

Spin 100-/1000+

news from the spin structure of the nucleon

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University of Warsaw

QCD and Diffraction
1000+

INP, Cracow, December 5 – 8, 2016

Outline

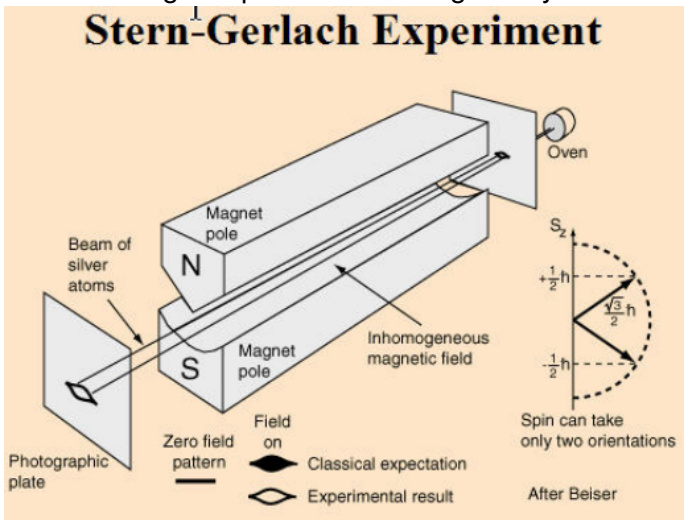
- 1 Introduction
- 2 Inclusive and semi-inclusive deep inelastic scattering
- 3 Charged hadron multiplicities
- 4 Measurements on a transversely polarised target
- 5 Drell-Yan process
- 6 Generalised Parton Distributions

100-

Spin; Stern–Gerlach experiment (1922)

"Right experiment – wrong theory"

Stern-Gerlach Experiment





Electron spin

Theory of the electron spin by Uhlenbeck & Goudsmit (1925)



George Uhlenbeck, Hendrik Kramers
& Samuel Goudsmit

I think you and Uhlenbeck have been very lucky to get your spinning electron published and talked about before Pauli heard of it. It appears that more than a year ago Krong believed in the spinning electron and worked out something; the first person he showed it to was Pauli. Pauli ridiculed the whole thing so much that the first person became also the last and no one else heard anything of it. Which all goes to show that the infallibility of the Deity does not extend to his self-styled vicar on earth.

Letter of B.L. Thomas to Sam Goudsmit (1926)

Read the story in:

<http://lorentz.leidenuniv.nl/history/spin/goudsmit.html>

Slide from Peter Oppeneer, UU 9

1000+

1988: European Muon Collaboration CERN (~ 100 members):

An Investigation of the Spin Structure of the Proton
in Deep Inelastic Muon-Proton Scattering

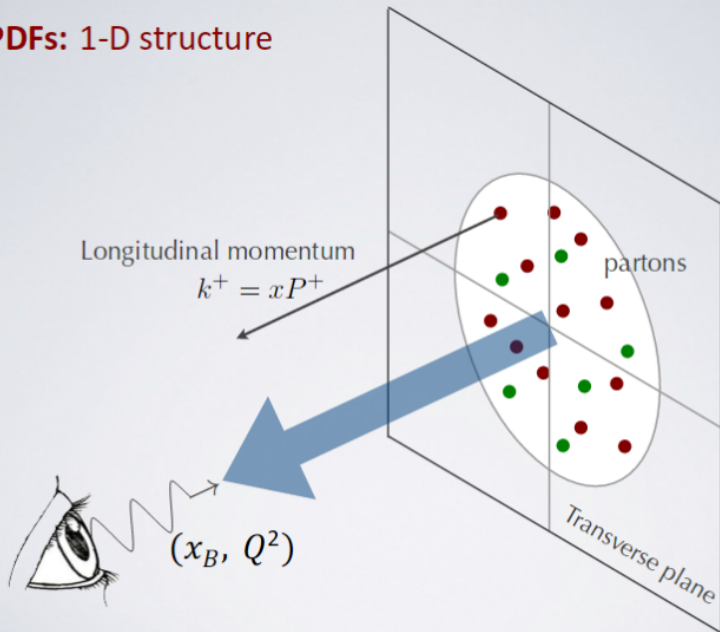
J. Ashman et al., Phys. Lett. **B206** (1988) 364

$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + \Delta L$$

EMC measured: $\Delta\Sigma \sim 0.1!$

cited **1000+** times (exactly **1954**)

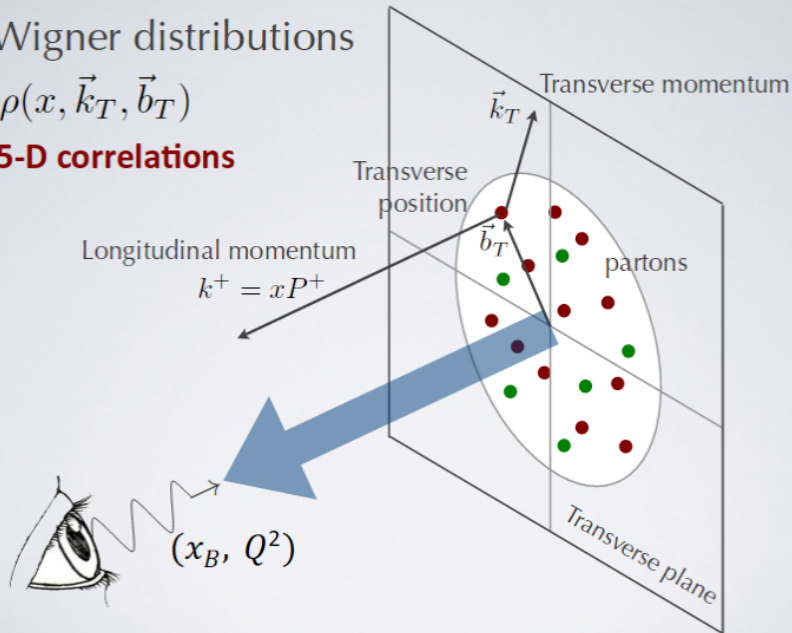
PDFs: 1-D structure



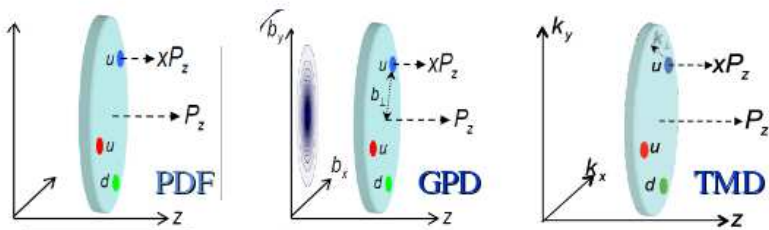
Wigner distributions

$$\rho(x, \vec{k}_T, \vec{b}_T)$$

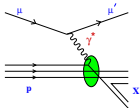
5-D correlations



Parton distributions in the nucleon

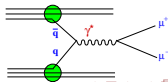


- parton intrinsic k_T taken into account in TMD
- TMD related to quark angular momentum, L !
- GPD and TMD are **NOT** connected via the Fourier transform
- TMD may be studied in 2 ways e.g. at COMPASS:
 - semi-inclusive DIS (polarised muons on unpolarised/transversely polarised target)
 - Drell-Yan process (π beam on unpolarised/transversely polarised target)



SIDIS

Obs.: final state interactions!



DY

Obs.: initial state interactions!

Partonic structure of the nucleon; distribution functions

- In LT and considering k_T , 8 PDF describe the nucleon
 \implies Transverse Momentum Dependent PDF

- QCD-TMD approach valid $k_T \ll \sqrt{Q^2}$

- After integrating over k_T only 3 survive: f_1, g_1, h_1

- TMD accessed in SIDIS and DY by measuring azimuthal asymmetries with different angular modulations

- SIDIS: e.g. $A_{\text{Sivers}} \propto \text{PDF} \otimes \text{FF}$

- DY: e.g. $A_{\text{Sivers}} \propto \text{PDF}^{\text{beam}} \otimes \text{PDF}^{\text{target}}$

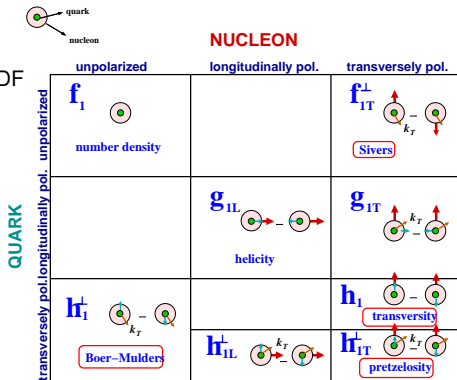
- OBS! Boer-Mulders and Sivers PDF are T-odd, i.e. process dependent

$$h_1^\perp(\text{SIDIS}) = -h_1^\perp(\text{DY})$$

$$f_{1T}^\perp(\text{SIDIS}) = -f_{1T}^\perp(\text{DY})$$

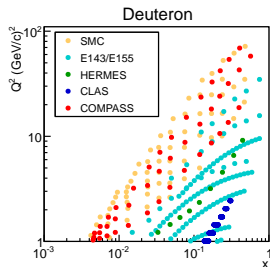
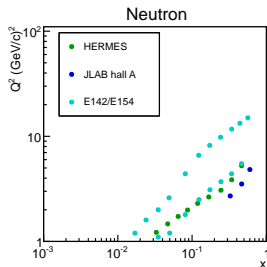
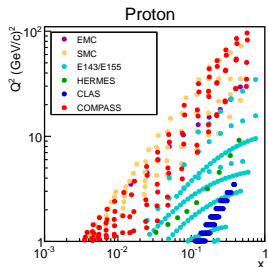
- OBS! transversity PDF is chiral-odd; may only be measured with another chiral-odd partner, e.g. fragmentation function.

- TMD parton distributions need TMD Fragmentation Functions!



The players @ $Q^2 > 1$ (GeV/c)²

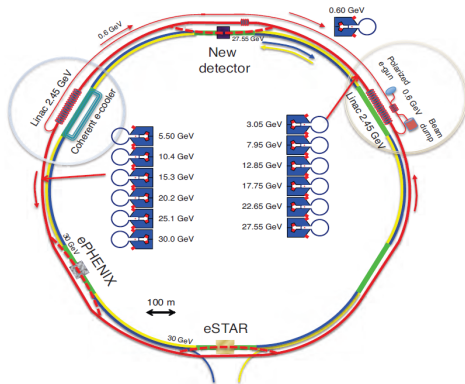
- Fixed target spin experiments:
 - JLab (Hall A, CLAS (Hall B)): polarised e of $\lesssim 12$ GeV, polarised targets
 - CERN (COMPASS): polarised μ^+ of 160-200 GeV, polarised protons, deuterons
 - (completed) DESY (HERMES): polarised e of 27 GeV, polarised targets
- Collider spin experiments: BNL (STAR, PHENIX) polarised protons, $\sqrt{s} \lesssim 510$ GeV



e-p machine, EIC, planned at BNL or JLab

BNL

Electron beam facility needed
(inside RHIC tunnel)



JLab

ELIC + injector needed

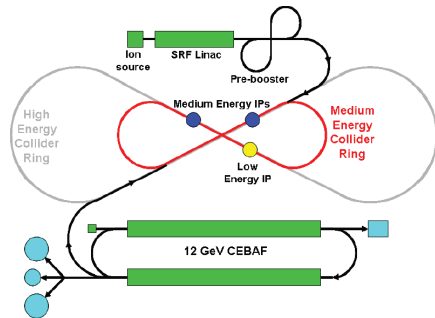
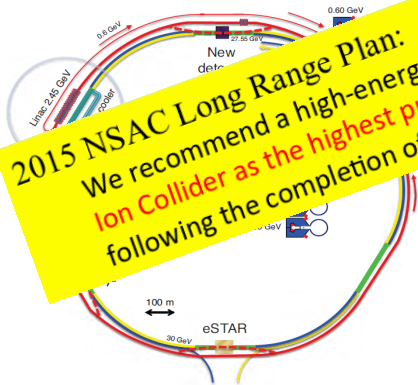


figure from The White Paper, arXiv:1212.1701

e-p machine, EIC, planned at BNL or JLab

BNL

Electron beam facility needed
(inside RHIC tunnel)



JLab

2015 NSAC Long Range Plan:
We recommend a high-energy, high-luminosity polarized Electron Ion Collider as the highest priority for new facility construction following the completion of FRIB

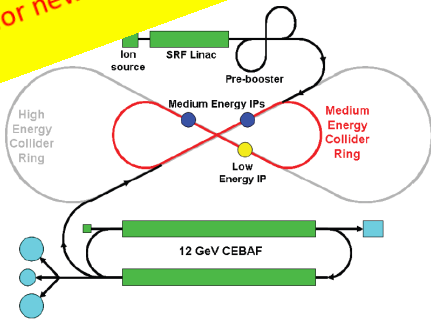


figure from The White Paper, arXiv:1212.1701

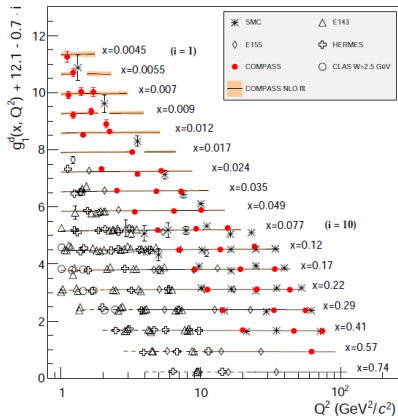
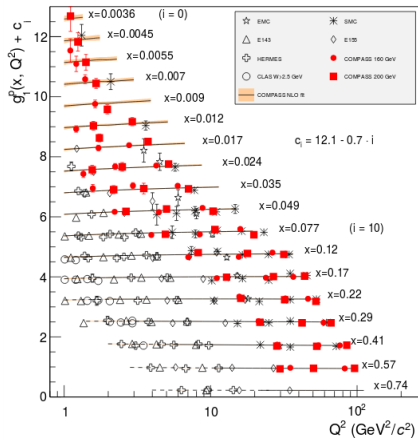
EIC: main features

- Highly polarised ($\sim 70\%$) e, N beams
- ions from deuteron to uranium (lead ?)
- variable \sqrt{s} from ~ 20 GeV to ~ 100 (150) GeV
- high luminosity: $\sim 10^{33-34} \text{ cm}^{-2} \text{ s}^{-1}$ (cooling of hadronic beam !)
- more than one interaction region
- limits of current technology \implies R & D!
- staged realisation; first stage: $\sqrt{s} = 60 - 100$ GeV and high luminosity.

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$g_1^p(x, Q^2)$ and $g_1^d(x, Q^2)$, world data



Curves: COMPASS NLO QCD fit for $W^2 > 10$ GeV² (dashed: extrapolation for $W^2 < 10$ GeV²)

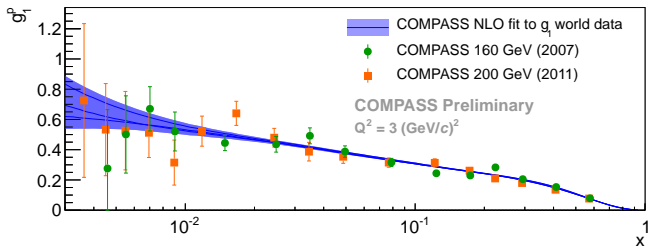
COMPASS measurements at high Q^2 important for the QCD analysis! but little sensitive to Δg

COMPASS, PLB 753 (2016) 18

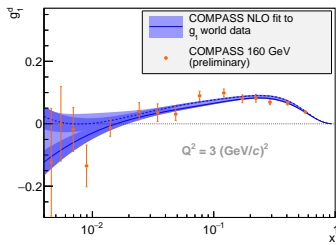
COMPASS, submitted PLB

COMPASS NLO fit to g_1 world data; $Q^2 = 3 \text{ (GeV/c)}^2$

Fitted: $\Delta q_{SI}, \Delta q_3, \Delta q_8, \Delta g$ at $Q_0^2 = 1 \text{ (GeV/c)}^2$; 679 points, 28 params; $\overline{\text{MS}}$ scheme



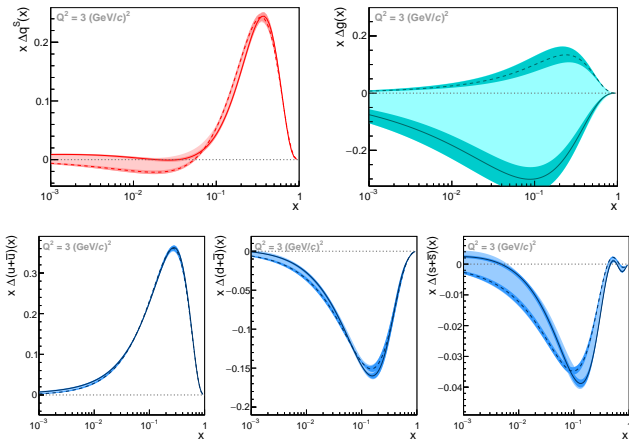
COMPASS, PLB 753 (2016) 18



COMPASS, submitted PLB

COMPASS NLO fit to g_1 world data... cont'd

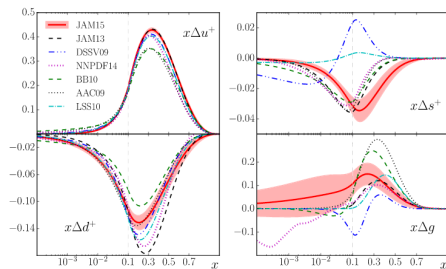
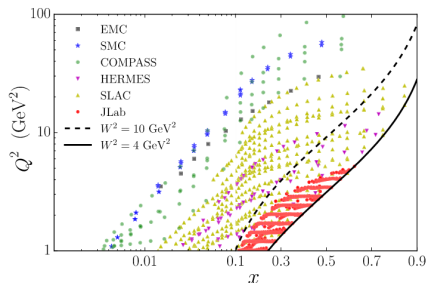
- Little sensitive to gluon polarisation
- Quark polarisation: $\Delta\Sigma = \int \Delta q_{SI}(x) dx \sim 0.3$



JAM NLO fit to world inclusive data (A_{\parallel}, A_{\perp})

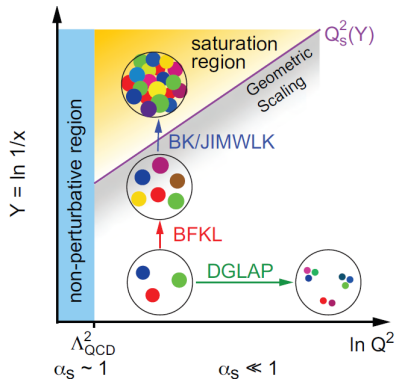
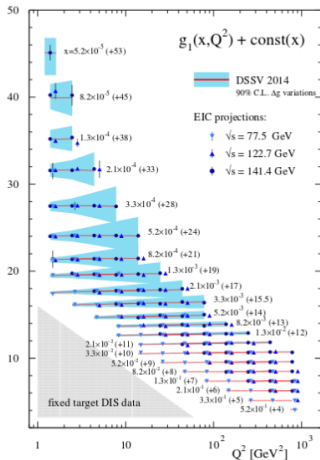
JAM: Jefferson Lab. Angular Momentum Collaboration

Included JLab data $W^2 > 4 \text{ GeV}^2 \implies$ reduced errors for valence & sea at $x > 0.1$



JAM, PRD 93 (2016) 074005

Inclusive $g_1(x, Q^2)$ at EIC (pseudo-data)



Errors statistical (EIC: expected, modest parameters); bands: from gluon helicity uncertainty

arXiv:1509.06489

"White paper", arXiv:1212.1701

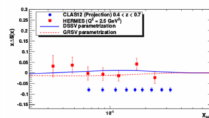
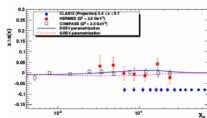
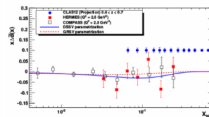
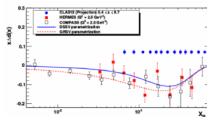
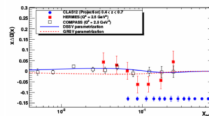
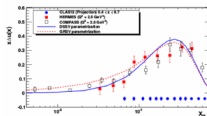
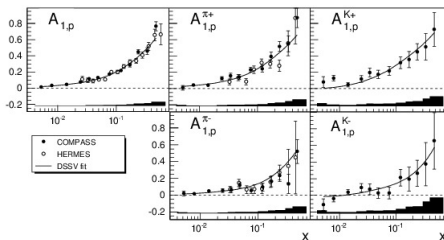
Semi-inclusive asymmetries and parton distributions

- COMPASS: measured on both proton and deuteron targets for identified, positive and negative pions and (for the first time) kaons

COMPASS, Phys. Lett. B **693** (2010) 227

DSSV, Phys. Rev. D **80** (2009) 034030

CLAS12, Update to E12-09-007



- COMPASS: LO DSS fragm. functions and LO unpolarised MRST assumed here.
- NLO parameterisation of DSSV describes the data well.

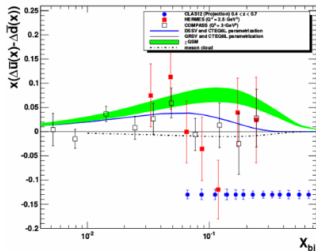
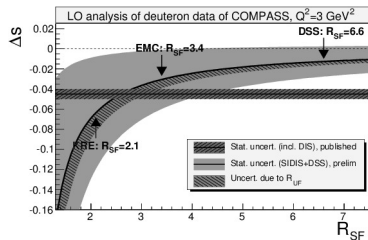
Polarisation of quark sea

- Δs puzzle. Strange quark polarisation:

$2\Delta S = \int_0^1 (\Delta s(x) + \Delta \bar{s}(x)) dx = -0.09 \pm 0.01 \pm 0.02$ from incl. asymmetries + SU_3 ,
while from semi-inclusive asymmetries it is compatible with zero

but depends upon chosen fragmentation functions. **Most critical:** $R_{SF} = \frac{\int D_{\bar{s}}^{K^+}(z) dz}{\int D_u^{K^+}(z) dz}$

\Rightarrow COMPASS extracts it from multiplicities.

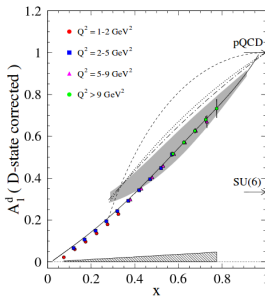
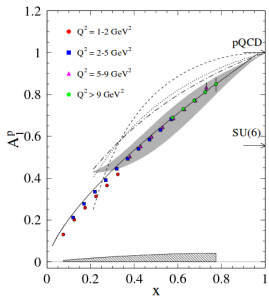


- The sea is not unsymmetric: COMPASS, Phys. Lett. B, **680** (2009) 217; \uparrow CLAS12, Update to E12-09-007

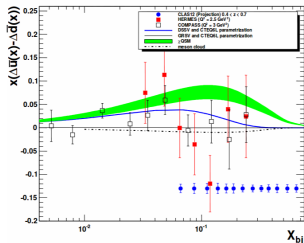
$$\int_{0.004}^{0.3} [\Delta \bar{u}(x, Q^2) - \Delta \bar{d}(x, Q^2)] dx = 0.06 \pm 0.04 \pm 0.02 \quad @ \quad Q^2 = 3 \text{ (GeV/c)}^2$$

Thus the data disfavour models predicting $\Delta \bar{u} - \Delta \bar{d} \gg \bar{d} - \bar{u}$

Nucleon spin structure @ high x : JLab at 12 GeV

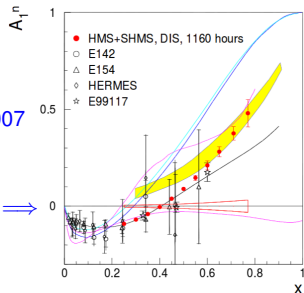


⇐ Hall B (CLAS), E12-06-109
 A_1^p and A_1^d



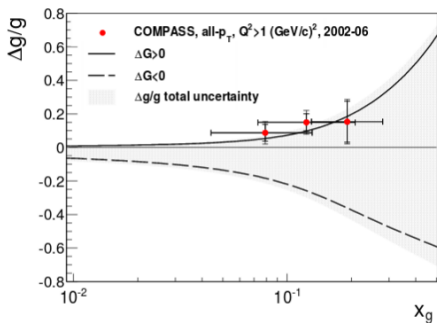
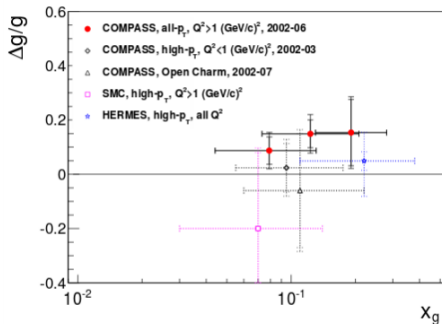
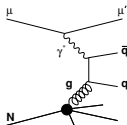
⇐ Hall B (CLAS), E12-09-007
symmetry of the sea

Hall C, E12-06-110, A_1^n ⇒



Direct measurements of $\Delta g(x)$

Direct measurements – *via* the cross section asymmetry for the photon–gluon fusion (PGF) with subsequent fragmentation into $c\bar{c}$ or $q\bar{q}$ pair.

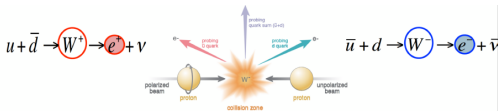


$$\Delta g/g = 0.113 \pm 0.038(\text{stat.}) \pm 0.035(\text{syst.}) \quad \text{at} \quad \langle Q^2 \rangle \approx 3 \text{ GeV}^2, \quad x_G \approx 0.10$$

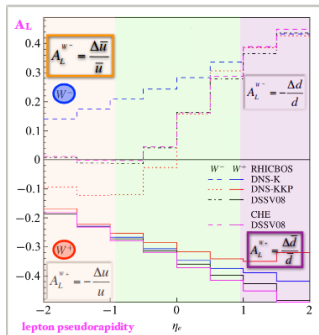
COMPASS, K. Klimaszewski, SPIN2016

A_L for W^\pm production at $\sqrt{s}=510$ GeV @ STAR

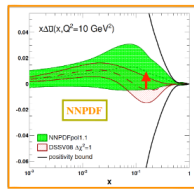
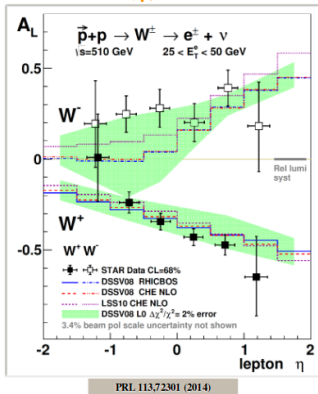
- Direct coupling to $q\bar{q}$ of interest
- Scale set by W mass
- Efficient spin separation
- Easy detection



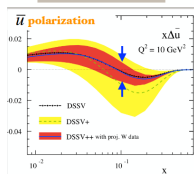
Cartoons from D.Gunarathne, DIS2015



$W A_L(\eta_e)$ 2012+2011

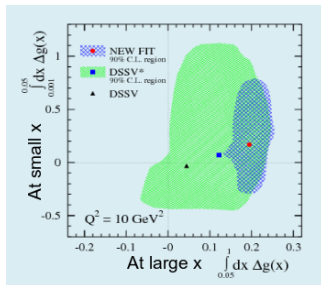
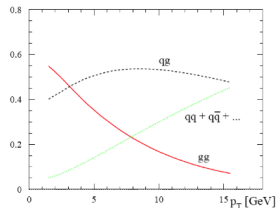
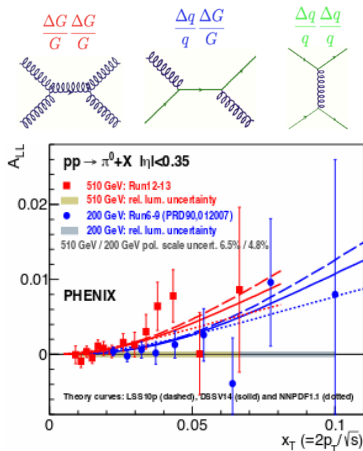


arXiv: 1403.0440



arXiv: 1304.0079

A_{LL} for π^0 production at $\sqrt{s}=200$ and 510 GeV @ PHENIX



DSSV++ with 200 GeV data:




$$\int_{0.05}^{1.0} \Delta g(x) dx = 0.2^{+0.06}_{-0.07}$$

DSSV, PRL 113 (2014) 012001

Global NLO fits

Compilation by M.Stratmann (2015 JLab Users Meeting)

overview of recent helicity PDF fits @ NLO

latest paper				uncertainties	features & focus
NNPDF 1406.5539 Ball, Forte, Guffanti, Nocera, Rodolfini, Rojo				jets W's 100 MC replicas stat. approach	pp data w/ reweighing method
DSSV 0904.3821 1404.4293 de Florian, Sassot, MS, Vogelsang				jets pions Lagrange mult. (Hessian)	pp data fitted fast Mellin method
JAM 1403.3355 Jimenez-Delgado, Accardi, Avakian, Melnitchouk, Sato, ...				Hessian	large x / JLab region pp soon
LSS 1010.0574 Leader, Sidorov, Stamenov				Hessian	higher twist, Δ_s
BBS 1502.02517 1408.7057 Bourrely, Buccella, Soffer				Hessian	statistical approach unpol/pol simult. fit
BB 1010.3113 Blumlein, Bottcher				Hessian	α_s , higher twist
⋮	⋮	⋮	⋮	⋮	⋮
GRSV 9508347 0011215 Gluck, Reya, MS, Vogelsang					1 st NLO analysis 1995

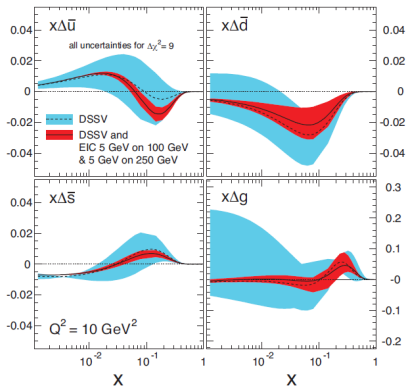
Moving towards NNLO

Higher Twist

Including more probes

31

EIC pseudo-data (inclusive and semi-inclusive)



From "White paper", arXiv:1212.1701

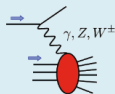
- $\Delta g(x)$ from scaling violation
- $\Delta\bar{u}$, $\Delta\bar{d}$, Δs from SIDIS
- Flavor separation at high Q^2 via CC DIS:

$$g_1^{W^+} = \Delta\bar{u} + \Delta d + \Delta\bar{c} + \Delta s$$

$$g_1^{W^-} = \Delta u + \Delta\bar{d} + \Delta c + \Delta\bar{s}$$

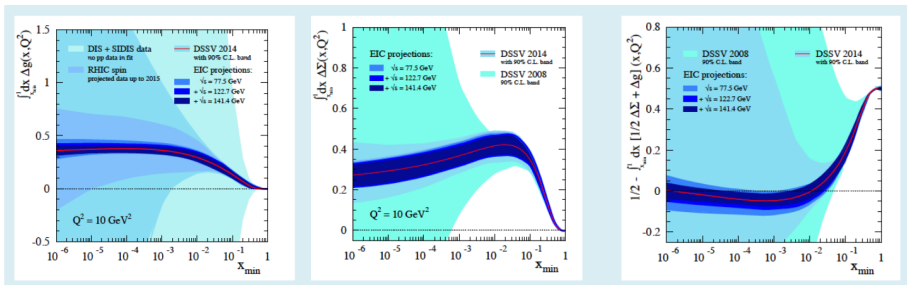
$$g_5^{W^+} = \Delta\bar{u} - \Delta d + \Delta\bar{c} - \Delta s$$

$$g_5^{W^-} = -\Delta u + \Delta\bar{d} - \Delta c + \Delta\bar{s}$$



E. Aschenauer, SPIN2016

Proton Spin Puzzle will be solved @ EIC ?



Aschenauer, Stratmann, Sassot arXiv : 1509.06489

Summary of the proton spin puzzle

- For the proton in \hbar units:

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + \Delta L$$

$$\Delta\Sigma \sim 0.3, \quad \Delta G \sim \text{sizable} \quad \Delta L = ?$$

Do we approach a solution of the proton spin puzzle?

- Yes, but an independent measurement of ΔL needed;**
from the 3D (5D) analysis?
plans at: COMPASS, BNL (USA), Jlab (USA).
- Electron-Ion Collider**
will facilitate in particular an accurate measurement of ΔG .

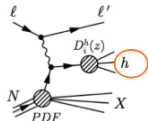
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Charged hadron multiplicities; identified kaons

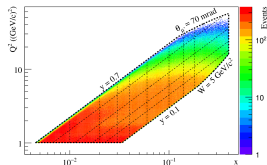
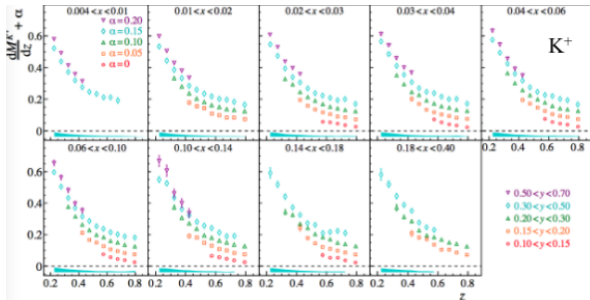
- Studied to measure fragmentation functions (FF), $D_q^h(z, Q^2)$ (\implies cf. Δs).
At LO:

$$\frac{dM^h(x, z, Q^2)}{dz} = \frac{\left(\frac{d\sigma}{dx dz dQ^2}\right)_{\text{SIDIS}}}{\left(\frac{d\sigma}{dx dQ^2}\right)_{\text{DIS}}} = \frac{\sum_q e_q^2 \left[q(x, Q^2) D_q^h(z, Q^2) + \bar{q}(x, Q^2) D_{\bar{q}}^h(z, Q^2) \right]}{\sum_q e_q^2 \left[q(x, Q^2) + \bar{q}(x, Q^2) \right]}$$



- 2006 data; ${}^6\text{LiD}$ target; 317 kinematic bins.

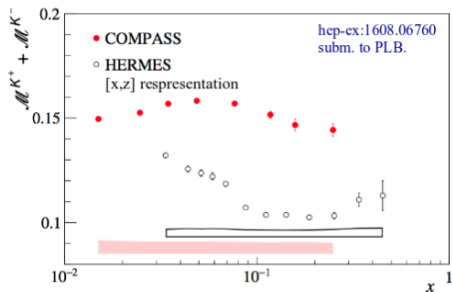
- $Q^2 > 1 \text{ (GeV/c)}^2$, $0.1 < y < 0.7$, $0.004 < x < 0.4$
 $0.2 < z < 0.85$, $12 < p_h < 40 \text{ GeV/c}$ (coverage in W : 5–17 GeV).



COMPASS, hep-ex:1608.06760

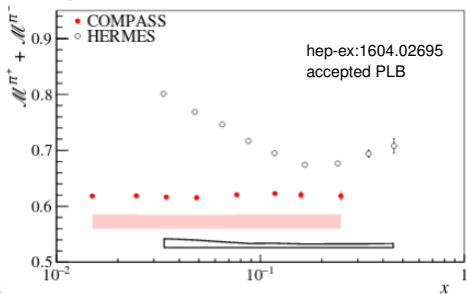
Charged hadron multiplicities; identified kaons and pions

Kaons:



HERMES, PRD 89 (2014)097101

pions:



HERMES, PRD 87 (2013) 074029

- Both π and K multiplicities on the ${}^6\text{LiD}$ (isoscalar) target
- strong discrepancies COMPASS/HERMES in the sum of multiplicities integrated over z, p_T, Q^2 (kinematics is similar)
- Ratio π^+/π^- is OK but K^+/K^- differ by $\sim 20\%$ \implies **under study!**

Outline

- 1 Introduction
- 2 Inclusive and semi-inclusive deep inelastic scattering
- 3 Charged hadron multiplicities
- 4 Measurements on a transversely polarised target**
- 5 Drell-Yan process
- 6 Generalised Parton Distributions

Properties of the transversity, $\Delta_T q(x)$ (or $h_1^q(x)$)

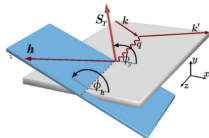
- it is chiral–odd
 \implies hadron(s) in final state needed to be observed (SIDIS reaction)
- simple QCD evolution since no gluons involved
- it is related to Generalised Parton Distributions (GPD)
- there is a sum rule for transverse spin
- first moment gives a “tensor charge” (now being studied on the lattice)

Examples (2 of 8) of measurements on a \perp polarised target

Collins asymmetry (first time by HERMES) \implies permits to access transversity,
 \perp polarised $q \iff p_T^h$ of unpolarised h (asymmetry in the distribution of hadrons):

$$N_h^\pm(\phi_C) = N_h^0 [1 \pm f P_T D_{NN} A_{Coll} \sin \phi_C]$$

$$\phi_C = \phi_h + \phi_S - \pi$$



which in turn gives at LO and at collinear approach:

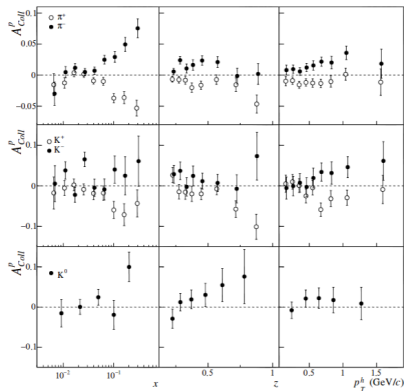
$$A_{Coll} \sim \frac{\sum_q e_q^2 \cdot \Delta_T q(x) \cdot \Delta_T^0 D_q^h(z, p_T^h)}{\sum_q e_q^2 \cdot q(x) \cdot D_q^h(z, p_T^h)}$$

But **transverse fragmentation functions $\Delta_T^0 D_q^h$ (universal!!)** needed to extract $\Delta_T q(x)$ from the Collins asymmetry! Recently FF measured using data of Belle, BaBar and BES III.

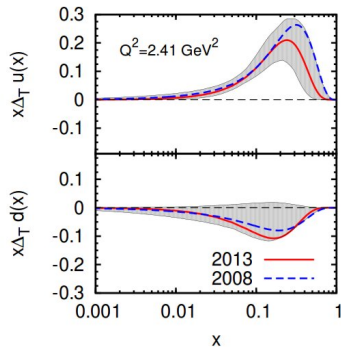
Sivers asymmetry ($\phi_S = \phi_h - \phi_S$, correlation of \perp nucleon spin with k_T of unpolarised q): if $\neq 0$ then $L_q \neq 0$ in the proton. **Fundamental !**

$$A_{Siv} \sim \frac{\sum_q e_q^2 \cdot \Delta_0^T q(x, p_T^h/z) \cdot D_q^h(z)}{\sum_q e_q^2 \cdot q(x, p_T^h/z) \cdot D_q^h(z)}$$

Results for the Collins asymmetry for protons



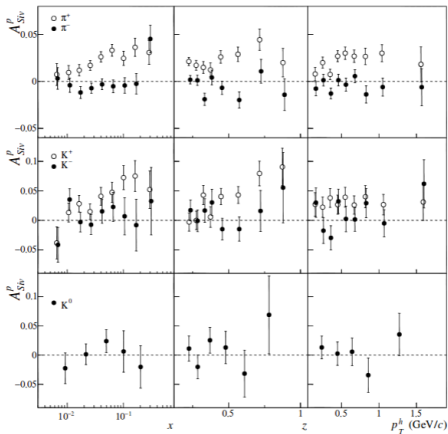
COMPASS, Phys.Lett. B744 (2015) 250



M. Anselmino et al., Phys.Rev. D87 (2013) 094019

- Collins asymmetries for proton measured for +/- unidentified and identified hadrons...
- ...are large at $x \gtrsim 0.03$ and consistent with HERMES (in spite of different Q^2 !)
- but negligible for the deuteron
- COMPASS data on p,d + HERMES data on p (2005) + BELLE on e^+e^- : $\implies \Delta_T u, \Delta_T d$
- Transversity also obtained from 2-hadron asymmetries (and "Interference Fragmentation Function")

Results for the Sivers asymmetry for protons



COMPASS, Phys.Lett. B744 (2015) 250

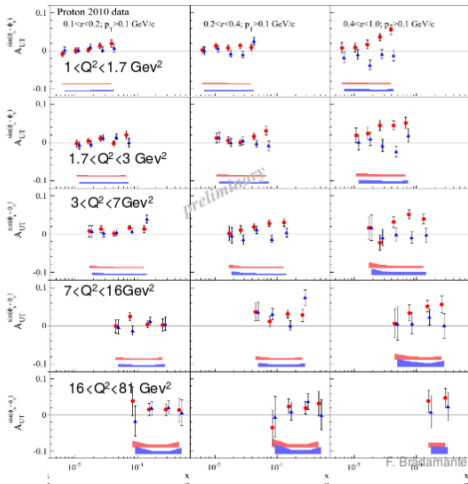
- Sivers asymmetries for proton measured for +/- identified hadrons are large for π^+ , K^+ ...
- ...and even larger at smaller Q^2 (HERMES)
- COMPASS deuteron data show very small asymmetry

Multidimensional analyses: Sivers asymmetry ($x, Q^2; z, p_T$)

the Sivers asymmetry

 $p_T > 0.1 \text{ GeV}/c$ $0.1 < z < 0.2$ $0.2 < z < 0.4$ $0.4 < z < 1.0$

multiD ($x, Q^2; z, p_T$)
 results
 an example



SPIN2016

Other azimuthal asymmetries

SIDIS x-section

A. Kotzinian, Nucl. Phys. B441, 234 (1995).

Bacchetta, Diehl, Goika, Metz, Mulders and Schlegel JHEP0702:093 (2007).



$$\frac{d\sigma}{dx dy dz dF_T^2 d\phi_n d\psi} = \left[\frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \right] (F_{UU,T} + \epsilon F_{UU,L}) \times$$

$$\left\{ \begin{aligned} & 1 + \cos\phi_n \left(\sqrt{2\epsilon(1+\epsilon)} A_{LU}^{n+\phi_n} \right) + \cos 2\phi_n \left(\epsilon A_{LU}^{n+2\phi_n} \right) \\ & + \lambda \sin\phi_n \left(\sqrt{2\epsilon(1-\epsilon)} A_{LU}^{n+\phi_n} \right) \\ & + S_L \left[\sin\phi_n \left(\sqrt{2\epsilon(1+\epsilon)} A_{LL}^{n+\phi_n} \right) + \sin 2\phi_n \left(\epsilon A_{LL}^{n+2\phi_n} \right) \right] \\ & + S_L \lambda \left[\sqrt{1-\epsilon^2} A_{LL} + \cos\phi_n \left(\sqrt{2\epsilon(1-\epsilon)} A_{LL}^{n+\phi_n} \right) \right] \end{aligned} \right.$$

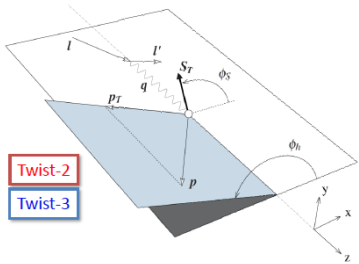
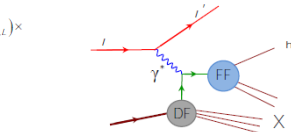
$$\left\{ \begin{aligned} & \sin(\phi_n - \phi_S) \left(A_{UT}^{n(\phi_n - \phi_S)} \right) \\ & + \sin(\phi_n + \phi_S) \left(\epsilon A_{UT}^{n(\phi_n + \phi_S)} \right) \\ & + S_T \left[\sin(3\phi_n - \phi_S) \left(\epsilon A_{UT}^{n(3\phi_n - \phi_S)} \right) \right. \\ & + \sin\phi_S \left(\sqrt{2\epsilon(1+\epsilon)} A_{UT}^{n+\phi_S} \right) \\ & \left. + \sin(2\phi_n - \phi_S) \left(\sqrt{2\epsilon(1+\epsilon)} A_{UT}^{n(2\phi_n - \phi_S)} \right) \right] \\ & \text{---} \\ & + S_T \lambda \left[\cos(\phi_n - \phi_S) \left(\sqrt{1-\epsilon^2} A_{LT}^{n(\phi_n - \phi_S)} \right) \right. \\ & + \cos\phi_S \left(\sqrt{2\epsilon(1-\epsilon)} A_{LT}^{n+\phi_S} \right) \\ & \left. + \cos(2\phi_n - \phi_S) \left(\sqrt{2\epsilon(1-\epsilon)} A_{LT}^{n(2\phi_n - \phi_S)} \right) \right] \end{aligned} \right.$$

SSA

↑

DSA

↓



Twist-2
Twist-3

$$A_{U(L),T}^{n(\phi_n)} = \frac{F_{U(L),T}^{n(\phi_n)}}{F_{UU,T} + \epsilon F_{UU,L}}; \quad \epsilon = \frac{1-y - \frac{1}{4}\gamma^2 y^2}{1-y + \frac{1}{2}y^2 + \frac{1}{4}\gamma^2 y^2}; \quad \gamma = \frac{2Mx}{Q}$$

22 October 2014

Bakur Parsamyan

8

Other azimuthal asymmetries...cont'd

SIDIS x-section

A.Kotzinian, Nucl. Phys. B441, 234 (1995).

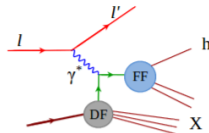
Bacchetta, Diehl, Goeke, Metz, Mulders and Schlegel JHEP 0702:093 (2007).



$$\frac{d\sigma}{dxdydzdP_{T,1}^2 d\phi_h d\psi} = \left[\frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{z^2}{2x} \right) \right] (F_{LU,T} + \varepsilon F_{UU,L}) \times$$

$$\left. \begin{aligned} & 1 + \cos\phi_h \left(\sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\phi_h} \right) + \cos 2\phi_h \left(\varepsilon A_{UU}^{\cos 2\phi_h} \right) \\ & + \lambda \sin\phi_h \left(\sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin\phi_h} \right) \\ & + S_L \left[\sin\phi_h \left(\sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\phi_h} \right) + \sin 2\phi_h \left(\varepsilon A_{UL}^{\sin 2\phi_h} \right) \right] \\ & + S_L \lambda \left[\sqrt{1-\varepsilon^2} A_{LL} + \cos\phi_h \left(\sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\phi_h} \right) \right] \end{aligned} \right\}$$

$$\left. \begin{aligned} & \left. \begin{aligned} & \sin(\phi_h - \phi_s) \left(A_{UT}^{\sin(\phi_h - \phi_s)} \right) \\ & + \sin(\phi_h + \phi_s) \left(\varepsilon A_{UT}^{\sin(\phi_h + \phi_s)} \right) \\ & + \sin(3\phi_h - \phi_s) \left(\varepsilon A_{UT}^{\sin(3\phi_h - \phi_s)} \right) \\ & + \sin\phi_h \left(\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin\phi_h} \right) \\ & + \sin(2\phi_h - \phi_s) \left(\sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\phi_h - \phi_s)} \right) \end{aligned} \right\} \text{SSA} \\ & \left. \begin{aligned} & \cos(\phi_h - \phi_s) \left(\sqrt{1-\varepsilon^2} A_{LT}^{\cos(\phi_h - \phi_s)} \right) \\ & + \cos\phi_h \left(\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos\phi_h} \right) \\ & + \cos(2\phi_h - \phi_s) \left(\sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\phi_h - \phi_s)} \right) \end{aligned} \right\} \text{DSA} \end{aligned} \right\}$$



$$A_{UT}^{\sin(\phi_h - \phi_s)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h$$

$$A_{UT}^{\sin(\phi_h + \phi_s)} \propto h_1^q \otimes H_{1q}^{\perp h}$$

$$A_{UT}^{\sin(3\phi_h - \phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$

$$A_{UT}^{\sin\phi_h} \propto Q^{-1} \left(h_1^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right)$$

$$A_{UT}^{\sin(2\phi_h - \phi_s)} \propto Q^{-1} \left(h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right)$$

$$A_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$$

$$A_{LT}^{\cos\phi_h} \propto Q^{-1} \left(g_{1T}^q \otimes D_{1q}^h + \dots \right)$$

$$A_{LT}^{\cos(2\phi_h - \phi_s)} \propto Q^{-1} \left(g_{1T}^q \otimes D_{1q}^h + \dots \right)$$

Twist-2

Twist-3

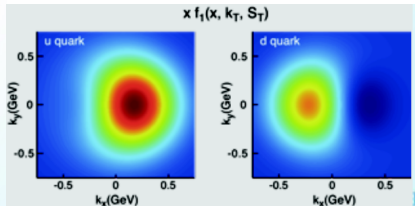
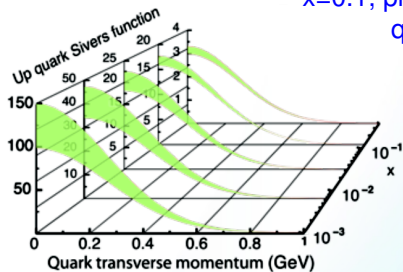
26 May 2015

Bakur Parsamyan

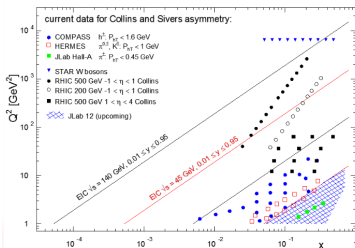
11

Sivers function at EIC

$x=0.1$, proton \perp polarised along y , moving along z
quark “flow” in a nucleon



From “White paper”, arXiv:1212.1701



← EIC acceptance for Sivers meas.

O. Eysler, SPIN2016

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- 1 Introduction
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Partonic structure of the nucleon; distribution functions

- In LT and considering k_T , 8 PDF describe the nucleon
 \implies Transverse Momentum Dependent PDF

- QCD-TMD approach valid $k_T \ll \sqrt{Q^2}$

- After integrating over k_T only 3 survive: f_1, g_1, h_1

- TMD accessed in SIDIS and DY by measuring azimuthal asymmetries with different angular modulations

- SIDIS: e.g. $A_{\text{Sivers}} \propto \text{PDF} \otimes \text{FF}$

- DY: e.g. $A_{\text{Sivers}} \propto \text{PDF}^{\text{beam}} \otimes \text{PDF}^{\text{target}}$

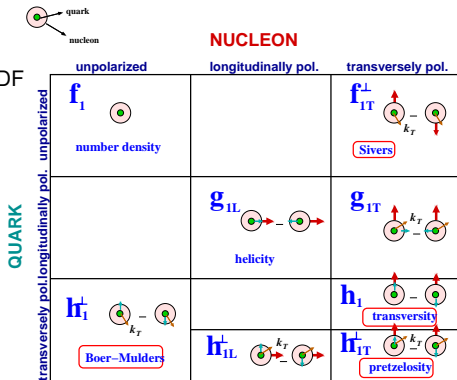
- OBS! Boer-Mulders and Sivers PDF are T-odd, i.e. process dependent

$$h_1^\perp(\text{SIDIS}) = -h_1^\perp(\text{DY})$$

$$f_{1T}^\perp(\text{SIDIS}) = -f_{1T}^\perp(\text{DY})$$

- OBS! transversity PDF is chiral-odd; may only be measured with another chiral-odd partner, e.g. fragmentation function.

- TMD parton distributions need TMD Fragmentation Functions!

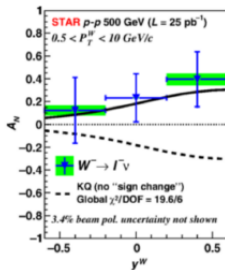
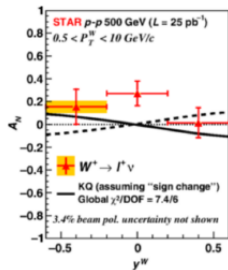


Sivers sign change?

The STAR experiment at RHIC recently reported the measurement of A_N in $p^\uparrow + p \rightarrow W^\pm/Z^0$ at $\sqrt{s} = 500\text{GeV}$. One of the beams is polarized ($\langle P \rangle = 53\%$)

STAR, Phys.Rev.Lett. **116**, 132301 (2016)

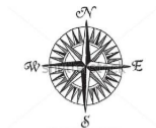
A_N compared to models where Sivers TMD is obtained from SIDIS data



- KQ: Z-B. Kang and J-W. Qiu, Phys.Rev.Lett. **103**, 172001 (2009)
- KQ model does not include TMD evolution effect. It does not take into account the very large difference between k_T at SIDIS and at DY.
- Data comparison with KQ model shows preference for a sign change of Sivers TMD from DY wrt SIDIS

★ Devika Gunarathne talk, tuesday morning

The COMPASS bridge



Courtesy of B. Parsamyan, COMPASS

Nucleon TMD PDFs accessed via SIDIS and Drell-Yan asymmetries

SIDIS $\ell \rightarrow N^\uparrow$	Nucleon TMD PDF	Drell-Yan πN^\uparrow (LO)
$A_{UU}^{\cos 2\phi_h}$, $A_{UU}^{\cos \phi_h}$	$h_1^{\perp q}$ - "Boer-Mulders"	$A_U^{\cos 2\varphi_{CS}}$
$A_{UT}^{\sin(\phi_h - \phi_s)}$, $A_{UT}^{\sin \phi_s}$, $A_{UT}^{\sin(2\phi_h - \phi_s)}$	$f_{1T}^{\perp q}$ - "Sivers"	$A_T^{\sin \varphi_s}$
$A_{UT}^{\sin(\phi_h + \phi_s - \pi)}$, $A_{UT}^{\sin \phi_s}$	h_1^q - "Transversity"	$A_T^{\sin(2\varphi_{CS} - \varphi_s)}$
$A_{UT}^{\sin(3\phi_h - \phi_s)}$, $A_{UT}^{\sin(2\phi_h - \phi_s)}$	$h_{1T}^{\perp q}$ - "Pretzelosity"	$A_T^{\sin(2\varphi_{CS} + \varphi_s)}$
$A_{LT}^{\cos(\phi_h - \phi_s)}$, $A_{LT}^{\cos \phi_s}$, $A_{LT}^{\cos(2\phi_h - \phi_s)}$	g_{1T}^q - "Worm-Gear" (T)	Double-polarized DY

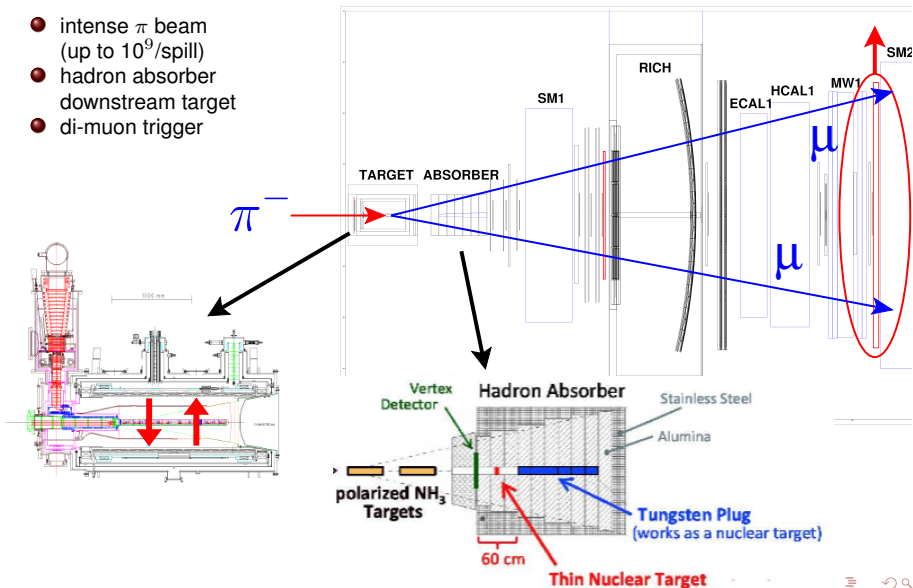
Color code:

LO asymmetries: twist 2 TMDs \otimes FFs

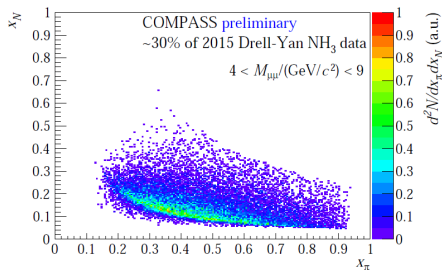
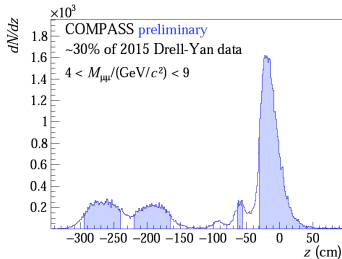
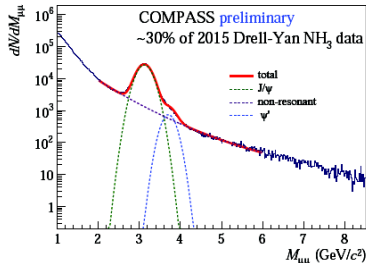
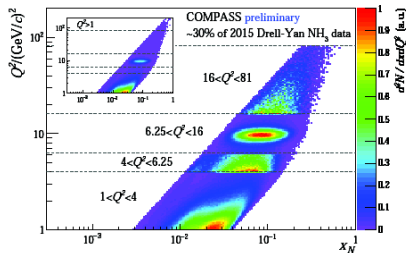
HT asymmetries

Drell-Yan @ COMPASS: experimental requirements

- intense π^- beam (up to 10^9 /spill)
- hadron absorber downstream target
- di-muon trigger



Drell-Yan @ COMPASS: preliminary results from 30% 2015 data



TSAs from (un)polarized DY – the future

After the check of sign of Sivers TMD in Drell-Yan wrt SIDIS, a new phase will come for studying in detail dependencies and TMD evolution. It will require input from both type of processes.

Several (un)polarized Drell-Yan experiments are being planned:

Experiment	type	$\sqrt{s}(GeV)$	when
STAR (RHIC)	collider; $p^\uparrow p$	510	2017
COMPASS (CERN)	fixed target; $\pi^- p^\uparrow, K^- p^\uparrow$	18.9	2018
E1039 (FNAL)	fixed target; $pp \uparrow$	15	2018-2019
J-PARC (KEK))	fixed target; $\pi^- p$	3-5.5	>2018
NICA (JINR)	collider; $p^\uparrow p^\uparrow, p^\uparrow d^\uparrow$	10-26	>2018
E1027 (FNAL)	fixed target; $p^\uparrow p$	15	>2020
PANDA (FAIR)	fixed target; $\bar{p}p$	5.5	>2022
J-PARC (KEK)	fixed target; $K^- p, \bar{p}p$	2.2-4.5	>2022
AFTER (CERN)	fixed target; pp^\uparrow	115	2025
COMPASS+ (CERN)	fixed target; $K^- p^\uparrow, \bar{p}p^\uparrow$	≈ 20	2025

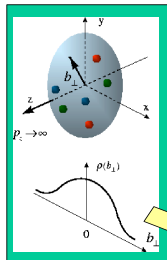
* List possibly not complete

Outline

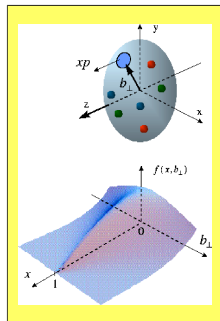
- 1 Introduction
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3D picturing of the proton *via* GPD

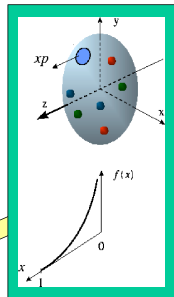
D. Mueller, X. Ji, A. Radyushkin, A. Belitsky, ...
M. Burkardt, ... Interpretation in impact parameter space



Proton form factors,
transverse charge &
current densities



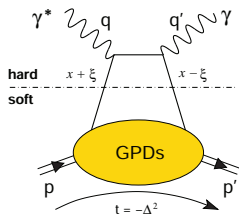
Correlated quark momentum
and helicity distributions in
transverse space - **GPDs**



Structure functions,
quark **longitudinal**
momentum & helicity
distributions

After V.D. Volker, LANL 2007

Access GPD through the DVCS/DVMP mechanism

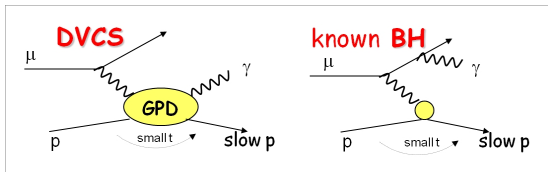
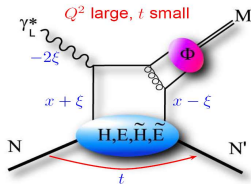


$Q^2 \rightarrow \infty$,
fixed $x_B, t \implies |t|/Q^2$ small

- 4 GDPs ($H, E, \tilde{H}, \tilde{E}$) for each flavour and for gluons plus 4 chiral odd ones ($H_T, E_T, \tilde{H}_T, \tilde{E}_T$)
- DVMP: factorisation proven for σ_L only
- All depend on 4 variables: x, ξ, t, Q^2 ; DIS @ $\xi = t = 0$; Later Q^2 dependence omitted. **Careful ! Here $x \neq x_B$!**
- H, \tilde{H} conserve nucleon helicity
 E, \tilde{E} flip nucleon helicity
- H, E refer to unpolarised distributions
 \tilde{H}, \tilde{E} refer to polarised distributions
- $H^q(x, 0, 0) = q(x), \tilde{H}^q(x, 0, 0) = \Delta q(x)$

- H, E accessed in vector meson production *via* A_{UT} asymmetries
- \tilde{H}, \tilde{E} accessed in pseudoscalar meson production *via* A_{UT} asymmetries
- All 4 accessed in DVCS (γ production) in $A_C, A_{LU}, A_{UT}, A_{UL}$
- Integrals of $H, E, \tilde{H}, \tilde{E}$ over x give Dirac-, Pauli-, axial vector- and pseudoscalar vector form factors respectively.
- **Important:** $J_z^q = \frac{1}{2} \int dx x [H^q(x, \xi, t=0) + E^q(x, \xi, t=0)] = \frac{1}{2} \Delta \Sigma + L_z^q$ (X. Ji)

DVCS/DVMP: $\mu p \rightarrow \mu p \gamma(M)$; observables



$$d\sigma^{\mu p \rightarrow \mu p \gamma} = d\sigma^{\text{BH}} + (d\sigma_{\text{unpol}}^{\text{DVCS}} + P_\mu d\sigma_{\text{pol}}^{\text{DVCS}}) + e_\mu (\text{Re}I + P_\mu \text{Im}I)$$

Observables (Phase 1):

$$\bullet S_{\text{CS,U}} \equiv \mu^{+\leftarrow} + \mu^{-\rightarrow} = 2 \left(d\sigma^{\text{BH}} + d\sigma_{\text{unpol}}^{\text{DVCS}} + e_\mu P_\mu \text{Im}I \right)$$

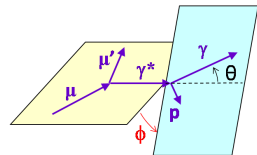
$$\bullet D_{\text{CS,U}} \equiv \mu^{+\leftarrow} - \mu^{-\rightarrow} = 2 \left(P_\mu d\sigma_{\text{pol}}^{\text{DVCS}} + e_\mu \text{Re}I \right)$$

$$\bullet A_{\text{CS,U}} \equiv \frac{\mu^{+\leftarrow} - \mu^{-\rightarrow}}{\mu^{+\leftarrow} + \mu^{-\rightarrow}} = \frac{D_{\text{CS,U}}}{S_{\text{CS,U}}}$$

• Each term ϕ -modulated

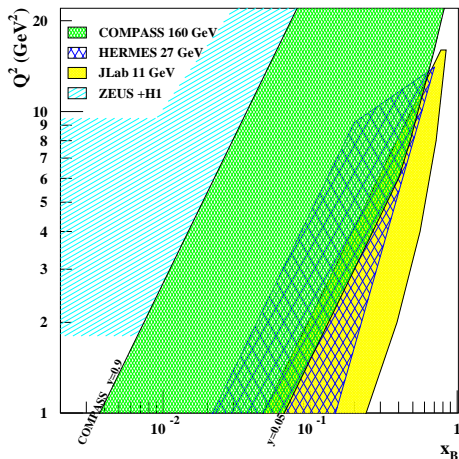
If ϕ -dependence integrated over \Rightarrow twist-2 DVCS contribution;

if ϕ -dependence analysed: $\Rightarrow \text{Im}(F_1 H)$ and $\text{Re}(F_1 H)$; H dominance @ COMPASS kin.



Analogously for transversely polarised target (Phase 2): $S_{\text{CS,T}}, D_{\text{CS,T}}, A_{\text{CS,T}} \Rightarrow E$

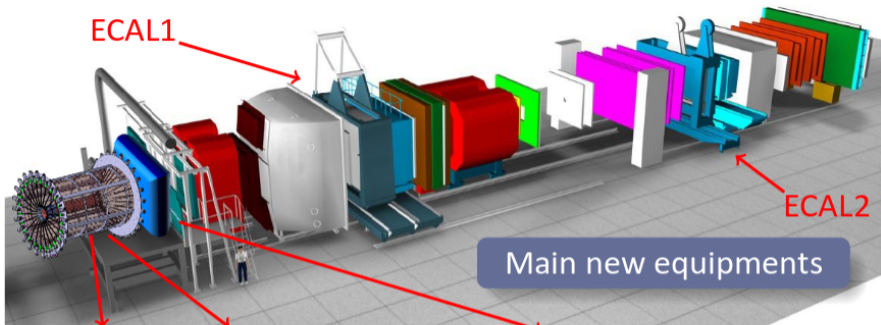
GPD at COMPASS: data taking in 2016-2017



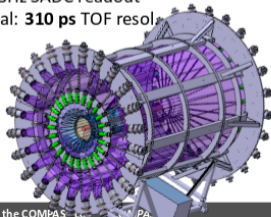
- CERN high energy muon beam
 - 100 - 190 GeV
 - 80% polarisation
 - $\mu^+ \leftarrow$ and $\mu^- \rightarrow$ beams
- Kinematic range
 - between HERA and HERMES/JLab12
 - intermediate x (sea and valence)
- Separation
 - pure B-H @ low x_B
 - predominant DVCS @ high x_B
- Plans
 - DVCS
 - DVMP
- Goals
 - from unpolarised target: H (Phase 1)
 - from \perp polarised target: E (Phase 2)

Test runs: 2008-9 and 2012; DVCS signal seen, full setup evaluated

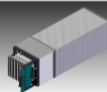
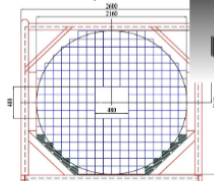
The COMPASS set-up for the GPD program



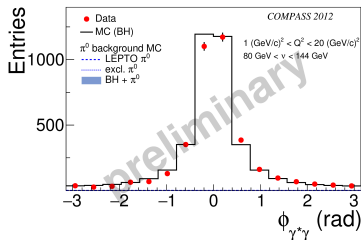
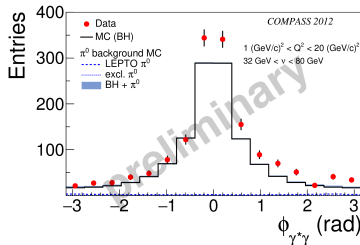
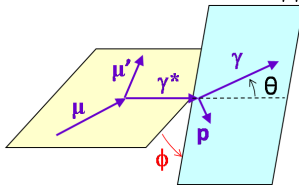
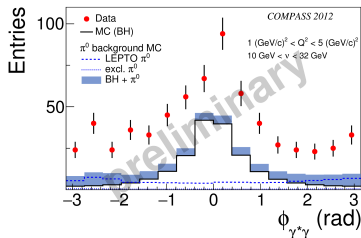
Target TOF System
24 inner & outer scintillators
1 GHz SADC readout
goal: **310 ps** TOF resol.



ECAL0 Calorimeter
Shashlyk modules + MAPD readout
 $\sim 2 \times 2 \text{ m}^2$, ~ 2200 ch.



DVCS signal

 $0.005 < x < 0.01$  $0.001 < x < 0.03$  $x > 0.03$ 

Plans for 2016–2017 run

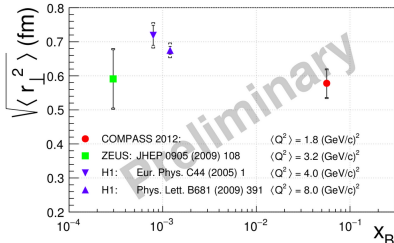
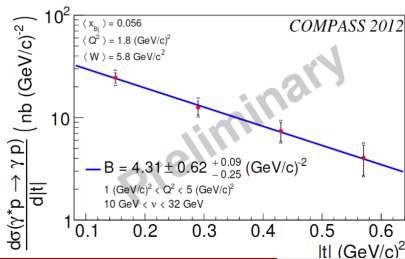
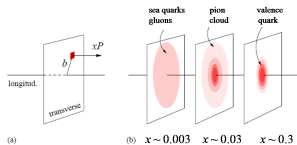
- $S_{CS,U}, D_{CS,U}, A_{CS,U}$ measured in $6 x_B \times 4 Q^2$ bins as function of ϕ
 \implies determination of H with flavour separation
 (from VM production)

- Azimuthal dependence $A_{CS,U}$ compared to models

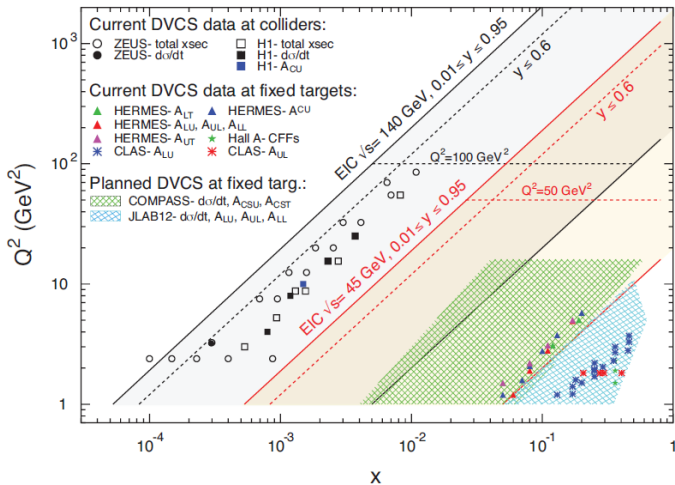
- Nucleon transverse imaging (“tomography”):

from $S_{CS,U} \implies \frac{d\sigma^{DVCS}}{dt} \propto e^{-B(x_B)|t|}$ where at low x_B : $B(x_B) \approx \frac{1}{2} \langle r_{\perp}^2(x_B) \rangle$

(here a simple ansatz was assumed: $B(x_B) = B_0 + 2\alpha' \log \frac{x_0}{x_B}$)



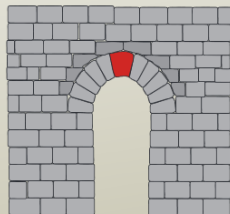
Acceptance of present and EIC DVCS



Instead of a summary

D. Soper, DIS2015

- Thus the DIS experiments on which the parton distribution functions are largely based are like a keystone in the arch that supports the edifice of particle physics.



P. Mulders, DIS2015

Spin Physics and Transverse Structure

Piet Mulders (Nikhef Theory Group/VU University Amsterdam)

Spin is a welcome complication in the study of partonic structure that has led to new insights, even if experimentally not all dust has settled, in particular on quark flavor dependence and gluon spin. At the same time it opened new questions on angular momentum and effects of transverse structure, in particular the role of the transverse momenta of partons. This provides again many theoretical and experimental challenges and hurdles. But it may also provide new tools in high-energy scattering experiments linking polarization and final state angular dependence.