

# Warm Magnets

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#### Contents

- Introduction: magnetic field and warm magnet principles
- Field description and magnet types
- Practical magnet design & manufacturing
- Permanent magnets
- Examples of accelerator magnets from the early times until the present
- Literature on warm Magnets



## **Maxwell equations**

Integral form

**Differential form** 

$$\begin{split} \oint \vec{H} d\vec{s} &= \int_{A} \left( \vec{J} + \frac{\partial \vec{D}}{\partial t} \right) d\vec{A} & \text{Ampere's law} & rot \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t} \\ \oint \vec{E} d\vec{s} &= -\frac{\partial}{\partial t} \int_{A} \vec{B} d\vec{A} & \text{Faraday's equation} & rot \vec{E} = -\frac{\partial \vec{B}}{\partial t} \\ \int_{A} \vec{B} d\vec{A} &= 0 & \text{Gauss's law for} \\ \int_{A} \vec{D} d\vec{A} &= \int_{V} \rho dV & \text{Gauss's law} & div \vec{B} = 0 \\ \end{split}$$

$$\end{split}$$

$$\begin{split} \text{With:} \quad \vec{B} &= \mu \vec{H} = \mu_{0} (\vec{H} + \vec{M}) \\ \vec{D} &= \varepsilon \vec{E} = \varepsilon_{0} (\vec{E} + \vec{P}) \\ \vec{J} &= \kappa \vec{E} + J_{imp.} \end{split}$$

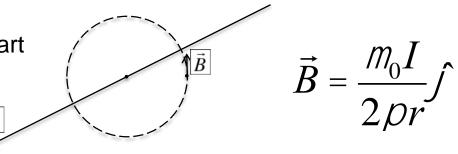


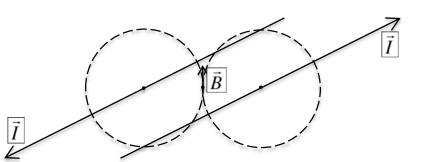
## **Magnetic fields**

From Ampere's law with no time dependencies (I

Integral form) 
$$\dot{D}_C \vec{B} \times d\vec{l} = \mathcal{M}_0 I_{encl.}$$

We can derive the law of Biot and Savart





If you wanted to make a B = 1.5 T magnet with just two infinitely thin wires placed at 100 mm distance in air one needs : I = 187500 A

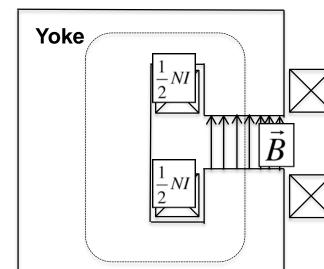
- To get reasonable fields ( *B* > 1 T) one needs large currents
- Moreover, the field homogeneity will be poor



## Iron dominated magnets

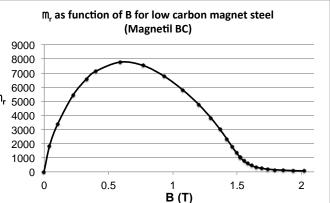
With the help of an iron yoke we can get fields with less current

Example: C shaped dipole for accelerators



 $N \times I = H_{iron} \times l_{iron} + H_{airgap} \times l_{airgap} \triangleright$  $N \times I = \frac{B}{M_0 M_r} \times l_{iron} + \frac{B}{M_0} \times l_{airgap} \bowtie$  $N \times I = \frac{l_{airgap} \times B}{M_0}$  This is valid as  $\mu_r \gg \mu_0$  in the iron : limited to B < 2 T coil B = 1.5 TGap = 50 mm9000 8000 *N* . *I* = 59683 A 7000 6000 2 x 30 turn coil m<sub>r 5000</sub> 4000 I = 994 A3000 2000 1000 @5 A/mm<sup>2</sup>, 200 mm<sup>2</sup> 0 0.5 0 1 14 x 14 mm Cu

 $[\tilde{\mathbf{0}}]_{\mathcal{C}}\vec{H} \times d\vec{l} = N \times I$ 



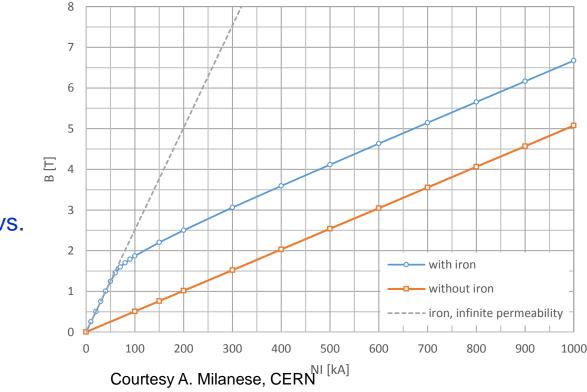
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# Comparison : iron magnet and air coil

Imagine a magnet with a 50 mm vertical gap (horizontal width ~100 mm) Iron magnet wrt to an air coil:

- Up to 1.5 T we get ~6 times the field
- Between 1.5 T and 2 T the gain flattens of : the iron saturates
- Above 2 T the slope is like for an air-coil: currents become too large to use resistive coils



These two curves are the transfer functions – B field vs. current – for the two cases



# Magnetic field quality: multipole description

$$B_{y}(z) + iB_{x}(z) = 10^{-4}B_{1}\sum_{n=1}^{\infty} (b_{n} + ia_{n}) \left(\frac{x + iy}{R_{ref}}\right)^{n-1}$$
  
with:

z = x + iy,

 $B_x$  and  $B_y$  the flux density components in the x and y direction,  $R_{ref}$  the radius of the reference circle,

 $B_1$  the dipole field component at the reference circle,

 $b_n$  the normal nth multipole component,

 $a_n$  the skew nth multipole component.

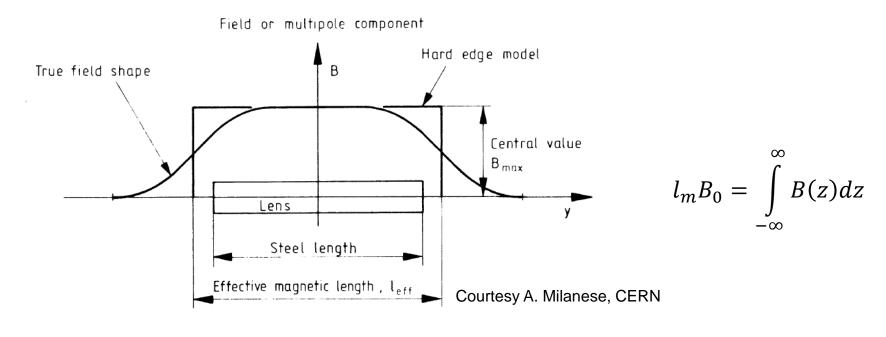
In a ring shaped accelerator, where the beam does multiple passes, one typically demands :

 $a_n, b_n \le 1 \text{ unit } 10^{-4}$ 



# **Magnetic Length**

#### In 3D, the longitudinal dimension of the magnet is described by a magnetic length



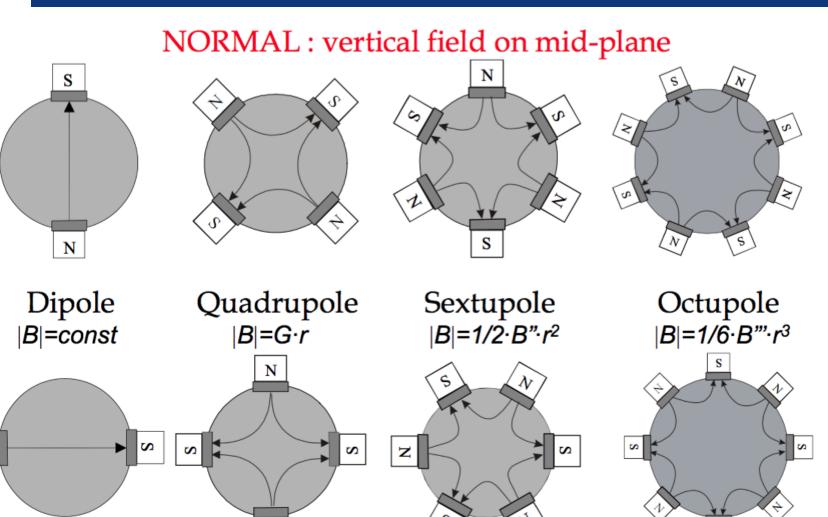
magnetic length  $L_{mag}$  as a first approximation:

- For dipoles  $L_{mag} = L_{yoke} + d$
- For quadrupoles:  $L_{mag} = L_{yoke} + r$

- d = pole distance
- r = radius of the inscribed circle between the 4 poles



## Types of magnet fields for accelerators



Courtesy D. Tommasini, CERN SKEW : horizontal field on mid-plane

N

 $\mathbf{z}$ 

S



## Symmetry and allowed harmonics

In a fully symmetric magnet certain field harmonics are natural.

Magnet type	Allowed harmonics $b_n$
n=1 Dipole	n=3,5,7,
n=2 Quadrupole	n=6,10,14
n=3 Sextupole	n=9,15,21
n=4 Octupole	n=12,20,28

Non-symmetric designs and fabrication errors give rise to non allowed harmonics:  $b_n$  with n other than listed above and  $a_n$  with any n

NB: For "skew" magnets this logic is inverted !



## **Basic magnet types**

Mag	gnet	Pole shape	<b>Transfer function</b>	Inductance (H)
W	: pole width : vertical gap	parallel	B=µ0NI/g	$L=\mu_0 N^2 A/g$ A \approx (w+1.2\cdot g)\cdot (l+g)
	: pole width : vertical gap	parallel	B=µ0NI/g	$L=\mu_0 N^2 A/g$ A \approx (w+1.2\cdot g)\cdot (l+g)
N N S txlaneturs : 20 t :	: pole width : pole gap coil width	parallel	B=µ0NI/g	$L=2\mu_0 N^2 A/g$ $A \approx (d+2/3t) \cdot (l+g)$
S N g	: pole width : pole gap coil width	parallel	$B=\mu_0 NI/g$	$L=\mu_0 N^2 A/g$ A \approx (d+2/3t)·(l+g)
	aperture radius coil distance coil width	2xy=R <sup>2</sup>	$\begin{array}{c} B(r)=G \cdot r\\ G=2\mu_0 NI/R^2 \end{array}$	$L=8\mu_{0}N^{2}A/R \\ A \approx (d+1/3t) \cdot (l+2/3R)$
d :	aperture radius coil distance coil width	$3x^2y-y^3=R^3$	$\begin{array}{c} B(r) = S \cdot r^2 = \frac{1}{2}B'' \cdot r^2 \\ S = 3\mu_0 NI/R^3 \end{array}$	$L=20\mu_0 N^2 A / R A \approx (d+1/3t) \cdot (l+1/2R)$
3	Courtesy D. Tomma	sini, CERN		11



# Practical magnet design & manufacturing

Steps in the process:

- 1. Specification
- 2. Conceptual design
- 3. Raw materials choice
- 4. Detailed design
  - 1. Coil cross-section geometry: cooling
  - 2. Yoke shape, pole shape: FE model optimization
  - 3. Yoke ends, coil ends design
- 5. Yoke manufacturing, tolerances, alignment, structure
- 6. Coil manufacturing, insulation, impregnation type
- 7. Magnetic field measurements



## **Specification**

Before you start designing you need to get from the accelerator designers:

- B(T) or G (T/m) (higher orders: G<sub>3</sub>(T/m<sup>2</sup>), etc)
- Magnet type: C-type, H-type, DC (slow ramp) or AC (fast ramp)
- Aperture:
  - Dipole : "good field region"  $\rightarrow$  airgap height and width
  - quads and higher order: "good field region"  $\rightarrow$  aperture inscribed circle
- Magnetic length and estimated real length
- Current range of the power convertor (and the voltage range: watch out for the cables )
- Field quality:

dipole:  $\frac{\Delta B}{B}$  (ref volume), quadrupole:  $\frac{\Delta G}{G}$  (reference circle)

or  $b_n, a_n$  for n = 1, 2, 3, 4, 5, ...

- Cooling type: air, water ( $\mathsf{P}_{max}$  ,  $\Delta p_{max}$  and  $\mathsf{Q}_{max}$  (I/min)
- Jacks and Alignment features
- Vacuum chamber to be used  $\rightarrow$  fixations, bake-out specifics

These need careful negotiation and often iteration after conceptual (and detailed) design



## **Conceptual design**

• From *B* and *I* you get *NI* (A)

$$NI = \frac{l_{airgap}B}{\mu_0}$$

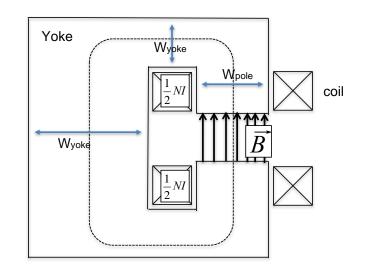
- From NI (A) and the power convertor I<sub>max</sub> you get N
- Then you decide on a coil X-section using:

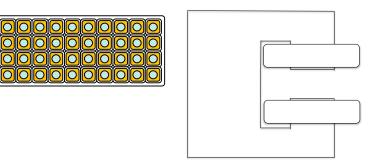
 $j_{coil} = 5 \ ^{A}/_{mm^{2}}$  for water cooled or  $j_{coil} = 1 \ ^{A}/_{mm^{2}}$  for air cooled

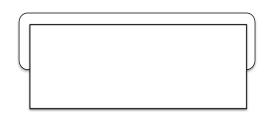
- This defines the coil cavity in the yoke (you add 0.5 mm insulation around each conductor and 1 mm ground insulation around the coil) and select the best fitting rectangular
- You can the draw the draft X-section using:

$$W_{yoke} = W_{pole} \frac{B}{B_{sat}}$$
 with  $1.5 T < B_{sat} < 2 T$ 

- Decide on the coil ends: racetrack, bedstead
- You now have the rough magnet cross section and envelope









### **Power generated**

Power generated by coil

• DC: from the length of the conductor  $N \cdot L_{turn}$ , the cross section  $\sigma$  and the specific resistivity  $\rho$  of the material one gets the spent Power in the coil

$$P/l[W/m] = \frac{\rho}{S}I^2 \quad \text{with:} \qquad \qquad \rho_{Cu} = 1.72(1+0.0039(T-20))10^{-8}\Omega m$$
$$\rho_{Al} = 2.65(1+0.0039(T-20))10^{-8}\Omega m$$

For AC: take the average  $l^2$  for the duty cycle

Power losses due to hysteresis in the yoke: (Steinmetz law up to 1.5 T)  $P[W/kg] = \eta f B^{1.6} \text{ with } \eta = 0.01 \text{ to } 0.1, \ \eta_{Si \text{ steel}} \approx 0.02$ 

Power losses due to eddy currents in the yoke

$$P[W/kg] = 0.05 \left( d_{lam} \frac{f}{10} B_{a\nu} \right)^2$$

with  $d_{lam}$  the lamination thickness in mm,  $B_{av}$  the average flux density



# **Cooling circuit parameters**

Aim: to design  $d_{cooling}$ ,  $P_{water}[bar]$ ,  $\Delta P[bar]$ , Q[l/min]

- Choose a desired  $\Delta T$  (20°C or 30°C depending on the  $T_{cooling water}$ )
- with the heat capacity of water (4.186 kJ/kg°C) we now know the required water flow rate: Q(I/min)
- The cooling water needs to be in moderately turbulent regime (with laminar flow the flow speed is zero on the wall !): Reynolds > 2000

$$R_e = \frac{dv}{v} \sim 140d[mm]v[m/s] \text{ for } T_{water} \sim 40^{\circ}C$$

A good approximation for the pressure drop in smooth pipes can be derived from the Blasius law, giving:

$$\Delta P[bar] = 60L[m] \frac{Q[l/min]^{1.75}}{d[mm]^{4.75}}$$



## **Theoretical pole shapes**

The ideal poles for dipole, quadrupole, sextupole, etc. are lines of constant scalar potential

Dipole  $y = \pm h/2$  straight line

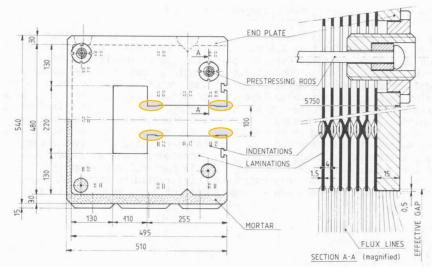
quadrupole 
$$2xy = \pm r^2$$
 hyperbola

sextupole 
$$3x^2y - y^3 = \pm r^3$$

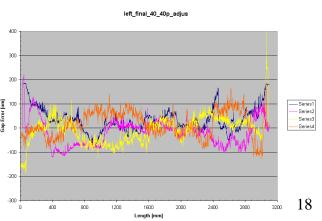


# Practical pole shapes: shims and alignment features

 Dipole example: below a lamination of the LEP main bending magnets, with the pole shims well visible



- Quadrupoles: at the edge of the pole one can put a combination a shim and alignment feature (examples: LHC-MQW, SESAME quads, etc)
- This then also allows to measure the pole distances : special instrumentation can be made for this





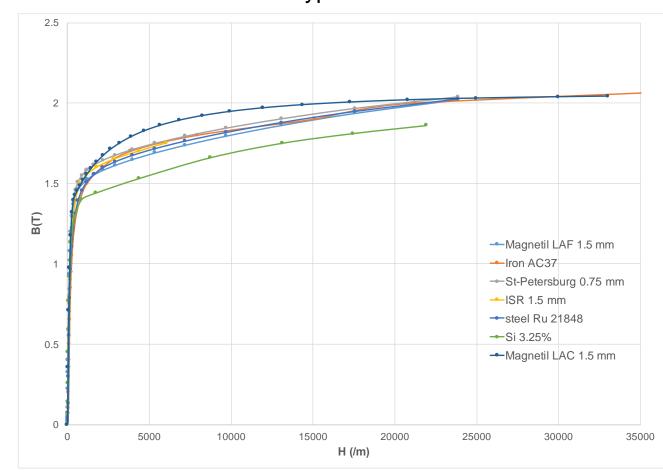
# Finite Element electromagnetic models

- Aim of the electromagnetic FE models:
  - The exact shape of the yoke needs to be designed
    - Optimize field quality: adjust pole shape, minimize high saturation zones
    - Minimize the total steel amount (magnet weight, raw material cost)
  - Calculate the field: needed for the optics and dynamic aperture modelling
    - transfer function  $B_{xsection}(I)$ , Bdl, magnetic length
    - multipoles (in the centre of the magnet and integrated)  $b_n$  and  $a_n$
  - Some Electromagnetic FE software packages that are often used:
    - Opera from Cobham: 2D and 3D commercial software see: <u>http://operafea.com/</u>
    - "Good old" Poisson, 2D: now distributed by LANL-LAACG see: http://laacg.lanl.gov/laacg/services/download\_sf.phtml
    - ROXIE (CERN) 2D and 3D, specialized for accelerator magnets; single fee license for labs & universities see: <u>ttps://espace.cern.ch/roxie/default.aspx</u>
    - ANSYS Maxwell: 2D and 3D commercial software see: <u>http://www.ansys.com/Products/Electronics/ANSYS-Maxwell</u>



## FE models: steel curves

You can use a close 'generic' B(H) curve for a first cut design You HAVE to use a measured, and smoothed, curve to properly calculate  $B_{xsection}(I)$ ,  $\int_{Bdl}$ ,  $b_n$  and  $a_n$ As illustration the curves for several types of steel:



CAS Budapest, 7-Oct-2016, warm magnets, GdR



GdR

magnets,

warm

**Dct-2016** 

CAS Budapest,

Btot (T)

2.069 1.960 1.852 1.743 1.634 1.525

1.416 1.307 1.198 1.089 0.980

0.871 0.762 0.653 0.544 0.436 0.327 0.218 0.109

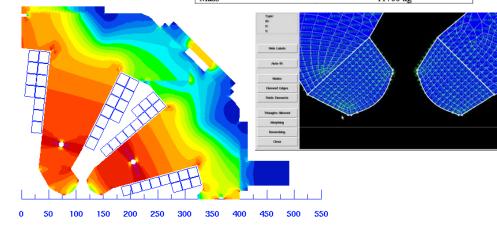
# Yoke shape, pole shape: FE model optimization

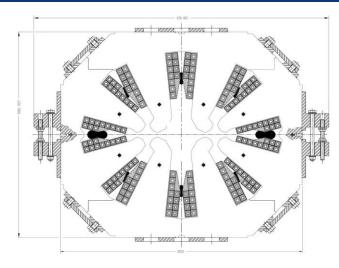
Use symmetry and the thus appropriate boundary conditions to model only  $\frac{1}{4}$ <sup>th</sup> (dipoles, quadrupoles) or even 1/6<sup>th</sup> sextupoles.

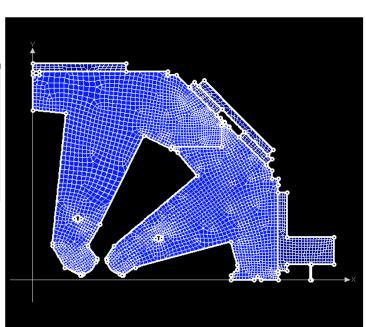
Meshing needs attention in the detailed areas like

poles, slits, etc

Magnet type	MQWA	MQWB
Magnetic length	3.1 m	
Beam separation	224 mm	
Aperture diameter	46 mm	
Operating temperature	< 65° C	
Nominal gradient	35 T/m	30 T/m
Nominal current	710 A	600 A
Inductance	28 mH	
Resistance	37 mΩ	
Conductor X-section	20.5 x 18.0 mm <sup>2</sup> inner poles	
Conductor X-section	17.0 x 17.0 mm <sup>2</sup> outer poles	
Cooling hole diameter	7 mm inner poles,	
Cooling hole diameter	8 mm outer poles	
Number of turns per magnet	8 x 11	
Minimum water flow	28 1/min	
Dissipated power at I <sub>nom</sub>	19 kW	14 kW
Mass	11700 kg	









## Yoke manufacturing

- Yokes are nearly always laminated to reduce eddy currents during ramping
- Laminations can be coated with an inorganic (oxidation, phosphating, Carlite) or organic (epoxy) layer to increase the resistance
- Magnetic properties: depend on chemical composition + temperature and • mechanical history
- Important parameters: coercive field  $H_c$  and the saturation induction.
  - $-H_c$  has an impact on the remnant field at low current
    - $H_c < 80$  A/m typical
    - $H_c < 20$  A/m for magnets ranging down also to low field B < 0.05 T
  - low carbon steel (C content < 0.006%) is best for higher fields B > 1 T

Field Strength [A/m]	Minimum Induction [T]	Example	Field Strength H [A/m]	Minimum Induction B [T]
40	0.20	specification for	100	0.07
60	0.50	1.5 mm epoxy	300	1.05
120	0.95	thick oxide steel	500	1.35
500	1.4	for the LHC	1000	1.50
1 200	1.5	warm separation	2500	1.62
2 500	1.62	magnets,	5000	1.72
5 000 10 000	1.71 1.81	$B_{max}$ = 1.53 T	10000	1.82
24 000	2.00	$D_{max} = 1.55$ T		

Example specification for 0.5 mm thick epoxy coated steel for LHC transfer line corrector magnet B<sub>max</sub>=0.3 T



## Yoke manufacturing

#### Stacking an MBW dipole yoke stack



#### Stacking an MQW quadrupole yoke stack



#### MQW yoke assembly





## Yoke stack manufacturing

#### Double aperture LHC quadrupole MQW

Stacking on a precision table







#### Welding the structural plates



#### Finished stack





# Yokes: holding a laminated stack together

- Yokes are either
  - Glued, using epoxy coated laminations
  - Welded, full length plates are welded on the outside
  - Compressed by tie rods in holes
  - or a combination of all these
- To be able to keep the yoke (or yoke stack) stable you probably need end plates (can range from  $\pm$  1 cm to 5 cm depending on the size)
  - The end plates have pole chamfers and often carry end shims
  - Glued yoke (MCIA LHC TL)





Welded stack





# Coil manufacturing, insulation, impregnation type

- Winding Cu conductors is an well established technique
- When the Cu conductor is thick it is best to use "dead soft" Cu (T treatment)
- Insulation of the coil
  - Glass fibre epoxy impregnated
    - Individual conductor 0.5 mm glass fibre, 0.25 mm tape wound half lapped
    - Impregnated with radiation resistant epoxy, total glass volume ratio >50%
  - For thin conductors: Cu emanel coated, possibly epoxy impregnated afterwards



## **Coil ends**

For dipoles some main types are racetrack of bedstead







#### Quadrupoles

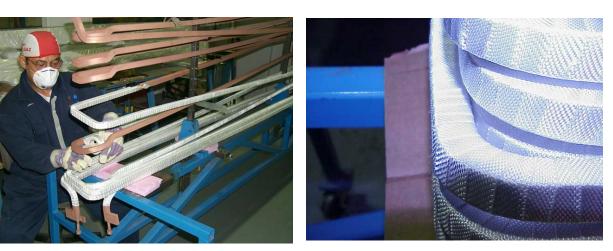






## **Coil manufacturing**

#### MQW Glass fibre tape wrapping.



Glass fiber tape winding



# Winding the hollow Cu conductor









## **Coil manufacturing**

Mounted coil



#### coil electrical test (under water !)



#### Dipoles racetrack coil



#### MBXW Coil winding

#### Finished MBXW coil

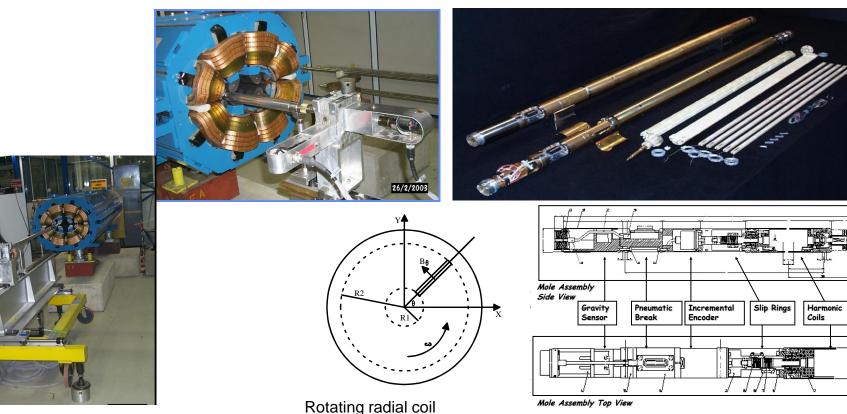




## **Magnetic field measurements**

Several Magnetic Measurements techniques can be applied, e.g.:

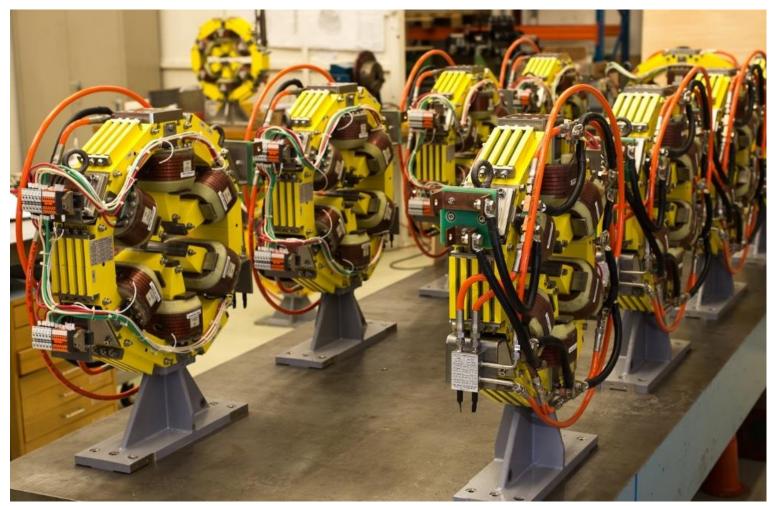
- Rotating coils: multipoles and integrated field or gradient in all magnets
- Stretched wire: magnetic centre and integrated gradient for n > 1 magnets
- Hall probes: field map
- Pickup coils: field on a current ramp
- Example below : MQW : double aperture quadrupole for the LHC.





## **Sextupoles**

• These are sextupoles (with embedded correctors) of the main ring of the SESAME light source

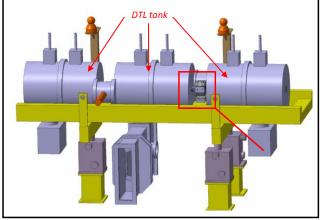


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### **Permanent magnets**

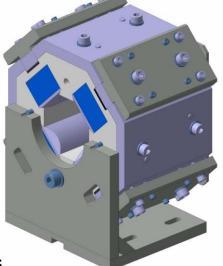
#### Linac4 @ CERN permanent magnets , quadrupoles

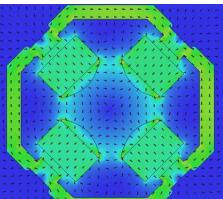


Pictured : Cell-Coupled Drift Tube Linac module.

- Permanent magnet because of space between DTL tanks
- Sm<sub>2</sub>Co<sub>17</sub> permanent magnets
- Integrated gradient of 1.3 to 1.6 Tesla
- 15 magnets
- Magnet length 0.100 m
- Field quality/amplitude tuning blocks





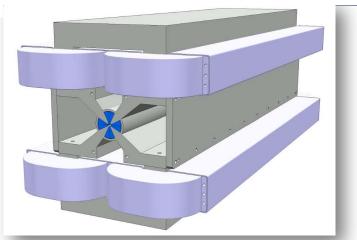


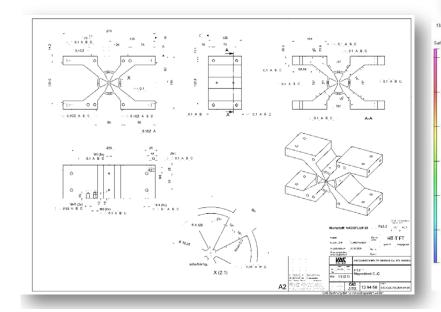


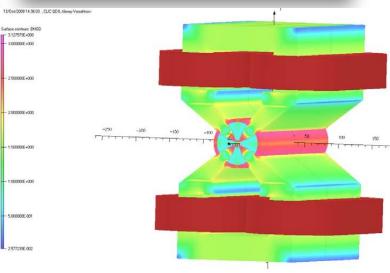
## Hybrid magnets

CLIC final focus,

*Gradient:* > 530 T/m *Aperture* Ø: 8.25 mm *Tunability:* 10-100%







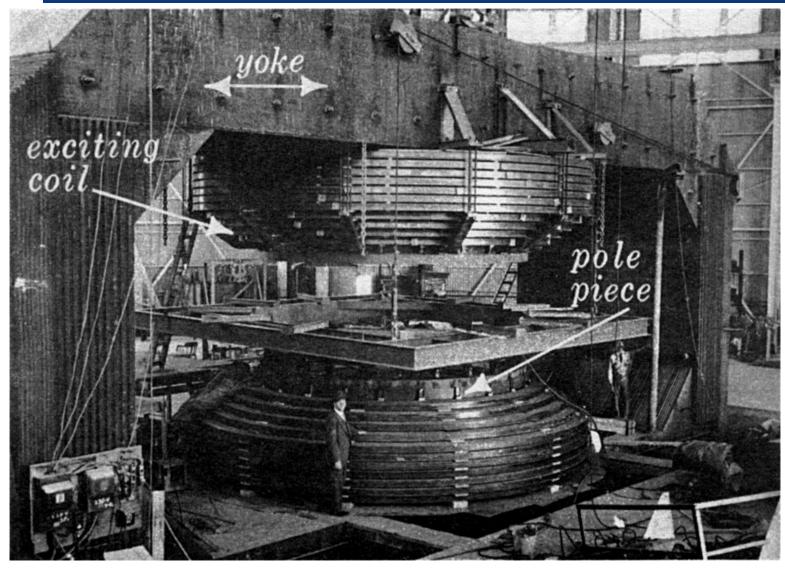


## Examples;

# Some history, some modern regular magnets and some special cases



## The 184" (4.7 m) cyclotron at Berkeley (1942)

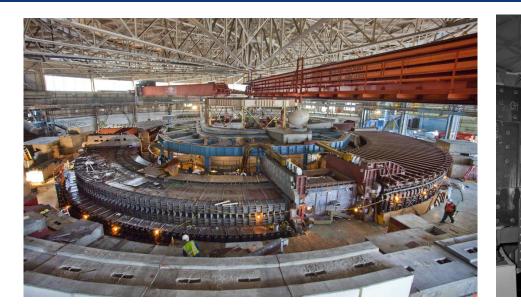




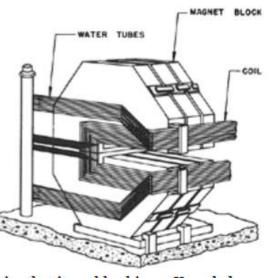
## Some early magnets (early 1950-ies)

Bevatron (Berkeley) 1954, 6.2 GeV











# **PS combined function dipole**

	Magnetic field:		Equation of hyperbolic part: (243.00+r) z = 12150 mm <sup>2</sup>
	at injection	147 G	
	for 24.3 GeV	1.2 T	
	maximum	1.4 T	
	Weight of one magnet unit	38 t	90.0 100.36 90.0 124.0
R	Gradient @1.2 T : 5 T/m		
	Equipped with pole-face		57*28'
GdR	windings for higher order	Water cooled AI race-	Tolerance within the shaded orea \$0.02 mm
S,	corrections	track coils	<b>₩-2</b> □ <sub>nom</sub> = 288,4 R = 70079mm
magnets,	Connection of the PFW main windings for R type magnet		
ag i	Defocusing upstream	TO JAIG	FINAL POLE PROFILE.
Ш			Fig. 9: Final pole profile.
Е			
warm	· · · · · · · · · · · · · · · · · · ·	100	Ratinange consers Devi-tilled stats
-Oct-2016,			
20			
Ч	Connection of the PFW main windings for magnet type S		
Ŏ	Focusing upstream ring center Defocusing downstream		Belt hairs
7		A Real Contraction of the Internet	
Budapest,			
be			a) "OPEN" BLOCK, CPS MAGNET BLOCKS,
Ida			(All dimensions in mm) Fig. 12: Final form of the magnet blocks.
AS			
Ċ			Courtesy D. Tommasini, CERN 37

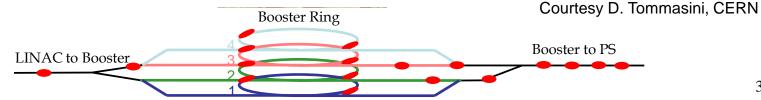


## **CPS** booster

4 accelerator rings in a common yoke. (increase total beam intensity by 4 in presence of space charge limitation at low energy): B=1.48 T @ 2 GeV Was originally designed for 0.8 GeV !

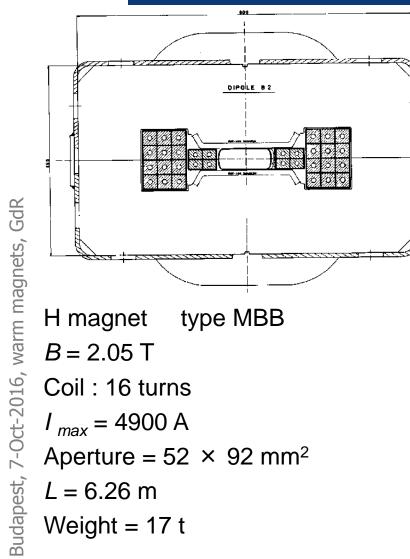








# dipole magnet : SPS dipole

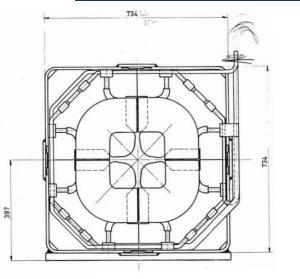




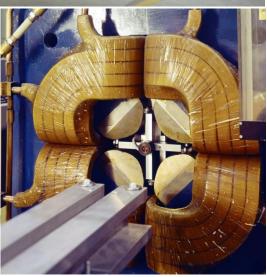




## **Quadrupole magnet : SPS quadrupole**







type MQ G = 20.7 T/mCoil : 16 turns  $I_{max} = 1938 \text{ A}$ Aperture inscribed radius = 44 mm  $L_{coil} = 3.2 \text{ m}$ Weight = 8.4 t



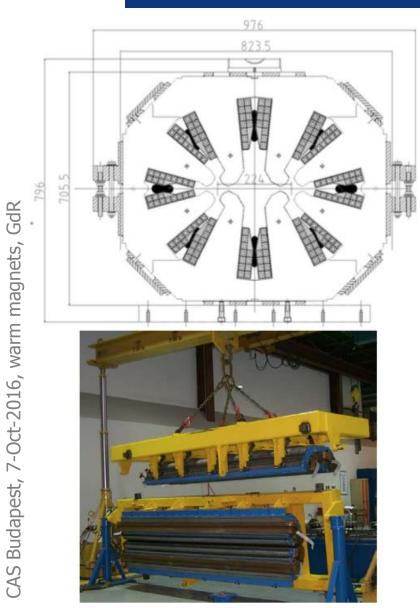
# **MBW LHC warm separation dipole (1)**

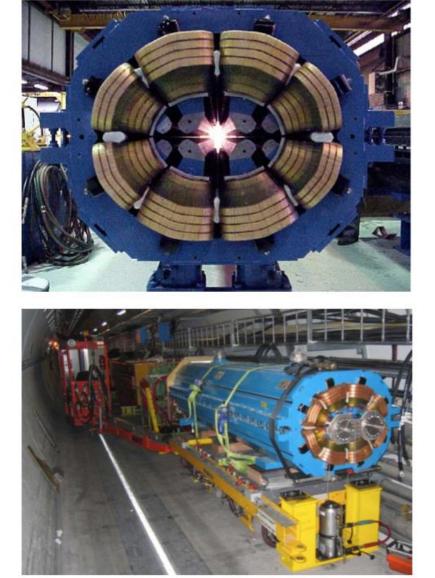
	1080	Parameter	Value
ŝ	Competition and a second as a	Aperture	52 mm
	:224	Nominal field	1.42 T
		Magnetic length	3.4 m
		Weight	18 t
		Water flow	19 l/min
		Power	29 kW
	2.17 - 2.284 1.88 - 2.17 1.81 - 1.89 1.84 - 1.78 1.82 - 1.44 1.82 - 1.74 1.82 - 1.41 1.78 - 1.23 1.78 - 1.43 1.78 - 1.44 1.78 - 1.44 1.79		

CAS Budapest, 7-Oct-2016, warm magnets, GdR



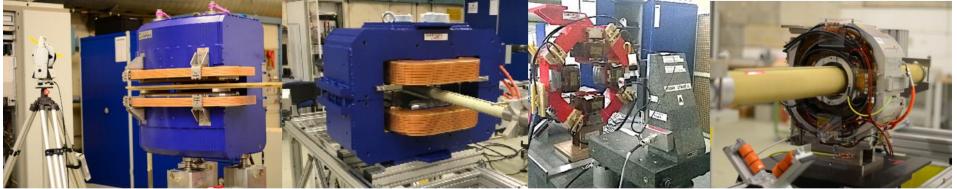
## MQW: LHC warm double aperture quadrupole







## Elena, anti proton decelerator



CAS Budapest, 7-Oct-2016, warm

Ring dipoles 8/8

TL dipoles 3/3

Skew quads 3/3

HV correctors 3/14



## Soleil, synchrotron light-source





Courtesy A. Dael, CEA



## Literature on warm accelerator magnets

- Books
  - G.E.Fisher, "Iron Dominated Magnets" AIP Conf. Proc., 1987 -- Volume 153, pp. 1120-1227
  - J. Tanabe, "Iron Dominated Electromagnets", World Scientific, ISBN 978-981-256-381-1, May 2005
  - P. Campbell, Permanent Magnet Materials and their Application, ISBN-13: 978-0521566889
  - S. Russenschuck, Field computation for accelerator magnets : analytical and numerical methods for electromagnetic design and optimization / Weinheim : Wiley, 2010. - 757 p.
  - Schools
    - CAS Bruges, 2009, specialized course on magnets, 2009, CERN-2010-004
    - CAS Frascati 2008, Magnets (Warm) by D. Einfeld
    - CAS Varna 2010, Magnets (Warm) by D. Tommasini
  - Papers and reports
    - D. Tommasini, "Practical definitions and formulae for magnets," CERN,Tech. Rep. EDMS 1162401, 2011



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