



Learning more about Simplified Models with 3D parameter scans

Thomas Jacques

Amelia Brennan

Johanna Gramling

Millie McDonald

Karl Nordstrom

JHEP 1506 (2015) 142 (arXiv:1502.05721), arXiv:1603.01366

Introduction

- We simply do not know the correct model and properties of the dark sector, so experimental searches should convey as much information as possible
- This is best done through searches for a series of EFTs, simplified models and UV complete theories, as well as presenting the information necessary for a recast
 - *See talks from “Reinterpreting LHC searches for DM models” workshop last week, including talk by Felix Kahlhoefer, for more context on the role of simplified models
- As part of this effort, how can we convey more information about simplified models?

Simplified Models

- At the most general level, even the simplest of simplified models has a large number of parameters; e.g. in a naive Z' model, including couplings to both quarks and leptons, there are up to 28 free parameters
- Necessary to make simplifying assumptions to keep the number of parameters small; e.g. in monojet Z' searches,

I. Examine vector and axial-vector individually: $c^q_A = c^{\chi}_A = 0$ or $c^q_V = c^{\chi}_V = 0$

II. MET searches for quark coupling, so assume $g_l = 0$

III. 'Minimal Flavor Violation':
 g_q equal for each quark

$$\begin{aligned}
 \mathcal{L} \supset & g_\chi Z'_\mu (\cancel{c^{\chi}_V \bar{\chi} \gamma^\mu \chi} + c^{\chi}_A \bar{\chi} \gamma^\mu \gamma^5 \chi) \\
 & + \sum_q g_q Z'_\mu (\cancel{c^q_V \bar{q} \gamma^\mu q} + c^q_A \bar{q} \gamma^\mu \gamma^5 q) \\
 & + \sum_l g_l Z'_\mu (\cancel{c^l_V \bar{l} \gamma^\mu l} + c^l_A \bar{l} \gamma^\mu \gamma^5 l)
 \end{aligned}$$

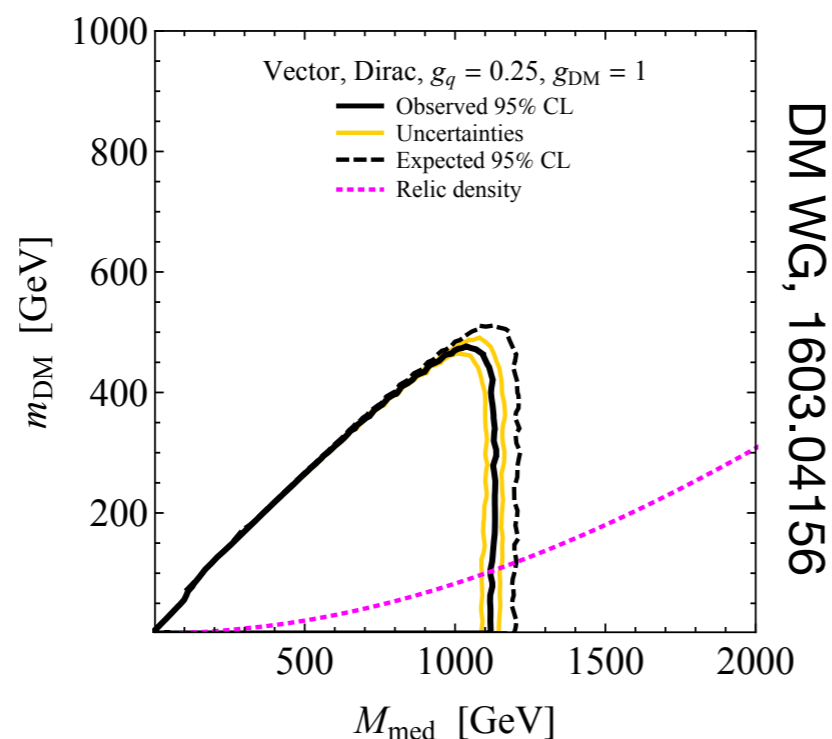
Vector Axial-vector

Simplified Models

- Given these simplifying assumptions, we should convey as much info as possible about the remaining parameters
- Currently, the recommendation is to start with one set of semi-arbitrary couplings (e.g. $g_q=0.25$, $g_{DM}=1$) and scan over masses (m_{DM} , M_{med})
- Alternative is to reparameterise to
$$\left\{ m_{DM}, M_{med}, g_{DM}, g_{SM} \right\} \rightarrow \left\{ m_{DM}, M_{med}, g_{DM} \cdot g_{SM}, g_{DM} / g_{SM} \right\}$$
and scan over (m_{DM} , M_{med} , $g_{DM} \cdot g_q$) for fixed g_{DM} / g_q

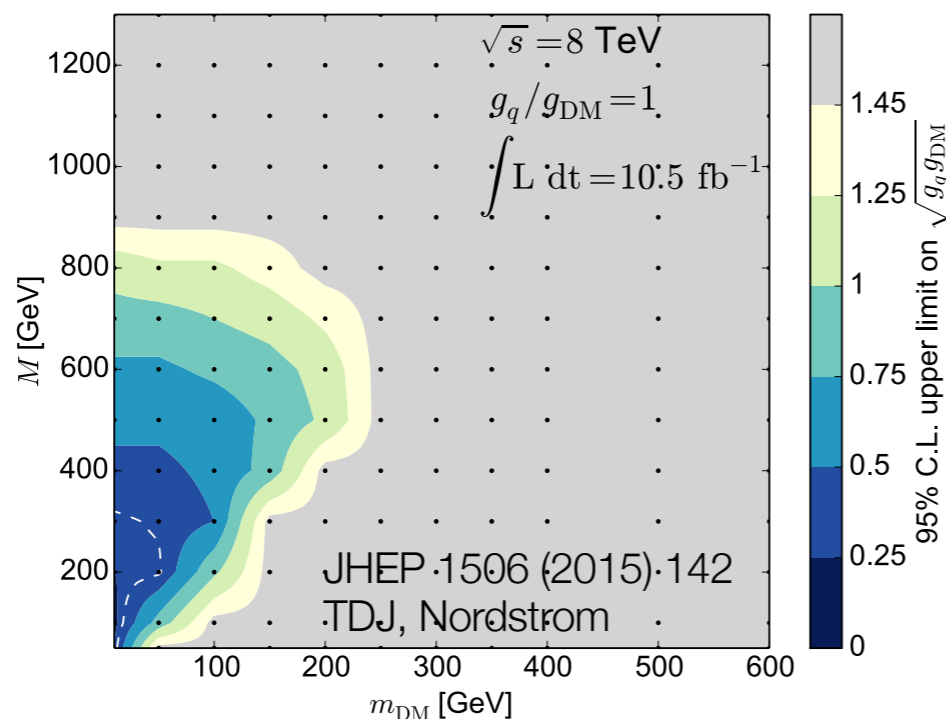
Comparing the options

Benchmark
coupling



- ✓ Only 2 parameters to scan
- ✓ Easier comparison between experiments
- ✗ Semi-arbitrary choice of coupling
- ✗ Less comprehensive: Difficult to translate to other couplings

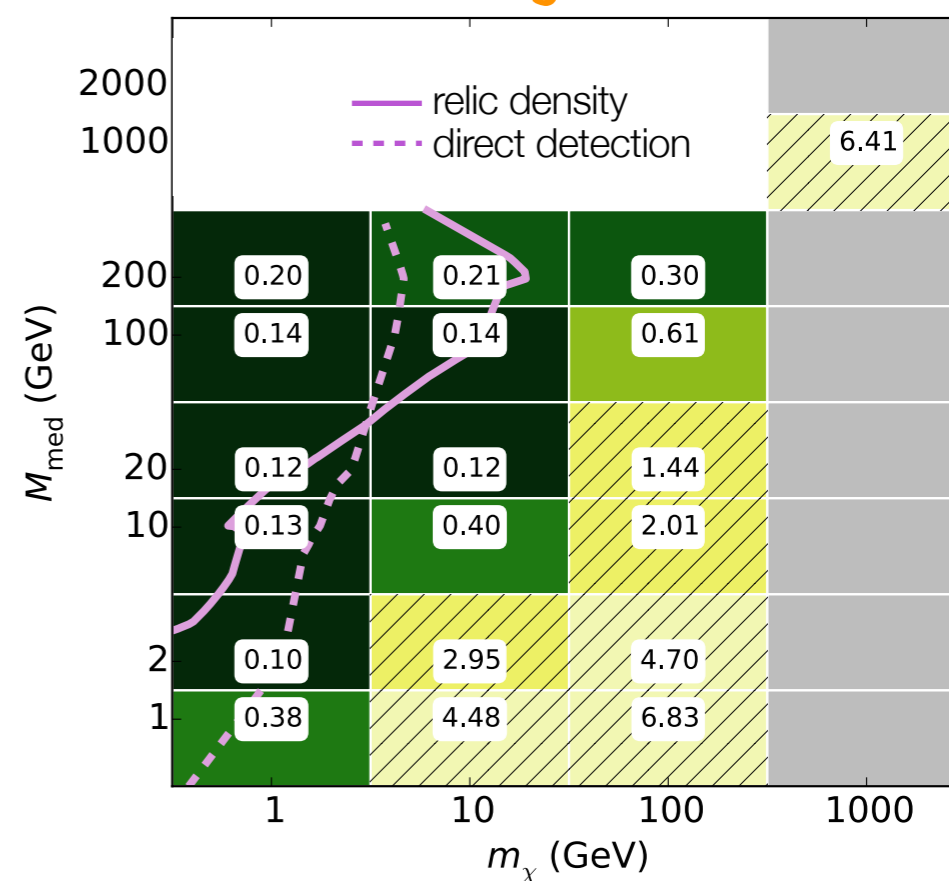
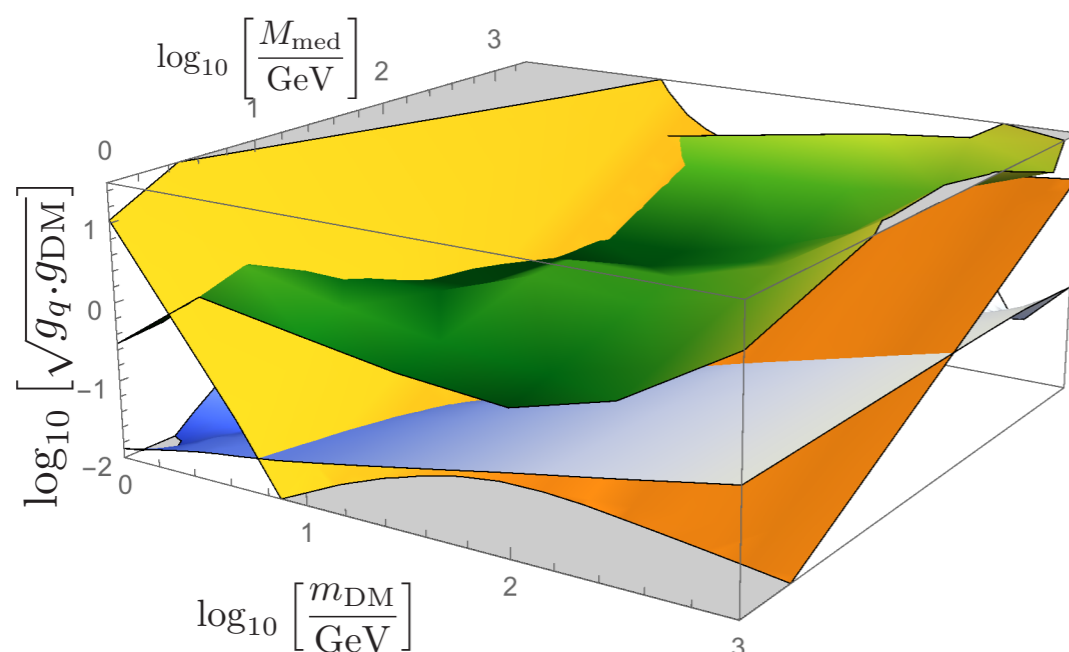
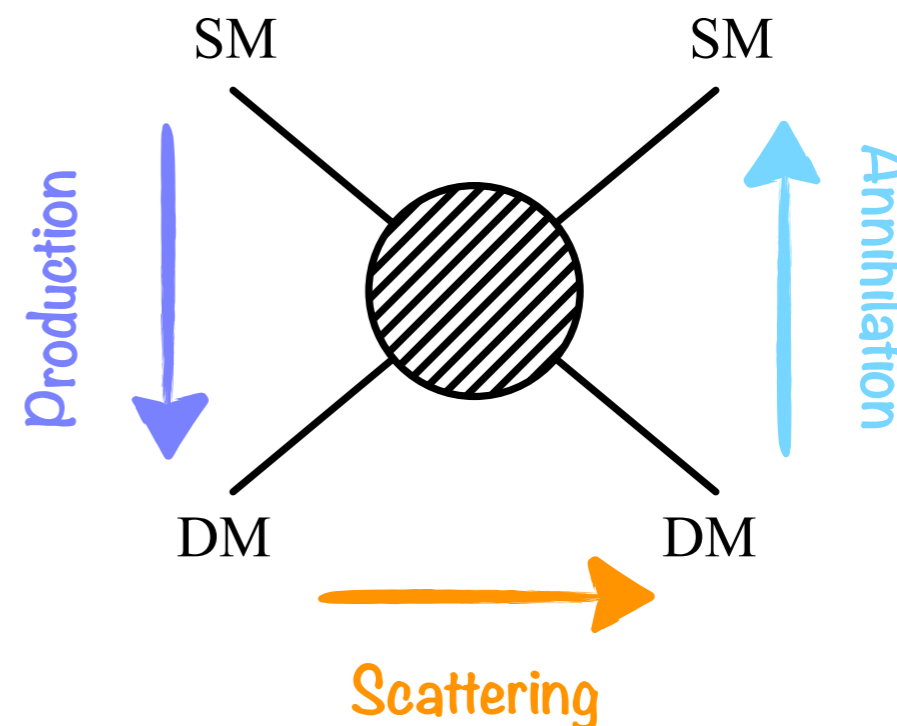
3-D scan



- ✓ Easy to interpret
- ✓ More comprehensive
- ✗ Difficult to compare results
- ✗ Scan over parameter space more challenging

Comparing to other constraints

- Difficult to compare multiple constraints in 3D parameter space!
- Intercept shows the boundary where one constraint becomes stronger than another, indicating the region where each class of constraints performs best

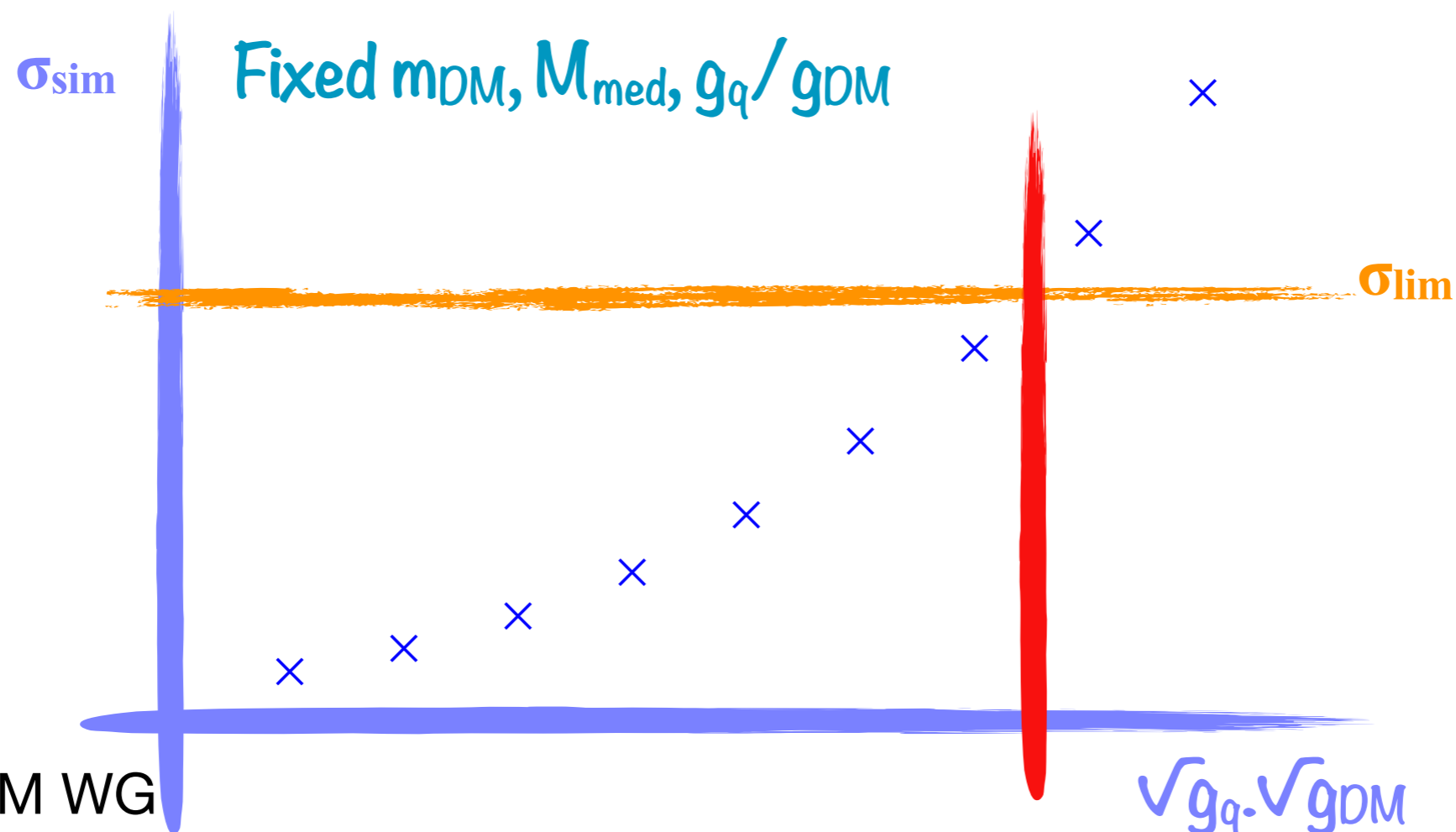


Rescaling relations

$$\left\{ m_{\text{DM}}, M_{\text{med}}, g_{\text{DM}}, g_{\text{SM}} \right\} \rightarrow \left\{ m_{\text{DM}}, M_{\text{med}}, g_{\text{DM}} \cdot g_{\text{SM}}, g_{\text{DM}} / g_{\text{SM}} \right\}$$

For each $\{m_{\text{DM}}, M_{\text{med}}, g_q/g_{\text{DM}}\}$, simulate signal cross section σ_{sim} for a range of $g_q \cdot g_{\text{DM}}$, compare with the experimental limit σ_{lim} .

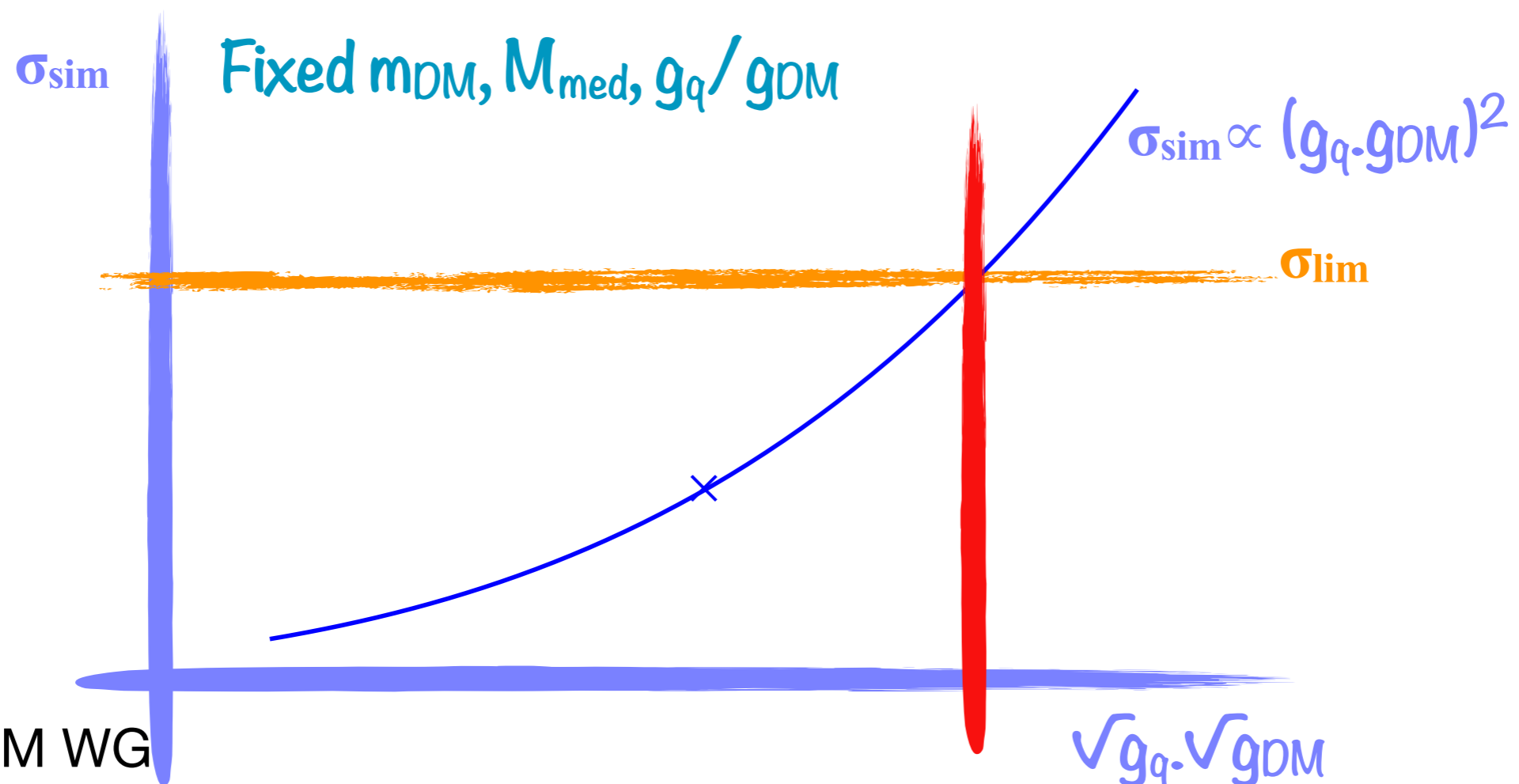
Value of $g_q \cdot g_{\text{DM}}$ where $\sigma_{\text{sim}} = \sigma_{\text{lim}}$ defines the constraint on $g_q \cdot g_{\text{DM}}$.



Rescaling relations

If we know how σ_{sim} varies with $g_q \cdot g_{\text{DM}}$, we can simulate for one value of $g_q \cdot g_{\text{DM}}$, avoiding the full scan

This is not always straightforward!



How good is the rescaling?

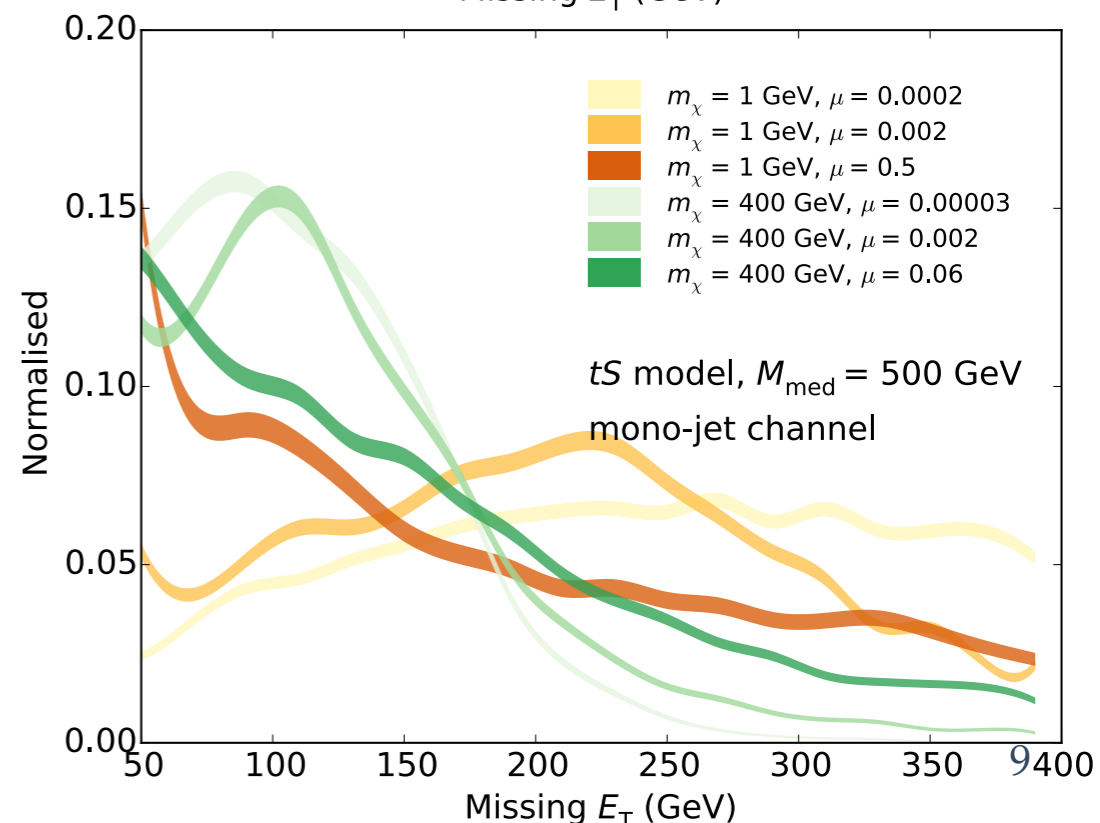
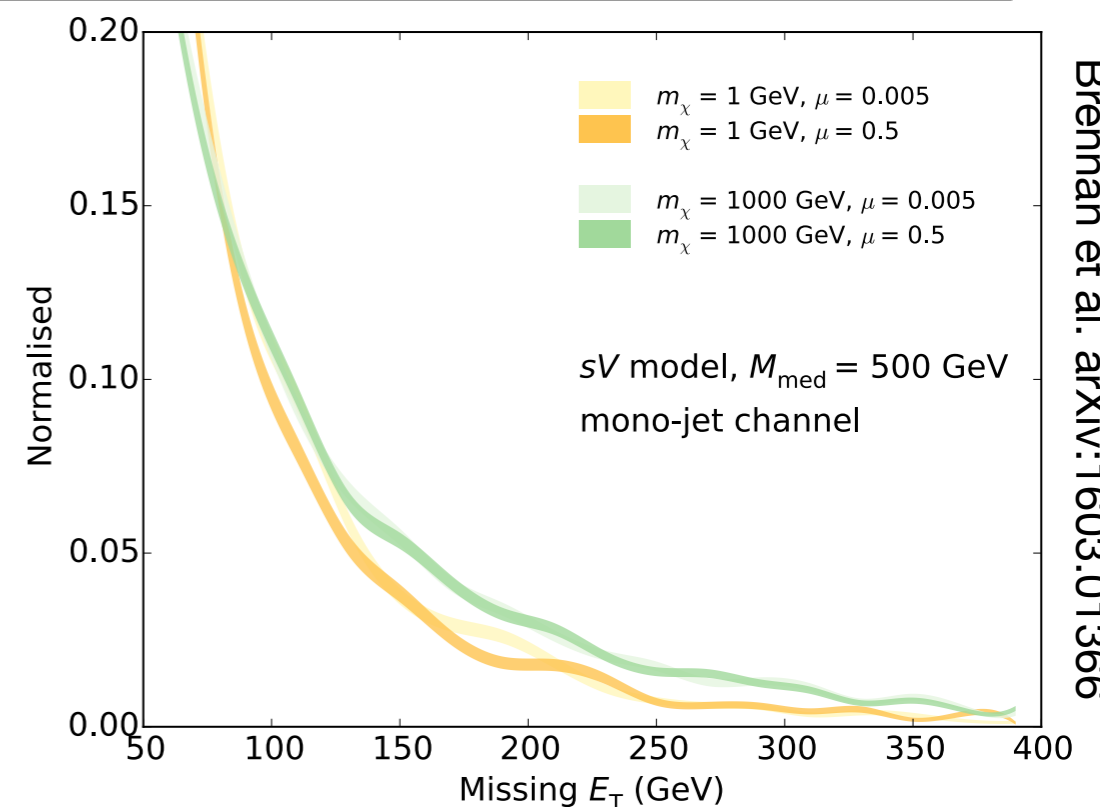
- What is the rescaling relation?

$$\sigma \propto \begin{cases} g_q^2 g_{\text{DM}}^2 / \Gamma_{\text{OS}} & \text{if } M > 2m_{\text{DM}} \\ g_q^2 g_{\text{DM}}^2 & \text{if } M < 2m_{\text{DM}} \end{cases}$$

- Holds only if the kinematic distribution of missing energy is independent of the width

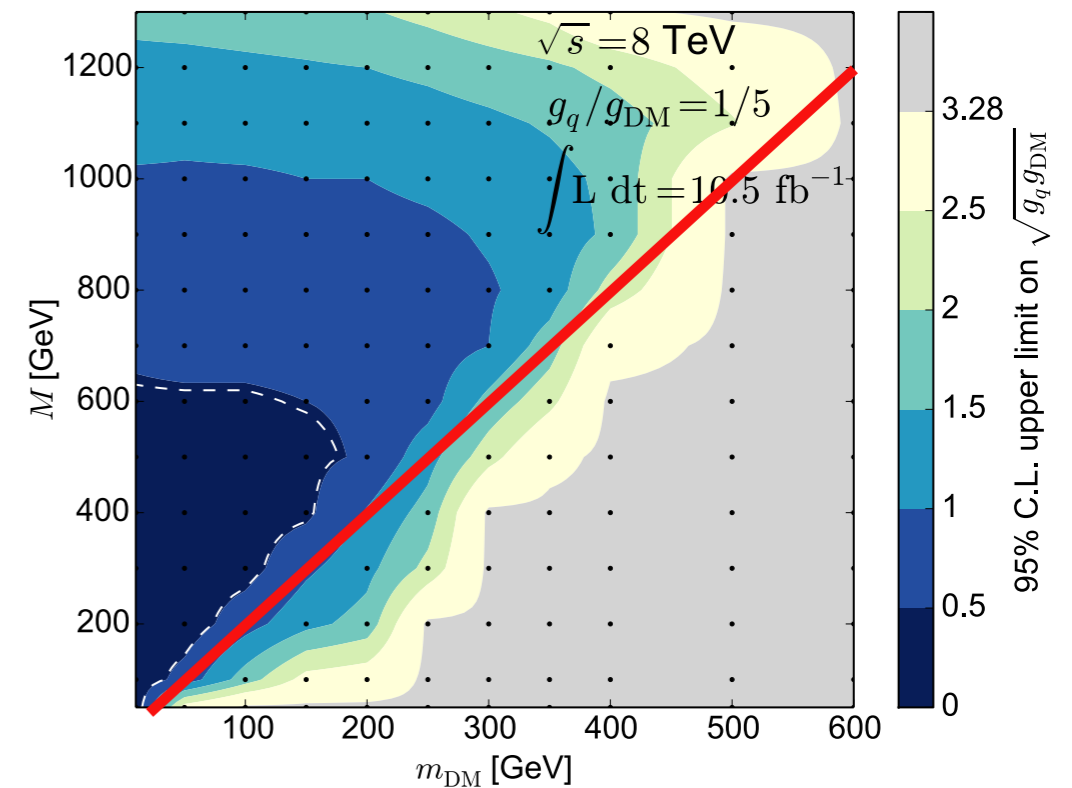
$$\sigma \propto \frac{g_{\text{DM}}^2 g_q^2}{(s - M^2)^2 + M^2 \Gamma^2},$$

- Kinematic behaviour not greatly affected for on-shell s-channel models when $\Gamma/M_{\text{med}} < 0.5$
- t-channel: additional monojet diagrams with on-shell mediator
 - Peak shape strongly depends on Γ/M_{med} !
Coupling scan absolutely needed

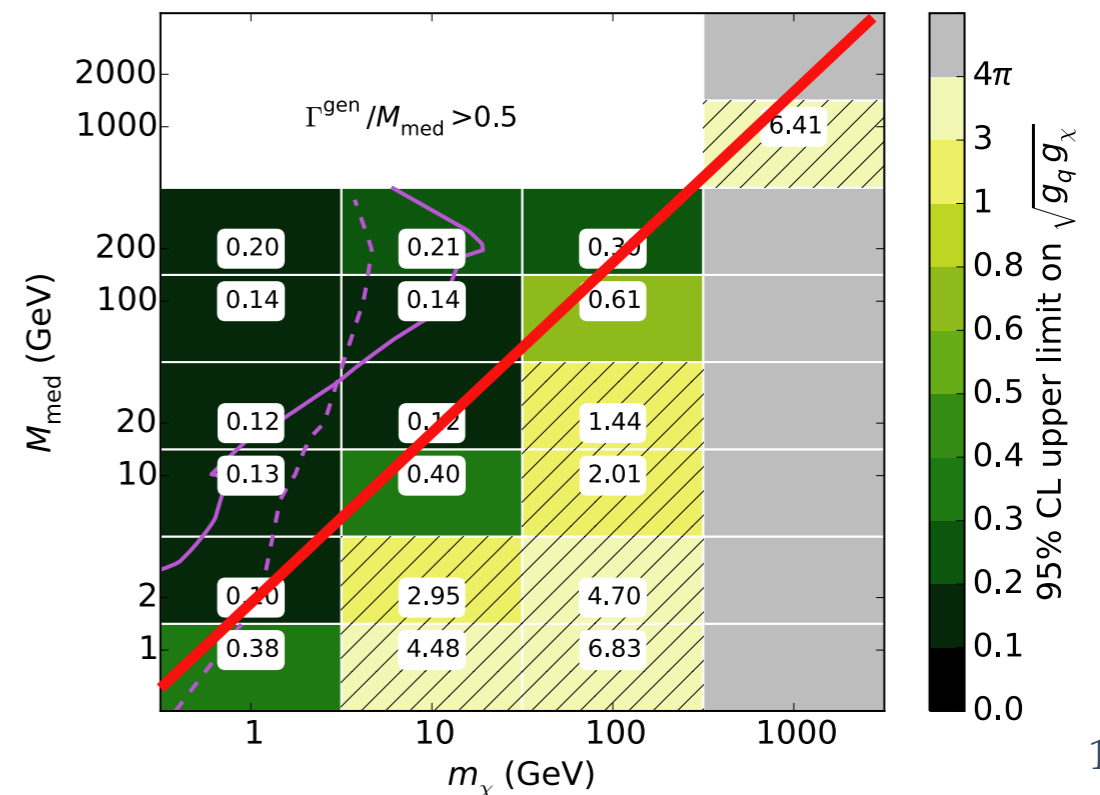


How good is the rescaling?

- Distinguish 3 regions:
 - On shell** ($M_{\text{med}} > 2m_{\text{DM}}$)
 - above red line
 - strong limits, weaker for high masses
 - Ensure $\Gamma/M_{\text{med}} < 0.5$ at generation
 - Off shell** ($M_{\text{med}} < 2m_{\text{DM}}$)
 - below red line
 - Pair production of DM turns off, limits weaken
 - Many points with $\Gamma/M_{\text{med}} > 0.5$
 - Transition region**
 - near red line



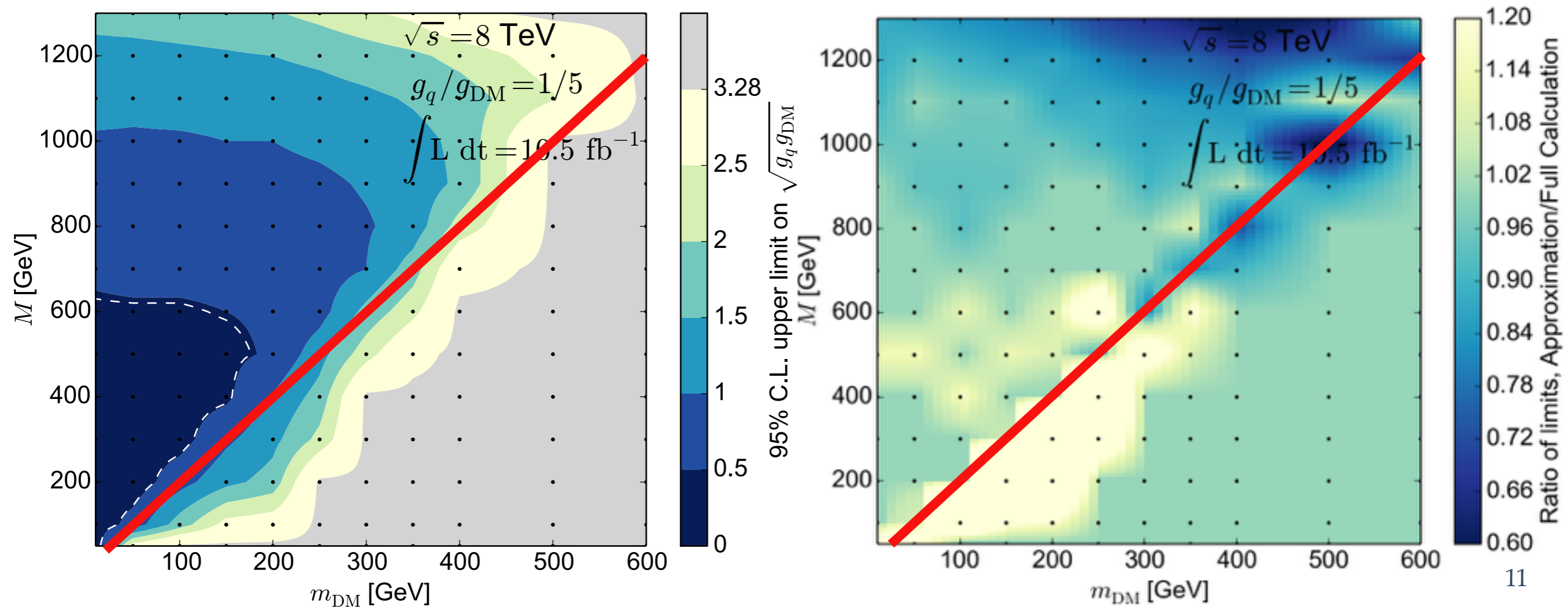
TJ, Nordstrom arXiv:1502.05721



Brennan et al. arXiv:1603.01366

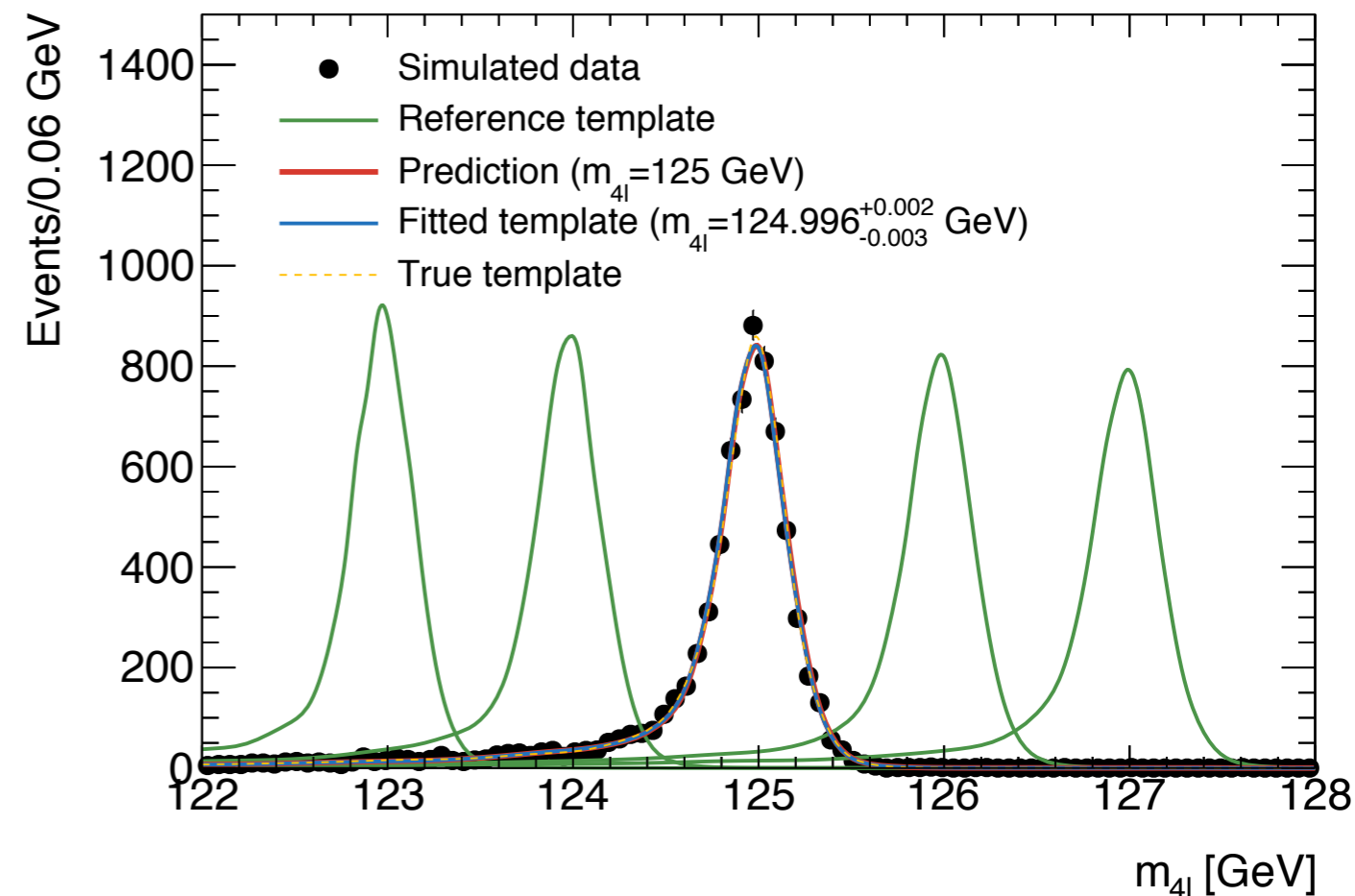
How good is the rescaling?

- Main indicator for validity of the rescaling is the **size of the width**
- OK for central **on-shell** region where constraints are strong and width is small
 - At large mediator masses, constraint becomes weaker, width becomes large, rescaling breaks down
- In **off-shell** region, rescaling works well if width is small, but constraints are weak and width is usually large
- Rescaling breaks down in **transition region**



Morphing

- Method for estimating physical distributions as a continuous function of an arbitrary number of theoretical parameters using non-linear interpolation between a number of input distributions, or factorising out dependence on mediator mass before generation
- Would allow regions where rescaling fails to be investigated for a reasonable computational cost
- Only works in regions with smooth change in distribution
- In use by other analyses



Baak et al, arXiv:1410.7388

Conclusion

- Current DMWG recommendation of benchmark couplings severely limits the scope of constraints on simplified models
- To get constraints on a 3D parameter space, it will be necessary to increase the dimension of the scan in some regions
- A combination of rescaling and morphing can offset this cost by reducing the size of the scan
- Rescaling works well when iff: the width is small, the model is FSR only, and away from transition between on- and off-shell region
- Further study required to determine how tight the scan points need to be for morphing to be effective
- Complementary to other efforts to convey more information to the community