



# Light Sources based on Storage Rings

Lenny Rivkin

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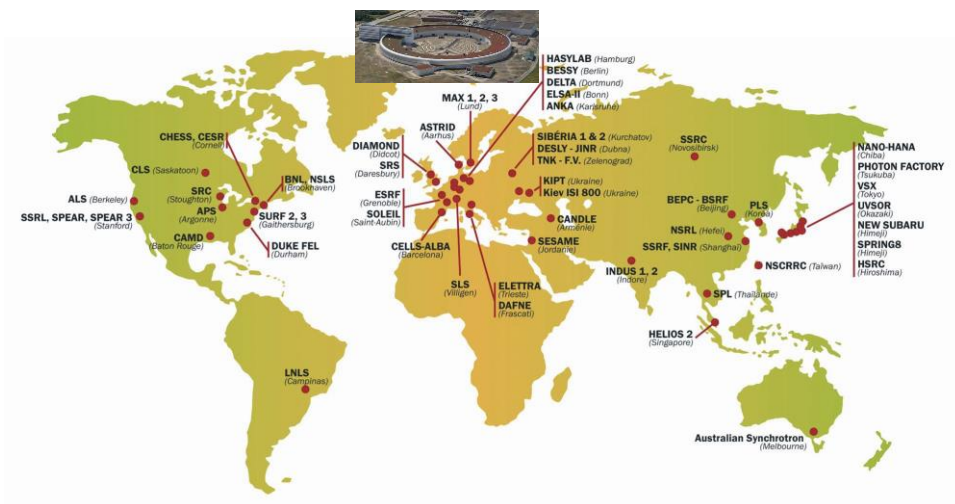
*and*

*Swiss Federal Institute of Technology Lausanne (EPFL)*

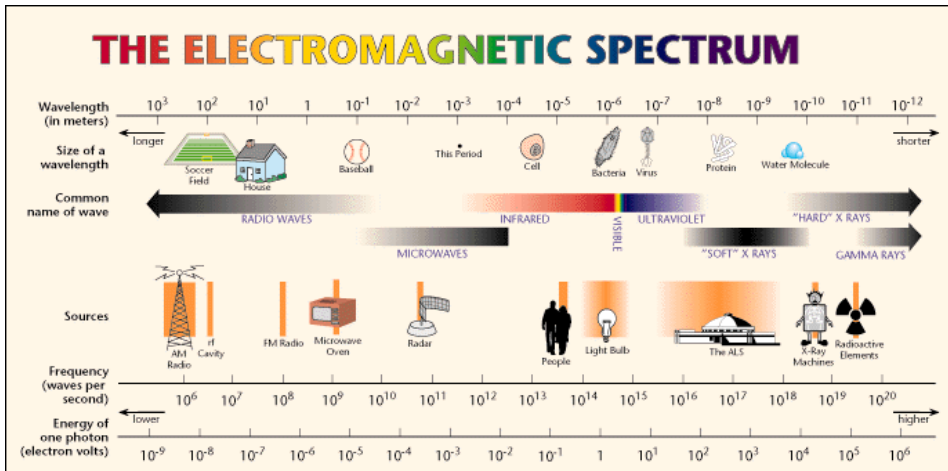
 Electron Beam Dynamics, L. Rivkin, Introduction to Accelerator Physics, Budapest 

Light sources: > 50 producing synchrotron light

60'000 users world-wide



 Electron Beam Dynamics, L. Rivkin, Introduction to Accelerator Physics, Budapest 



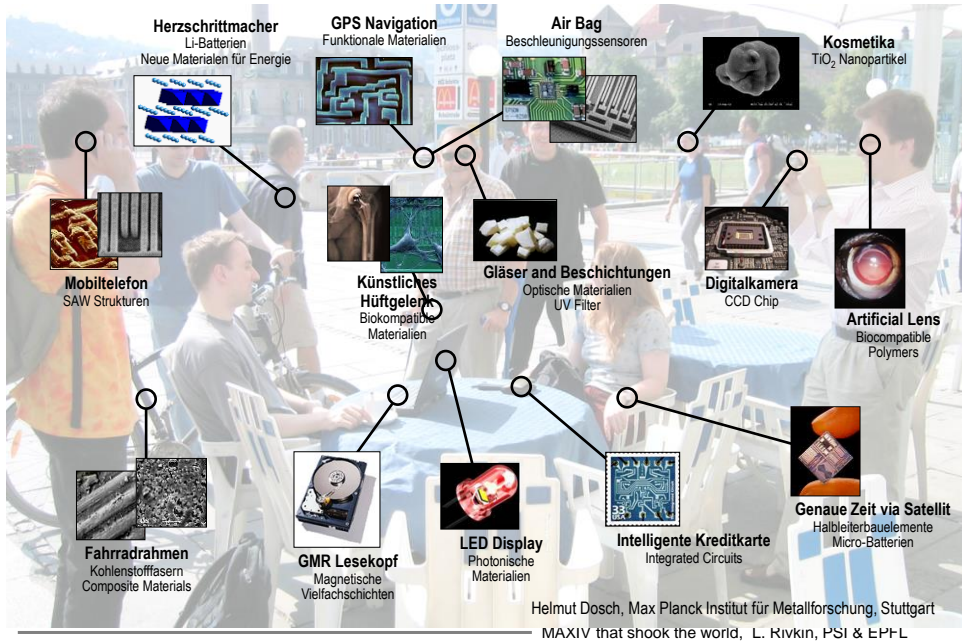
**Wavelength continuously tunable !**

## Materials – key to our technologies

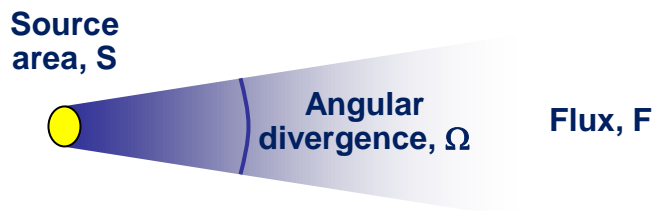


MAXIV that shook the world, L. Rivkin, PSI & EPFL

# Materials – key to our technologies



## The "brightness" of a light source:



$$\text{Brightness} = \text{constant} \times \frac{F}{S \times \Omega}$$

# Steep rise in brightness

**XFEL**

the second wave

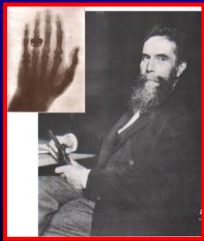
SLS  
SOLEIL (F)  
DIAMOND (UK)

ESRF

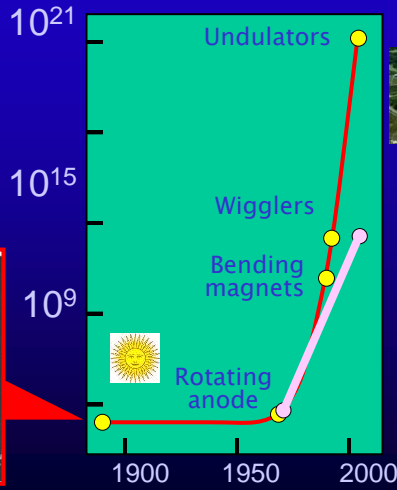
Spring8

APS

Moore's Law for semiconductors

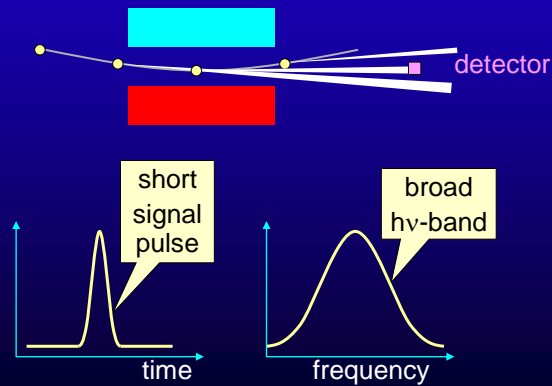


Bertha Roentgen's hand (exposure: 20 min)



## 3 types of storage ring sources:

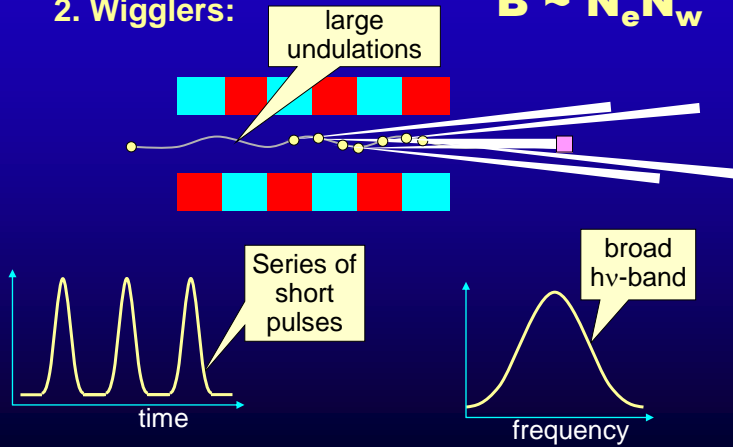
1. Bending magnets:  $B \sim N_e$



### 3 types of storage ring sources:

#### 2. Wigglers:

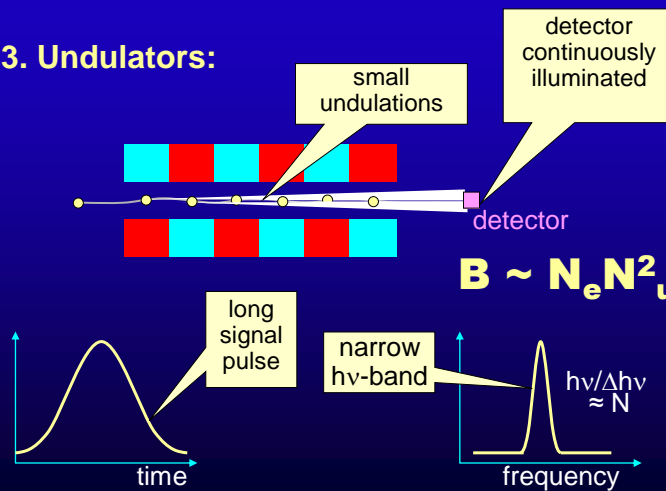
$$B \sim N_e N_w \times 10$$



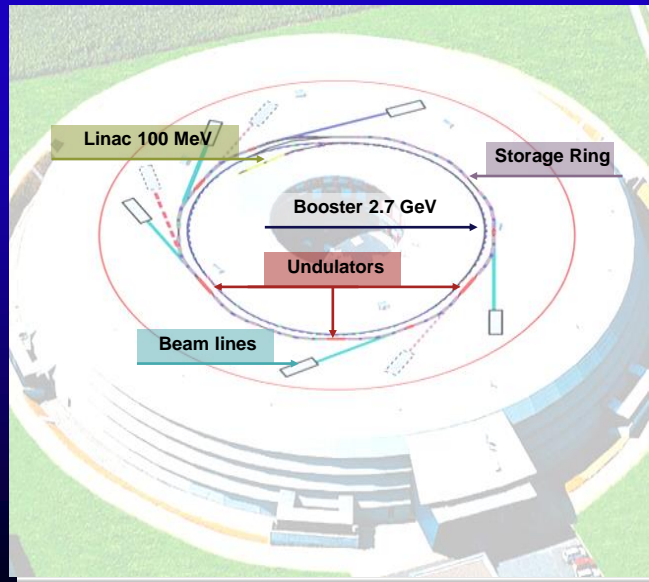
### 3 types of storage ring sources:

#### 3. Undulators:

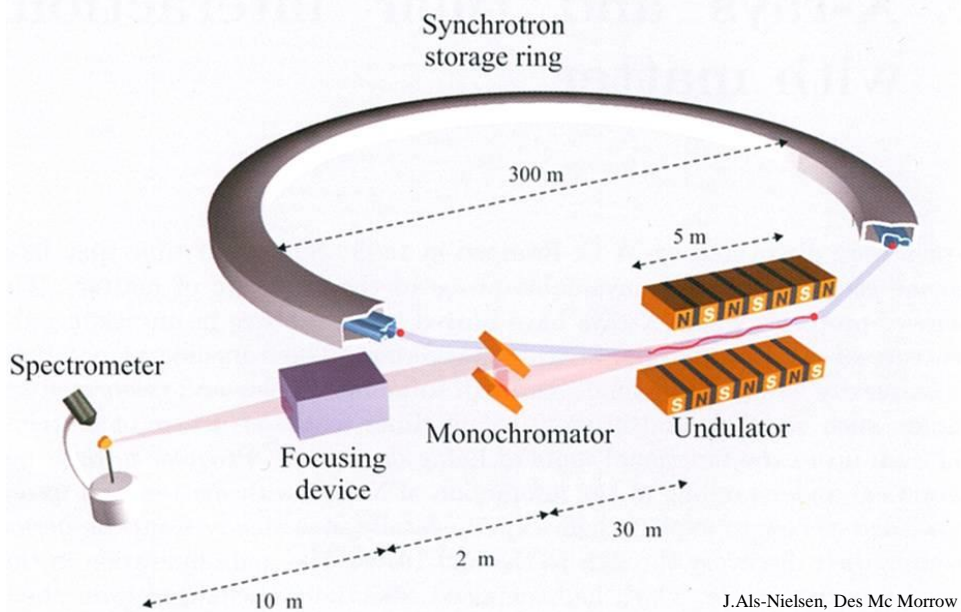
$$B \sim N_e N_u^2 \times 10^3$$



# Anatomy of a light source



## Undulator based beamline



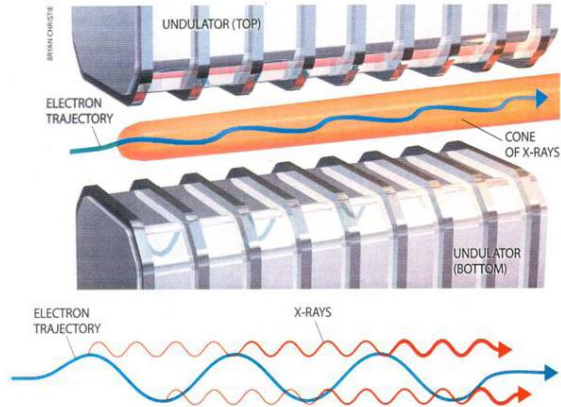
# Bright beams of particles: phase space density

Incoherent, spontaneous emission of light:



Large phase space

Coherent, stimulated emission of light

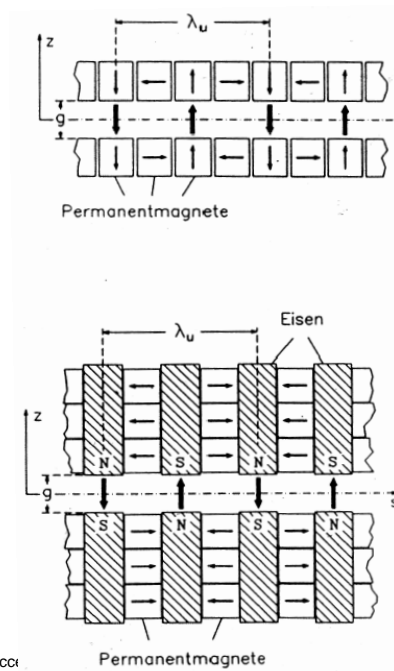


## Permanent magnet undulators

Permanent magnet materials:  $\text{SmCo}_5$ ,  $\text{NdFeB}$

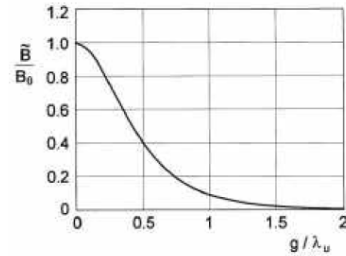
e.g. a pencil made of such material corresponds to 15'000 A-turns!

Hybrid undulator:  
permanent magnets and iron



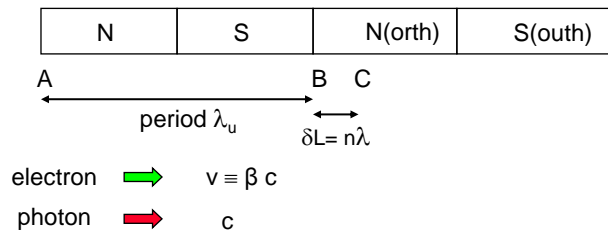
## Field tuning with gap

$$B \approx 1.8 \cdot B_r \cdot e^{-\pi \cdot \frac{gap}{\lambda_u}}$$



Permanent magnet material	Remanent field [T]
SmCo <sub>5</sub>	0.9 – 1.0
Sm <sub>2</sub> Co <sub>17</sub>	1.0 – 1.1
NdFeB	1.0 – 1.4

## Selection of wavelength in an undulator II



The path difference

$$\delta L \equiv n\lambda \approx (1 - \beta) \lambda_u, \quad 1 - \beta \approx \frac{1}{2\gamma^2}$$

$$\lambda = \frac{\lambda_u}{2n\gamma^2} \left( 1 + \frac{K^2}{2} \right)$$

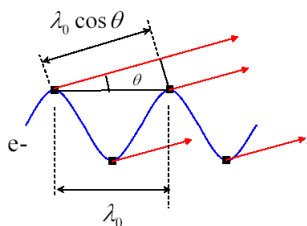
detour through slalom



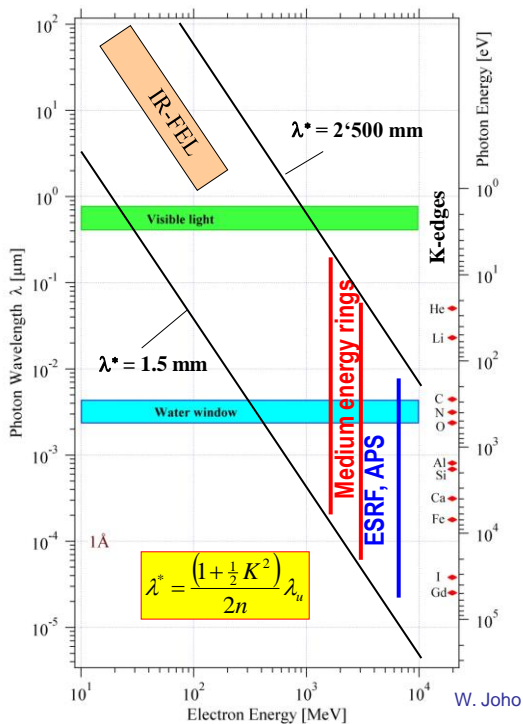
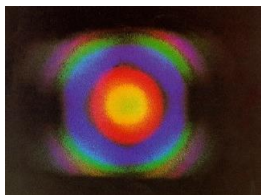
$$K = 0.0934 \cdot \lambda_u [\text{mm}] \cdot B [\text{T}]$$



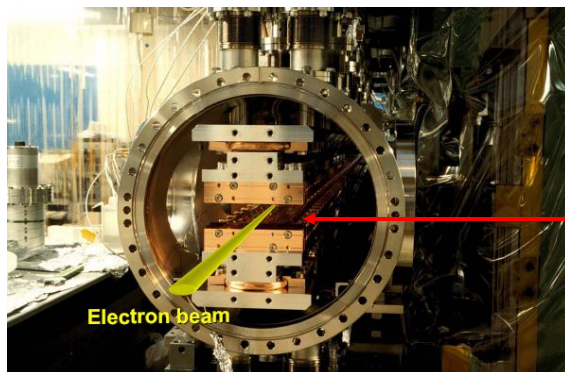
# Undulator radiation



$$\lambda = \frac{\lambda_u}{2n\gamma^2} \left( 1 + \frac{K^2}{2} + \gamma^2\theta^2 \right)$$

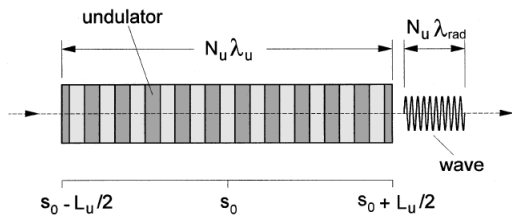


## In-vacuum undulators / s.c. undulators



Gaps  
down  
to  
3 mm

# Undulator line width



Undulator of infinite length

$$N_u = \infty \Rightarrow \frac{\Delta\lambda}{\lambda} = 0$$

Finite length undulator

- radiation pulse has as many periods as the undulator
- the line width is

$$\frac{\Delta\lambda}{\lambda} \sim \frac{1}{N_u}$$

Due to the electron energy spread

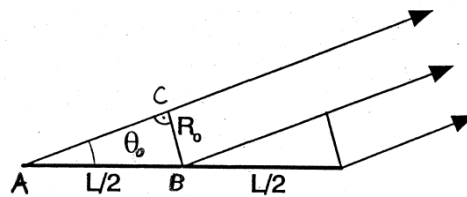
$$\frac{\Delta\lambda}{\lambda} = 2 \frac{\sigma_E}{E}$$

## Radiation cone of an undulator

Undulator radiates from the whole length  $L$  into a narrow cone.

Propagation of the wave front  $BC$  is suppressed under an angle  $\theta_0$ ,

if the path length  $AC$  is just shorter by a half wavelength compared to  $AB$  (negative interference). This defines the central cone.



$$\Delta L = AB - AC = \frac{1}{2} L (1 - \cos \theta_0) \approx \frac{1}{4} L \theta_0^2$$

Negative interference for  $\Delta L = \frac{\lambda}{2}$

$$\theta_0 = \sqrt{\frac{2\lambda}{L}}$$

$$R_0 = \sqrt{\frac{\lambda \cdot L}{2}}$$

$$\varepsilon_0 = \theta_0 R_0 = \lambda$$

W. Joho

## WHAT DO USERS EXPECT FROM A HIGH PERFORMANCE LIGHT SOURCE ?

- PROPER PHOTON ENERGY FOR THEIR EXPERIMENTS
- BRILLIANCE →
- STABILITY

$$B = \frac{\Phi}{(2\pi)^2 \Sigma_x \Sigma_{x'} \Sigma_y \Sigma_{y'}}$$

**FIGURE OF MERIT**

$$\Sigma^2 = \sigma_e^2 + \sigma_\gamma^2$$

$$\Sigma_x \Sigma_{x'} \approx \sigma_x \sigma_{x'} \sim \epsilon_x$$

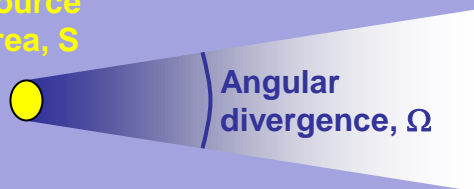
Photon beam size (U):

$$\sigma_{x'} = \sqrt{\frac{\lambda}{L}}$$

$$\sigma_\gamma = \frac{\sqrt{\lambda L}}{4\pi}$$

The electron beam "emittance":

Source area, S

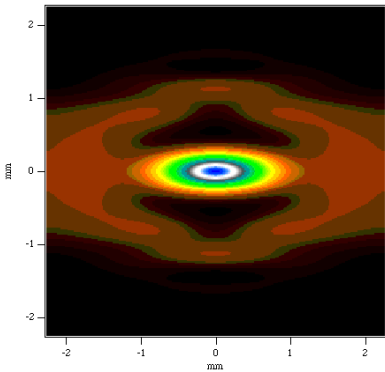
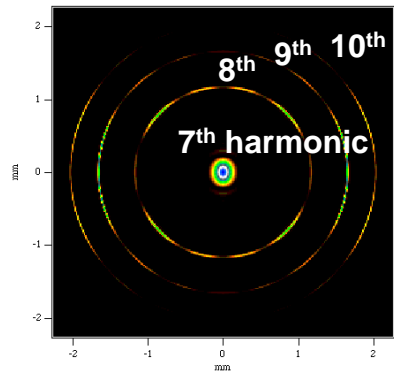


Angular divergence,  $\Omega$

The brightness depends on the geometry of the source, i.e., on the electron beam emittance

$$\text{Emittance} = S \times \Omega$$

Undulator radiation from 6 GeV beam with zero emittance, energy spread (example ESRF)



Emittance 4 nm·rad, 1% coupling, finite energy spread

## Electron beam phase space

Emittance Units of  $\epsilon$  [m·rad]

Transverse electron beam distribution

- Gaussian
- “Typical” particle: 1 -  $\sigma$  ellipse (in a place where  $\alpha = \beta' = 0$ )

$$\sigma_x = \sqrt{\epsilon \beta}$$

$$\sigma_{x'} = \sqrt{\epsilon / \beta}$$

$$\epsilon = \sigma_x \cdot \sigma_{x'}$$

$$\beta = \frac{\sigma_x}{\sigma_{x'}}$$

Area =  $\pi \cdot \epsilon$

## Radiation effects in electron storage rings

Average radiated power restored by RF

- Electron loses energy each turn to synchrotron radiation
- RF cavities accelerate electrons back to the nominal energy

Radiation damping

- Average rate of energy loss produces **DAMPING** of electron oscillations in all three degrees of freedom (if properly arranged!)

Quantum fluctuations

- Statistical fluctuations in energy loss (from quantized emission of radiation) produce **RANDOM EXCITATION** of these oscillations

**Equilibrium** distributions

- The balance between the damping and the excitation of the electron oscillations determines the equilibrium distribution of particles in the beam

## Small emittance lattices

Equilibrium horizontal emittance

$$\epsilon_{x0} \equiv \frac{\sigma_{x\beta}^2}{\beta} = \frac{C_q E^2}{J_x} \cdot \frac{\langle \mathcal{H} \rangle_{mag}}{\rho}$$

- one tries to optimize the  $\mathcal{H}$  function in **bending magnets**

$$\mathcal{H} = \gamma D^2 + 2\alpha D D' + \beta D'^2$$

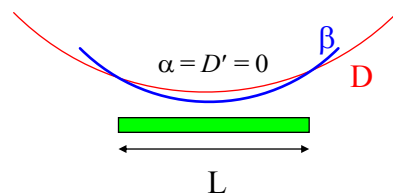
- the equilibrium emittance can be written as:

$$\epsilon_{x0} = \frac{C_q E^2}{J_x} \cdot \theta^3 \cdot F_{latt}$$

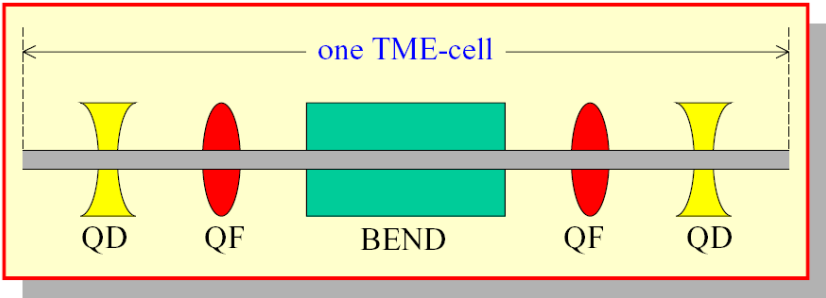
$$F_{min} = \frac{1}{12\sqrt{15}}$$

there exists a minimum

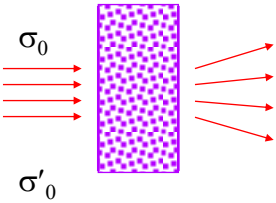
$$\beta^* = \frac{L}{2\sqrt{15}}, \quad D^* = \frac{L\theta}{24}$$



# Theoretical minimum emittance

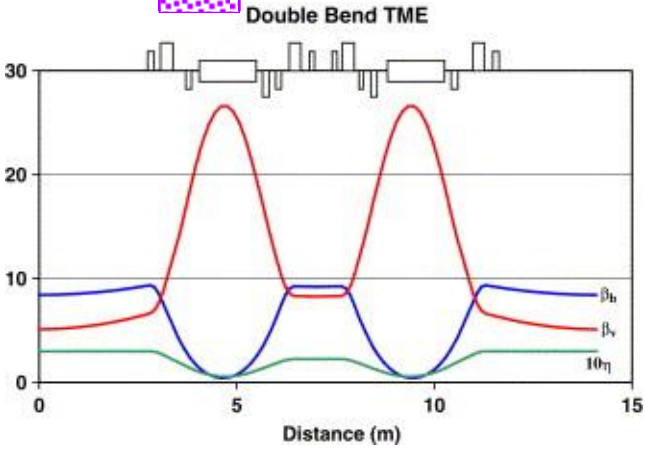


## Minimum emittance lattices



$$\epsilon_{x0} = \frac{C_q E^2}{J_x} \cdot \theta^3 \cdot F_{latt}$$

$$F_{min} = \frac{1}{12\sqrt{15}}$$

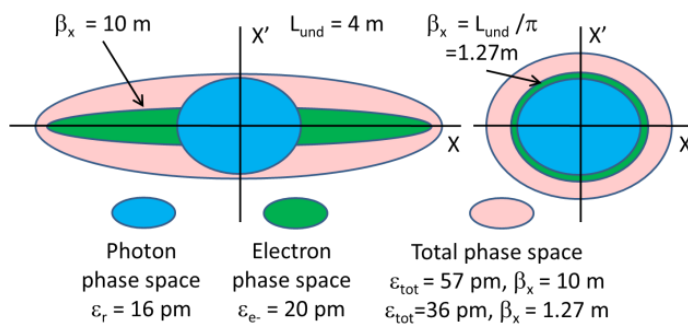


Tight focus in the middle of the bending magnets – need space!

Many bending magnets – need space!

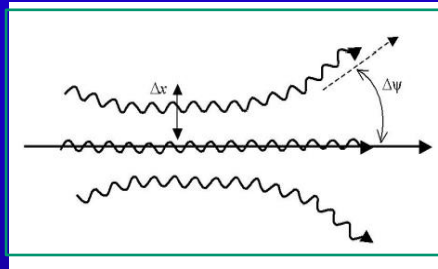
**X-ray emittance from electron source:  
a convolution of electron and photon phase space**

$$\text{Brightness} = \frac{\Phi}{(2\pi)^2 \Sigma_x \Sigma_{x'} \Sigma_y \Sigma_{y'}} \quad \Sigma^2 = \sigma_e^2 + \sigma_\gamma^2$$

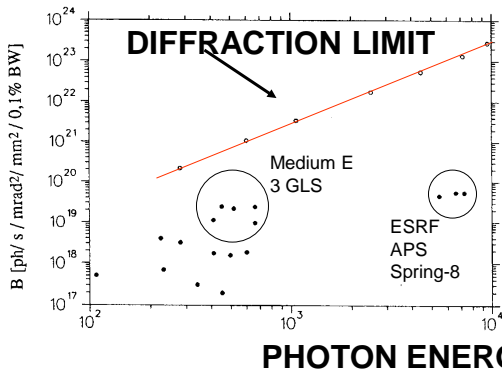


R. Hettel

# HITTING THE DIFFRACTION LIMIT

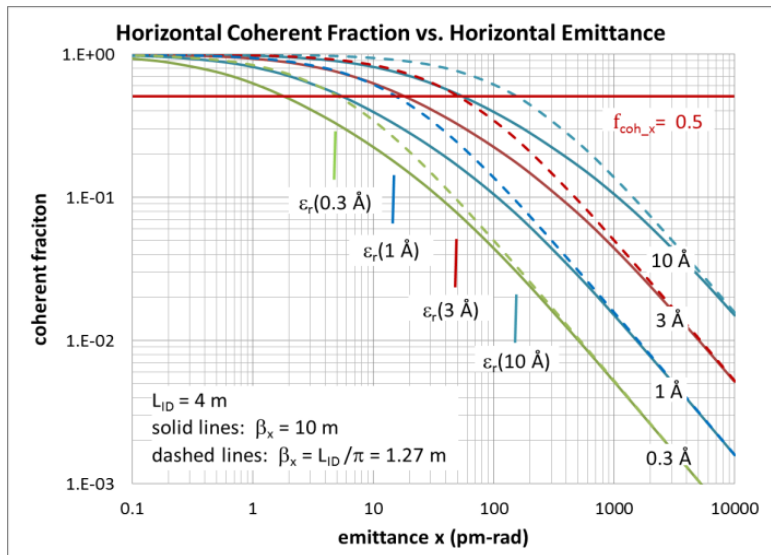


**BRIGHTNESS:**



Light of wavelength  $\lambda$   
 focused to spot size  $\Delta x$   
 will diffract with angle  $\Delta \psi = \sim \lambda / \Delta x$

## Coherence fraction

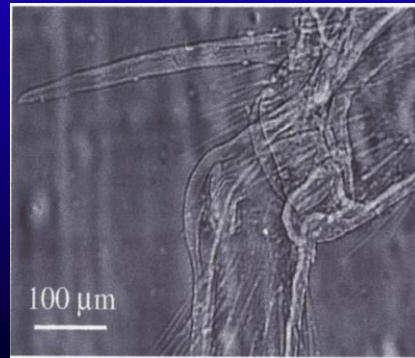




# Transverse coherence

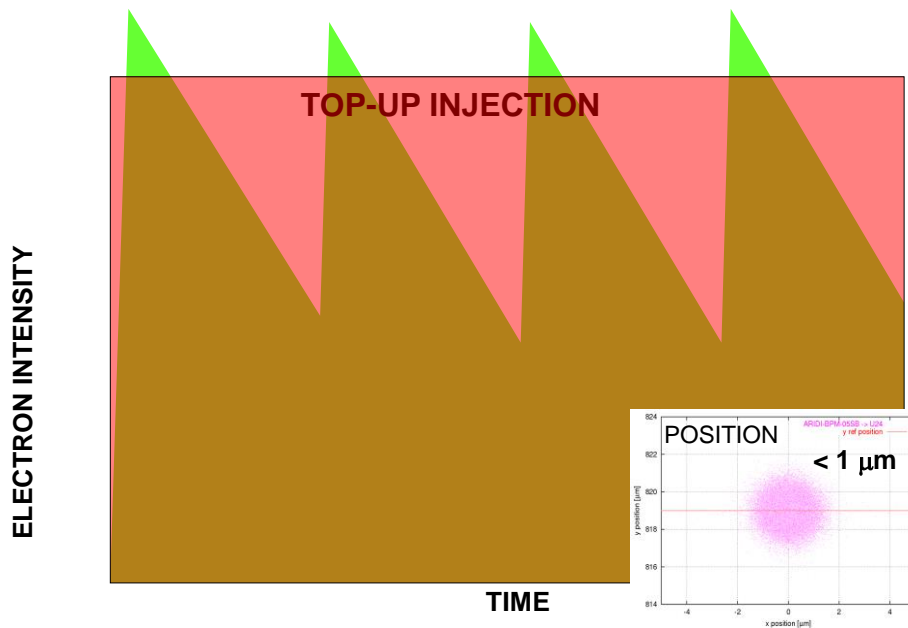
- High brightness gives coherence
- Wave optics methods for X-rays (all chapters in Born & Wolf)
- Holography

The knee of a spider



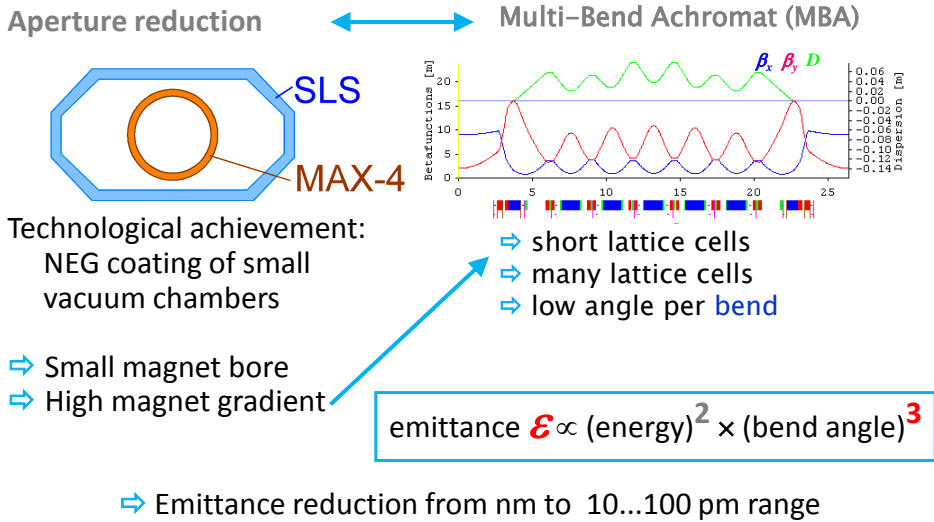
phase contrast imaging

## Top-up injection: key to stability



# A revolution in storage ring technology

Pioneer work: MAX IV (Lund, Sweden)

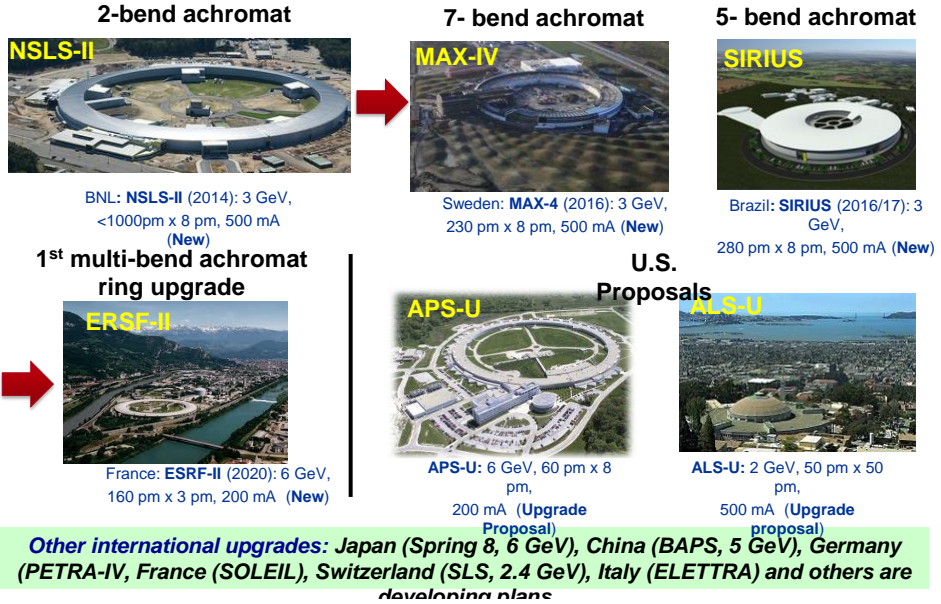


## The MAX IV Laboratory in Lund, Sweden

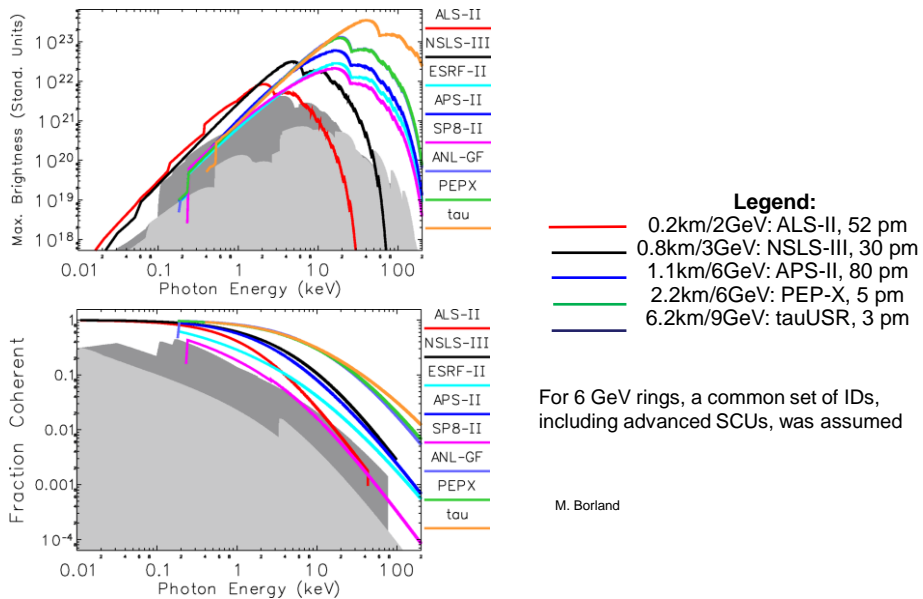


MAXIV that shook the world, L. Rivkin, PSI & EPFL

## The world is moving to ever brighter ring sources



## Brightness and coherence of 3<sup>rd</sup> and 4<sup>th</sup> gen rings



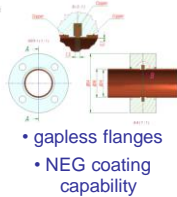
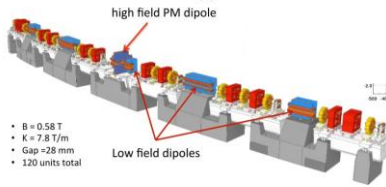
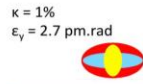
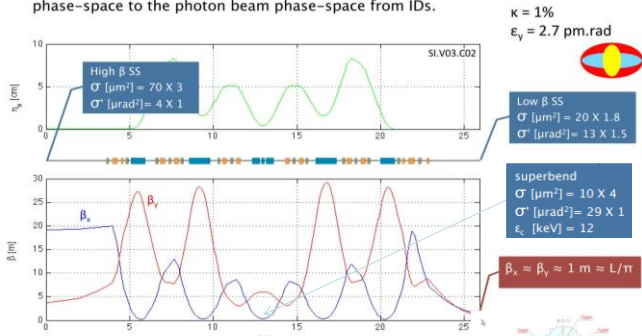
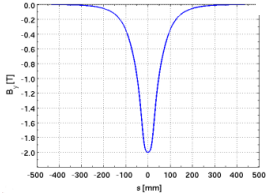
# Sirius: 5 Bend Achromat

$\epsilon_{x/y} = 190\text{-}270/3 \text{ pm}\cdot\text{rad} @ 3 \text{ GeV}, 350 \text{ mA}, C = 518$

- New optics with lower  $\beta$  at the 6 m straight sections to match the electron beam phase-space to the photon beam phase-space from IDs.

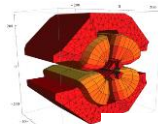


- PM Superbend
- B = 2 T
- Gap = 28 mm
- Field flexibility = 6% (using lateral control gap)
- 20 units total



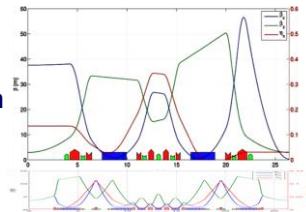
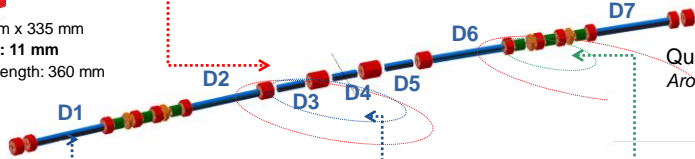
# ESRF-II – hybrid 7BA

6 GeV, 844 m, 4 nm  $\rightarrow$  0.15 nm



High gradient quadrupoles  
85 T/m

- Spec: 100 T/m x 335 mm
- Bore radius: 11 mm
- Mechanical length: 360 mm
- 1 kW

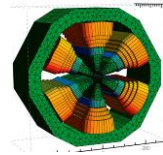
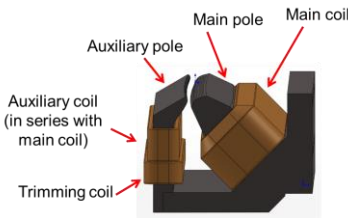


Quadrupole  
Around 50 T/m

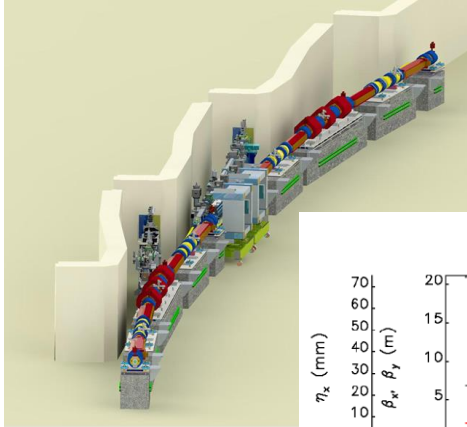
Sextupoles  
1700 T/m<sup>2</sup>

Combined dipole quadrupoles  
0.85 T / 45 T/m & 0.34 T / 50 T/m

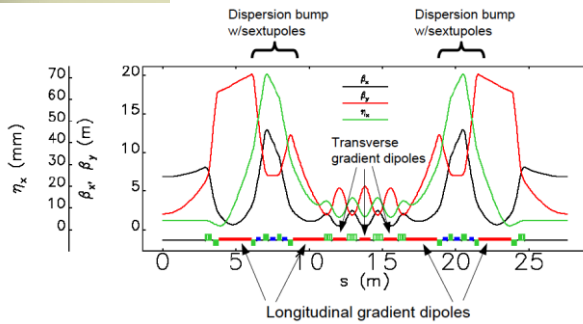
Permanent magnet dipoles  
longitudinal gradient 0.16 – 0.6 T,  
magnetic gap 22 mm  
2 metre long, 5 modules  
With a small tuning coil 1%



## APS-U – hybrid 7BA



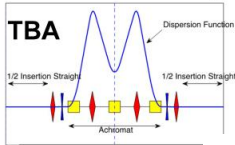
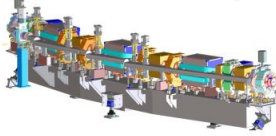
- $\epsilon_{x/y} = 67/8 \text{ pm}\cdot\text{rad}$  @ 6 GeV, 200 mA
- C = 1.1 km
- 41-pm.rad option using reverse bend lattice



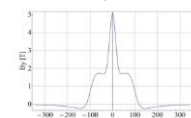
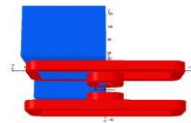
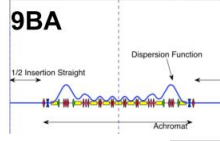
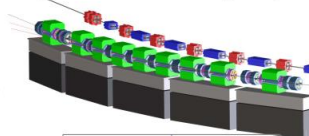
## ALS-U – hybrid 9 Bend Achromat

$\epsilon_{x/y} = 50/50 \text{ pm}\cdot\text{rad}$  @ 2 GeV, 500 mA

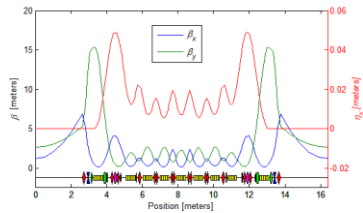
ALS today  
triple-bend achromat (TBA)



ALS-U  
multi-bend achromat (9BA)



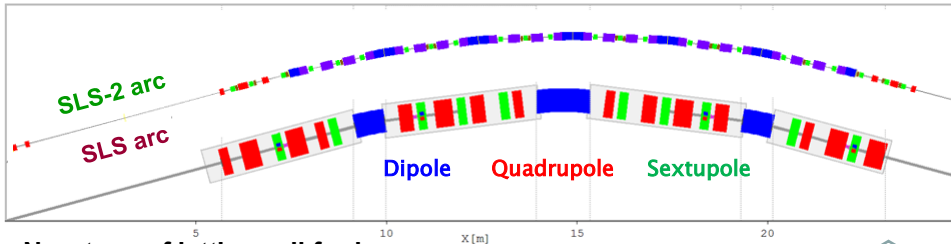
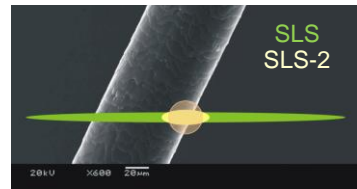
superbend option



includes  
octupoles

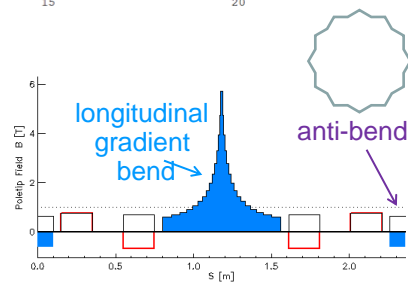
## SLS 2.0 upgrade plans

$$\epsilon_x = 140 \text{ pm.rad @ 2.4 GeV}$$

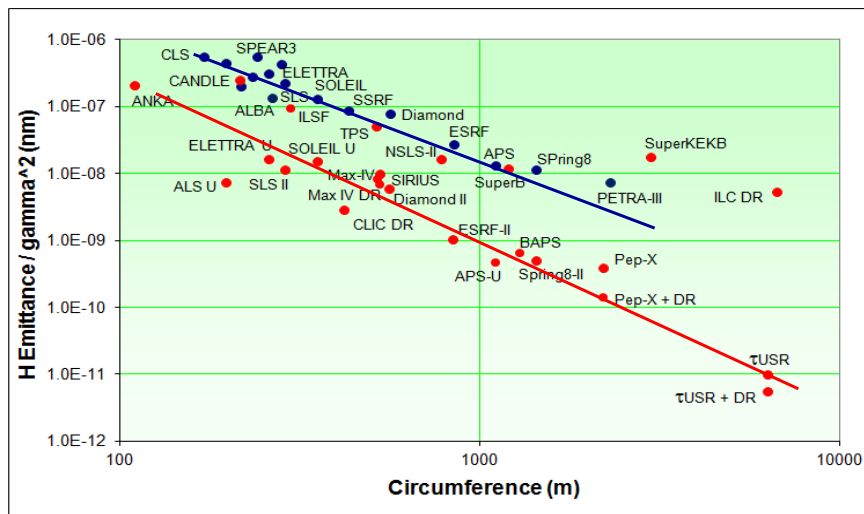


### New type of lattice cell for low emittance

- bending magnets with longitudinal field variation (2 T peak)
- options for 5-6 T peak field superbends
- anti-bends for beam dynamics  
⇒ star-shaped lattice



## Diffraction limited rings: the new wave

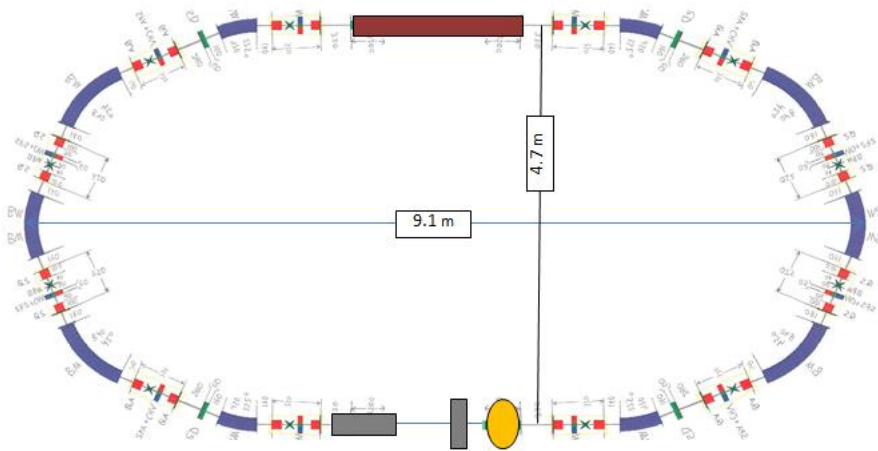




Storage rings in operation (•) and planned (•).  
The old (—) and the new (—) generation.

R. Bartolini

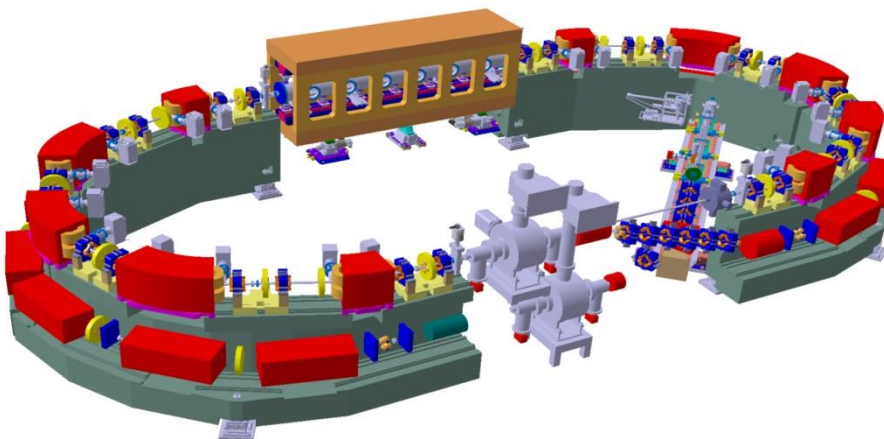
# Compact light source COSAMI

Conventional, normal conducting magnetic structure



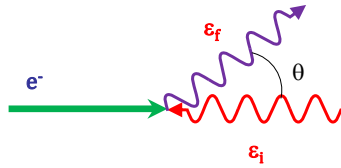
 Electron Beam Dynamics, L. Rivkin, Introduction to Accelerator Physics, Budapest 

## Injector and storage ring integration



# When an electron collides with a photon...

Also known as **Compton** or Thomson scattering

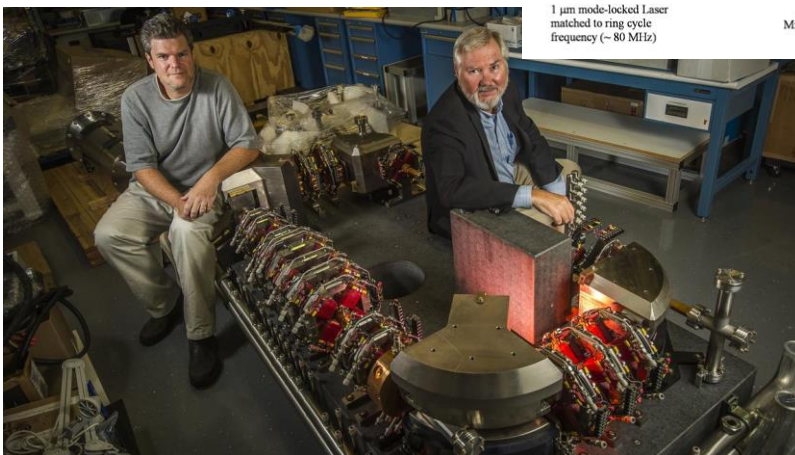
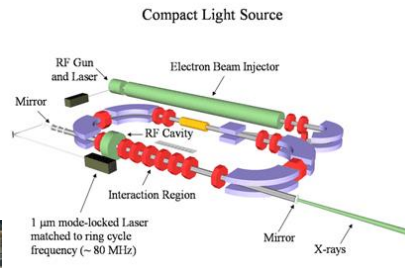


$$\epsilon_f = \frac{4\gamma^2 \epsilon_i}{1 + \gamma^2 \theta^2}$$

- backscattered photon has the maximum energy
- at an angle of  $1/\gamma$  the energy drops by a factor of 2
- undulator's periodic magnetic field could be viewed as a «photon», with useful parallels between the two cases

EPFL — Electron Beam Dynamics, L. Rivkin, Introduction to Accelerator Physics, Budapest — PSI

## Compact light source based on Compton scattering



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