

“Exclusive  $J/\psi$  process tamed to probe the  
low  $x$  gluon: power correction”

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S.P. Jones, A.D. Martin, M.G. Ryskin and T. Teubner

Exclusive  $J/\psi$  production in  $\gamma p$  or  
in ultraperipheral  $pp \rightarrow p + J/\psi + p$  processes allows to probe  
gluons at *very* low  $x$ .  
down to  $x = 3 \cdot 10^{-6}$  for LHCb at 13 TeV.

$$\left. \frac{d\sigma}{dt}(\gamma^* p \rightarrow J/\psi p) \right|_{t=0} = \frac{\Gamma_{ee} M_\psi^3 \pi^3}{3\alpha_{\text{QED}}} \left[ \frac{4\alpha_s}{(Q^2 + M_\psi^2)^2} x g(x, \mu_F^2) \right]^2 \left( 1 + \frac{Q^2}{M_\psi^2} \right)$$

The problems:

D.Y.Ivanov, A.Schafer, L.Szymanowski, G.Krasnikov EPJ C34 (2004) 297

A. Bad perturbative convergency –  $|\text{NLO}_{\text{correct.}}| > |\text{LO}|$

B. Strong dependence on  $\mu_F$  due to:

i) large  $\ln(1/x)$  in  $(\alpha_s \ln(1/x) \ln \mu_F^2)^n$  terms

ii) cancellation between NLO and LO contributions.

(for  $\Upsilon$  situation is better)

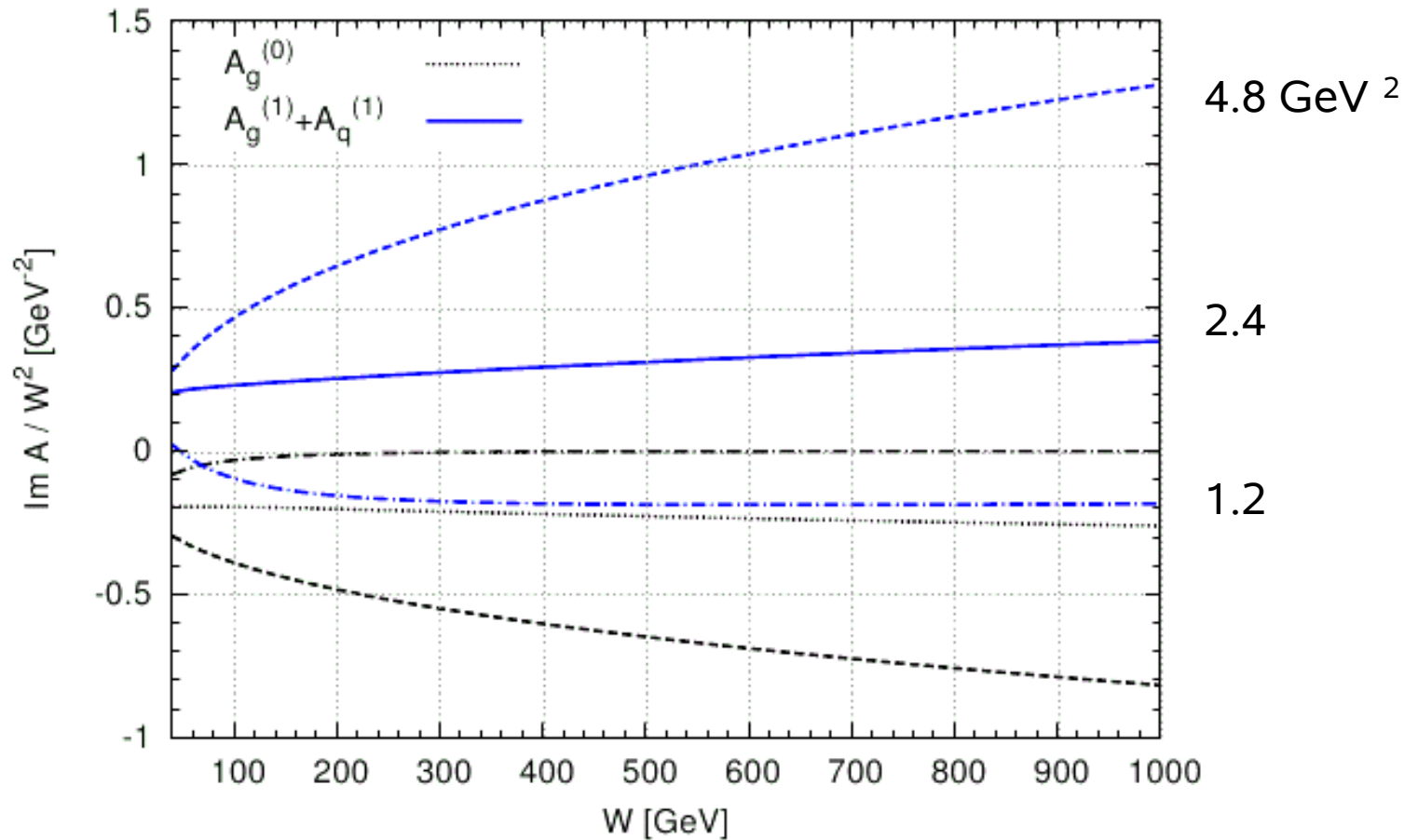


Figure 1: Predictions of  $\text{Im}A/W^2$  for  $\gamma p \rightarrow J/\psi + p$  as a function of the  $\gamma p$  centre-of-mass energy  $W$ , produced using CTEQ6.6 partons [4] with scales  $\mu \equiv \mu_F = \mu_R$ . The bottom (top) set of curves corresponds to the Born (1-loop) contribution with the scale variation  $\mu^2 = m_c^2/2, m_c^2, 2m_c^2 \text{ GeV}^2$ , where  $m_c \equiv M_\psi/2$ . The dot-dashed, solid and dashed lines correspond to the low, central and high values of the scale  $\mu$ , respectively. Note that the bands overlap for energies bigger than about 70 GeV. The figure is taken from Ref. [3]. JMRT J.Phys. G43 (2016) 035002

## Power $Q_0^2/\mu_F^2$ correction

We start DGLAP at  $Q_0$ .

*Everything* below  $Q_0$  is included in INPUT  $PDF(Q_0)$ . NLO contr. from  $|q^2| < Q_0^2$  is the double counting.

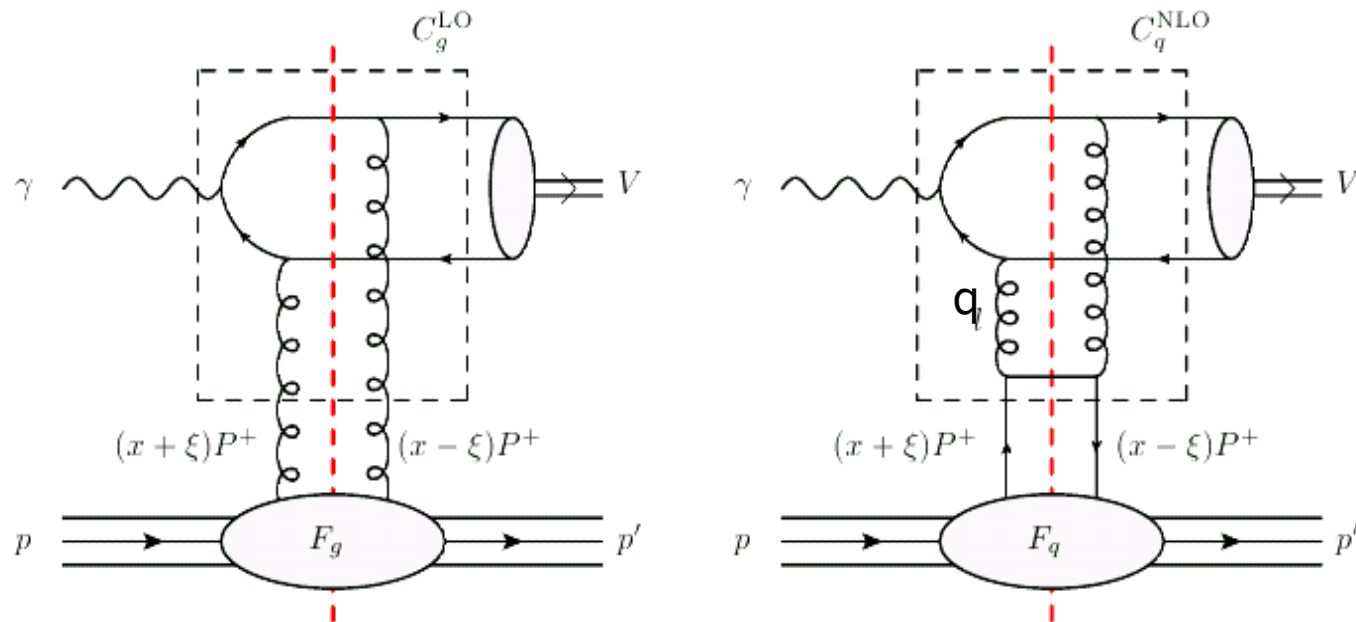


Figure 2: (a) The LO contribution to  $\gamma p \rightarrow V + p$ . (b) The NLO quark contribution. For these graphs all permutations of the parton lines and coupling of the gluon lines to the heavy-quark pair are to be understood. Here  $P \equiv (p + p')/2$  and  $l$  is the loop momentum.

Solution:

A. to subtract NLO( $|q^2| < Q_0^2$ ) contribution

B. to resum the  $(\alpha_s \ln(1/x) \ln \mu_F^2)^n$  double Log.s

by choosing  $\mu_F = M_\psi/2$  [JMRT, J. Phys. G43 \(2016\) 035002](#)

$$\mathbf{A}^{(0+1)}(\mu_f) \equiv \mathbf{C}^{\text{LO}} \otimes \mathbf{GPD}(\mu_F) + \mathbf{C}^{\text{NLO}}(\mu_F) \otimes \mathbf{GPD}(\mu_f)$$

$$\mu_R = \mu_F$$

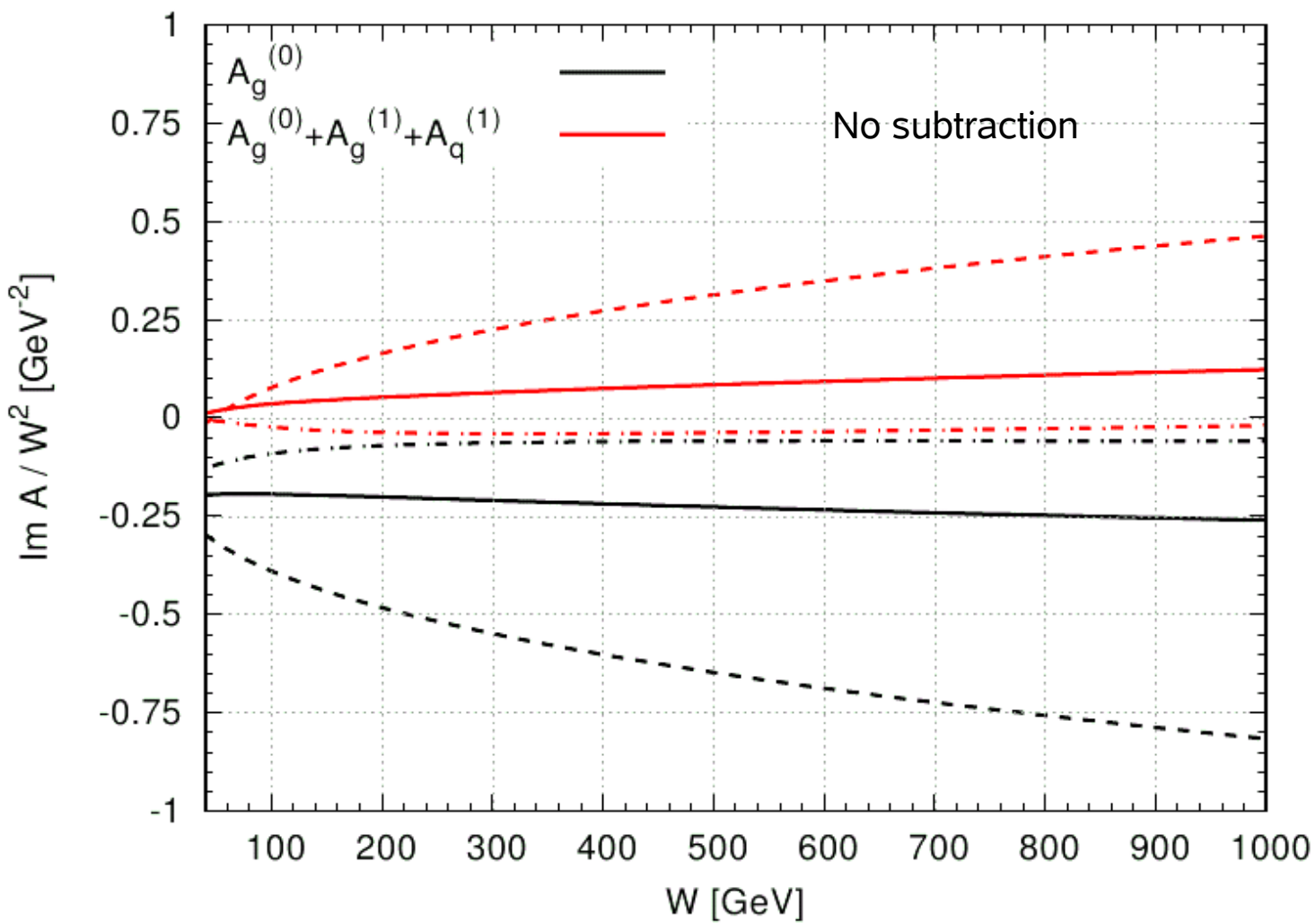
a) BLM prescription – the NLO term  $\beta_0 \ln(\mu_R/\mu_F) = 0$

b) Consider the quark loop in gluon propagator.

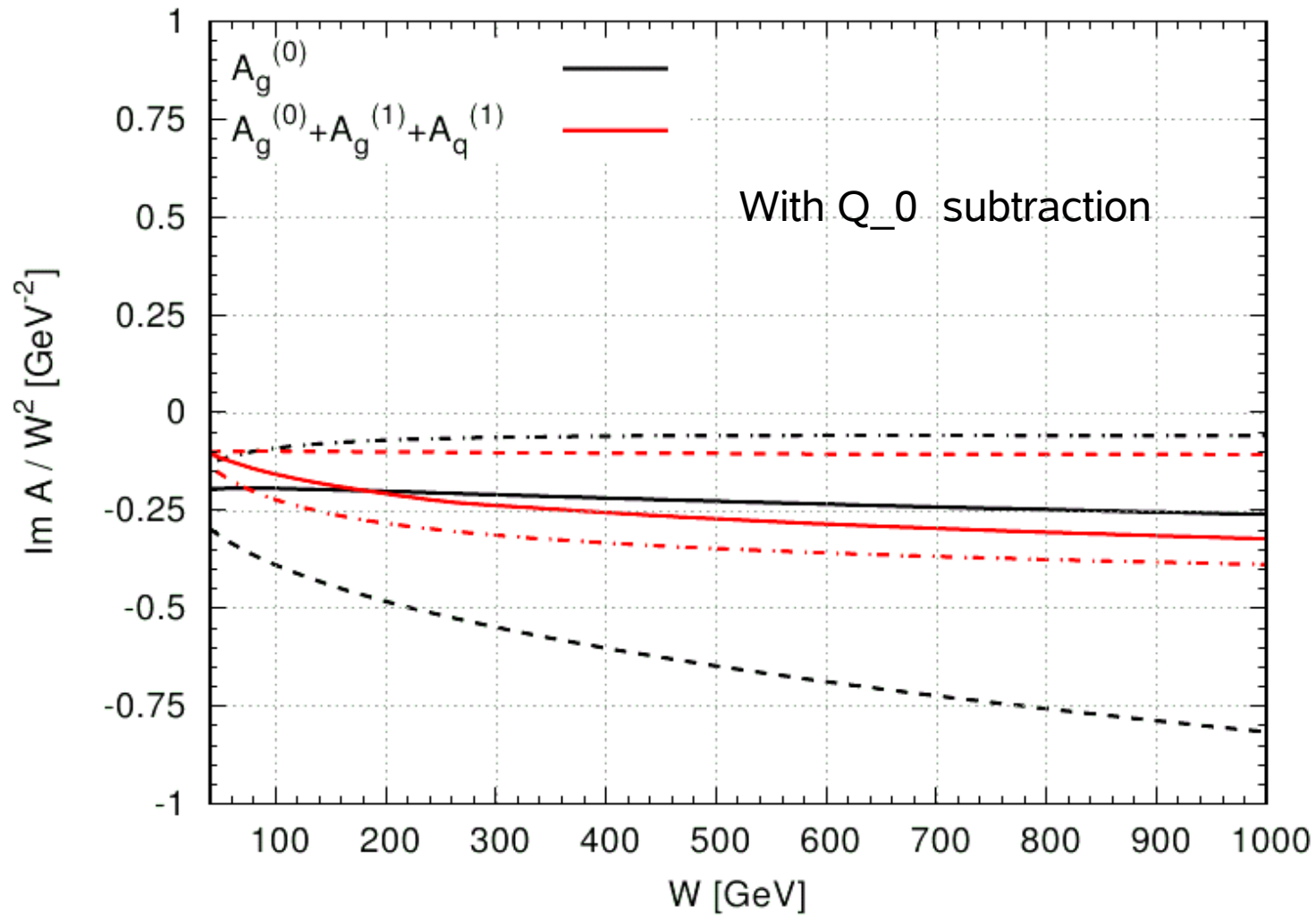
It contains the  $\ln(\mu_F/Q_0)$  from DGLAP and

$\ln(\Lambda_{UV}/\mu_R)$  from  $\alpha_s(\mu_R)$

$\mu_R = \mu_F$  provides smooth matching without the double counting.

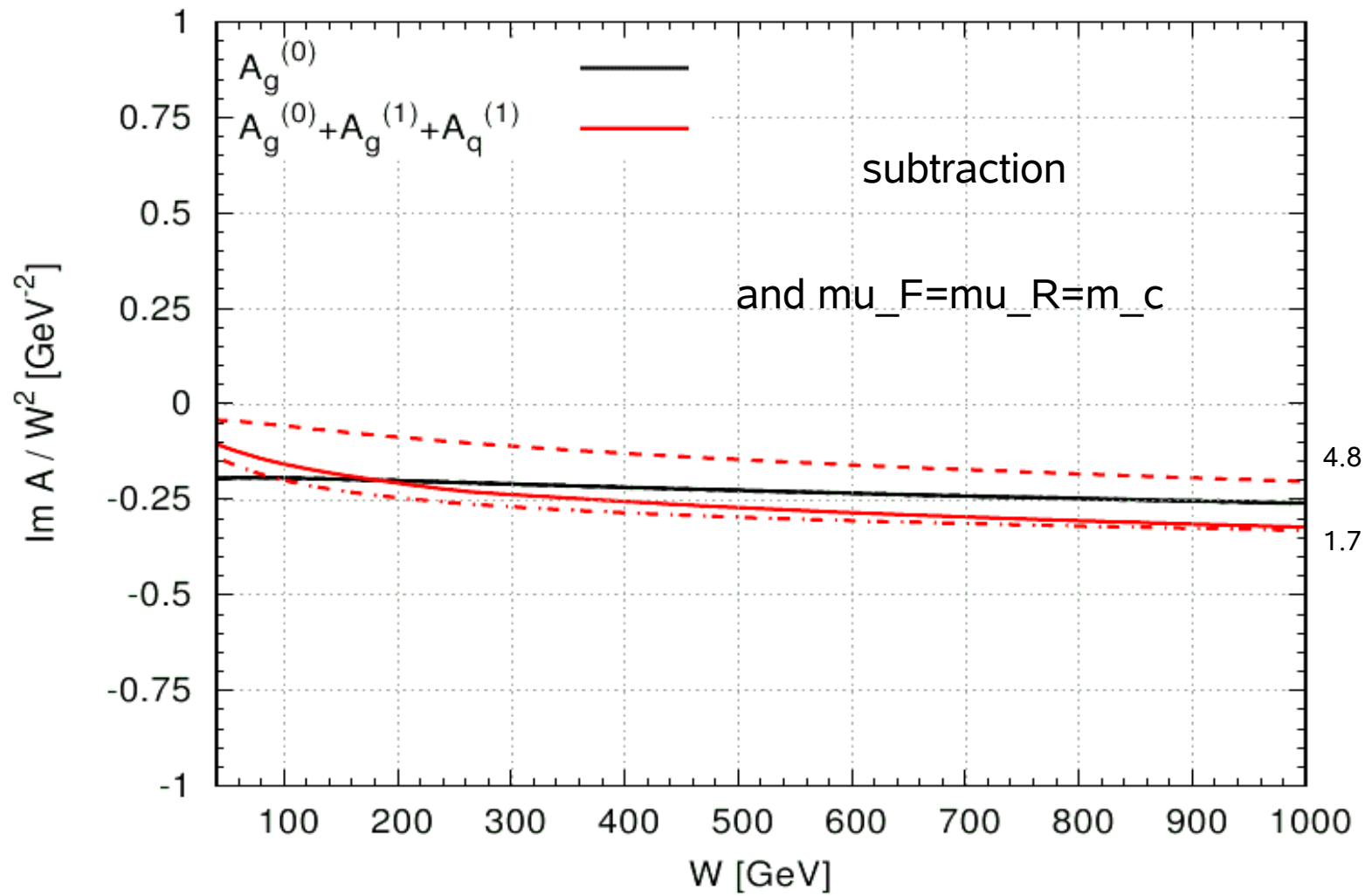


$\mu_F = \mu_R = 1.7, 2.4, 4.8 \text{ GeV}^2$



preliminary





preliminary

# Conclusion

Subtraction of  $\text{NLO}(q^2 | < Q_0^2)$  plus  $\mu_F = M_\psi/2$  choice

(no double counting)

(resum of double Logs)

**provide good accuracy** for  $\gamma p \rightarrow J/\psi + p$  amplitude.

## Backup

The SUM of relativistic correct. plus  $\alpha_s$ -correct. in  $J/\psi$  wave. funct. is small ( $\sim$  few %) [P.Hoodbhoy PR D56 \(1997\) 388](#)

For a low  $x$   $\text{GPD}(\mathbf{x}) = \text{PDF}(\mathbf{x}) \otimes$  Shuvaev transform  
assuming  $H_N = M_N$  and no singularity in the right half  $N$ -plane  
in PDF input

Re/Im can be calculated via the dispersion relation  
for positive signature amplitude.