

# Electroweak Physics at FCC-eh

**Electroweak Physics in ep**

**Data Simulation**

**Observables and Role of PDFs**

**Masses (W,Z,H,t)**

**Weinberg angle and its scale dependence**

**Light Quark Weak Neutral Current Couplings**

Daniel Britzger (DESY) and Max Klein (U Liverpool)  
for the LHeC/FCC-eh Study Group

Note:  
All FCC-eh  
results  
are work in  
progress  
and some  
of LHeC too

Contribution to the FCC Physics Week, CERN, 17. January, 2017

# Electroweak Effects in NC DIS Cross Section

$$\begin{aligned}
 \mathbf{F}_2^\pm &= F_2 + \kappa_Z(-v_e \mp Pa_e) \cdot F_2^{\gamma Z} + \kappa_Z^2(v_e^2 + a_e^2 \pm 2Pv_e a_e) \cdot F_2^Z \\
 x\mathbf{F}_3^\pm &= \kappa_Z(\pm a_e + Pv_e) \cdot xF_3^{\gamma Z} + \kappa_Z^2(\mp 2v_e a_e - P(v_e^2 + a_e^2)) \cdot xF_3^Z.
 \end{aligned}$$

$$\kappa_Z(Q^2) = \frac{Q^2}{Q^2 + M_Z^2} \cdot \frac{1}{4 \sin^2 \Theta \cos^2 \Theta} \quad v_f = i_f - e_f 2 \sin^2 \Theta \quad a_f = i_f$$

$$\begin{aligned}
 (F_2, F_2^{\gamma Z}, F_2^Z) &= x \sum (e_q^2, 2e_q v_q, v_q^2 + a_q^2)(q + \bar{q}) \\
 (xF_3^{\gamma Z}, xF_3^Z) &= 2x \sum (e_q a_q, v_q a_q)(q - \bar{q}),
 \end{aligned}$$

	$e^2$	$2ev$
u	4/9	2/9
d	1/9	2/9

NC:  $\gamma\gamma, \gamma Z, ZZ$ . Lepton beam helicity  $P$ ,  $M_Z$ ,  $v$  and  $a$  couplings, PV through  $va$

CC: pure weak cross section ( $G_F, M_W$ )  $\rightarrow$  3 independent variables, DIS: OMS

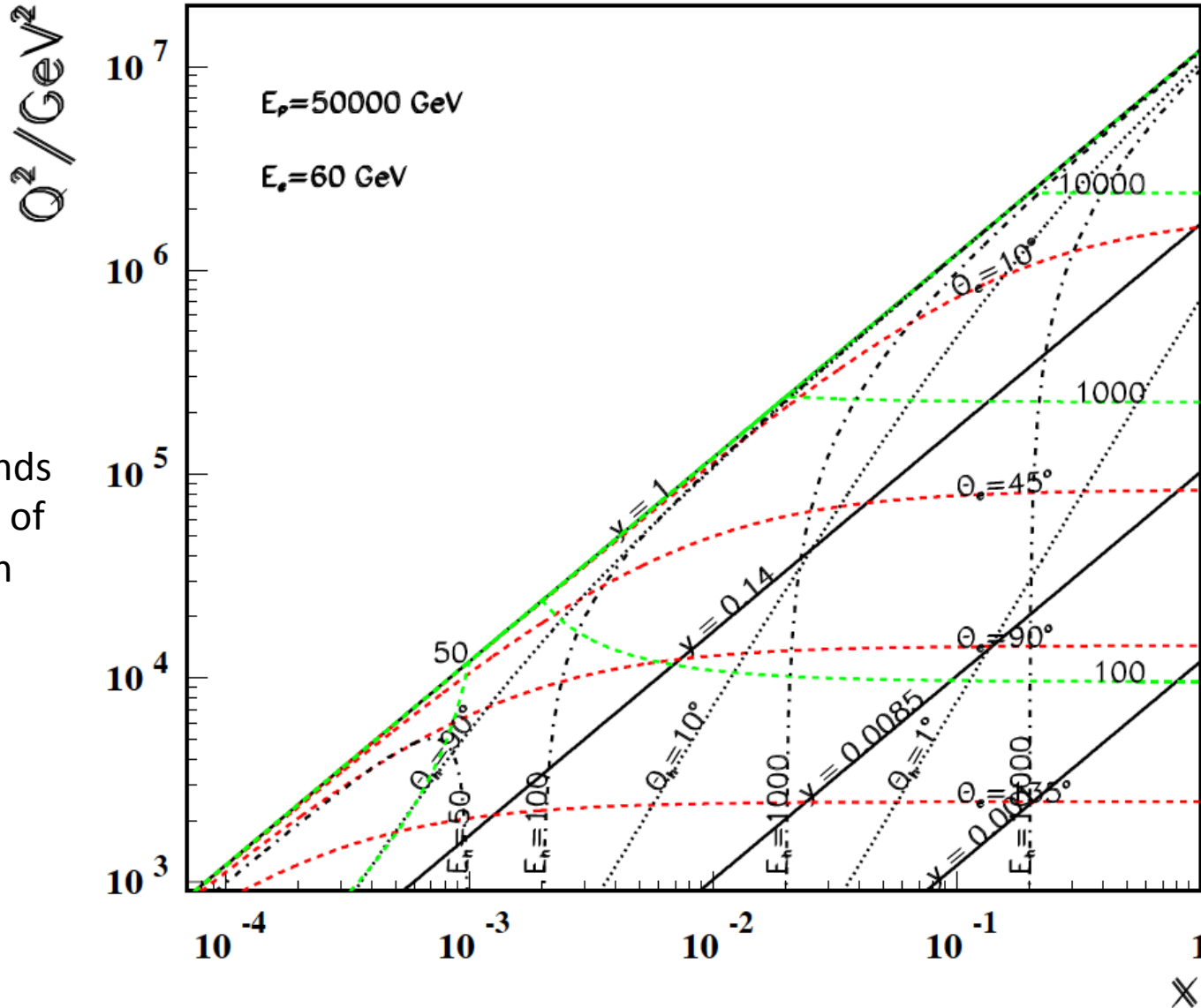
M. Klein and T. Riemann<sup>1</sup>

Institut für Hochenergiephysik der AdW der DDR, DDR-1615 Berlin-Zeuthen

Received 19 October 1983 Z. Phys. C - Particles and Fields 24, 151-155 (1984)

# Can we measure at high $Q^2$ ? Yes, we could!

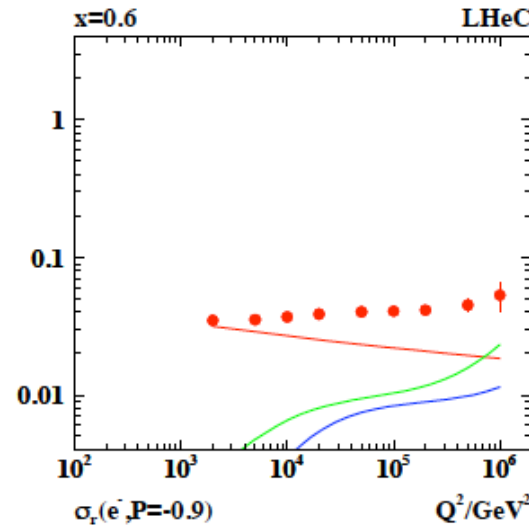
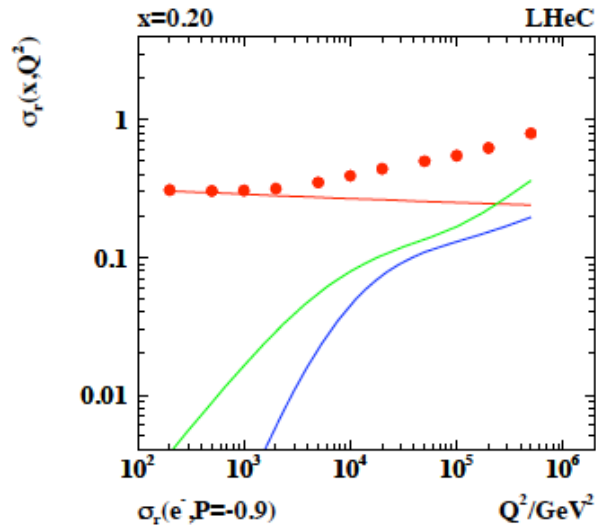
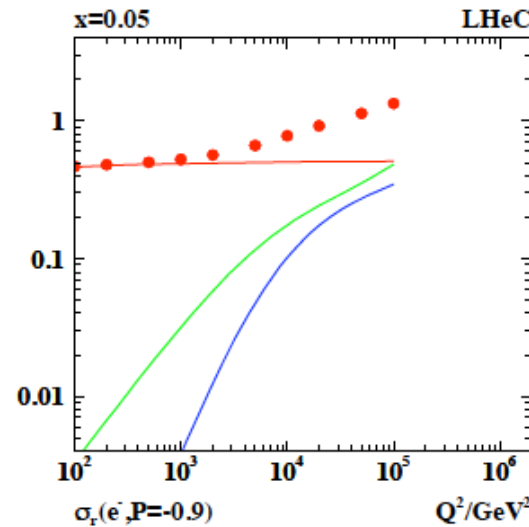
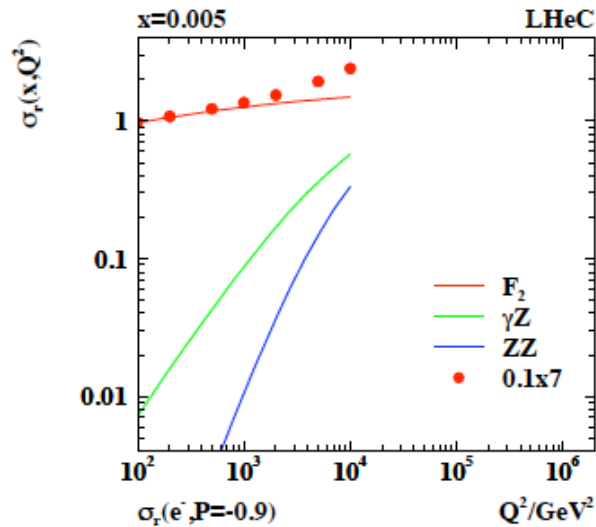
## Electroweak Physics Plane at FCC-eh



FCC-eh extends three orders of magnitude in  $Q^2$  beyond

$$Q^2 = M_Z^2 \rightarrow$$

# Reduced NC e-p Scattering Cross Section [ $P=-0.9, 10\text{fb}^{-1}$ ]



Huge Z exchange effects  
→

At small  $Q^2$ ,  $\sigma_r = F_2$

Both at  $x=0.2$  (the point of Bj scaling) and at larger  $x$  (the region of gluon bremsstrahlung which makes  $F_2$  decrease with  $Q^2$ ), the reduced NC cross section rises

## Polarisation Asymmetry and R=NC/CC

$$\frac{2}{P_L - P_R} \cdot A^\pm \simeq \mp \kappa_Z a_e \frac{F_2^{\gamma Z}}{(F_2 + \kappa_Z a_e Y_- x F_3^{\gamma Z} / Y_+)} \simeq \mp \kappa_Z a_e \frac{F_2^{\gamma Z}}{F_2}$$

$$\frac{2}{P_L - P_R} \cdot A^\pm \simeq \pm \kappa \frac{1 + d_v/u_v}{4 + d_v/u_v}$$

Classic asymmetry (Prescott et al, 1978) accesses weak interaction,  $F_2^{\gamma Z}$  is a new, direct measure of valence quarks at high x

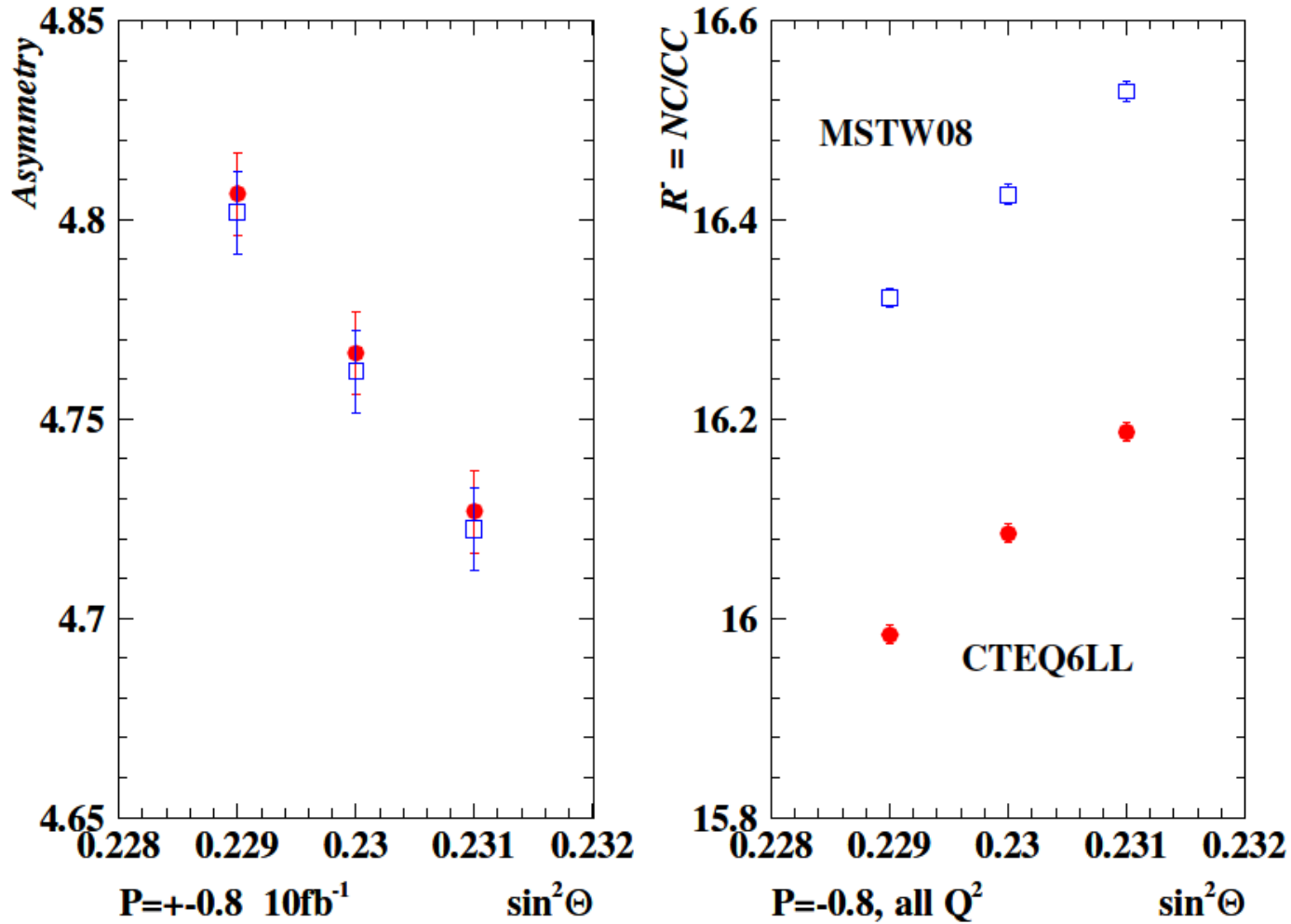
$$R^\pm = \frac{\sigma_{NC}^\pm}{\sigma_{CC}^\pm} = \frac{2}{(1 \pm P)\kappa_W^2} \cdot \frac{\sigma_{r,NC}^\pm}{\sigma_{r,CC}^\pm}$$

$$R^\pm \simeq \frac{2a_e^2}{(1 \pm P)\cos^2 \Theta} \cdot \frac{Y_+ F_2^Z - Y_- P x F_3^Z}{Y_+ W_2^\pm + Y_- x W_3^\pm}$$

R accesses weak interaction and the pure weak structure functions which are best measured at the FCC-eh

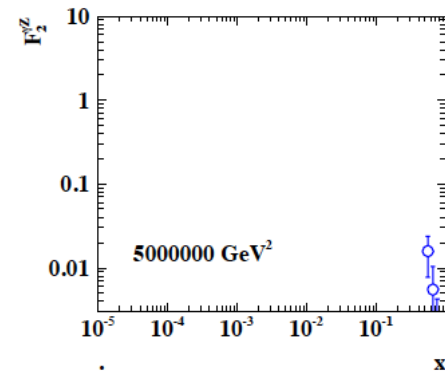
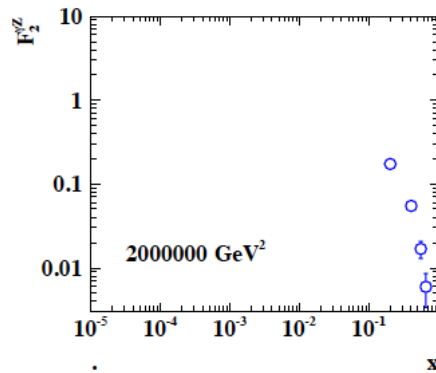
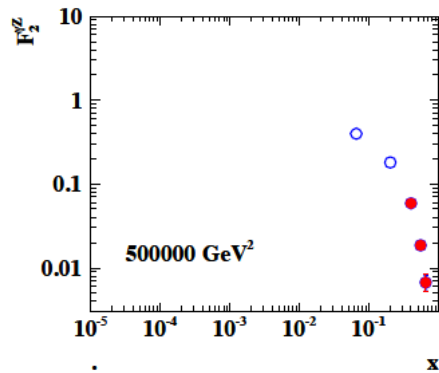
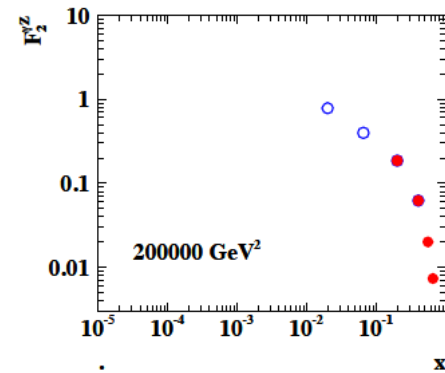
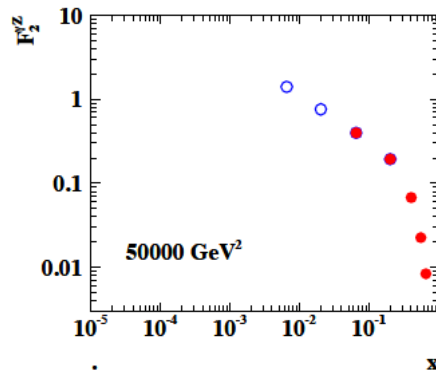
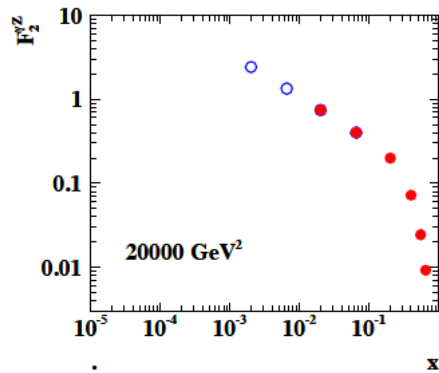
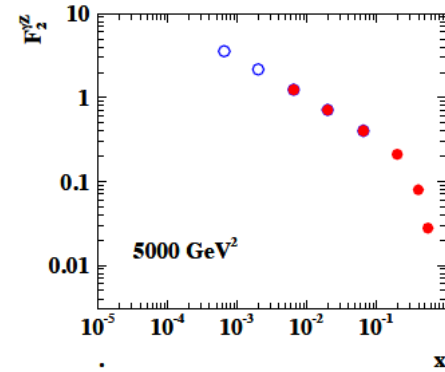
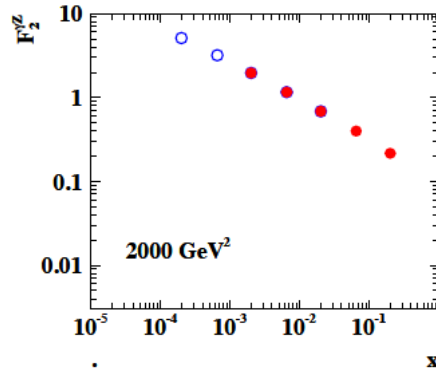
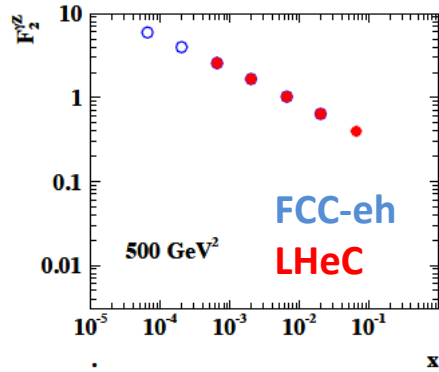
Note that in experiment you would measure the cross sections and determine all correlations which is still more informative than A or R but contains their physics.

# Polarisation Asymmetry and $R=NC/CC$

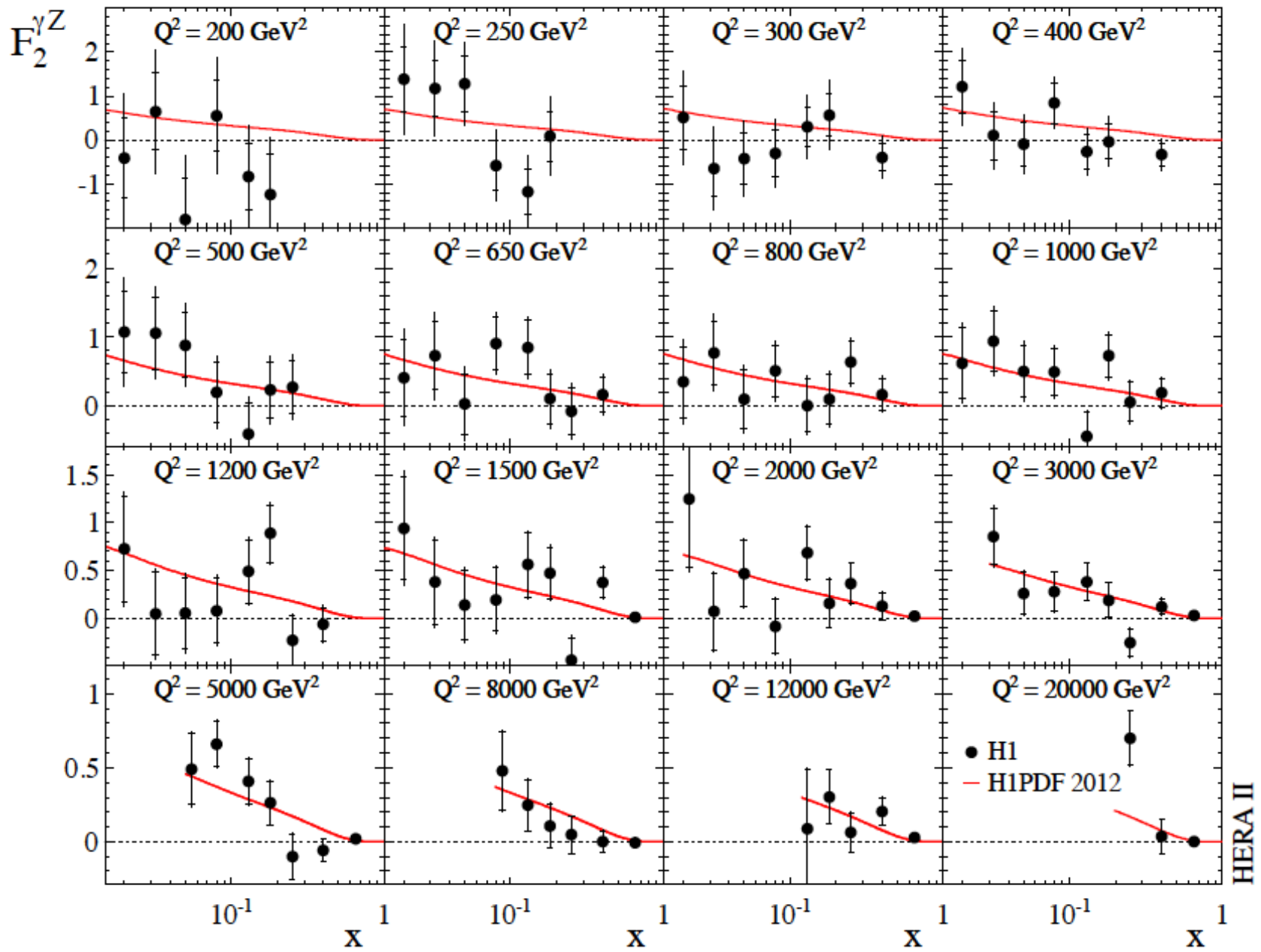


Strong sensitivity to Glashow's Weinberg angle. PDF effects to R largely an artefact

# Parity Violation Structure Function $F_2^{yZ} = x \sum 2 e_q v_q (q + \bar{q})$



**LHeC: 7 TeV, FCC-eh: 50 TeV,  $E_e=60$  GeV, integrated L of  $100 \text{ fb}^{-1}$  for  $P= \pm 0.8$**



H1: arXiv:1207.7007: much smaller  $x$  and  $Q^2$  range, imprecise, but first measurement ever



# Data (NC,CC) Simulation for QCD + el.weak Evaluation

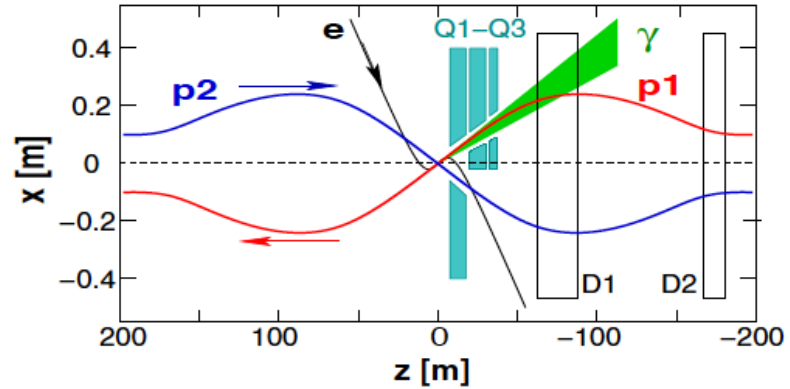
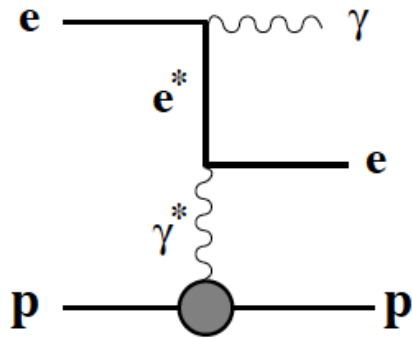
Numerical treatment of correlated and uncorrelated systematic and statistical errors  
[based on PHE-1990-02 (J.Blümlein, M.Klein), cross checked with H1 Monte Carlo]

source of uncertainty	error on the source or cross section
scattered electron energy scale $\Delta E'_e/E'_e$	0.1 %
scattered electron polar angle	0.1 mrad
hadronic energy scale $\Delta E_h/E_h$	0.5 %
calorimeter noise (only $y < 0.01$ )	1-3 %
radiative corrections	0.5%
photoproduction background (only $y > 0.5$ )	1 %
global efficiency error	0.7 %

- Assumptions gauged with H1, probably conservative.
- This approach determines full set of uncorrelated and correlated uncertainties
- ALL PDFs and electroweak fit results presented to this workshop have full systematic error
- This also holds for the LHeC CDR alphas analysis leading to 0.1-0.2% total uncertainty

# Luminosity measurement at the LHeC

CDR  
 JPhysG39  
 075001(12)  
 p561-566



Method	Stat. error	Syst.error	Systematic error components	Application
BH ( $\gamma$ )	0.05%/sec	1–5%	$\sigma(E \gtrsim 10\text{GeV})$ acceptance, $A$ $E$ -scale, pileup	0.5% $10\%(1-A)$ 0.5 – 4% Monitoring, tuning, short term variations
BH ( $e$ )	0.2%/sec	3–6%	$\sigma(E \gtrsim 10\text{GeV})$ acceptance background $E$ -scale	0.5% 2.5 – 5% 1% 1% Monitoring, tuning, short term variations
QEDC	0.5%/week	1.5%	$\sigma(\text{el/inel})$ acceptance vertex eff. $E$ -scale	1% 1% 0.5% 0.3% Absolute $\mathcal{L}$ , global normalisation
NC DIS	0.5%/h	2.5%	$\sigma(y < 0.6)$ acceptance vertex eff. $E$ -scale	2% 1% 1% 0.3% Relative $\mathcal{L}$ , mid-term variations

LR: photon detector  
 ← acceptance 95%

→ Luminosity from  
 BH photons to 1%

BH to another order

... BH( $e$ ), QEDC,  $F_2$   
 as cross checks

Table 13.1: Dominant systematics for various methods of luminosity measurement.

# NC Cross Section Correlated Uncertainties ( $Q^2=20000 \text{ GeV}^2$ )

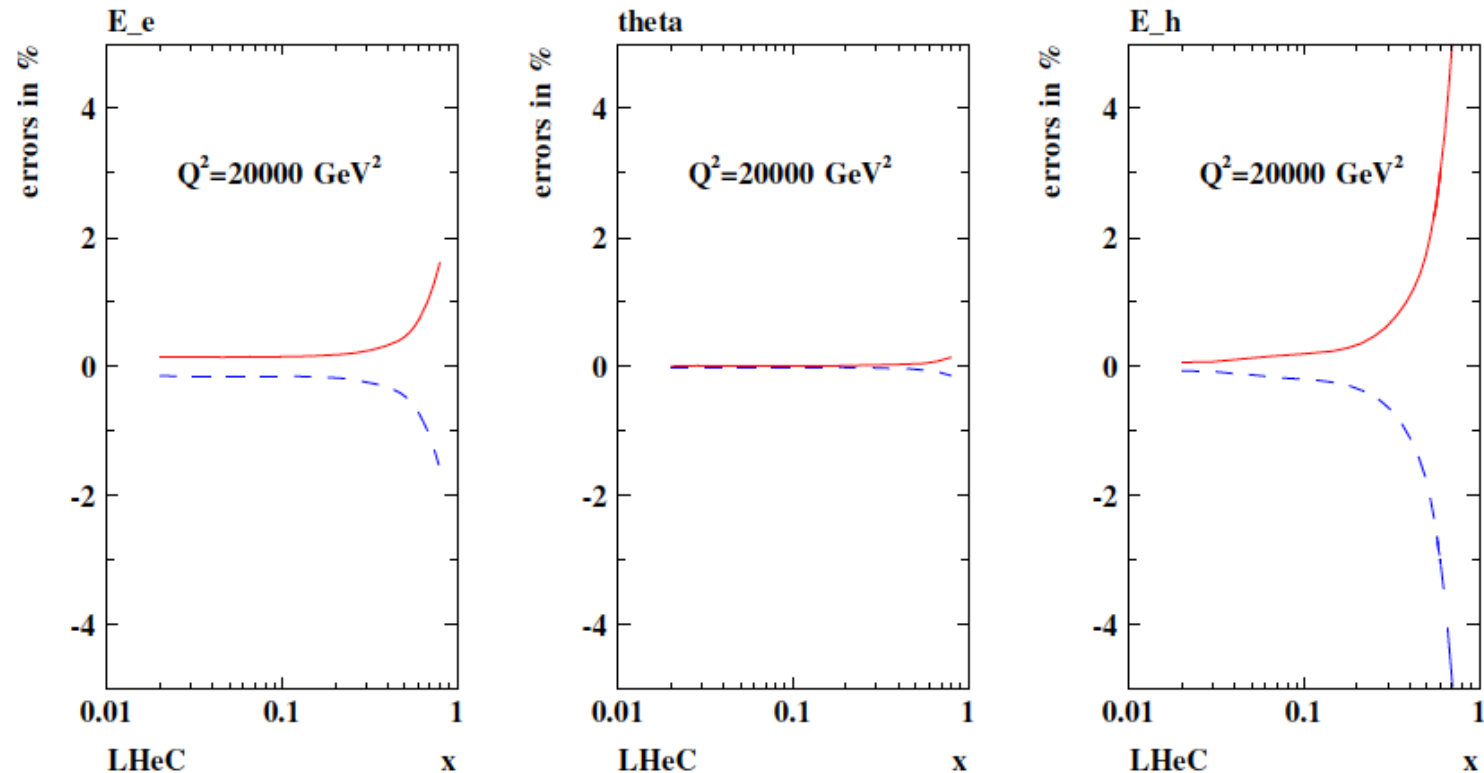


Figure 3.3: Neutral current cross section errors, calculated for  $60 \times 7000 \text{ GeV}^2$  unpolarised  $e^-p$  scattering, resulting from scale uncertainties of the scattered electron energy  $\delta E'_e/E'_e = 0.1\%$ , of its polar angle  $\delta\theta_e = 0.1 \text{ mrad}$  and the hadronic final state energy  $\delta E_h/E_h = 0.5\%$ , at large  $Q^2 = 20000 \text{ GeV}^2$  and correspondingly large  $x$ . Note that the characteristic behaviour of the relative uncertainty at large  $x$ , i.e. to diverge  $\propto 1/(1-x)$ , is independent of  $Q^2$ , i.e. persistently observed at  $Q^2 = 200000 \text{ GeV}^2$  for example too.

# NC Cross Section Correlated Uncertainties ( $Q^2=2 \text{ GeV}^2$ )

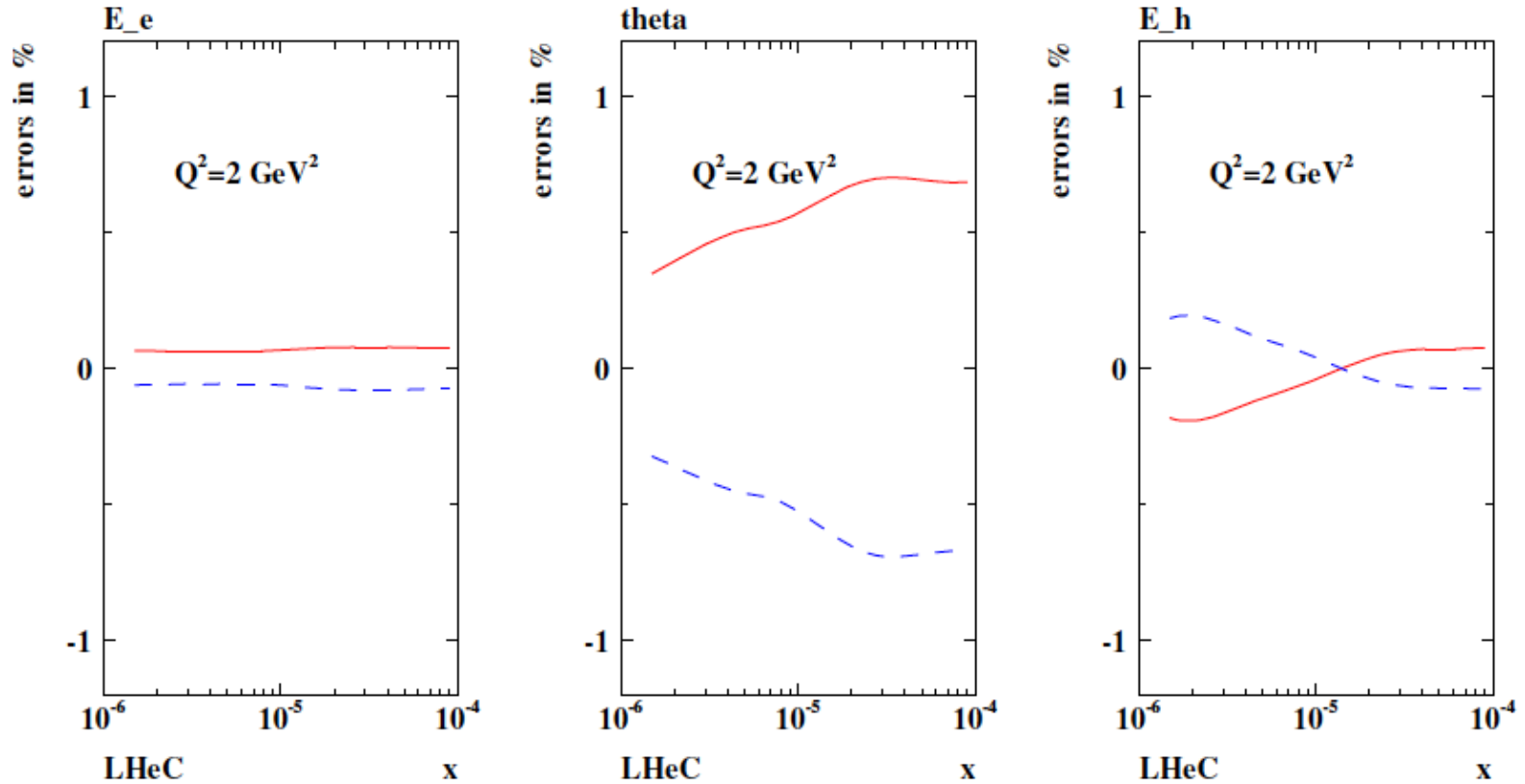


Figure 3.2: Neutral current cross section errors, calculated for  $60 \times 7000 \text{ GeV}^2$ , resulting from scale uncertainties of the scattered electron energy  $\delta E'_e/E'_e = 0.1 \%$ , of its polar angle  $\delta\theta_e = 0.1 \text{ mrad}$  and the hadronic final state energy  $\delta E_h/E_h = 0.5 \%$ , at low  $Q^2 = 2 \text{ GeV}^2$  and correspondingly low  $x$ .

# PDFs and their effect on electroweak physics

FCC-eh and LHeC: Input: high precision (stat+syst) data on  
Neutral Current ( $x: 10^{-6}-1; Q^2: 1-10^6$ ) Charged Current ( $10^{-4}-1; 100-10^6$ )  
Tagging of Charm and Beauty with high precision and coverage. ep (eD)

## Completely new PDF Programme

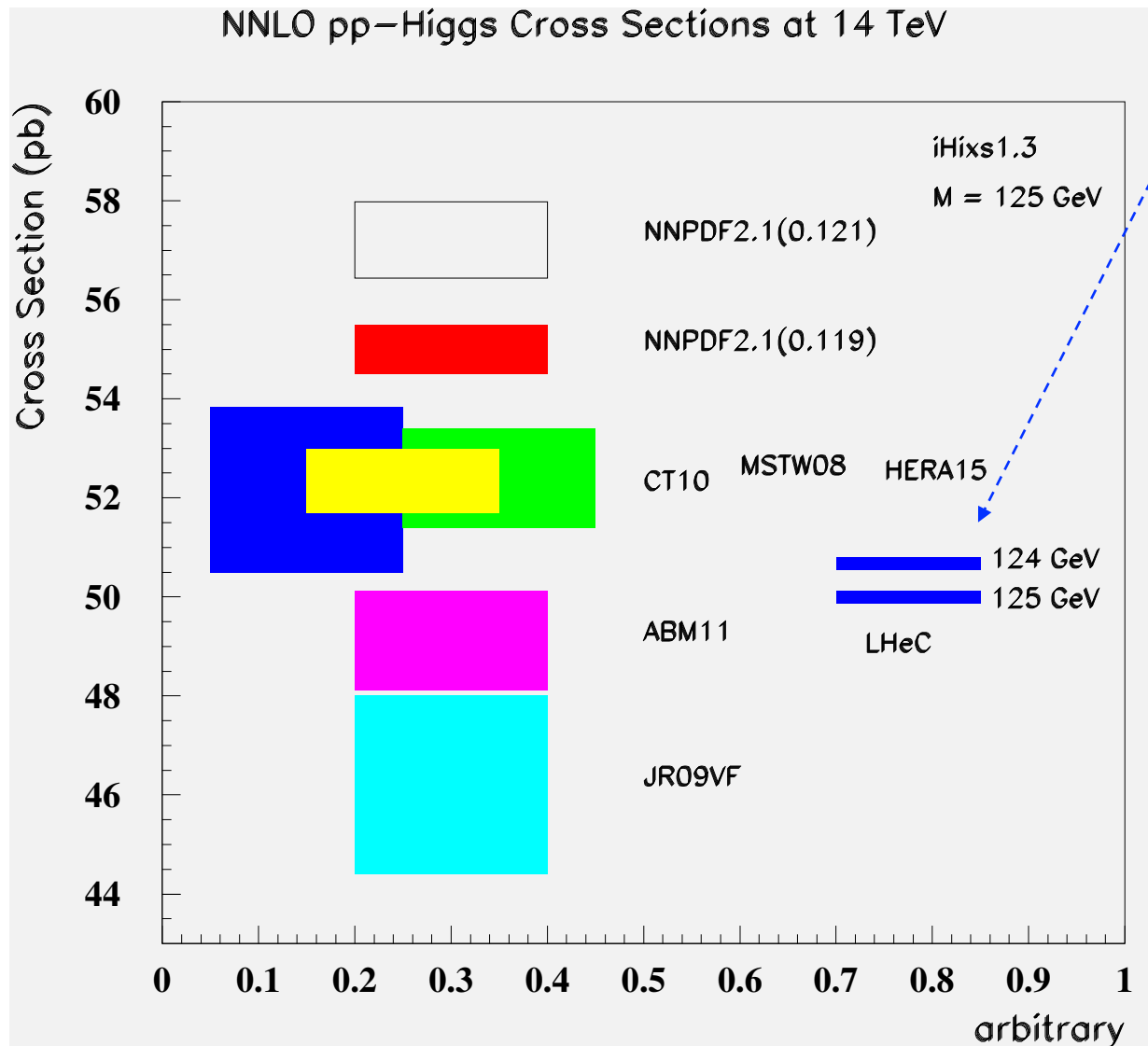
Determine ALL pdfs in a coherent way + the strong coupling to 0.1% accuracy  
No higher twists, no nuclear corrections, no symmetry assumptions, N<sup>3</sup>LO

→  $\bar{u}$ ,  $\bar{v}$ ,  $\bar{d}$ ,  $\bar{v}$ ,  $s$ ,  $c$ ,  $b$ ,  $t$ ,  $xg$  and  $\alpha_s$

**This essentially removes the PDF uncertainties on the electroweak variables, in ep but as well for pp.**

**For the Higgs this means that ep can turn pp into a precision Higgs facility**

# Precision PDFs for Higgs at the LHC



## LHeC:

Exp uncertainty of predicted H cross section is 0.25% (sys+sta), using LHeC only.

Leads to H mass sensitivity.

Strong coupling underlying parameter (0.005  $\rightarrow$  10%).  
LHeC: 0.0002 !

Needs N<sup>3</sup>LO

HQ treatment important ...

# Determination of EW parameters

## *On-mass shell scheme used for determination of EW-parameters*

- Inclusive NC and CC cross sections  
-> Only indirect determinations of mass parameters
- Explore experimental uncertainty (assume PDF to be known)
- PDF uncertainty (assume PDFs are determined together with the EW-parameters)

Uncertainty on EW parameters from inclusive DIS data

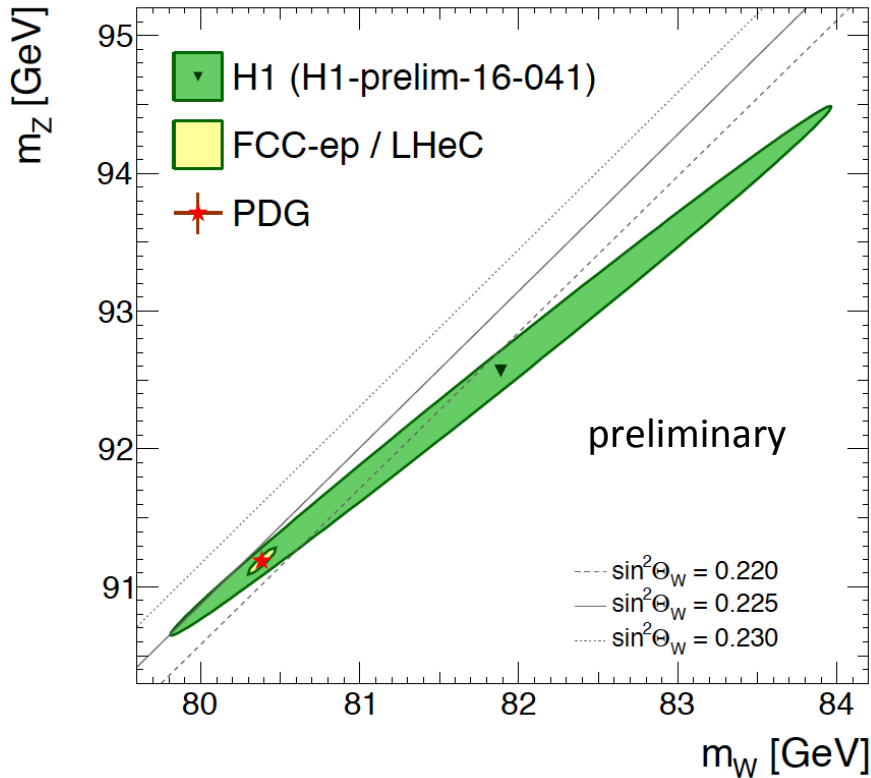
Parameter	HERA	LHeC	FCC	LHeC + FCC
$\Delta m_W$ [MeV]	$\pm 63_{(\text{exp})} 29_{(\text{pdf})}$	$\pm 14_{(\text{exp})} 10_{(\text{pdf})}$	$\pm 19_{(\text{exp})} 14_{(\text{pdf})}$	$\pm 11_{(\text{exp})} 6_{(\text{pdf})}$
$\Delta m_Z$ [MeV]	$\pm 56_{(\text{exp})} 25_{(\text{pdf})}$	$\pm 16_{(\text{exp})} 10_{(\text{pdf})}$	$\pm 23_{(\text{exp})} 14_{(\text{pdf})}$	$\pm 13_{(\text{exp})} 6_{(\text{pdf})}$
$\Delta m_t$ [GeV]	$\pm 10_{(\text{exp})} 5_{(\text{pdf})}$	$\pm 2.6_{(\text{exp})} 1.7_{(\text{pdf})}$	$\pm 3.2_{(\text{exp})} 2.1_{(\text{pdf})}$	$\pm 2.0_{(\text{exp})} 1.0_{(\text{pdf})}$
$\Delta m_H$ [GeV]	$> \mathcal{O}(100 \text{ GeV})$	$\pm 31_{(\text{exp})} 22_{(\text{pdf})}$	$\pm 38_{(\text{exp})} 25_{(\text{pdf})}$	$\pm 24_{(\text{exp})} 13_{(\text{pdf})}$
$\Delta g_f$ (MOMS) ( $10^{-8} \text{GeV}^{-2}$ )	$\pm 4.7_{(\text{exp})} 1.9_{(\text{pdf})}$	$\pm 1.9_{(\text{exp})} 1.2_{(\text{pdf})}$	$\pm 2.8_{(\text{exp})} 1.8_{(\text{pdf})}$	$\pm 1.6_{(\text{exp})} 0.7_{(\text{pdf})}$

$g_f$ : Calculation in  
'modified on-shell scheme'  
( $\alpha_{\text{em}}, m_Z, g_f, \Delta r$ )

## *LHeC and FCC*

- Greatly improve precision of HERA data
- Uncertainty on  $W$ -boson mass will become competitive to best-known value
- Correlation with PDF-determinations will not be the limiting factor !

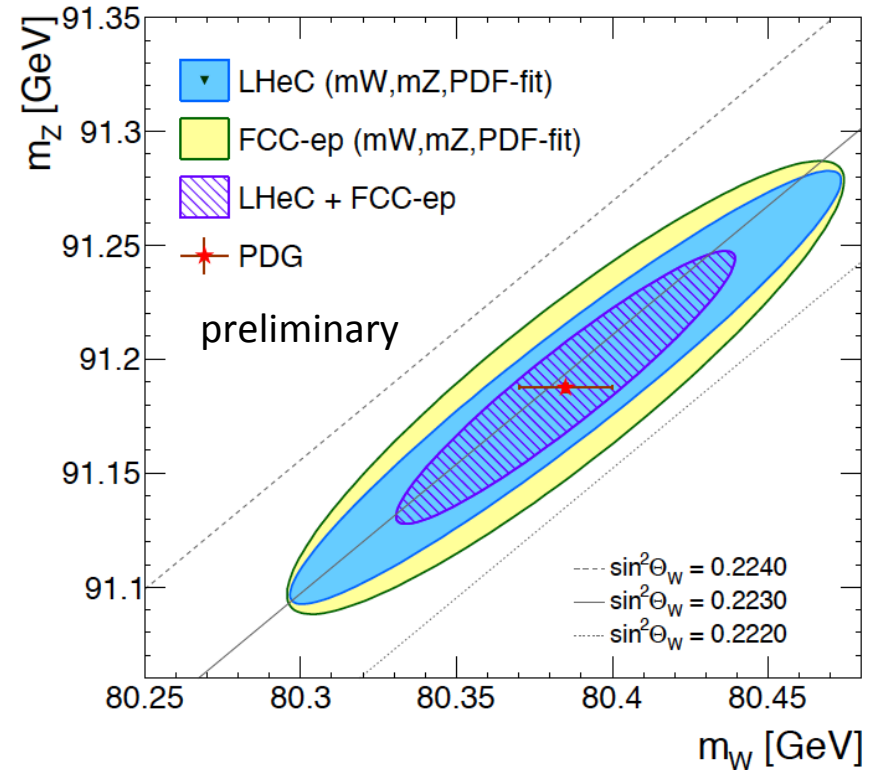
# Determination of W,Z Masses in Deep Inelastic Scattering with FCC-eh



Huge improvement wrt HERA due to higher energy and luminosity

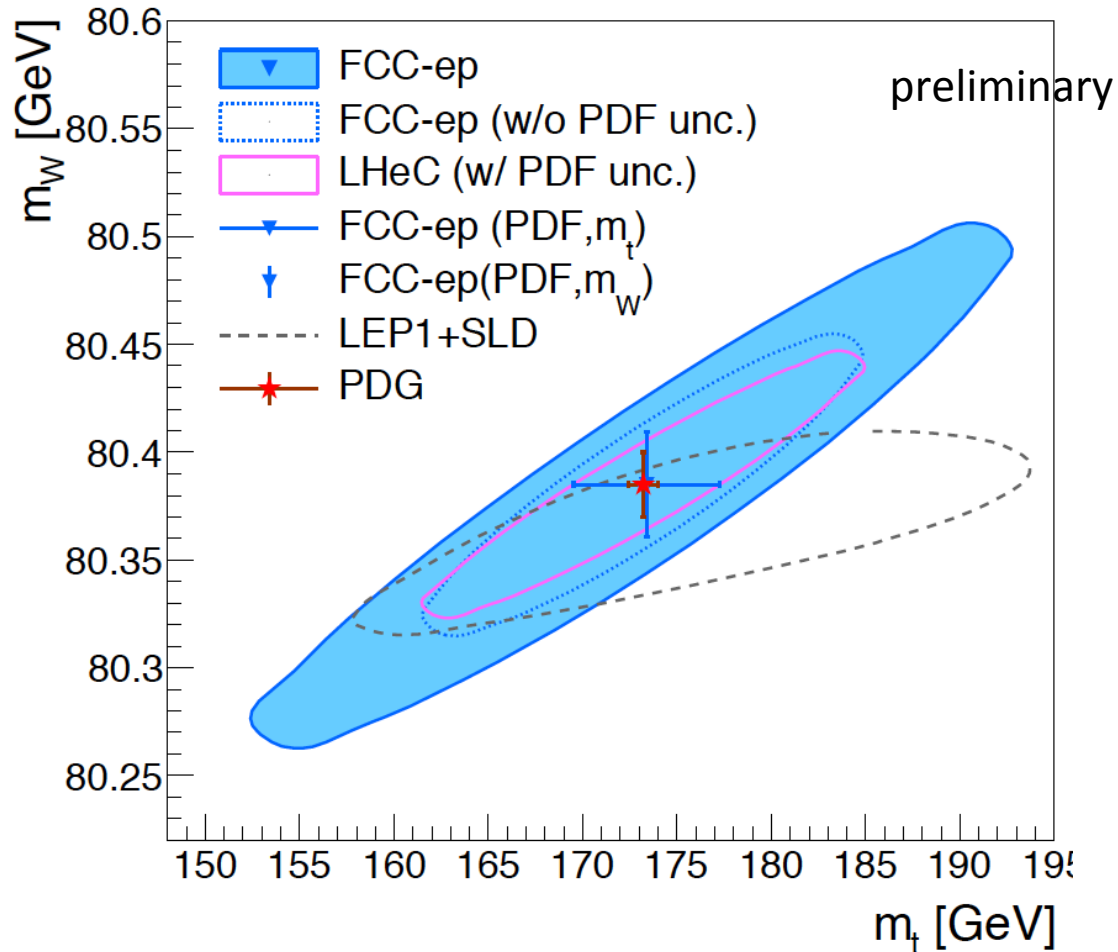
10 MeV  $m_W$  error important cross check through spacelike measurement comparable to pp but inferior precision to dedicated timelike ee measurement

An example study for how LHeC and FCC-eh would improve measurement precision





# W and Top Mass in DIS



Hugely improved wrt HERA. Precision comparable to LEP

FCC-eh (and LHeC) is a top factory. Therefore one can directly measure  $M_t$ , still to be studied

# Weak mixing angle

## Weak mixing angle

- Define  $\sin^2\theta_w$  in on-shell scheme

$$\sin^2\theta_w = 1 - \frac{m_W^2}{m_Z^2}$$

- No scale dependence in this definition

## On-shell value can be translated

- into 'effective' weak mixing angle
- into  $\overline{\text{MS}}$  definition

## Weak mixing angle

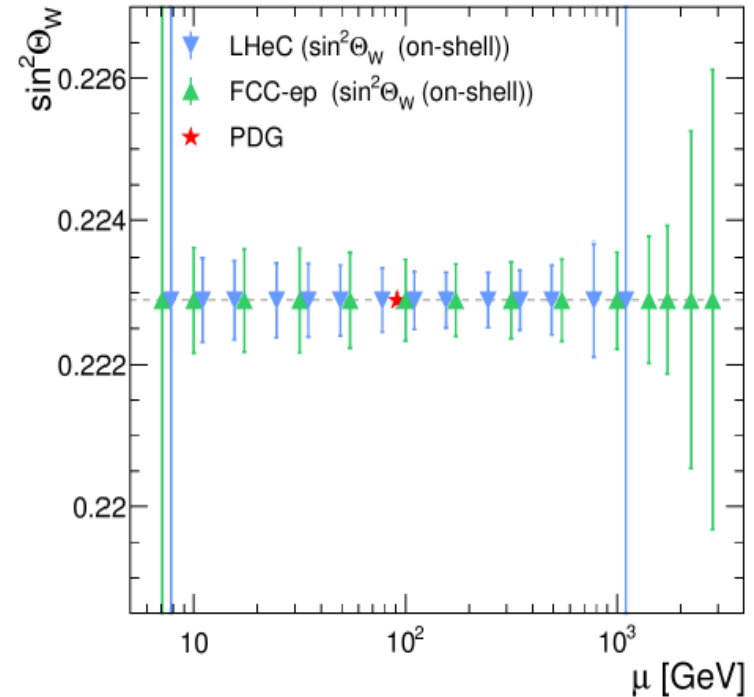
- Expected precision:

LHeC:  $\pm 0.0003$  (exp)  $0.0002$  (PDF)

FCC:  $\pm 0.0004$  (exp)  $0.0003$  (PDF)

- Inclusive data will only be somewhat competitive with the direct extractions at the Z-pole, but:

- Scale-dependence** of EW physics is studied up to TeV range
- Inclusive DIS data from LHeC and FCC probes scale dependence of EW theory in impressive range from **10 GeV up to highest accessible scales**

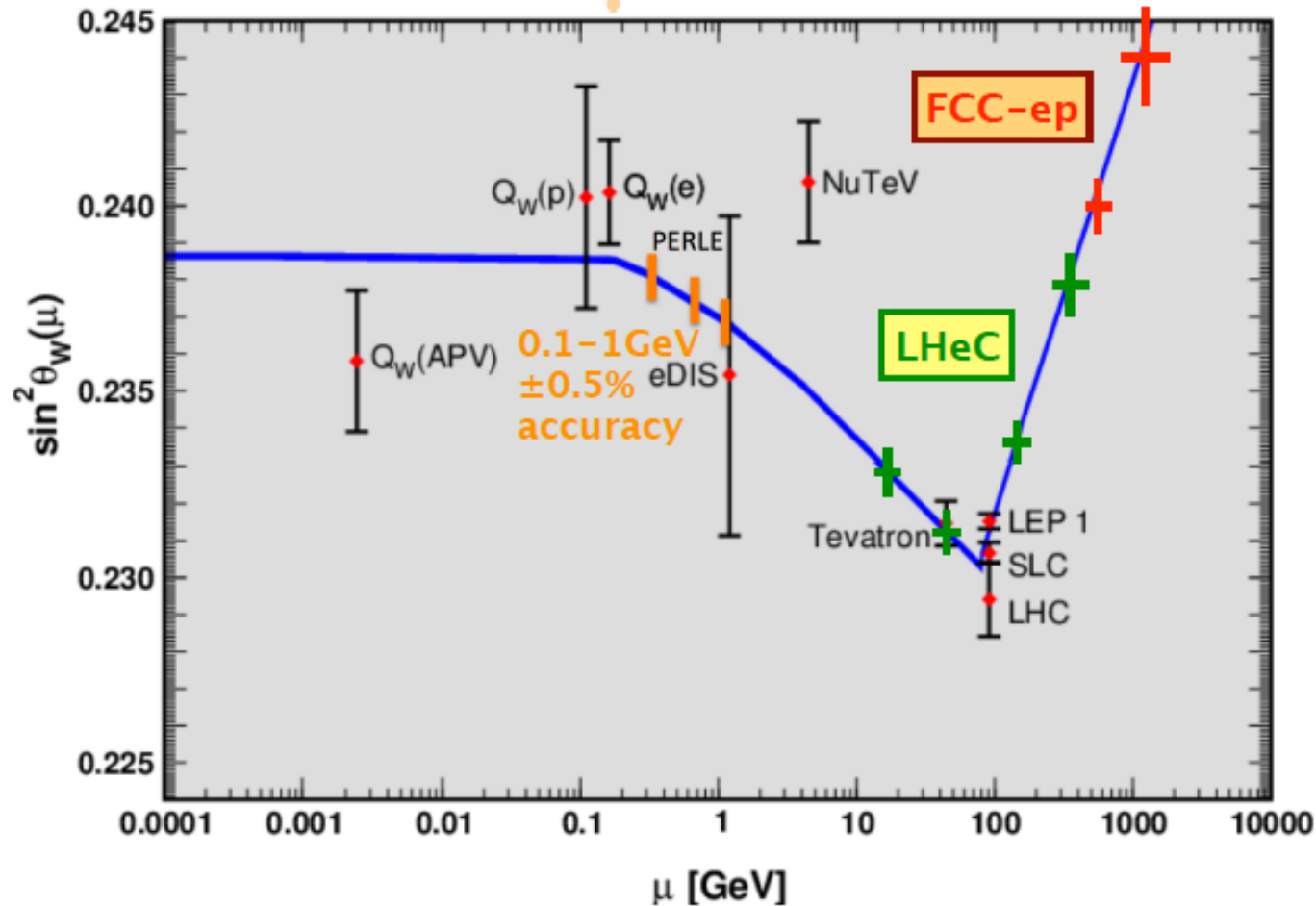


# Scale Dependence of $\sin^2\theta_W$

PERLE CDR, Arduini et al, to be published  
ICFA BeamNewsletter 68 (January 2016)

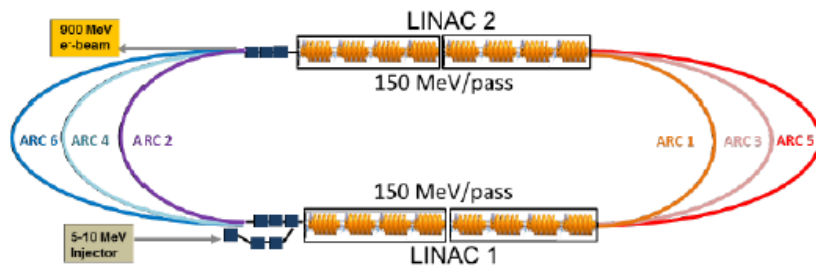


LHeC CDR,  
J.Phys. G39,  
075001 (2012)



Also  
MESA  
Jlab  
Exp's.

→ probe large range of scale dependence

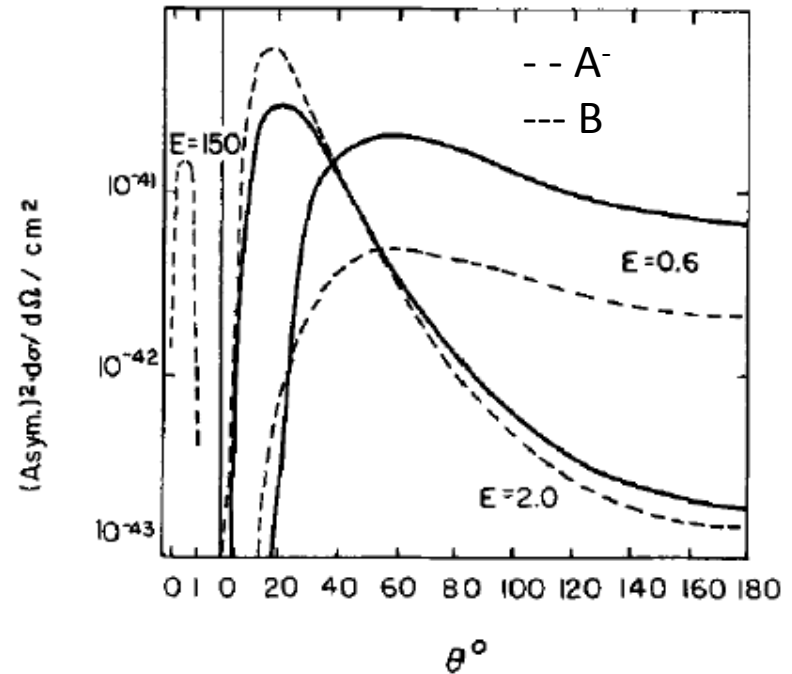


Conceptual Design Report

Draft 1.3 November 10<sup>th</sup>, 2016

CELIA Bordeaux, MIT Boston, CERN, Cockcroft and Astec  
 Daresbury, TU Darmstadt, U Liverpool, Jefferson Lab  
 Newport News, BINP Novosibirsk, IPNO and LAL Orsay

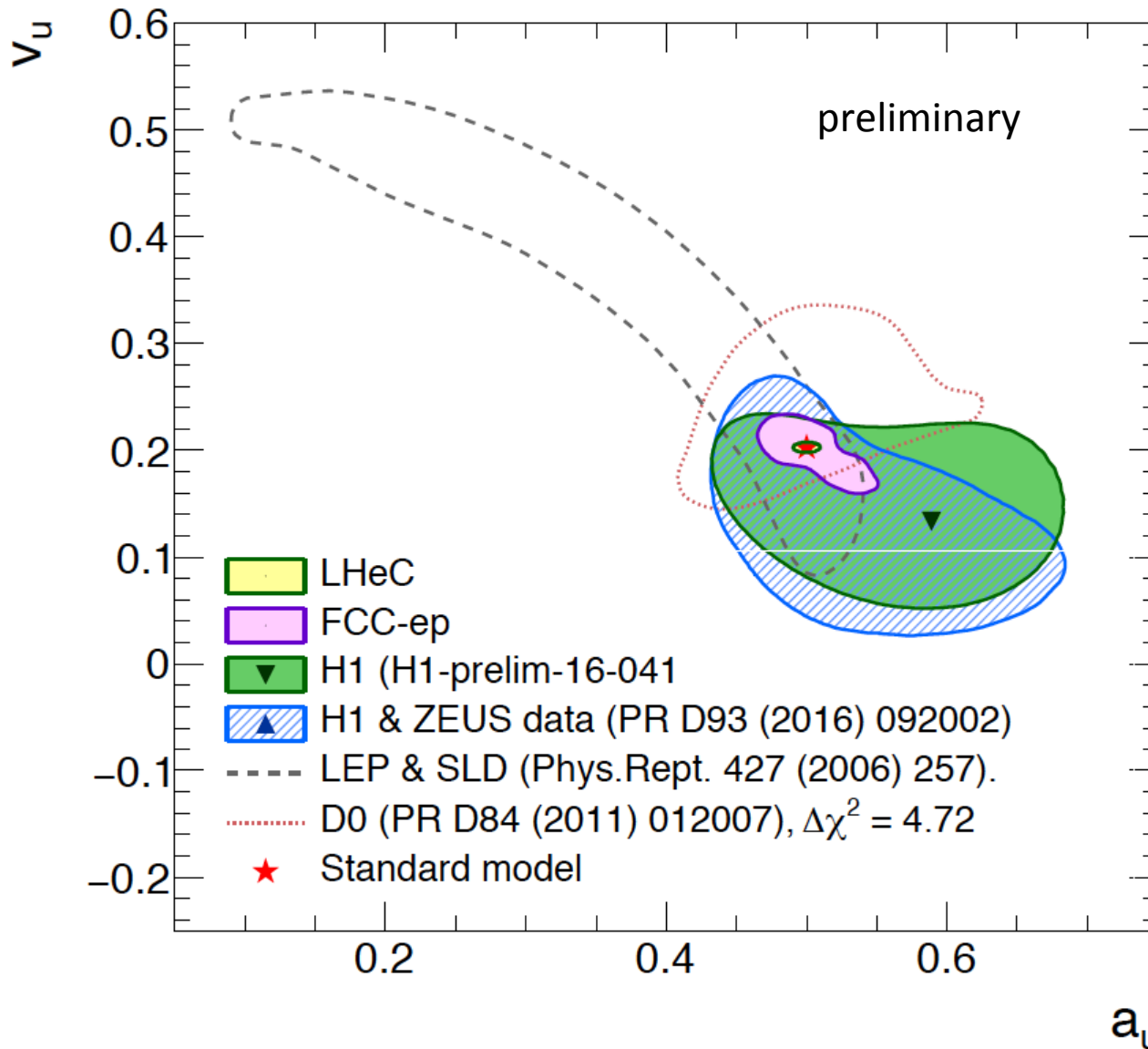
Potential to precisely measure  $\sin^2\Theta$  in elastic polarised ep scattering with high intensity ERL test facility.



Optimum signal conditions for  $E_e \approx 0.1$  GeV  
 M.Klein, T. Riemann Zphys C8(81)239

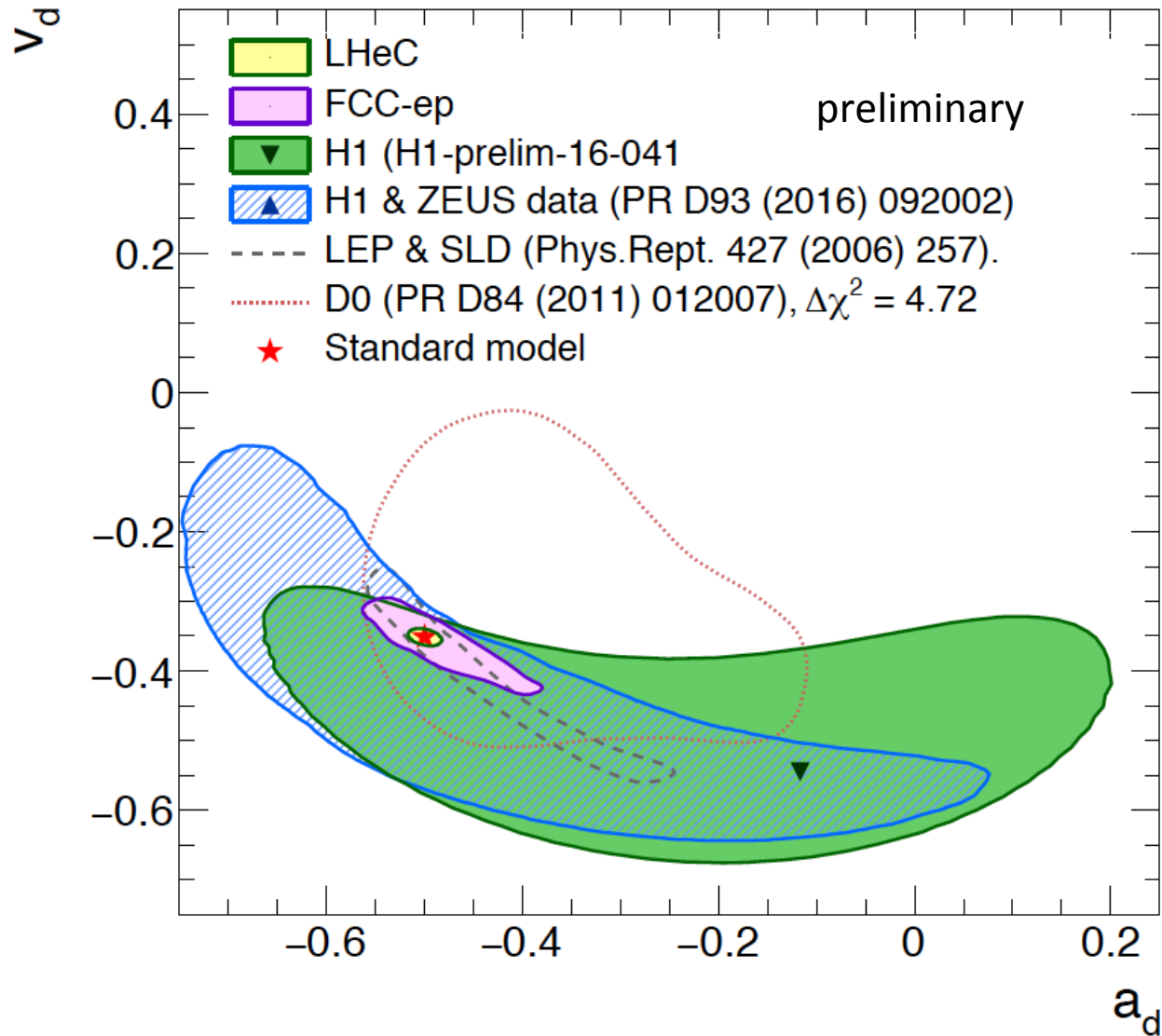
PERLE: 802 MHz 3 turns 15mA. TDR in 2017

# $v_u, a_u$ of up Quarks



Note: FCC-eh data set still needs to include  $P=+0.8$  data which for LHeC are considered

# $v_d, a_d$ of down Quarks



Note: FCC-eh data set still needs to include  $P=+0.8$  data which for LHeC are considered

# Summary

- First pass made on electroweak measurements with FCC-eh
- Very high precision with LHeC and FCC-eh:  $L=1000L(\text{HERA})$ , higher energy offers important and unique tests of eweak SM in the spacelike region
- Systematics included, probably somewhat conservative
- Through its own PDF programme, the  $p$  structure uncertainty effects on electroweak measurements at FCC-eh/LHeC is negligible. This is of crucial value also to LHC and FCC-hh measurements, especially Higgs physics
- Eweak effects for the first time can be used to probe nuclear structure
- In general the ew precision is (expected to be) less than that FCCee promises
- Of special value are the scale dependence of the mixing angle and the couplings of  $u,d$
- There is much more to be studied, for example: place of  $ep$  for EFT tests, final state ( $W,Z,t,H$  masses) or heavy quark couplings + signs through  $\gamma Z$

Electron-proton colliders open new horizons on all three of the fundamental questions: the spectroscopy of fundamental fermions, the spectroscopy of gauge bosons, and the problem of hadron structure. In addressing these issues, the ep collider is approaching the same physics as is studied in  $e^+e^-$  and  $\bar{p}p$  colliders, but in a complementary way, with emphasis on the t-channel. Each technique has its own strengths and weaknesses, which I leave you to contemplate.

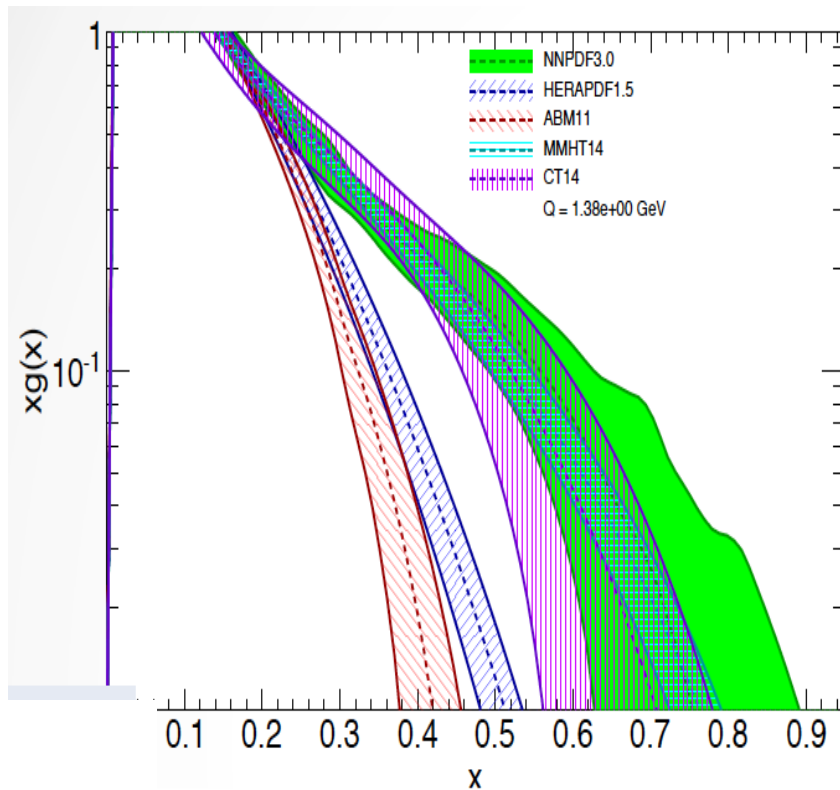
Chris Quigg  
Fermi National Accelerator Laboratory

FERMILAB-Conf-81/52-THY



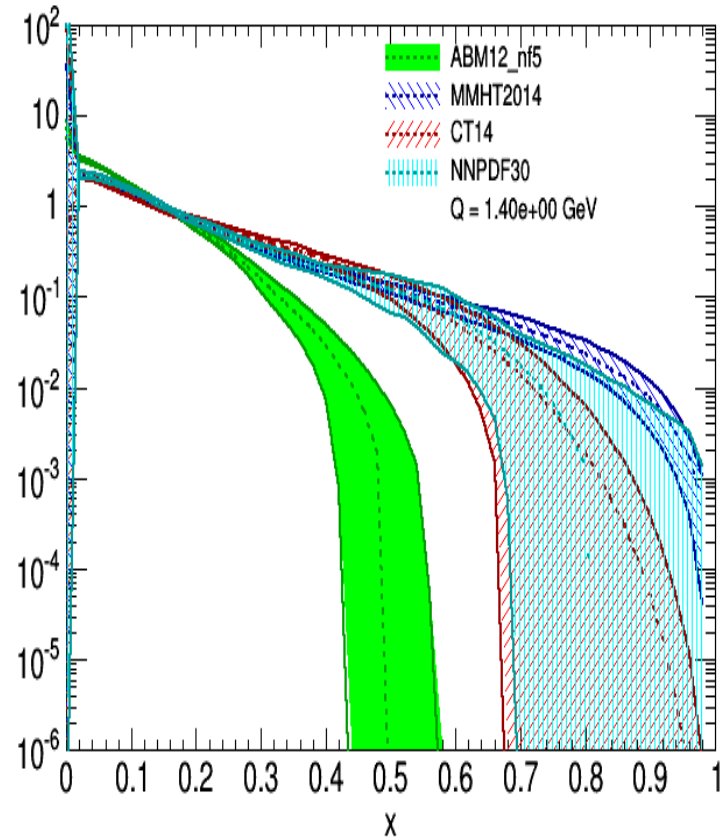


# Gluon Distribution at High x



Generated with APFEL 2.4.0 Web

$xg(x,Q)$ , comparison



Generated with APFEL 2.4.0 Web

Gluon at large  $x$  becomes very small and is hugely uncertain while  $M_x^2 = sx_1x_2 \dots$

**The determination of  $xg$  at large  $x$  is a severe challenge + not just for one channel**

# Strong Coupling Constant

-  $\alpha_s$  least known of coupling constants

Grand Unification predictions need smaller  $\delta\alpha_s$

- Is  $\alpha_s(\text{DIS})$  lower than world average (?)

- LHeC: per mille - independent of BCDMS!

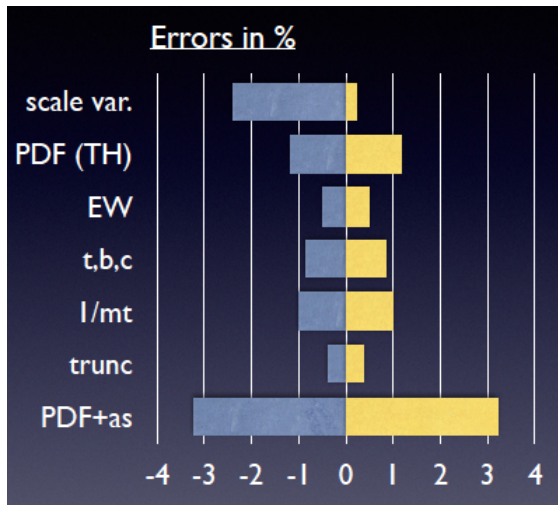
- High precision from inclusive data –  $\alpha_s(\text{jets})$ ??

- Challenge lattice QCD

LHeC simulation, NC+CC inclusive, total exp error

case	cut [ $Q^2$ in $\text{GeV}^2$ ]	relative precision in %
HERA only (14p)	$Q^2 > 3.5$	1.94
HERA+jets (14p)	$Q^2 > 3.5$	0.82
LHeC only (14p)	$Q^2 > 3.5$	0.15
LHeC only (10p)	$Q^2 > 3.5$	0.17
LHeC only (14p)	$Q^2 > 20.$	0.25
LHeC+HERA (10p)	$Q^2 > 3.5$	0.11
LHeC+HERA (10p)	$Q^2 > 7.0$	0.20
LHeC+HERA (10p)	$Q^2 > 10.$	0.26

Two independent QCD analyses using LHeC+HERA/BCDMS



## Uncertainty on Higgs cross section

Giulia Zanderighi, Vietnam 9/16,  
from C.Anastasiou et al, 1602.00695  
who also discuss the ABM  $\alpha_s$ .

