

# Supersymmetry at FCC

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Harvard University

1st FCC Physics Workshop  
CERN

[1606.00947]

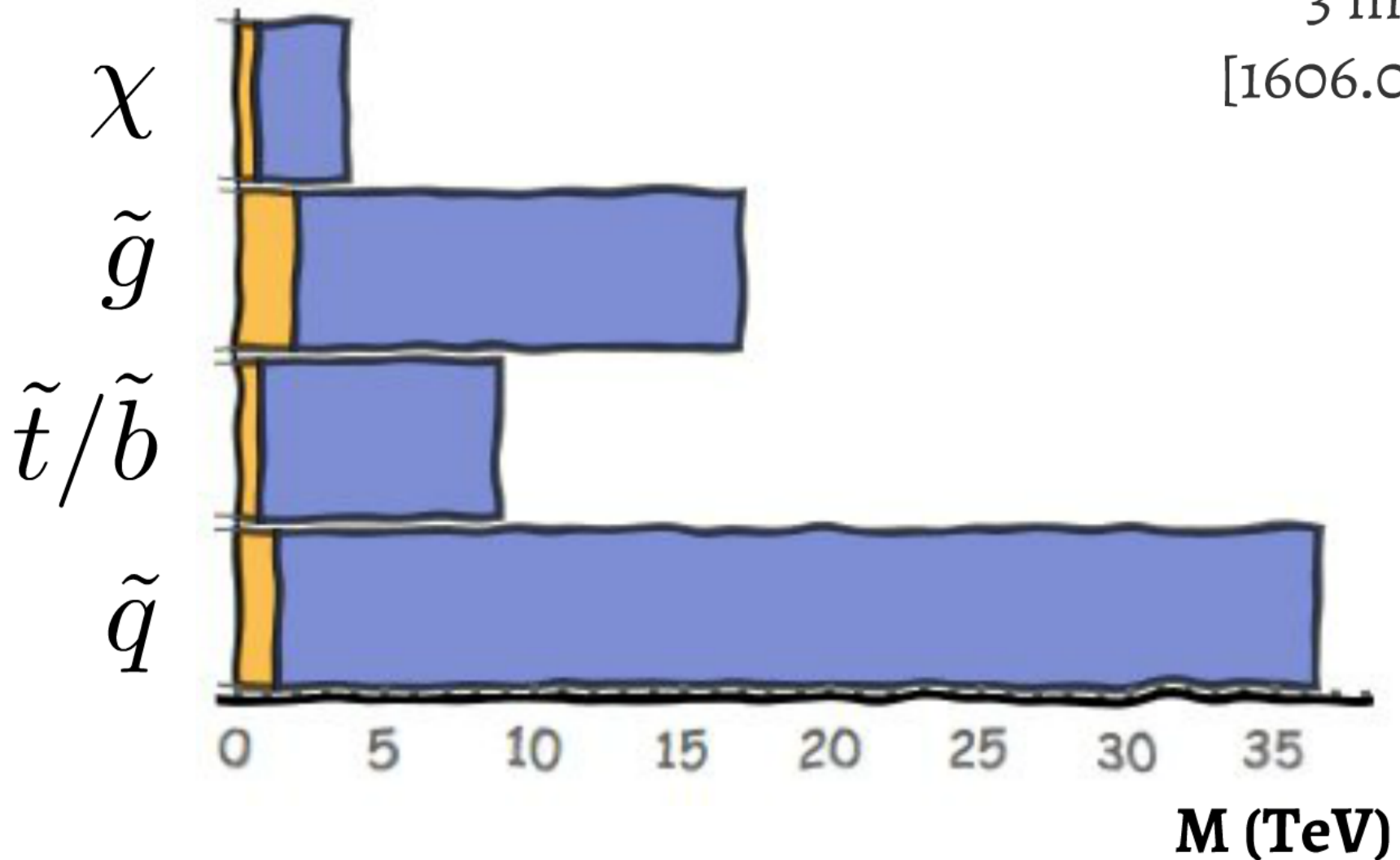
with Jiji Fan, Matt Reece, Wei Xue  
to appear

# SUSY searches

Current limits and discovery potential at FCC-hh

3 inv. ab

[1606.0094]



# Split Supersymmetry

## *Naturalness?*

A quantitative problem: prefer low scalar masses values

A new qualitative input: what holds down scalar scale then?

Flavor constraints prefer  $m_0 > 100\text{--}1000$  TeV

Dark Matter, unification still preserved for  $\sim\text{TeV}$   
gauginos

Scalar mass scale is not fixed

Arkani-Hamed, Dimopoulos  
[hep-th/0405159]  
Giudice, Romanino  
[hep-ph/0406088]

# The Higgs mass in the MSSM

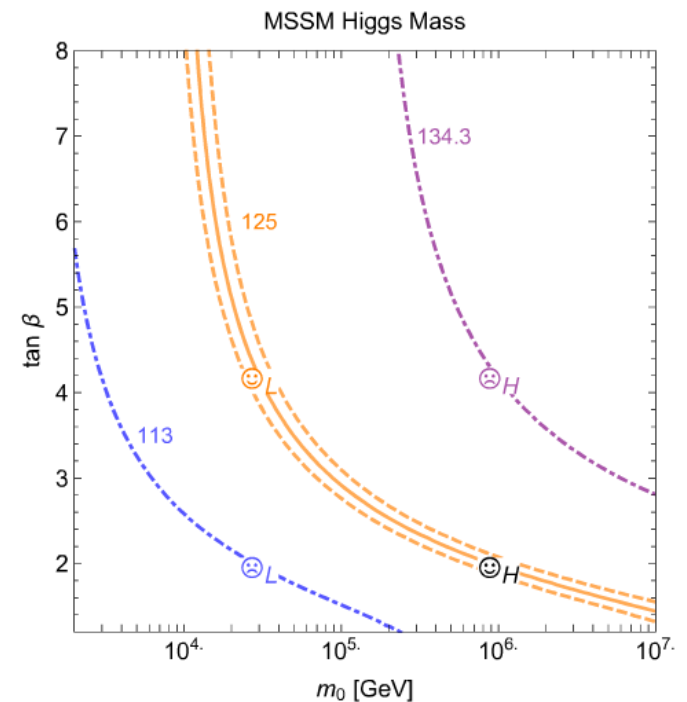
## (Mini)-split

Arvanitaki, Craig, Dimopoulos, Villadoro [1210.0555]

1 crucial piece of data

$$m_h = 125.09 \text{ GeV}$$

$$m_h^2 \approx m_Z^2 \cos^2(2\beta) + \frac{3m_t^4}{4\pi^2 v^2} \left( \log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} - \frac{X_t^4}{12m_{\tilde{t}}^4} \right)$$



Bonus: Not Planck-scale tuned, maybe points to a combo solution to the hierarchy problem?

e.g. relaxion

## Setting a target

(How far) can we test the origin of the Higgs mass?

Can we measure  $m_0$  and  $\tan \beta$  at FCC-hh?

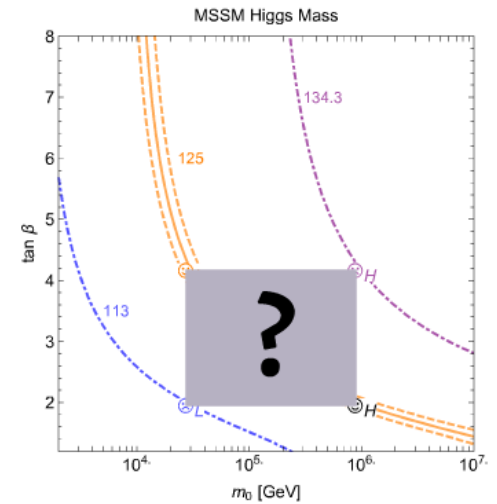
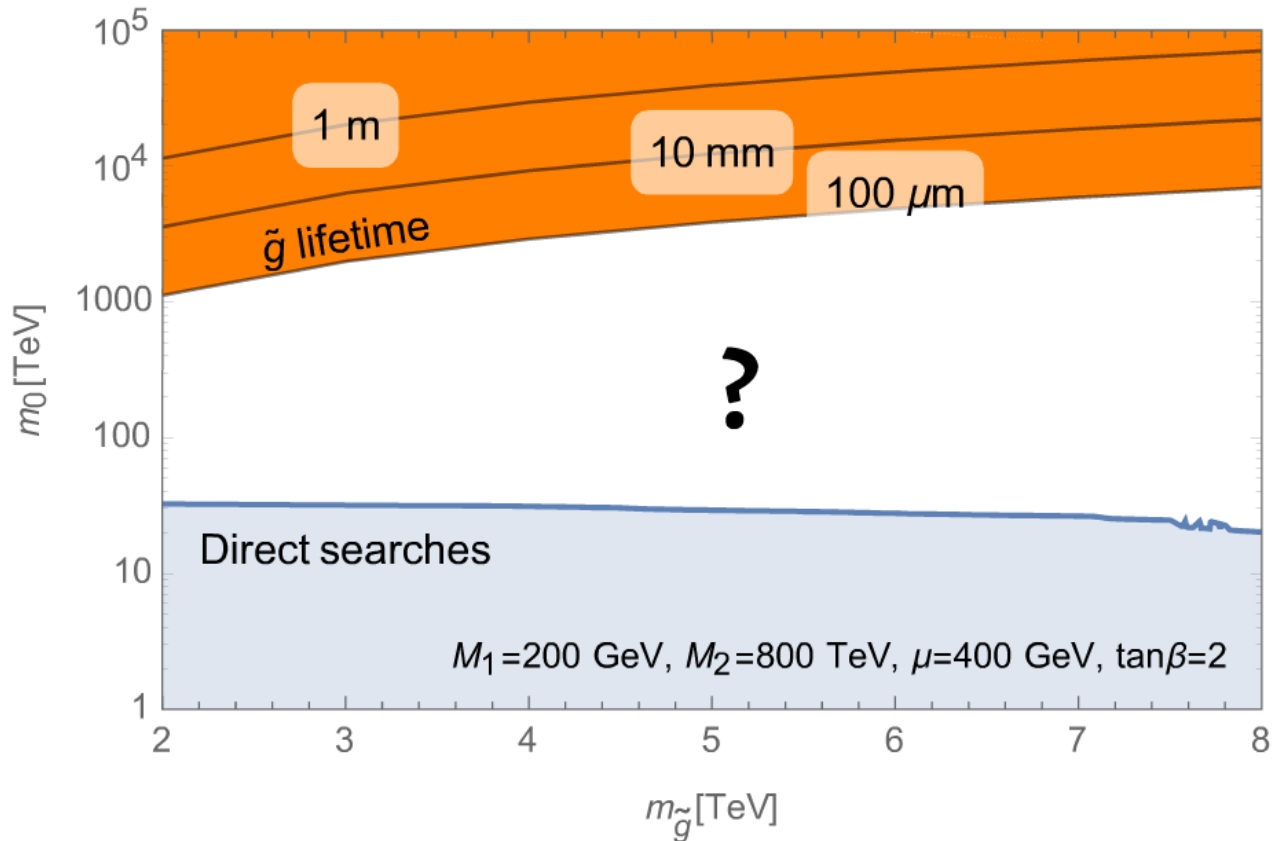
[post-discovery]

Q: Why not wait for discovery before measuring parameters?

Sharpens the physics case

Tells us what we would need in terms of energies, luminosity, detectors, technology

# Gauginos



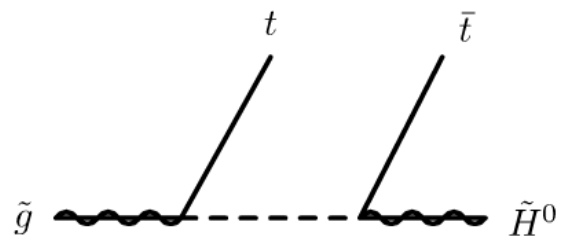
Scalar superpartners might be out of reach

Gauginos are often 1-loop (or more) suppressed relative to scalar masses

Anomaly mediation  
No-scale structure

# Gluino branching fractions

Tree level branching ratios are independent of  $m_0$



$$\sim \frac{m_{\tilde{g}}^5}{m_{\tilde{t}}^4}$$

One-loop decay to gluon+higgsino logarithmically sensitive



$$\sim \frac{m_{\tilde{g}}^3 m_t^2}{m_{\tilde{t}}^4} \left( \log \frac{m_{\tilde{t}}^2}{m_t^2} \right)^2$$

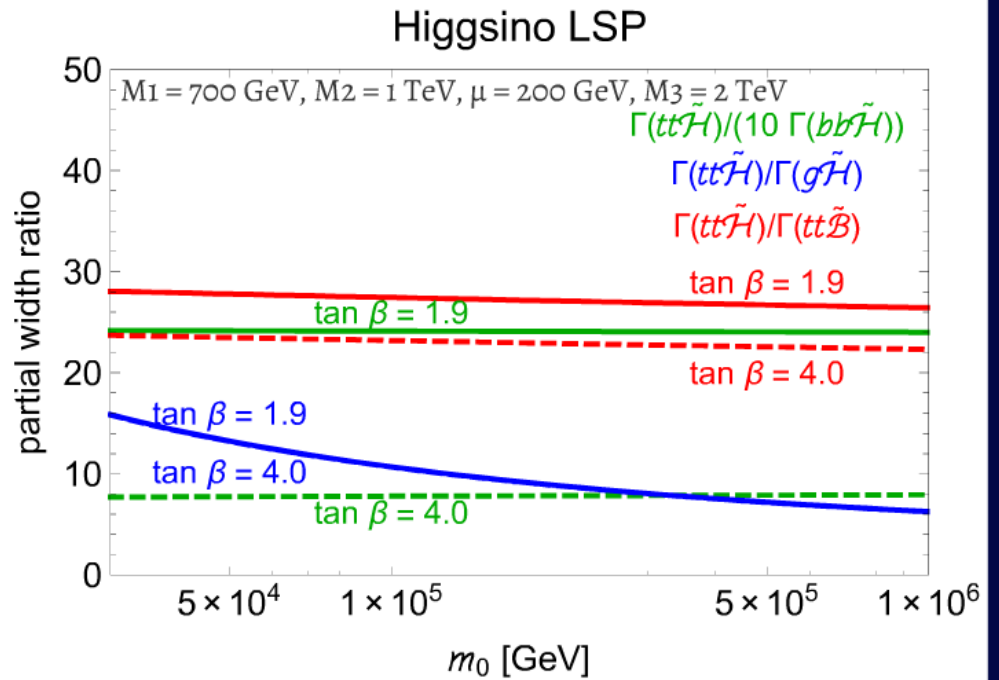
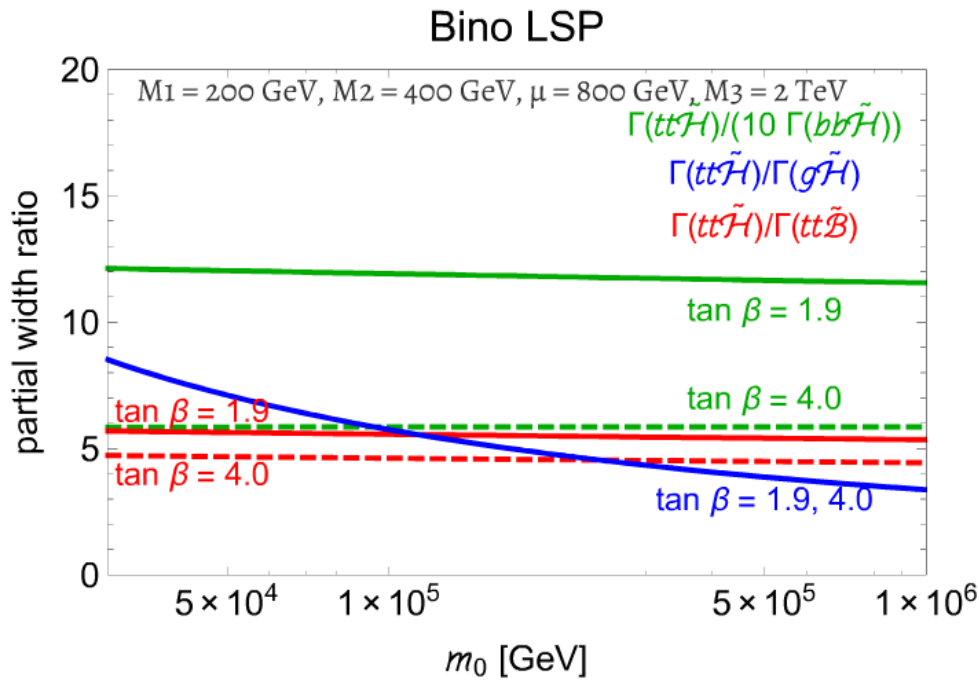
Toharia, Wells: hep-ph/0503175

Gambino, Giudice, Slavich: hep-ph/0506214

Sato, Shirai, Tobioka: 1207.3608

# Gluino branching fractions

$$\frac{\Gamma(g\tilde{H}^0)}{\Gamma(t\bar{t}\tilde{H}^0)} \propto \frac{m_t^2}{m_{\tilde{g}}^2} \left( \log \frac{m_{\tilde{t}}^2}{m_t^2} \right)^2$$

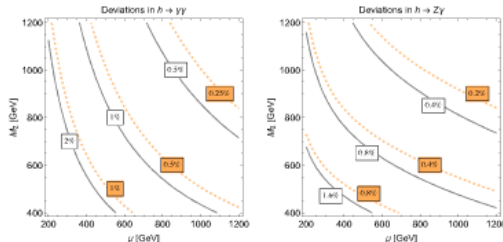




# Observables for $\tan \beta$

## Assuming scalars are inaccessible

### Higgs branching ratios



$$\frac{\Gamma(h \rightarrow \gamma\gamma)}{\Gamma(h \rightarrow \gamma\gamma)_{SM}} \approx 1 + \frac{0.82 m_W^2 \sin(2\beta)}{\mu M_2 - m_W^2 \sin(2\beta)}$$

Higgs Couplings

FCC-ee projection: 1.5%

FCC-hh stat reach (20 inv ab) ~1% at pT(H)~100 GeV

Measure ratios to reduce uncertainties

d'Enterra[1701.02663]

see Aram Apyan's talk

see Michelangelo's talk

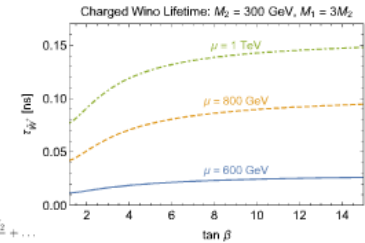
talk

### Chargino lifetime

Wino LSP

Disappearing tracks

Low, Wang [1404.0682]



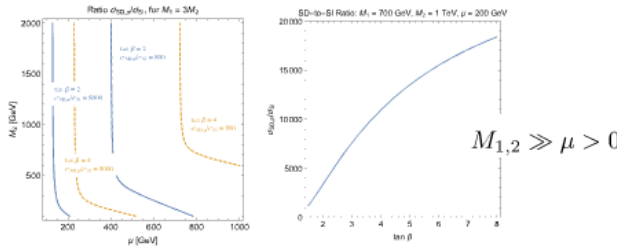
$$\delta m_W^{(loop)} \approx \frac{m_W^2 \sin^2(2\beta)}{(M_1 - M_2)^2} \tan^2 \theta_W + 2 \frac{m_W^2 M_2 \sin(2\beta)}{(M_1 - M_2)^2} \tan^2 \theta_W + \frac{m_W^2 M_2}{2\epsilon^2} + \dots$$

$$\delta m_W^{loop} \approx \frac{\alpha m_W}{2(1 + \cos \theta_W)} \approx 165 \text{ MeV.}$$

$$\Gamma(\chi^\pm \rightarrow \chi_0 \pi^\pm) = \Gamma(\pi^\pm \rightarrow \nu_\mu \mu^\pm) \times 16 \frac{(\delta m_W)^3}{m_\pi m_\mu^2} \left(1 - \frac{m_\pi^2}{(\delta m_W)^2}\right)^{1/2} \left(1 - \frac{m_\mu^2}{m_\pi^2}\right)^{-2}$$

Ibe, Matsumoto, Sato [1212.5989]

### Direct detection (SD vs SI)



$$c_{hXX}^* \approx \frac{g m_W (1 + \sin(2\beta))}{2} \left[ \frac{1}{M_2 - \mu} + \frac{\tan^2 \theta_W}{M_1 - \mu} \right]$$

$$c_{ZXX}^* \approx \frac{g m_W^2}{4\mu \cos \theta_W} \cos(2\beta) \left[ \frac{1}{M_2 - \mu} + \frac{\tan^2 \theta_W}{M_1 - \mu} \right]$$

$$\sigma_{SI} = |c_{hXX}|^2 \times (5.3 \times 10^{-43} \text{ cm}^2)$$

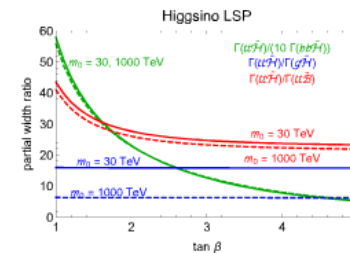
$$\sigma_{SD,p} = |c_{ZXX}|^2 \times (2.9 \times 10^{-37} \text{ cm}^2)$$

$$\sigma_{SD,n} = |c_{ZXX}|^2 \times (2.2 \times 10^{-37} \text{ cm}^2)$$

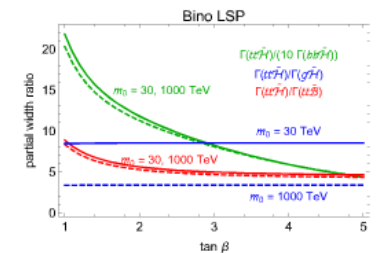
### Gluino branching fractions

$$\frac{\Gamma(\tilde{g} \rightarrow t\bar{t}\tilde{H}^0)}{\Gamma(\tilde{g} \rightarrow t\bar{t}\tilde{B}^0)}, \frac{\Gamma(\tilde{g} \rightarrow t\bar{t}\tilde{W}^0)}{\Gamma(\tilde{g} \rightarrow t\bar{t}\tilde{W}^0)} \propto \frac{1}{\sin^2 \beta}$$

$$\frac{\Gamma(\tilde{g} \rightarrow b\bar{b}\tilde{H}^0)}{\Gamma(\tilde{g} \rightarrow t\bar{t}\tilde{H}^0)} \propto \tan^2 \beta$$

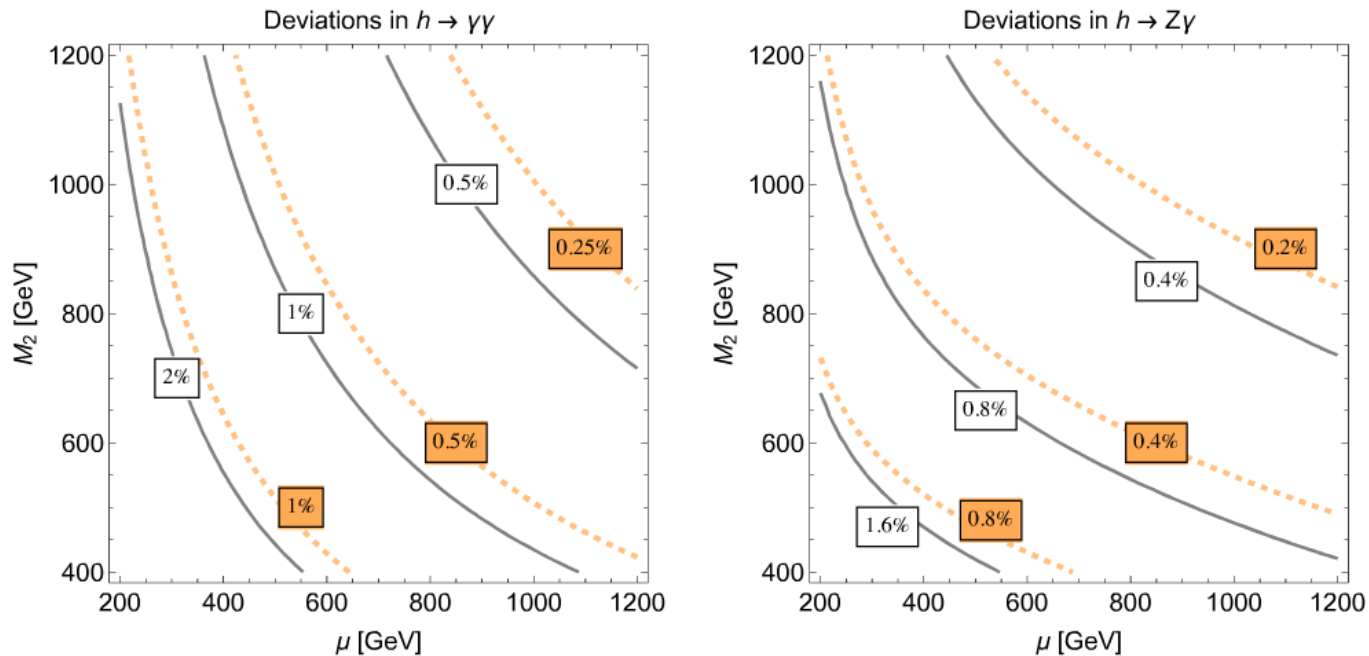


M1 = 700 GeV, M2 = 1 TeV, mu = 200 GeV, M3 = 2 TeV



M1 = 200 GeV, M2 = 400 GeV, mu = 800 GeV, M3 = 2 TeV

# Higgs branching ratios



$$\frac{\Gamma(h \rightarrow \gamma\gamma)}{\Gamma(h \rightarrow \gamma\gamma)_{\text{SM}}} \approx 1 + \frac{0.82m_W^2 \sin(2\beta)}{\mu M_2 - m_W^2 \sin(2\beta)}$$

## Higgs Couplings

FCC-ee projection: 1.5%

FCC-hh stat reach (20 inv ab)  $\sim 1\%$  at  $p_T(H) \sim 100$  GeV

Measure ratios to reduce uncertainties

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# Chargino lifetime

Wino LSP

Disappearing tracks

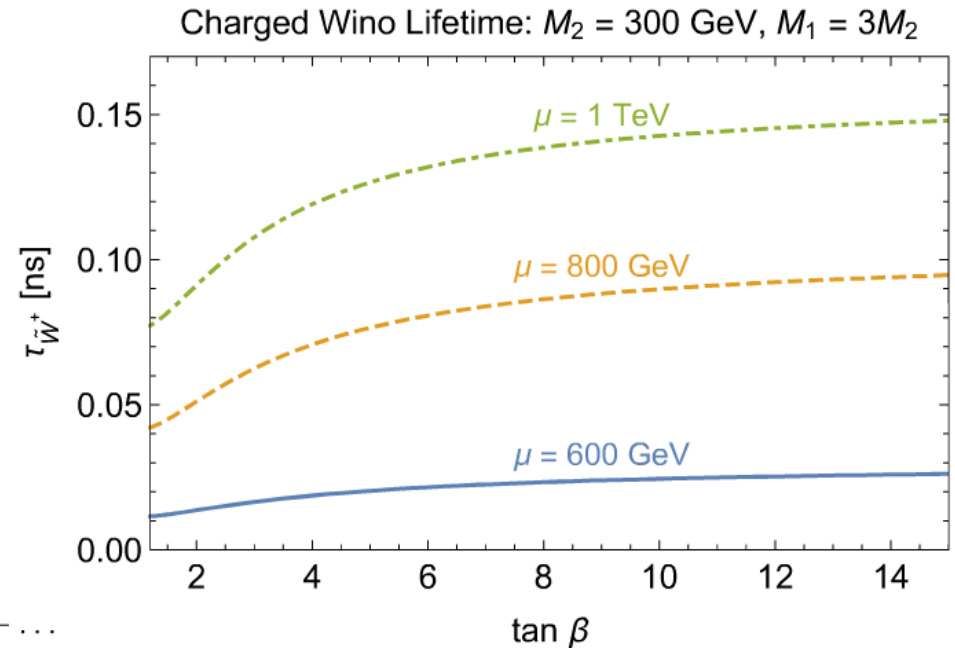
Low, Wang [1404.0682]

$$\delta m_{\tilde{W}}^{\text{tree}} \approx \frac{m_W^4 \sin^2(2\beta)}{(M_1 - M_2)\mu^2} \tan^2 \theta_W + 2 \frac{m_W^4 M_2 \sin(2\beta)}{(M_1 - M_2)\mu^3} \tan^2 \theta_W + \frac{m_W^4 M_2}{2\mu^4} + \dots$$

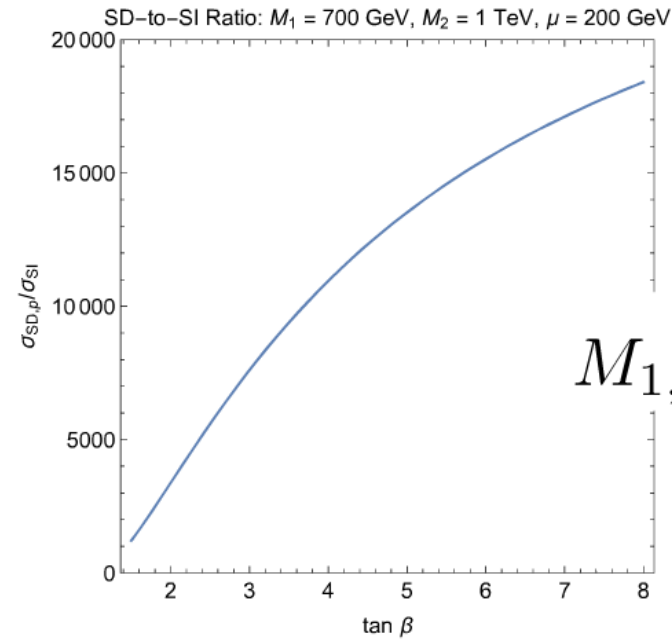
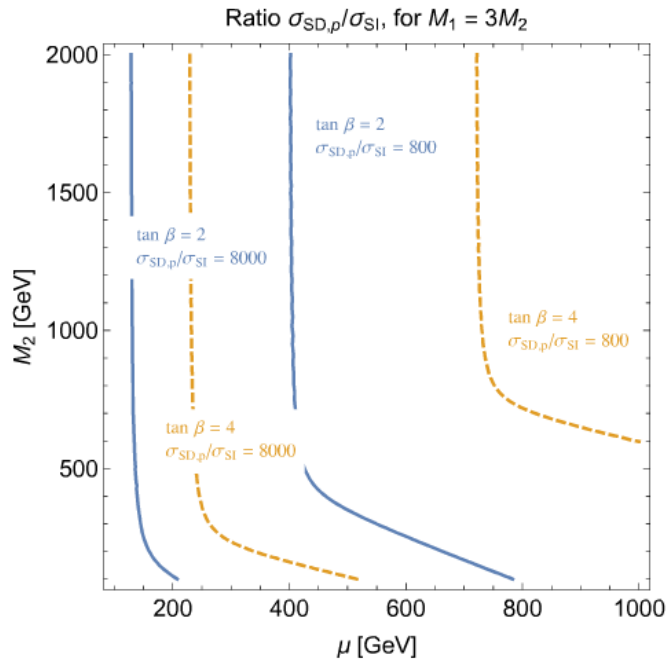
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$$\Gamma(\chi^\pm \rightarrow \chi_0 \pi^\pm) = \Gamma(\pi^\pm \rightarrow \nu_\mu \mu^\pm) \times 16 \frac{(\delta m_{\tilde{W}})^3}{m_\pi m_\mu^2} \left(1 - \frac{m_\pi^2}{(\delta m_{\tilde{W}})^2}\right)^{1/2} \left(1 - \frac{m_\mu^2}{m_\pi^2}\right)^{-2}$$

Ibe, Matsumoto, Sato [1212.5989]



# Direct detection (SD vs SI)



$$M_{1,2} \gg \mu > 0$$

$$c_{h\chi\chi}^* \approx \frac{gm_W(1 + \sin(2\beta))}{2} \left[ \frac{1}{M_2 - \mu} + \frac{\tan^2 \theta_W}{M_1 - \mu} \right]$$

$$c_{Z\chi\chi} \approx \frac{gm_W^2}{4\mu \cos \theta_W} \cos(2\beta) \left[ \frac{1}{M_2 - \mu} + \frac{\tan^2 \theta_W}{M_1 - \mu} \right]$$

$$\sigma_{SI} = |c_{h\chi\chi}|^2 \times (5.3 \times 10^{-43} \text{ cm}^2)$$

$$\sigma_{SD,p} = |c_{Z\chi\chi}|^2 \times (2.9 \times 10^{-37} \text{ cm}^2)$$

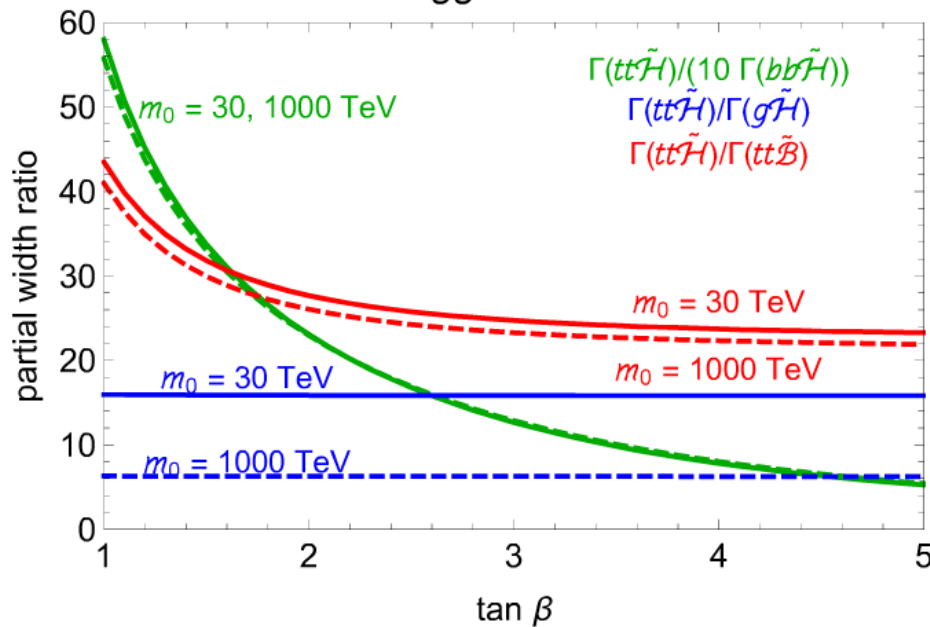
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# Gluino branching fractions

$$\frac{\Gamma(\tilde{g} \rightarrow t\bar{t}\tilde{H}^0)}{\Gamma(\tilde{g} \rightarrow t\bar{t}\tilde{B}^0)}, \frac{\Gamma(\tilde{g} \rightarrow t\bar{t}\tilde{H}^0)}{\Gamma(\tilde{g} \rightarrow t\bar{t}\tilde{W}^0)} \propto \frac{1}{\sin^2 \beta}$$

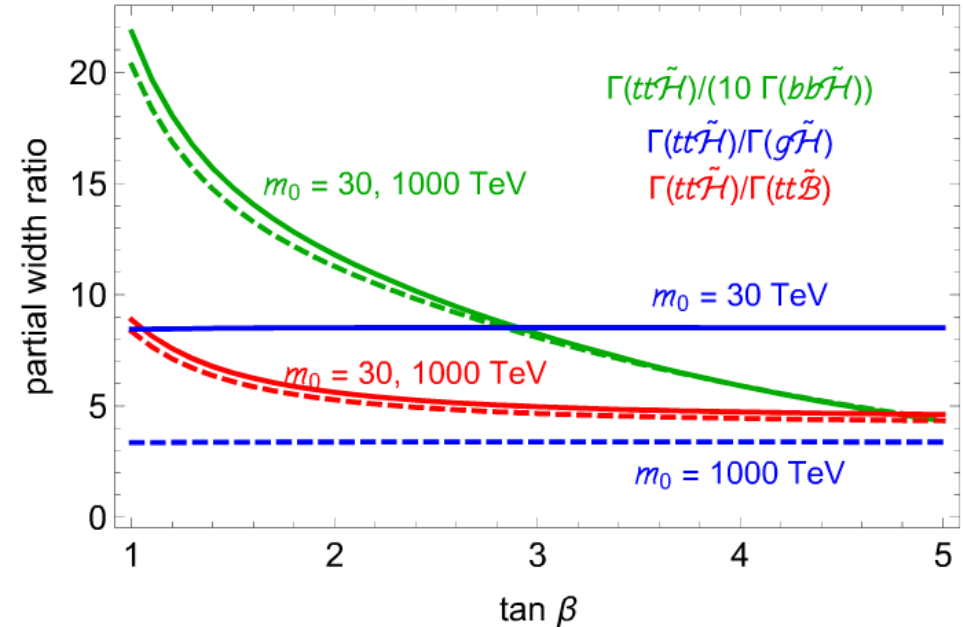
$$\frac{\Gamma(\tilde{g} \rightarrow b\bar{b}\tilde{H}^0)}{\Gamma(\tilde{g} \rightarrow t\bar{t}\tilde{H}^0)} \propto \tan^2 \beta$$

Higgsino LSP



$M_1 = 700 \text{ GeV}, M_2 = 1 \text{ TeV}, \mu = 200 \text{ GeV}, M_3 = 2 \text{ TeV}$

Bino LSP



$M_1 = 200 \text{ GeV}, M_2 = 400 \text{ GeV}, \mu = 800 \text{ GeV}, M_3 = 2 \text{ TeV}$

## Blind spot

$\tan \beta = 1$  is a special point

$$\tilde{H}_{\pm}^0 \equiv \frac{1}{\sqrt{2}} \left( \tilde{H}_u^0 \pm \tilde{H}_d^0 \right)$$

Z couples off-diagonally

$$-\frac{1}{2}\mu\tilde{H}_+^0\tilde{H}_+^0 + \frac{1}{2}\mu\tilde{H}_-^0\tilde{H}_-^0 - \frac{eZ_\mu}{\sin(2\theta_W)} \left[ \tilde{H}_+^{0\dagger}\bar{\sigma}^\mu\tilde{H}_-^0 + \tilde{H}_-^{0\dagger}\bar{\sigma}^\mu\tilde{H}_+^0 \right]$$

$\tilde{H}_-^0$  does not mix with  $\tilde{B}^0$ ,  $\tilde{W}^0$ , or couple to Higgs

$$\left( \begin{array}{cc} \begin{bmatrix} M_1 & 0 \\ 0 & M_2 \end{bmatrix} & \\ \frac{m_Z \cos \beta}{\sqrt{2}} \begin{bmatrix} (1 + \tan \beta) s_W & (1 + \tan \beta) c_W \\ (-1 + \tan \beta) s_W & (1 - \tan \beta) c_W \end{bmatrix} & \frac{m_Z \cos \beta}{\sqrt{2}} \begin{bmatrix} (1 + \tan \beta) s_W & (-1 + \tan \beta) s_W \\ (1 + \tan \beta) c_W & (1 - \tan \beta) c_W \end{bmatrix} \\ & \begin{bmatrix} \mu & 0 \\ 0 & -\mu \end{bmatrix} \end{array} \right)$$

(Direct detection blind spot)

Cheung, Hall, Pinner, Ruderman

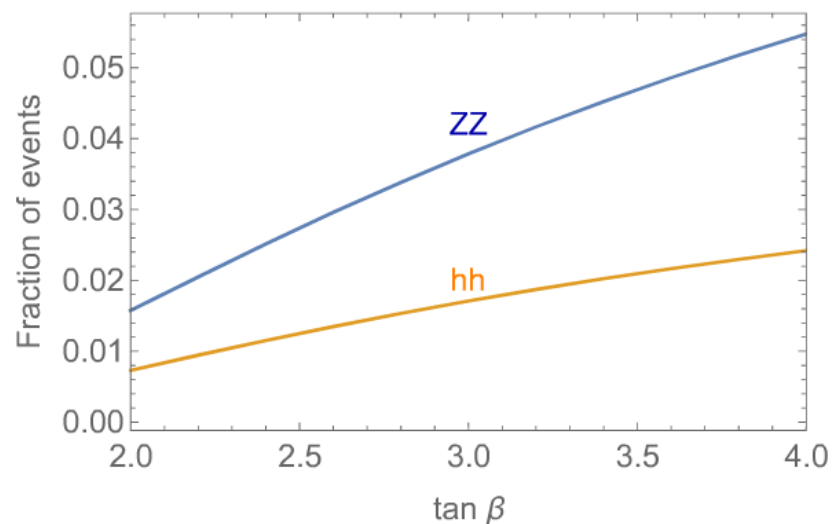
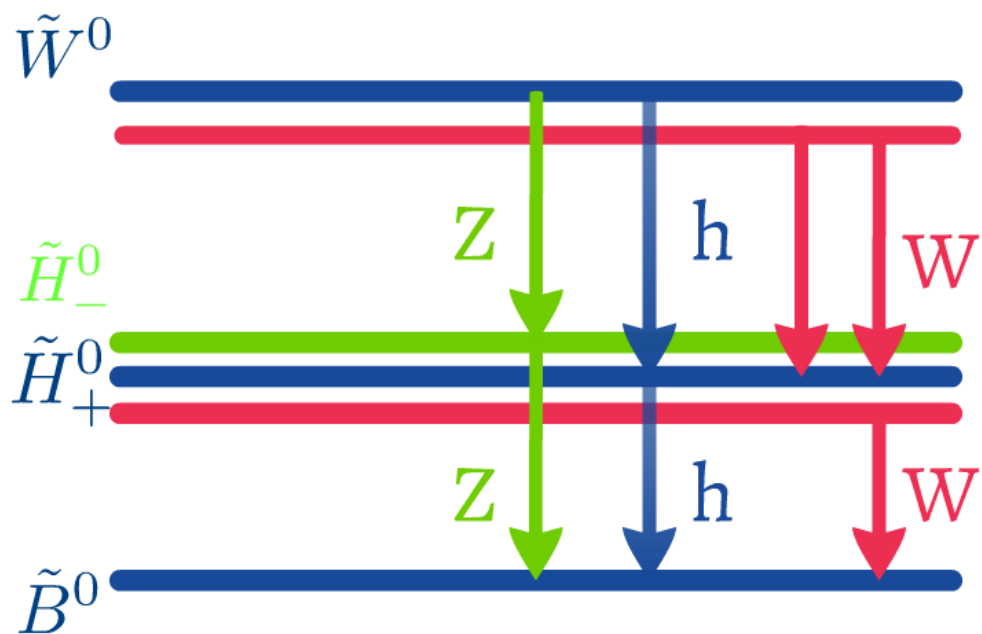
[1211.4873]

# Electroweakino decays

$\tan \beta = 1$  is a special point

Electroweakino decays can help measure  $\tan \beta$

$$pp > \tilde{H}_+^0 \tilde{H}_-^0$$



$M_1 = 200 \text{ GeV}$ ,  $M_2 = 800 \text{ GeV}$ ,  $M_3 = 2 \text{ TeV}$ ,  $\mu = 400 \text{ GeV}$

# Specific example @ FCC-hh

$\tan \beta$

- Two pairs of OSSF leptons, with  $|m_{\ell\ell} - m_Z| < 10$  GeV
- MET > 150 GeV
- Scalar sum of pT of all visible particles < 600 GeV

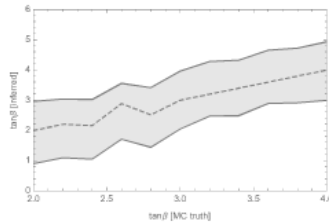
Signal

$$pp \rightarrow \chi_2^0 \chi_3^0 \rightarrow (Z \rightarrow \ell\ell)^2 \chi_1^0 \chi_1^0 \quad 8.4 - 28.8$$

Backgrounds

$$\left. \begin{aligned} ZZZ \rightarrow (Z \rightarrow \ell\ell)^2 (Z \rightarrow \nu\nu) \\ hZ \rightarrow (h \rightarrow ZZ^* \rightarrow \ell\nu\nu) (Z \rightarrow \ell\ell) \end{aligned} \right\} 86.4$$

$$\left. \begin{aligned} \chi\chi \rightarrow \text{cascades} \\ \tilde{g}\tilde{g} \rightarrow \text{cascades} \\ \chi_2 \chi_3 \rightarrow hZ \chi_1^0 \chi_1^0 \rightarrow (Z \rightarrow \ell\ell)^2 \chi_1^0 \chi_1^0 + X \end{aligned} \right\} 35.2$$



$m_0$

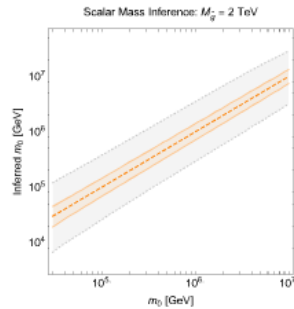
$$H_T > 2 \text{ TeV}, \quad p_T^{\text{missing}} > 1 \text{ TeV}, \quad p_T(j_i) > 1 \text{ TeV}, \\ N_{\text{jet}} < 5, \text{ one leptonic } Z (80 \text{ GeV} < m_{\ell\ell} < 100 \text{ GeV}), \\ m_{j,Z} > m_{\text{all other jets}}$$

Signal

$$(\tilde{g} \rightarrow \chi_3^0 g \rightarrow Z \chi_1^0 g)(\tilde{g} \rightarrow X) \quad \text{O}(500)$$

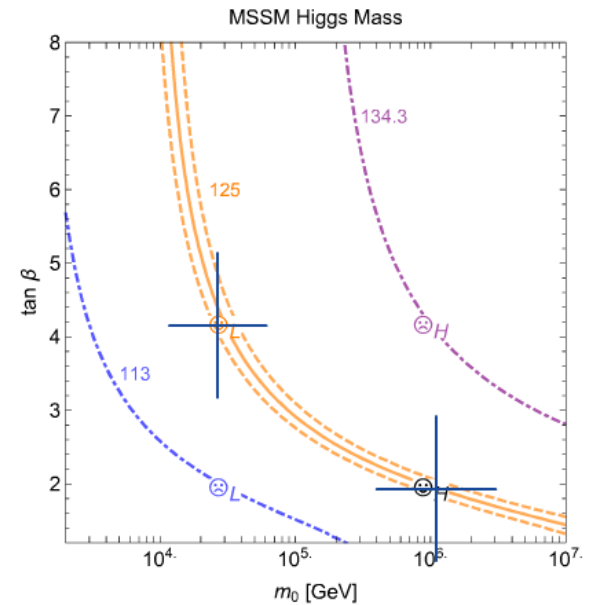
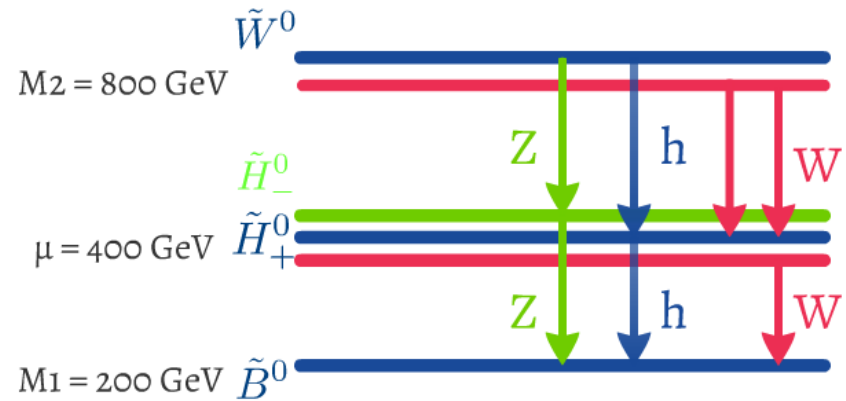
Backgrounds

$$\left. \begin{aligned} (\tilde{g} \rightarrow q\bar{q})(\chi \rightarrow \text{cascades})^2 \\ ZZ + \text{jets} \rightarrow (Z \rightarrow \ell^* \ell^-), (Z \rightarrow \nu\nu) \\ t\bar{t} \rightarrow (W \rightarrow \ell\nu)^2 \\ t\bar{t}Z \rightarrow t\bar{t}(Z \rightarrow \ell\ell) \end{aligned} \right\} 1680$$



3 inv ab  
5 % syst

$$M_3 = 2 \text{ TeV } \tilde{g}$$



for a few other examples see [1606.00947]



# tan $\beta$

1. Two pairs of OSSF leptons, with  $|m_{\ell\ell} - m_Z| < 10$  GeV
2. MET > 150 GeV
3. Scalar sum of pT of all visible particles < 600 GeV

## Signal

$$pp \rightarrow \chi_2^0 \chi_3^0 \rightarrow (Z \rightarrow \ell\ell)^2 \chi_1^0 \chi_1^0 \quad 8.4 - 28.8$$

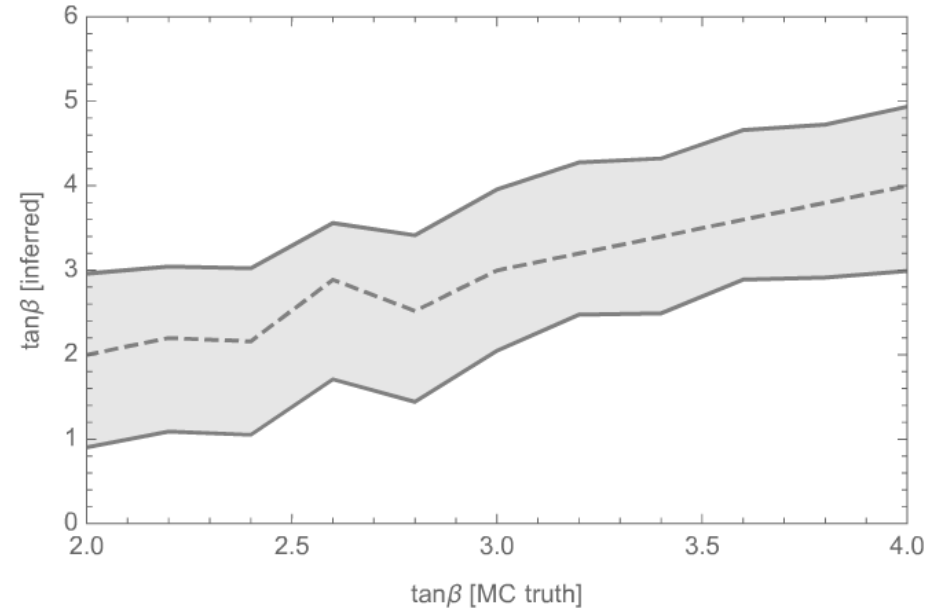
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$$\chi\chi \rightarrow \text{cascades}$$

$$\tilde{g}\tilde{g} \rightarrow \text{cascades}$$

$$\left. \begin{aligned} \chi_2 \chi_3 &\rightarrow hZ \chi_1^0 \chi_1^0 \rightarrow (Z \rightarrow \ell\ell)^2 \chi_1^0 \chi_1^0 + X \end{aligned} \right\} 35.2$$



# $m_0$

$H_T > 2 \text{ TeV}$ ,  $p_T^{\text{missing}} > 1 \text{ TeV}$ ,  $p_T(j_1) > 1 \text{ TeV}$ ,  
 $N_{\text{jet}} < 5$ , one leptonic  $Z$  ( $80 \text{ GeV} < m_{\ell\ell} < 100 \text{ GeV}$ ),  
 $m_{j_1 Z} > m_{\text{all other jets}}$ .

## Signal

$$(\tilde{g} \rightarrow \chi_3^0 g \rightarrow Z \chi_1^0 g)(\tilde{g} \rightarrow X)$$

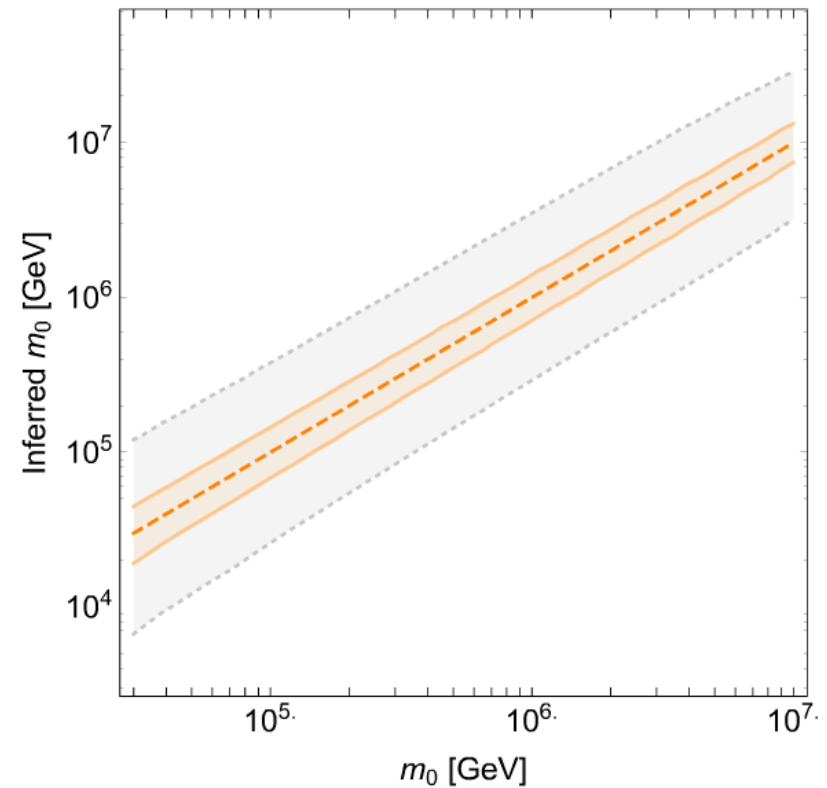
$O(500)$   
 17-35% of the  
 SUSY sample

## Backgrounds

$$(\tilde{g} \rightarrow q\bar{q}(\chi \rightarrow \text{cascades}))^2$$

$$\left. \begin{aligned}
 ZZ + \text{jets} &\rightarrow (Z \rightarrow \ell^+\ell^-), (Z \rightarrow \nu\nu) \\
 t\bar{t} &\rightarrow (W \rightarrow \ell\nu)^2 \\
 t\bar{t}Z &\rightarrow t\bar{t}(Z \rightarrow \ell\ell)
 \end{aligned} \right\} 1680$$

Scalar Mass Inference:  $M_{\tilde{g}} = 2 \text{ TeV}$



## Conclusions

The simplest supersymmetric model consistent with the Higgs mass is a reasonable candidate for new physics

A class of theories predicts gauginos will be kinematically accessible at FCC-hh

It will be valuable to further develop observables and analyses at FCC that can test the origin of the Higgs mass

Interesting to think about other bracketed questions that we care about and can answer at future colliders