

Cosmological signature of (e.m.) decaying Dark Matter

Vivian Poulin

LAPTh, Annecy, France and RWTH, Aachen, Germany

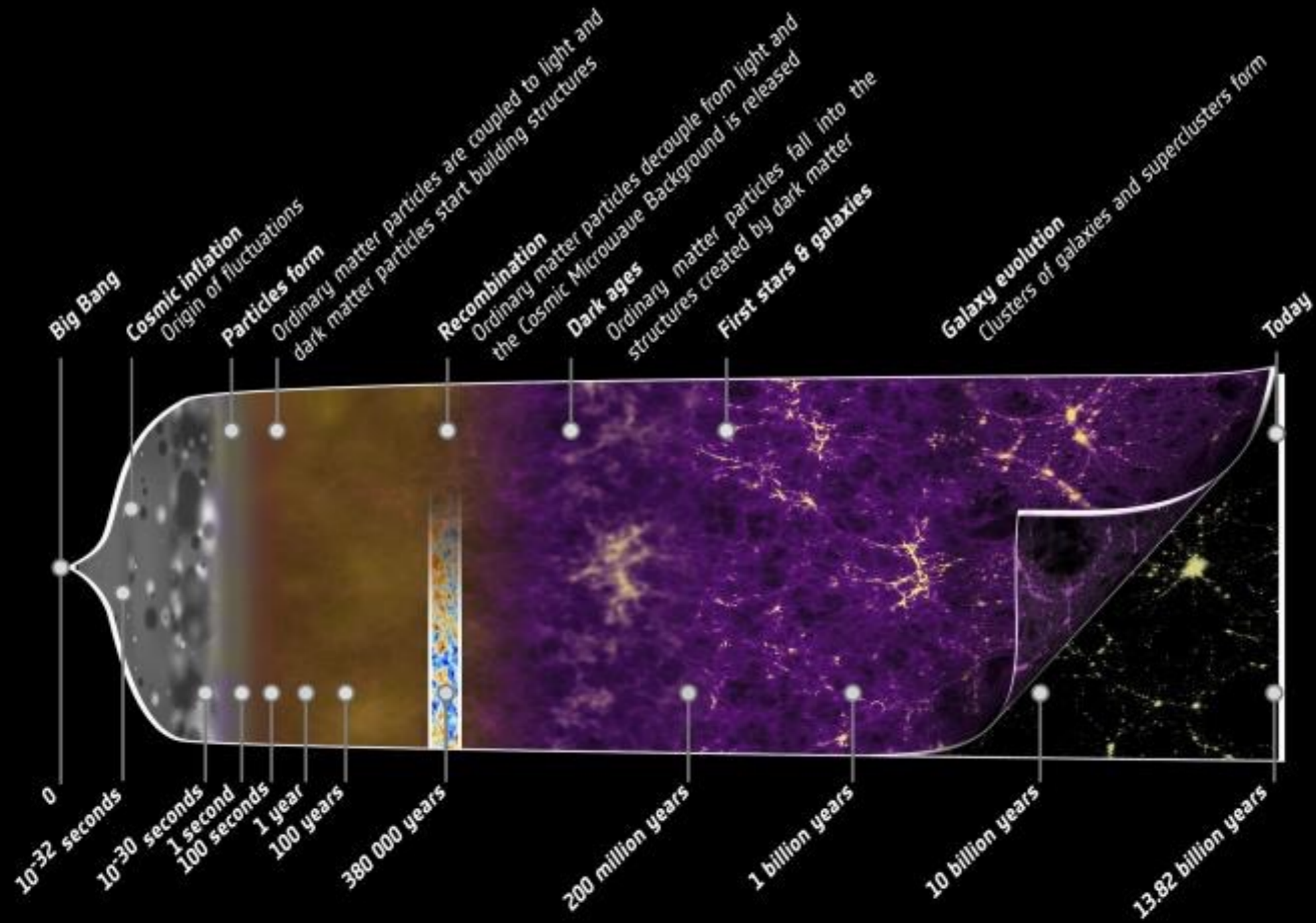
In collaboration with
Julien Lesgourgues (RWTH, Aachen)
and Pasquale D. Serpico (LAPTh, Annecy)

mainly : VP, Serpico & Lesgourgues JCAP 1703 (2017) no.03, 043

see also : VP & Serpico PRL 114 (2015) no.9, 091101

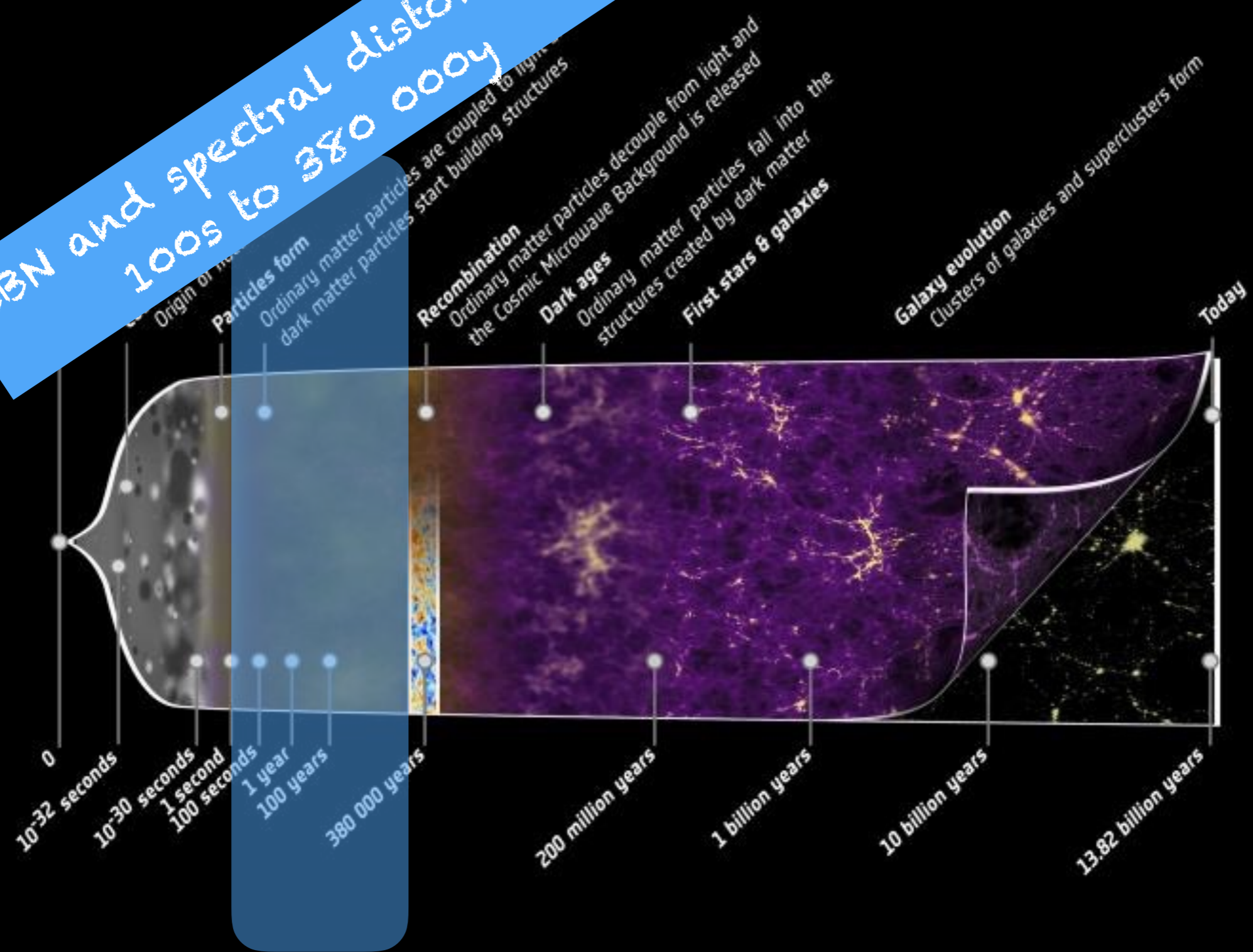
VP & Serpico PRD 91 103007 (2015) no.10

VP, Serpico & Lesgourgues JCAP 1512 (2015) no.12 041



Our Universe is a great particle physics laboratory !

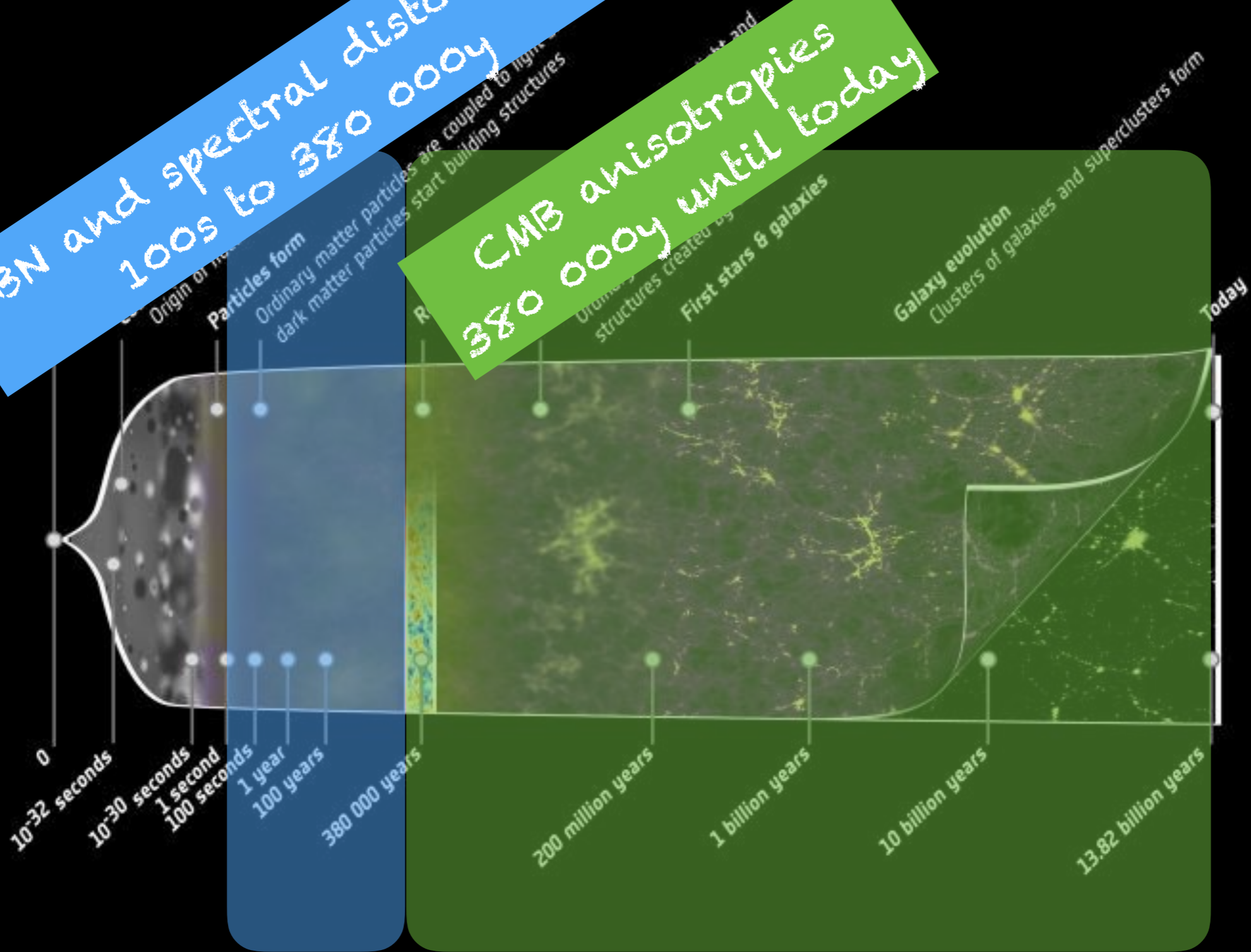
BBN and spectral distortions 100s to 380 000y



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BBN and spectral distortions
100s to 380 000y

CMB anisotropies
380 000y until today

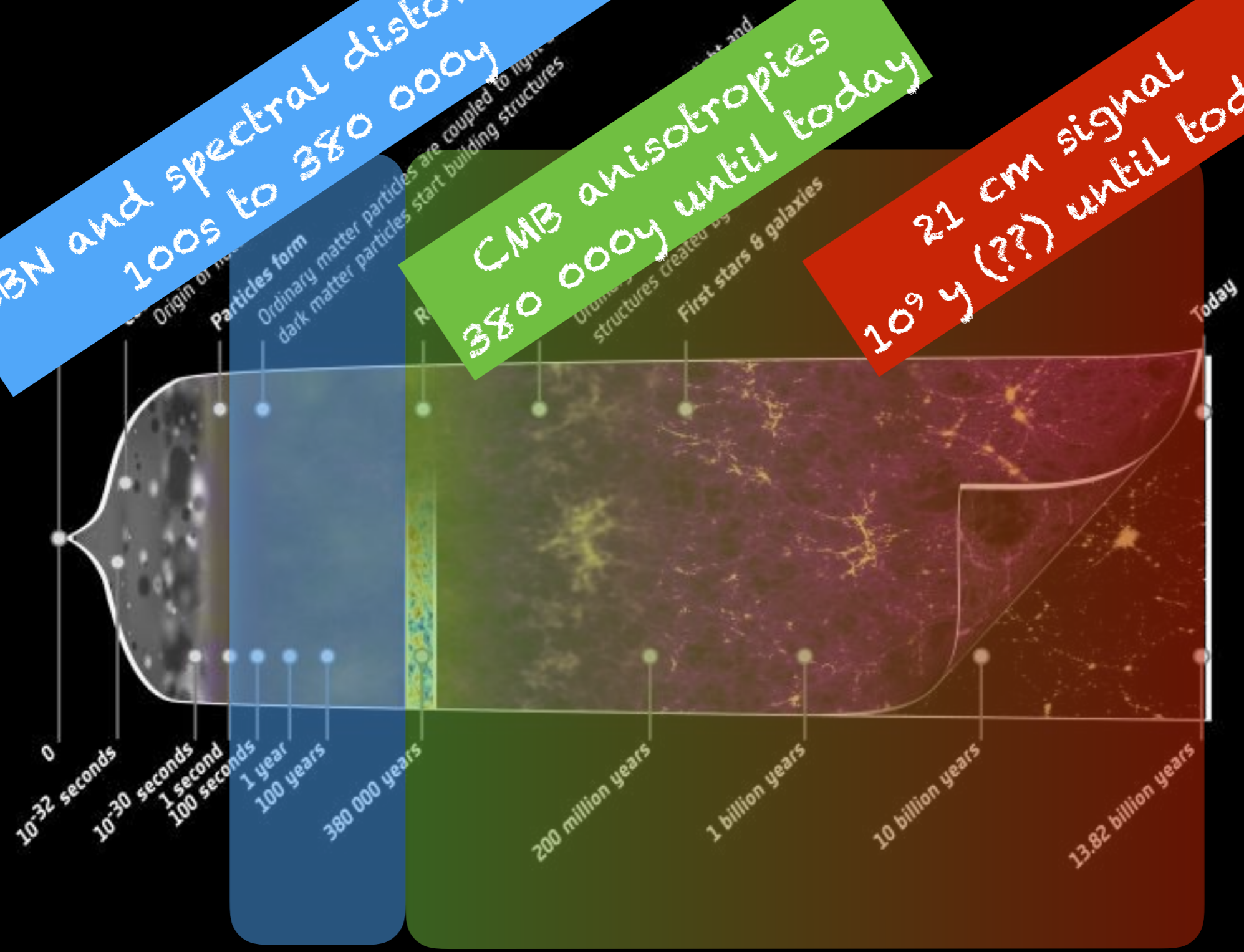


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100s to 380 000y

CMB anisotropies
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10^9 y 21 cm signal
(??) until today



Our Universe is a great particle physics laboratory !

A Journey in Wonderland of particle physics

see e.g.

*[hep-ph/0404175],
[arXiv:0810.0713],
[arXiv:0912.5297],
[arXiv:1602.04816]*

Q. : What models are concerned by these constraints ?

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- SUSY / UED inspired : excited states, unstable -inos e.g. gravitinos, superWIMP, WIMPzillas ...
- Sterile neutrinos / Majoron
- Primordial Black Holes

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- Big Bang Nucleosynthesis

- Spectral Distortions of the BB distribution

- CMB power spectra

- Matter power spectrum

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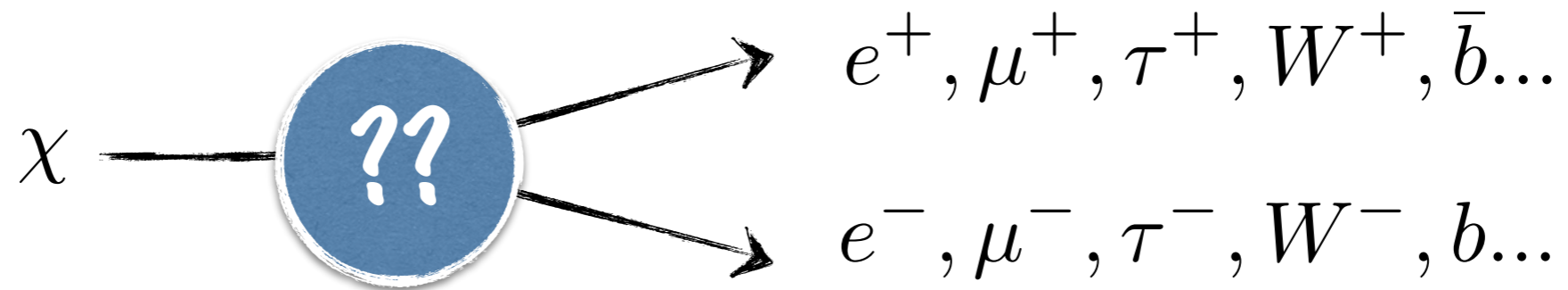
- Matter power spectrum

- Future: 21 cm ? ?

Electromagnetic decay products

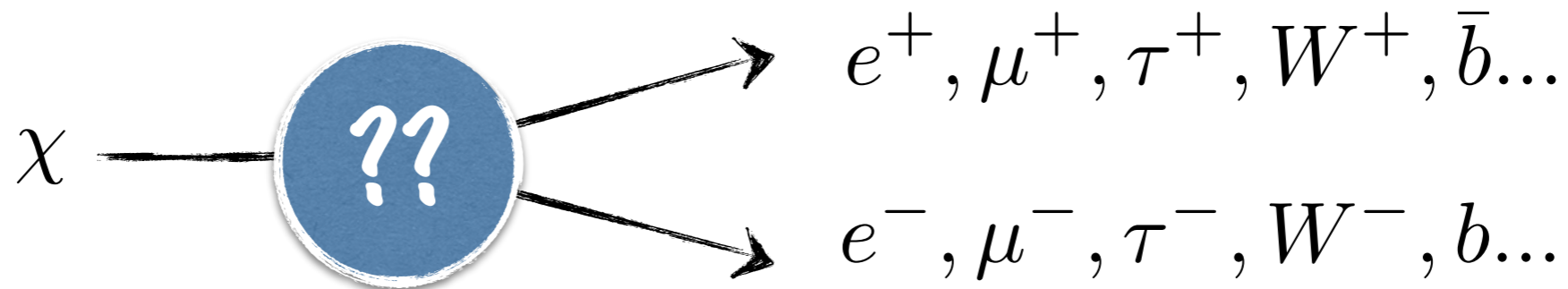
Purely gravitational impact of the decay

The typical electromagnetic decay of an exotic particle



What happens to the decay products ?

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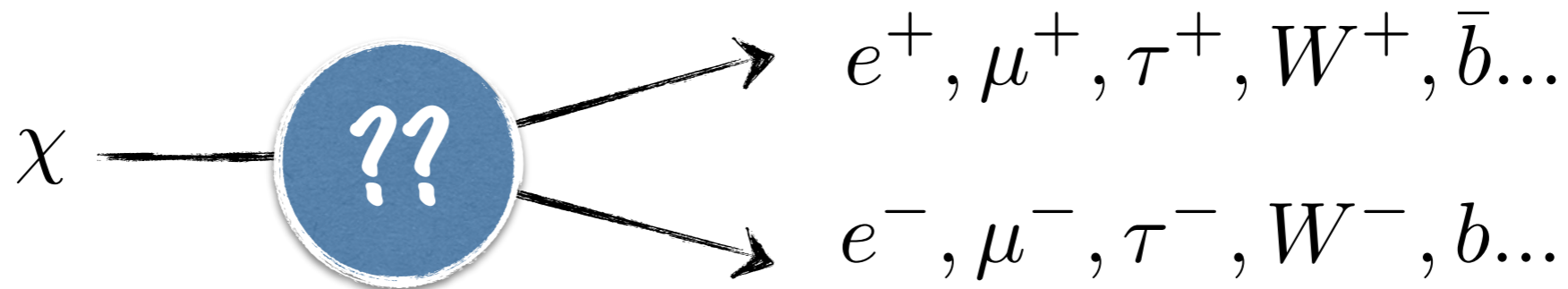
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One Caveat : We restrict ourself to lifetime > 1000 s.
 => We can neglect **hadronic products**!

Only BBN constraints (for very short lifetime) are sensitive.

e.g. Kawasaki et al.
PRD D71 (2005) 083502
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The typical electromagnetic decay of an exotic particle



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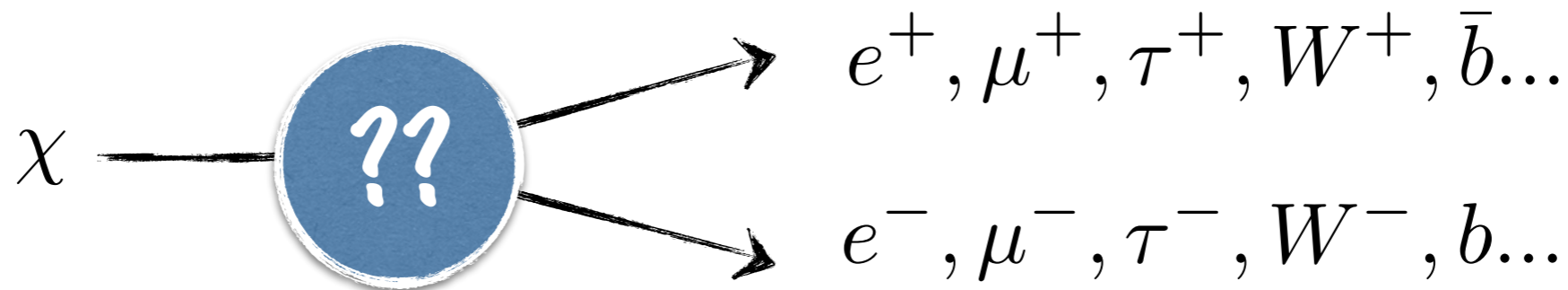
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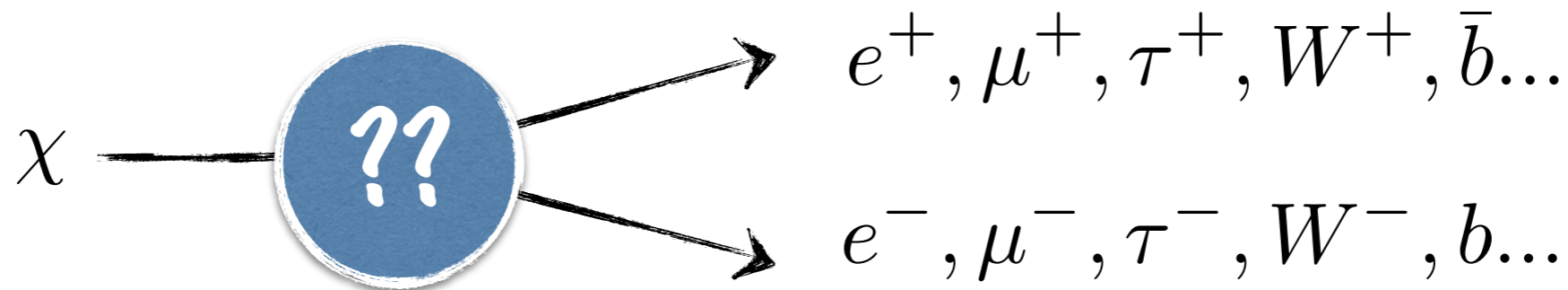
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- Development of E.M. cascade through interactions with CMB

$$\gamma\gamma_{\text{CMB}} \rightarrow e^+e^- \quad e\gamma_{\text{CMB}} \rightarrow e\gamma \quad \gamma\gamma_{\text{CMB}} \rightarrow \gamma\gamma$$

spectral distortions

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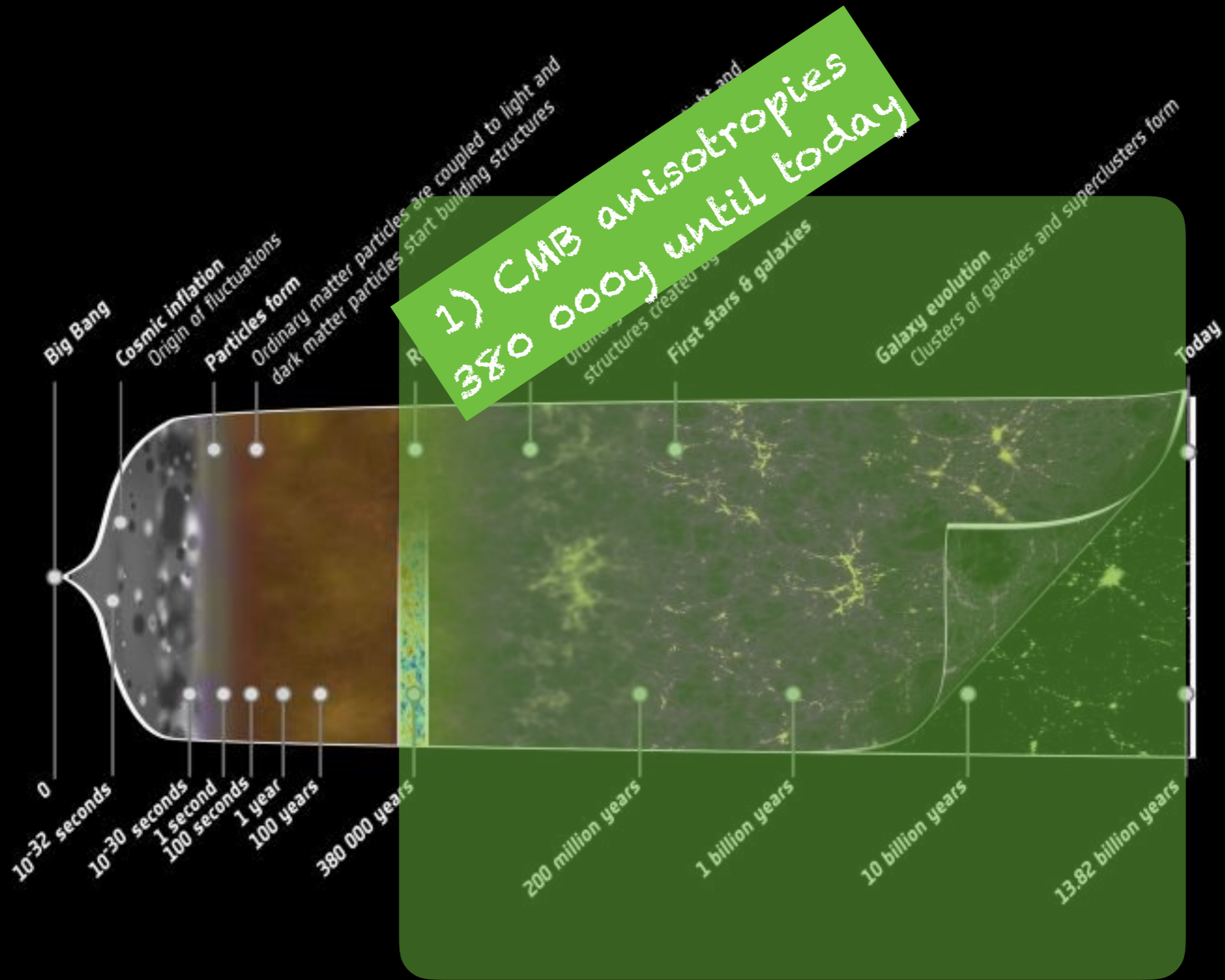
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- They ionize, excite or heat the IGM... and break atoms !

spectral distortions

BBN, CMB anisotropies



From perturbations to spectrum of temperature anisotropies

see e.g. textbook « *The Cosmic Microwave Background* » by R. Durrer; « *Cosmology* » By Weinberg.
or original papers Seljak & Zaldarriaga APJ. 469 (1996) 437-444; Kamionkowski et al. PRD55 (1997) 7368-7388

In the L.O.S formalism:

(Here, I only recall computation of Temp. anisotropies at 1st order, Newt. gauge)

$$C_\ell^{\text{TT}} = \int \frac{dk}{k} \mathcal{P}_{\mathcal{R}}(k) [\Theta_\ell(\tau_0, k)]^2$$

Temperature power spectrum

$$\Theta_\ell(\tau_0, k) = \int_\tau^{\tau_0} d\tau S_T(\tau, k) j_\ell(k(\tau_0 - \tau))$$

Transfer function

$$S_T(k, \tau) \equiv \underbrace{g(\Theta_0 + \psi)}_{\text{SW}} + \underbrace{(gk^{-2}\theta_B)'}_{\text{Doppler}} + \underbrace{e^{-\kappa}(\phi' + \psi')}_{\text{ISW}} + \text{polarisation}$$

Temperature source function

$$g(\tau) \equiv -\kappa' e^{-\kappa} \quad \kappa(\tau) = \int_\tau^{\tau_0} d\tau \sigma_T a n_e x_e$$

Visibility function, optical depth

What could DM decay do to these functions?

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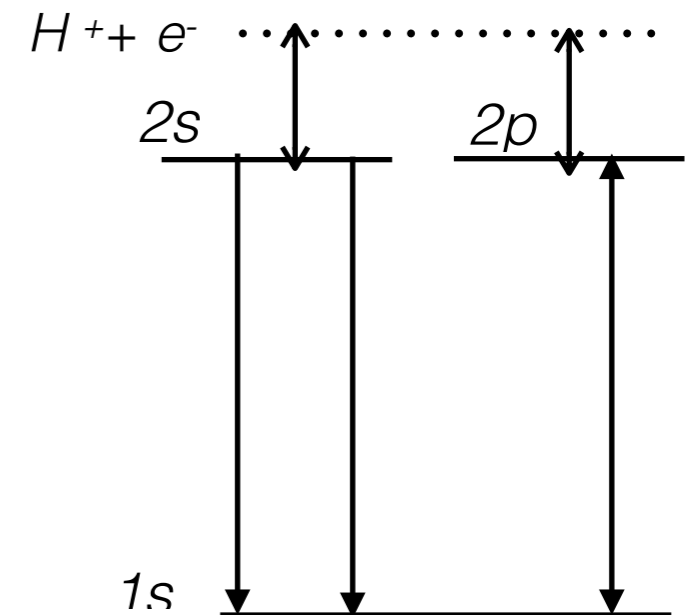
non e.m. decay : modify ϕ' and ψ'

Evolution equations for x_e : the free electron fraction
and T_m : the matter temperature

$$\frac{dx_e}{dz} = \frac{1}{(1+z)H(z)} [R_s(z) - I_s(z)]$$

$$\frac{dT_M}{dz} = \frac{1}{1+z} \left[2T_M + \gamma(T_M - T_{\text{CMB}}) \right]$$

*VP, Serpico & Lesgourgues
ArXiv:1610.10051
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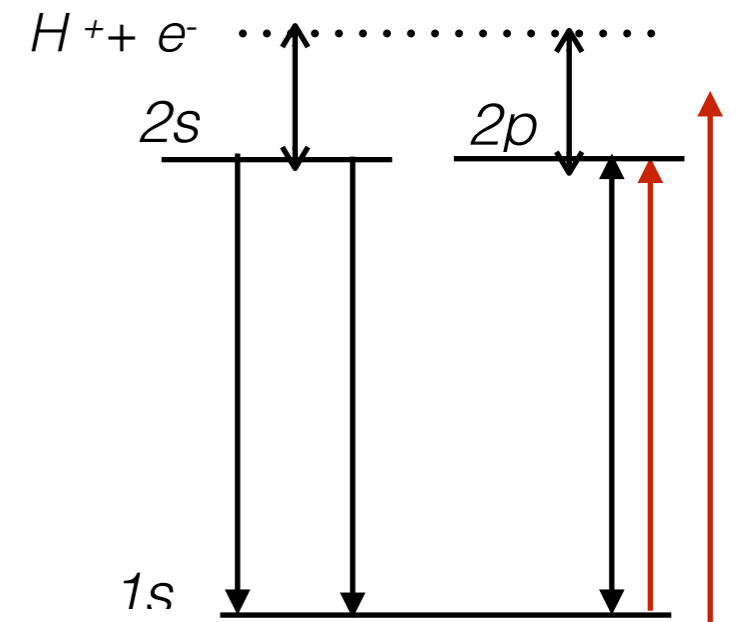
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by Peebles++ largely extended
nowadays ! e.g. **CosmoRec**
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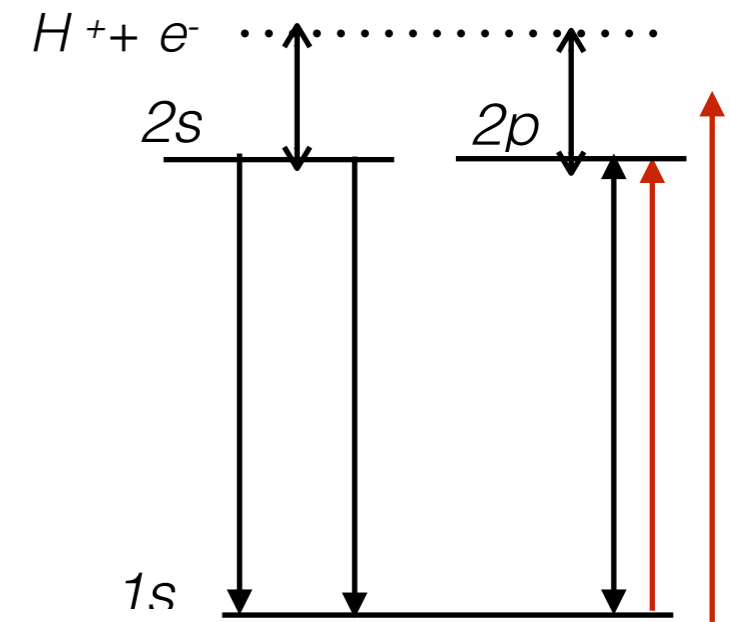


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$$I_X(z) \text{ and } K_h(z) \propto \left. \frac{dE}{dV dt} \right|_{\text{dep,c}}$$

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Key quantity $dE/dVdt|_{\text{dep,c}}$:

- The energy deposition rate by the decay per unit volume in each channel:
ionization, excitation, heating.
- Depending on z and x_e , the plasma can be **very inefficient at absorbing energy** !

$$\left. \frac{dE}{dV dt} \right|_{\text{inj}}(z) = (1+z)^3 f_{\text{dcdm}} \rho_{\text{dm}} c^2 \times \Delta_{\text{em}} \times \frac{e^{-t/\tau}}{\tau}$$

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e.m. energy
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Typical parametrization through the $f_c(z, x_e)$ functions :

$$\left. \frac{dE}{dV dt} \right|_{\text{dep,c}}(z) = f_c(z, x_e) \left. \frac{dE}{dV dt} \right|_{\text{inj}}(z)$$

see e.g. Slatyer et al.
PRD80 (2009) 043526
updated in
PRD93 (2016) no.2, 023521

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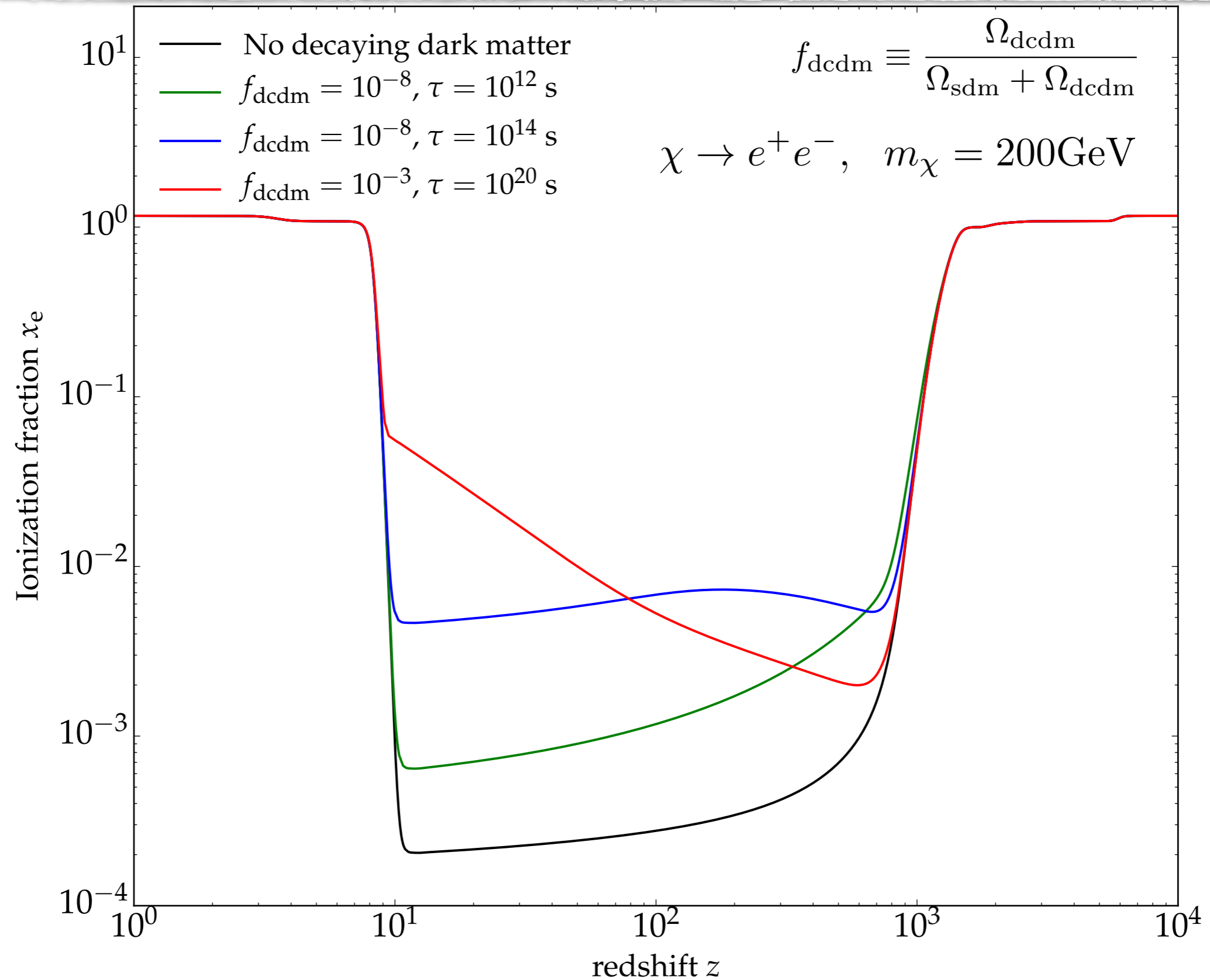
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$f_c(z, x_e)$ is the key quantity, it encodes:

- What fraction of the injected energy is left to interact with the IGM
- How this energy is distributed among each channel : 'heat', 'ionization', 'excitation'

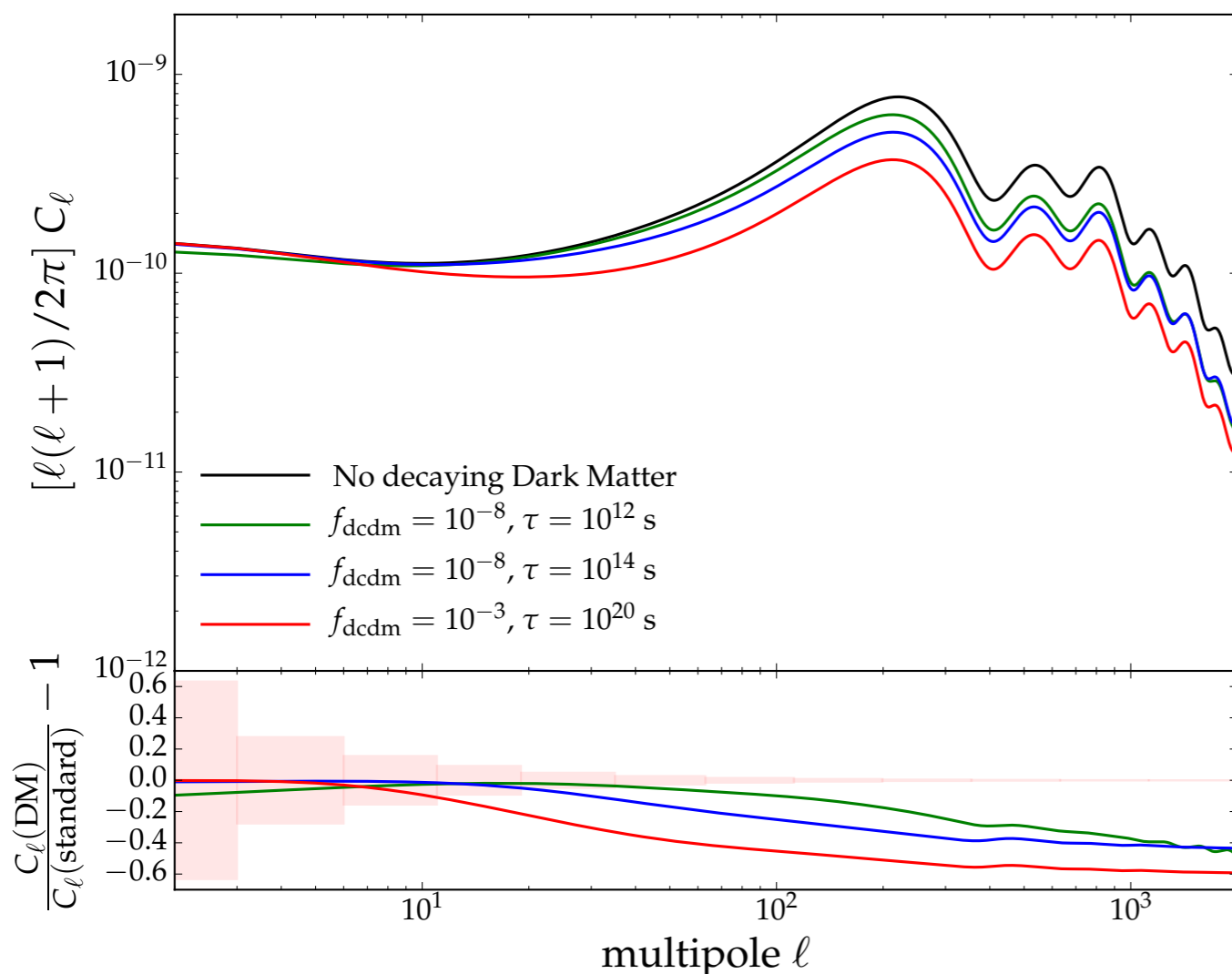
In practice, it depends on details of the particle physics and injection history.

x_e carries information on the time / amount of energy injection !

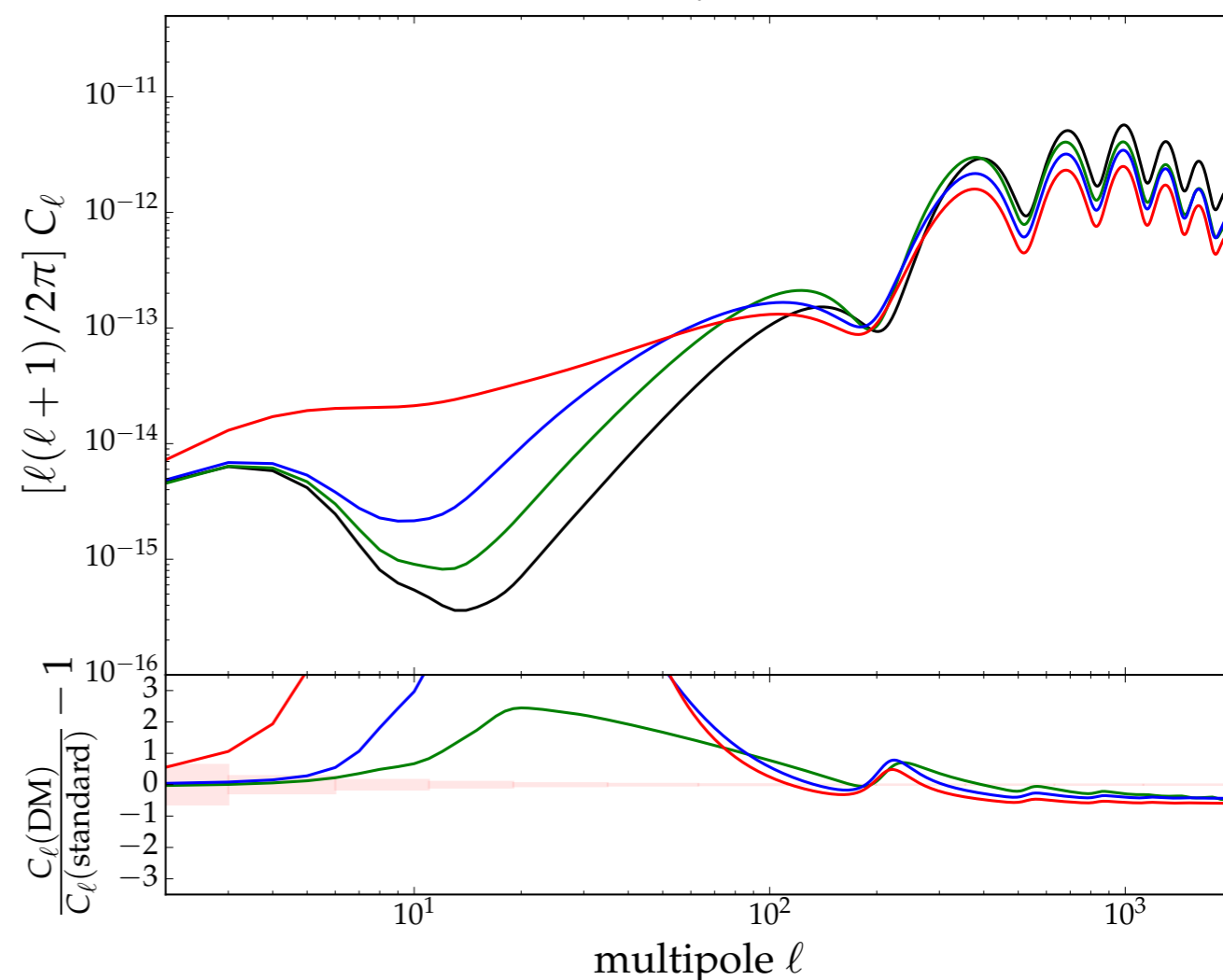


Many lifetime dependent effects on the CMB power spectra !

temperature anisotropies

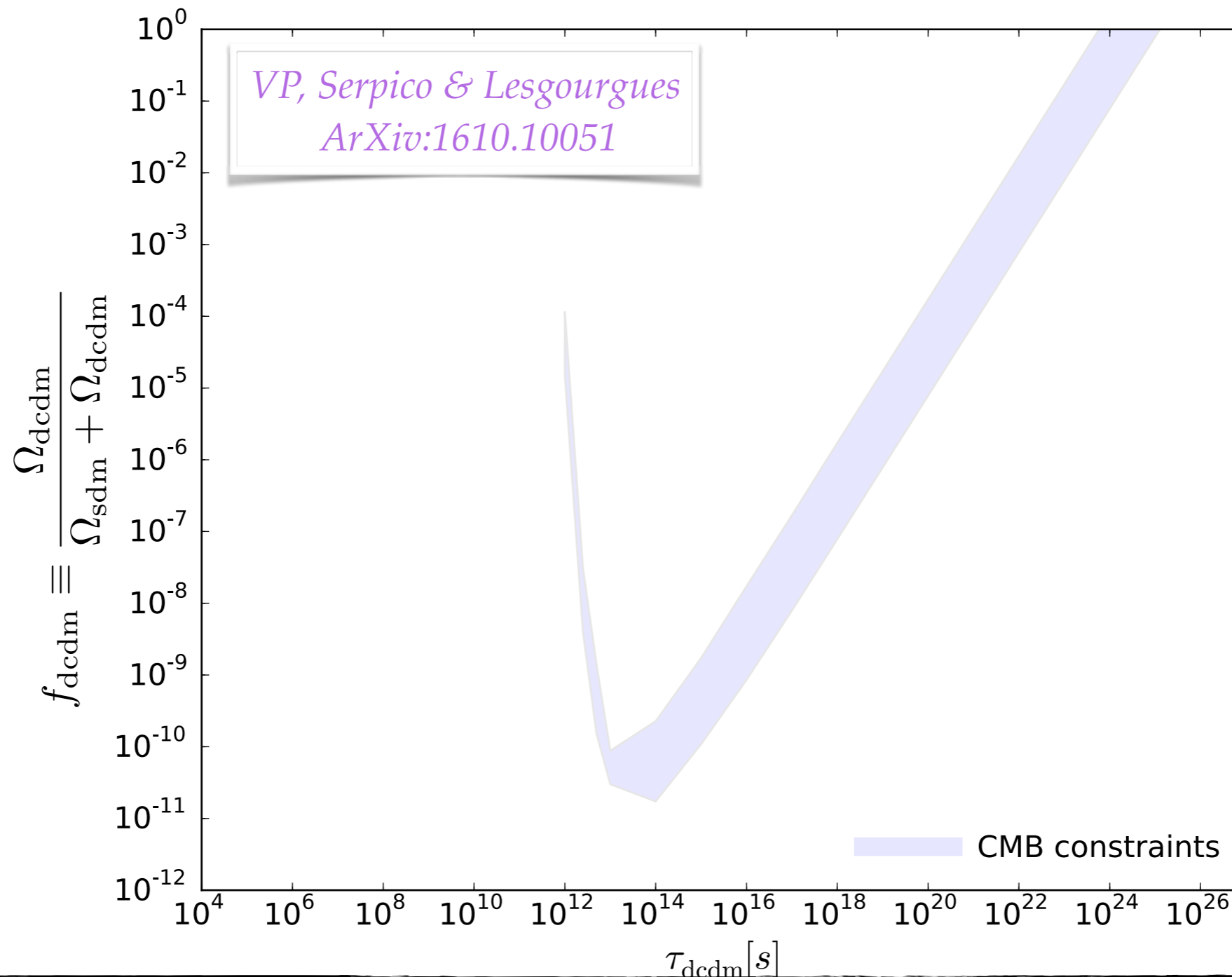
 C_ℓ^{TT}


polarization anisotropies

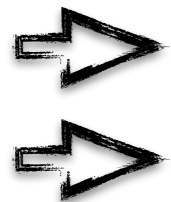
 C_ℓ^{EE}


- Long lifetime : looks like **early reionization**, i.e. increase of κ_{reio} leads to step-like suppression above $l = 10$ and bigger reionization bump.
- Short lifetime: can have **very peculiar behaviour**! Larger damping tail, shifted/broaden reionization bump and suppress LISW.

CMB anisotropies very powerful at constraining $\tau = [10^{12}, 10^{25}]s$



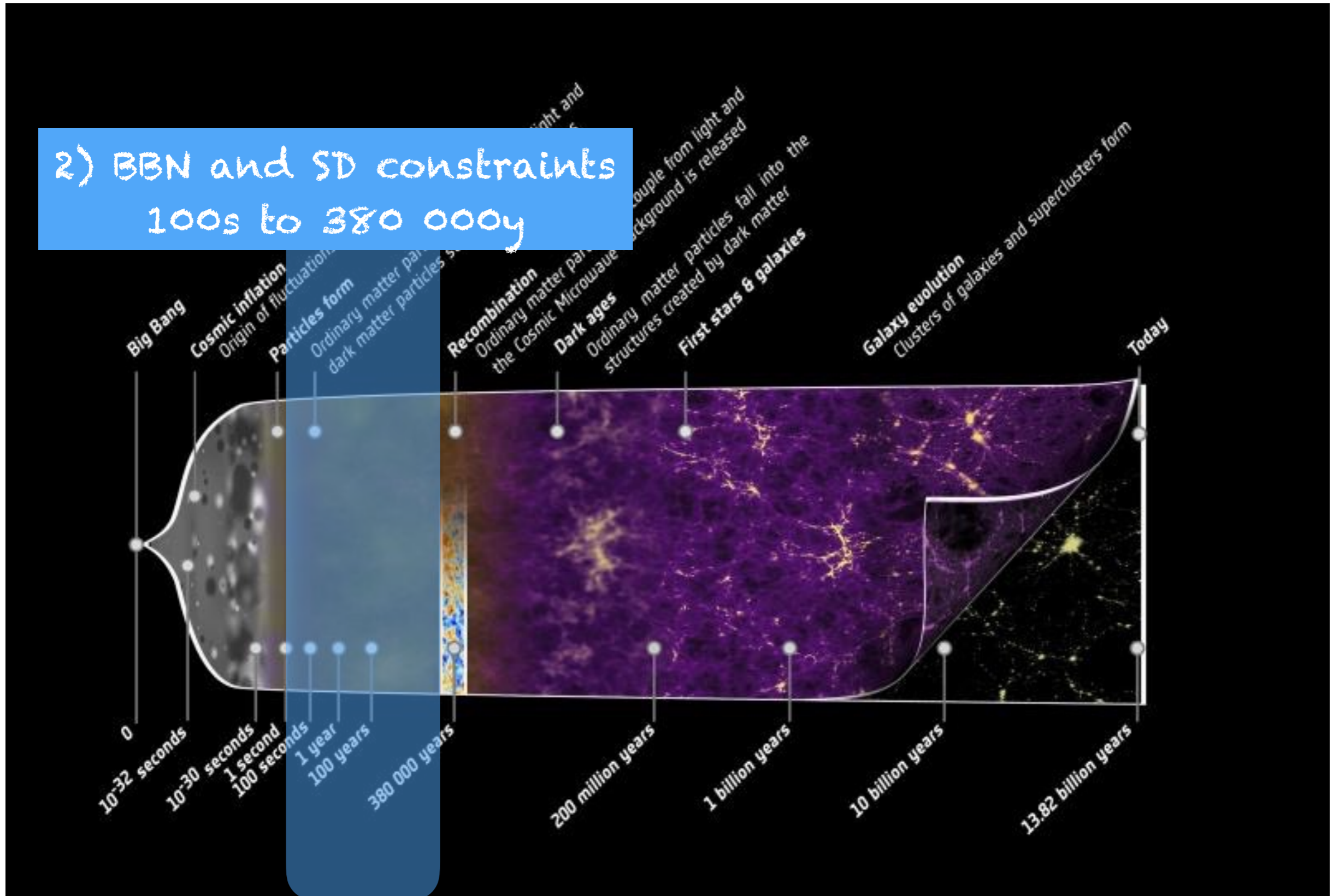
see also
Slatyer & Wu
PRD (2017)
no.2, 023010



Blue band : reflects difference between **energy deposition efficiency**.

Results are reliable for m_χ in $[10^3, 10^{12}]$ eV **whatever decay channel** !

2) BBN and SD constraints
100s to 380 000y



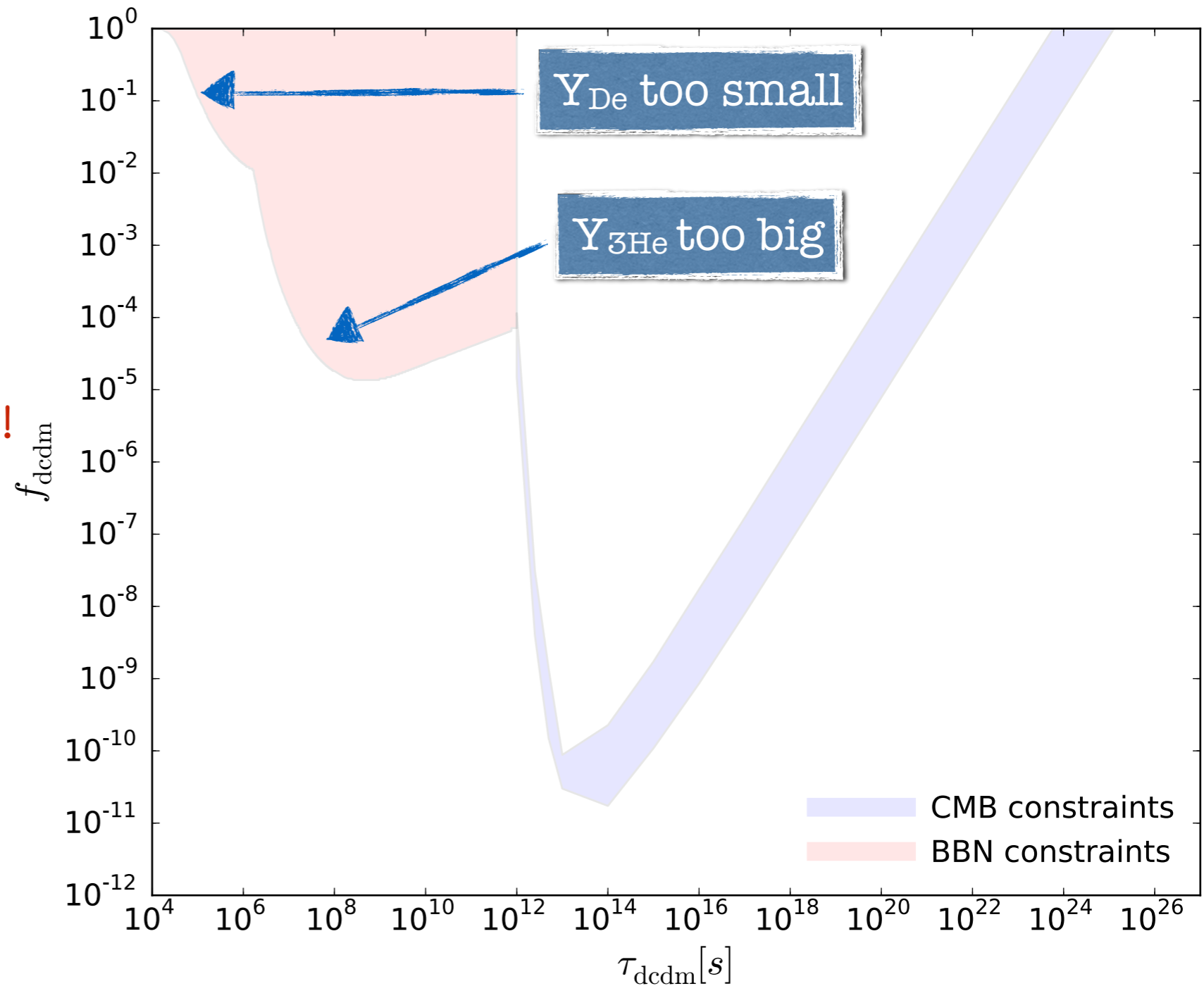
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Injected high energy particles initiate an E.M. Cascade :

Same idea as before but now $\Gamma_{\text{scat}} \gg \Gamma_{\text{hubble}}$!
(valid until recombination)

Those bounds are universal !!

*Kawasaki & Moroi,
ApJ 452,506 (1995)*



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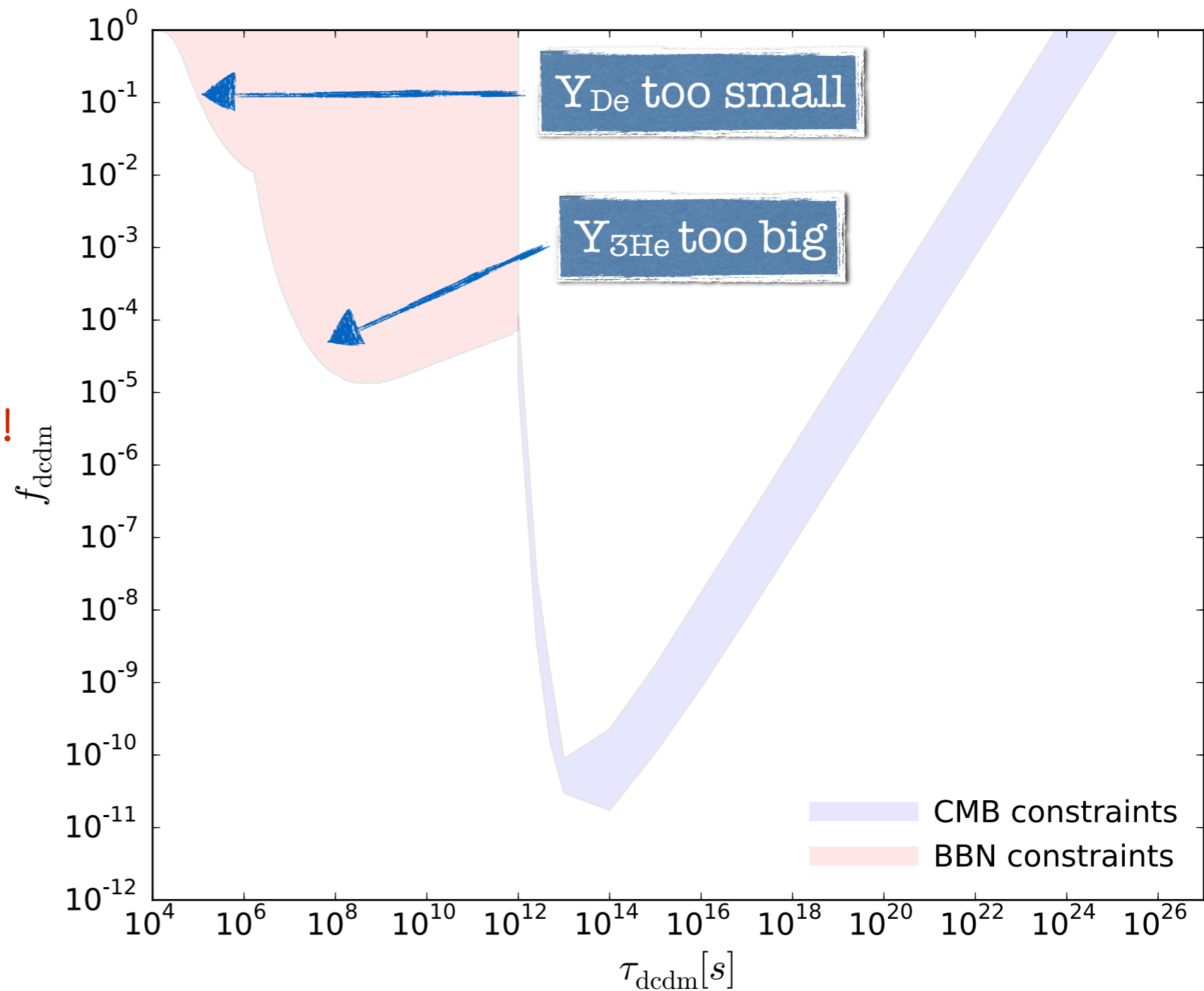
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For MeV-GeV energy injection, bounds can be much stronger.

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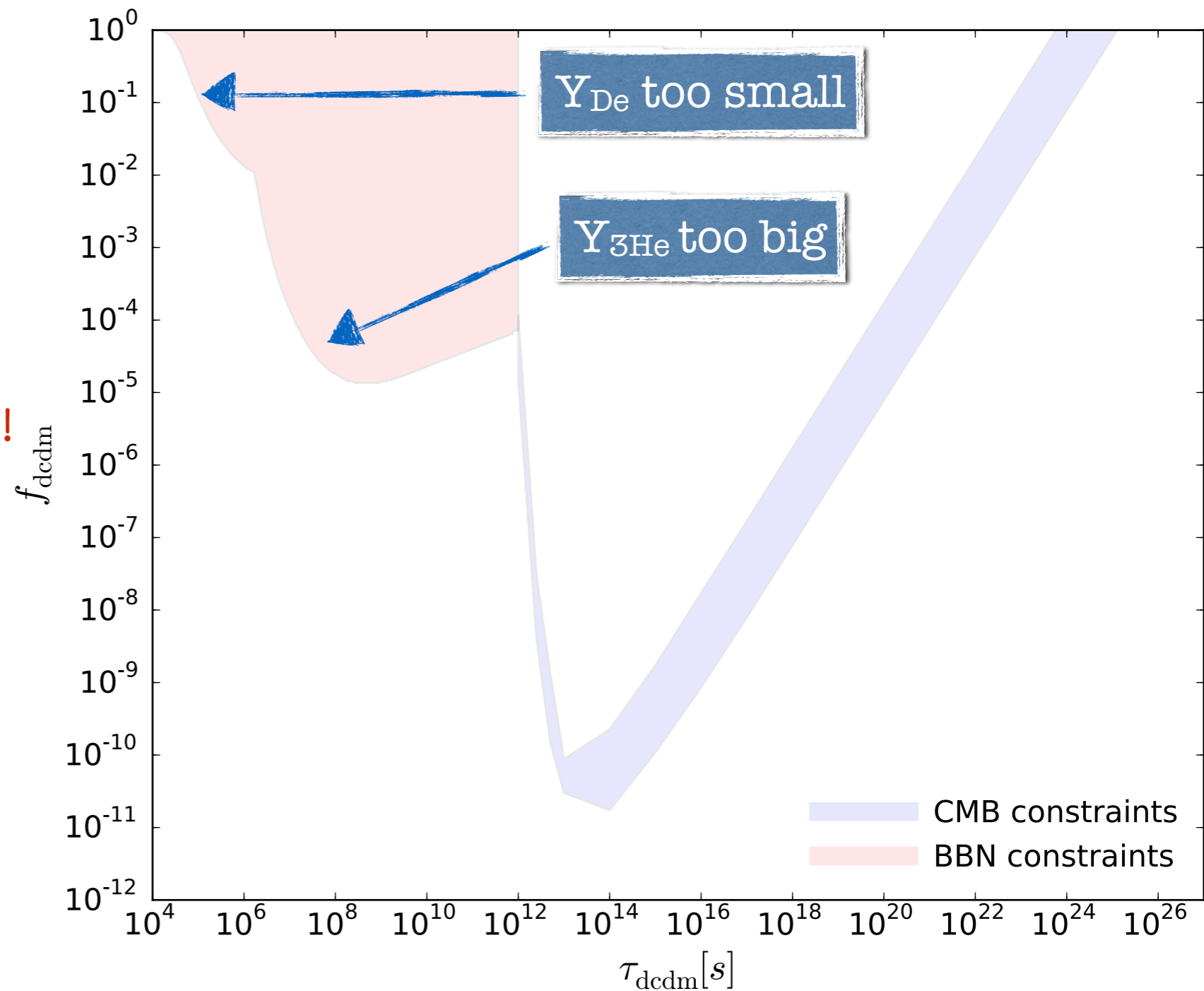
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Those bounds are very conservative !

CMB vs BBN vs spectral distortions

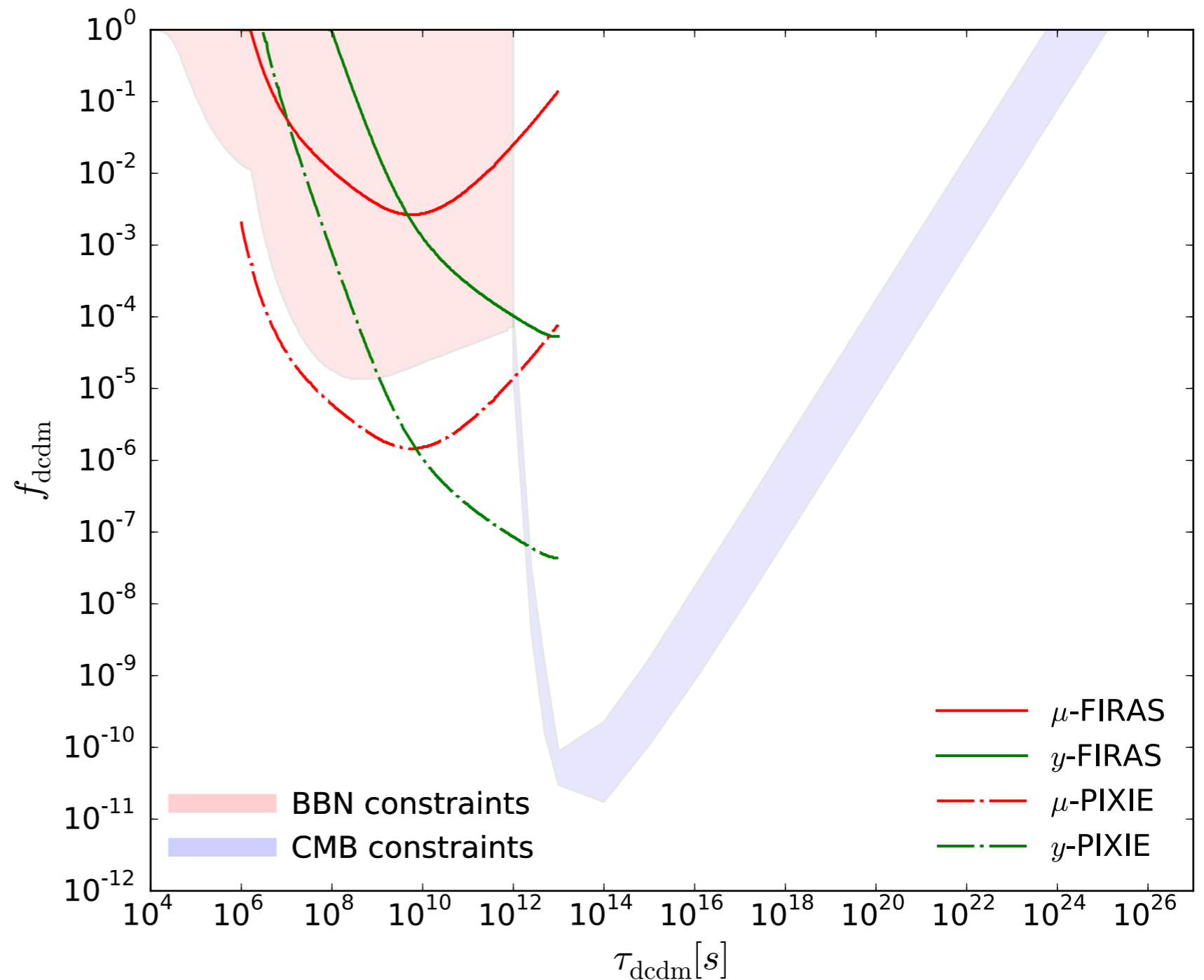
➤ Double Compton /
Bremsstrahlung off

μ = creation of a chemical
potential

➤ Compton Scattering off

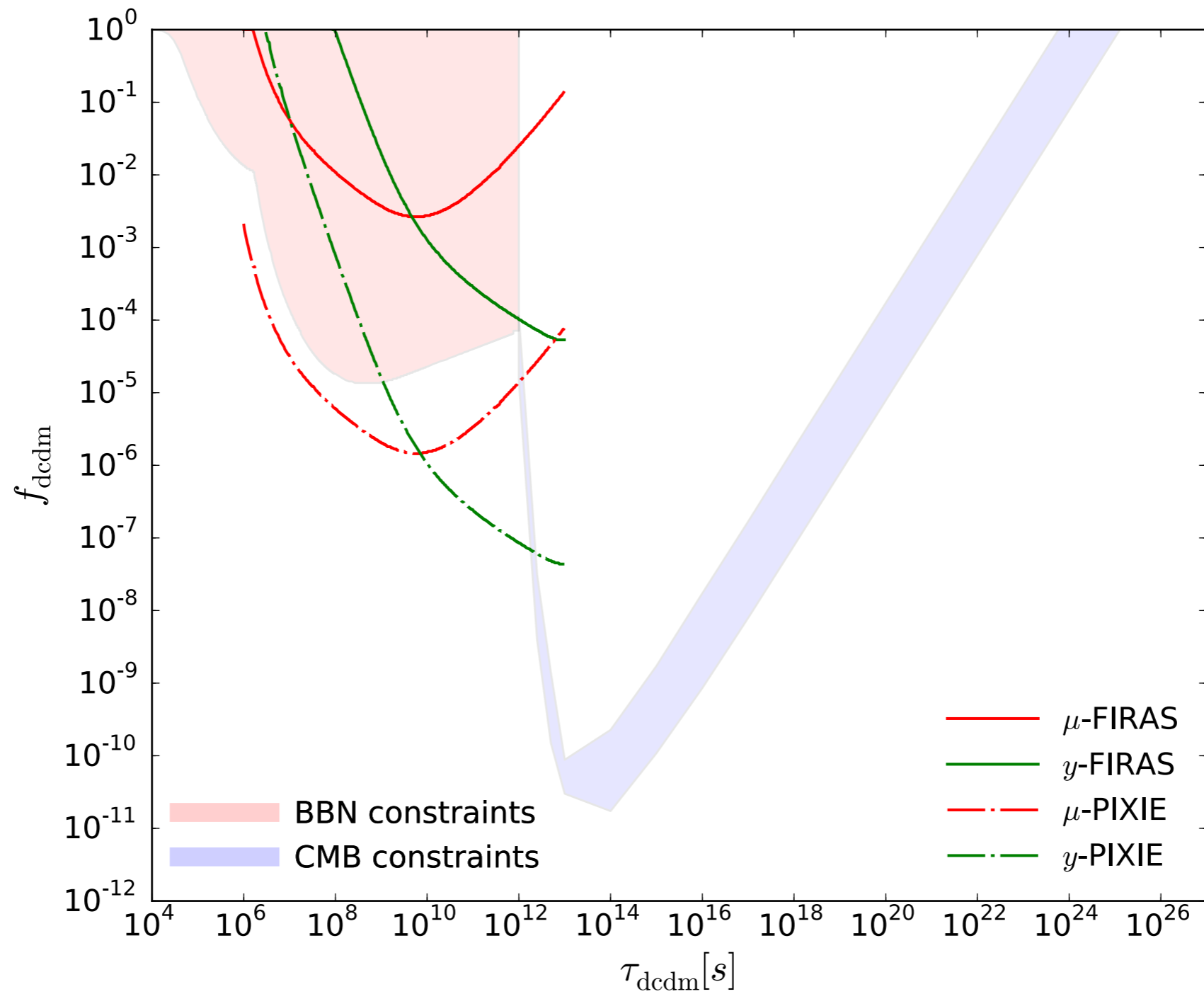
y = Compton heating
(or cooling!) of the CMB gas

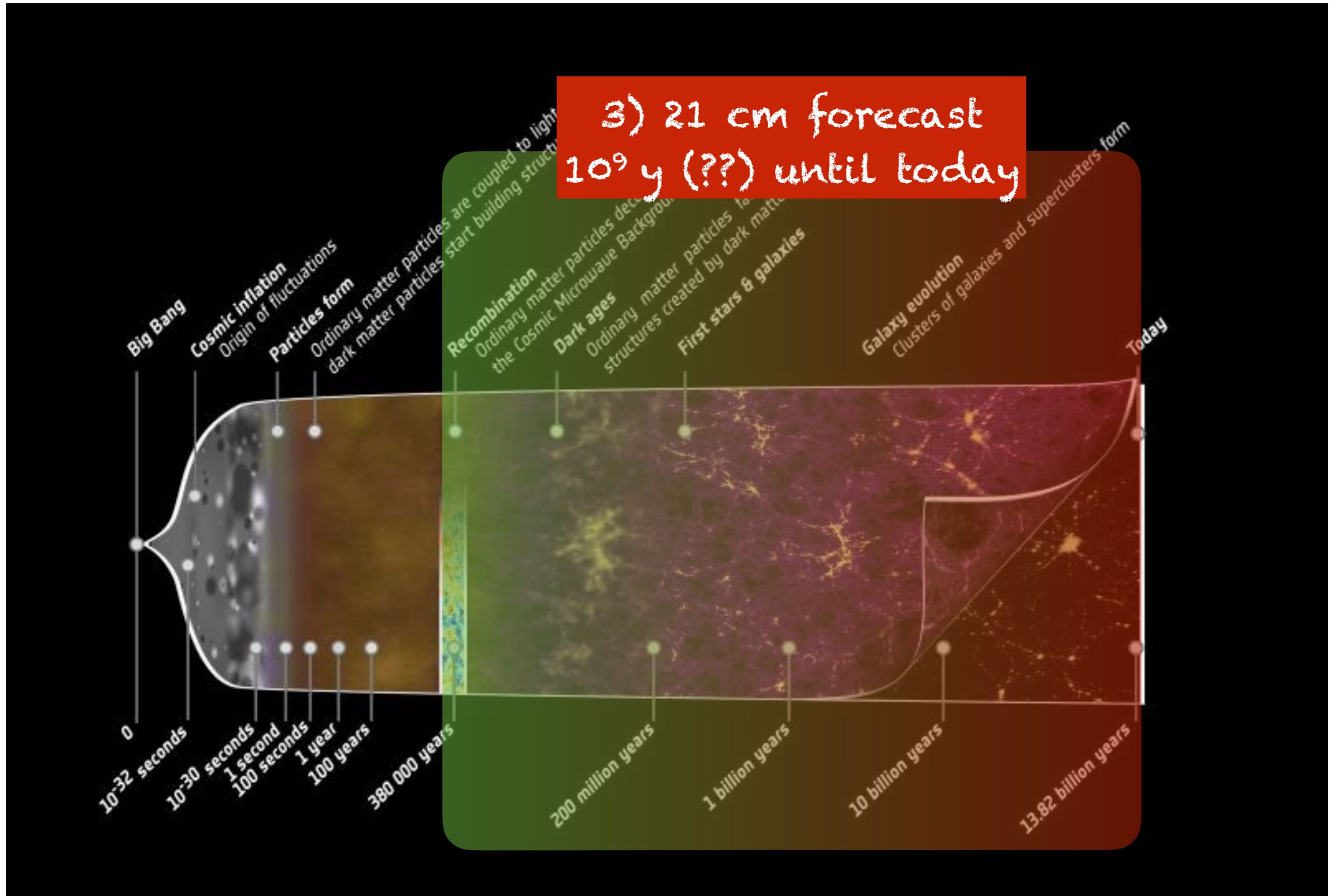
*Review: Chluba & Sunyaev
[arXiv:1109.6552]*

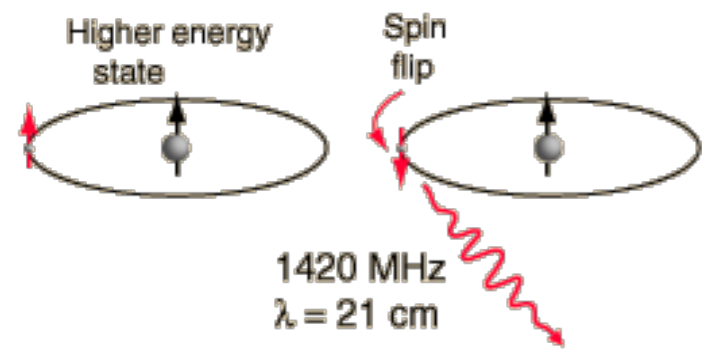


Current constraints from **FIRAS** on the μ and y parameters are worst than BBN.
This will (might) change in the future with **PIXIE** !

A fair « Status of the art », what's next ?







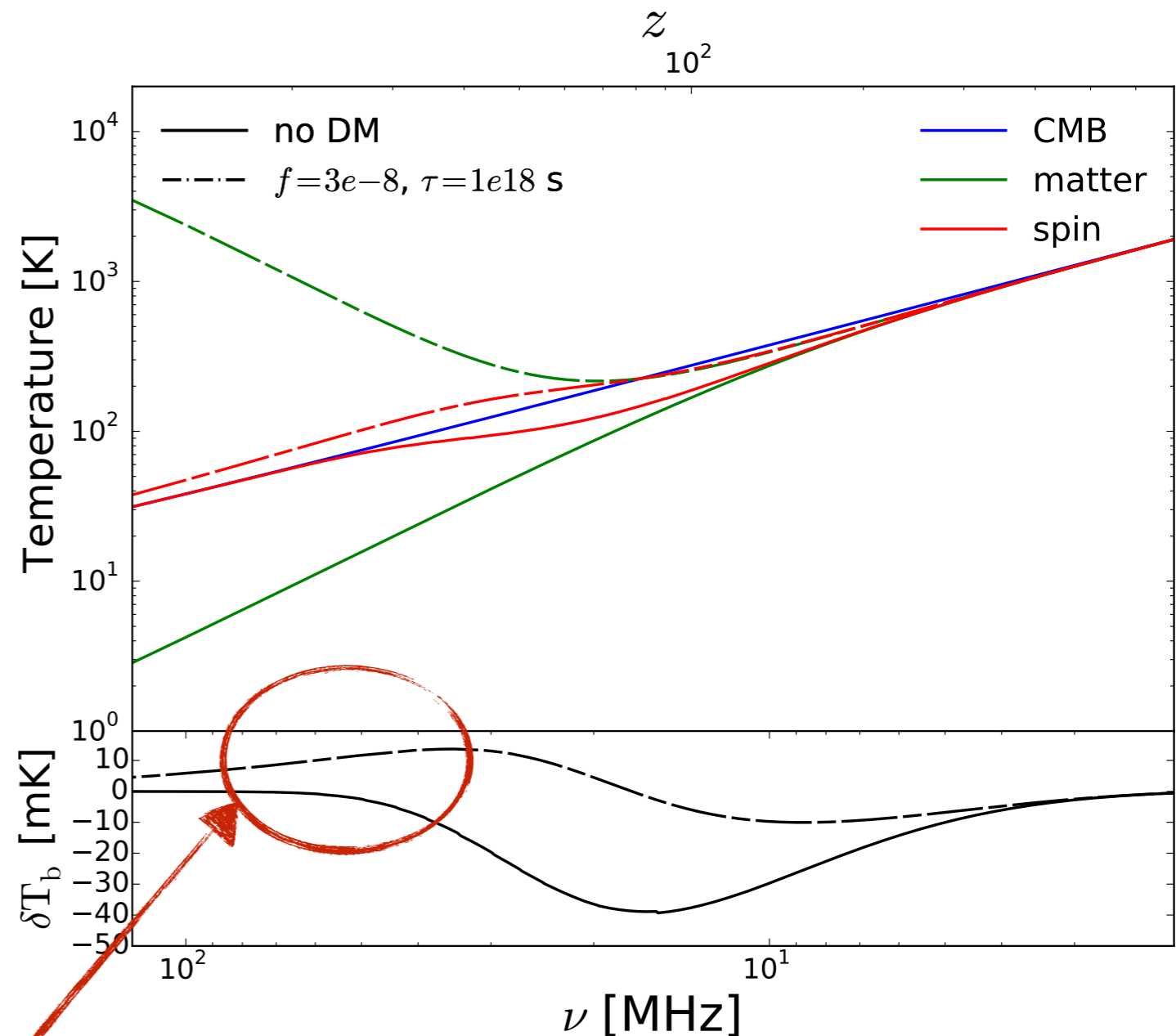
The next-generation experiment : 21 cm with SKA

$$\delta T_b(\nu) = \frac{T_s - T_{\text{CMB}}}{1 + z} (1 - \exp(-\tau_{\nu 21}))$$

At low- z , **large uncertainty** due to star formation leads to **pessimistic results**.

Lopez-Honorez et al.
JCAP 1608 (2016) no.08, 004

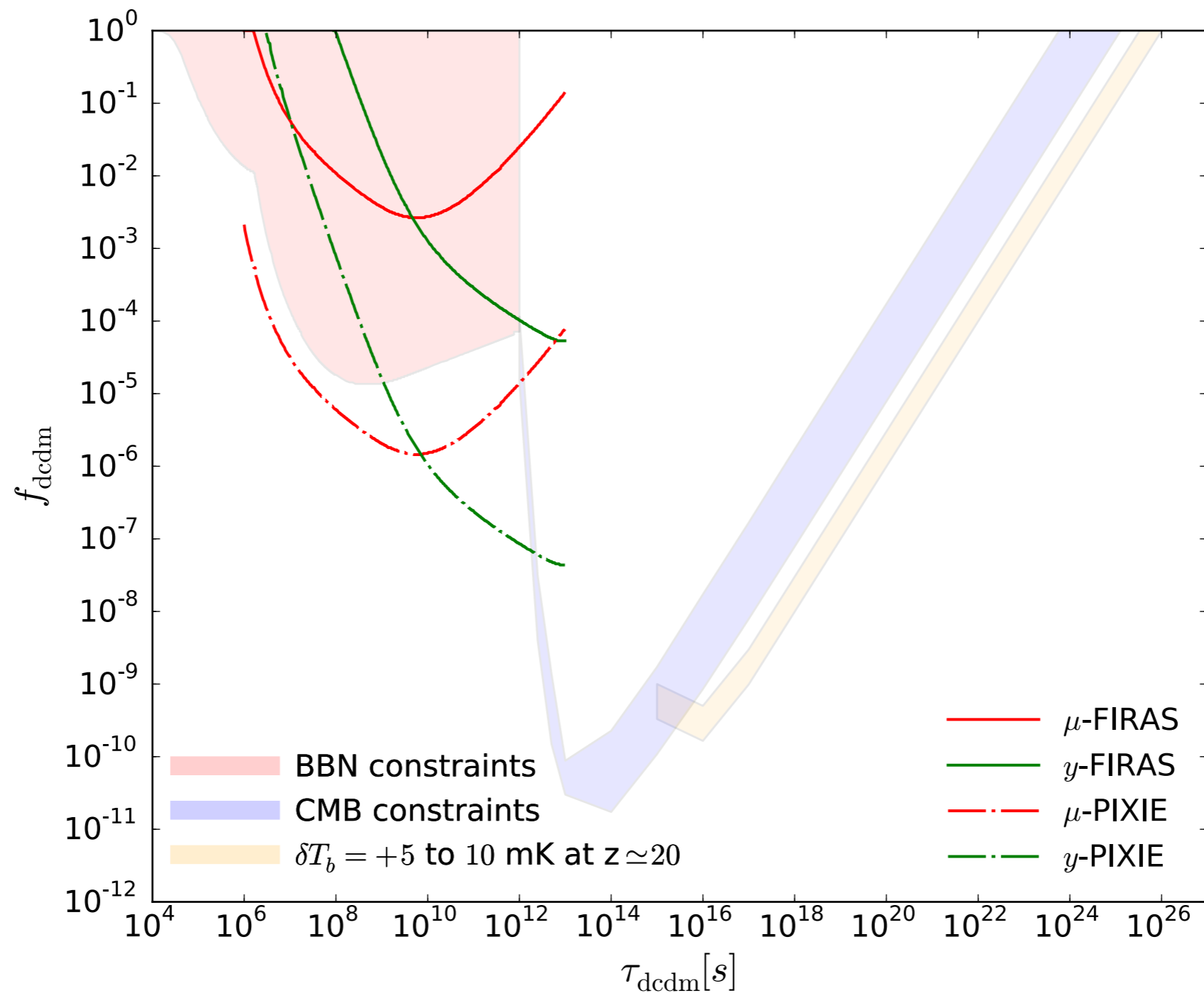
We neglect stars : valid until $z = 20$.
=> SKA will measure $\delta T_b = 5-10$ mK
up to $z = 20/25$ ($\nu = 60$ MHz) !



Potential « smoking gun » signal from DM e.m. decay at the end (and during !) the dark ages

SKA could be better at detecting - or constraining - e.m. decay

very crude treatment, for illustration only :
 next step => add information from power spectrum analysis



Take-home message

Exotic particle decays (including DM) can be strongly constrained by Cosmology.

- Bounds are **competitive with diffuse gamma-ray background** ones.
- Combination of BBN /spectral distortions / CMB allow constraining more than **20 orders of magnitude in lifetime**, and **10 orders of magnitude in abundances**.
- can also **constrain non-electromagnetic decay!**

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Next Step : 21 cm and reionization ! Many experiments are launched (e.g. SKA, HERA).

- First result quite pessimistic given the **huge astrophysical uncertainties**.
- Some hope : the **dark ages**, when no stars were there.

Take-home message

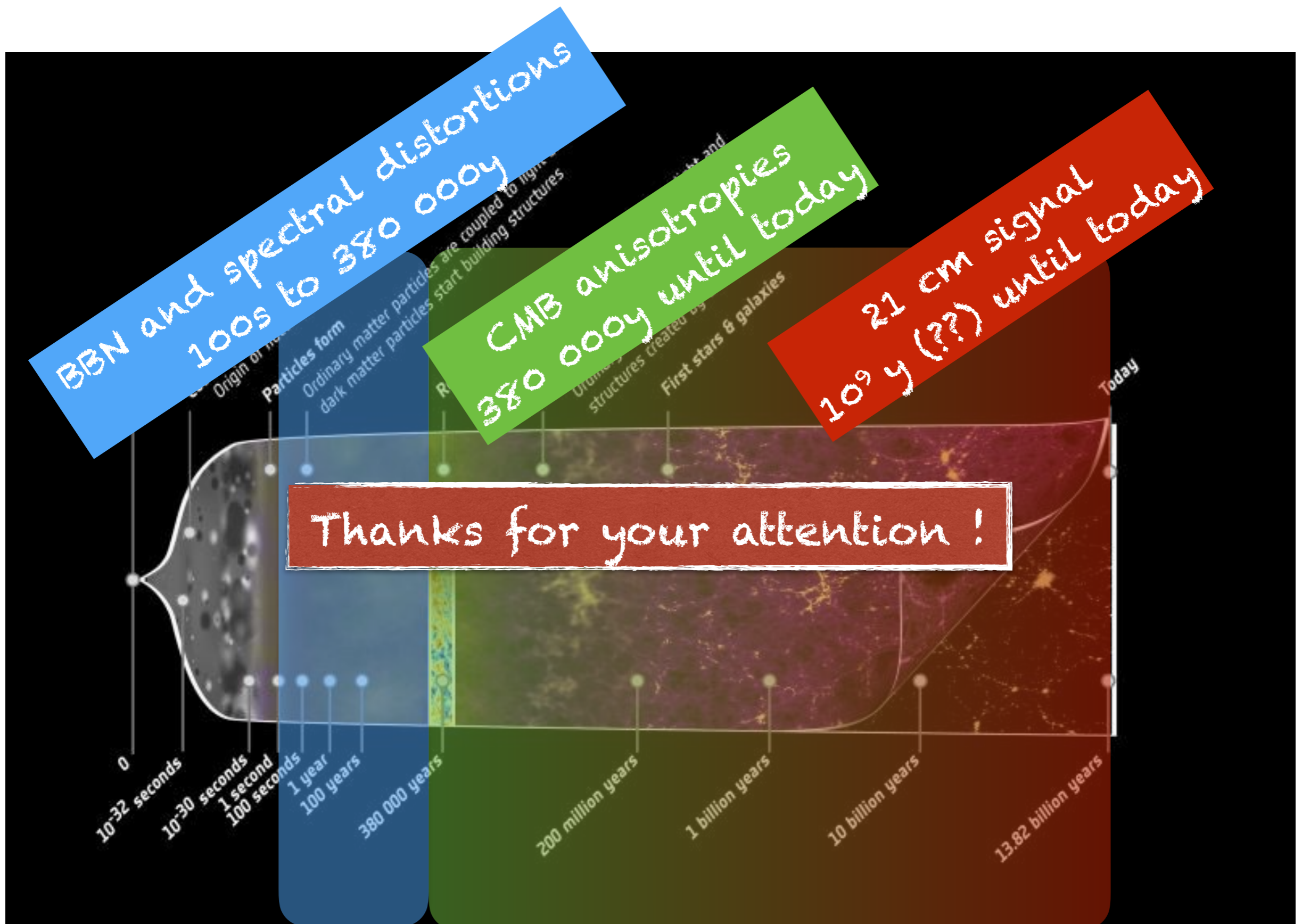
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Stay tuned ! Many results to come !



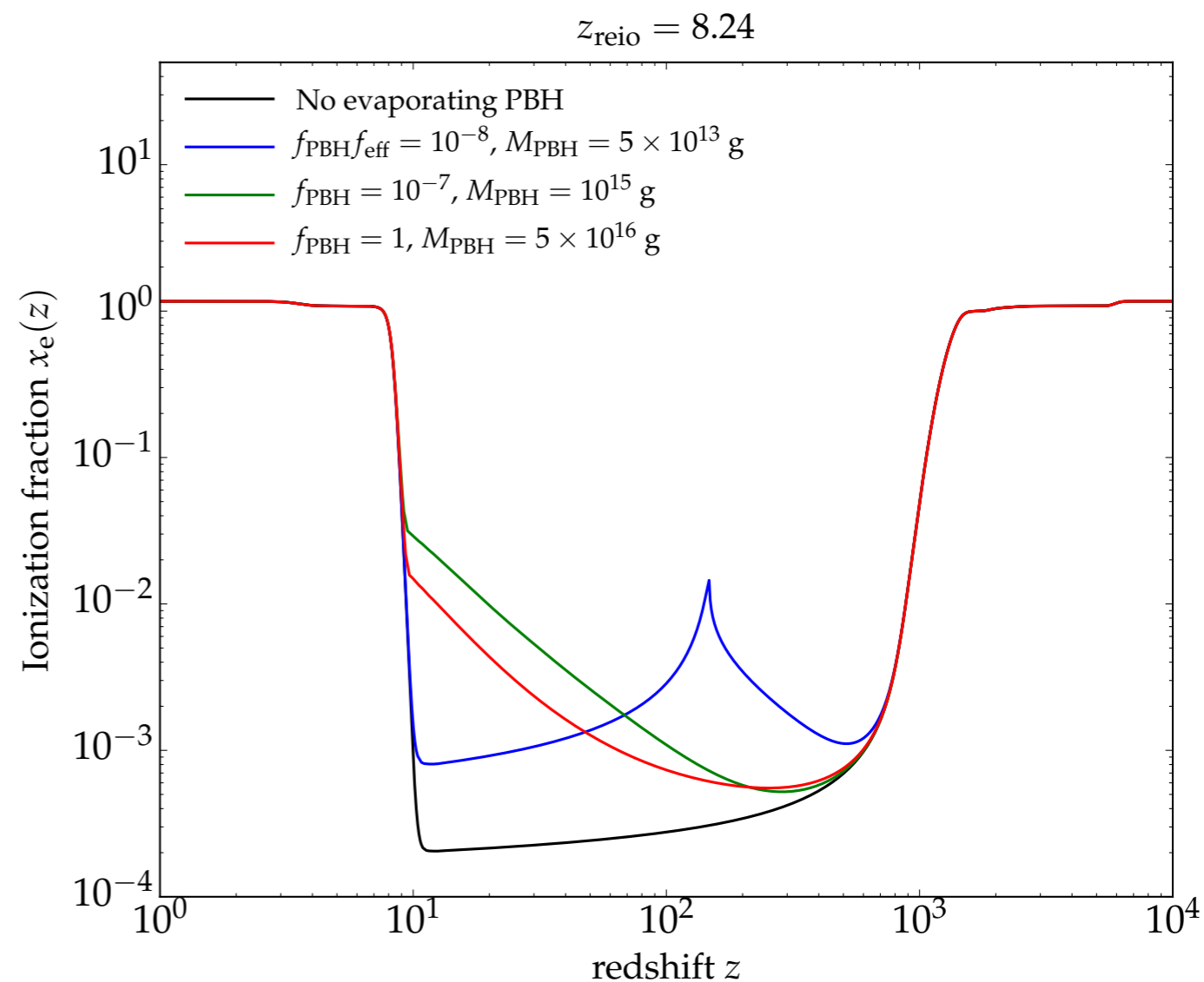
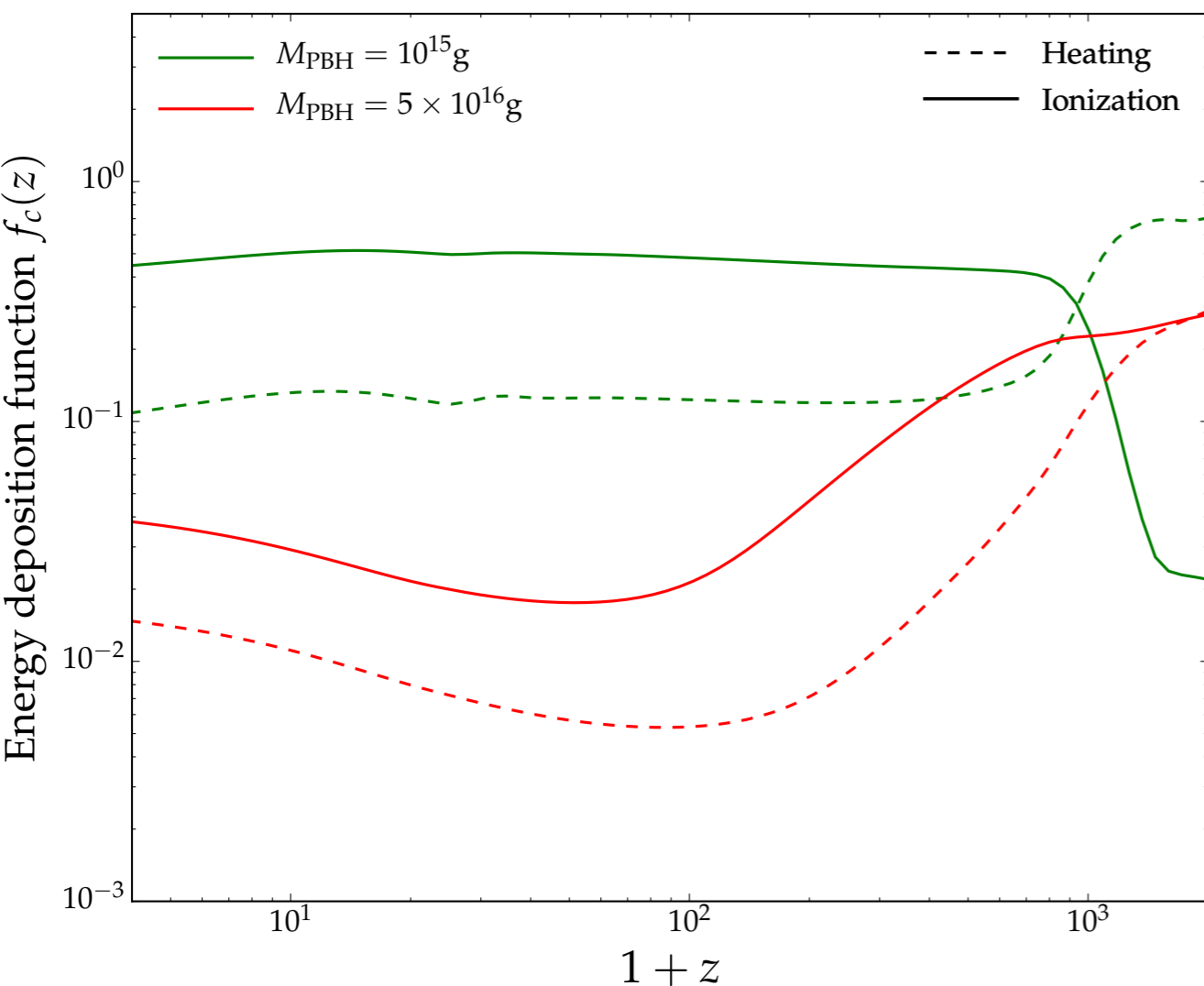
Backup slides

Constraints on evaporating PBH (1)

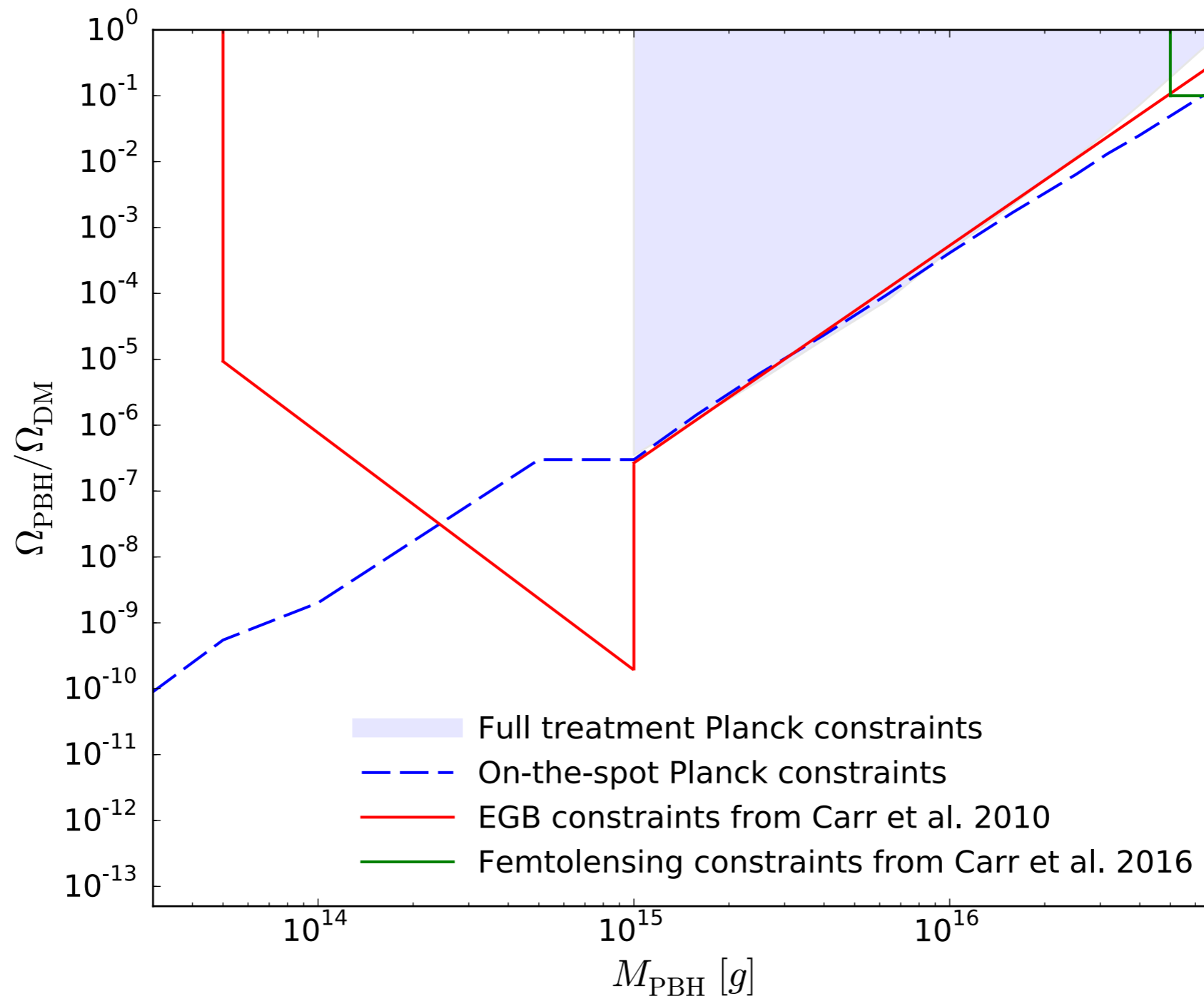
Hawking, Nature 248, 30 (1974), more details in Carr et al. PRD81 (2010) 104019

$$T_{\text{BH}} = \frac{1}{8\pi GM} \simeq 1.06 \left(\frac{10^{10} \text{g}}{M} \right) \text{TeV}$$

$$\Gamma_{\text{PBH}}^{-1} \simeq 407 \left(\frac{15.35}{\mathcal{F}(M)} \right) \left(\frac{M}{10^{10} \text{g}} \right)^3 \text{s}$$

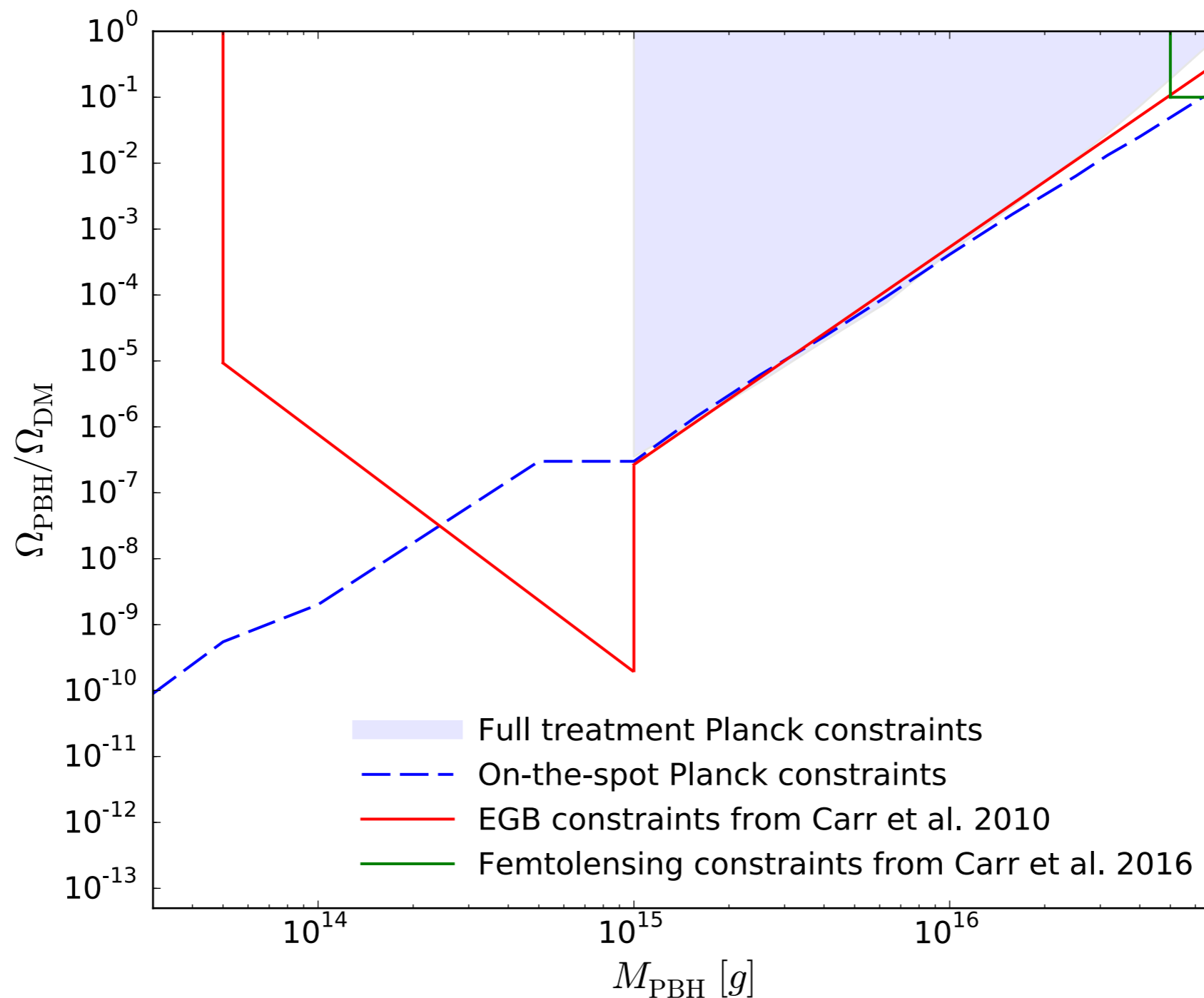


Constraints on evaporating PBH (2)



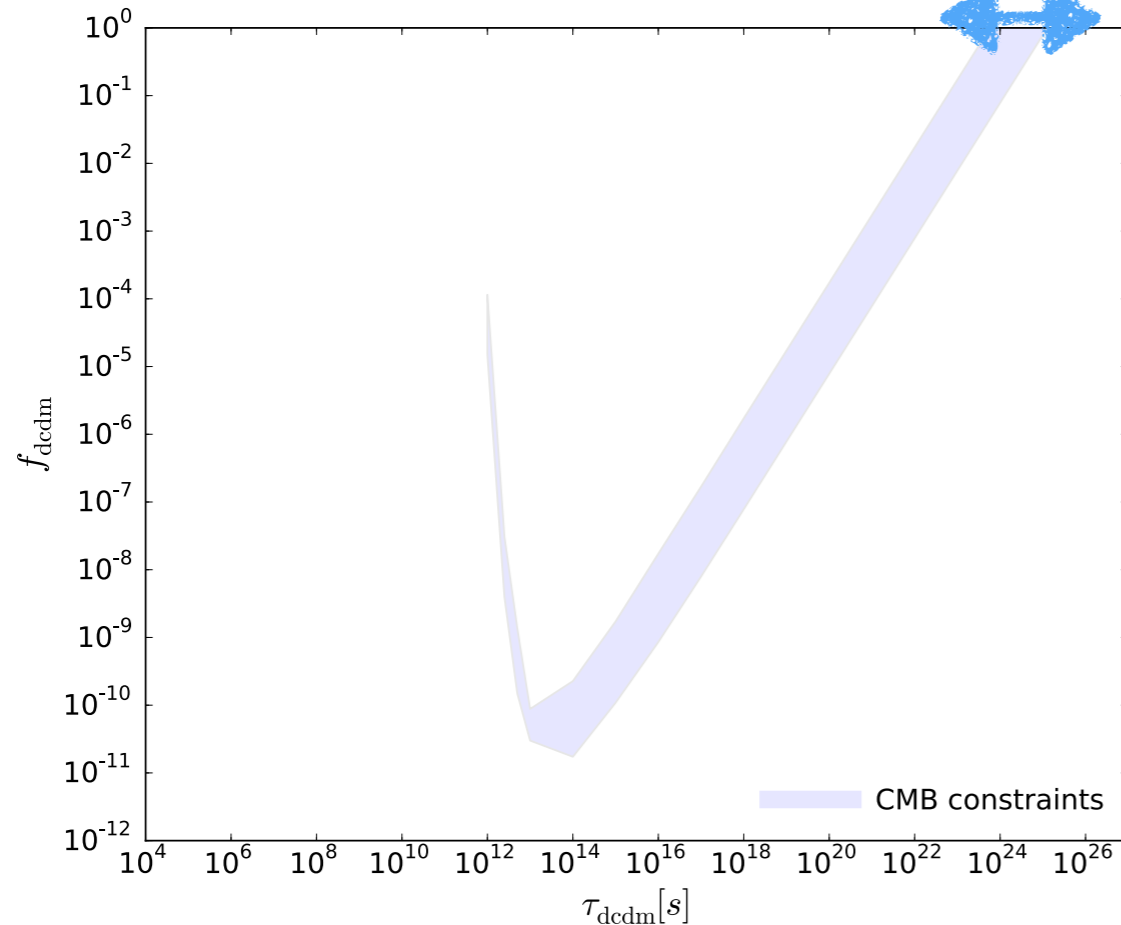
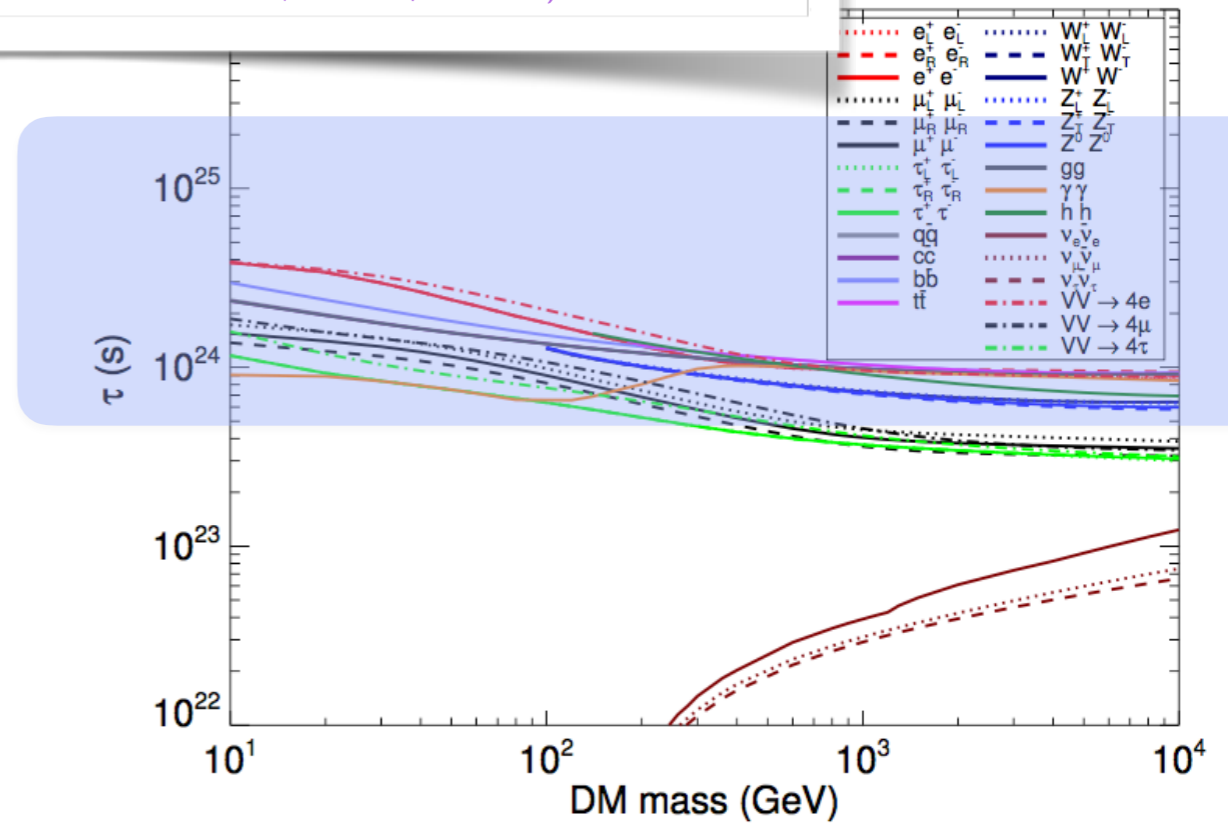
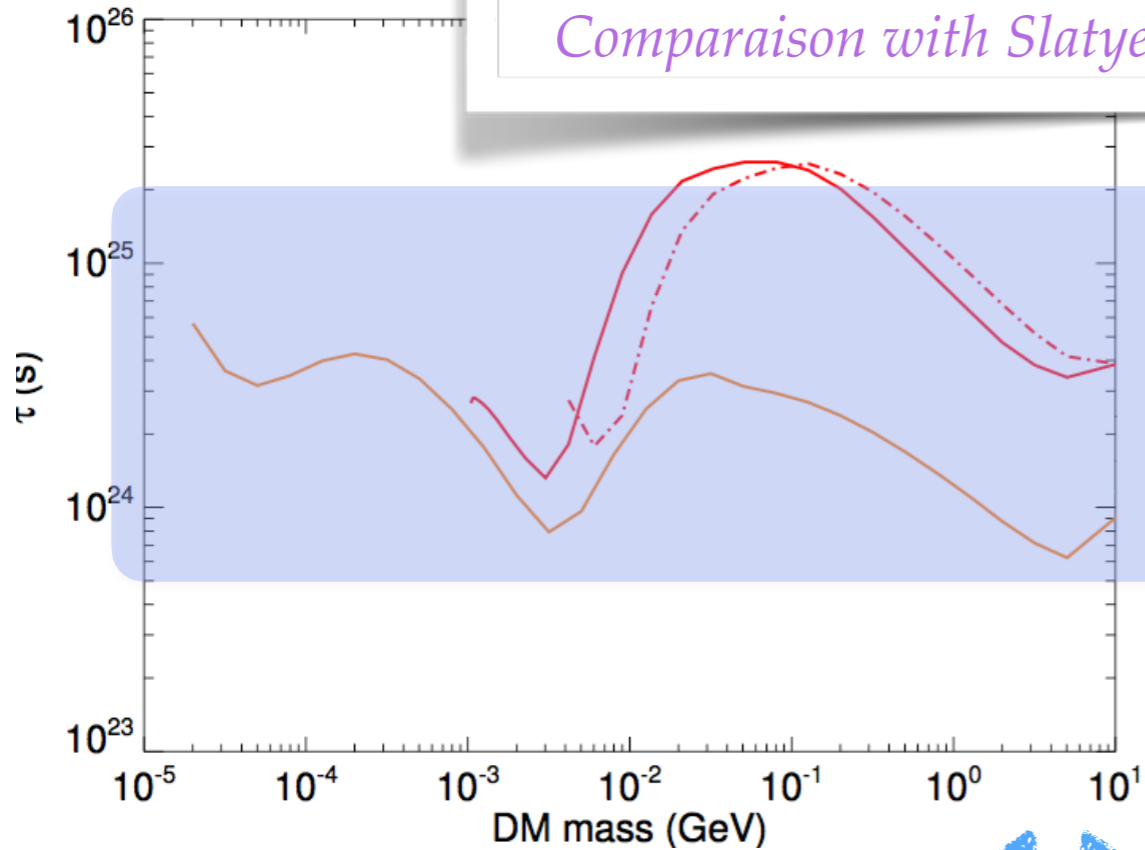
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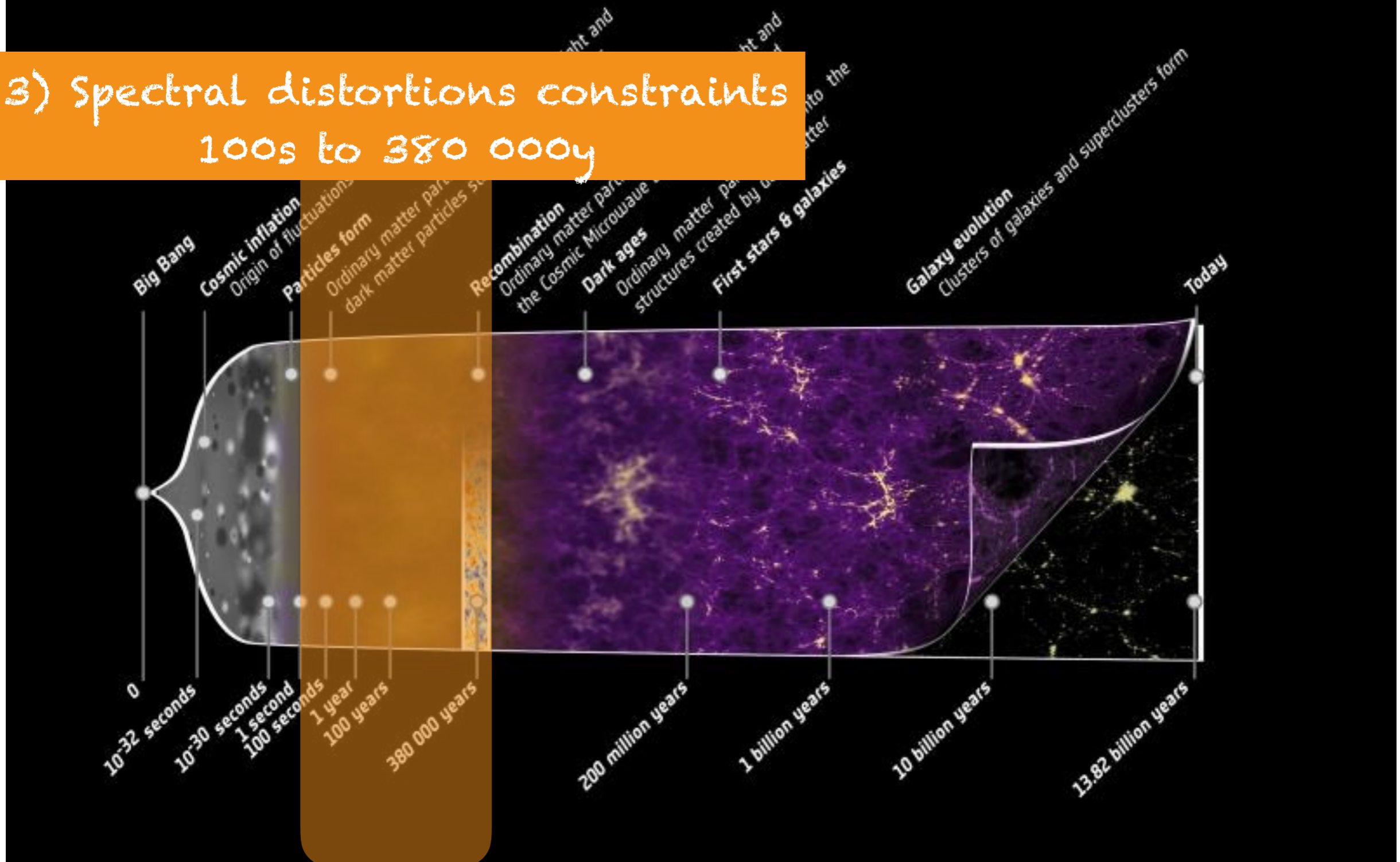
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Comparison with Slatyer & Wu PRD 95 (2017) no.2, 023010



- « Proof of principle »:
All decay channels and masses are contained in the uncertainty band, except neutrinos.
- Models with invisible decay products should typically rescale bound by the corresponding e.m. BR

3) Spectral distortions constraints 100s to 380 000y



μ and y spectral distortions

*see e.g. Chluba & Sunyaev
[arXiv:1109.6552]*

Most important processes to thermalize any energy injection are
Bremsstrahlung, Compton and Double-Compton scattering.

If those processes go out of equilibrium, in full generality:

$$\Delta I(\nu) = I_{\text{true}}(\nu) - I_{\text{bb}}(\nu)$$

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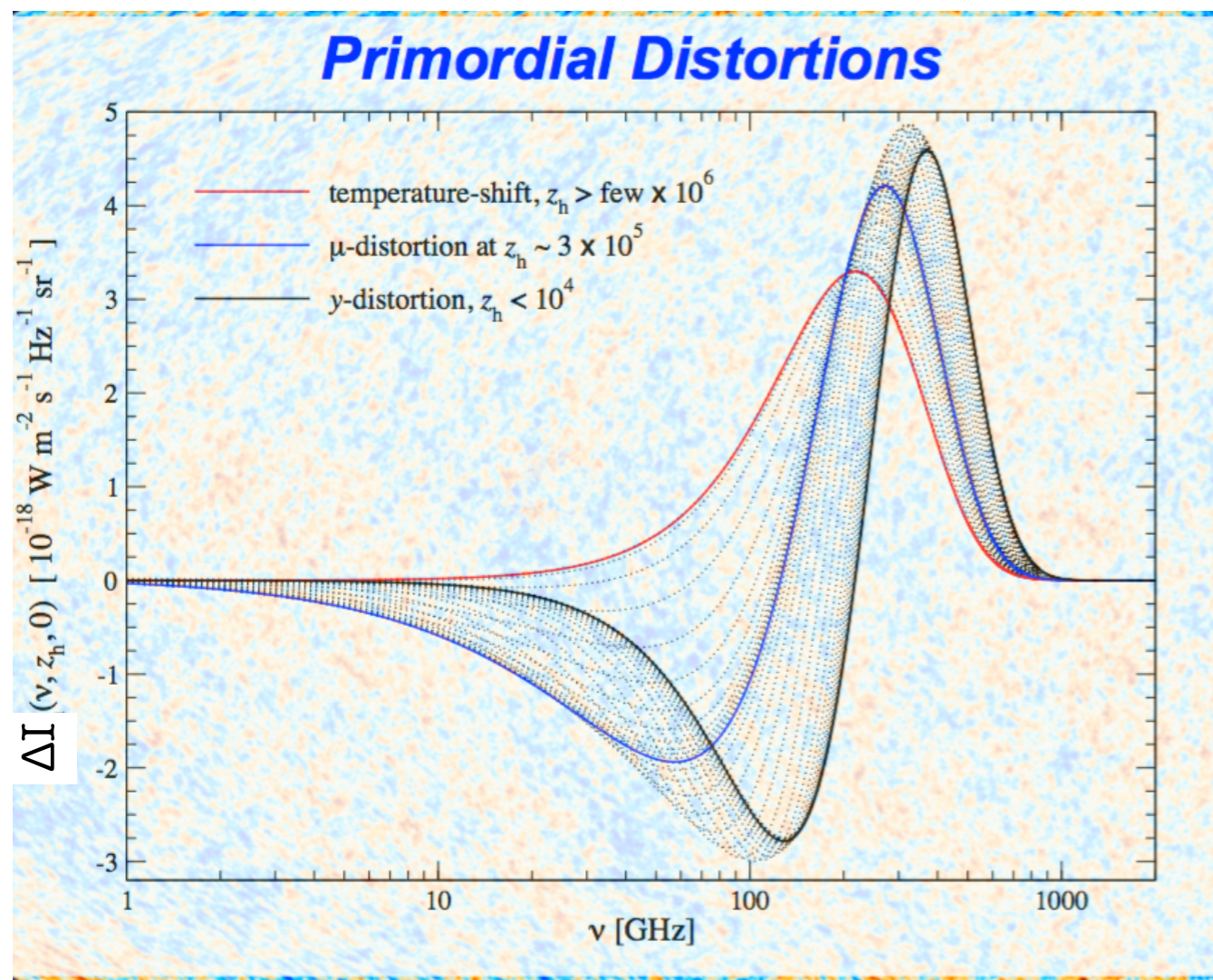
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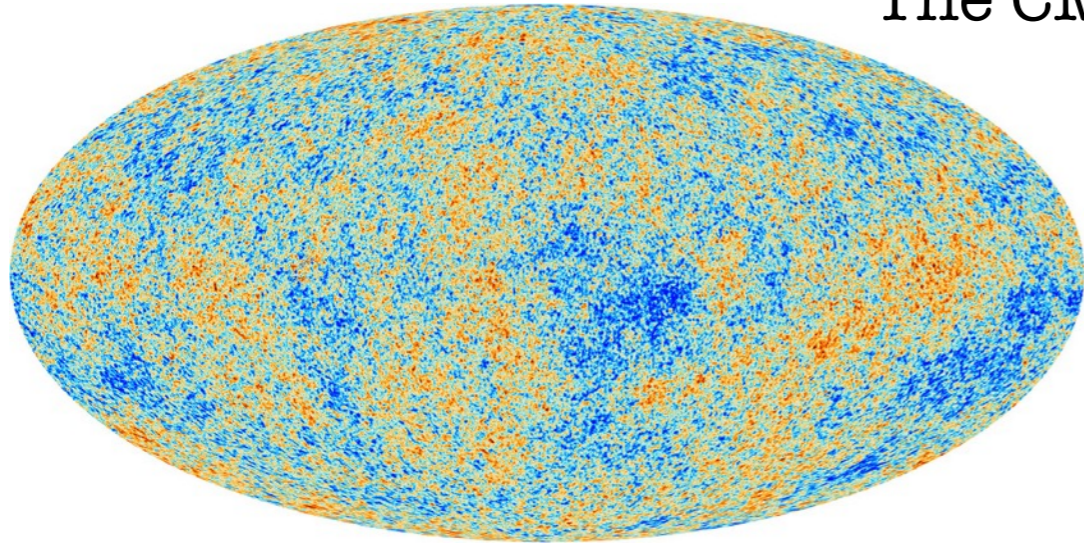
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Intermediate distortions probe the time dependence of the energy injection history

credit: Jens Chluba, « Ecole de Gif », 2014

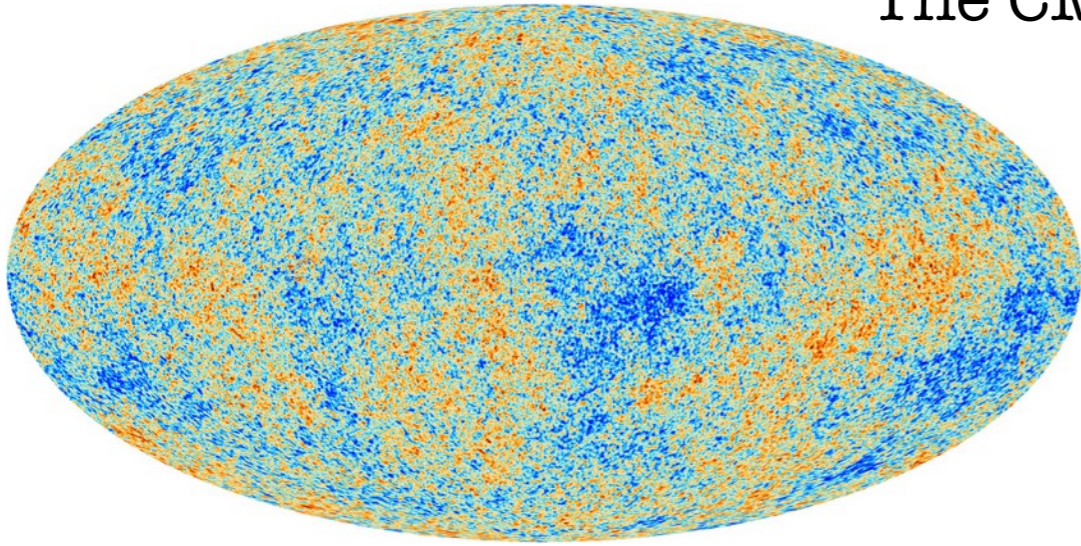
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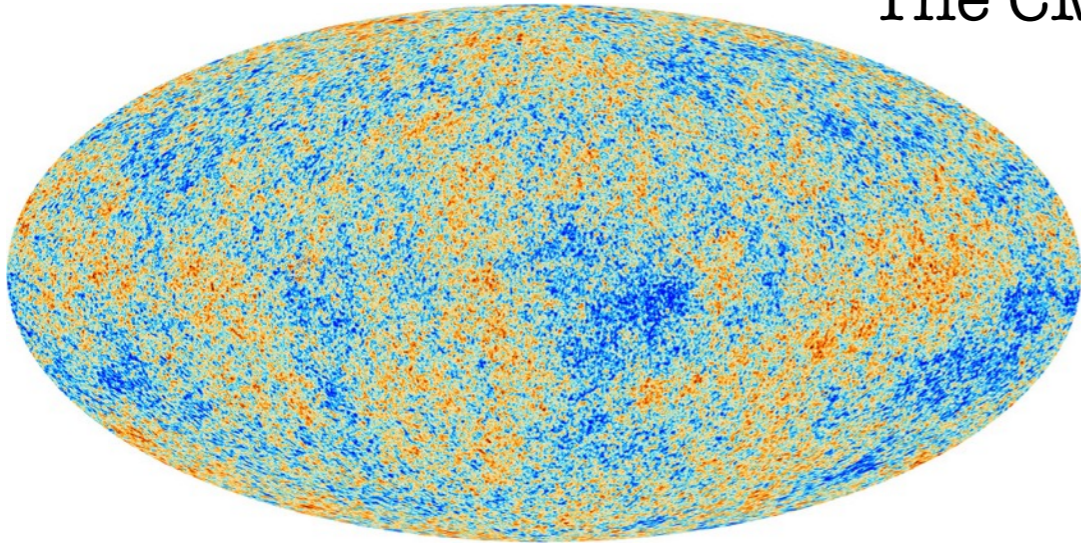
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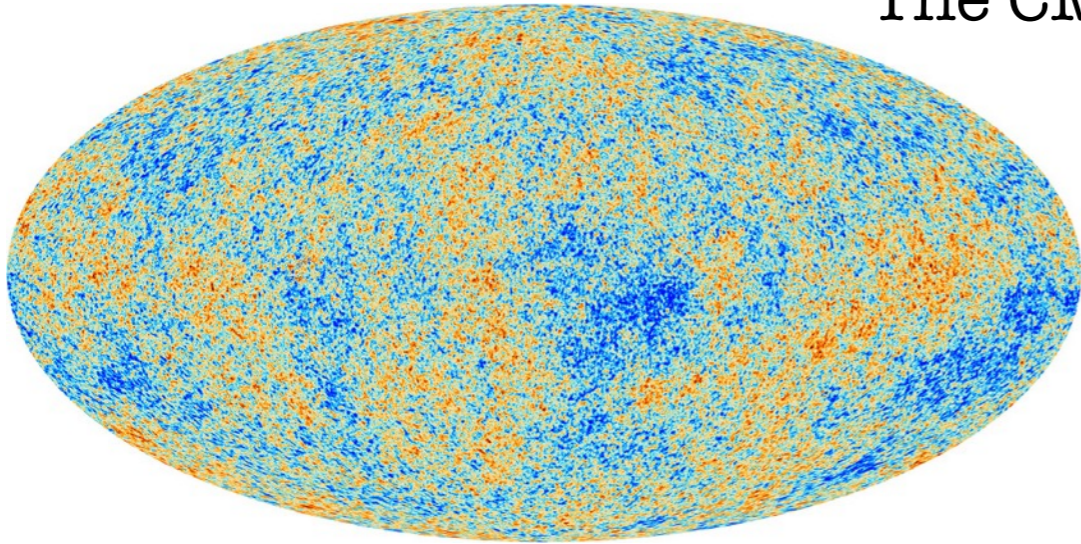
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the so called « n-points correlation functions »

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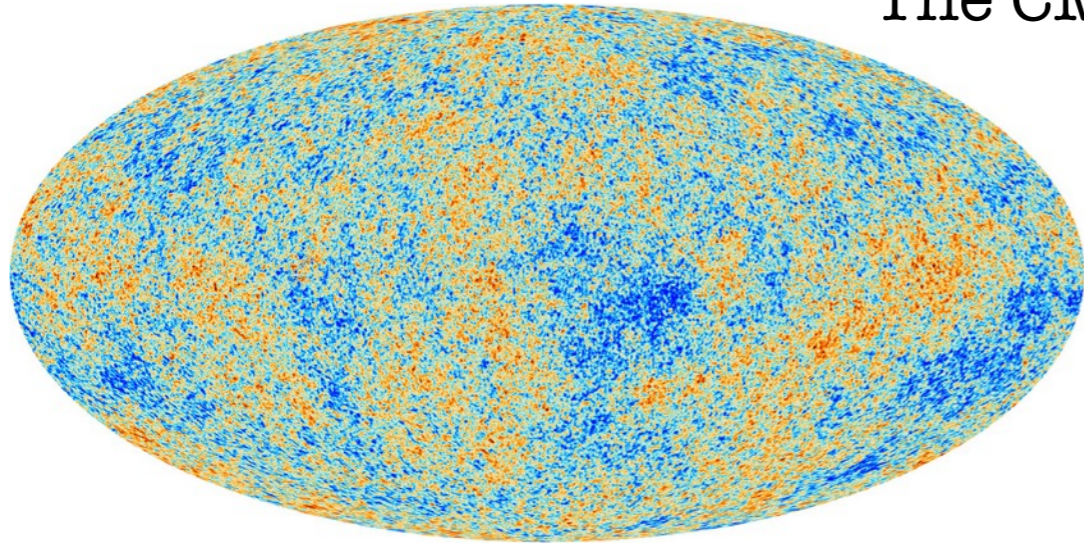
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Only 2 moments of interest :

$$\langle \Theta(\vec{n}) \rangle = 0 \quad \langle \Theta(\vec{n}_1) \Theta(\vec{n}_2) \rangle \neq 0$$

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6 free parameters to fit : $\{\omega_b, \omega_{cdm}, h, A_s, n_s, z_{reio}\}$

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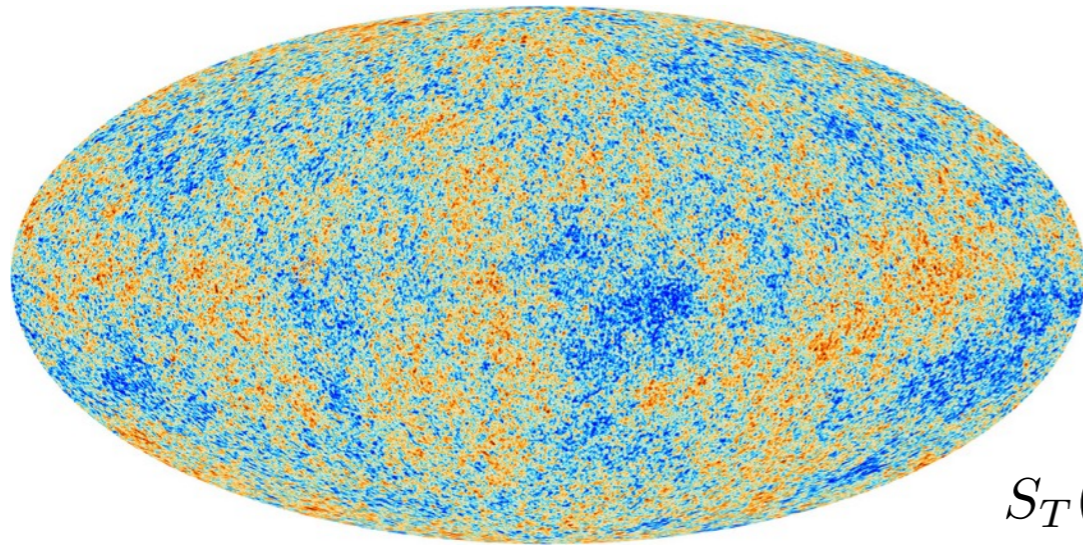
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DM interacts only gravitationally in the standard Cosmology
=> Constraints can be derived

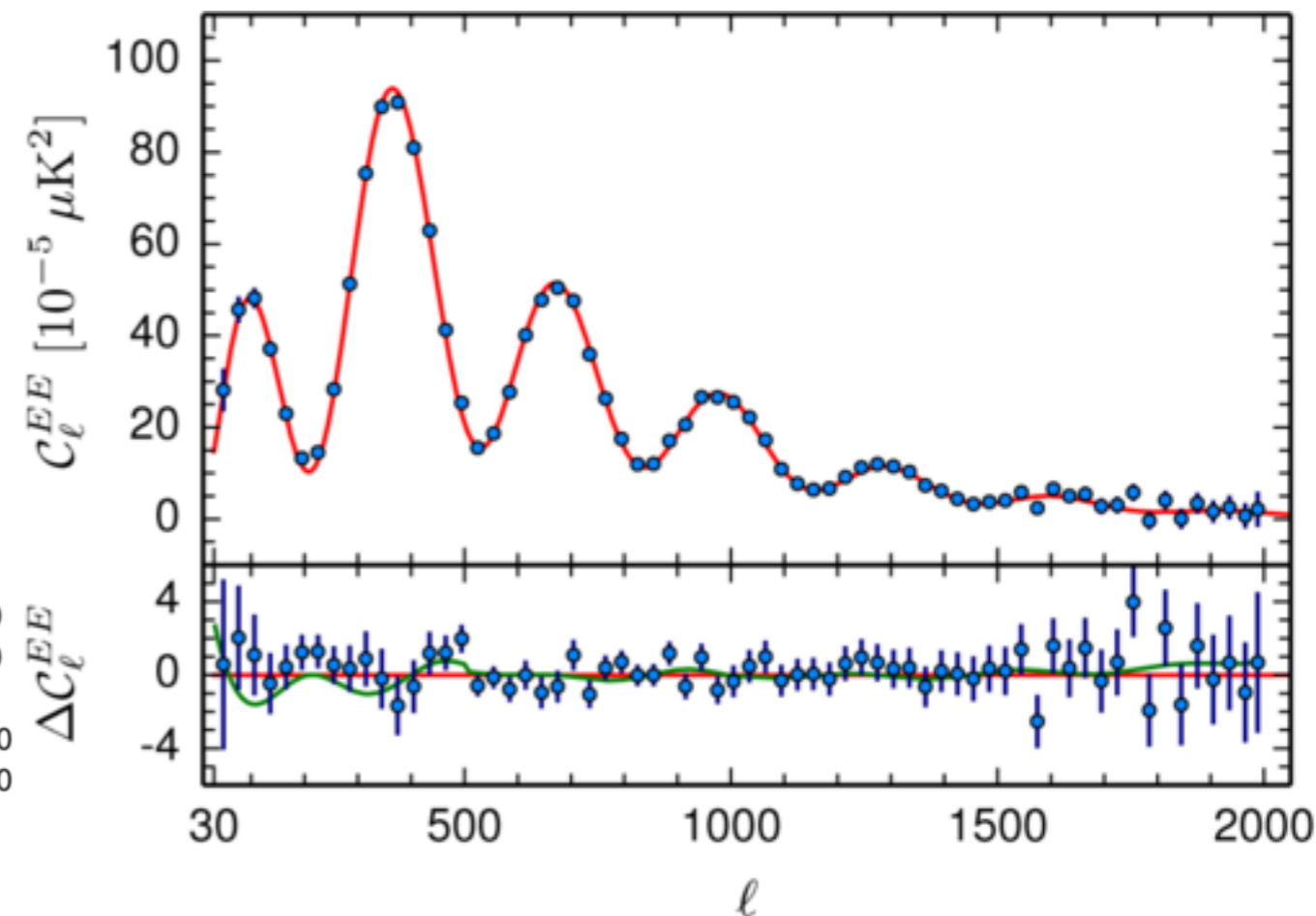
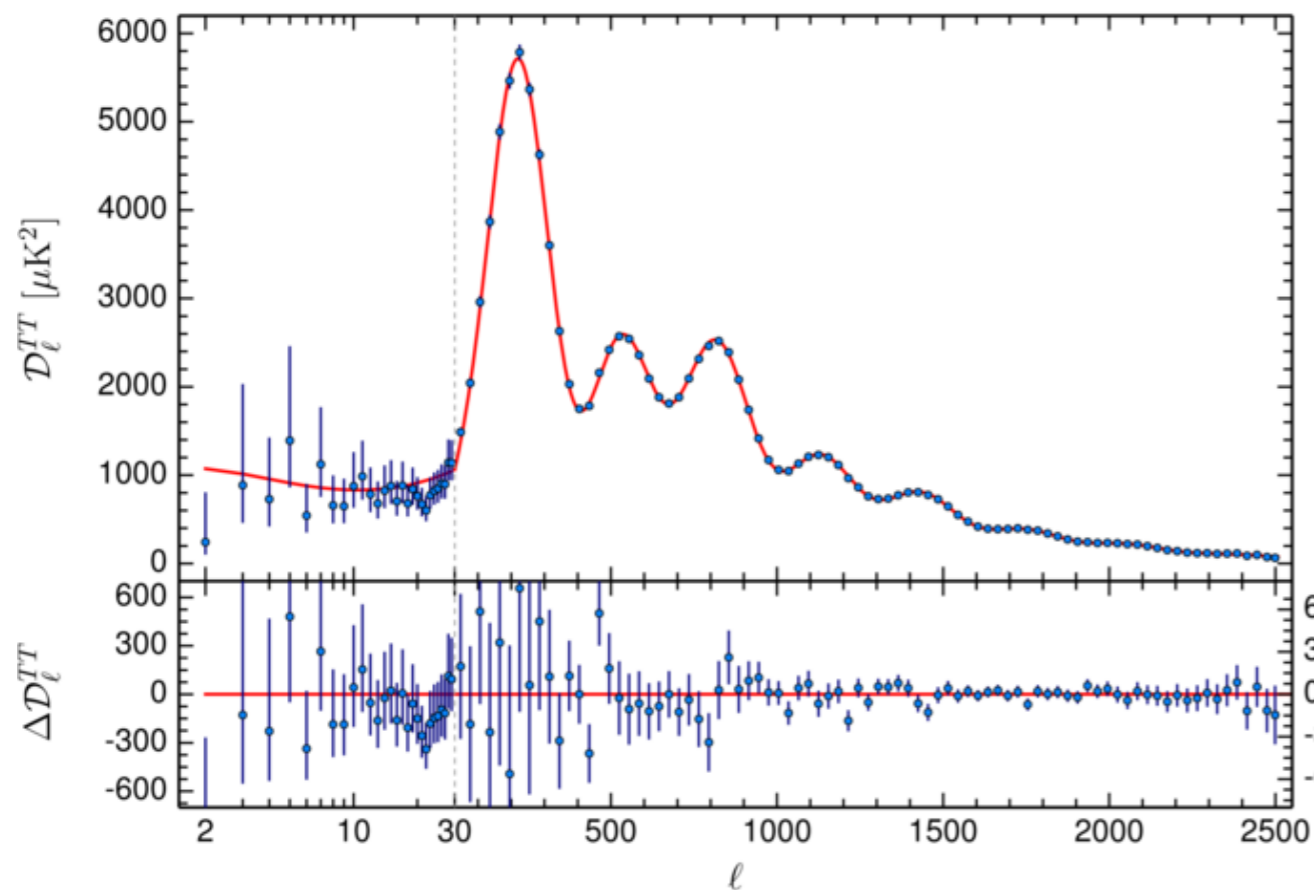


$$C_\ell = \int \frac{dk}{k} \mathcal{P}_{\mathcal{R}}(k) [\Theta_\ell(\tau_0, k)]^2$$

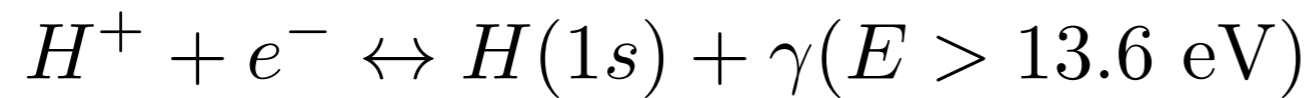
$$\Theta_\ell(\tau_0, k) = \int_\tau^{\tau_0} d\tau S_T(\tau, k) j_\ell(k(\tau_0 - \tau))$$

$$S_T(k, \tau) \equiv \underbrace{g(\Theta_0 + \psi)}_{\text{SW}} + \underbrace{(gk^{-2}\theta_B)'}_{\text{Doppler}} + \underbrace{e^{-\kappa}(\phi' + \psi')}_{\text{ISW}} + \text{polarisation}$$

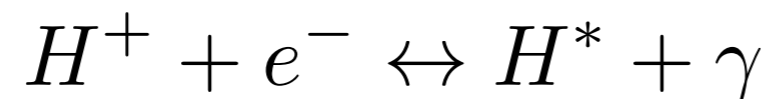
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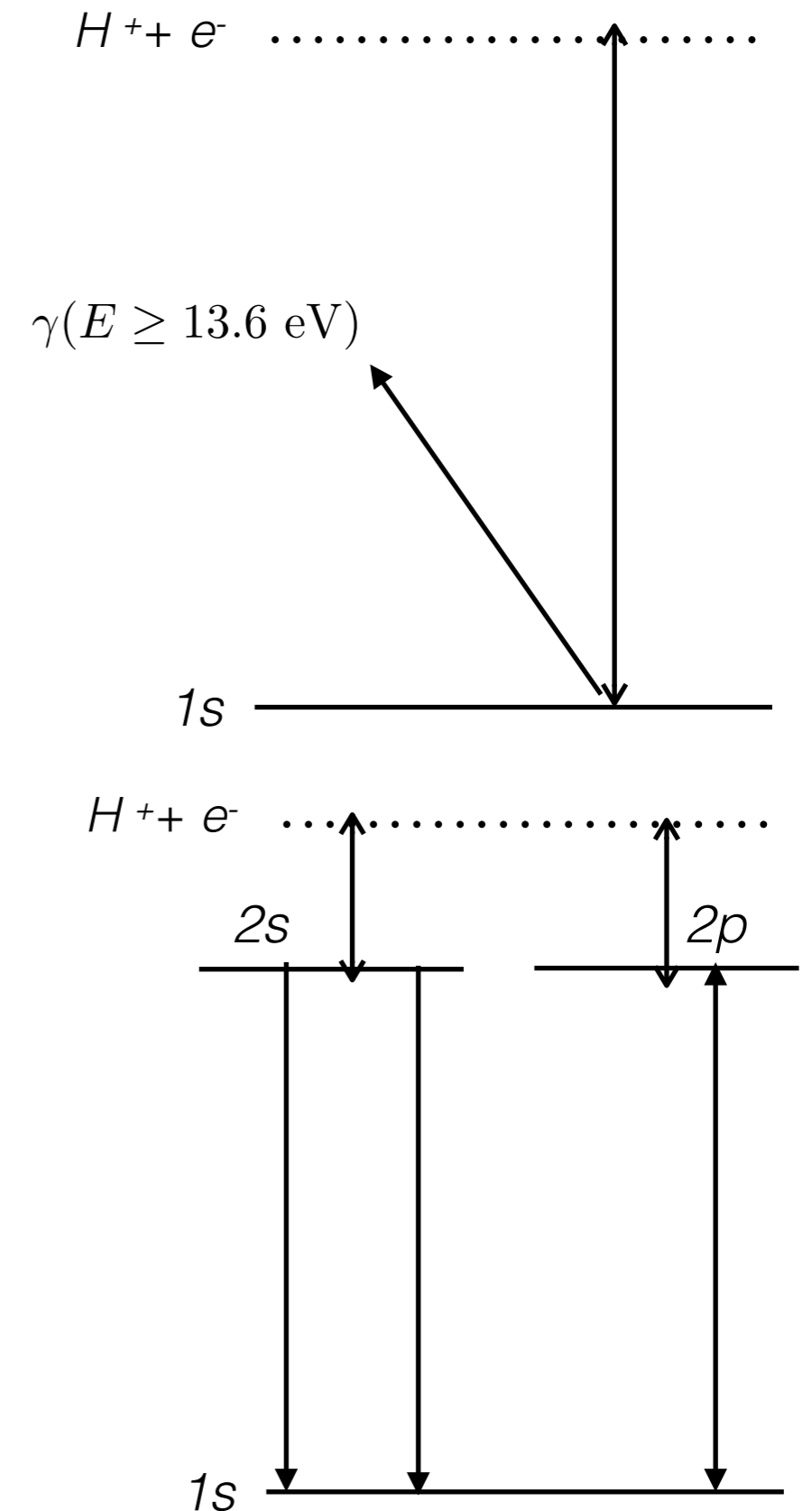
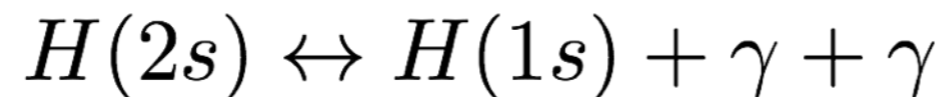
Recombination in a nutshell



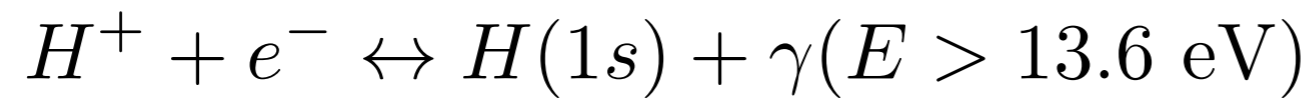
leads to the « saha » equation at equilibrium



followed by

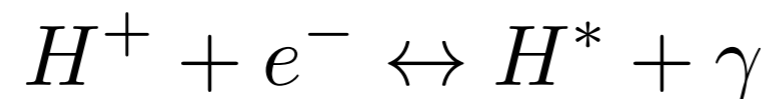


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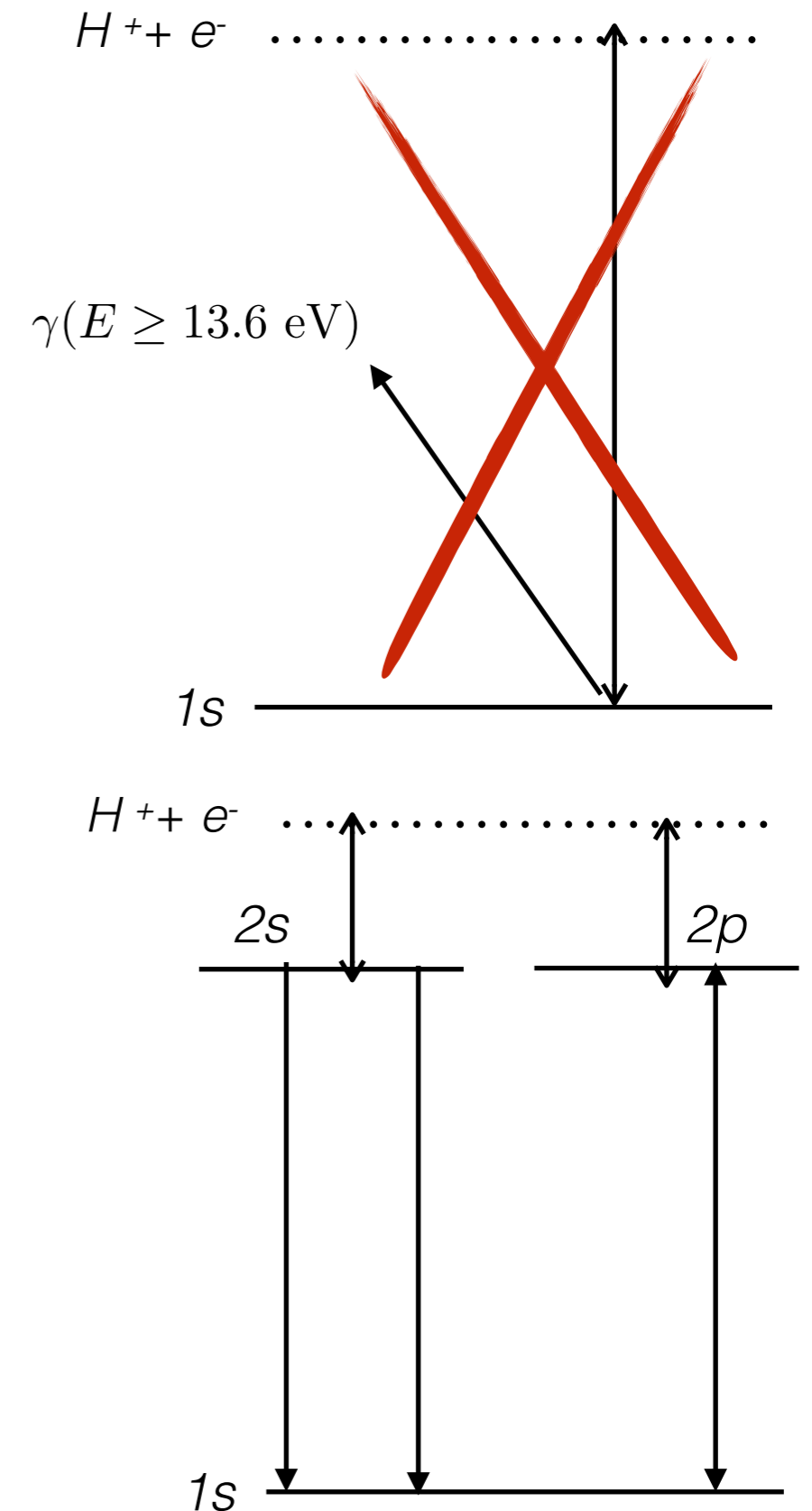
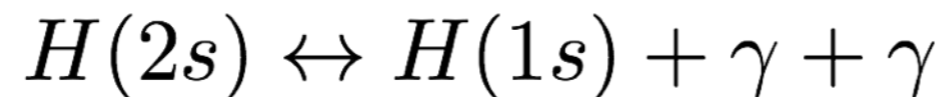


leads to the « saha » equation at equilibrium

The « three-levels atom »



followed by



Recombination as a nutshell

Peebles « case-b » recombination

$$e^- \leftrightarrow H(1s) + \gamma(E > 13.6 \text{ eV})$$

leads to the « saha » equation at equilibrium

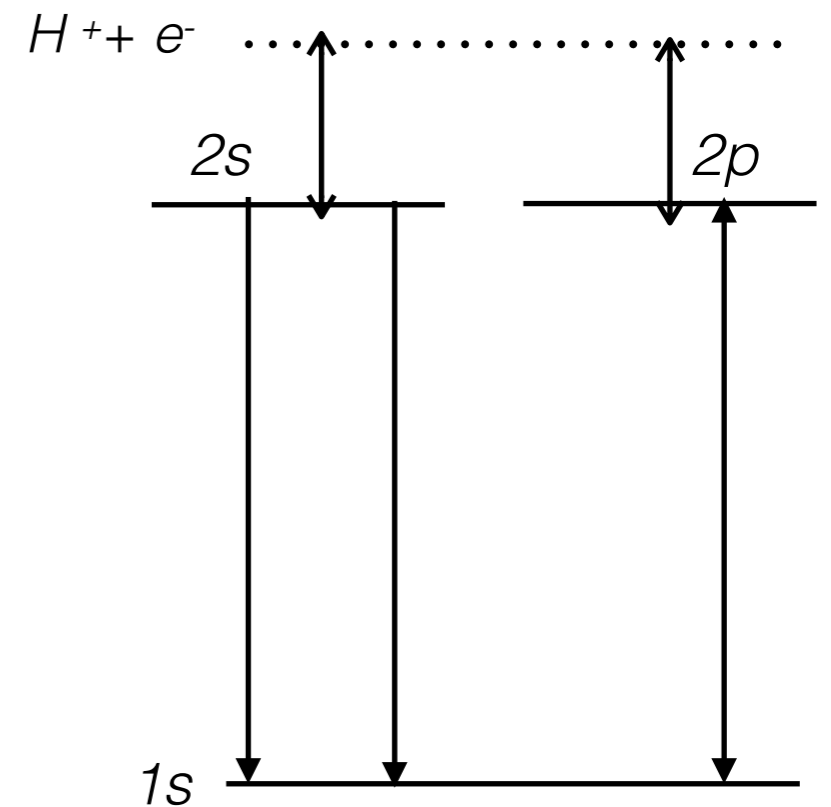
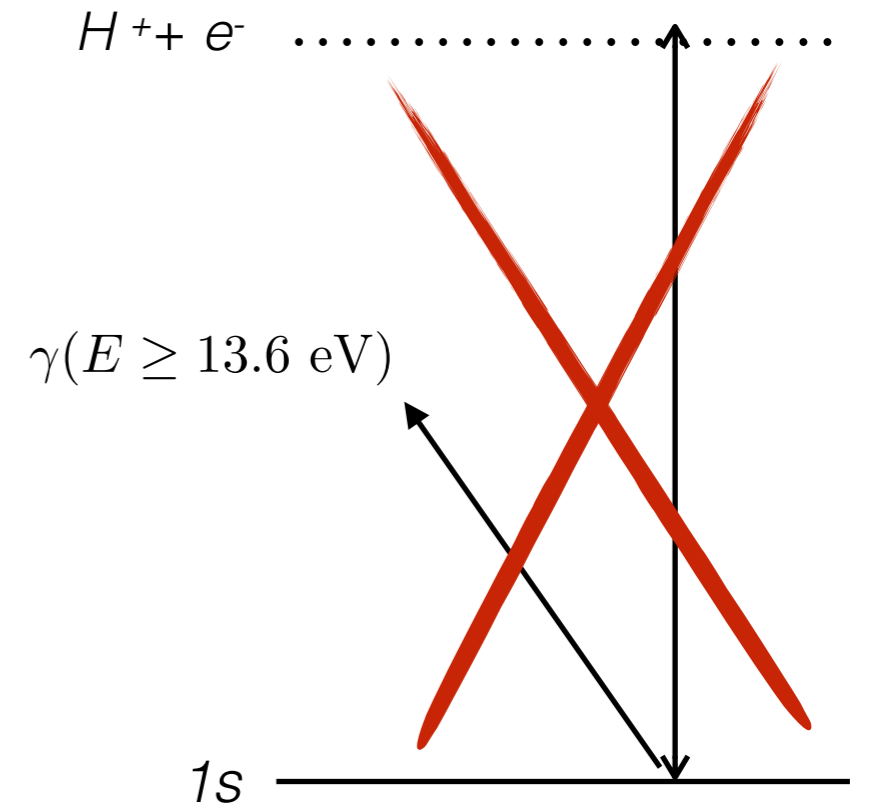
The « three-levels atom »

$$H^+ + e^- \leftrightarrow H^* + \gamma$$

followed by

$$H(2p) \leftrightarrow H(1s) + \gamma$$

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μ and y spectral distortions

*see e.g. Chluba & Sunyaev
[arXiv:1109.6552]*

Scattering processes should thermalize the injected photons, but if those processes go out of equilibrium

In full generality: $\Delta I(\nu) = I_{\text{true}}(\nu) - I_{\text{bb}}(\nu)$ μ and y are (almost) eigenmodes in the PCA!

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$$y \equiv \frac{1}{4} \left[\frac{\Delta \rho_\gamma}{\rho_\gamma} \right]_y \simeq \frac{1}{4} \int \mathcal{J}_{\text{bb}} \mathcal{J}_y \frac{1}{\rho_\gamma} \left(\frac{dE}{dt} \Big|_\gamma \right) dt$$

creation of a chemical potential
(more/less photons than a BB)

compton heating (or cooling!)
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$$\mathcal{J}_{\text{bb}}(z) \approx \exp[-(z/z_\mu)^{5/2}], \quad \mathcal{J}_y(z) \approx \left[1 + \left(\frac{1+z}{6 \times 10^4} \right)^{2.58} \right]^{-1}, \quad \mathcal{J}_\mu(z) \approx 1 - \mathcal{J}_y.$$

Visibility functions related to the range of efficiency of typical processes:

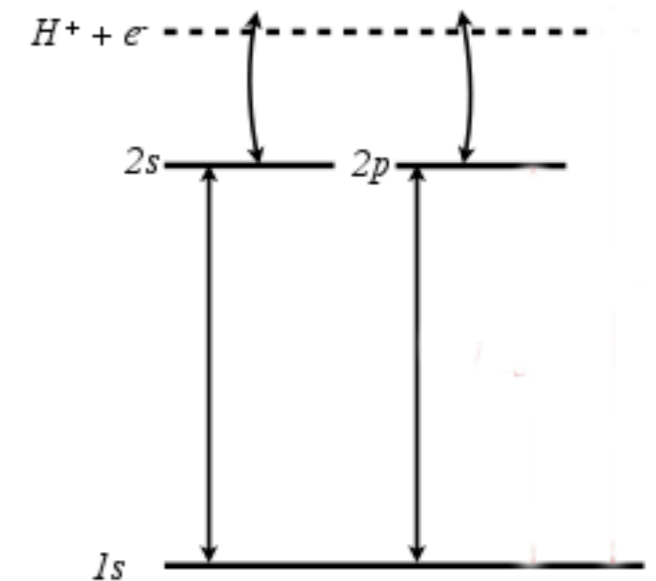
- Compton scattering for Comptonization-y
- Double Compton and Bremsstrahlung for μ-distortion

Evolution equations for x_e : the free electron fraction
and T_m : the matter temperature

$$\frac{dx_e}{dz} = \frac{1}{(1+z)H(z)} [R_s(z) - I_s(z)]$$

$$\frac{dT_M}{dz} = \frac{1}{1+z} \left[2T_M + \gamma(T_M - T_{\text{CMB}}) \right]$$

$$I_x(z) \text{ and } K_h(z) \propto \left. \frac{dE}{dV dt} \right|_{\text{dep,c}}$$



Key quantity $dE/dVdt|_{\text{dep,c}}$:

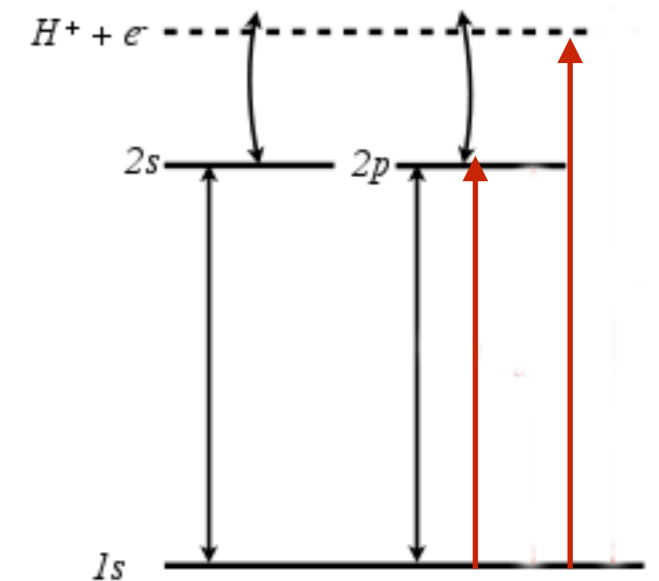
- The energy deposition rate by the decay per unit volume in each channel: ionization, excitation, heating
- Depending on z and x_e , the plasma can be very inefficient at absorbing energy !
- In full generality, very complicated to compute, need MC simulations.

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$$\frac{dx_e}{dz} = \frac{1}{(1+z)H(z)} [R_s(z) - I_s(z) - I_X(z)]$$

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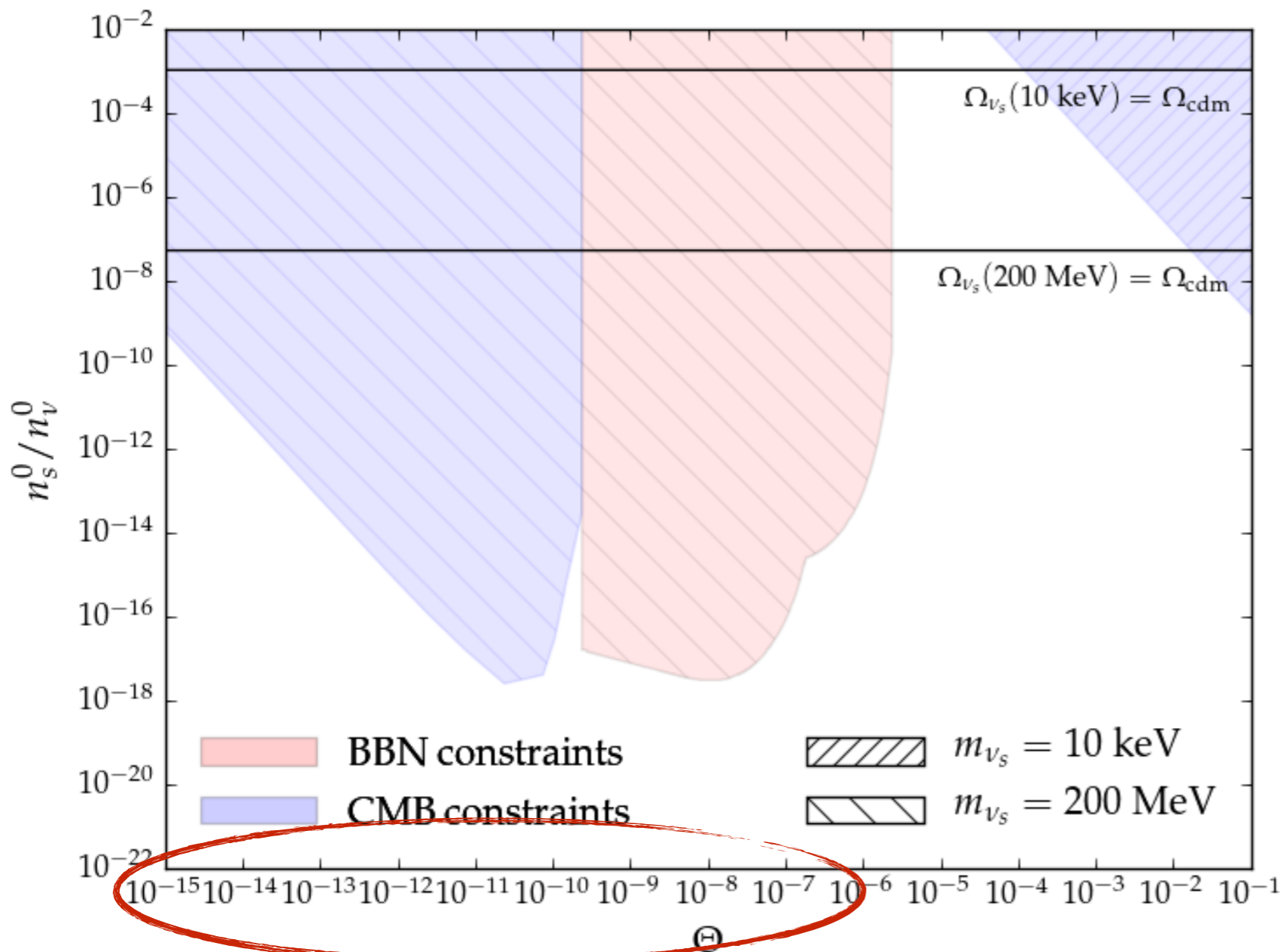
Constraints on keV-MeV scale majorana sterile neutrinos

- Below 200MeV, main decay channels are :

e.g. Drewes et al. JCAP 1701(2017) 025

$$\Gamma_{3\nu}^{-1} \simeq 3 \times 10^4 \text{s} \left(\frac{\text{MeV}}{M_s} \right) \Theta^{-2} \quad \Gamma_{\nu\gamma} \simeq 1.6\% \Gamma_{3\nu} \quad \Gamma_{\nu e^+e^-} \simeq \mathcal{O}(10\%) \Gamma_{3\nu}$$

- See saw requires typically, $\Theta^2 \gtrsim 10^{-5} M_{\text{MeV}}^{-1}$ what do we learn then ?



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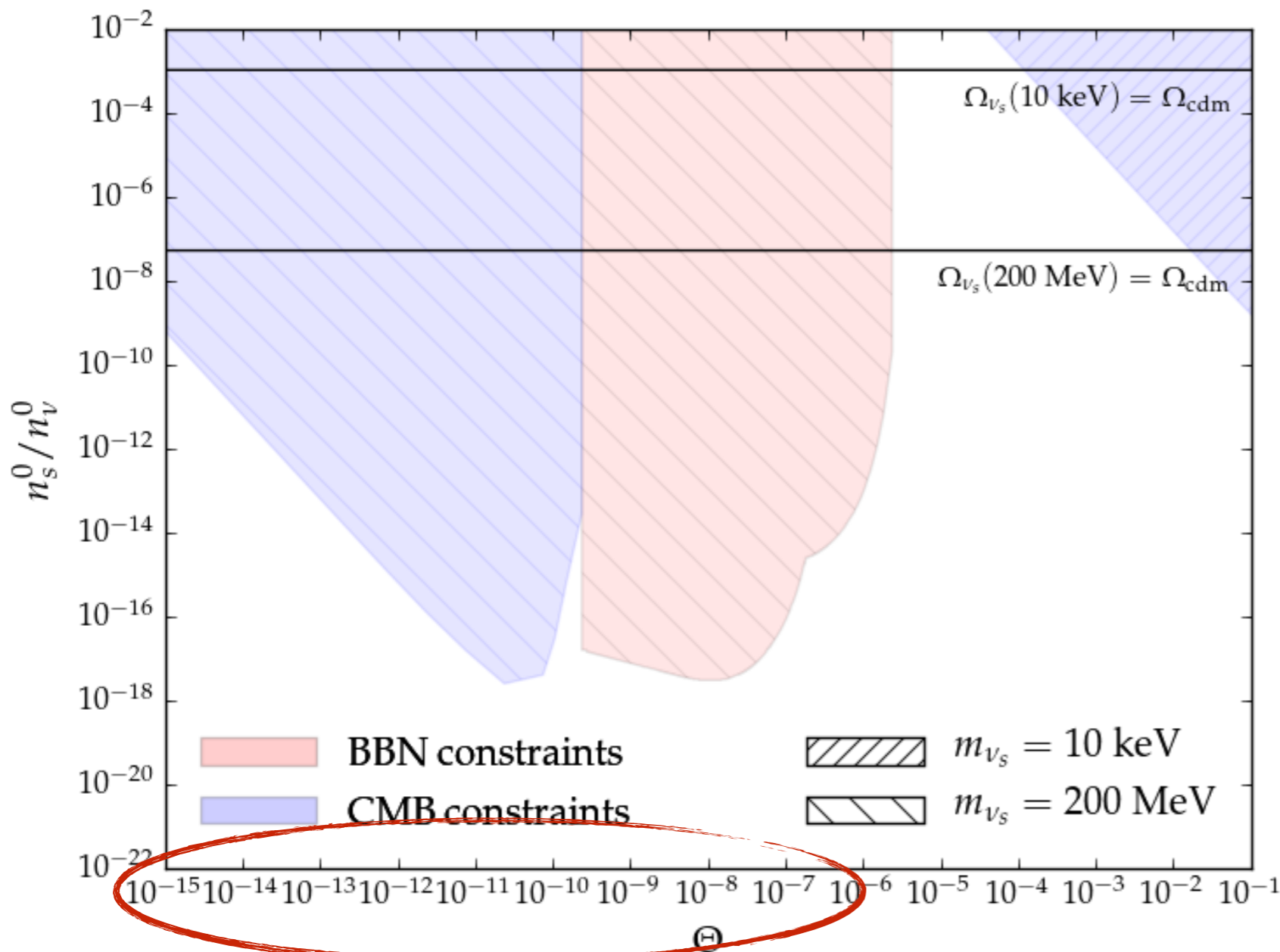
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$$\Gamma_{\nu\gamma} \simeq 1.6\% \Gamma_{3\nu}$$

$$\Gamma_{\nu e^+e^-} \simeq \mathcal{O}(10\%) \Gamma_{3\nu}$$

e.g. Drewes et al. JCAP 1701(2017) 025

- See saw requires typically, $\Theta^2 \gtrsim 10^{-5} M_{\text{MeV}}^{-1}$ what do we learn then ?

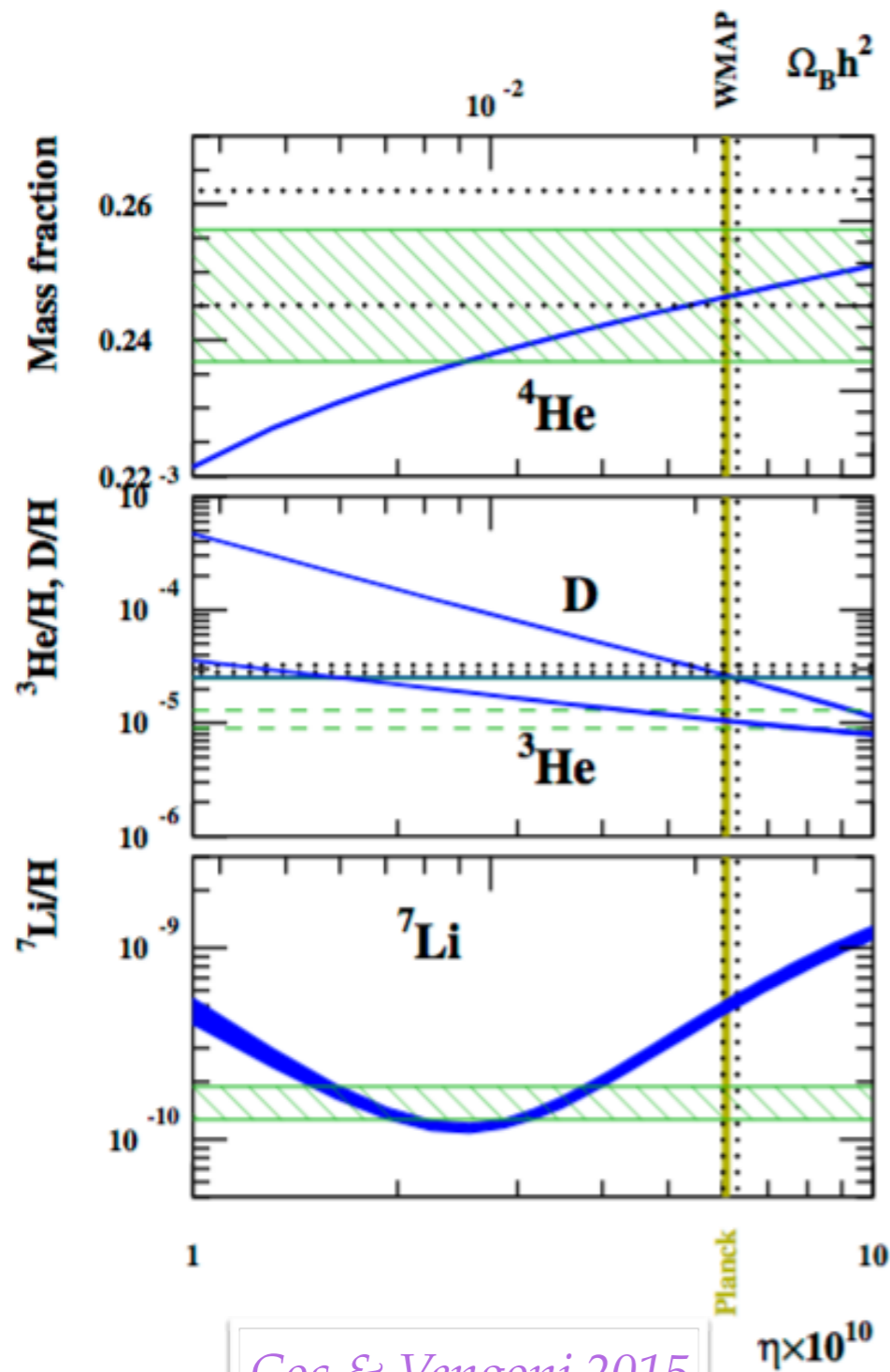


- Cosmology is mostly sensitive to **sterile neutrinos more weakly coupled** than those evolve in see-saw mechanism;
- Still, it is interesting since **masses and mixing of the right-handed neutrinos are not constrained** by fundamental physics arguments !
- KeV-scale neutrinos are usually better constrained by diffuse X-ray background

*Boyarsky et al.
MNRAS 370 (2006) 213–218*

The light element abundances

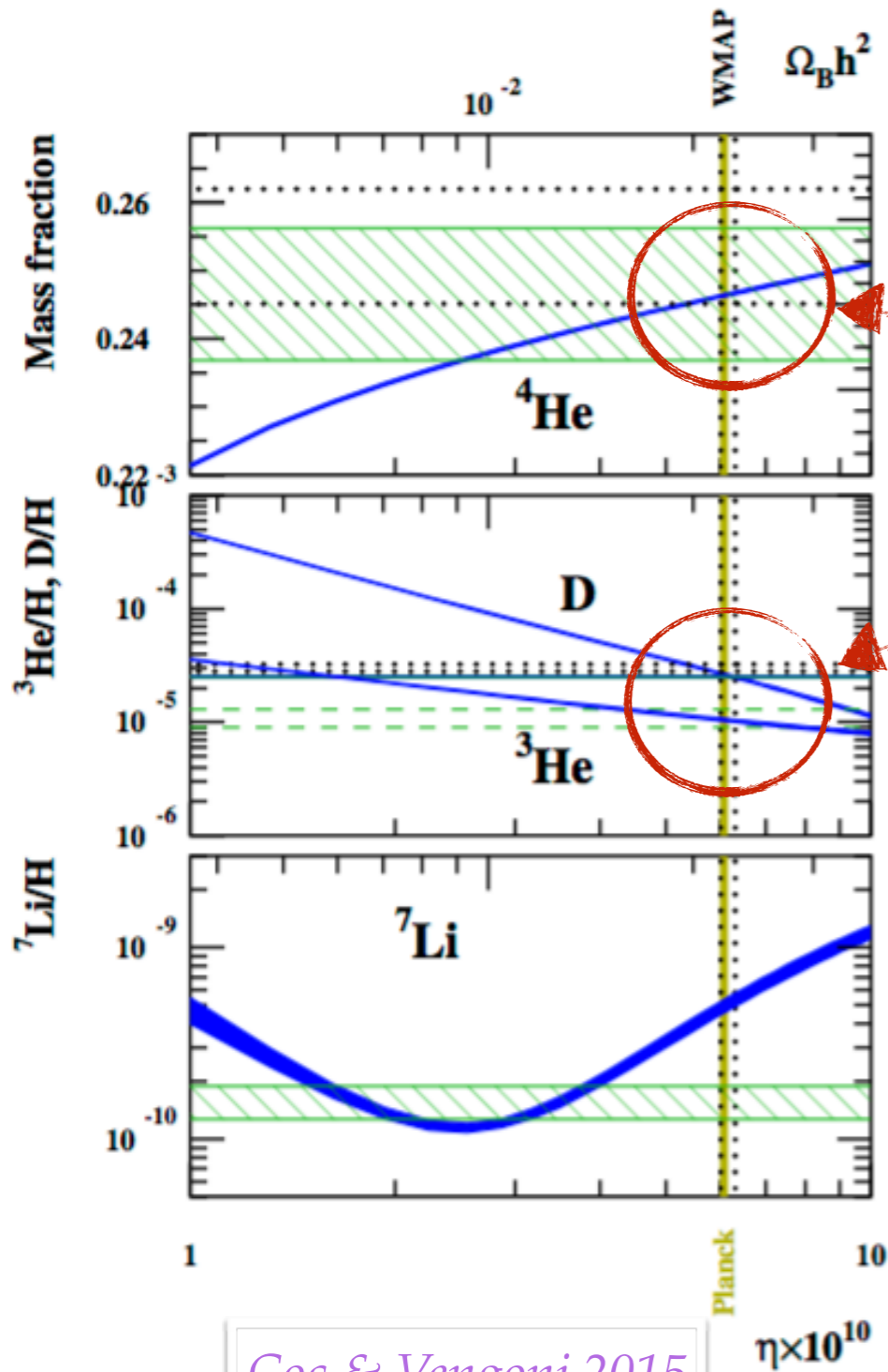
BBN happened few s / min after BB when $T \approx \text{KeV} - \text{MeV}$



Coc & Vengoni 2015

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For 3 nuclei :

Strong observational constraints

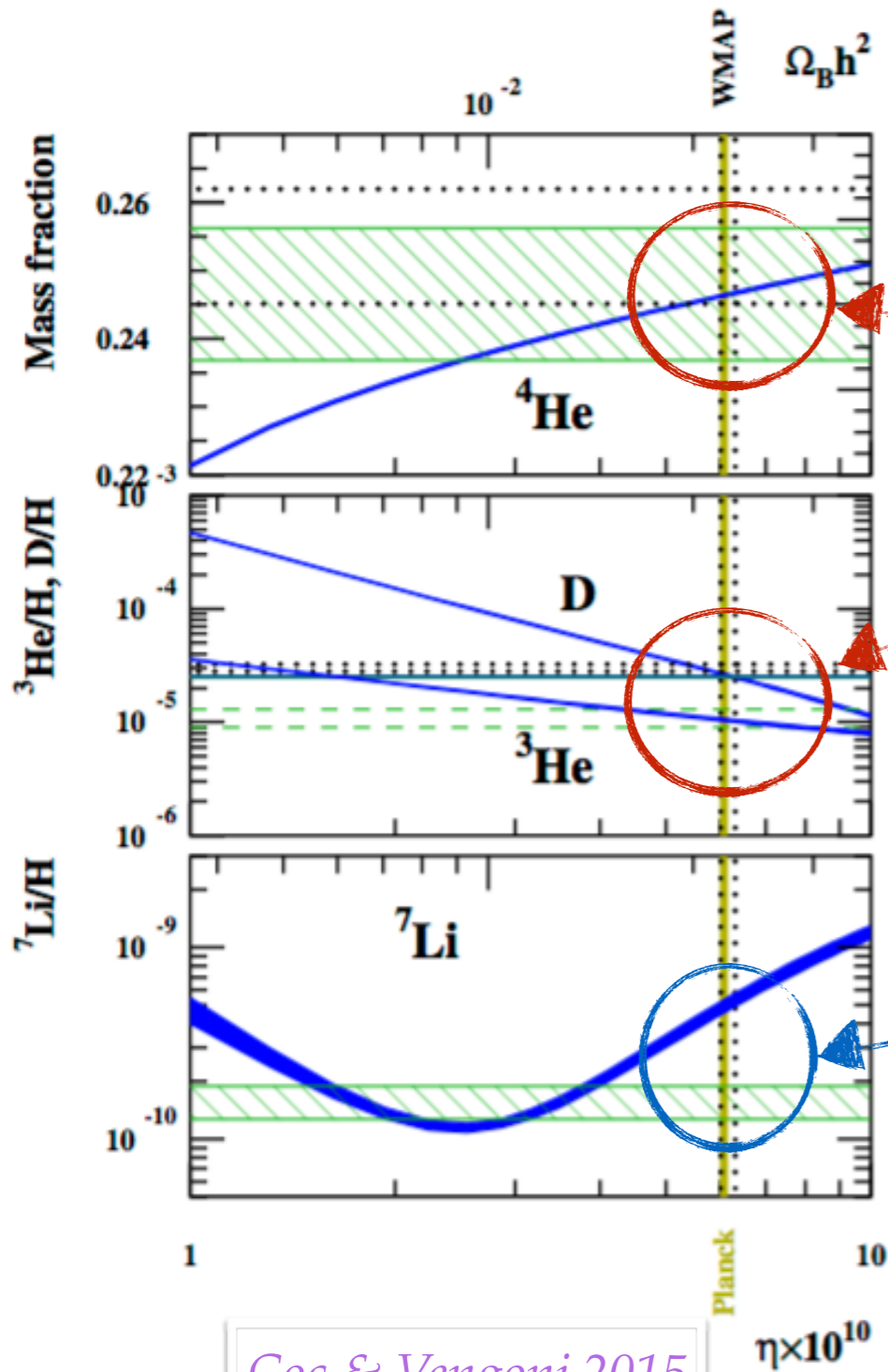
$$Y_p > 0.2368$$

$$2.56 \times 10^{-5} < {}^2\text{H}/\text{H} < 3.48 \times 10^{-5}$$

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The Lithium problem :
 Overprediction of the ${}^7\text{Li}$ abundance
 $Y_{\text{Li}}^{\text{theo}} \simeq 3 \times Y_{\text{Li}}^{\text{obs}}$
 ignored today !

*e.g. Poulin & Serpico
 PRL 114 (2015) no.9, 091101*

same « EM cascade » to compute ... But much simpler

We inject electromagnetic energy in a plasma with $n_\gamma \gg n_b$

Q : What is the **resulting metastable distribution of photons** ?

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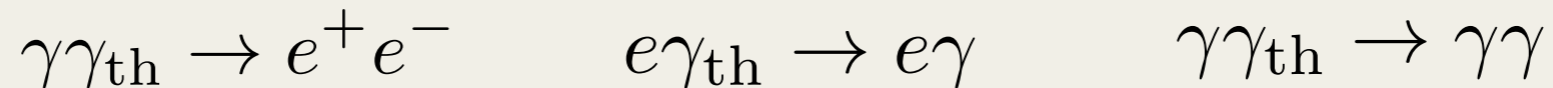
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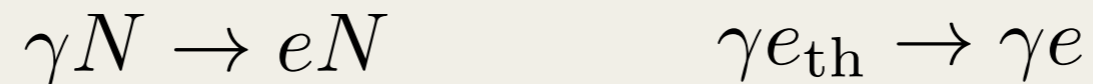
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Basic processes are (at high energies)



and eventually (very low rates)



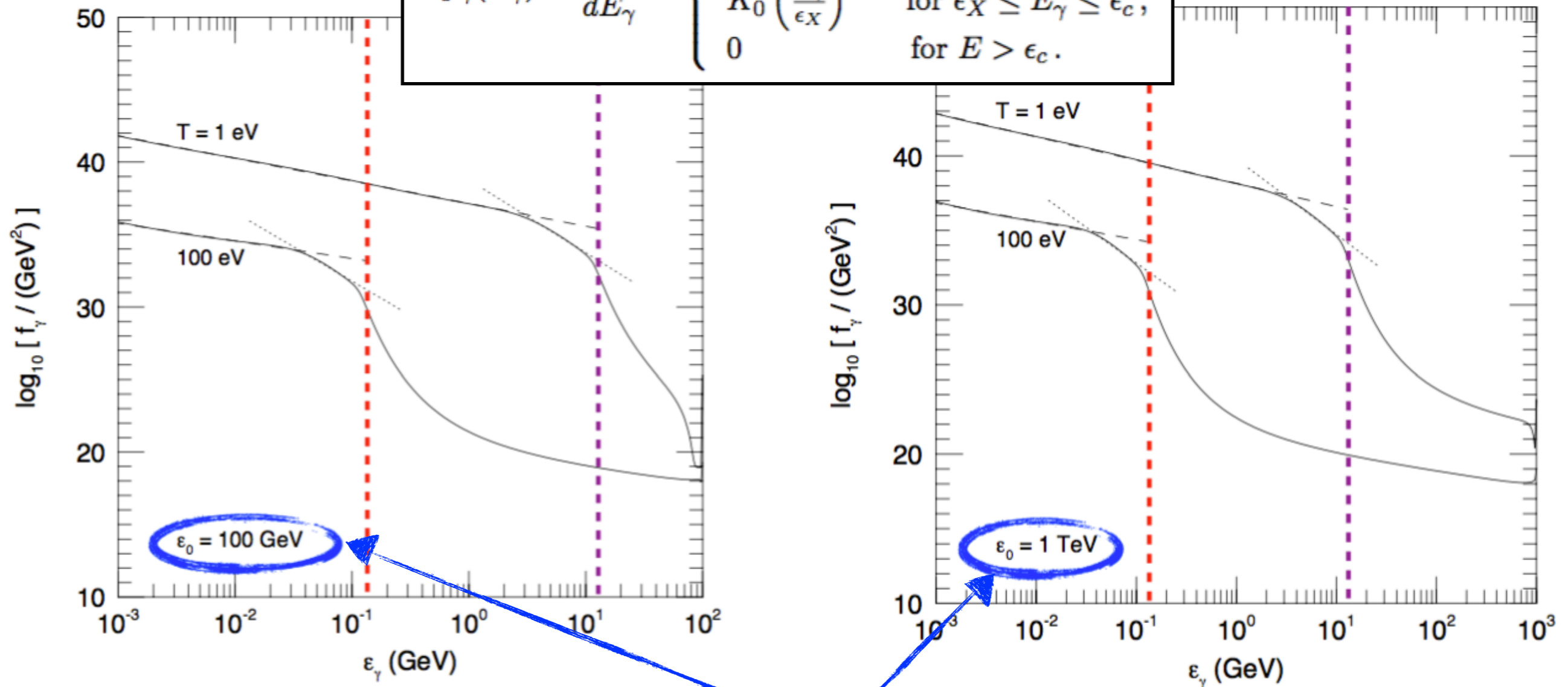
Particle multiplication and energy redistribution

=> **Electromagnetic cascade** !

*Kawasaki & Moroi,
ApJ 452,506 (1995)*

This has been shown to lead to a universal spectrum

$$p_\gamma(E_\gamma) \equiv \frac{dN_\gamma}{dE_\gamma} = \begin{cases} K_0 \left(\frac{E_\gamma}{\epsilon_X}\right)^{-3/2} & \text{for } E_\gamma < \epsilon_X, \\ K_0 \left(\frac{E_\gamma}{\epsilon_X}\right)^{-2} & \text{for } \epsilon_X \leq E_\gamma \leq \epsilon_c, \\ 0 & \text{for } E > \epsilon_c. \end{cases}$$



- Shape independent of the energy / temperature of the bath:
Only dictates the overall normalisation;
- Threshold due to pair production.

Non-Universal BBN bounds

Typically, after the end of standard BBN (5 keV) :

$$E_{\text{cutoff}}(1 \text{ keV}) \sim 12 \text{ MeV} \quad E_{\text{cutoff}}(10 \text{ eV}) \sim 1.2 \text{ GeV}$$

All cases simulated inject energy such that $E_\gamma \gg E_{\text{cutoff}}$
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After « standard » BBN :

$$E_{\text{threshold}}(\text{Be}) = 1.58 \text{ MeV} < E_{\text{cutoff}}$$

If $E_{\text{threshold}} < E_0 < E_{\text{cutoff}}$

results in the literature are wrong !

Consider a photon injection and start by neglecting diffused electrons.

Remaining processes are :

$$\gamma\gamma_{\text{th}} \rightarrow \gamma\gamma, \quad \gamma e_{\text{th}}^{\pm} \rightarrow \gamma e^{\pm}, \quad \gamma N \rightarrow N e^{\pm}$$

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whose stationary solution is

$$f_{\gamma}^{\text{S}}(E_{\gamma}) = \frac{\mathcal{S}(E_{\gamma}, t)}{\Gamma_{\gamma}(E_{\gamma}, t)}$$

Hubble rate much smaller than
all particle physics interaction rate,
thus neglected

where for a decaying particle

$$\mathcal{S}(E_{\gamma}, t) = \frac{n_{\gamma}^0 \zeta_X (1 + z(t))^3 e^{-t/\tau_X}}{E_0 \tau_X} p_{\gamma}(E_{\gamma}, t)$$

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Starting from two body decay

$$p_\gamma(E_\gamma) = \delta(E_\gamma - E_0) \text{ with } E_0 = \frac{m_X}{2}$$

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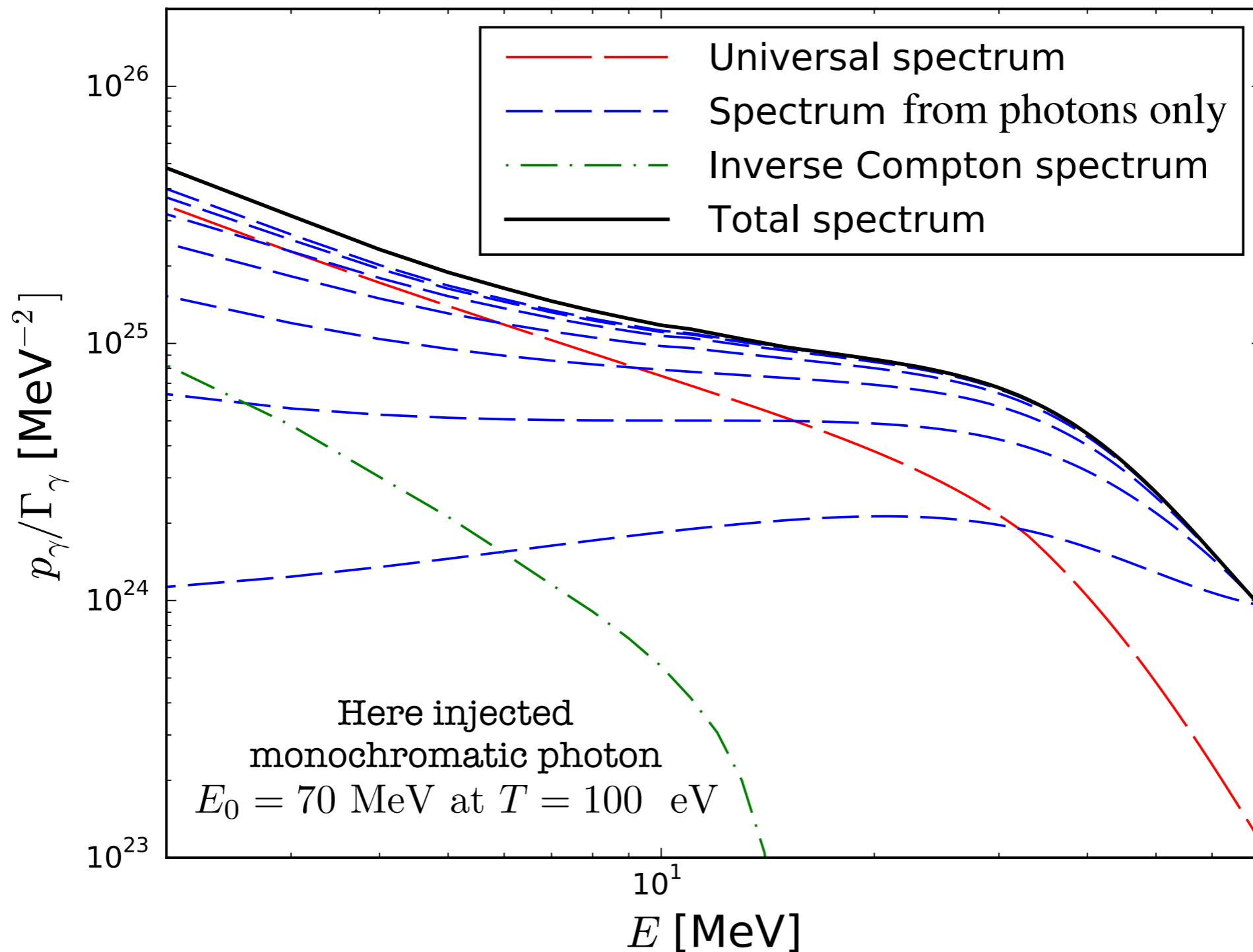
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Production from photodissociation
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Destruction from its
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$$Y_A \equiv n_A/n_b$$

Typical results for a given energy and a given temperature of the thermal bath



Proof of principle solution :
monochromatic photon injection

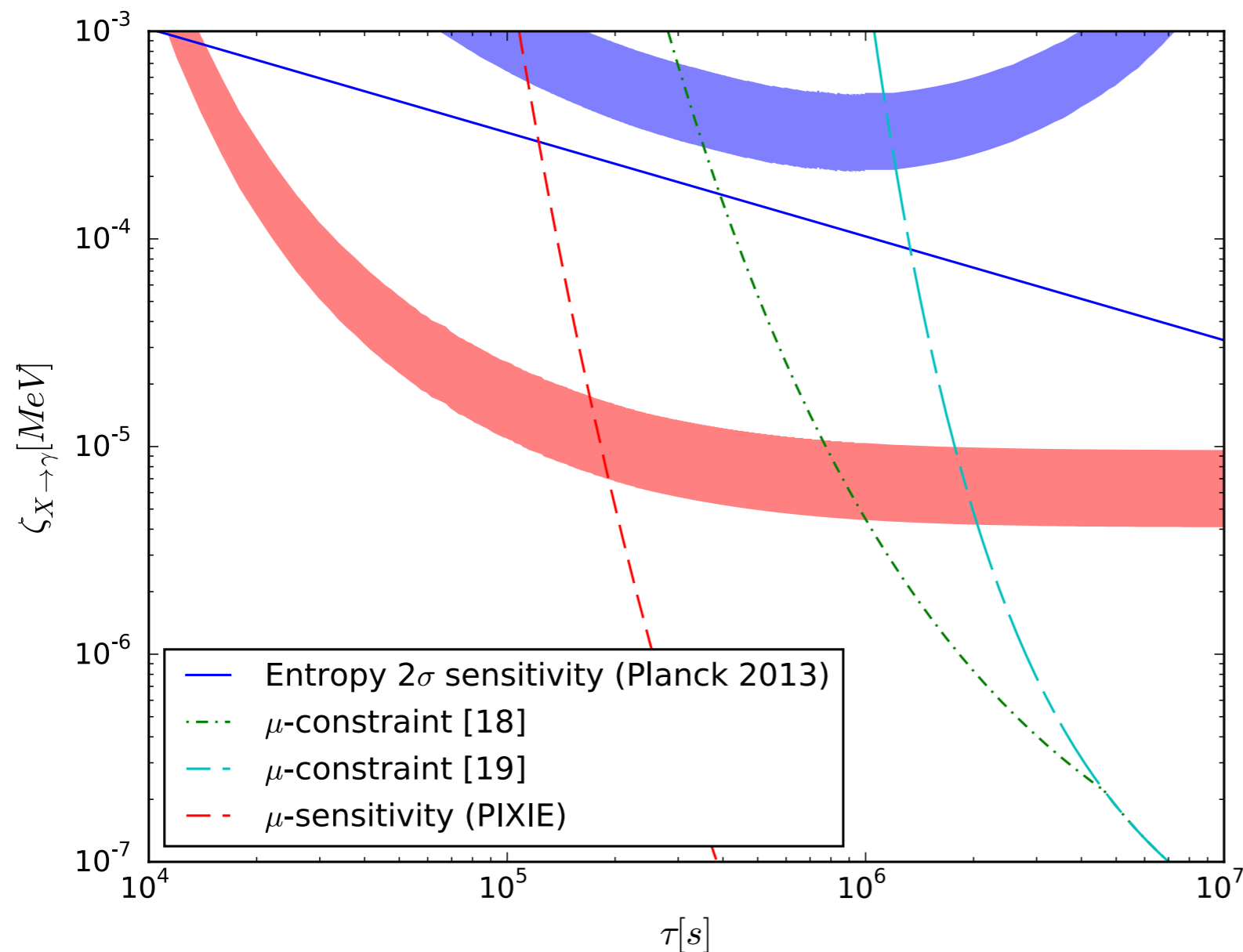
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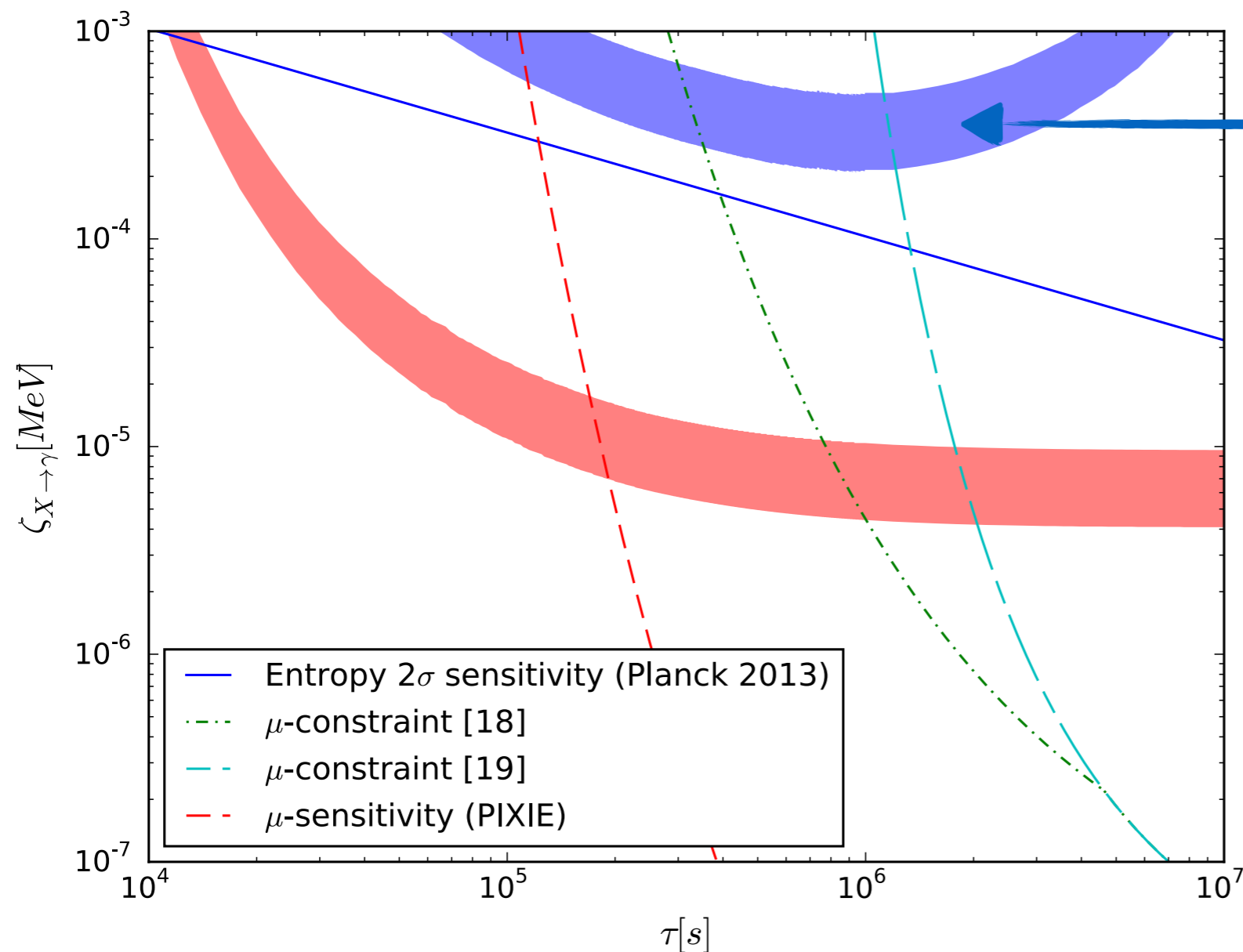
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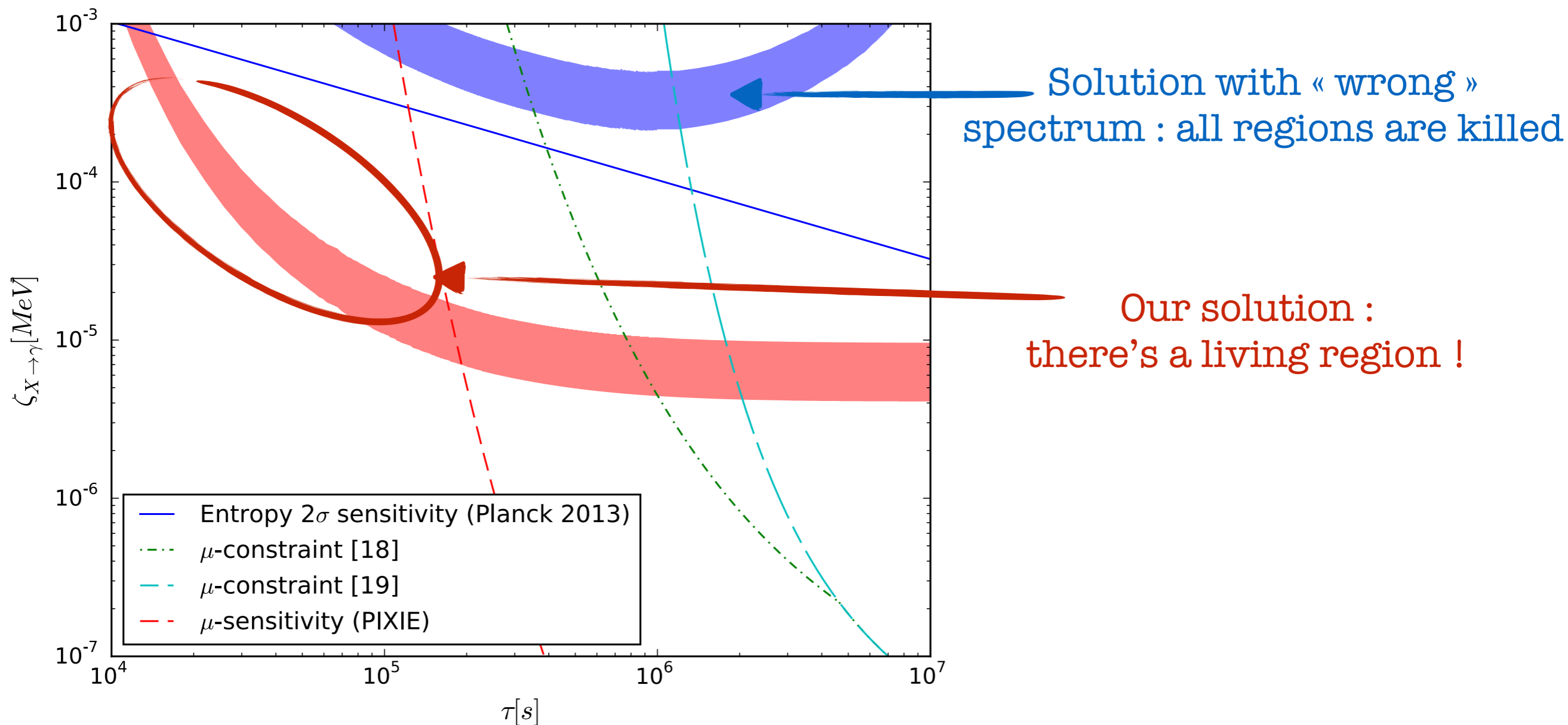


Solution with « wrong »
spectrum : all regions are killed

Proof of principle solution :
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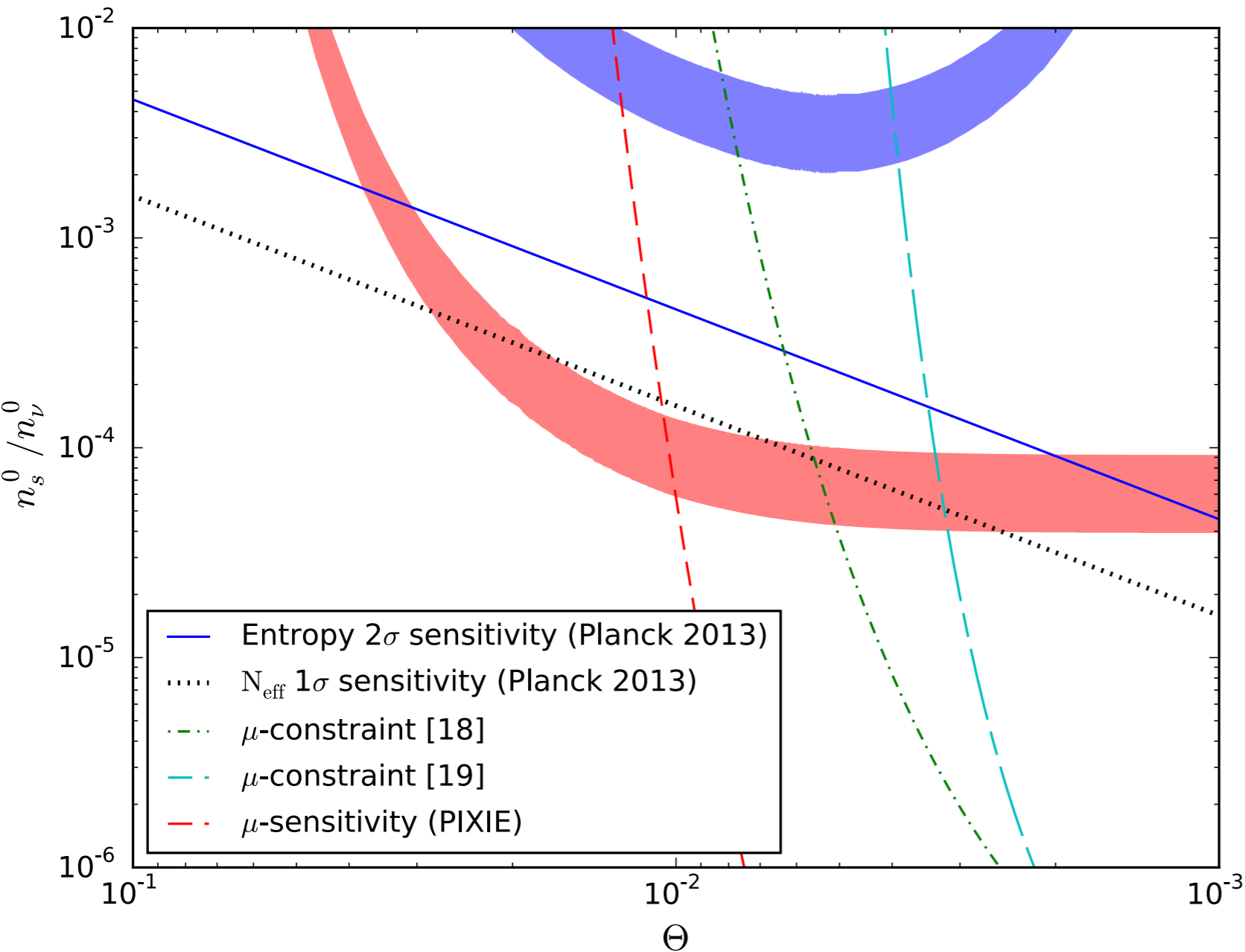
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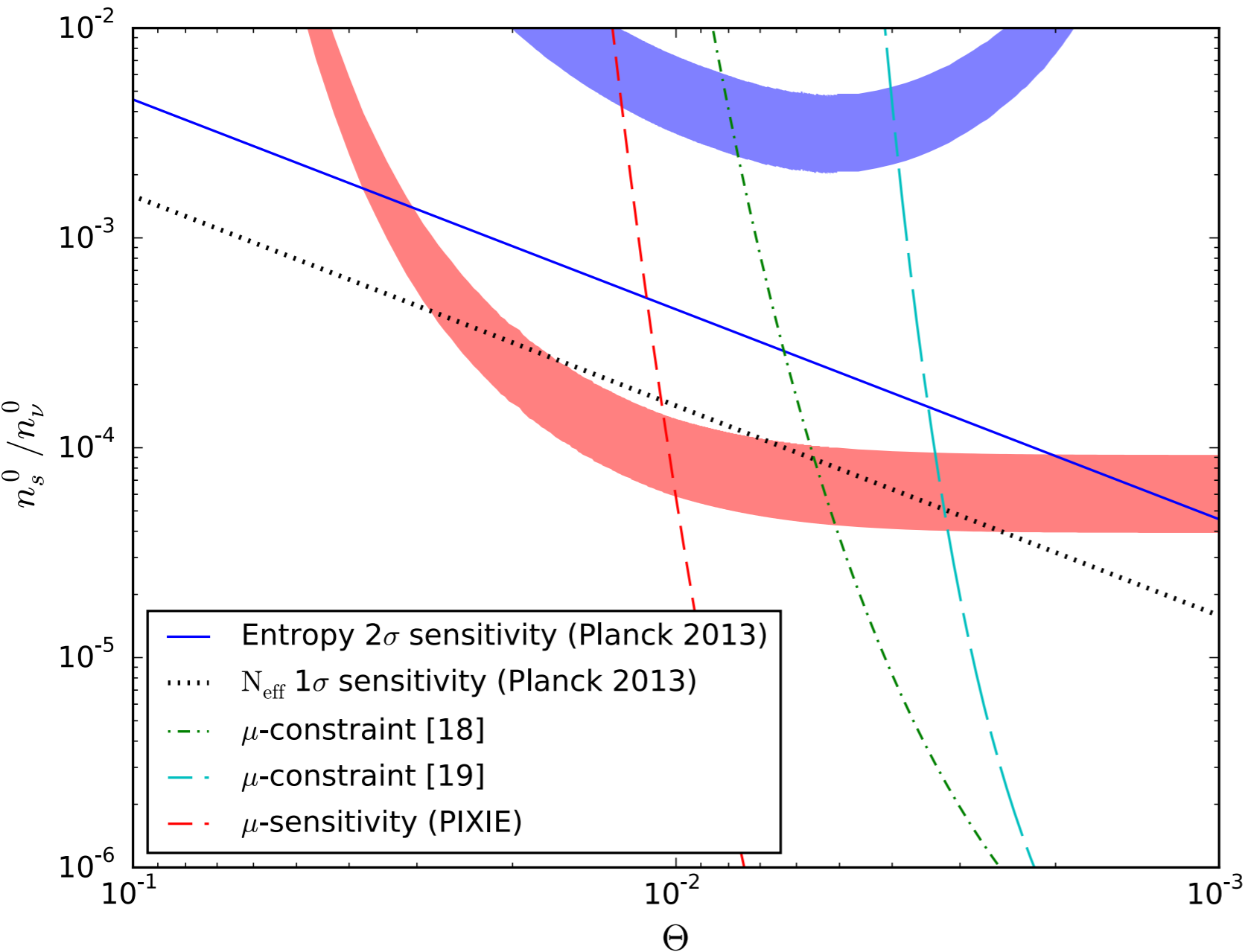
Try with a « real » model that was known to fail
when using universal spectrum :
the Sterile (majorana) Neutrino

H. Ishida et al.
PRD 90, 8, 083519 (2014)



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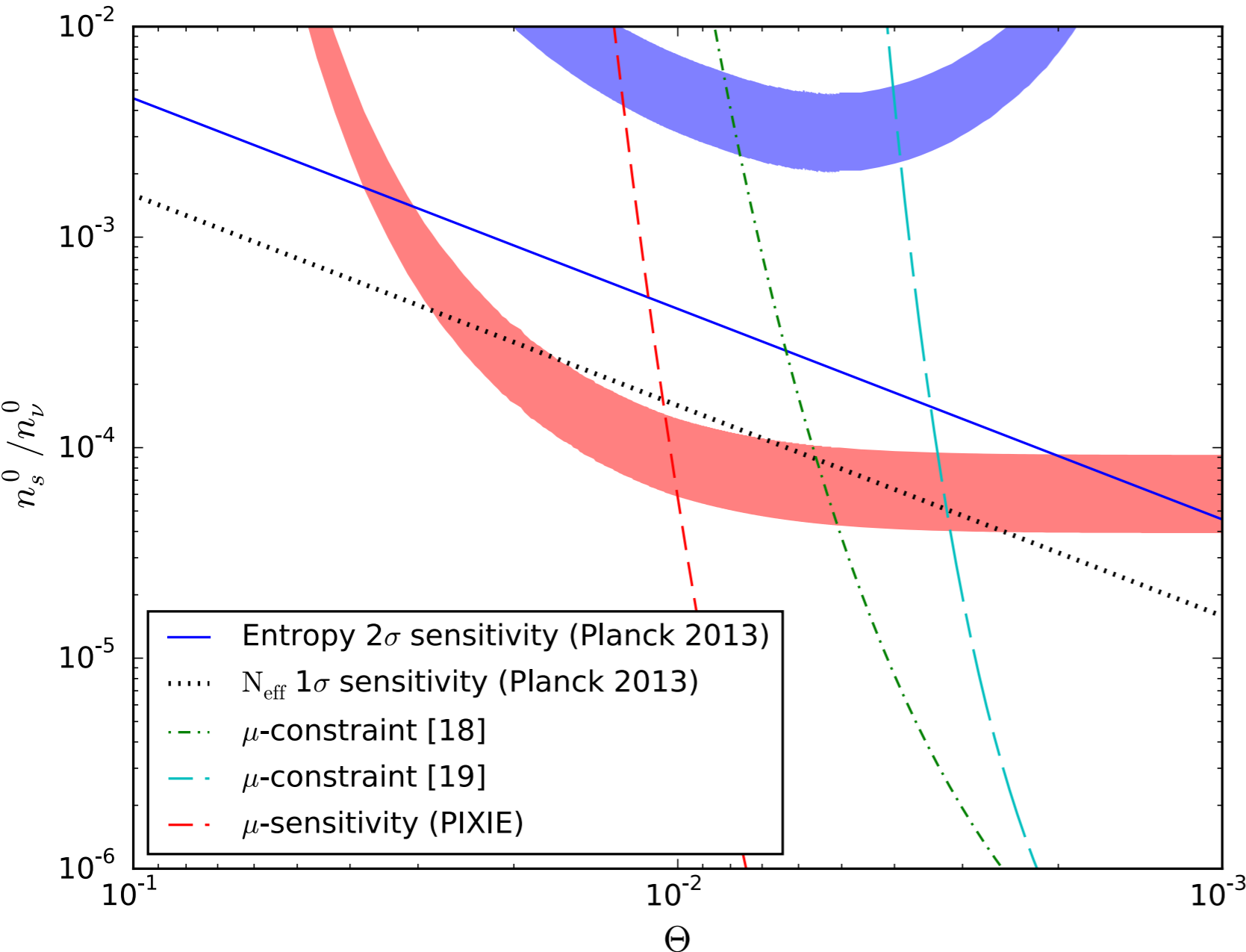
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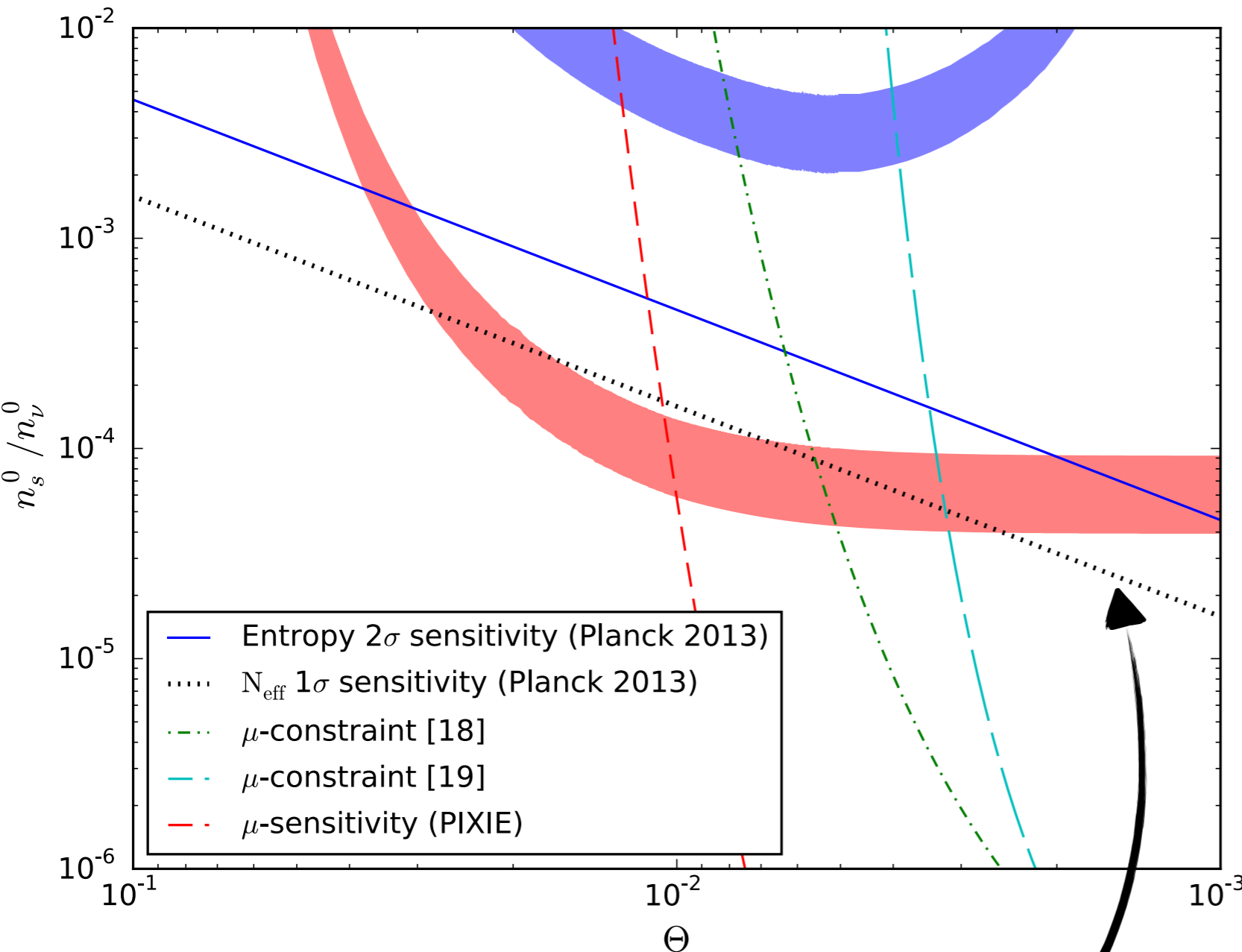
To avoid constraints from
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required to be mostly ν_μ or ν_τ

Typical branching ratio

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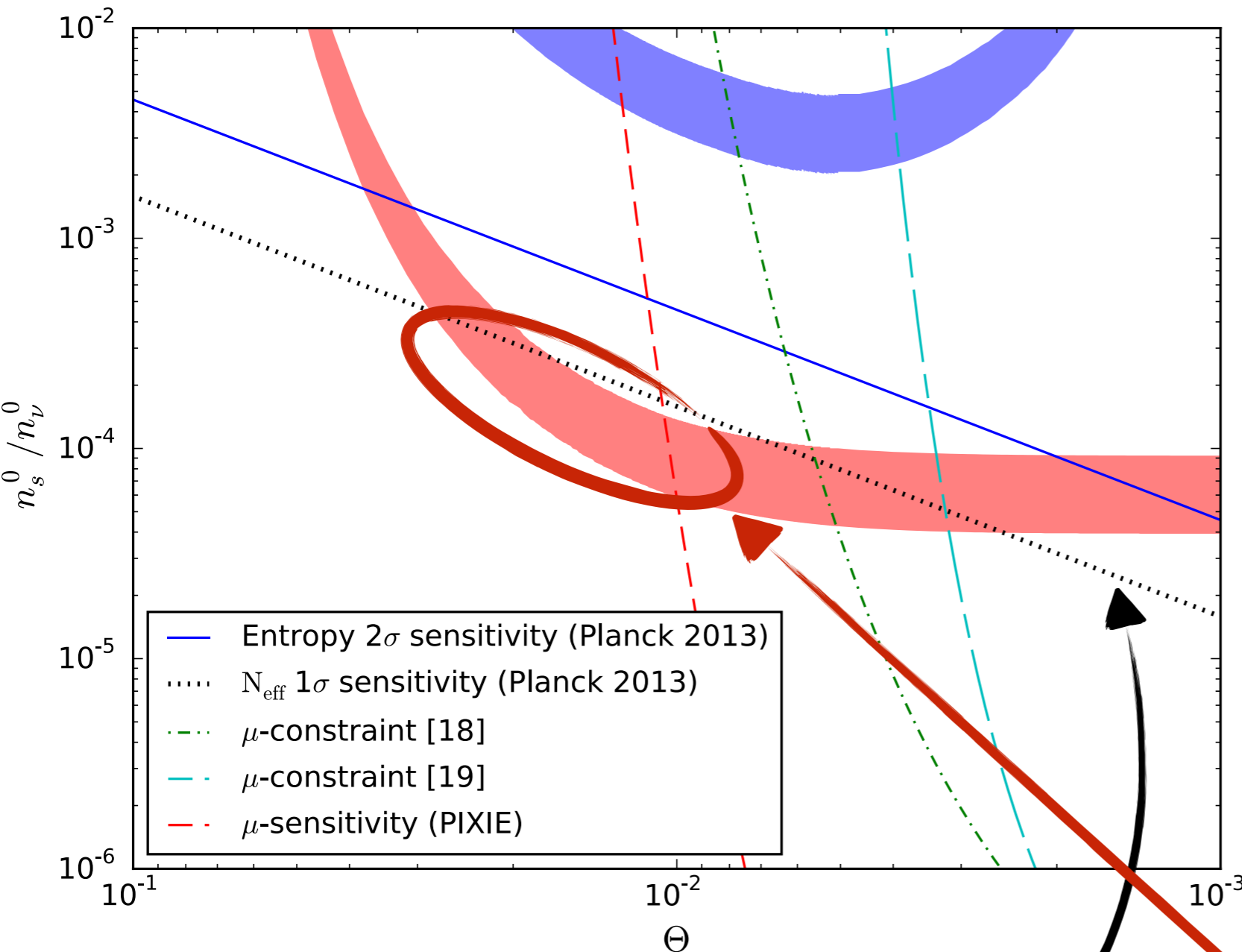
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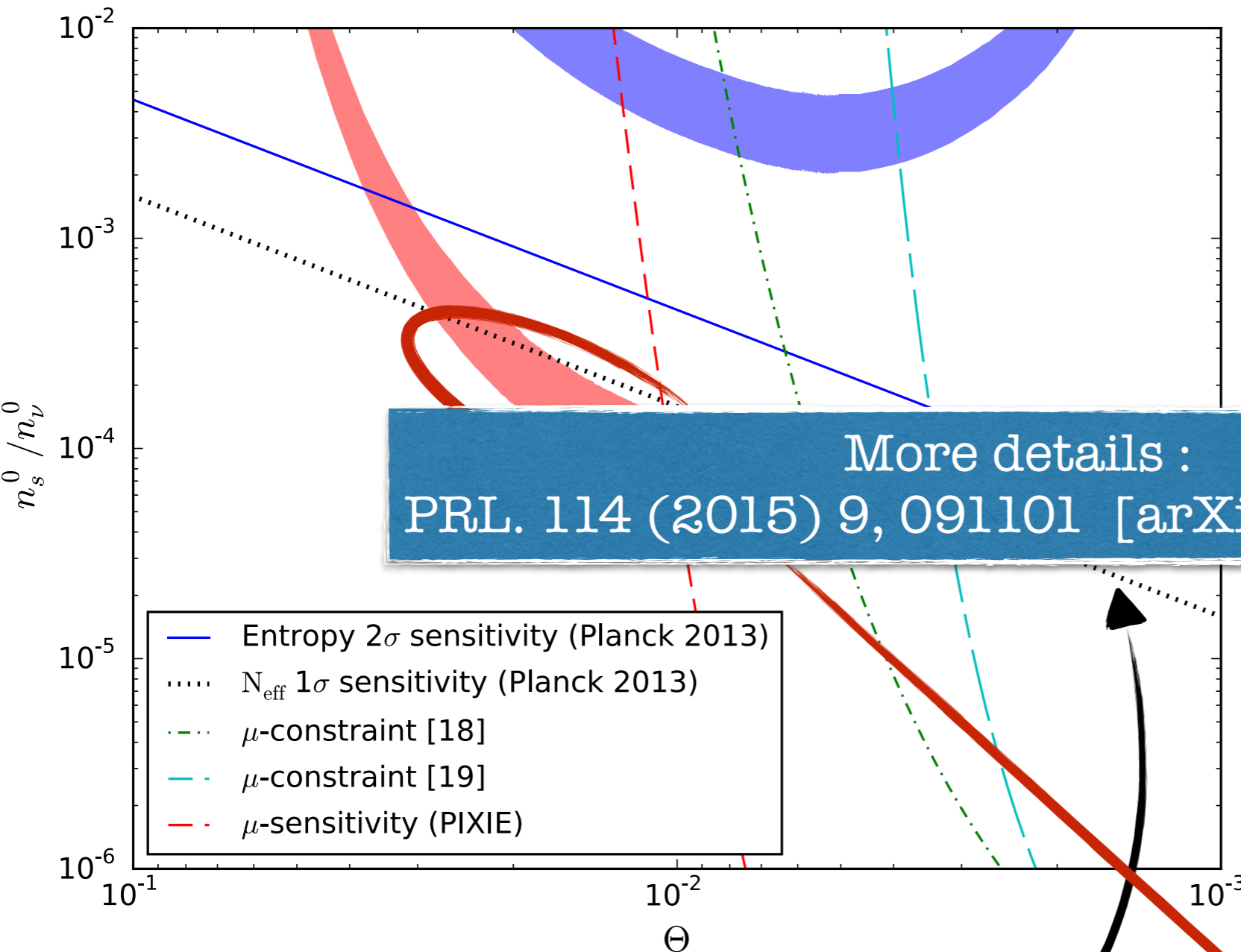
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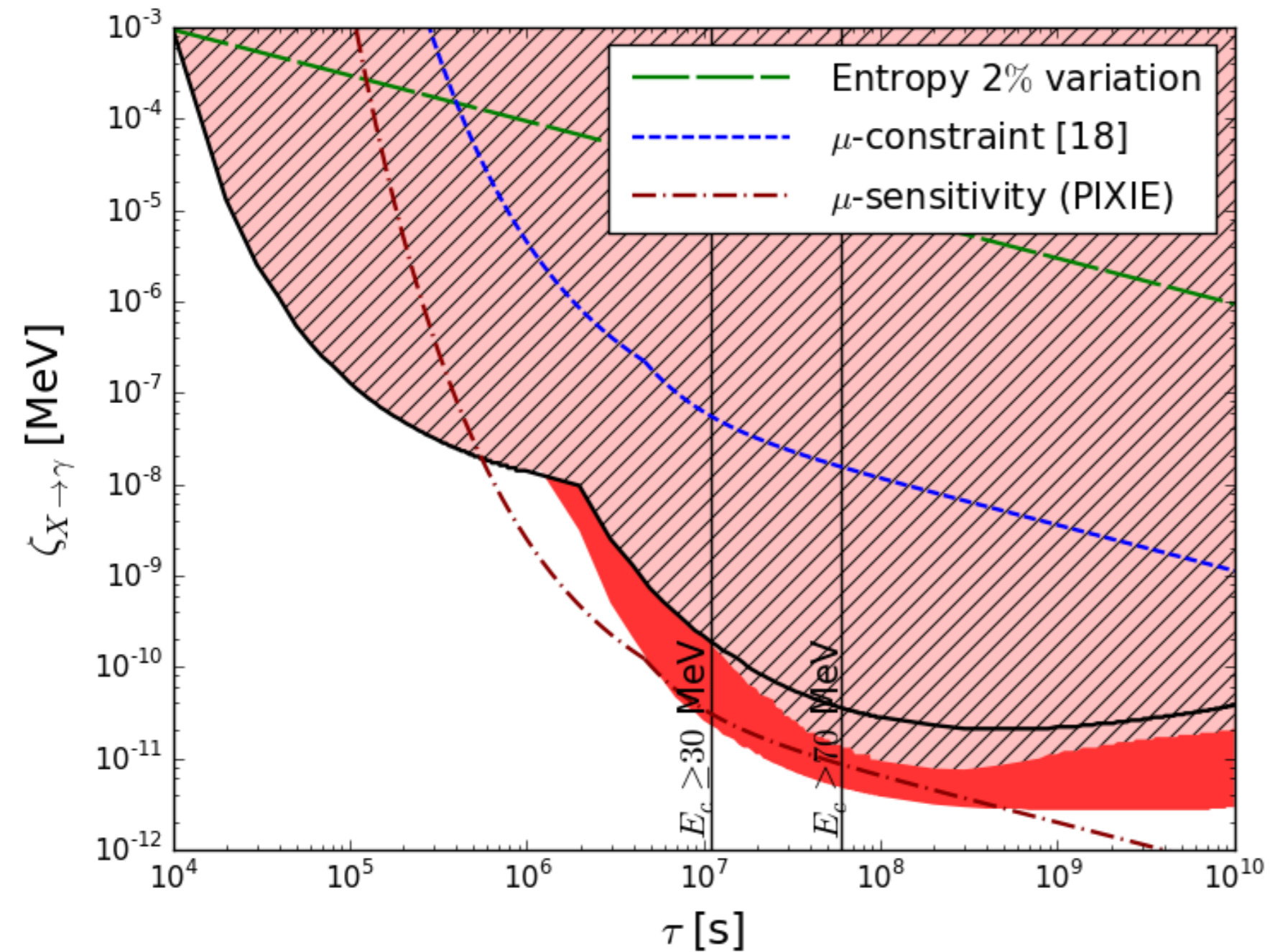
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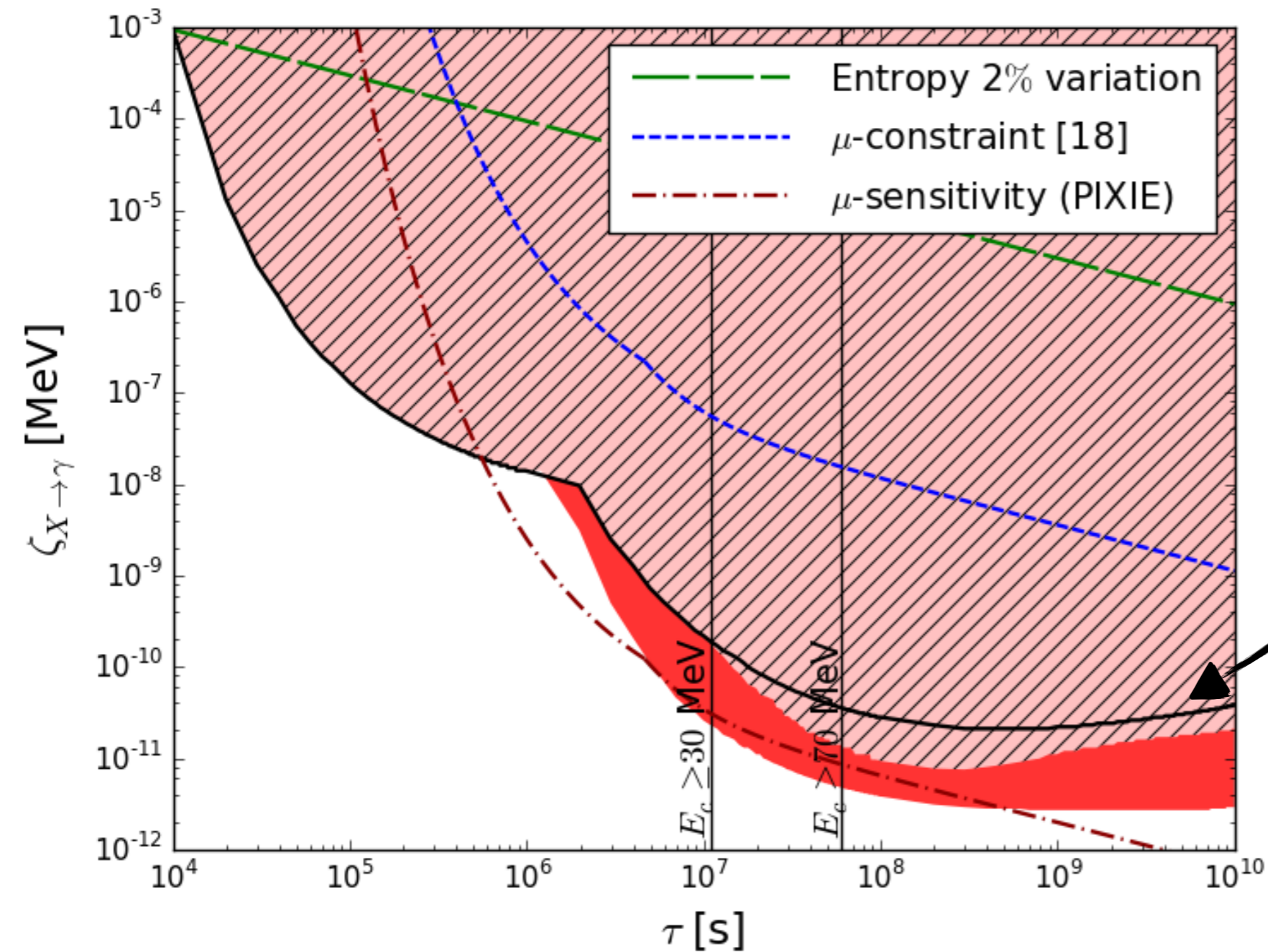
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VP & Serpico
PRD. 91 (2015) 10,
103007

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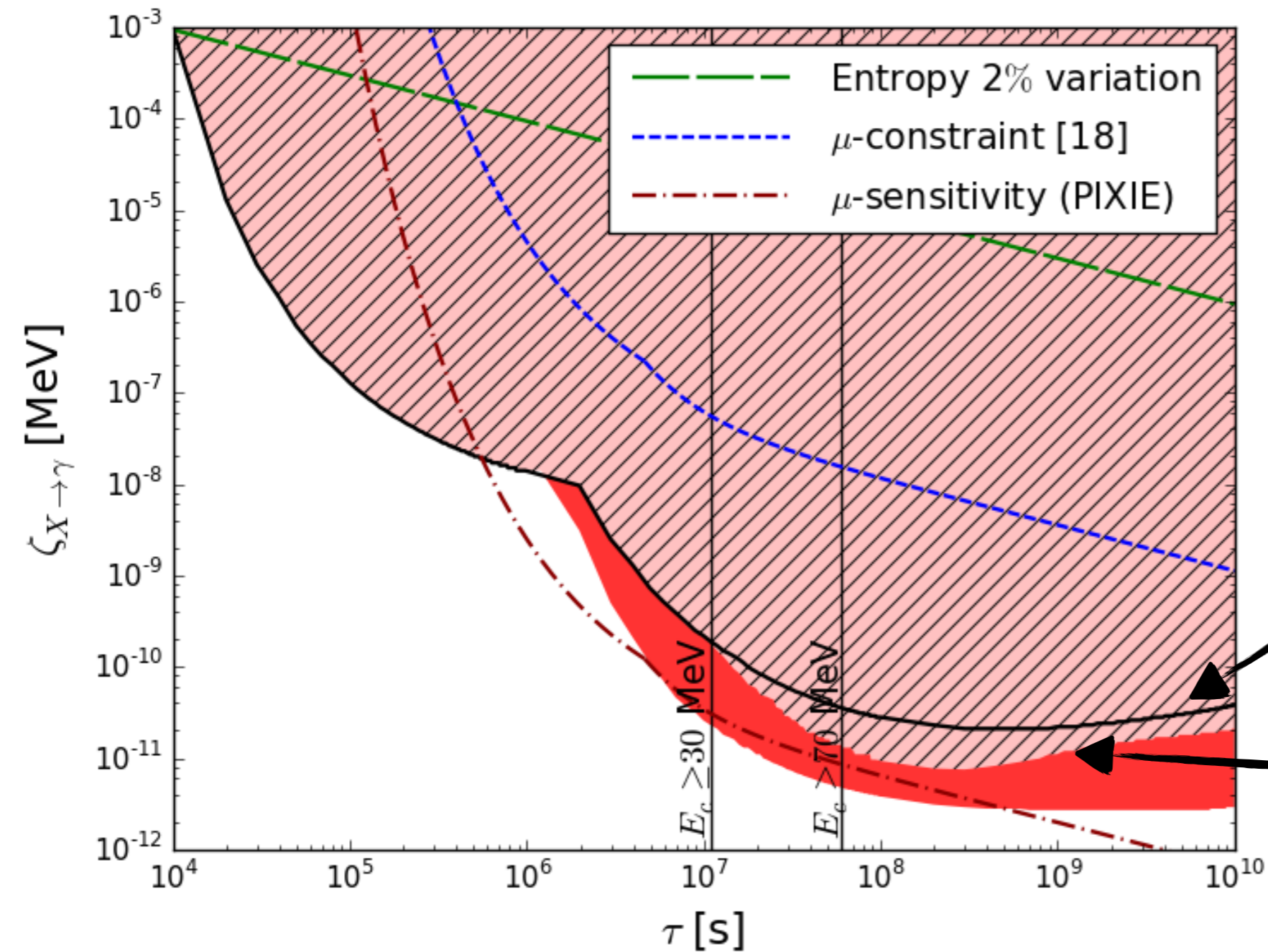


Standard (wrong) bound

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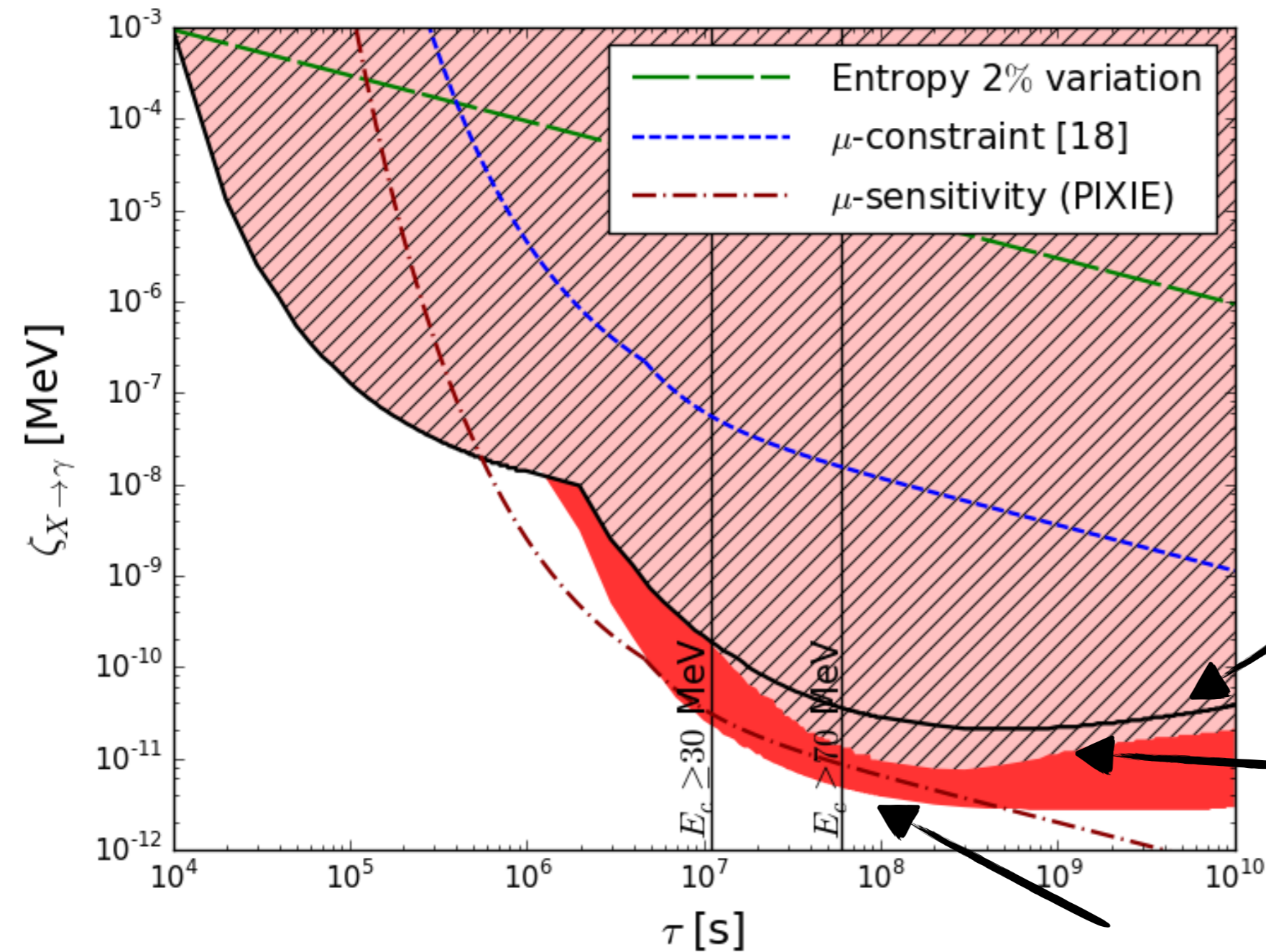
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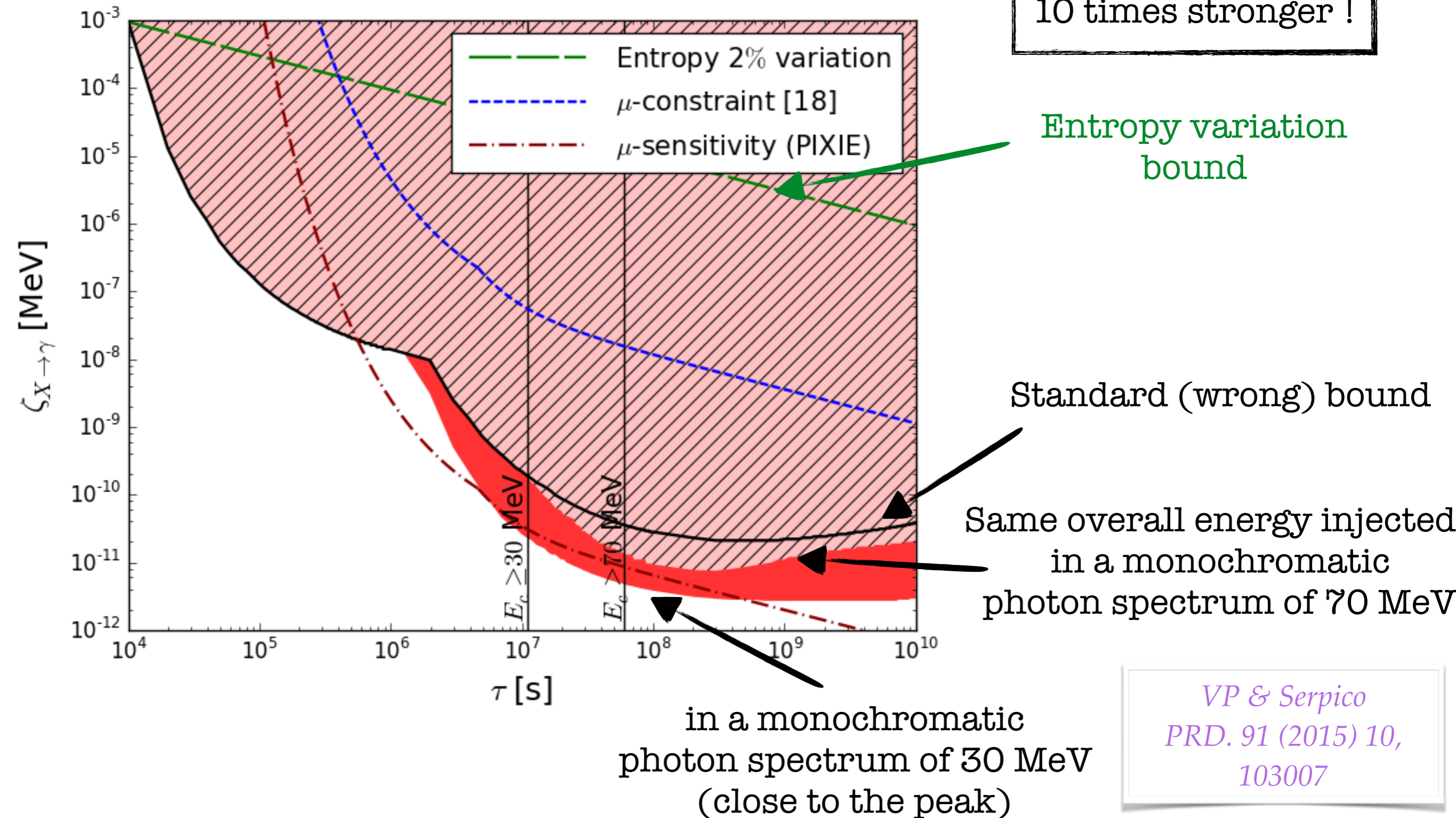
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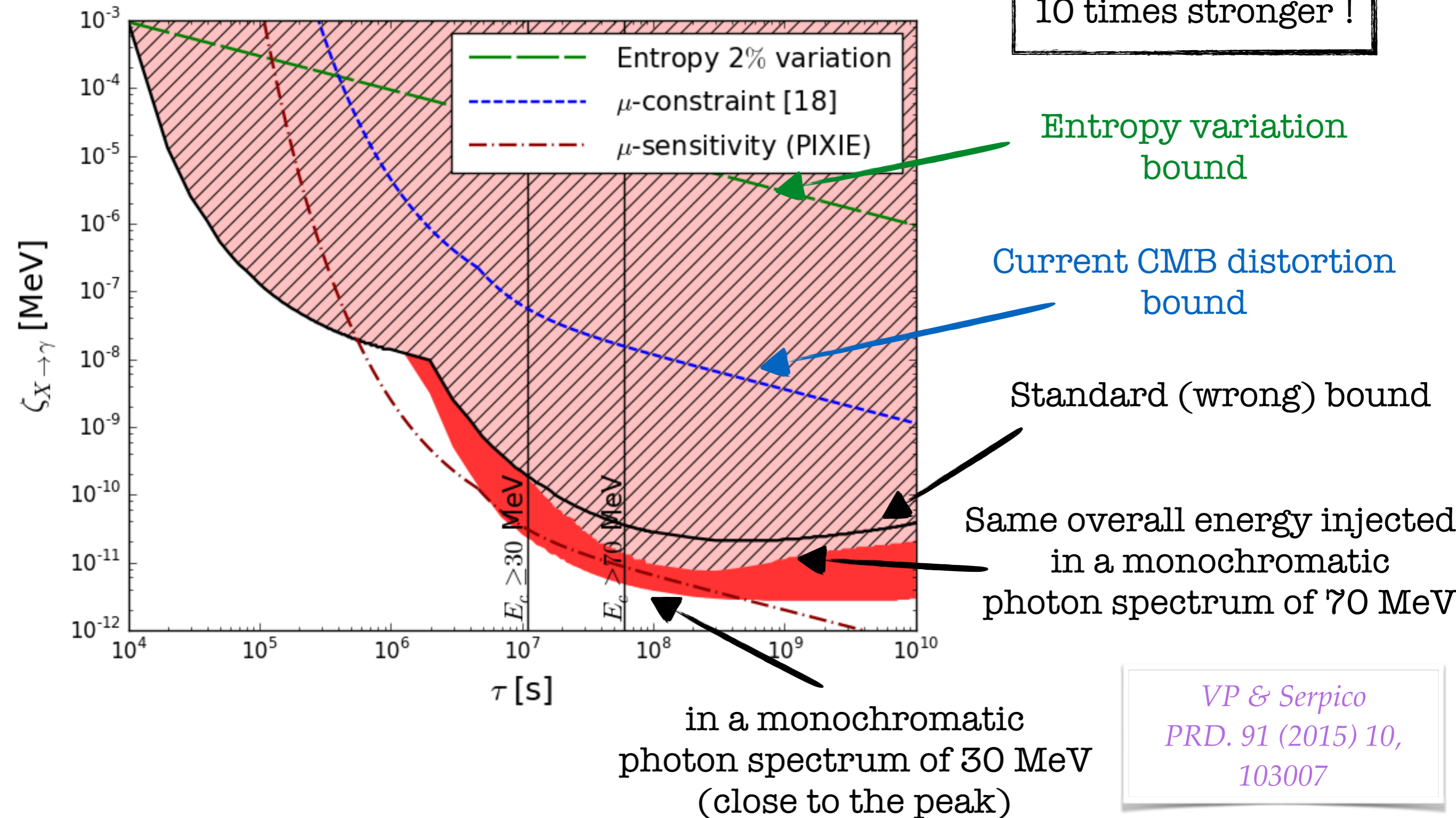
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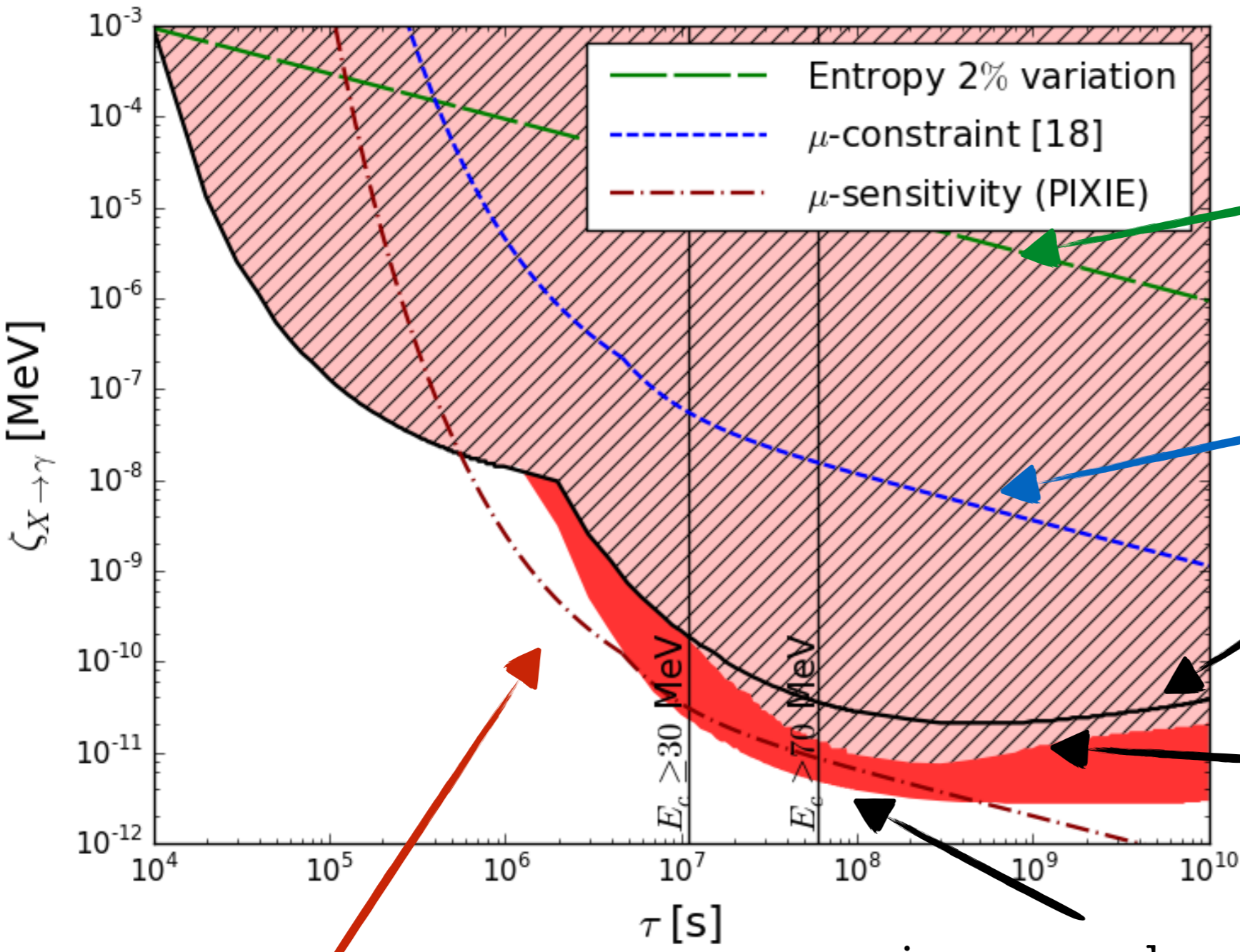


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Entropy variation bound

Current CMB distortion bound

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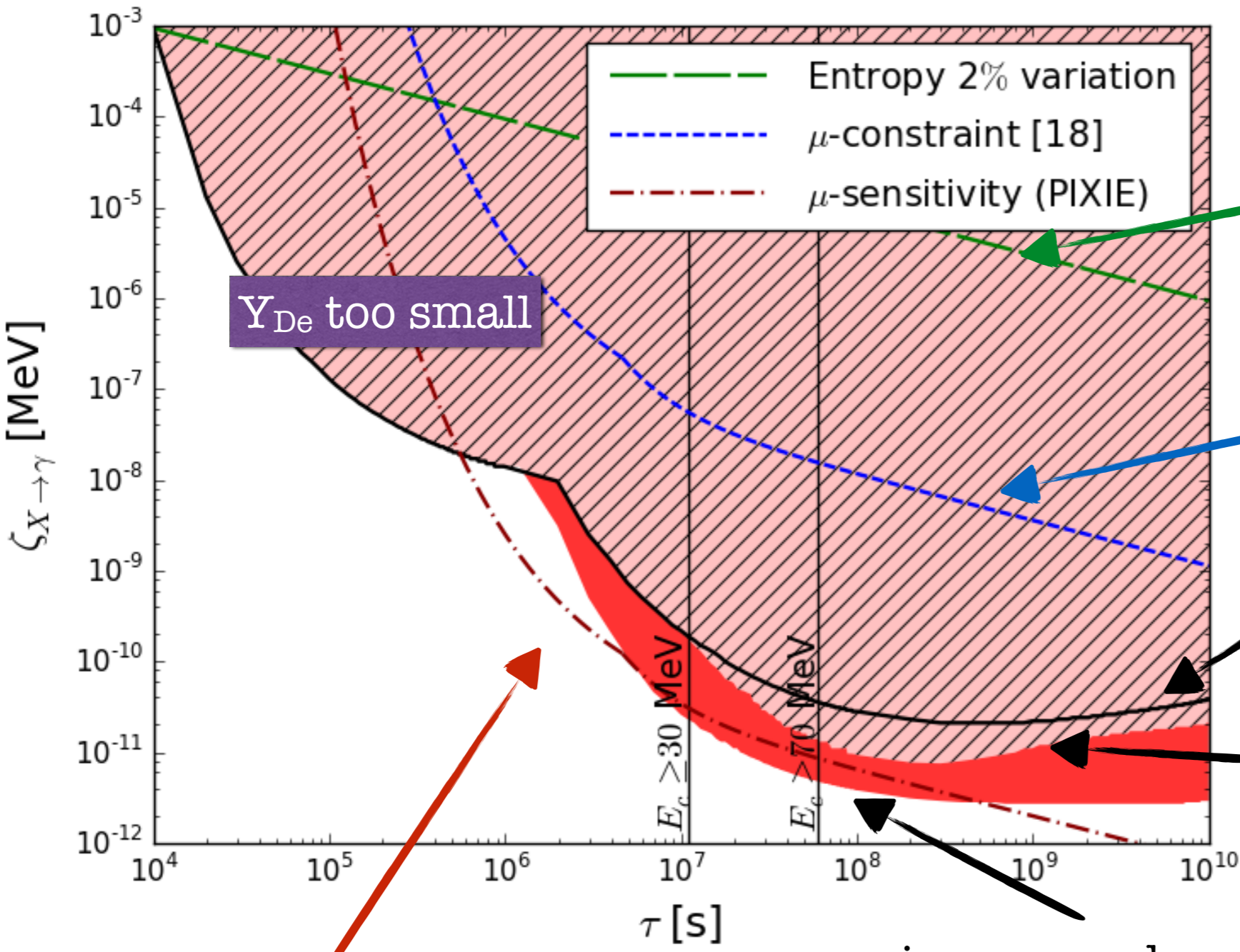
Forecast CMB distortion sensitivity of PIXIE

in a monochromatic photon spectrum of 30 MeV (close to the peak)

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PRD. 91 (2015) 10,
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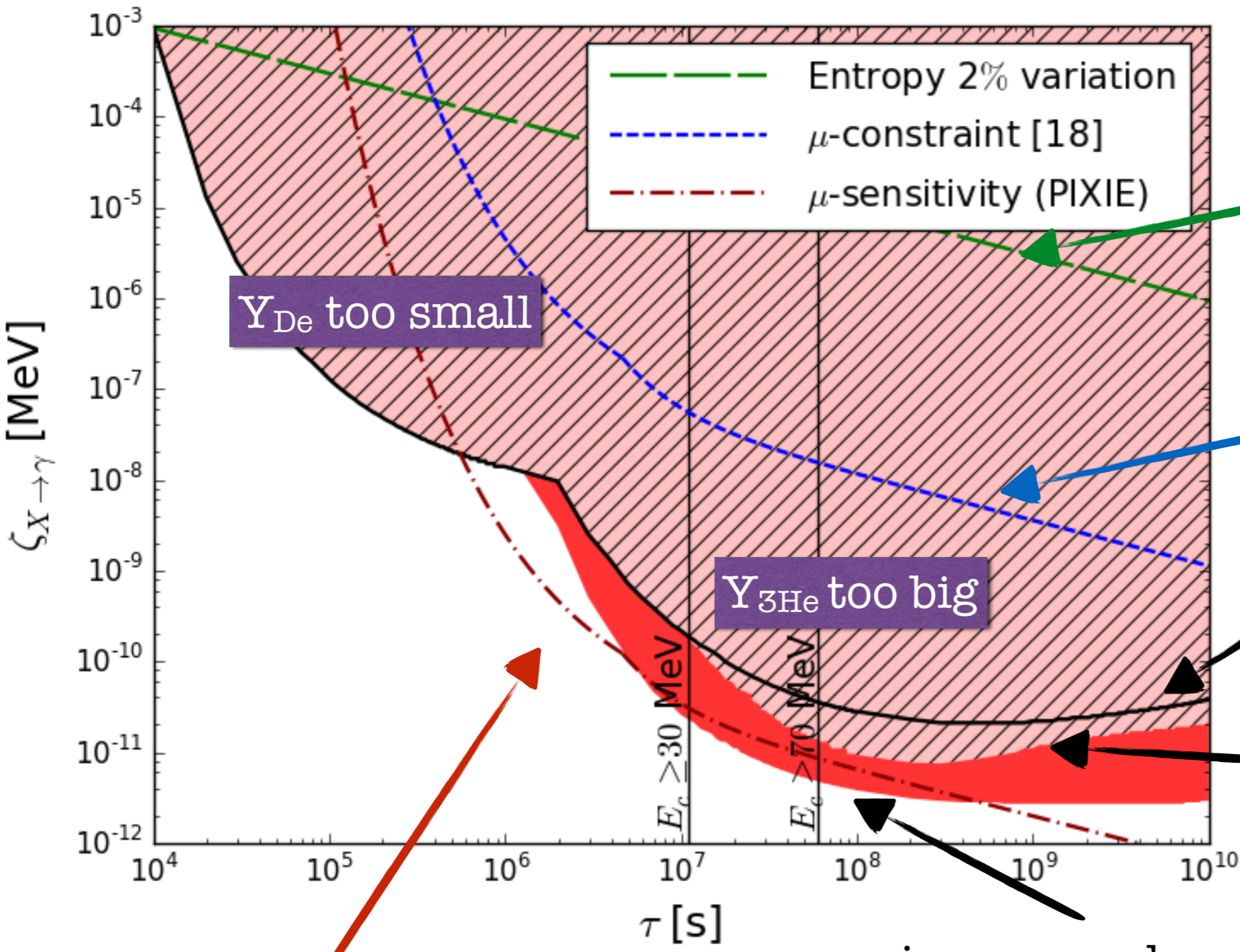
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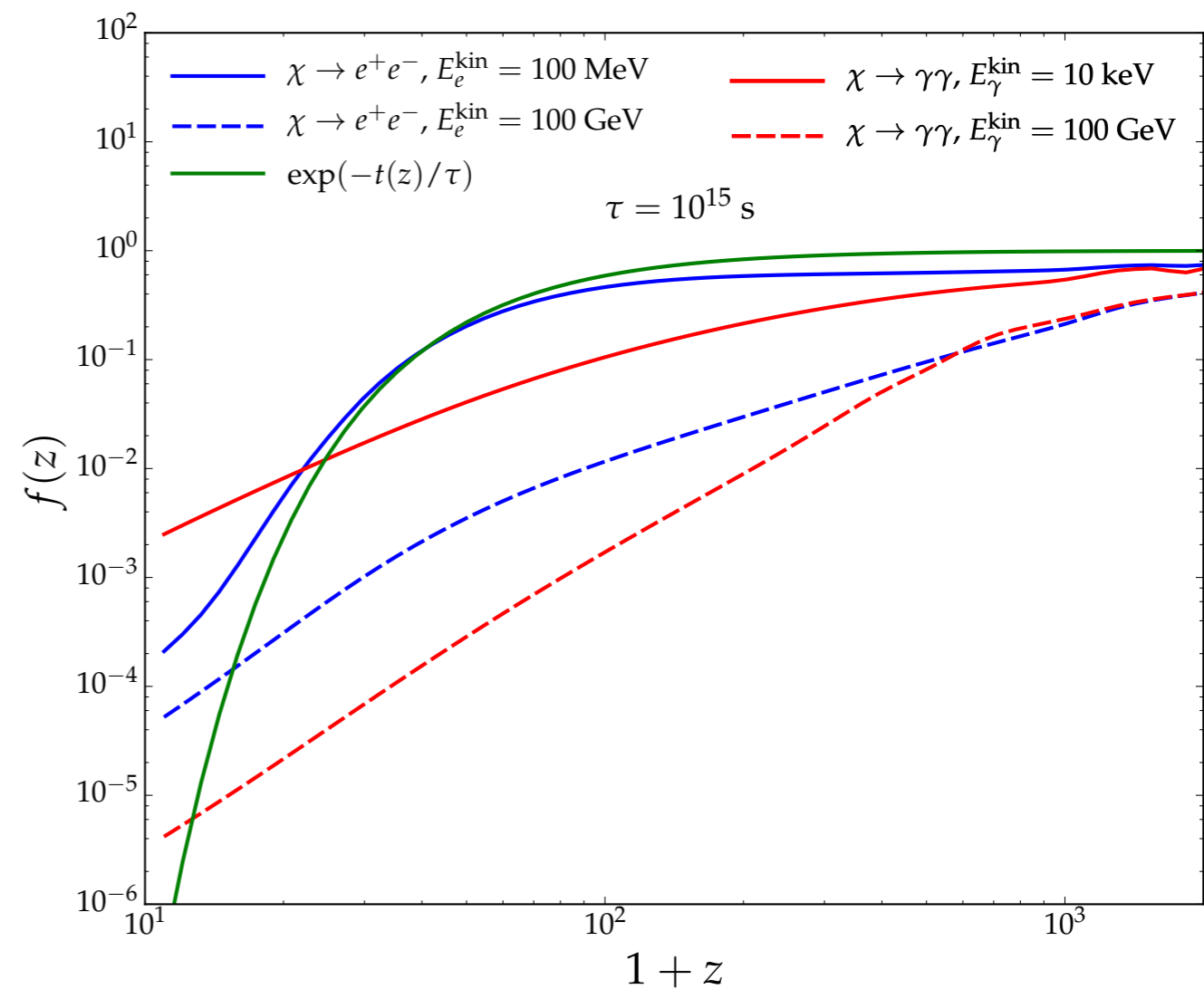
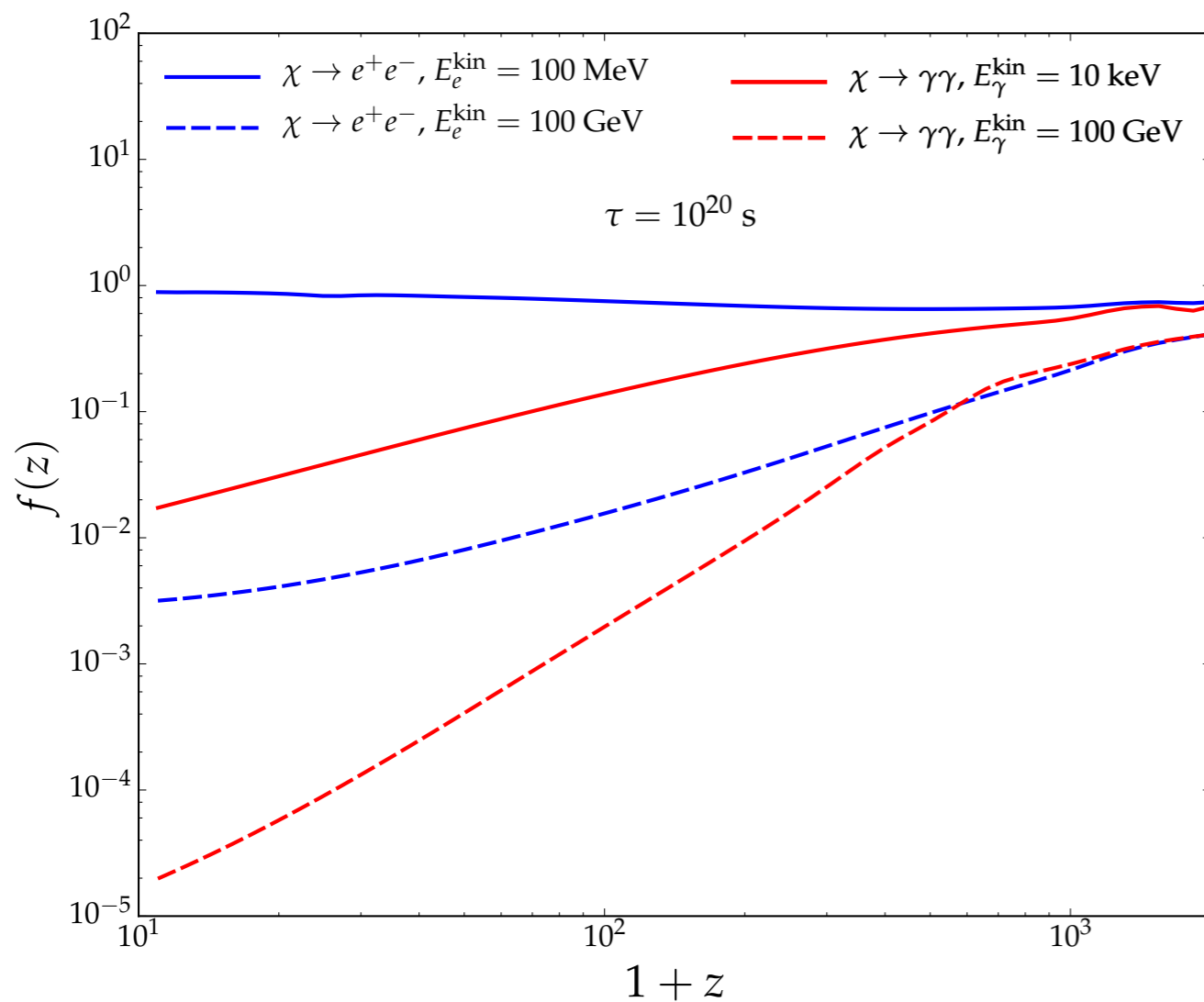
Y_{3He} too big

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PRD. 91 (2015) 10, 103007

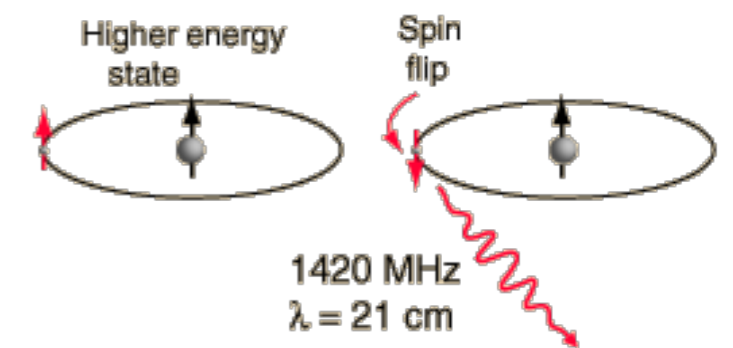
examples of energy deposition efficiency function



- Here, the deposition efficiency is **summed over all channels** : It represents the efficiency of the plasma at absorbing energy.
- It typically depends on the lifetime, particle energy and nature!

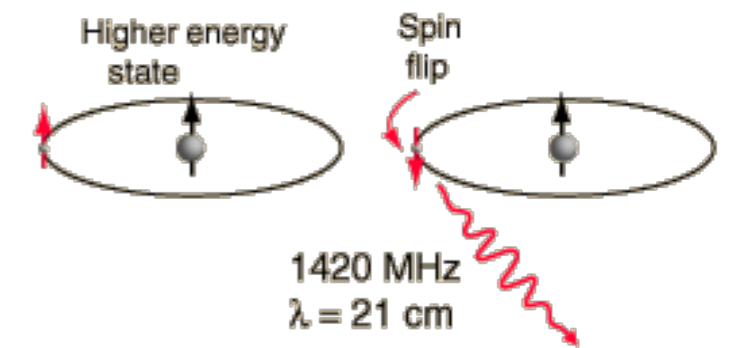
The next-generation experiment : 21 cm with SKA

- Hyperfine transition from neutral hydrogen
- Very sensitive probes of the Epoch of Reionization (EoR)
- Key quantities : **Spin temperature** and **differential brightness temperature**



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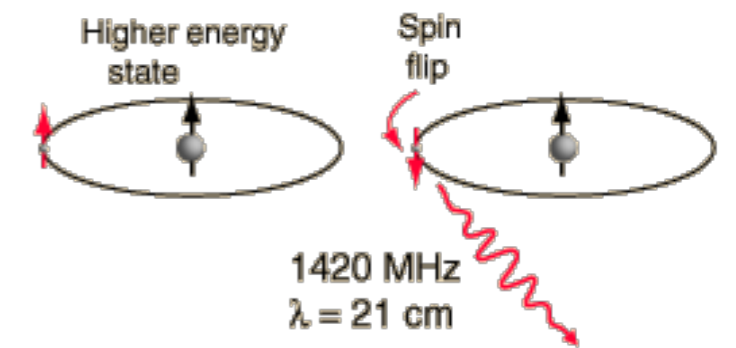
scattering with CMB

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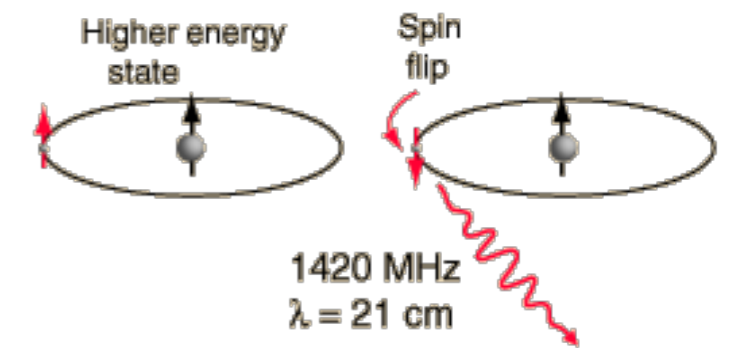
Compare patch of the sky with/without hydrogen clouds:

$$\delta T_b(\nu) = \frac{T_s - T_{\text{CMB}}}{1 + z} (1 - \exp(-\tau_{\nu 21}))$$

see e.g. Furlanetto et al. [astro-ph/0608032]

The next-generation experiment : 21 cm with SKA

- Hyperfine transition from neutral hydrogen
- Very sensitive probes of the Epoch of Reionization (EoR)
- Key quantities : **Spin temperature** and **differential brightness temperature**



$$\frac{n_1}{n_0} = 3e^{-E_{10}/k_B T_S}$$



Exc. = Des-exc.

$$T_S^{-1} = \frac{T_{\text{CMB}}^{-1} + x_c T_K^{-1} + x_\alpha T_c^{-1}}{1 + x_c + x_\alpha}$$

scattering with CMB

collision within the gas

interaction with UV from stars

Compare patch of the sky with/without hydrogen clouds:

$$\delta T_b(\nu) = \frac{T_s - T_{\text{CMB}}}{1 + z} (1 - \exp(-\tau_{\nu 21}))$$

see e.g. Furlanetto et al. [astro-ph/0608032]

Difficulty = **Huge astrophysical uncertainty**, one trick :

SKA will be able to measure $\delta T_b = 5\text{-}10$ mK up to $z = 20/25$ ($\nu = 60$ MHz)