
Hadronic Decay studies of τ lepton at B-factories

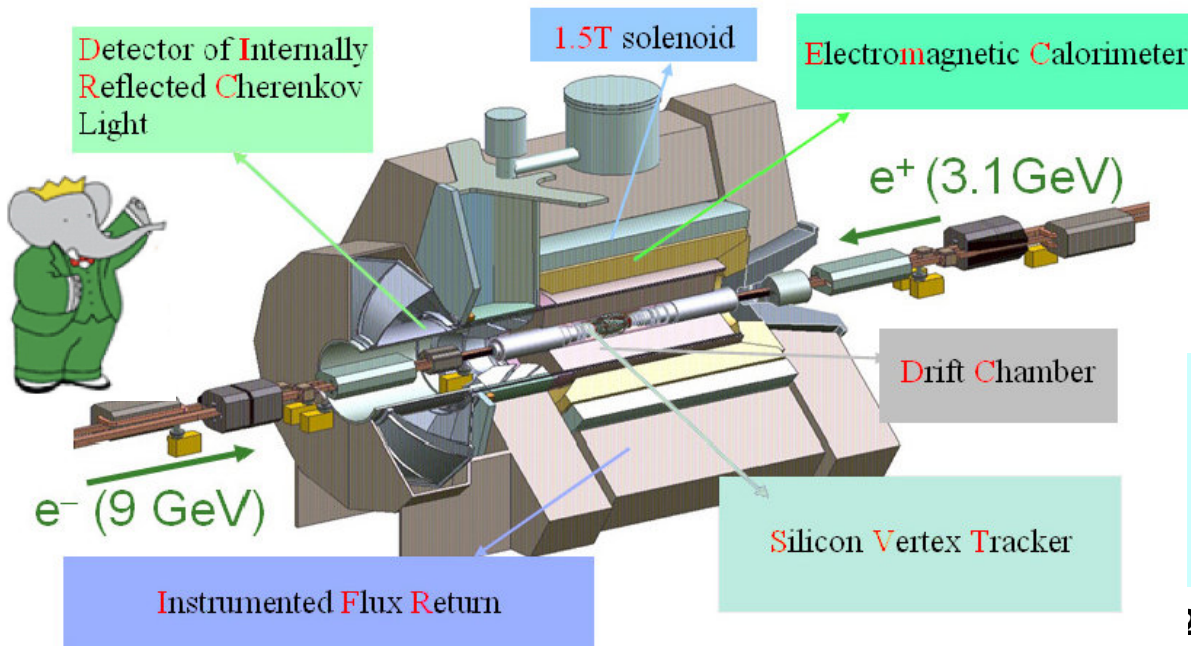
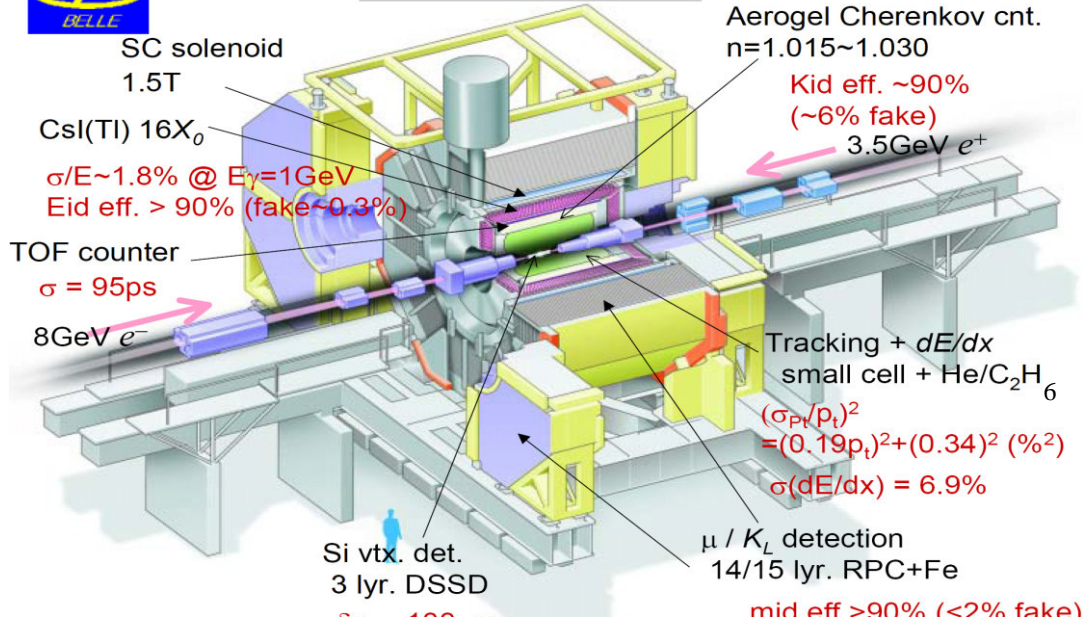
MyeongJae Lee (Seoul National Univ.)

International workshop on Weak Interactions
and Neutrinos, Sep.15, 2009

Belle & BaBar experiments



Belle Detector

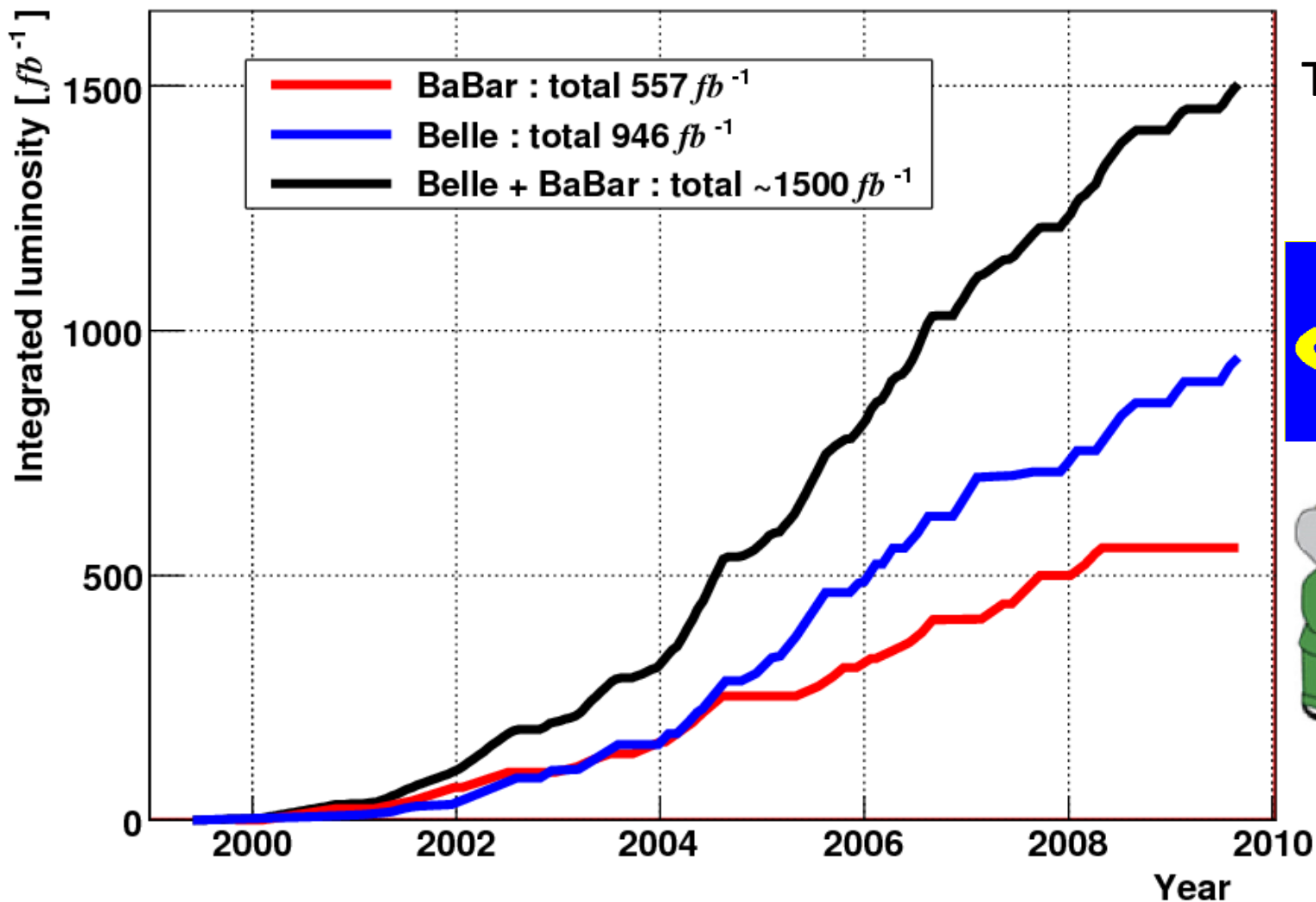


- Good vertexing
- Good PID
- Good photon detection, E_γ resolution
- Energy asymmetry
- High luminosity

Decay mode	$\sigma(\text{nb})$
$\Psi(4S) \rightarrow \text{BB}$	1.15
$e^+e^- \rightarrow \tau\tau$	0.919
$e^+e^- \rightarrow \text{ff}$ (f=udsc)	2.8
$e^+e^- \rightarrow \mu\mu$	1.15
Bhabha (Barrel)	44
$\gamma\gamma$ (Barrel)	2.4
2γ (Barrel, $P_t > 0.1\text{GeV}$)	~ 15

- $\sigma(\text{BB}) \approx \sigma(\tau\tau)$: Not just a B-factory but a τ -factory

10 years of B-factories



Total : $\sim 1500 fb^{-1}$



946 fb^{-1}
(Jul, 2009)



557 fb^{-1}
(Apr, 2008)

$1500fb^{-1} \sim 1.4 \times 10^9 \tau$ pair events!

Decay Mode	Experiment	Reference	Result
$(\tau \rightarrow K^- \nu)/(\tau \rightarrow e^- \bar{\nu} \nu)$	BaBar	arXiv:0811.1429 [hep-ex]	$(0.03882 \pm 0.00032 \pm 0.00056)$ $ g_\tau / g_\mu = (0.9836 \pm 0.0087)$
$\tau \rightarrow K^- \pi^0 \nu$	BaBar	Phys.Rev.D76:051104,2007	$(0.416 \pm 0.003 \pm 0.018) \times 10^{-2}$
$\tau \rightarrow \bar{K}^0 \pi^- \nu$	BaBar	arXiv:0808.1121 [hep-ex]	$(0.840 \pm 0.004 \pm 0.023) \times 10^{-2}$
	Belle	Phys.Lett.B654:65-73,2007	$(0.808 \pm 0.004 \pm 0.026) \times 10^{-2}$
$\tau \rightarrow K^- \pi^+ \pi^0 \nu$ (excl. K_S^0)	BaBar	Phys.Rev.Lett.100:011801,2008	$(0.273 \pm 0.002 \pm 0.009) \times 10^{-2}$
	Belle	EPS2009	$(0.328 \pm 0.002 \pm 0.012) \times 10^{-2}$
$\tau \rightarrow K^- \pi^+ K^0 \nu$	BaBar	Phys.Rev.Lett.100:011801,2008	$(1.346 \pm 0.010 \pm 0.036) \times 10^{-3}$
	Belle	EPS2009	$(1.53 \pm 0.01 \pm 0.05) \times 10^{-3}$
$\tau \rightarrow K^- K^+ K^0 \nu$	BaBar	Phys.Rev.Lett.100:011801,2008	$(1.58 \pm 0.13 \pm 0.12) \times 10^{-5}$
	Belle	EPS2009	$(2.62 \pm 0.23 \pm 0.22) \times 10^{-5}$
$\tau \rightarrow K^- \phi \nu$	BaBar	Phys.Rev.Lett.100:011801,2008	$(3.39 \pm 0.20 \pm 0.28) \times 10^{-5}$
	Belle	Phys.Lett.B643:5-10,2006	$(4.05 \pm 0.25 \pm 0.26) \times 10^{-5}$
$\tau \rightarrow K^* K^- \nu$	Belle	arXiv:0808.1059 [hep-ex]	$(1.56 \pm 0.02 \pm 0.09) \times 10^{-3}$
$\tau \rightarrow K^* K^- \pi^0 \nu$	Belle	arXiv:0808.1059 [hep-ex]	$(2.39 \pm 0.46 \pm 0.26) \times 10^{-5}$
$\tau \rightarrow K^- \eta \nu$	Belle	Phys.Lett.B672:209-218,2009	$(1.58 \pm 0.05 \pm 0.09) \times 10^{-4}$
$\tau \rightarrow K^- \pi^0 \eta \nu$	Belle	Phys.Lett.B672:209-218,2009	$(4.5 \pm 1.1 \pm 0.4) \times 10^{-5}$
$\tau \rightarrow K_S^0 \pi^+ \pi^- \nu$	Belle	Phys.Lett.B672:209-218,2009	$(4.4 \pm 0.7 \pm 0.2) \times 10^{-5}$
$\tau \rightarrow K^* \eta \nu$	Belle	Phys.Lett.B672:209-218,2009	$(1.34 \pm 0.12 \pm 0.09) \times 10^{-4}$

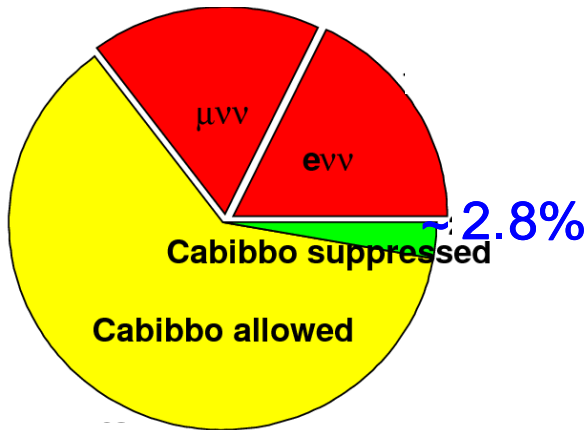
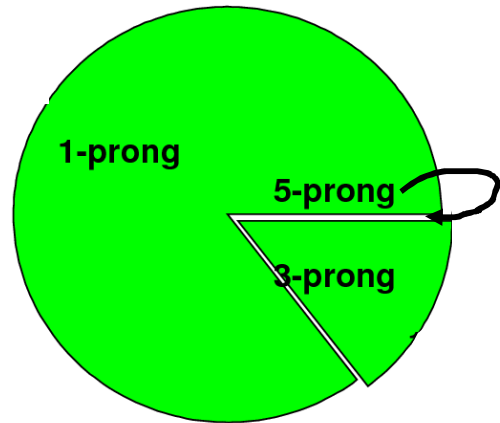
Really many measurements
are done and on-going
in $B^- (\tau^-)$ factory

Decay Mode	Experiment	Reference	Result
$(\tau \rightarrow \pi^- \nu)/(\tau \rightarrow e^- \bar{\nu} \nu)$	BaBar	arXiv:0811.1429 [hep-ex]	$(0.5943 \pm 0.0014 \pm 0.00131)$ $ g_\tau / g_\mu = (0.9859 \pm 0.0057)$
$\tau \rightarrow \pi^- \pi^0 \nu$	Belle	Phys.Rev.D78:072001,2008	$(25.94 \pm 0.01 \pm 0.39) \times 10^{-2}$ $f_{\tau \rightarrow \pi^- \pi^0} = 52.5 \pm 1.5 \text{ (exp)} \pm 2.6 \text{ (BR)} \pm 2.5 \text{ (isospir)}$
$\tau \rightarrow \pi^- \pi^+ \pi^0 \nu$ (excl. K_S^0)	BaBar	Phys.Rev.Lett.100:011801,2008	$(8.83 \pm 0.01 \pm 0.13) \times 10^{-2}$
	Belle	EPS2009	$(8.42 \pm 0.00 \pm 0.24) \times 10^{-2}$
$\tau \rightarrow \pi^- \pi^0 \eta \nu$	Belle	Phys.Lett.B672:209-,2009	$(1.35 \pm 0.03 \pm 0.07) \times 10^{-3}$
$\tau \rightarrow \pi^- \eta \nu$ (Second Class Current)	Belle	EPS2009	$(4.4 \pm 1.6 \pm 0.8) \times 10^{-5}$ $< 7.3 \times 10^{-5} \text{ @ 90\% C.L.}$
$\tau \rightarrow f_1(1285) \pi^- \nu$	BaBar	Phys.Rev.D77:112002,2008	$(3.19 \pm 0.18 \pm 0.16 \pm 0.99) \times 10^{-4}$
$\tau \rightarrow f_1(1285) \pi^- \nu \rightarrow 2\pi^- \pi^+ \eta \nu$	BaBar	Phys.Rev.D77:112002,2008	$(1.11 \pm 0.06 \pm 0.05) \times 10^{-4}$
$\tau \rightarrow 2\pi^- \pi^+ \eta \nu$	BaBar	Phys.Rev.D77:112002,2008	$(1.60 \pm 0.05 \pm 0.11) \times 10^{-4}$
$\tau \rightarrow \pi^- \eta' \nu$ (Second Class Current)	Belle	EPS2009	$(-0.47^{+3.97}_{-3.85} \pm 0.26) \times 10^{-6}$ $< 6.1 \times 10^{-6} \text{ @ 90\% C.L.}$
$\tau \rightarrow \pi^- \eta' \nu$ (Second Class Current)	BaBar	Phys.Rev.D77:112002,2008	$< 7.2 \times 10^{-6} \text{ @ 90\% C.L.}$
$\tau \rightarrow \pi^- \omega \nu$ (Second Class Current)	BaBar	Ph	
$\tau \rightarrow \pi^- \phi \nu$	BaBar	Phys.Rev.Lett.100:011801,2008	$(3.42 \pm 0.55 \pm 0.25) \times 10^{-5}$

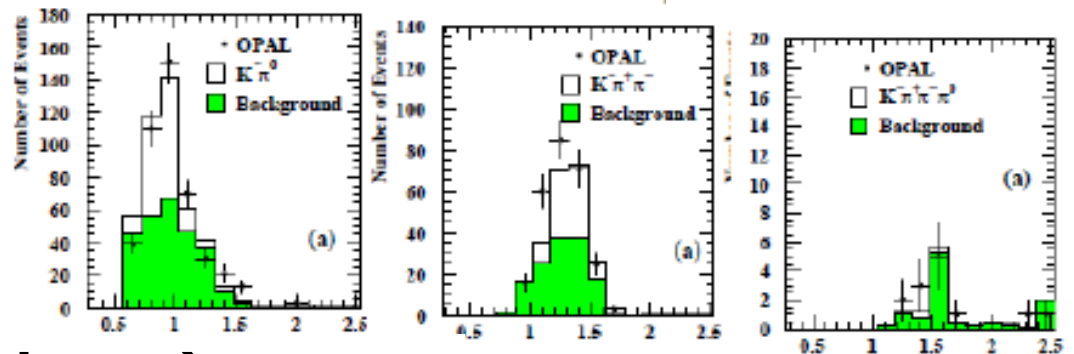
<http://www.slac.stanford.edu/xorg/hfag/tau/index.html>

Hadronic decays of tau lepton

- The only lepton which can decay to hadrons
 - Rather large mass (1.78GeV)
 - Clean initial state - single τ pair decays decide the kinematics
- Test of CVC and evaluation of a_μ from spectral function.
- Measurements of important physics quantities : V_{us} , m_s , α_s
- Look for **leptonic CP violation (NP)**



Have been waiting for enough statistics from B-factories (especially, to measure strangeness decays)



Hadronic τ decay programs

■ Non-strange final state

- $\tau \rightarrow \eta \pi \nu_\tau, \tau \rightarrow \eta' \pi \nu_\tau$: Second Class Current
- $\tau \rightarrow \pi \pi^0 \nu_\tau$: Test of CVC and $(g-2)_\mu$ (PRD78:0701006,2008)
- $\tau \rightarrow \eta \pi \pi^0 \nu_\tau$: Wess-Zumino anomaly

■ Strange final state

* “Blue” will be presented
In this talk

- $\tau \rightarrow K \pi \nu_\tau, \tau \rightarrow K \eta X \nu_\tau$
- 3-prong : $\tau \rightarrow h^\pm h^+ h^- \nu_\tau$ ($h = \pi, K$)
- V_{us} measurement
- V_{us} using $\Gamma(\tau \rightarrow K \nu_\tau) / \Gamma(\tau \rightarrow \pi \nu_\tau)$
- Strange spectral function and V_{us}, m_s measurements

■ Other researches

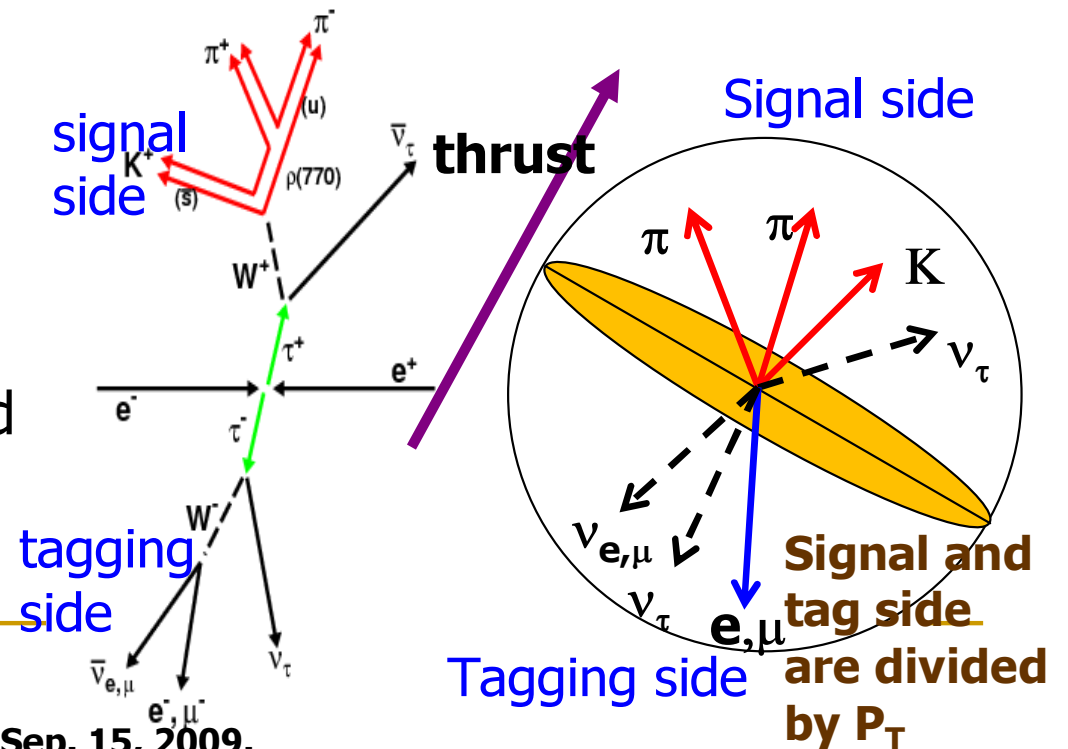
- 5-prongs, 7-prongs....
- τ mass measurements (via $\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu_\tau$)
- Search for CP violation in the charged lepton....

Analysis of hadronic τ decay event

Features of τ pair decays : Low mult., Large P_T , missing E_{tot} and P_{tot}

Main backgrounds	Discrimination
Bhabha, dimuon ($e^+e^- \rightarrow e^+e^-, \mu^+\mu^-$)	Reconstructed total energy, momentum, multiplicity
Continuum ($e^+e^- \rightarrow qq, q=uds$)	Event topology, thrust , invariant mass, multiplicity
Two-photon	Small transverse momentum, M_{miss}, P_{miss} recon.
Beam background	Quality of decay vertex
Other tau decays	Efficient reconstruction of signal mode

- Typically, require pure leptonic decay in the tagging side
- In many cases, π/K separation is very important
- Estimate the tau decay background from the MC, or the sideband of resonances



$\tau \rightarrow \eta \pi \nu_\tau$: Second Class Current

- 1st Class Current : $PG(-1)^J = +1$
 - $J^{PG} = 0^-(\pi), 1^-(\rho), 1^-(a_1), \dots$
- 2nd Class Current : $PG(-1)^J = -1$
 - $J^{PG} = 0^{++}(a_0), 1^{++}(b_1), \dots$
 - S.Weinberg (PR112:1375 (1958))
 - Should be suppressed by isospin symmetry in SM $\propto (m_d - m_u)$
 - $J^{PG}(\tau \rightarrow \eta \pi \nu_\tau) = 0^{+-}, B(\tau \rightarrow \eta \pi \nu_\tau) = 10^{-6} \sim 10^{-5}$
 - Main background : All τ decays containing η

Experiments	$B(\tau \rightarrow \eta \pi \nu_\tau), 10^{-4}$ @95% C.L.
MARK3	<250 (@90%)
CLEO, 1987	<180
ARGUS, 1988	<90
CLEO, 1992	<3.4
ALEPH, 1997	<6.2
CLEO, 1996	<1.4 (PDG avg.)

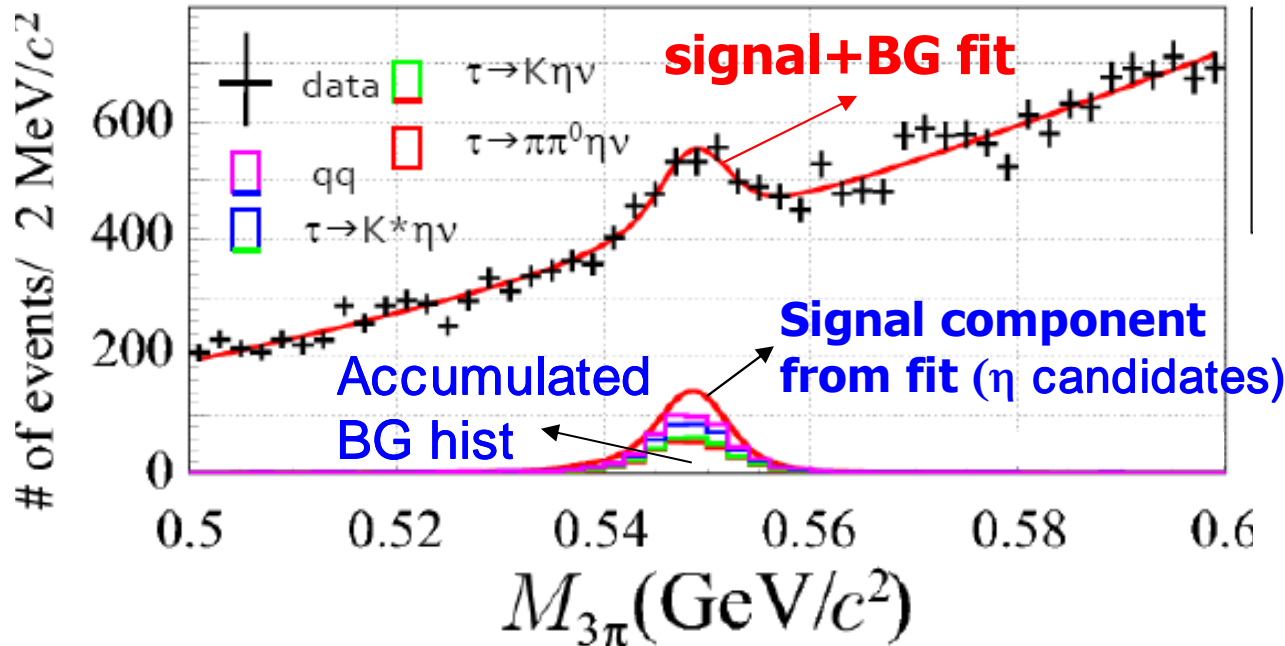
All measurements
by Belle Collab.
(PLB672,209(2009))



Mode	BF ($\times 10^{-4}$)	Mode	BF ($\times 10^{-5}$, @90%)
$\pi^- \pi^0 \eta \nu$	$13.5 \pm 0.3 \pm 0.7$	$K^- K^0 \eta \nu$	<0.45
$K^- \eta \nu$	$1.58 \pm 0.05 \pm 0.09$	$\pi^- K_s^0 \eta \nu$	<2.5
$K^- \pi^0 \eta \nu$	$0.46 \pm 0.11 \pm 0.04$	$K^- \eta \eta \nu$	<0.3
$\pi^- K_s^0 \eta \nu$	$0.44 \pm 0.07 \pm 0.03$	$\pi^- \eta \eta \nu$	<0.74

Analysis of $\tau \rightarrow \eta \pi \nu_\tau$ ($\eta \rightarrow 3\pi$)

- With standard event selection + $M(4\pi) < 1.2 \text{ GeV}$...

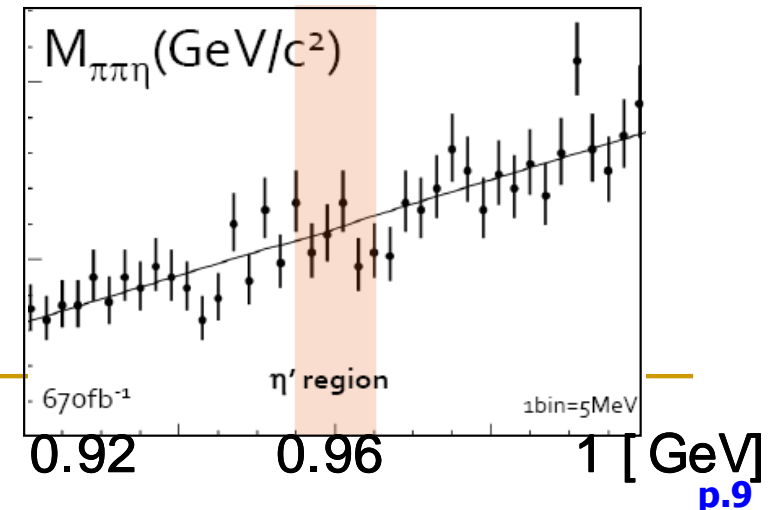


Belle Preliminary (EPS09)

$N_{\tau\tau}$	$\sim 620\text{M}$ (670 fb^{-1})
N^{fit}	749 ± 62
N^{sig}	191 ± 69
BF	$(4.4 \pm 1.6 \pm 0.8) \times 10^{-5}$ (2.4σ) or 7.3×10^{-5} @90% C.L.

- Other SCC study : $\tau \rightarrow \eta'(958) \pi \nu_\tau$
 - BF $< 6.1 \times 10^{-6}$ @90% C.L. (Belle)
 - BF $< 7.2 \times 10^{-6}$ @90% C.L. (BaBar)
- (Phys.Rev.D77:112002,2008)

Belle Preliminary (EPS09)



Strange final state decay of τ

- B-factory detectors have a good π/K separation
 - Useful to discriminate Cabibbo-suppressed decay
- Rather small BR for strangeness decays
 - Need large statistics for studying suppressed decays
- For V_{us} measurement
 - Inclusive measurements of $\tau \rightarrow s$ decays
 - Strange spectral function and simultaneous fit on V_{us} and m_s : need enough statistics and measurements
 - τ decays are the most clean environment to measure V_{us} .
 - Uncertainties are dominated by experimental error.

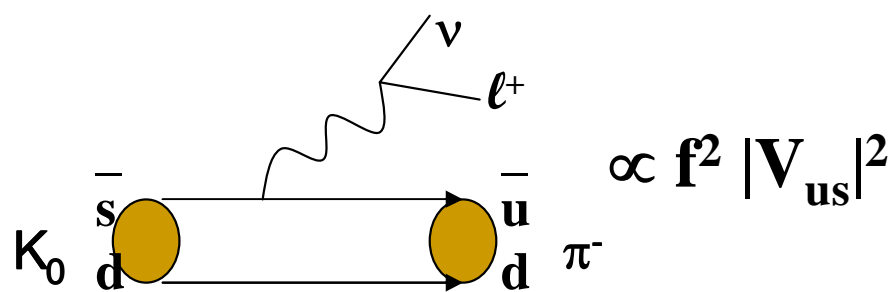
V_{us} measurement

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \sim \begin{pmatrix} \text{red} & \text{red} & \text{grey} \\ \text{red} & \text{red} & \text{red} \\ \text{grey} & \text{red} & \text{red} \end{pmatrix}$$

- Estimate from the unitarity condition :

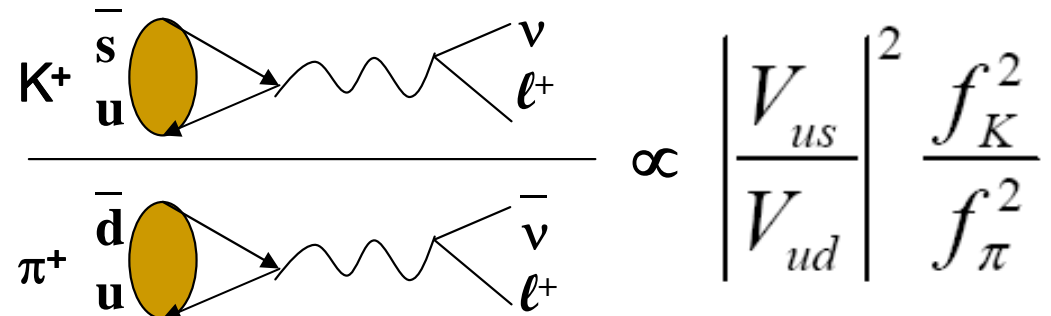
$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1 \Rightarrow |V_{us}| = 0.2255 \pm 0.0010$$

- From $K_{\ell 3}$ decays



$$|V_{us}| = 0.2247 \pm 0.0012$$

- or From $K_{\ell 2}$ decays



$$|V_{us}| = 0.2261 \pm 0.0015$$

Good agreements with Unitarity !

V_{us} measurement from τ decay

$$R_\tau = \frac{\Gamma(\tau^- \rightarrow (\text{hadrons})^- \nu_\tau)}{\Gamma(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)} = R_{\tau, \text{non-strange}} + R_{\tau, \text{strange}}$$

Measured from the branching fraction and invariant mass spectra

$$|V_{us}|^2 = \frac{R_{\tau, \text{strange}}^W}{R_{\tau, \text{non-strange}}^W / |V_{ud}|^2 - \delta R_\tau^W}$$

- $|V_{ud}|$ is well measured from super allowed $0^+ \rightarrow 0^+$ beta decay
- δR_τ^W is determined from Finite Energy Sum Rule, and is relatively small ($\delta R_\tau^W \sim 0.06 \times R_{\tau, \text{non-strange}}^W / |V_{ud}|^2 \pm 10\%$)
- $R_\tau = \frac{1 - \text{BF}(\tau \rightarrow e \nu \nu_\tau) - \text{BF}(\tau \rightarrow \mu \nu \nu_\tau)}{\text{BF}(\tau \rightarrow e \nu \nu_\tau)} = R_{\tau, \text{non-strange}} + R_{\tau, \text{strange}}$

: inclusive measurement of strange decays is required.

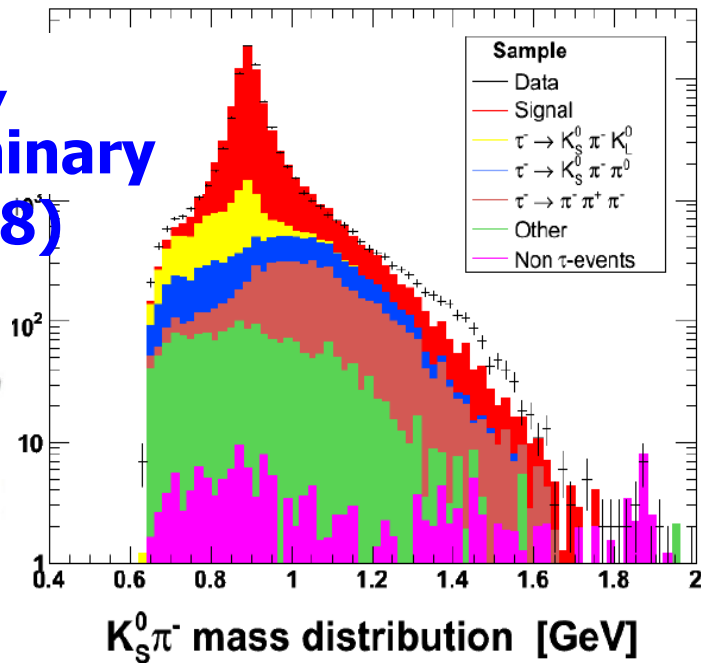
Listing the strange decays : $\tau^- \rightarrow K_S \pi^- \nu_\tau$

$$M(K^{*0}(892)) = 895.47 \pm 0.20(\text{stat}) \pm 0.44(\text{sys}) \pm 0.59(\text{mod}) \text{ MeV}/c^2$$

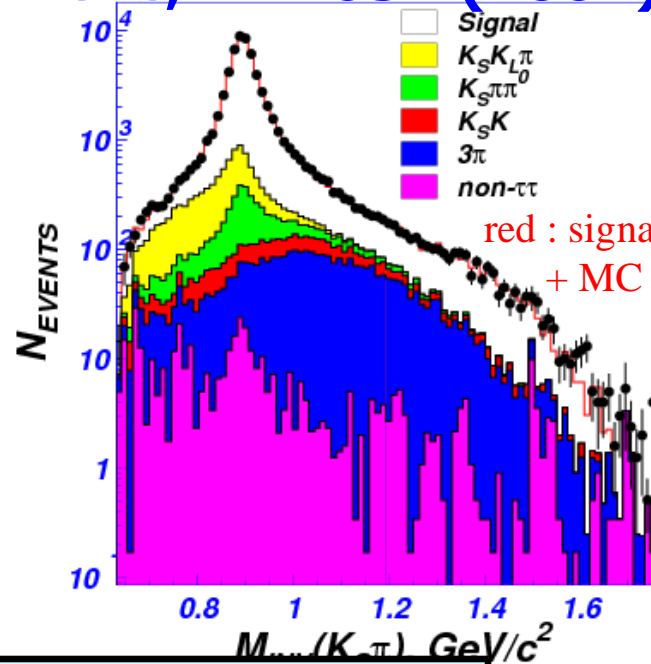
$$\Gamma(K^{*0}(892)) = 42.2 \pm 0.6(\text{stat}) \pm 1.0(\text{sys}) \pm 0.7(\text{mod}) \text{ MeV}$$

$$(\text{PDG07} : 896.00 \pm 0.25, 50.3 \pm 0.6)$$

BaBar,
Preliminary
(TAU08)

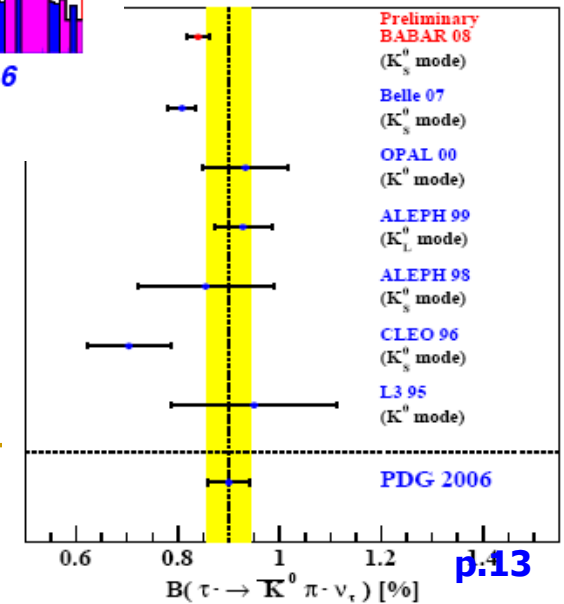


Belle, PRD654 (2007)

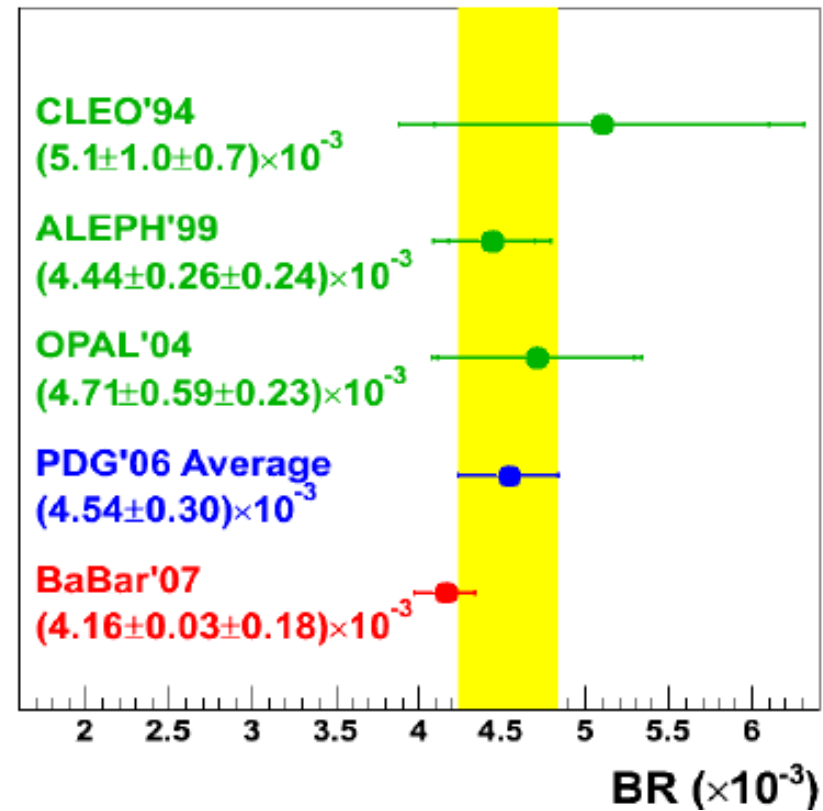
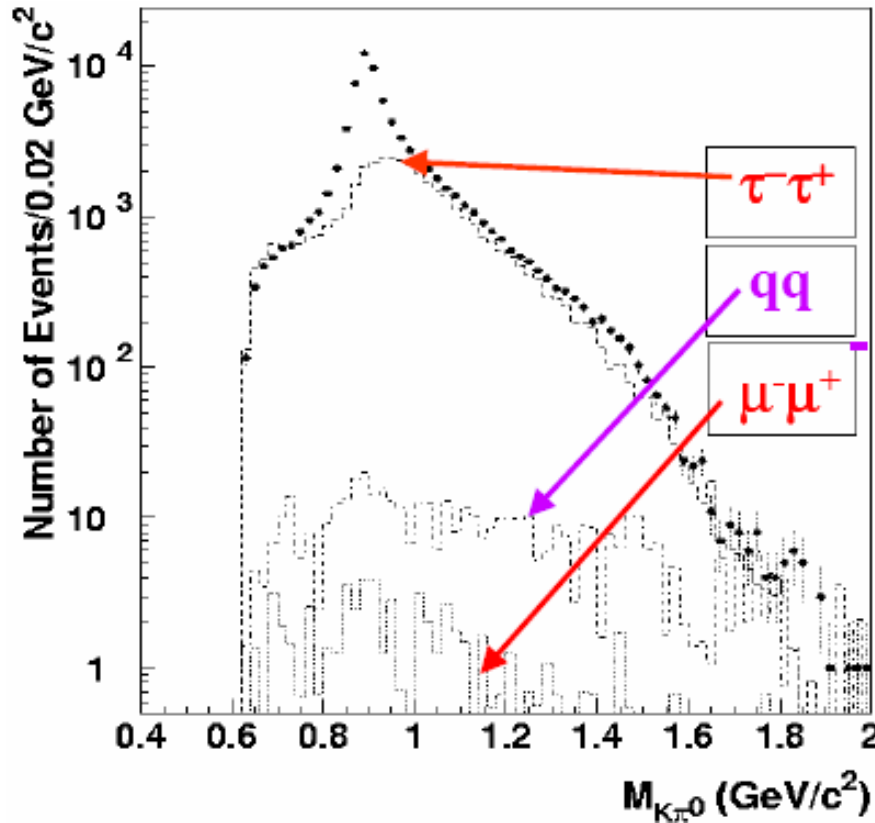


red : signal fit
+ MC background

	$N_{\tau\tau}$	ϵ	N_{signal}	BF (%), $B(\tau^- \rightarrow K^0 \pi^- \nu_\tau)$ $= 2 \times B(\tau^- \rightarrow K_S \pi^- \nu_\tau)$
Belle	310M	$\sim 5.8\%$	$\sim 53\text{k}$	$0.808 \pm 0.004 \pm 0.026$
BaBar	350M	$\sim 1.1\%$	$\sim 33\text{k}$	$0.840 \pm 0.004 \pm 0.023$
PDG07				0.90 ± 0.04



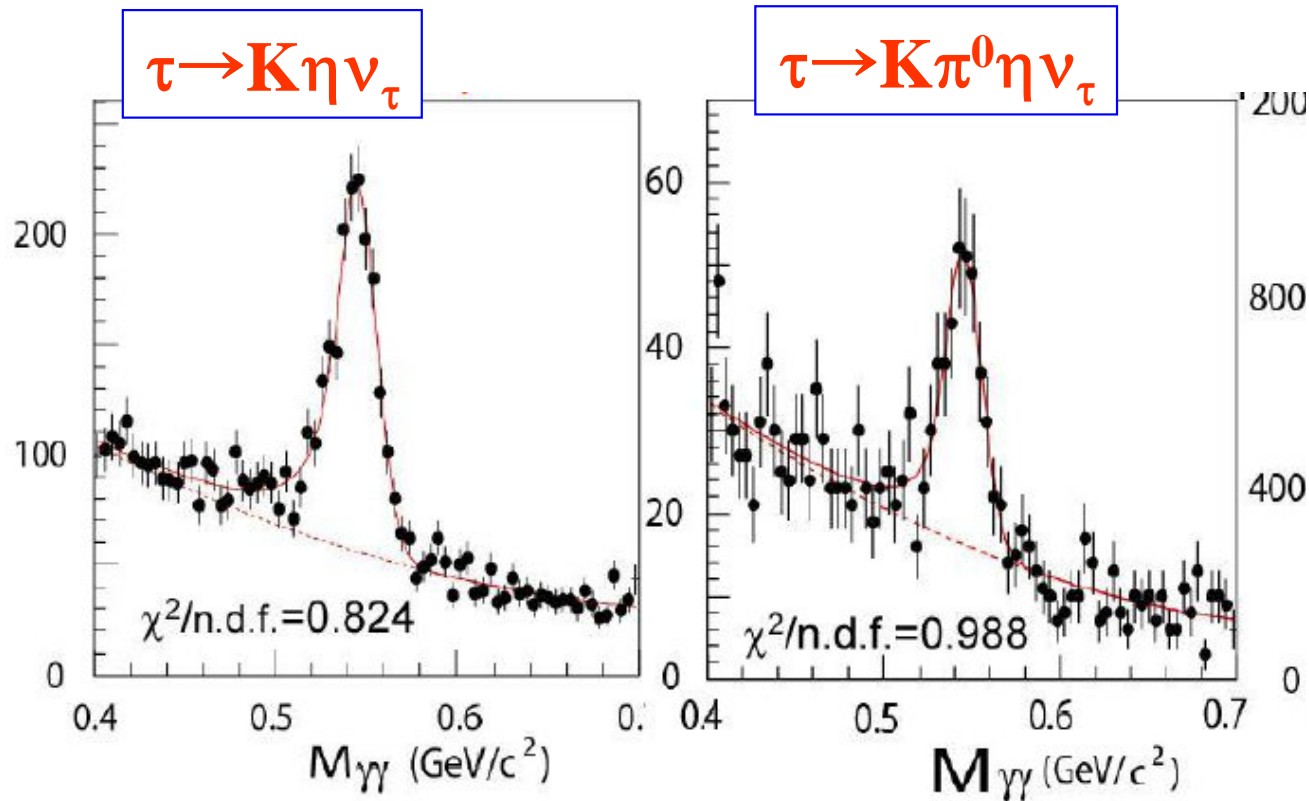
$$\tau^- \rightarrow K^- \pi^0 \nu_\tau$$



$N_{\tau\tau}$	211M (230 fb ⁻¹)
ϵ	~2.3%
$N^{\text{signal}}/N^{\text{BG}}$	78k / 38k
BF(%)	$0.416 \pm 0.003 \pm 0.018$
PRD 76:051104, 2007 (BaBar)	

Large BG from $\tau \rightarrow \pi\pi^0\nu_\tau$ (BF~25%)
cross-feed,
due to **particle mis-identification**

τ decays with η : $\tau \rightarrow K\eta\nu_\tau$, $\tau \rightarrow K\pi^0\eta\nu_\tau$



Belle,
PLB 672:209 (2009)

	$\tau \rightarrow K\eta\nu_\tau$ ($\eta \rightarrow \gamma\gamma, \eta \rightarrow 3\pi$)	$\tau \rightarrow K\pi^0\eta\nu_\tau$ ($\eta \rightarrow \gamma\gamma, \eta \rightarrow 3\pi$)
$N_{\tau\tau}$	450M (490 fb ⁻¹)	
BF	$(1.58 \pm 0.05 \pm 0.09) \times 10^{-4}$	$(0.46 \pm 0.11 \pm 0.04) \times 10^{-4}$
BF (CLEO, 1996)	$(2.6 \pm 0.5 \pm 0.5) \times 10^{-4}$	$(1.77 \pm 0.56 \pm 0.71) \times 10^{-4}$

$\tau^- \rightarrow h^- h^+ h^- \nu_\tau$ ($h = \pi, K$)



- Four decay modes are **correlated** due to the particle mis-identification, that one decay mode contributes to the BG of the other decay mode
- Large differences btw BFs make this cross-feed effect significant.

$$N_i^{true} = \varepsilon^{-1}_{ij} (N_j^{rec} - N_j^{OtherBG})$$

N_i^{true} : Number of true signal events for i-th mode

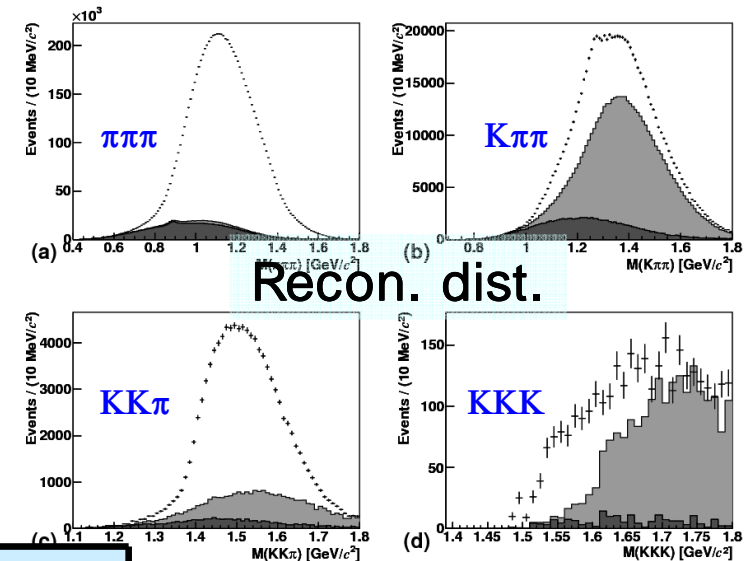
N_i^{rec} : Number of reconstructed events for i-th mode

$N_i^{OtherBG}$: Number of estimated backgrounds for i-th mode from non-3prong decay

ε : efficiency migration matrix

Efficiency migration matrix ε (%)

rec \ true	$\tau \rightarrow \pi\pi\nu$	$\tau \rightarrow K\pi\nu$	$\tau \rightarrow KK\pi\nu$	$\tau \rightarrow KKK\nu$
$\tau \rightarrow \pi\pi\nu$	23.0	7.6	2.3	0.73
$\tau \rightarrow K\pi\nu$	1.3	17.2	4.8	2.3
$\tau \rightarrow KK\pi\nu$	4.1×10^{-2}	0.47	12.9	6.0
$\tau \rightarrow KKK\nu$	5.0×10^{-4}	1.4×10^{-2}	0.28	9.4



- Efficiency : 10 ~ 20%
- Fake rate from $\pi\pi\pi$ to $K\pi\pi$ is sufficiently small

Branching fraction of $\tau^- \rightarrow h^- h^+ h^- \nu_\tau$



	Branching ratio	N^{rec}	$N^{\text{other}} / N^{\text{rec}}$
$\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu_\tau$	$(8.42 \pm 0.01(\text{st.})^{+0.26}_{-0.25}(\text{sy.})) \times 10^{-2}$	8.86×10^6	10.6%
$\tau^- \rightarrow K^- \pi^+ \pi^- \nu_\tau$	$(3.28 \pm 0.01(\text{st.})^{+0.16}_{-0.16}(\text{sy.})) \times 10^{-3}$	7.94×10^5	12.2%
$\tau^- \rightarrow K^- K^+ \pi^- \nu_\tau$	$(1.53 \pm 0.01(\text{st.})^{+0.05}_{-0.05}(\text{sy.})) \times 10^{-3}$	1.08×10^5	6.70%
$\tau^- \rightarrow K^- K^+ K^- \nu_\tau$	$(2.62 \pm 0.15(\text{st.})^{+0.17}_{-0.17}(\text{sy.})) \times 10^{-5}$	3.16×10^3	5.45%

$N_{\tau\tau} = 613\text{M}$, Belle, Preliminary (TAU08 and EPS09)

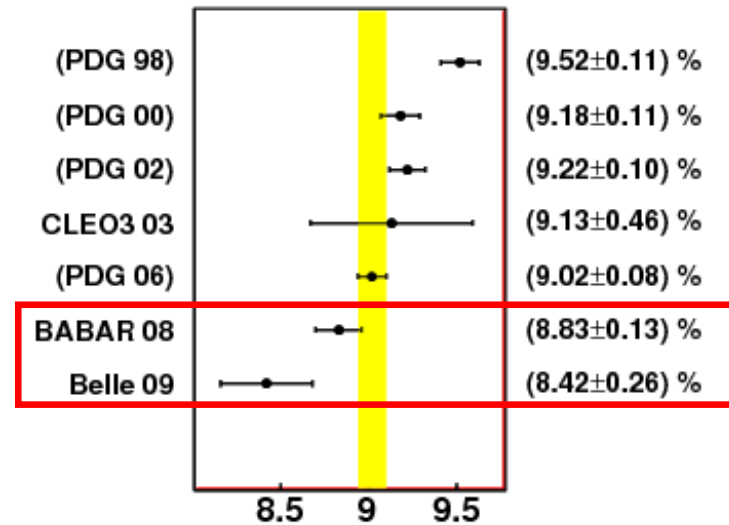
	Branching ratio	N^{rec}
$\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu_\tau$	$(8.83 \pm 0.01 \pm 0.13) \times 10^{-2}$	1.60×10^6
$\tau^- \rightarrow K^- \pi^+ \pi^- \nu_\tau$	$(2.73 \pm 0.02 \pm 0.09) \times 10^{-3}$	6.96×10^4
$\tau^- \rightarrow K^- K^+ \pi^- \nu_\tau$	$(1.35 \pm 0.01 \pm 0.04) \times 10^{-3}$	1.82×10^4
$\tau^- \rightarrow K^- K^+ K^- \nu_\tau$	$(1.58 \pm 0.13 \pm 0.12) \times 10^{-5}$	2.75×10^2

$N_{\tau\tau} = 314\text{M}$, BaBar, PRL100:011801, 2008

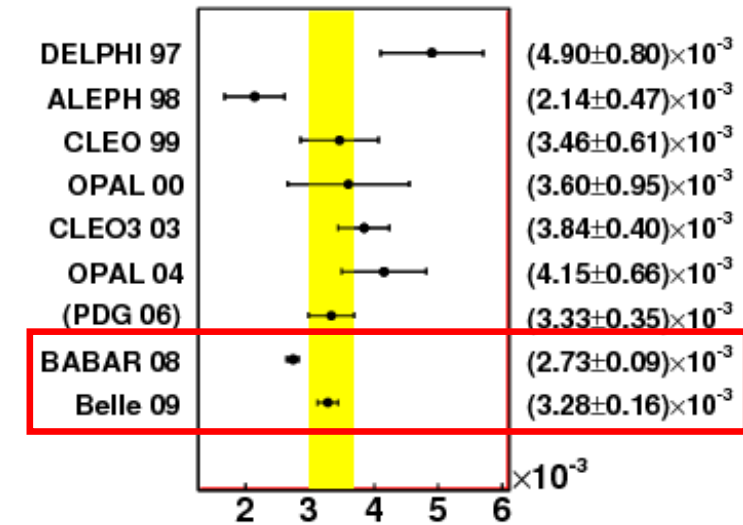


Branching fraction of $\tau^- \rightarrow h^- h^+ h^- \nu_\tau$

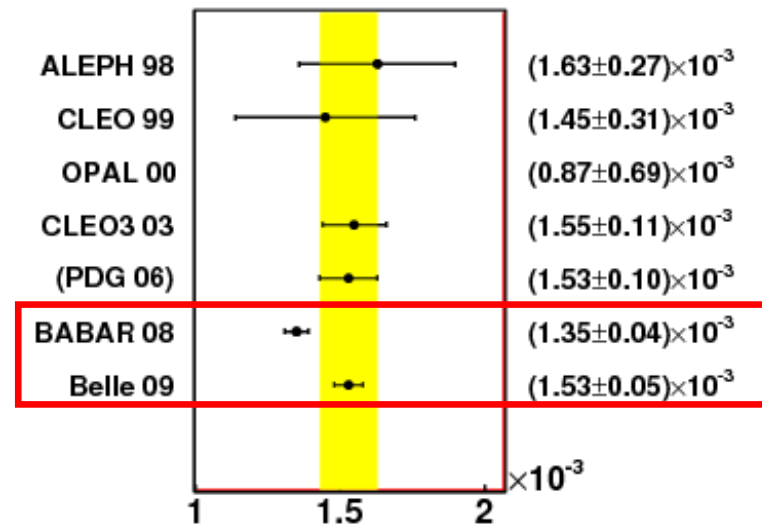
Branching ratio of $\tau \rightarrow \pi\pi\pi\nu$ decay



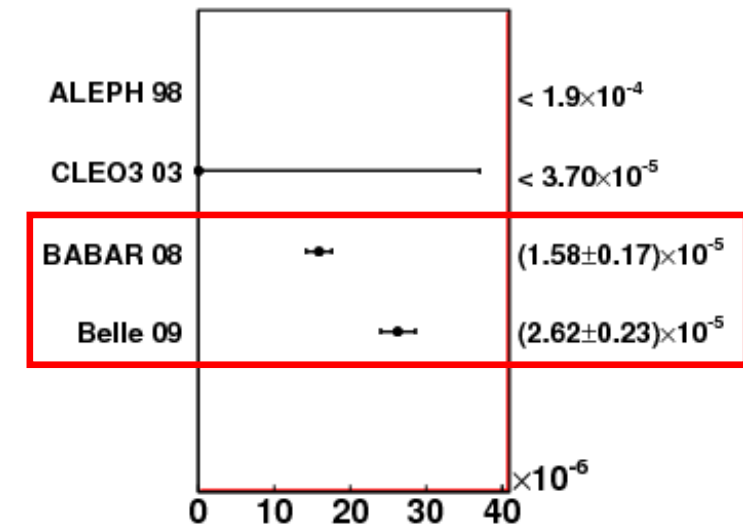
Branching ratio of $\tau \rightarrow K\pi\pi\nu$ decay



Branching ratio of $\tau \rightarrow KK\pi\nu$ decay



Branching ratio of $\tau \rightarrow KKK\nu$ decay





Mass spectra of $\tau^- \rightarrow h^- h^+ h^- \nu_\tau$

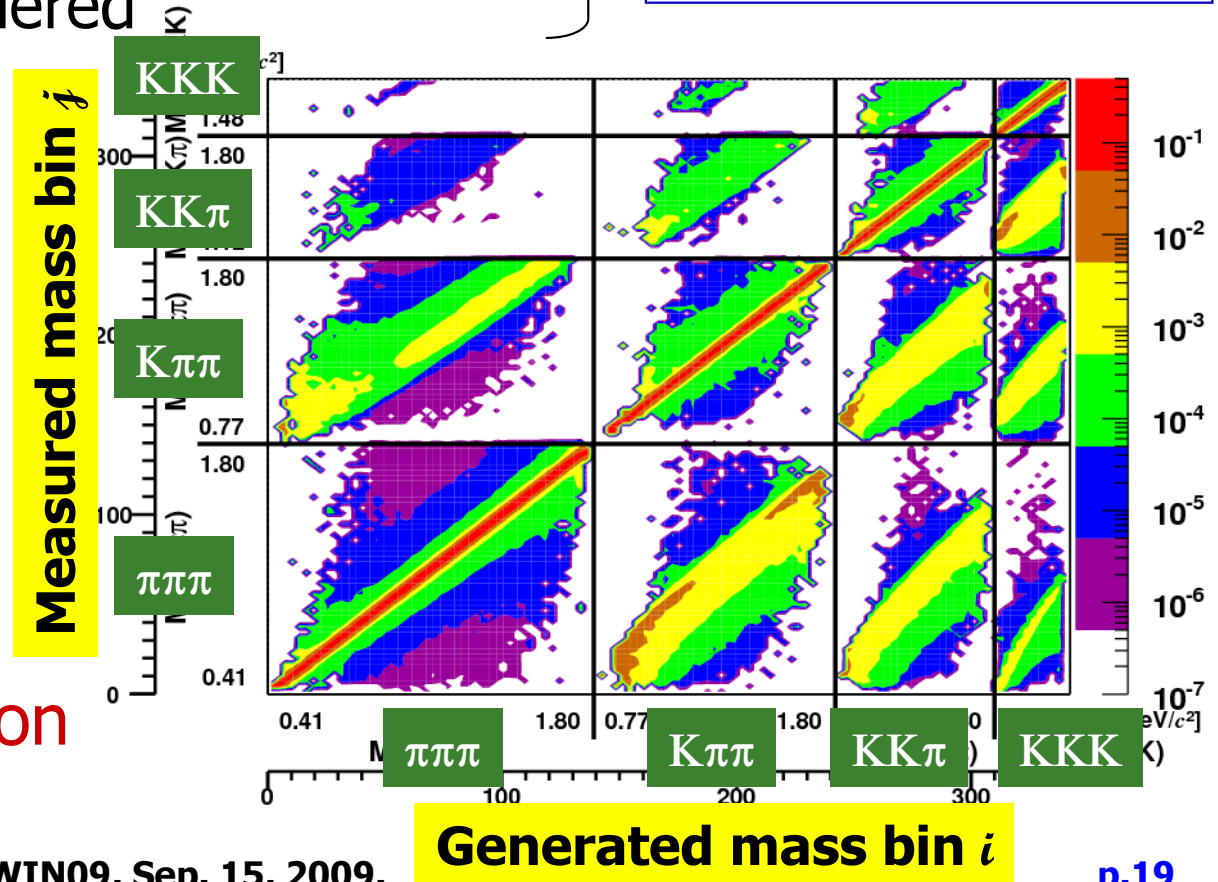
- Motivation
 - : to contribute to the evaluation of strange spectral function
- From the **unfolding** analysis
 - Taking into account the **smearing effect**
 - Also the **feed-down from other modes** simultaneously considered

Removing detector effects and get "real" spectrum

Unfolding is a inverse-problem for $A_{ij}x_j = b_i$

A : Response matrix
 x : unfolded spectrum
 b : observed spectrum (with other τ decay BG subtracted)

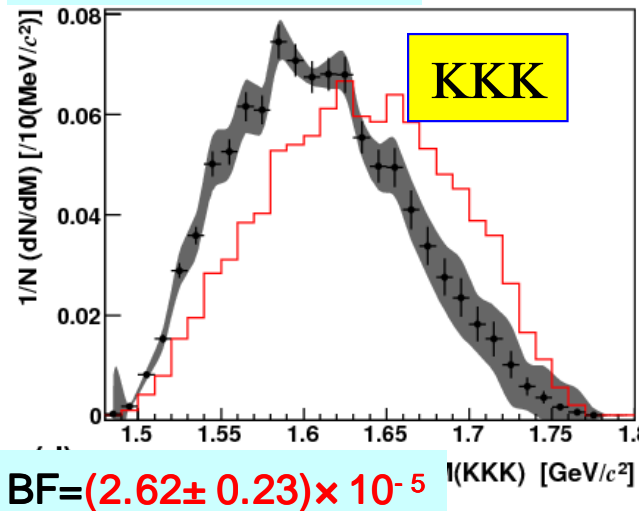
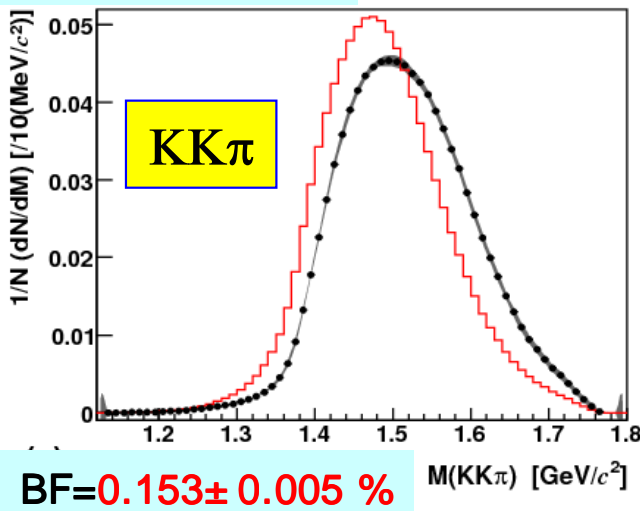
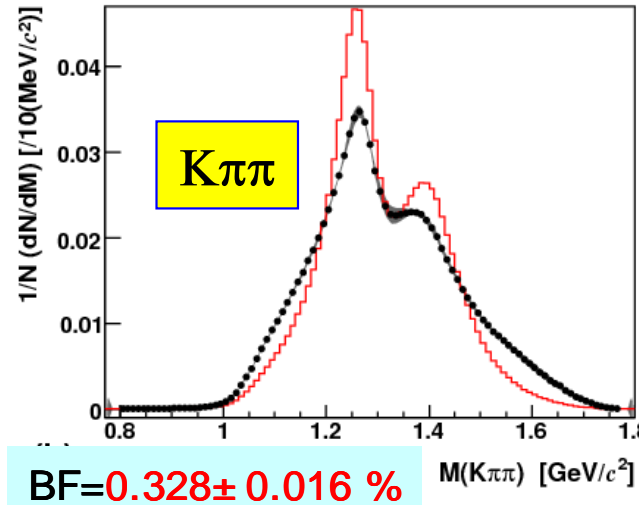
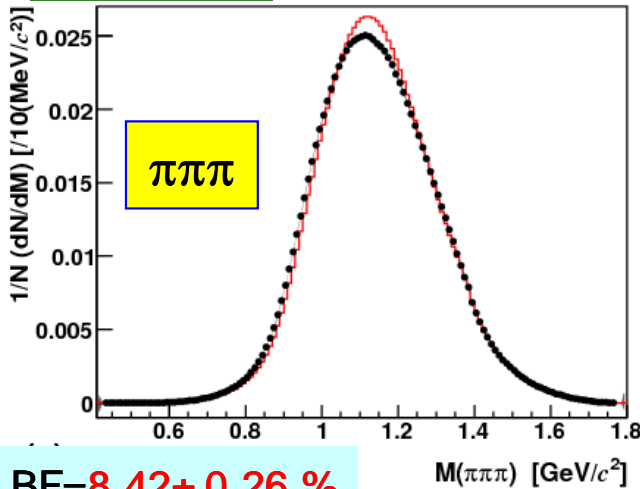
A^{-1} is obtained from **Singular Value Decomposition** techniques



Mass spectra of $\tau^- \rightarrow h^- h^+ h^- \nu_\tau$



dN/NdM (Normalized distribution)



Black point : unfolded spectra
+ stat. uncert.

Gray band : syst. uncert.

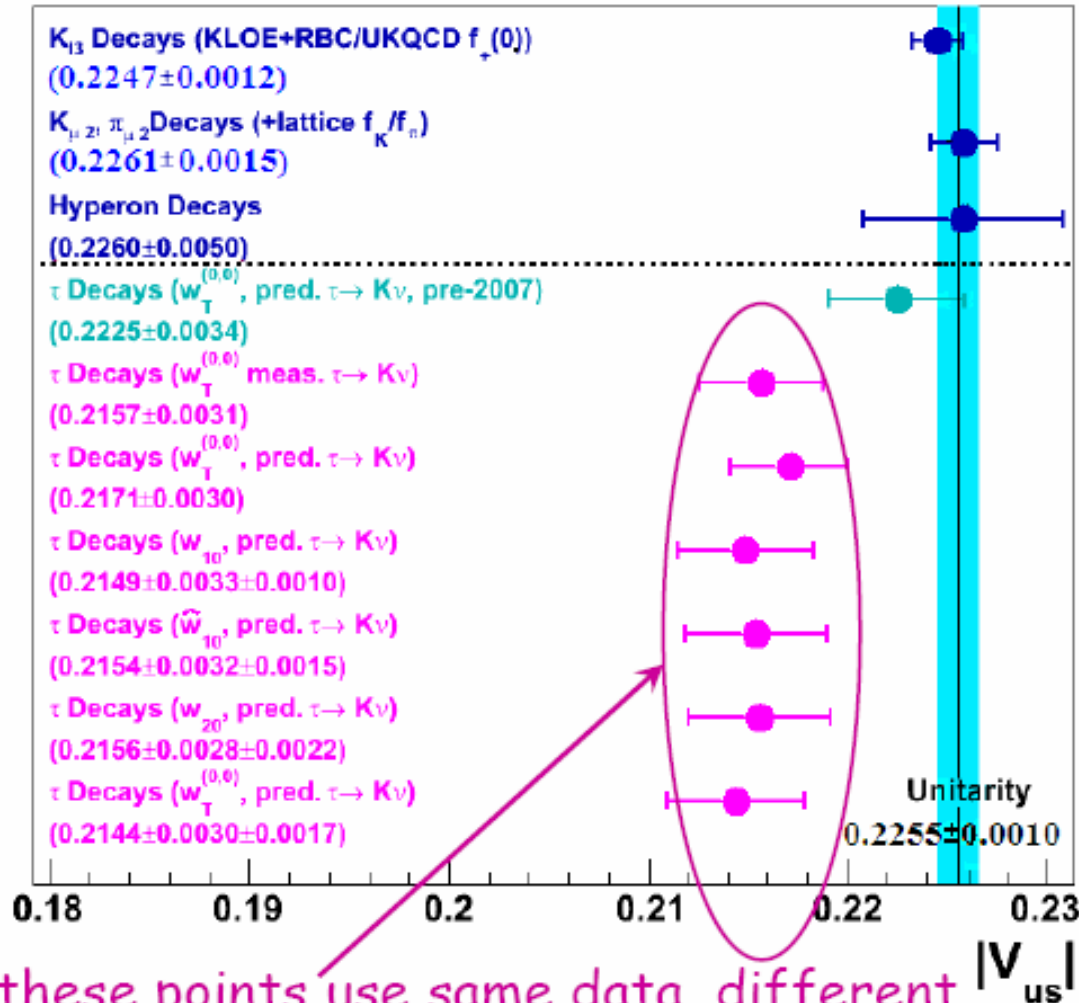
Red line : MC (TAUOLA)
expectations

(normalized to the unfolded dist.)

- First unfolded spectrum for $K\pi\pi$, $KK\pi$, KKK decays
- Clear differences with theoretical models.




- Incorrect resonance properties?
- Incorrect mixing parameter
- New resonances?
- Non-resonant decays?

(Semi-)Final V_{us} estimation (BaBar)



these points use same data, different weight functions in FESR

(J.Roney, HINT09 (2009, KEK))

Mode	$B(10^{-3})$
K^-	6.81 ± 0.23
$K^- \pi^0$	4.54 ± 0.30 → 
$\bar{K}^0 \pi^-$	8.78 ± 0.38 
$K^- \pi^0 \pi^0$	0.58 ± 0.24
$\bar{K}^0 \pi^- \pi^0$	3.60 ± 0.40
$K^- \pi^+ \pi^-$	3.30 ± 0.28 → 
$K^- \eta$	0.27 ± 0.06
$(\bar{K}3\pi)^-$ (estimated)	0.74 ± 0.30
$K_1(1270)^- \rightarrow K^- \omega$	0.67 ± 0.21
$(\bar{K}4\pi)^-$ (estimated) and $K^{*-} \eta$	0.40 ± 0.12
Sum	29.69 ± 0.86

- Using the updated BF measurements and PDG avg.
 - Mass spectra are not used
- $\sim 3\sigma$ differences with unitarity!

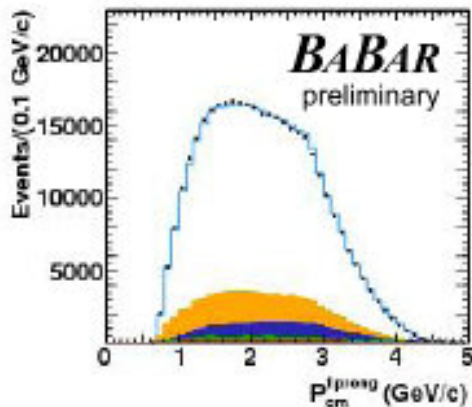
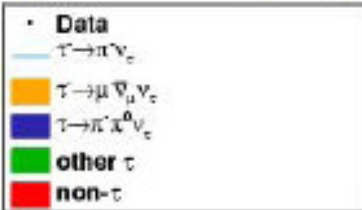
Independent measurement on V_{us}

$$\frac{\mathcal{B}(\tau \rightarrow K\nu)}{\mathcal{B}(\tau \rightarrow \pi\nu)} = \frac{f_K^2 |V_{us}|^2 (1 - m_K^2/m_\tau^2)^2}{f_\pi^2 |V_{ud}|^2 (1 - m_\pi^2/m_\tau^2)^2}$$

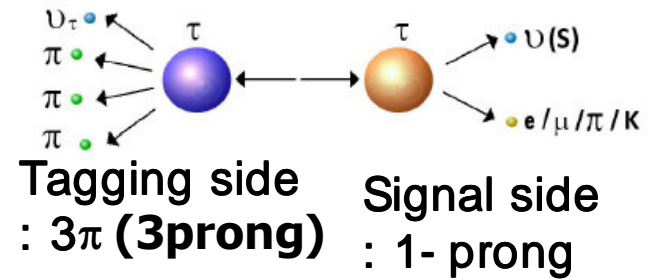
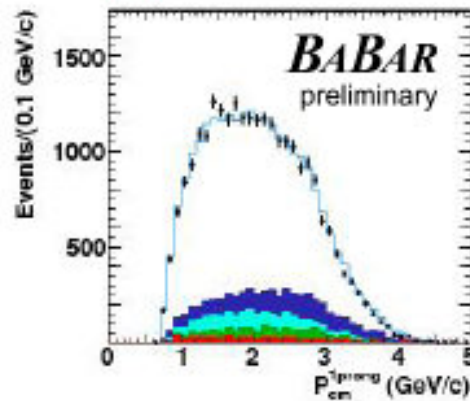
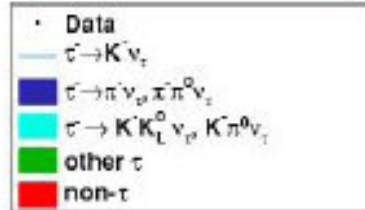
- $f_K/f_\pi = 1.189 \pm 0.007$ (Lattice QCD)
- Small ($\sim 0.03\%$) theoretical uncertainty can be ignored.
- Use $|V_{ud}| = 0.97408 \pm 0.00026$ from super-allowed $0^+ \rightarrow 0^+$ beta decay
- An independent study has been done by BaBar

$$\tau \rightarrow K \nu_\tau, \quad \tau \rightarrow \pi \nu_\tau$$

$$\tau^- \rightarrow \pi^- \nu_\tau$$



$$\tau^- \rightarrow K^- \nu_\tau$$



Branching ratios (BaBar, preliminary)

$B(\tau \rightarrow \pi \nu_\tau) / B(\tau \rightarrow e \nu_\tau \nu_e)$	$(5.945 \pm 0.014 \pm 0.061) \times 10^{-1}$
$B(\tau \rightarrow K \nu_\tau) / B(\tau \rightarrow e \nu_\tau \nu_e)$	$(3.882 \pm 0.032 \pm 0.056) \times 10^{-2}$
$B(\tau \rightarrow K \nu_\tau) / B(\tau \rightarrow \pi \nu_\tau)$	$(6.531 \pm 0.056 \pm 0.093) \times 10^{-2}$

PDG'08 Average (ALEPH'05)

$$(10.828 \pm 0.070 \pm 0.078) \times 10^{-2}$$

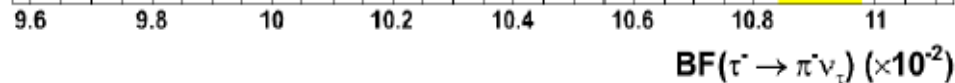
PDG'08 Global Fit

$$(10.91 \pm 0.07) \times 10^{-2}$$

This Work

$$(10.59 \pm 0.04 \pm 0.11) \times 10^{-2}$$

$$\tau^- \rightarrow \pi^- \nu_\tau$$



CLEO'94
 $(6.6 \pm 0.7 \pm 0.9) \times 10^{-3}$

DELPHI'94
 $(8.5 \pm 0.18) \times 10^{-3}$

ALEPH'99
 $(6.96 \pm 0.25 \pm 0.24) \times 10^{-3}$

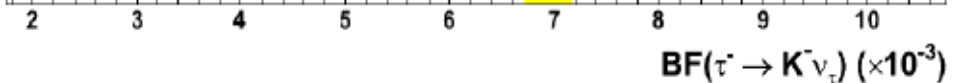
OPAL'01
 $(6.58 \pm 0.27 \pm 0.29) \times 10^{-3}$

PDG'08 Average
 $(6.85 \pm 0.23) \times 10^{-3}$

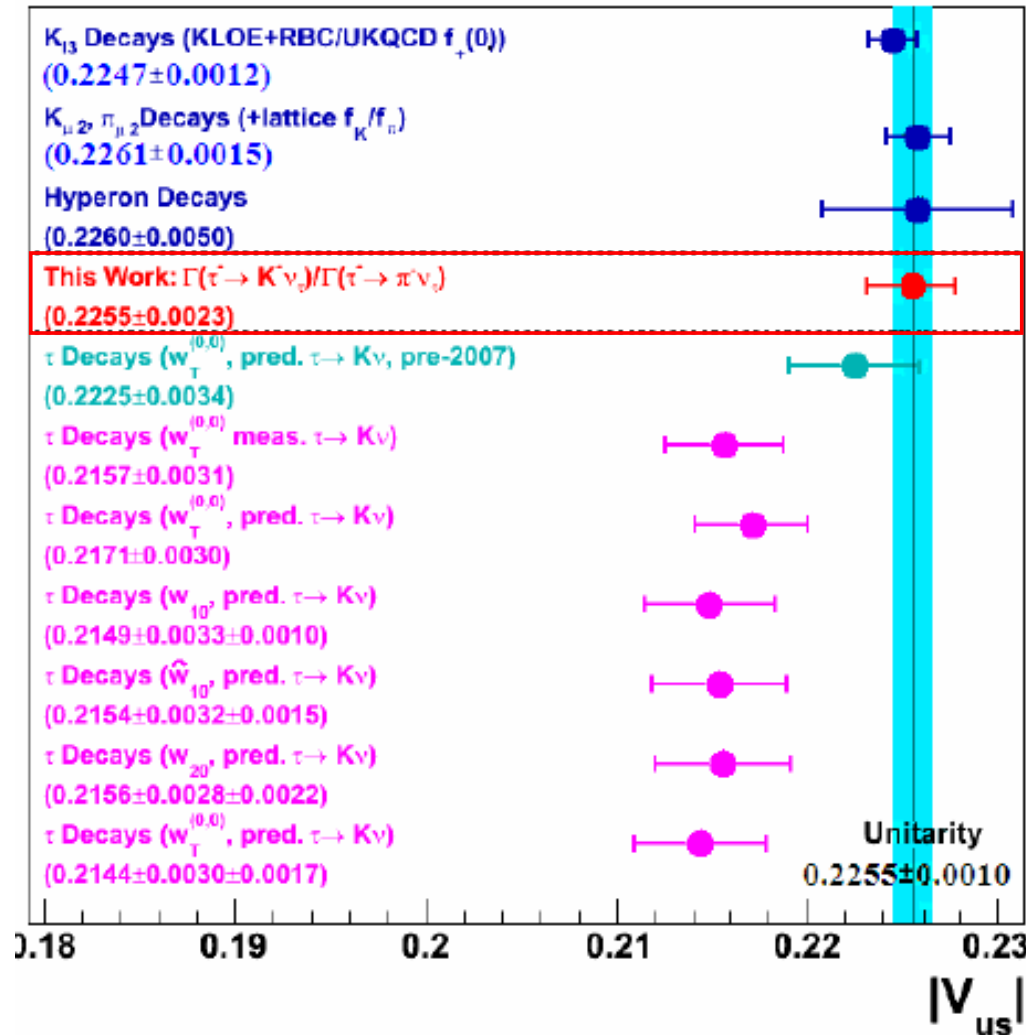
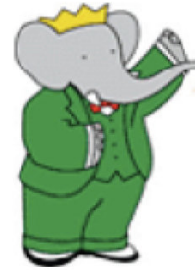
PDG'08 Global Fit
 $(6.95 \pm 0.23) \times 10^{-3}$

This Work
 $(6.92 \pm 0.06 \pm 0.10) \times 10^{-3}$

$$\tau^- \rightarrow K^- \nu_\tau$$



Updated result on V_{us}



$$|V_{us}| = 0.2255 \pm 0.0023$$

BaBar preliminary
consistent with
unitarity.

M.Roney, HINT09 (2009, KEK)

Summary and conclusion

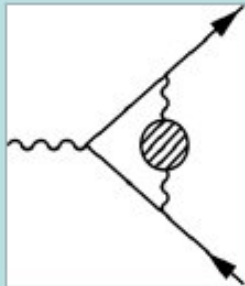
- B-factory = τ -factory
- Many measurements have been done and are ongoing, specially in hadronic decays of τ
- Recent progress :
 - Second Class Current
 - Can not find any positive signal – SM is still very healthy
 - V_{us} measurement through inclusive measurements on the strange decay of τ
 - Had been an important issue for a few years recently.
 - May be due to the lack of measurements on the strange decay of tau – need more measurements
 - We need simultaneous measurement with m_s – need more studies and (if possible) more statistics.



backups



Hadronic contribution a_{had}

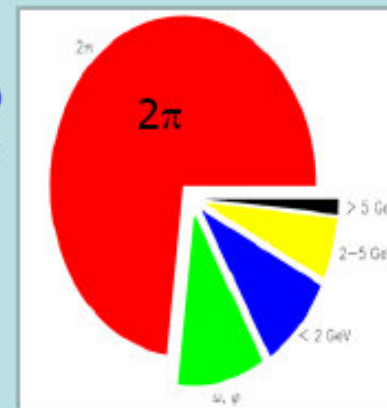


$$a_{\mu}^{had,LO} = \left(\frac{\alpha m_{\mu}}{3\pi} \right)^2 \int_{4m_{\pi}^2}^{\infty} ds \frac{R(s) \hat{K}(s)}{s^2}$$

$$R(s) = \frac{\sigma(e^+e^- \rightarrow hadrons)}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}, \quad \sigma_{\mu^+\mu^-} = \frac{85.86nb}{s[GeV^2]}$$

\hat{K} grows from 0.63 at $s = 4m_{\pi}^2$ to 1 at $s \rightarrow \infty$, $1/s^2$ emphasizes the role of low energies, particularly important is the reaction $e^+e^- \rightarrow \pi^+\pi^-$ with a large cross section below 1 GeV.

Central values



Uncertainties





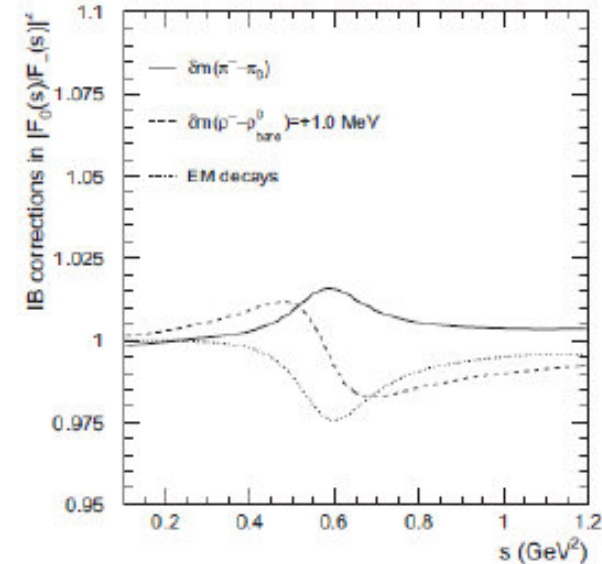
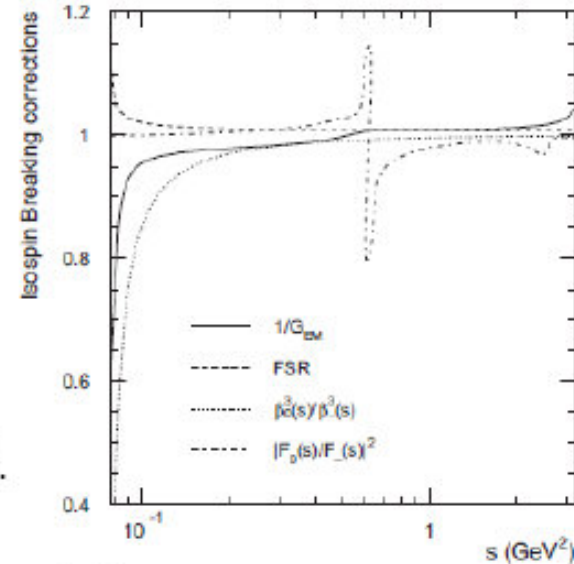
Isospin-breaking corrections

arxiv:0906.5442v2

G.L. Castro,
M. Davier, etc

Other references:

- V. Cirigliano et al., J. High Energy Phys. 08, 002(2002)
- A. Flores-Tlalpa et al., Phys. Rev. D 74, 071301 (2006)



S_{EW} : short distance rad. Cor.

G_{EM} : long distance rad. Cor.

FSR: final state radiation in $ee \rightarrow \pi\pi$

π^0 and π^- mass difference in the phase sp.

ρ - ω interference

ρ^- - ρ^0 mass difference

EM decays

Source	$\Delta a_{\mu}^{\text{had, LO}}[\pi\pi, \tau] (10^{-10})$	
	GS model	KS model
S_{EW}	-12.21 ± 0.15	
G_{EM}	-1.92 ± 0.90	
FSR	$+4.67 \pm 0.47$	
ρ - ω interference	$+2.80 \pm 0.19$	$+2.80 \pm 0.15$
$m_{\pi^{\pm}} - m_{\pi^0}$ effect on σ		-7.88
$m_{\pi^{\pm}} - m_{\pi^0}$ effect on Γ_{ρ}	$+4.09$	$+4.02$
$m_{\rho^{\pm}} - m_{\rho^0}$	$0.20^{+0.27}_{-0.19}$	$0.11^{+0.19}_{-0.11}$
$\pi\pi\gamma$, electrom. decays	-5.91 ± 0.59	-6.39 ± 0.64
Total	-16.07 ± 1.22	-17.00 ± 1.23
	-16.07 ± 1.53	



$a_{\mu}^{2\pi}$: 2π contribution to a_{μ}



Experiment	$a_{\mu}^{\text{had,LO}}[\pi\pi, \tau] (10^{-10})$	
	$2m_{\pi^{\pm}} - 0.36 \text{ GeV}$	$0.36 - 1.8 \text{ GeV}$
ALEPH	$9.46 \pm 0.33_{\text{exp}} \pm 0.05_{\text{B}} \pm 0.07_{\text{IB}}$	$499.19 \pm 5.20_{\text{exp}} \pm 2.70_{\text{B}} \pm 1.54_{\text{IB}}$
CLEO	$9.65 \pm 0.42_{\text{exp}} \pm 0.17_{\text{B}} \pm 0.07_{\text{IB}}$	$504.51 \pm 5.36_{\text{exp}} \pm 8.77_{\text{B}} \pm 1.54_{\text{IB}}$
OPAL	$11.31 \pm 0.76_{\text{exp}} \pm 0.15_{\text{B}} \pm 0.07_{\text{IB}}$	$515.56 \pm 9.98_{\text{exp}} \pm 6.95_{\text{B}} \pm 1.54_{\text{IB}}$
Belle	$9.74 \pm 0.28_{\text{exp}} \pm 0.15_{\text{B}} \pm 0.07_{\text{IB}}$	$503.95 \pm 1.90_{\text{exp}} \pm 7.84_{\text{B}} \pm 1.54_{\text{IB}}$
Combined	$9.76 \pm 0.14_{\text{exp}} \pm 0.04_{\text{B}} \pm 0.07_{\text{IB}}$	$505.46 \pm 1.97_{\text{exp}} \pm 2.19_{\text{B}} \pm 1.54_{\text{IB}}$

Integrated from 2π threshold to 1.8GeV

Smallest experimental error for Belle !

$$\tau : a_{\mu}^{\pi\pi} = (514.1 \pm 3.2) \times 10^{-10}$$

$$e^+e^- (\text{CMD, SND, KLOE}) : a_{\mu}^{\pi\pi} = (503.5 \pm 3.5) \times 10^{-10}$$

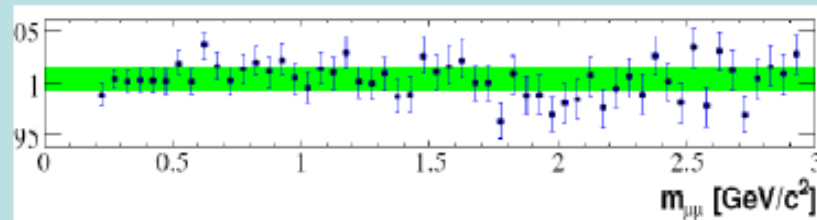
There is a difference btw τ and e^+e^-



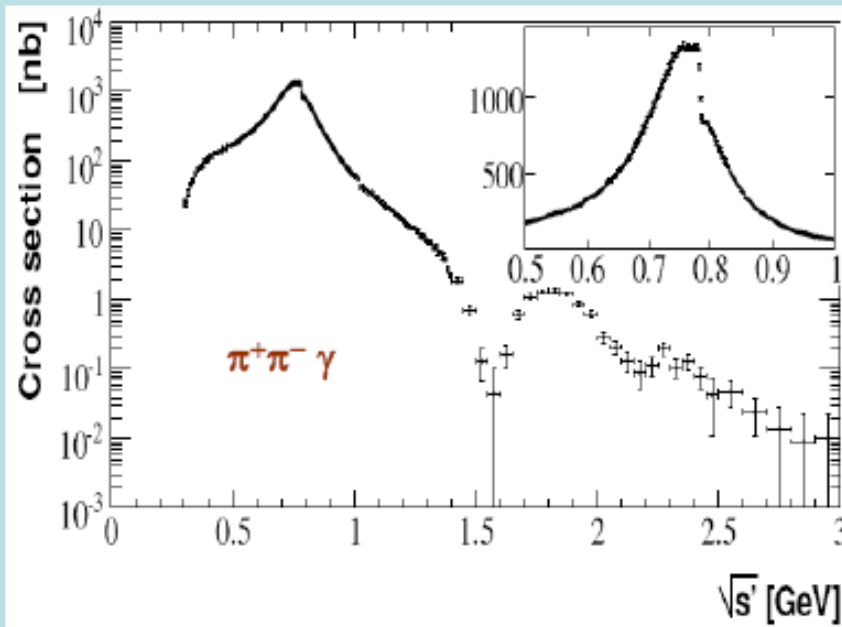
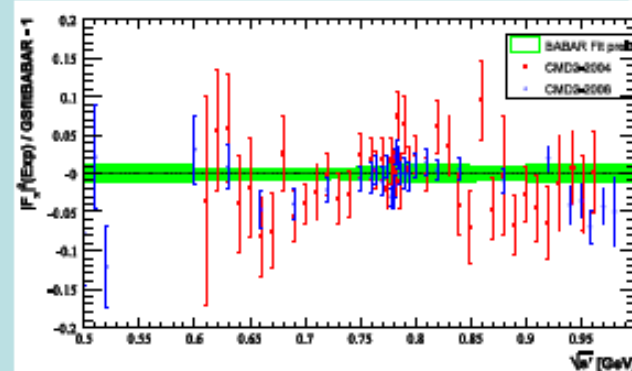
$e^+e^- \rightarrow \pi^+\pi^-\gamma$

(first presented at LP09)

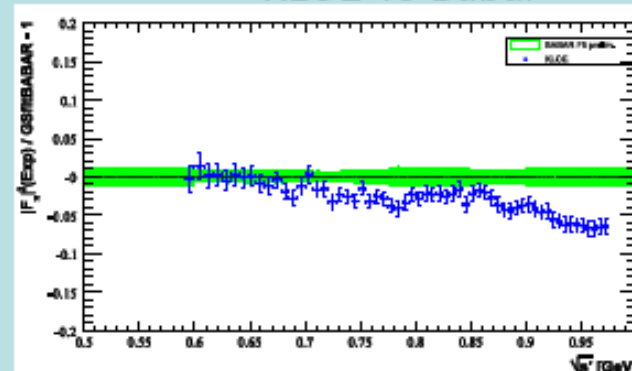
$\mu^+\mu^-\gamma$ - exp/QED



CMD2 vs Babar



KLOE vs Babar



Babar collab.arxiv:0908.3589

21.08.2009

Lepton-Photon 2009

17



Computing $a_{\mu}^{\pi\pi}$

$$\frac{\sigma_{\mu\mu\gamma}^{data}}{\sigma_{\mu\mu\gamma}^{NLO QED}} = 1 + (4.0 \pm 2.0 \pm 5.5 \pm 9.4) \times 10^{-3}$$



From $\pi^+\pi^-$ threshold to 1.8 GeV

$$a_{\mu}^{\pi\pi(\gamma)} = (514.1 \pm 2.2 \pm 3.1) \times 10^{-10}$$

Previous e^+e^- data: $(502.8 \pm 3.2) \times 10^{-10}$

updated value from $\tau^- \rightarrow \pi^- \pi^0 \nu_{\tau}$: $(514.3 \pm 3.0) \times 10^{-10}$

M.Davier et al., arXiv:0906.5443v1 (hep-ph)

According to these results $\Delta a_{\mu, \text{hadr}}$ reduces to $\sim 2\sigma$