

111d Lisa - WFCF 2009 - CE111

# azimuthally-sensitive femtoscopy and the energy scan program(s)

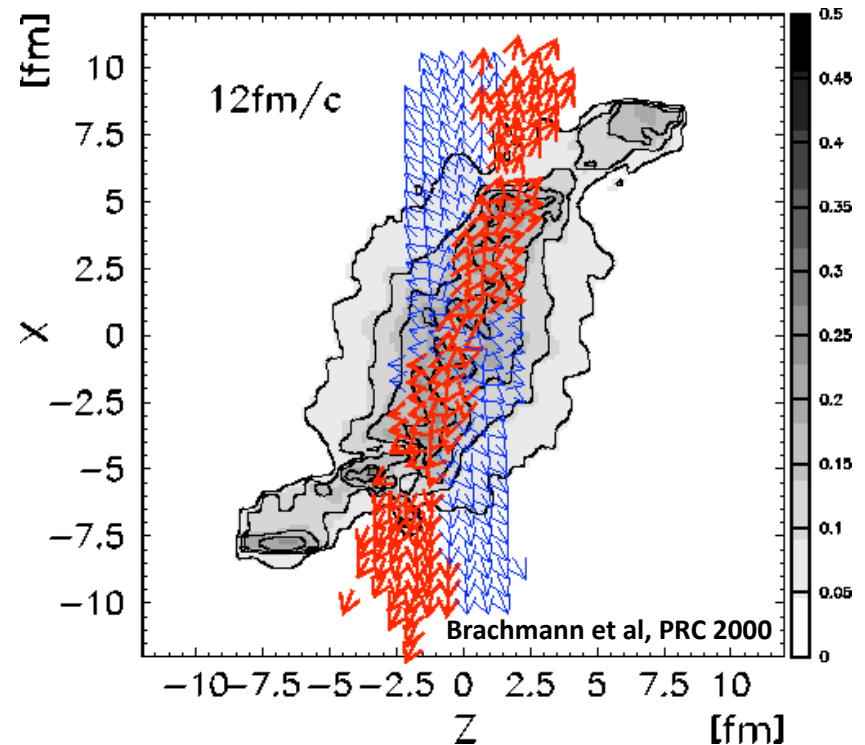
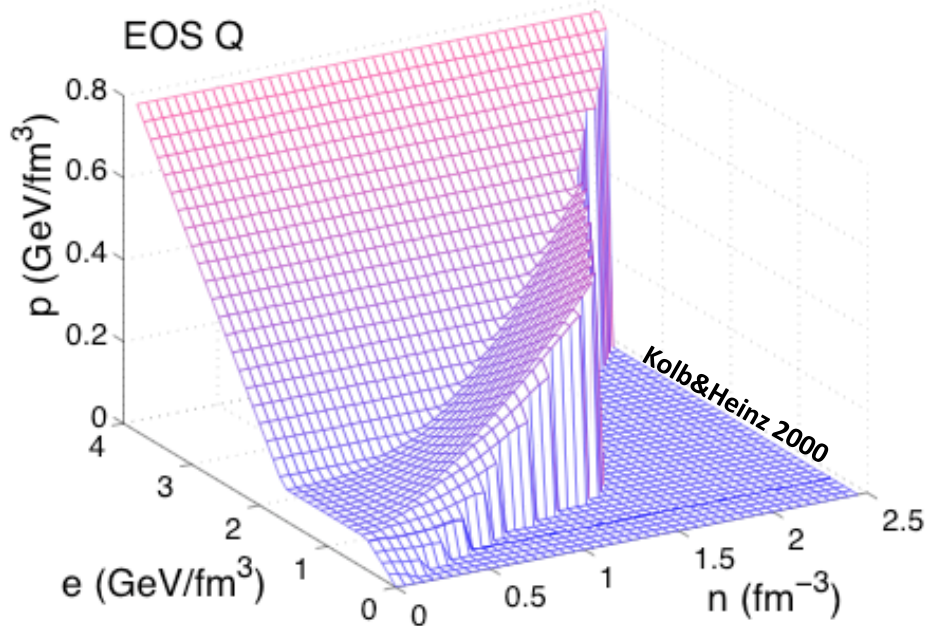
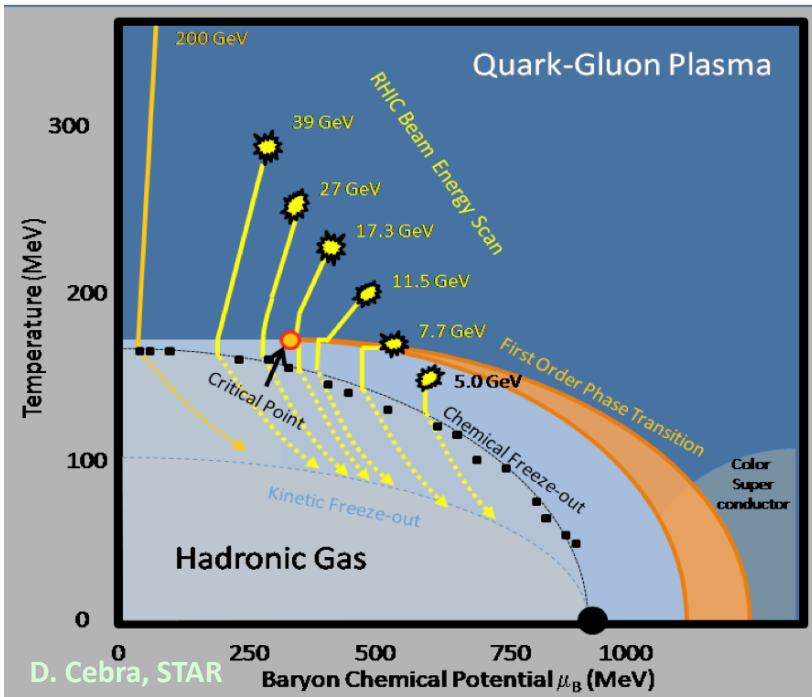
Mike Lisa

In collaboration with: E. Frodermann (U. Minn),  
M. Mitrovski, H. Petersen, M. Bleicher (Frankfurt)

# RHIC energy scan: $\sqrt{s}=7\text{-}40$ GeV (2010~2012 (?))

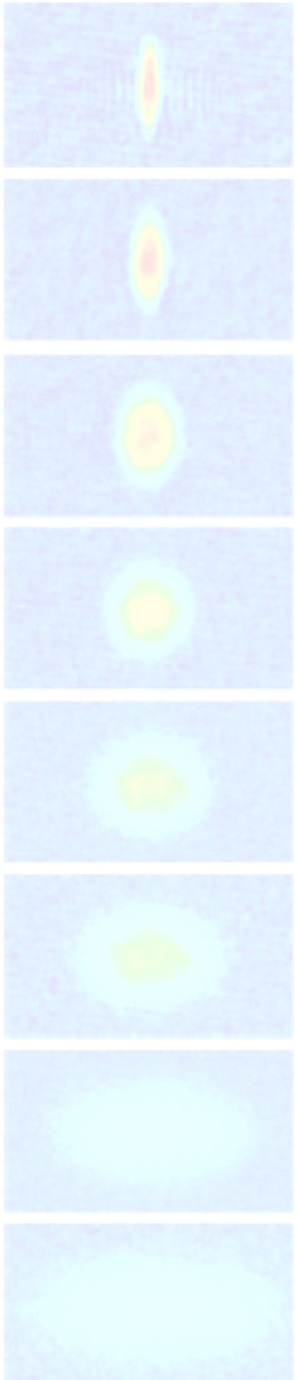
Probe QCD phase diagram via

- statistics/fluctuations
- ✓ dynamic system response
  - transport models (phase structure in EoS)
  - bulk collectivity (low- $p_T$  measurements)

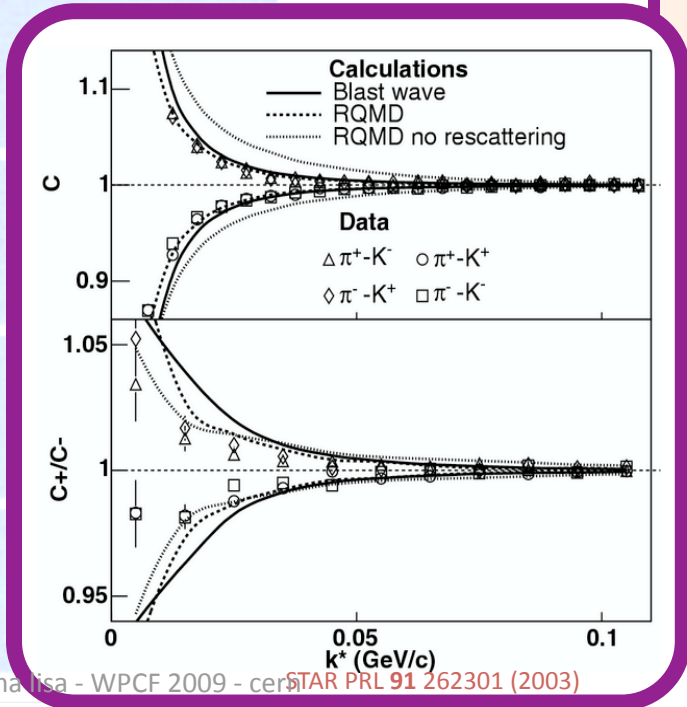
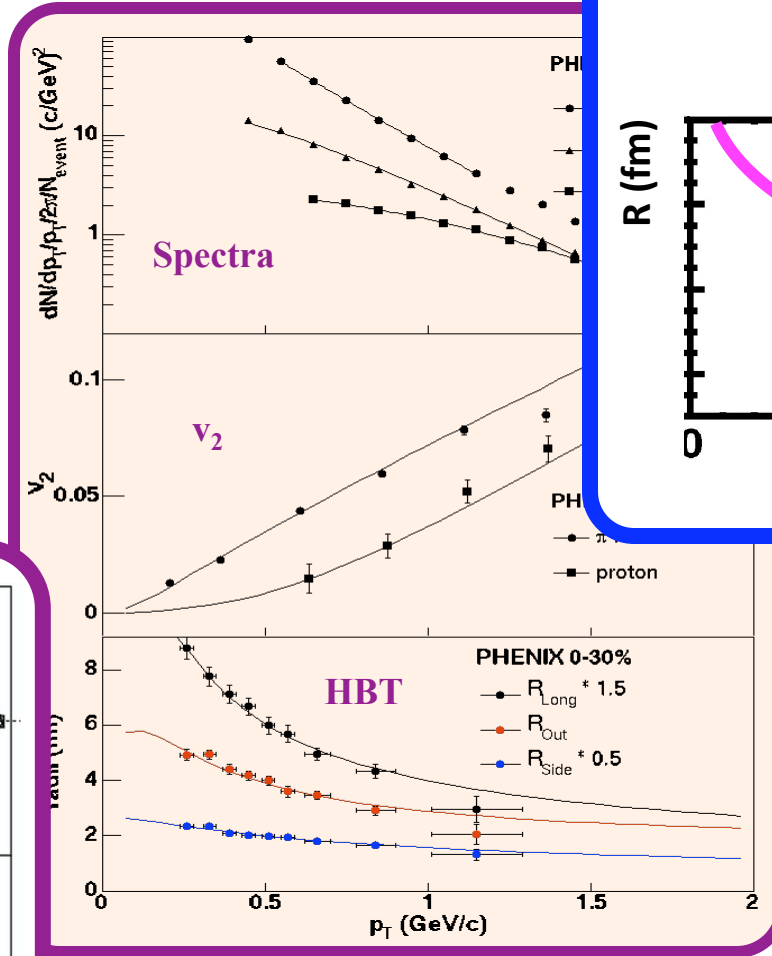
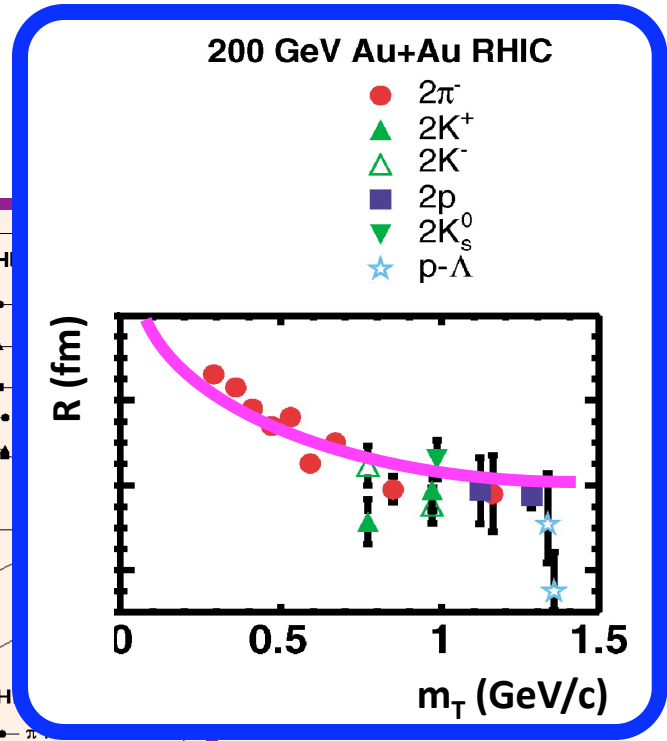
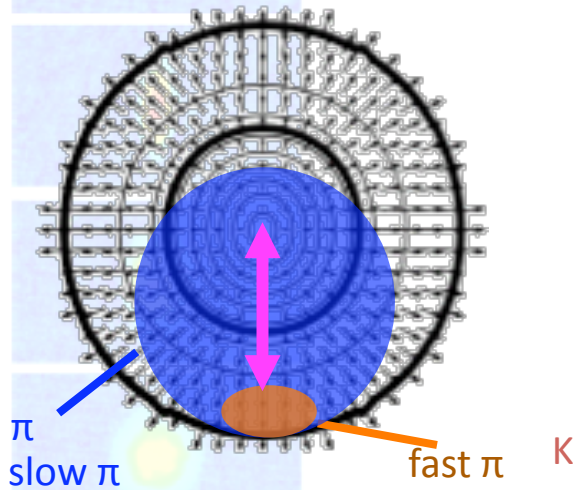


# Outline

- femtoscopy (HBT) and collectivity in R.H.I.C.
  - radial, longitudinal, **directed, elliptic**
- azimuthally-sensitive HBT (asHBT)
  - what is measured
  - what it measures
  - what's been measured
  - what needs to be measured!
- model calculations
  - 2D hydro
  - RQMD, UrQMD
  - 3D hydro + UrQMD
- status



# R(mT) – spatial aspect of radial flow

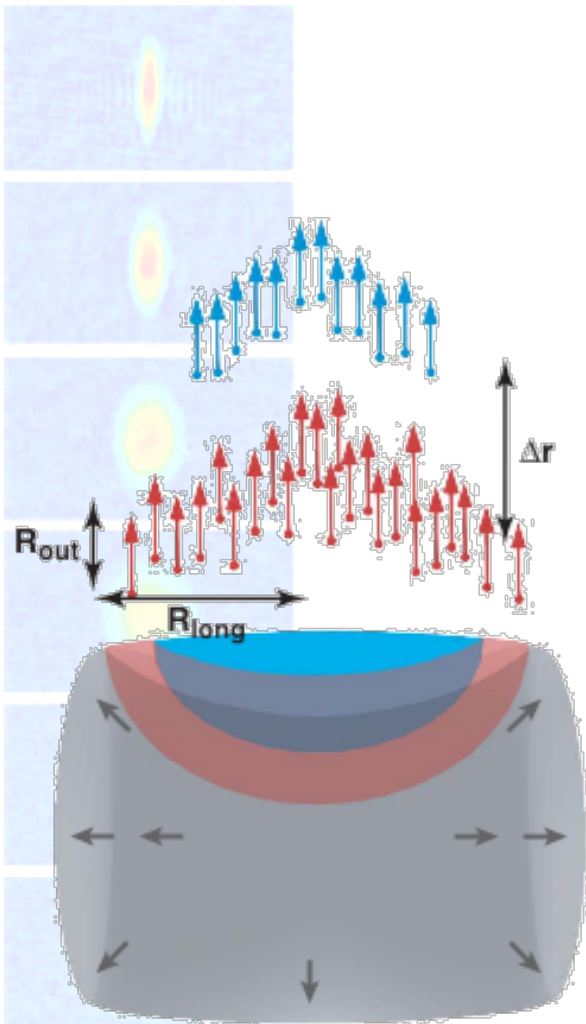
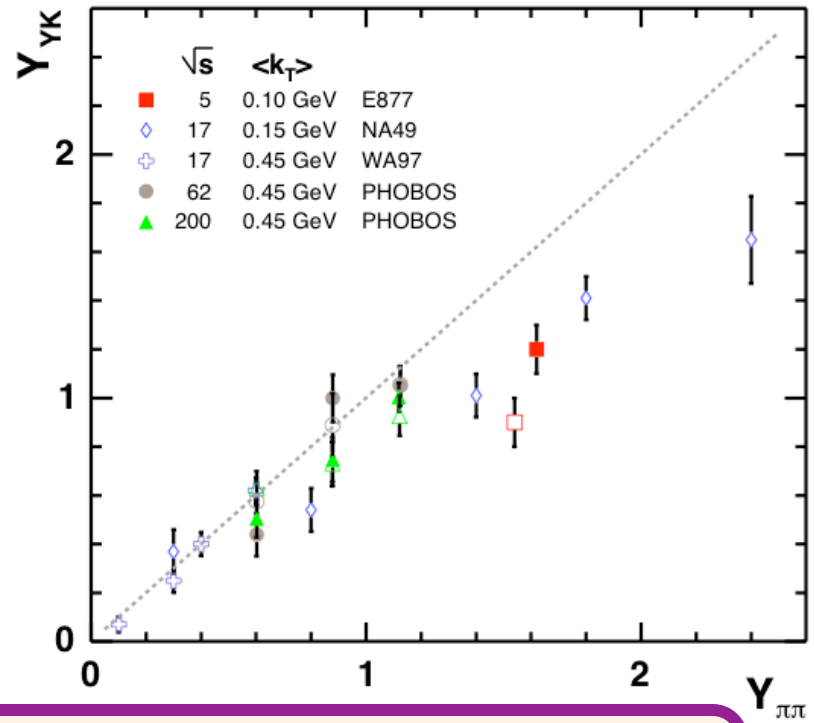


(radial) space-momentum substructure mapped *in detail*



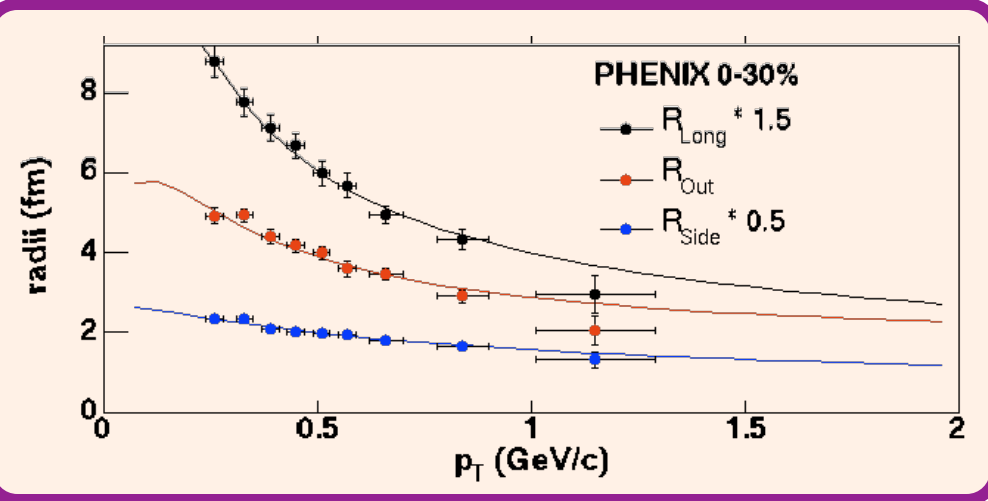
# strong longitudinal flow (not necc B.I.)

Ann Rev Nucl Part Sci (2005) nucl-ex/0505014

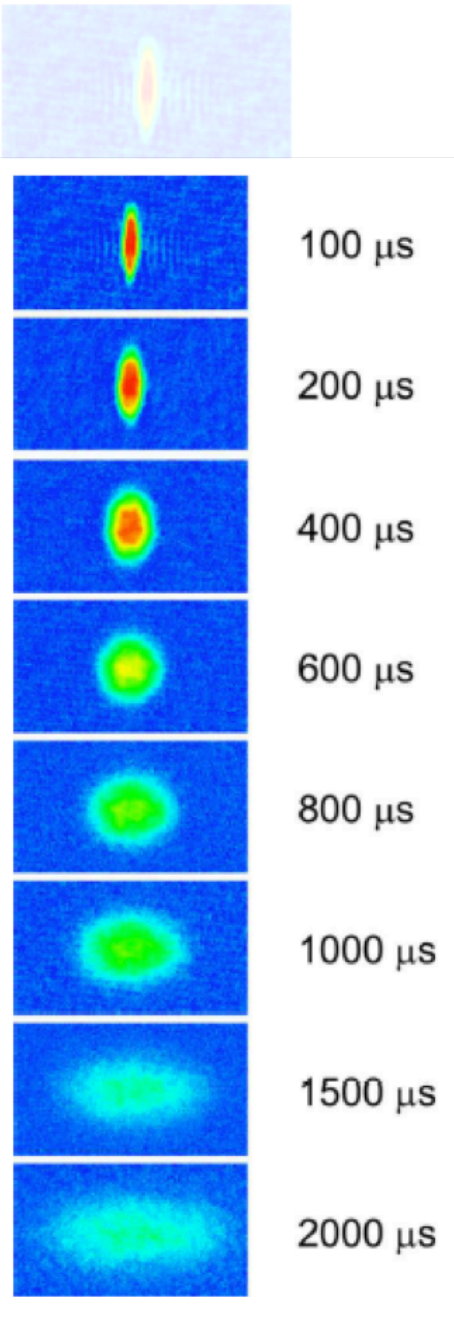


Also:  $R_{ol}^2(y, p_T)$

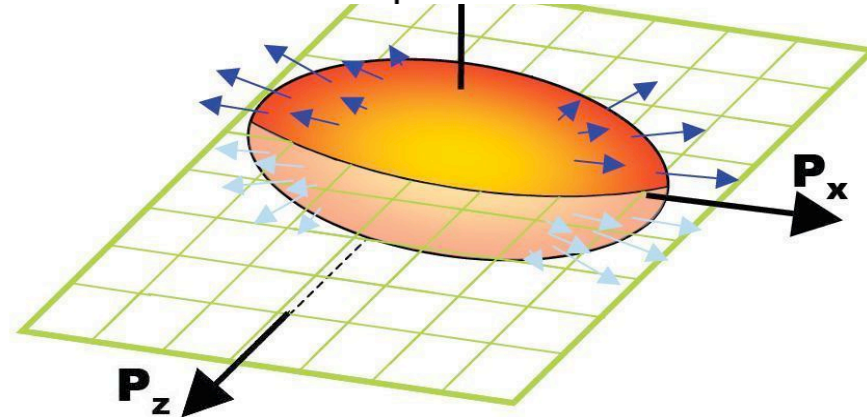
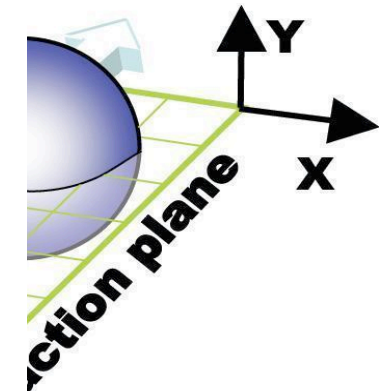
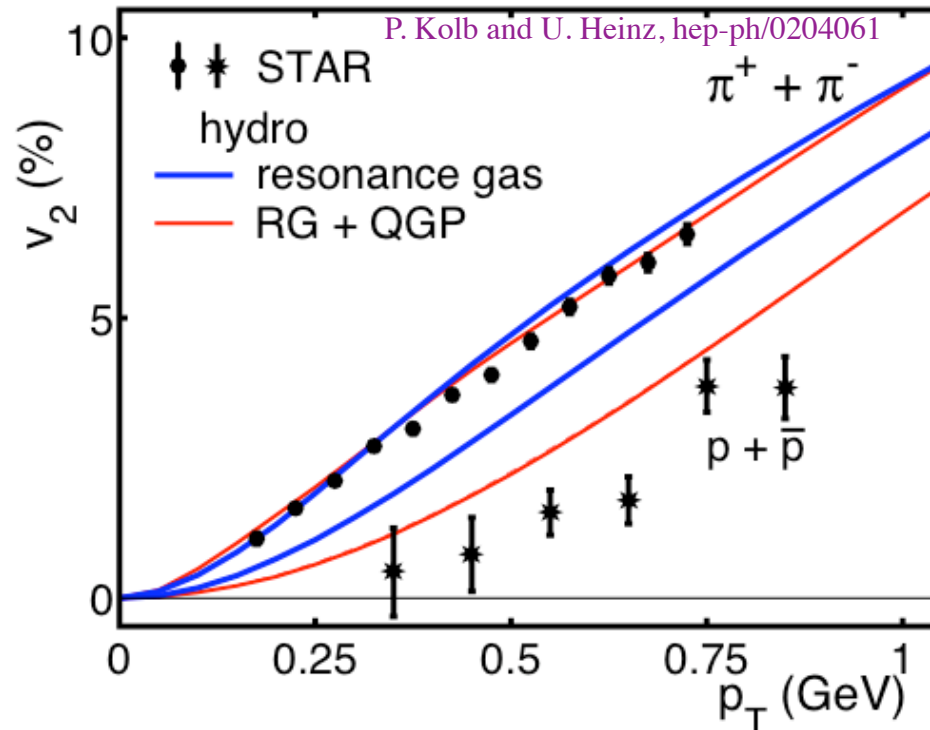
less attention to longitudinal d.o.f. in HBT



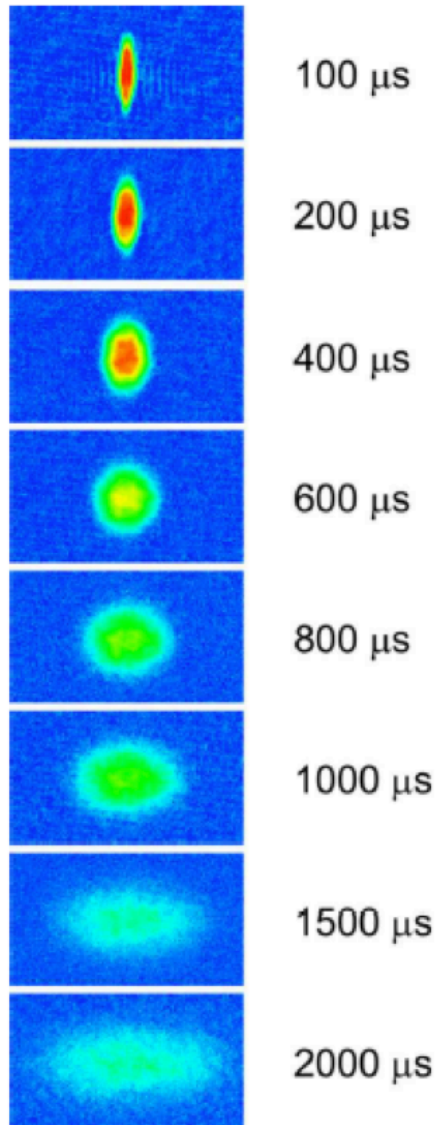
# phi- the sexy direction



O'Hara et al, *Science* 2002



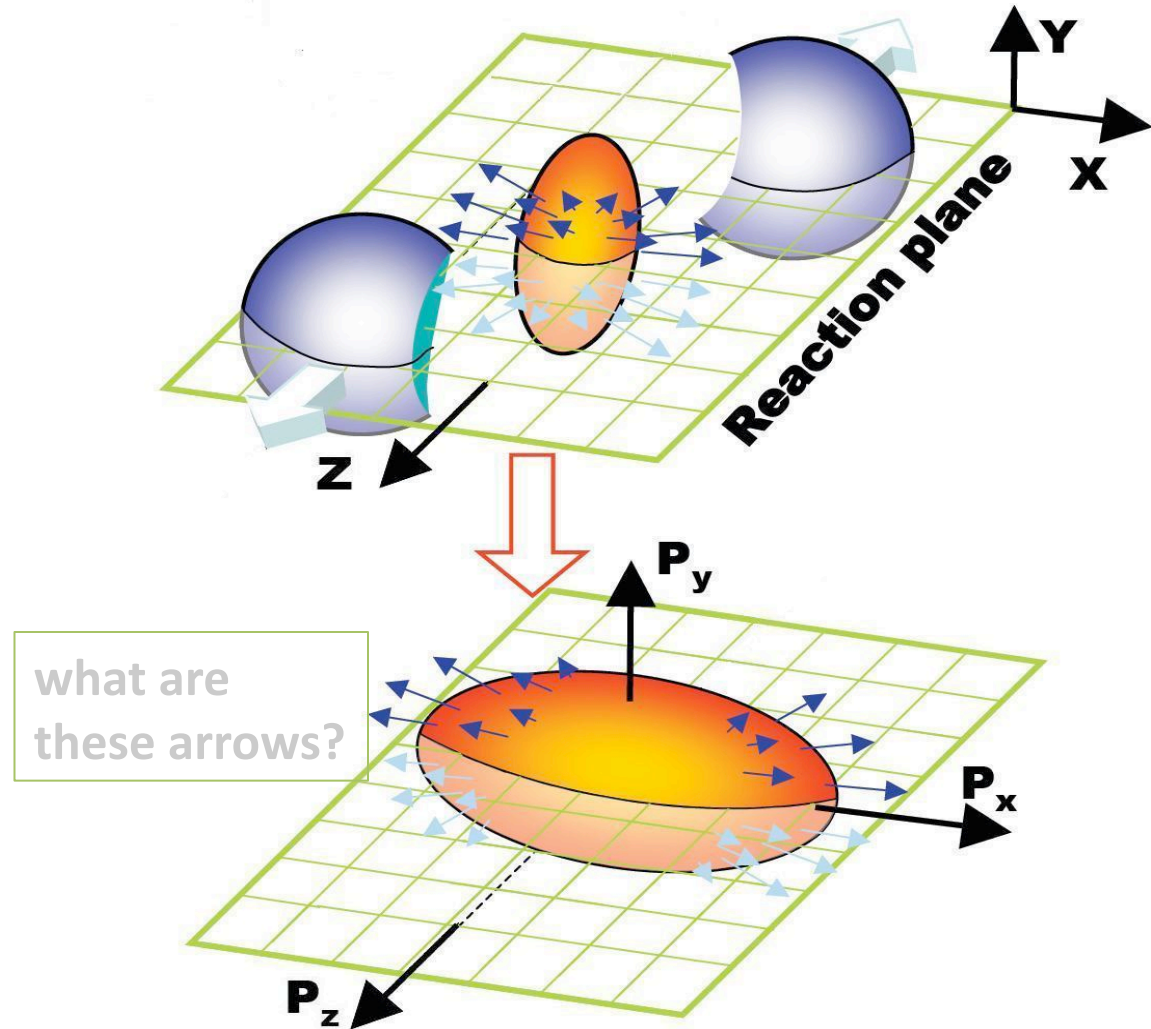
this is *space*



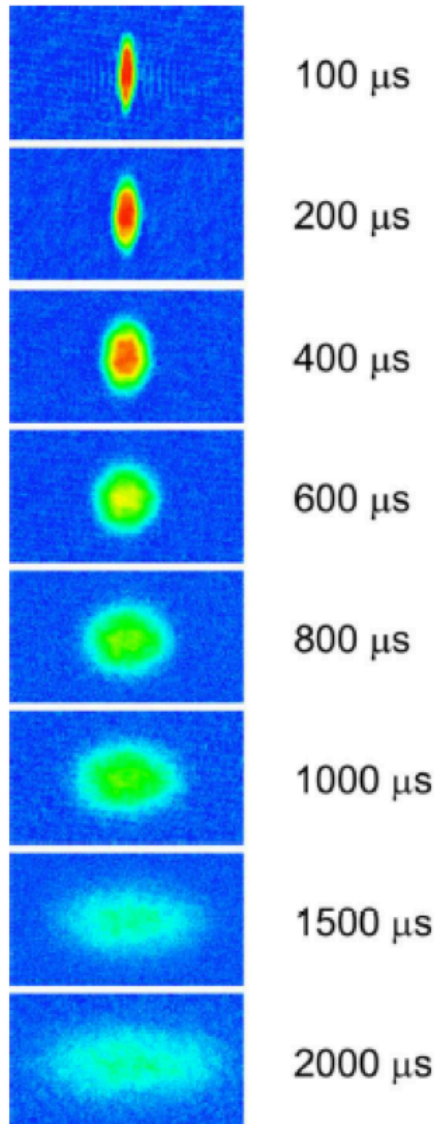
O'Hara et al, *Science* 2002

ma lisa - WPCF 2009 - cern

## phi- the sexy direction

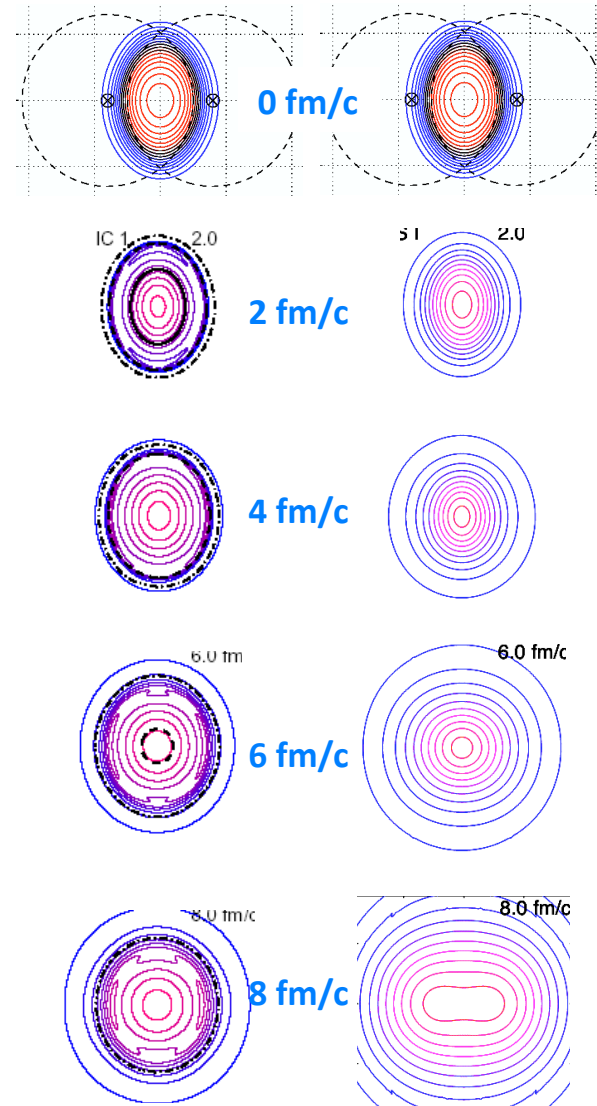


ultra-cold atoms



O'Hara et al, *Science* 2002

ultra-hot partons



P. Kolb, PhD 2002

# phi- the sexy direction

evolution from initial “known”  
shape depends on

- pressure anisotropy (“stiffness”)
- lifetime \*

\* O'Hara could *choose* when to  
destroy his system



# phi- the sexy direction

evolution from initial “known” shape depends on

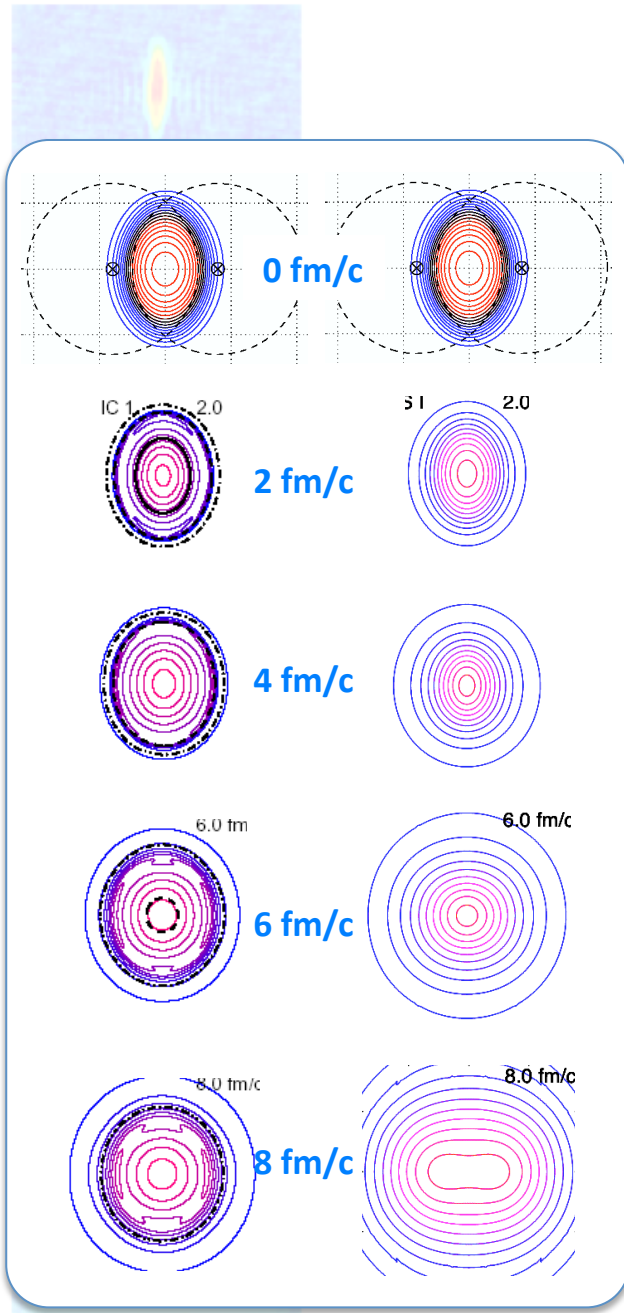
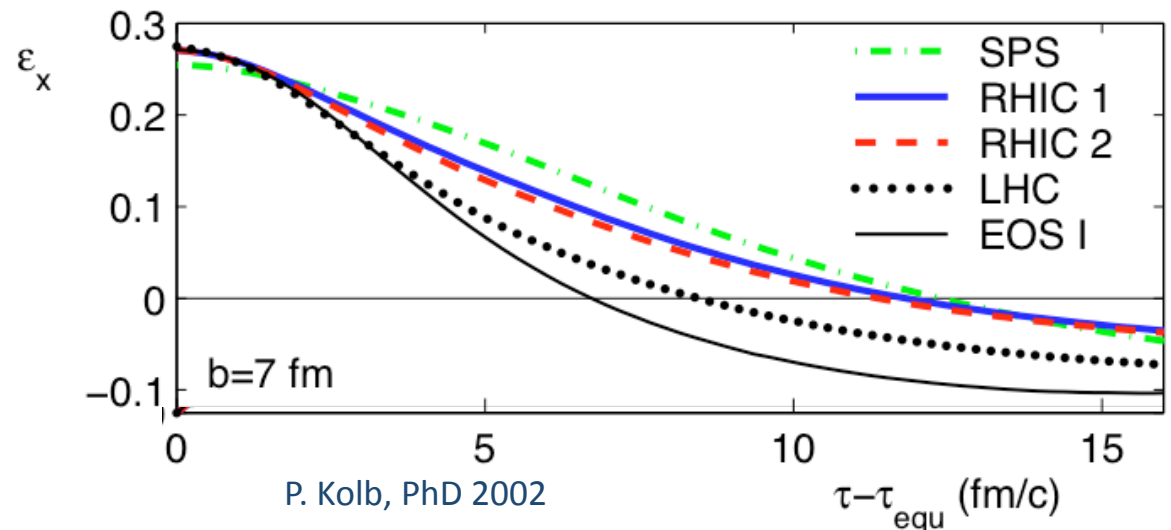
- pressure anisotropy (“stiffness”)
- lifetime

Both are interesting!

We will measure a convolution over freezeout

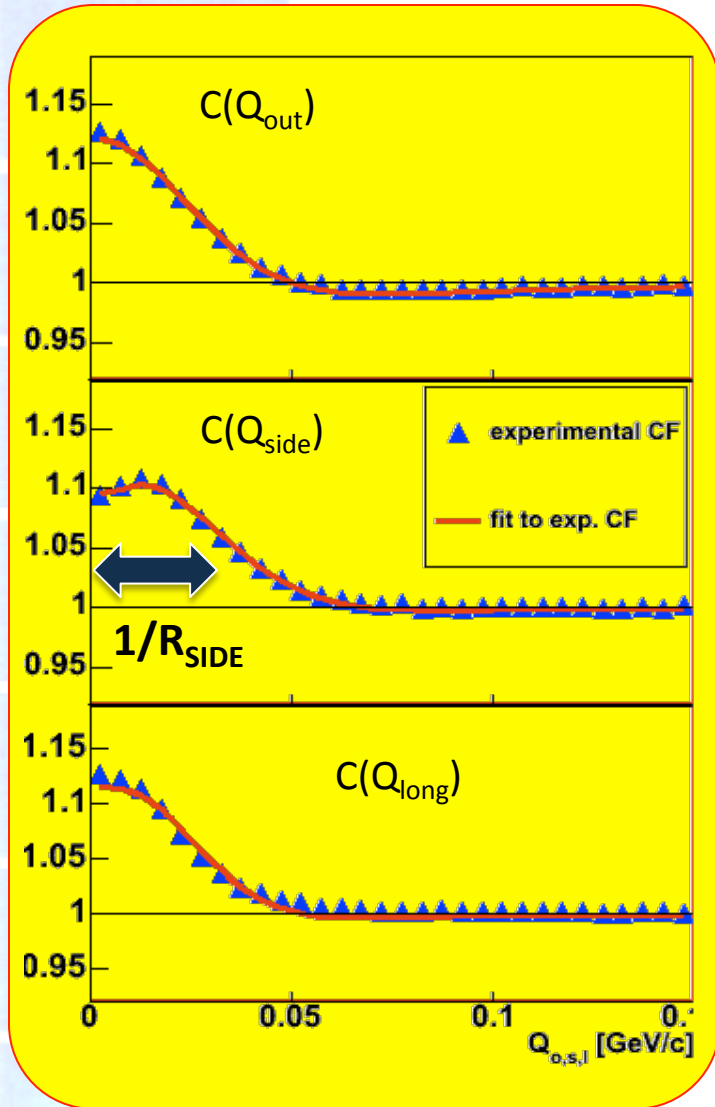
- model needed

$$\varepsilon \equiv \frac{\langle y^2 \rangle - \langle x^2 \rangle}{\langle y^2 \rangle + \langle x^2 \rangle}$$



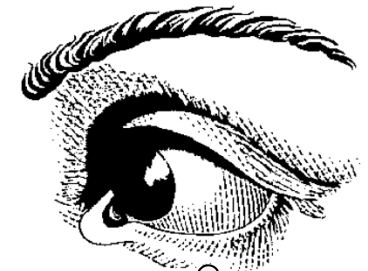
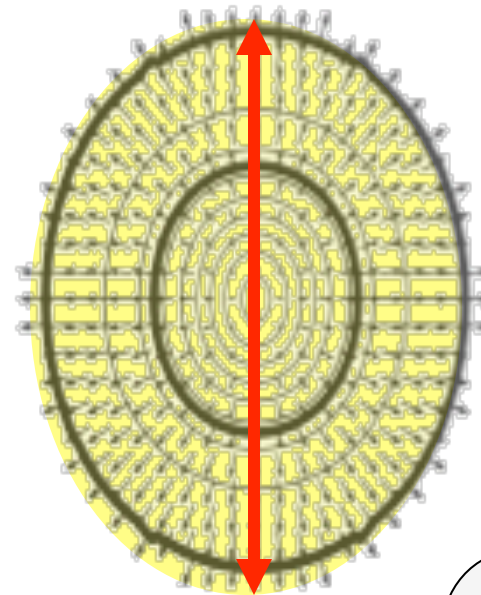


# measuring lengths

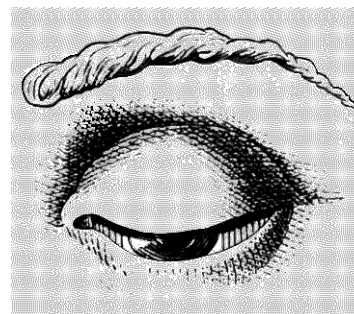


$$C(\vec{q}) = N \cdot \left[ 1 + \lambda \cdot \left( K_{\text{coul}}(\vec{q}) \cdot \left\{ 1 + e^{-\left( q_o^2 R_o^2 + q_s^2 R_s^2 + q_l^2 R_l^2 \right)} \right\} - 1 \right) \right]$$

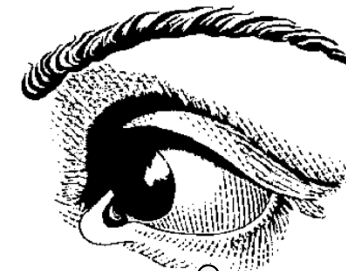
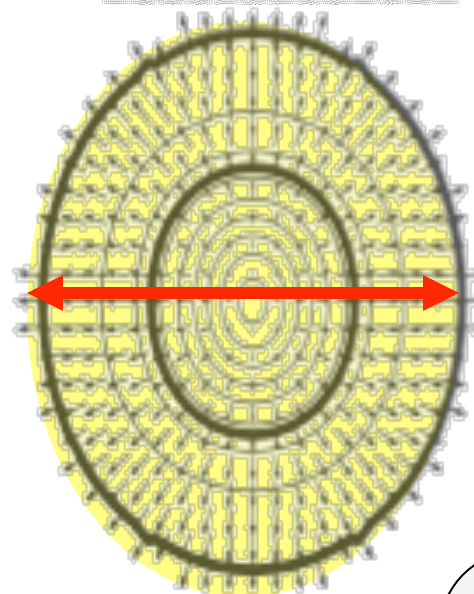
typical "Gaussian" fitting function



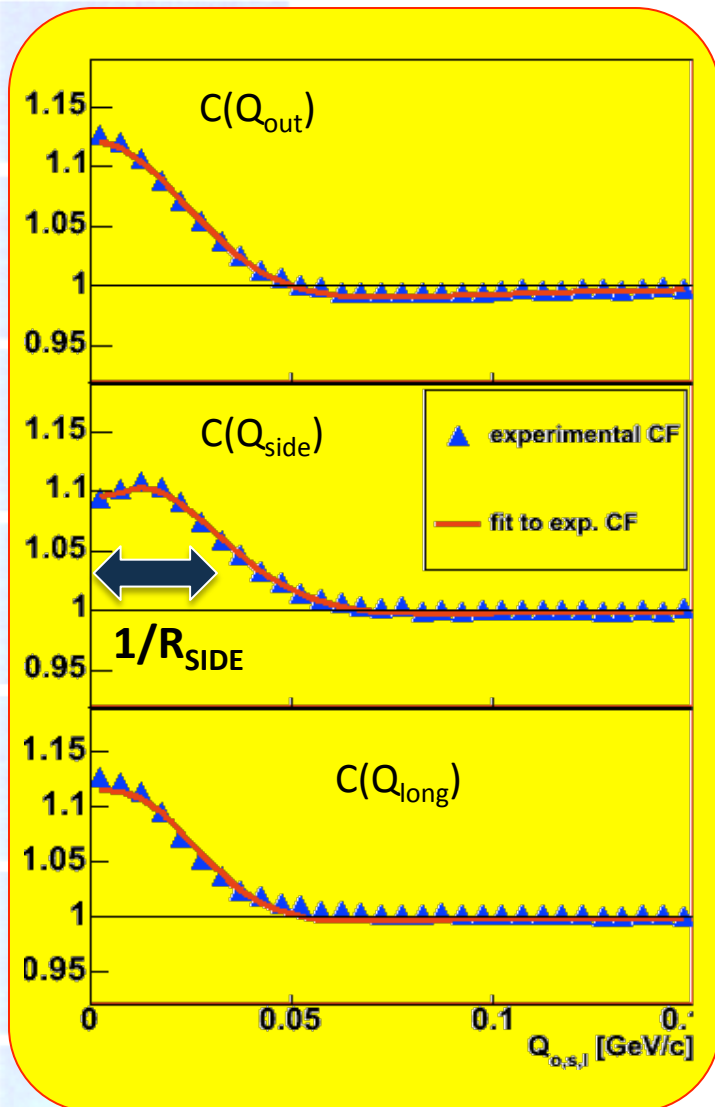
# measuring shape



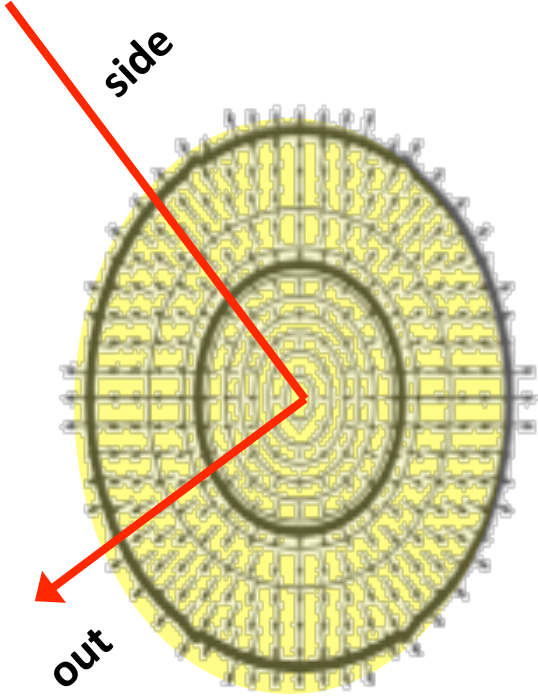
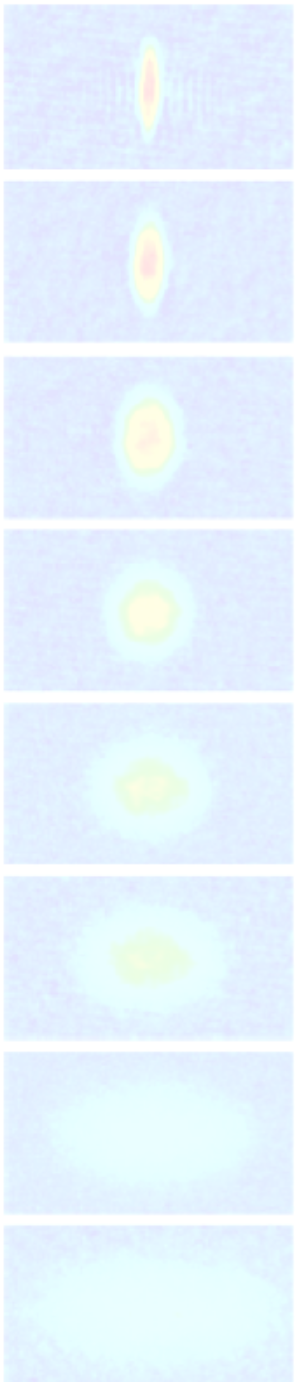
small  $R_S$



big  $R_S$



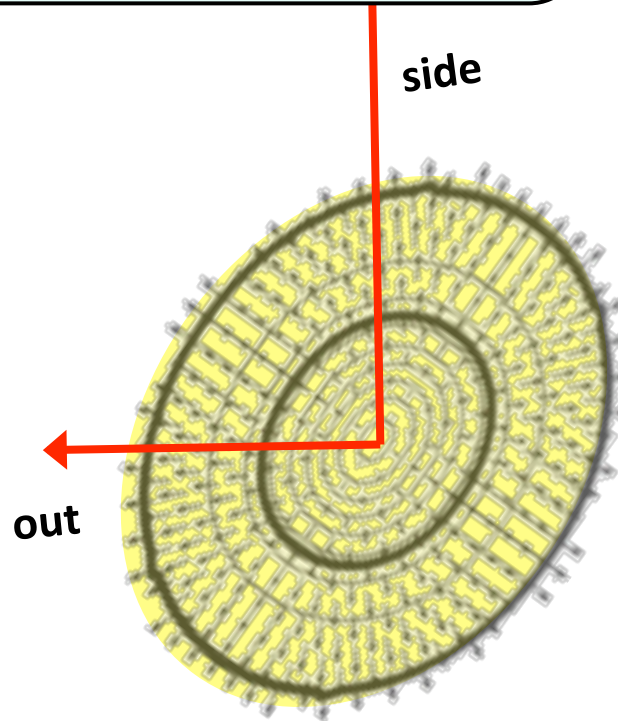
# measuring shape



# measuring shape

$$C(\vec{q}) = N \cdot \left[ 1 + \lambda \cdot \left( K_{coul}(\vec{q}) \cdot \left\{ 1 + \exp(-q_i q_j R_{ij}^2) \right\} - 1 \right) \right]$$

more info. **six** "HBT radii"  $R_o^2, R_s^2, R_l^2, R_{os}^2, R_{sl}^2, R_{ol}^2$



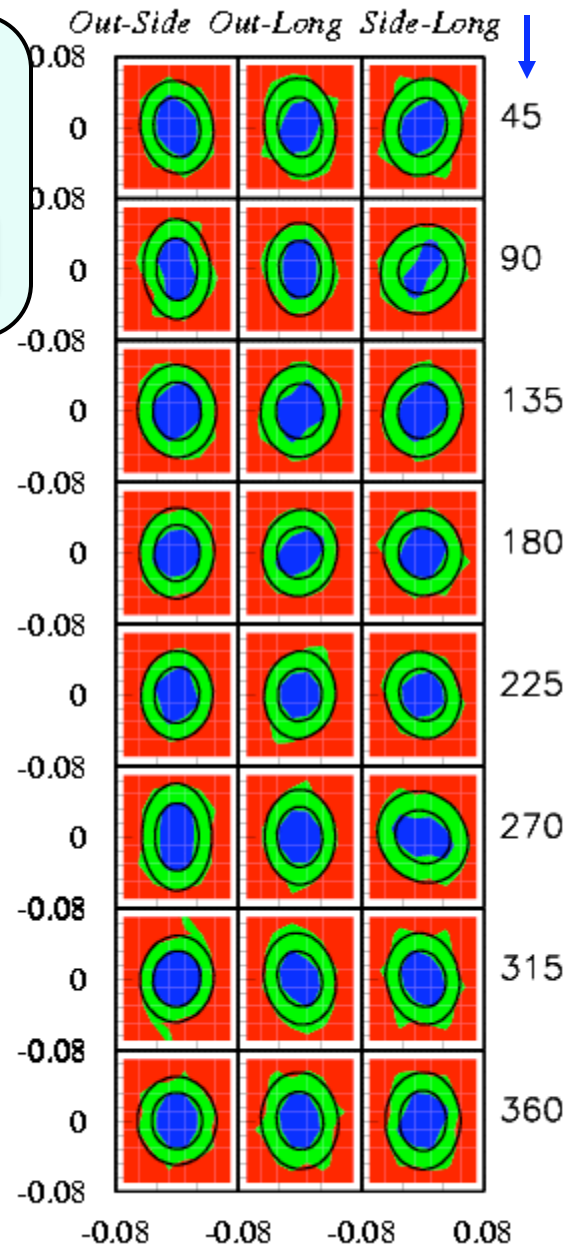
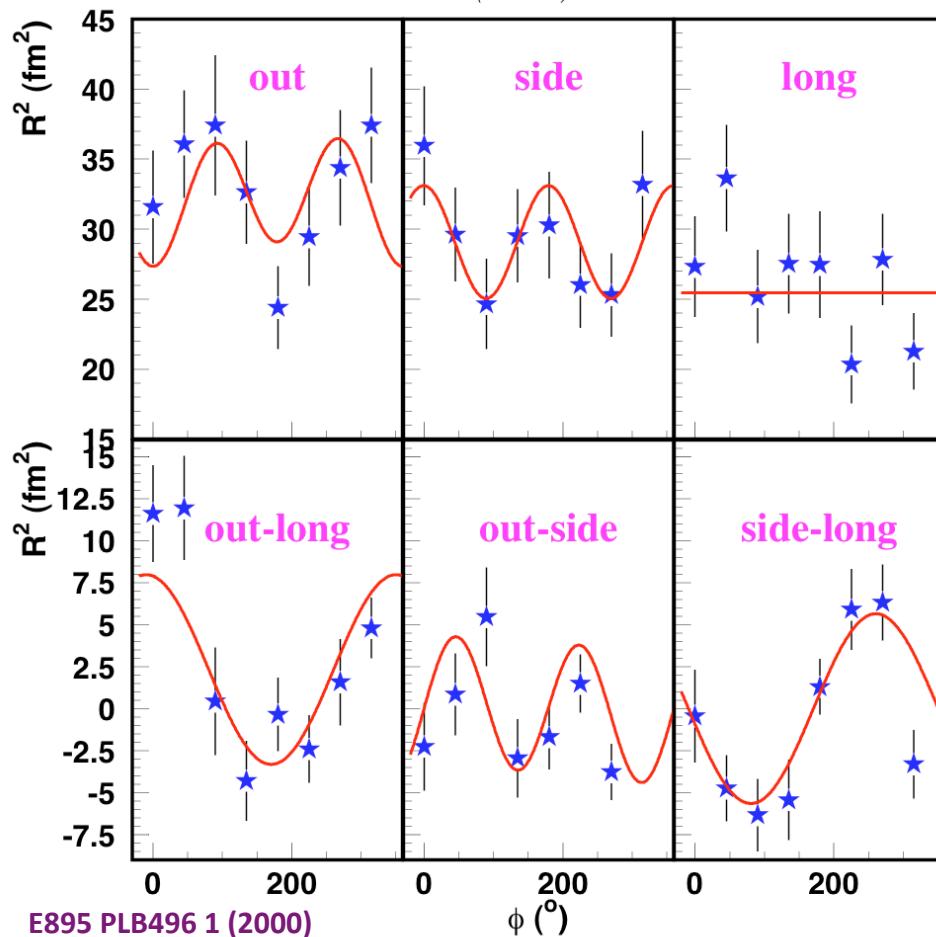
$R_{out-side}^2 < 0$

# measuring shape

$$C(\vec{q}) = N \cdot \left[ 1 + \lambda \cdot \left( K_{coul}(\vec{q}) \cdot \left\{ 1 + \exp(-q_i q_j R_{ij}^2) \right\} - 1 \right) \right]$$

more info. **six** "HBT radii"

$$R_o^2, R_s^2, R_l^2, R_{os}^2, R_{sl}^2, R_{ol}^2$$



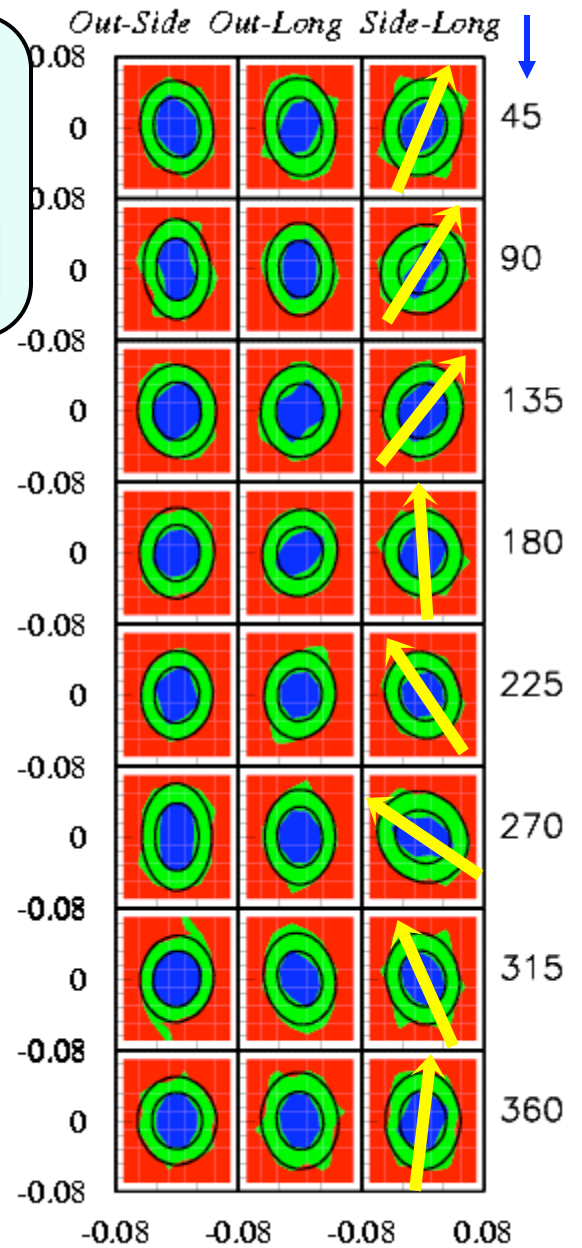
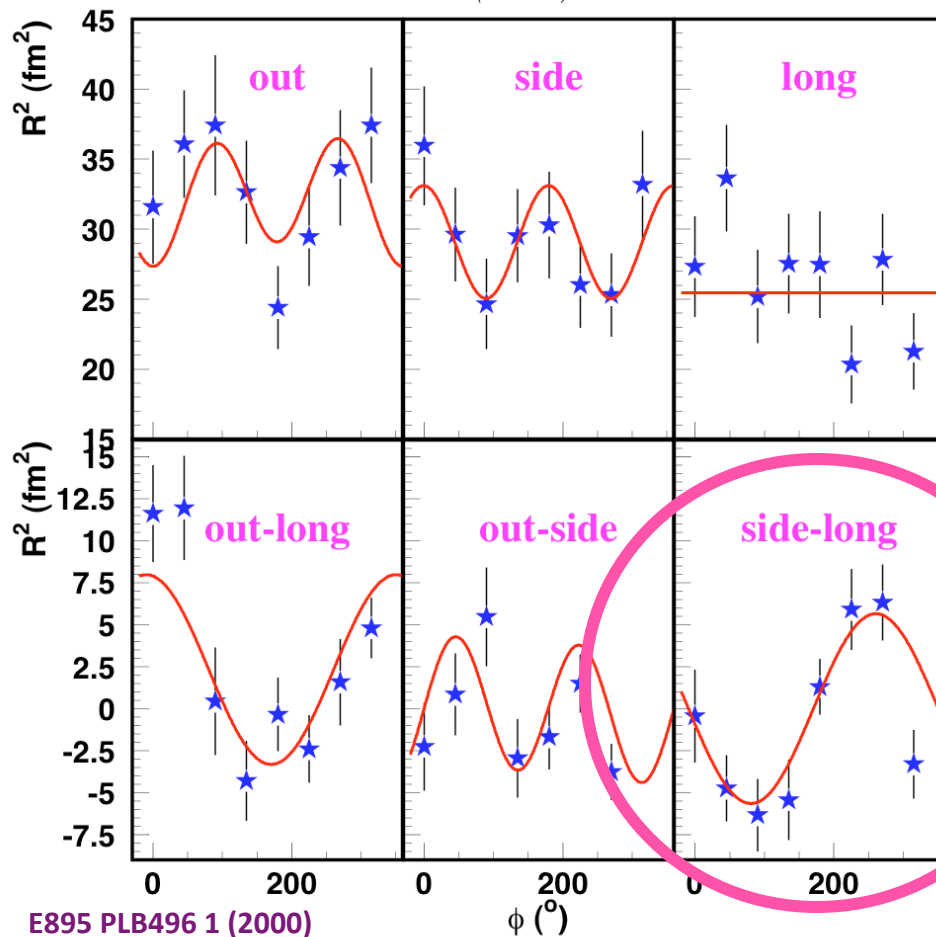


# measuring shape

$$C(\vec{q}) = N \cdot \left[ 1 + \lambda \cdot \left( K_{coul}(\vec{q}) \cdot \left\{ 1 + \exp(-q_i q_j R_{ij}^2) \right\} - 1 \right) \right]$$

more info. **six** "HBT radii"

$$R_o^2, R_s^2, R_l^2, R_{os}^2, R_{sl}^2, R_{ol}^2$$



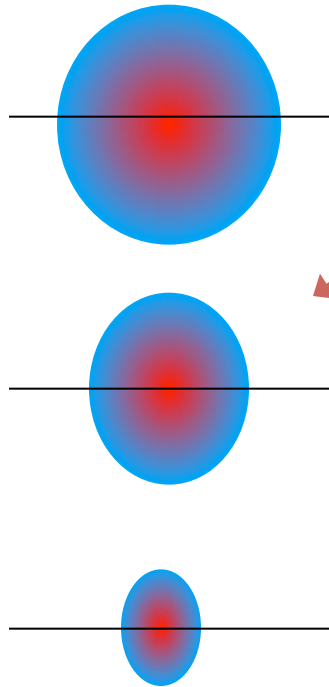
# expected systematics



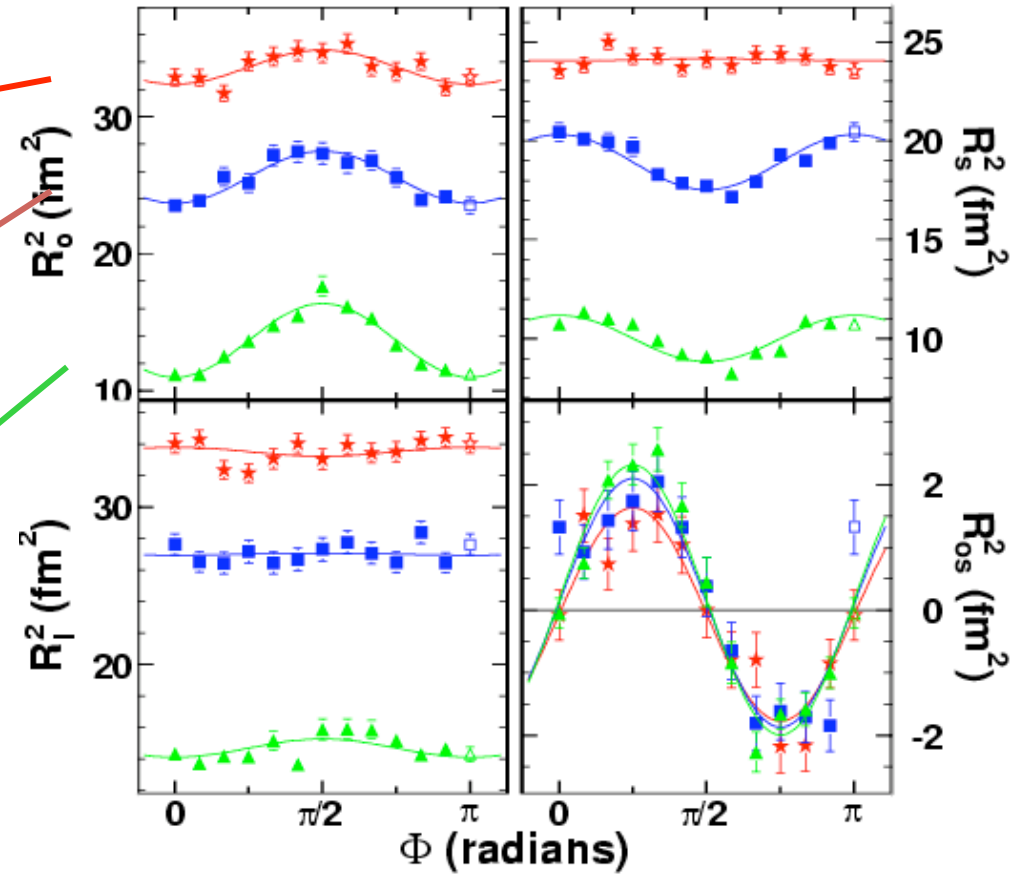
central collisions

mid-central collisions

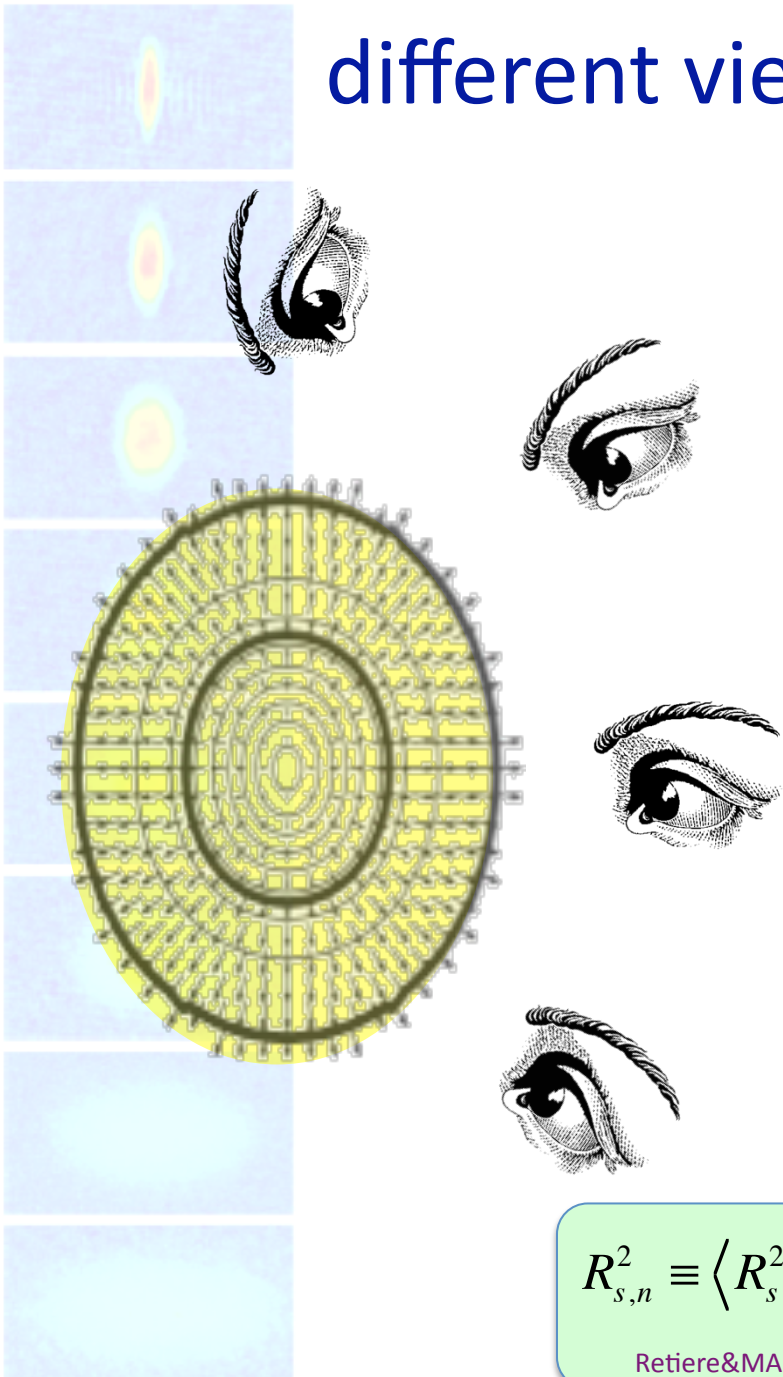
peripheral collisions



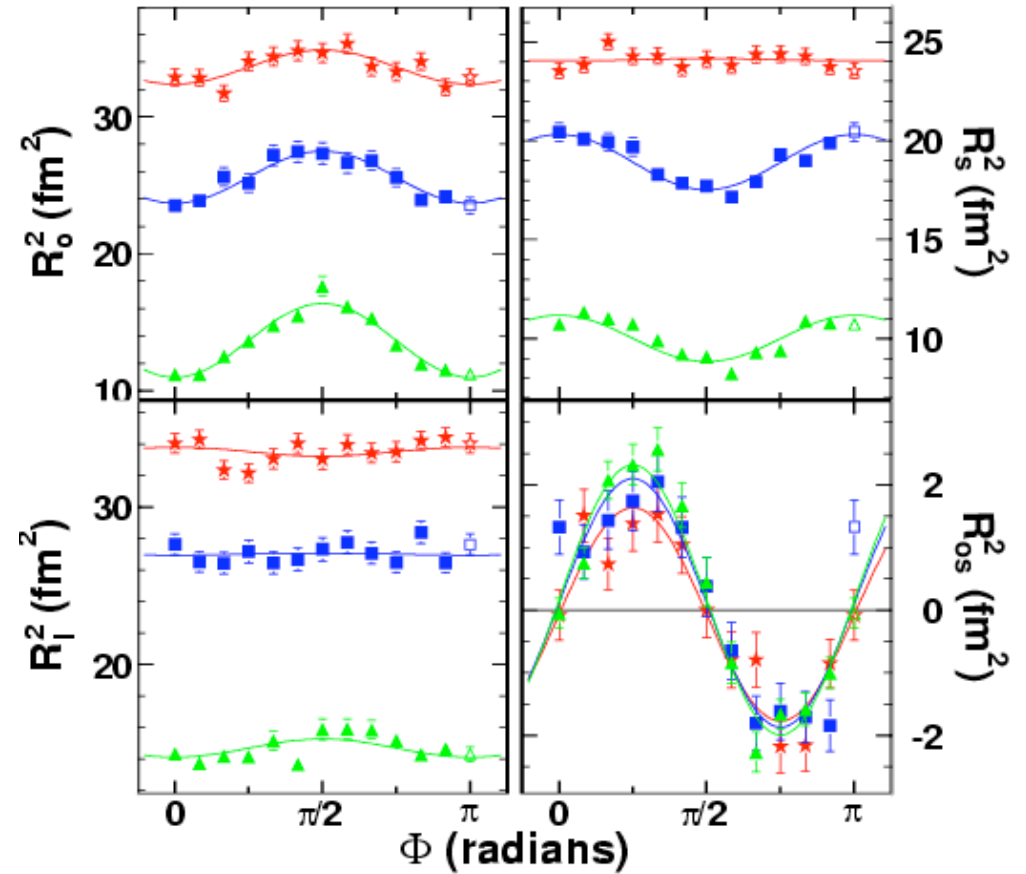
STAR, PRL93 012301 (2004)



# different views of the “same” source?



STAR, PRL93 012301 (2004)

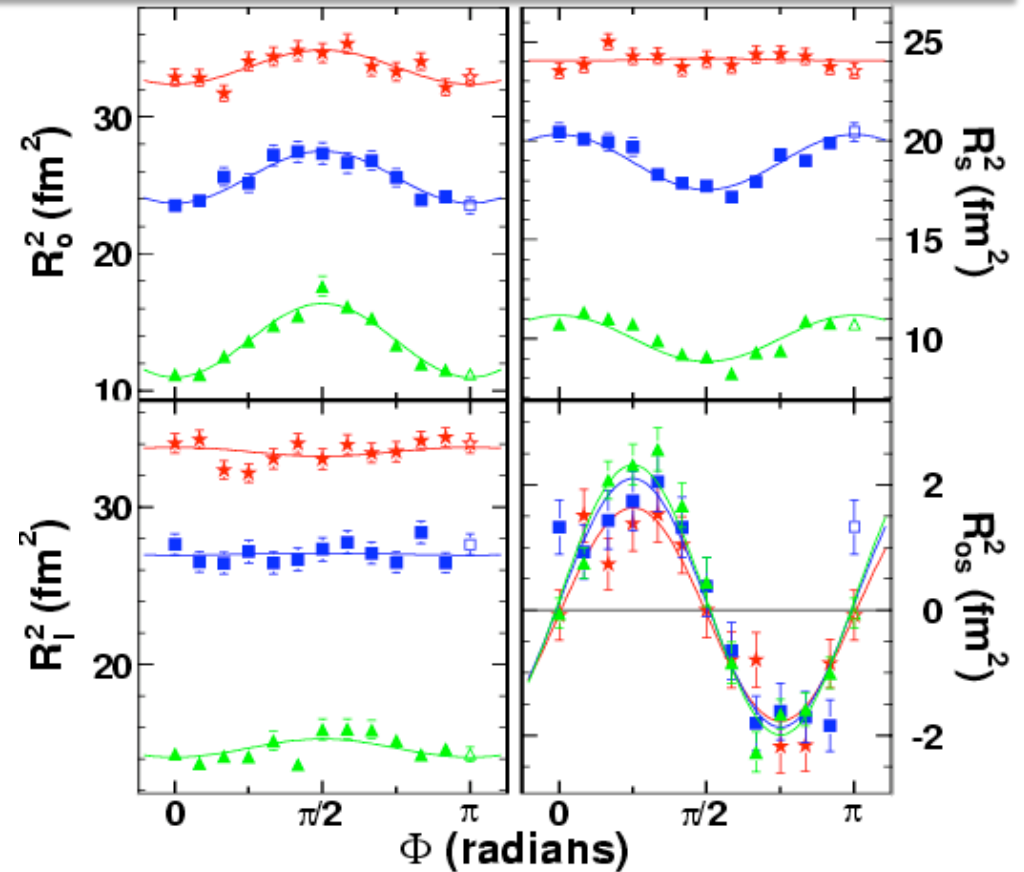
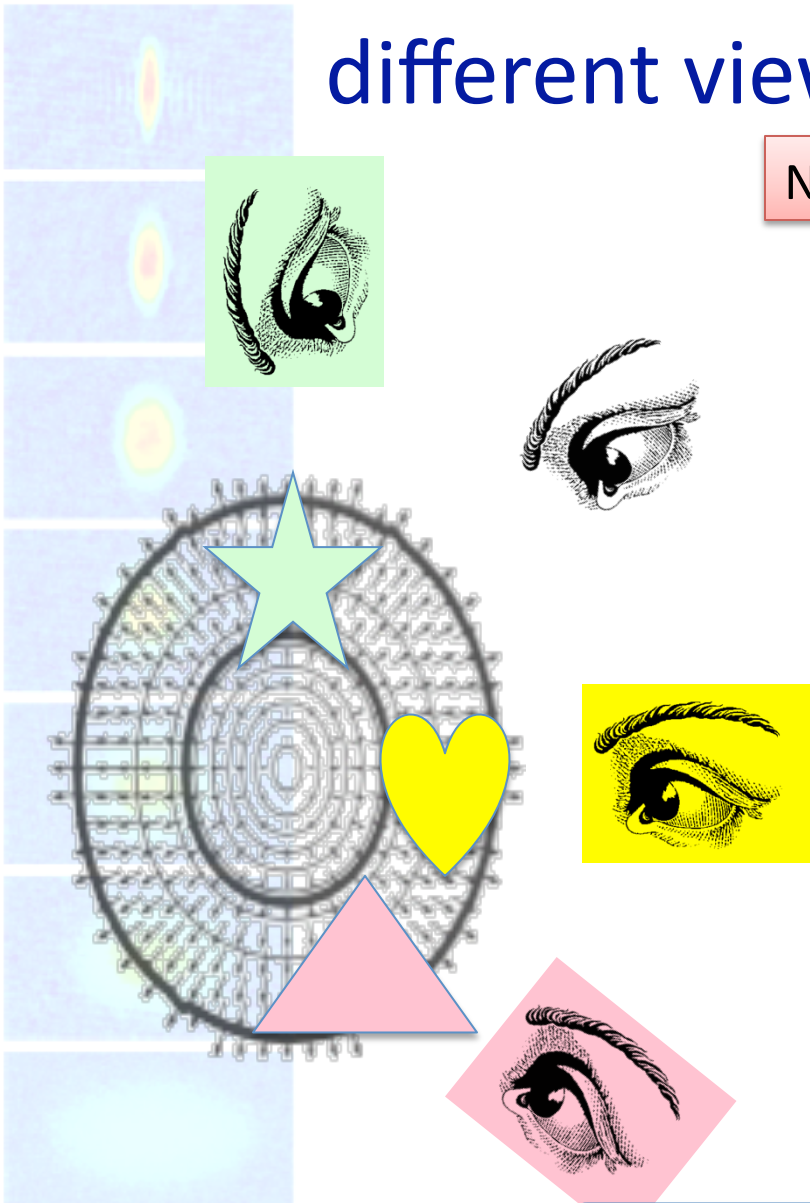


$$R_{s,n}^2 \equiv \langle R_s^2(\phi) \cdot \cos(n\phi) \rangle \quad \varepsilon = 2 \frac{R_{s,2}^2}{R_{s,0}^2} = 2 \frac{R_{os,2}^2}{R_{s,0}^2} = -2 \frac{R_{o,2}^2}{R_{s,0}^2}$$

Retiere&MAL PRC70 (2004) 044907

# different views of the “same” source?

No! Homogeneity regions can be totally different!



$$R_{s,n}^2 \equiv \langle R_s^2(\phi) \cdot \cos(n\phi) \rangle \quad \varepsilon = 2 \frac{R_{s,2}^2}{R_{s,0}^2} = 2 \frac{R_{os,2}^2}{R_{s,0}^2} = -2 \frac{R_{o,2}^2}{R_{s,0}^2}$$

Retiere&MAL PRC70 (2004) 044907



# White cow perspectives



There are white cows in Ohio!

There is a cow in Ohio, with one white side

There is a white cow in Ohio.

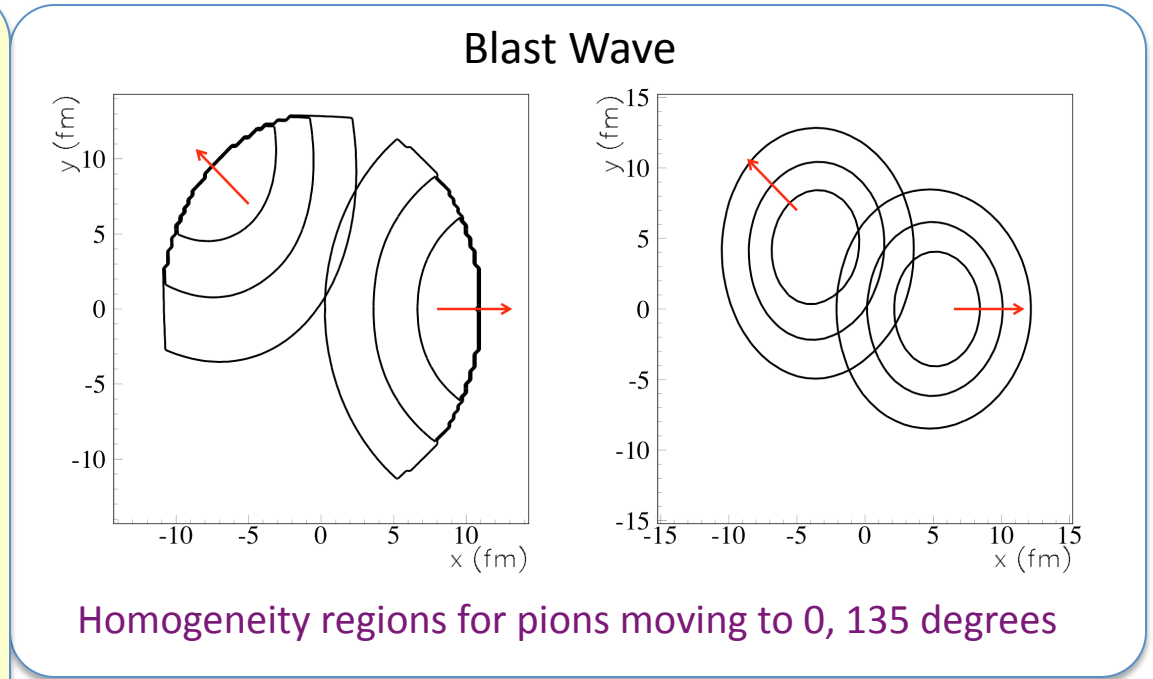
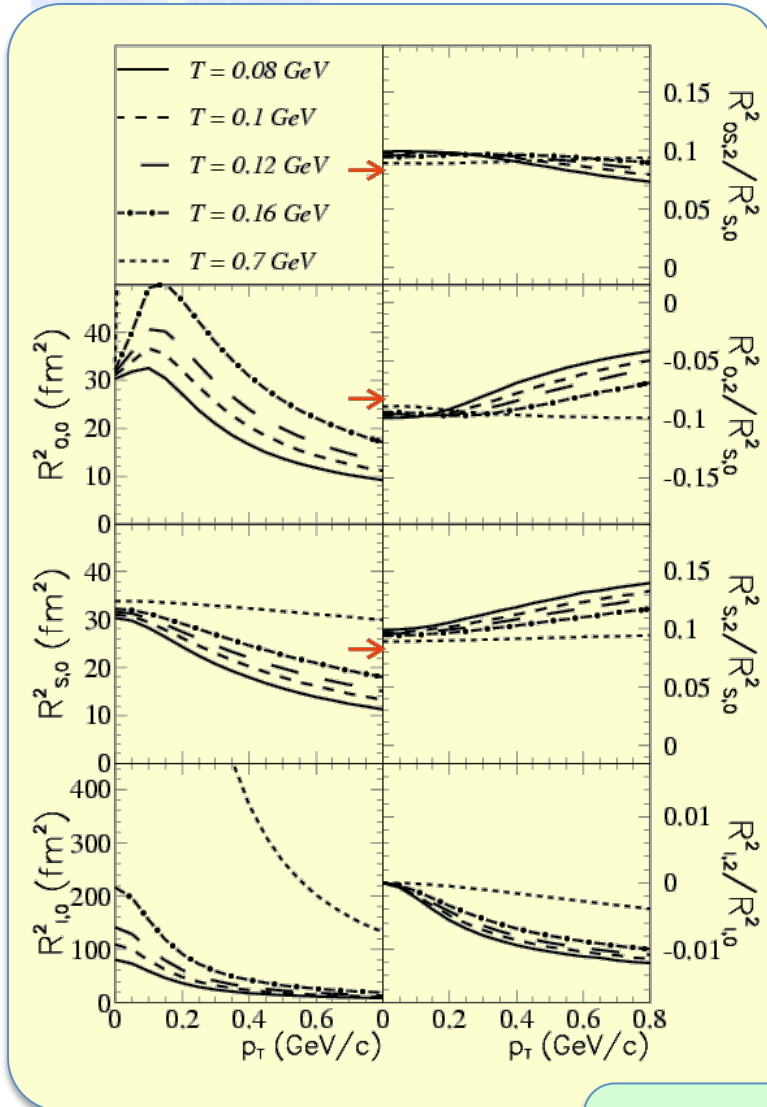
**(American) undergraduate**

**Mathematician**

**physicist**



# BW: "typical" model of flow-induced substructure

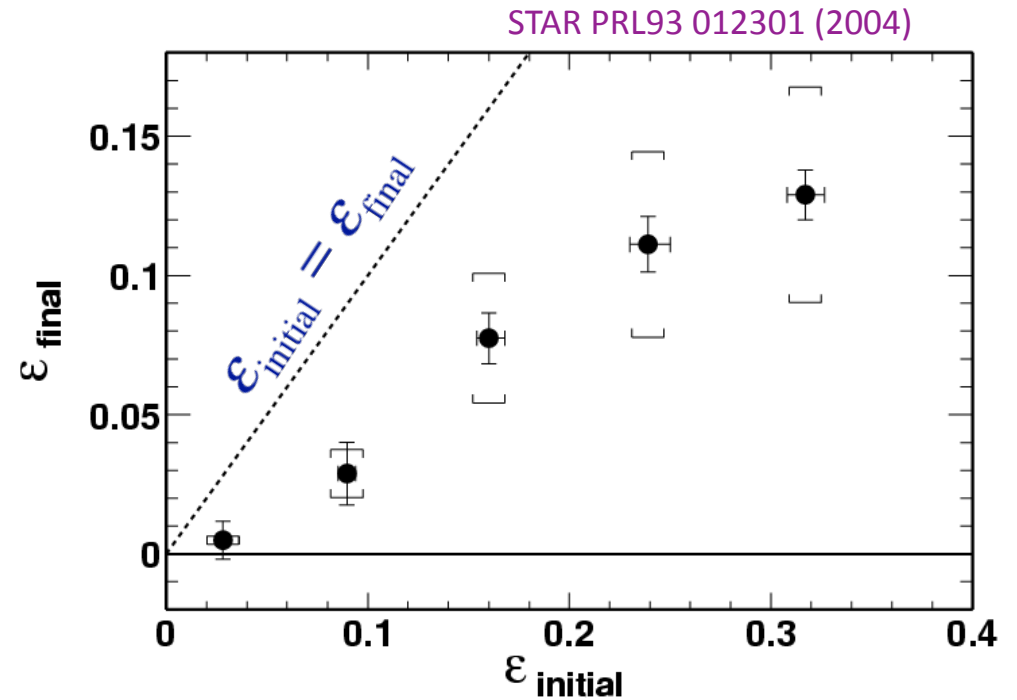
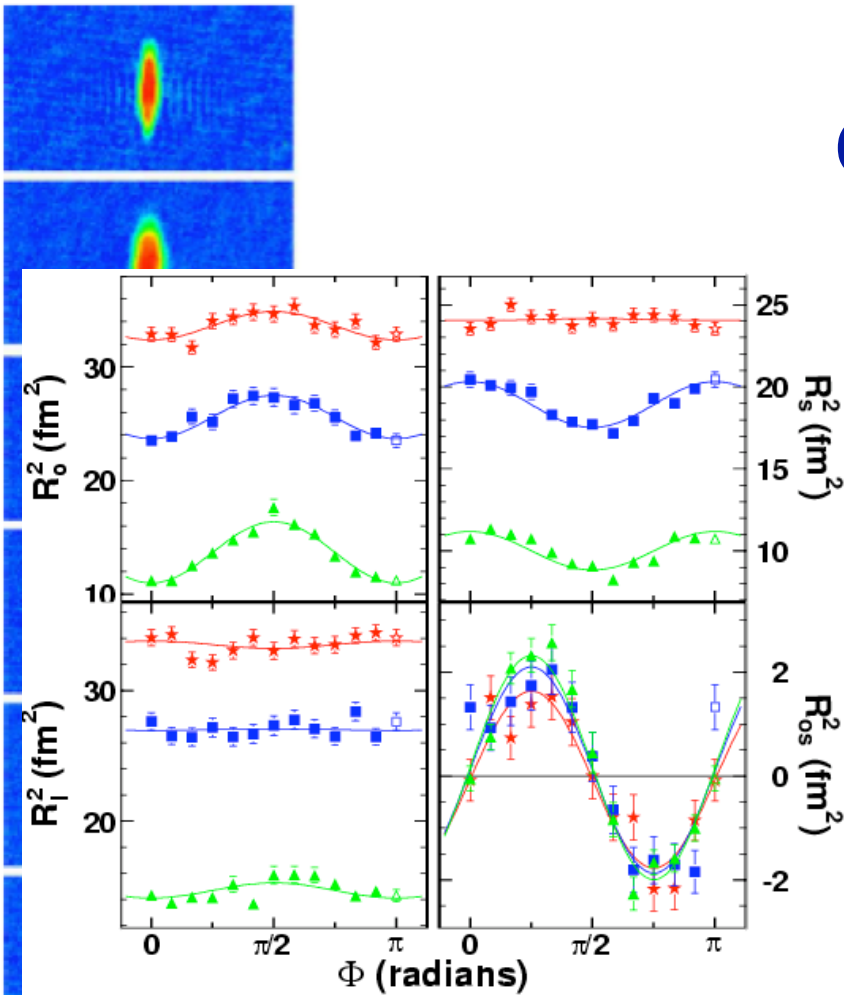


"No-flow formula" estimated good within ~ 30% (low pT)

$$R_{s,n}^2 \equiv \langle R_s^2(\phi) \cdot \cos(n\phi) \rangle \quad \varepsilon \approx 2 \frac{R_{s,2}^2}{R_{s,0}^2} \approx 2 \frac{R_{os,2}^2}{R_{s,0}^2} \approx -2 \frac{R_{o,2}^2}{R_{s,0}^2}$$

Retiere&MAL PRC70 (2004) 044907

# “Spatial elliptic flow”: Centrality Evolution at RHIC

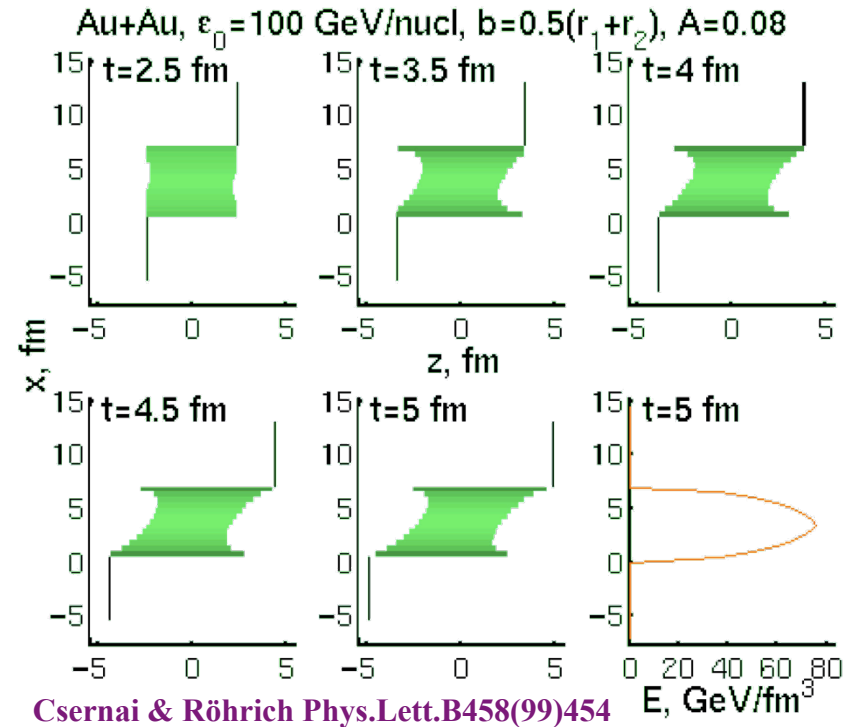
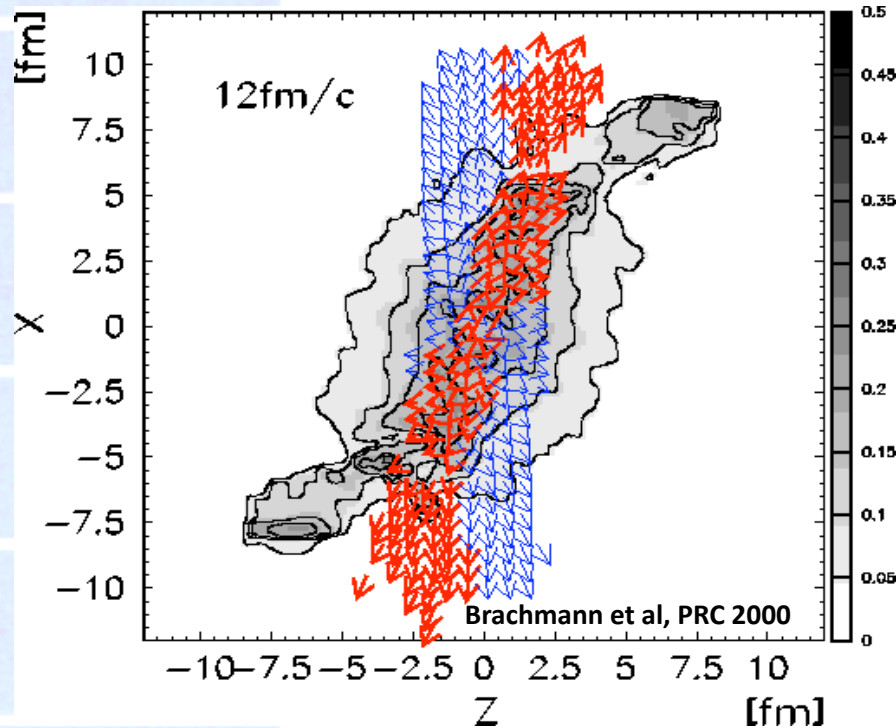


“No-flow formula” estimated good within  $\sim 30\%$  (low pT)

$$R_{s,n}^2 \equiv \langle R_s^2(\phi) \cdot \cos(n\phi) \rangle \quad \epsilon \approx 2 \frac{R_{s,2}^2}{R_{s,0}^2} \approx 2 \frac{R_{os,2}^2}{R_{s,0}^2} \approx -2 \frac{R_{o,2}^2}{R_{s,0}^2}$$

Retiere&MAL PRC70 (2004) 044907

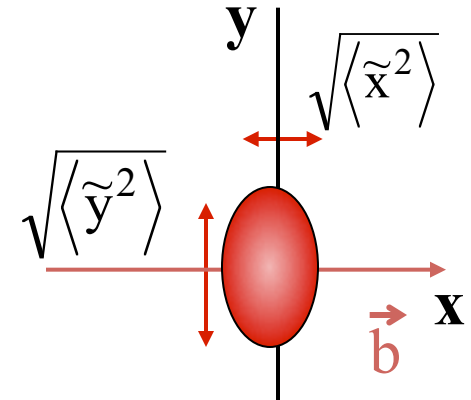
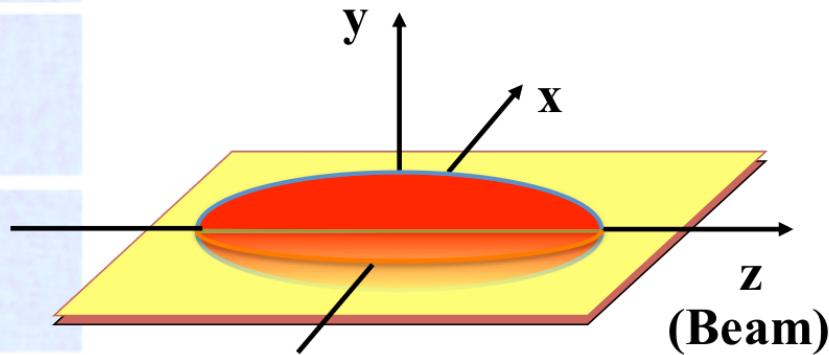
# Effects of “spatial directed flow?”



$$R_{s,n}^2 \equiv \langle R_s^2(\phi) \cdot \cos(n\phi) \rangle \quad \epsilon \approx 2 \frac{R_{s,2}^2}{R_{s,0}^2} \approx 2 \frac{R_{os,2}^2}{R_{s,0}^2} \approx -2 \frac{R_{o,2}^2}{R_{s,0}^2}$$

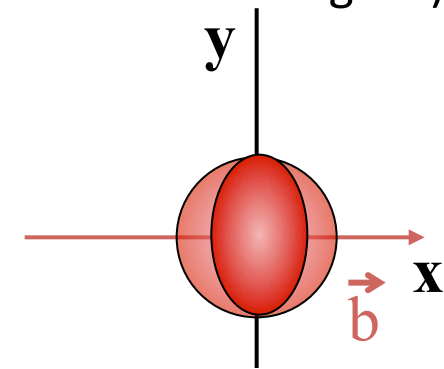
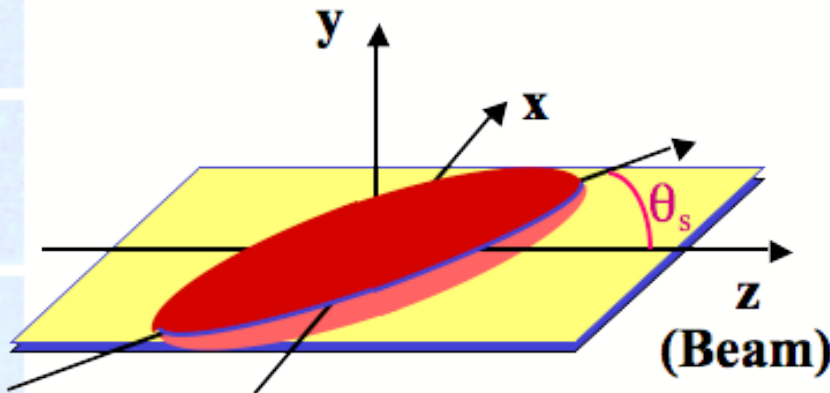
Retiere&MAL PRC70 (2004) 044907

# Effects of “spatial *directed* flow?”



**Tilt angle  $\theta_s$**  – analog of “flow angle”

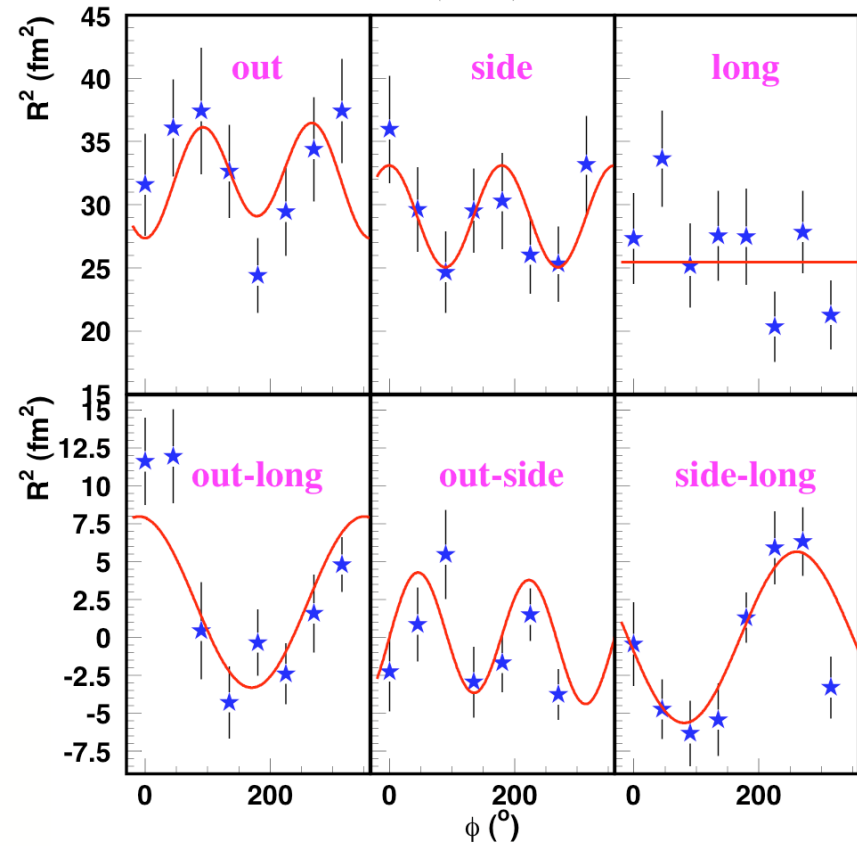
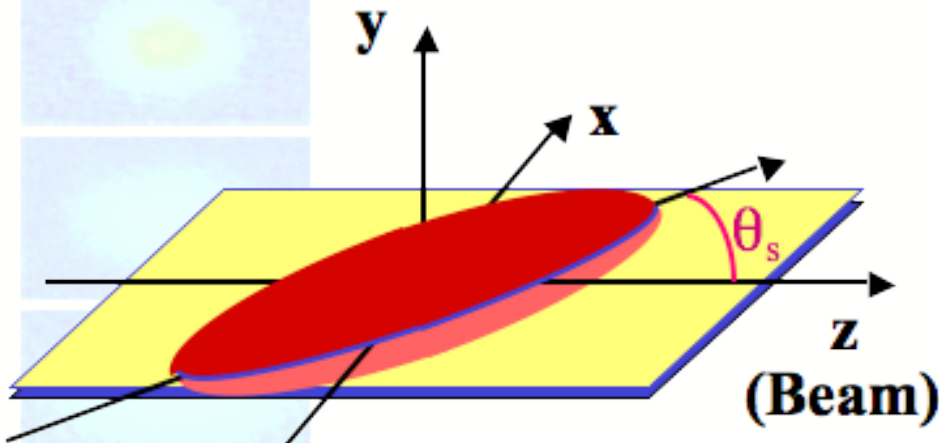
(... and “squeezeout” should be referenced to flow angle...)



$$R_{s,n}^2 \equiv \langle R_s^2(\phi) \cdot \cos(n\phi) \rangle \quad \varepsilon \approx 2 \frac{R_{s,2}^2}{R_{s,0}^2} \approx 2 \frac{R_{os,2}^2}{R_{s,0}^2} \approx -2 \frac{R_{o,2}^2}{R_{s,0}^2}$$

# first-order oscillations reveal large tilts @ AGS

First-order R.P. needed

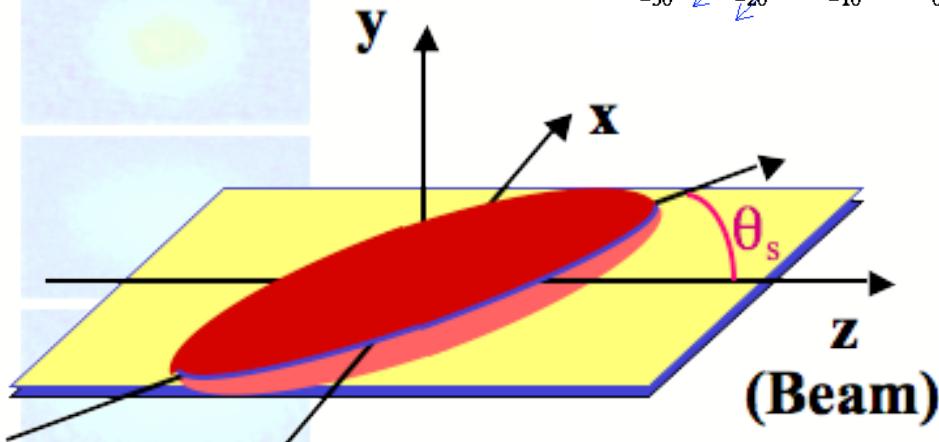
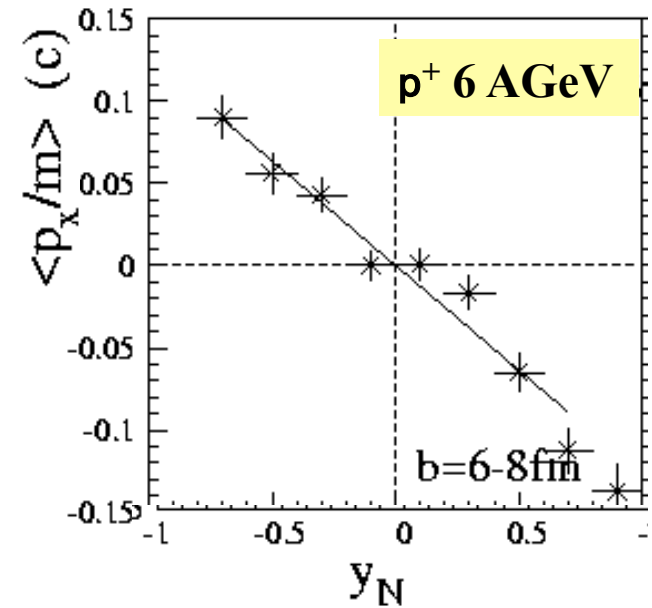
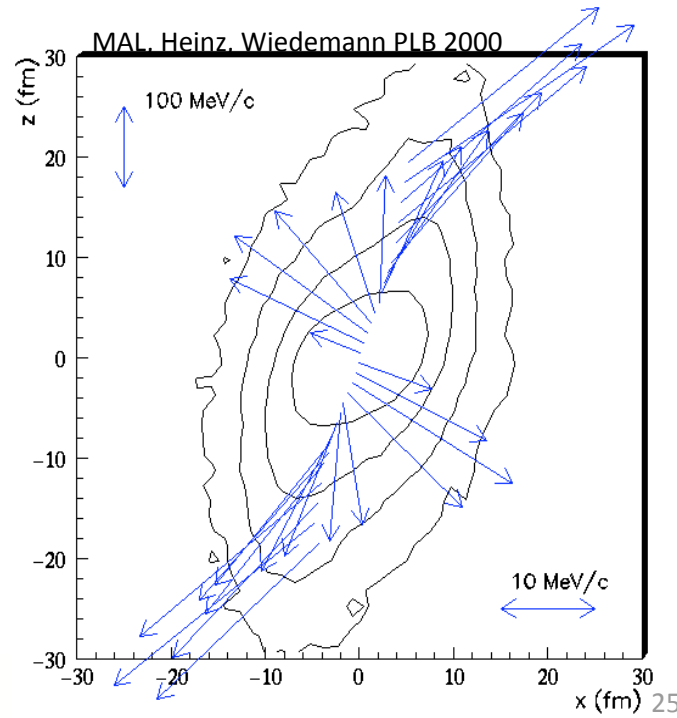




# first-order oscillations reveal large tilts @ AGS

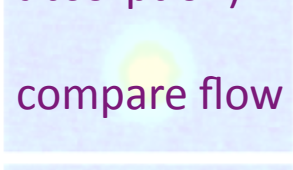
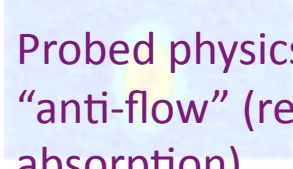
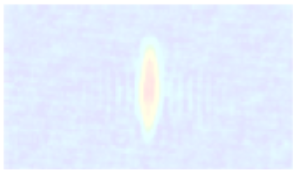
First-order R.P. needed

Probed physics *behind* pion  
“anti-flow” (reflection, not absorption)



# large tilts @ AGS

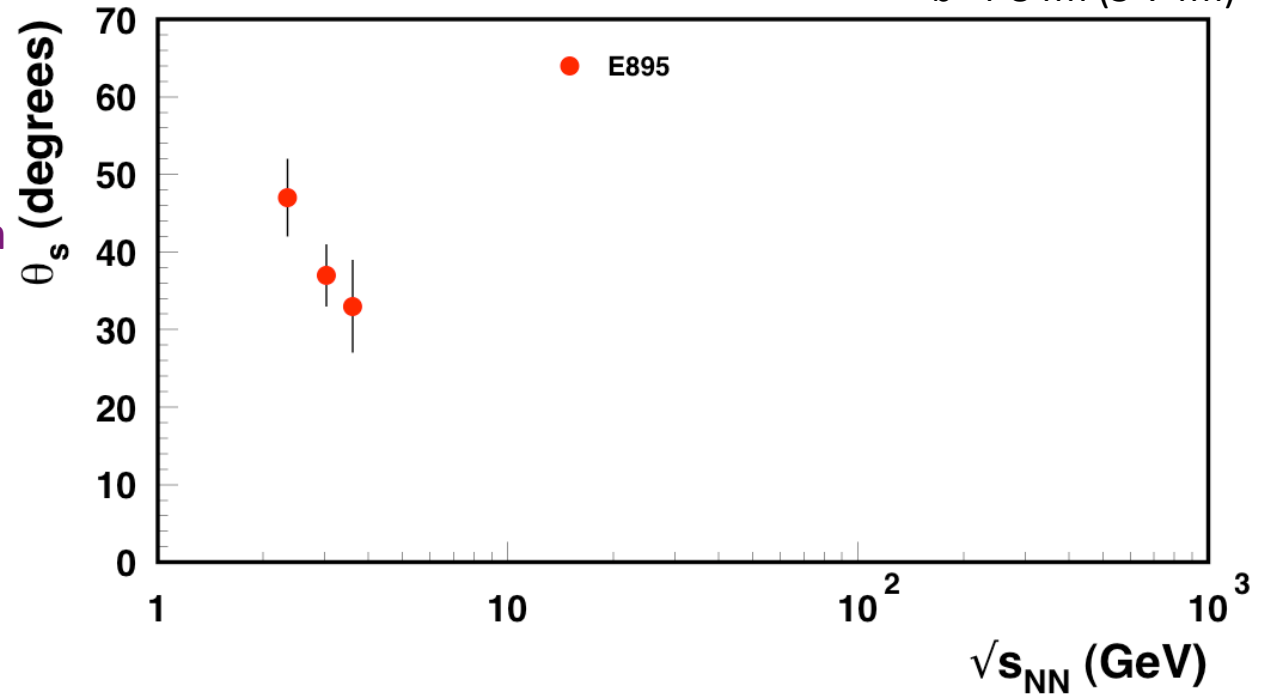
b=4-8 fm (5-7 fm)



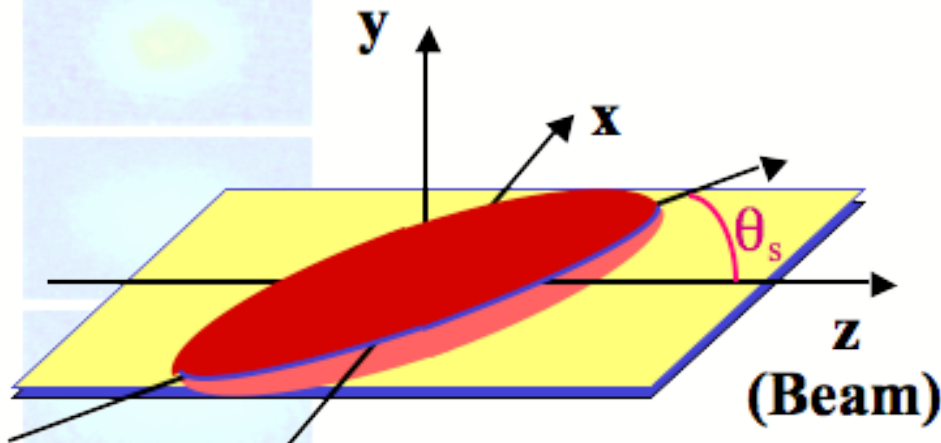
First-order R.P. needed

Probed physics *behind* pion  
“anti-flow” (reflection, not  
absorption)

compare flow angle  $\sim 1^\circ$

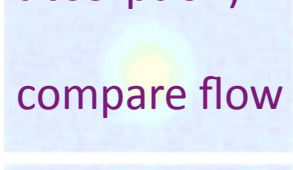
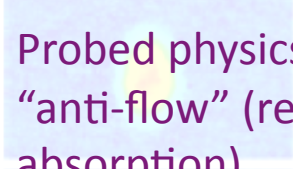
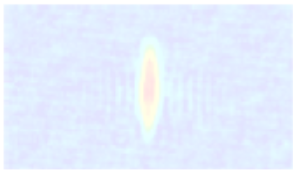


- $\theta_s$  large, falls rapidly



# models: large tilts @ AGS

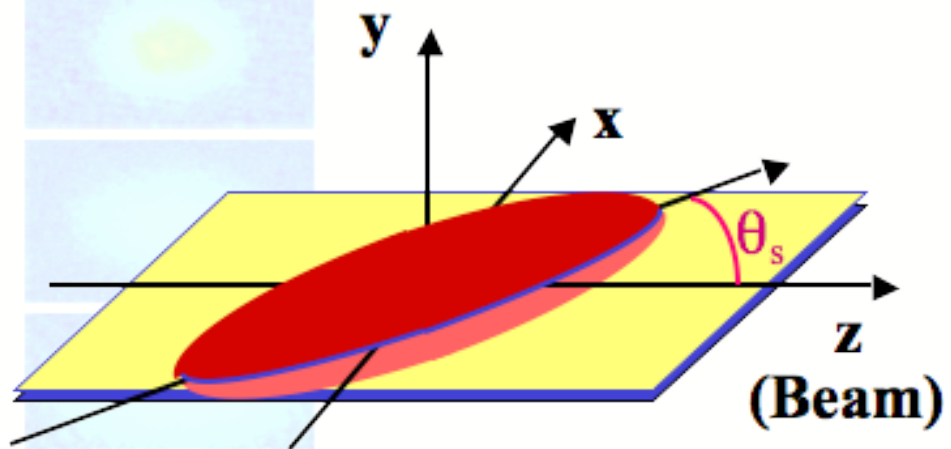
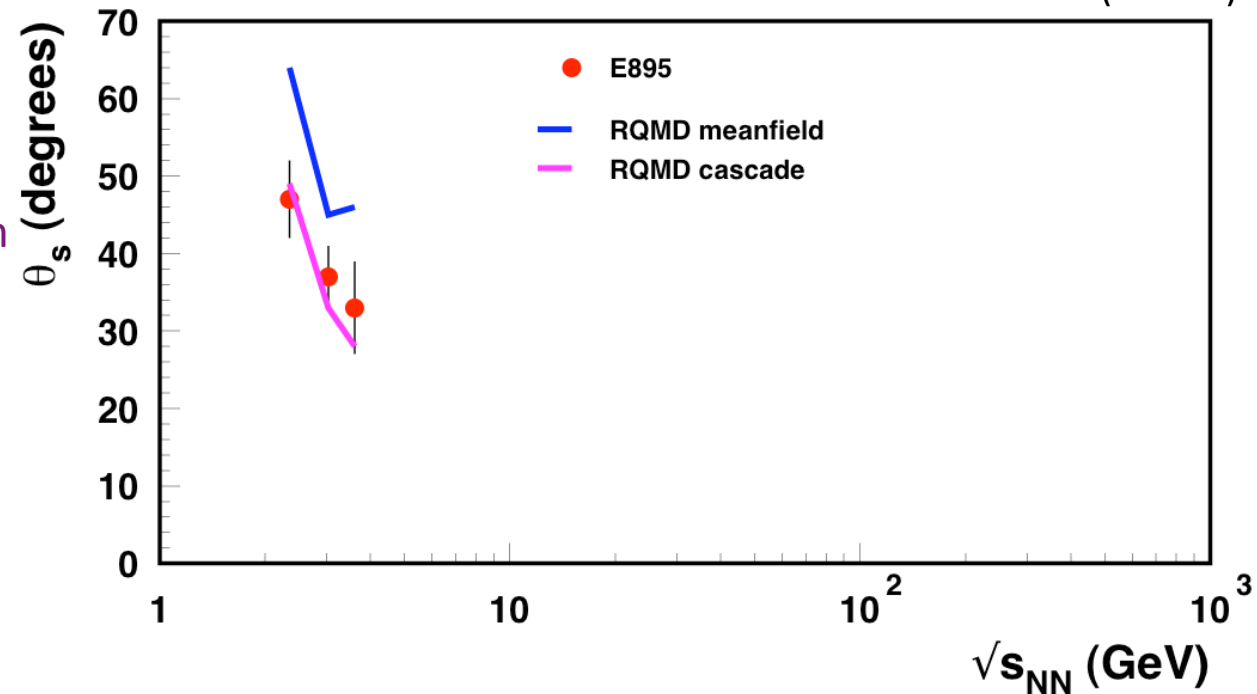
b=4-8 fm (5-7 fm)



First-order R.P. needed

Probed physics *behind* pion  
“anti-flow” (reflection, not  
absorption)

compare flow angle  $\sim 1^\circ$



- $\theta_s$  large, falls rapidly
- spatial tilt disfavors mf, contrary directed flow

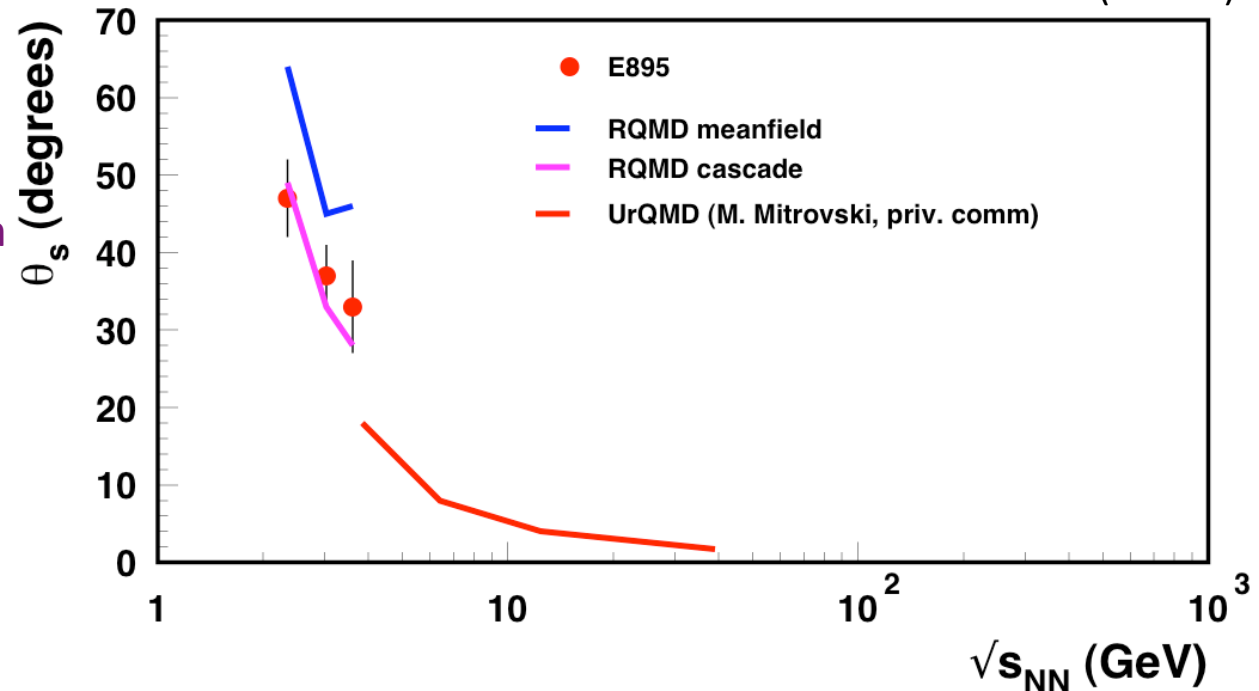
# models: large tilts @ AGS

b=4-8 fm (5-7 fm)

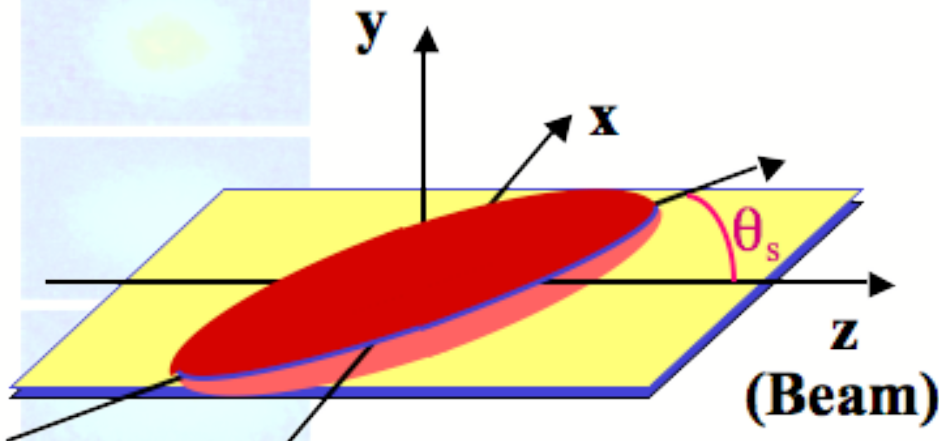
First-order R.P. needed

Probed physics *behind* pion  
“anti-flow” (reflection, not  
absorption)

compare flow angle  $\sim 1^\circ$

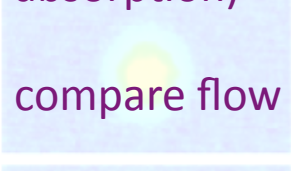
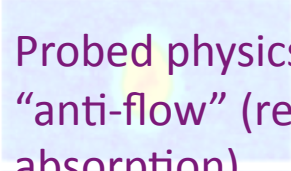
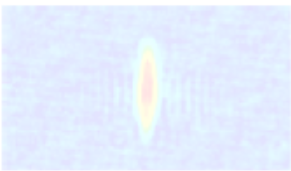


- $\theta_s$  large, falls rapidly
- spatial tilt disfavors mf, contrary directed flow



# models: large tilts @ AGS

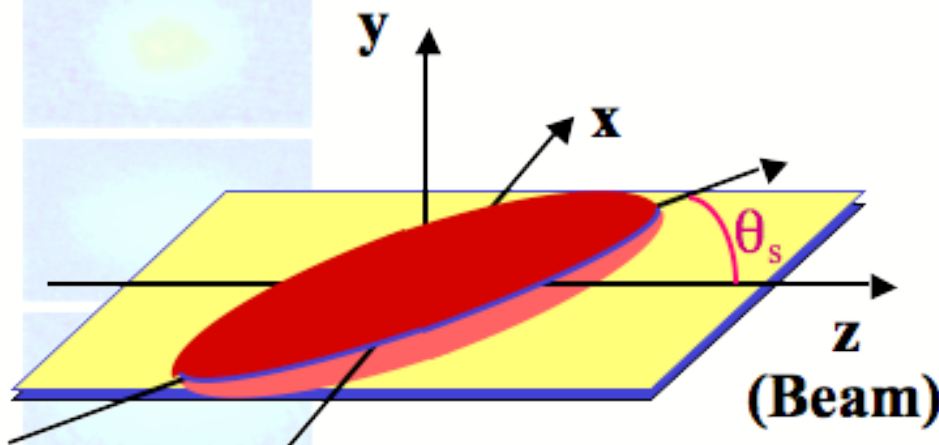
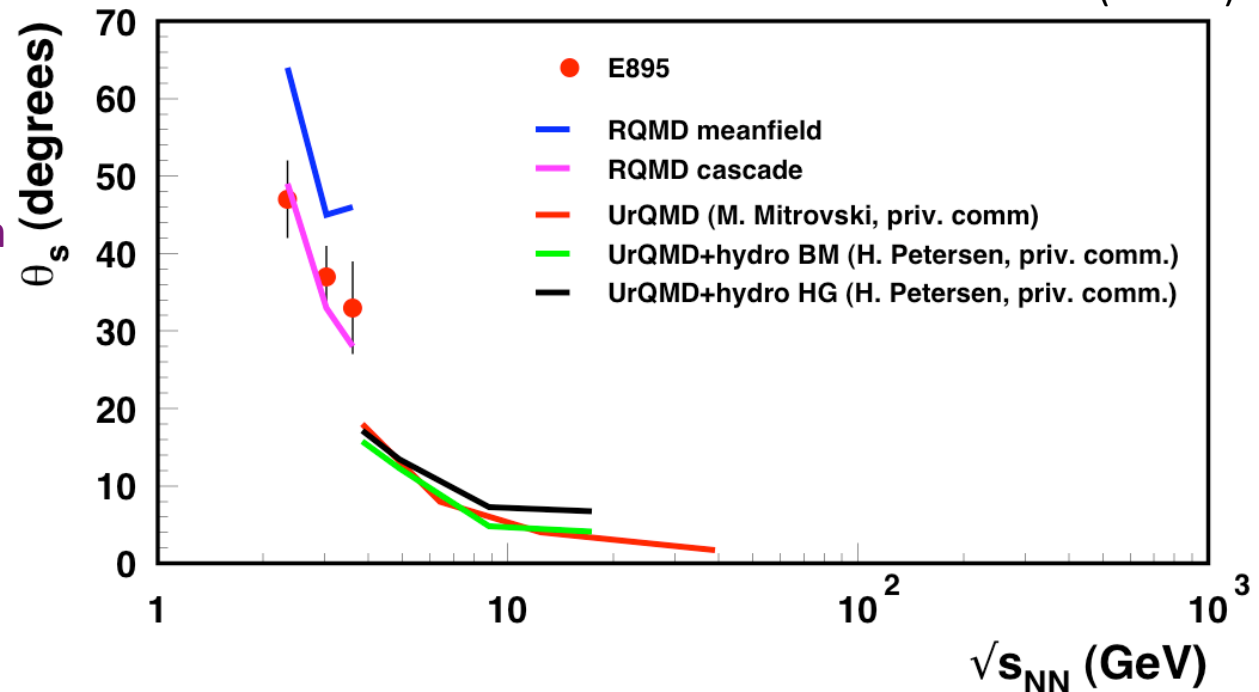
$b=4-8$  fm (5-7 fm)



First-order R.P. needed

Probed physics *behind* pion  
“anti-flow” (reflection, not absorption)

compare flow angle  $\sim 1^\circ$



- $\theta_s$  large, falls rapidly
- spatial tilt disfavors mf, contrary directed flow
- significantly lower tilt (too low?) predicted by UrQMD & hybrids
- RHIC energies – probably negligible
  - **2D hydro OK?**
- **SPS?**

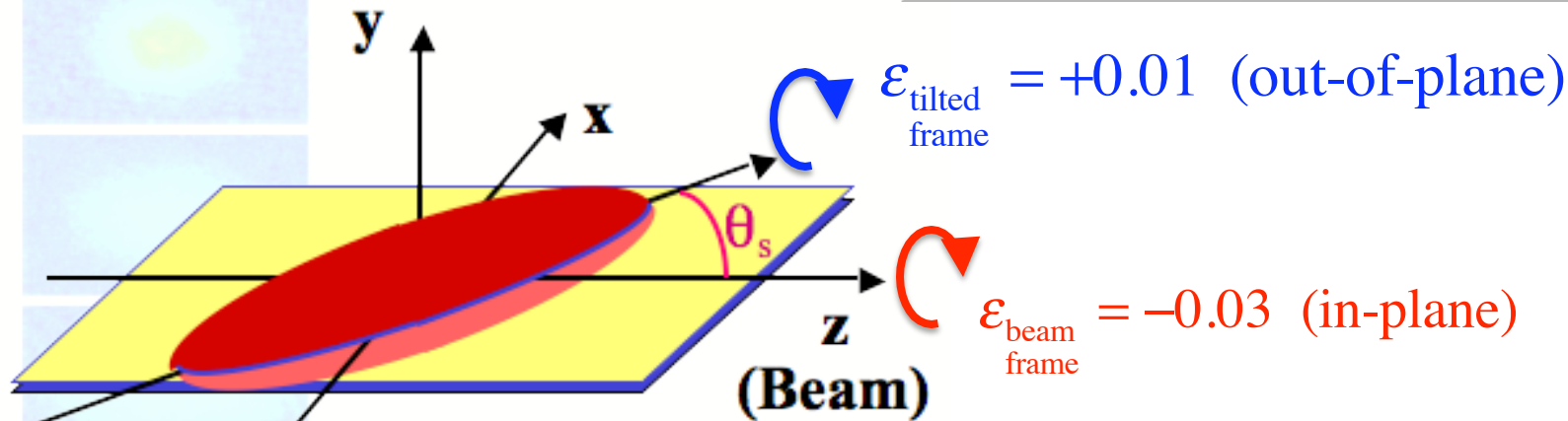
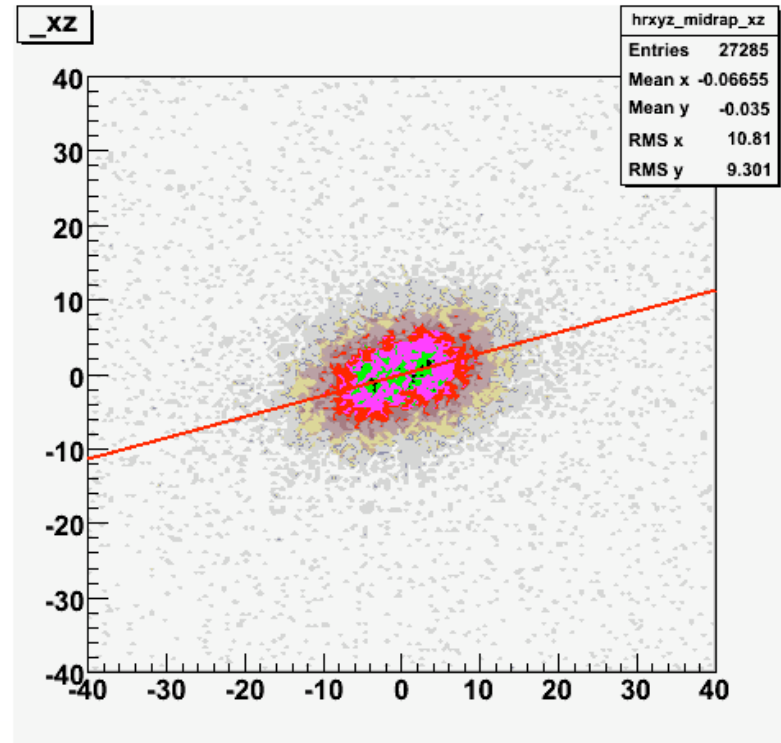


# complications from large tilts?

## measurement:

UrQMD+hydro[BM]@ 3.8 GeV:

$\varepsilon$  in non-natural frame  
significantly reduced from  $\varepsilon$  in  
natural (tilted) frame  
affects CERES measurement?



# complications from large tilts?

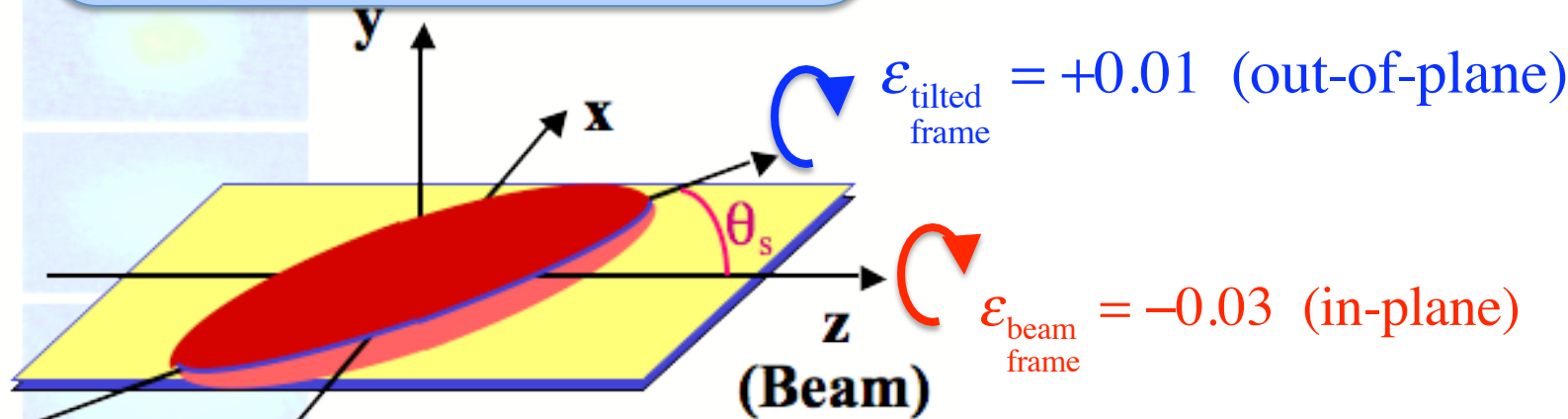
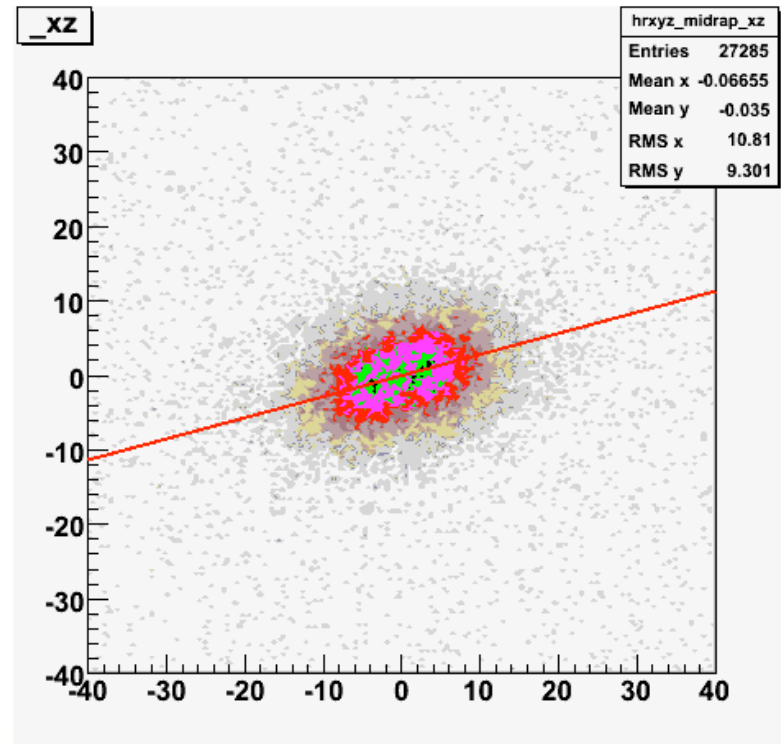
## measurement:

UrQMD+hydro[BM]@ 3.8 GeV:

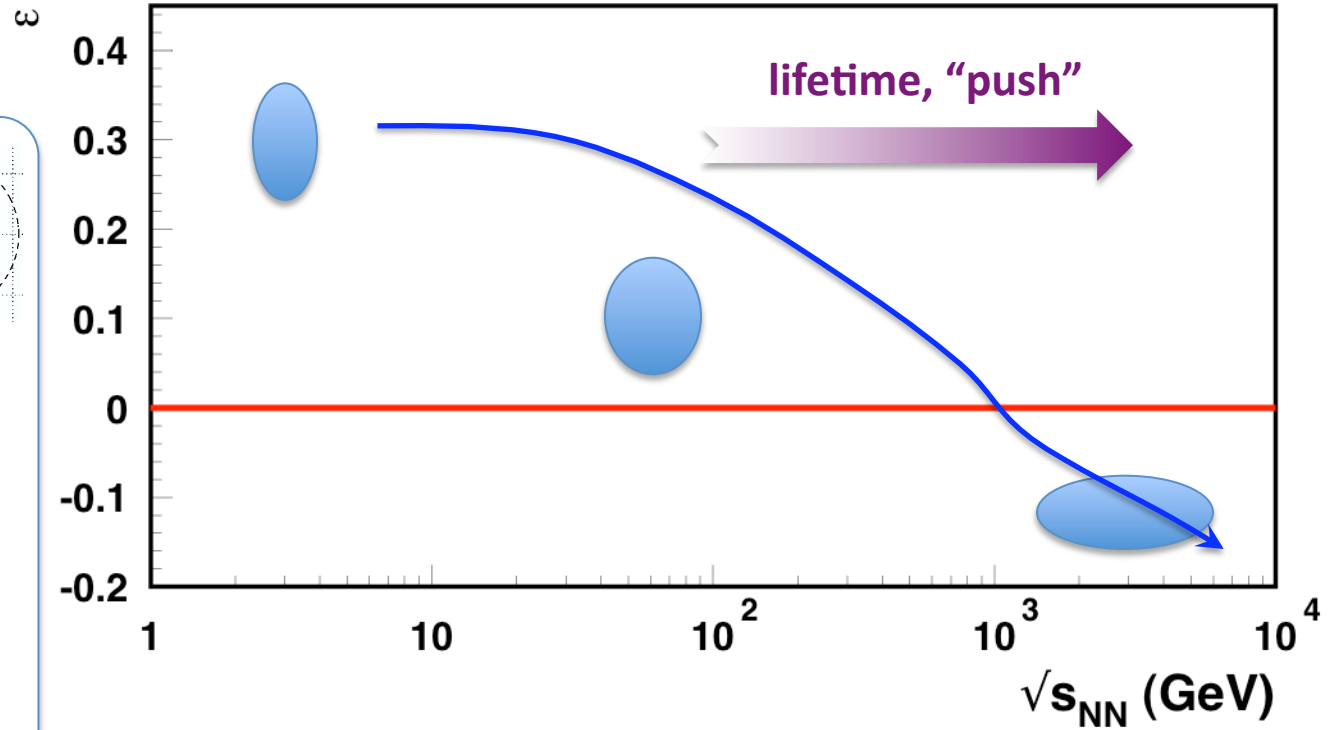
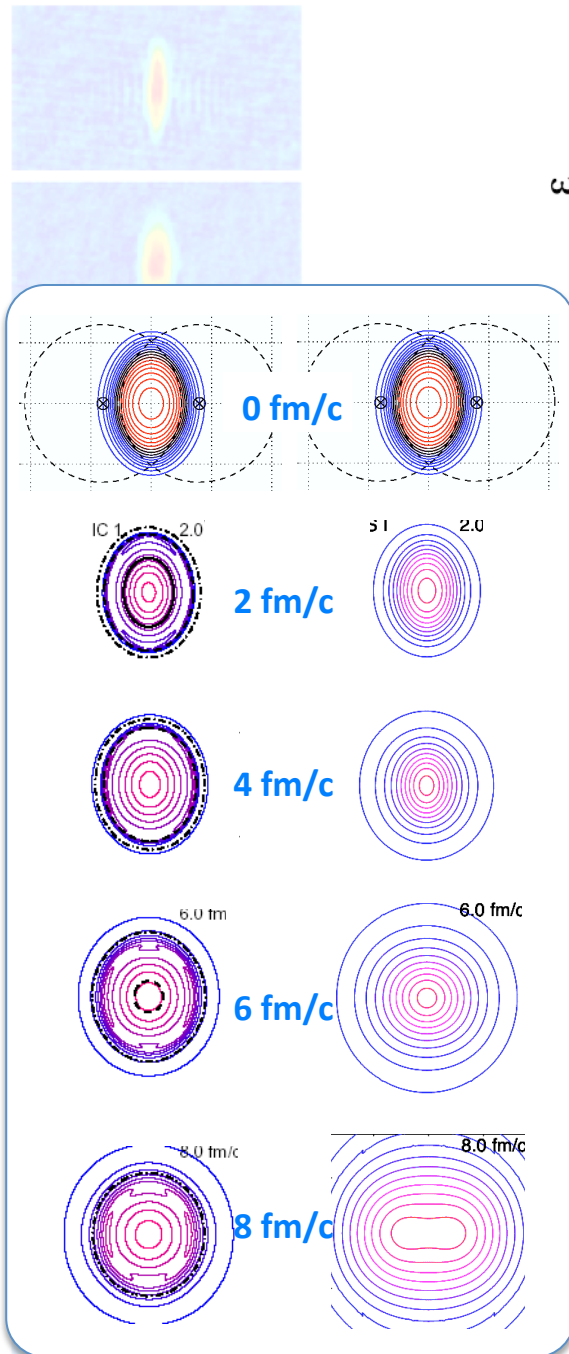
$\varepsilon$  in non-natural frame  
significantly reduced from  $\varepsilon$  in  
natural (tilted) frame  
affects CERES measurement?

## transport

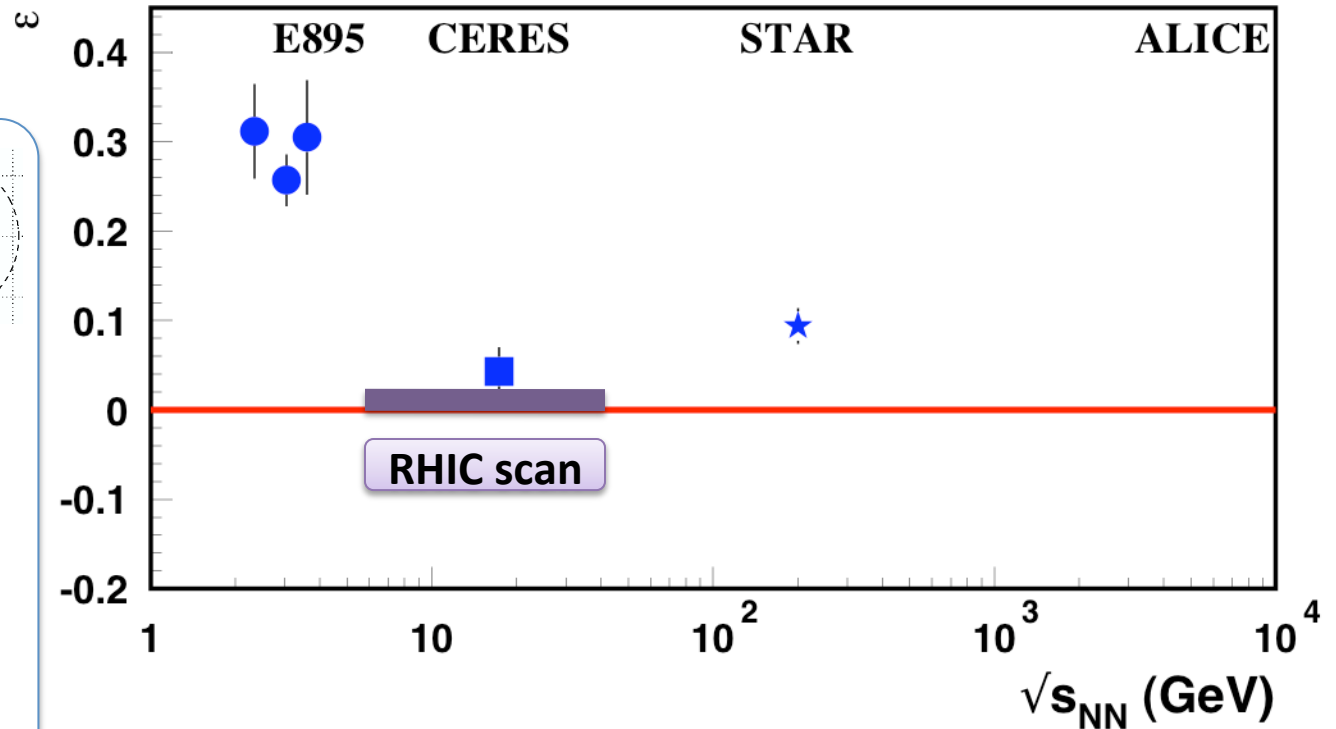
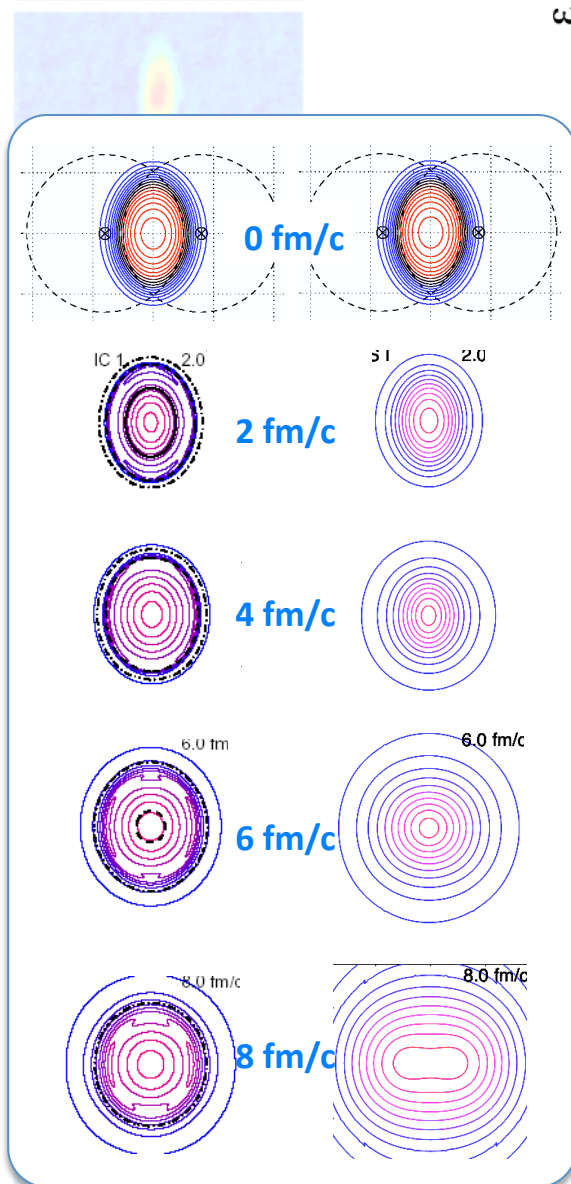
Tilts are manifestly “boost variant,”  
in *space* even *at*  $y=0$   
2D hydro codes?



# Generic expectation

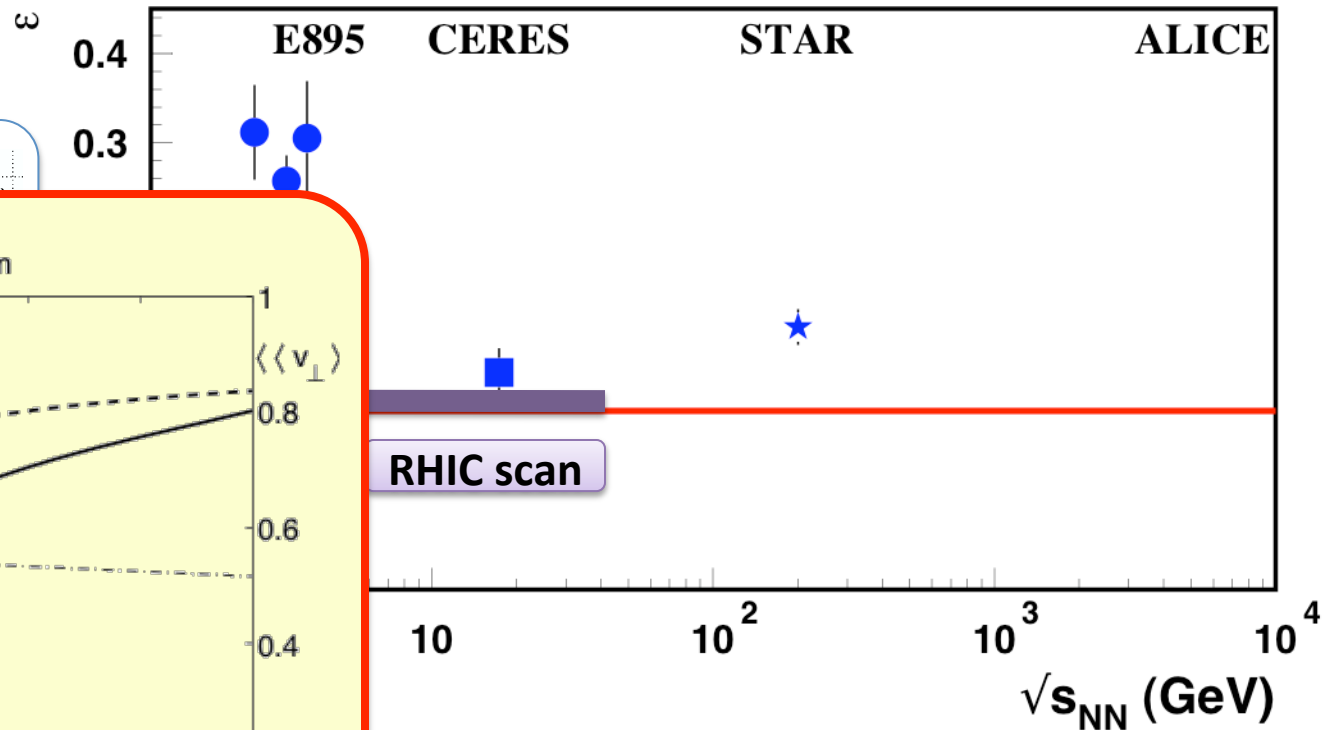
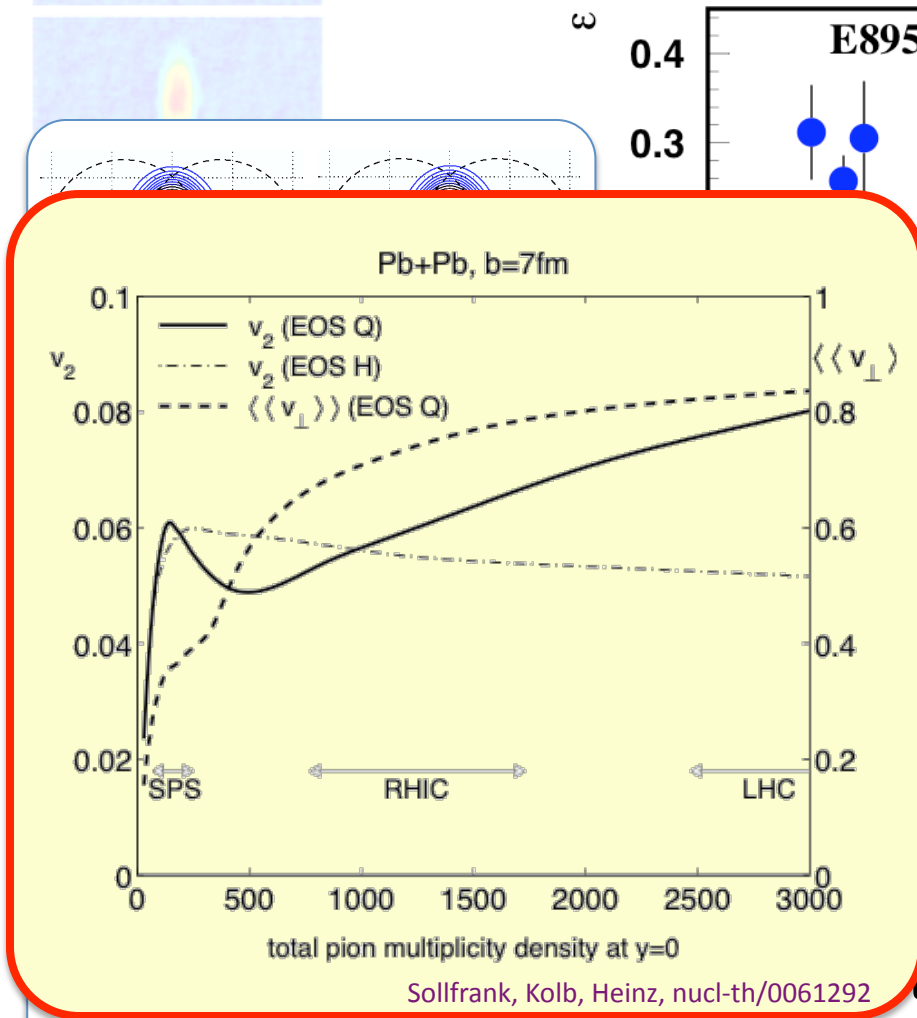


# An excitation function begging for more



- non-monotonic excitation function of bulk observable?
  - interesting in proposed scan region
  - **but**: tilt issue – need 1<sup>st</sup>-order plane in scan!!

# An excitation function begging for more

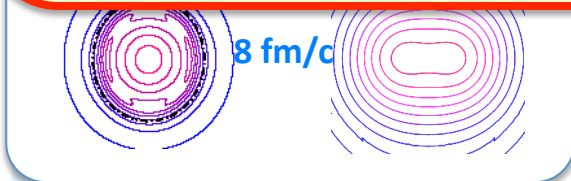


Excitation function of bulk observable?

Missing in proposed scan region

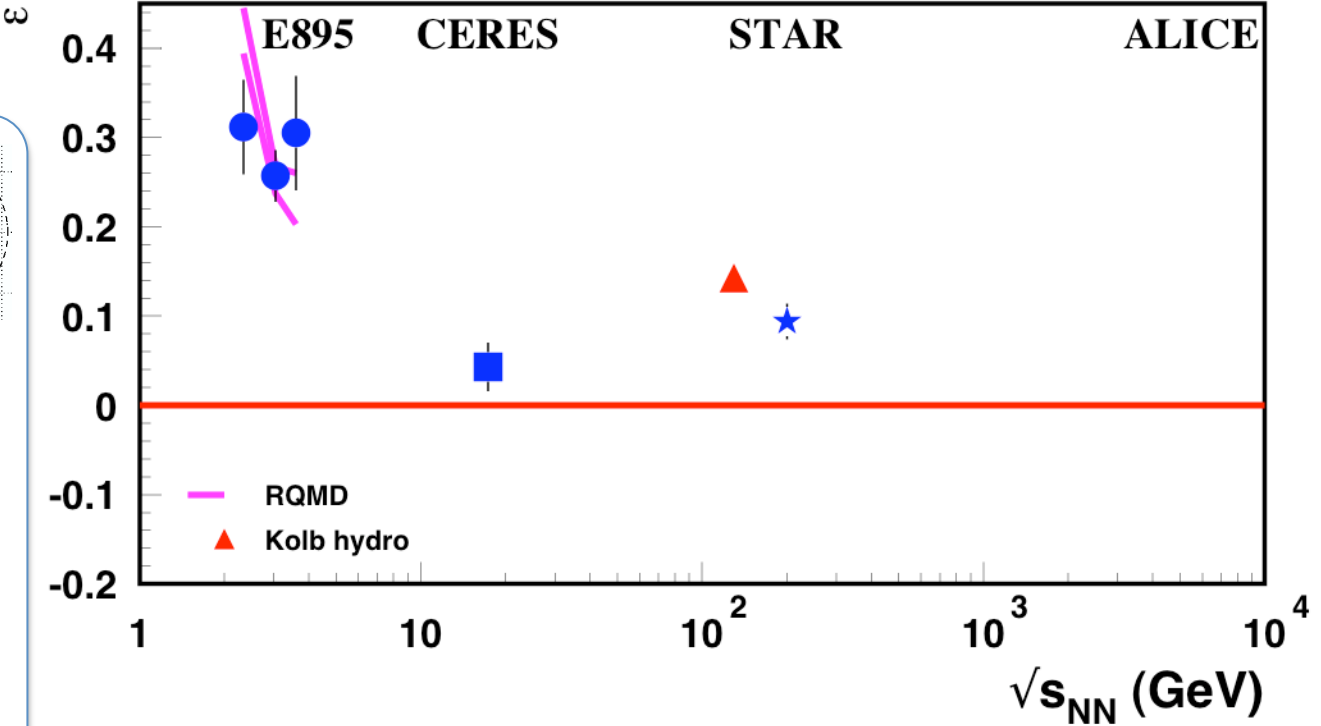
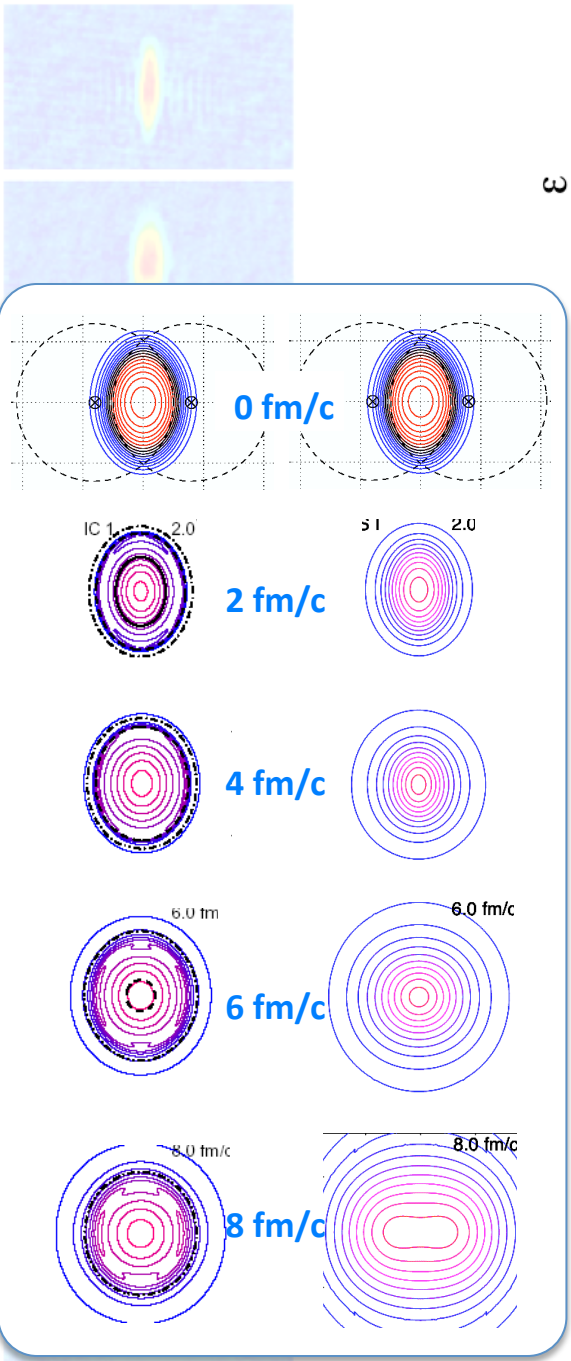
Key issue – need 1<sup>st</sup>-order plane in scan!!

- reminiscent of (unobserved) non-monotonic  $v_2(\sqrt{s})$



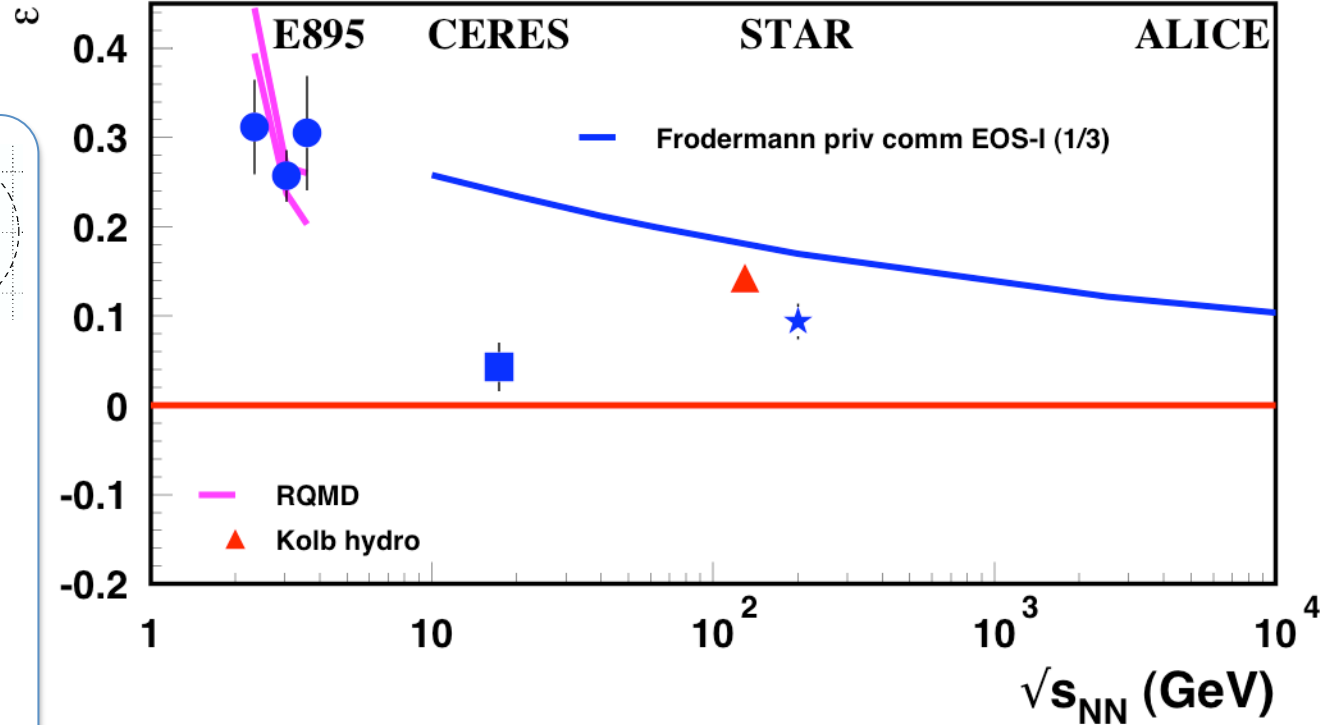
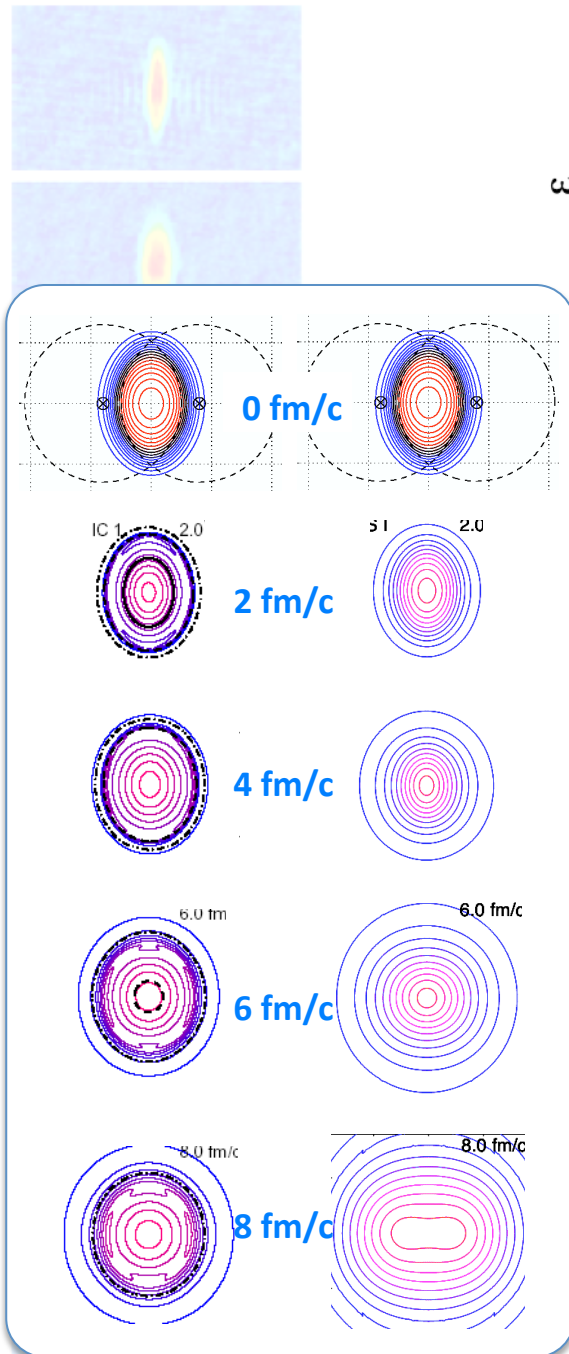


# Model comparisons



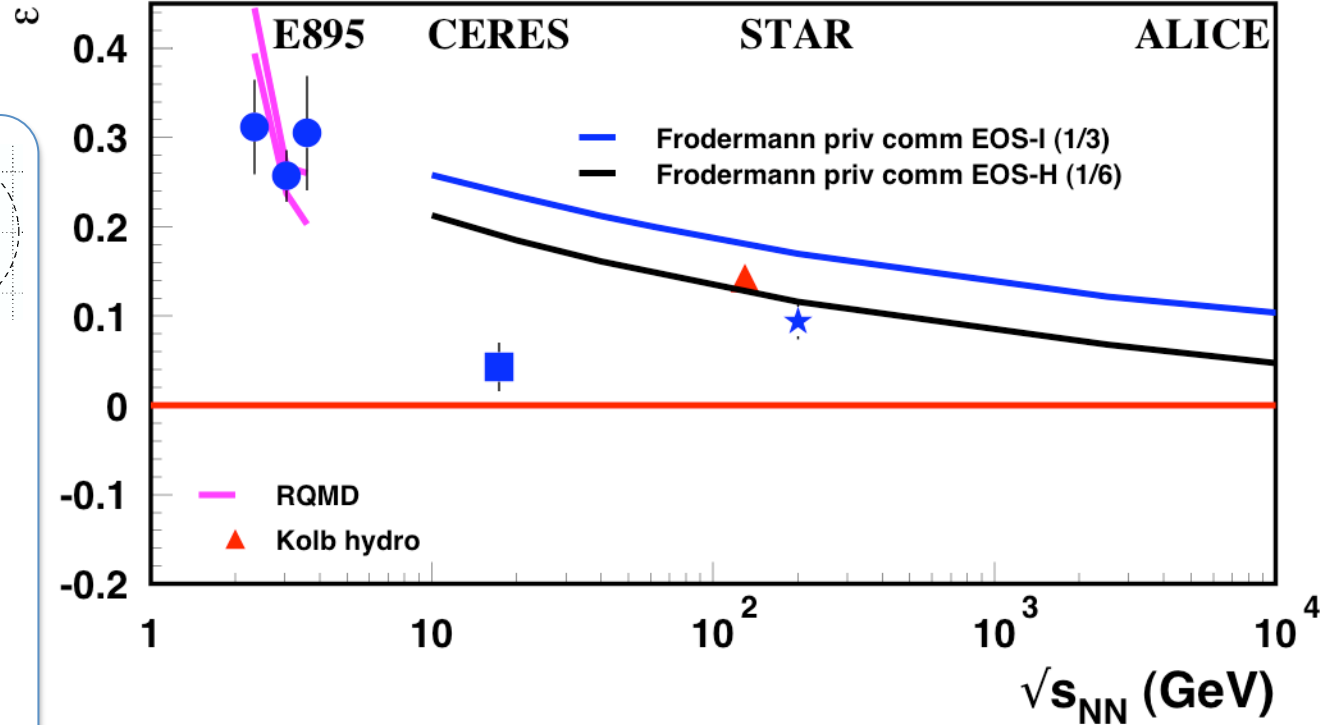
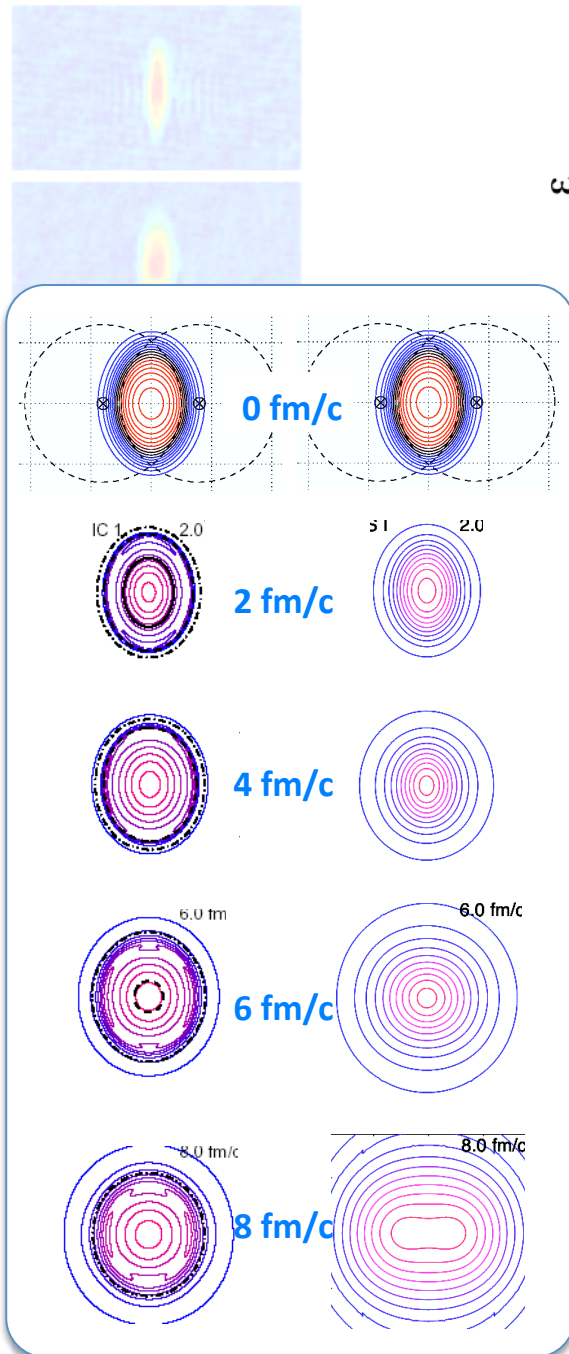
- ✓ RQMD (not UrQMD) @ low energy
- ✓ 2D hydro of Kolb/Heinz @ RHIC

# effect of EoS – 2D hydro



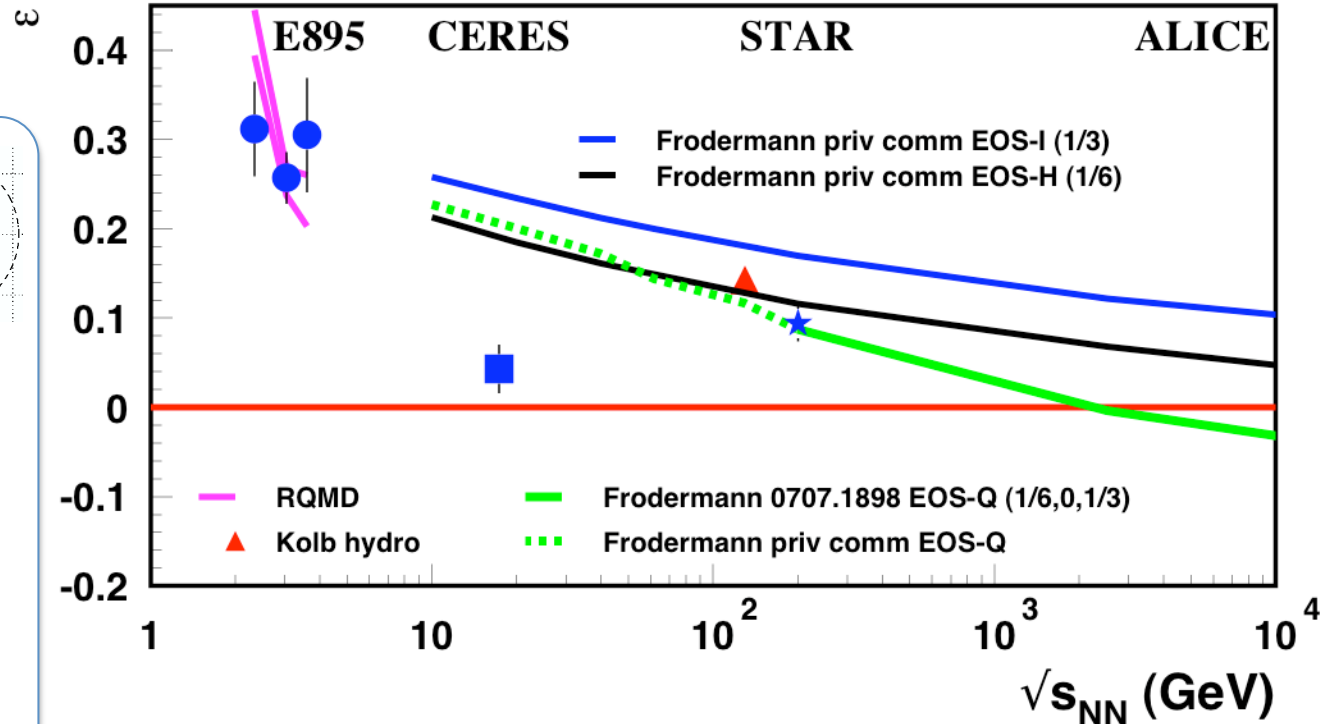
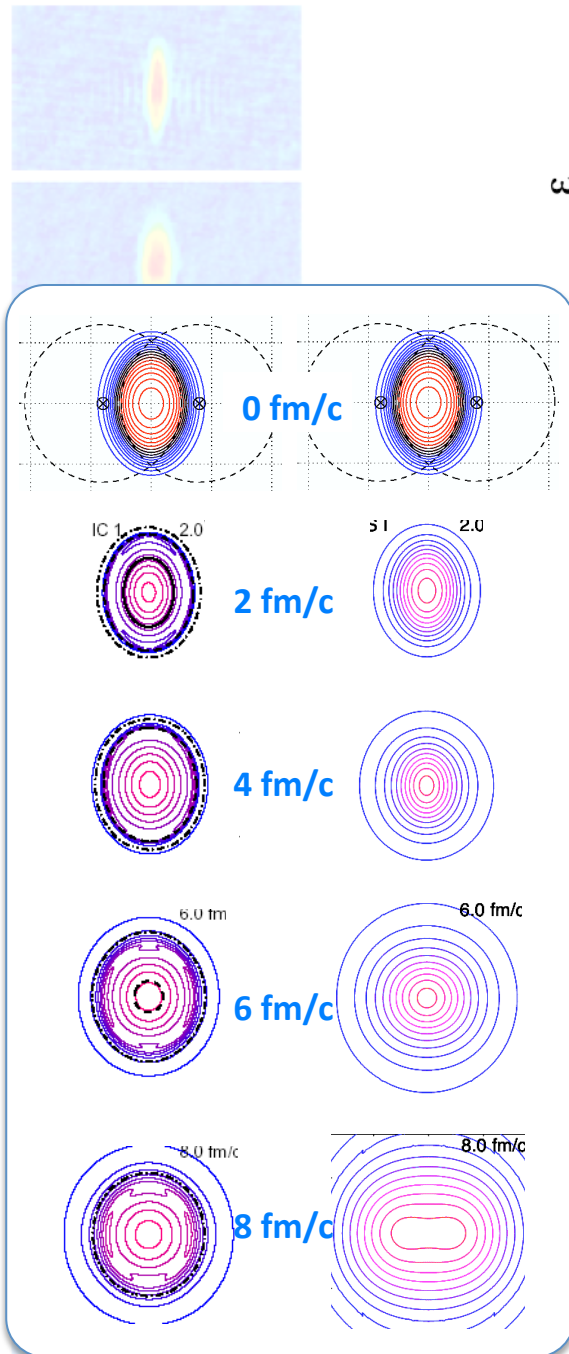
- ✓ RQMD (not UrQMD) @ low energy
- ✓ 2D hydro of Kolb/Heinz @ RHIC
- scan with varying EoS 2D hydro

# effect of EoS – 2D hydro



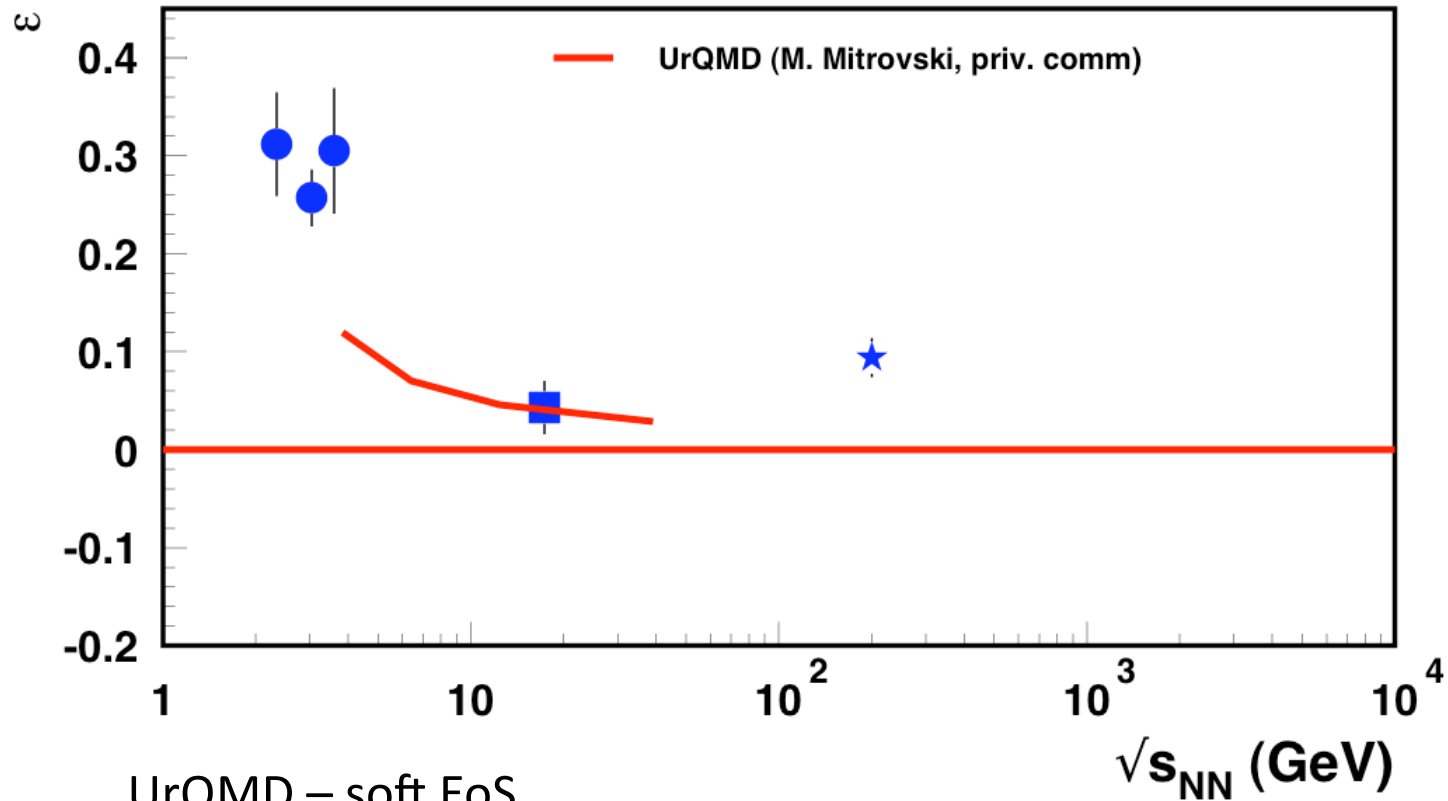
- ✓ RQMD (not UrQMD) @ low energy
- ✓ 2D hydro of Kolb/Heinz @ RHIC
- scan with varying EoS 2D hydro

# effect of EoS – 2D hydro



- ✓ RQMD (not UrQMD) @ low energy
- ✓ 2D hydro of Kolb/Heinz @ RHIC
- scan with varying EoS 2D hydro
  - dependence on stiffness stresses lifetime
  - no non-monotonic behaviour predicted
  - **but**: 2D boost-invariant – no tilt

# 3D transport

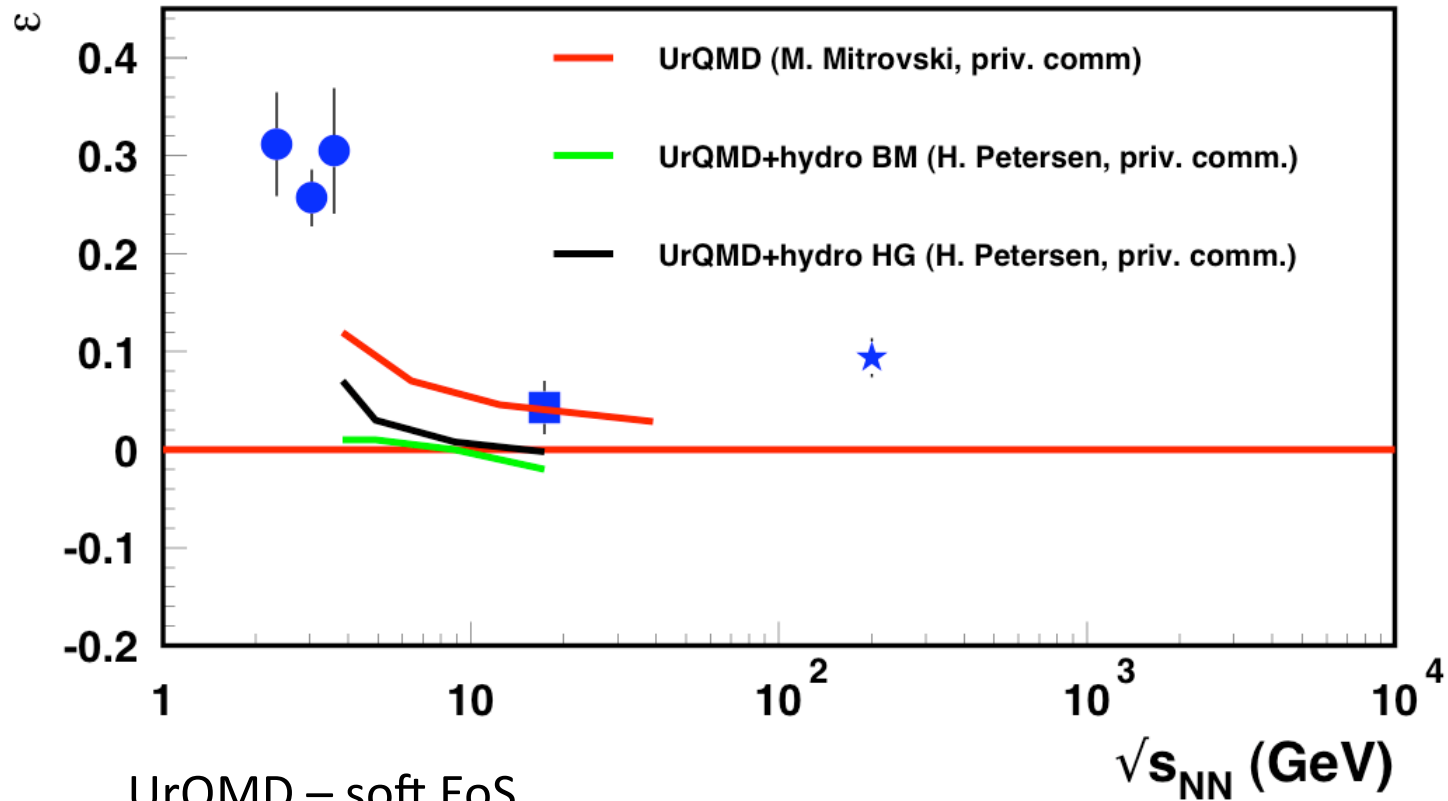


UrQMD – soft EoS

- ✓ reproduces CERES' anisotropy
- root(s) dependence looks unlikely



# 3D transport

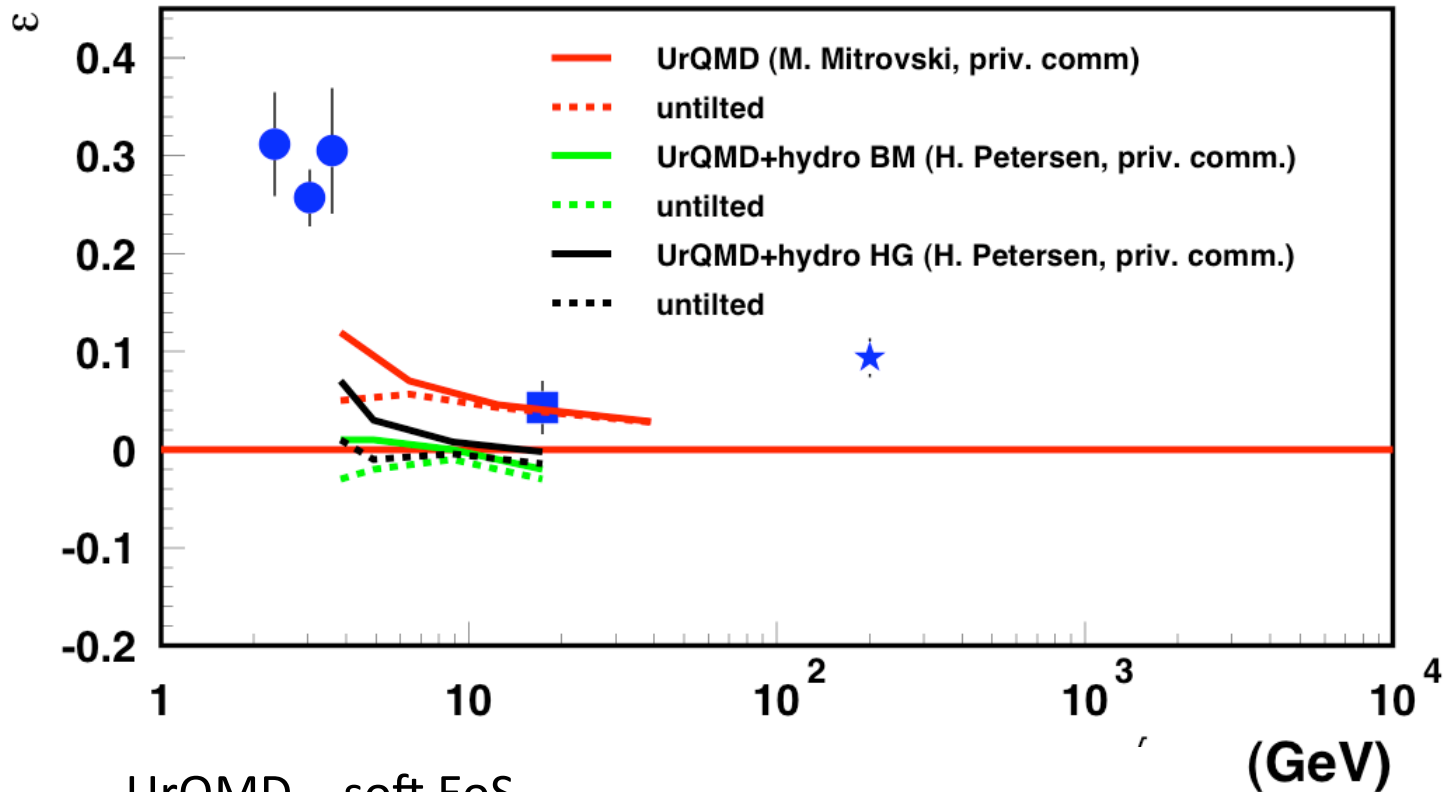


UrQMD – soft EoS

- ✓ reproduces CERES' anisotropy
- root(s) dependence looks unlikely

hybrid models: long-lived system evolves to round

# 3D transport



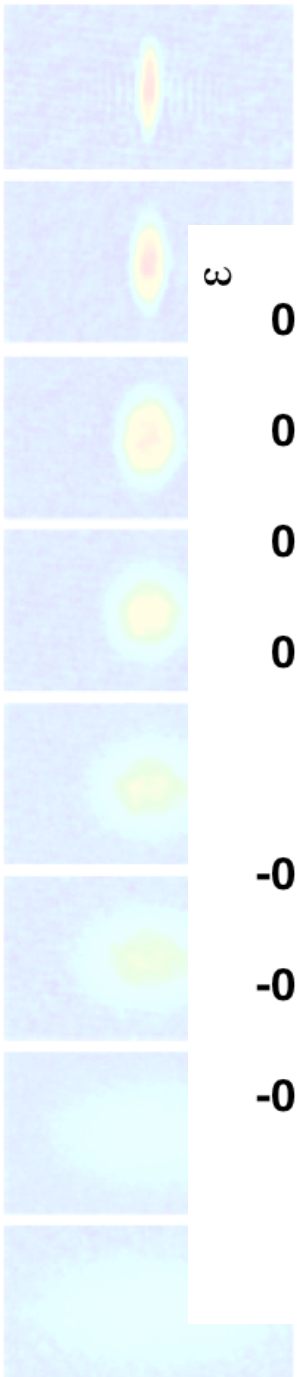
UrQMD – soft EoS

- ✓ reproduces CERES' anisotropy
- root(s) dependence looks unlikely

hybrid models: long-lived system evolves to round

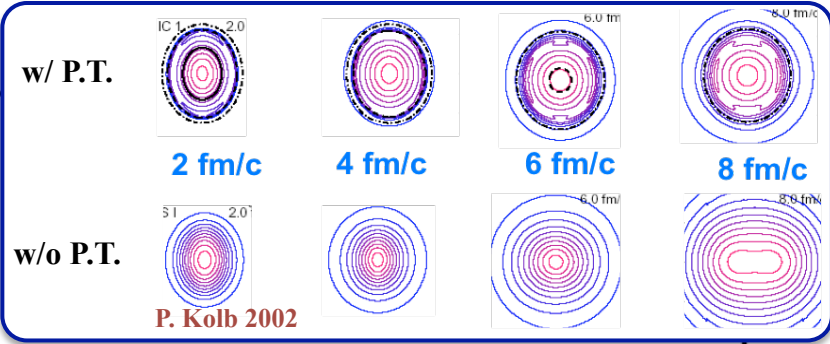
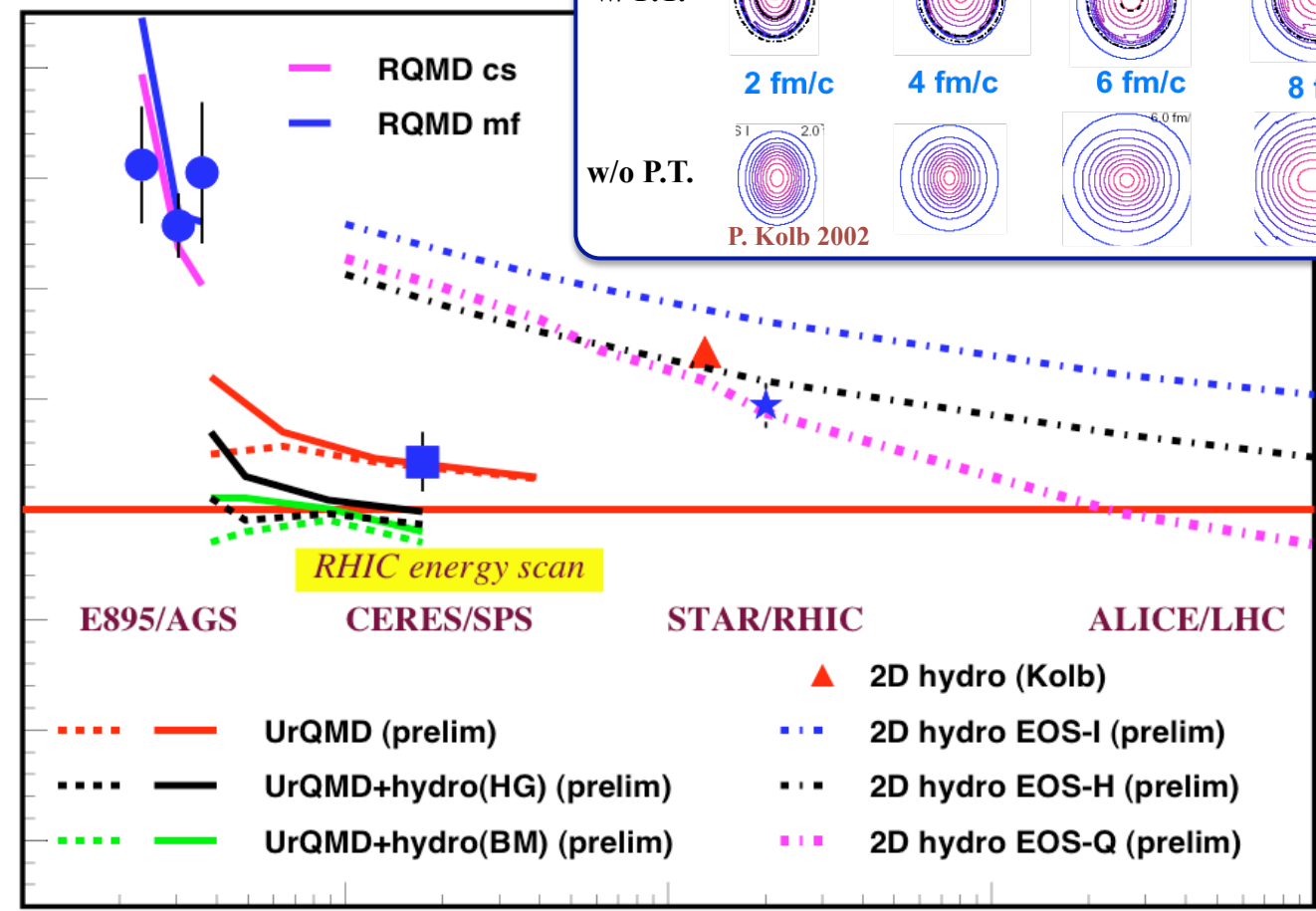
\* tilt not important (because  $\theta$  and  $\varepsilon$  both small)

# A Unified picture?



$\epsilon$

0.4  
0.3  
0.2  
0.1  
0  
-0.1  
-0.2  
-0.3



E895/AGS

CERES/SPS

STAR/RHIC

ALICE/LHC

RHIC energy scan

UrQMD (prelim)

UrQMD+hydro(HG) (prelim)

UrQMD+hydro(BM) (prelim)

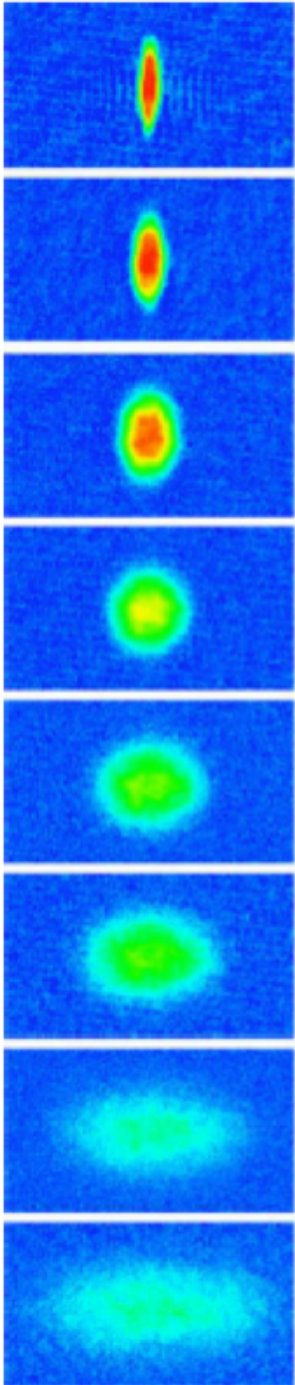
▲ 2D hydro (Kolb)

■ 2D hydro EOS-I (prelim)

■ 2D hydro EOS-H (prelim)

■ 2D hydro EOS-Q (prelim)

$\sqrt{s_{NN}}$  (GeV)



111d 113d - WFCV 2009 - CE111

## how to spend 30 min discussing 5 data points

- **p**-dep femtoscopy reveals flow-generated substructure
  - mT-dependence: radial flow
  - y-dependence: longitudinal flow
  - asHBT measures detailed spatial analogs of  $v_1$ ,  $v_2$
- bulk observable with
  - sensitivity to EoS & dynamical time (& 3<sup>rd</sup> flow component, early softening...?)
  - !! non-monotonic excitation function:  
interesting feature @ “interesting” energy  
asHBT part of B.E.S. program
- true 3D, unified modeling important, to map out spatial dynamics
- 1<sup>st</sup>-order R.P. necessary during RHIC energy scan
- much more work on experimental and theoretical/modeling side

# asHBT model calculations- *THANKS!*

- **P. Kolb** [Regensburg, Ohio] – 2D hydro EOS-Q @ 130 GeV
- **E. Frodermann** [Minnesota]– 2D hydro EOS-Q, EOS-I, EOS-H, 10 GeV - 300 TeV
- **M. Mitrovski & M. Bleicher** [Frankfurt] – UrQMD,  $\sqrt{s} = 4\text{-}39$  GeV
- M. Lisa [Ohio] – RQMD **meanfield on/off**  $\sqrt{s} = 2\text{-}4$  GeV
- **H. Petersen** [Frankfurt] – UrQMD + 3D hydro,  $\sqrt{s}=4 - 17$  GeV, **BM & HG EoS**

See also:

- A. Kisiel et al – hydro+Therminator: PR **C79** 014902 (2009)
- T. Humanic – hadronic rescattering (HRM): Int.J.Mod.Phys.**E15**, 197 (2006)
- D. Teaney, J. Lauret, & E. Shuryak – RQMD & hybrid - nucl-th/0110037