8
Cu	29	9	20	1.43	15.1
W	74	19.3	8.1	0.35	9.6
Pb	82	11.3	6.9	0.56	17.1
U	92	19	6.2	0.32	10.5

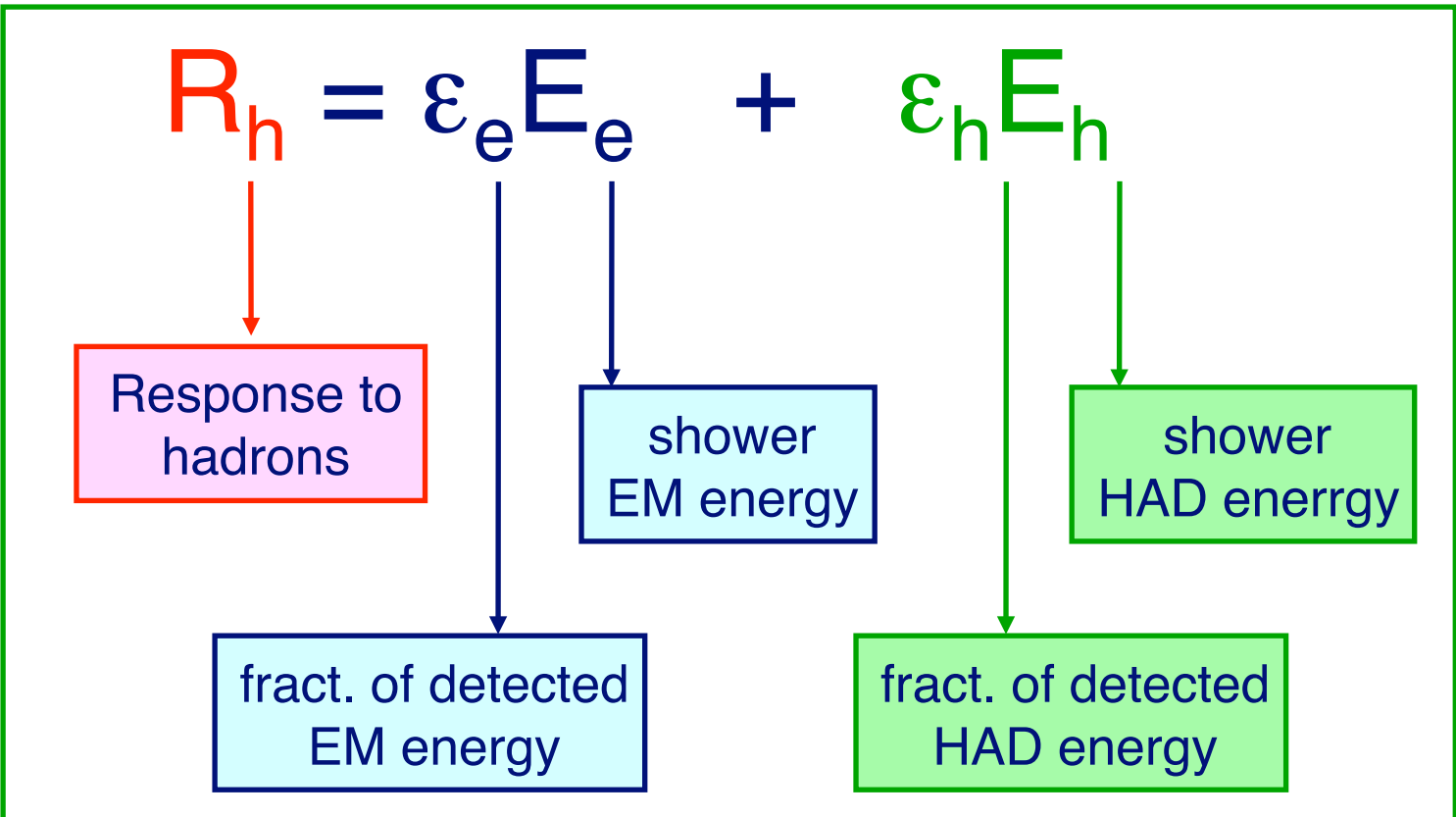
# HADRONIC SHOWERS

**1.** Individual hadron showers are quite **2.** similar



red - e.m. component  
blue - charged hadrons

# HADRONIC SHOWERS and NON-COMPENSATION



$$\frac{e}{h} = \frac{\epsilon_e}{\epsilon_h}$$

$\approx 1$  : compensating calorimeter

$> 1$  : non compensating calorimeter

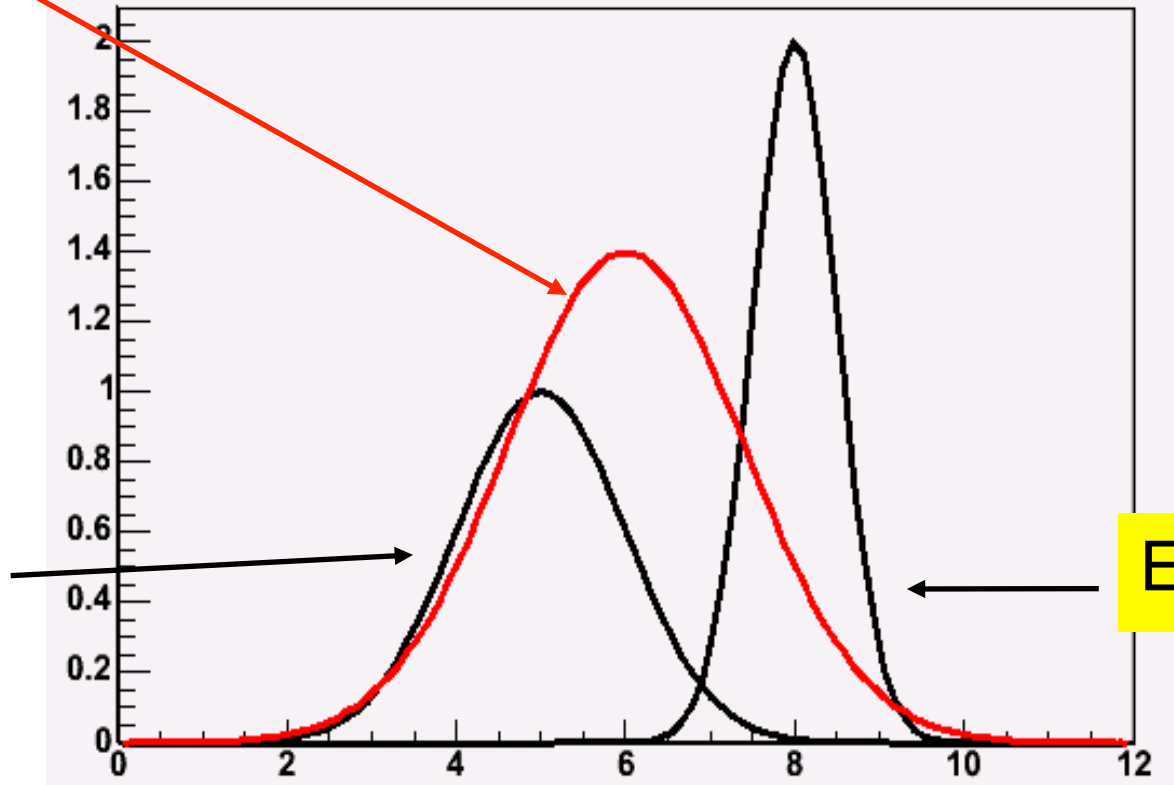
# HADRONIC SHOWERS and NON-COMPENSATION

$$R_h = \epsilon_e E_e + \epsilon_h E_h$$

$$\epsilon_e > \epsilon_h$$

$$E_e \ll E_h$$

$$E_e \gg E_h$$





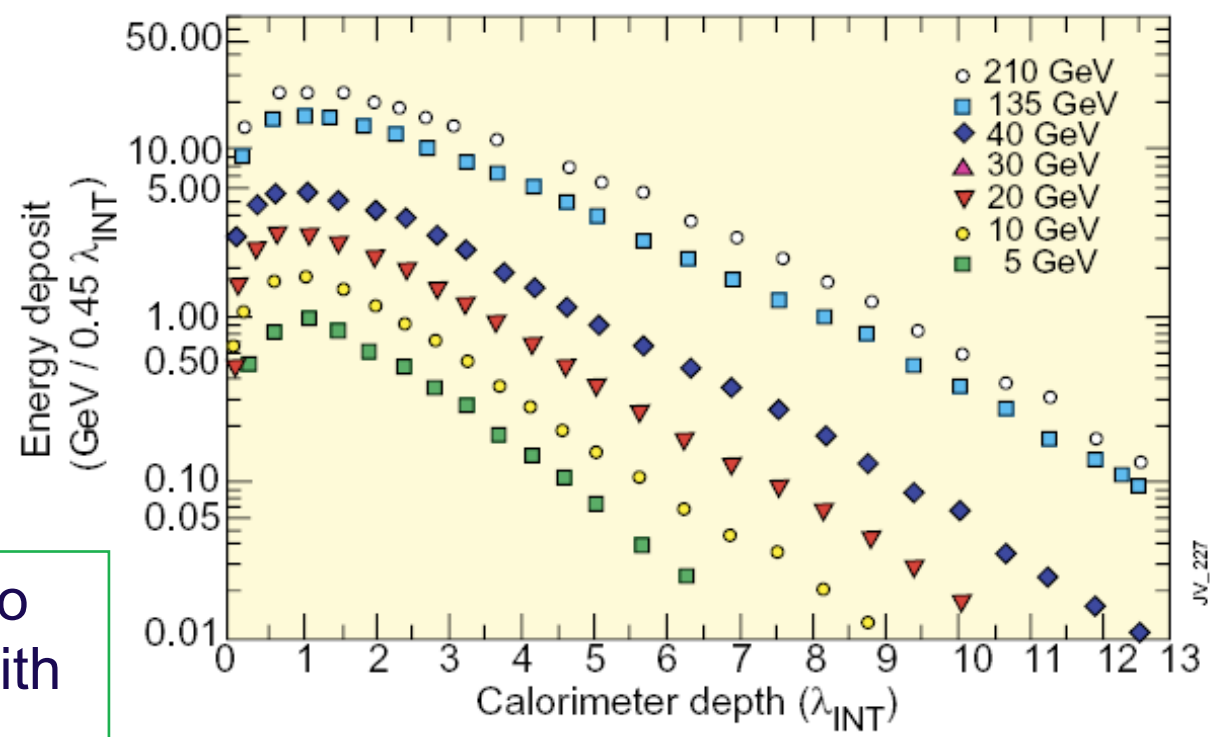
# HADRONIC SHOWER LONGITUDINAL DEVELOPMENT

## Longitudinal profile

Initial peak from  $\pi^0$ s produced in the first interaction length

Gradual falloff characterised by the nuclear interaction length,  $\lambda_{int}$

WA78 :  $5.4\lambda$  of 10mm U / 5mm Scint +  $8\lambda$  of 25mm Fe / 5mm Scint



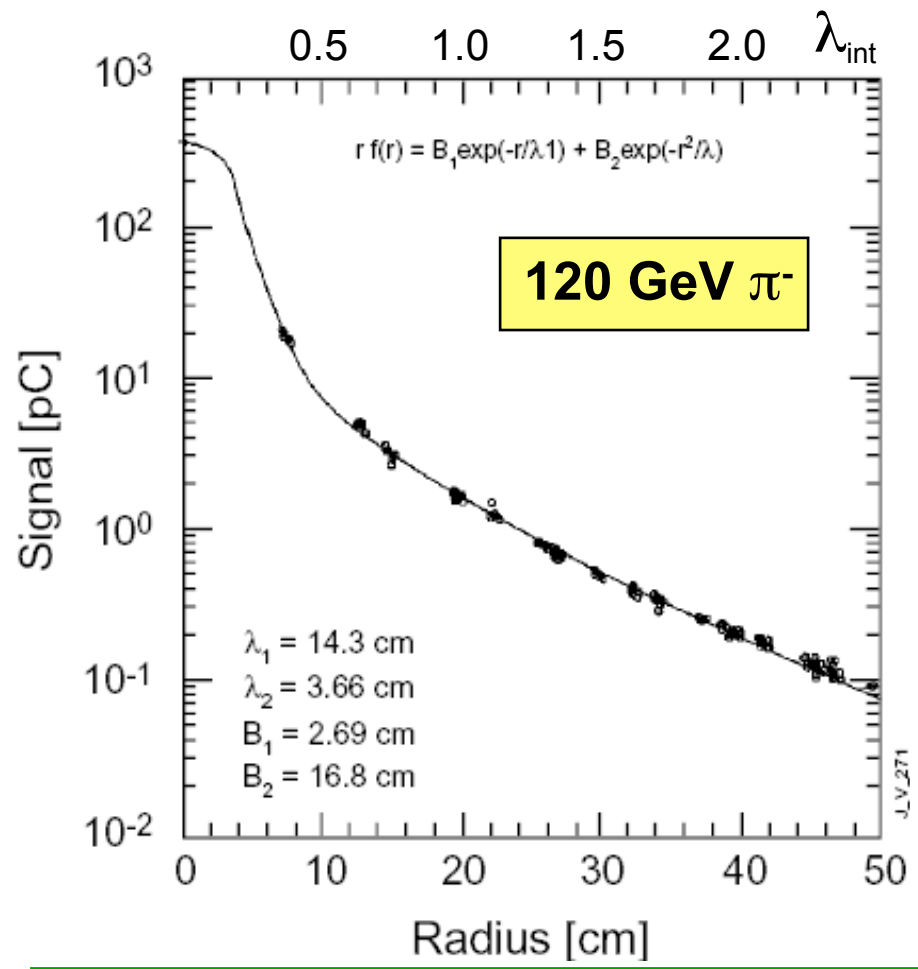
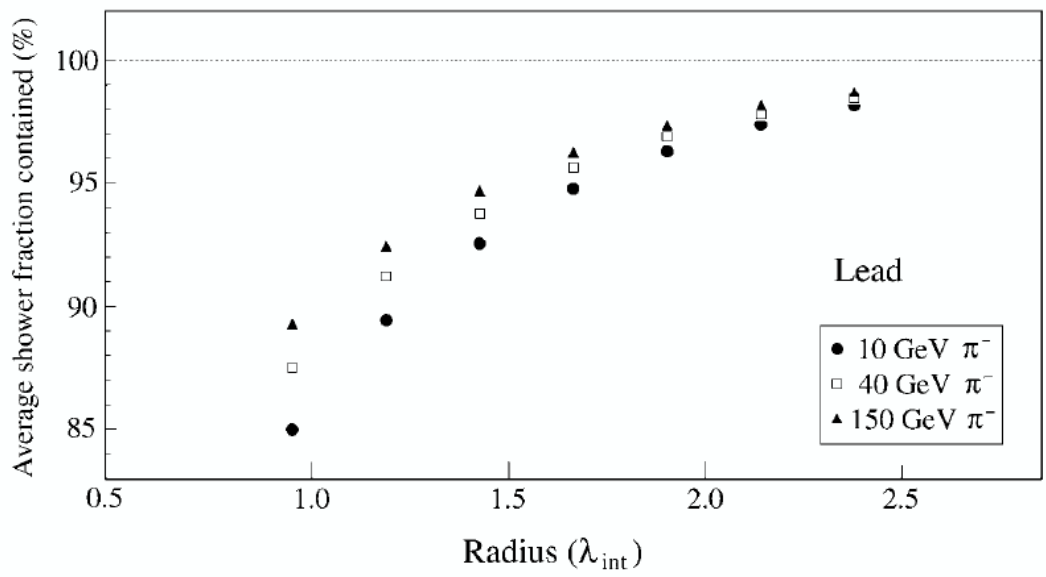
As with e.m. showers: depth to contain a shower increases with  $\log(E)$

# HADRONIC SHOWERS TRANSVERSE PROFILE

Mean transverse momentum from interactions,  $\langle p_T \rangle \sim 300$  MeV, is about the same magnitude as the energy lost traversing  $1\lambda$  for many materials

So radial extent of the cascade is well characterized by  $\lambda$

The  $\pi^0$  component of the cascade results in an electromagnetic core



Lateral containment increases with energy

# JETS at HIGH ENERGY COLLIDERS

At Hadronic Colliders, quarks & gluons produced, evolves (parton shower, hadronisation) to become jets

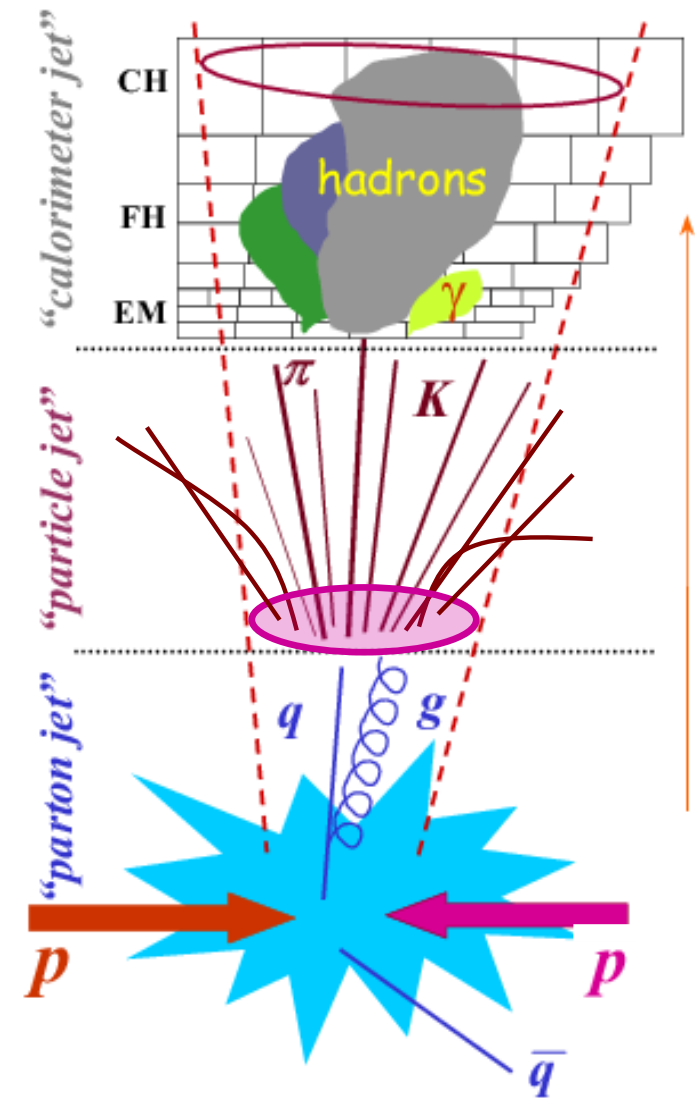
In a cone around the initial parton: high density of hadrons

LHC calorimeters cannot separate all the incoming hadrons

Use dedicated calibration schemes (based on simulation in ATLAS)

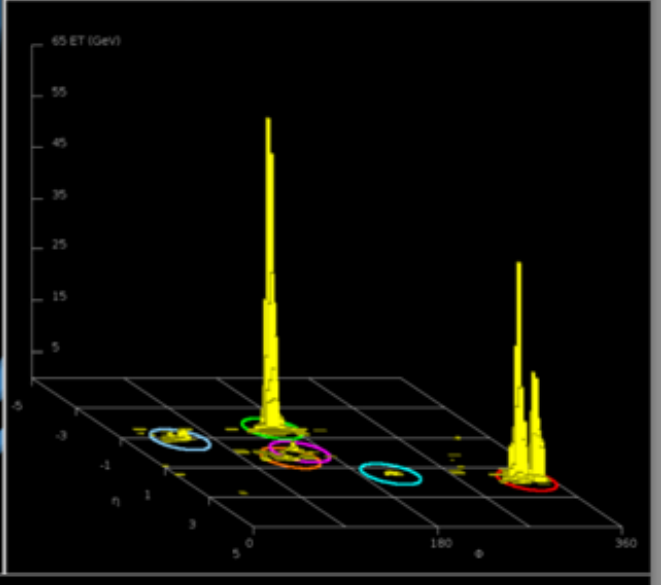
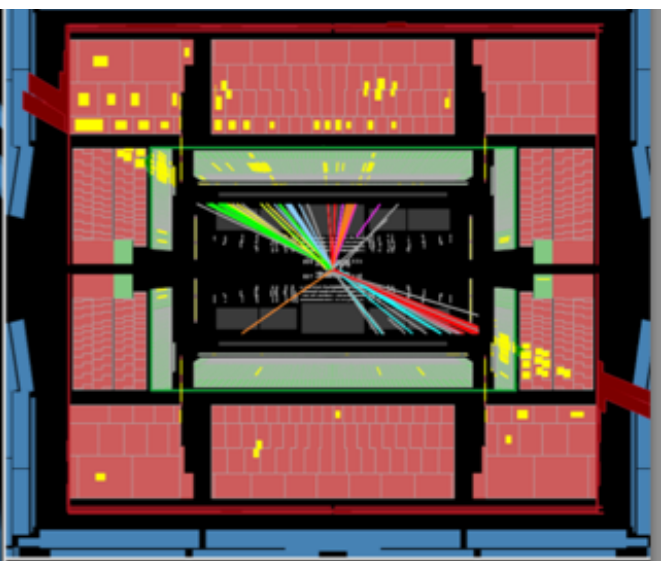
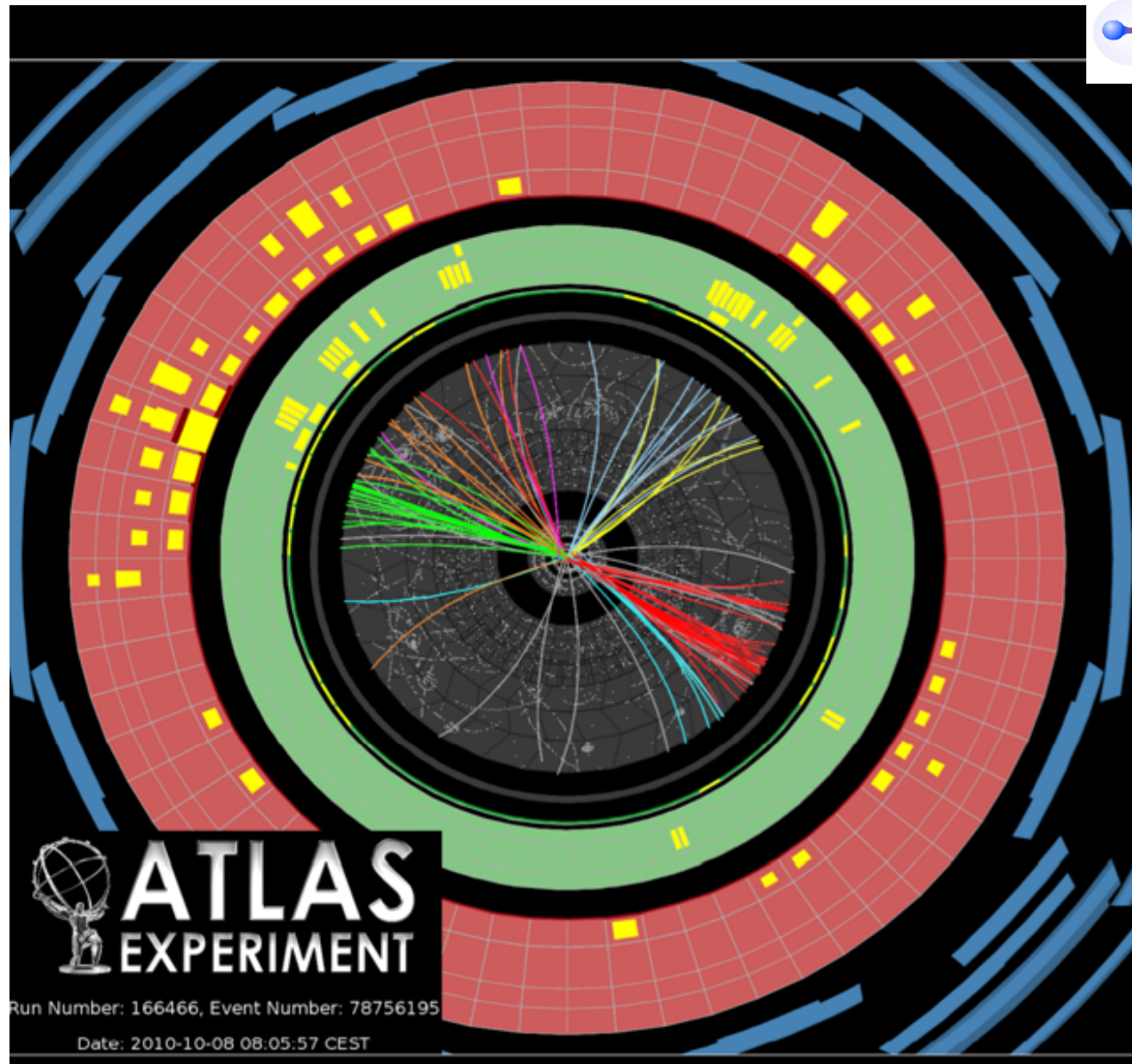
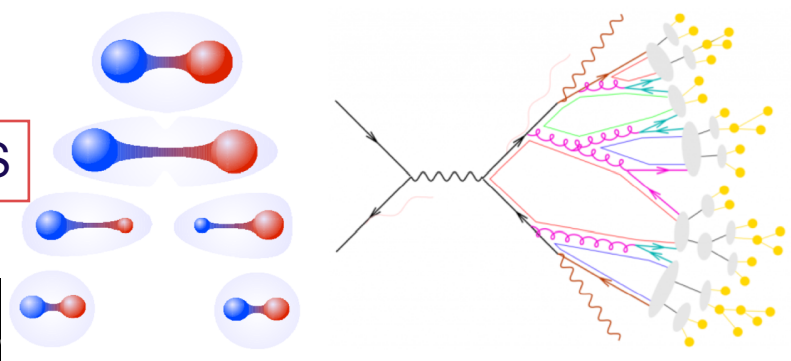
Use tracking system to identify charged hadrons (Particle Flow in CMS)

In the future, very highly segmented calorimeters



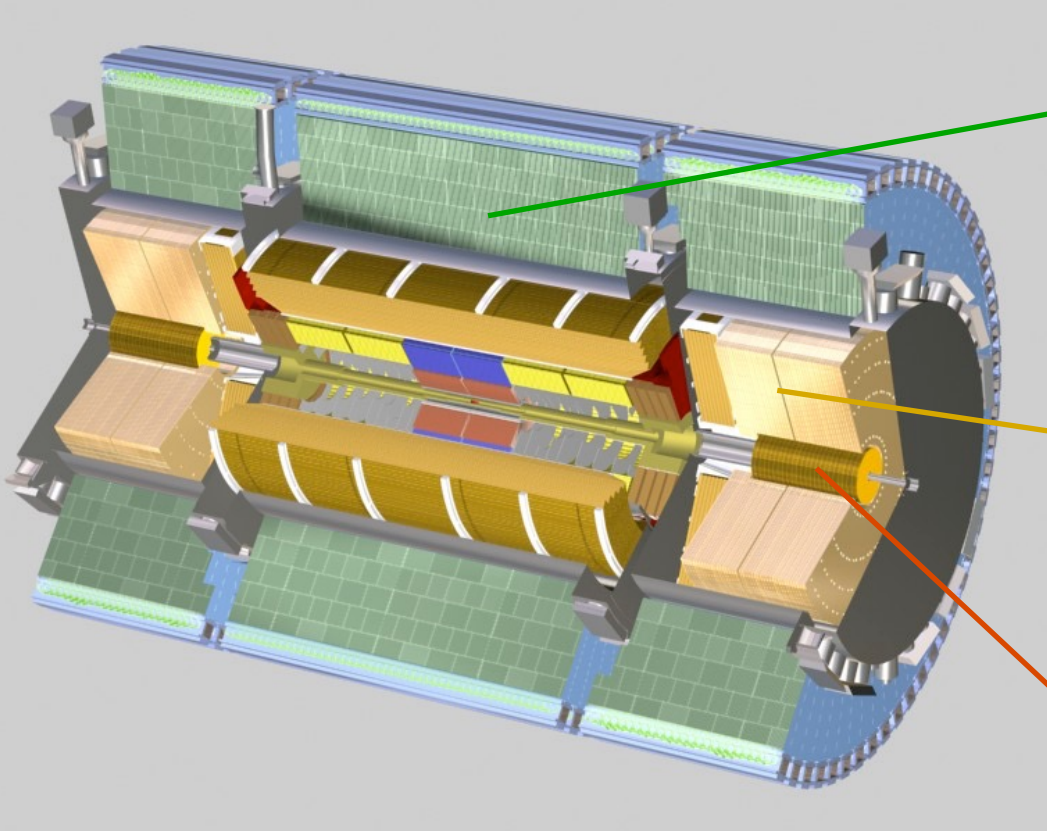
# JETS

NEED a REFINED CALIBRATION PROCEDURE FOR JETS





# ATLAS HADRON CALORIMETER



Tiles Calorimeter  $|\eta| < 1.7$   
 Fe / Scintillator  
 3 layers in depth

LAr/Cu  $1.7 < |\eta| < 3.2$   
 4 layers in depth

Forward: 1 layer EM, 2 HAD  
 LAr/Cu or W  $3.2 < |\eta| < 4.9$

Total thickness:  $\sim 8 - 10 \lambda$   
 Use of different technics: cope with radiations in forward region

Scintillator tile calorimeter

	Barrel	Extended barrel
$ \eta $ coverage	$ \eta  < 1.0$	$0.8 <  \eta  < 1.7$
Number of layers	3	3
Granularity $\Delta\eta \times \Delta\phi$	$0.1 \times 0.1$	$0.1 \times 0.1$
Last layer	$0.2 \times 0.1$	$0.2 \times 0.1$
Readout channels	5760	4092 (both sides)

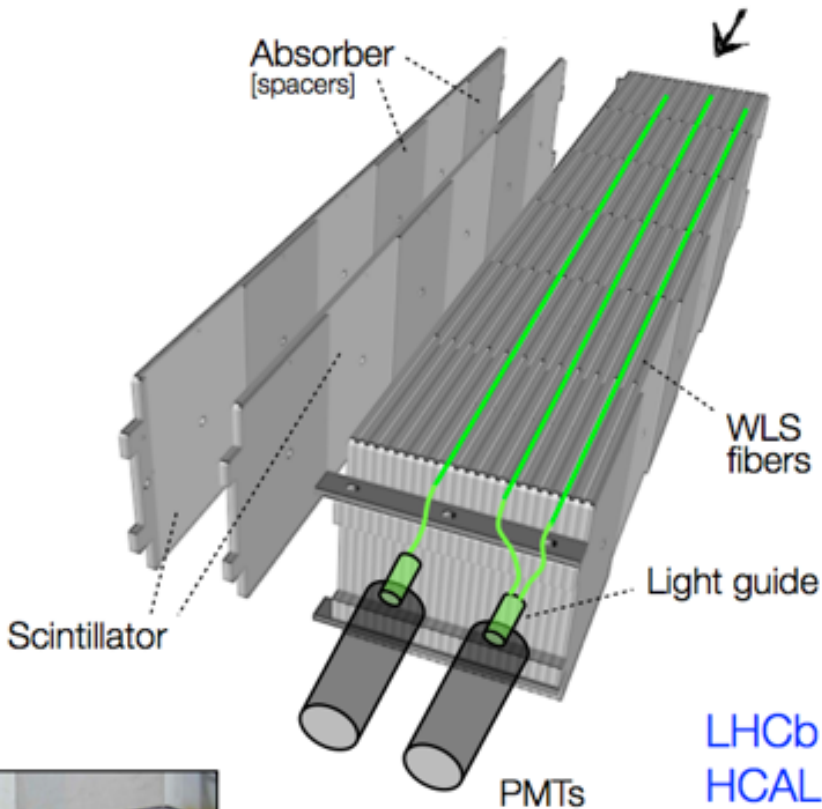
# HADRONIC CALORIMETER

Most common realization: **Sampling Calorimeter**

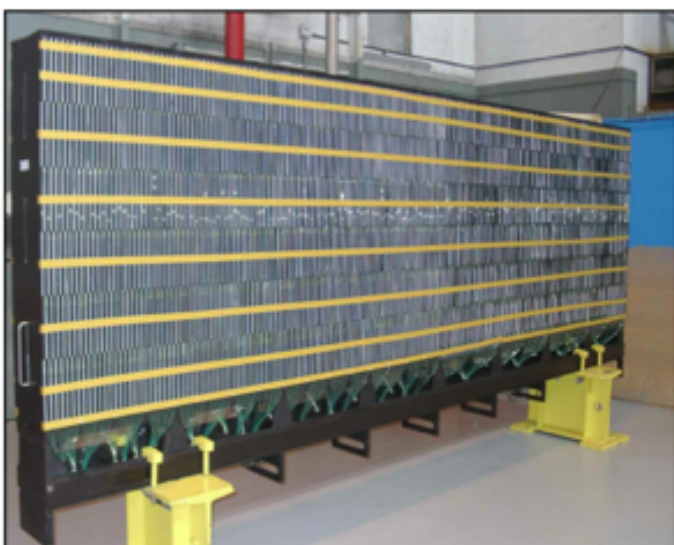
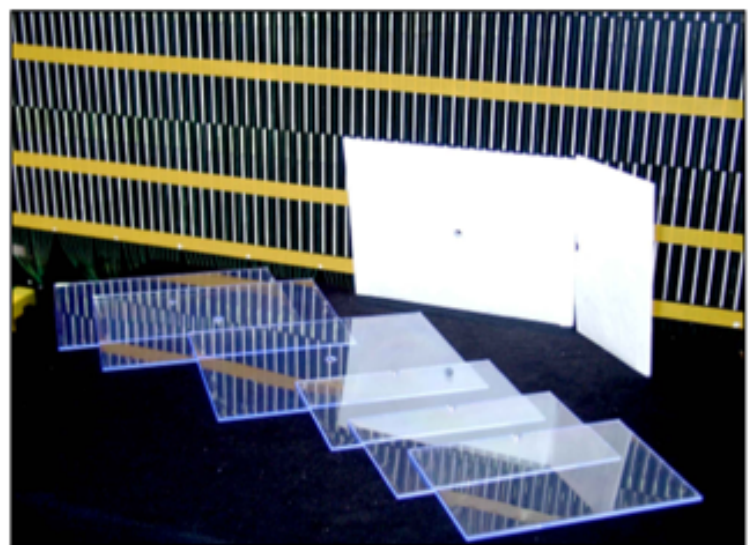
Utilization of homogenous calorimeters unnecessary (and thus too expensive) due to fluctuations of invisible shower components ...

Typical absorbers : Fe, Pb, U ...  
Sampling elements : Scintillators, LAr, MWPCs ...

Typical setup:  
Alternating layers of active and passive material  
[also: 'spaghetti' or 'shashlik' calorimeter]



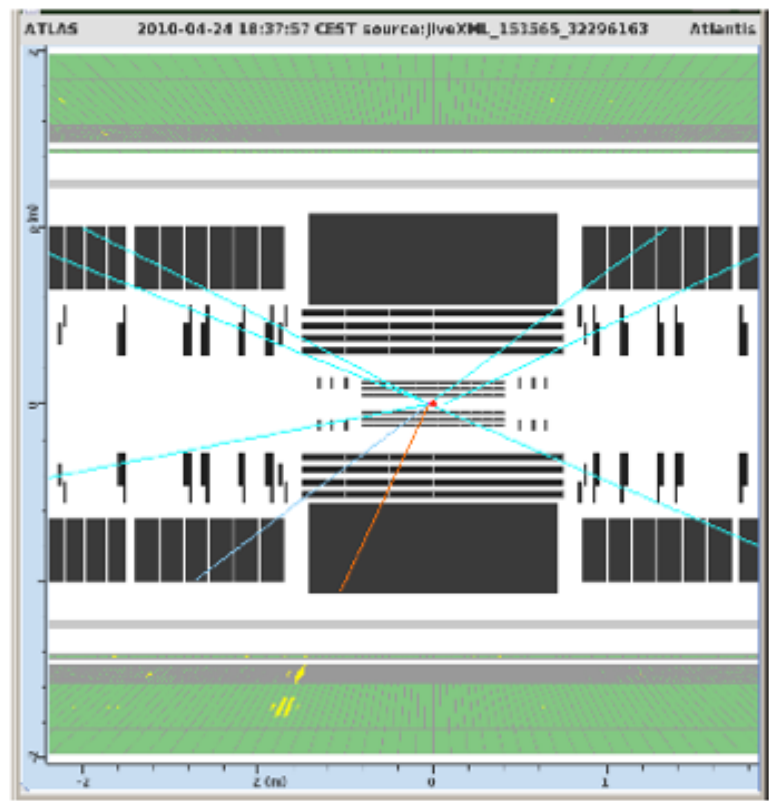
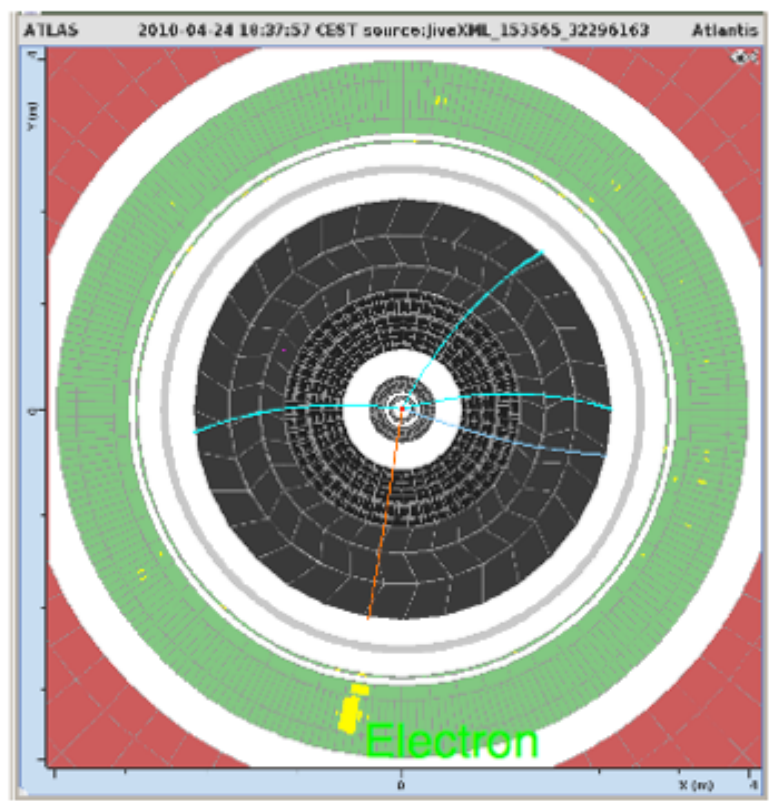
LHCb  
HCAL



Example:  
LHCb Hadron Calorimeter

# MISSING TRANSVERSE ENERGY

## Missing transverse energy : $W \rightarrow e \nu$ candidate



For a pp collision, for instance, and in the absence of escaping particles (neutrinos, neutralinos, DM,..) the transverse energy is ~balanced.

Missing transverse energy is interpreted as the presence of a neutrino.

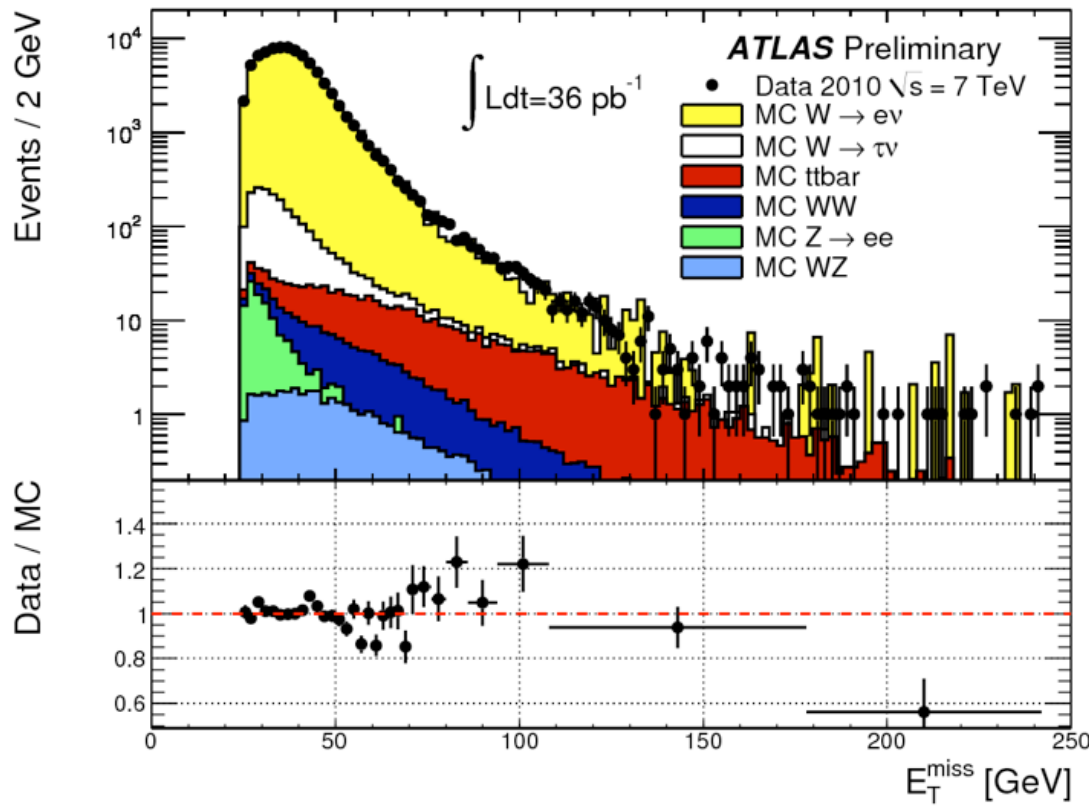
$$\vec{E}_T^{miss} = - \sum_i^{cells} \vec{E}_T$$

$E_T^{miss}$  is the modulus of the vectorial sum of energy deposited in each calorimeter cell

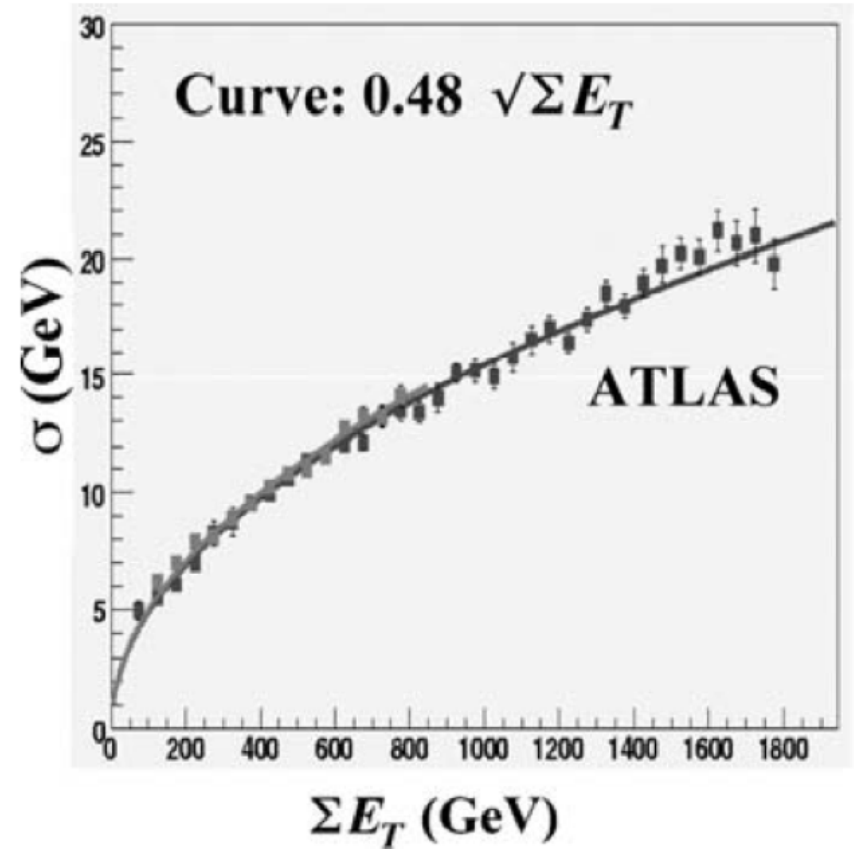


# MISSING TRANSVERSE ENERGY: CALIBRATION

Missing transverse energy in ATLAS for  $W \rightarrow e\nu$  events



Missing transverse energy expected resolution in ATLAS





# A FEW SUMMARY WORDS on CALORIMETERS

**Calorimeters are attractive in our field for various reasons:**

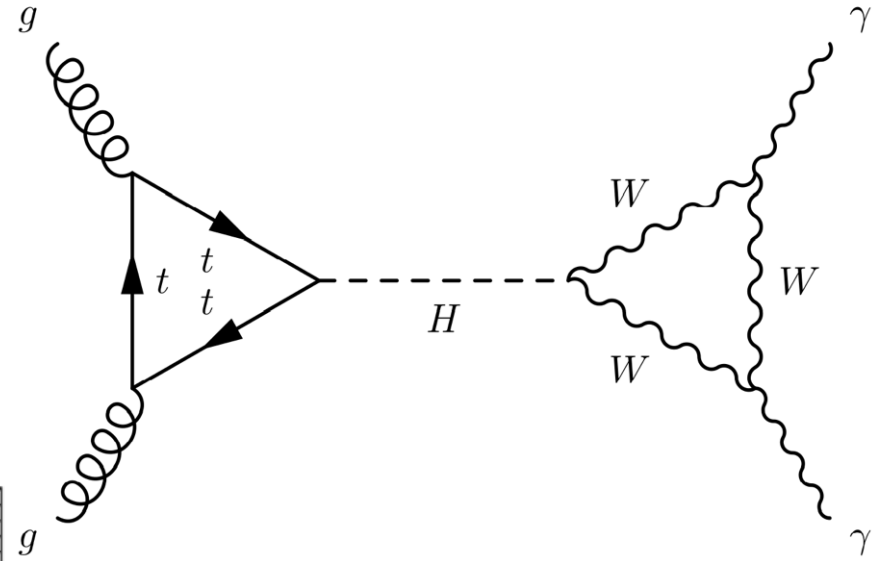
**In contrast with magnet spectrometers, in which the momentum resolution deteriorates linearly with the particle momentum, on most cases the calorimeter energy resolution improves as  $1/\text{Sqrt}(E)$ , where  $E$  is the energy of the incident particle. Therefore calorimeters are very well suited for high-energy physics experiments.**

**In contrast to magnet spectrometers, calorimeters are sensitive to all types of particles, charged and neutral. They can even provide indirect detection of neutrinos and their energy through a measurement of the event missing energy.**

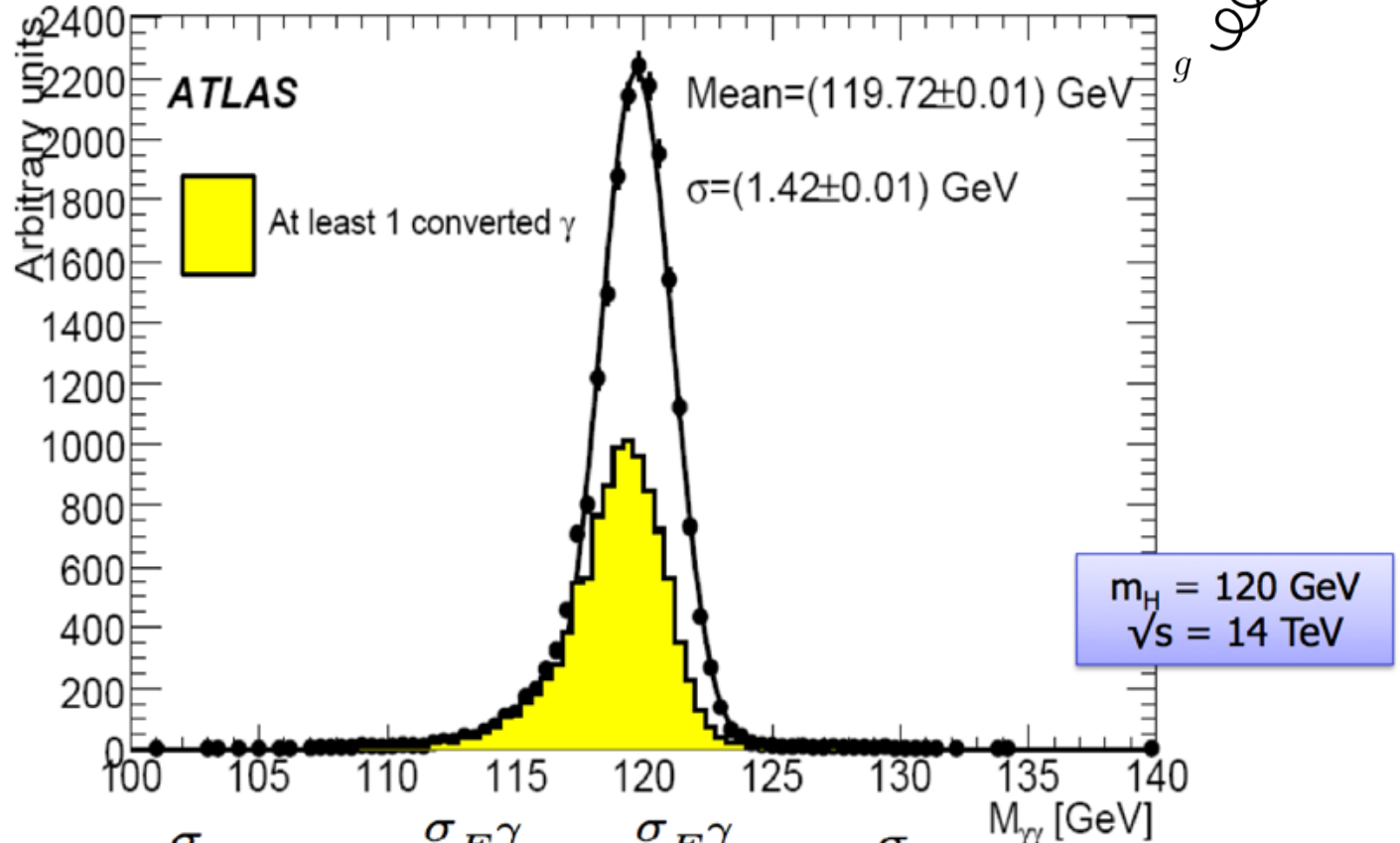
**Calorimeters are commonly used for trigger purposes since they can provide fast signals that are easy to process and interpret.**

**They are space and therefore cost effective. Because the shower length increases only logarithmically with energy, the detector thickness needs to increase only logarithmically with the energy of the particles. In contrast for a fixed momentum resolution, the bending power  $BL^2$  of a magnetic spectrometer must increase linearly with the particle momentum.**

# HIGGS MASS RESOLUTION

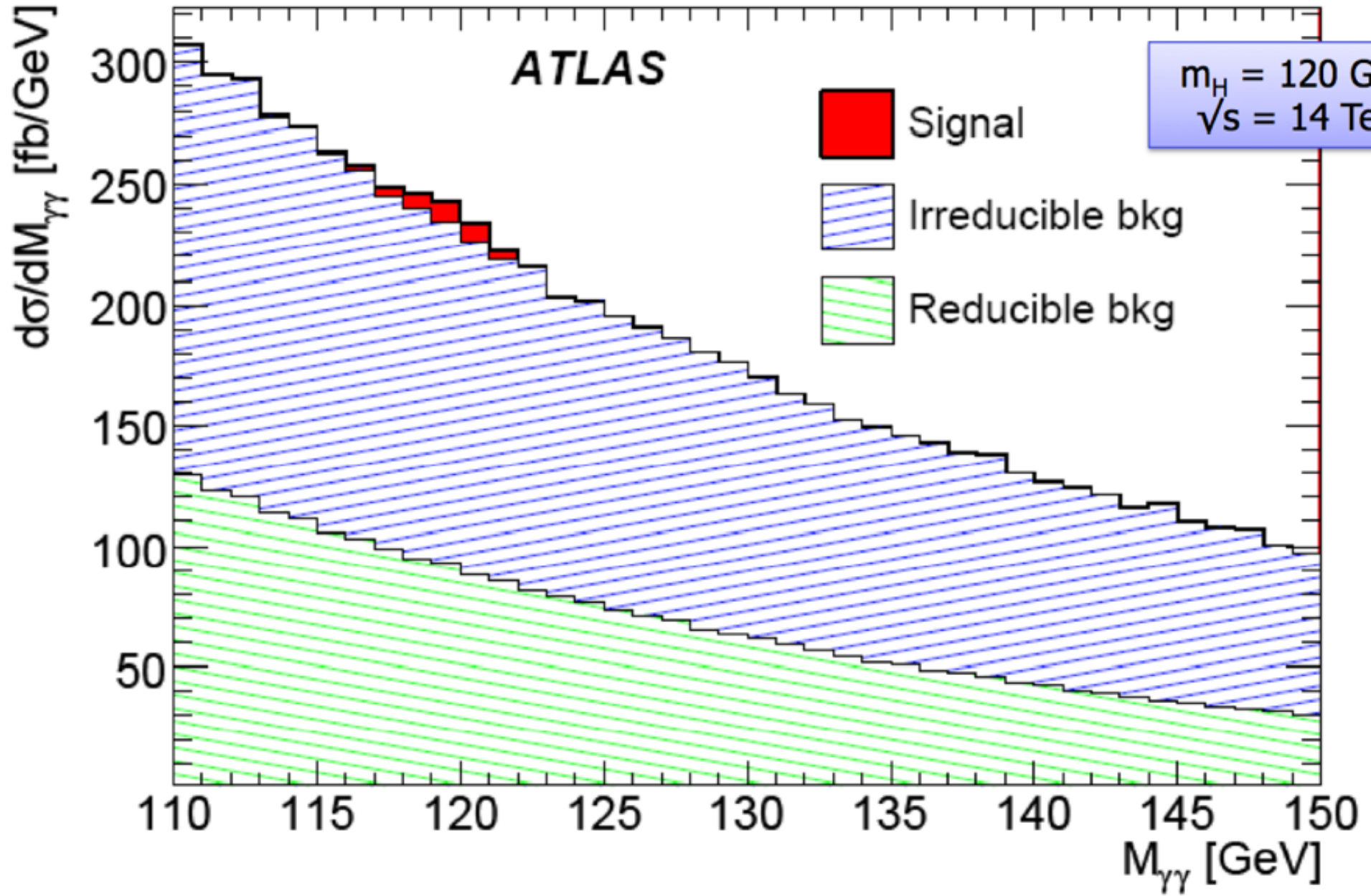


$$m_{\gamma\gamma} = \sqrt{E_1^\gamma E_2^\gamma (1 - \cos \alpha_{12})}$$



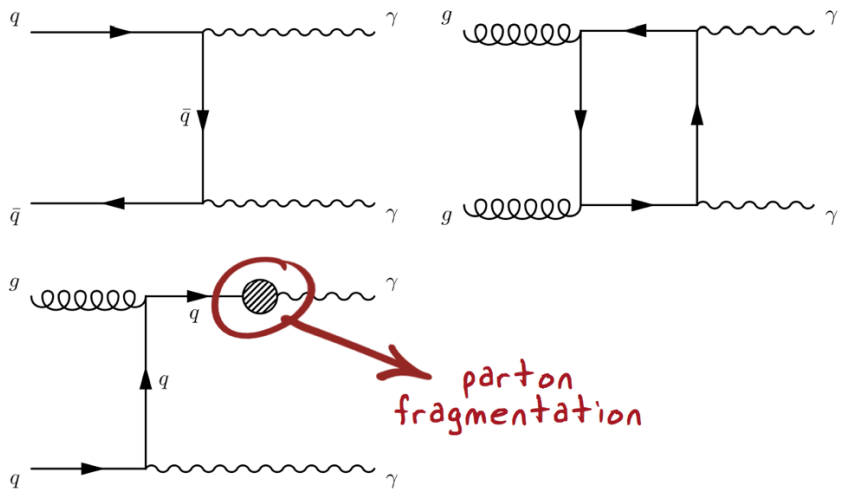
$$\frac{\sigma_{m_{\gamma\gamma}}}{m_{\gamma\gamma}} = \frac{\sigma_{E_1^\gamma}}{E_1^\gamma} \oplus \frac{\sigma_{E_2^\gamma}}{E_2^\gamma} \oplus \frac{\sigma_{\alpha_{12}}}{\tan \alpha_{12}}$$

# SIGNAL on a LARGE BACKGROUND

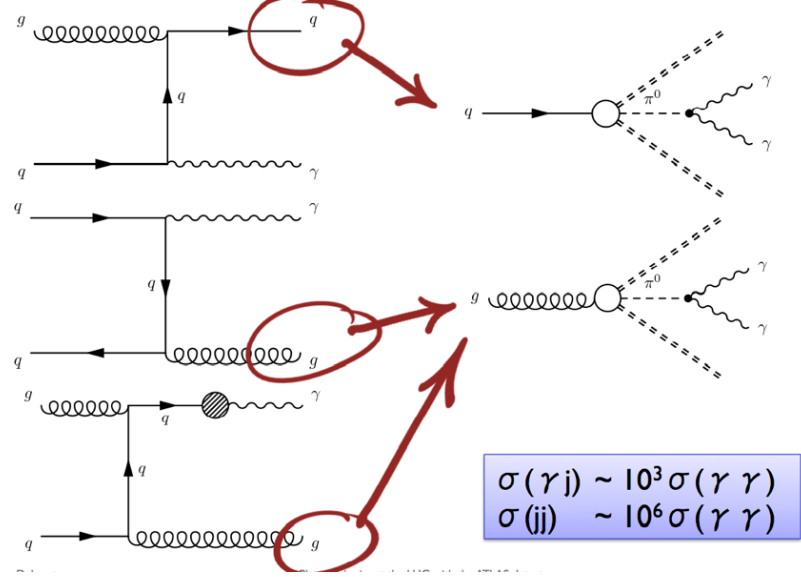


# SIGNAL on a LARGE BACKGROUND

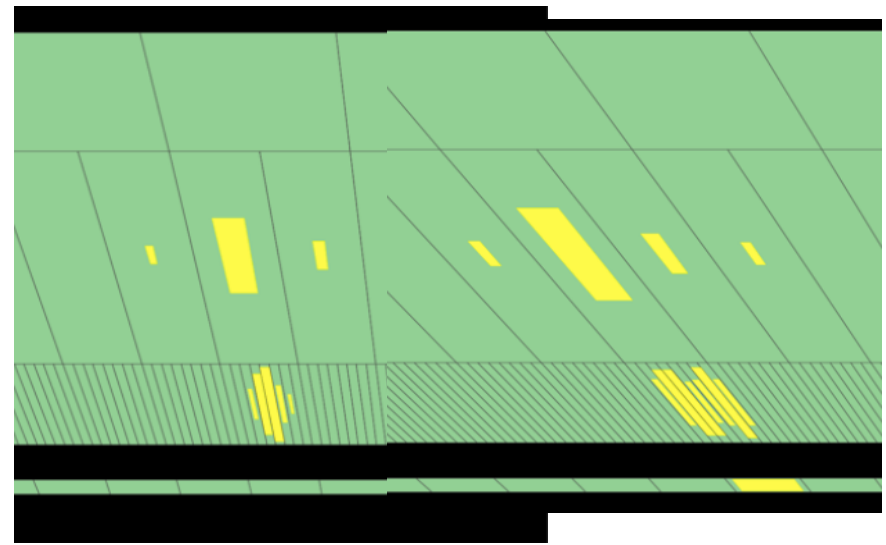
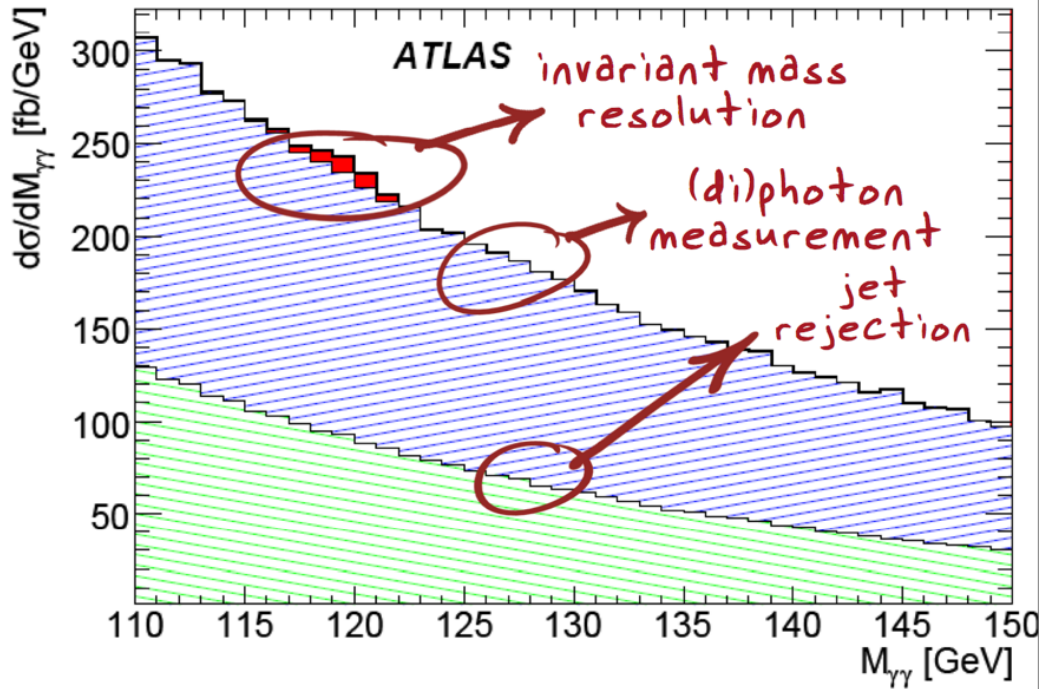
**IRREDUCIBLE BACKGROUND**  
 $\gamma$  in the FINAL STATE



**REDUCIBLE BACKGROUND**  
 $\pi^0$  in the FINAL STATE

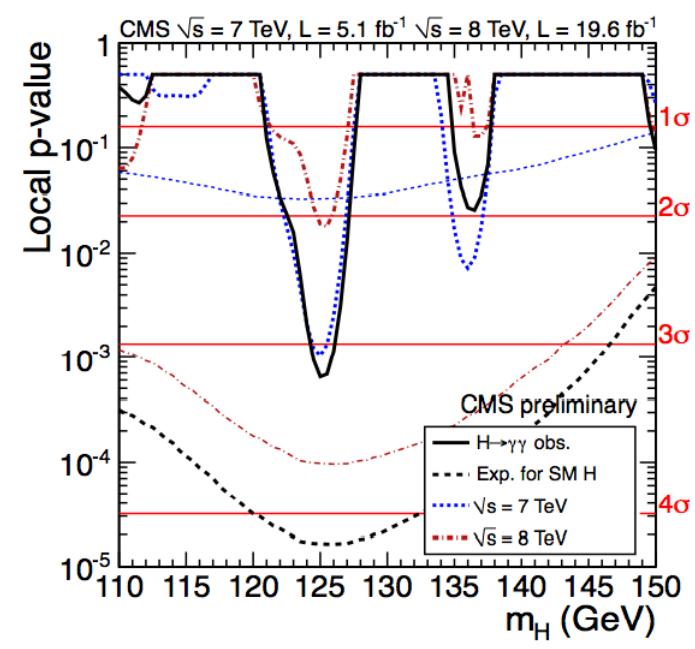
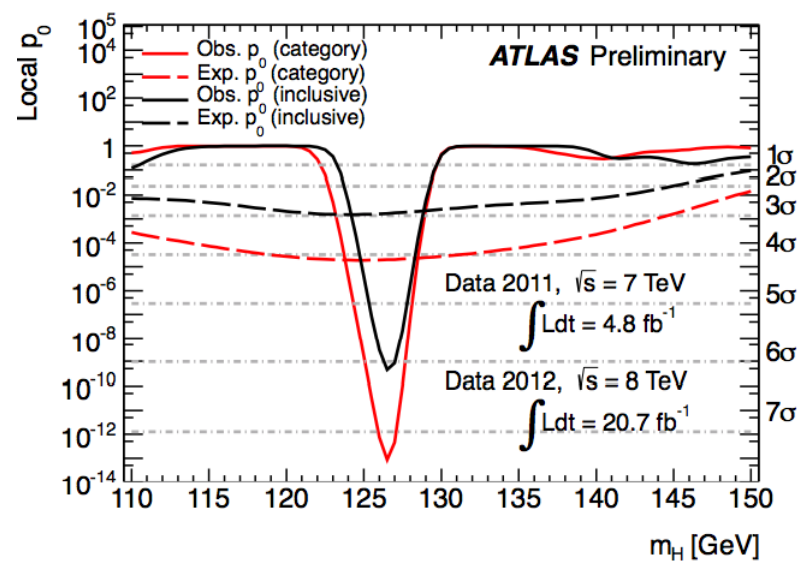
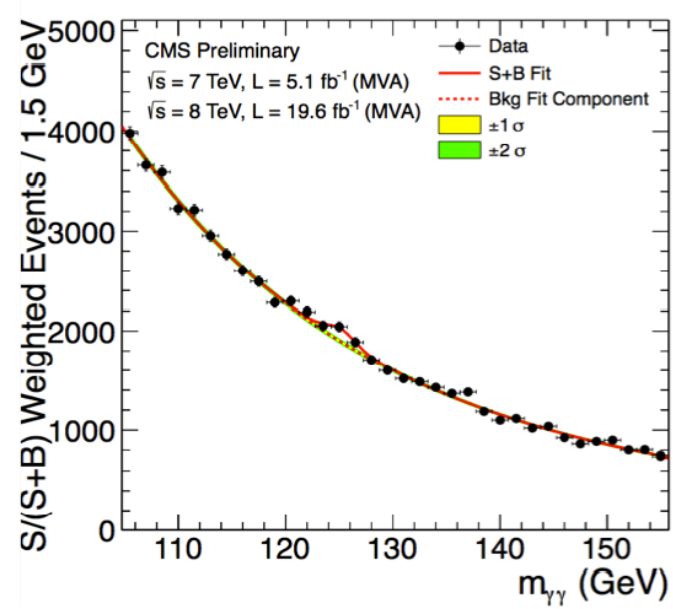
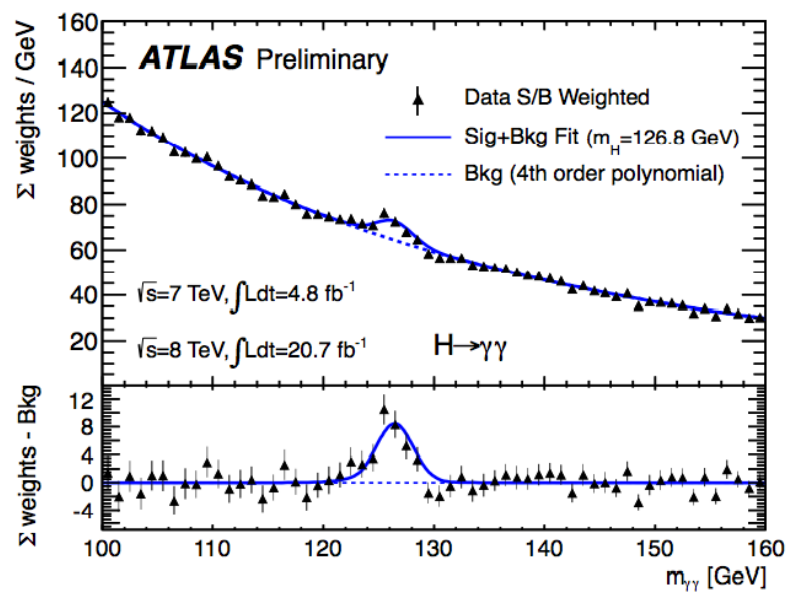


$\sigma(\gamma j) \sim 10^3 \sigma(\gamma\gamma)$   
 $\sigma(jj) \sim 10^6 \sigma(\gamma\gamma)$





# H → γγ MASS SPECTRA & SIGNAL OBSERVATION



# CONSTANT TERM

The constant term describes the level of uniformity of response of the calorimeter as a function of **position, time, temperature** and which are not corrected for.

- Geometry non uniformity
- Non uniformity in electronics response
- Signal reconstruction
- Energy leakage

Dominant term at high energy

Correlated contributions	Impact on uniformity	ATLAS LAr EMB testbeam
Calibration	0.23%	
Readout electronics	0.10%	
Signal reconstruction	0.25%	
Monte Carlo	0.08%	
Energy scheme	0.09%	
Overall (data)	0.38% ( <b>0.34%</b> )	
Uncorrelated contribution	P13	P15
Lead thickness	0.09%	0.14%
Gap dispersion	0.18%	0.12%
Energy modulation	0.14%	0.10%
Time stability	0.09%	0.15%
Overall (data)	0.26% ( <b>0.26%</b> )	0.25% ( <b>0.23%</b> )