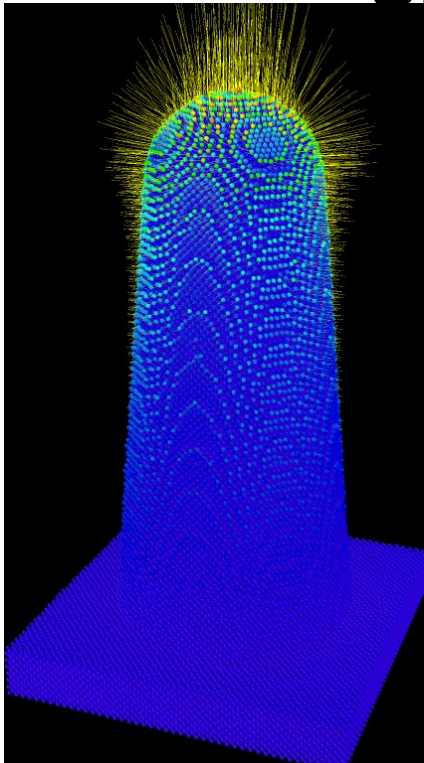


A generalized method for calculating electron emission and thermal evolution of metallic nanotips



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F. Djurabekova

MeVarc 2017
Jerusalem 20.03.2017

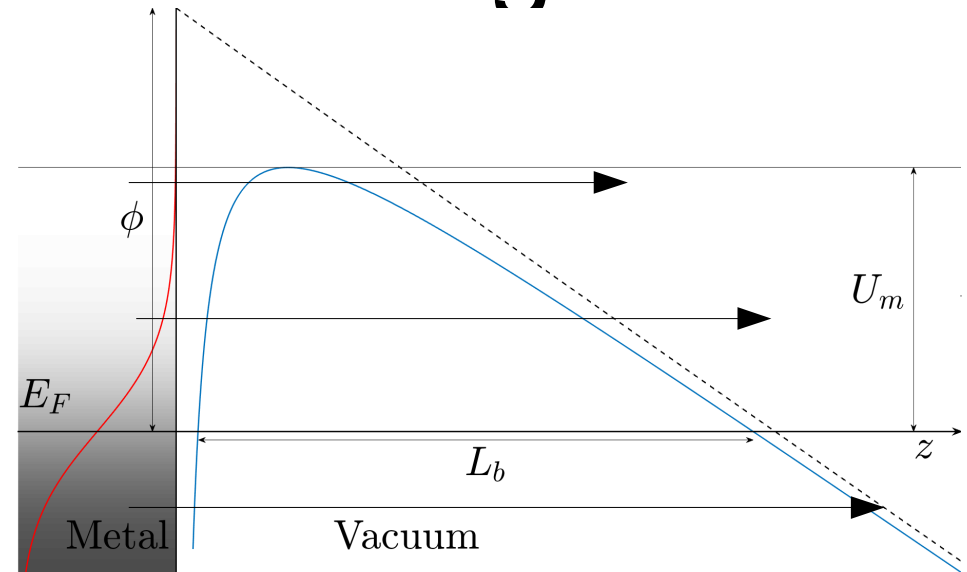
Motivation

- It is established that electron emission plays an important role in the initiation of vacuum arcs.
- However the exact mechanism that leads from intense emission to plasma initiation is still unclear
- Fundamental questions:
 - How do we go from field emission to plasma?
 - PIC simulations assume supply of neutral atoms. What is their source?
- Need for simulations that take into account more phenomena:
 - Electron emission from sharp tips
 - Joule and Nottingham heating
 - Field-induced stress

Electron emission: problems and challenges

- Problem I: T-F Emission

Thermionic and Field emission cannot be always separated. General Thermal-Field (GTF) theory is needed (especially in the case of high-temperature melting nanotips.)



- Problem II: Sharp nano-tips

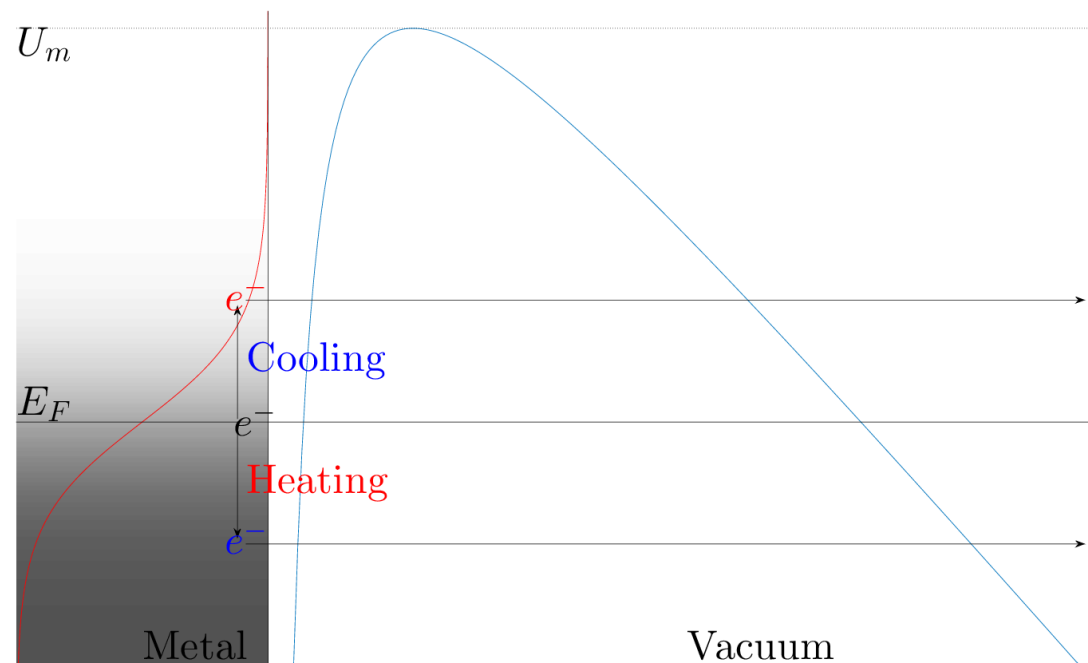
Sharp emitters have curved potential. The classical Shottky-Nordheim (SN) barrier, based on planar geometry and linear potential cannot describe them. The emission might be overestimated by orders of magnitude

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Creator:MATLAB, The MathWorks, Inc. Vers
CreationDate:10/09/2015 14:27:41
LanguageLevel:2

Heating processes

- Nottingham heating

Electrons leaving from the surface cause either heating or cooling, depending on the conditions



- Joule Heating

Current running through the emitter causes Joule heating. In standard metallic tips conditions, Nottingham heating is dominant. **However** this might change when tips reach **high temperatures beyond melting point**.

Electron emission computational tool requirements

- Field emission calculations are much more complicated than applying simple equations.
- Need for a general computational tool for electron emission that:
 - Calculates emitted current density and Nottingham heating power
 - Is applicable to all regimes (thermal, field, intermediate)
 - Takes into account the curvature of the emitters
 - Costs affordable computational time
 - Is versatile and generally applicable to various emission calculations
- Development of a new tool named GETELEC.

!!Download it from <https://github.com/AndKyr/GETELEC>

What can GETELEC do?

- Take as input the work function φ , temperature T and electrostatic data as:
 - Either already calculated electrostatic potential distribution $\Phi(\mathbf{x})$
 - Or the parameters (F, R, γ) of a simple electrostatic model
- Find the regime (thermal, field, intermediate, blunt, sharp)
- Calculate the current density J and the Nottingham heating power P_N
- Automatically analyse experimental I-V data and extract:
 - Enhancement factor β
 - Radius of curvature R

GETELEC Results

- GETELEC calculations for various regimes and comparison to previous theories:

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CreationDate:Thu Oct 27 15:10:49 2016

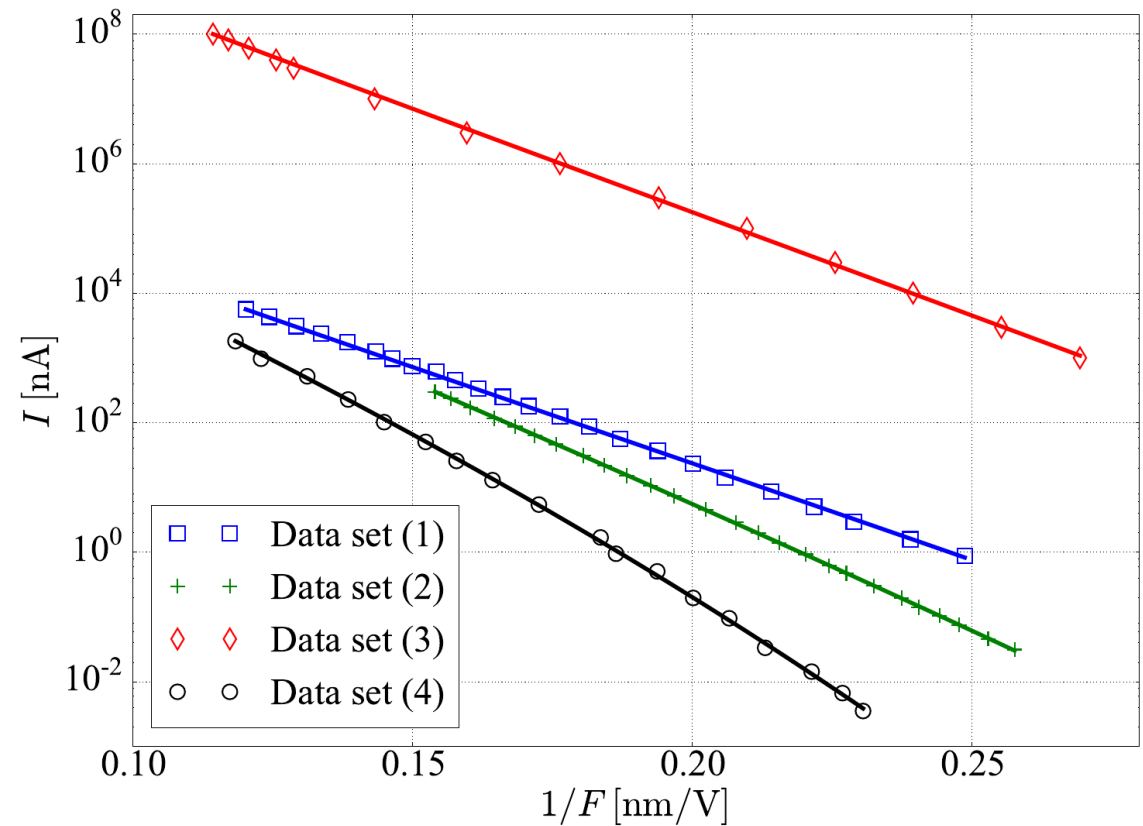
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- Current and Nottingham heat are overestimated by several orders of magnitude by the standard GTF or FN theory

GETELEC Results II: Experimental I-V data

- Fitting data from various experimental groups
- Extracted parameters in good agreement with

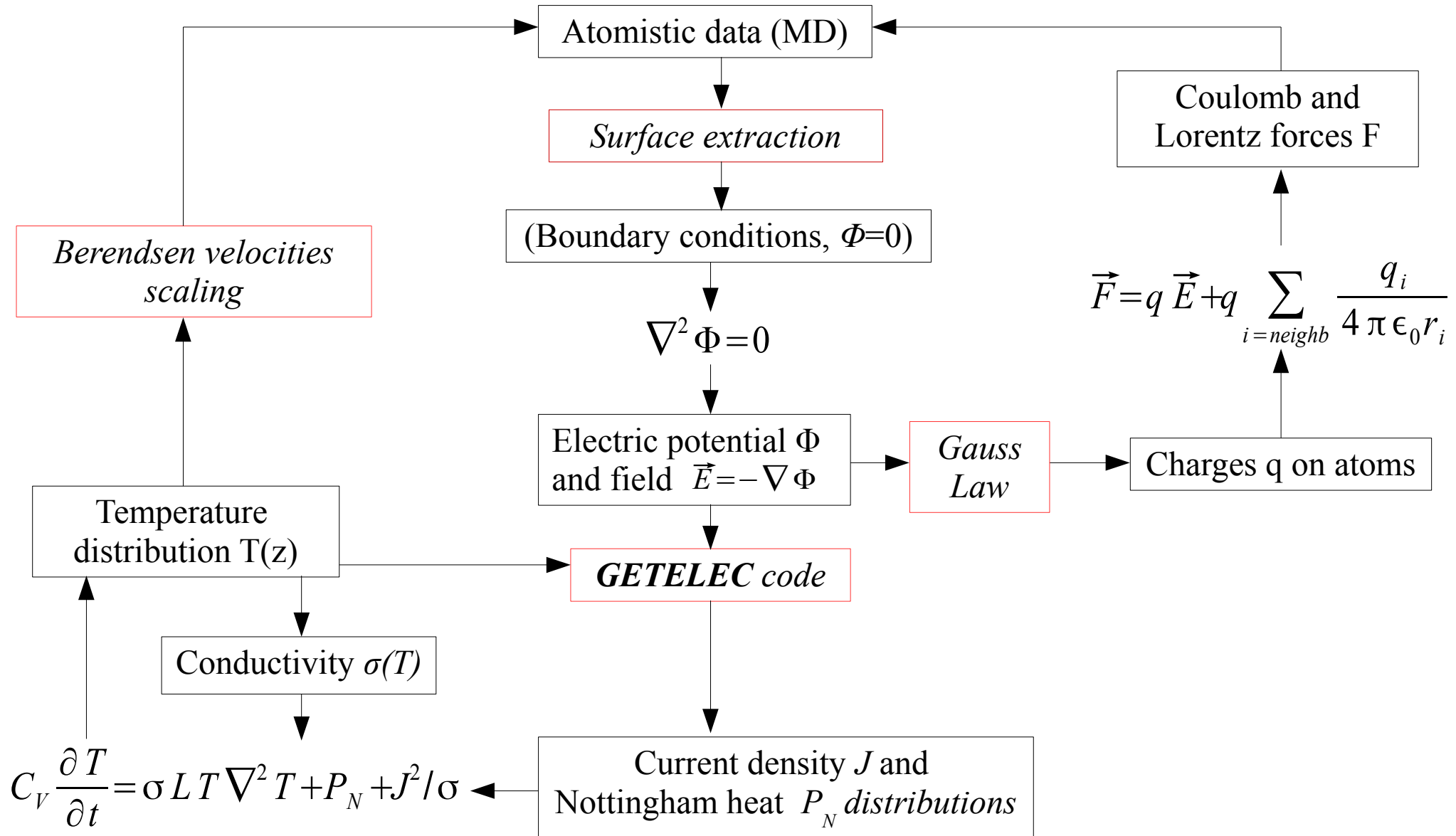
Set	ϕ (eV)	β	R(nm)
1	4.05	0.017/nm	10.08
2	4.5	$1.007\beta_{\text{exp}}$	6.87
3	4.35	0.065/nm	16.22
4	4.5	68.6	2.96

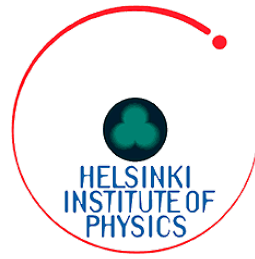


Integrating GETELEC into multi-physics simulation tools

- The power of GETELEC is that it is general, versatile and computationally efficient
- It can be easily integrated with other simulation tools
- We combined it with our multi-physics codes under development into a complete simulation tool that combines various processes:
 - Molecular Dynamics (MD): Parcas
 - ElectroDynamics (ED): Helmod or Femocs
 - Electron Emission (EE): GETELEC
 - Heat Evolution (HE): Helmod or Femocs

Integrated Multi-physics simulations





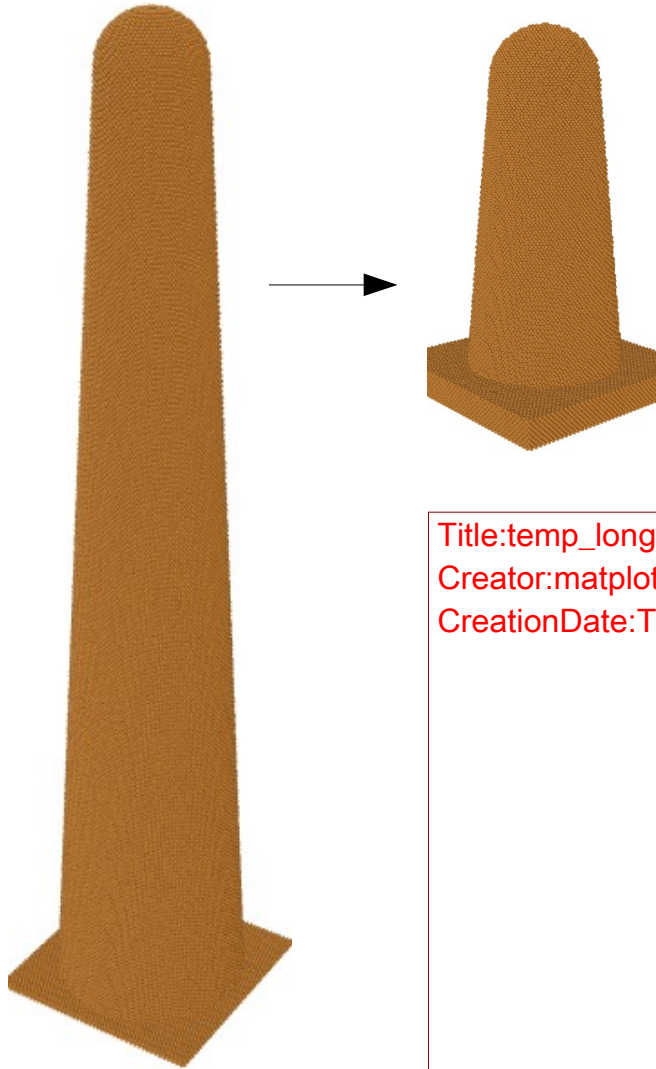
Results: Temperature

- Test on a simple cylindrical tip with $R=1.5\text{nm}$, $h=21\text{nm}$ and applied field = 1.25GV/m
- Two modes for comparison on a :
 - **Mode A:** Full calculation with GETELEC, including both Nottingham and Joule heating components
 - **Mode B:** Simple Classical F-N equation, including only Joule heating

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A bigger tip



- Experiments have shown enhancement factors of the order of $\beta \sim 20-50$
- Assuming tips of the size that can produce an enhancement factor of $\beta \sim 20$: $h=61\text{nm}$, $R=4\text{nm}$
- Emitters with this enhancement easily reach melting temperature at the top for an applied field of about 0.43GV/m
- To simulate in a plausible computational time, we assume a smaller system, but apply higher field to get the same local, and higher bottom temperature 600K

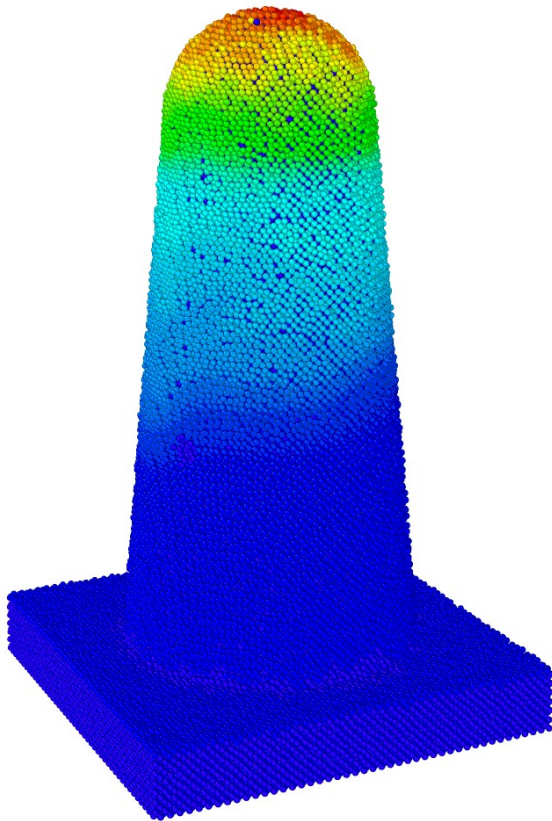
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Positive feedback and evaporation

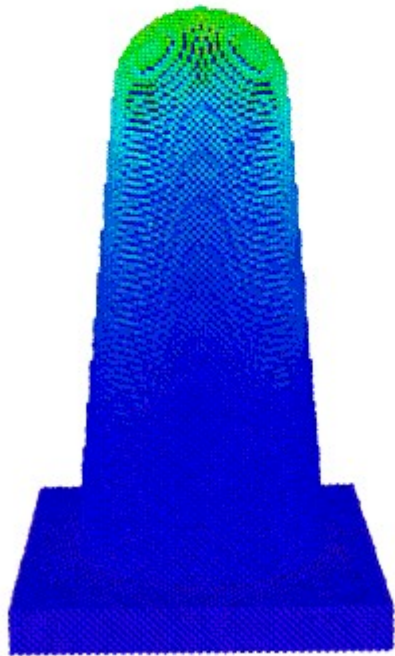
- If the applied field is enough to melt the top, the tip enters in a positive feedback loop:
- The field-induced stress make it pointier and the current increases
 - The current increases the temperature
 - The temperature increases the thermal and electric resistivity and makes the tip more “flexible”, tending to grow higher and pointier
 - Eventually it will reach temperatures as high as 3000K and start evaporating



Including the space charge

$$E_{\text{appl}} = 1.2 \text{ GV/m}$$

$$t = 2.0 \text{ ps}$$

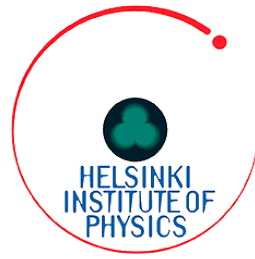


- Beyond a point the electron emission enters the space-charge limited regime.
- We took it into account with the simple analytical 1-D approximation.
- The space charge does not let the local field and the emitted current reach too high levels.
- However as the temperature rises, the resistivity of the material rises a lot and the Joule heating leads it to very high temperatures
- The result does not change qualitatively but the whole process becomes slower



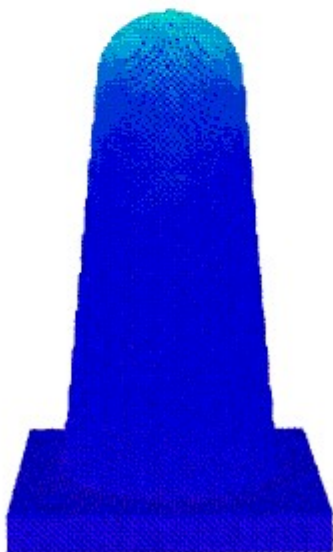
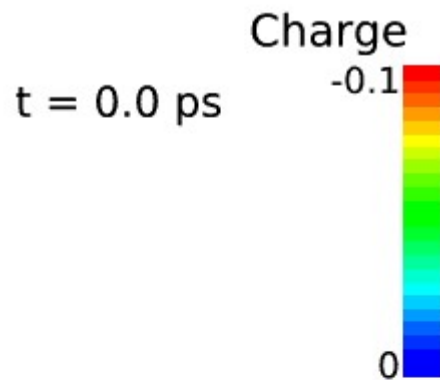
UNIVERSITY OF HELSINKI

Running at constant temperatures



$$E_{\text{appl}} = 1.2 \text{ GV/m}$$

$$T_{\text{top}} = 1600 \text{ K}$$



- We ran at constant temperature distributions, to investigate under what conditions the tips enter this positive feedback loop
- With constant temperature the shape is kept much smoother as the tip does not reach boiling temperatures
- A large cluster with total charge of $\sim 20e$ is evaporating in the end
- We found that a temperature of at least $\sim 1300 \text{ K}$ is required to see a deformation in MD timescale
- We found that a minimum local field of about $\sim 8 \text{ GV/m}$ is required to pull the structures upwards and not let them melt down

Future plans

- Run more extensive simulations to see what are the exact conditions that lead to tip “explosion”
- Include space charge effects with better models
- Improve the tools and run various geometries and fields
- Investigate the size and the charge of the evaporated clusters
- Simulate the possibility that the evaporated clusters get more charge due to the electron beam.
- Simulate the bombardment of the anode side with the charged clusters, and the resulting possible sputtering.



Thank you!!!!