

# Susceptibilities from a Black Hole Engineered EoS with a Critical Point

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# Exploring QCD Phase Diagram

## Lattice QCD

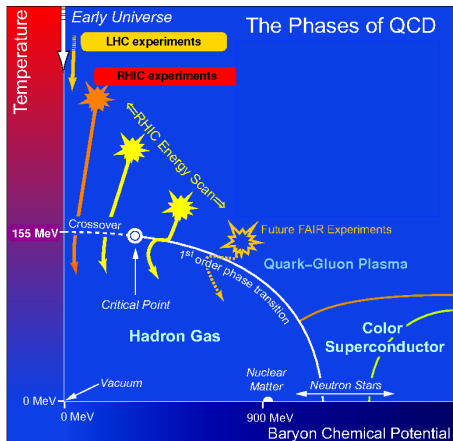
Perform calculations at  $\mu_B = 0$ , and extrapolate via Taylor expansion to finite  $\mu_B$

## Black Hole Engineering

Based on Lattice data at  $\mu_B = 0$ , allows us to calculate observable at finite density.

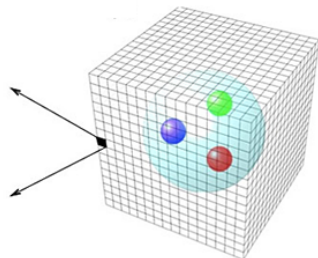
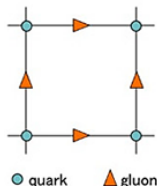
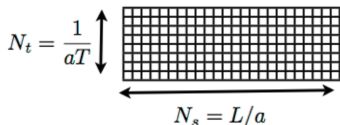
## Fluctuations of conserved Charges

Provide essential information about the effective degrees of freedom of a system.



# Lattice QCD

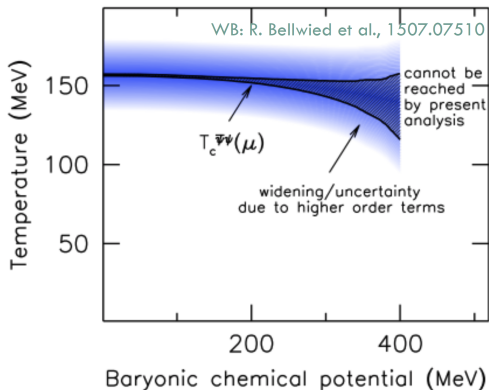
## QCD on a discretized lattice



- Study QCD from first principles in the **non-perturbative** region.
- Calculates equilibrium properties at  $\mu_B = 0$  or at imaginary- $\mu_B$  (**sign problem!**)
- It has technical difficulties to compute **transport properties**
- **Critical behavior of the CEP can be lost** when extrapolate calculations at finite  $\mu$

# Lattice at Finite $\mu_B$

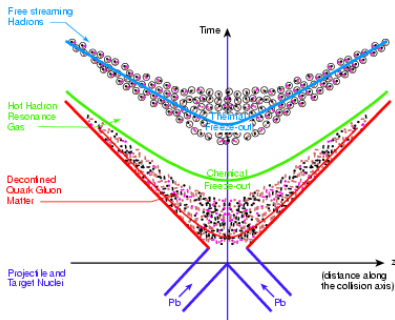
Phase diagram bases on the  $\mu$ -dependent  $T_c$  from the chiral condensate (analytically continued from the **imaginary- $\mu_B$** )



[WB:] R. Bellwied *et. al.*, Phys. Lett. B **751** (2015) 053

# Evolution of a heavy ion collision

- **Chemical freeze-out:** all inelastic interactions cease. The chemical composition of the system is fixed
- **Kinetic freeze-out:** all elastic interactions cease: the spectra of the particles are fixed



- We want to study the chemical freeze-out
- **Observable:** fluctuations of conserved charges
  - They are fixed at the freeze-out
  - They can be measured and calculated
  - They are sensitive to the critical point

# Susceptibilities

A system in thermal equilibrium is characterized by

$$Z = \text{Tr} \left[ -\frac{H - \sum_i \mu_i Q_i}{T} \right]$$

$$P = \frac{T}{V} \ln Z$$

$$\mu_u = \frac{1}{3}\mu_B + \frac{2}{3}\mu_Q$$

$$\mu_d = \frac{1}{3}\mu_B - \frac{1}{3}\mu_Q$$

$$\mu_s = \frac{1}{3}\mu_B - \frac{1}{3}\mu_Q - \mu_S$$

The Susceptibilities  $\chi_{lmn}^{BSQ}$  are defined as

$$\chi_{lmn}^{BSQ} = \frac{\partial^l}{\partial(\mu_B/T)^l} \frac{\partial^m}{\partial(\mu_S/T)^m} \frac{\partial^n}{\partial(\mu_Q/T)^n} \left( \frac{P}{T^4} \right)$$

# Fluctuations of Conserved Charges

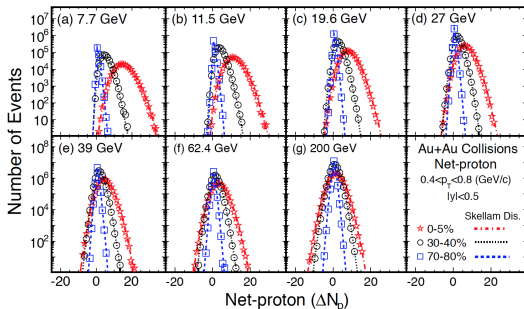
- The susceptibilities  $\chi_i = \chi_i^B(T, \mu_B)$  are related directly to the moments of the distribution.
- The volume-independent ratios are useful quantities to compare to experimental data.

$$\text{mean : } M = \chi_1$$

$$\text{variance : } \sigma^2 = \chi_2$$

$$\text{skewness : } S = \chi_3/\chi_2^{3/2}$$

$$\text{kurtosis : } \kappa = \chi_4/\chi_2^2$$



$$M/\sigma^2 = \chi_1/\chi_2$$

$$S\sigma = \chi_3/\chi_2$$

$$\kappa\sigma^2 = \chi_4/\chi_2$$

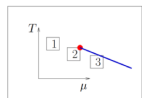
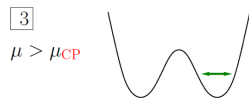
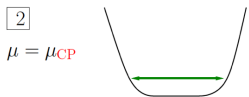
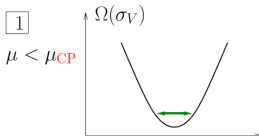
$$S\sigma^3/M = \chi_3/\chi_1$$

[STAR] Phys. Rev. Lett. **112** (2014) 032302

Karsch Central Eur.J.Phys. **10** (2012) 1234



# Fluctuations at the Critical End Point



The probability distribution for the order parameter

$$P[\sigma] \sim \exp \{-\Omega[\sigma]/T\}$$

$$\Omega = \int d^3x \left[ \frac{1}{2}(\nabla\sigma)^2 + \frac{m_\sigma^2}{2}\sigma^2 + \frac{\lambda_3}{3}\sigma^3 + \dots \right]$$

The **correlation length** ( $\xi = m_\sigma^{-1}$ )

$$\xi \sim |T - T_c|^{-\nu} \text{ where } \nu > 0$$

$$\chi_2 = VT\xi^2$$

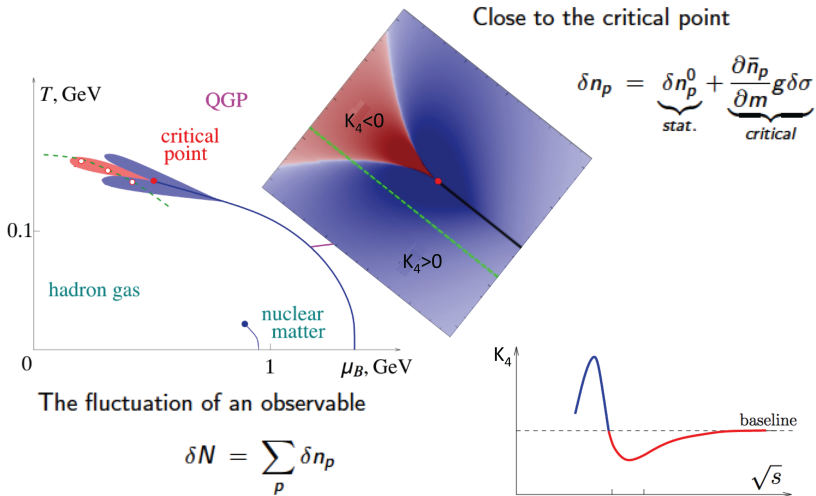
$$\chi_3 = 2VT^{3/2}\hat{\lambda}_3\xi^{9/2}$$

$$\chi_4 = 6VT^2[2\hat{\lambda}_3^2 - \hat{\lambda}_4]\xi^7$$

M. A. Stephanov, Phys. Rev. Lett. **102** (2009) 032301



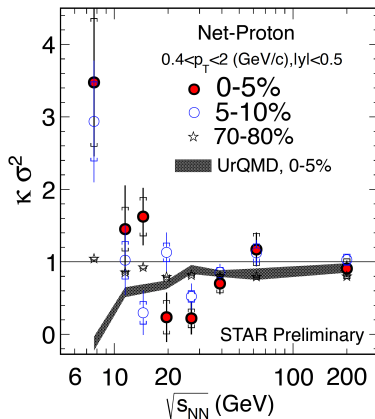
# Kurtosis at the Critical End Point



M. A. Stephanov, Phys. Rev. Lett. **107** (2011) 052301

# Net-Proton Fluctuations from STAR

- Preliminary STAR data for net-proton fluctuations ( $\kappa\sigma^2 = \chi_4/\chi_2$ )
- Non-monotonic behavior at low energies
- Is it due to the critical point?
- If so, how close to the critical point does the Non-monotonic behavior show up?



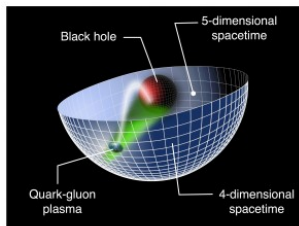
[STAR] Xiaofeng Luo, Quark Matter 2015

# Black Hole Engineering

## Holography (gauge/string duality at Strong Coupling)

Quantum Field Theory in 4- dimension  $\iff$  Classical Gravity in at least 5-dimension

- Coupling  $\gg 1$  in QFT  $\rightarrow$  vanishing string coupling
- $(T, \mu)$  in QFT  $\rightarrow$  black hole solution
- Holography  $\rightarrow$  Near Perfect fluidity



J M Maldacena 1999 Int. J. Theor. Phys. (38) 1113

# Holographic model

Lagrangian of non-conformal General Relativity in 5 dimensions

$$\mathcal{S} = \frac{1}{16\pi G_5} \int dx^5 \sqrt{-g} \left[ \mathcal{R} - \frac{1}{2} (\partial_M \phi)^2 - \underbrace{V(\phi)}_{\text{nonconformal}} - \frac{1}{4} \underbrace{f(\phi) F_{MN}^2}_{\mu_B \neq 0} \right]$$

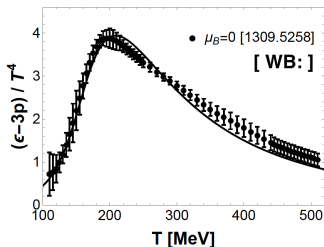
$\phi$  scalar field

$A_M$  abelian vector field

$G_5$  gravitational constant

$V(\Phi)$  dilaton potential

$f(\phi)$  Maxwell-dilaton coupling



O DeWolfe, S S Gubser, and C Rosen, Phys. Rev. D **83**, (2011) 086005

R Rougemont, A Ficnar, S Finazzo and J Noronha, High Energy. Phys. (2016) **102**.

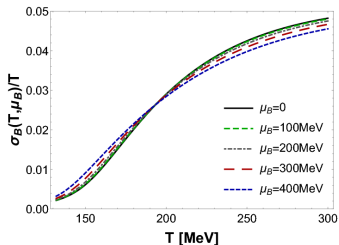
# Black Hole Engineering

## Black Hole Model

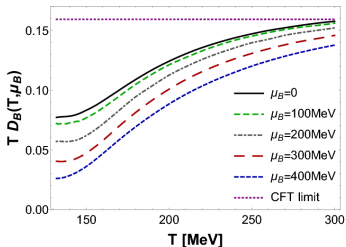
- Input parameter are fixed by Lattice data at  $(T, \mu_B = 0)$
- Non-conformal Equation of State
  - at finite  $T$  and finite  $\mu_B$
  - with a critical end point
  - agrees with lattice data at small  $\mu_B$
  - allows to extract freeze-out parameters
- Near perfect fluidity
  - Ability to compute transport coefficients near the crossover and at large  $\mu_B$

# Baryon Transport Coefficients

## Baryon dc conductivity



## Baryon diffusion constant



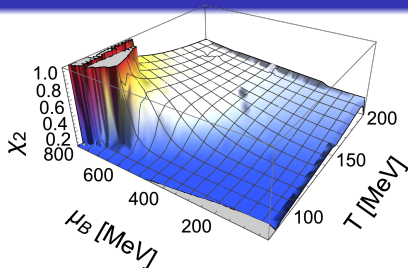
R Rougemont, J Noronha, and J Noronha-Hostler Phys.Rev.Lett. **115** (2015) 202301

# Model Predictions

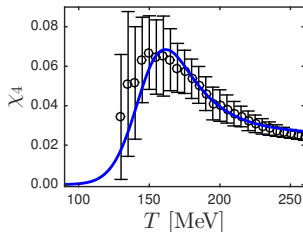
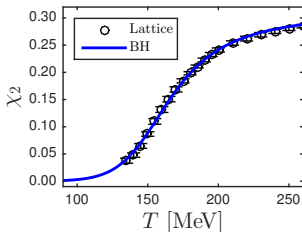
## Critical end point

$$\mu_B = 705 \text{ MeV}$$

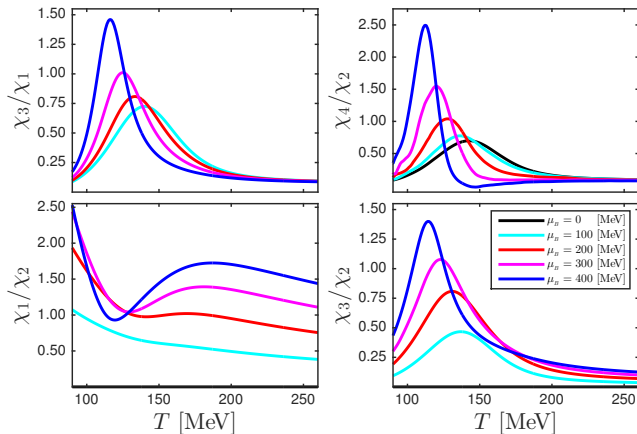
$$T = 80 \text{ MeV}$$



$\chi_2$  and  $\chi_4$  agree with lattice points

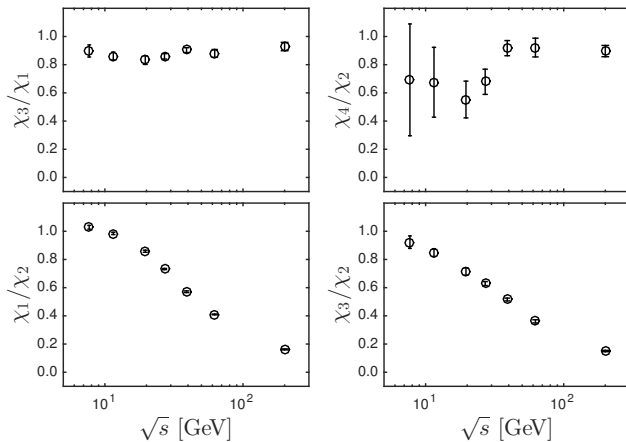


# Black Hole Susceptibility Ratios





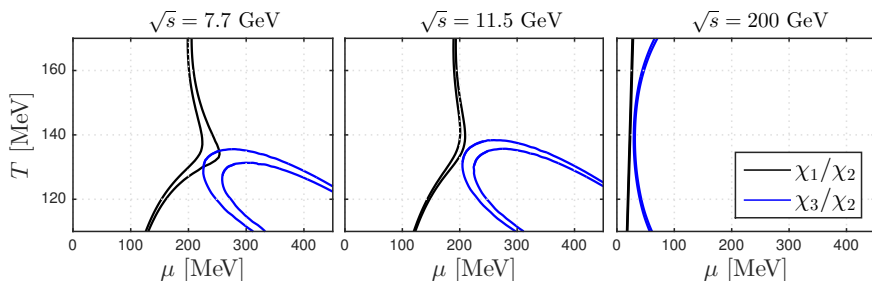
# [STAR] Net Proton Fluctuation Susceptibility Ratios



[STAR] Phys. Rev. Lett. **112** (2014) 032302

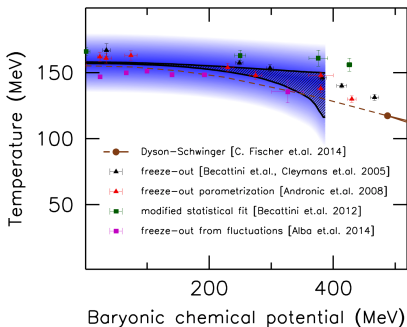
# Freeze out: Extracted from $\chi_1/\chi_2$ and $\chi_3/\chi_2$

Trajectory in the  $[T - \mu]$  plane that satisfy the experimental values

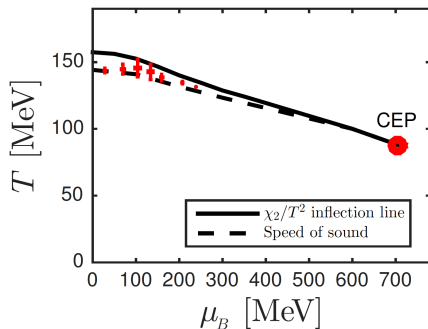


- Freeze out points  $[T - \mu_B]$  are extracted from the line made by the closer points between  $\chi_1/\chi_2$  and  $\chi_3/\chi_2$

# Freeze-out Line



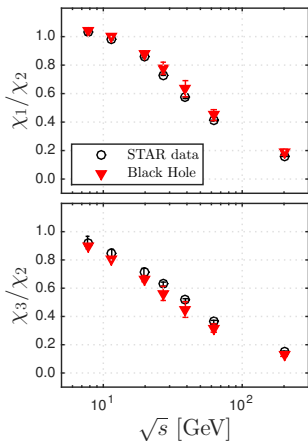
[WB:] R. Bellwied *et. al.*,  
 Phys. Lett. B **751** (2015) 053



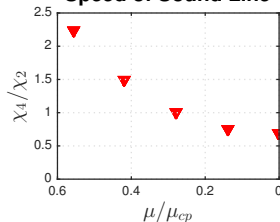
Black Hole Model

# Model Predictions

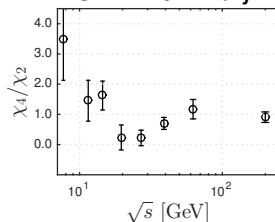
## Ratios



## Black Hole Speed of Sound Line



## STAR Preliminary



# Conclusions

We study a Black Hole Model that up to a  $\mu_B = 400\text{MeV}$  and found that

- Reproduces lattice data at  $\mu_B = 0$
- Contains a critical end point at  $\mu_B = 705\text{MeV}$  and  $T = 80\text{MeV}$
- The freeze-out points we found are very close to the points obtained by HRG, and they are far from our critical end point
- When we extrapolate to points close to the CEP we found a monotonic behavior of  $\chi_4/\chi_2$ .

# Outlooks

- Explore susceptibilities for  $\mu_B$  closer to the critical end point
- Study sensitivity of the location of the critical point to initial parameters
- Determine the universality class of the critical end point in the black hole model