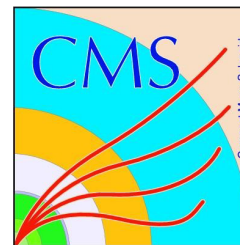


# W helicity: latest LHC results

10<sup>th</sup> Open LHC TopWG meeting: Nov. 21<sup>st</sup>–23<sup>rd</sup> 2016

María Moreno Llácer

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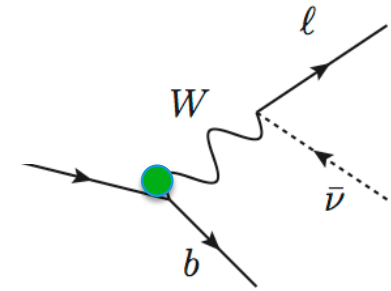


- $Wtb$  vertex Lagrangian and sensitive observables to probe it
- $W$  helicity using  $\cos\theta_l^*$  distributions
  - analysis methods
- Latest LHC results
  - \* ATLAS 8 TeV: single lepton results
  - \* CMS 8 TeV: single lepton results
  - \* Comparisons between them

## Wtb vertex Lagrangian:

- Top quark decay:  $t \rightarrow Wb$  ( $\approx 100\%$ )
- SM: Weak coupling with (V-A) structure
- Only coupling to left-handed fermions

Nucl.Phys. B812 (2009) 181-204  
Eur.Phys.J. C50, 519 (2007)



$$L_{Wtb} = -\frac{g}{\sqrt{2}} \bar{u}_b \gamma^\mu (V_L P_L + V_R P_R) u_t W_\mu^+ - \frac{g}{\sqrt{2}} \bar{u}_b \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (g_L P_L + g_R P_R) u_t W_\mu^+ + \text{h.c.}$$

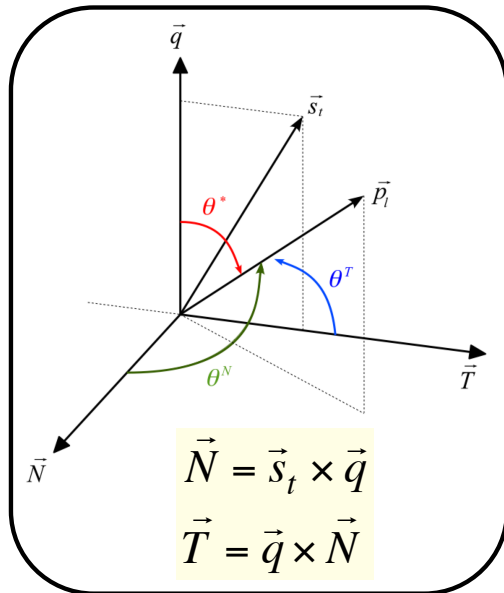
$V_{L,R}$  and  $g_{L,R}$   
left and right - handed vector and tensor couplings

$SM \Rightarrow V_L = V_{tb} \sim 1$

$V_R = g_L = g_R = 0$

Right-handed contribution?  
Tensor couplings?

## Angular observables to probe the Wtb vertex:



Nucl. Phys. B 840(2010)349

→ For unpolarised top quark decays, the only meaningful direction in the top RF is the one of the  $W$  boson momentum ( $q$ )

→ For polarised (spin direction  $s_t$ ) top quarks produced via electroweak interaction, further directions may be considered:  $N$  and  $T$ .

→ Three angular distributions:  $\theta_l^*$ (q,l),  $\theta_l^N$ (N,l) and  $\theta_l^T$ (T,l)

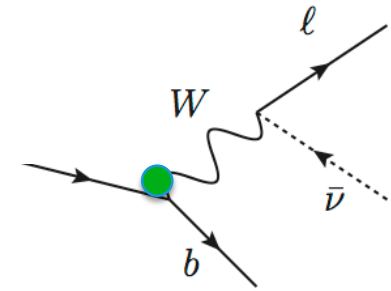
$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_l^X} = \frac{3}{8} (1 + \cos \theta_l^X)^2 F_+^X + \frac{3}{8} (1 - \cos \theta_l^X)^2 F_-^X + \frac{3}{4} \sin^2 \theta_l^X F_0^X$$

$$A_{FB}^X = \frac{N(\cos \theta_l^X > 0) - N(\cos \theta_l^X < 0)}{N(\cos \theta_l^X > 0) + N(\cos \theta_l^X < 0)} \propto (F_+^X - F_-^X)$$

## Wtb vertex Lagrangian:

- . Top quark decay:  $t \rightarrow Wb$  ( $\approx 100\%$ )
- . SM: Weak coupling with (V-A) structure
- . Only coupling to left-handed fermions

Nucl.Phys. B812 (2009) 181-204  
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$$L_{Wtb} = -\frac{g}{\sqrt{2}} \bar{u}_b \gamma^\mu (V_L P_L + V_R P_R) u_t W_\mu^+ - \frac{g}{\sqrt{2}} \bar{u}_b \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (g_L P_L + g_R P_R) u_t W_\mu^+ + \text{h.c.}$$

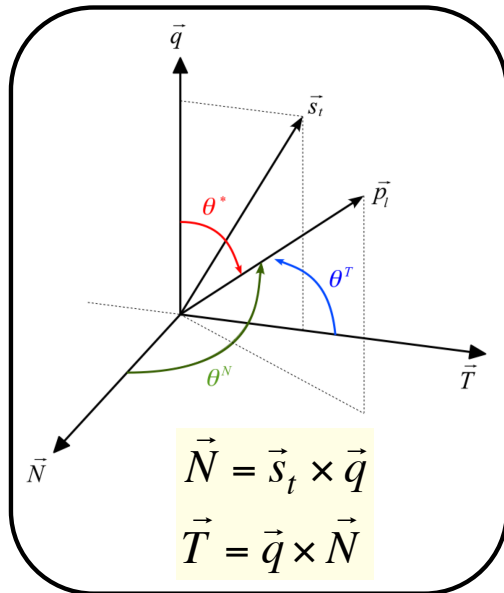
$V_{L,R}$  and  $g_{L,R}$   
left and right - handed vector and tensor couplings

$SM \Rightarrow V_L = V_{tb} \sim 1$

$V_R = g_L = g_R = 0$

Right-handed contribution?  
Tensor couplings?

## Angular observables to probe the Wtb vertex:



Nucl. Phys. B 840(2010)349

- For unpolarised top quark decays, the normal direction in the top RF is the one of the W boson
- For polarised (spin direction  $s_t$ ) top quark decays produced via electroweak interaction, further directions may be considered: N and T.

→ Three angular distributions:  $\theta_l^*$ (q,l),  $\theta_l^N$ (N,l) and  $\theta_l^T$ (T,l)

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_l^X} = \frac{3}{8} (1 + \cos \theta_l^X)^2 F_+^X + \frac{3}{8} (1 - \cos \theta_l^X)^2 F_-^X + \frac{3}{4} \sin^2 \theta_l^X F_0^X$$

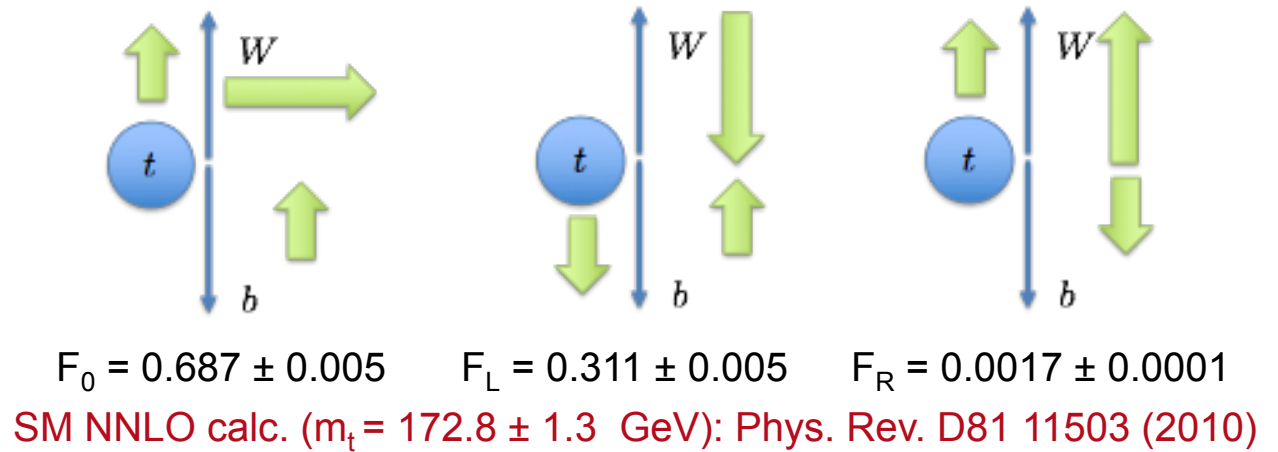
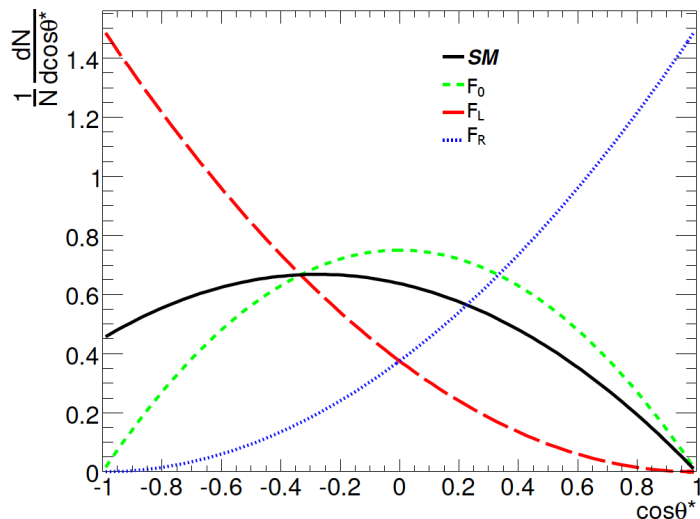
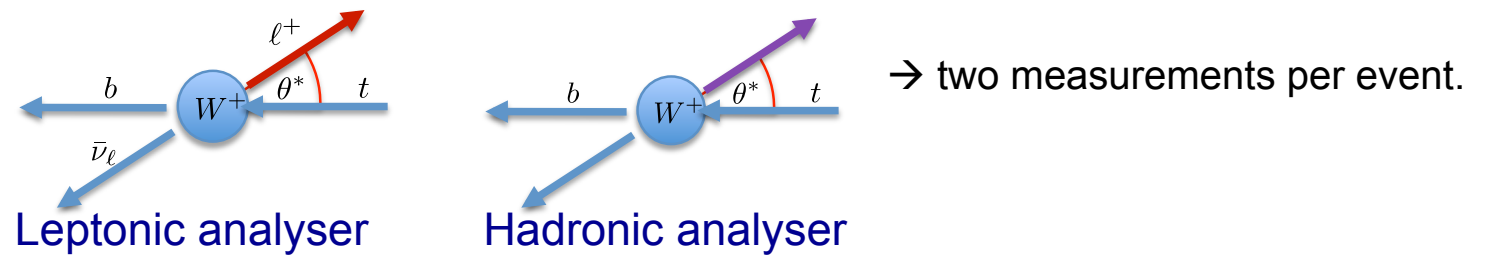
$$A_{FB}^X = \frac{N(\cos \theta_l^X > 0) - N(\cos \theta_l^X < 0)}{N(\cos \theta_l^X > 0) + N(\cos \theta_l^X < 0)} \propto (F_+^X - F_-^X)$$

More on this in EFT sessions  
later in the workshop.

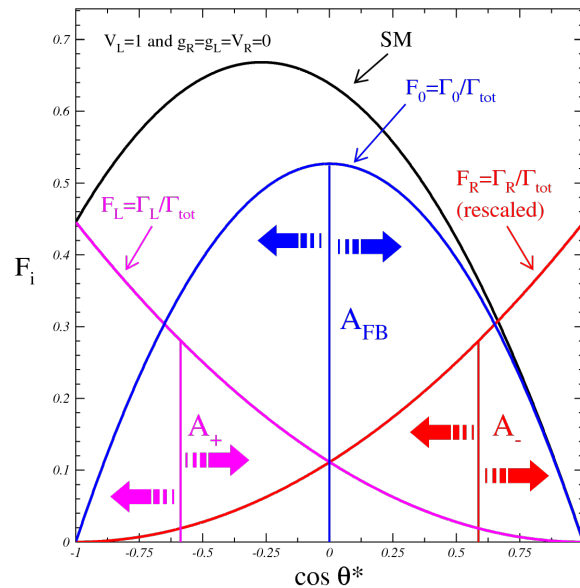
W bosons from top quark decays  $\rightarrow$  3 possible polarizations (helicity fractions): left-handed  $F_L$ , right-handed  $F_R$ , longitudinal  $F_0$

$$\frac{1}{\sigma} \frac{d\sigma}{d\cos\theta^*} = \frac{3}{4} (1 - \cos^2\theta^*) F_0 + \frac{3}{8} (1 - \cos\theta^*)^2 F_L + \frac{3}{8} (1 + \cos\theta^*)^2 F_R$$

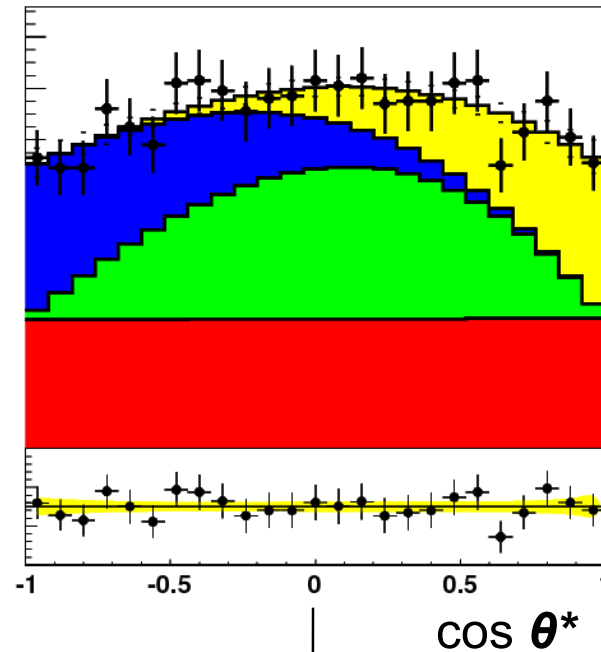
Sensitive observable:  $\cos\theta_i^*$  being  $\theta_i^*$  the angle between the down-type fermion (charged lepton or down-type quark) from the W boson decay and the reversed direction of the top quark, both in the W boson rest frame.



## Angular asymmetries

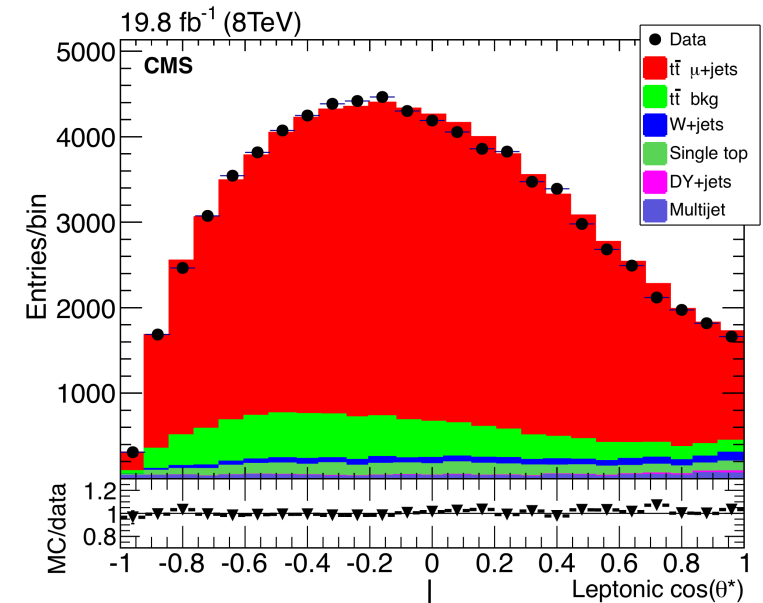


## Templates



Dedicated  $t\bar{t}$  signal templates for a specific  $F_i$  are created.  
 \* ATLAS 7 TeV:  
 dedicated  $F_0$ ,  $F_R$  &  $F_L$  MC samples at LO  
 \* ATLAS 8 TeV:  
 by reweighting MC SM  $t\bar{t}$  events

## Reweighting



The number of expected events in a given bin is modified by reweighting each event in that bin by a factor  $w$ .

## ATLAS+CMS Preliminary LHCTopWG Sept 2016

Theory (NNLO QCD)  
PRD 81 (2010) 111503 (R)

Data ( $F_R/F_L/F_0$ )

ATLAS 2010 single lepton,  $\sqrt{s}=7$  TeV,  $L_{int}=35$  pb<sup>-1</sup>  
ATLAS-CONF-2011-037

ATLAS 2011 single lepton and dilepton,  $\sqrt{s}=7$  TeV,  $L_{int}=1.04$  fb<sup>-1</sup>  
JHEP 1206 (2012) 088

CMS 2011 single lepton,  $\sqrt{s}=7$  TeV,  $L_{int}=2.2$  fb<sup>-1</sup> \*  
CMS-PAS-TOP-11-020

**LHC combination,  $\sqrt{s}=7$  TeV**  
ATLAS-CONF-2013-033, CMS-PAS-TOP-12-025

ATLAS 2012 single lepton,  $\sqrt{s}=8$  TeV,  $L_{int}=20.2$  fb<sup>-1</sup>  
Paper in preparation

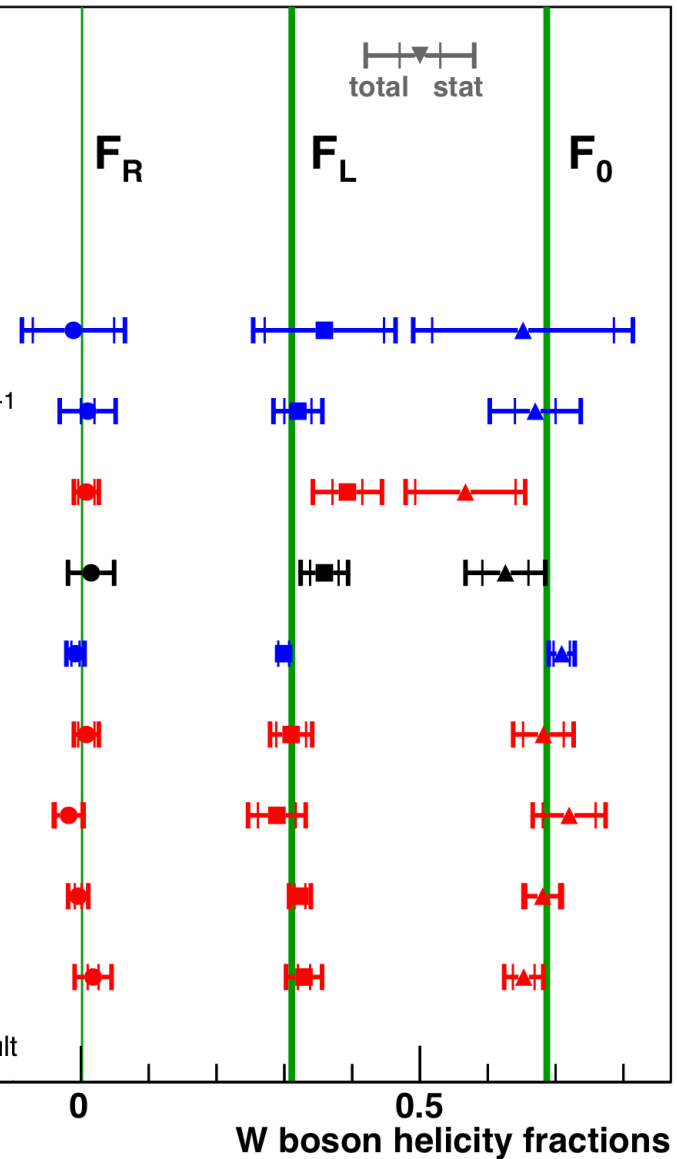
CMS 2011 single lepton,  $\sqrt{s}=7$  TeV,  $L_{int}=5.0$  fb<sup>-1</sup>  
JHEP 10 (2013) 167



CMS 2012 single top,  $\sqrt{s}=8$  TeV,  $L_{int}=19.7$  fb<sup>-1</sup>  
JHEP 01 (2015) 053

CMS 2012 single lepton,  $\sqrt{s}=8$  TeV,  $L_{int}=19.8$  fb<sup>-1</sup>  
arXiv:1605.09047 **PLB 762 (2016) 512-534**



CMS 2012 dilepton,  $\sqrt{s}=8$  TeV,  $L_{int}=19.7$  fb<sup>-1</sup>  
CMS-PAS-TOP-14-017

\* superseded by published result



	7 TeV	8 TeV
<b>ATLAS</b> 	<p><b>ttbar single lepton &amp; dilepton</b>  <b>1.04 fb<sup>-1</sup> [JHEP 1206 (2012) 088]</b>  <math>F_0 = 0.67 \pm 0.03</math> (stat.) <math>\pm 0.06</math> (syst.)  <math>F_L = 0.32 \pm 0.02</math> (stat.) <math>\pm 0.03</math> (syst.)  <math>F_R = 0.01 \pm 0.01</math> (stat.) <math>\pm 0.04</math> (syst.)</p>	<p><b>ttbar single lepton</b>  <b>20.2 fb<sup>-1</sup> [Paper in preparation]</b>  <math>F_0 = 0.709 \pm 0.012</math> (stat.*) <math>\pm 0.015</math> (syst.)  <math>F_L = 0.299 \pm 0.008</math> (stat.*) <math>\pm 0.013</math> (syst.)  <math>F_R = -0.008 \pm 0.006</math> (stat.*) <math>\pm 0.012</math> (syst.)</p>
<b>CMS</b> 	<p><b>ttbar single lepton</b>  <b>5.0 fb<sup>-1</sup> [JHEP 1310 (2013) 167]</b>  <math>F_0 = 0.682 \pm 0.030</math> (stat.) <math>\pm 0.033</math> (syst.)  <math>F_L = 0.310 \pm 0.022</math> (stat.) <math>\pm 0.022</math> (syst.)  <math>F_R = 0.008 \pm 0.012</math> (stat.) <math>\pm 0.014</math> (syst.)</p>	<p><b>ttbar single lepton</b>  <b>19.8 fb<sup>-1</sup> [PLB 762 (2016) 512-534]</b>  <math>F_0 = 0.681 \pm 0.012</math> (stat.) <math>\pm 0.023</math> (syst.)  <math>F_L = 0.323 \pm 0.008</math> (stat.) <math>\pm 0.014</math> (syst.)  <math>F_R = -0.004 \pm 0.005</math> (stat.) <math>\pm 0.014</math> (syst.)</p> <p><b>ttbar dilepton</b>  <b>19.7 fb<sup>-1</sup> [CMS-PAS-TOP-14-017]</b>  <math>F_0 = 0.653 \pm 0.016</math> (stat.) <math>\pm 0.024</math> (syst.)  <math>F_L = 0.329 \pm 0.009</math> (stat.) <math>\pm 0.025</math> (syst.)  <math>F_R = 0.018 \pm 0.008</math> (stat.) <math>\pm 0.026</math> (syst.)</p> <p><b>Single top</b>  <b>19.7 fb<sup>-1</sup> [JHEP 01 (2015) 053]</b>  <math>F_0 = 0.720 \pm 0.039</math> (stat.) <math>\pm 0.037</math> (syst.)  <math>F_L = 0.298 \pm 0.028</math> (stat.) <math>\pm 0.032</math> (syst.)  <math>F_R = -0.018 \pm 0.019</math> (stat.) <math>\pm 0.011</math> (syst.)</p>



	7 TeV	8 TeV
<b>ATLAS</b> 	<b>ttbar single lepton &amp; dilepton</b> <b>1.04 fb<sup>-1</sup> [JHEP 1206 (2012) 088]</b> $F_0 = 0.67 \pm 0.03$ (stat.) $\pm 0.06$ (syst.) $F_L = 0.32 \pm 0.02$ (stat.) $\pm 0.03$ (syst.) $F_R = 0.01 \pm 0.01$ (stat.) $\pm 0.04$ (syst.)	<div style="border: 2px solid blue; border-radius: 15px; padding: 10px;"> <b>ttbar single lepton</b>  <b>20.2 fb<sup>-1</sup> [Paper in preparation]</b>  <math>F_0 = 0.709 \pm 0.012</math> (stat.*) <math>\pm 0.015</math> (syst.)  <math>F_L = 0.299 \pm 0.008</math> (stat.*) <math>\pm 0.013</math> (syst.)  <math>F_R = -0.008 \pm 0.006</math> (stat.*) <math>\pm 0.012</math> (syst.)                     </div>
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## Event selection

- Single lepton triggers
- Exactly one lepton (e/μ) with  $p_T > 25$  GeV and  $|\eta| < 2.5$
- $\geq 4$  jets with  $p_T > 25$  GeV and  $|\eta| < 2.5$ 
  - $\geq 1$  b-tagged
- $E_T^{\text{miss}} > 20$  GeV and  $E_T^{\text{miss}} + m_T^W > 60$  GeV for  $N_{\text{b-tag}} = 1$
- Cut on likelihood of reconstruction algorithm:  $\text{Log } \mathcal{L} > -48$

## Event reconstruction

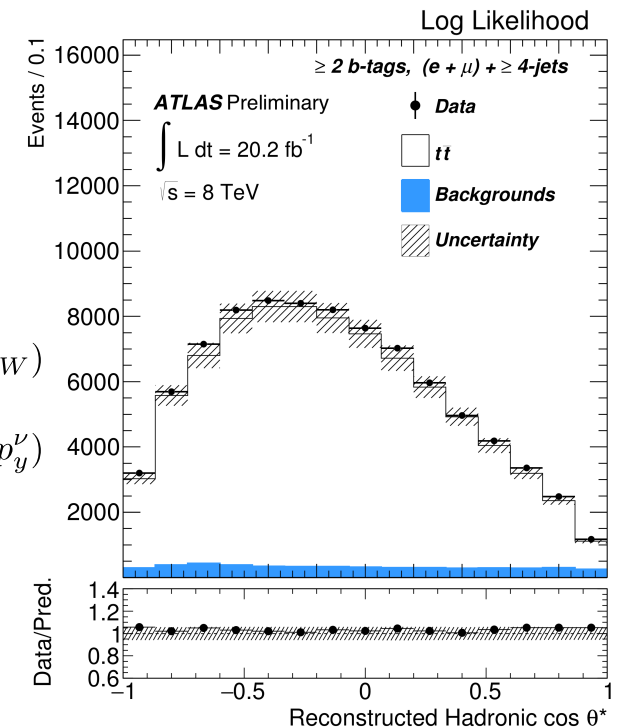
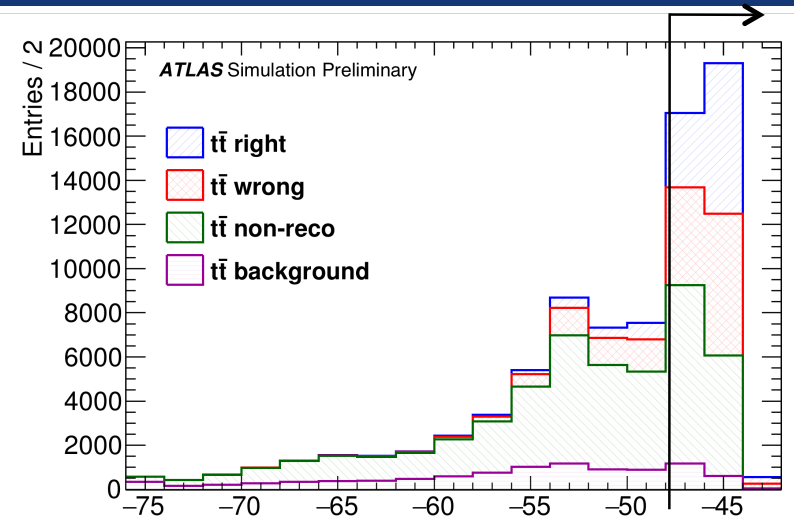
using an “extended kinematic likelihood fit” with KLFFitter (referred to as “normalized event probability  $p_i$ ”) including  $p_T$  and  $b$ -tag weight of jets (for up/down-type quark separation):

- Optimized jet feeding:
- .2 jets with highest  $b$ -tag weight
  - .2/3 further jets with highest  $p_T$
  - .Best of 5! = 120 (24 for  $n_{\text{jet}} = 4$ ) permutations is selected

$$\mathcal{L} = BW(m_{q_1 q_2 q_3} | m_t, \Gamma_t) \cdot BW(m_{q_1 q_2} | m_W, \Gamma_W) \cdot BW(m_{q_4 \ell \nu} | m_t, \Gamma_t) \cdot BW(m_{\ell \nu} | m_W, \Gamma_W) \\ \cdot \prod_{i=1}^4 W_{\text{jet}}(E_i^{\text{meas}} | E_i) \cdot W_{\ell}(E_{\ell}^{\text{meas}} | E_{\ell}) \cdot W_{\text{miss}}(E_x^{\text{miss}} | p_x^{\nu}) \cdot W_{\text{miss}}(E_y^{\text{miss}} | p_y^{\nu})$$

$$p_i = \frac{\mathcal{L}_i \prod_j \Delta p_{i,j}}{\sum_i \mathcal{L}_i \prod_j \Delta p_{i,j}}$$

→ leptonic analyzer  
→ hadronic analyzer





## Template fit method (using reweighting)

- Signal templates (3: one for each helicity state)  
No dedicated  $F_i$  simulated samples available.  
Instead, **reweighting SM  $t\bar{t}$ bar sample using analytic expression.**
- Background templates (5: W+light, c, bb/cc jets, QCD, rem.bkg.)

- Binned likelihood fit:

$$\mathcal{L} = \prod_{k=1}^{N_{\text{bins}}} \text{Poisson}(n_{\text{data},k}, n_{\text{exp},k}) \prod_{j=1}^{N_{\text{bkg}}} \frac{1}{\sqrt{2\pi}\sigma_{\text{bkg},j}} \exp\left(-\frac{(n_{\text{bkg},j} - \hat{n}_{\text{bkg},j})^2}{2\sigma_{\text{bkg},j}^2}\right)$$

$$n_{\text{exp}} = n_0 + n_L + n_R + n_{W+\text{light}} + n_{W+c} + n_{W+bb/cc} + n_{\text{fake}} + n_{\text{rem. bkg.}}$$

- Fit parameters:

Yields of signal ( $n_0, n_L, n_R$ ) and backgrounds (W+jets, fakes, rem.bkg.)

allowed to float within their norm. unc.

Background	Norm. unc.
W + light jets	5 %
W + c	25 %
W + cc/bb	7 %
Fake leptons	30 %
Remaining background (Single top, Z+jets, VV)	16 % / 17 % ( $\geq 2b, \geq 1b$ )

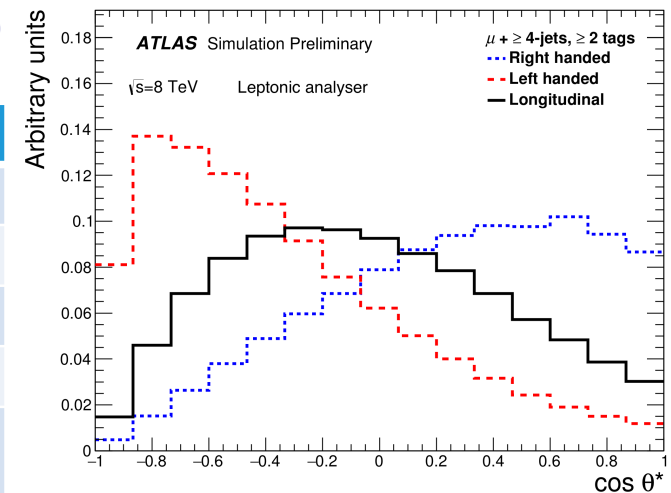
- Fractions are extracted as:

$$F_i = \frac{N_i}{N_0 + N_L + N_R}, \quad n_i = \epsilon_i^{\text{sel}} N_i \quad \text{for } i=0, L, R.$$

$$W_L = \frac{\frac{3}{8}(1 - \cos\theta_{\text{gen}}^*)^2}{f_L \cdot \frac{3}{8}(1 - \cos\theta_{\text{gen}}^*)^2 + f_0 \cdot \frac{3}{4}(1 - \cos^2\theta_{\text{gen}}^*) + f_R \cdot \frac{3}{8}(1 + \cos\theta_{\text{gen}}^*)^2}$$

$$W_0 = \frac{\frac{3}{4}(1 - \cos^2\theta_{\text{gen}}^*)}{f_L \cdot \frac{3}{8}(1 - \cos\theta_{\text{gen}}^*)^2 + f_0 \cdot \frac{3}{4}(1 - \cos^2\theta_{\text{gen}}^*) + f_R \cdot \frac{3}{8}(1 + \cos\theta_{\text{gen}}^*)^2}$$

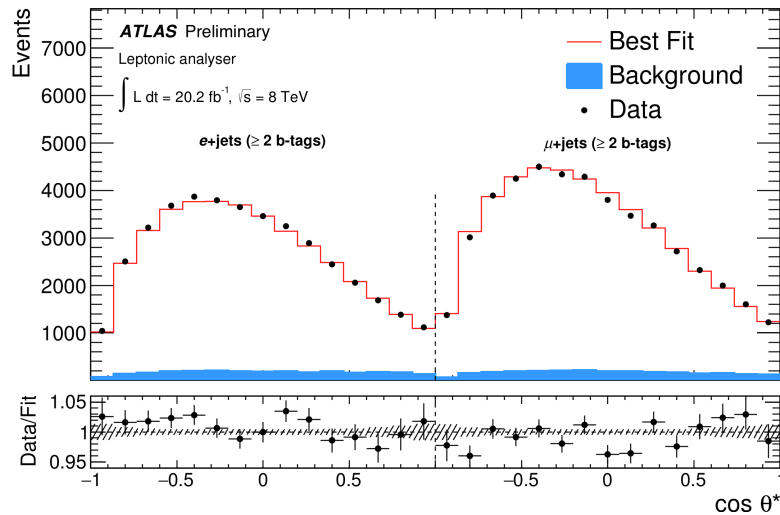
$$W_R = \frac{\frac{3}{8}(1 + \cos\theta_{\text{gen}}^*)^2}{f_L \cdot \frac{3}{8}(1 - \cos\theta_{\text{gen}}^*)^2 + f_0 \cdot \frac{3}{4}(1 - \cos^2\theta_{\text{gen}}^*) + f_R \cdot \frac{3}{8}(1 + \cos\theta_{\text{gen}}^*)^2}$$



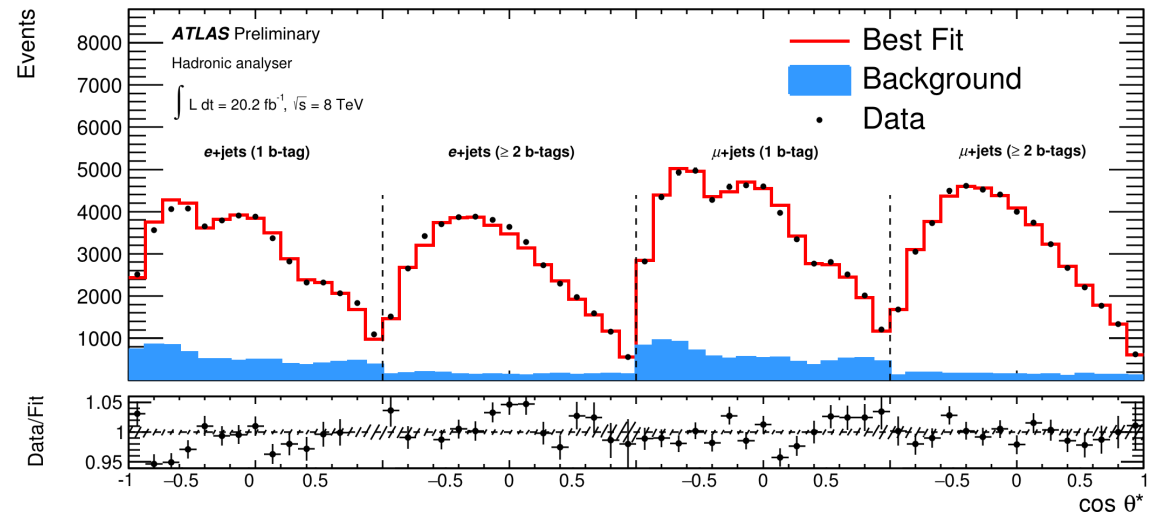
## Results

- In total, 8 orthogonal channels; all possible combinations studied.
- Channel combination using simultaneous fit on the “glued-templates” (more bins).
- Best results obtained for each analyzer:
  - . Leptonic:  $[e + \mu] \times [\geq 2b]$  → **most sensitive / best result**
  - . Hadronic:  $[e + \mu] \times [1b + \geq 2b]$
  - . Overall best combination: same as leptonic
  - . Main syst. unc.: jet energy scale and resolution, ttbar modelling

### [Leptonic analyzer] x $[e + \mu] \times [\geq 2b]$



### [Hadronic analyzer] x $[e + \mu] \times [1b + \geq 2b]$



$$F_0 = 0.709 \pm 0.012 \text{ (stat.+bkg.norm)} \pm 0.015 \text{ (syst.)}$$

$$F_L = 0.299 \pm 0.008 \text{ (stat.+bkg.norm)} \pm 0.013 \text{ (syst.)}$$

$$F_R = -0.008 \pm 0.006 \text{ (stat.+bkg.norm)} \pm 0.012 \text{ (syst.)}$$

$$F_0 = 0.659 \pm 0.010 \text{ (stat.+bkg.norm)} \pm 0.053 \text{ (syst.)}$$

$$F_L = 0.281 \pm 0.021 \text{ (stat.+bkg.norm)} \pm 0.065 \text{ (syst.)}$$

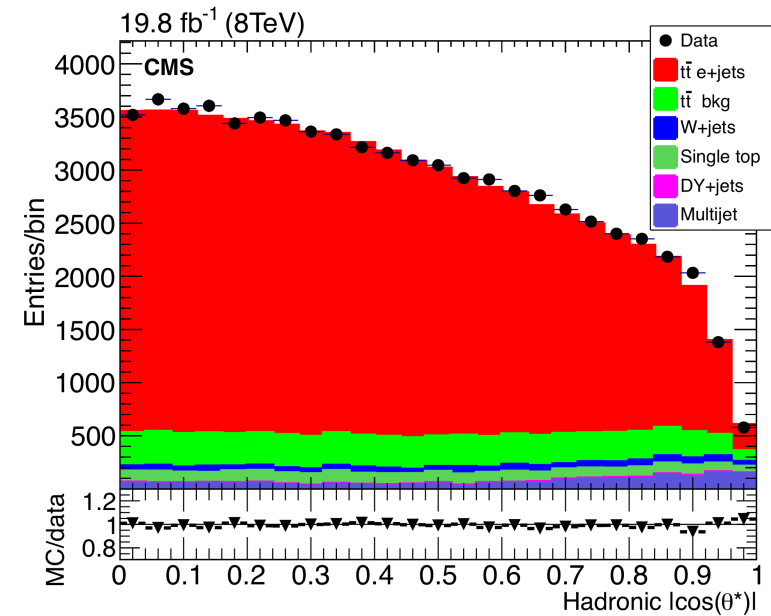
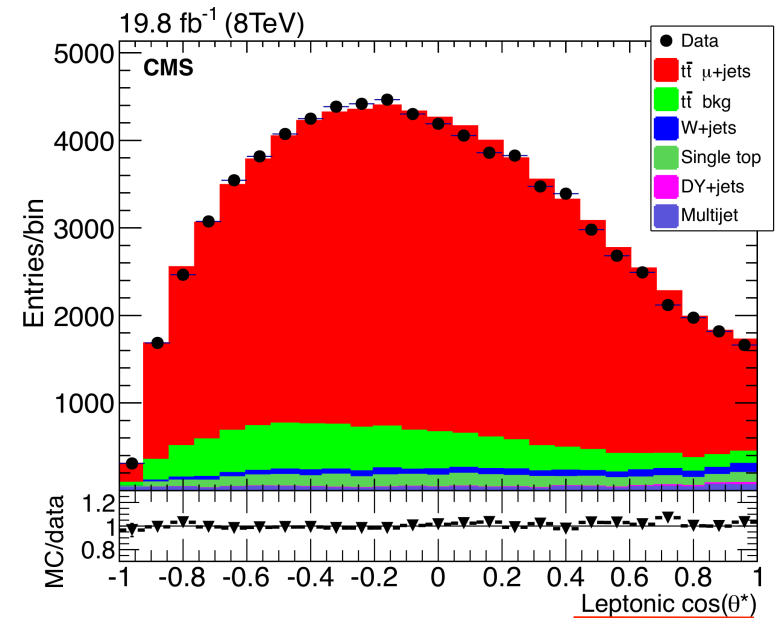
$$F_R = 0.061 \pm 0.022 \text{ (stat.+bkg.norm)} \pm 0.105 \text{ (syst.)}$$

## Event selection

- Single lepton triggers
- Exactly one lepton (e/μ) with  $p_T > 30/26$  GeV and  $|\eta| < 2.5/2.1$
- At least 4 jets with  $|\eta| < 2.4$ 
  - increased  $p_T$  cut for first 4 jets: 55, 45, 25 and 20 GeV
  - at least two of them b-tagged (with  $p_T > 20$  GeV)
- Cut on  $m_T^W$ :  $30 < m_T^W < 200$  GeV

## Event reconstruction

- using a kinematic fit:
  - $p_z^v$  determination using top & W masses constraints
  - jets and lepton momentum resolution taken into account
- Final sample composition: 82% (e/μ+jets), 10% (other ttbar decays, with  $\tau$ ), 3.5% (single top), rest (other bkgs.)
- Build  $\cos\theta_l^*$  for the leptonic analyzer  
(for illustration, absolute value for hadronic analyzer also shown).



## Reweighting method & binned likelihood fit

- Binned likelihood fit:

$$\mathcal{L}(\vec{F}) = \prod_i \frac{N_{MC}(i; \vec{F})^{N_{data}(i)}}{[N_{data}(i)]!} \exp[-N_{MC}(i; \vec{F})]$$

- Fit parameters:  $F_{tt}$ ,  $F_0$ ,  $F_L$  ( $F_R=1-F_0-F_L$ )
- Background normalisation is fixed (its uncertainty is included as syst. unc.)

$$w_{lep/had/single-t}(\cos \theta_{gen}^*; \vec{F}) \equiv \left[ \begin{aligned} & \frac{3}{8} F_L (1 - \cos \theta_{gen}^*)^2 \\ & + \frac{3}{4} F_0 \sin^2 \theta_{gen}^* \\ & + \frac{3}{8} F_R (1 + \cos \theta_{gen}^*)^2 \end{aligned} \right] / \left[ \begin{aligned} & \frac{3}{8} F_L^{SM} (1 - \cos \theta_{gen}^*)^2 \\ & + \frac{3}{4} F_0^{SM} \sin^2 \theta_{gen}^* \\ & + \frac{3}{8} F_R^{SM} (1 + \cos \theta_{gen}^*)^2 \end{aligned} \right],$$

$$N_{MC}(i; \vec{F}) = N_{t\bar{t}}(i; \vec{F}) + N_{single-t}(i; \vec{F}) + N_{W+jets}(i) + N_{DY+jets}(i) + N_{multijet}(i),$$

where

$$N_{t\bar{t}}(i; \vec{F}) = \mathcal{F}_{t\bar{t}} \left[ \sum_{t\bar{t} \text{ events in bin } i} \frac{w_{lep}(\cos \theta_{gen}^*; \vec{F})}{w_{had}(\cos \theta_{gen}^*; \vec{F})} \right],$$

$$N_{single-t}(i; \vec{F}) = \sum_{single-t \text{ events in bin } i} w_{single-t}(\cos \theta_{gen}^*; \vec{F})$$

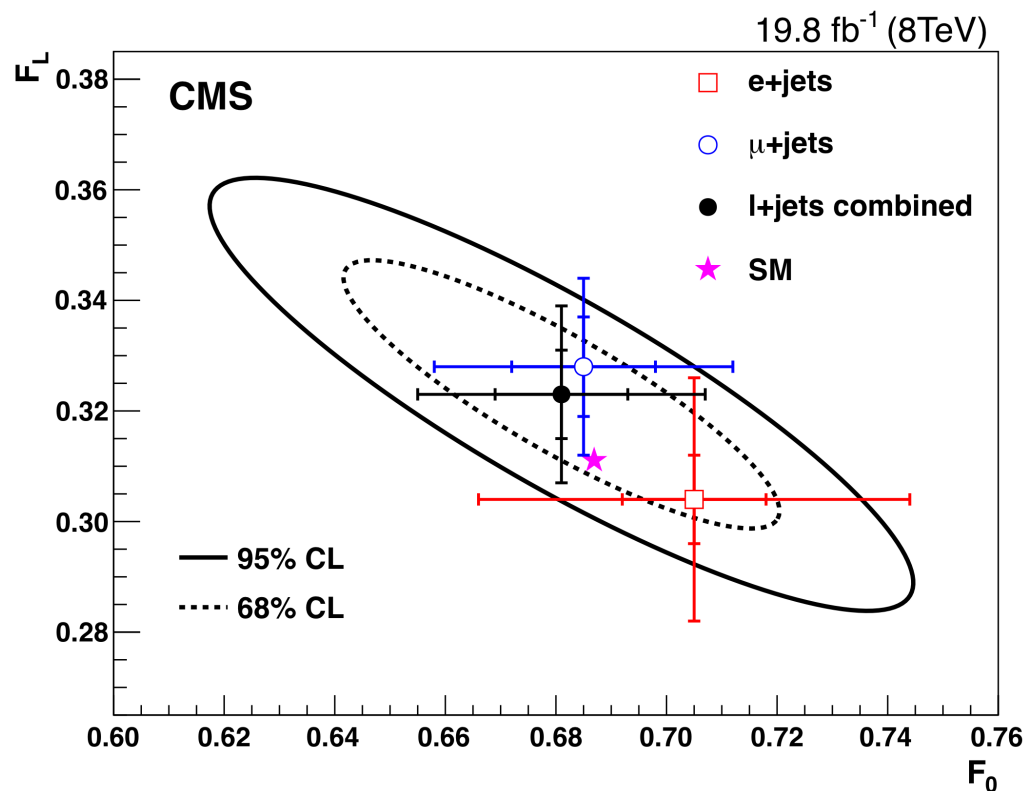
Background	Norm. unc.
Z + jets	±30 %
W + light jets	±30 %
W + heavy flavour	+100% / -50 %
Fake leptons	±50% (e), <sup>+40%</sup> <sub>-50%</sub> (μ)
Single top	±30 %

## Results

- Electron & muon channel are combined using BLUE.

Channel	$F_0 \pm (\text{stat}) \pm (\text{syst})$	$F_L \pm (\text{stat}) \pm (\text{syst})$	$F_R \pm (\text{stat}) \pm (\text{syst})$	Stat.correlation
				$\rho_{0,L}$
e + jets	$0.705 \pm 0.013 \pm 0.037$	$0.304 \pm 0.009 \pm 0.020$	$-0.009 \pm 0.005 \pm 0.021$	-0.950
$\mu$ + jets	$0.685 \pm 0.013 \pm 0.024$	$0.328 \pm 0.009 \pm 0.014$	$-0.013 \pm 0.005 \pm 0.017$	-0.957
$\ell$ + jets	$0.681 \pm 0.012 \pm 0.023$	$0.323 \pm 0.008 \pm 0.014$	$-0.004 \pm 0.005 \pm 0.014$	-0.959

with syst.  $\rho_{0,L} = -0.87$



## Systematic uncertainties

Main syst. unc.	$\Delta F_0$	$\Delta F_L$
Jet energy scale	0.005	0.003
W+jets bkg.	0.007	0.001
Fake leptons bkg.	0.008	0.001
top quark mass	0.010*	0.007*
tt ME scales	0.012*	0.007*
tt PS scale	0.009*	0.007*
tt ME, PS & hadr. MC	0.006	0.004
Total	0.023	0.014

\* Stat. precision of the limited sample size is assigned as syst. variation.



Start with the combination in the single lepton channel.

- Both analyses use the same sensitive variable and channel: **leptonic analyzer with  $\geq 2b$  jets**.
- Central values are quite close.
- Both comparable within the uncertainties with the SM predictions.
- Differences in the treatment and list of syst. unc.  $\rightarrow$  differences in correlations btw. fractions and size of the uncertainties.
- Syst. uncertainty for ATLAS is smaller.



## ttbar single lepton

**20.2 fb<sup>-1</sup> [Paper in preparation]**

$$F_0 = 0.709 \pm 0.012 \text{ (stat.+bkg.norm.)} \pm 0.015 \text{ (syst.)}$$

$$F_L = 0.299 \pm 0.008 \text{ (stat.+bkg.norm.)} \pm 0.013 \text{ (syst.)}$$

$$F_R = -0.008 \pm 0.006 \text{ (stat.+bkg.norm.)} \pm 0.012 \text{ (syst.)}$$

$$\rho_{0,L} = -0.55, \rho_{0,R} = -0.75, \rho_{L,R} = +0.16$$

NNLO QCD calculation  
Phys.Rev.D81:111503,2010

$$F_0 = 0.687 \pm 0.005$$

$$F_L = 0.311 \pm 0.005$$

$$F_R = 0.0017 \pm 0.0001$$



## ttbar single lepton

**19.6 fb<sup>-1</sup> [PLB 762, 2016] 512-534**

$$F_0 = 0.681 \pm 0.012 \text{ (stat.)} \pm 0.023 \text{ (syst.)}$$

$$F_L = 0.323 \pm 0.008 \text{ (stat.)} \pm 0.014 \text{ (syst.)}$$

$$F_R = -0.004 \pm 0.005 \text{ (stat.)} \pm 0.014 \text{ (syst.)}$$

$$\rho_{0,L} = -0.87$$



## ATLAS

- e/μ channel combination using simultaneous fit on the “glued-templates” (more bins).
- Bkg. normalisations: free floating parameters in the fit (unc. in table below).
- Syst. unc. estimated using ensemble tests: repeat fit using nominal templates and syst. varied pseudo-data.

- Some differences in list of MC samples and syst. unc.

\* ttbar signal modelling → ATLAS: Powheg(NLO)+Py6, CMS: MG5 (LO≤3p)+Py6

\* bkg. norm. unc.

\* jet vertex fraction (to suppress pile-up jets), jet reco. eff.



Background	Norm. unc.
W + light jets	5 %
W + c	25 %
W + cc/bb	7 %
Fake leptons	30 %
Remaining background (Single top, Z+jets, VV)	16 % / 17 % (≥ 2b, ≥1b)

## CMS

- Reweighting also for single top quark events.
- e/μ channel combination with BLUE.
- Bkg. normalisations are fixed in the fit.
- Syst. effects\* estimated changing the signal and bkg. templates and fitting to (nominal) data.



Background	Norm. unc.
Z + jets	±30 %
W + light jets	±30 %
W + heavy flavour	+100% / -50 %
Fake leptons	±50% (e), <sup>+40%</sup> <sub>-50%</sub> (μ)
Single top	±30 %

\* Stat. precision of the limited sample size is assigned as syst. variation if it is larger than the latter.



Source	ATLAS		CMS	
	F <sub>0</sub>	F <sub>L</sub>	F <sub>0</sub>	F <sub>L</sub>
<b>Reconstructed objects</b>				
Jet energy scale	+0.0063 / -0.0033	+0.0028 / -0.0025	±0.005	±0.003
Jet energy resolution	+0.0062 / -0.0059	+0.0048 / -0.0018	±0.003	±0.003
<i>b</i> -tagging efficiency	+0.0017 / -0.0021	+0.0012 / -0.0013	±0.001	<0.001
Electron/Muon efficiency	+0.0028 / -0.0030 +0.0024 / -0.0029	+0.0018 / -0.0020 +0.0013 / -0.0015	±0.001	±0.001
Jet vertex fraction	+0.0036 / -0.0017	+0.0019 / -0.0013	--	--
Jet reconstruction efficiency	+0.0002 / -0.0002	<0.0001 / <0.0001	--	--
<b>Signal modelling</b>				
Top quark mass	±0.0017	±0.0050	±0.010*	±0.007*
Showering & hadronisation	±0.0019 (P+P6 vs. P+HW)	±0.0019	±0.006	±0.004
ME generator	±0.0025 (P+HW vs. MC@NLO+HW)	±0.0032	(MG5+Py6 vs. MC@NLO+HW)	
PDF	±0.0033	±0.0042	±0.002	±0.001
ISR/FSR (PP6 with varied h <sub>damp</sub> , μ <sub>R</sub> & μ <sub>F</sub> , P2012 tune)	±0.0033	±0.0058	--	--
μ <sub>R</sub> & μ <sub>F</sub> scales (MG5 LO)	--	--	±0.012*	±0.007*
Matching scale (MG5+Py6)	--	--	±0.009*	±0.007*
<b>Method uncertainty</b>				
MC statistics	±0.0091	±0.0056	±0.002	±0.001
<b>Total systematics</b>	+0.015 / -0.014	+0.013 / -0.012	±0.023** (w. bkg. norm.) ±0.020 (wo. bkg. norm.)	±0.014** (w. bkg. norm.) ±0.014 (wo. bkg. norm.)
<b>2 Stat. + bkg. norm.</b>	±0.012	±0.008	±0.012** (stat.) ±0.016 (stat.+bkg.norm)	±0.008** (stat.) ±0.008 (stat.+bkg.norm)

# Limits on anomalous couplings



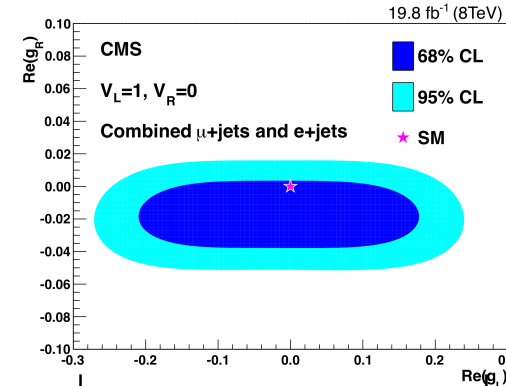
$$\begin{aligned}
 F_0 &= 0.709 \pm 0.012 \text{ (stat.+bkg.norm)} \pm 0.015 \text{ (syst.)} \\
 F_L &= 0.299 \pm 0.008 \text{ (stat.+bkg.norm)} \pm 0.013 \text{ (syst.)} \\
 F_R &= -0.008 \pm 0.006 \text{ (stat.+bkg.norm)} \pm 0.012 \text{ (syst.)}
 \end{aligned}$$

$$\rho_{0,L} = -0.55, \rho_{0,R} = -0.75, \rho_{L,R} = +0.16$$

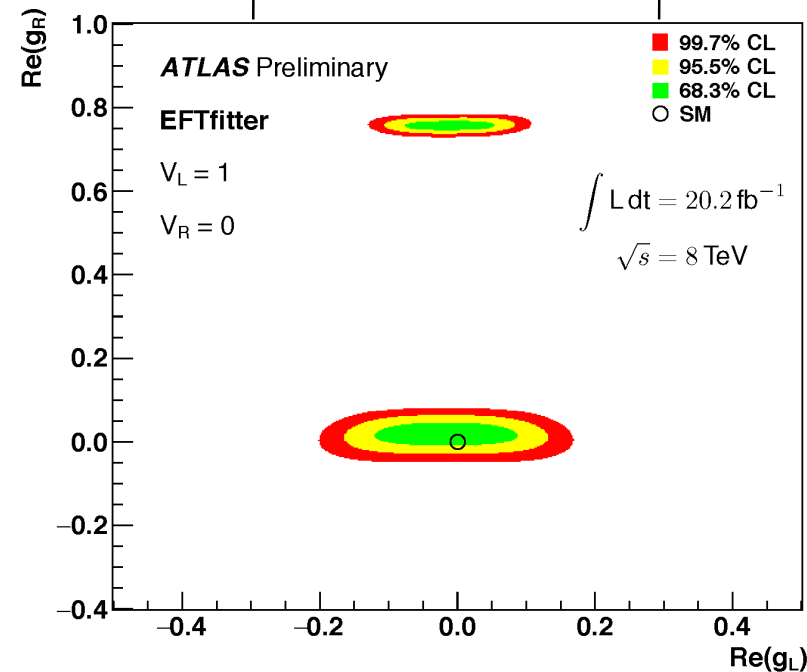
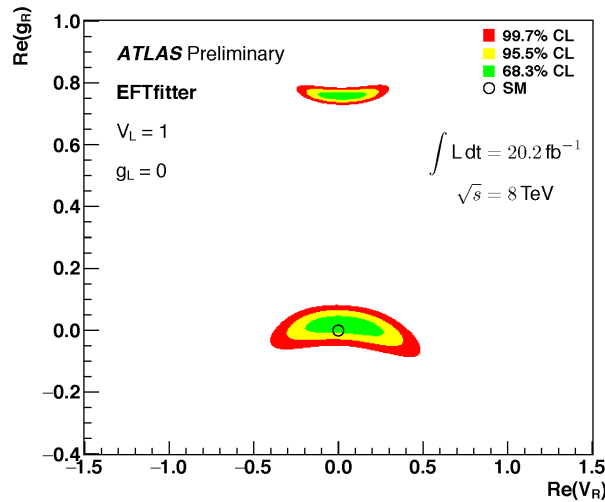


$$\begin{aligned}
 F_0 &= 0.681 \pm 0.012 \text{ (stat.)} \pm 0.023 \text{ (syst.)} \\
 F_L &= 0.323 \pm 0.008 \text{ (stat.)} \pm 0.014 \text{ (syst.)} \\
 F_R &= -0.004 \pm 0.005 \text{ (stat.)} \pm 0.014 \text{ (syst.)}
 \end{aligned}$$

$$\rho_{0,L} = -0.87$$



Coupling	95% CL limit
$V_R$	[-0.24, 0.31]
$g_L$	[-0.14, 0.11]
$g_R$	[-0.02, 0.06], [0.74, 0.78]



- Both ATLAS and CMS have new results in  $t\bar{t}$  lepton+jets using leptonic analyzer  
→ combination exercise could be started soon (person power?)
- Both comparable within the uncertainties with the SM predictions.
- Differences in strategy, correlations btw. fractions and size of the uncertainties:

### ATLAS

- $e/\mu$  channel combination using simultaneous fit on the “glued-templates” (more bins).
- Bkg. norm.: free floating parameters in the fit
  - Differences in estimation of syst. unc.:
    - \* strategy
    - \*  $t\bar{t}$  signal modelling
    - \* bkg. normalisation uncertainties
    - \* jet vertex fraction (to suppress pile-up jets), jet reco. eff.

### CMS

- Reweighting also for single top quark events.
- $e/\mu$  channel combination with BLUE.
- Bkg. normalisations are fixed in the fit.



# BACK-UP



Process	MC sample (ME+PS)	Normalisation
tt	Powheg (NLO, CT10 PDF)+Pythia6	NNLO+NNLL
Single top	Powheg (NLO, CT10 PDF)+Pythia6	aNNLO
W+jets	Alpgen (LO multileg $\leq 5p$ , CTEQ6L1 PDF) + Pythia6	Data-driven: ttbar charge asym. K_light = 0.80 +- 0.04 (5%) K_c = 1.07 +- 0.27 (25%) K_bb/K_cc = 1.50 +- 0.11 (7%)
Z+jets	Alpgen (LO multileg $\leq 5p$ , CTEQ6L1 PDF) + Pythia6	NNLO
Dibosons	Sherpa (LO multileg $\leq 3p$ , CT10 PDF) + Sherpa	NLO
Fake leptons	----	Data-driven: matrix method

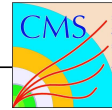


Process	MC sample (ME+PS)	Normalisation
tt	MadGraph (LO multileg $\leq 3p$ , CTEQ6L1 PDF) +Pythia6	NNLO+NNLL
Single top	Powheg (NLO, CTEQ6M PDF)+Pythia6	aNNLO
W+jets	MadGraph (LO multileg $\leq ?p$ , CTEQ6L1 PDF) +Pythia6	NNLO
Z+jets	MadGraph (LO multileg $\leq ?p$ , CTEQ6L1 PDF) +Pythia6	NNLO
Fake leptons	Pythia6	Data-driven



## Uncertainties

Source	Leptonic analyzer $\geq 2$ b-tags		
	$F_0$	$F_L$	$F_R$
<b>Reconstructed objects</b>			
Jet energy scale	+0.0063 / -0.0033	+0.0028 / -0.0025	+0.0037 / -0.0014
Jet energy reso.	+0.0062 / -0.0059	+0.0048 / -0.0018	+0.0071 / -0.0067
$b$ tagging eff.	+0.0017 / -0.0021	+0.0012 / -0.0013	+0.0011 / -0.0012
Ele/Muon eff	+0.0028 / -0.0030 +0.0024 / -0.0029	+0.0018 / -0.0020 +0.0013 / -0.0015	+0.0011 / -0.0011 +0.0010 / -0.0015
Jet vertex fraction	+0.0036 / -0.0017	+0.0019 / -0.0013	+0.0017 / -0.0006
Jet reco. Eff.	+0.0002 / -0.0002	<0.0001 / <0.0001	+0.0002 / -0.0002
<b>Signal modelling</b>			
Top quark mass	$\pm 0.0017$	$\pm 0.0050$	$\pm 0.0033$
PS & Hadr.	$\pm 0.0019$	$\pm 0.0019$	$\pm 0.0037$
ME generator	$\pm 0.0025$	$\pm 0.0032$	$\pm 0.0057$
ISR/FSR	$\pm 0.0033$	$\pm 0.0058$	$\pm 0.0034$
PDF	$\pm 0.0033$	$\pm 0.0042$	$\pm 0.0009$
<b>Method uncertainty</b>			
Template statistics	$\pm 0.0091$	$\pm 0.0056$	$\pm 0.0044$
<b>Total systematics</b>	+0.015 / -0.014	+0.013 / -0.012	+0.013 / -0.012
<b>Stat. + bkg. norm.</b>	$\pm 0.012$	$\pm 0.008$	$\pm 0.006$



	$\ell + \text{jets}$	
	$\pm \Delta F_0$	$\pm \Delta F_L$
JES	0.005	0.003
JER	0.003	0.003
$b$ tagging eff.	0.001	$< 10^{-3}$
Lepton eff.	0.001	0.001
Single top normal	0.003	0.001
W + jets bkg.	0.007	0.001
DY + jets bkg.	0.001	$< 10^{-3}$
Multijet bkg.	0.008	0.001
Pileup	0.001	$< 10^{-3}$
Top quark mass	0.010	0.007
$t\bar{t}$ scales	0.012	0.007
$t\bar{t}$ match. scale	0.009	0.007
$t\bar{t}$ MC and hadron	0.006	0.004
$t\bar{t}$ $p_T$ reweight	$< 10^{-3}$	0.002
Limited MC size	0.002	0.001
PDF	0.002	0.001
<b>Total</b>	<b>0.023</b>	<b>0.014</b>



## Systematic unc.

- using ensemble tests
- pseudo-data for each systematic variation
- repeat fit using nominal templates and syst. varied pseudodata
- bkg. norm. directly evaluated in the fit

Uncertainties						
Source	Leptonic analyzer $\geq 2$ b-tags			Hadronic analyzer $1 b + \geq 2$ b-tags		
	$F_0$	$F_L$	$F_R$	$F_0$	$F_L$	$F_R$
Reconstructed objects						
Jet energy scale	+0.0063 / -0.0033	+0.0028 / -0.0025	+0.0037 / -0.0014	+0.0069 / -0.0070	+0.012 / -0.008	+0.014 / -0.005
Jet energy reso.	+0.0062 / -0.0059	+0.0048 / -0.0018	+0.0071 / -0.0067	+0.027 / -0.031	+0.033 / -0.041	+0.057 / -0.071
$b$ tagging eff.	+0.0017 / -0.0021	+0.0012 / -0.0013	+0.0011 / -0.0012	+0.029 / -0.031	+0.013 / -0.014	+0.034 / -0.035
Ele/Muon eff	+0.0028 / -0.0030 +0.0024 / -0.0029	+0.0018 / -0.0020 +0.0013 / -0.0015	+0.0011 / -0.0011 +0.0010 / -0.0015	+0.0025 / -0.0021 +0.0026 / -0.0037	+0.0028 / -0.0038 +0.0046 / -0.0035	+0.0051 / -0.0058 +0.0072 / -0.0072
Jet vertex fraction	+0.0036 / -0.0017	+0.0019 / -0.0013	+0.0017 / -0.0006	+0.013 / -0.009	+0.0012 / -0.0046	+0.011 / -0.005
Jet reco. Eff.	+0.0002 / -0.0002	<0.0001 / <0.0001	+0.0002 / -0.0002	+0.0008 / -0.0008	+0.0004 / -0.0004	+0.0011 / -0.0011
Signal modelling						
Top quark mass	$\pm 0.0017$	$\pm 0.0050$	$\pm 0.0033$	$\pm 0.0033$	$\pm 0.0100$	$\pm 0.0068$
PS & Hadr.	$\pm 0.0019$	$\pm 0.0019$	$\pm 0.0037$	$\pm 0.015$	$\pm 0.001$	$\pm 0.014$
ME generator	$\pm 0.0025$	$\pm 0.0032$	$\pm 0.0057$	$\pm 0.016$	$\pm 0.024$	$\pm 0.040$
ISR/FSR	$\pm 0.0033$	$\pm 0.0058$	$\pm 0.0034$	$\pm 0.018$	$\pm 0.039$	$\pm 0.057$
PDF	$\pm 0.0033$	$\pm 0.0042$	$\pm 0.0009$	$\pm 0.0010$	$\pm 0.0020$	$\pm 0.0020$
Method uncertainty						
Template statistics	$\pm 0.0091$	$\pm 0.0056$	$\pm 0.0044$	$\pm 0.0076$	$\pm 0.0016$	$\pm 0.0016$
<b>Total systematics</b>	<b>+0.015 / -0.014</b>	<b>+0.013 / -0.012</b>	<b>+0.013 / -0.012</b>	<b>+0.052 / -0.054</b>	<b>+0.063 / -0.067</b>	<b>+0.100 / -0.110</b>
<b>Stat. + bkg. norm.</b>	<b><math>\pm 0.012</math></b>	<b><math>\pm 0.008</math></b>	<b><math>\pm 0.006</math></b>	<b><math>\pm 0.010</math></b>	<b><math>\pm 0.021</math></b>	<b><math>\pm 0.022</math></b>



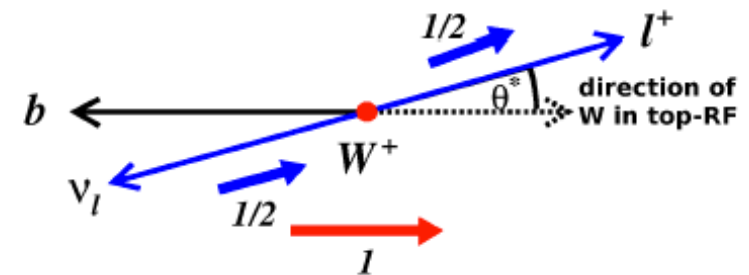
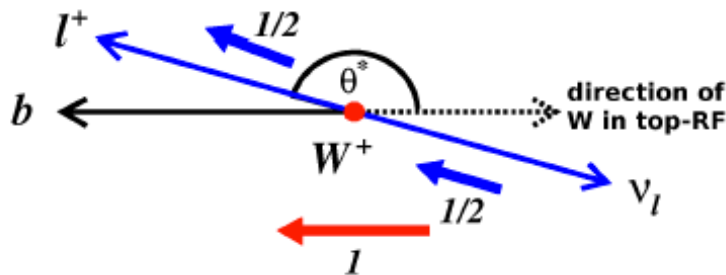
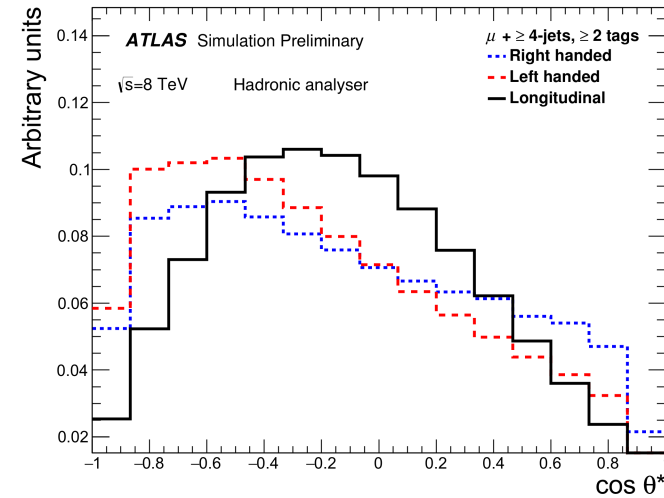
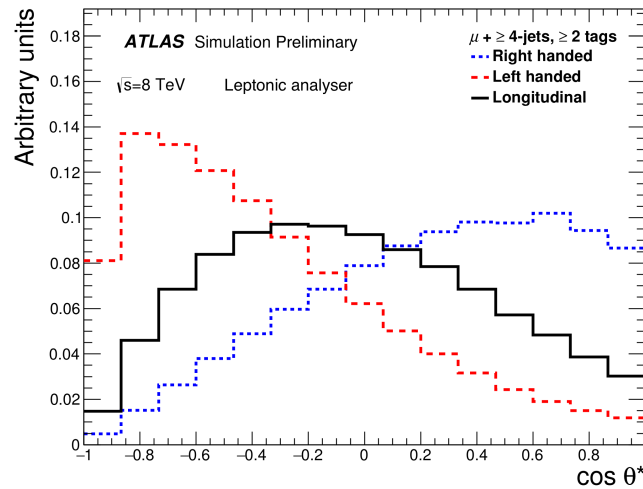
## Systematic uncertainties

	e + jets		$\mu$ + jets		$\ell$ + jets	
	$\pm\Delta F_0$	$\pm\Delta F_L$	$\pm\Delta F_0$	$\pm\Delta F_L$	$\pm\Delta F_0$	$\pm\Delta F_L$
JES	0.004	0.003	0.005	0.003	0.005	0.003
JER	0.001	0.002	0.004	0.003	0.003	0.003
b tagging eff.	0.001	$<10^{-3}$	0.001	$<10^{-3}$	0.001	$<10^{-3}$
Lepton eff.	0.001	0.002	0.001	0.001	0.001	0.001
Single top normal.	0.002	$<10^{-3}$	0.003	0.001	0.003	0.001
W + jets bkg.	0.008	0.001	0.007	0.001	0.007	0.001
DY + jets bkg.	0.002	$<10^{-3}$	0.001	$<10^{-3}$	0.001	$<10^{-3}$
Multijet bkg.	0.023	0.007	0.007	0.003	0.008	0.001
Pileup	0.001	0.001	$<10^{-3}$	$<10^{-3}$	0.001	$<10^{-3}$
Top quark mass	0.012	0.008	0.010 (*)	0.008 (*)	0.010	0.007
$t\bar{t}$ scales	0.011	0.008 (*)	0.014	0.007 (*)	0.012	0.007
$t\bar{t}$ match. scale	0.011 (*)	0.007 (*)	0.010	0.007	0.009	0.007
$t\bar{t}$ MC and hadronisation	0.015	0.009	0.005	0.003	0.006	0.004
$t\bar{t}$ $p_T$ reweight	0.011	0.010	$<10^{-3}$	0.001	$<10^{-3}$	0.002
Limited MC size	0.002	0.001	0.002	0.001	0.002	0.001
PDF	0.004	0.001	0.002	0.001	0.002	0.001
Total	0.037	0.020	0.024	0.014	0.023	0.014

Systematics uncertainty	$\Delta F_L$	$\Delta F_0$
Lepton ID and trigger	< 0.001	< 0.001
b tagging	0.001	0.002
Background normalisations	0.002	0.005
Jet energy resolution	0.003	0.002
Jet energy scale	0.002	0.009
Top $p_T$ reweighting	0.007	0.010
Factorization/renormalization scales (signal)	0.013	0.010
Factorization/renormalization scales (DY)	0.004	0.007
Hadronization model	0.006	0.008
Jet-parton matching	0.017	0.012
Top mass ( $\pm 1\text{GeV}/c^2$ )	0.004	0.005
Pileup	0.001	< 0.001
PDF	< 0.001	< 0.001
Integrated luminosity	0.001	< 0.001
Limited simulated signal statistics	0.003	0.004
Total uncertainty	0.025	0.024

	Muon channel		Electron channel		Combination	
	$\Delta F_0$	$\Delta F_L$	$\Delta F_0$	$\Delta F_L$	$\Delta F_0$	$\Delta F_L$
Experimental	0.010	0.009	0.008	0.005	0.010	0.010
Modeling	0.025	0.017	0.025	0.022	0.025	0.020
Normalization	0.002	0.008	0.012	0.014	0.011	0.012
SM W helicities	0.007	0.004	0.005	0.003	0.007	0.004
MC sample size	0.026	0.012	0.025	0.015	0.020	0.012
tWb in prod.	0.014	0.016	0.010	0.018	0.011	0.014
Total	0.041	0.030	0.040	0.036	0.037	0.032

$$\left. \begin{aligned}
 F_L &= 0.298 \pm 0.028 \text{ (stat)} \pm 0.032 \text{ (syst)}, \\
 F_0 &= 0.720 \pm 0.039 \text{ (stat)} \pm 0.037 \text{ (syst)}, \\
 F_R &= -0.018 \pm 0.019 \text{ (stat)} \pm 0.011 \text{ (syst)},
 \end{aligned} \right\} \text{ total correlation of } \mathbf{-0.80}$$



-  $\cos\theta^* \sim -1$ : corresponds to events in which the charged lepton is emitted backward to the direction of motion of the W boson and thus parallel to the b-quark momentum.

The strong suppression of events after event selection can be linked to the event-selection requirements on the charged lepton candidates: isolation and the cut on its momentum.

-  $\cos\theta^* \sim +1$  corresponds to events in which the neutrino is emitted backward with respect to the direction of motion of the W boson and thus in the same direction as the b-quark. Therefore the momentum of the neutrino (and thus also the missing transverse energy) decreases and these events are more likely to fail the missing transverse energy cut. Mismeasurements on this also affect the angular distribution.

## The Wtb vertex Lagrangian:

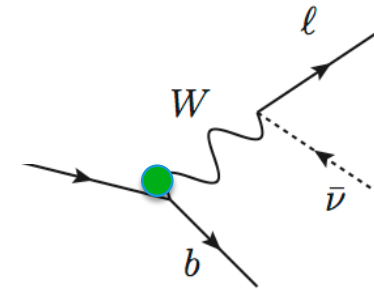
$$SM \Rightarrow L_{Wtb}^{SM} = -\frac{g}{\sqrt{2}} \bar{u}_b \gamma^\mu V_{tb} P_L u_t W_\mu^+ + \text{h.c.}$$

A general extension:

Nucl.Phys. B812 (2009) 181-204  
Eur.Phys.J. C50, 519 (2007)

$$L_{Wtb} = -\frac{g}{\sqrt{2}} \bar{u}_b \gamma^\mu (V_L P_L + V_R P_R) u_t W_\mu^+ - \frac{g}{\sqrt{2}} \bar{u}_b \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (g_L P_L + g_R P_R) u_t W_\mu^+ + \text{h.c.}$$

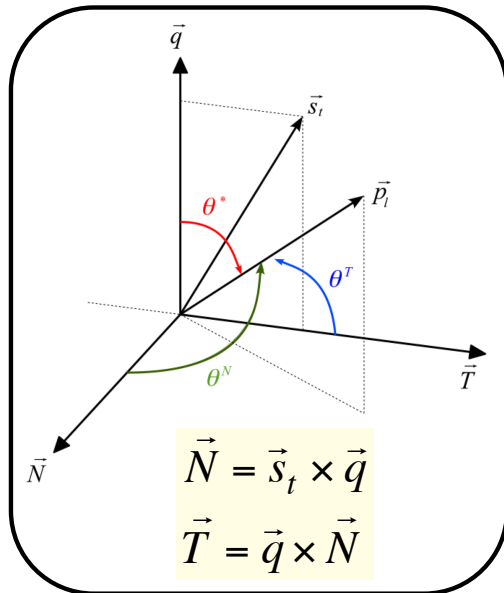
$$SM \Rightarrow V_L = V_{tb} \sim 1 \quad V_R = g_L = g_R = 0$$



$V_{L,R}$  and  $g_{L,R}$

left and right - handed vector and tensor couplings

## Angular observables to probe the Wtb vertex:



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→ For unpolarised top quark decays, the only meaningful direction in the top RF is the one of the W boson momentum (q)

→ For polarised (spin direction  $s_t$ ) top quarks produced via electroweak interaction, further directions may be considered: N and T.

→ Three angular distributions:  $\theta_l^*$ (q,l),  $\theta_l^N$ (N,l) and  $\theta_l^T$ (T,l)

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_l^X} = \frac{3}{8} (1 + \cos \theta_l^X)^2 F_+^X + \frac{3}{8} (1 - \cos \theta_l^X)^2 F_-^X + \frac{3}{4} \sin^2 \theta_l^X F_0^X$$

$$A_{FB}^X = \frac{N(\cos \theta_l^X > 0) - N(\cos \theta_l^X < 0)}{N(\cos \theta_l^X > 0) + N(\cos \theta_l^X < 0)} \propto (F_+^X - F_-^X)$$



$$\frac{1}{N} \frac{dN}{d \cos \theta^*} = \frac{3}{8} (1 - \cos \theta^*)^2 F_L + \frac{3}{4} \sin^2 \theta^* F_0 + \frac{3}{8} (1 + \cos \theta^*)^2 F_R$$

$$W_L = \frac{\frac{3}{8} (1 - \cos \theta_{\text{gen}}^*)^2}{f_L \cdot \frac{3}{8} (1 - \cos \theta_{\text{gen}}^*)^2 + f_0 \cdot \frac{3}{4} (1 - \cos^2 \theta_{\text{gen}}^*) + f_R \cdot \frac{3}{8} (1 + \cos \theta_{\text{gen}}^*)^2}$$

$$W_0 = \frac{\frac{3}{4} (1 - \cos^2 \theta_{\text{gen}}^*)}{f_L \cdot \frac{3}{8} (1 - \cos \theta_{\text{gen}}^*)^2 + f_0 \cdot \frac{3}{4} (1 - \cos^2 \theta_{\text{gen}}^*) + f_R \cdot \frac{3}{8} (1 + \cos \theta_{\text{gen}}^*)^2}$$

$$W_R = \frac{\frac{3}{8} (1 + \cos \theta_{\text{gen}}^*)^2}{f_L \cdot \frac{3}{8} (1 - \cos \theta_{\text{gen}}^*)^2 + f_0 \cdot \frac{3}{4} (1 - \cos^2 \theta_{\text{gen}}^*) + f_R \cdot \frac{3}{8} (1 + \cos \theta_{\text{gen}}^*)^2}$$