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Theoretical Progress in Heavy-Ion Collisions

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See the previous talk by David d'Enterria.

Contents:

1. Introduction.

2. Initial conditions:

2.1. Nuclear wave function.

2.2. Factorization.

3. Collective behavior:

3.1. Elliptic flow.

3.2. Hydrodynamical modeling.

3.3. Strong coupling calculations.

4. Hard probes: high- p_T particles and jets:

4.1. Successes and problems in radiative energy loss.

4.2. In-medium parton showers.

5. Summary.

Accelerator	Collisions
SPS	pp to PbPb at $E_{\text{cm}}=17\text{-}30\text{ AGeV}$
RHIC	pp to AuAu at $E_{\text{cm}}=20\text{-}200\text{ AGeV}$
LHC	pp to PbPb at $E_{\text{cm}}=5.5\text{-}14\text{ ATeV}$

Not a full review, see e.g. the contributions to QGP4 in arXiv '09.

Introduction (I):

- URHIC is an interdisciplinary field, whose goal is the understanding of confinement through the study of matter at high parton densities \rightarrow through asymptotic freedom \rightarrow QGP.
- Experiments at RHIC claim (NPA757 '05): the creation of partonic matter with $\epsilon > \epsilon_{\text{crit}}$ (HM \rightarrow QGP), with large coherence in soft particle production, very early behaving like a quasi-ideal fluid and extremely opaque to energetic partons traversing it.

Observable at RHIC	Standard interpretation
Low multiplicity compared to pre-RHIC expectations	Strong coherence in particle production
v_2 in agreement with ideal hydro	Almost ideal fluid
Strong jet quenching	Opaque medium

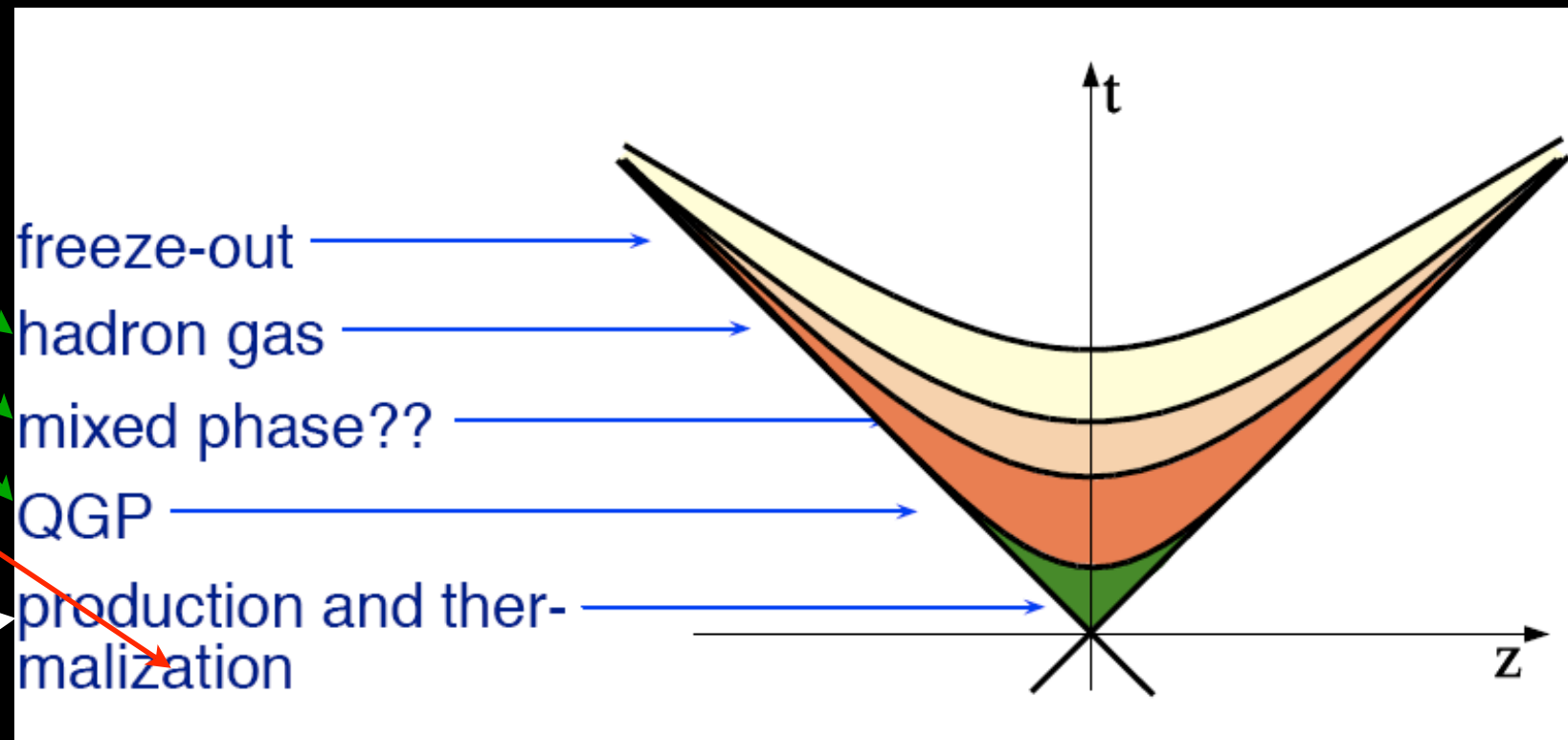
Introduction (II):

- ‘**Medium**’: particles with momenta $\sim \langle p \rangle (T)$.
- **Hard probes**: those pQCD-computable in vacuum, whose medium-modification characterizes it.
- At variance with other fields, here the **space-time evolution** has to be considered: interplay between usual evolution (momentum) variables and dimensions of the ‘medium’.

Hydrodynamics

pQCD or strong
coupling

Nuclear WF,
factorization



2. Initial conditions:

2.1. Nuclear wave function.

2.2. Factorization.

See the talk by Jochen Bartels.

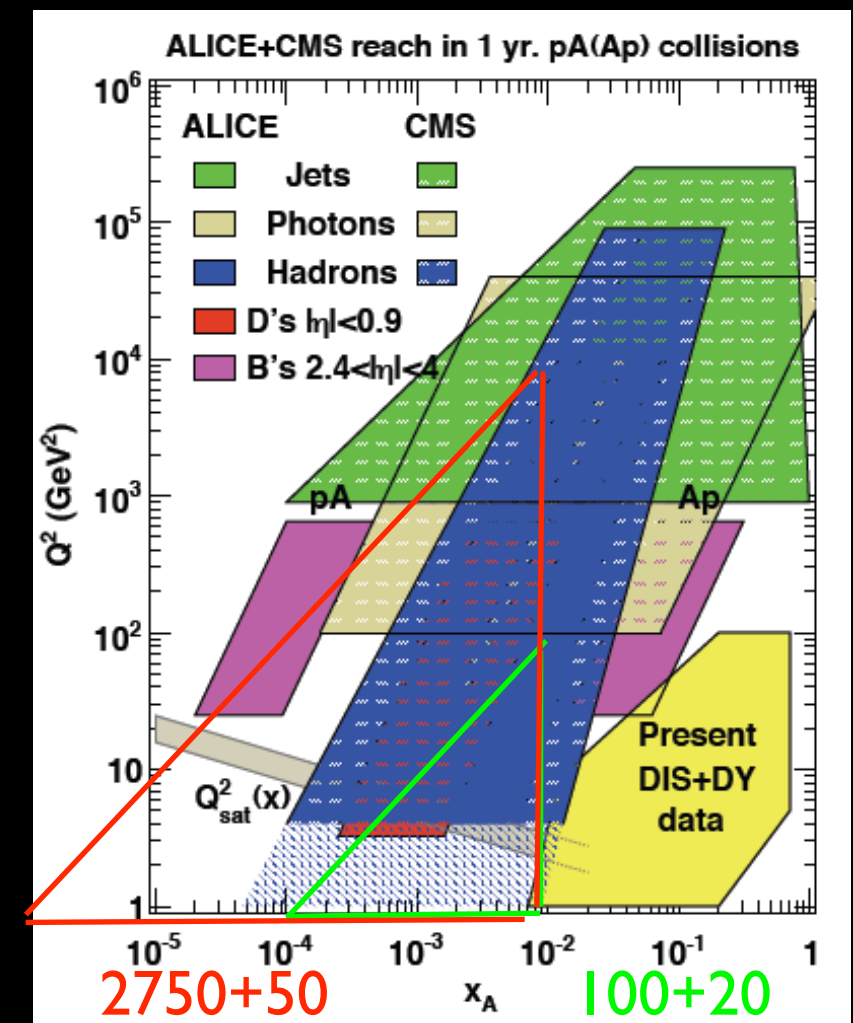
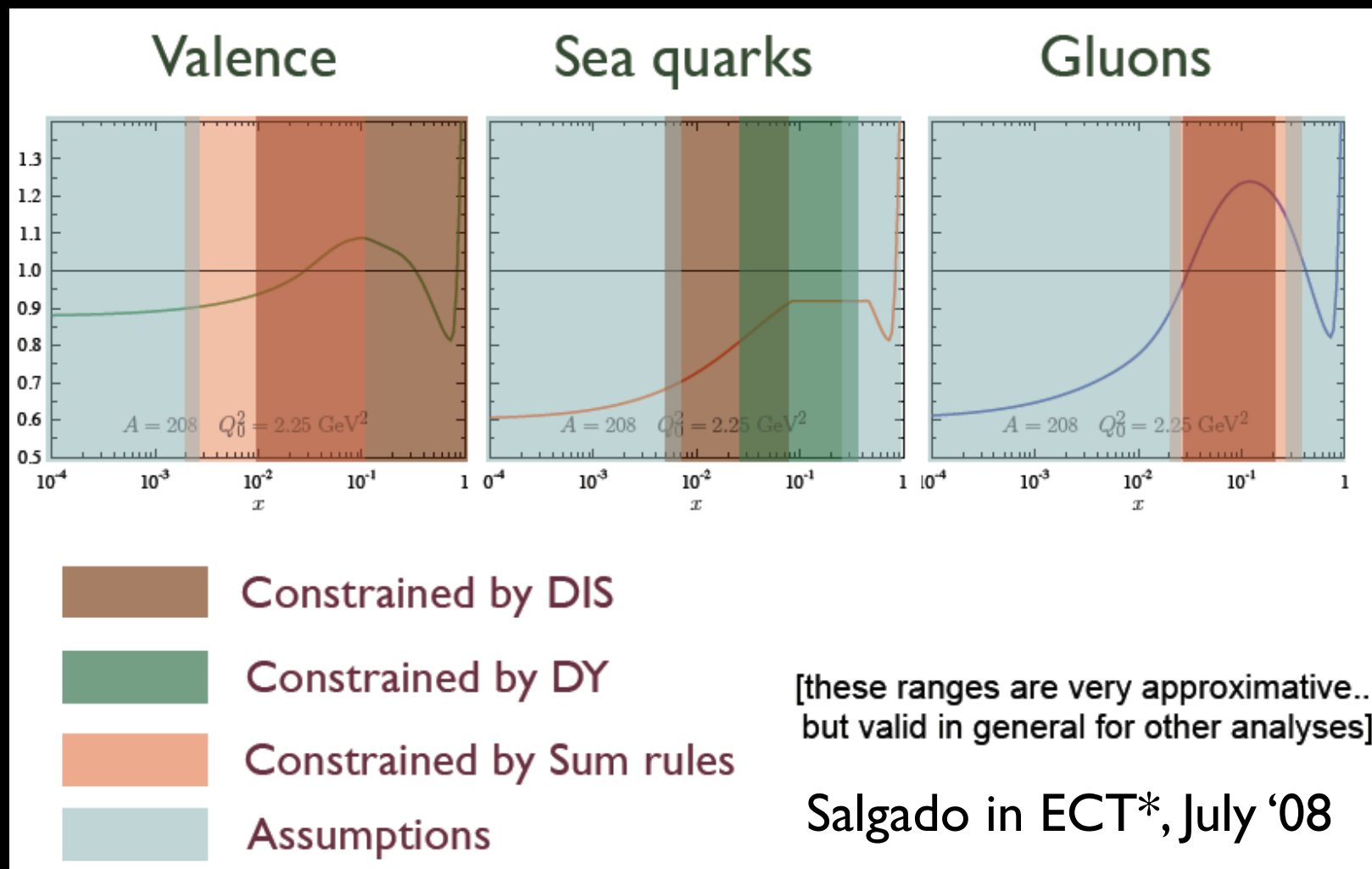
$$R = \frac{\text{Measured (on nuclei)}}{\text{Expected if no nuclear effects}}$$

$$R_{F_2}^A(x, Q^2) = \frac{F_2^A(x, Q^2)}{A F_2^{\text{nucleon}}(x, Q^2)}$$

$$R_{dAu} = \frac{\frac{dN^{dAu}}{d\eta d^2b d^2p}}{N_{coll} \frac{dN^{pp}}{d\eta d^2b d^2p}}$$

Nuclear WF - DGLAP analysis

- **DGLAP** analysis at LO (EPS08) and **NLO** (HKN07,dFS, EPS09) and with **error analysis** through the Hessian method available: HKN, EPS.
- **Limitation**: existing data do not cover the LHC kinematics: pA@LHC and future eA colliders (talks on EIC and LHeC; Lappi).



Nuclear WF - DGLAP analysis

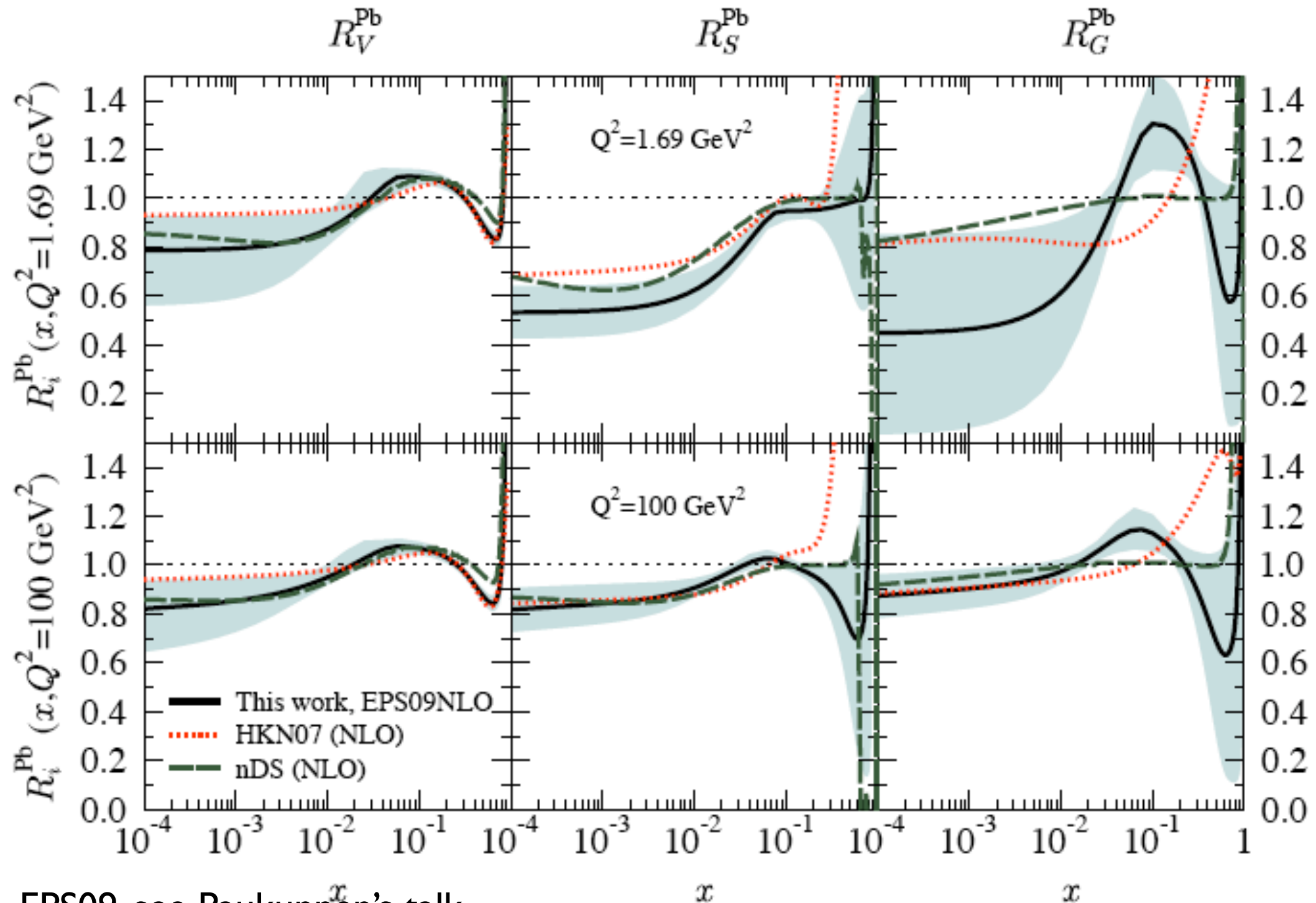
- **DGLAP** analysis at LO (EPS08) and **NLO** (HKN07,dFS, EPS09)

and with **convolution** through the **collinear** method available

HKN

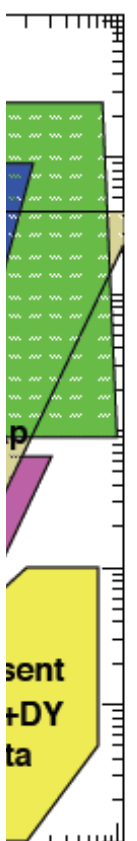
- **Li**

pA@



EPS09, see Paukunen's talk

Collisions



-20

Nuclear WF - models

- For ep, several models including saturation exist: dipole (GBW and descendants), Regge,... **Geometric scaling** is the striking feature (**only** suggestive, DGLAP also leads to it!).

$$x \ll \frac{1}{2m_N R_A} \simeq 0.1 A^{-1/3}$$

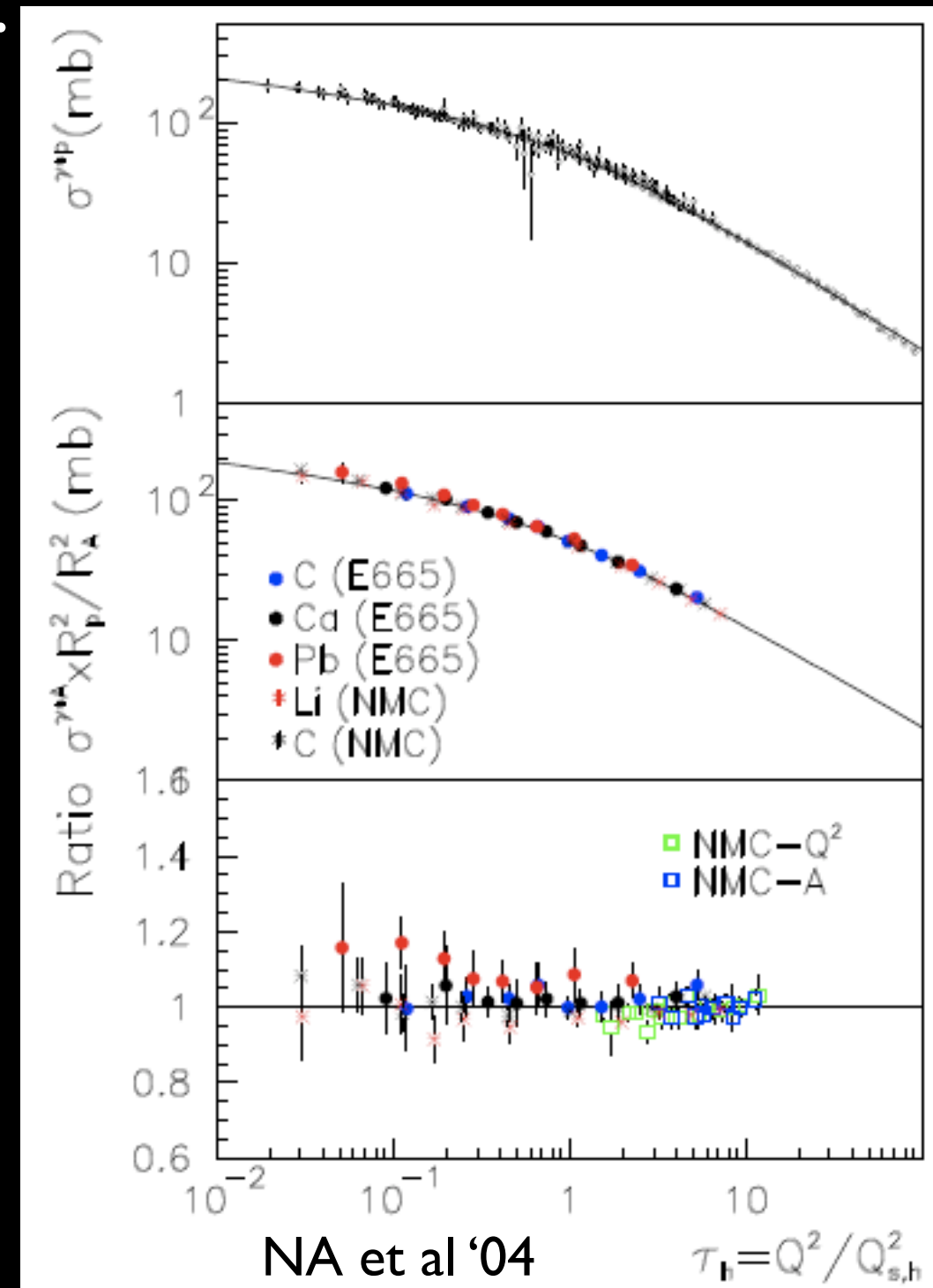
- Geometric scaling also works for nuclei for $x < 0.02$ (Rummukainen et al '03, NA et al '04):

$$\frac{\sigma^{\gamma^* A}(\tau_A)}{\pi R_A^2} = \frac{\sigma^{\gamma^* p}(\tau_A)}{\pi R_p^2}$$

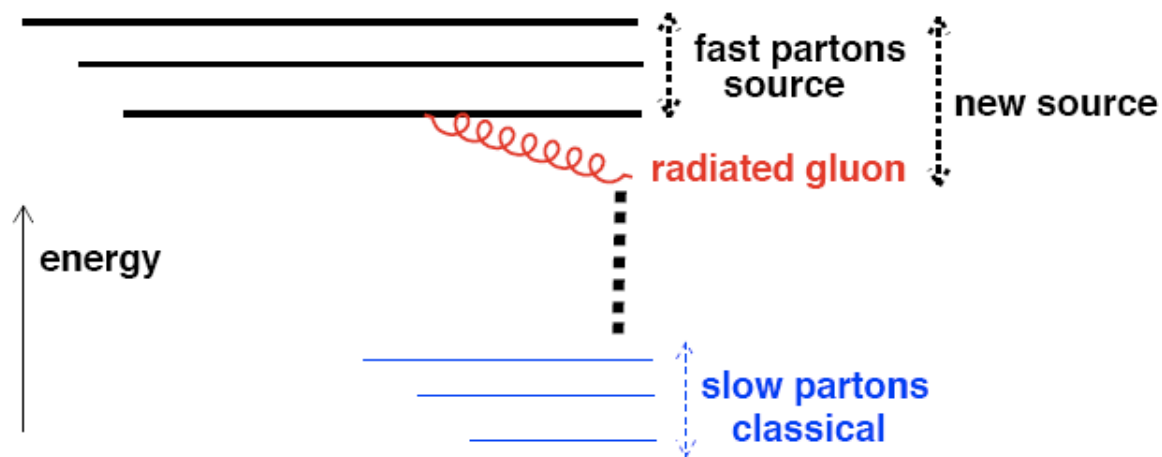
$$\frac{Q_{s,A}^2}{Q_{s,p}^2} = \left(\frac{A \pi R_p^2}{\pi R_A^2} \right)^{\frac{1}{\delta}} \Rightarrow \frac{\tau_A}{\tau_p} = \left(\frac{\pi R_A^2}{A \pi R_p^2} \right)^{\frac{1}{\delta}}$$

$$\delta = 0.79 \pm 0.02 \quad (x < 0.02).$$

$$Q_s^2 \propto x^{-\lambda} A^{\beta}$$



Nuclear WF - theory



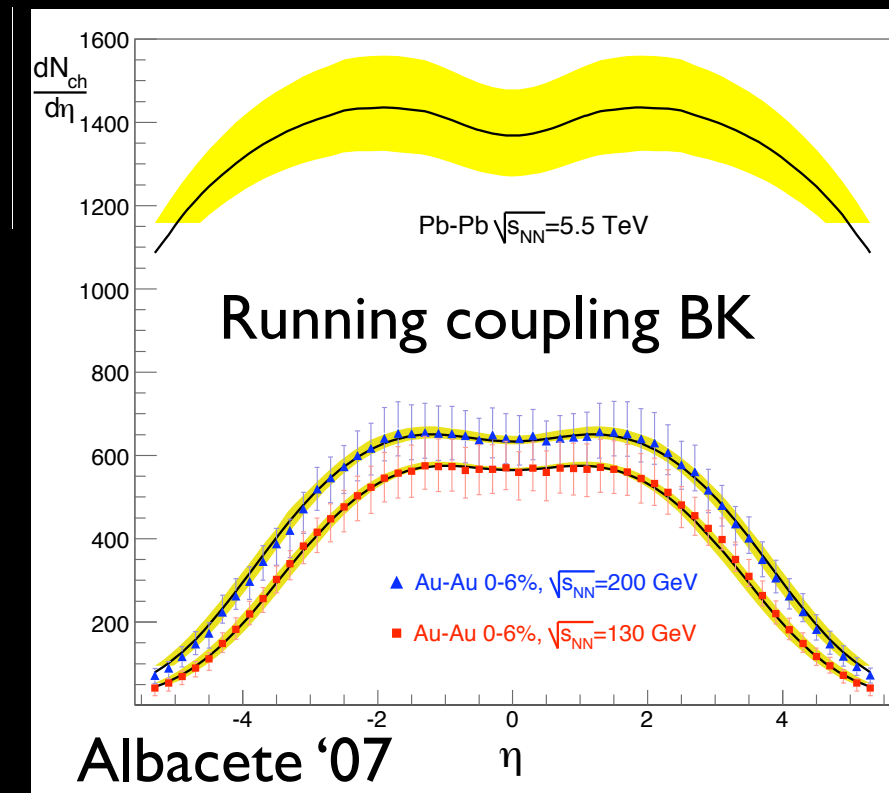
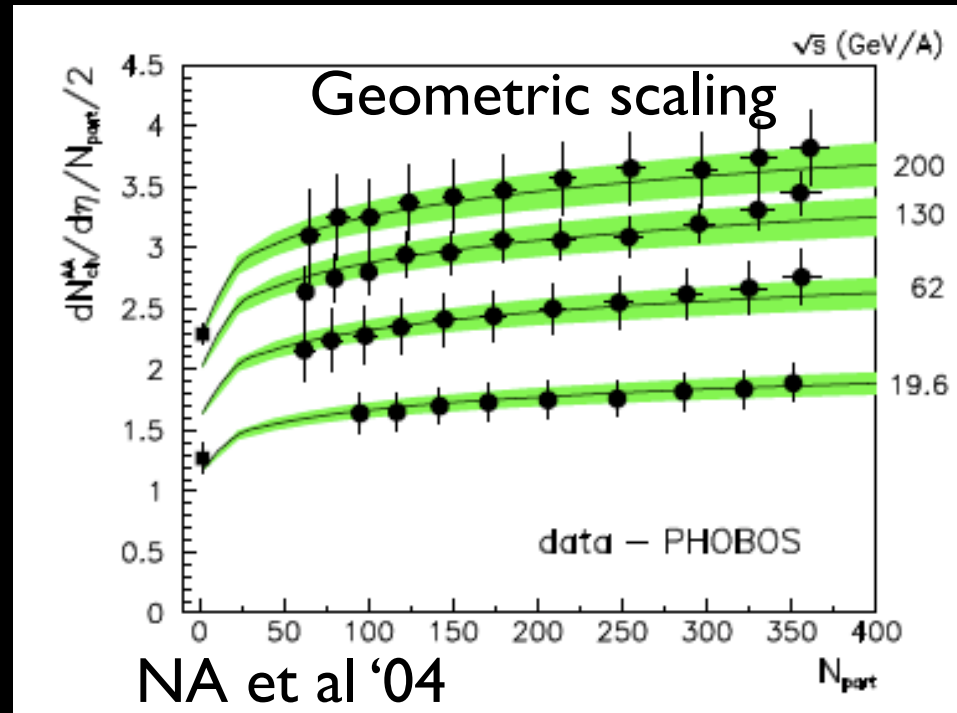
- RG functional equation: **JIMWLK**, $\rho_p \sim O(1)$, $\rho_t \sim O(1/\alpha_s)$, mean field version: **BK**, from LL to NLL (talks: Balitsky, Albacete, Weigert, Avsar).

- **Beyond JIMWLK**: $\rho_p \sim \rho_t \sim O(1/\alpha_s)$ (Kovner; Triantafyllopoulos '05)
 - Beyond tree diagrams: Pomeron loops, H_{RFT} (Kovner et al '09).
 - Statistical mechanics analogies: sFKPP, important for large E.
 - Corrections to BK within JIMWLK: small! (Kovchegov et al '08).

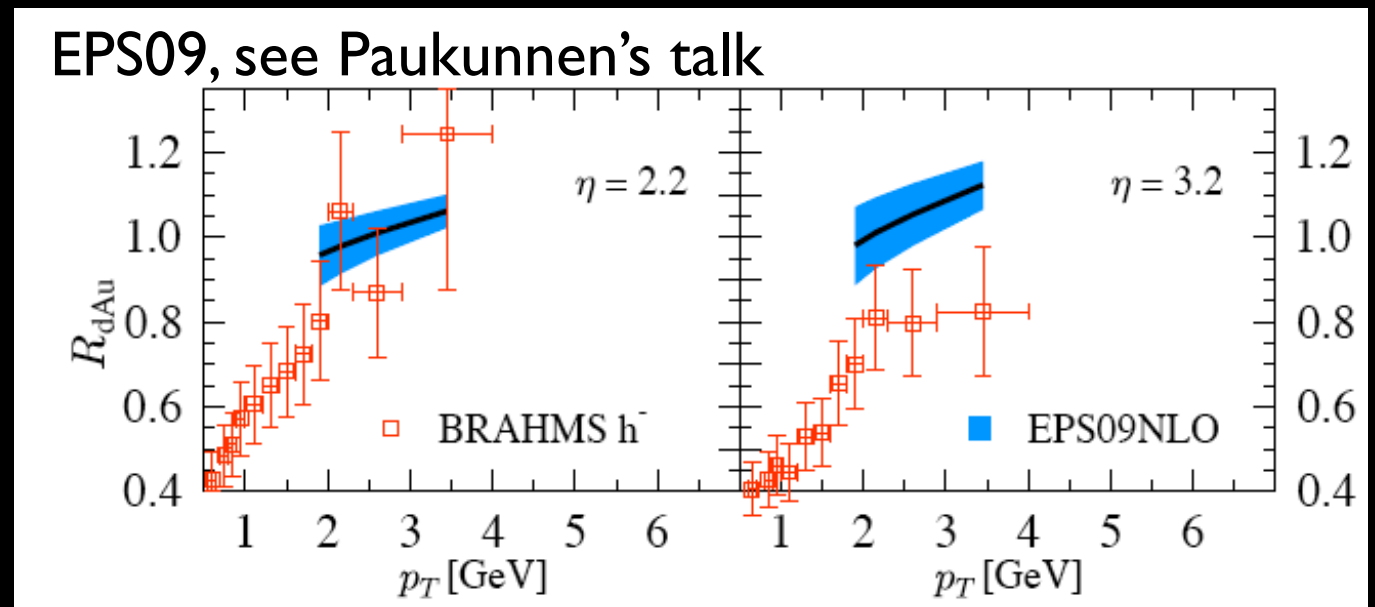
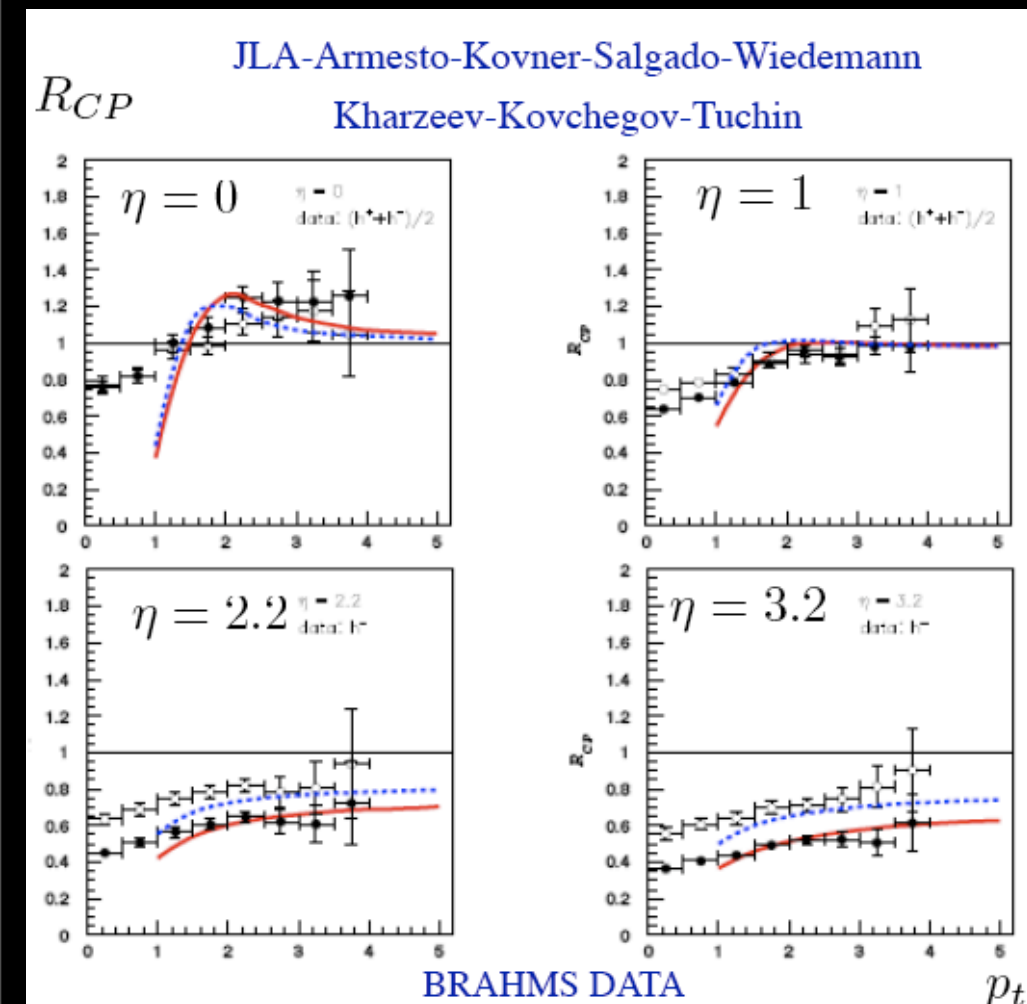
BK vs. ep/eA data	λ	β	slope of tail
Data	0.25-0.3	$\geq 1/3$	0.75
fixed coupling	$4.88\alpha_s$	initial conditions	0.63
running coupling	OK	small evolution	?

Factorization (I):

- k_T -factorization + LPHD (or DGLAP FF) used in nuclear collisions, for low-intermediate p_T particle production.

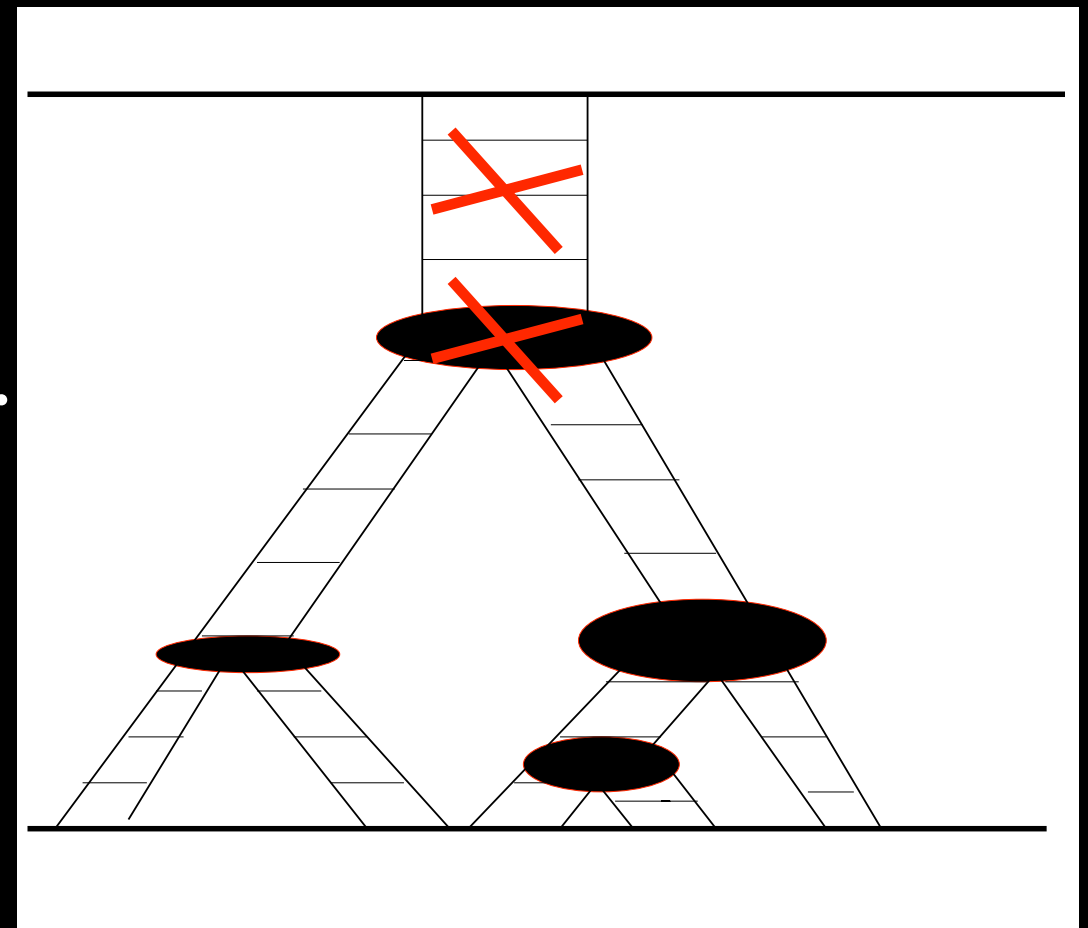


- Suppression in pA at forward rapidities constrains gluon shadowing.



Factorization (II):

- Analysis of k_T -like factorization or particle production in CYM, and of the validity of DGLAP-FF are under development. Several groups attempt to prove factorization for gluon or quark production:
 - In momentum space, the BFKL Pomeron language (Braun, Bartels et al).
 - In the dipole model (Kovchegov et al).
 - In classical gluodynamics: expansion in projectile and target densities (Gelis et al, Balitsky et al, McLerran et al, Marquet, Fukushima et al).
 - Hadron wave function (Nikolaev et al, Kovner et al).
- In **dilute-dense**: k_T -factorization OK? for single gluon, not for quark or for 2 gluons. Several pieces evolving BK-like.
- In **dense-dense**, usual k_T -factorization not valid (quantitative inaccuracy?); factorization becomes more involved.



3. Collective behavior:

3.1. Elliptic flow.

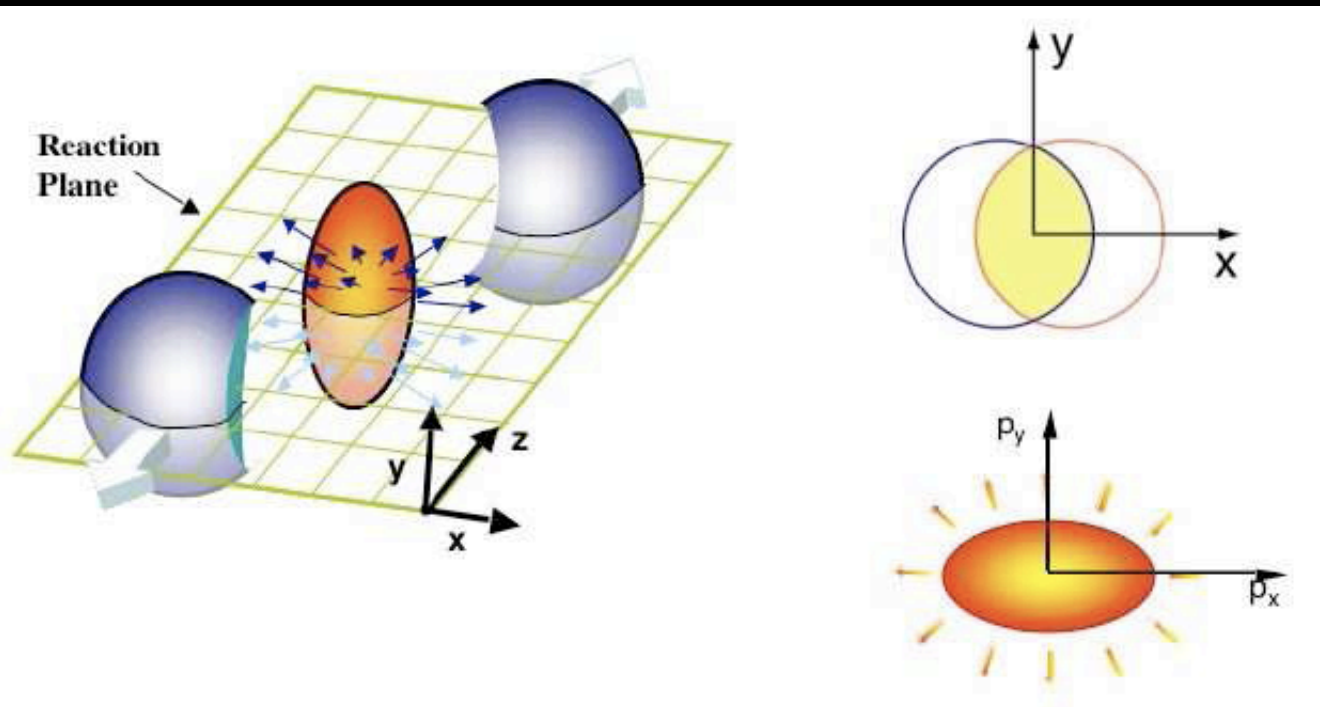
3.2. Hydrodynamical modeling.

See the reviews: Heinz et al '03, Hirano et al '08, Romatschke '09.

3.3. Strong coupling calculations.

See the review Edelstein et al '09.

Elliptic flow:

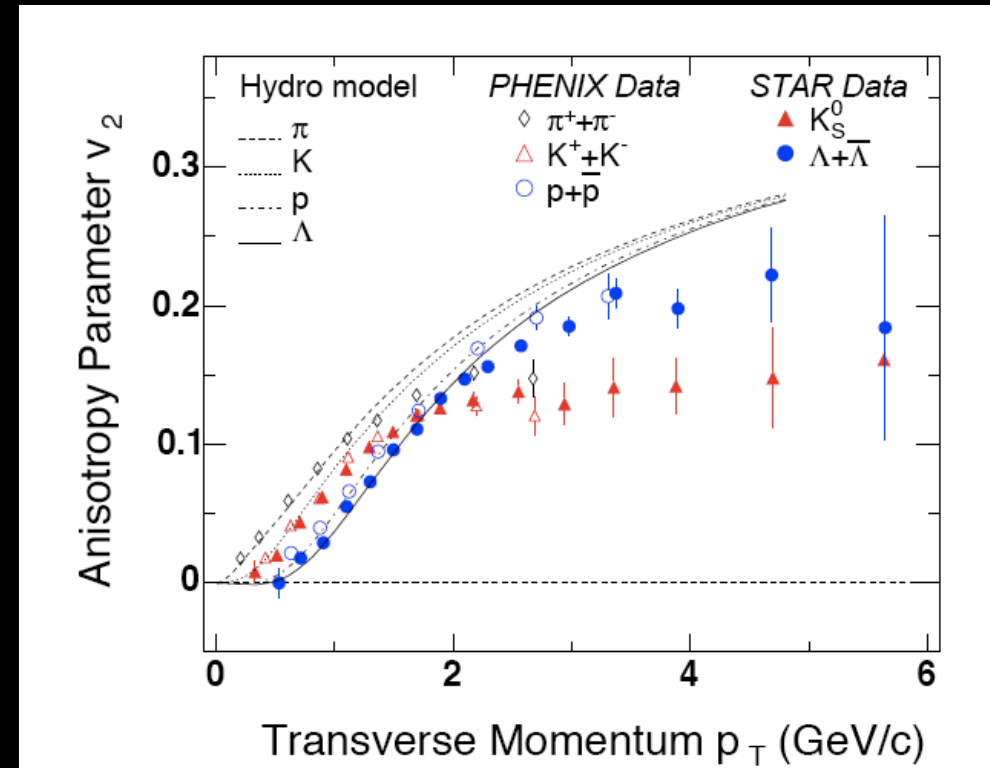
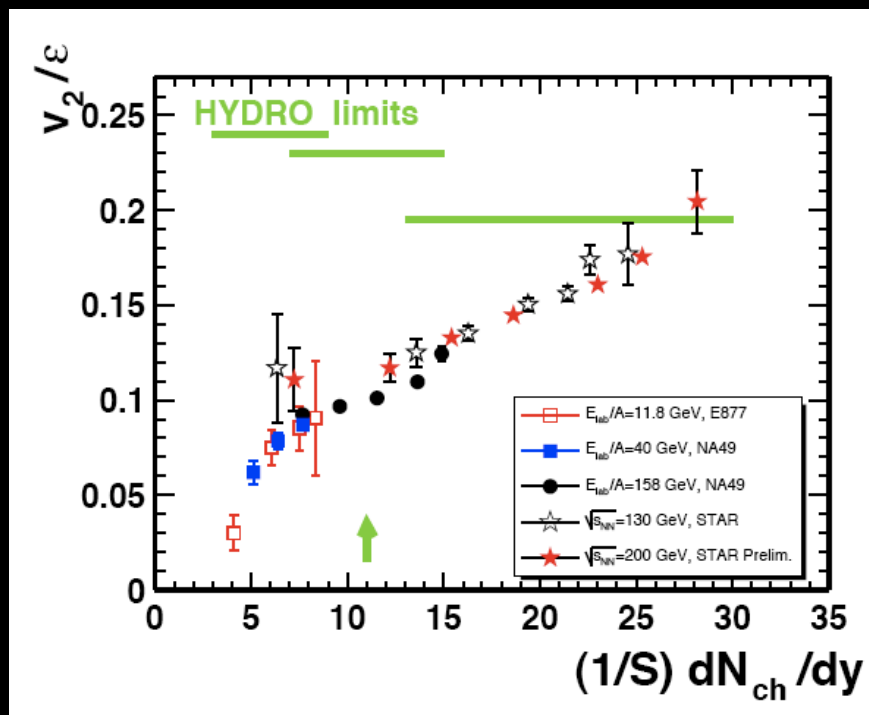


$$\frac{dN_k}{dy dp_T^2 d\phi} = \frac{dN_k}{dy dp_T^2} \frac{1}{2\pi} [1 + 2v_1 \cos(\phi - \phi_R) + 2v_2 \cos 2(\phi - \phi_R) + \dots]$$

$$v_2 = \langle \cos 2(\phi - \phi_R) \rangle = \left\langle \frac{p_x^2 - p_y^2}{p_T^2} \right\rangle$$

$$\epsilon_x = \frac{\langle y^2 - x^2 \rangle}{\langle y^2 + x^2 \rangle}$$

- v_2 , also called elliptic flow, is usually interpreted in terms of a final momentum anisotropy dictated by an initial space anisotropy.



Hydrodynamical behavior:

- **Ideal hydro:** plus an (lattice) EOS, initial conditions and a hadronization prescription.

$$u^\mu = \gamma (1, v_x, v_y, v_z)$$

$$T_{(0)}^{\mu\nu}(x) = (e(x) + p(x)) u^\mu(x) u^\nu(x) - p(x) g^{\mu\nu}$$

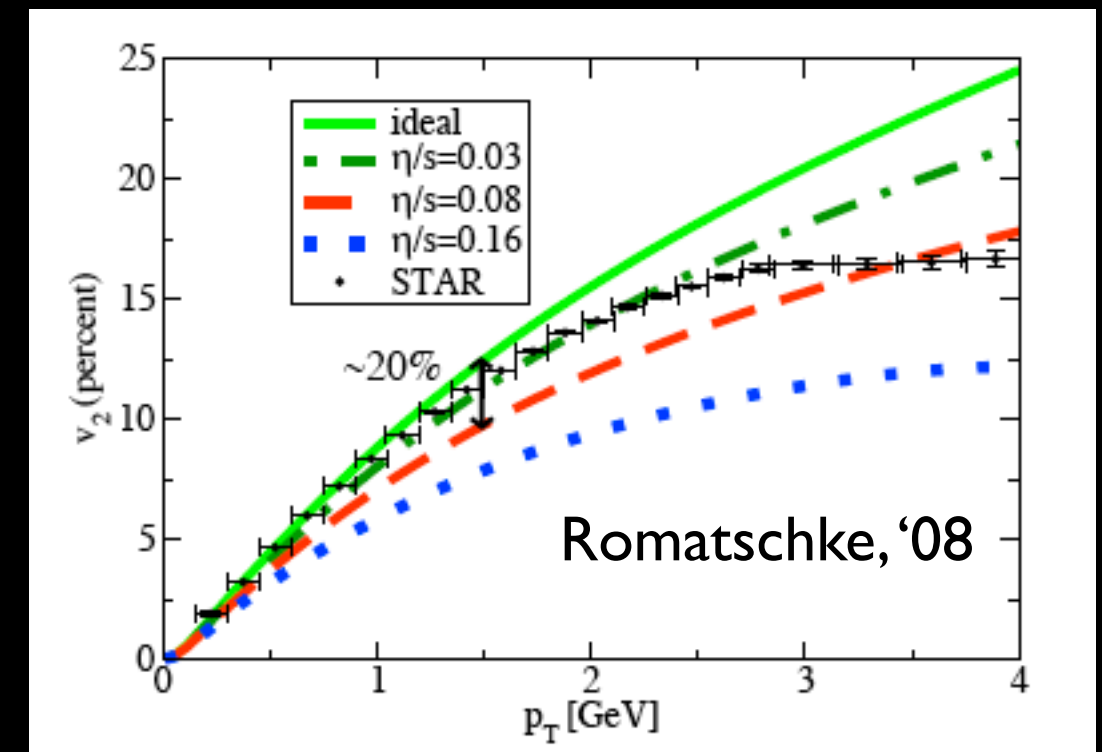
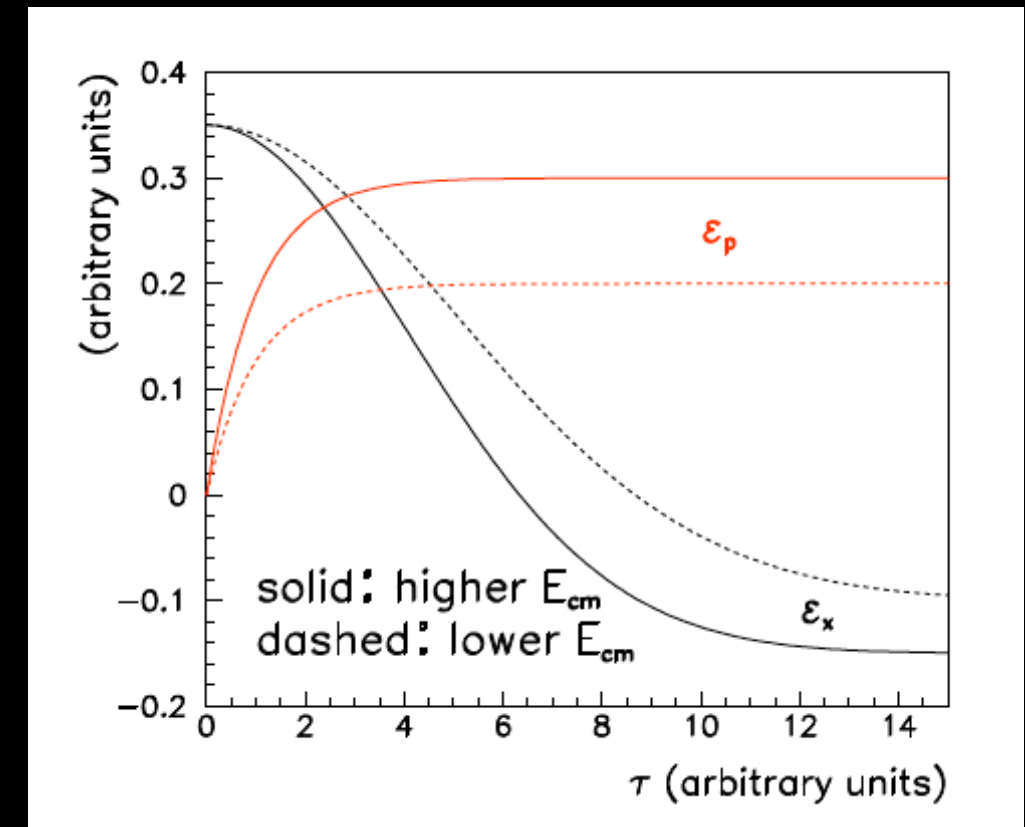
$$\partial_\mu T_{(0)}^{\mu\nu}(x) = 0, \quad (\nu = 0, \dots, 3)$$

$$\partial_\mu j_i^\mu(x) = 0, \quad i = 1, \dots, M$$

- **Non-ideal hydro:** dissipative (viscous) corrections.

$$T^{\mu\nu} = T_{(0)}^{\mu\nu} + \Pi^{\mu\nu}$$

- $\Pi^{\mu\nu}$ introduces bulk viscosity plus gradients of u : 1st order (shear viscosity), 2nd order (5 constants for a CFT),...

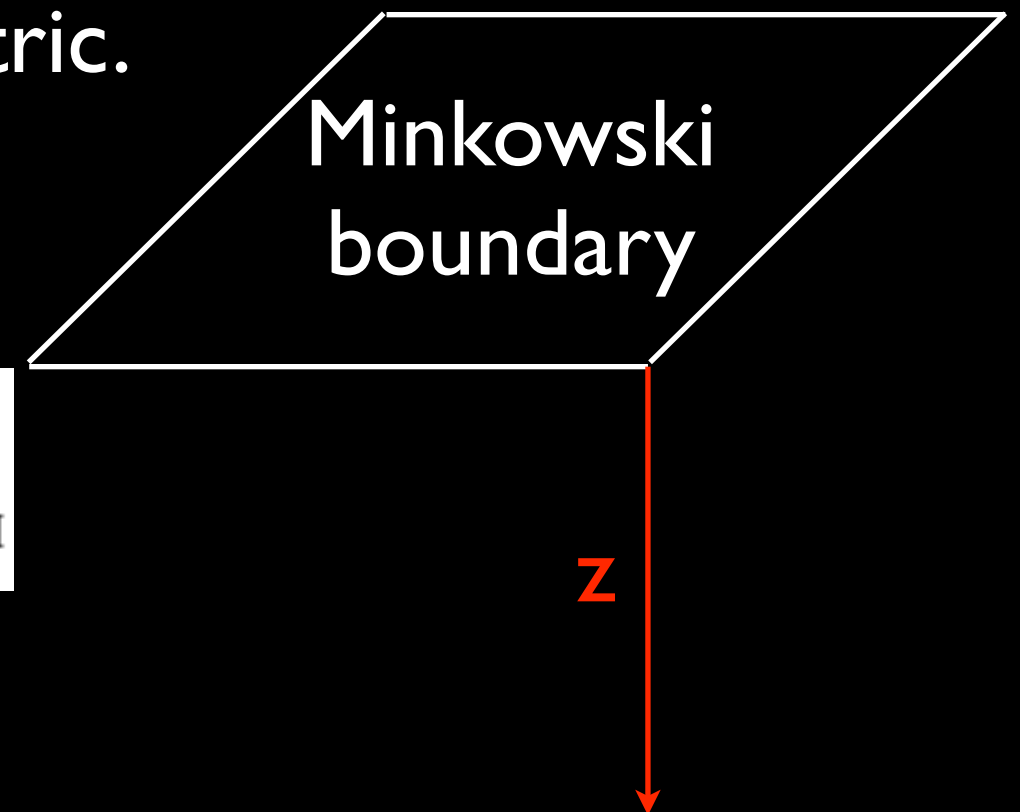


Strong coupling calculations (I):

- **Strong coupling** is suggested by:
 - The quasi-ideal fluid behavior ($\lambda=(\rho\sigma)^{-1}\ll R$).
 - The early isotropization/thermalization, difficult to explain in pQCD (Romatschke et al '04, Xu et al '05).
 - The strong quenching of high-energy particles.
- **AdS/CFT correspondence:** dynamics of N=4 SUSY QCD for $N_c, \lambda=g^2 N_c \rightarrow \infty$ can be computed using classical gravity in $AdS_5 \times S^5$.
 - Temperature through black-hole metric.
 - No confinement, no asymptotic freedom, no quarks,...

$$\mathcal{Z}_{\text{string}} \left[\Phi_i(z, x^\mu) \Big|_{z=0} = \varphi_i(x^\mu) \right] = \left\langle \exp \left(\int d^4x \varphi_i \mathcal{O}_i \right) \right\rangle_{\text{SYM}}$$

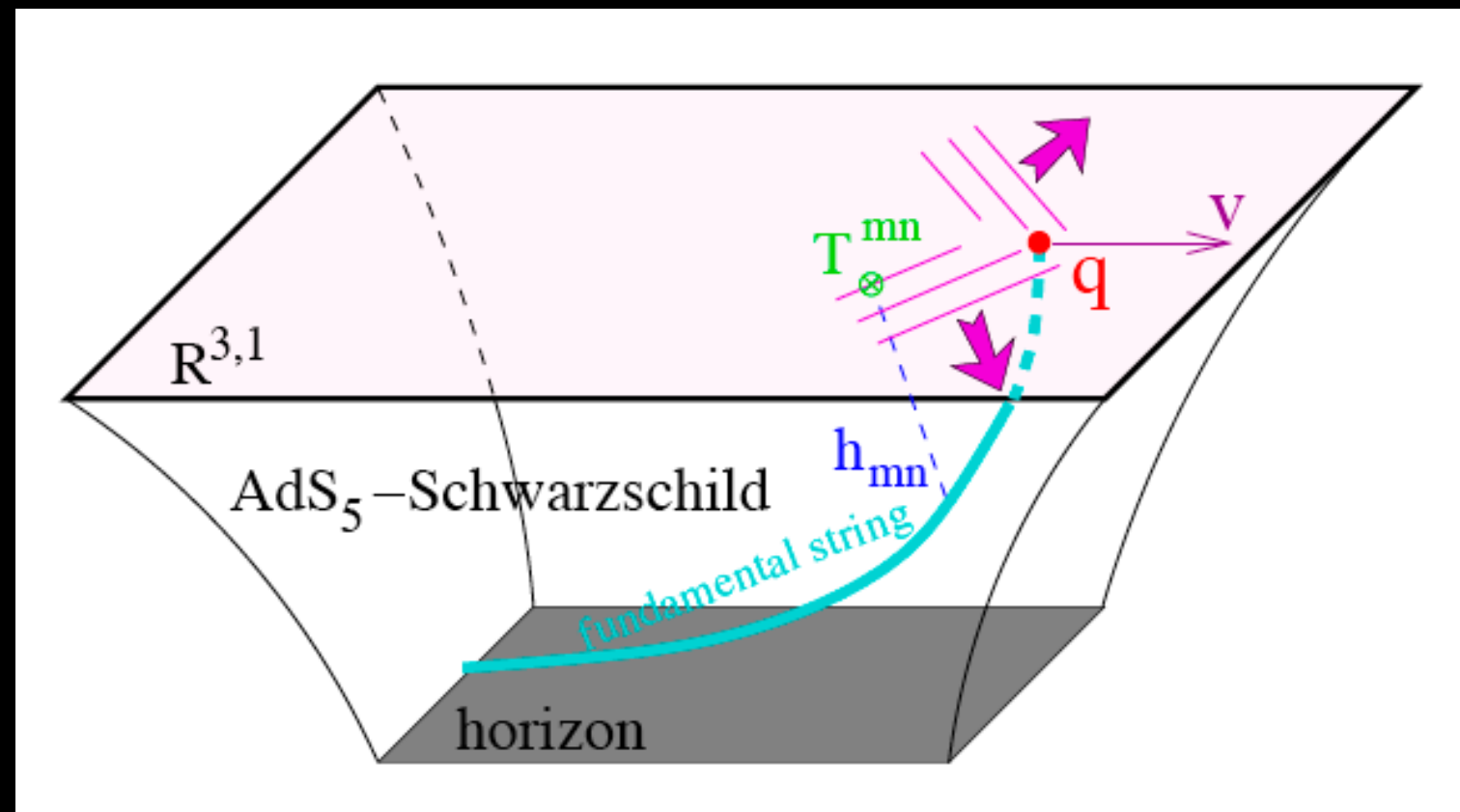
\mathcal{O}_i is the SYM associated with the supergravity field Φ_i .



Strong coupling calculations (II):

- **AdS/CFT has been applied to several aspects of HIC:**
 - The energy loss of fast (Liu et al '06) and slow partons (Gubser et al '09).

→ The energy deposition and medium disturbance created by the energetic particle.



- The early isotropization/thermalization problem.
- The hydrodynamical behavior (Janik et al '07; Kovchegov '07).

$$\tilde{g}_{\mu\nu}(x, z) = \tilde{g}_{\mu\nu}^{(0)}(x) + z^2 \tilde{g}_{\mu\nu}^{(2)}(x) + z^4 \tilde{g}_{\mu\nu}^{(4)}(x) + \dots$$

$$\langle T_{\mu\nu} \rangle = \frac{N_c^2}{2\pi^2} \tilde{g}_{\mu\nu}^{(4)}(x)$$

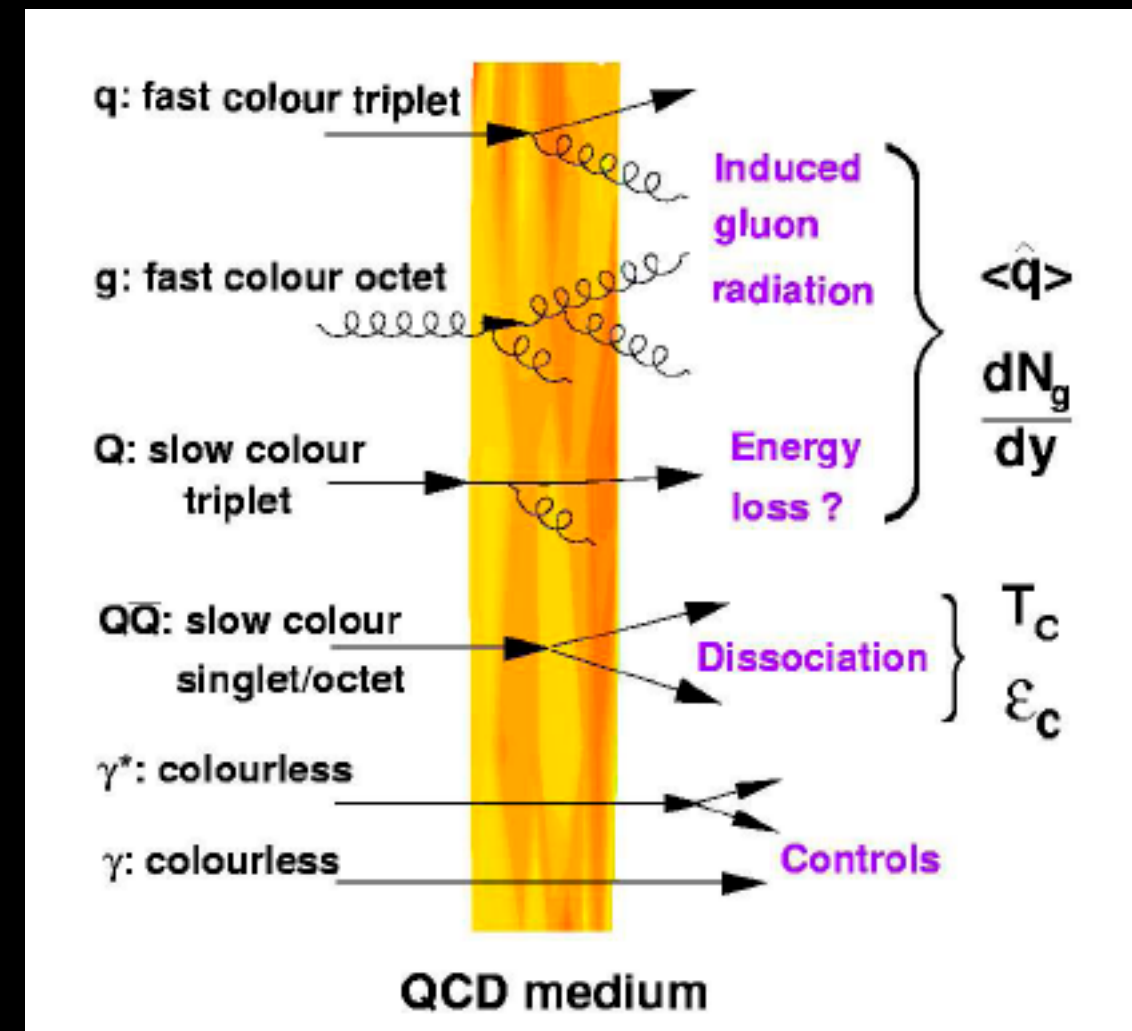
- The initial conditions for a HIC (Albacete et al '08).

4. Hard probes: high- p_T particles and jets:

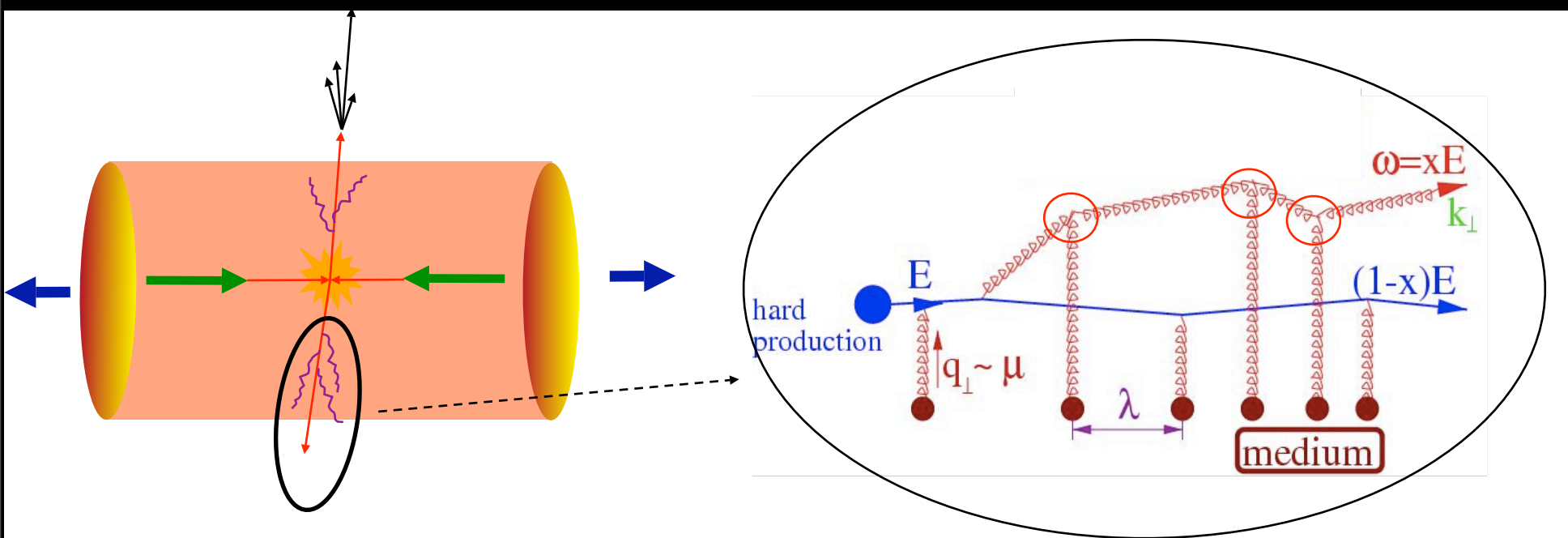
4.1. Successes and problems in radiative energy loss.

4.2. In-medium parton showers.

See the reviews: d'Enterria '09; Casalderrey-Solana et al '07; Yellow Report on Hard and EM Probes '04.



Radiative eloss - successes:

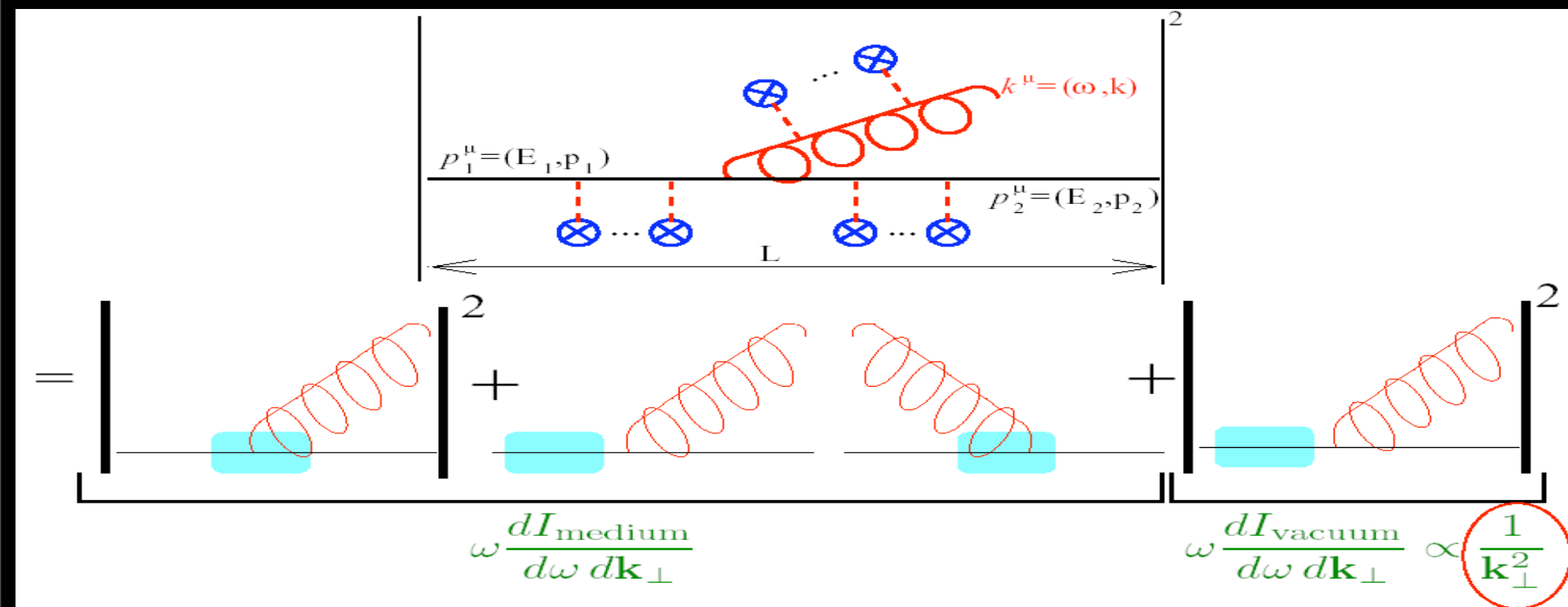


$$\hat{q} = \frac{\mu^2}{\lambda}$$

BDMPS

$$\Delta E \propto C_R \alpha_s \hat{q} L^2$$

- **Medium-modified gluon radiation:** production/rescattering.



- **Two medium parameters:** \hat{q} or gluon density plus mean free path, and length (geometry, dynamical expansion).

Radiative eloss - successes:

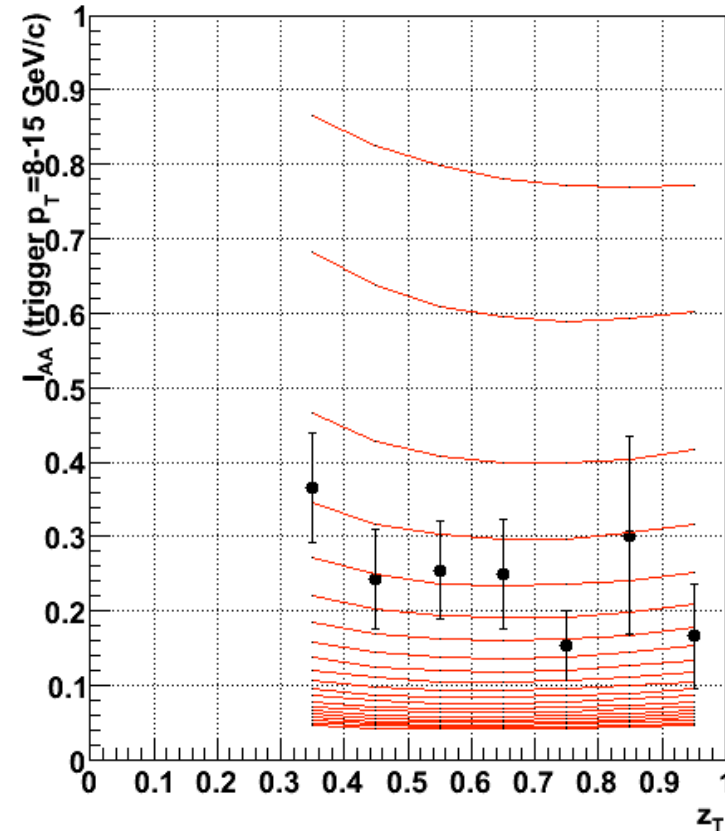
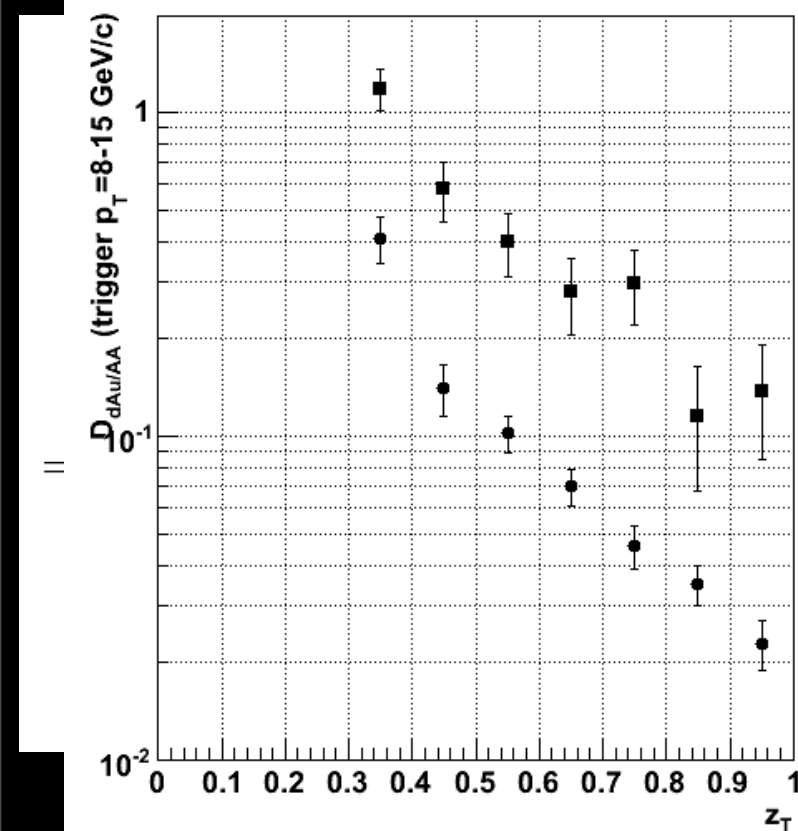
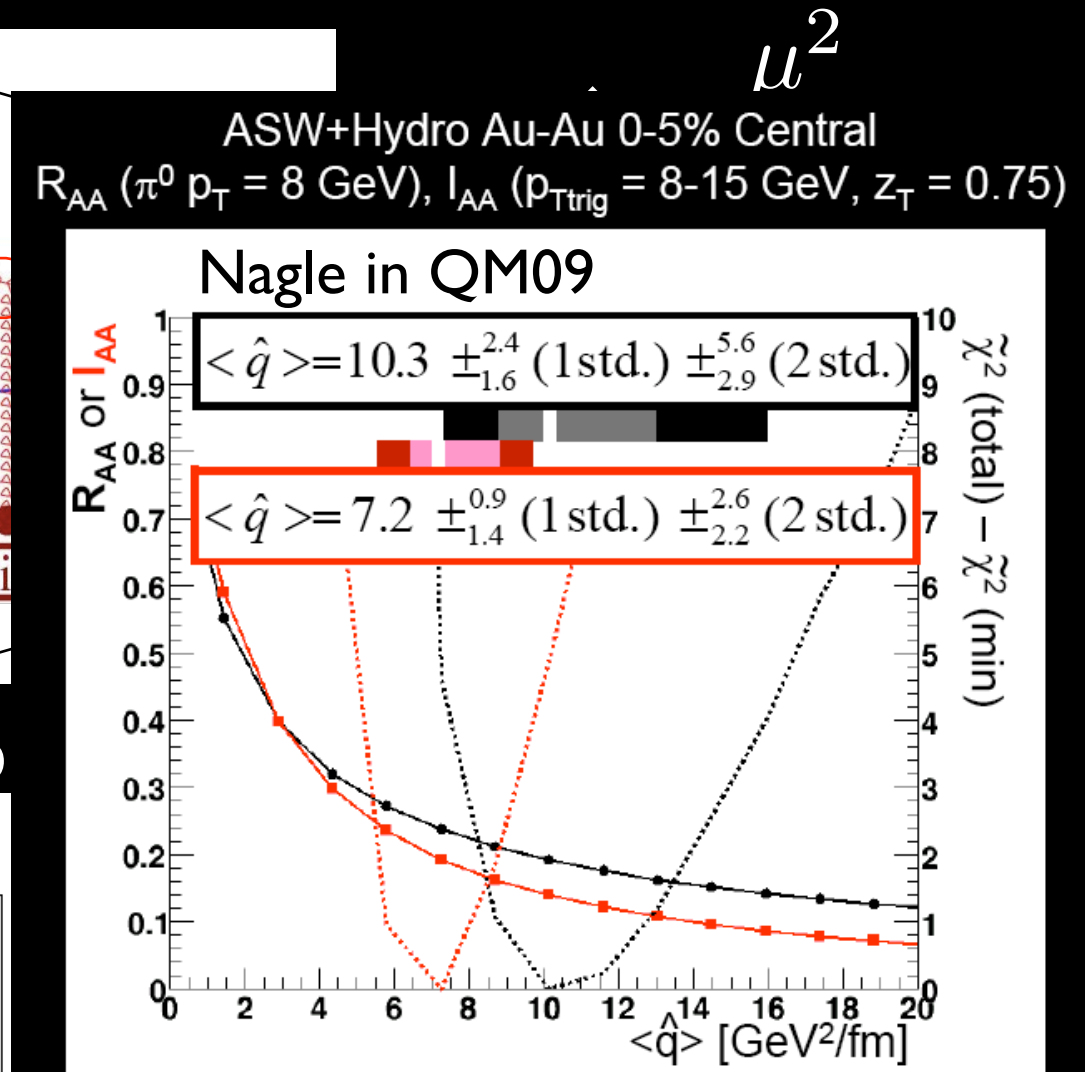
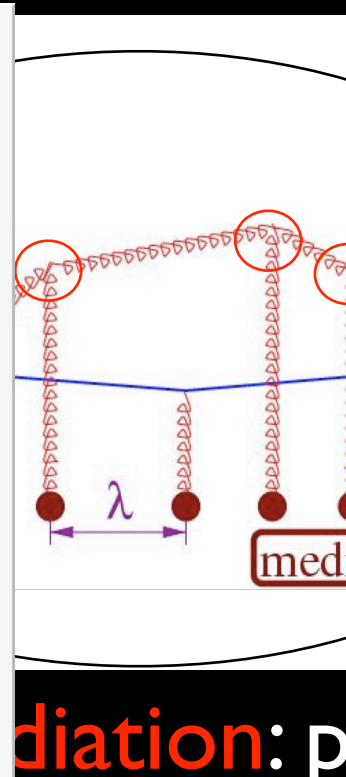
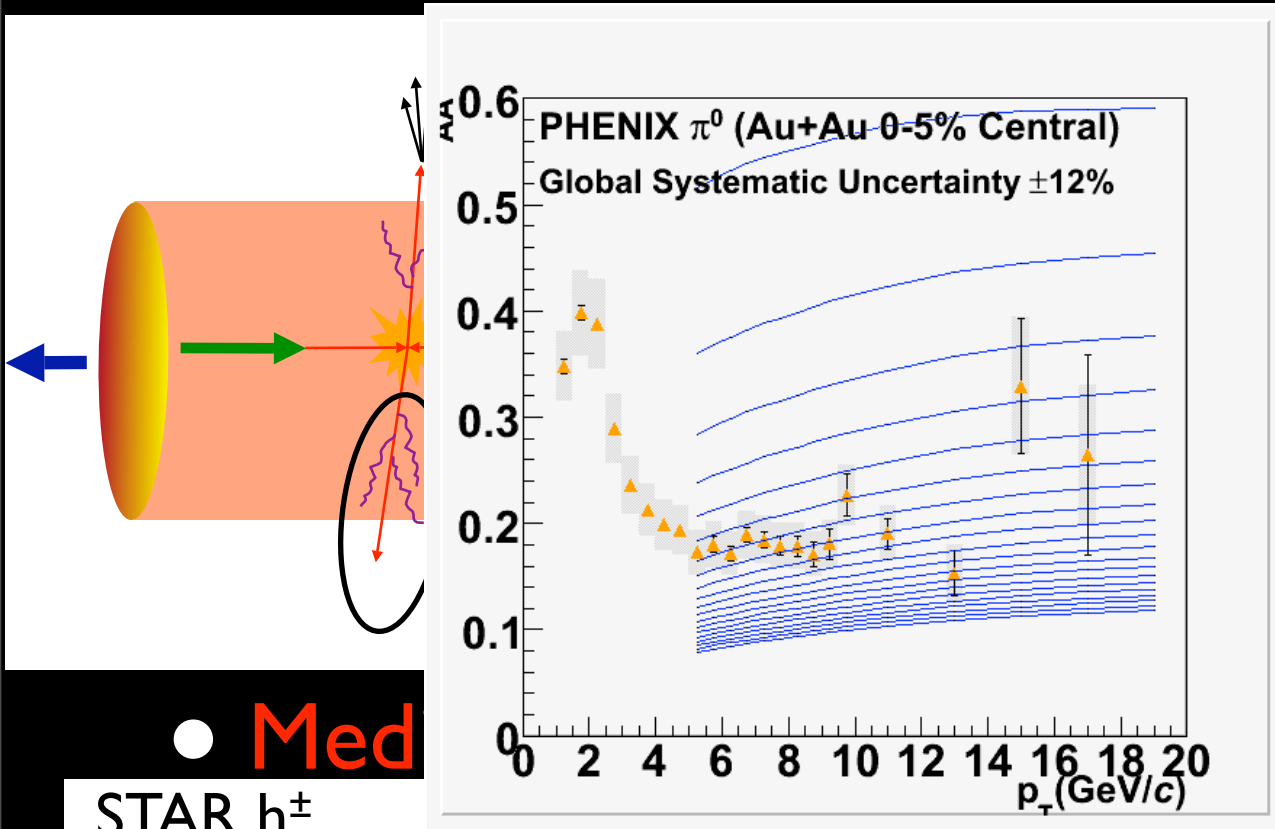


Diagram of a heavy-ion collision showing the collision zone and the resulting particle production. The plot shows the PHENIX π^0 (Au+Au 0-5% Central) Global Systematic Uncertainty $\pm 12\%$ as a function of p_T (GeV/c). The data points are shown with error bars, and the theoretical curves are shown as blue lines.

or gluon density plus mean free path, and length (geometry, dynamical expansion).

Radiative eloss - problems:

- $\Delta E(g) > \Delta E(q) > \Delta E(Q)$; but e^- from c,b are too suppressed: collisional contributions, hadronization, problems in pQCD?
- The extracted value of \hat{q} depends on medium model:
 $1 < \hat{q} < 15 \text{ GeV}^2/\text{fm} \Rightarrow$ interface with realistic medium (TECHQM).
- Calculations done in the high-energy approximation: **only soft emissions**, energy-momentum conservation imposed a posteriori \Rightarrow Monte Carlo.
- **Multiple gluon emission: Quenching Weights** (Baier et al '01), independent (Poissonian) gluon emission: assumption! \Rightarrow Monte Carlo (PQM, PYQUEN, YaJEM, JEWEL, Q-PYTHIA).
- No role of **virtuality** in medium emissions; medium and vacuum treated **differently** \Rightarrow modified DGLAP evolution (Guo et al '01-..., Salgado et al '06, Armesto et al '07).

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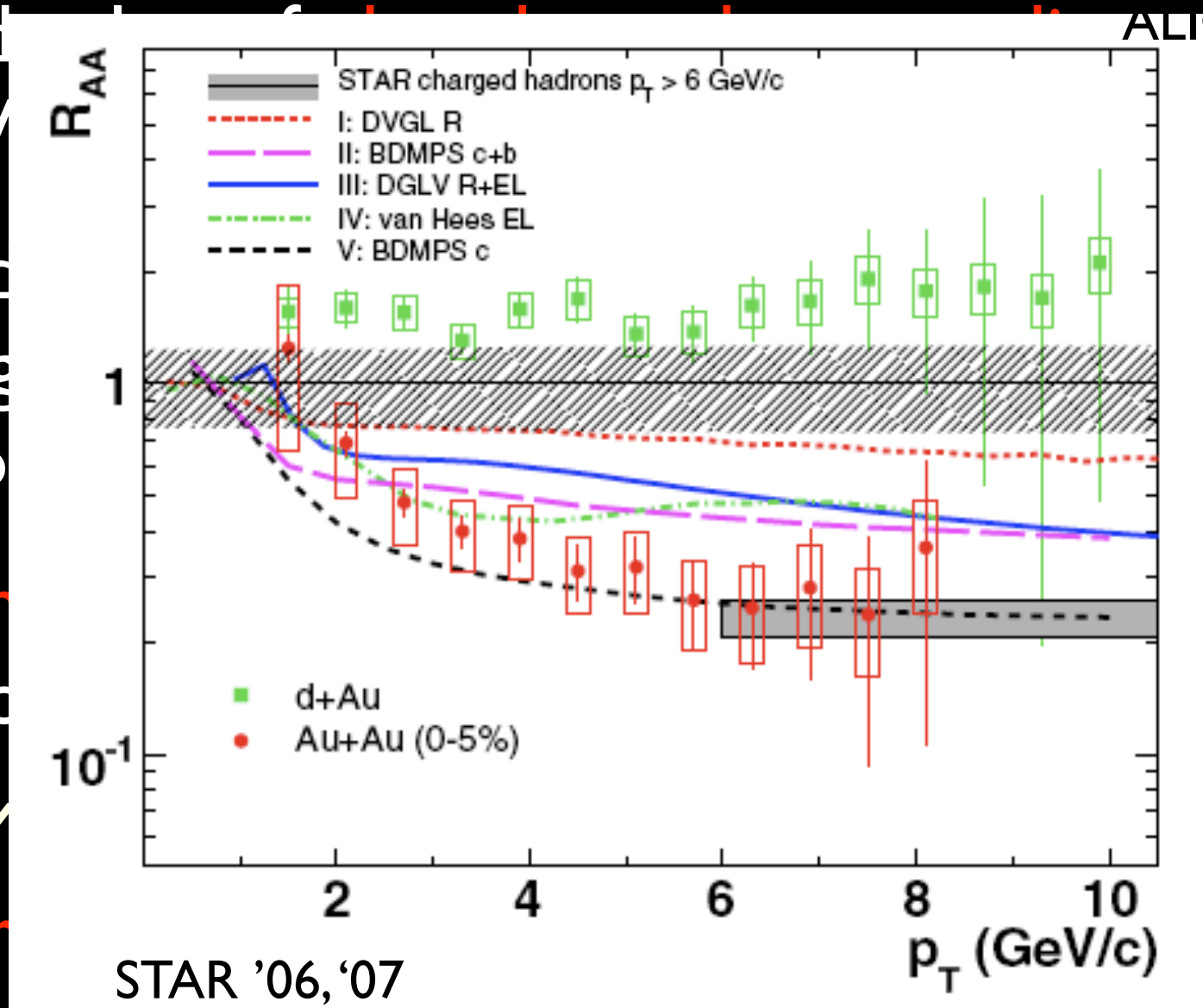
- The extracted R_{AA} for $1 < q_{hat} < 15$ GeV

- Calculations of R_{AA} for $q_{hat} > 10$ GeV: **emissions**, energy loss \Rightarrow Monte Carlo

- **Multiple gluon** emissions: R_{AA} independent (PQM)

- Monte Carlo (PQM, PYTHIA)

- No role of **virtual** emissions: treated **differently** \Rightarrow modified DGLAP evolution (Guo et al '01-..., Salgado et al '06, Armesto et al '07).



STAR '06, '07

ALICE model: R_{AA} (TECHQM).

on: **only soft** emissions a posteriori

et al '01), $R_{AA} \Rightarrow$ Monte

h and vacuum R_{AA} (Guo et al '01-..., Salgado et al '06, Armesto et al '07).

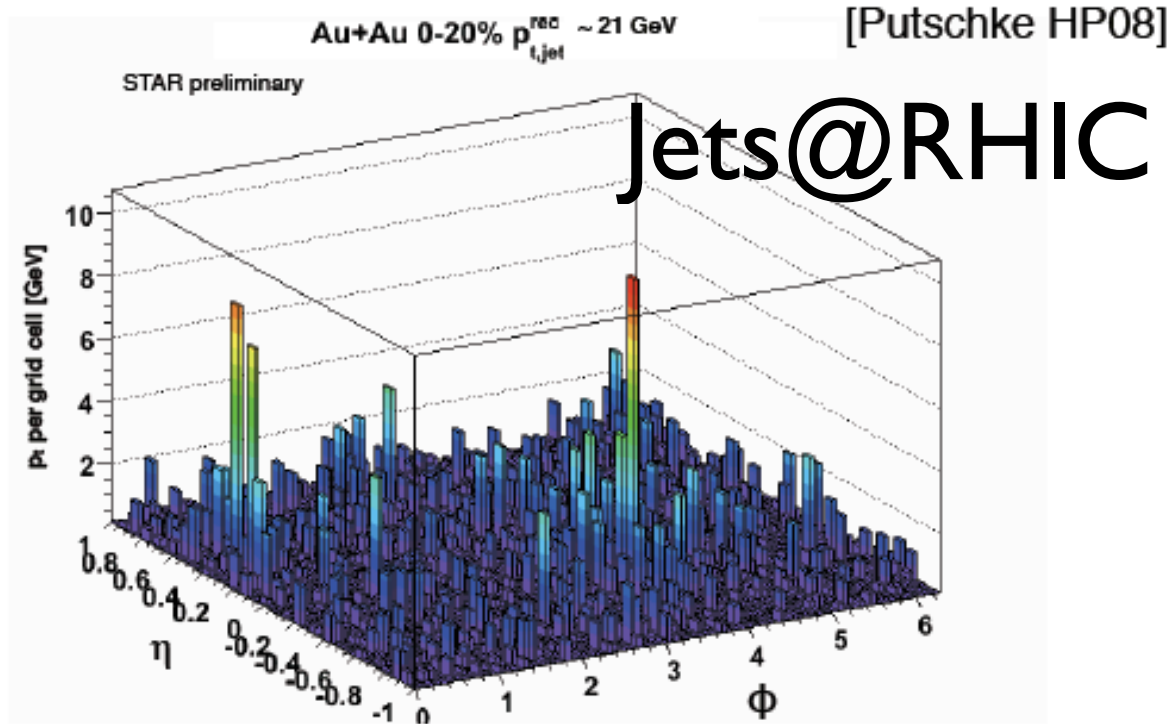
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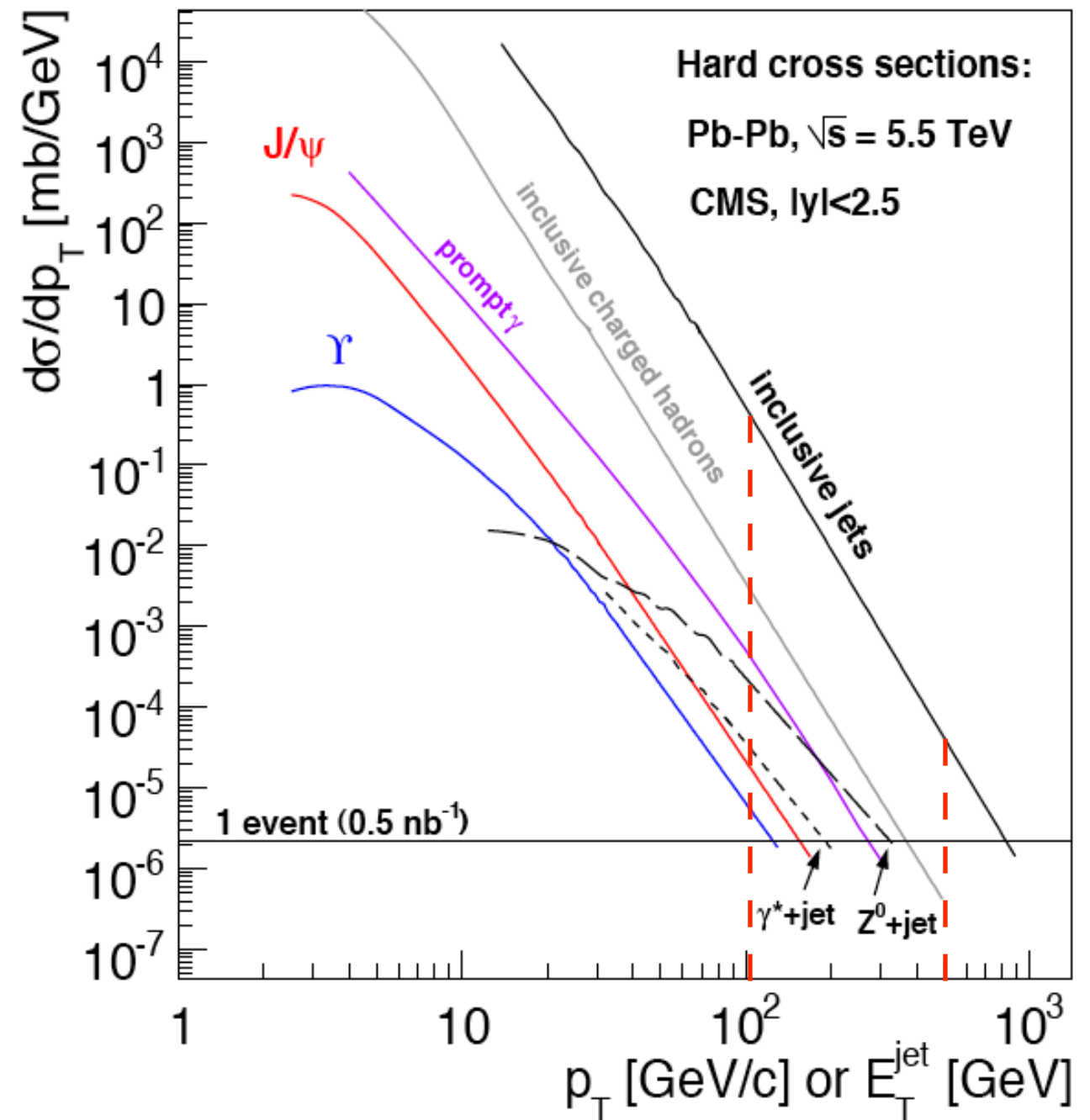
Radiative eloss - problems:

- $\Delta E(g) > \Delta E(q) > \Delta E(Q)$; but e^- from c, b are too suppressed: collisional contributions, hadronization
- The extracted value of \hat{q} depends on the choice of p_T cut
 $1 < \hat{q} < 15 \text{ GeV}^2/\text{fm} \Rightarrow$ interface with soft physics

First results appeared in HP2008!

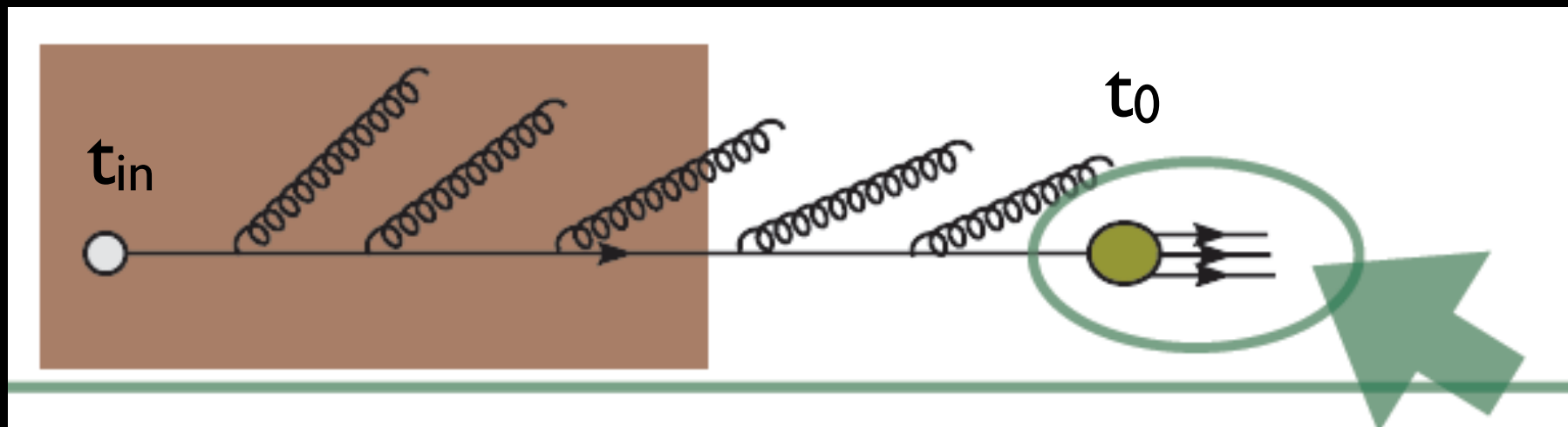


A lot of work still needed



Salgado et al '06, Armesto et al '07).

In-medium FSR (I):



- **Assumption:** hadronization is not affected by the medium: looks OK at RHIC for $p_T > 7-10$ GeV.
- The **splittings are modified:** either radiatively (Q-PYTHIA) or radiative+collisionally (JEWELL, PYQUEN); or the evolution is enlarged due to momentum broadening (YaJEM).

$$P_{i \rightarrow j}(z) \longrightarrow P_{i \rightarrow j}(z) + \Delta P_{i \rightarrow j}(z, t, E, L, \hat{q})$$

- **Underlying ingredients:** factorization no emission/emission/no emission/... (Sudakov/splitting/Sudakov/...) holds in the medium, and the evolution scale (t, k_T, Θ) can be related with the medium length \rightarrow both to be proved (Jet Calculus in a medium).

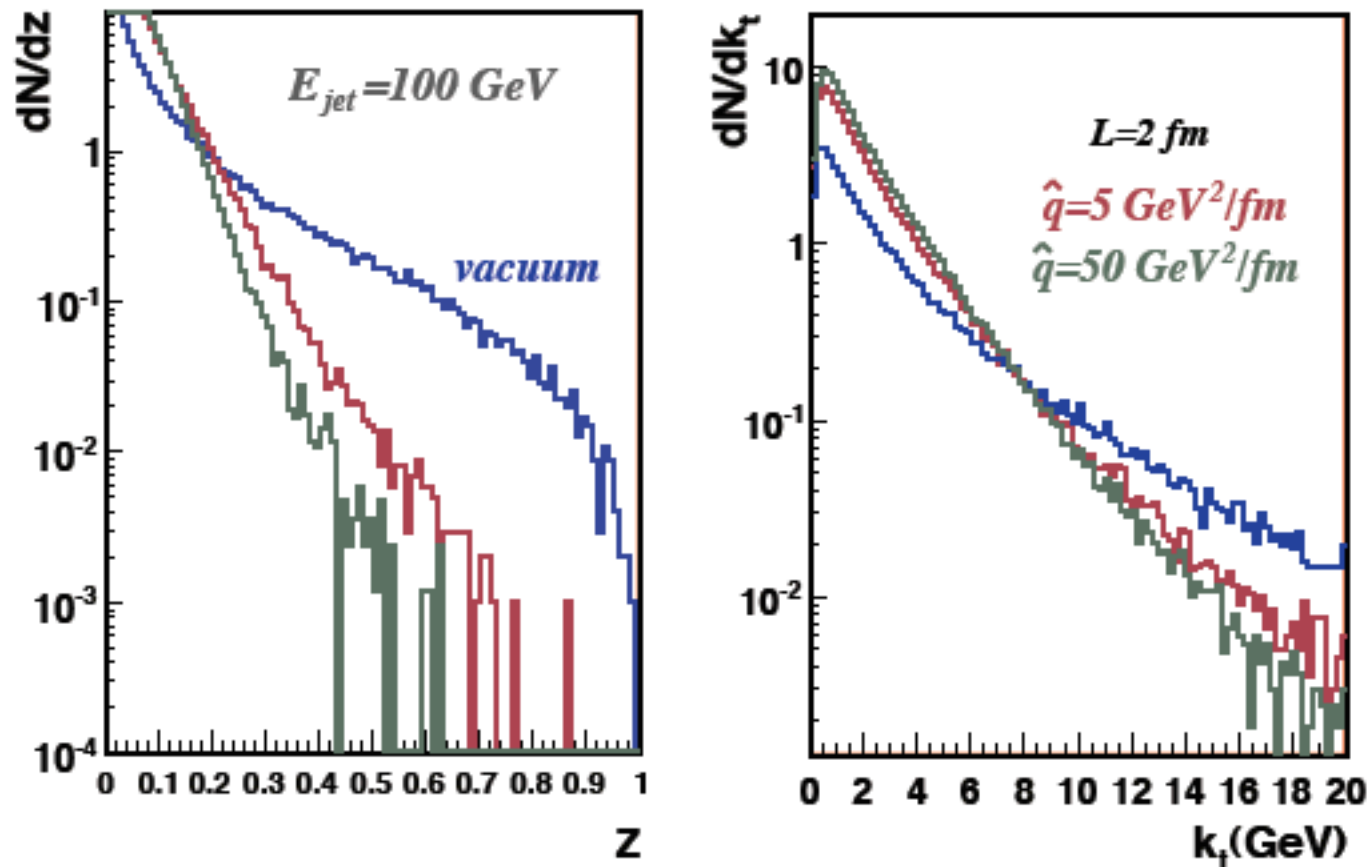
In-medium FSR (II):

- The MC's generically reproduce the **expectations**:
 - Particle spectrum softens (jet quenching).
 - Larger emission angles (jet broadening).
 - Intra-jet multiplicity enlarges.

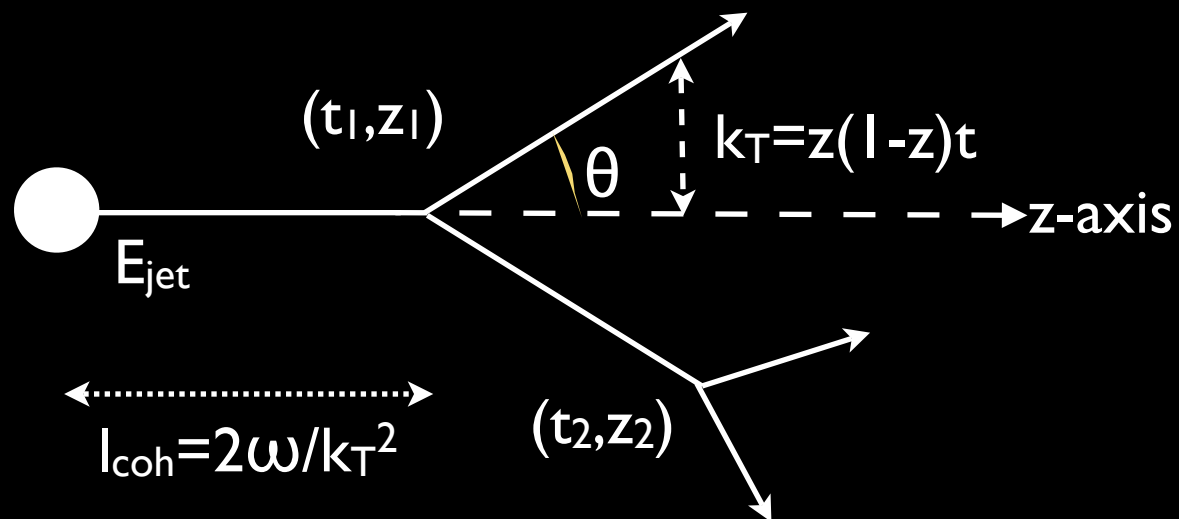
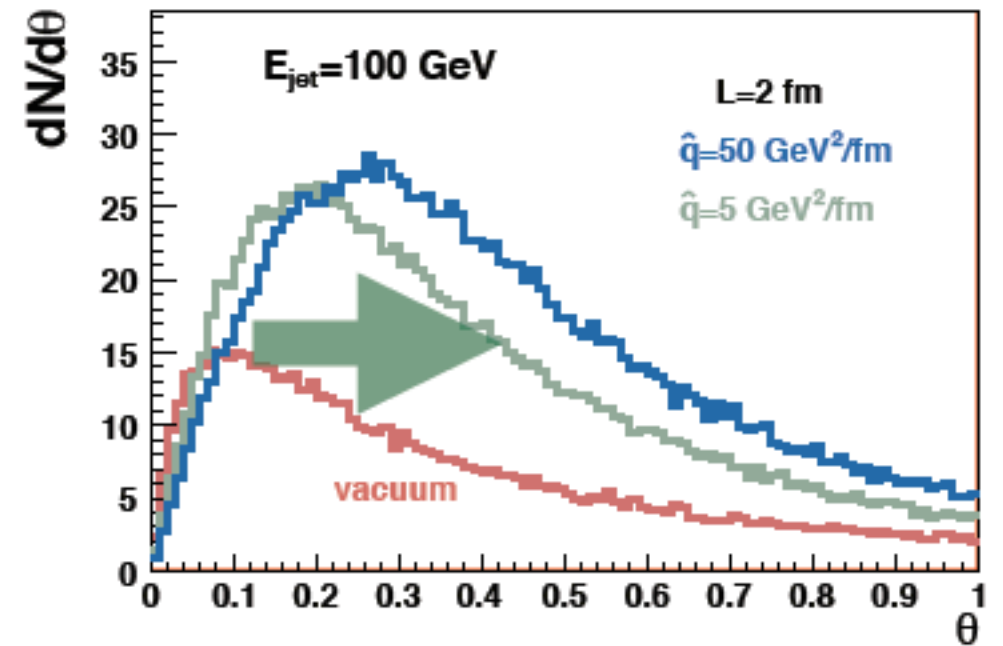
In-medium FSR (II):

Q-PYTHIA

Fragmentation function



Angular distribution



- Intense activity at RHIC and the LHC: jet reconstruction in a large background (small clustering parameters versus out-of-cone medium modification).

In-medium FSR (II):

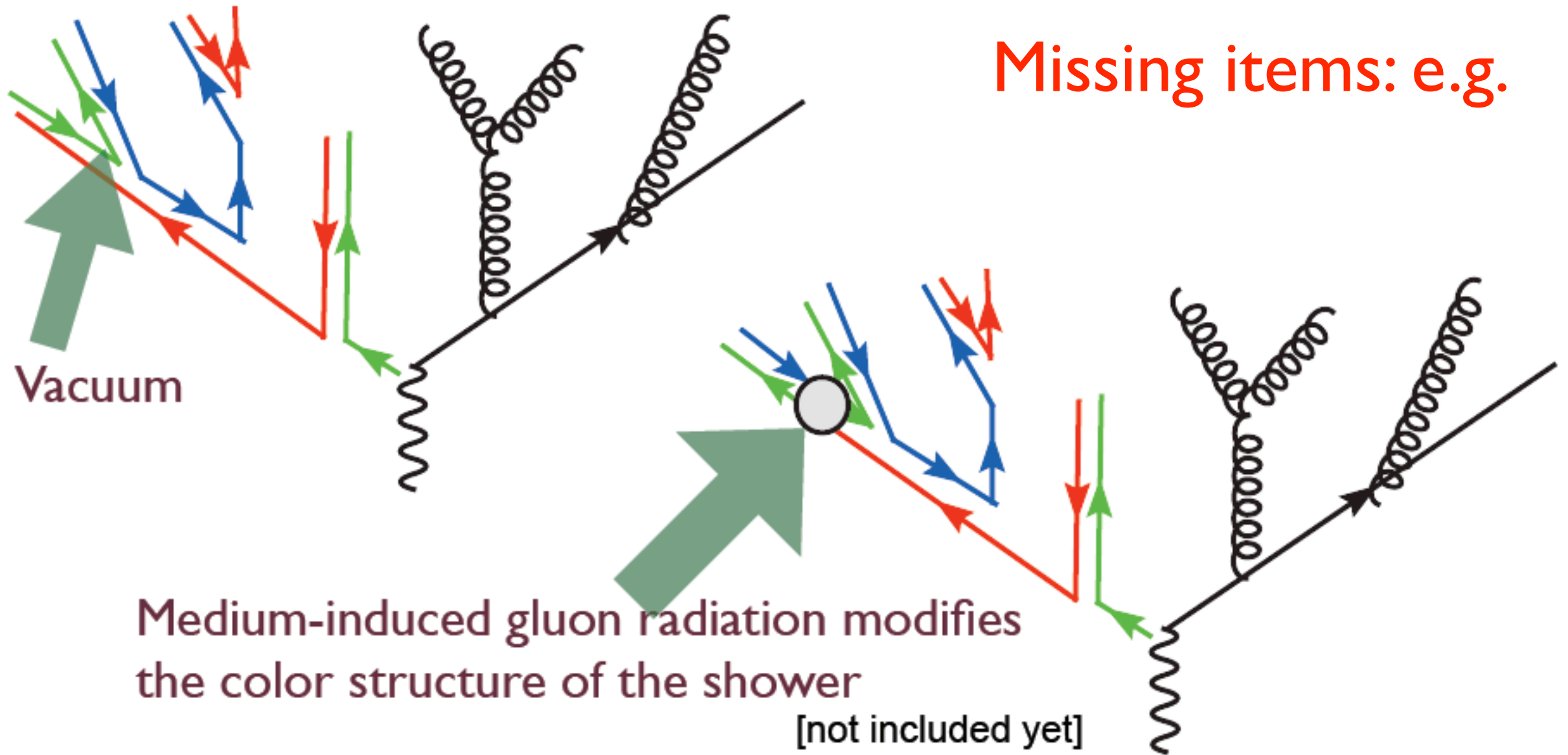
Q-PYTHIA

Fragmentation function

Angular distribution



Missing items: e.g.



$$l_{coh} = 2\omega/k_T^2$$

(t_2, z_2)

parameters versus out-of-cone medium modification).

Summary:

- The **interpretations of the three main observables at RHIC** (low multiplicity, collective flow, jet quenching) have triggered a lot of ongoing theoretical activity on (to mention just a few):
 - A) Small-x physics and particle production in nuclear collisions.
 - B) Early thermalization and viscous hydrodynamics.
 - C) Strong coupling computations: AdS/CFT for HIC.
 - D) New formalisms for eloss: correlations, jets, Monte Carlo,...
- The **LHC and RHIC-II** offer huge possibilities to verify or falsify the picture arising from RHIC with new observables: jets, identified heavy flavor, EW boson production,... Much work has been done but much remains to be done.
- Points A) and D) in the list above have clear **connections with pp and DIS**: link with plans on **future eA colliders**.