

# Vacuum Field Emission Models, Measurements, and Simulations

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<sup>5</sup>Materials Characterization and Performance

<sup>6</sup>Radiation Effects Theory

<sup>7</sup>Multiscale Science

<sup>8</sup>Electrical Science and Experiments

<sup>9</sup>Electromagnetic Theory

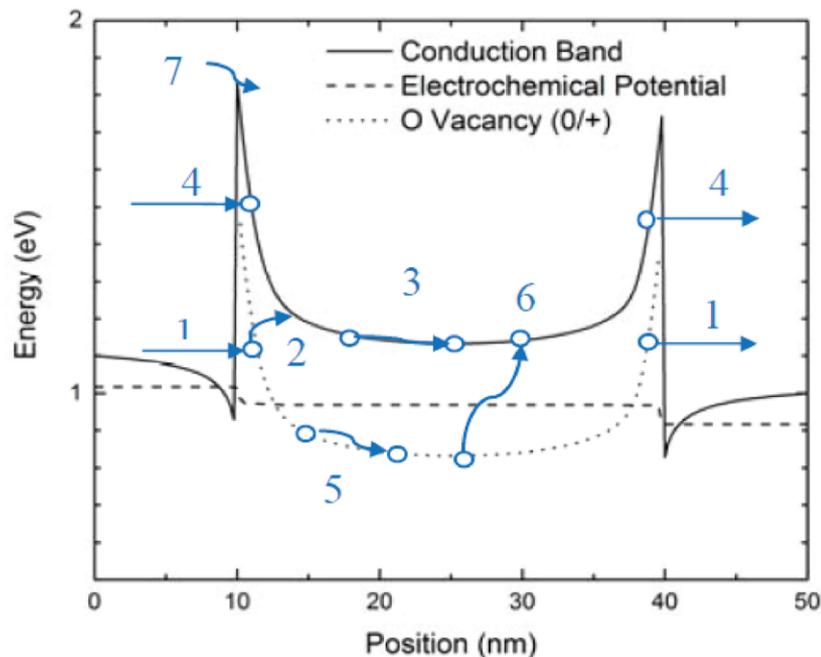
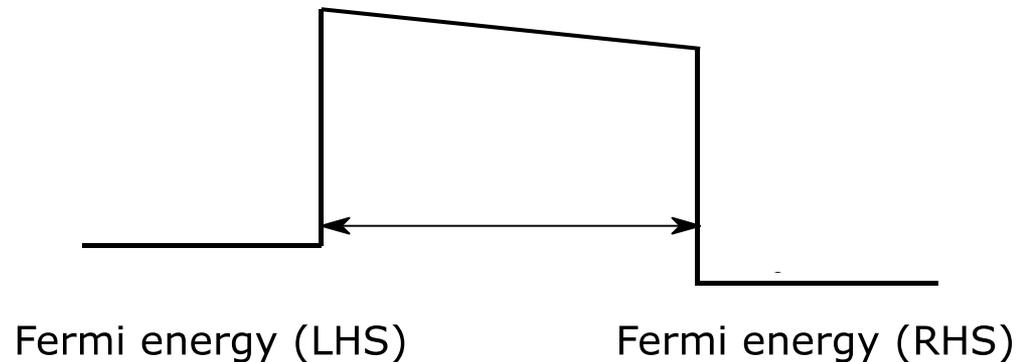
# Introduction/Motivation

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We have begun a new project to understand vacuum field emission from well-controlled surfaces to create physics-based models.

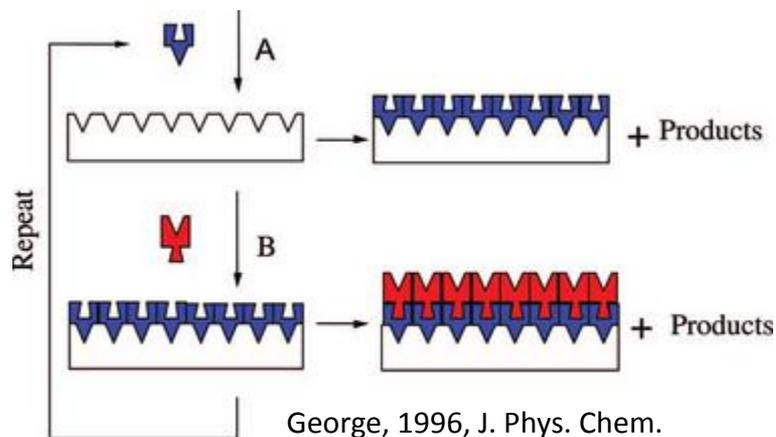
- Restricted to *vacuum* field emission to concentrate solely on field (and temperature) effects – no feedback from gas/plasma species.
- Field emission is viewed as the necessary precursor to a breakdown event. No field emission → no breakdown.
- Employ state-of-the-art microscopy and other techniques to characterize surface very locally, and then apply high fields. Very locally → single metal grain and much smaller (down to atom).
- Address the problem of not knowing state prior to discharge at location of discharge by characterizing and then discharging.
- Apply known layers of dielectric ( $\text{TiO}_2$ ) to challenge models and begin investigation of role of surface contaminants.
- Simulate electron transport resulting in field emission for some experimental situations. Extrapolate to uglier ones.

# Band Structures



- 1: Free-to-defect tunneling
- 2: Defect-to-free tunneling
- 3: Free carrier transport
- 4: Free-to-free tunneling
- 5: Defect-to-defect hopping
- 5: Defect-to-defect Poole-Frenkel tunneling
- 6: Defect capture and emission
- 7: Thermionic emission

# ALD (Atomic Layer Deposition)



Kim, 2011, J. Electrochem Soc.

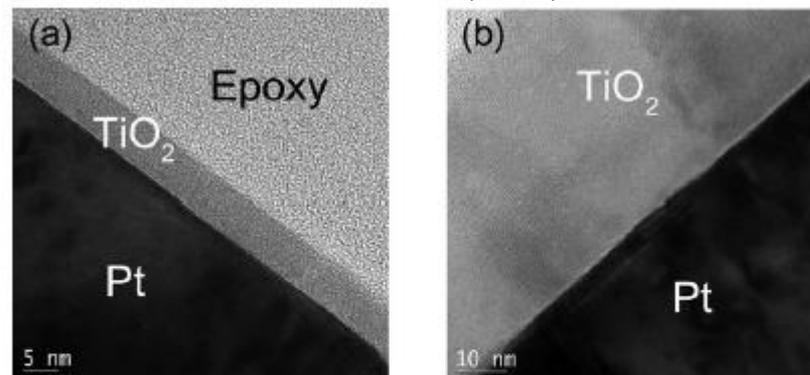


Figure 4. HRTEM images of TiO<sub>2</sub> films grown at 260°C: (a) 6 nm thick and (b) 50 nm thick.

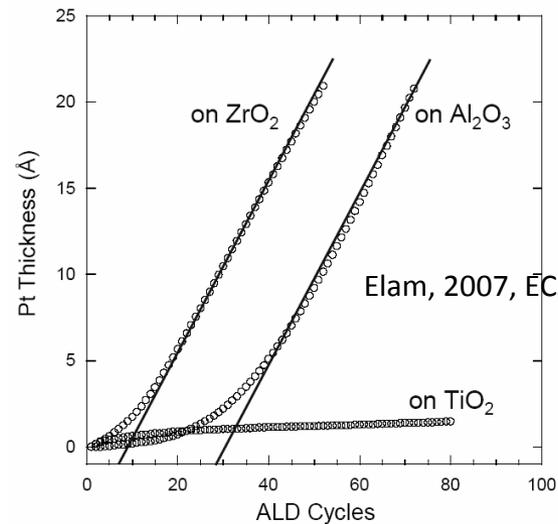
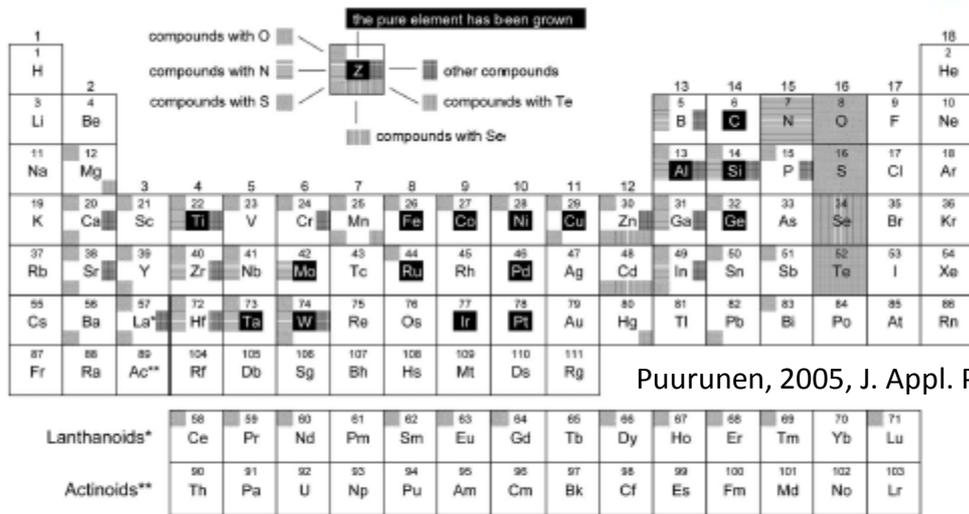


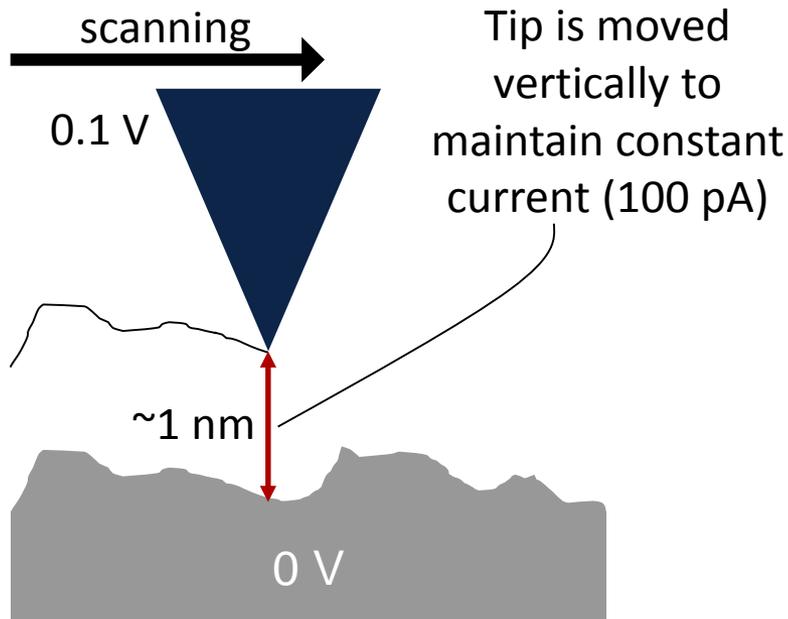
FIG. 3. Overview of the materials grown by ALD. Classification according to Reactant A, with details of the investigations in Table III. Growth of pure elements as well as compounds with oxygen, nitrogen, sulphur, selenium, tellurium, and other compounds grouped together are indicated through shadings of different types at different positions. The elements are named according to the recommendations of The International Union of Pure and Applied Chemistry (IUPAC, [http://www.iupac.org/reports/periodic\\_table/](http://www.iupac.org/reports/periodic_table/), dated 1 November 2004).

# STM (Scanning Tunneling Microscopy)

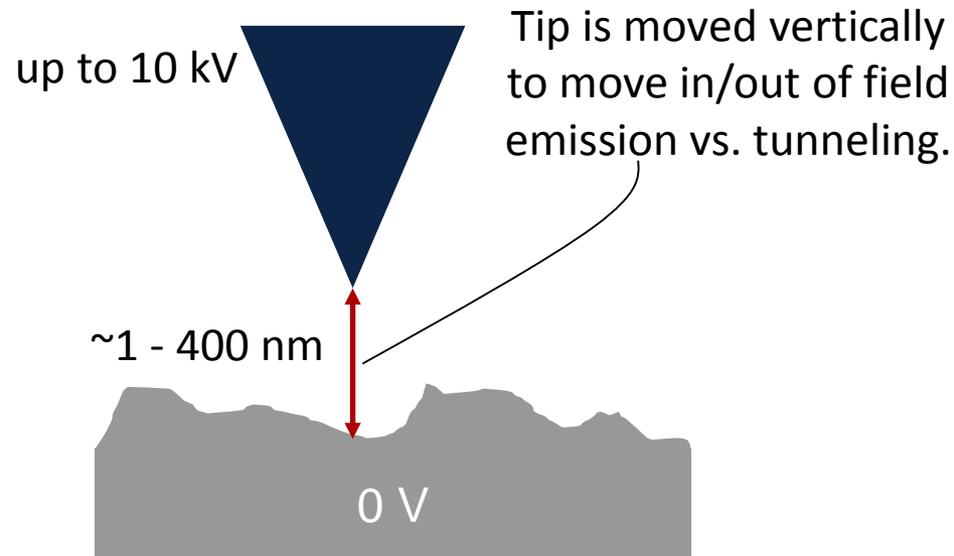
Expected to be a workhorse for field emission and breakdown studies.

- Can go down to sub-nm resolutions.
- Can measure topography in fixed current mode.
- Can measure field emission at applied E.

Typical “correct” usage.



Our planned special usage includes *performing discharge in the STM!*

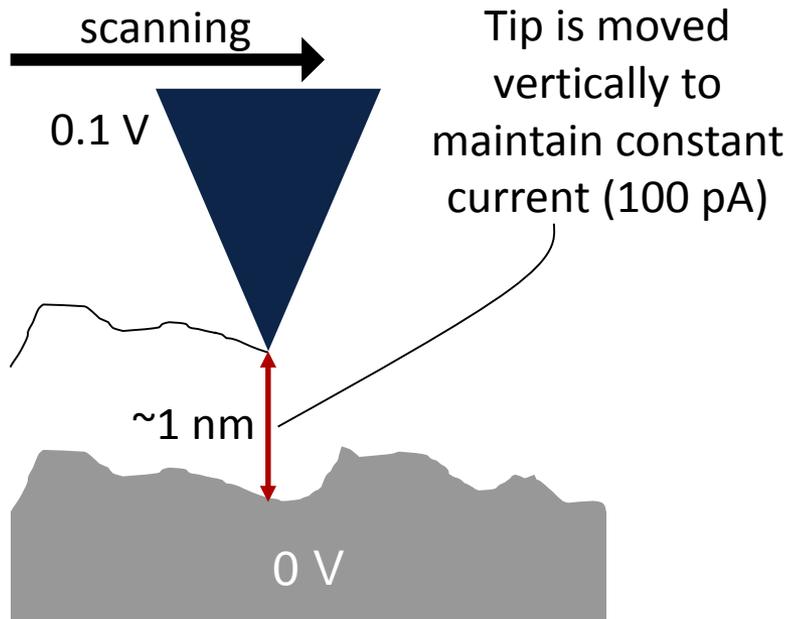


# STM (Scanning Tunneling Microscopy)

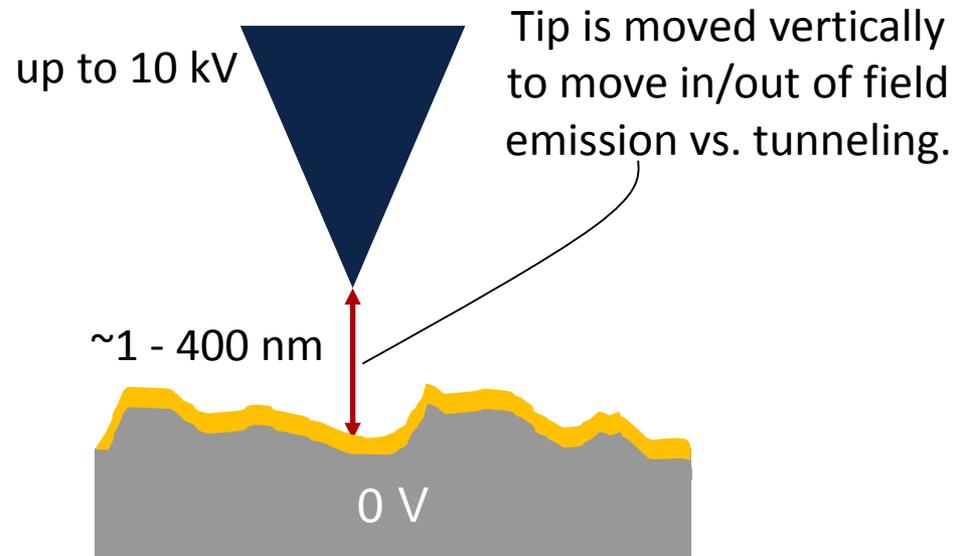
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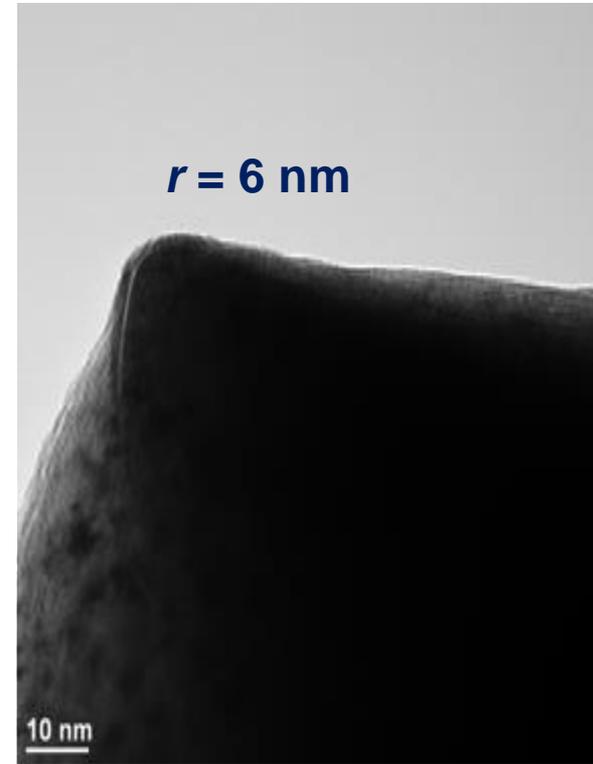


Locality, locality, locality...

# STM Results

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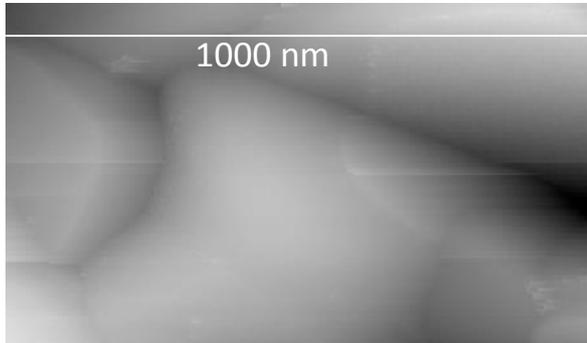
TEMs of an STM tip.



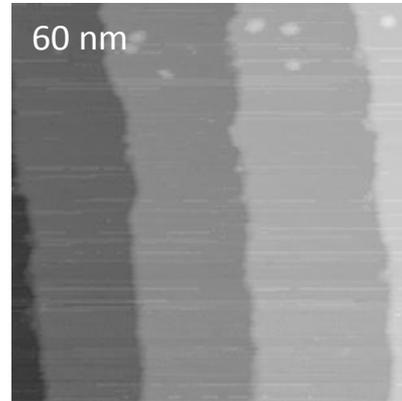
# STM Results

Sean sputtered Pt/ZnO/SiO<sub>2</sub>/Si annealed to 900C  
After heating to 640 C/5 mins in ultrahigh vacuum.

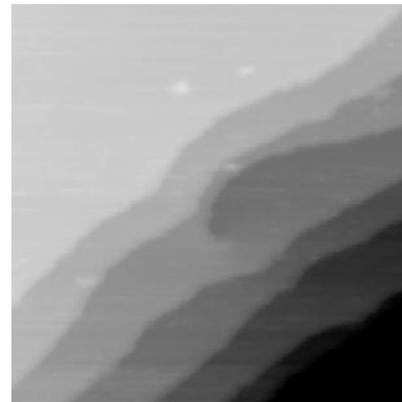
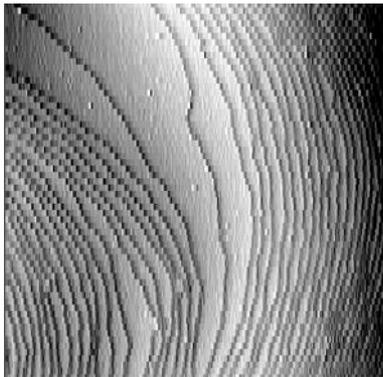
All atomic steps are 2.2-2.4 Å,  
consistent with 111. A 100  
step is 1.9 Å.



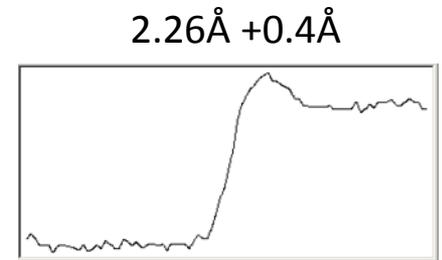
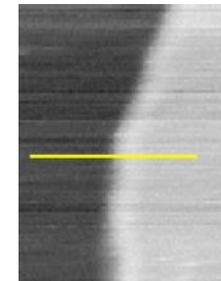
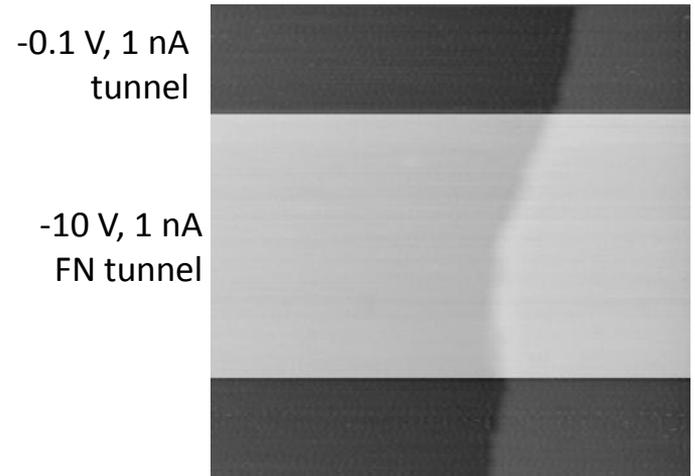
20150210\_00x



200 nm

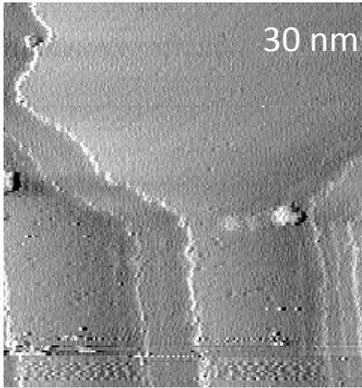


-0.1 V, 1 nA



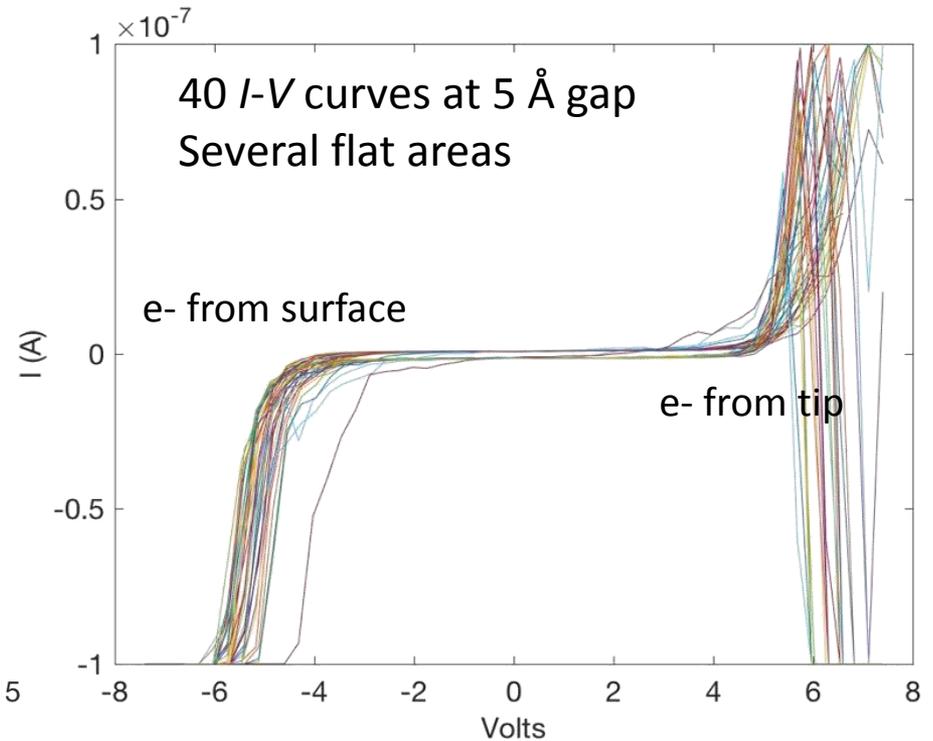
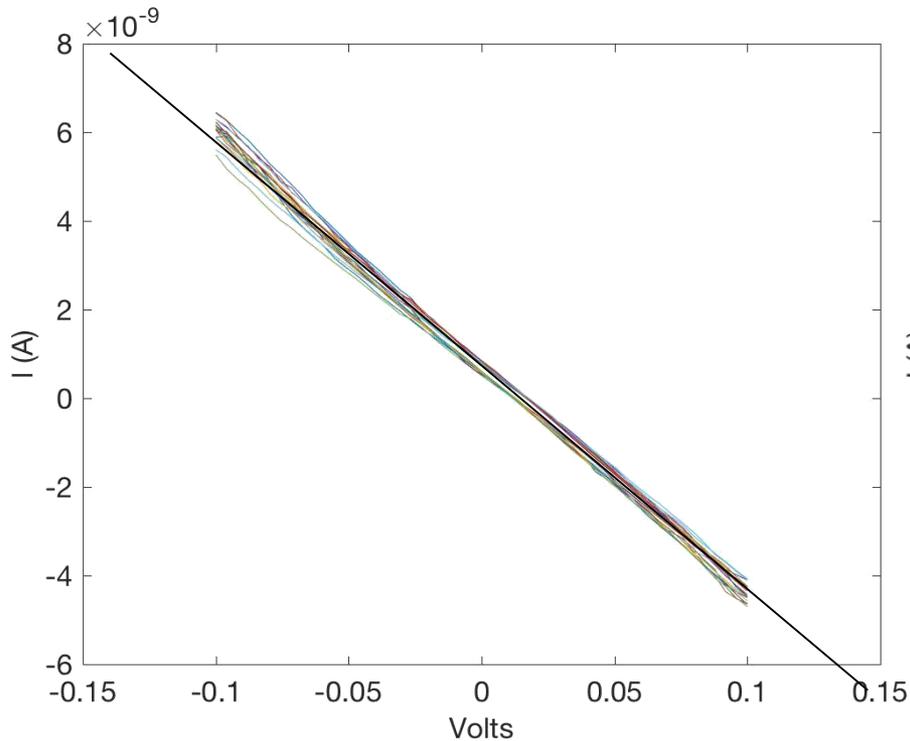
Step edge anomaly field enhancement

# STM Results

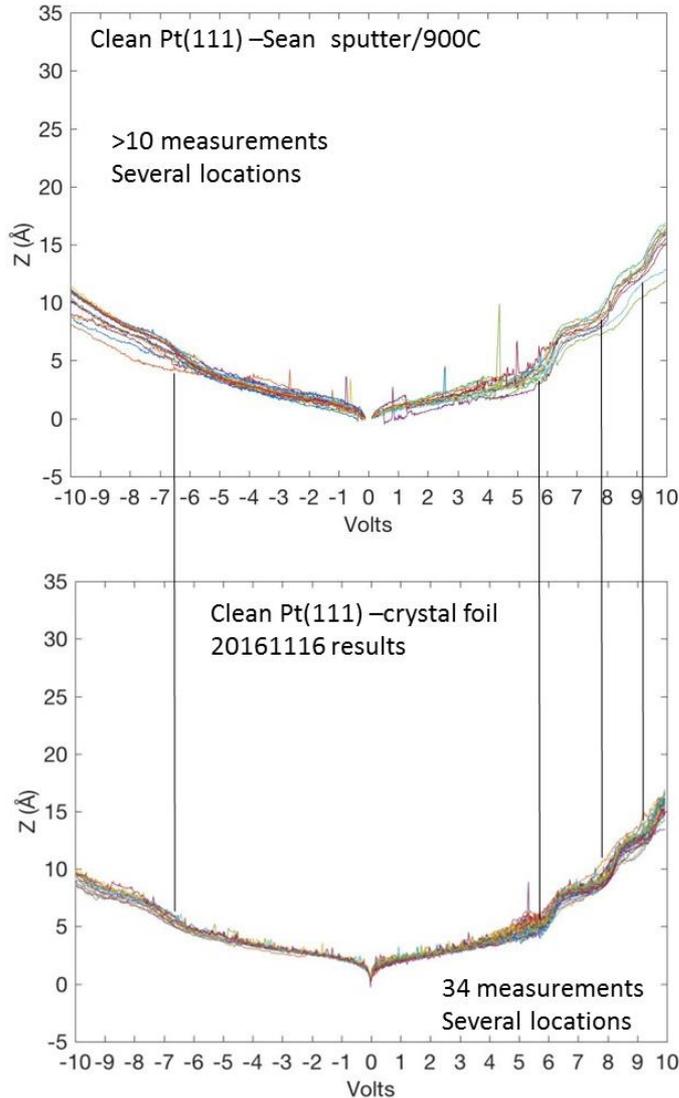


Surface is metallic  $\rightarrow$  no bandgap.

1. Find a clean flat area.
2. Check tunnel gap is Ohmic around 0 V.
3. Establishes that tip is reasonably free of dielectric crud & surface is metallic.



# STM Results



- FN resonances line up.
- Amazing that anything compares at all, these are from *different* tips with very different geometries.
- Prepared by different techniques and battered against surface in different ways.

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PHYSICAL REVIEW LETTERS

26 AUGUST 1985

## Electron Interferometry at Crystal Surfaces

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AT&T Bell Laboratories, Murray Hill, New Jersey 07974

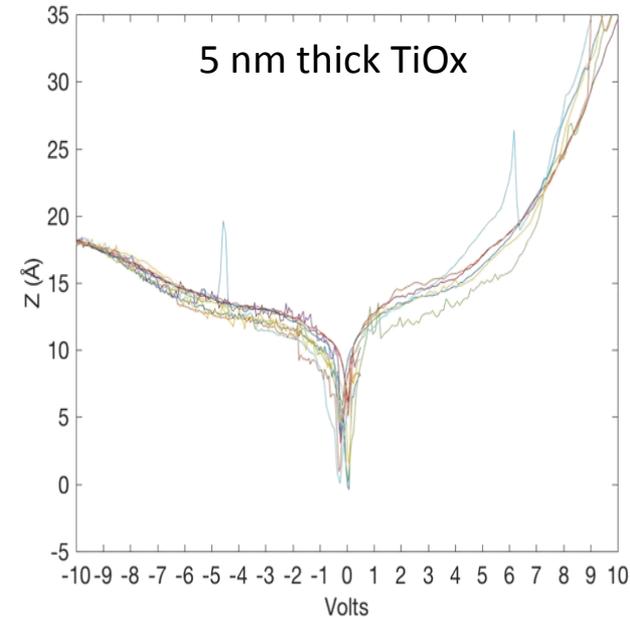
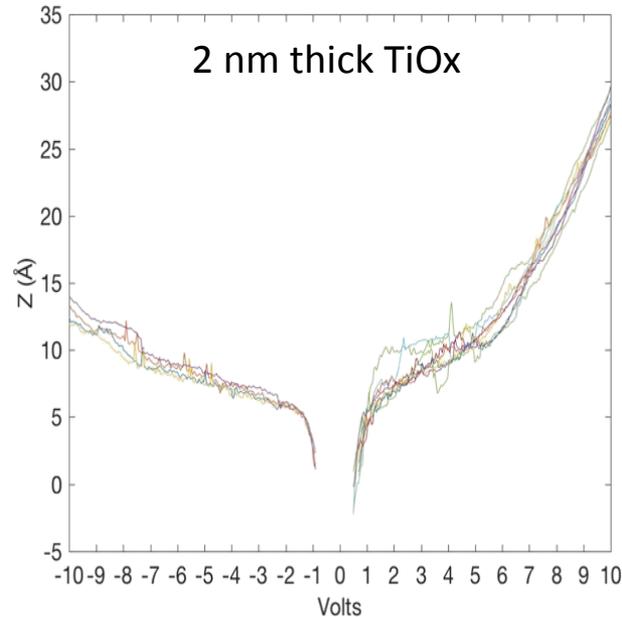
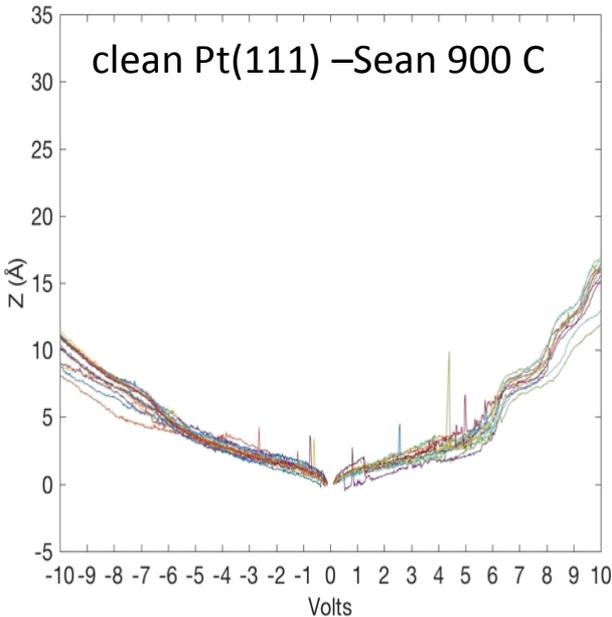
(Received 10 April 1985)

Electron standing waves formed in the vacuum gap between the probe and the sample of the tunneling microscope are observed. The sensitivity of the standing-wave positions and frequencies to the surface potential are demonstrated. Further effects possibly due to Bragg backscattering from the surface atomic planes of the sample are discussed.

PACS numbers: 73.20.Cw, 73.40.Gk

# STM Results

Characterize variability by looking at a few locations for each type of sample.



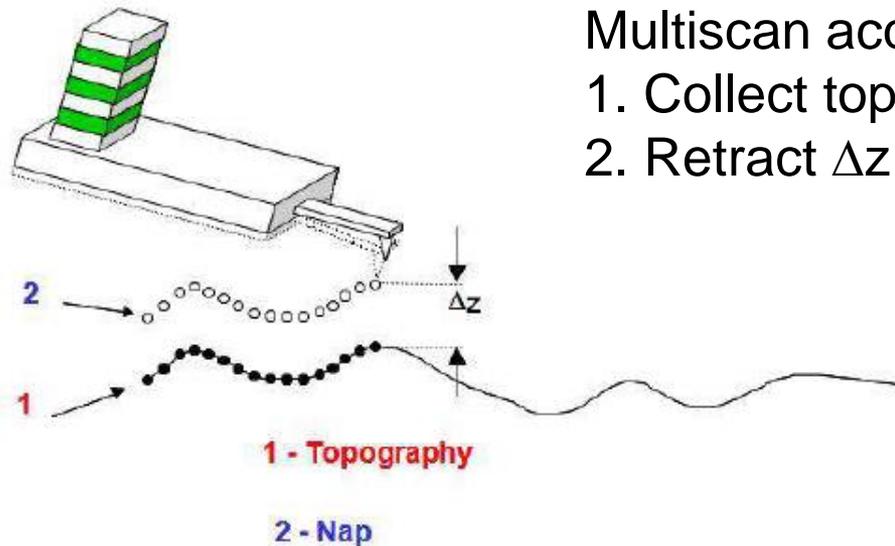
Note that at fixed voltage a larger gap in the 5 nm layer can achieve the same current as a smaller gap for 2 nm layer, and even smaller gap for clean Pt.

→ The oxide layer *increased* field emission!

# AFM (Atomic Force Microscopy)

Scanning Surface Potential Microscopy (SSPM) aka  
Kelvin Probe Microscopy (KPM) aka  
Scanning Kelvin Probe Microscopy (SKPM)

Method to detect potential difference between probe tip and sample



Multiscan acquisition

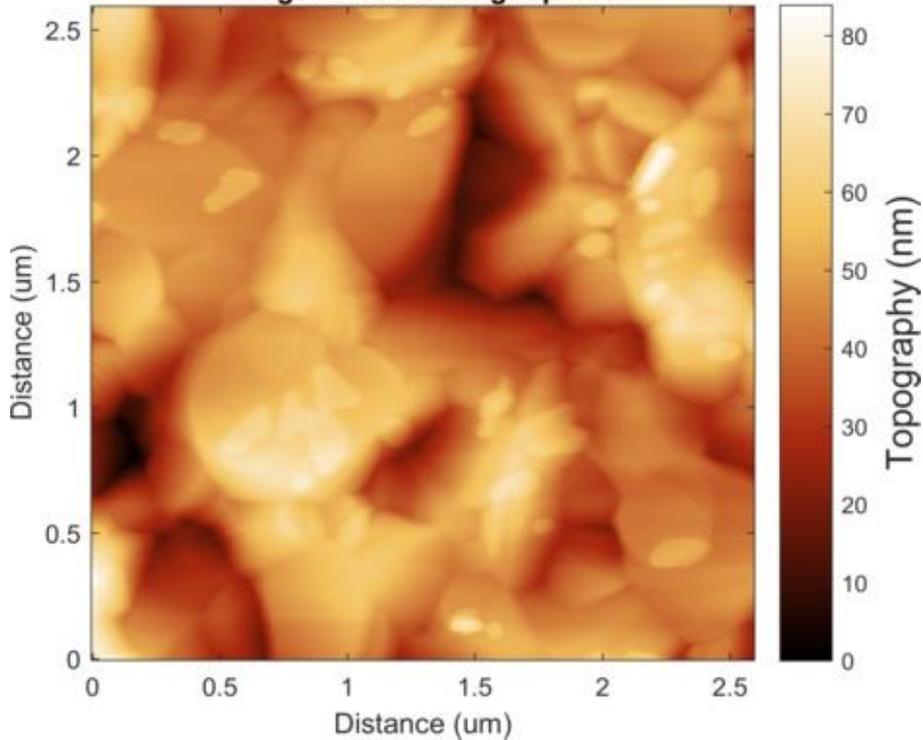
1. Collect topography
2. Retract  $\Delta z$  and collect electrical image

Resolution < contact mode measurements

# AFM Comparison

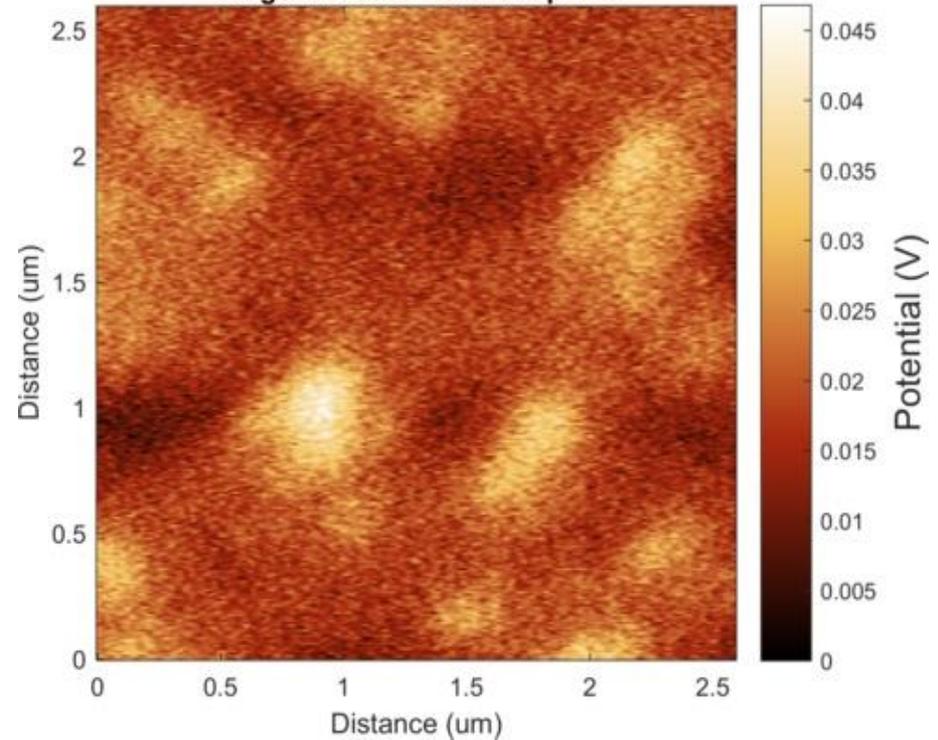
5 nm TiO<sub>2</sub> on 900°C Pt/ZnO/SiO<sub>2</sub>/Si

Image02130010 Height p+f+0



Topography

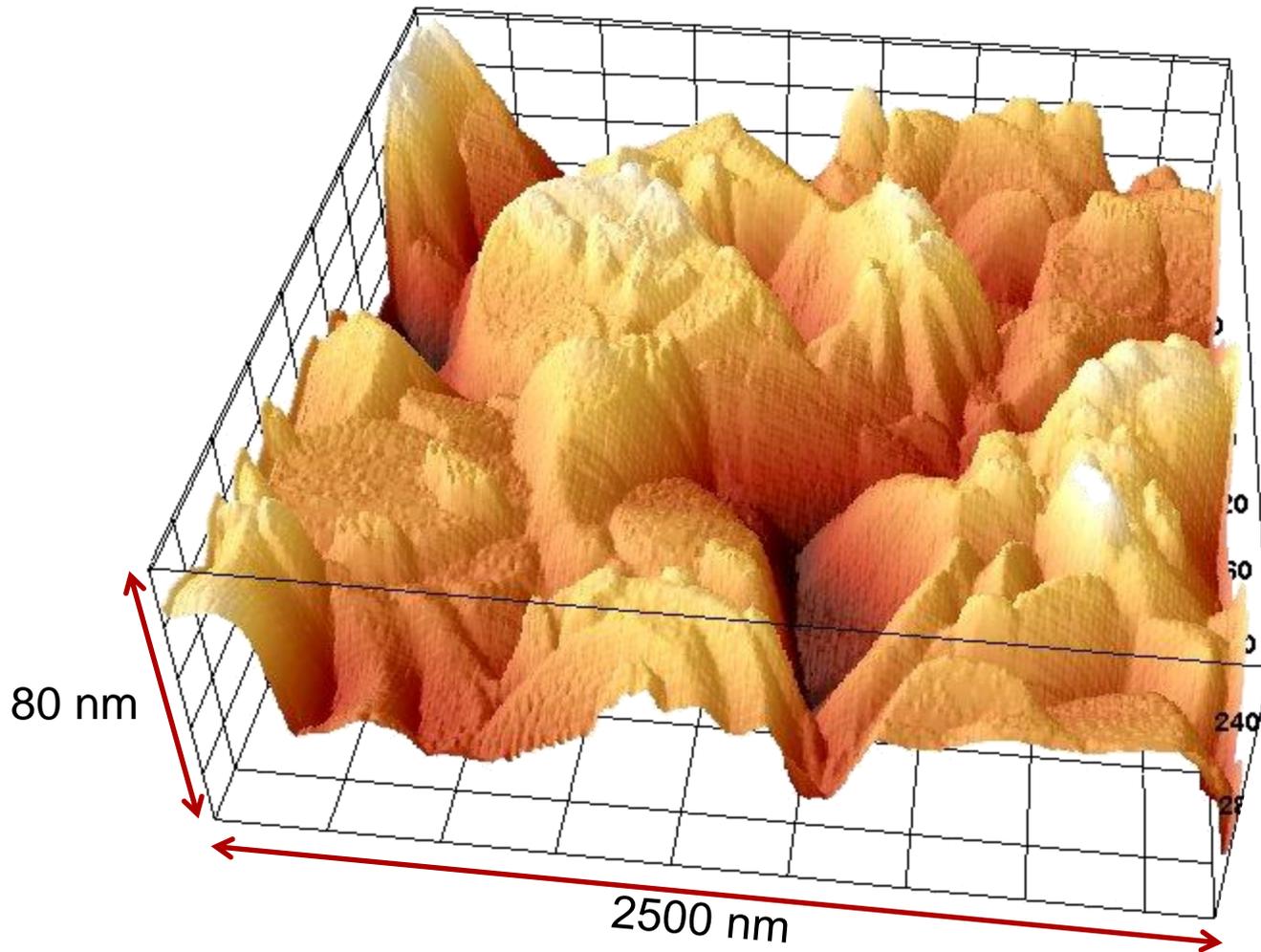
Image02130010 Potential p+f+0



Potential

# AFM Comparison

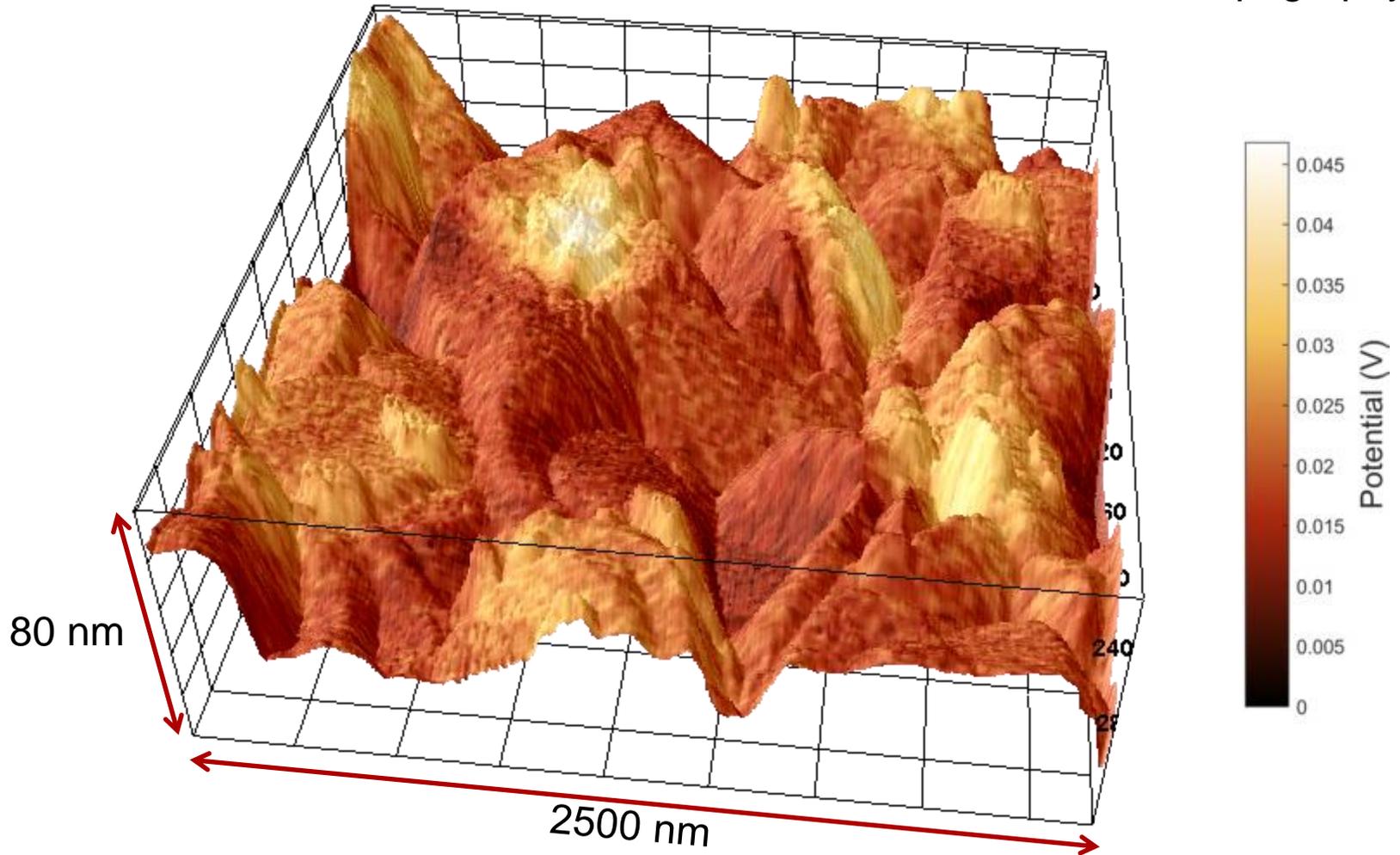
5 nm  $\text{TiO}_2$  on 900°C Pt/ZnO/SiO<sub>2</sub>/Si



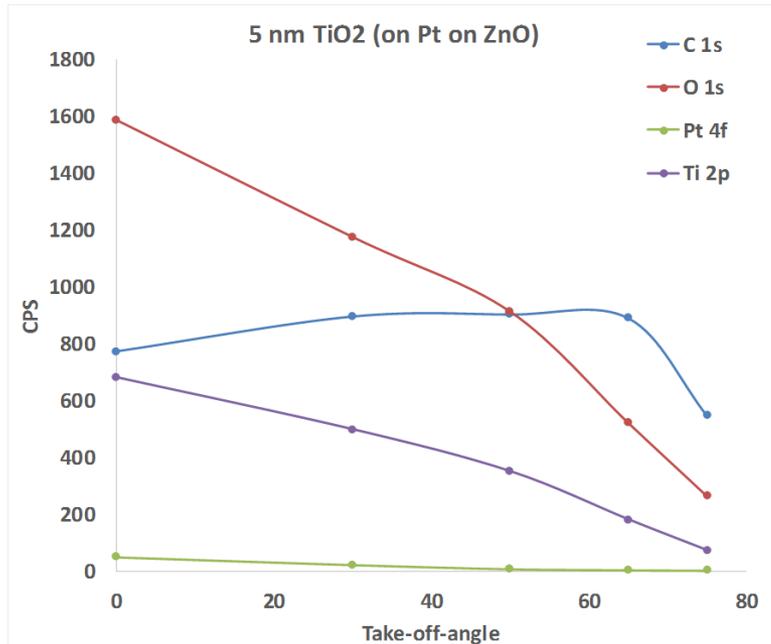
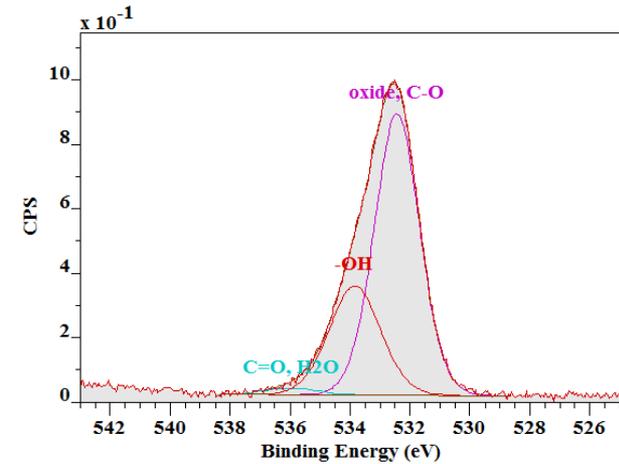
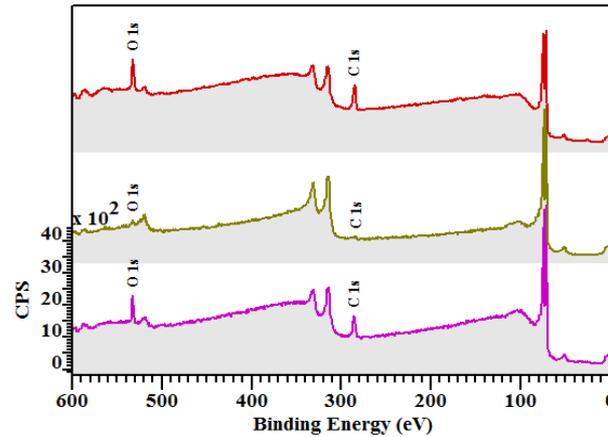
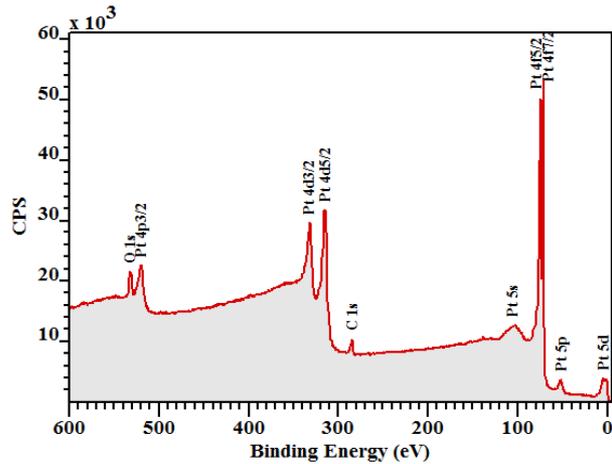
# AFM Comparison

5 nm TiO<sub>2</sub> on 900°C Pt/ZnO/SiO<sub>2</sub>/Si

Potential is not always correlated to topography!



# XPS (X-Ray Photoelectron Spectroscopy)



Substrate Designator: 5 nm TiO <sub>2</sub> on Pt on ZnO_00				
Intensity				
Emission Angle (degrees)	C 1s	O 1s	Pt 4f	Ti 2p
0		772	1585.85	48.1921 680.766
30	894.801		1174.42	20.9266 497.498
50	901.677		912.071	6.13556 349.818
65	888.825		520.7	2.35738 180.272
75	544.989		262.51	0.893102 71.4935
Hydrocarbon Thickness (Å):				15.93
Uncertainty (Å):				
RMSE of Fit:				0.9255
Oxide Thickness (Å):				69.28
Uncertainty (Å):				
RMSE of Fit:				0.007656

# Electron Transport

A continuum approach, REOS (Radiation Effects in Oxides and Semiconductors), models the reactive transport of electrons, holes and other species such as vacancies. Energy transport in terms of the heat equation as well as electron, hole and lattice temperatures.

Continuity Equations

$$\frac{\partial c_i}{\partial t} = -\nabla \cdot \mathbf{J}_{si} + \sum_j \nu_{ij} R_{ij} + G_i$$

$$\left\{ \begin{array}{l} c_i = \text{Density of species } i \\ J_{si} = \text{Current density of species } i \\ \nu_{ij} = \text{Reaction coefficient for species } i \text{ in reaction } j \\ R_{ij} = \text{Reaction rate for species } i \text{ in reaction } j \\ G_i = \text{Generation rate for species } i \end{array} \right.$$

Drift-Diffusion Species Current

$$\mathbf{J}_{si} = z_i c_i \bar{\mu}_i \mathbf{E} - D_i \nabla c_i$$

$$\left\{ \begin{array}{l} \bar{\mu}_i = \text{mobility} \\ \mathbf{E} = \text{electric field} \\ z_i = \text{species charge sign} \end{array} \right.$$

# Electron Transport

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A stochastic approach, EMC (Ensemble Monte Carlo), explicitly models electron scattering events, vacancy generation, etc.

The Boltzmann equation that describes transport in solids can be written as

$$\frac{\partial f(\mathbf{r}, \mathbf{p}, t)}{\partial t} = -\frac{1}{2\pi\hbar} \sum_{\mathbf{r}', \mathbf{p}'} |V_{\mathbf{r}\mathbf{p}, \mathbf{r}'\mathbf{p}'}|^2 f(\mathbf{r}, \mathbf{p}, t) \{1 - f(\mathbf{r}', \mathbf{p}', t)\} - f(\mathbf{r}', \mathbf{p}', t) \{1 - f(\mathbf{r}, \mathbf{p}, t)\} \delta(E_i - E_f)$$

in which  $f(\mathbf{r}, \mathbf{p}, t)$  is the particle distribution function for position  $\mathbf{r}$ , momentum  $\mathbf{p}$  and time  $t$ . The effects of scattering are contained in the interaction potential  $V$ .

The software EMC obtains a steady-state solution to this equation by using an iterative method that uses a Monte Carlo technique.

An important feature of this software is the use of a distribution function that includes Fermi statistics. This feature is necessary for the inclusion of carrier-carrier scattering effects that control fully developed electrical breakdown effects.

# Electronic Structure – Density Functional Theory

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To inform continuum models of electron transport, we need detailed information of the electronic structure of bulk materials, interfaces and surfaces, and defects that comprise the physical system.

A first principle approach, SeqQuest models the electronic structure using a pseudopotential approach and local orbitals, used to model large computational models with accurate treatment of defects. We will also use VASP when a plane wave approach is more appropriate.

- Band structure – transport of electrons through surface oxides
- Electronic levels of bulk defects – defect-mediated transport
- $\Phi$  – work functions – transport between the surface material and vacuum
- Surface structure and defects – modifies transport to vacuum
- First principles treatment of charge and fields

# Conclusions

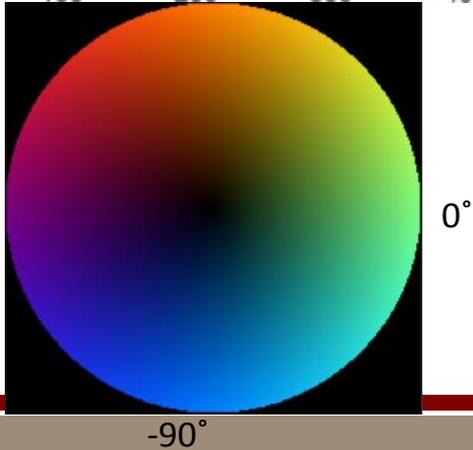
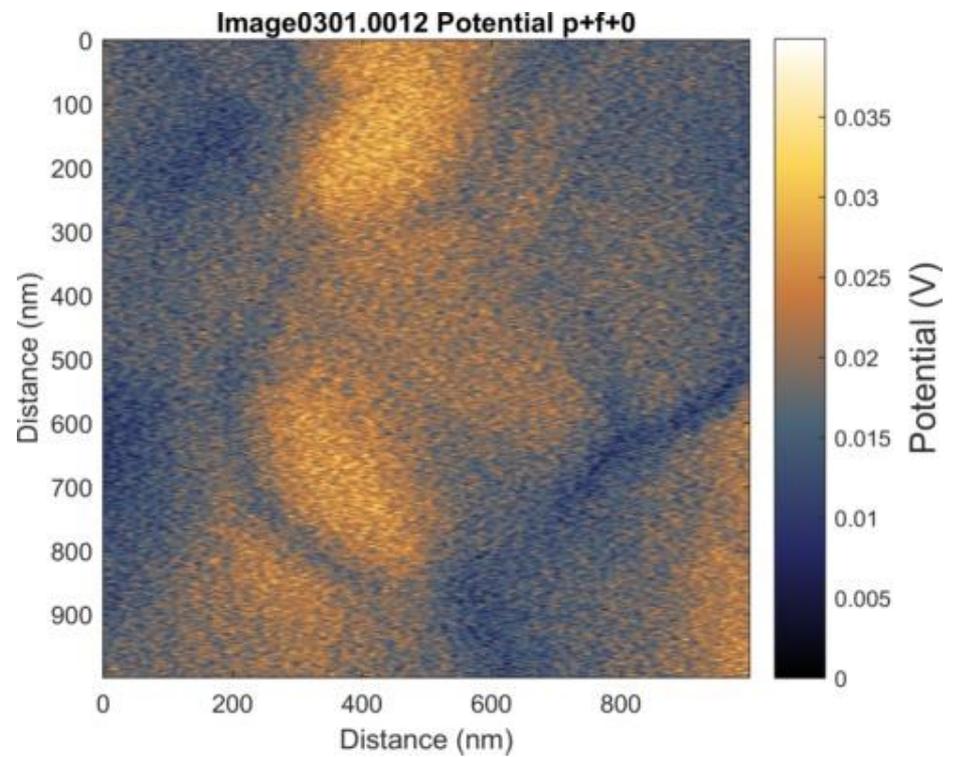
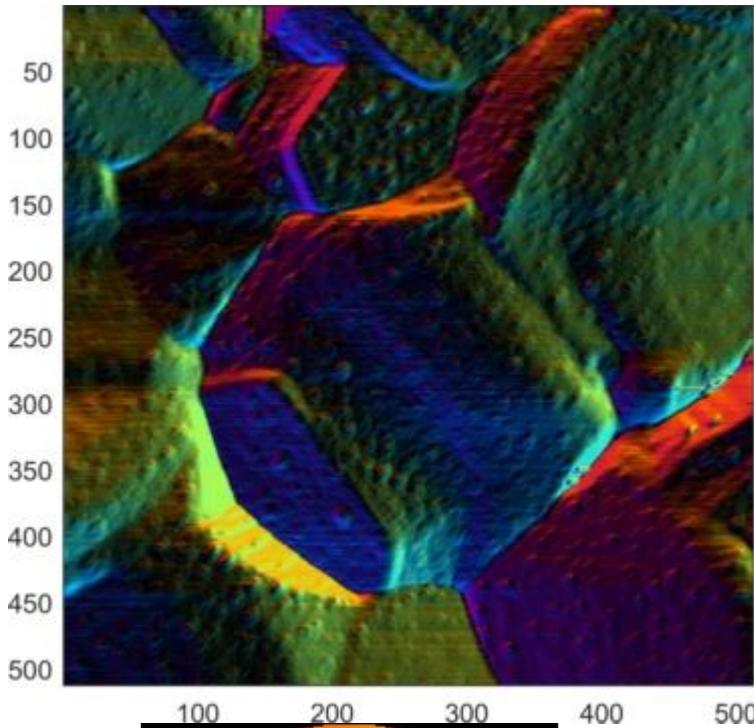
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- Investigating surfaces at the atomic scale to characterize features relevant to vacuum field emission.
- By examining field emission at the nanoscale, we expect to build global models for physics-based and experimentally corroborated local models.
- Want to clarify  $\beta$ -based field emission so  $\beta$  really is only geometry induced field concentration.
- “Work function” + (purely geometric)  $\beta$  is not the whole story in practice.
- Will characterize region, then perform discharge by strongly spatially constraining surface participation.
- Surprising to some of us, adding a thin dielectric layer made it *easier* to extract current.

THANK YOU!

BACKUP SLIDES FOLLOW

Combined, where angle  $\phi$  is indicated by color radially, and magnitude of slope ( $\vartheta$ ) represented by magnitude from middle where edge is  $15^\circ$



Not obvious there is a relation between emission and slope.

# Ensemble Monte Carlo (EMC)

1. Injection of particles, photons or energetic electrons, at a constant rate
2. Electron-hole creation by the absorbed particle
  1. Determined by the collision process or the absorption spectrum
3. “Free flight” of electrons and holes in momentum space
  1. Solve the equations of motion for momentum and position
4. Scattering (changes in momentum and energy)
  1. Plasmon emission
  2. Impact ionization
  3. Phonon emission
  4. Radiative recombination
  5. Emission from the sample (with no return)
5. Collection or emission

# AFM

Force between tip and surface

$$F = \frac{1}{2} \frac{\partial C}{\partial z} V^2$$

Apply bias to tip and scan a sample

$$V = (V_{DC} - V_{sp}) + V_{AC} \sin(\omega t)$$

$V_{DC}$  = applied DC bias

$V_{AC}$  = applied AC bias

$V_{sp}$  = surface potential

$$V^2 = (V_{DC} - V_{sp})^2 + 2(V_{DC} - V_{sp})V_{AC} \sin(\omega t) + V_{AC}^2 \sin^2(\omega t)$$

Combine

$$F = \frac{1}{2} \frac{\partial C}{\partial z} \left( \left[ (V_{DC} - V_{sp})^2 + \frac{1}{2} V_{AC}^2 \right] + 2[(V_{DC} - V_{sp})V_{AC} \sin(\omega t)] - \left[ \frac{1}{2} V_{AC}^2 \cos(2\omega t) \right] \right)$$

Signal at 1<sup>st</sup> harmonic

Apply  $V_{DC}$  to nullify this signal

Contributors to the DC potential difference:

- Difference in work function between the tip and surface
- Trapped charge
- Any permanent or applied voltage between the tip and the sample