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Where innovation starts

## Why contrast?









#### Why contrast?





#### [Olszewski et al. Eur Heart J 2007]



#### Dynamic contrast-enhanced ultrasound

#### **Ultrasound transducer**

#### **Pressure waves**

#### **Microbubbles**









## Applications

- Detection of intracardiac shunts
- Intrapulmonary shunt
- Left ventricular opacification/endocardial border definition
- Assessment of myocardial perfusion
- Cancer diagnostics (angiogenesis)
- Atherosclerotic plaque characterization



## Mechanical index

- Microbubbles are deformed by higher ultrasound power to point of destruction.
- Mechanical Index (MI) = Acoustic Power [kPa] /  $\sqrt{f_0}$ [MHz]. It defines the mechanical interaction US/bubbles
- Low mechanical index (up to 0.3) is typically used for imaging (bubble detection).
- MI > 0.7 is associated with bubble destruction and cavitation fenomena.



- > UCA are microbubbles with a diameter 1-10  $\mu$ m
- They are made of an inert gas enclosed in a phospholipidic, albumin, or polymer shell.
- When invested by ultrasound waves they start oscillating and scattering energy with a nonlinear behavior



Electron microscopy 13500×

7

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Name	Manufacturer	Year	Gas	Coating	Approved	Available
Echovist	Bayer Schering Pharma AG	1991	air	galactose	EU, Japan, Canada	
Albunex	Molecular Biosystems	1994	air	human albumin	EU, USA, Canada	
Levovist	Bayer Schering Pharma AG	1996	air	galactose, trace palmitin	$Worldwide^1$	2
Optison	GE Healthcare AS	1997	$C_3F_8$	human albumin	EU, USA	EU, $USA^3$
Definity	Lantheus Medical Imaging	2001	$C_3F_8$	phospholipids	Worldwide <sup>4</sup>	Worldwide
SonoVue	Bracco SpA	2001	$SF_6$	phospholipids	Europe, China, S Korea, India, Hong Kong, Singapore	Europe, China, S Korea, India, Hong Kong, Singapore
Imagent	Alliance Pharmaceutical Corp.	2002	$C_6F_{14}$	phospholipids	USA	
Sonazoid	Amersham Health	2006	$C_4F_{10}$	phospholipids	Japan	Japan
$BR38^5$	Bracco SpA		$C_4F_{10}/N_2$	phospholipids		

TABLE I. COMMERCIALLY AVAILABLE ULTRASOUND CONTRAST AGENTS.

 $^1\!\mathrm{Approved}$  in 65 countries, but not in the United States.

 $^{2}$ Expected to finish in 2010.

<sup>3</sup>Temporarily unavailable 2006–2010.

<sup>4</sup>Approved in United States, Canada, Mexico, Israel, Europe, India, Australia, Koria, Singapore, UAE, and New Zealand. <sup>5</sup>In clinical development.

#### [Faes et al, IEEE TUFFC 2013]





#### Free-bubble dynamics



#### **Encapsulated-bubble dynamics**

#### Rayleigh Plesset Equation

$$\rho R\ddot{R} + \frac{3}{2}\rho \dot{R}^2 = \left(\frac{2\sigma}{R_0} + P_0 - P_v\right) \left[\left(\frac{R_0}{R}\right)^{3k} - 1\right] - P(t)$$

Modified Rayleigh Plesset Nolting Neppiras Poritsky (RPNNP) Equation

$$\rho R\ddot{R} + \frac{3}{2}\rho \dot{R}^{2} = \left(\frac{2\sigma}{R_{0}} + P_{0} - P_{v}\right) \cdot \left[\left(\frac{R_{0}}{R}\right)^{3k} - 1\right] + 4\frac{\mu_{f}\dot{R}}{R} - P(t)$$
Pressure drop by viscous damping due to fluid viscosity  $\mu_{f}$ 

Model for shell encapsulated bubbles (de Jong, 1991)

$$\rho R\ddot{R} + \frac{3}{2}\rho\dot{R}^{2} = \left(\frac{2\sigma}{R_{0}} + P_{0} - P_{v}\right) \cdot \left[\left(\frac{R_{0}}{R}\right)^{3k} - 1\right] + S_{p}\left(\frac{1}{R} - \frac{1}{R_{0}}\right) - \omega\delta_{t}\rho R\dot{R} - P(t)$$
natural frequency
Shell elasticity parameter (N/m)
Total damping factor =  $b/2\pi f_{n}m_{t}$ 

damping cooff

mass

## Damping factor

$$\delta_{\rm t} = \delta_{\rm rad} + \delta_{\rm vis} + \delta_{\rm th} + \delta_{\rm f}$$

$$\begin{array}{ll} \mbox{Re-radiation damping} & \delta_{\rm rad} = \frac{2\pi f_{\rm n}}{c} R_{0}, \\ \mbox{Fluid viscosity damping} & \delta_{\rm vis} = \frac{2\mu_{\rm f}}{\pi f_{\rm n} \rho R_{0}^{2}}, \\ \mbox{Thermal damping} & \delta_{\rm th} = B(f, R_{0}) \frac{f_{\rm n}^{2}}{f^{2}}, \\ \mbox{Shell friction damping} & \delta_{\rm f} = \frac{6\mu_{s}T_{s}}{\pi f_{\rm n} \rho R_{0}^{3}}. \end{array}$$

[T.G. Leighton, *The acoustic bubble*, Oxford University Press, 1995]



#### Small oscillations for encapsulated bubbles

#### Natural frequency for free bubbles

$$f_{\rm n} = \frac{1}{2\pi} \sqrt{\frac{s}{m}} = \frac{1}{2\pi\sqrt{\rho}R_0} \sqrt{3k\left(P_0 - P_{\rm v} + \frac{2\sigma}{R_0}\right) - \frac{2\sigma}{B_0} + \frac{2S_{\rm p}}{R_0}} + \frac{2S_{\rm p}}{R_0}$$

#### Minnaert resonance:

$$f_n = \frac{1}{2\pi R_0} \sqrt{\frac{3\kappa P_0}{\rho}}$$



#### Backscatter coefficient

The ultrasound backscatter is defined by the *backscatter coefficient*  $\beta$ , which is the *scattering cross-section* (cm<sup>2</sup>) per unit volume (cm<sup>3</sup>) and per scattering angle (sr).

The scattering cross-section of a bubble is the ratio between the power scattered in all directions, W (average power over a period T=1/f), and acoustic intensity  $I_i$ .

$$\epsilon(t) = \epsilon_0 \cos(2\pi ft) \qquad b_{rad} = 2\pi fm \delta_{rad} = \frac{16\pi^3 \rho R_0^4 f^2}{c}$$

$$W = \frac{1}{T} \int_0^T (F \cdot \dot{\epsilon}(t)) dt = \frac{1}{T} \int_0^T (\dot{\epsilon}(t) \dot{b} \cdot \dot{\epsilon}(t)) dt = \frac{1}{2} 4\pi^2 f^2 \epsilon_0^2 b$$
Force to compensate damping
$$\Sigma(R_0, f) = \frac{W}{I_i} = \frac{\frac{1}{2} 4\pi^2 f^2 \epsilon_0^2 b}{P_i^2 (2Z)^{-1}} = \frac{4\pi R_0^2}{\left[ (f_n (R_0)/f)^2 - 1 \right]^2 + \delta_t^2 (R_0, f) \right]}$$
Which is the scattering cross-section if  $f > f_0$ ?

#### **Backscatter coefficient**

$$\Sigma_{\rm tot}(f) = \int_{R_{\rm min}}^{R_{\rm max}} n(R) \Sigma(R, f) dR$$

Total scattering cross-section accounts for interaction forces depending on normalized radius distribution n(R).

Backscatter coefficient [cm<sup>-1</sup> sr<sup>-1</sup>]:  $\beta(f) = \frac{\rho_n \Sigma_{tot}(f)}{4\pi}$ , with  $\rho_n$  number of bubbles per unit volume.

Intensity received by the transducer:

sample volume  

$$I = \frac{dV}{z^2}\beta(f)I_{\rm i} = \frac{dV}{z^2}\frac{\rho_{\rm n}\Sigma_{\rm tot}(f)}{4\pi}I_{\rm i}$$

#### distance from the transducer

The average  $\beta(f)$  over the spectrum is the Integrated backscatter coefficient (IBI).

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### Thresholding and buckling







The tension as a function of the bubble radius  $(R_0=2 \mu m)$  for Marmottant model in elastic regime, buckling, and rupture of the shell.

Notice the compression only behavior...

#### Attenuation

#### Extinction cross-section (similar to backscatter but for power loss)



 $a_{\rm e}$  depends on scattering in all directions and damping. A term  $a_{\rm d}$  can also be considered to account for chemical decay (dissolution).

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#### Nonlinear behavior



#### Backscatter spectrum





## 2<sup>nd</sup> harmonic imaging



Frinking et al, Ultras Med Biol, 2000:26(6):965-975.

#### **Pulse** inversion

**Tx:** transmitting two pulses  $p_1$  and  $p_2$ , where:  $p_2 = -p_1$ 

**Rx:** summing the two echoes:  $e_{pi} = e_1 + e_2$ 



#### **Power modulation**

**Tx:** transmitting two pulses  $p_1$  and  $p_2$ , where:  $p_2 = \alpha p_1$ 

**Rx:** scaling and subtracting the two echoes:  $e_{pm} = e_1 - e_2/\alpha$ 



## **Contrast-specific imaging**

## Power modulation





### **Contrast-specific imaging**



Contrast concentration



## Power modulation





### Data calibration / linearization



#### Video density:

- Low UCA concentrations:  $I \propto C$
- Dynamic-range compression:  $Q \propto \log(I)$

$$Q(C) = a_0 \ln(a_1 C + 1) + a_2$$

- Dynamic-range parameter a<sub>0</sub>
- I(C) regression-line angle a<sub>1</sub>
- Baseline a<sub>2</sub>



#### Data calibration / linearization

If we inject a dose *m* in a compartment of unknown volume *V*,

we can estimate **V** by measuring **C**: 
$$V = \frac{m}{C}$$

What are *m* and *C* in contrast-enhanced ultrasound (CEUS)?

- Based on the adopted calibration, *C* is the concentration corresponding to the measured signal (acoustic intensity or gray levels), usually expressed in volume fraction.
- Therefore, *m* is the volume of injected contrast agent.



#### Mono-compartment model



$$\frac{dC_0(t)}{dt}V = \left(C_i(t) - C_0(t)\right)Q$$

- $C_i(t)$  = input concentration
- $C_{o}(t)$  = output concentration (or concentration in the compartment)
- *V* = volume of the compartment
- Q = flow through the compartment



#### Mono-compartment model



$$\frac{dC_0(t)}{dt}V = \left(C_i(t) - C_0(t)\right)Q$$

#### Laplace transform *L*[.]

$$\tau \frac{dC_0(t)}{dt} + C_0(t) = C_i(t) \quad \longleftrightarrow \quad \frac{C_0(s)}{C_i(s)} = \frac{1}{\tau s + 1}$$

with  $\tau$  = system *time constant* = V/Q

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## Dilution impulse response of a compartment



- $C_{i}(t)$  = input concentration
- $C_{o}(t)$  = output concentration
- V = volume of the compartment
- Q = flow through the compartment
- $\tau$  = system *time constant* = V/Q

convolution Impulse  $C_{o}(t) = C_{i}(t) * h(t)$   $C_{o}(s) = C_{i}(s)H(s)$  H(s) = L[h(t)] $h(t) = L^{-1}\left[\frac{1}{\tau s + 1}\right] = \frac{1}{\tau}e^{-\frac{t}{\tau}}$ 

#### Mono-compartment step response

Assume for  $t \le 0$ ,  $C_0 = 0$ , and at time t = 0 the input quantity,  $C_i$ , increases instantly by an amount A, i.e.,



#### Mono-compartment step response

MP indicates the blood flow in the myocardium [flow/unit tissue volume], which is the heart muscle.

The major vessels in the myocardium are the coronary arteries, which draw oxygenated blood from the root of the aorta, and the coronary veins, which carry de-oxygenated blood to the right atrium (RA).

A lack of perfusion is known as ischemia, which leads to reduced wall thickening/motion (ipokinesis) and dyssinchrony of the ventricular contraction.





#### Destruction (flash) replenishment method



$$C_0(t) = A\left(1 - e^{-\frac{t}{\tau}}\right)$$

Perfusion 
$$\propto A/\tau$$

Wei et al, Circulation, 1998.





$$A \propto \frac{V_{v}}{V_{t}} \Longrightarrow \frac{A}{\tau} \propto \frac{V_{v}}{V_{t}} \cdot \frac{1}{\tau} = \frac{V_{v}}{V_{t}} \cdot \frac{Q}{V_{v}} = \frac{Q}{V_{t}}$$



Stress echo is a well known procedure in clinical practice to look at wall motion and MP. The echocardiographic investigation is made at about 85% of maximal PR.

In young patients exercise is the preferred option.

Only when exercise is not possible:

- Injection of vasodilators (more to look at MP, increase PR of ~10%)
  - Adenosine (faster effect)
  - Dipyridamole (slower effect, 10-15 min side effects, but more time for imaging...)
- Injection of dobutamine (more for wall motion)



#### Indicator dilution curve / time intensity curve

## Evolution over time of the contrast concentration after a contrast <u>bolus</u> injection



#### Heuristic features

Features used for semi-quantitative interpretation of the IDC:

- Peak Intensity (PI)
- Area Under the Curve (AUC)
- Wash-in Time (WIT)
- Wash-in Rate (WIR)



### Qualitative cancer diagnostics by CEUS

## Qualitative diagnosis of liver lesions by early wash-in (arterial phase) and wash-out (portal phase).



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#### Mass conservation

$$\frac{dm}{dt} = \frac{dV}{dt}\frac{dm}{dV} = Q(t)C(t)$$

We are interested in the integral of the mass-conservation equation, i.e., the *Stewart-Hamilton* equation:

$$\int_{0}^{\infty} dm = \int_{0}^{\infty} Q(t)C(t)dt \to m = Q\int_{0}^{\infty} C(t)dt.$$

Therefore,  $Q = \frac{m}{\int_{0}^{\infty} C(t)dt}$ with Q = constantm = injected dose

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### Mean transit time (MTT) and volume (V)



 $\mathbf{V} = \mathbf{M}\mathbf{T}\mathbf{T}\cdot\boldsymbol{Q}$ 

$$V = \frac{m \int_{0}^{\infty} t \cdot C(t) dt}{\left(\int_{0}^{\infty} C(t) dt\right)^{2}}$$



#### Mean transit time and volume

$$MTT = \frac{\int_{0}^{\infty} t \cdot C(t) dt}{\int_{0}^{\infty} C(t) dt}$$
$$V = MTT \cdot Q$$
$$m\int_{0}^{\infty} t \cdot C(t) dt$$
$$V = \frac{0}{(m-1)^{2}}$$

 $\left(\int_{\Omega}^{\infty} C(t) dt\right)$ 

## Requirements

Linear relationship concentration vs. measured quantity

Fully determined relationship concentration vs. measured quantity



#### Pulmonary blood volume



[Mischi et al, IEEE TUFFC 2004]



#### Pulmonary blood volume



#### **Recirculation problem**



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#### Poor signal-to-noise ratio

#### IDC measured from single pixels in the prostate...



## Need for model fitting



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### (main) IDC distributed models

#### Lognormal

$$C(t) = \left(\frac{m}{Q}\right) \frac{1}{\sqrt{2\pi\sigma t}} e^{\frac{-(\ln(t)-\mu)^2}{2\sigma^2}}$$

$$MTT = e^{\mu + \frac{\sigma^2}{2}}$$

[Qian & Bassingthwaighte J Theoretical Biology 2000]

#### Local Density Random Walk (LDRW)

$$C(t) = \left(\frac{m}{Q}\right) \sqrt{\frac{\lambda}{2\pi\mu t}} e^{\lambda - \frac{\lambda}{2} \left(\frac{t}{\mu} + \frac{\mu}{t}\right)}$$

[Sheppard and Savage *Phys. Rev.* 1951] [Mischi *et al.* ERASIP J Appl Signal Processing 2003] [Kuenen *et al.* IEEE T-MI 2011]

#### Gamma

shape factor  $C(t) = \left(\frac{m}{Q}\right) \frac{\beta^{\alpha}}{\Gamma(\alpha)} t^{\alpha-1} e^{-t\beta} \quad \text{rate factor}$ Gamma operator [Thompson *et al.* Circ Res 1964] [Mischi *et al.* Physiol Meas 2008]  $\Gamma(\alpha) = \int_{0}^{\infty} x^{\alpha-1} e^{-x} dx$   $MTT = \mu$ 

*MRT* (mean resident time) =  $\mu \left(1 + \frac{1}{\lambda}\right)$ 

$$MTT = \alpha\beta$$

#### Atherosclerotic plaque





#### Intravascular echography





#### Imaging plaque perfusion

Plaque angiogenesis related to plaque instability and reduced by statin therapy [Circulation 2002;105(4):415-418].

Plaques may be considered tumors, and specific drugs (angiogenesis inhibitors) could be carried and locally delivered by targeted microbubbles [Circulation 1999, 99:1726-1732].

Plaque vascularization imaging by CEUS [SB Feinstein, JACC 2006, 48(2):236-43].

Instability and risk assessment?





Courtesy of Prof. S.B. Feinstein

#### **Bubbles for medical treatment**

#### The most destructive shock is due to cavitation Ultrasound in Med. and Biol. 21(1),97-107,1995



#### Claw jet

#### Thrombosis

#### Myocardial Infarction (1,000,000 cases/year in the USA)



A clot, which may consist of a blood coagulation or a plaque fragment, obstructs a coronary artery and interrupts the blood flow to a specific area of the myocardium. The consequence is a myocardial infarction.



#### Thrombosis

#### Ischemic stroke (500,000 cases/year in the USA)



A clot, which may consist of a blood coagulation as well as a plaque fragment, interrupts the blood flow to a specific area of the brain, which stops functioning and is damaged due to anoxia.

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## Thrombolysis

## 1 - Surgical intervention

- Bypass
- Thrombectomy catheters (angioplasty)

## 2 - Non-invasive intervention

- Infusion (~ 0.9 mg/kg) of thrombolytic drugs such as t-PA (tissue-plasminogen activators), Urokinase, etc.
- Sonolysis with low frequency (24 kHz 1 MHz) and high intensity (>1W/cm<sup>2</sup>) ultrasound (high MI).



Open vessel

### **Bubble thrombolysis**

## Sonolysis

It is far more efficient when combined with infusion of microbubbles. In this process, sub-micron bubbles are the most effective.

Possible explanations:

- The presence of microbubbles lowers the cavitation threshold shortening the thrombolysis time.

- Increased permeation of thrombolytic agent into clots.



**Bubble thrombolysis** 

## Sonolysis



[E.C. Unger, T. Porter W. Culp, et al., Advanced Drug Delivery Reviews, vol. 56, pp. 1291-1314, 2004]



### Targeted bubbles for drug delivery

Cavitation also induces a temporary increase of membrane permeability that leads to increased uptake of genes and drugs. Most efficient frequency around 1 MHz.

Microbubbles can therefore be loaded with genes or drugs and destroyed by high power ultrasound bursts for targeted drug release.





[J. Chomas, P. Dayton, D. May, K. Ferrara, Journal of Biomedical Optics, 6(2):141-150, 2001]

## Targeted bubbles for drug delivery

- 1. Natural binding of leukocytes to bubble phospholipidic shells (enhanced by shell inclusion of phosphatidylserine) makes bubbles stick to inflamed areas, such as unstable atherosclerotic plaques, which contain macrophages, i.e., foam cells.
- 2. Targeted microbubbles can also be obtained by conjugating specific ligands to the shell. The main applications are:
  - Bubbles targeted to attach to fibrin and integrin for thrombosis detection, adenosine delivery (myocardial reflow), and clot-lysis.
  - Bubbles targeted to  $\alpha_v$ -integrins or vascular endothelial growth factor (VEGF) expressed in neo-vessels for early tumor and atherosclerosis detection.



#### Blood Brain Barrier (BBB) opening for brain medical treatment

#### The BBB prevents delivery of therapeutic agents to the brain

Probably due to cavitation, microbubbles with high intensity ultrasound open the BBB, as confirmed by histology and Gd MRI studies.

This techniques might allow efficient chemotherapy treatment of brain tumor metastases. Brain neurodegenerative diseases, such as Alzheimer, might be treated too.



K. Hynynen, N. McDonald, N. Vykhodtseva, F.A. Jolesz, Radiology, vol. 220, pp. 640-646, 2001

## Thank you!



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