



## Summer Student Lecture

# Superconductivity and superconducting magnets for the LHC Upgrade

Paolo Ferracin

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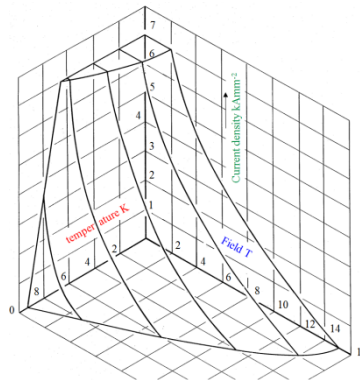
European Organization for Nuclear Research (CERN)

# Introduction

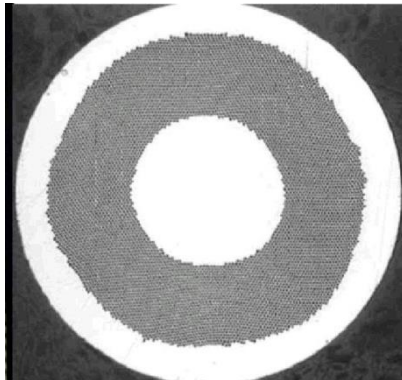
## Goal of the lecture

- Overview of **superconducting magnets** for particle accelerators (dipoles and quadrupoles)
  - Description of the components and their function
  - **...past, present, and future:** HiLumi LHC and FCC
- From the superconducting material to the full magnet

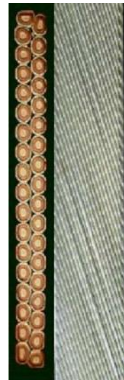
Superconducting material



Superconducting strand



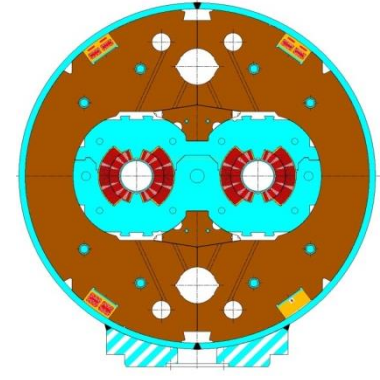
Superconducting cable



Superconducting coil



Superconducting magnet

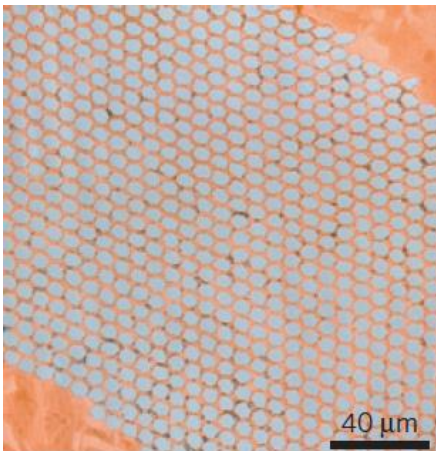




# Introduction

## Superconducting magnet technology

- Multidisciplinary field: mixture of
  - Chemistry and material science: **superconducting materials**
  - Quantum physics: the key mechanisms of **superconductivity**
  - Classical electrodynamics: **magnet design**
  - Mechanical engineering: **support structures**
  - Electrical engineering: powering of the magnets
  - Cryogenics: keep them **cool** ...
- Very different order of magnitudes





# Outline

- **Particle accelerators and superconductors**
- **Magnetic design and coils**
- **Mechanics of superconducting magnets**
- **Quench and protection**
- **HiLumi LHC and FCC**





# References

- **Particle accelerators and superconductors**
  - K.-H. Mess, P. Schmuser, S. Wolff, “*Superconducting accelerator magnets*”, Singapore: World Scientific, 1996.
  - Martin N. Wilson, “*Superconducting Magnets*”, 1983.
  - Fred M. Asner, “*High Field Superconducting Magnets*”, 1999.
  - P. Ferracin, E. Todesco, S. Prestemon, “*Superconducting accelerator magnets*”, US Particle Accelerator School, [www.uspas.fnal.gov](http://www.uspas.fnal.gov).
    - Units 2 by E. Todesco
  - A. Devred, “*Practical low-temperature superconductors for electromagnets*”, CERN-2004-006, 2006.
  - Presentations from Luca Bottura and Martin Wilson



# Particle accelerators and magnets

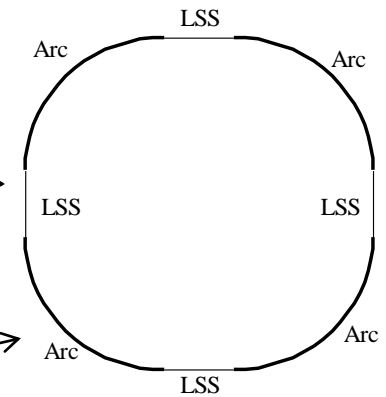
by E. Todesco

- Principle of synchrotrons
  - Driving particles in the same accelerating structure several times
- **Electro-magnetic field** accelerates particles

$$\vec{F} = e\vec{E}$$

- **Magnetic field** steers the particles in a ~circular orbit

$$\vec{F} = e\vec{v} \times \vec{B}$$



- Particle accelerated  $\rightarrow$  energy increased  $\rightarrow$  magnetic field increased ("**synchro**") to keep the particles on the same orbit of curvature

$$p = eB\rho$$

Constant



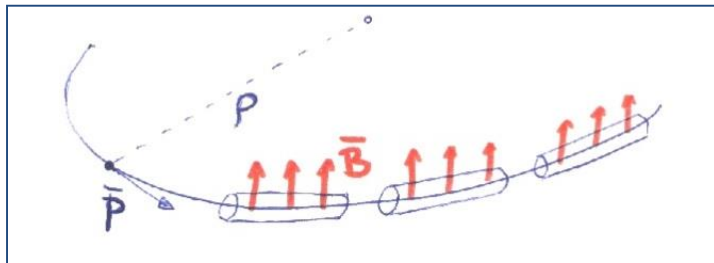
# Particle accelerators and magnets

## Dipoles

- Main field components is  $B_y$ 
  - Perpendicular to the magnet axis  $z$
- **Electro-magnets**: field produced by a current (or current density)

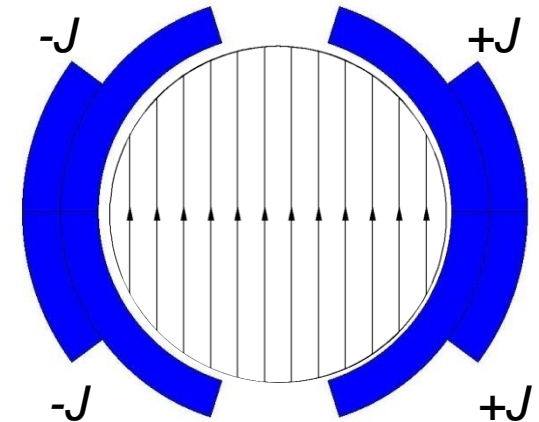
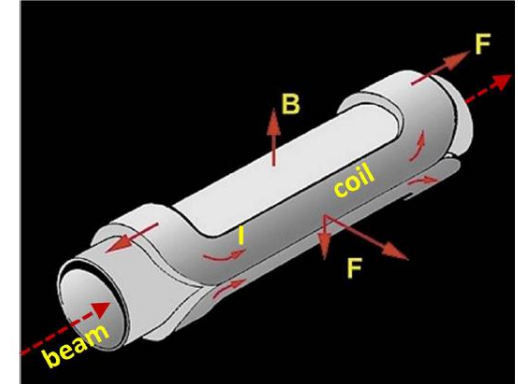
$$B_y = -\frac{\mu_0 J_0}{2} (r_{out} - r_{in})$$

- Magnetic field steers (**bends**) the particles in a  $\sim$ circular orbit



by E. Todesco

$$p = eB\rho$$

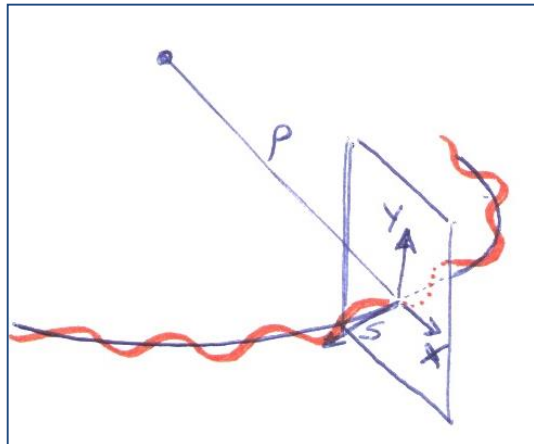
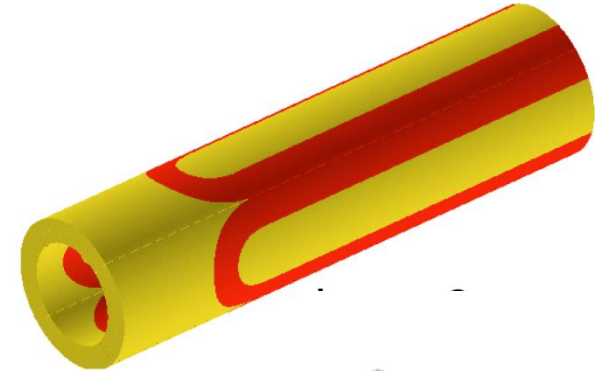




# Particle accelerators and magnets

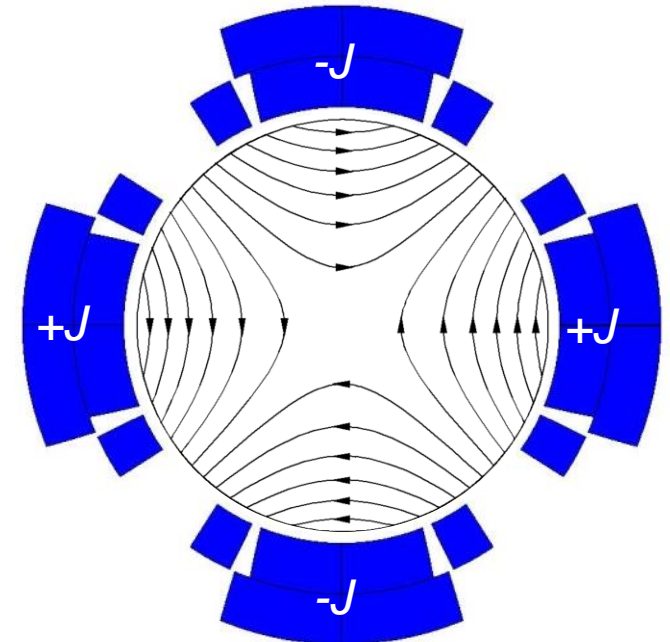
## Quadrupoles

- The force necessary to **stabilize** linear motion is provided by the quadrupoles
- They provide a field equal to **zero** in the **center**
  - increasing linearly with the radius
- They act as a spring: **focus** the beam
- Prevent protons from **falling** to the bottom of the aperture due to the **gravitational force**
  - it would happen in less than 60 ms



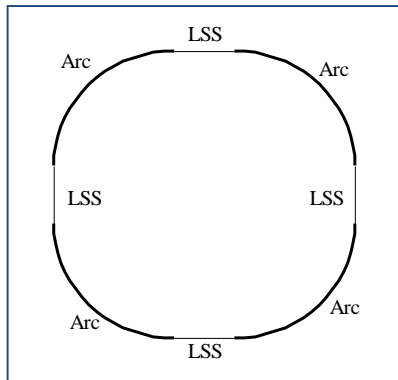
by E. Todesco

$$G = \frac{B_y}{r} = -\frac{\mu_0 J_0}{2} \ln \frac{r_{out}}{r_{in}}$$

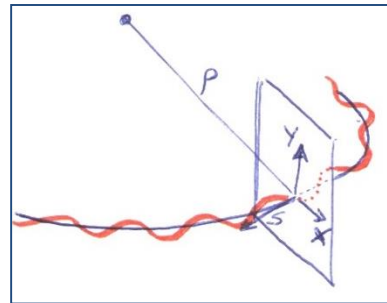
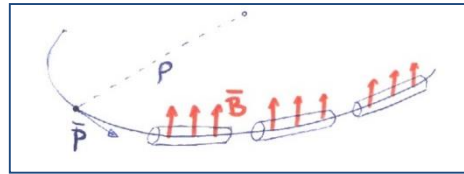


# Particle accelerators and magnets

- Dipoles: the larger **B**, the larger the **energy**
- Quadrupoles: the larger **B**, the larger the **focusing** strength
- For an electro-magnet, the larger **B**, the larger must be **J**

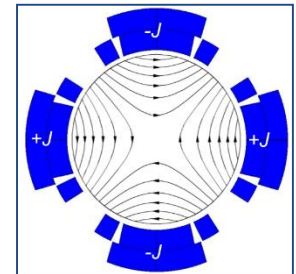
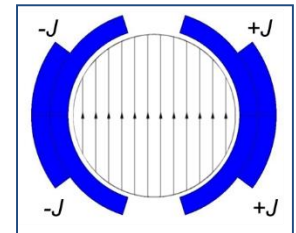


$$p = eB\rho$$



$$B_y = -\frac{\mu_0 J_0}{2} (r_{out} - r_{in})$$

$$G = \frac{B_y}{r} = -\frac{\mu_0 J_0}{2} \ln \frac{r_{out}}{r_{in}}$$



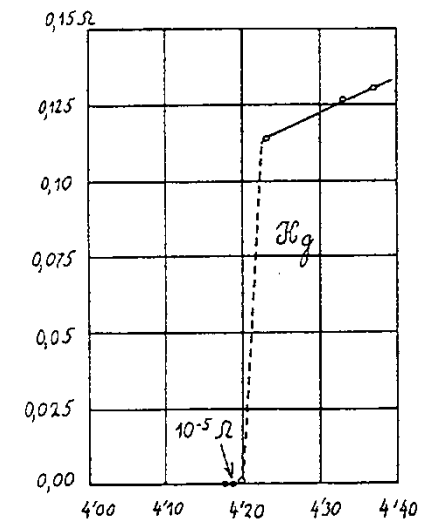
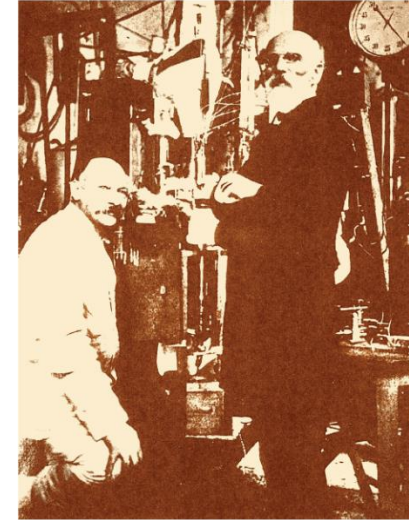
- In **normal** conducting magnets,  $J \sim 5 \text{ A/mm}^2$
- In **superconducting** magnets,  $J_e \sim 600-700 \text{ A/mm}^2$



# Superconductivity

## The discovery

- Superconductivity discovered in 1911 by Kammerling-Onnes
  - **ZERO resistance** of mercury wire at 4.2 K
- Temperature at which the transition takes place: **critical temperature  $T_c$**
- Observed in many materials
  - but not in the typical best conductors (Cu, Ag, Au)
- At  $T > T_c$ , superconductor very poor conductor
- 2 kinds of superconductors
  - **Type I and Type II**
    - Different behaviour with magnetic field

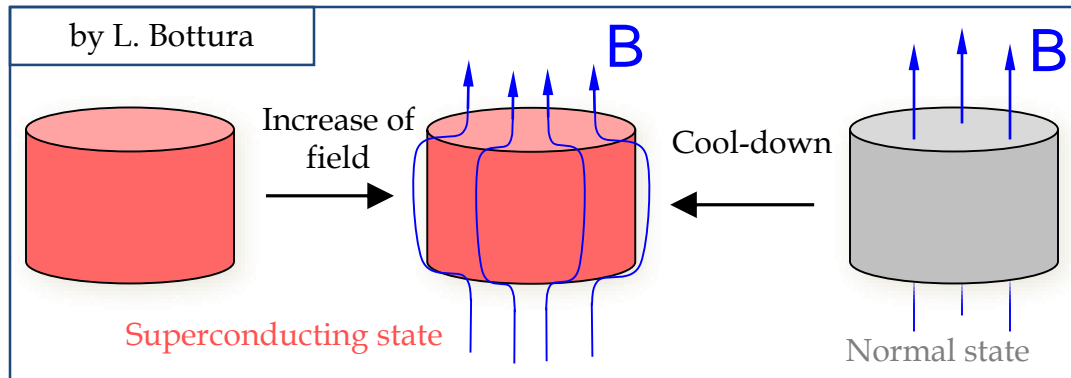




# Superconductivity

## Type I superconductors

- Meissner-Ochsenfeld effect (1933)
- Perfect diamagnetism
  - With  $T < T_c$  magnetic field is expelled
- But, the  $B$  must be  $<$  **critical field  $B_c$** 
  - Otherwise superconductivity is lost



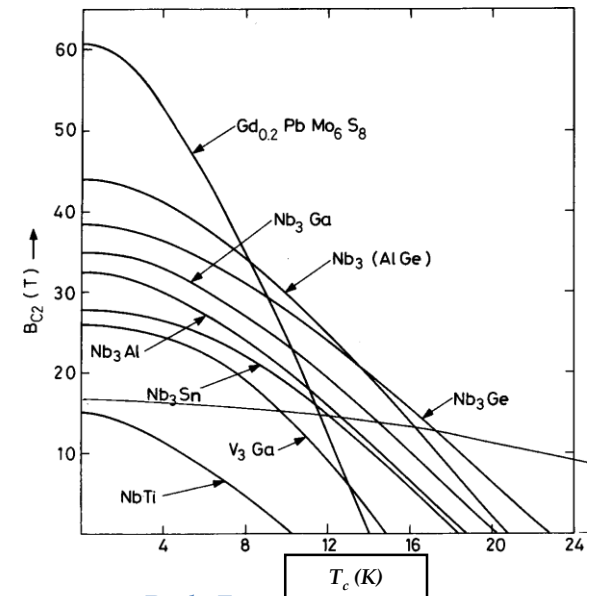
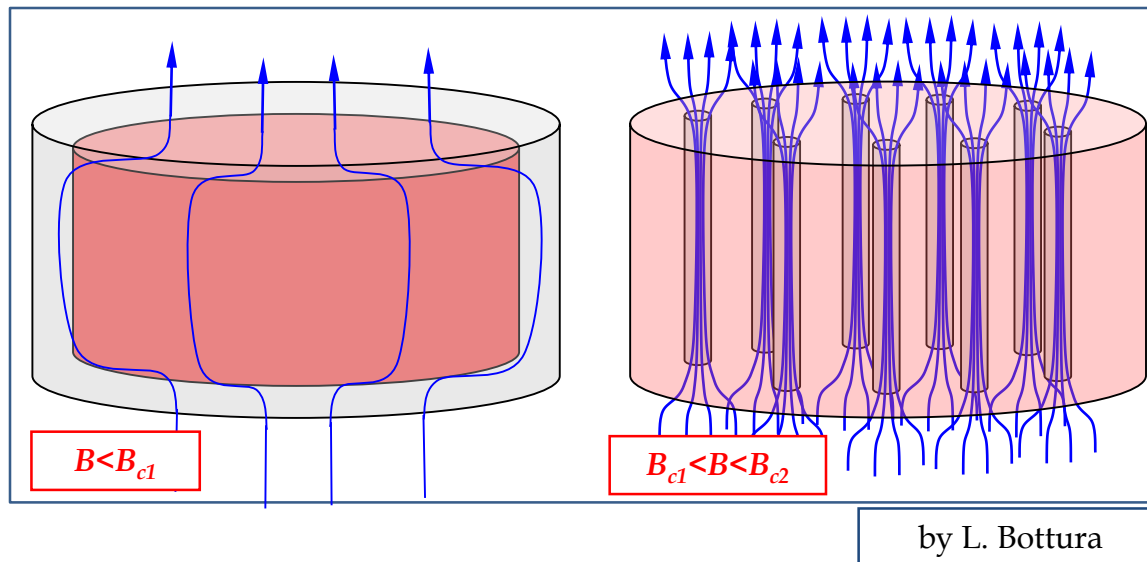
- Unfortunately, first discovered superconductors (**Type I**) with **very low  $B_c$**  ( $\leq 0.1$  T)
  - not practical for electro-magnets

Material	$T_c$ (K)	$\mu_0 H_0$ (mT)
Aluminum	1.2	9.9
Cadmium	0.52	3.0
Gallium	1.1	5.1
Indium	3.4	27.6
Iridium	0.11	1.6
Lanthanum $\alpha$	4.8	
$\beta$	4.9	
Lead	7.2	80.3
Lutecium	0.1	35.0
Mercury $\alpha$	4.2	41.3
$\beta$	4.0	34.0
Molybdenum	0.9	
Osmium	0.7	$\sim 6.3$
Rhenium	1.7	20.1
Rhodium	0.0003	4.9
Ruthenium	0.5	6.6
Tantalum	4.5	83.0
Thalium	2.4	17.1
Thorium	1.4	16.2
Tin	3.7	30.6
Titanium	0.4	
Tungsten	0.016	0.12
Uranium $\alpha$	0.6	
$\beta$	1.8	
Zinc	0.9	5.3
Zirconium	0.8	4.7

# Superconductivity

## Type II superconductors

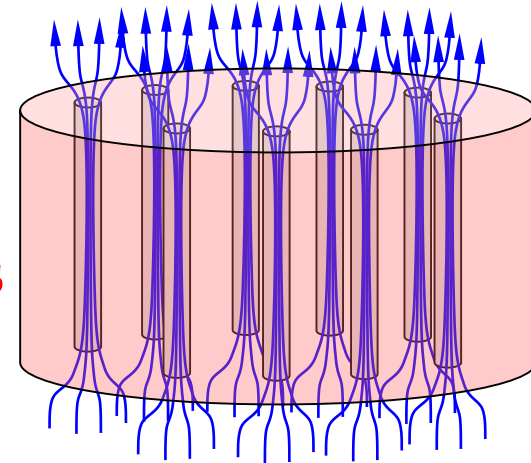
- So, for 40-50 years, superconductivity was a research activity
- Then, in the 50's, **type II superconductors**
  - Between  $B_{c1}$  and  $B_{c2}$ : mixed phase
    - $B$  penetrates as flux tubes: *fluxoids*
      - with a flux of  $\phi_0 = h/2e = 2 \cdot 10^{-15} \text{ Wb}$
- Much higher fields and link between  $T_c$  and  $B_{c2}$



# Superconductivity

## Hard superconductors

- ...but, if a current passes through the tubes
  - Lorentz force on the fluxoids:  $F_L = J \times B$
- The force causes a **motion** of tubes
  - Flux motion ( $dB/dt$ )  $\rightarrow$  (V)  $\rightarrow$  **dissipation** (VI)
- Fluxoids must be locked by **pinning centers**
  - Defects or impurities in the structure



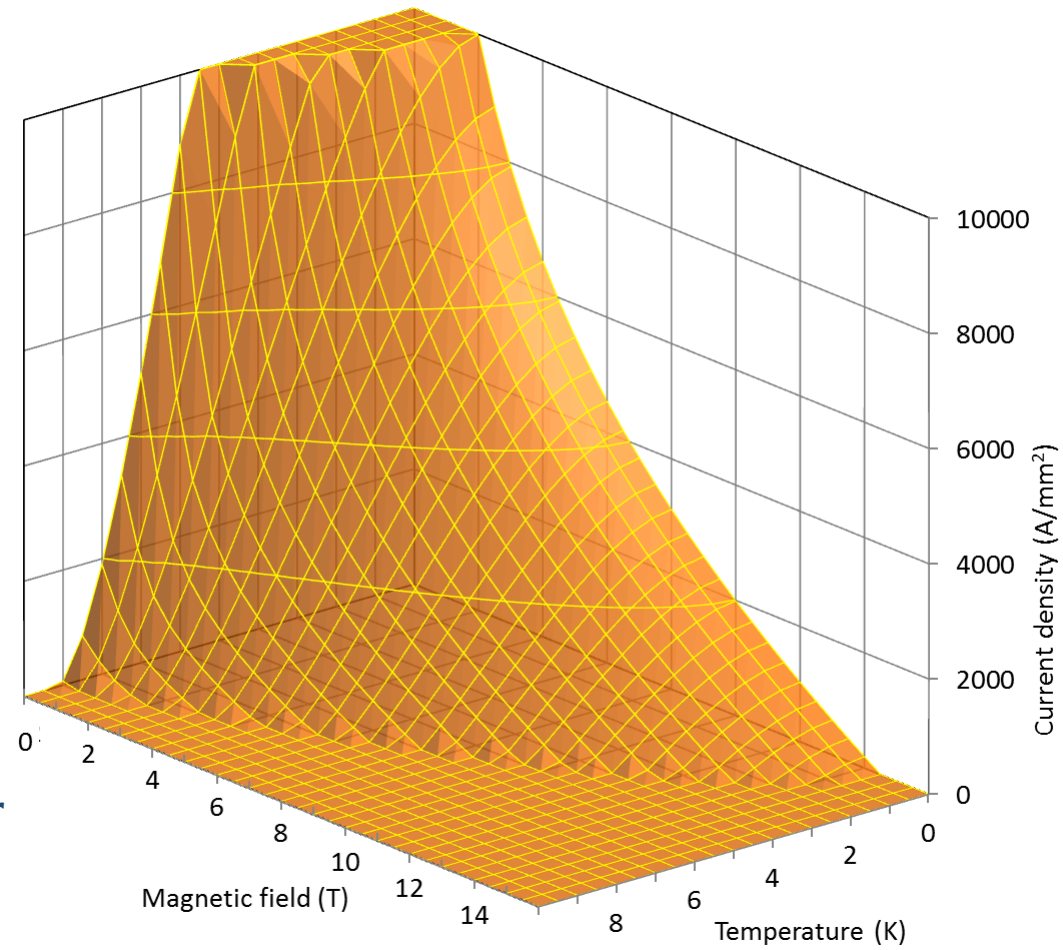
- The pinning centres exert a pinning force  $F_p$
- As long as  $F_p \leq J \times B$ 
  - No flux motions  $\rightarrow$  no dissipation
- $J_c$  is the current density at which, for a given  $B$  and at a given  $T$  the pinning force is exceeded by the Lorentz force



# Superconductivity

## Critical surface

- A type II material is supercond. below the **critical surface** defined by
  - Critical temperature  $T_c$ 
    - Property of the material
  - Upper critical field  $B_{c2}$ 
    - Property of the material
  - Critical current density  $J_c$ 
    - Hard work by the producer



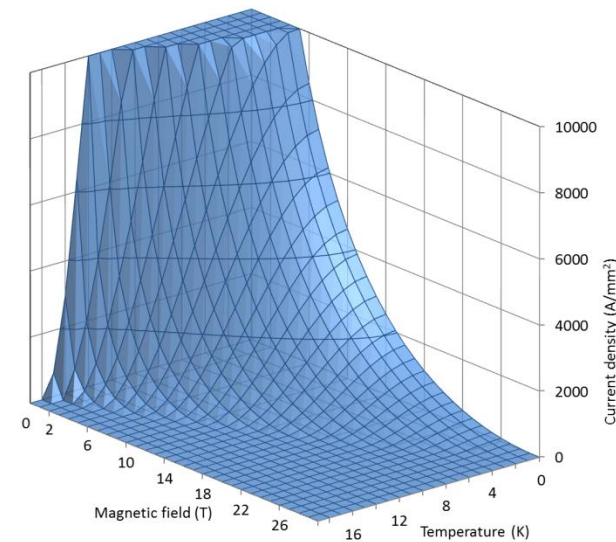
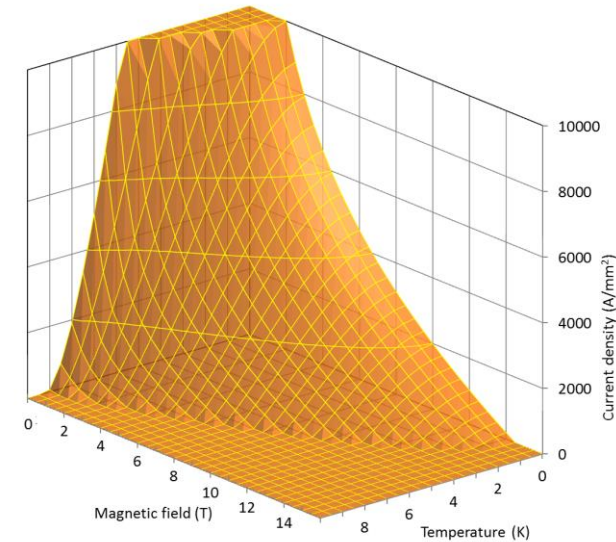




# Superconductivity

## Nb-Ti (1961) and Nb<sub>3</sub>Sn (1954)

- Nb and Ti → ductile alloy
  - Extrusion + drawing
  - $T_c$  is ~**9.2 K** at 0 T
  - $B_{C2}$  is ~**14.5 T** at 0 K
  - Firstly in **Tevatron** (80s), then all the other
  - ~50-200 US\$ per kg of wire (1 euro per m)
- Nb and Sn → intermetallic compound
  - Brittle, strain sensitive, formed at ~650-700°C
  - $T_c$  is ~**18 K** at 0 T
  - $B_{C2}$  is ~**28 T** at 0 K
  - Used in **NMR, ITER**
  - ~700-1500 US\$ per kg of wire (5 euro per m)

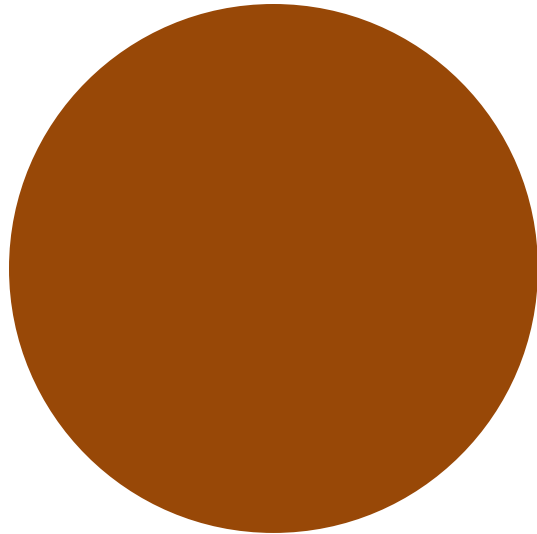




# Superconductivity from Cu to Nb<sub>3</sub>Sn

- Typical operational conditions (0.85 mm diameter strand)

Cu

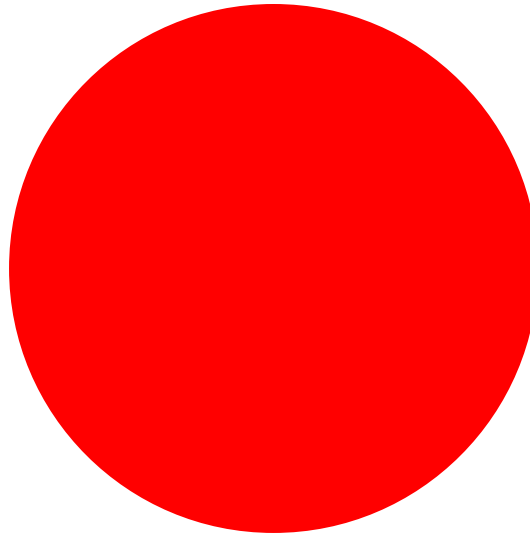


$$J_e \sim 5 \text{ A/mm}^2$$

$$I \sim 3 \text{ A}$$

$$B = 2 \text{ T}$$

Nb-Ti

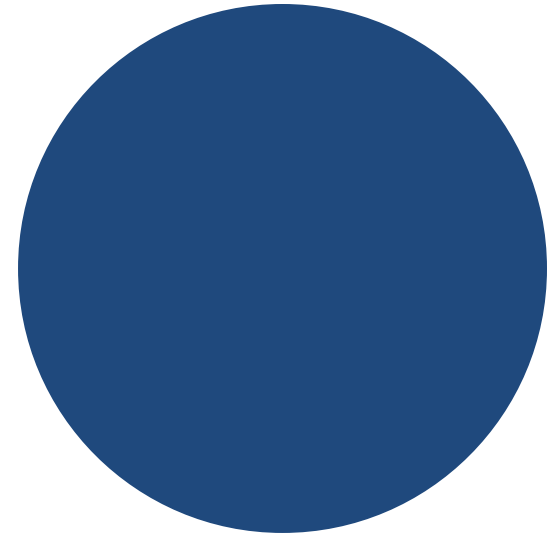


$$J_e \sim 600\text{-}700 \text{ A/mm}^2$$

$$I \sim 300\text{-}400 \text{ A}$$

$$B = 8\text{-}9 \text{ T}$$

Nb<sub>3</sub>Sn



$$J_e \sim 600\text{-}700 \text{ A/mm}^2$$

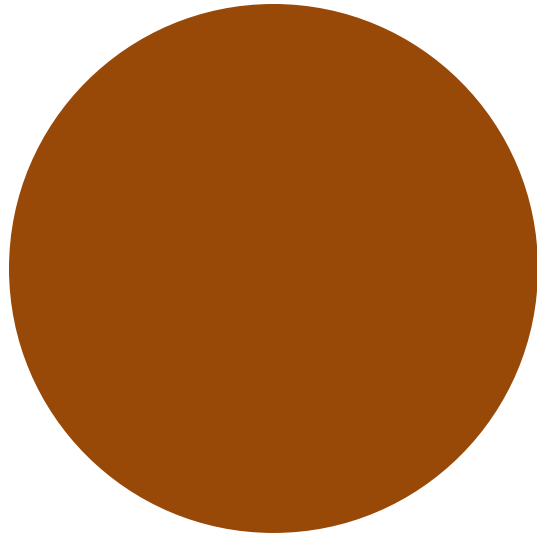
$$I \sim 300\text{-}400 \text{ A}$$

$$B = 12\text{-}13 \text{ T}$$

# Practical superconductors

- Typical operational conditions (0.85 mm diameter strand)

Cu

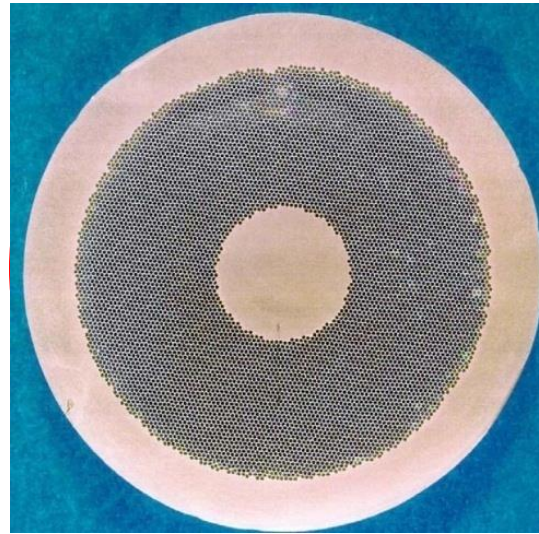


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Nb-Ti

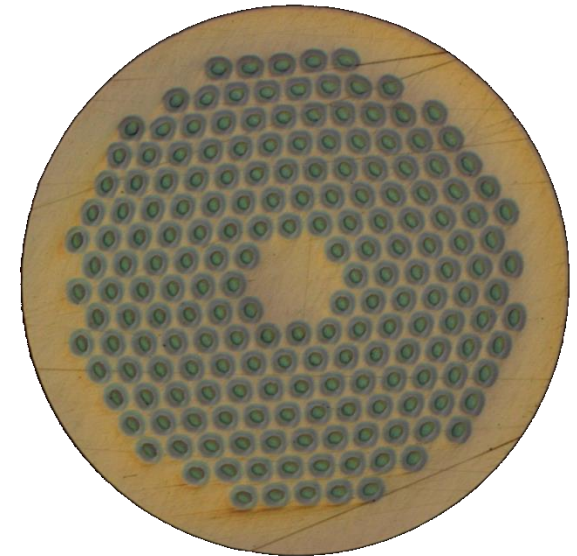


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Nb<sub>3</sub>Sn



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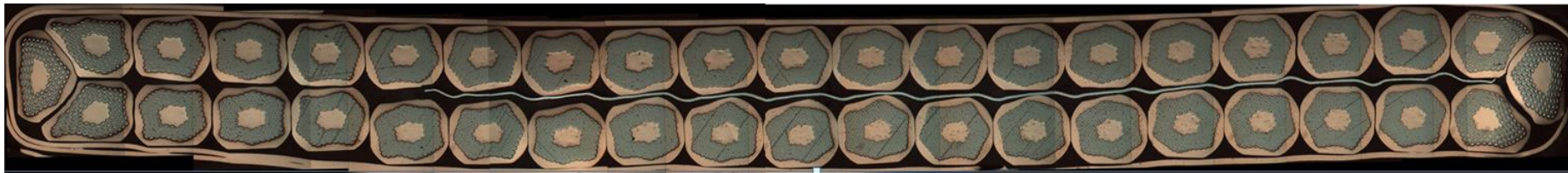
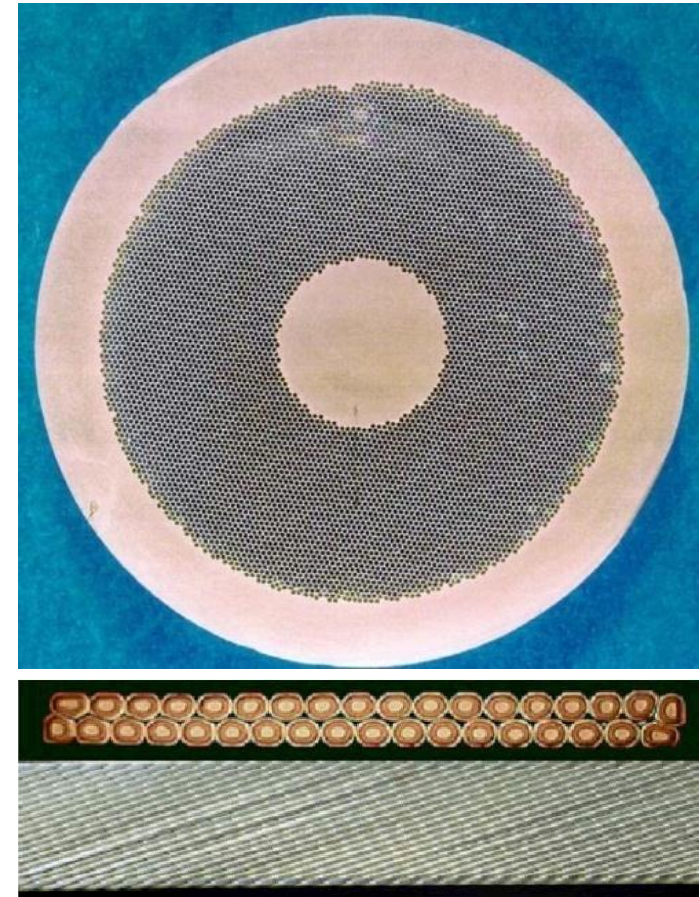




# Practical superconductors

## Introduction

- Superconducting materials are produced in small filaments and surrounded by a stabilizer (typically copper) to form a *multi-filament wire* or *strand*.
- A superconducting cable is composed by several wires: *multi-strand cable*.





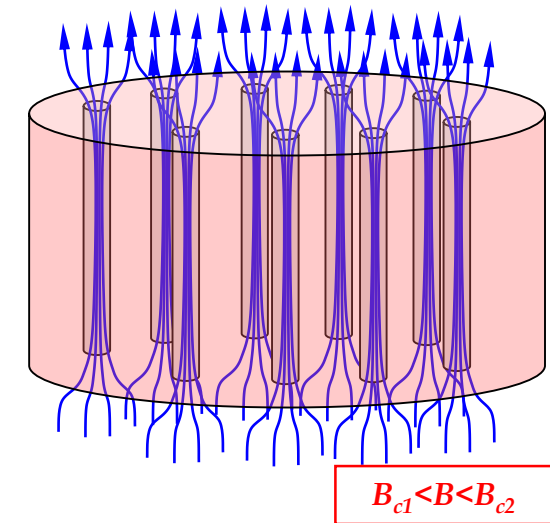
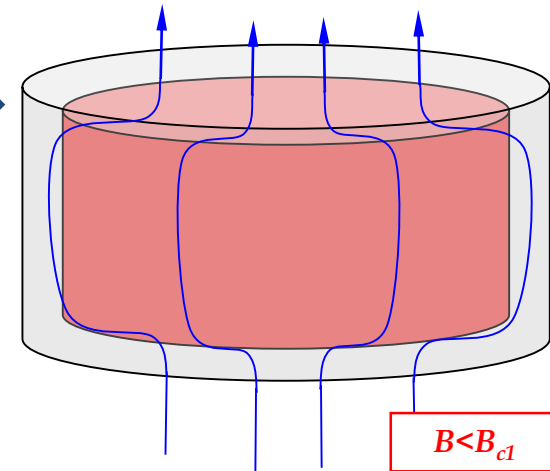
# Practical superconductors

## Multi-filament wires motivations

- Fluxoid distribution depends on  $B$  and  $J_c$
- Thermal disturbance  $\rightarrow$  the local change in  $J_c \rightarrow$  motion or “**flux jump**”  $\rightarrow$  power dissipation
- Stability criteria for a slab (adiabatic condition)

$$a \leq \sqrt{\frac{3\gamma C(\theta_c - \theta_0)}{\mu_0 j_c^2}}$$

- $a$  is the half-thickness of the slab
  - $j_c$  is the critical current density [ $\text{A m}^{-2}$ ]
  - $\gamma$  is the density [ $\text{kg m}^{-3}$ ]
  - $C$  is the specific heat [ $\text{J kg}^{-1}$ ]
  - $\theta_c$  is the critical temperature.
- Filament diameters usually  $< 50 \mu\text{m}$



by L. Bottura

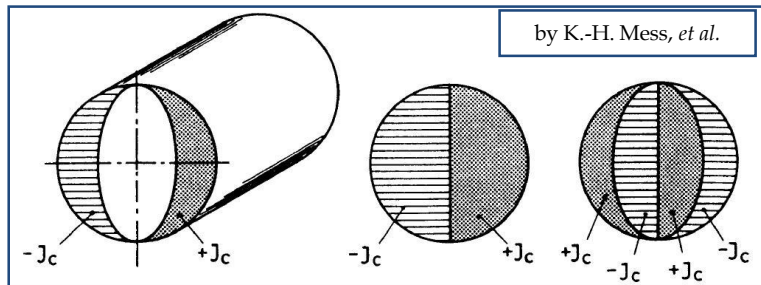


# Practical superconductors

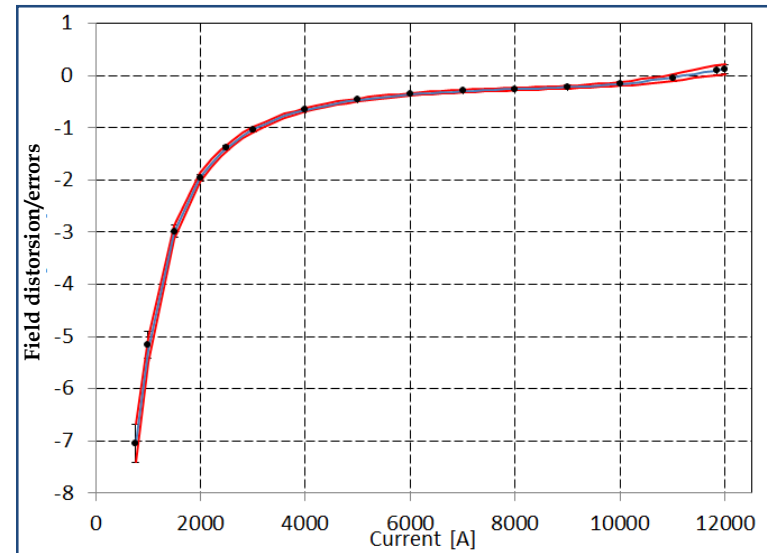
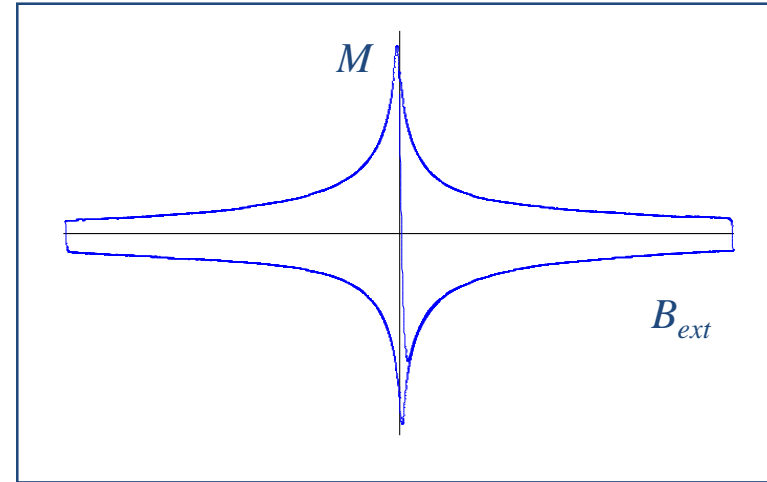
## Multi-filament wires motivations

### Superconductor magnetization

- When a filament is in a varying  $B_{ext}$ , its inner part is shielded by currents distribution in the filament periphery
  - They **do not decay** when  $B_{ex}$  is held constant  $\rightarrow$  **persistent currents**



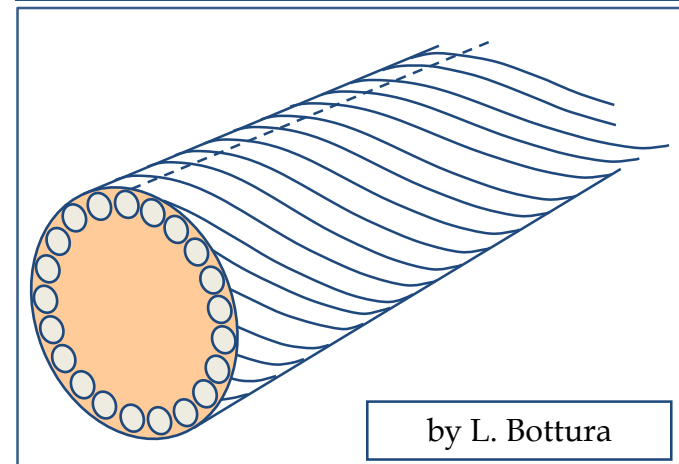
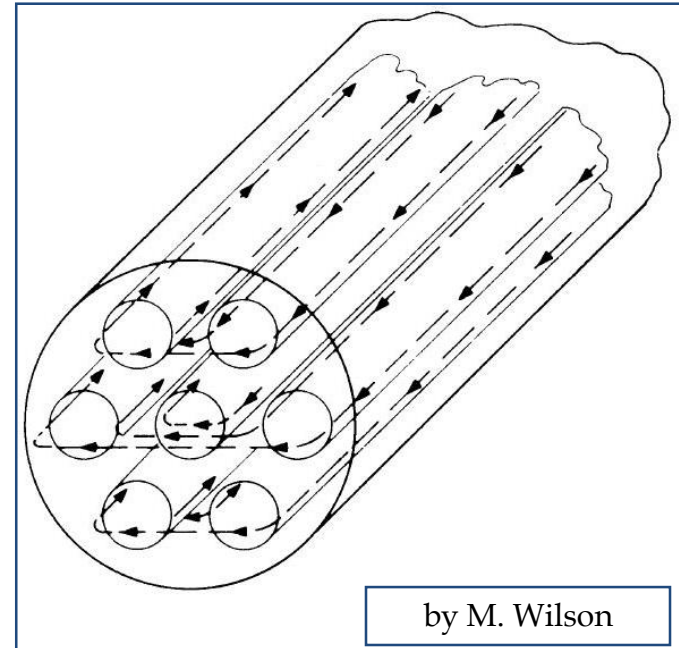
- These currents produce **field errors** and **ac losses** proportional to  $J_c r_f$ 
  - LHC filament diameter 6-7  $\mu\text{m}$ .
  - HERA filament diameter 14  $\mu\text{m}$ .



# Practical superconductors

## Multi-filament wires motivations

- **Inter-filament coupling**
  - When a multi-filamentary wire is subjected to a time varying magnetic field, **current loops** are generated between filaments.
  - If filaments are straight, large loops with large currents → **ac losses**
  - If the strands are magnetically coupled the effective filament size is larger → **flux jumps**
- To reduce these effects, filaments are **twisted**
  - twist pitch of the order of 20-30 times of the wire diameter.

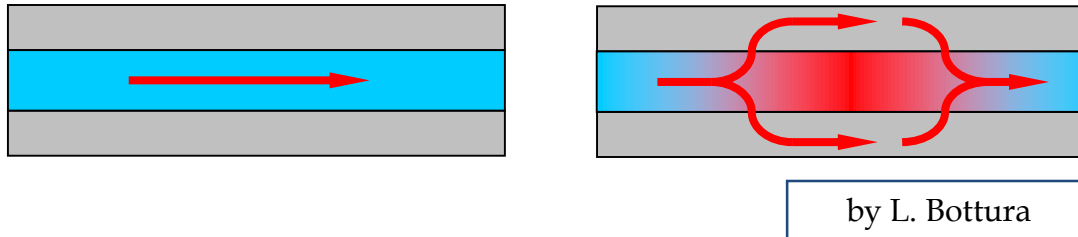


# Practical superconductors

## Multi-filament wires motivations

- **Quench protection**

- Superconductors have a very high normal state resistivity
  - If quenched, could reach very high temperatures in few ms.
- If embedded in a **copper matrix**, when a quench occurs, current redistributes in the low-resistivity matrix → **lower peak temperature**



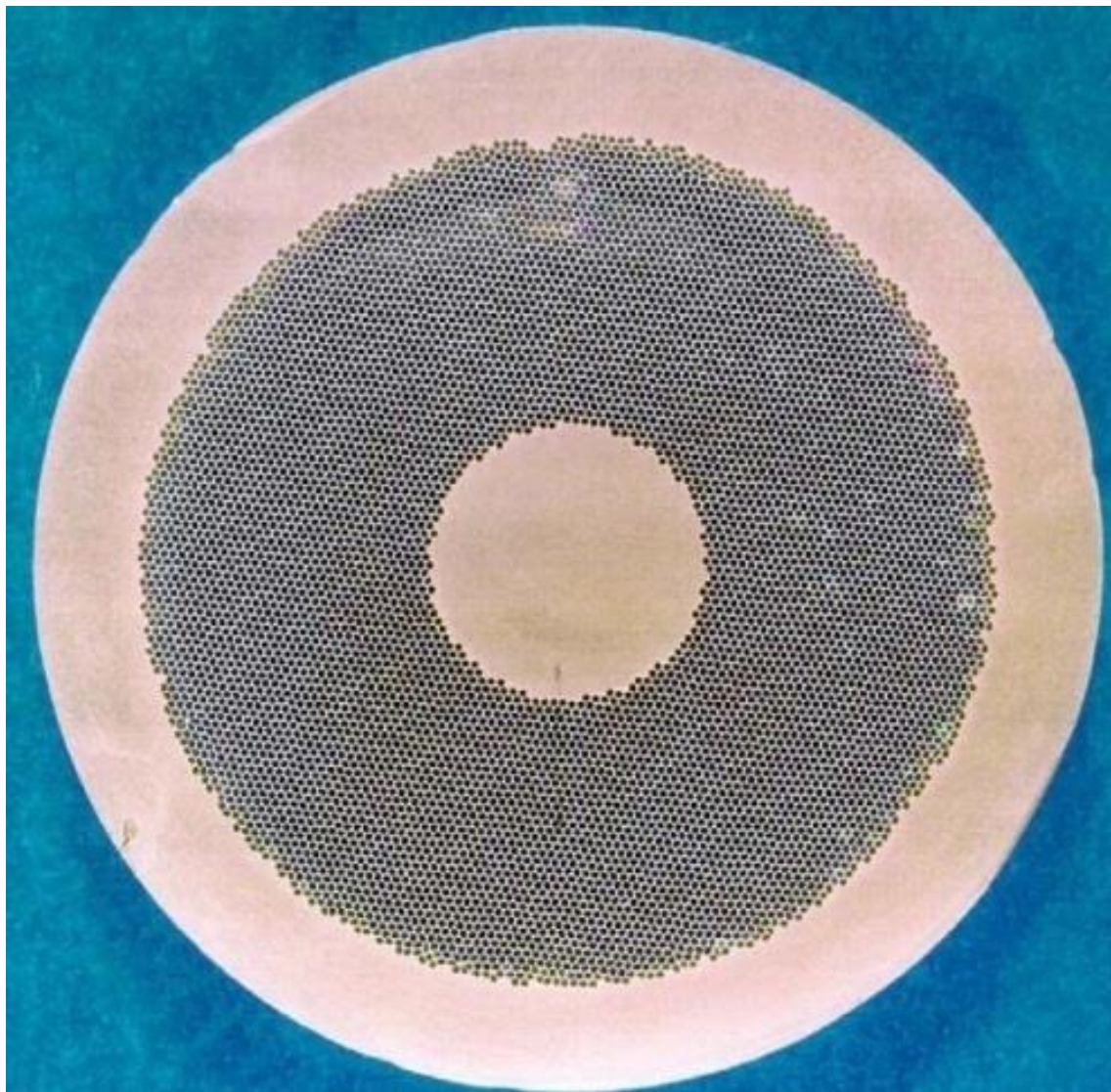
- The copper matrix provides **time to act** on the power circuit
- In the case of a small volume of superconductor heated beyond the critical temperature the current can flow in the copper for a short moment, allowing the filament to **cool-down and recover** supercond.
- The matrix also helps stabilizing the conductor against **flux jumps**



# Practical superconductors

## Multi-filament wires motivations

- **Flux jumps**
- **Persistent currents**
- **AC losses**
- **Quench protection**







# Practical superconductors

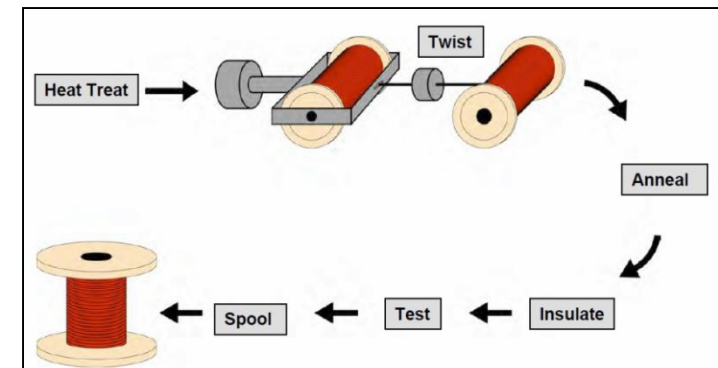
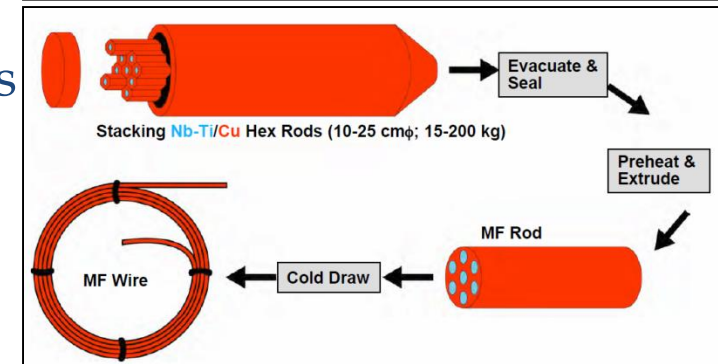
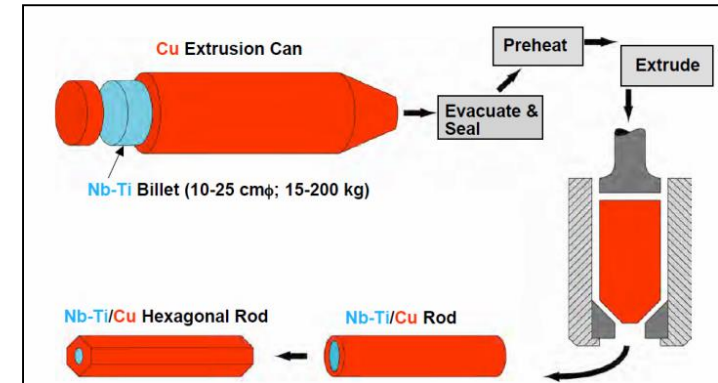
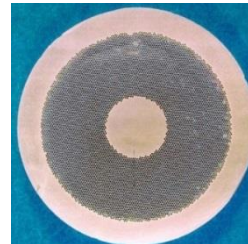
## Fabrication of Nb-Ti multifilament wires

### Nb-Ti ingots

- 200 mm  $\phi$ , 750 mm long

### Monofilament rods are stacked to form a multifilament billet

- then extruded and drawn down
- can be re-stacked: double-stacking process

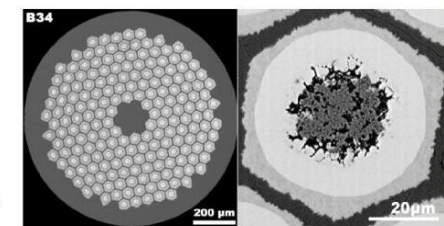
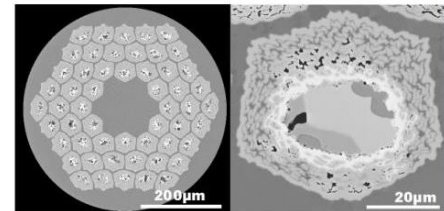
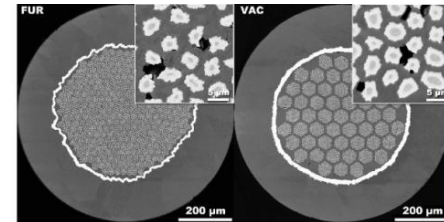
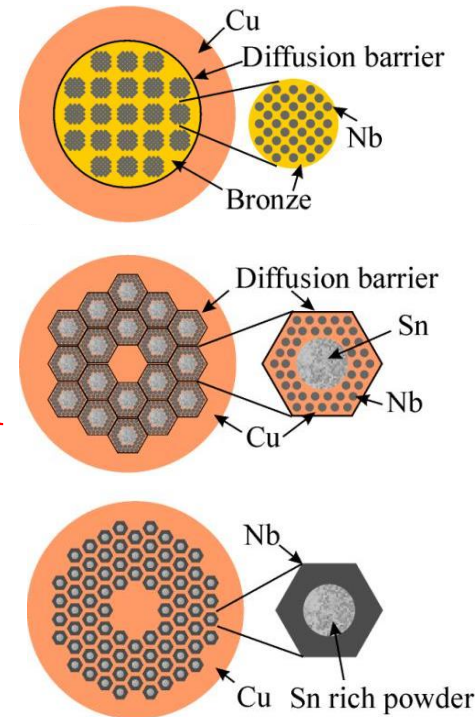




# Multifilament wires

## Fabrication of Nb<sub>3</sub>Sn multifilament wires

- Since Nb<sub>3</sub>Sn is brittle
  - it cannot be extruded and drawn like Nb-Ti.
- Process in several steps
  - Assembly multifilament billets from with **Nb and Sn separated**
  - Fabrication of the wire through extrusion-drawing
    - Fabrication of the cable
    - Fabrication of the coil
  - **“Reaction”**
    - Sn and Nb are heated to 600-700 C
    - Sn diffuses in Nb and reacts to form Nb<sub>3</sub>Sn



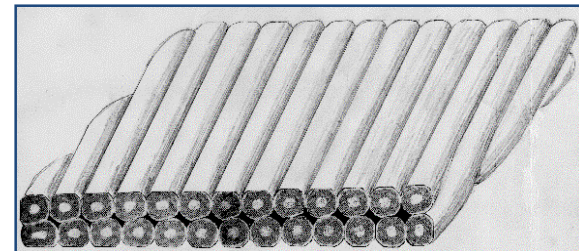
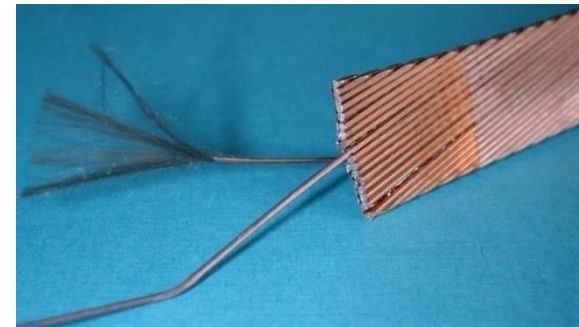
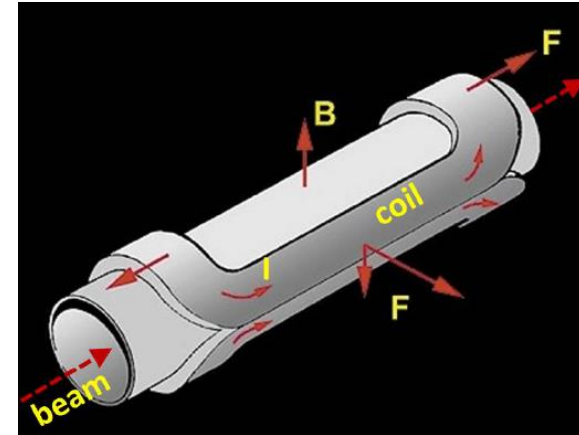
by A. Godeke



# Practical superconductors

## Multi-strand cables motivations

- Most of the superconducting coils for particle accelerators wound from a multi-strand cable (**Rutherford cable**)
  - Reduction of strand **piece length**
  - reduction of **number of turns**
    - easy winding
    - smaller coil inductance
      - less V for power supply during ramp-up;
      - after a quench, faster discharge and V
  - **current redistribution** in case of a defect or a quench in one strand
- The strands are **twisted** to
  - Reduce **inter-strand coupling currents**
    - Losses and field distortions
  - Provide more **mechanical stability**

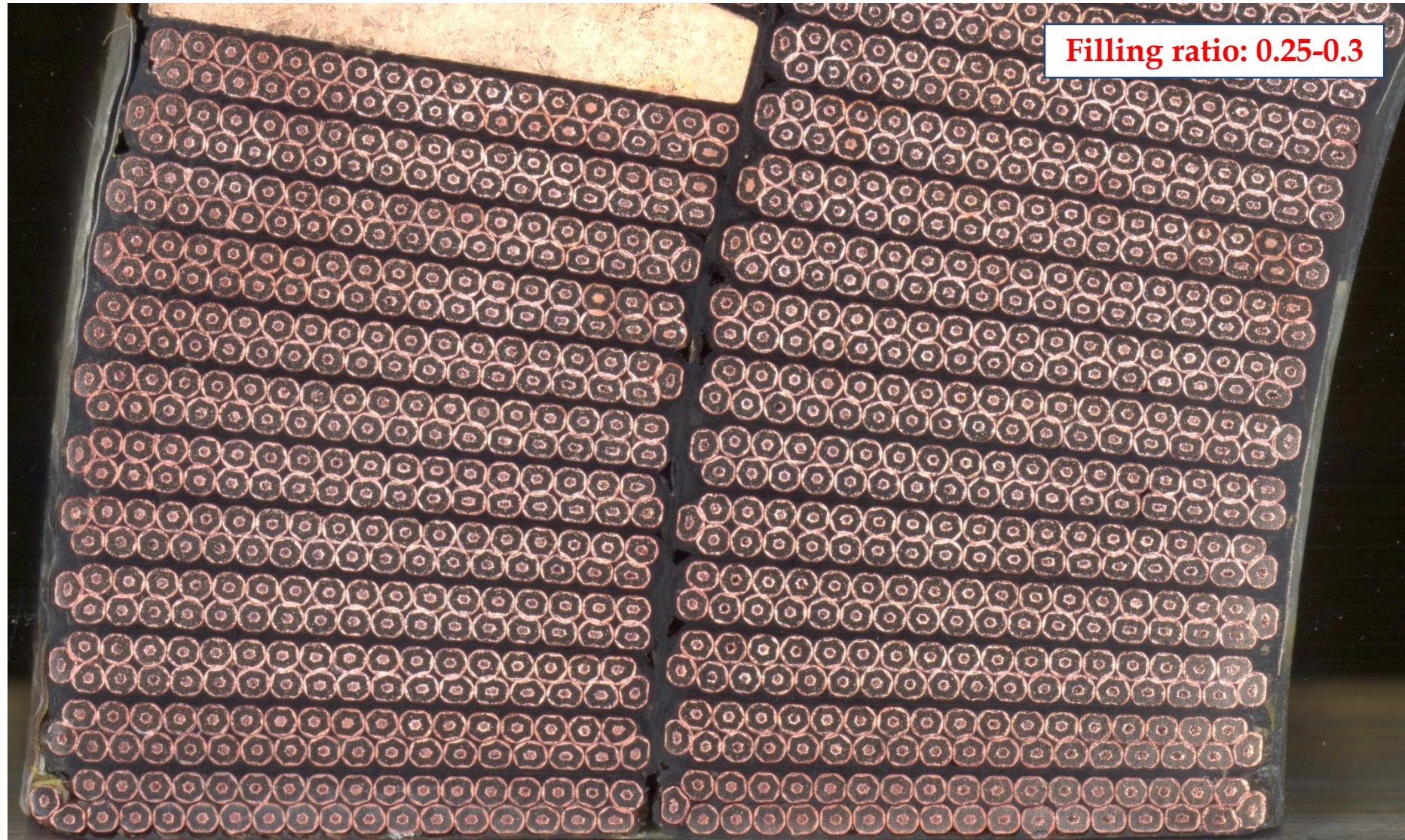


by M. Wilson



# Practical superconductors

## Superconducting cables



Filling ratio: 0.25-0.3





# Outline

- Particle accelerators and superconductors
- **Magnetic design and coils**
- Mechanics of superconducting magnets
- Quench and protection
- HiLumi LHC and FCC



# References

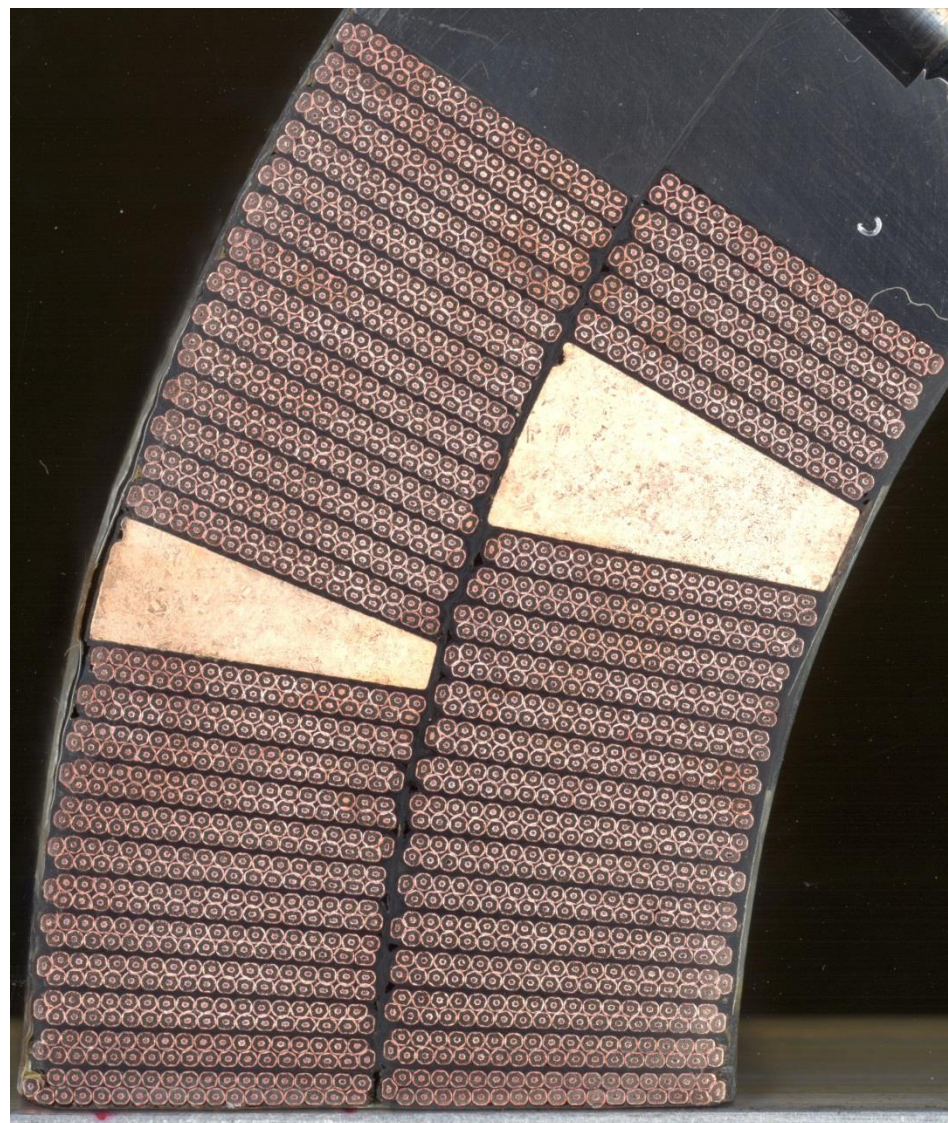
## ● **Magnetic design and coils**

- K.-H. Mess, P. Schmuser, S. Wolff, "*Superconducting accelerator magnets*", Singapore: World Scientific, 1996.
- Martin N. Wilson, "*Superconducting Magnets*", 1983.
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  - Units 5, 8, 9 by E. Todesco
- A. Jain, "*Basic theory of magnets*", CERN 98-05 (1998) 1-26
  
- L. Rossi, E. Todesco, "*Electromagnetic design of superconducting quadrupoles*", Phys. Rev. ST Accel. Beams 10 (2007) 112401.
- L. Rossi and Ezio Todesco, "*Electromagnetic design of superconducting dipoles based on sector coils*", Phys. Rev. ST Accel. Beams 9 (2006) 102401.



# Magnetic design and coils

- How do we create a **perfect field**?
- How do we **express** field and its “**imperfections**”?
- How do we design a coil to **minimize field errors**?
- How do we **fabricate** a coil?

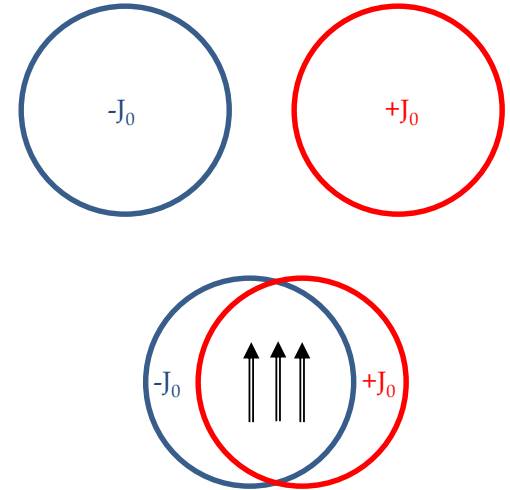


# Perfect dipole field

## Intercepting circles (or ellipses)

- Within a cylinder carrying  $j_0$ , the field is perpendicular to the radial direction and proportional to the distance to the centre  $r$ :

$$B = -\frac{\mu_0 j_0 r}{2}$$

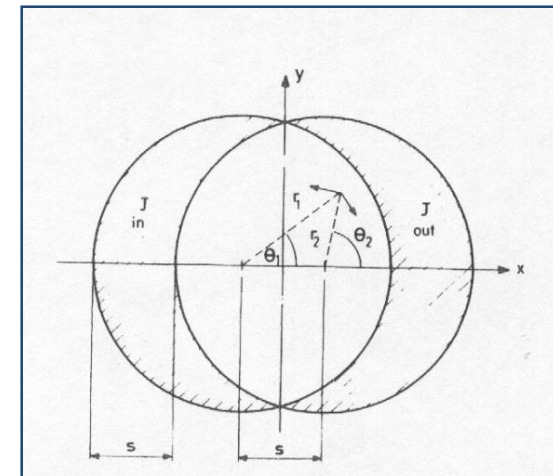


- Combining the effect of two intersecting cylinders

$$B_x = \frac{\mu_0 j_0 r}{2} \{-r_1 \sin \theta_1 + r_2 \sin \theta_2\} = 0$$

$$B_y = \frac{\mu_0 j_0 r}{2} \{-r_1 \cos \theta_1 + r_2 \cos \theta_2\} = -\frac{\mu_0 j_0}{2} s$$

- A uniform current density in the area of two **intersecting circles** produces a pure dipole
  - The aperture is not circular
  - Not easy to simulate with a flat cable
- Similar proof for **intersecting ellipses**



by M. Wilson



# Perfect dipole field

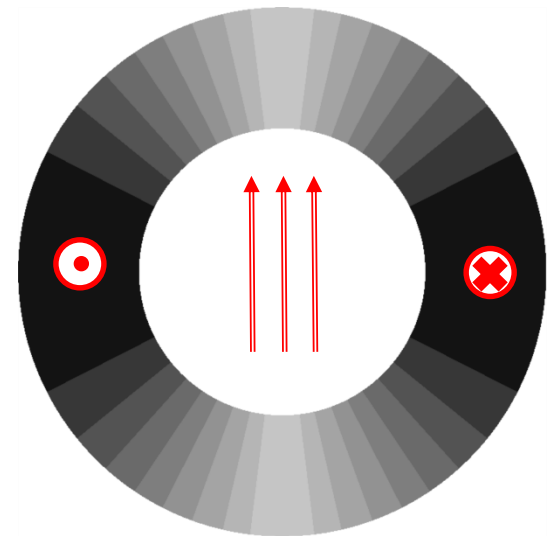
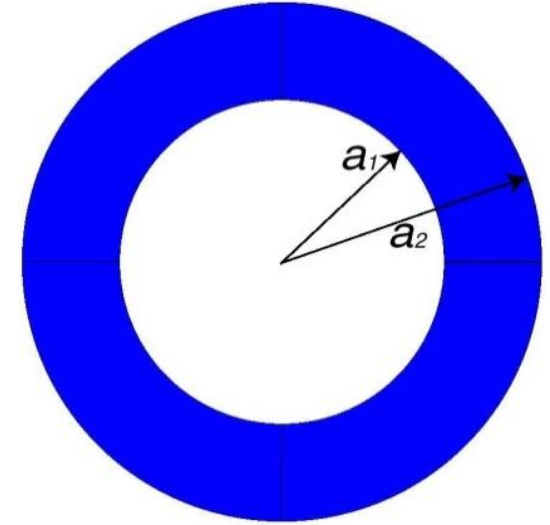
## Thick shell with $\cos\theta$ current distribution

- If we assume
  - $J = J_0 \cos\theta$  where  $J_0$  [A/m<sup>2</sup>] is  $\perp$  to the cross-section plane
  - Inner (outer) radius of the coils =  $a_1$  ( $a_2$ )

- The generated field is a **pure dipole**

$$B_y = -\frac{\mu_0 J_0}{2} (a_2 - a_1)$$

- Linear dependence on **coil width**
- **Easier** to achieve with a Rutherford cable

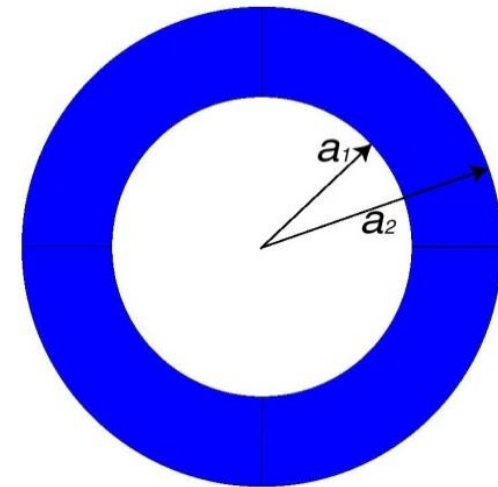
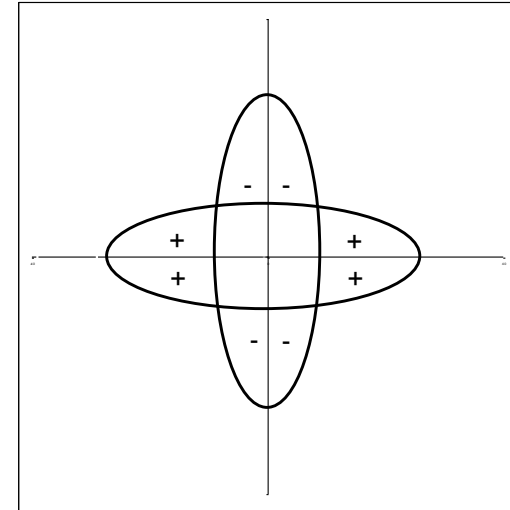


# Perfect quadrupole field

- **Intercepting ellipses or circles**
- Thick shell with  **$\cos 2\theta$  current distribution**
- If we assume
  - $J = J_0 \cos 2\theta$  where  $J_0$  [A/m<sup>2</sup>] is  $\perp$  to the cross-section plane
  - Inner (outer) radius of the coils =  $a_1$  ( $a_2$ )

$$G = \frac{B_y}{r} = -\frac{\mu_0 J_0}{2} \ln \frac{a_2}{a_1}$$

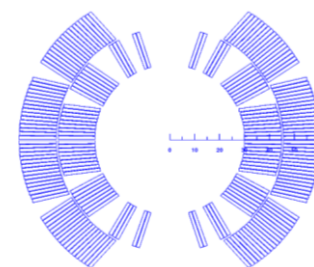
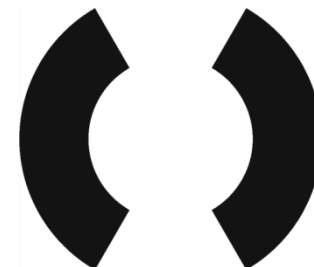
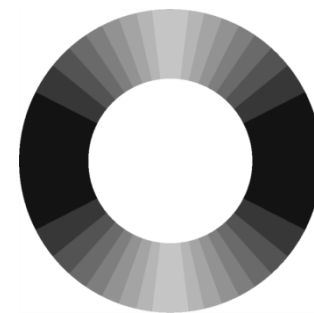
- And so on...
  - Perfect sextupoles:  **$\cos 3\theta$**  or **3** intersect. ellipses
  - Perfect  $2n$ -poles:  **$\cos n\theta$**  or  **$n$**  intersecting ellipses





# From ideal to practical configuration

- How can I reproduce **thick shell with a  $\cos\theta$**  distribution with a cable?
  - Rectangular cross-section and constant  $J$
- First “rough” approximation
  - **Sector dipole**
- Better ones
  - More **layers** and **wedges** to reduce  $J$  towards  $90^\circ$
- As a result, the field is **not perfect** anymore
  - How can I express in improve the “imperfect” field inside the aperture?





# Field representation

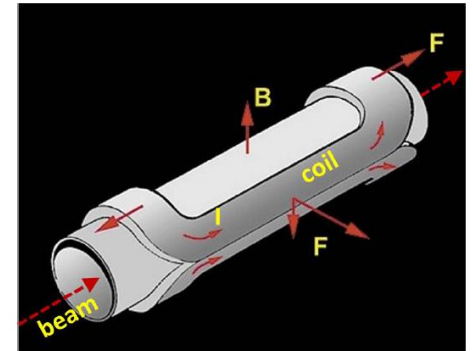
## Maxwell equations

- **Maxwell equations** for magnetic field

$$\nabla \cdot \mathbf{B} = \frac{\partial B_x}{\partial x} + \frac{\partial B_y}{\partial y} + \frac{\partial B_z}{\partial z} = 0 \quad \nabla \times \mathbf{B} = \mu_0 \mathbf{J} + \mu_0 \epsilon_0 \frac{\partial \mathbf{E}}{\partial t}$$

- In absence of charge and magnetized material

$$\nabla \times \mathbf{B} = \left( \frac{\partial B_y}{\partial z} - \frac{\partial B_z}{\partial y}, \frac{\partial B_z}{\partial x} - \frac{\partial B_x}{\partial z}, \frac{\partial B_x}{\partial y} - \frac{\partial B_y}{\partial x} \right) = 0$$



- If  $\frac{\partial B_z}{\partial z} = 0$  (constant longitudinal field), then

$$\frac{\partial B_x}{\partial x} + \frac{\partial B_y}{\partial y} = 0 \quad \frac{\partial B_x}{\partial y} - \frac{\partial B_y}{\partial x} = 0$$



# Field representation

## Analytic functions

- If  $\frac{\partial B_z}{\partial z} = 0$

Maxwell gives

$$\frac{\partial B_y}{\partial x} - \frac{\partial B_x}{\partial y} = 0$$

$$\frac{\partial B_y}{\partial y} + \frac{\partial B_x}{\partial x} = 0$$

$$\begin{cases} \frac{\partial f_x}{\partial x} - \frac{\partial f_y}{\partial y} = 0 \\ \frac{\partial f_x}{\partial y} + \frac{\partial f_y}{\partial x} = 0 \end{cases}$$

**Cauchy-Riemann conditions**

and therefore the function  $B_y + iB_x$  is analytic

$$B_y(x, y) + iB_x(x, y) = \sum_{n=1}^{\infty} C_n (x + iy)^{n-1}$$

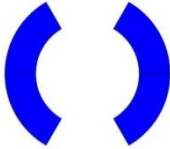
where  $C_n$  are **complex coefficients**

$$B_y(x, y) + iB_x(x, y) = \sum_{n=1}^{\infty} C_n (x + iy)^{n-1} = \sum_{n=1}^{\infty} (B_n + iA_n) (x + iy)^{n-1}$$

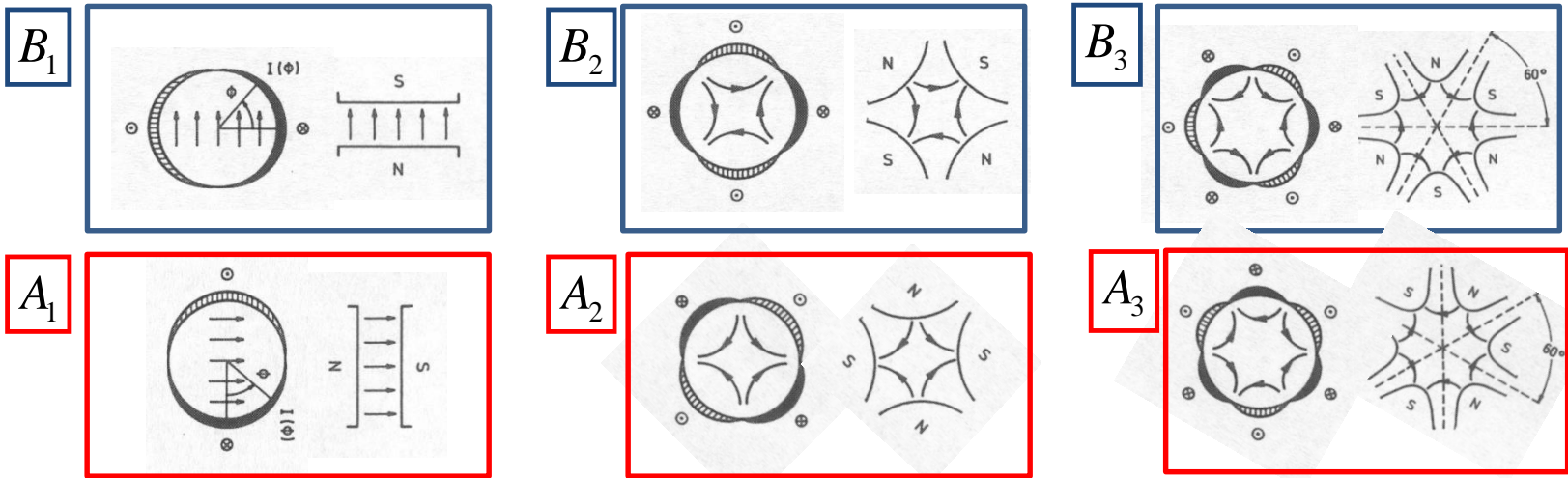
- Advantage: we reduce the description of the field to a (simple) series of complex coefficients

# Magnetic design Harmonics

- The field can be expressed as (simple) series of coefficients
- So, each coefficient corresponds to a “pure” multipolar field



$$B_y(x, y) + iB_x(x, y) = \sum_{n=1}^{\infty} C_n(x + iy) = \sum_{n=1}^{\infty} (B_n + iA_n)(x + iy)$$



- The field harmonics are rewritten as

by K.-H. Mess, *et al.*

$$B_y + iB_x = 10^{-4} B_1 \sum_{n=1}^{\infty} (b_n + ia_n) \left( \frac{x + iy}{R_{ref}} \right)^{n-1}$$

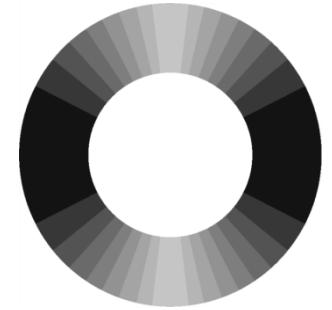
- The coefficients  $b_n, a_n$  are called **normalized multipoles**
  - $b_n$  are the **normal**,  $a_n$  are the **skew** (adimensional)



# Back to the original issue: From ideal to practical configuration

- How can I reproduce **thick shell with a  $\cos\theta$**  distribution with a cable?

- Rectangular cross-section and constant  $J$



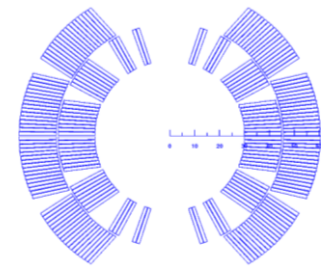
- First “rough” approximation

- **Sector dipole**



- Better ones

- More **layers** and **wedges** to reduce  $J$  towards  $90^\circ$



- Now, I can use the multipolar expansion to **optimize** my “practical” **cross-section**



# A “good” field quality dipole Sector dipole

- We compute the central field given by a **sector dipole with 2 blocks**

- Equations to set to zero  $B_3, B_5$  and  $B_7$

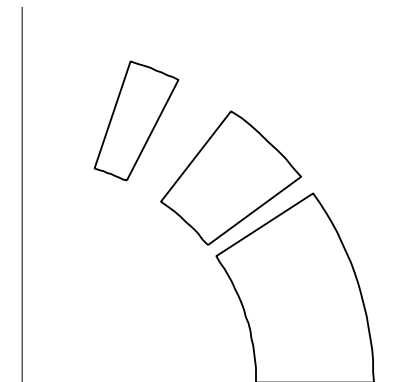
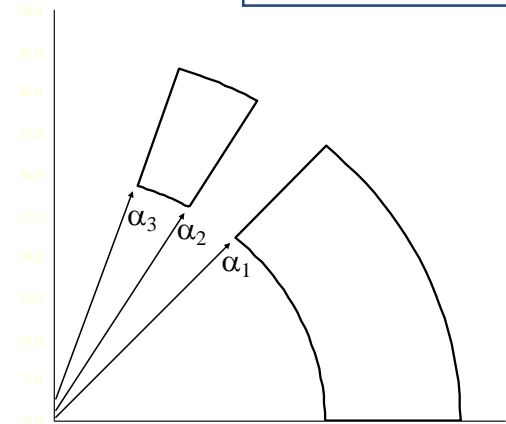
$$\begin{cases} \sin(3\alpha_3) - \sin(3\alpha_2) + \sin(3\alpha_1) = 0 \\ \sin(5\alpha_3) - \sin(5\alpha_2) + \sin(5\alpha_1) = 0 \end{cases}$$

- And the one given by a **3 blocks**

- Equations to set to zero  $B_3, B_5, B_7, B_9$  and  $B_{11}$

$$\begin{aligned} \sin(3\alpha_5) - \sin(3\alpha_4) + \sin(3\alpha_3) - \sin(3\alpha_2) + \sin(3\alpha_1) &= 0 \\ \sin(5\alpha_5) - \sin(5\alpha_4) + \sin(5\alpha_3) - \sin(5\alpha_2) + \sin(5\alpha_1) &= 0 \\ \sin(7\alpha_5) - \sin(7\alpha_4) + \sin(7\alpha_3) - \sin(7\alpha_2) + \sin(7\alpha_1) &= 0 \\ \sin(9\alpha_5) - \sin(9\alpha_4) + \sin(9\alpha_3) - \sin(9\alpha_2) + \sin(9\alpha_1) &= 0 \\ \sin(11\alpha_5) - \sin(11\alpha_4) + \sin(11\alpha_3) - \sin(11\alpha_2) + \sin(11\alpha_1) &= 0 \end{aligned}$$

by E. Todesco



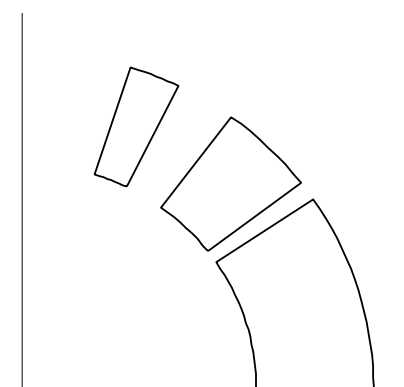
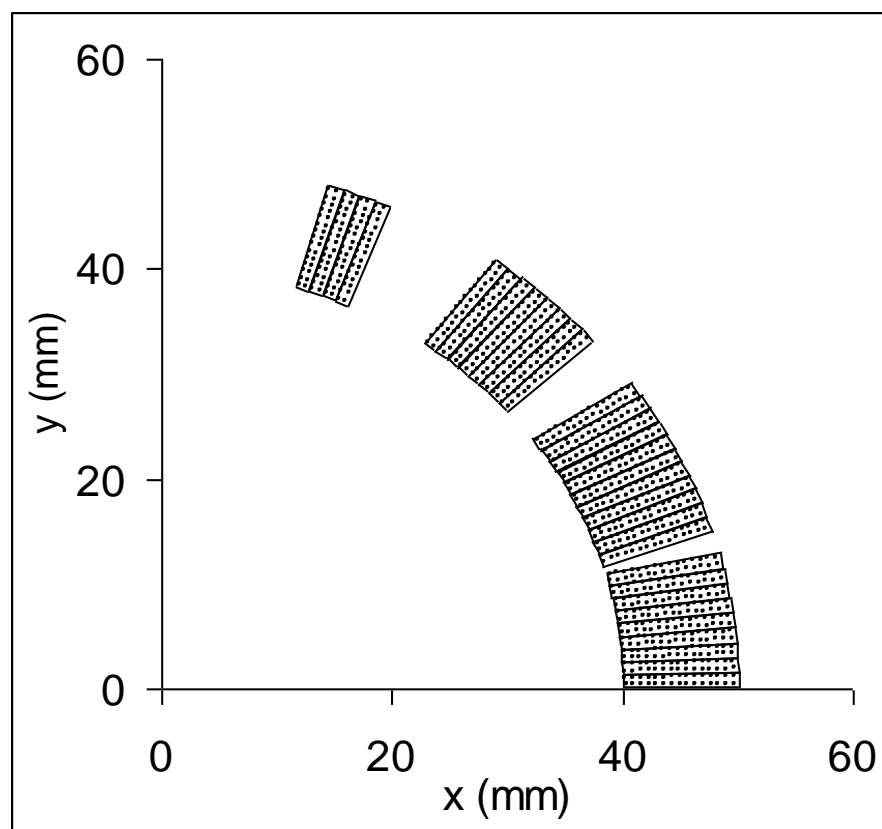
Two wedges,  $b_3=b_5=b_7=b_9=b_{11}=0$   
[0°-33.3°, 37.1°-53.1°, 63.4°- 71.8°]





# A “good” field quality dipole Sector dipole

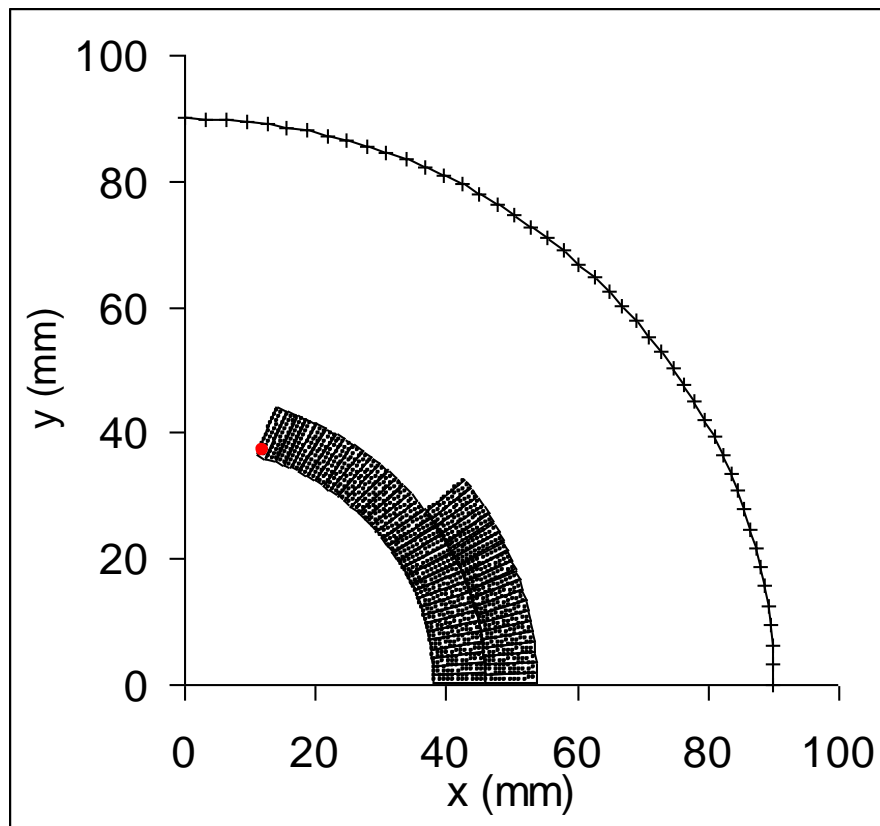
- Let us see two coil lay-outs of real magnets
  - The **RHIC dipole** has **four blocks**



Two wedges,  $b_3=b_5=b_7=b_9=b_{11}=0$   
[0°-33.3°, 37.1°-53.1°, 63.4°- 71.8°]

# A review of dipole lay-outs

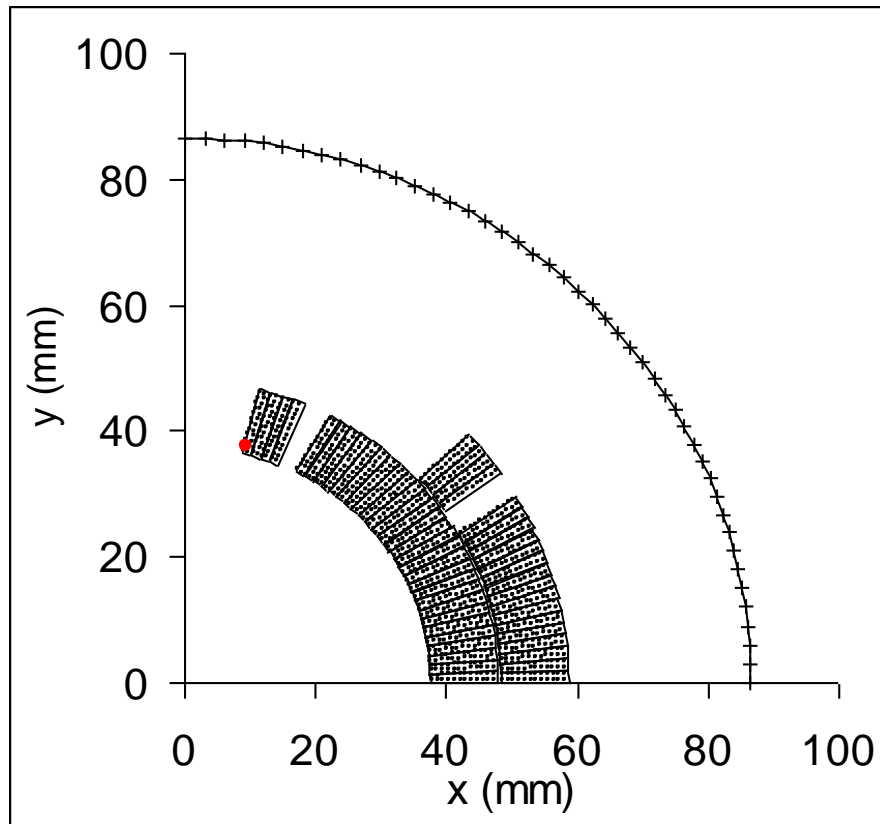
- Tevatron MB





# A review of dipole lay-outs

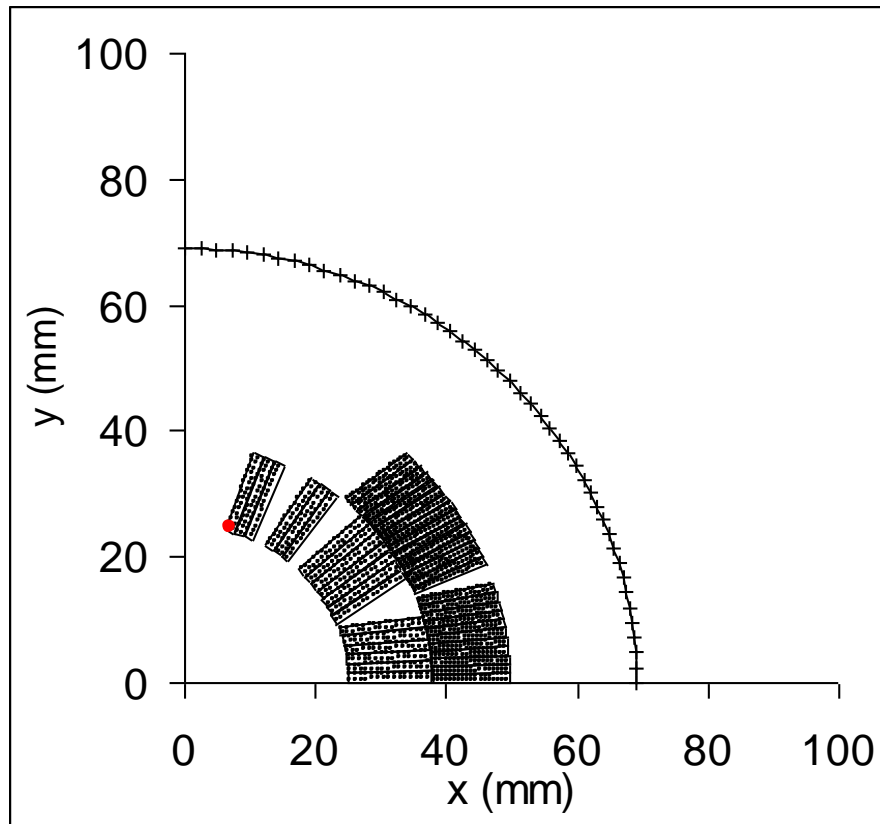
- HERA MB





# A review of dipole lay-outs

- SSC MB

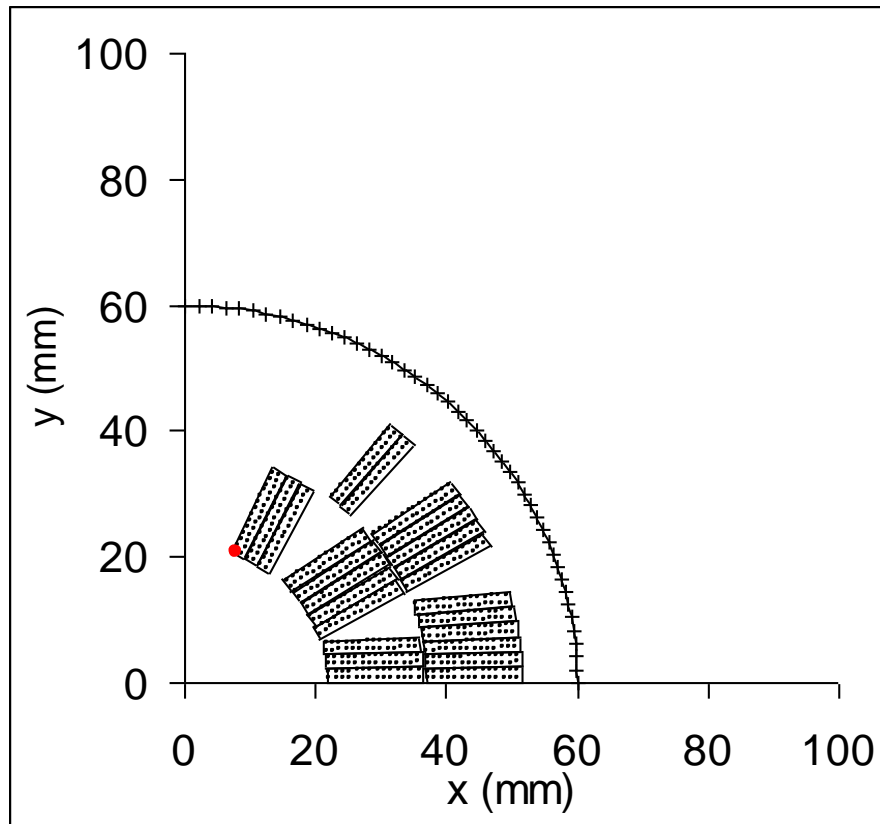






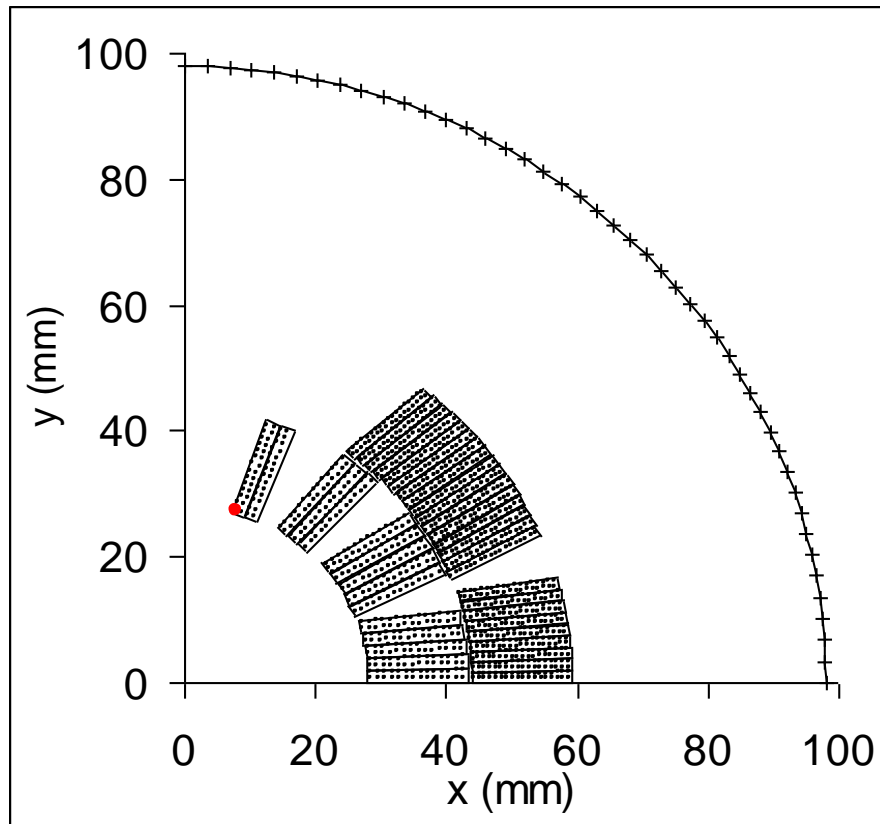
# A review of dipole lay-outs

- HFDA dipole



# A review of dipole lay-outs

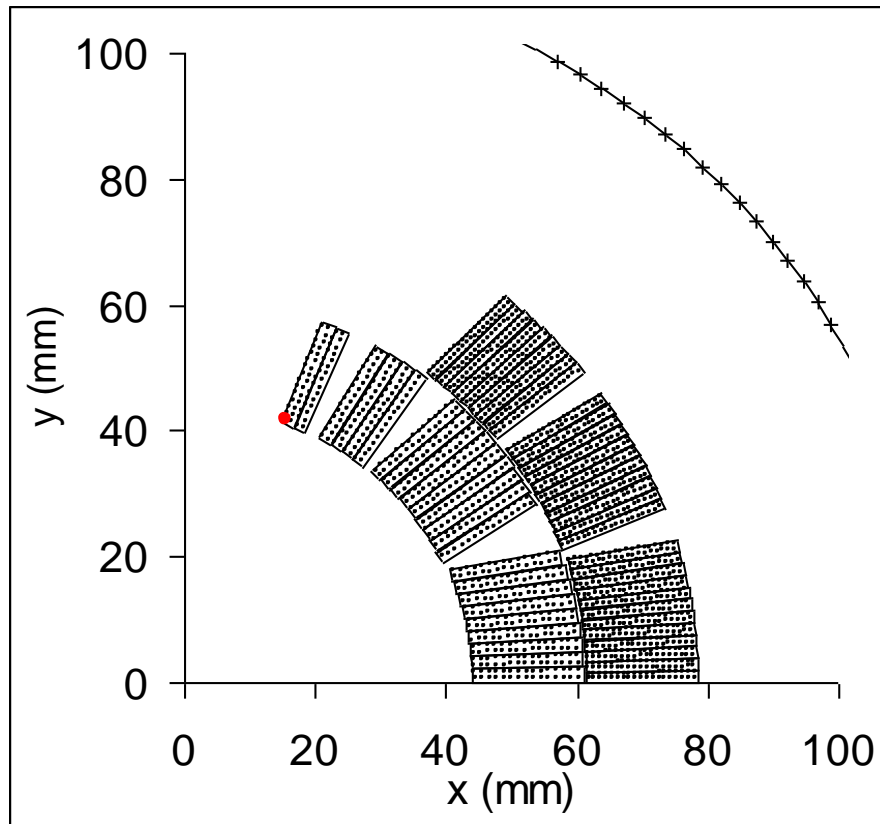
- LHC MB





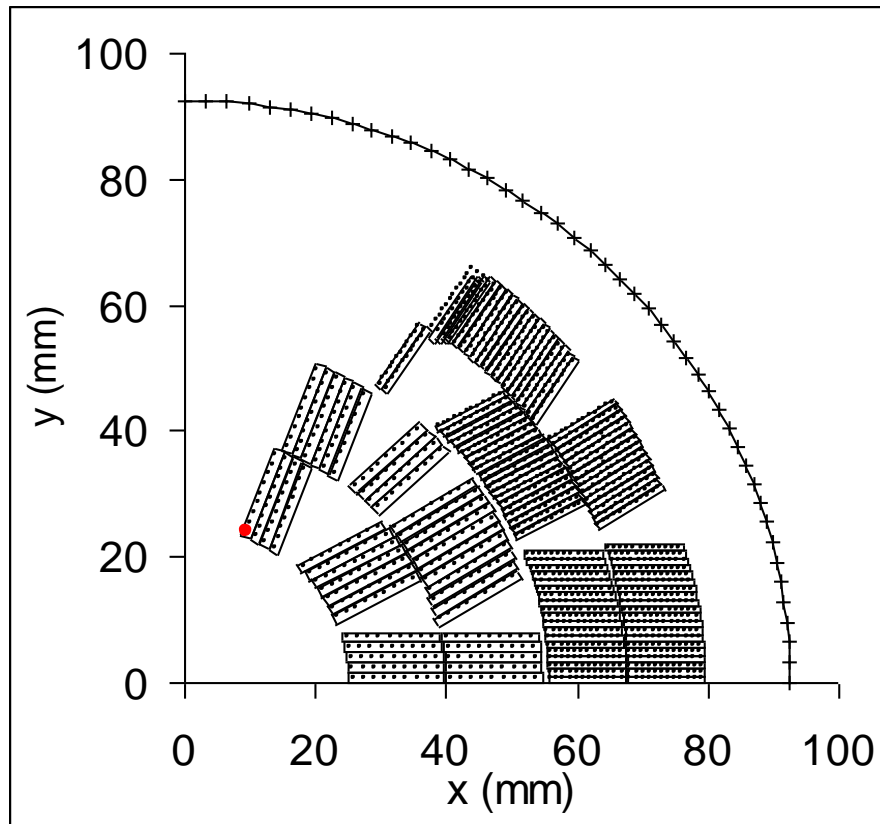
# A review of dipole lay-outs

- FRESCA



# A review of dipole lay-outs

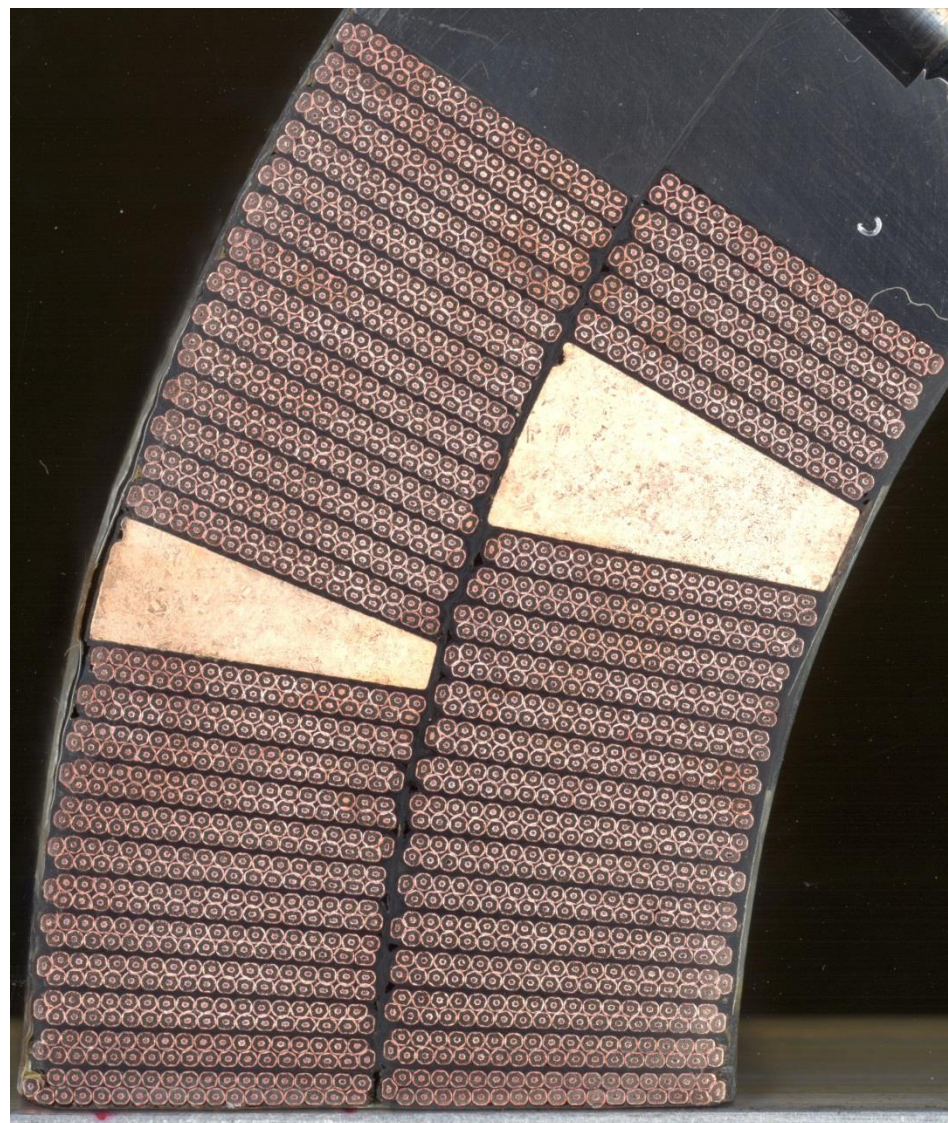
- D20





# Magnetic design and coils

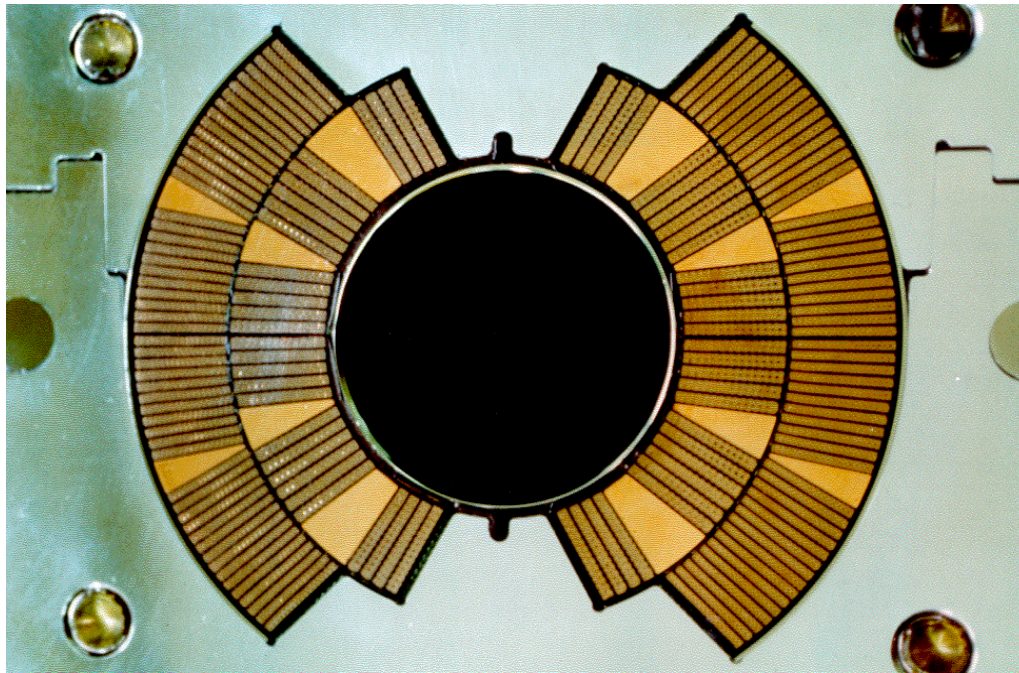
- How do we create a **perfect field**?
- How do we **express** field and its “**imperfections**”?
- How do we design a coil to **minimize field errors**?
- How do we **fabricate** a coil?





# Coil fabrication Winding

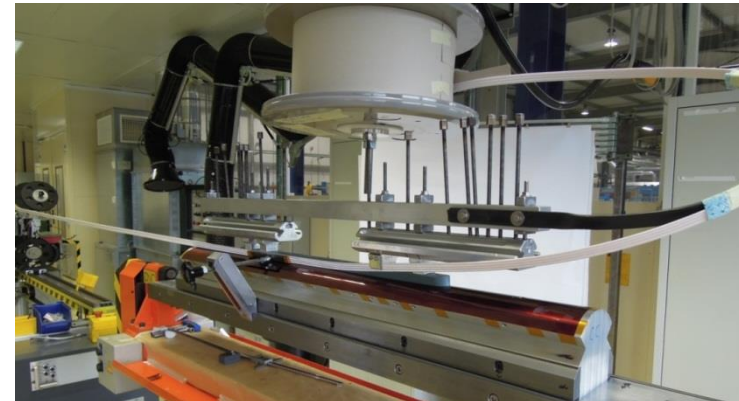
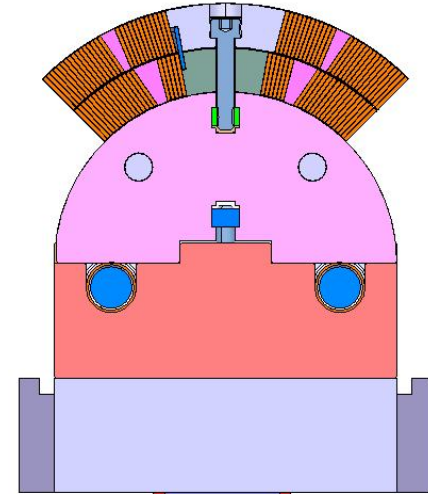
- The coil: most **critical component** of a superconducting magnet
- **Cross-sectional accuracy** of few hundredths of millimeters over  $\sim 15$  m
- **Laminated tooling**





# Coil fabrication Winding

- The cable is wound around a **pole** on a mandrel.
  - The mandrel is made of laminations
- Winding starts from **pole turn** of the inner layer
- Cable maintained in **tension** (200 N)
- For large production → **automated winding machines**



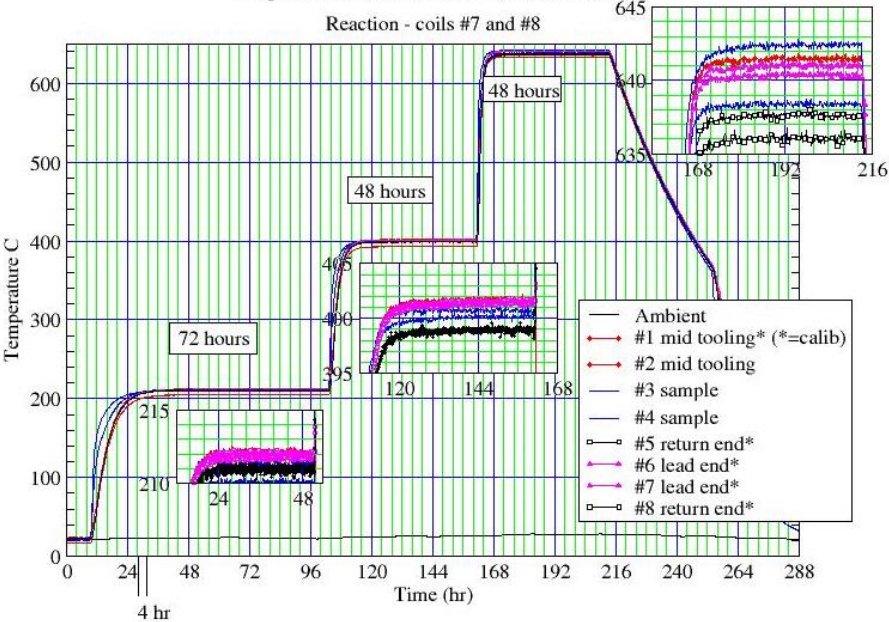




# Coil fabrication

## Reaction of Nb<sub>3</sub>Sn coils

TQS01 REACTION (calibrated)



### ● Heat treatment

- Sn and Nb are heated to 650-700 C in vacuum or inert gas (argon)
  - They react to form Nb<sub>3</sub>Sn
- The cable becomes **brittle**
- The reaction is characterized by **three temperature steps**
  - Homogeneity is of about  $\pm 3$  °C

### ● Reaction oven with argon gas flow

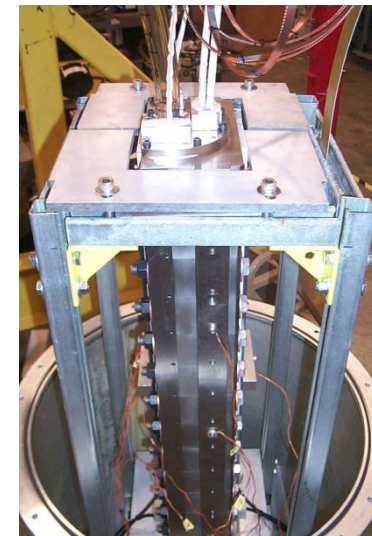
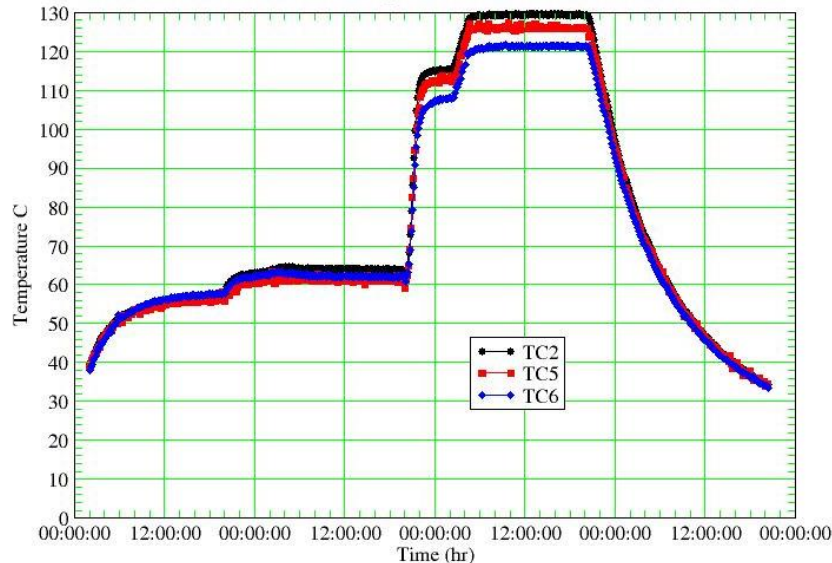
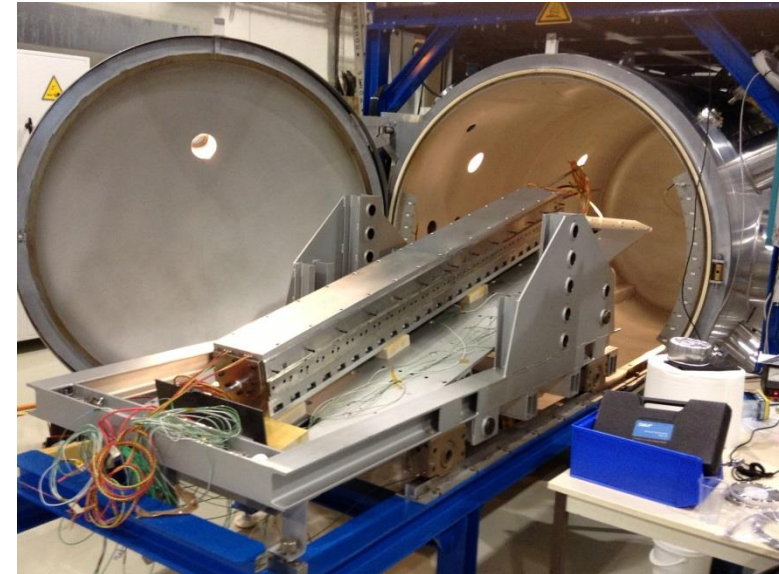
- **Minimize O<sub>2</sub> content** and Cu oxidation



# Coil fabrication

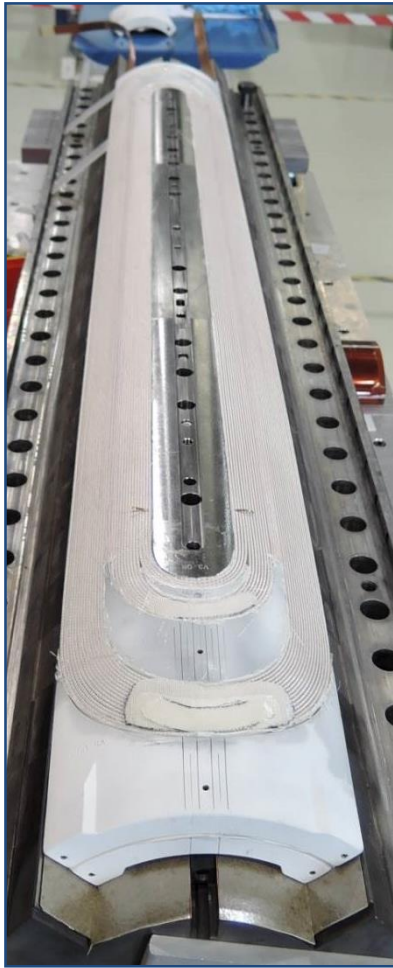
## Vacuum impregnation of Nb<sub>3</sub>Sn coils

- After reaction, coil placed in a **impregnation fixture**
  - The fixture is inserted in a vacuum tank, evacuated → **epoxy injected**
  - high viscosity at room temperature,
  - low viscosity at ~60 °C
  - Then, **curing** at ~150 °C → solid block





# Overview of coil fabrication stages



After winding/curing

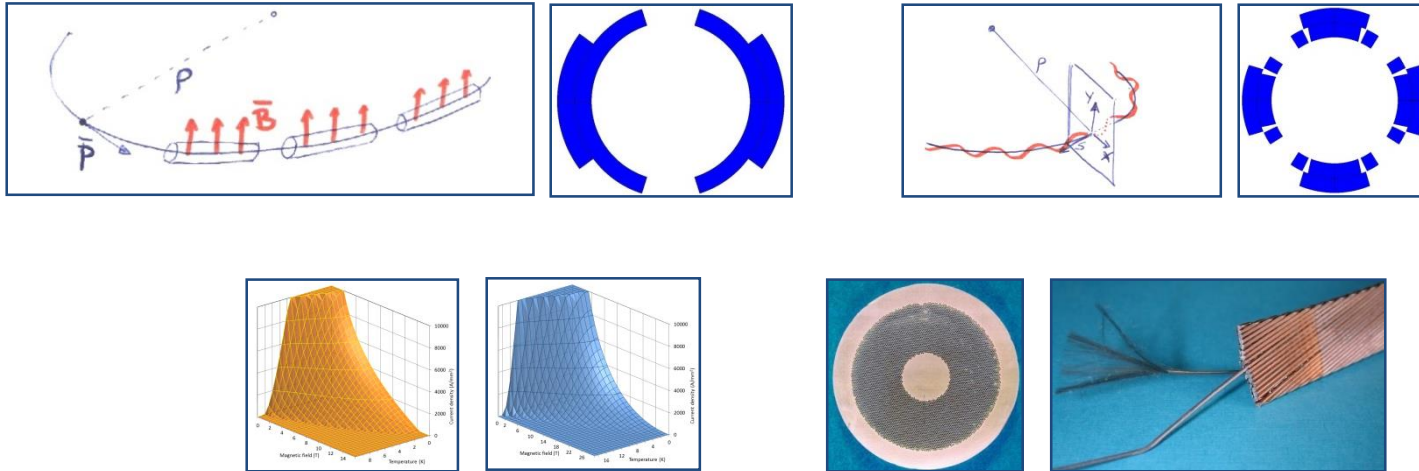


After reaction

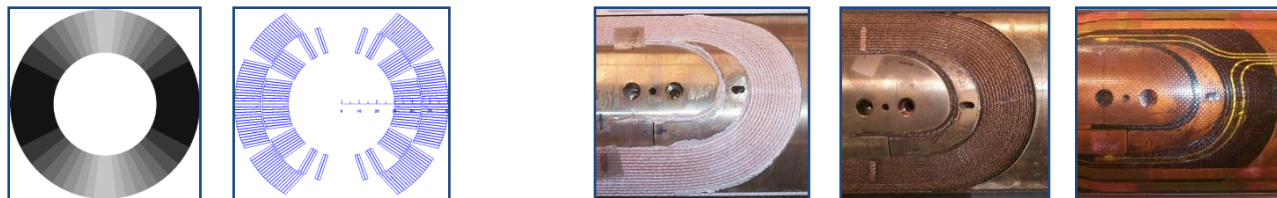


After impregnation

- **Particle accelerators and superconductors**



- **Magnetic design and coils**





# Next lecture

- **Mechanics of superconducting magnets**
- **Quench and protection**
- **HiLumi LHC and FCC**

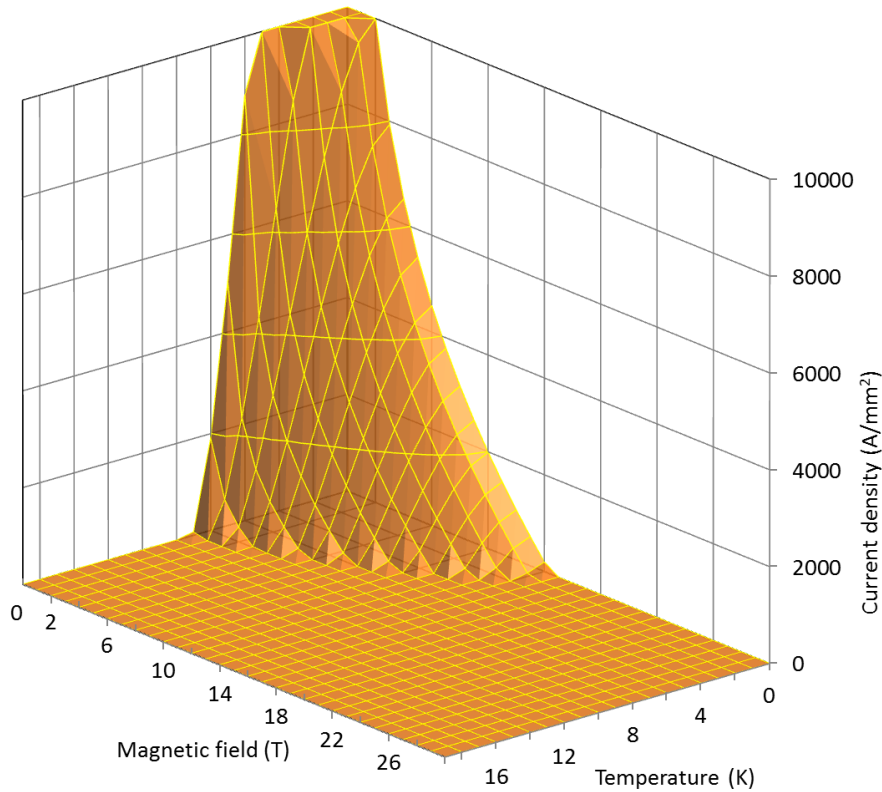


# Appendix

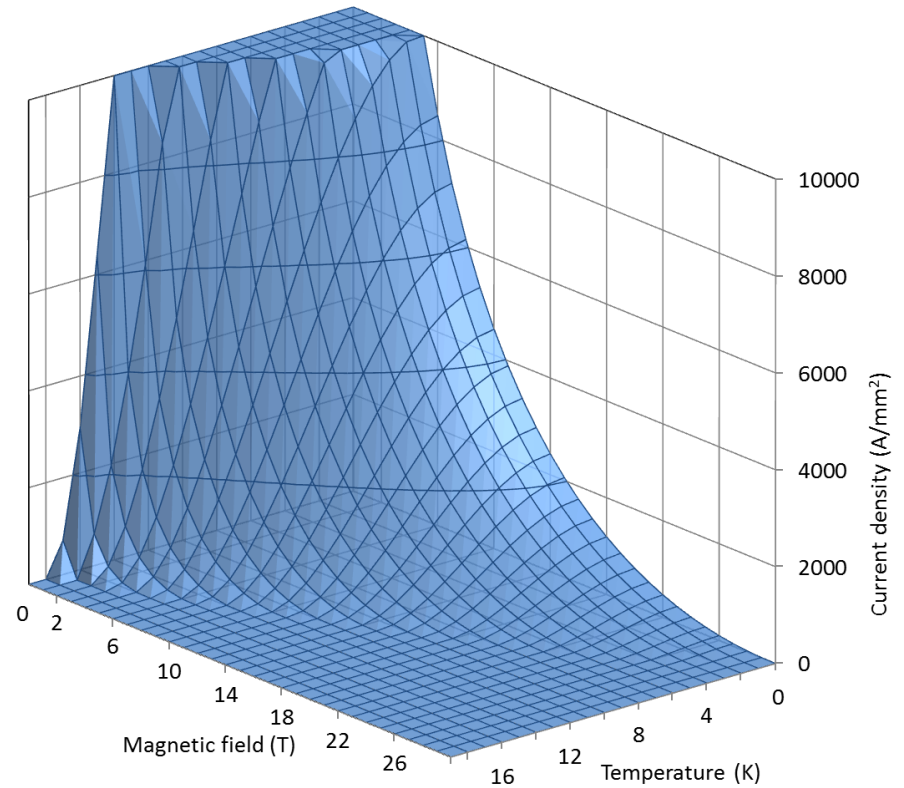


# Superconductivity Nb-Ti vs. Nb<sub>3</sub>Sn

Nb-Ti



Nb<sub>3</sub>Sn

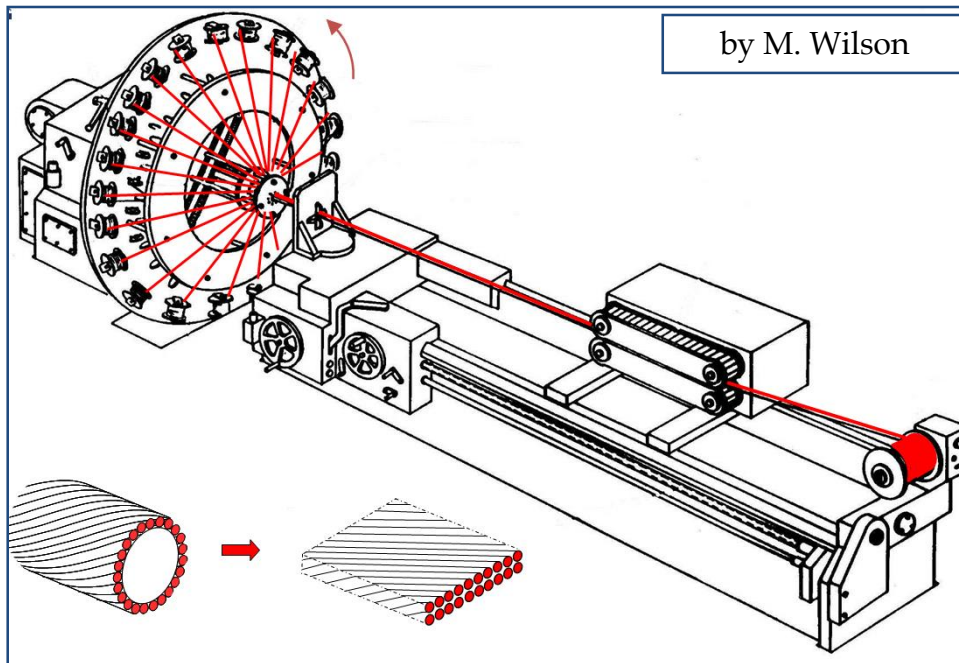
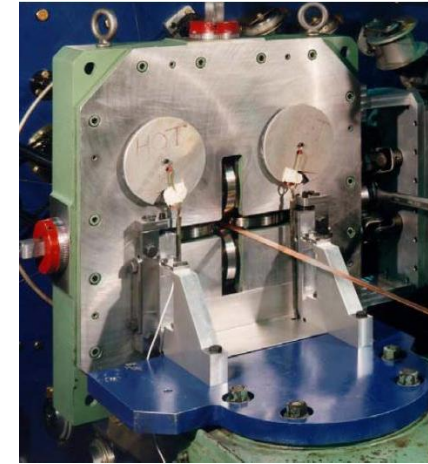




# Practical superconductors

## Multi-strand cables motivations

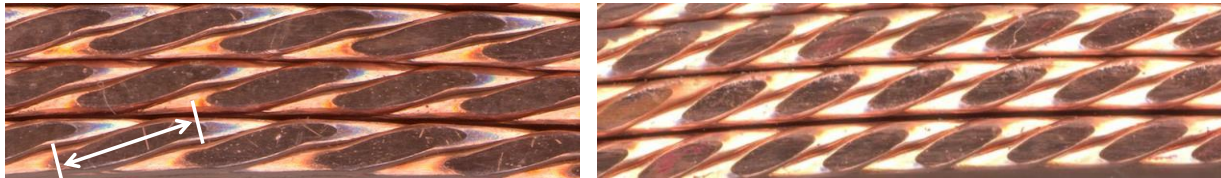
- Rutherford cables fabricated by **cabling machine**
  - Strands wound on spools mounted on a rotating drum
  - Strands twisted around a conical mandrel into rolls (Turk's head)
  - The rolls compact the cable and provide the final shape



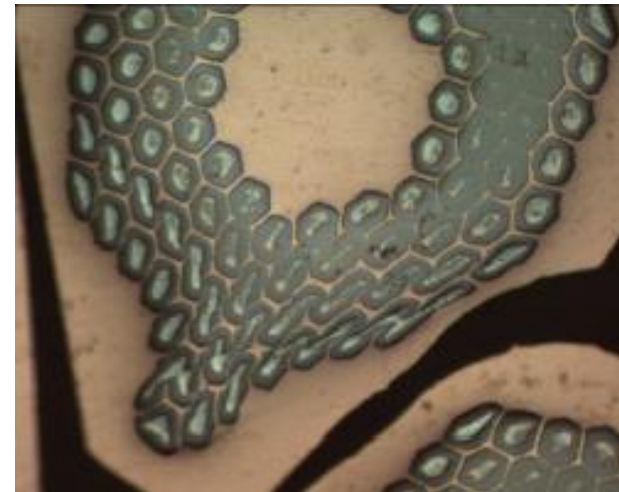
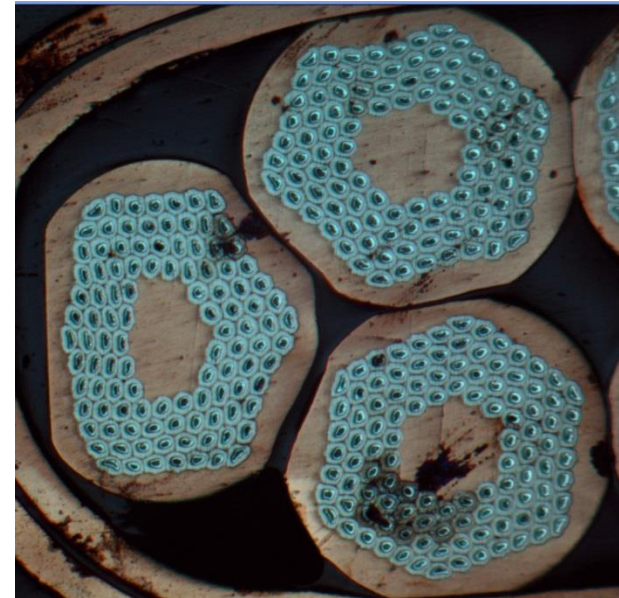
# Practical superconductors

## Multi-strand cables

- **Edge deformation** may cause
  - reduction of the filament cross-sectional area (Nb-Ti)
  - breakage of reaction barrier with incomplete tin reaction ( $\text{Nb}_3\text{Sn}$ )
- In order to avoid degradation
  - strand cross-section investigated
  - Edge facets are measured
    - General rule: no overlapping of facets



- **Keystone angle** is usually of  $\sim 1^\circ$  to  $2^\circ$

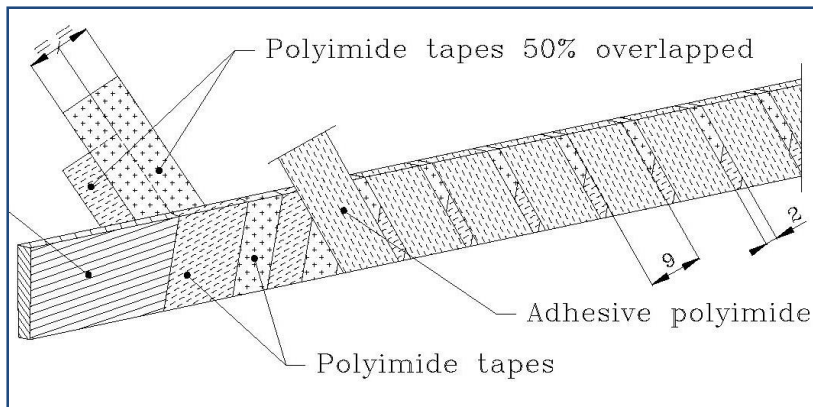




# Practical superconductors

## Cable insulation

- The cable insulation must feature
  - Good **electrical properties** to withstand turn-to-turn  $V$  after a quench
  - Good **mechanical properties** to withstand high pressure conditions
  - **Porosity** to allow penetration of helium (or epoxy)
  - **Radiation hardness**
- In Nb-Ti magnets overlapped layers of **polyimide**
- In Nb<sub>3</sub>Sn magnets, **fiber-glass** braided or as tape/sleeve.
- Typically the insulation thickness: 100 and 200  $\mu\text{m}$ .

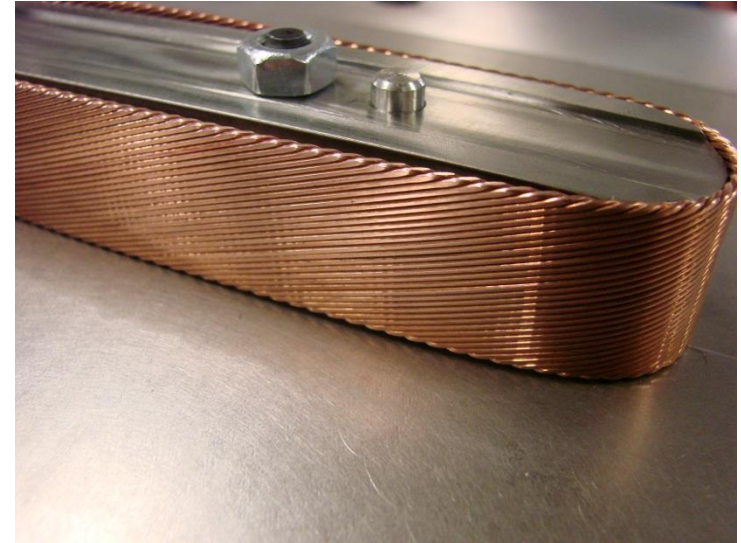




# Coil fabrication

## Winding and curing

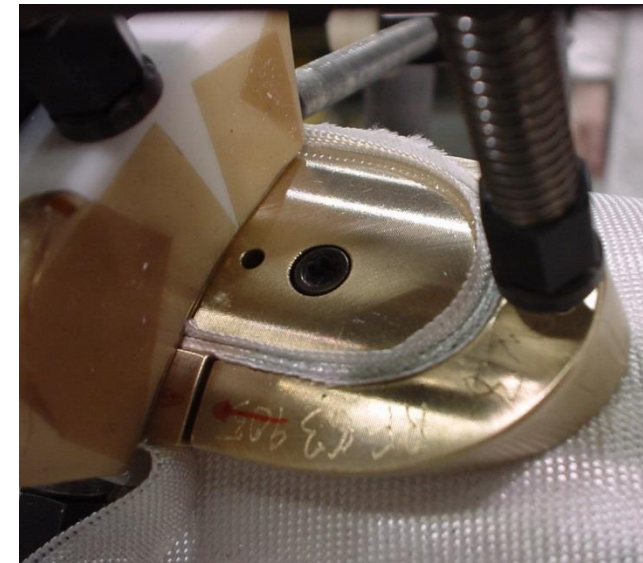
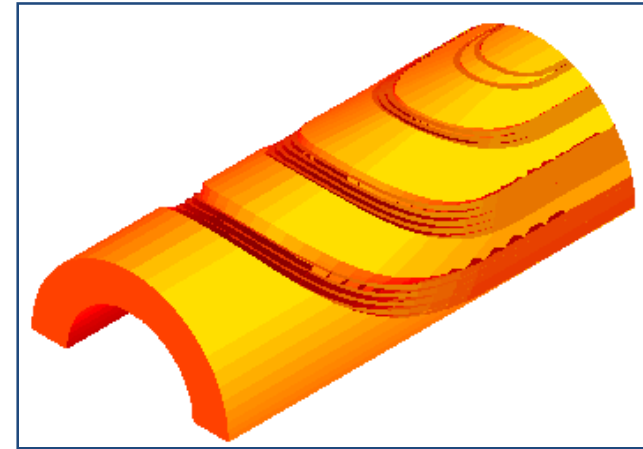
- There is a **minimum bending radius**, which depends on the cable dimensions.
  - Is there a general rule?
    - No, but usually the bending radius is 10-15 times the cable thickness.
  - The cable must be constantly monitored during winding.
- If the bending radius is too small
  - **De-cabing** during winding;
  - Strands “**pop-out**”.



# Coil fabrication

## Winding and curing

- In the **end region**, more difficult to constrain the turns
  - bent over the narrow edge
- To improve the mechanical stability and to reduce the peak field → **end spacers**
  - **constant perimeter** approach
    - The two narrow edges of the turn in the ends follow curves of equal lengths.
- In Nb-Ti magnets, end spacers are produced by 5-axis machining of epoxy impregnated fiberglass
  - Remaining voids are then filled by resins
- In Nb<sub>3</sub>Sn magnets, end spacers are made of aluminum bronze or stainless steel.

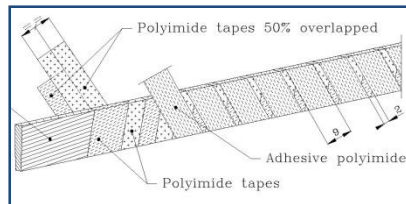




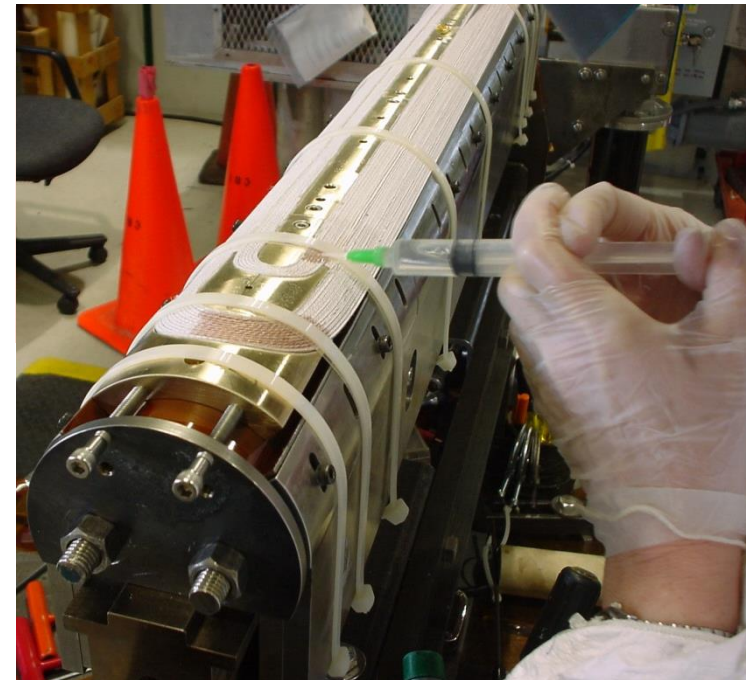
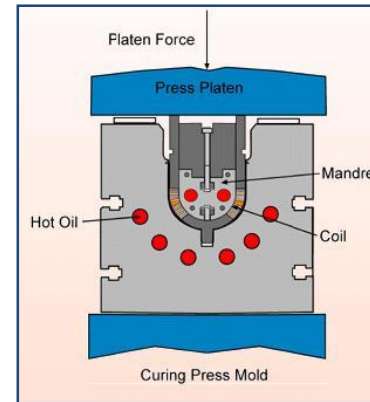
# Coil fabrication

## Winding and curing

- The goal of curing
  - Glue turns facilitating **handling**
- Coils are placed in the **curing mould** equipped with a **heating** system, and **compressed** in press
- Nb-Ti coils cured up to  $190 \pm 3$  °C at 80-90 MPa (LHC) to **activate resin**



- In  $\text{Nb}_3\text{Sn}$  coils, cable insulation is injected with **ceramic binder**
  - Cured at 150° C and at ~10-30 MPa



# ...more on field harmonics

- As we said, we **minimize** harmonics during **design** phase
- After fabrication we can **measure** them
  - Reproducibility of coil positioning is  $\sim 20\text{-}50$  mm ( $1\sigma$ )
- If an anomaly is observed  $\rightarrow$  **inverse problem**
  - Which coil **defect** could cause such an **anomaly**?

