

Contributions of Electrons and Holes to Total Collected Charge in Heavily Irradiated Si Pad and Strip/Pixel Detectors: A Comparison Simulation Study

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Outline

1. The simplified Model of Electric and Weighting Fields:
analytical solutions for collected charge
2. Simulation Results in Analytical Forms and plots
3. Increased Hole Contribution in Collected Charge in
Heavy Irradiation Environments
4. Some Approximations
5. Summary

Simplified Model of Electric and Weighting Fields

analytical solutions for collected charge

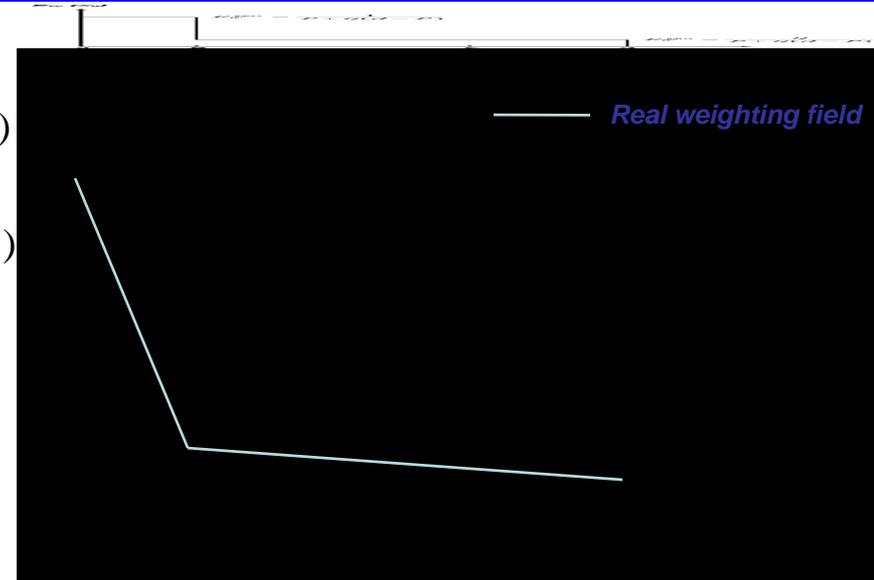
Weighting field:

$$E_W(x_0) = \begin{cases} \frac{1}{P + \eta(d - P)} & (0 < x_0 < P) \\ \frac{\eta}{P + \eta(d - P)} & (P < x_0 < d) \end{cases}$$

$$0 \leq \eta \leq 1$$

P is the segmentation pitch

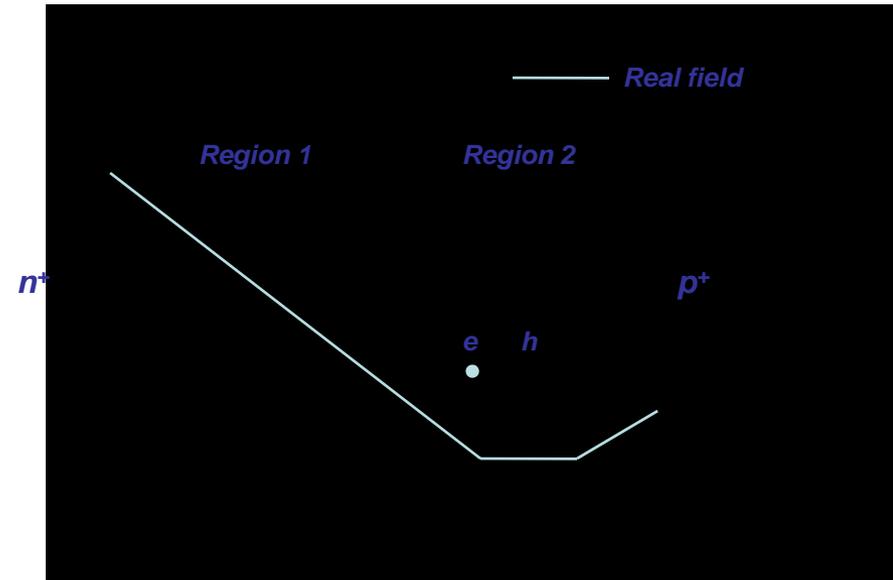
d the detector thickness, or depletion depth



Electric Field:

$$E(x_0) = \begin{cases} E_0 & (0 < x_0 < L) \\ \xi E_0 & (L < x_0 < d) \end{cases} \quad (\xi > 0)$$

$$E_0 = \frac{V}{L + \xi(d - L)}$$



Simplified Model of Electric and Weighting Fields

Two typical cases:

Strip/pixel front, Junction front (SFJF)

Strip/pixel front, Junction back (SFJB)

Region 1

Region 2

Simplified Model of Electric and Weighting Fields

Basic equations

Carrier drift velocity:

$$v_{dr}(x(t)) = \frac{dx(t)}{dt} = \frac{\mu E(x(t))}{1 + \mu E(x(t)) / v_s}$$

Depletion Depth:

$$w = \sqrt{\frac{2\epsilon\epsilon_0 V}{eN_{eff}}}, \quad N_{eff} = 0.02 \cdot \Phi_{n_{eq}}$$

Trapping time constant:

$$\frac{1}{\tau_t} = \eta \cdot \Phi_{n_{eq}} = 5 \times 10^{-7} \text{ cm}^2 / \text{s} \cdot \Phi_{n_{eq}}$$

Induced current by a

Charge layer $\frac{Q_0}{d} \Delta x_0$ **at** x_0 :

$$di^{e,h}(t) = \frac{Q_0}{d} \Delta x_0 \cdot E_W \cdot v_{dr}^{e,h} \cdot e^{-\frac{t}{\tau_t}} = 80 \text{ e's} / \mu\text{m} \cdot \Delta x_0 \cdot E_W \cdot v_{dr}^{e,h} \cdot e^{-\frac{t}{\tau_t}}$$

Total collected charge:

$$Q = \int_0^d 80 \text{ e's} / \mu\text{m} \cdot dx_0 \cdot \left[\int_0^{t_{dr}^e} E_W \cdot v_{dr}^e \cdot e^{-\frac{t}{\tau_t}} dt + \int_0^{t_{dr}^h} E_W \cdot v_{dr}^h \cdot e^{-\frac{t}{\tau_t}} dt \right]$$

Simulation Results

Solutions

We can obtain analytical solutions for collected charges:

Electrons:

$$Q^e = 80e's / \mu m \cdot v_{dr,1}^e \tau_t \frac{P - v_{dr,1}^e \tau_t (1 - e^{-\frac{P}{v_{dr,1}^e \tau_t}})}{P + \eta(d - P)} +$$
$$80e's / \mu m \cdot v_{dr,1}^e \tau_t \frac{\eta[(L - P) - v_{dr,1}^e \tau_t (1 - e^{-\frac{L-P}{v_{dr,1}^e \tau_t}})] + v_{dr,1}^e \tau_t [(1 - e^{-\frac{L-P}{v_{dr,1}^e \tau_t}}) - (e^{-\frac{P}{v_{dr,1}^e \tau_t}} - e^{-\frac{L}{v_{dr,1}^e \tau_t}})]}{P + \eta(d - P)} +$$
$$80e's / \mu m \cdot \frac{\eta v_{dr,2}^e \tau_t [(d - L) - v_{dr,2}^e \tau_t (1 - e^{-\frac{d-L}{v_{dr,1}^e \tau_t}})] + \eta v_{dr,1}^e \tau_t [v_{dr,2}^e \tau_t (1 - e^{-\frac{d-L}{v_{dr,2}^e \tau_t}}) (1 - e^{-\frac{L-P}{v_{dr,2}^e \tau_t}})] + v_{dr,1}^e \tau_t [v_{dr,2}^e \tau_t (1 - e^{-\frac{d-L}{v_{dr,2}^e \tau_t}}) (e^{-\frac{L-P}{v_{dr,1}^e \tau_t}} - e^{-\frac{L}{v_{dr,1}^e \tau_t}})]}{P + \eta(d - P)}$$

(L > P)

Holes:

$$Q^h = 80e's / \mu m \cdot \frac{\eta v_{dr,2}^h \tau_t}{P + \eta(d - P)} \cdot [(d - L) - v_{dr,2}^h \tau_t (1 - e^{-\frac{d-L}{v_{dr,2}^h \tau_t}})] +$$
$$80e's / \mu m \cdot \frac{\eta}{P + \eta(d - P)} \{v_{dr,1}^h \tau_t [(L - P) - v_{dr,1}^h \tau_t (1 - e^{-\frac{L-P}{v_{dr,1}^h \tau_t}})] + v_{dr,2}^h \tau_t [v_{dr,1}^h \tau_t (1 - e^{-\frac{L-P}{v_{dr,1}^h \tau_t}}) (1 - e^{-\frac{d-L}{v_{dr,2}^h \tau_t}})]\} +$$
$$80e's / \mu m \cdot \frac{1}{P + \eta(d - P)} \{v_{dr,1}^h \tau_t [P - v_{dr,1}^h \tau_t (1 - e^{-\frac{P}{v_{dr,1}^h \tau_t}})] + \eta v_{dr,1}^h \tau_t [v_{dr,1}^h \tau_t (1 - e^{-\frac{P}{v_{dr,1}^h \tau_t}}) (1 - e^{-\frac{L-P}{v_{dr,1}^h \tau_t}})] +$$
$$+ \eta v_{dr,2}^h \tau_t [v_{dr,1}^h \tau_t (e^{-\frac{L-P}{v_{dr,1}^h \tau_t}} - e^{-\frac{L}{v_{dr,1}^h \tau_t}}) (1 - e^{-\frac{d-L}{v_{dr,2}^h \tau_t}})]\} \quad (L > P)$$

Where:

$$v_{dr,1}^{e,h} = \mu^{e,h} \cdot E_0, \quad v_{dr,2}^{e,h} = \mu^{e,h} \cdot \xi E_0$$

$$E_0 = \frac{V}{L + \xi(d - L)}$$

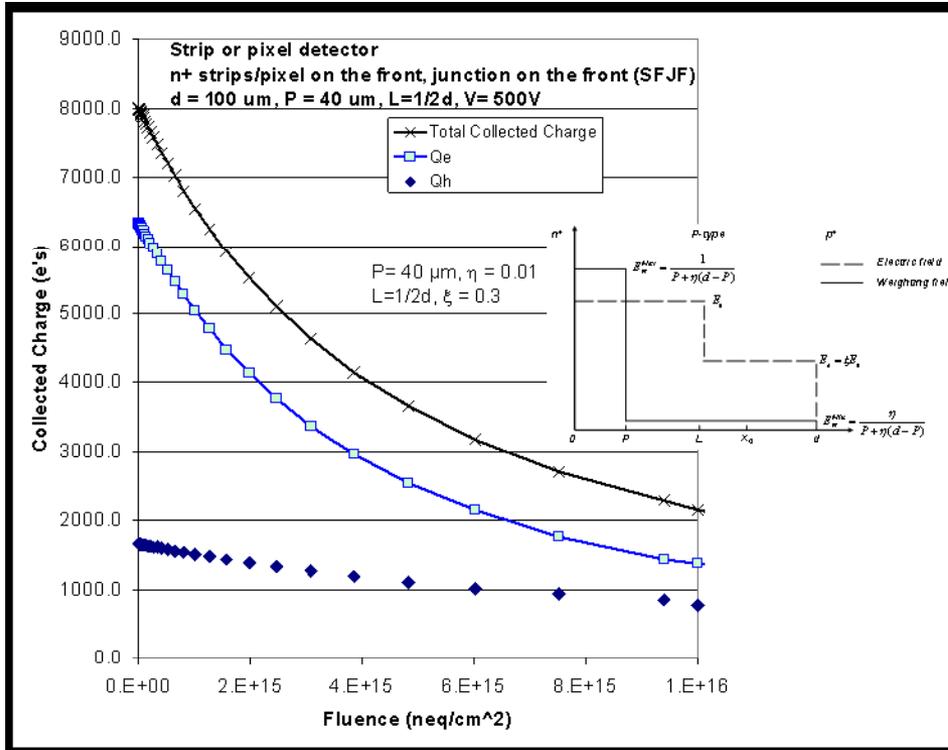
$$Q = f(P, \eta, L, \xi, V, d(\text{or } w)), \mu^e, \mu^h)$$

Simulation Results

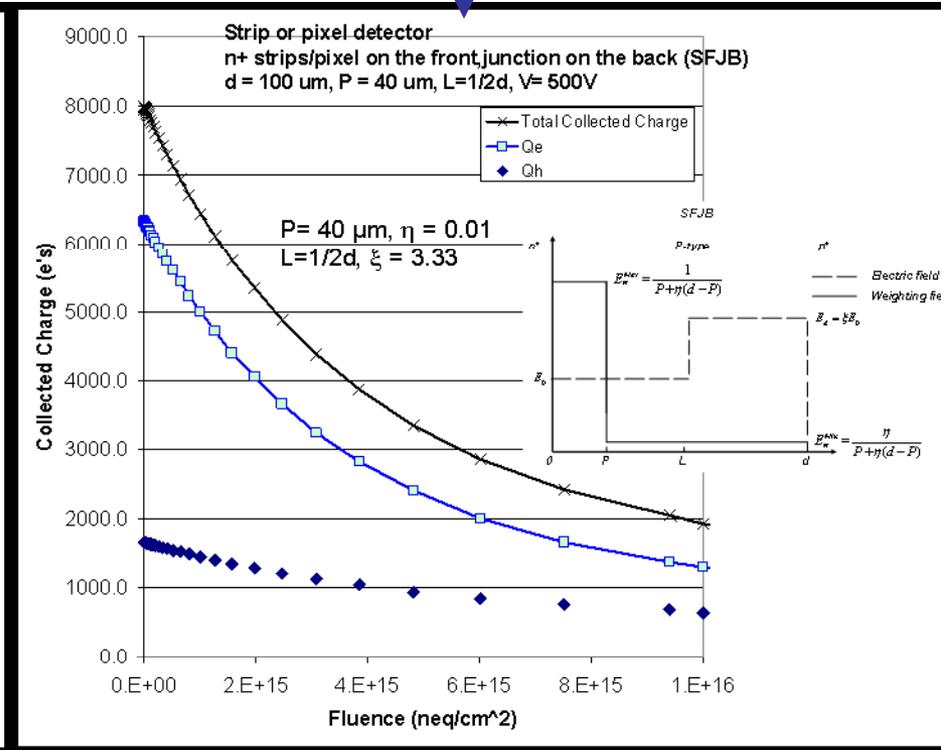
Plots

We can make some plots for some typical cases:

The total collected charge is a little bit lower, but not by much if the low E-field region at the strip side is not too low.



a) SFJF



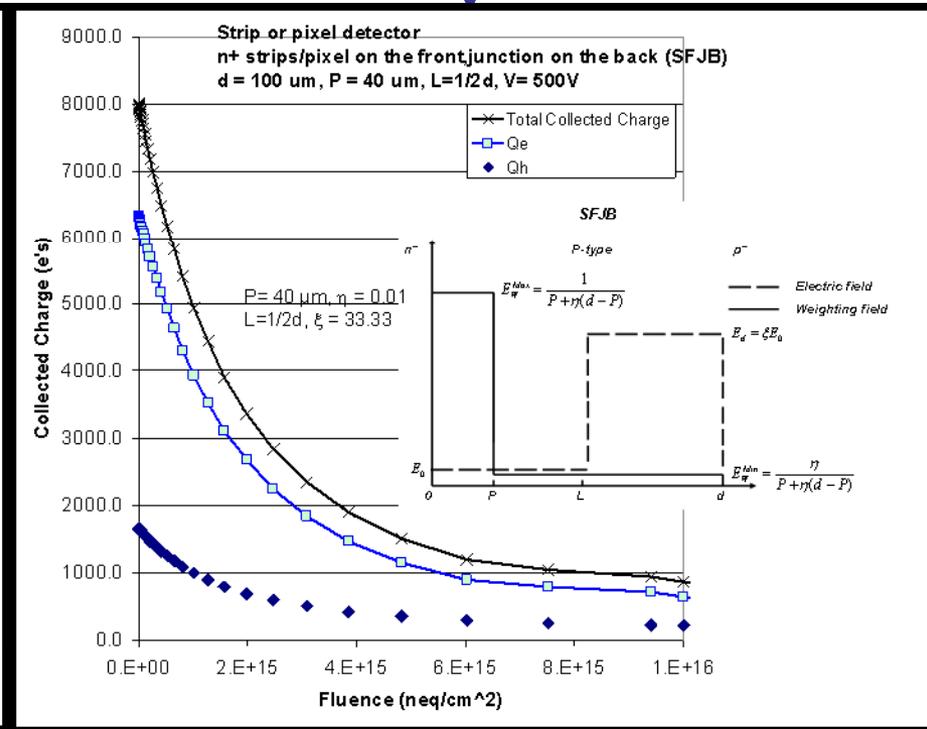
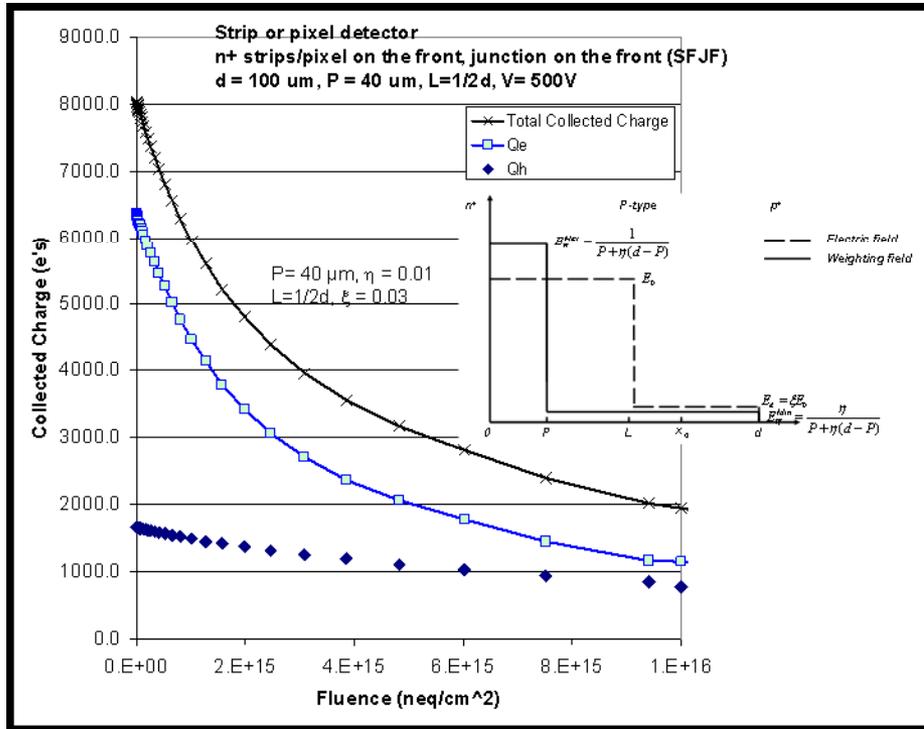
b) SFJB

Fig. 5 Collected charges for a strip or pixel detector with a) junction on the strip side (SFJF), and, b) junction on the backside (SFJB). The high-weighting field is 100 times more than the low one ($\eta = 0.01$), and high-electric field is 3 times more than the low one ($\xi = 0.3$ for JF, and 3.333 for JB).

Simulation Results

Plots

The total collected charge much lower if the low E-field region at the strip side is very low.



a) SFJF

b) SFJB

Fig. 5 Collected charges for a strip or pixel detector with a) junction on the strip side (SFJF), and, b) junction on the backside (SFJB). The high-weighting field is 100 times more than the low one ($\eta = 0.01$), and high-electric field is 30 times more than the low one ($\xi = 0.03$ for JF, and 33.33 for JB).

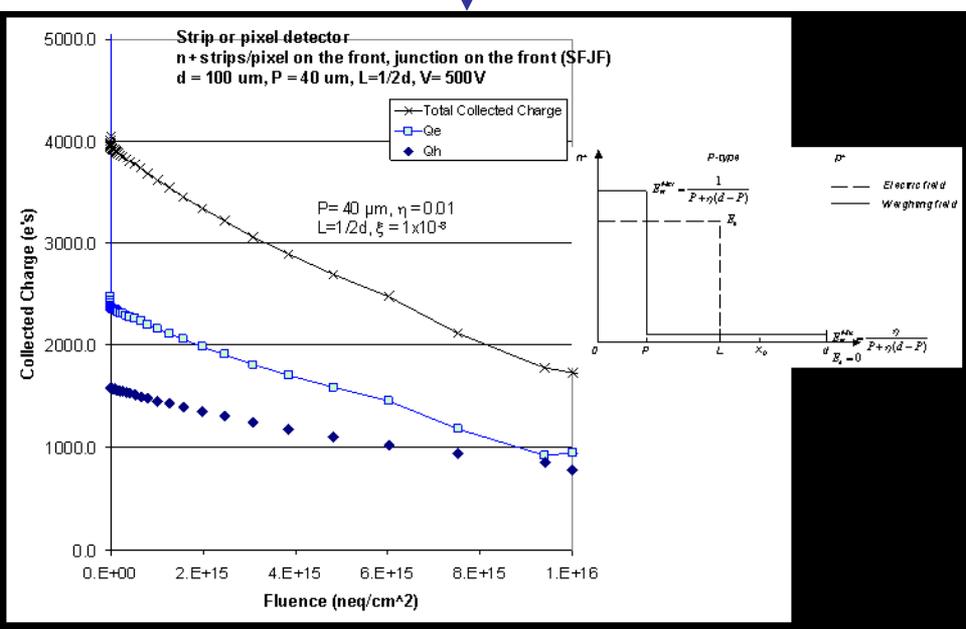
Simulation Results

Plots

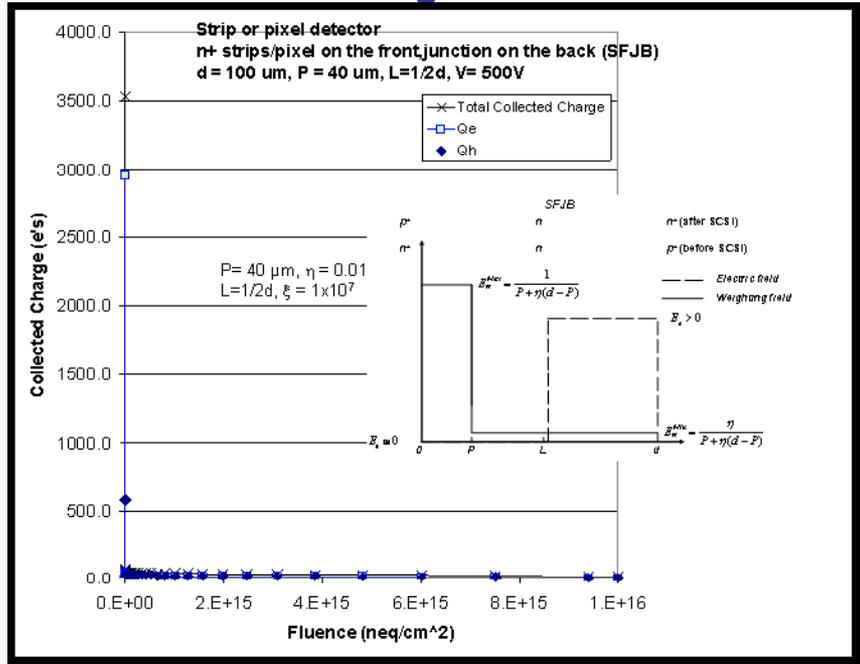
Partial depletion cases:

Half of total collected charge if only half of the detector is depleted.

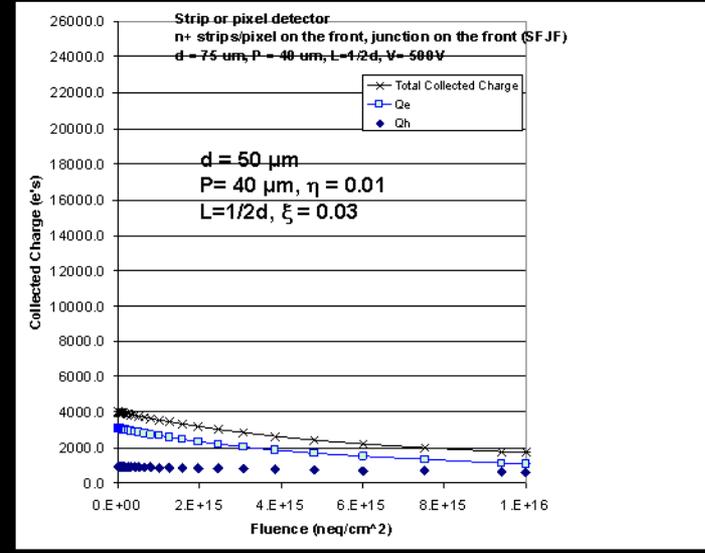
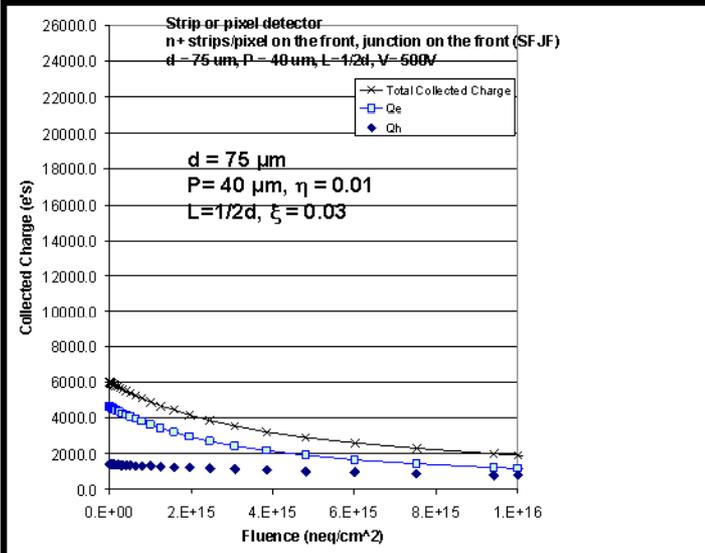
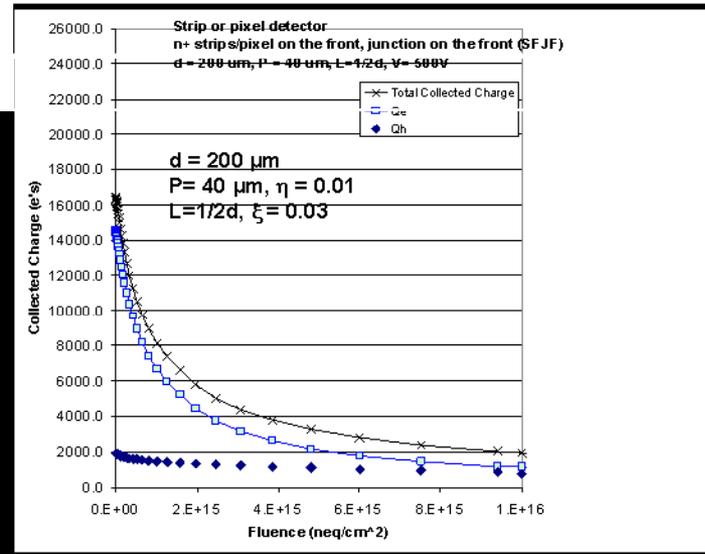
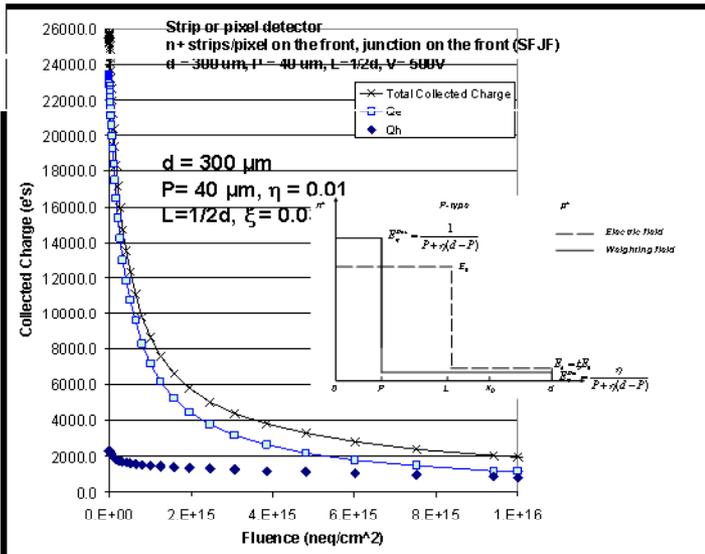
Zero total collected charge if there is no E-field near the strip side.



a) SFJF



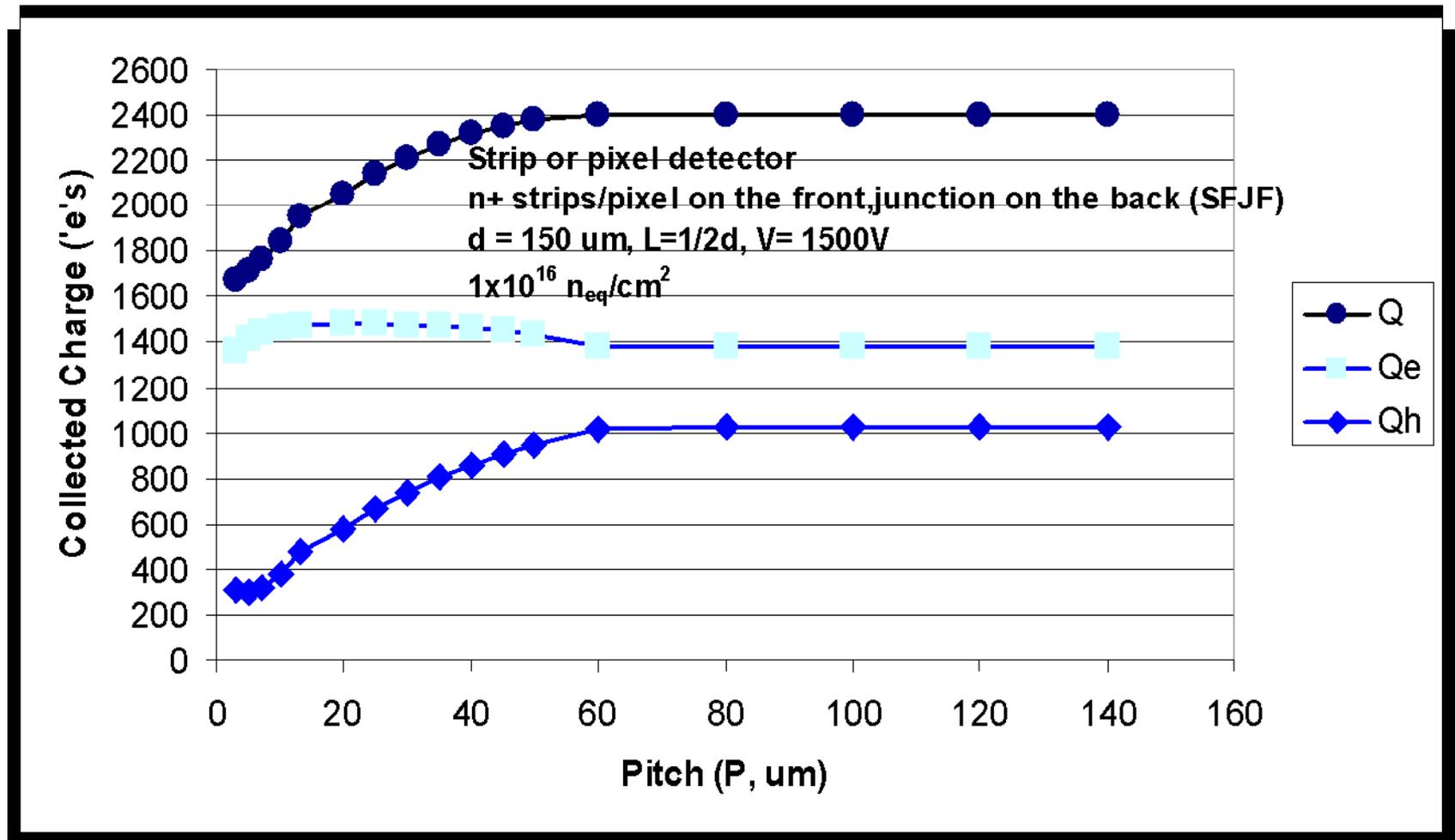
b) SFJB



The thickness the detector, the more contribution of e⁻s to Q at low fluences
 At high fluences (>5x10¹⁵ neq/cm²), total collected charge are almost the same and contribution by holes are approaching those of e⁻s for all thickness >P.

Increased Hole Contribution in Collected Charge in Heavy Irradiation Environments

Detector segmentation/pitch dependence:



For $P \geq 60 \mu\text{m}$, the hole contribution is about 43% due to $P \gg d_{\text{CCE}}$ or d_t d_{CCE} (or d_t) = $v_{\text{dr}} \cdot \tau_t \leq v_s \cdot \tau_t$

For $P < 60 \mu\text{m}$, the hole contribution decreases as the P approaches d_{CCE} or d_t

Increased Hole Contribution in Collected Charge in Heavy Irradiation Environments

Detector segmentation/pitch dependence: Explanations

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For $P \gg d_{CCE}$ or d_{ν}

(cases of high radiation, or large pitch)

hole contribution is compatible to that of electron

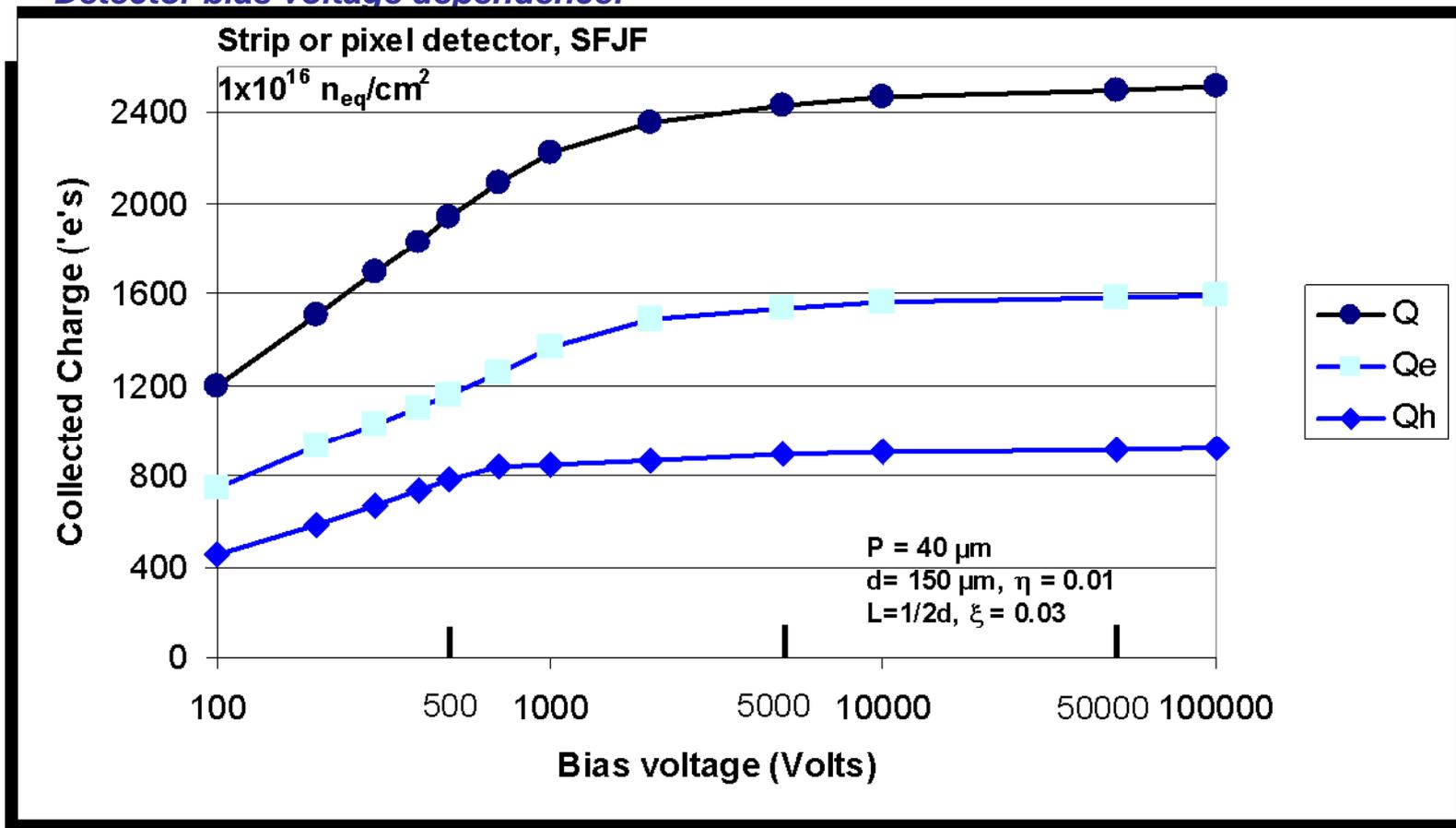
For $P \leq d_{CCE}$ or d_{ν}

(cases of low radiation, or very small pitch)

hole contribution is much smaller than
that of electron

Increased Hole Contribution in Collected Charge in Heavy Irradiation Environments

Detector bias voltage dependence:



For $V \geq 1000$ volts, Q reaches more than **90%** of the maximum

For $P = 40 \mu\text{m}$, the hole contribution is about **36%**

Some Approximations

Partially depleted detector: E-field in region 2 is zero ($\xi=0$), $w = L$

$$Q^e = 80e's / \mu m \cdot v_{dr,1}^e \tau_t \frac{P - v_{dr,1}^e \tau_t (1 - e^{-\frac{P}{v_{dr,1}^e \tau_t}})}{P + \eta(L - P)} +$$

$$80e's / \mu m \cdot v_{dr,1}^e \tau_t \frac{\eta[(L - P) - v_{dr,1}^e \tau_t (1 - e^{-\frac{L-P}{v_{dr,1}^e \tau_t}})] + v_{dr,1}^e \tau_t [(1 - e^{-\frac{L-P}{v_{dr,1}^e \tau_t}}) - (e^{-\frac{P}{v_{dr,1}^e \tau_t}} - e^{-\frac{L}{v_{dr,1}^e \tau_t}})]}{P + \eta(L - P)} +$$

$(L > P)$



$$Q^h = 80e's / \mu m \cdot \frac{\eta}{P + \eta(L - P)} v_{dr,1}^h \tau_t [(L - P) - v_{dr,1}^h \tau_t (1 - e^{-\frac{L-P}{v_{dr,1}^h \tau_t}})] +$$

$$80e's / \mu m \cdot \frac{1}{P + \eta(L - P)} \{ v_{dr,1}^h \tau_t [P - v_{dr,1}^h \tau_t (1 - e^{-\frac{P}{v_{dr,1}^h \tau_t}})] + \eta v_{dr,1}^h \tau_t [v_{dr,1}^h \tau_t (1 - e^{-\frac{P}{v_{dr,1}^h \tau_t}}) (1 - e^{-\frac{L-P}{v_{dr,1}^h \tau_t}})] \}$$

$(L > P)$

Some Approximations

At high fluences (SLHC):

$$Q^e = 80e's / \mu m \cdot v_{dr,1}^e \tau_t = 80e's / \mu m \cdot d_{CCE}^e$$

$$Q^h = 80e's / \mu m \cdot v_{dr,1}^h \tau_t = 80e's / \mu m \cdot d_{CCE}^h$$

$$Q = 80e's / \mu m \cdot (d_{CCE}^e + d_{CCE}^h)$$

At $1 \times 10^{16} n_{eq}/cm^2$: $d_{CCE} = 20 \mu m$:

$$Q \sim 3200 e's$$

Some Approximations

At low fluences ($\leq 10^{15} n_{eq}/cm^2$)

For pad detectors:

$$Q_{pad} \cong Q_0 \left[1 - \frac{1}{6} \left(\frac{L}{v_{dr,1}^e \tau_t} + \frac{L}{v_{dr,1}^h \tau_t} \right) \right]$$

For fully depleted pad detectors:

$$Q_{pad} \cong Q_0 \left[1 - \frac{1}{6} \left(\frac{d}{v_{dr,1}^e \tau_t} + \frac{d}{v_{dr,1}^h \tau_t} \right) \right] = Q_0 \left[1 - \frac{1}{6} \left(\frac{d}{d_{CCE}^e} + \frac{d}{d_{CCE}^h} \right) \right]$$

Summary

1. A simple model has been developed to simulate segmented Si detectors

2. Analytical solutions can be obtained for collected charge $Q = f(P, \eta, L, \xi, V, d(\text{or } w)), \mu^e, \mu^h$

3. Contribution of hole to the total collected charge increases with radiation fluence in a n^+ segmentation Si detector

4. At SLHC fluences close to $1 \times 10^{16} \text{ n}_{\text{eq}}/\text{cm}^2$, contribution of hole to the total collected charge is comparable to that of electrons

5. At SLHC fluences, total collected charge can be approximated as: $Q = 80e's / \mu\text{m} \cdot (d_{\text{CCE}}^e + d_{\text{CCE}}^h)$

6. To improve radiation hardness, carrier trapping distance has to be increased --- e.g. by pre-filling of the traps, or decrease carrier drift distance (3D)

Collected charges simulated with real weighting field

