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# Testing neutrino mass models @ LHC

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# Outline

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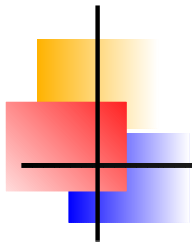
*I.* Introduction

*II.* “Low-scale” seesaw

*III.* Radiative neutrino mass models

*IV.*  $R_p$  Supersymmetric neutrino masses

*V.* High-scale Seesaw and SUSY

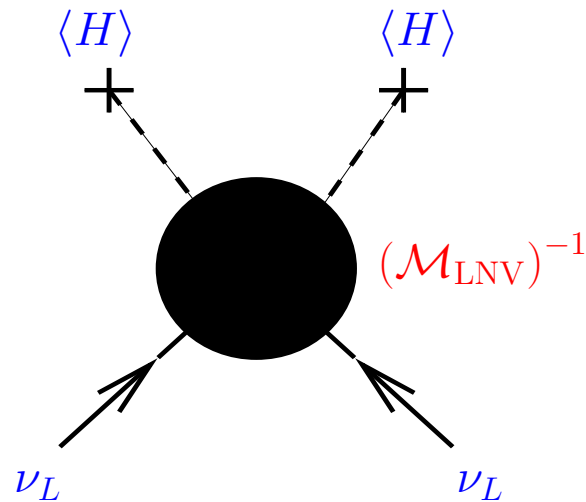


*I.*

# Introduction

# Majorana $\mathcal{M}_\nu$

If **L**epton **N**umber is **V**iolated:

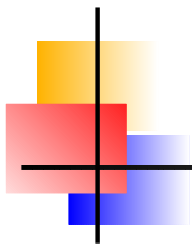


Weinberg, 1979

$$(\mathcal{M}_\nu)_{\alpha\beta} = \frac{\kappa_{\alpha\beta}}{\mathcal{M}_{LNV}} (L_\alpha H)(L_\beta H)$$

Many realizations:

- (i) **Seesaw mechanism**: Type-I, Type-II, Type-III, Inverse seesaw, etc ...
- (ii) **Radiative models**: Zee, Babu, LQs ...
- (iii) **SUSY neutrino masses**: R-parity violation
- (iv) ...



*II.*

Non-supersymmetric

“Low-scale” seesaw

# 'Classical' Seesaw

In the basis  $(\nu_L, \nu_R)$  write mass matrix:

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & m_D \\ m_D & M_M \end{pmatrix}.$$

Minkowski, 1977

Yanagida, 1979

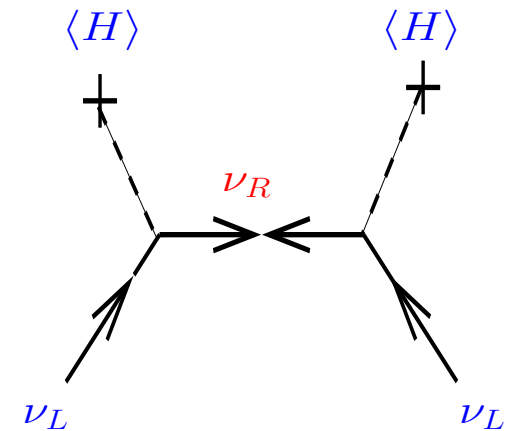
Gell-Mann, Ramond & Slansky, 1979

Mohapatra & Senjanovic, 1980

.....

If  $m_D \ll M_M$ :

$$m_{1/2} \simeq \left( -\frac{m_D^2}{M_M}, M_M \right)$$



Santamaria, 1993

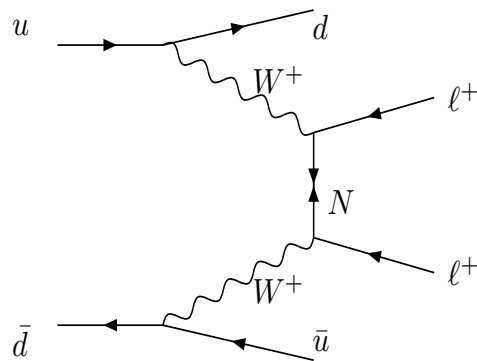
⇒ For 3  $\nu_R$  21 parameters

⇒ At low energy 12 parameters measurable:

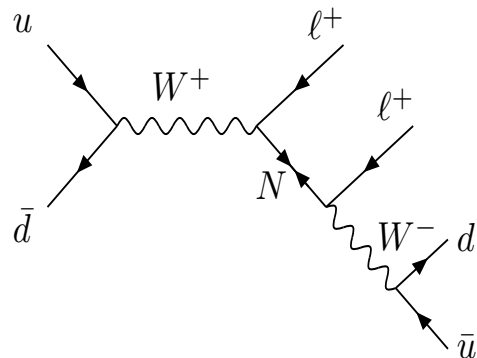
3  $m_{l_i}$ , 3  $m_{\nu_i}$ , 3 angles & 3 phases

# Seesaw type-I and LHC

Diagrams for  $N_R$  production at LHC:



$$\sigma \propto |V_{lN}^4|$$



$$\sigma \propto |V_{lN}^2|$$

del Aguila et al., 2008:

$$\sum_i |V_{eN_i}|^2 \leq 0.0030$$

$$\sum_i |V_{\mu N_i}|^2 \leq 0.0032$$

$$\sum_i |V_{\tau N_i}|^2 \leq 0.0062$$

From  $0\nu\beta\beta$  decay:

$$\sum_i |V_{eN_i}^2 \frac{1}{m_{N_i}}| \leq 5 \times 10^{-8} \text{ GeV}^{-1}$$

del Aguila &

Aguilar-Saavedra, 2009:

$$\sigma(LHC) \leq 180 \text{ fb}^{-1} \text{ for } m_N = 100 \text{ GeV}$$

Han & Zhang, 2006:

$$\sum_i |V_{\mu N_i}|^2 \leq 10^{-4} \text{ (} 10^{-6} \text{)}$$

$$\text{for } m_N = 100 \text{ GeV (} m_N = 50 \text{ GeV)}$$



# Seesaw-I, LHC and $M_\nu$

Estimate Yukawas:

$$h_\nu \sim \sqrt{\frac{m_\nu M_M}{v_U^2}} \sim \mathcal{O}(1) \left( \frac{m_\nu}{0.05 \text{ eV}} \right)^{1/2} \left( \frac{M_M}{10^{15} \text{ GeV}} \right)^{1/2}$$
$$\sim \mathcal{O}(10^{-6}) \left( \frac{m_\nu}{0.05 \text{ eV}} \right)^{1/2} \left( \frac{M_M}{1 \text{ TeV}} \right)^{1/2}$$

⇒ Recall:

$\sqrt{s} = 10$  (14) TeV @ LHC

EW cross sections @ LHC:  $\sigma(W \rightarrow l\nu) = 15 \text{ nb}$

Estimate:  $\sigma(W \rightarrow lN) \leq \sigma(W \rightarrow l\nu) \times |V_{lN}|^2$

Luminosity:  $\mathcal{L} = 10 \text{ fb}^{-1}$  per year (planned)

→ less than  $10^{-4}$  events/year for  $h_\nu \sim 10^{-6}$

Possible exception: Inverse Seesaw

Mohapatra & Valle, 1986



# Seesaw: Type II

Y=2 Scalar triplet:  $\Delta = (\Delta^{++}, \Delta^+, \Delta^0)$

$$\mathcal{M}_\nu = \begin{pmatrix} m_M & 0 \\ 0 & 0 \end{pmatrix}$$

with:

$$m_M \simeq Y^\nu \langle \Delta^0 \rangle$$

Example:

$SU(5)$  with **15**:

$$\langle \Delta^0 \rangle \sim \frac{\langle h^0 \rangle^2}{m_{15}}$$

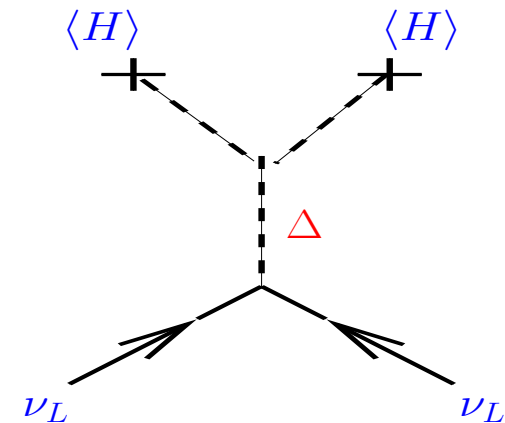
⇒ With **2 triplets** (SUSY) **15 parameters**

Schechter & Valle, 1980, 1982

Cheng & Li, 1980

Mohapatra, Senjanovic, 1981

...



# Seesaw-II and LHC

Production at LHC through gauge bosons:

$$q\bar{q} \rightarrow Z/\gamma \rightarrow \Delta^{++}\Delta^{--}$$

$$q\bar{q} \rightarrow Z/\gamma \rightarrow \Delta^{\pm}\Delta^{\mp}$$

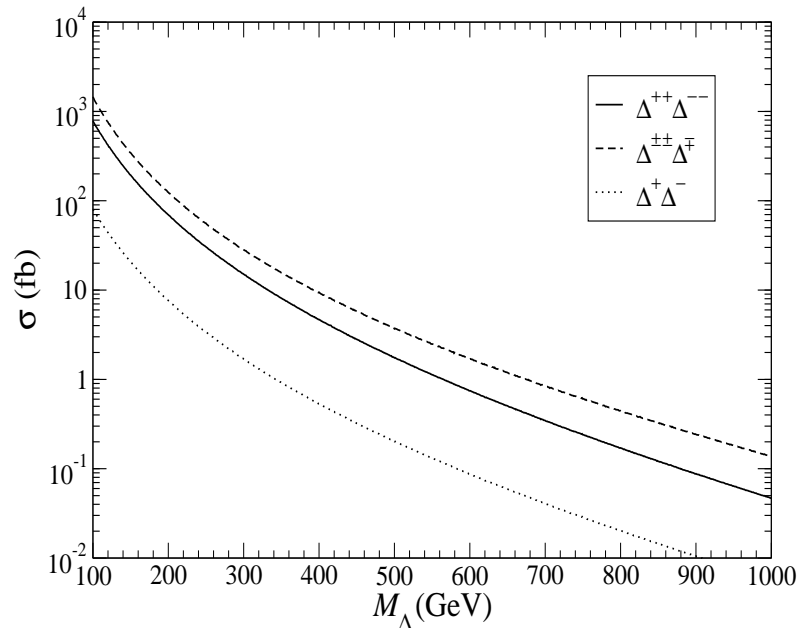
$$q\bar{q}' \rightarrow W \rightarrow \Delta^{\pm\pm}\Delta^{\mp}$$

Gunion et al., 1996

$$m_{\Delta} \leq 925 \text{ GeV}$$

with  $\mathcal{L} = 100 \text{ fb}^{-1}$

del Aguila & Aguilar-Saavedra, 2009:



Garayoa & Schwetz, 2008

Test neutrino mass

hierarchy from:

$$\text{Br}(\Delta^{++} \rightarrow l_i^{+} l_j^{+})$$

many others ...

# Seesaw: Type-III

As in seesaw type-I. Replace  $\nu_R$  by  $\Sigma = (\Sigma^+, \Sigma^0, \Sigma^-)$ .  
In the basis  $(\nu_L, \Sigma)$  write mass matrix:

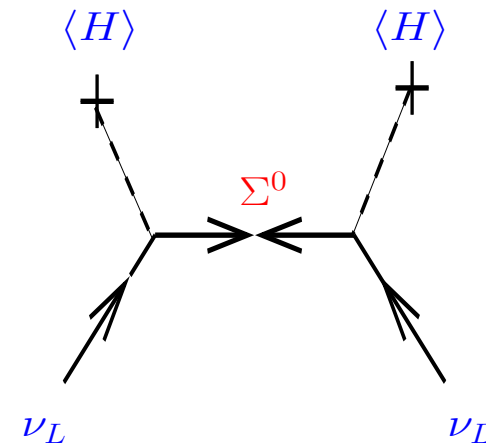
$$\mathcal{M}_\nu = \begin{pmatrix} 0 & m_D \\ m_D & M_\Sigma \end{pmatrix}.$$

R. Foot et al., 1988  
E. Ma, 1998

If  $m_D \ll M_\Sigma$ :

$$m_{1/2} \simeq \left( -\frac{m_D^2}{M_\Sigma}, M_\Sigma \right)$$

⇒ For 3  $\Sigma$  21 parameters

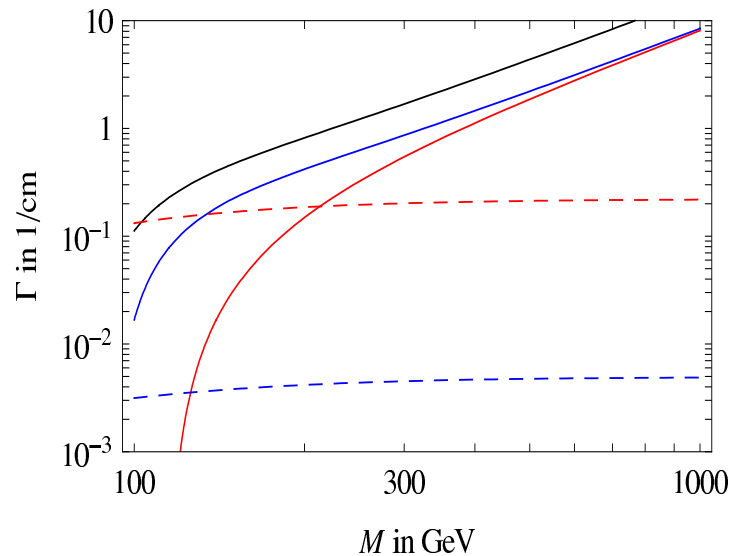


# Seesaw-III and LHC

As in type-II: Production at LHC through **gauge bosons**, estimate:

Up to (roughly)  $m_{\Sigma} \sim 1$  TeV

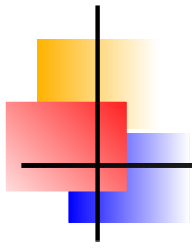
Franceschini et al., 2008



- $N_0 \rightarrow \nu h, N^\pm \rightarrow \ell^\pm h$
- $N_0 \rightarrow Z\nu, N^\pm \rightarrow Z\ell^\pm$
- $N_0 \rightarrow W^\pm \ell^\pm, N^\pm \rightarrow W^\pm \nu$
- -  $N^\pm \rightarrow N_0 \pi^\pm$
- -  $N^\pm \rightarrow N_0 \ell^\pm \nu$

Displaced vertex!

⇒ For 3 generations of  $\Sigma$  **no correlation** of decays of  $\Sigma$   
with neutrino angles



*III.*

# Radiative neutrino mass models

Only two examples!

# Babu model

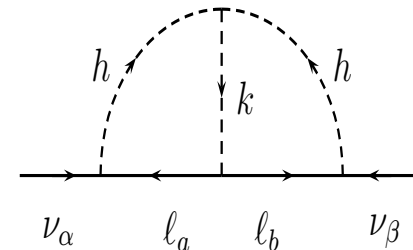
Cheng & Li, 1980; Zee, 1985; Babu, 1988:

$$\mathcal{L} = f_{\alpha\beta}(L_{\alpha L}^{Ti} C L_{\beta L}^j)\epsilon_{ij}h^+ + h'_{\alpha\beta}(e_{\alpha R}^T C e_{\beta R})k^{++} + \text{h.c.}$$

Scalar sector:

$$\mathcal{L} = -\mu h^+ h^+ k^{--} + \text{h.c.}$$

$$\mathcal{M}_\nu = \left(\frac{1}{(16\pi^2)}\right)^2 (f h f)(m_l)^2 \times \mathcal{I} =$$



Babu & Macesanu, 2002 :

$m_{k^{++}}$  up to 800 GeV with  $100 \text{ fb}^{-1}$  at LHC

Aristizabal & Hirsch, 2006:

Decay branching ratios of new scalars fixed by neutrino angles

# Leptoquarks

Hypothetical particles coupling to lepton-quark pairs:

$$\mathcal{L}_{LQ-l-q} = +\lambda_{\tilde{S}_{1/2}}^{(R)} \bar{d} P_L l \tilde{S}_{1/2}^\dagger + \lambda_{S_{1/2}}^{(L)} \bar{q} P_R i\tau_2 e S_{1/2}^{L\dagger} + \dots$$

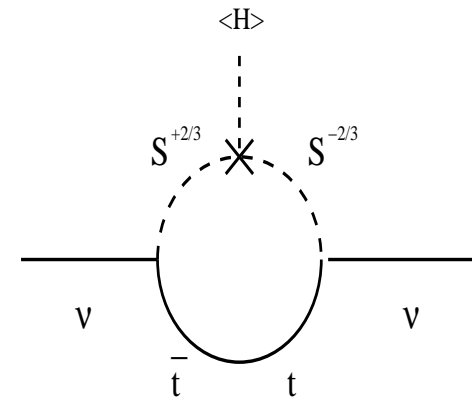
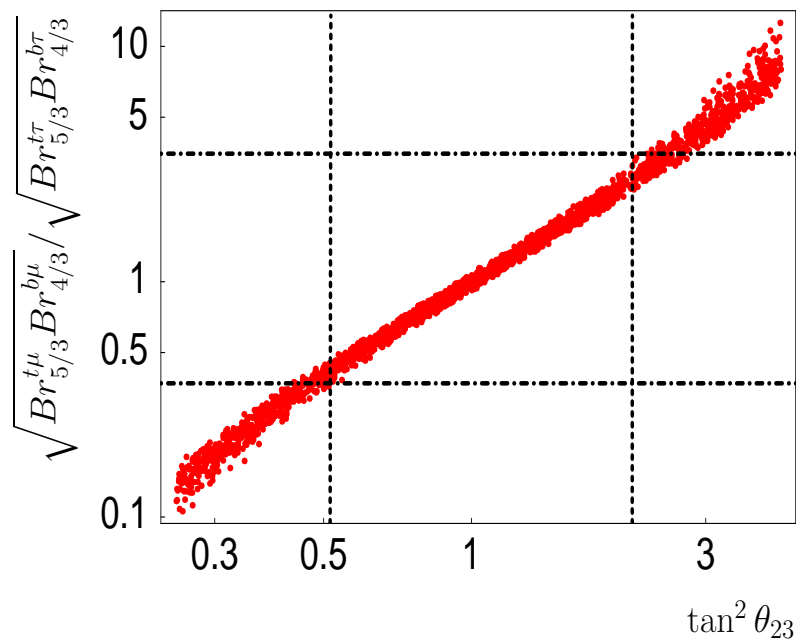
Buchmüller et al., 1987

LQ-Higgs interaction mixes different LQ states:

$$V = Y_{S_{1/2}}^{(i)} \left( H i\tau_2 S_{1/2}^i \right) \left( \tilde{S}_{1/2}^\dagger H \right) + \dots$$

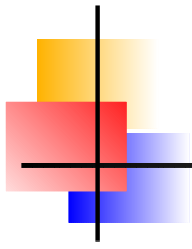
Hirsch et al. 1996

Aristizabal et al. 2008



Up to  $m_{LQ} \leq (1.2 - 1.5) \text{ TeV @ LHC}$

Kramer et al., 2005



*IV.*

# Supersymmetric neutrino masses

R-parity violation

bilinear  $R_p$ , spontaneous  $R_p$ ,  $\mu\nu$ SSM



# Supersymmetric $\mathcal{M}_\nu$

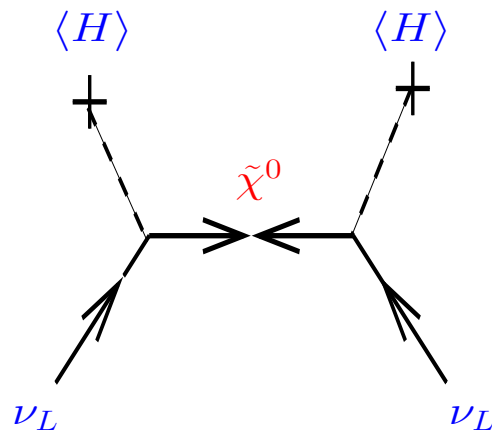
R-parity violation as origin  
of neutrino mass:

Aulakh & Mohapatra, 1982

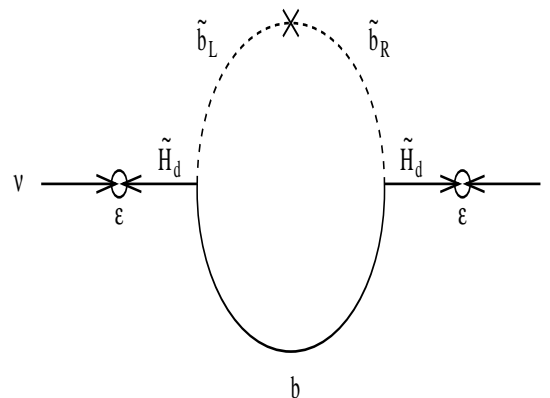
Hall & Suzuki, 1984

Ross & Valle, 1985

...



Tree-Level



+ 1-Loop

weak-scale Seesaw + radiative

Neutrino mass  
calculations  
after Super-K:

Drees et al., 1998

Chun et al., 1999

Hirsch et al., 2000, 2002

...

⇒ Easy to fit neutrino data, but no prediction for angles in general  
... as in seesaw!



# LHC and $R_p$

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With R-parity violated **LSP decays**, thus ...  
... **any superpartner can be the LSP!**

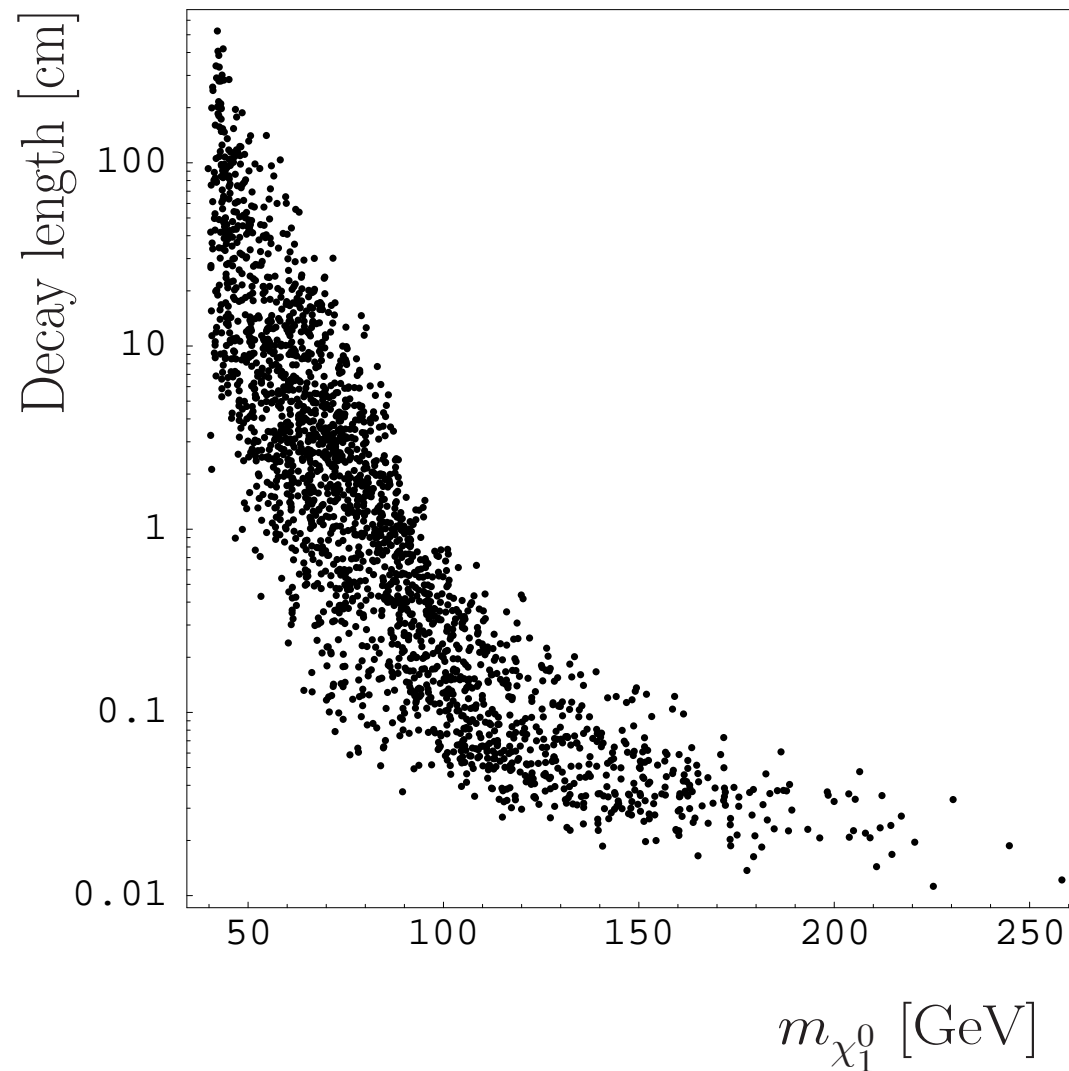
- ⇒ Neutralino
- ⇒ Chargino
- ⇒ Gluino
- ⇒ Charged scalar
- ⇒ Scalar neutrino
- ⇒ Scalar quark

Phenomenology  
depends on which is LSP,  
detailed studies so far only  
 $\chi_1^0$  and charged scalar

See, however:  
Hirsch & Porod 2003

# Neutralino decay length

All Points with correct  $\Delta m_{\text{Atm}}^2$  and  $\Delta m_{\odot}^2$ :



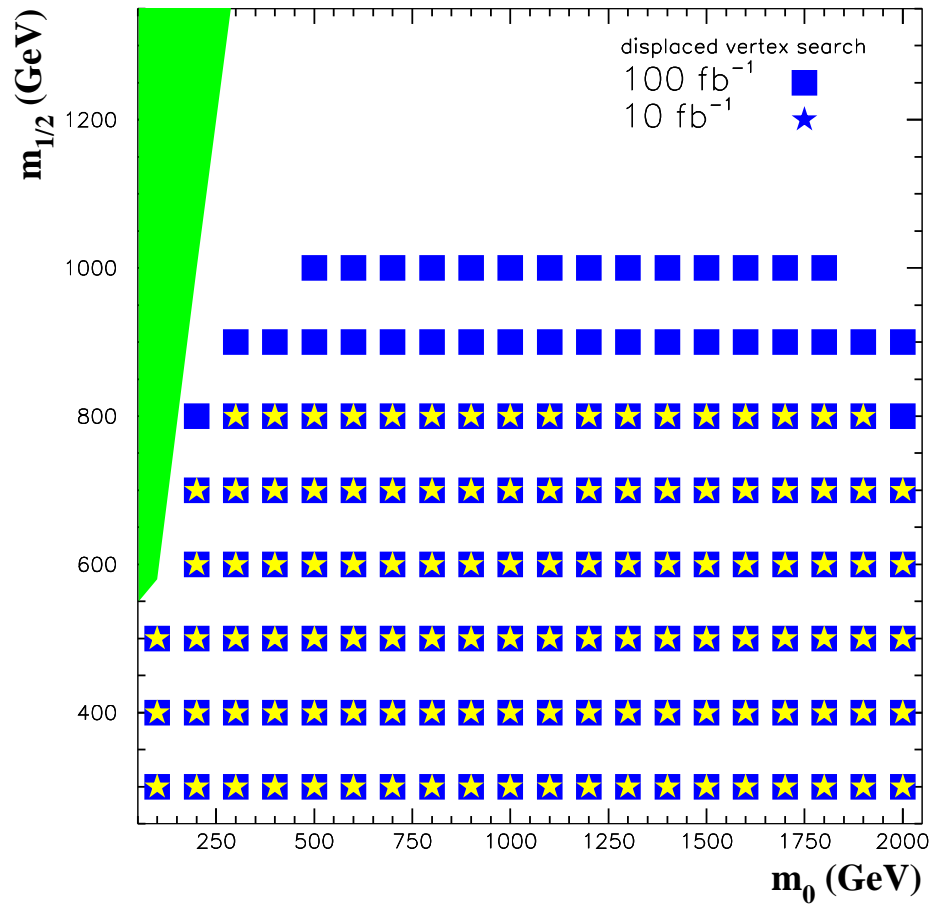
Porod et al., 2001

Displaced vertex!

No known SM  
background!

# LHC reach

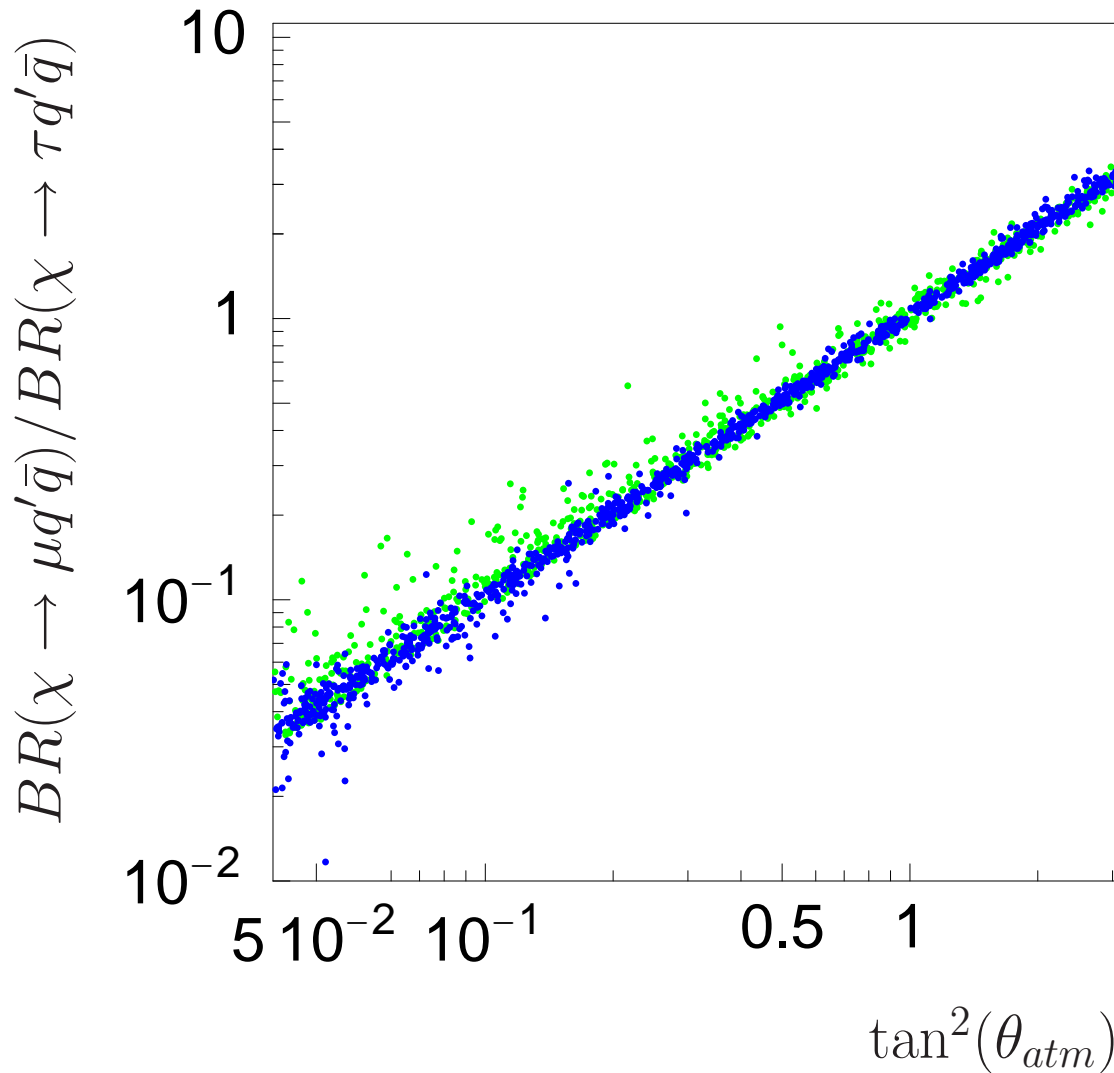
de Campos et al., 2008



Displaced vertex  
search

$\sqrt{s} = 14$  TeV,  
 $\mathcal{L} = 10$  and 100 fb<sup>-1</sup>

# Neutralino decay and $\theta_{Atm}$



Ratio of  
branching  
ratios  
predicted  
from  
atmospheric  
neutrino  
measurement

Porod et al., 2001

# Spontaneous $R_p$

$$\mathcal{W} = h_U^{ij} \hat{Q}_i \hat{U}_j \hat{H}_u + h_D^{ij} \hat{Q}_i \hat{D}_j \hat{H}_d + h_E^{ij} \hat{L}_i \hat{E}_j \hat{H}_d \\ + h_\nu^{ij} \hat{L}_i \hat{\nu}_j^c \hat{H}_u - h_0 \hat{H}_d \hat{H}_u \hat{\Phi} + h^{ij} \hat{\Phi} \hat{\nu}_i^c \hat{S}_j$$

- ⇒ Explains absence for trilinear terms
- ⇒ If scalar singlet gets vacuum expectation value:  
 $\epsilon_i = h_i^\nu \langle \tilde{\nu}^c \rangle$
- ⇒ Spontaneous breaking of lepton number,  
 Goldstone boson: **Majoron**
- ⇒  $\hat{\Phi}$  potentially **solves  $\mu$ -problem** à la NMSSM

Aulakh & Mohapatra, 1982  
 Ross & Valle 1985  
 Masiero & Valle 1990

...

Changes Pheno from explicit model due to:

- ⇒ Possibly invisible Higgs ( $h^0 \rightarrow JJ$ )
- ⇒  $\chi_1^0 \rightarrow J\nu$
- ⇒  $\mu \rightarrow eJ$  anticorrelates with  $\chi_1^0 \rightarrow J\nu$

Hirsch et al., 2004, 2009



# The $\mu\nu$ SSM

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$$\mathcal{W} = h_U^{ij} \widehat{Q}_i \widehat{U}_j \widehat{H}_u + h_D^{ij} \widehat{Q}_i \widehat{D}_j \widehat{H}_d + h_E^{ij} \widehat{L}_i \widehat{E}_j \widehat{H}_d \\ + h_\nu^{ij} \widehat{L}_i \widehat{\nu}_j^c \widehat{H}_u - \lambda_i \widehat{H}_d \widehat{H}_u \widehat{\nu}_i^c + \kappa_{ijk} \widehat{\nu}_i^c \widehat{\nu}_j^c \widehat{\nu}_k^c$$

As Next-to MSSM, but:

- ⇒  $\widehat{\Phi}$  identified as same field as  $\nu^c$
- ⇒ violates  $L$  explicitly
- ⇒ violates  $R_p$  explicitly
- ⇒ for heavy singlets approaches explicit bilinear model
- ⇒ For one  $\widehat{\nu}^c$ :  $m_\nu = \text{Tree} + \text{Loop}$
- ⇒ More than one  $\widehat{\nu}^c$  all  $m_{\nu_i}$  at tree-level

Lopez-Fogliani & Munoz, 2006

Escudero et al., 2008

Ghosh & Roy, 2009

Bartl et al., 2009

# Distinguish $R_p$ models?

Bartl et al., 2009

	Displaced vertex	Comment	Br(invisible)	Higgs decays
$b\text{-}R_p$	Yes	Visible	$\leq 10\%$	standard
$s\text{-}R_p$	Yes/No (short)	anti-correlates with invisible	any	non-standard (invisible)
$\mu\nu\text{SSM}$	Yes/No (long)	anti-correlates with non-standard	$\leq 10\%$	non-standard

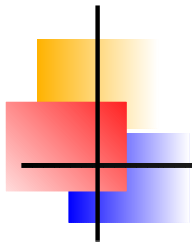
Note:

$\Rightarrow$  All models approach explicit  $R_p$  if new singlet fields “heavy”

$\Rightarrow$  Correlation with neutrino angles lost if trilinear  $R_p$  sizeable

... unless  $m_{\chi_1^0} > m_W$  + displaced vertex allows  $m_{\chi_1^0}$  reconstruction



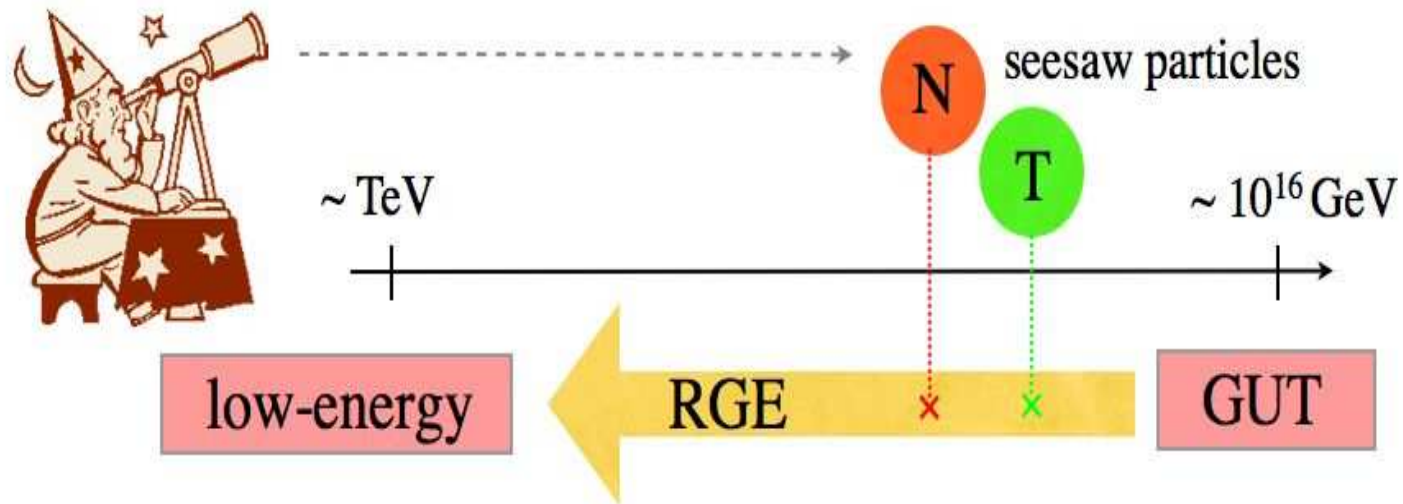


$\nu$ .

# Supersymmetric Seesaw

(Indirect signals for seesaw)

# Can we extrapolate from LHC to $M_{GUT}$ ?





# *mSugra and RGEs*

---

mSugra defined by:

$$m_0, M_{1/2}, A_0, t_\beta, \text{sgn}(\mu)$$

⇒ No LFV in pure mSugra

Add Seesaw type-I:

Borzumati & Masiero, 1986

$$(\Delta M_{\tilde{L}}^2)_{ij} \sim -\frac{1}{8\pi^2} f(m_0, A_0, \dots) (Y_\nu^\dagger L Y_\nu)_{ij}$$

$$(\Delta M_{\tilde{E}}^2)_{ij} \simeq 0$$

Note:  $L_i = \log[M_G/M_{R_i}]$ .

Or Seesaw type-II:

Rossi, 2002

$$(\Delta M_{\tilde{L}}^2)_{ij} \sim -\frac{1}{8\pi^2} g(m_0, A_0, M_{1/2}, \dots) (Y_T^\dagger Y_T)_{ij} \log(M_G/M_T)$$

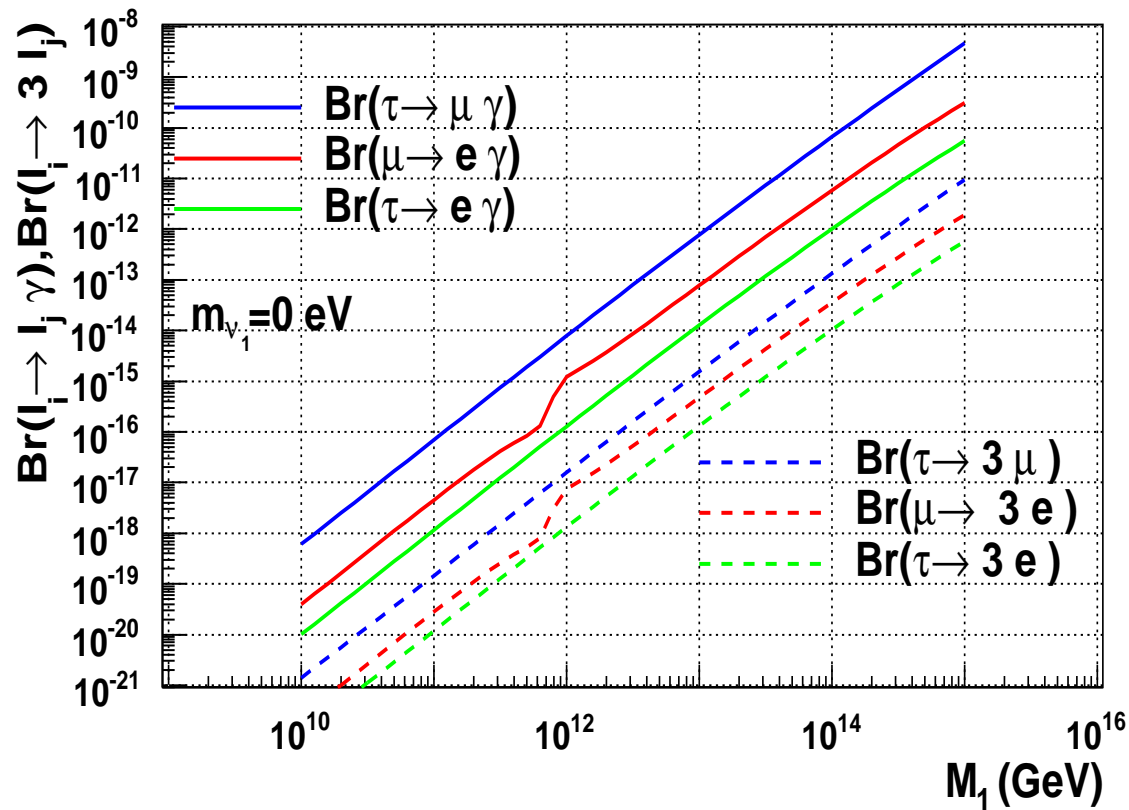
$$(\Delta M_{\tilde{E}}^2)_{ij} = 0$$

⇒ Learn about  $\hat{M}_R$  or  $M_T$  from  $(\Delta M_{\tilde{L}}^2)_{ij}$

# Numerical results: SPheno3

Example: Seesaw-I, SPS3

Calculated assuming: (i) Degenerate  $N^c$ , (ii) TBM angles, (iii) best fit  $\Delta m_{\Delta}^2$  and  $\Delta m_{\odot}^2$ , (iv)  $m_{\nu_1} \equiv 0$ :



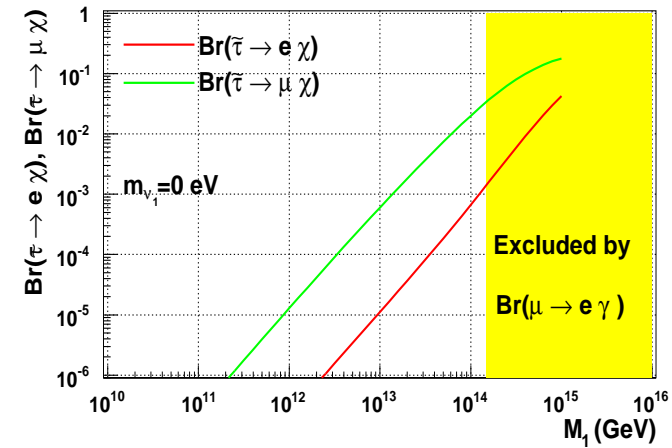
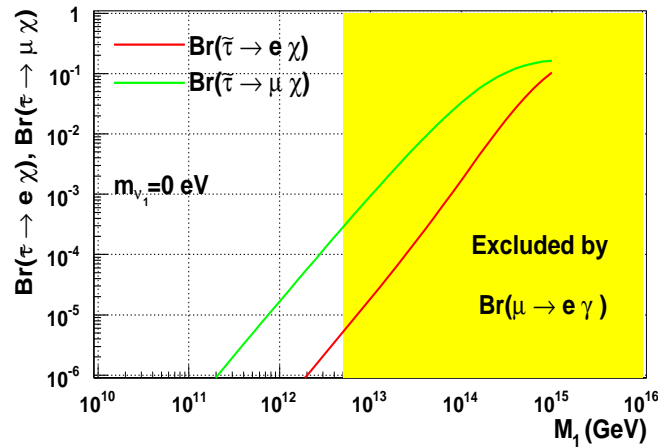
⇒ Ratios constant as function of seesaw scale!

# Numerical results: LHC

Seesaw-I:

Left: SPS1a'

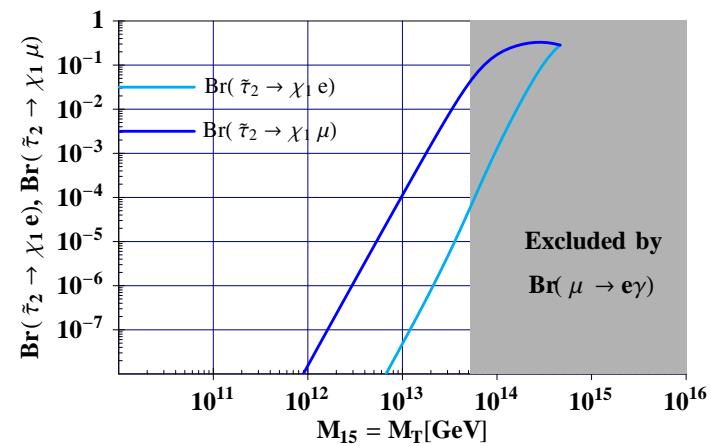
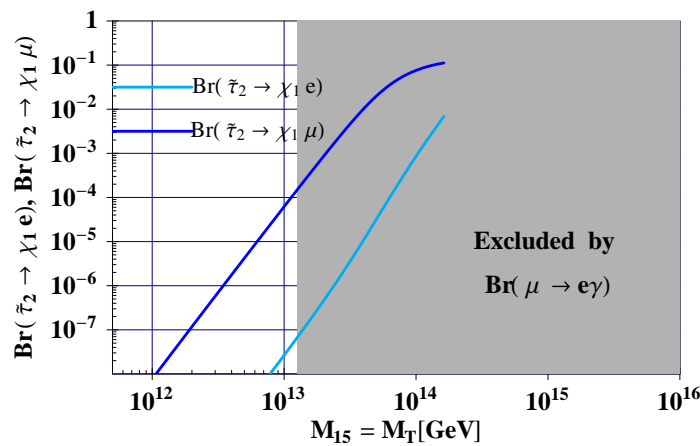
Right: SPS3



Seesaw-II:

Left: SPS1a'

Right: SPS3



⇒ LHC can see LFV (if SPS3-like ...)

Hirsch et al. 2008



# $V_{\text{soft}}$ & *the seesaw-II scale*

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RGEs allow to calculate low-scale SUSY masses. Example:

$$m_{\tilde{L}}^2 \simeq m_0^2 + 0.5M_{1/2}^2$$

Blair, Porod  
& Zerwas, 2003

$$m_{\tilde{E}}^2 \simeq m_0^2 + 0.15M_{1/2}^2$$

Buckley &  
Murayama, 2006

$$M_1 \simeq 0.45M_{1/2}$$

Form “invariants”:

$$(m_{\tilde{L}}^2 - m_{\tilde{E}}^2)/M_1^2 \simeq 1.7$$

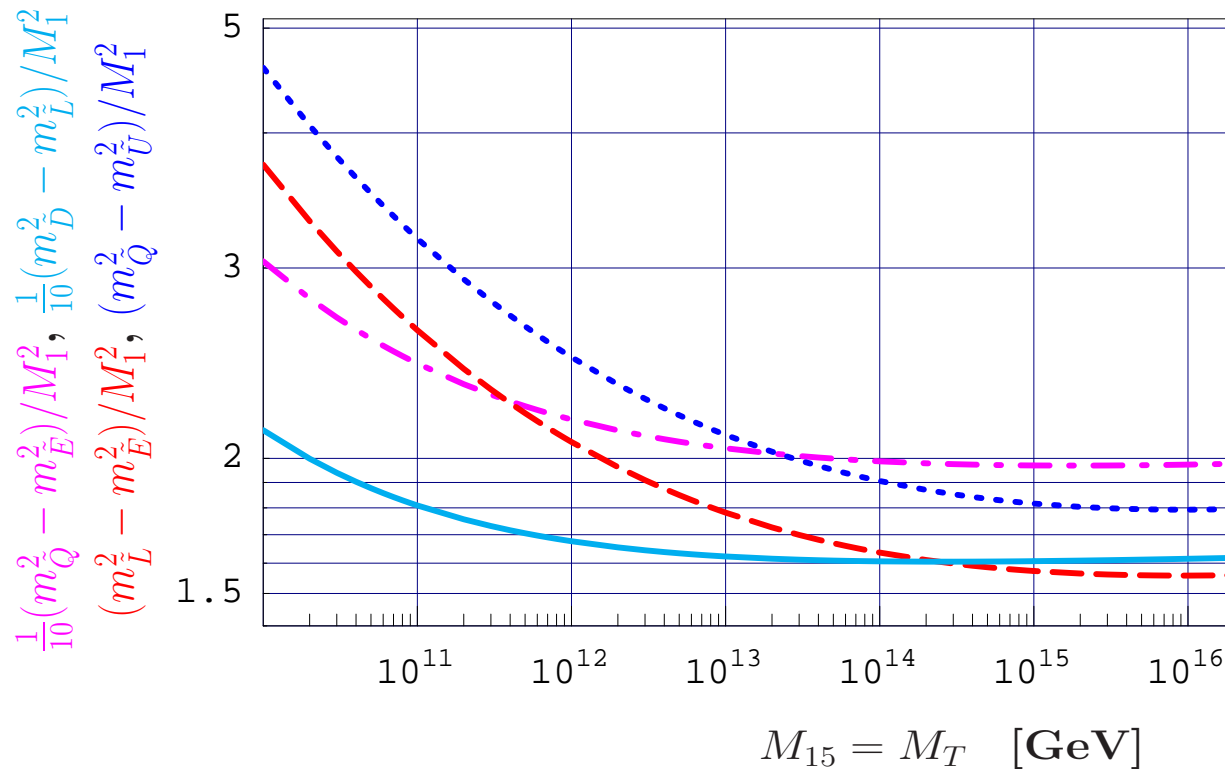
Idea!

⇒ To first approximation **no dependence** on  $m_0$  and  $M_{1/2}$

⇒ **Departure** from mSugra expectation contains **info on high energy physics!**

# Soft masses and seesaw-II

Four examples of “invariants” as function of  $M_{15} = M_T$ :



Analytic  
1-loop  
leading-log  
approximation

Hirsch et al., 2008

⇒ Consistent departures from mSugra point to  $M_T$

⇒ Dependence on  $M_T$  only  $\log(M_T)$



# Conclusions

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## II. “Low-scale” seesaw

Seesaw-I: (most probably) hopeless

Seesaw-II: **LNV**, up to  $m_{\Delta} \sim 1$  TeV

Seesaw-III: **Displaced vertex**, up to  $m_{\Sigma} \sim 1$  TeV

## III. Radiative neutrino mass models

LQs up to 1.5 TeV;  $k^{++}$  up to 800 GeV;  $h^+ / S^0$  (few) 100 GeV;

$\theta_{\nu}$  correlate with decay properties

## IV. $R_p$ Supersymmetric neutrino masses

LSP decays;  $\chi_1^0$  with **displaced vertex** up to  $M_{1/2} = 1$  TeV

$\theta_{\nu}$  correlate with decay properties

## V. High-scale Seesaw and SUSY

LFV decays as indirect signals; precision measurements on masses for  $M_{LNV}$