

The LUX approach to the photon PDF

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Outline

- ▶ The Master Equation
- ▶ The LUX PDF set
- ▶ Structure functions data
- ▶ Elastic data
- ▶ Uncertainties
- ▶ Some applications
- ▶ LUX and Hoppet resources
- ▶ Conclusions

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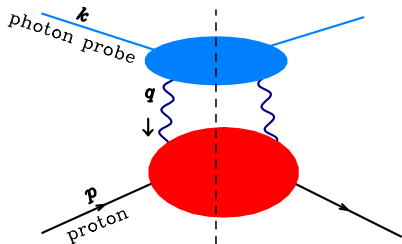
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The Master Equation



$$\begin{aligned}\sigma &= \int \frac{d^4q}{(2\pi)^4} \frac{e_{\text{phys}}^4(q^2)}{q^4} \\ &\times \langle k | \tilde{J}_p^\mu(-q) J_p^\nu(0) | k \rangle \\ &\times \langle p | \tilde{J}_\mu(q) J_\nu(0) | p \rangle\end{aligned}$$

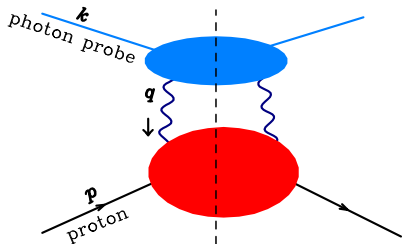
Kinematics constraints:

$$Q^2 = -q^2 > 0,$$

$$0 < x_{\text{bj}} = Q^2 / (2p \cdot q) \leq 1.$$

- ▶ Same kinematic restrictions as in DIS.
- ▶ $\frac{1}{4\pi} \langle p | \tilde{J}_\mu(q) J_\nu(0) | p \rangle = -g_{\mu\nu} F_1(Q^2, x_{\text{bj}}) + \frac{p^\mu p^\nu}{p \cdot q} F_2(Q^2, x_{\text{bj}}) + \dots$
(Notice: full F_1 and F_2 , not only inelastic)
- ▶ Photon induced process can be given in terms of F_1, F_2
- ▶ Hence: the photon PDF must be calculable in terms of F_1, F_2 .

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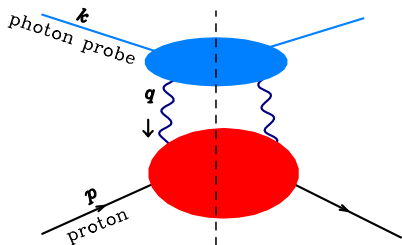
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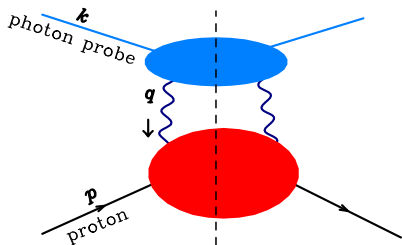
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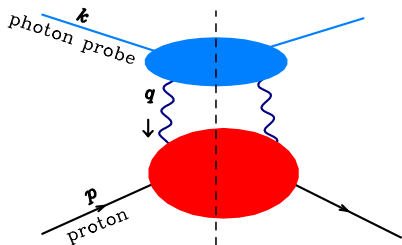
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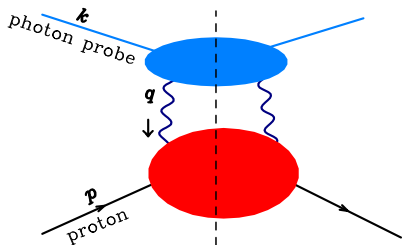
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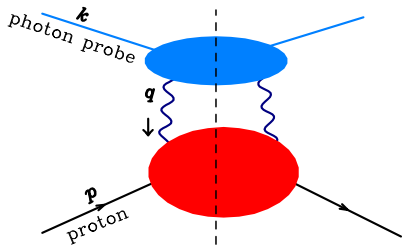
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- ▶ Take a BSM interaction of the form $\frac{e}{\Lambda} \bar{l}[\gamma^\mu, \gamma^\nu] L F_{\mu\nu} + \text{cc}$, l massless, L massive with mass M , both neutral.
- ▶ Compute the cross section with the Master Formula
- ▶ Compute the cross section with the Parton Model formula
- ▶ Extract f_γ by identifying the two cross sections.

We obtain in the $\overline{\text{MS}}$ scheme at NLO:

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- ▶ $f_\gamma \approx \alpha \log \frac{\mu^2}{m_p^2} \approx \alpha/\alpha_s$ relative to $f_{u/d}$ ($\alpha_s(\mu^2) \approx 1/\log \frac{\mu^2}{\Lambda^2}$).
- ▶ $Q^2 \approx m_p^2$ region **formally of order α** , i.e. **NLO** (as $\overline{\text{MS}}$ term).
- ▶ Straightforward to improve at NNLO in α_s (Master Equation is exact, compute the parton model process at NNLO)
- ▶ Also accurate at $(\alpha/\alpha_s)^2$, provided that $\alpha(Q^2)$ and F_2 include leading log electromagnetic evolution.
- ▶ Valid at all μ 's: **MUST** match evolution accuracy with one extra α_s . **Agrees with De Florian, Sborlini, Rodrigo** $\alpha\alpha_s$ splitting functions, arXiv:1512.00612.

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Use:

Ideal use:

- ▶ Get $F_{2/L}$ at low Q^2 from available data.
- ▶ PDF global fit, including EM evolution, with the photon density constrained by the previous equation, $F_{2/L}$ taken from data at low Q^2 and computed from the PDF's at high Q^2

Much can be done without performing a dedicated global fit.

However, if we aim at NLO accuracy:

- ▶ Low Q^2 region cannot be neglected.
- ▶ $(\alpha/\alpha_s)^2$ terms arising from the evolution of QED coupling **cannot be neglected** ($\alpha(m_\mu^2)/\alpha(M_Z^2) \approx 0.94$)
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Much can be done without performing a dedicated global fit.

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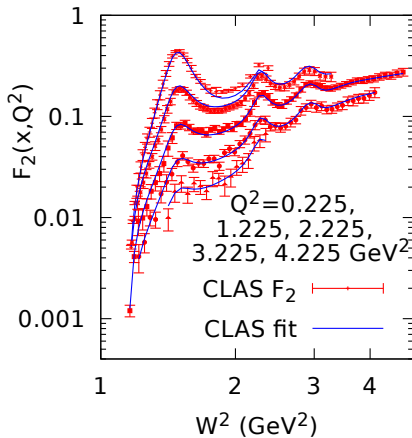
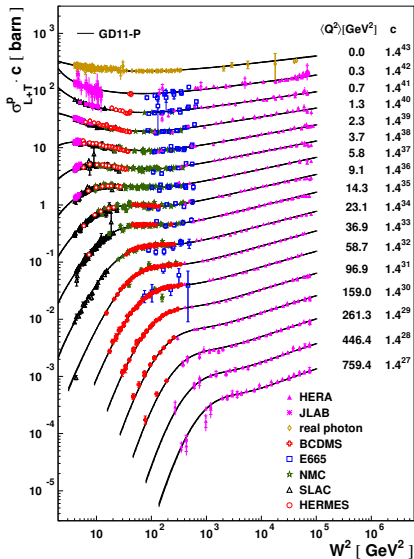
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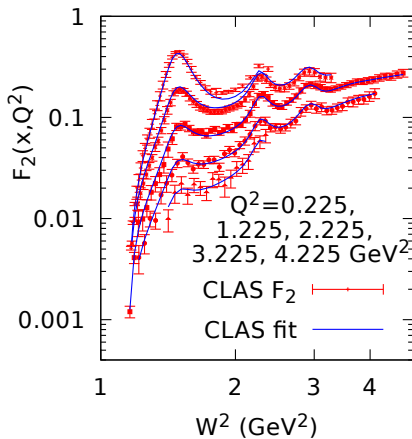
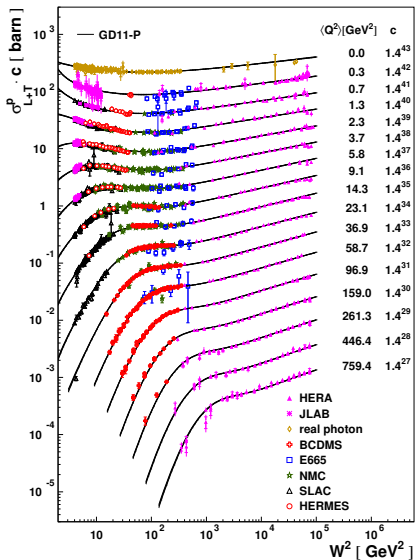
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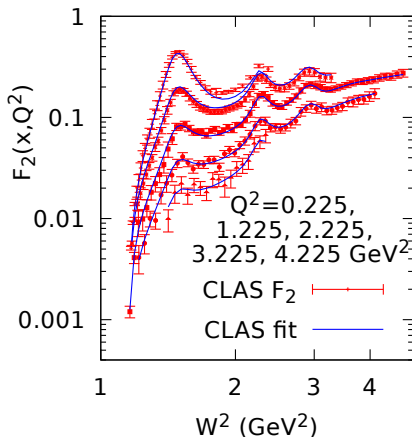
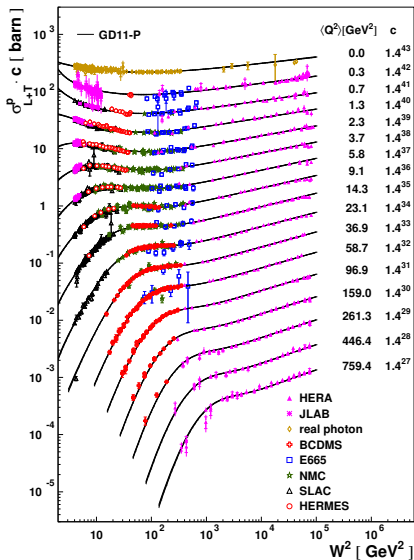
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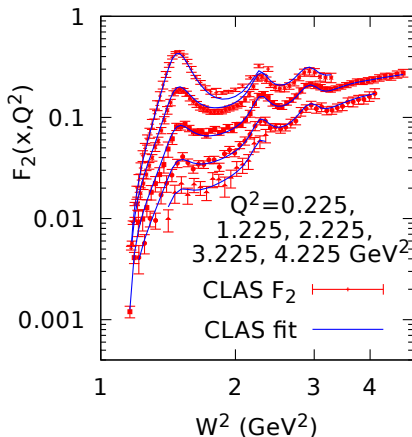
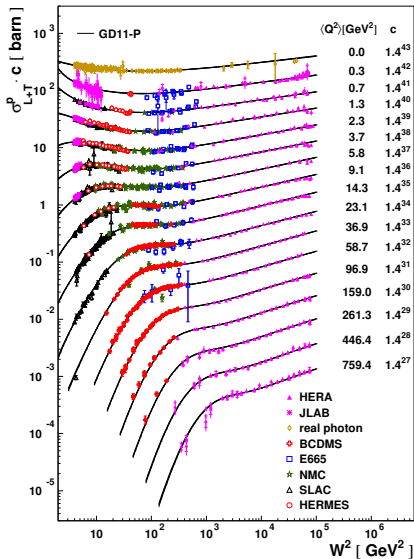
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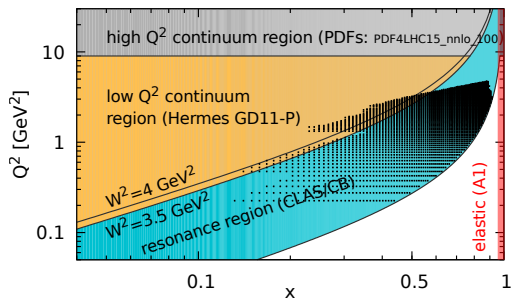
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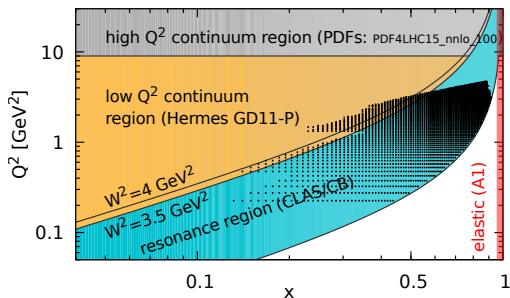
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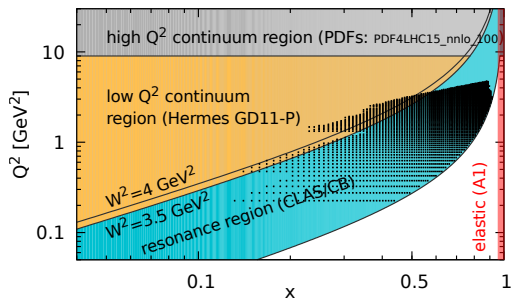
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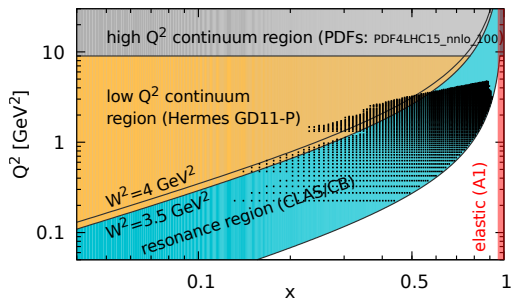
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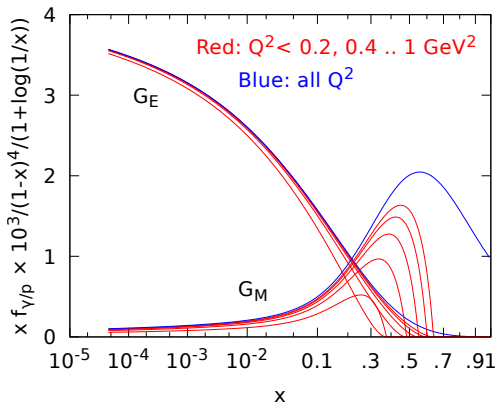
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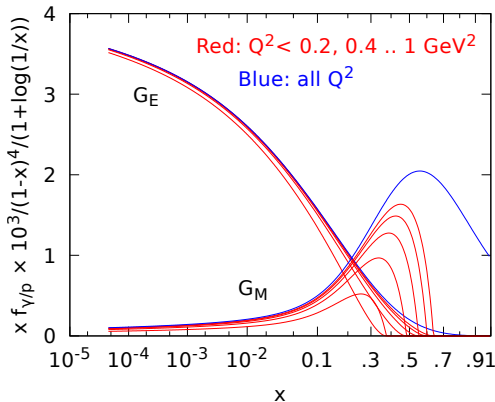


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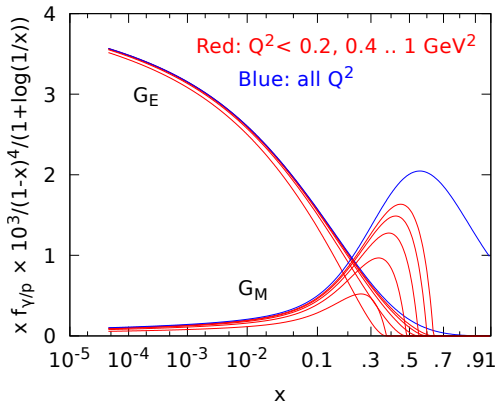


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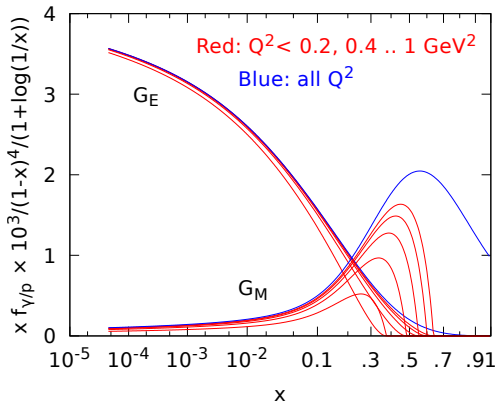


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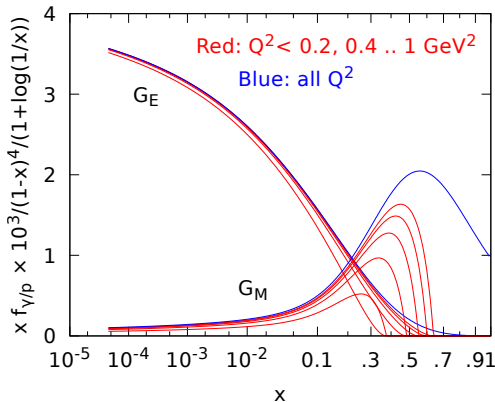


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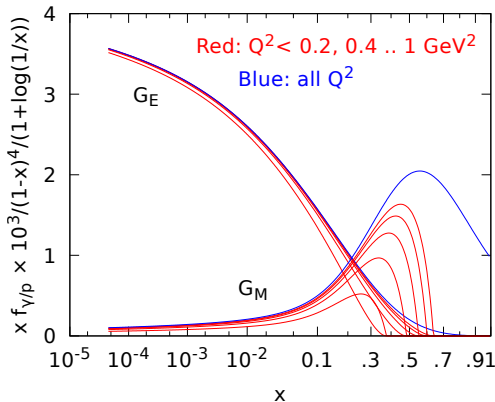


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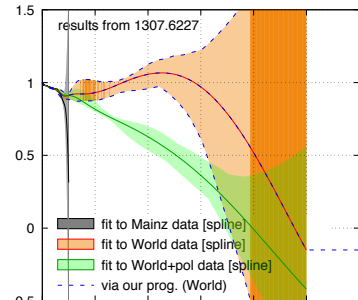
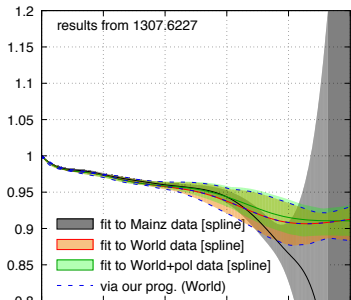
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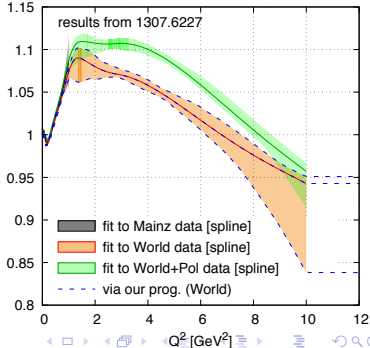
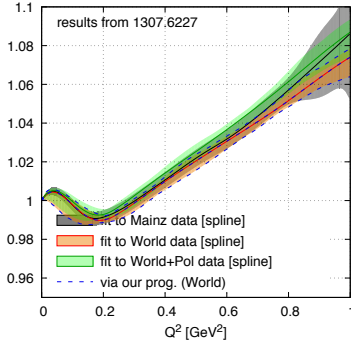


Elastic Data, A1 experiment and World data

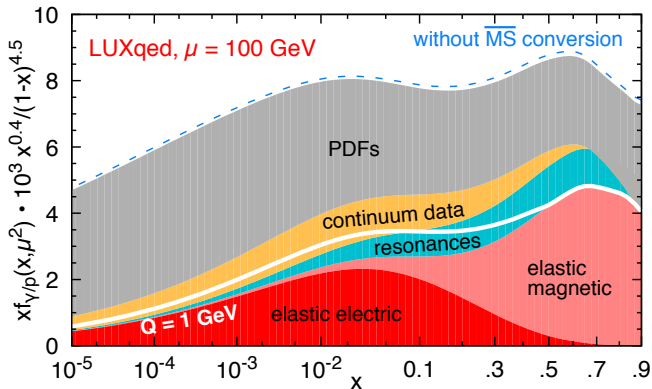
$$G_E/G_E^{\text{dipole}}$$



$$G_M/G_M^{\text{dipole}}$$

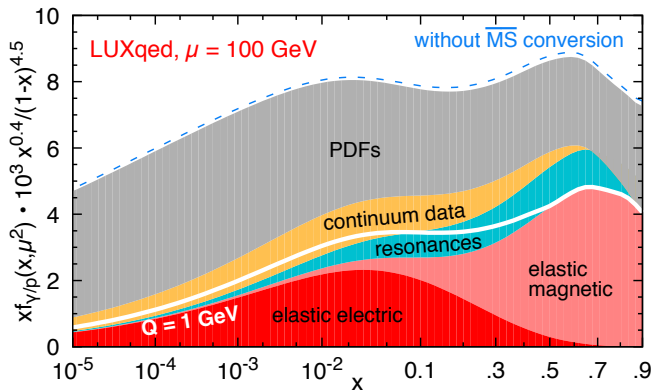


Contributions to f_γ :



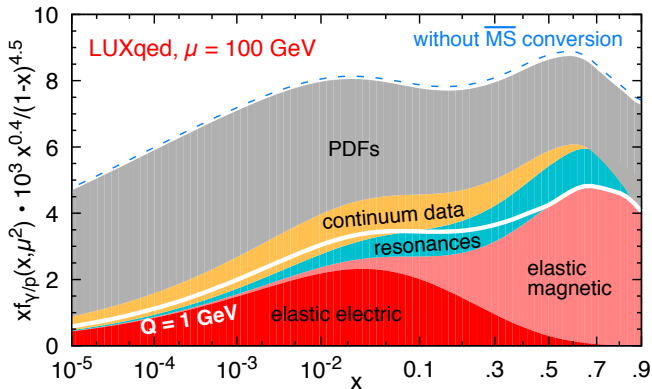
- ▶ $Q^2 > 9 \text{ GeV}^2$, computed from standard PDF sets
- ▶ Important elastic component. Magnetic prevails for $x > 0.2$.
- ▶ Continuum and resonance contributions not negligible
- ▶ Very important contribution from $Q^2 < 1 \text{ GeV}^2$.

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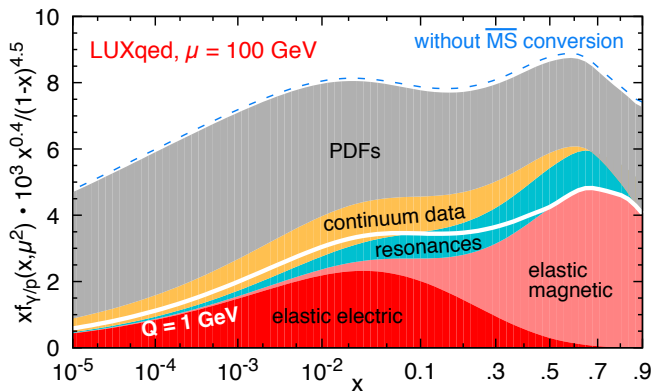
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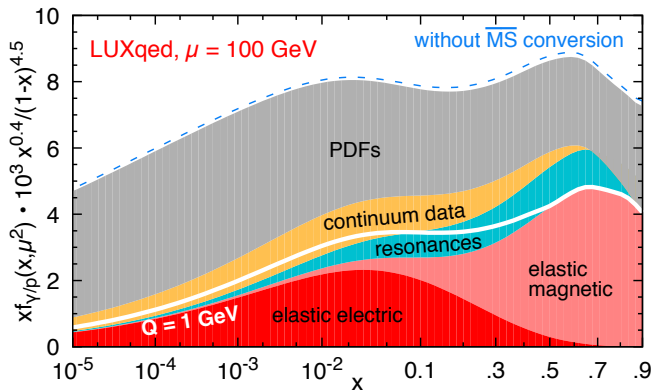
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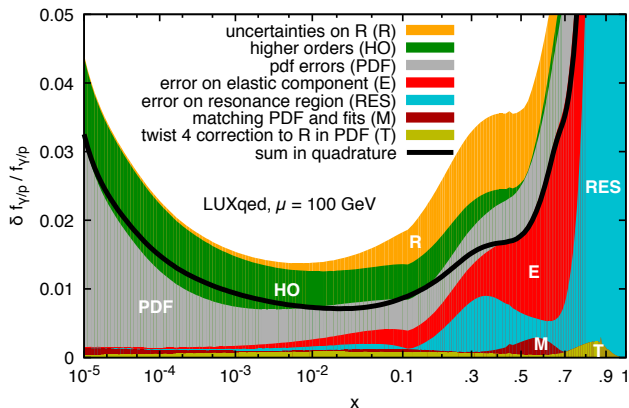
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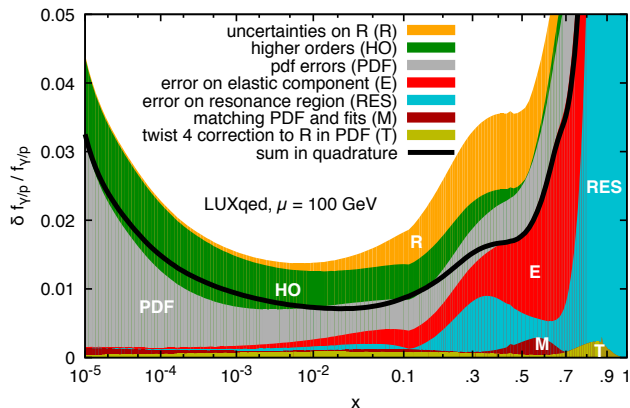
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Uncertainties



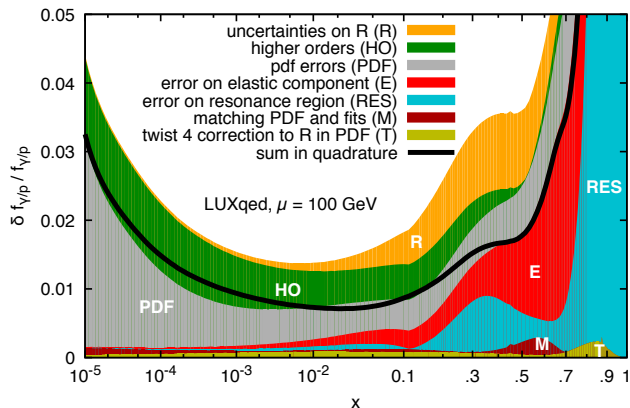
- ▶ At small x , higher order effects and PDF's dominate the error.
- ▶ At large x , elastic and resonant region dominant.
- ▶ Total uncertainty at the percent level.
Further improvements possible!

Uncertainties



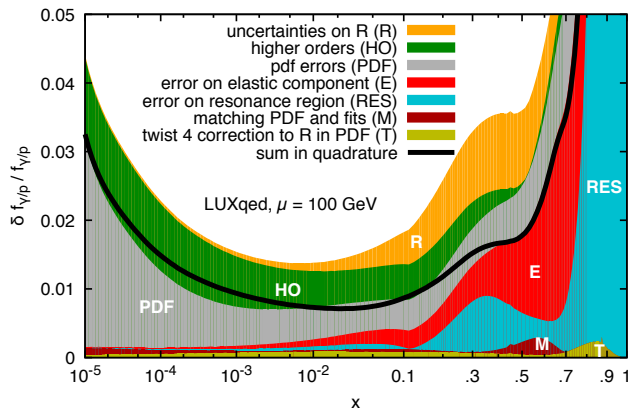
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Added members with variations in photon PDF calculation:

- ▶ 0-100: original PDF members (PDF4LHC15_nnlo_100)
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- ▶ 105: Use lower edge of elastic fit error band.
- ▶ 106: Start using PDF's from $Q^2 = 5$ rather than 9 GeV^2 .
- ▶ 107: Upper limit of integration in f_γ formula changed to μ^2 instead of $\mu^2/(1-z)$, with suitable correction of \overline{MS} term.

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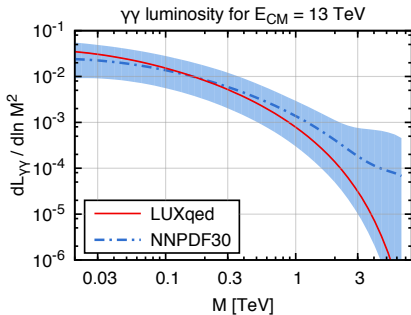
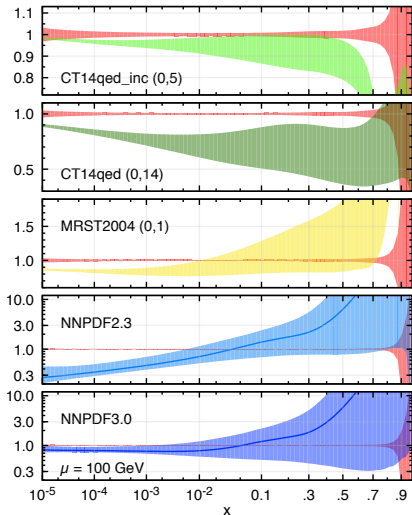
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Since it **only relies upon knowledge of the quark distributions**, the LUX method achieves **by far better precision** than other methods.

Approaches that use some lepton scattering information (in particular CT14qed_inc) do achieve better precision (note different y axis in panel).

APPLICATION TO HIGGS PHYSICS

$pp \rightarrow H W^+ (\rightarrow l^+ \nu) + X$ at 13 TeV

non-photon induced contributions

91.2 ± 1.8 fb

photon-induced contribs (NNPDF23)

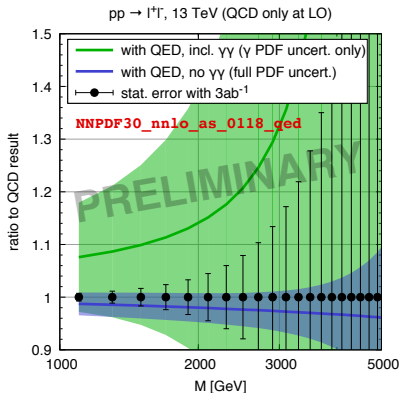
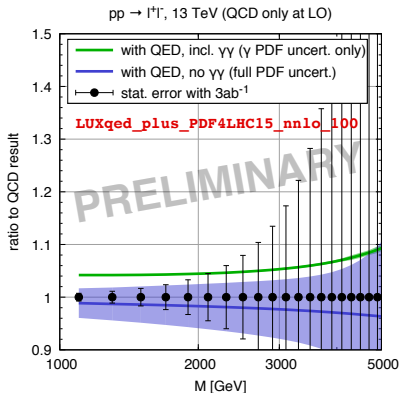
$6.0^{+4.4}_{-2.9}$ fb

photon-induced contribs (LUXqed)

4.4 ± 0.1 fb

non-photon numbers from LHCHSWG (YR4)

di-lepton spectrum



LUXQED photon has few % effect on di-lepton spectrum and negligible uncertainties

RESOURCES

- ▶ LUXqed_plus_PDF4LHC15_nnlo_100 set available from LHAPDF
- ▶ Additional plots and validation info available from <http://cern.ch/luxqed>
- ▶ Preliminary version of HOPPET DGLAP evolution code with QED (order α and $\alpha\alpha_s$) corrections available from hepforge:

```
svn checkout http://hepforge.org/svn/branches/qed hoppet-qed
```

(look at `tests/with-lhapdf/test_qed_evol_lhapdf.f90` for an example; interface may change, documentation missing)

Conclusions

- ▶ Photon PDF can be extracted with great precision from available knowledge of proton structure function and form factors.
- ▶ The needed low Q^2 data is available thanks to extensive low and intermediate energy Nuclear Physics studies.
- ▶ Our study aimed at NLO precision including terms suppressed by one power of α_s or by a power of α/α_s relative to the leading term. This leads to precisions at the percent level.
- ▶ The study of structure functions and form factors at low energy is still ongoing in the Nuclear Physics Community (further progress will come).
- ▶ It is possible to go to higher orders.

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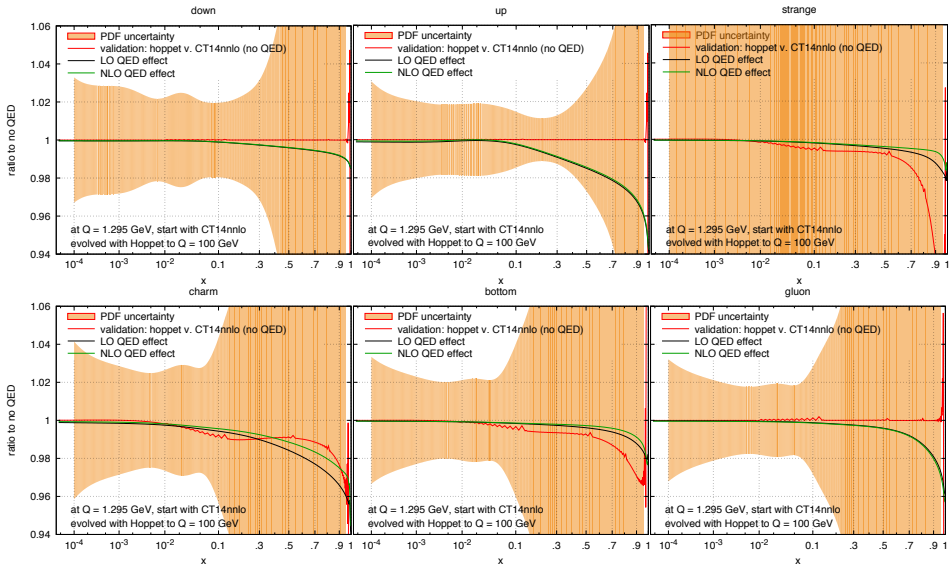
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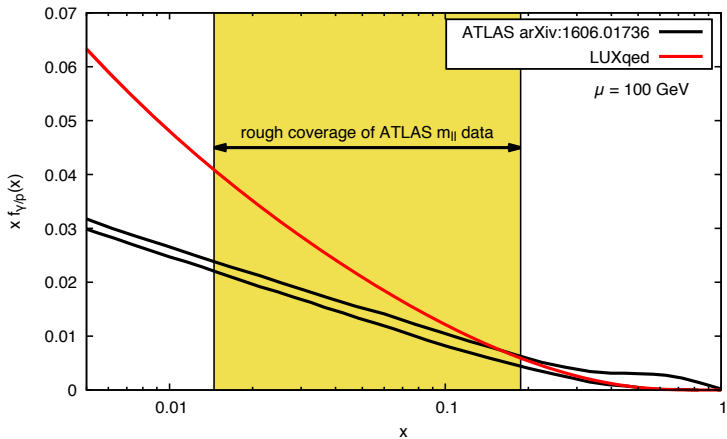
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EXTRA SLIDES

Impact of QED evolution



ratio of ATLAS photon (1606.01736) to LUXqed



ATLAS result based on reweighting of NNPDF23 with high-mass ($M_{ll} > 116$ GeV) data