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# Chiral symmetry restoration in heavy-ion collisions

Elena Bratkovskaya

(GSI, Darmstadt & Uni. Frankfurt)

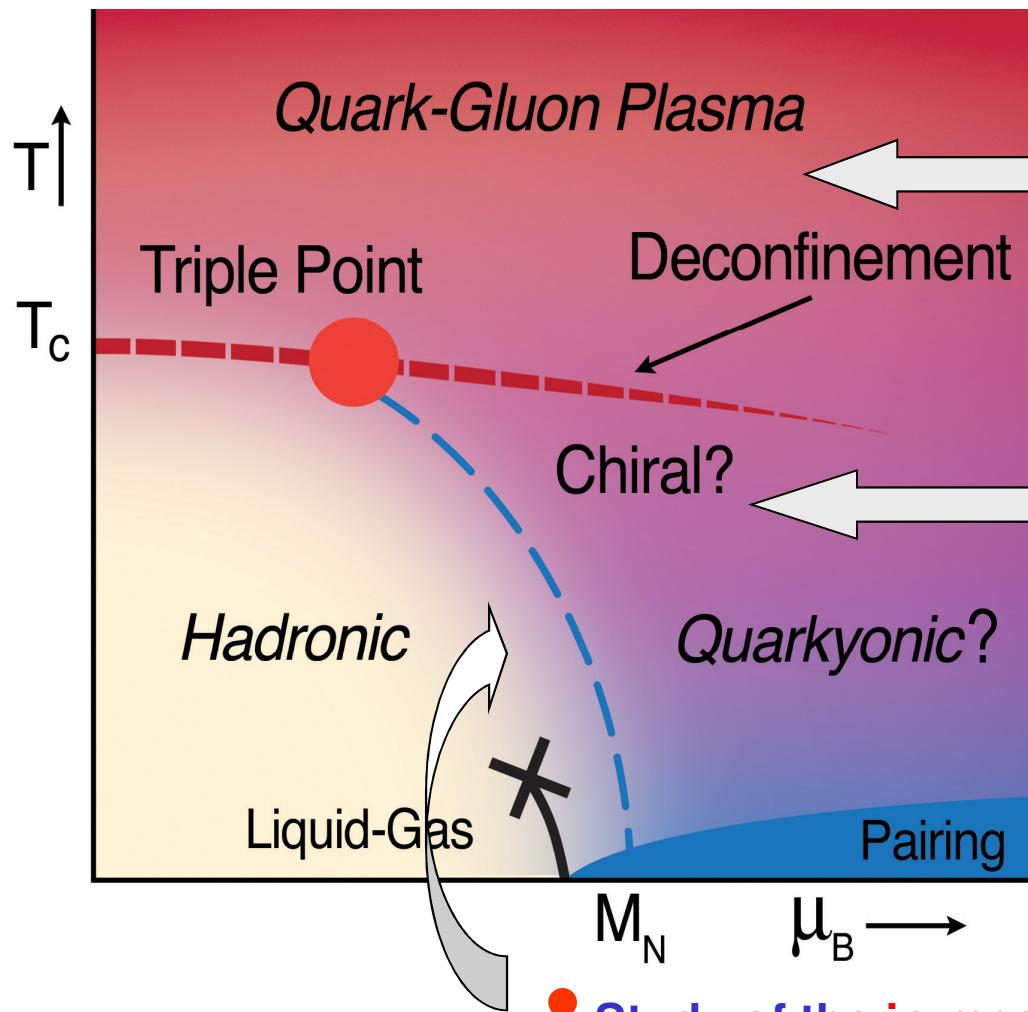


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8-14 January 2017

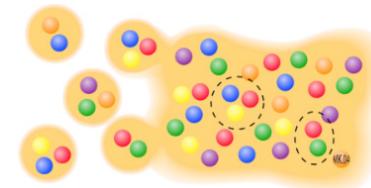


# The 'holy grail' of heavy-ion physics:

The phase diagram of QCD



- Search for the **critical point**



- Study of the **phase transition** from hadronic to partonic matter – **Quark-Gluon-Plasma**

- Search for the signatures of **chiral symmetry restoration**

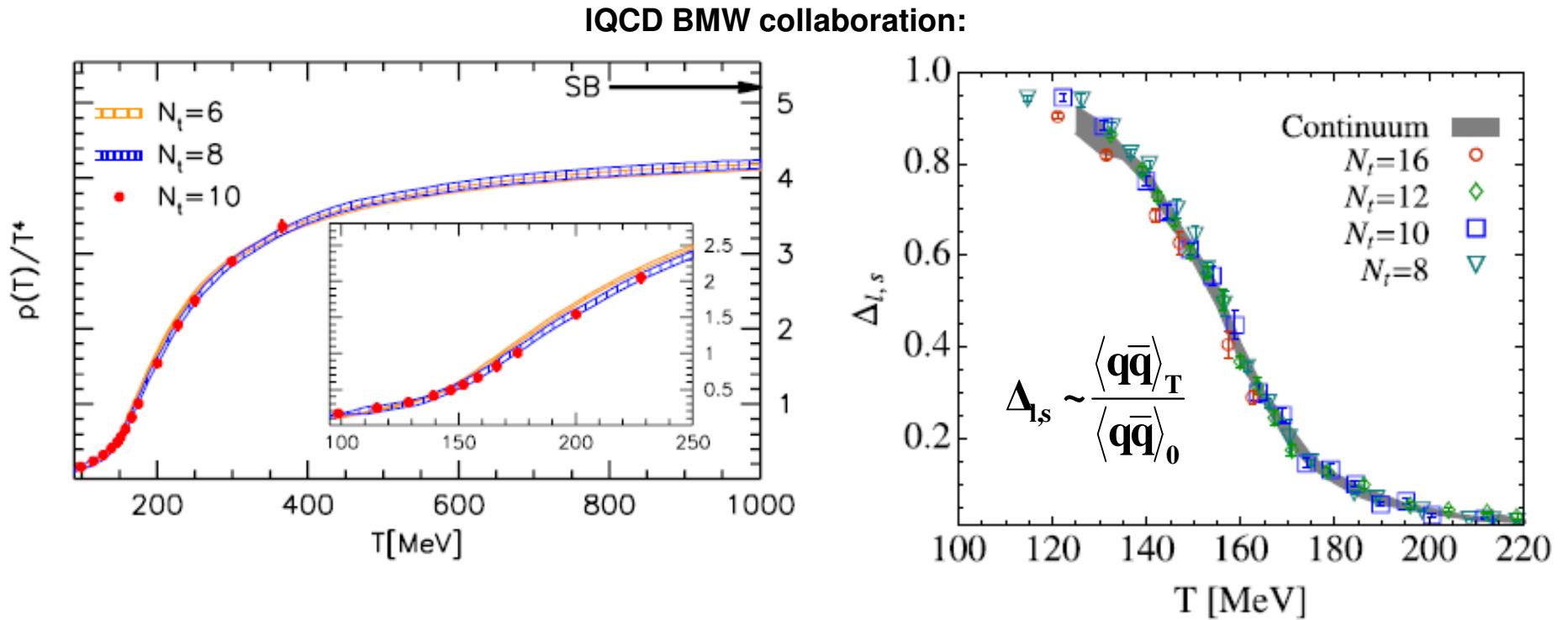
- Study of the **in-medium properties** of hadrons at high baryon density and temperature

# Information from lattice QCD

I. deconfinement phase transition  
with increasing temperature



II. chiral symmetry restoration  
with increasing temperature

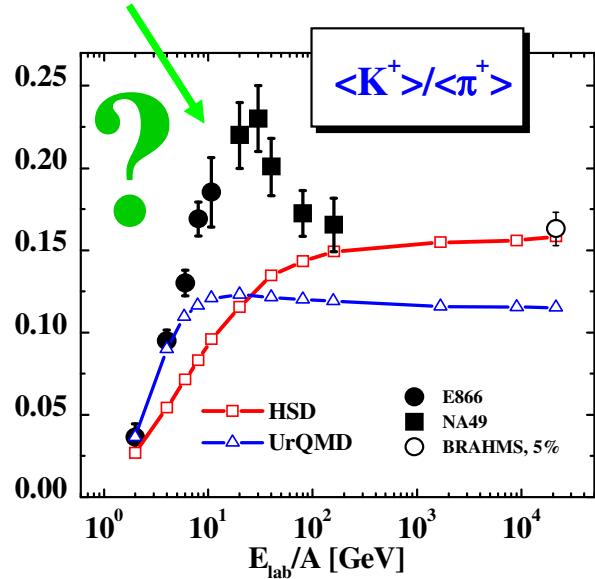


- Scalar quark condensate  $\langle q\bar{q} \rangle$  is viewed as an order parameter for the restoration of chiral symmetry:**
- $$\langle \bar{q}q \rangle = \begin{cases} \neq 0 & \text{chiral non-symmetric phase;} \\ = 0 & \text{chiral symmetric phase.} \end{cases}$$
- Crossover:**  
both transitions occur at about the same temperature  $T_c$  for low chemical potentials

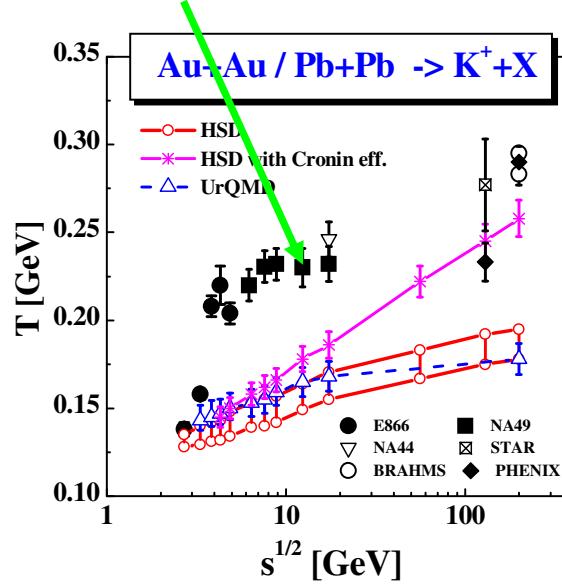
# Signals for the phase transition

**Hadron-string transport models (HSD, UrQMD) versus observables at  $\sim 2000$**

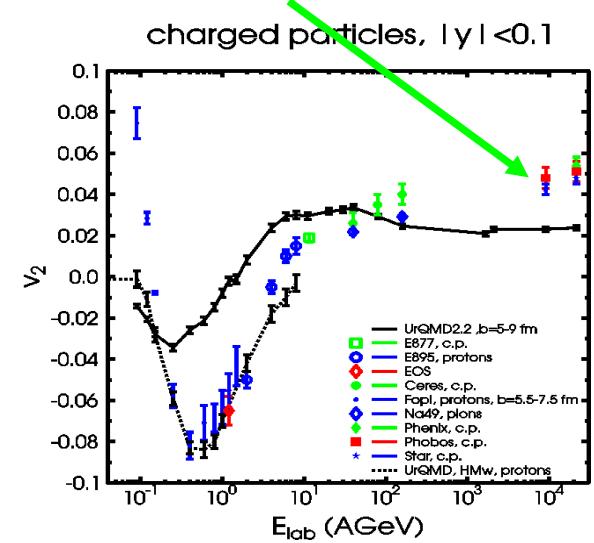
□,horn' in  $K^+/\pi^+$



□ ,step' in slope T



□ elliptic flow  $v_2$



Exp. data are not reproduced in terms of the hadron-string picture  
 → evidence for partonic degrees of freedom + .... ?!

# Dynamical description of heavy-ion collisions

**The goal:**

to study the properties of strongly interacting matter under extreme conditions from a microscopic point of view

**Realization:**

to develop a **dynamical many-body transport approach**

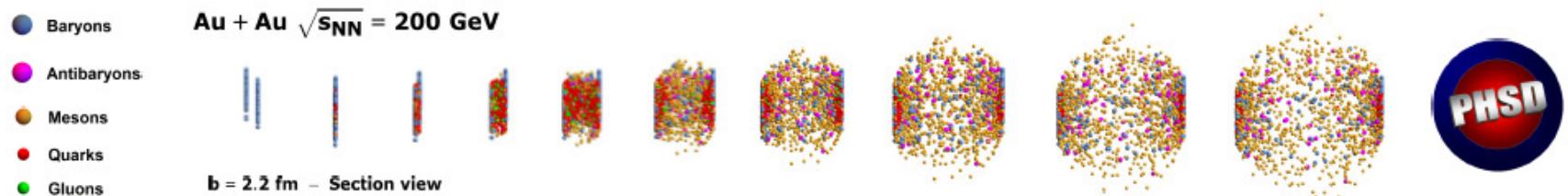
1) applicable for **strongly interacting systems**,

which includes:

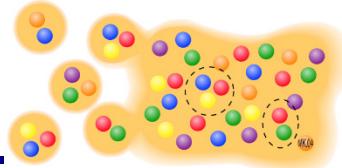
2) **phase transition** from hadronic matter to QGP

3) **chiral symmetry restoration**

2004-2016



# From SIS to LHC: from hadrons to partons



The goal: to study of the phase transition from hadronic to partonic matter and properties of the Quark-Gluon-Plasma on a microscopic level

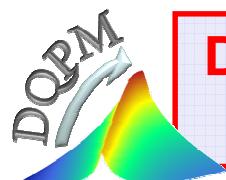
→ need a consistent non-equilibrium transport approach

- with explicit parton-parton interactions (i.e. between quarks and gluons)
- explicit phase transition from hadronic to partonic degrees of freedom
- IQCD EoS for partonic phase ('cross over' at  $\mu_q=0$ )
- Transport theory for strongly interacting systems: off-shell Kadanoff-Baym equations for the Green-functions  $S_h^<(x,p)$  in phase-space representation for the partonic and hadronic phase



**Parton-Hadron-String-Dynamics (PHSD)**

QGP phase is described by



**Dynamical QuasiParticle Model  
(DQPM)**

W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919;  
NPA831 (2009) 215;

W. Cassing, EPJ ST 168 (2009) 3

A. Peshier, W. Cassing, PRL 94 (2005) 172301;  
Cassing, NPA 791 (2007) 365; NPA 793 (2007)

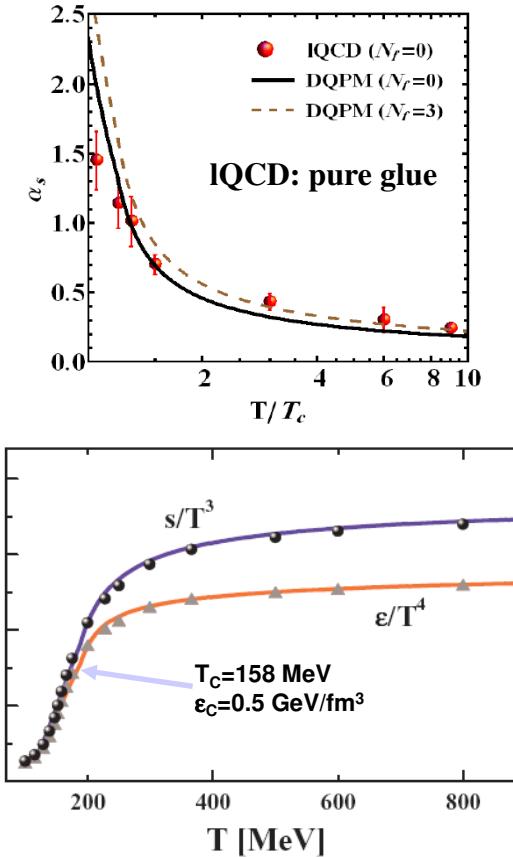
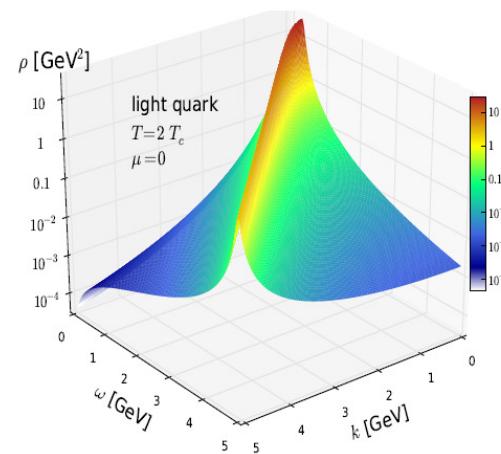
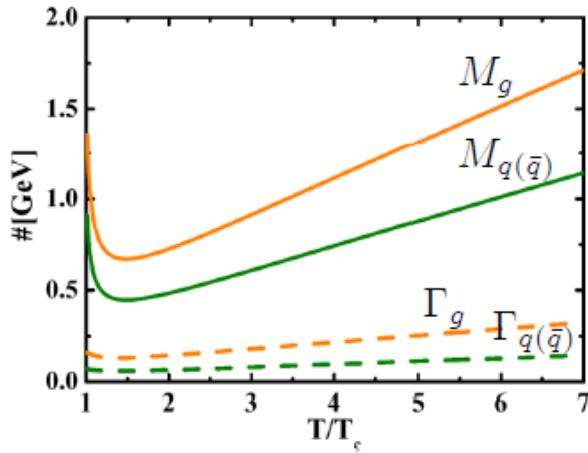
# The Dynamical QuasiParticle Model (DQPM)

- Basic idea: interacting quasi-particles: massive quarks and gluons ( $g, q, \bar{q}$ ) with Lorentzian spectral functions :

$$\rho_i(\omega, T) = \frac{4\omega\Gamma_i(T)}{\left(\omega^2 - \vec{p}^2 - M_i^2(T)\right)^2 + 4\omega^2\Gamma_i^2(T)} \quad (i = q, \bar{q}, g)$$

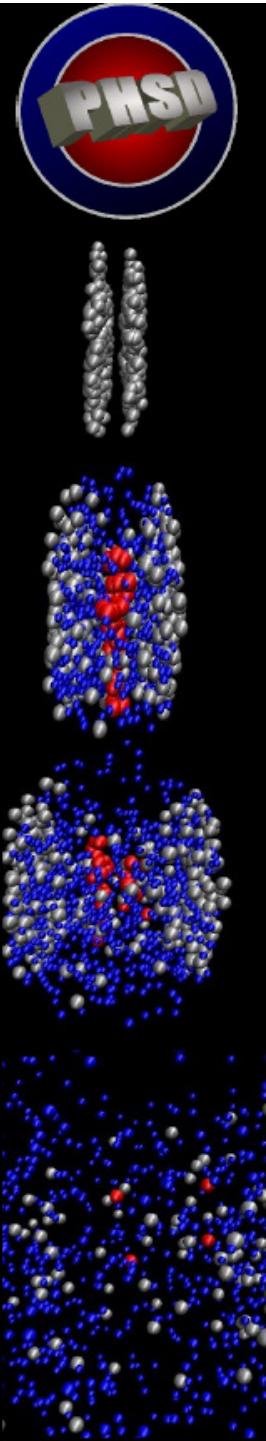
- Modeling of the quark/gluon masses and widths → HTL limit at high T with 3 model parameters – fitted to lattice QCD data

→ Quasi-particle properties:  
large width and mass for gluons and quarks



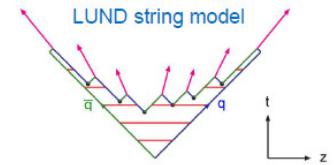
- DQPM provides mean-fields (1PI) for gluons and quarks as well as effective 2-body interactions (2PI)
- DQPM gives transition rates for the formation of hadrons → PHSD

DQPM: Peshier, Cassing, PRL 94 (2005) 172301;  
Cassing, NPA 791 (2007) 365; NPA 793 (2007)

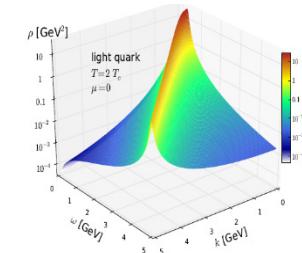


# Parton-Hadron-String-Dynamics (PHSD)

- **Initial A+A collisions :**  
 $N+N \rightarrow$  string formation  $\rightarrow$  decay to pre-hadrons



- **Formation of QGP stage if  $\epsilon > \epsilon_{\text{critical}}$  :**  
dissolution of pre-hadrons  $\rightarrow$  (DQPM)  $\rightarrow$   
**→ massive quarks/gluons + mean-field potential  $U_q$**

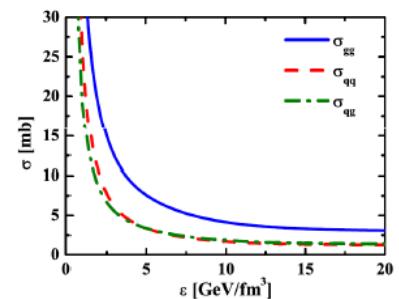
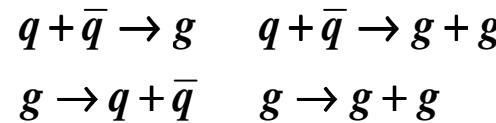


- **Partonic stage – QGP :**  
based on the **Dynamical Quasi-Particle Model (DQPM)**

▪ **(quasi-) elastic collisions:**

$$\begin{array}{ll} q + q \rightarrow q + q & g + q \rightarrow g + q \\ q + \bar{q} \rightarrow q + \bar{q} & g + \bar{q} \rightarrow g + \bar{q} \\ \bar{q} + \bar{q} \rightarrow \bar{q} + \bar{q} & g + g \rightarrow g + g \end{array}$$

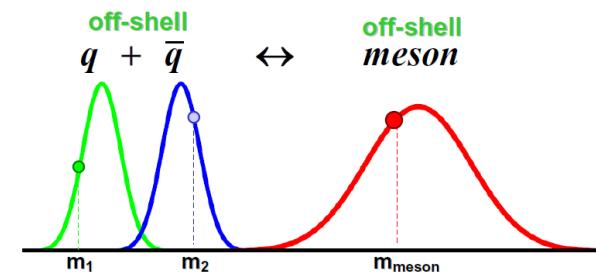
▪ **inelastic collisions:**



- **Hadronization (based on DQPM):**

$$g \rightarrow q + \bar{q}, \quad q + \bar{q} \leftrightarrow \text{meson (or 'string')}$$

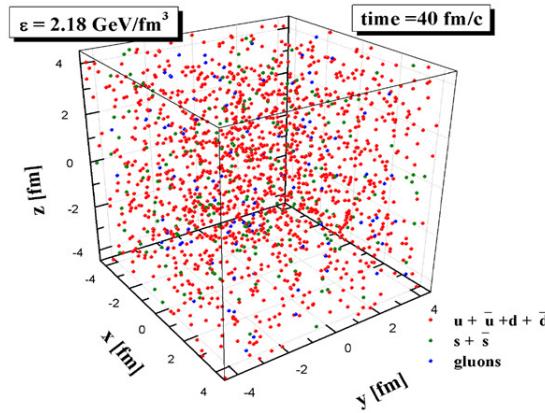
$$q + q + q \leftrightarrow \text{baryon (or 'string')}$$



- **Hadronic phase: hadron-hadron interactions – off-shell HSD**

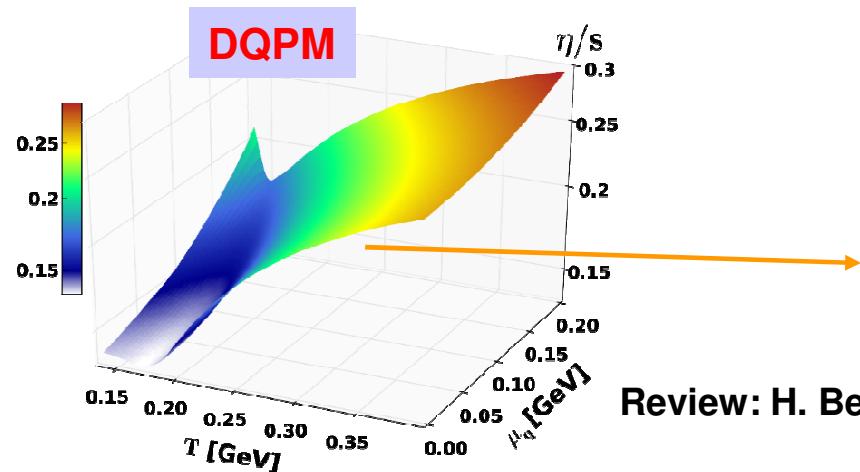
# QGP in equilibrium: Transport properties at finite $(T, \mu_q)$ : $\eta/s$

Infinite hot/dense matter =  
PHSD in a box:



**Shear viscosity  $\eta/s$  at finite  $(T, \mu_q)$**

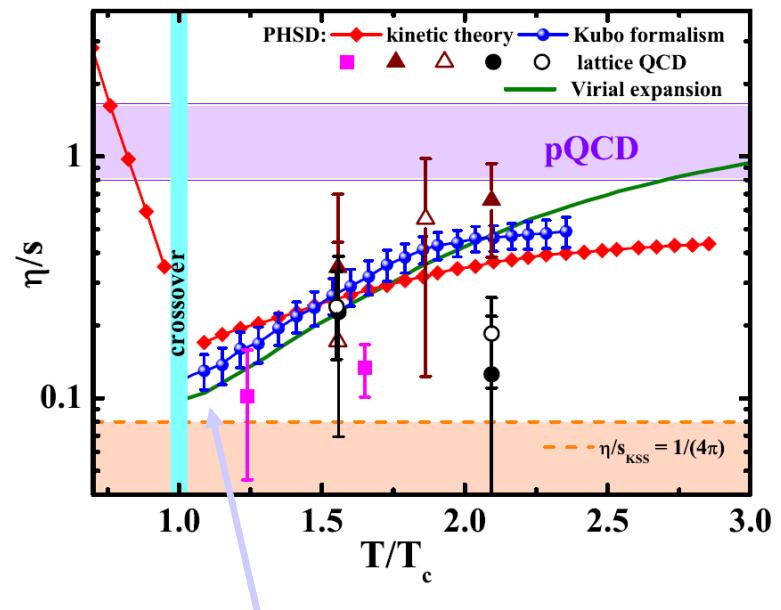
IQCD: 
$$\frac{T_c(\mu_q)}{T_c(\mu_q = 0)} = \sqrt{1 - \alpha \mu_q^2} \approx 1 - \alpha/2 \mu_q^2 + \dots$$



Review: H. Berrehrah et al. Int.J.Mod.Phys. E25 (2016) 1642003

**Shear viscosity  $\eta/s$  at finite  $T$**

V. Ozvenchuk et al., PRC 87 (2013) 064903

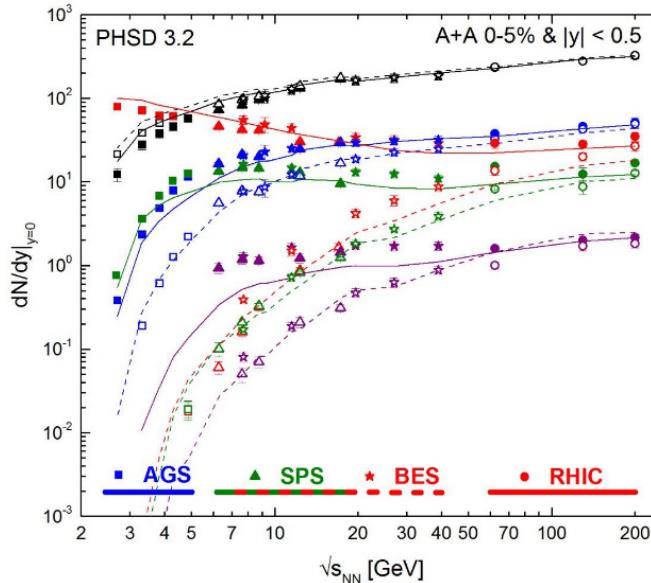


**QGP in PHSD = strongly-interacting liquid-like system**

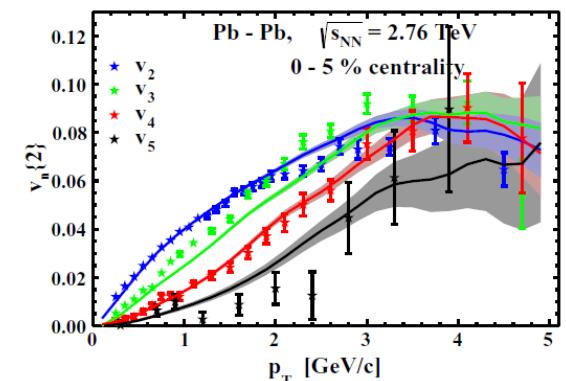
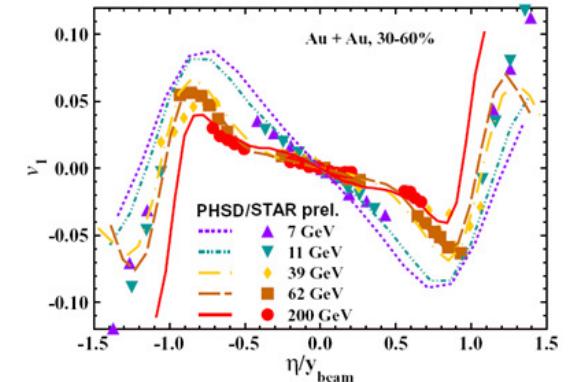
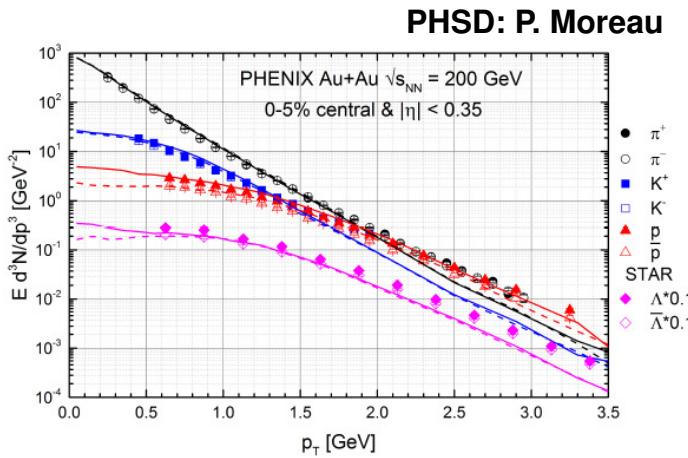
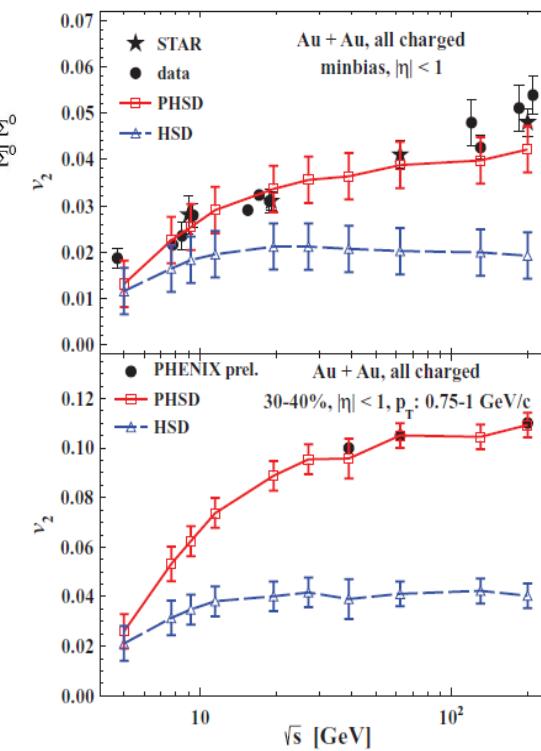
$\eta/s$ :  $\mu_q=0 \rightarrow$  finite  $\mu_q$ : smooth increase as a function of  $(T, \mu_q)$



# Non-equilibrium dynamics: description of A+A with PHSD



## □ PHSD: highlights



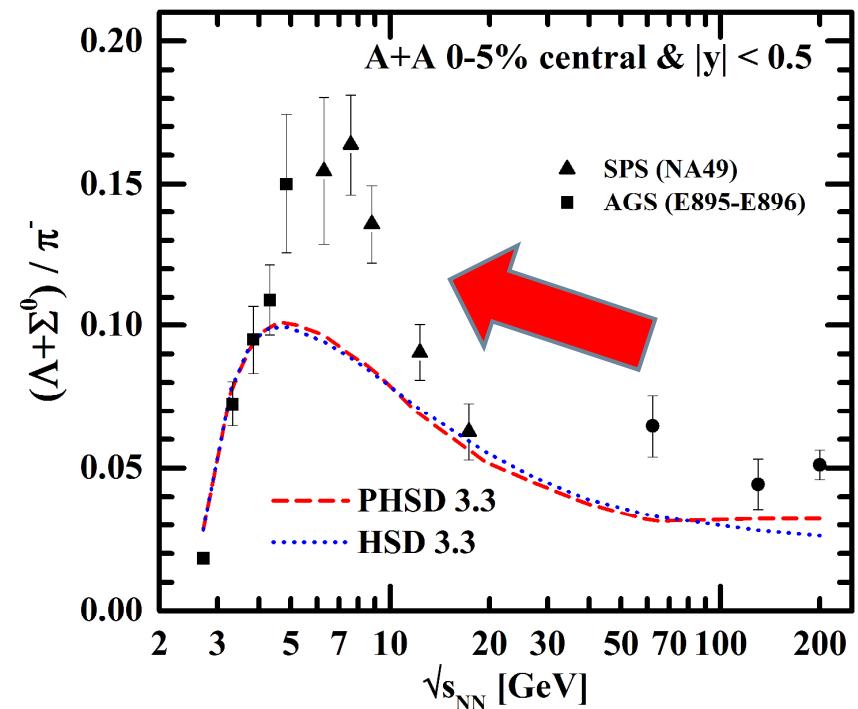
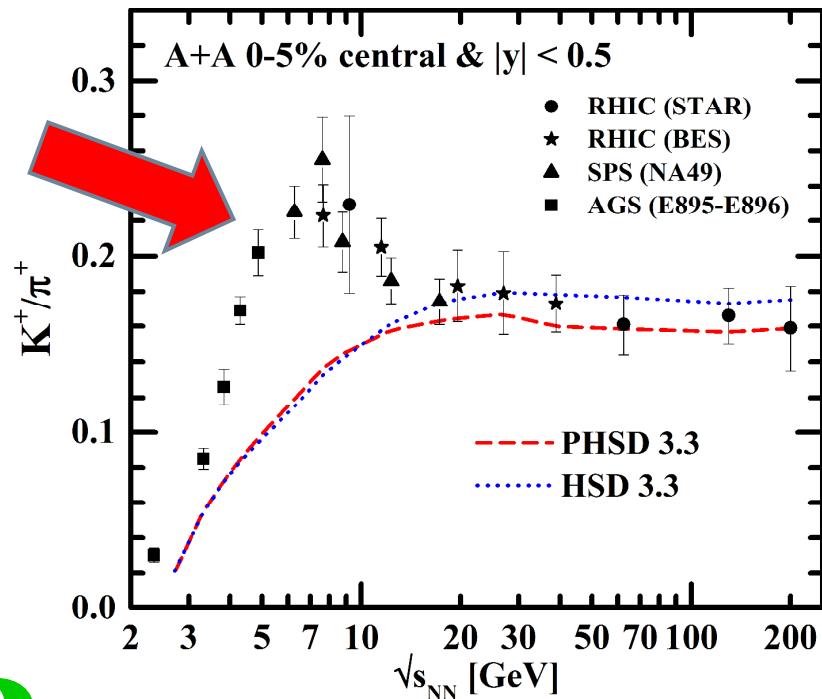
V. Konchakovski et al.,  
PRC 85 (2012) 011902; JPG42 (2015) 055106

□ PHSD provides a good description of 'bulk' observables ( $y$ -,  $p_T$ -distributions, flow coefficients  $v_n$ , ...) from SIS to LHC

## Problem: $K^+/\pi^+$ , horn' – 2015

**PHSD:** even when considering the creation of a QGP phase, the  $K^+/\pi^+$ , horn' seen experimentally by NA49 and STAR at a bombarding energy  $\sim 30$  A GeV (FAIR/NICA energies!) remains unexplained !

→ The origin of 'horn' is not traced back to deconfinement ?!

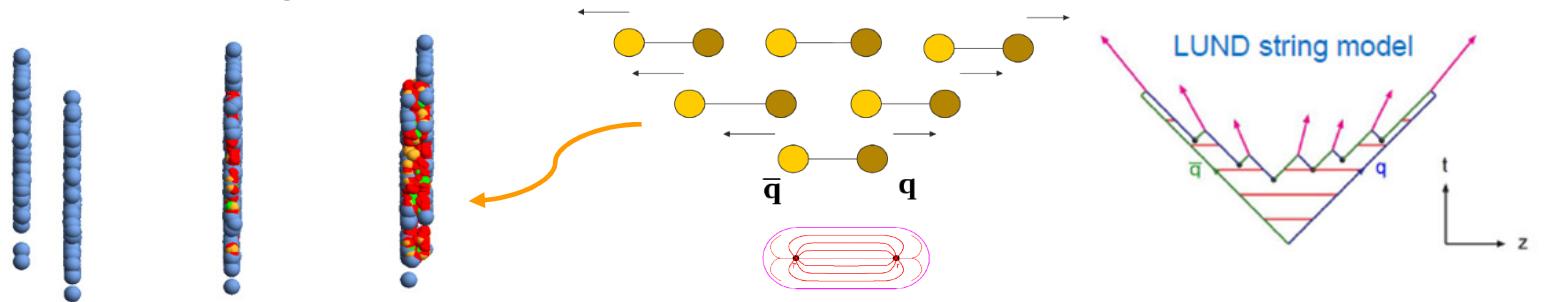


Can it be related to chiral symmetry restoration in the hadronic phase?!



# Chiral symmetry restoration via Schwinger mechanism

- Initial stage of HIC: string formation



- the 'flavor chemistry' of the final hadrons in the PHSD is mainly defined by the LUND string model
- 'quark flavor chemistry' in the LUND model is determined by the Schwinger-formula
- According to the Schwinger-formula, the probability to form a massive  $s\bar{s}$  pair in a string-decay is suppressed in comparison to a light flavor pair ( $u\bar{u}, d\bar{d}$ ) :

$$\frac{P(s\bar{s})}{P(u\bar{u})} = \frac{P(s\bar{s})}{P(d\bar{d})} = \gamma_s = \exp\left(-\pi \frac{m_s^2 - m_q^2}{2\kappa}\right)$$

with  $\kappa$ - string tension;  
in vacuum:  $\kappa \sim 0.9 \text{ GeV/fm} = 0.176 \text{ GeV}^2$

- $m_s, m_q$  ( $q=u,d$ ) – constituent ('dressed') quark masses



# Dressing of the quark masses

- $m_s, m_q$  ( $q=u,d$ ) – constituent ('dressed') quark masses: 'dressing' of bare quark masses is due to the coupling to the scalar quark condensate  $\langle q\bar{q} \rangle$ :

## I. In vacuum (e.g. p+p collisions) :

$$m_q^V = m_q^0 - g_s \langle q\bar{q} \rangle_V$$

bare quark masses:

$$m_u^0 = m_d^0 \approx 7 \text{ MeV}, \quad m_s^0 \approx 100 \text{ MeV}$$

vacuum scalar quark condensate

fixed from Gell-Mann-Oakes-Renner

relation  $f_\pi^2 m_\pi^2 = -\frac{1}{2} (m_u^0 + m_d^0) \langle \bar{q}q \rangle_V$

$$\rightarrow \langle q\bar{q} \rangle_V \approx -3.2 \text{ fm}^{-3}$$

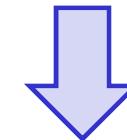
→ Constituent quark masses in vacuum :

$$(m_q \equiv m_q^V) \quad m_u^V = m_d^V \approx 0.35 \text{ GeV}, \quad m_s^V \approx 0.5 \text{ GeV}$$

## II. In medium (e.g. A+A collisions) :

In the presence of a hot and dense hadronic medium, the degrees of freedom modify their properties, e.g. the in-medium constituent quark masses:

$$m_q^* = m_q^0 - g_s \langle q\bar{q} \rangle \quad (q=u,d,s)$$



$$m_q^* = m_q^0 + (m_q^V - m_q^0) \frac{\langle q\bar{q} \rangle}{\langle q\bar{q} \rangle_V}$$

\* mean-field results (1PI)



# Scalar quark condensate in the hadronic medium

- The behavior of the scalar quark condensate  $\langle q\bar{q} \rangle$  in the **hadronic medium (baryons + mesons)** can be obtained e.g. from

B. Friman et al., Eur. Phys. J. A 3, 165, 1998

**non-linear  $\sigma - \omega$  model:**

$$\frac{\langle q\bar{q} \rangle}{\langle q\bar{q} \rangle_V} = 1 - \frac{\Sigma_\pi}{f_\pi^2 m_\pi^2} \rho_S - \sum_h \frac{\sigma_h \rho_S^h}{f_\pi^2 m_\pi^2}$$

baryonic  
medium

mesonic  
medium

- $\rho_s$  is the **scalar density of baryonic matter** :

from non-linear  $\sigma - \omega$  model:

$$m_\sigma^2 \sigma(x) + B \sigma^2(x) + C \sigma^3(x) = g_s \rho_S = g_s d \int \frac{d^3 p}{(2\pi)^3} \frac{m_N^*(x)}{\sqrt{p^2 + m_N^{*2}}} f_N(x, p)$$

$$m_N^*(x) = m_N^V - g_s \sigma(x)$$

where  $\Sigma_\pi \approx 45$  MeV

is the pion-nucleon  $\Sigma$ -term,  
 $\sigma_h = m_\pi/2$  for light mesons;  
 $= m_\pi/4$  - strange mesons

Scalar field  $\sigma(x)$  mediates the scalar interaction of baryons with the surrounding medium with a  $g_s$  coupling

from PHSD

- $\sigma(x)$  is determined locally by solution of the nonlinear gap equation ;
- parameters  $g_s$ ,  $m_\sigma$ ,  $B$ ,  $C$  are fixed to reproduce the main nuclear matter quantities, i.e. saturation density, binding energy per nucleon, compression modulus and the effective nucleon mass.

- $\rho_s^h$  is the **scalar density of mesons** of type  $h \rightarrow$  from PHSD



# Scalar quark condensate in HIC

PHSD:

Ratio of the scalar quark condensate

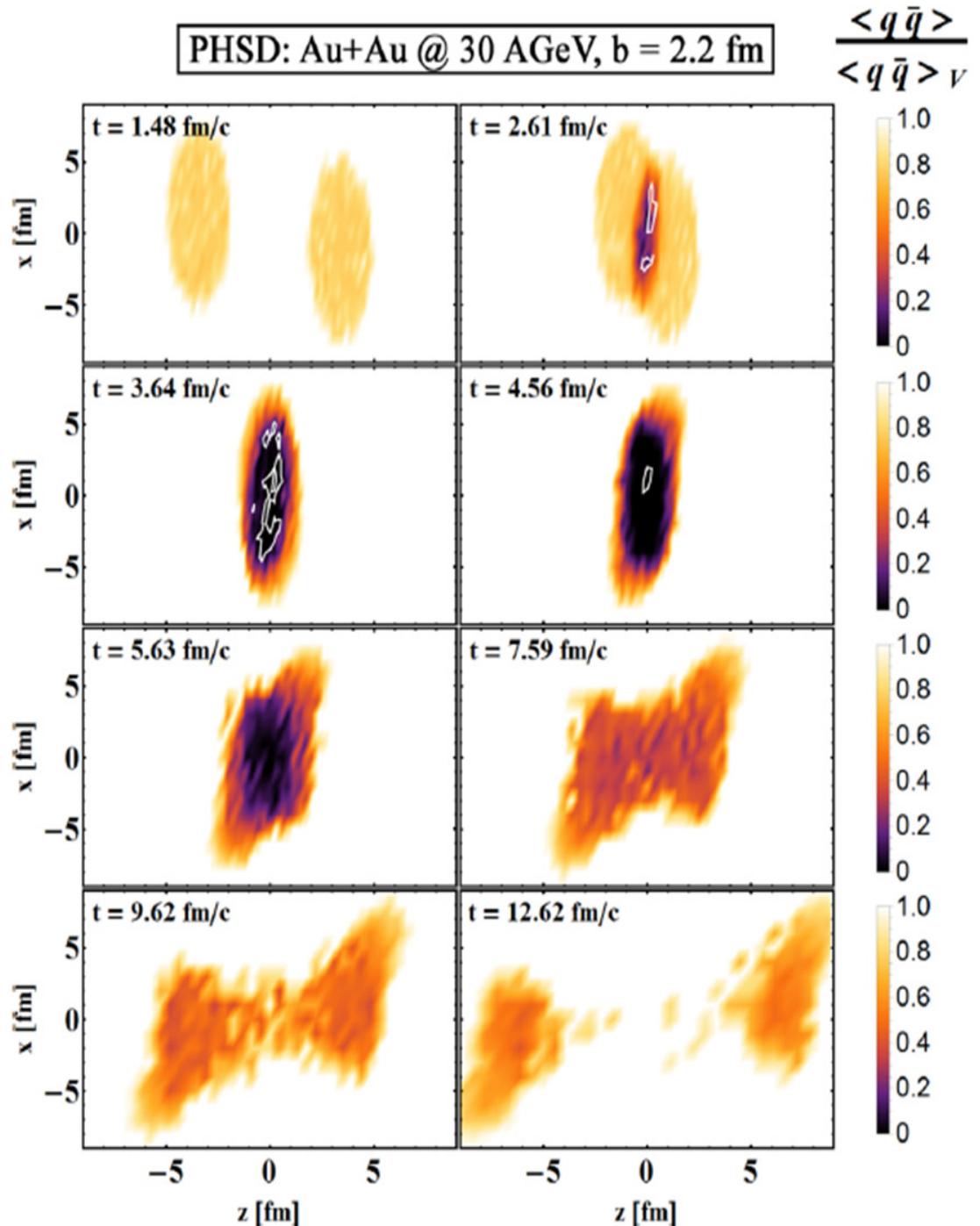
$$\frac{\langle q \bar{q} \rangle}{\langle q \bar{q} \rangle_V}$$

compared to the vacuum as a function of  $x, z$  ( $y=0$ ) at different time  $t$  for central Au+Au collisions at 30 AGeV



- restoration of chiral symmetry:  
 $\langle q \bar{q} \rangle / \langle q \bar{q} \rangle_V \rightarrow 0$

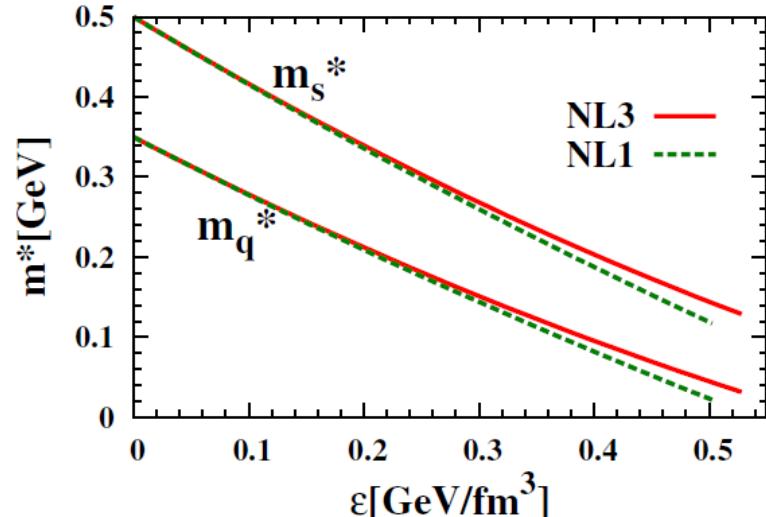
PHSD: Au+Au @ 30 AGeV,  $b = 2.2$  fm



# Modeling of the chiral symmetry restoration in PHSD

- HIC: in the **Schwinger formula** the **in-medium constituent masses**  $m^*_{q,s}$  (instead of vacuum  $m_{q,s}$ ) have to be considered:

$$\frac{P(s\bar{s})}{P(u\bar{u})} = \frac{P(s\bar{s})}{P(d\bar{d})} = \gamma_s = \exp\left(-\pi \frac{m_s^{*2} - m_q^{*2}}{2\kappa}\right)$$



→ Strangeness ratio  $s/u$

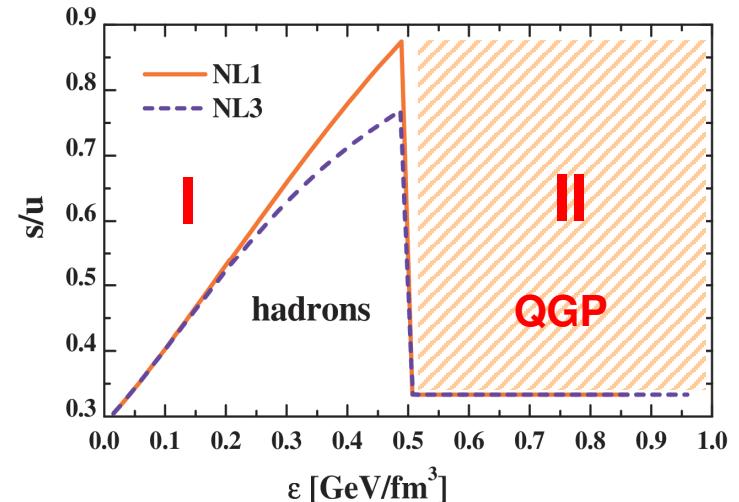
I. hadronic phase :  $\epsilon < \epsilon_c$

As a consequence of the **chiral symmetry restoration (CSR)**, the **strangeness production probability increases** with the local energy density  $\epsilon$ .

II. QGP:  $\epsilon > \epsilon_c$

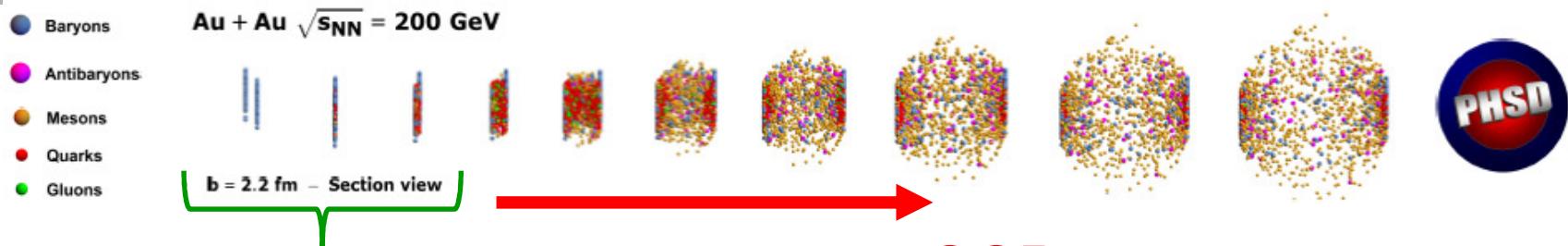
In the **QGP** phase, the string formation doesn't occur anymore and this effect is therefore suppressed

The strangeness ratio  $s/u$  in the string decay

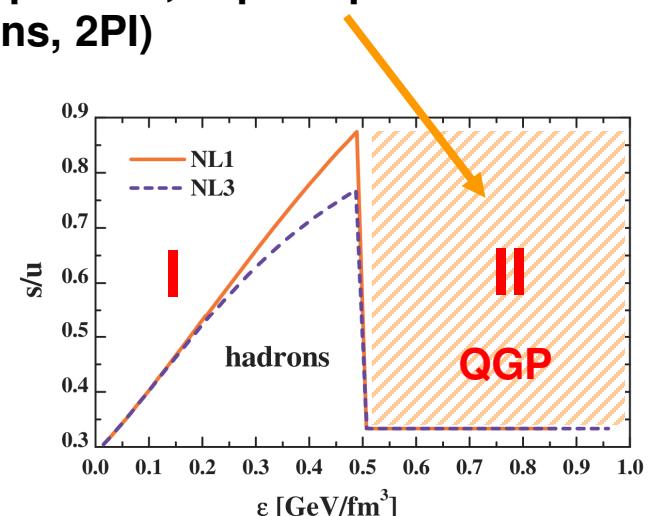
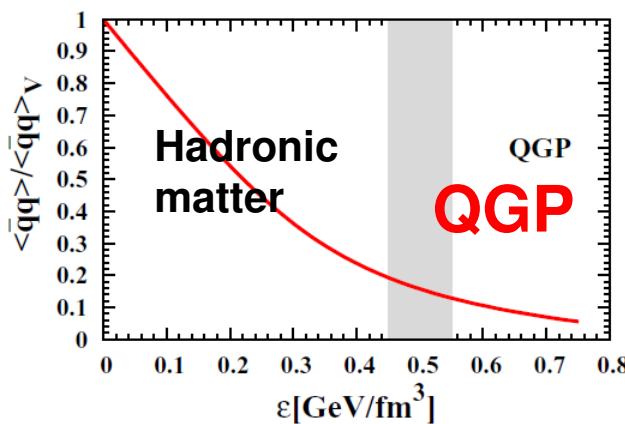
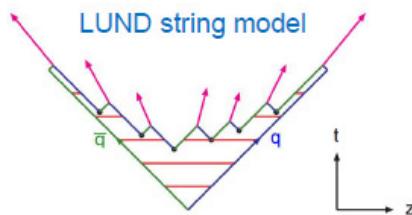




# Chiral symmetry restoration vs. deconfinement



**I. Initial stage of HIC collisions:**  
Hadronic matter → string formation

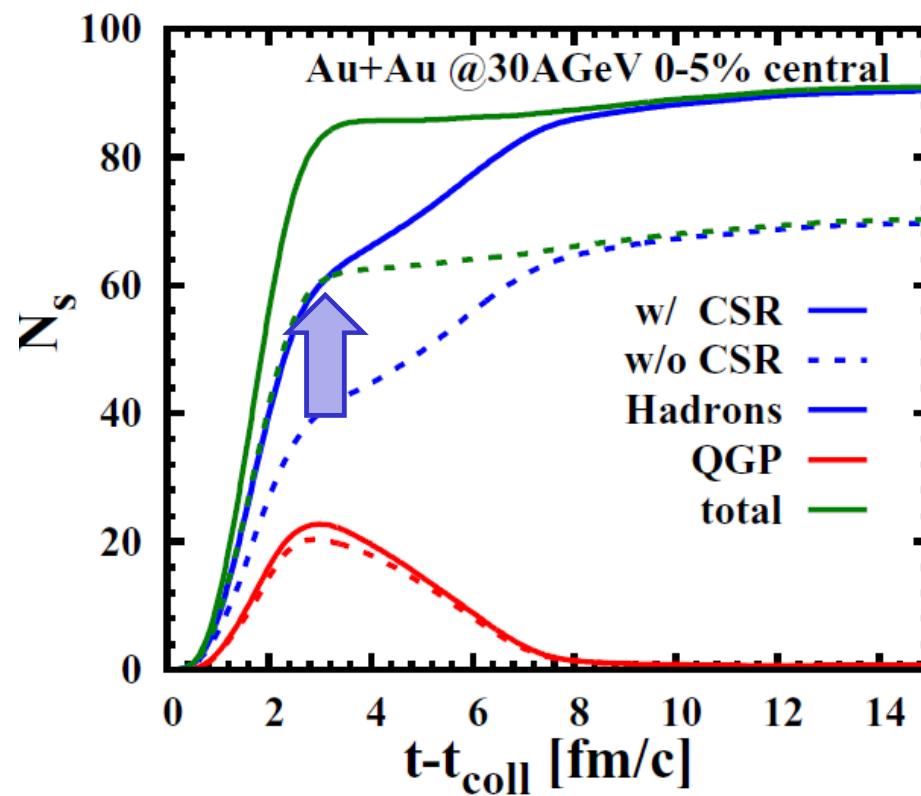


- Chiral symmetry restoration via **Schwinger mechanism** (and non-linear  $\sigma - \omega$  model) changes the „flavour chemistry“ in string fragmentation (1PI):
 
$$\langle q\bar{q} \rangle / \langle q\bar{q} \rangle_V \rightarrow 0 \rightarrow m_s^* \rightarrow m_s^0 \rightarrow s/u \text{ grows}$$

→ the **strangeness production probability increases** with the local energy density  $\varepsilon$ .

## Time evolution of strangeness

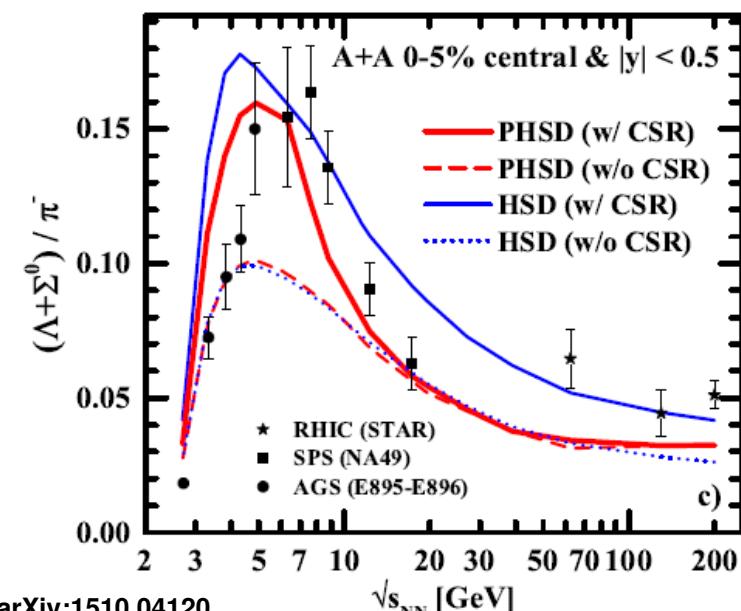
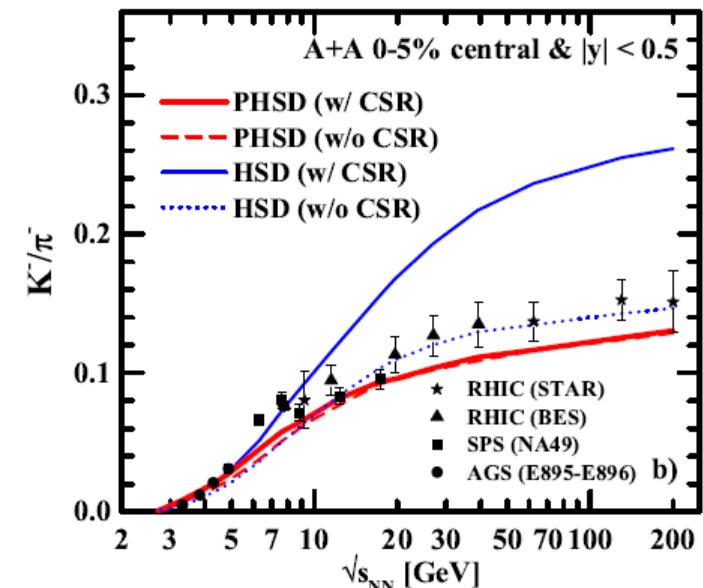
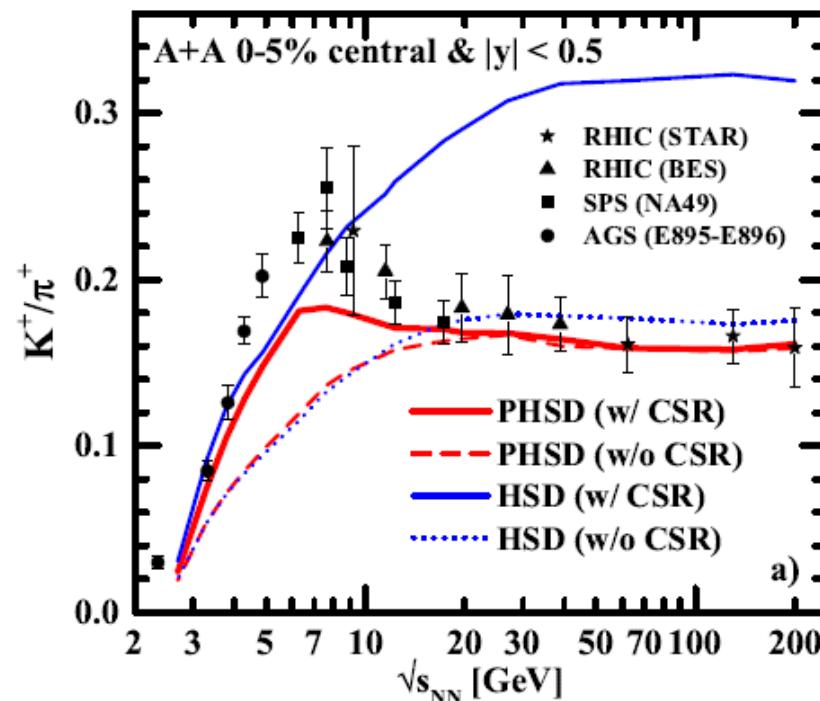
The strange particle number  $N_s$  as a function of time in 5% central Au+Au collision at 30 AGeV



Chiral symmetry restoration leads to the enhancement of strangeness production during the string fragmentation in the beginning of HIC

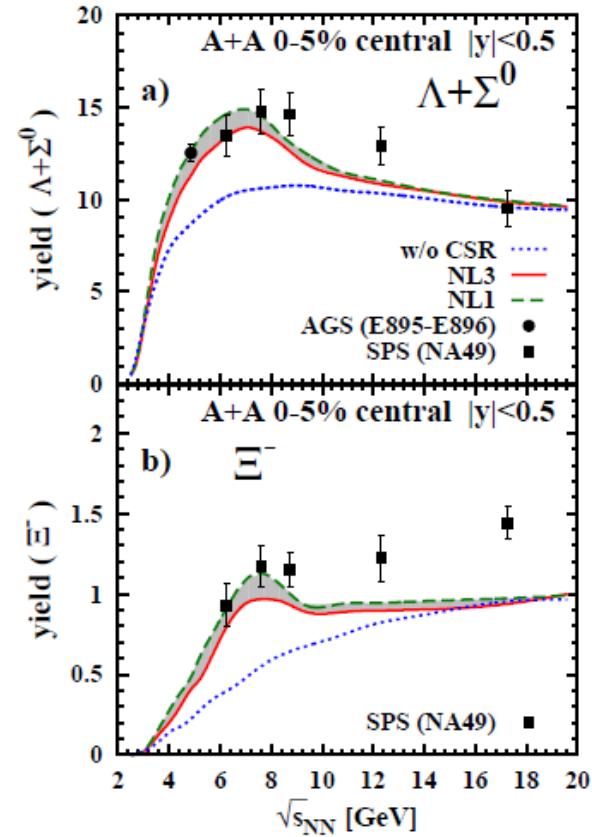
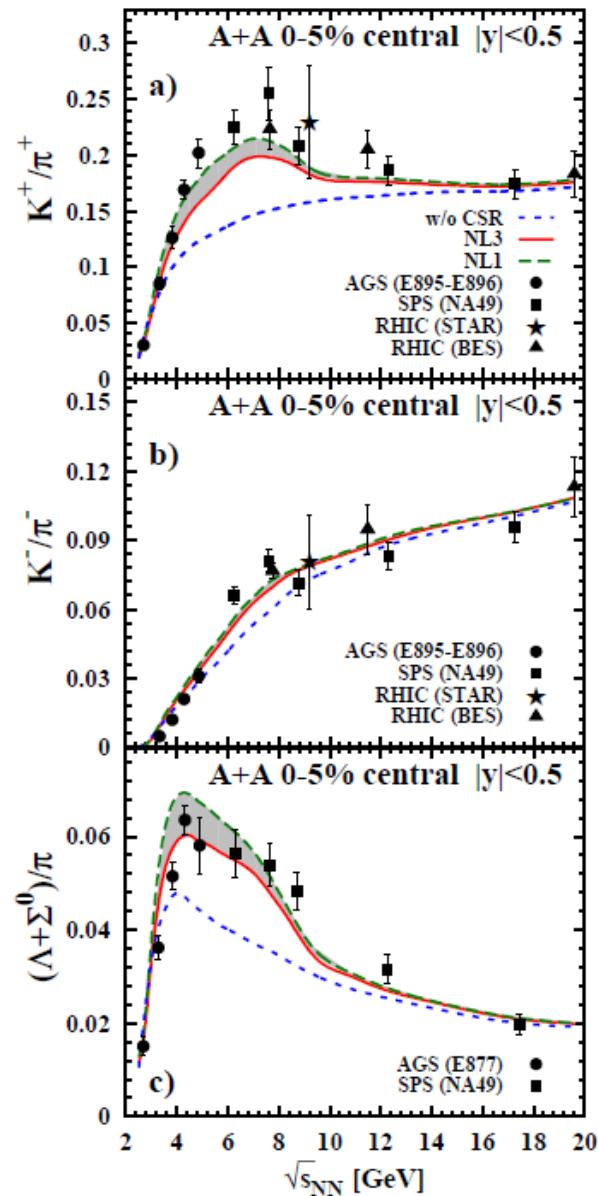


# PHSD results with chiral symmetry restoration



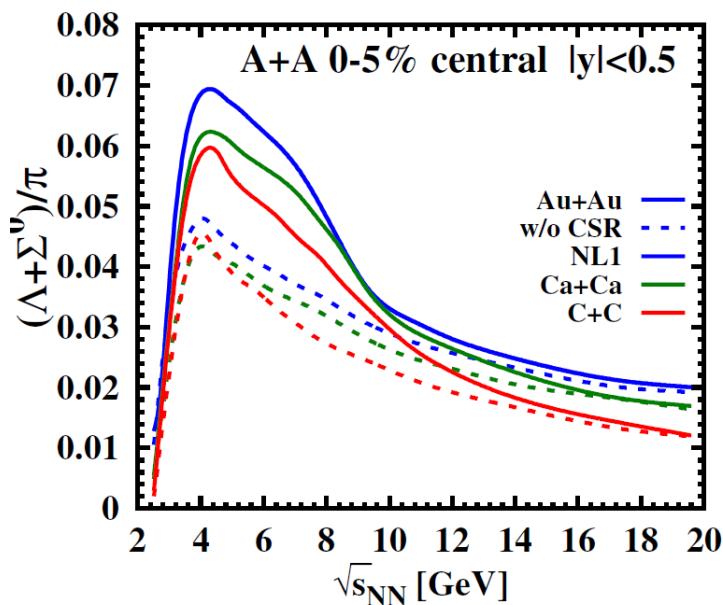
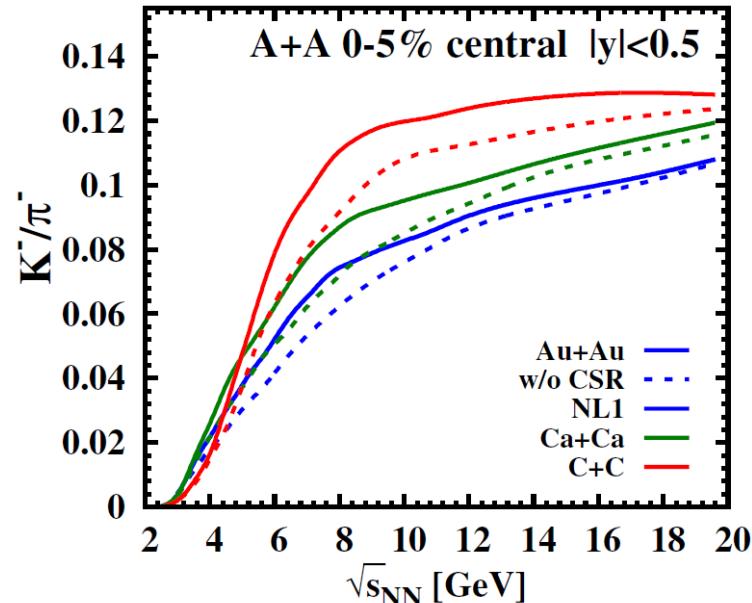
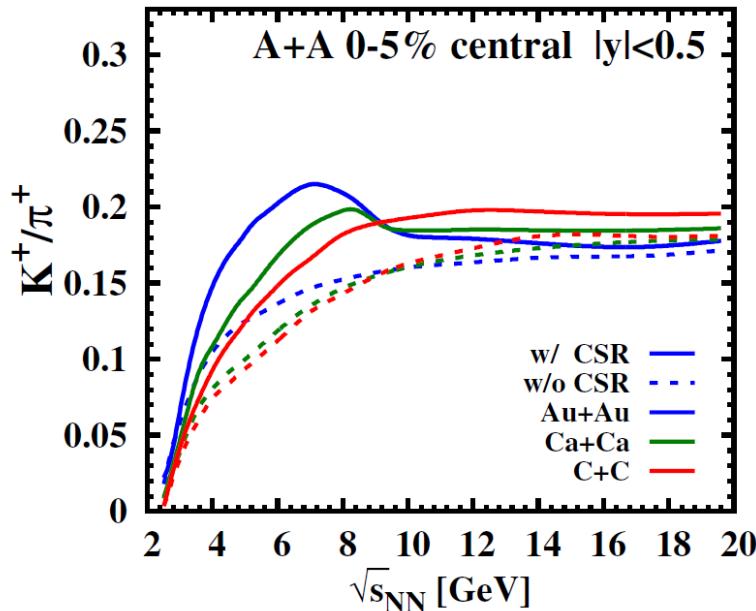
→ The **strangeness enhancement** seen experimentally at FAIR/NICA energies probably involves the approximate **restoration of chiral symmetry** in the hadronic phase

# Excitation function of hadron ratios and yields



- Influence of EoS: NL1 vs NL3 → low sensitivity to the nuclear EoS
- Excitation function of the hyperons  $\Lambda+\Sigma^0$  and  $\Xi^-$  show analogous peak as  $K^+/\pi^+$ ,  $(\Lambda+\Sigma^0)/\pi$  ratios due to CSR

# Sensitivity to the system size: A+A collisions

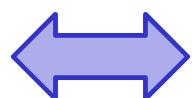
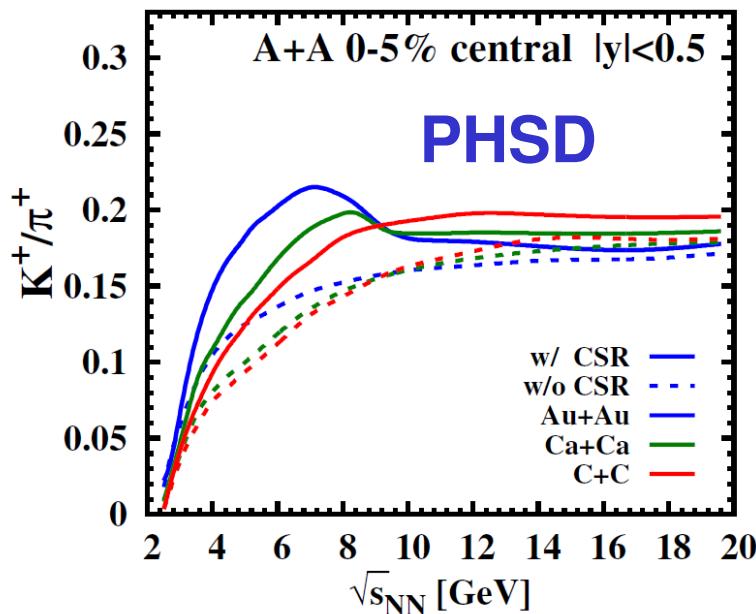


If the **system size is smaller**:

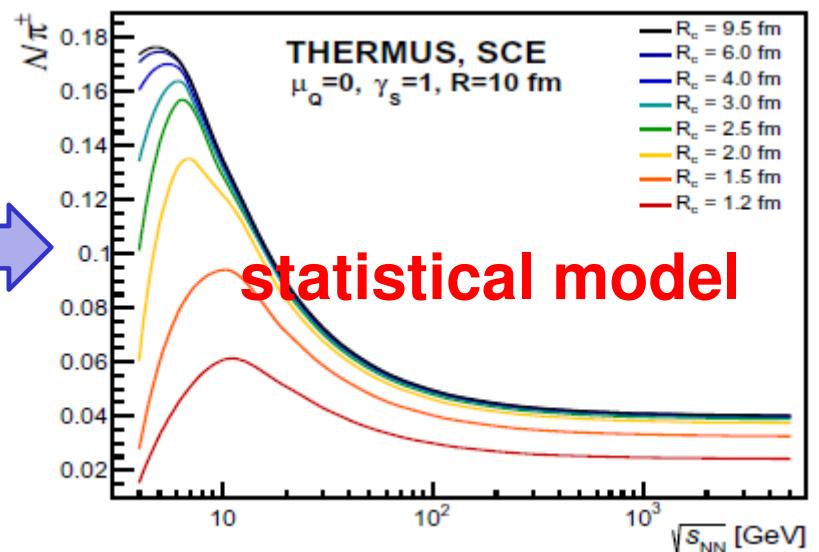
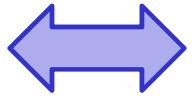
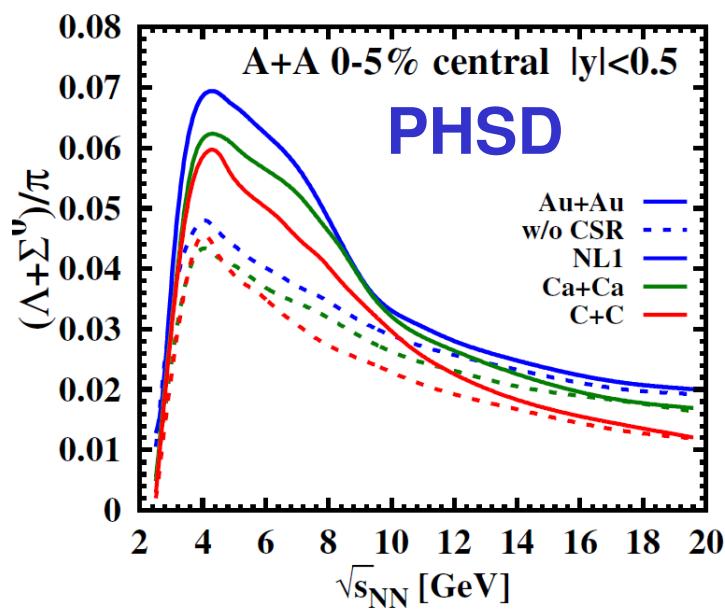
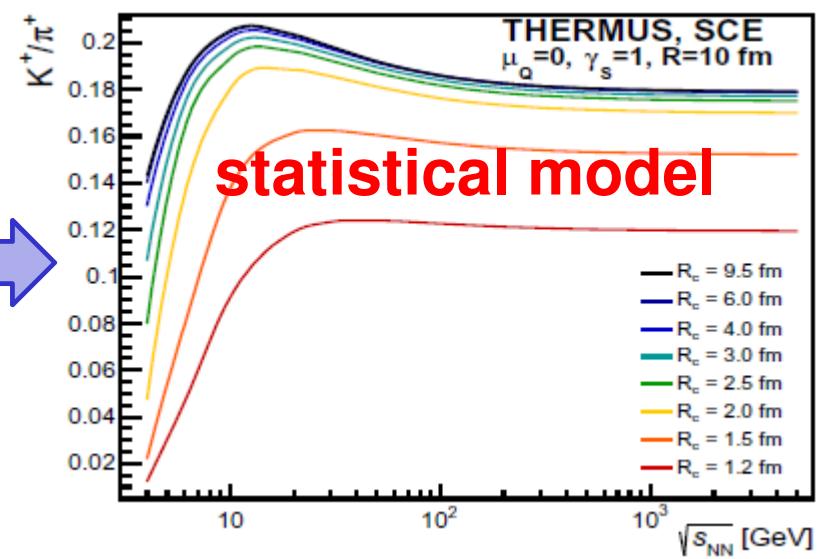
- the peak of  $K^+/\pi^+$  disappears
- the peak of  $(\Lambda+\Sigma^0)/\pi$  remains in the same position in energy, but getting smaller



## PHSD vs. statistical model

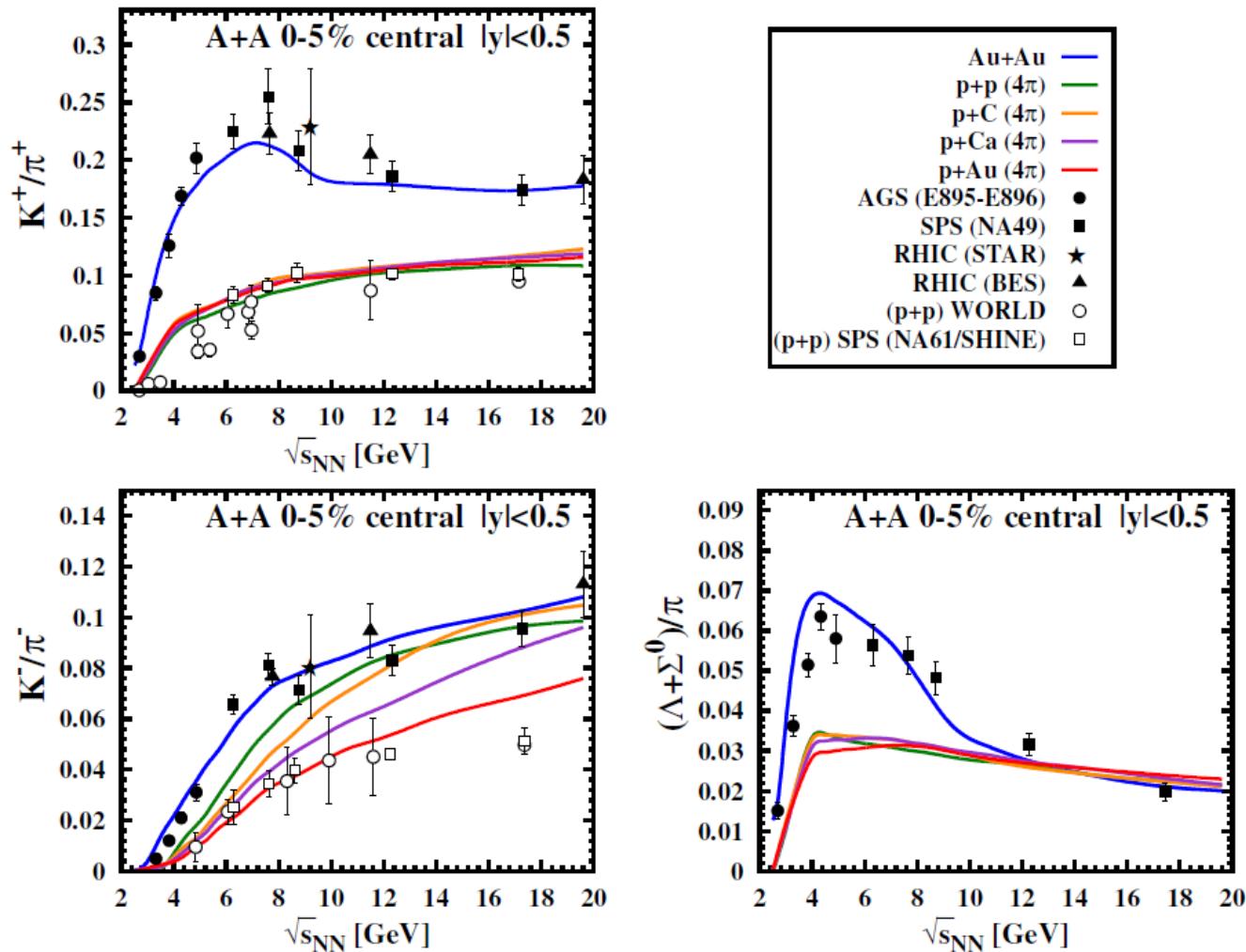


THERMUS: J. Cleymans et al., arXiv:1603.09553



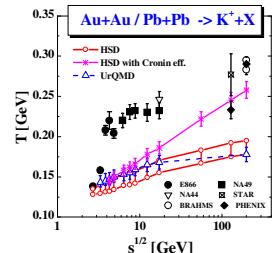
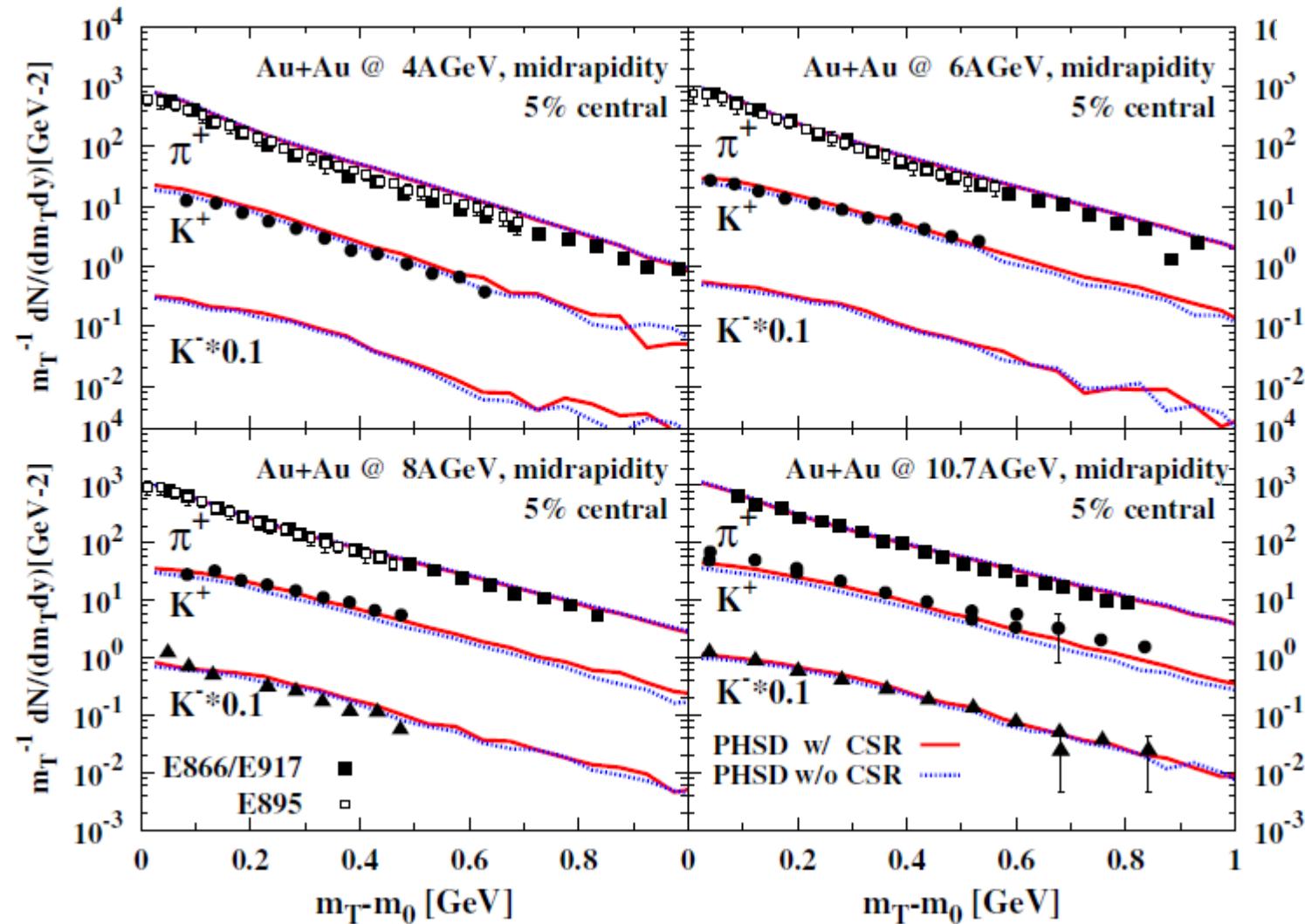
# Sensitivity to the system size: p+A collisions

- In p+A collisions strange to non-strange particle ratios show no peaks



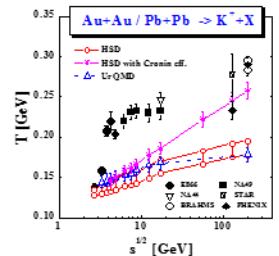
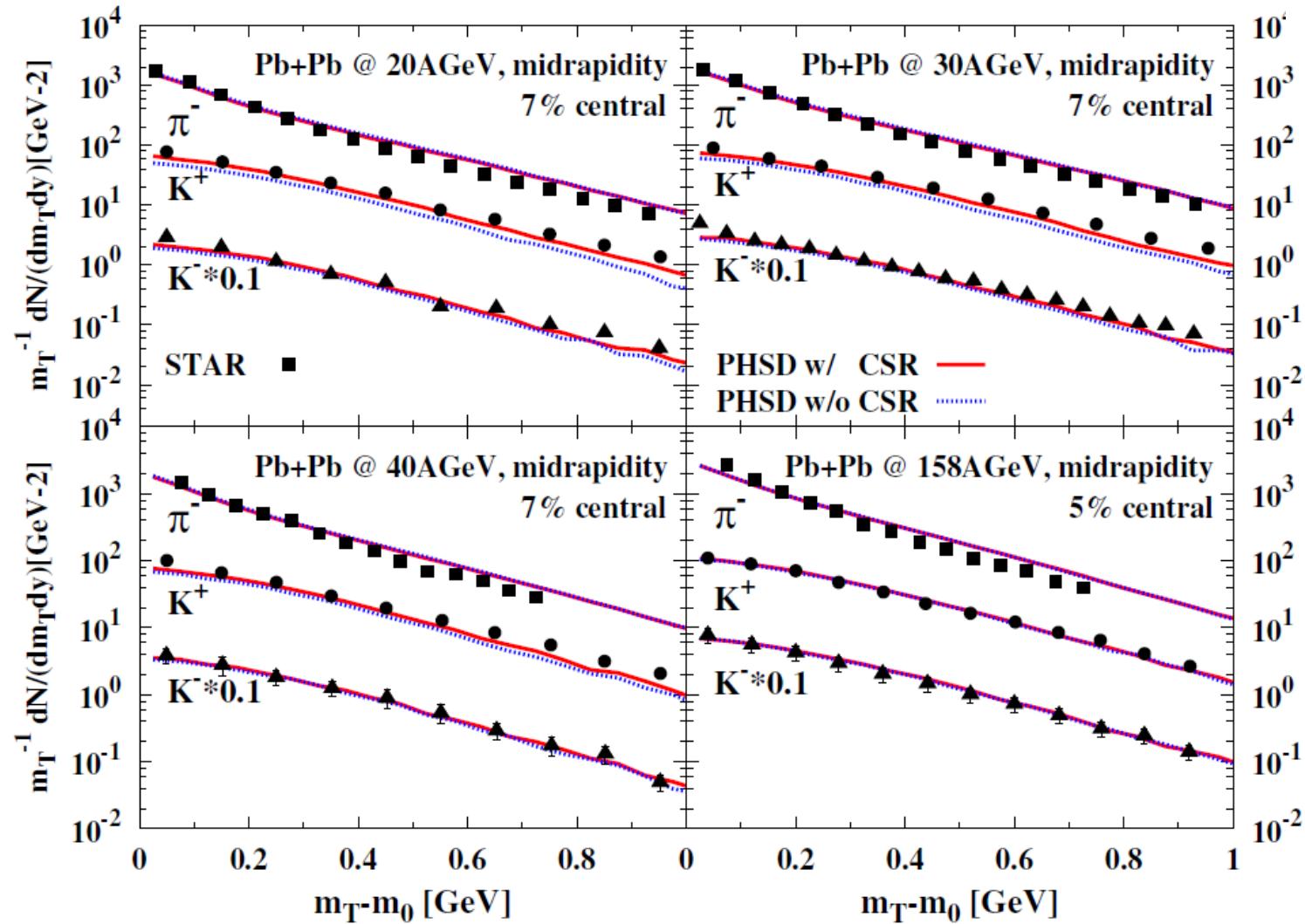


# $m_T$ spectra of pions and $K^{+/-}$ at AGS energies



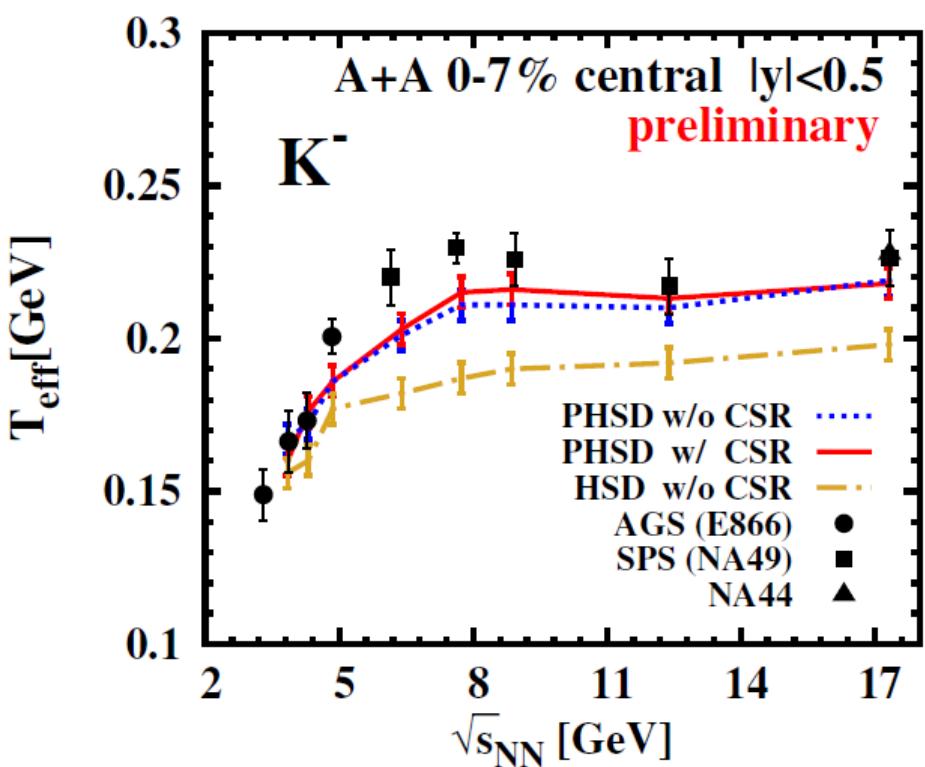
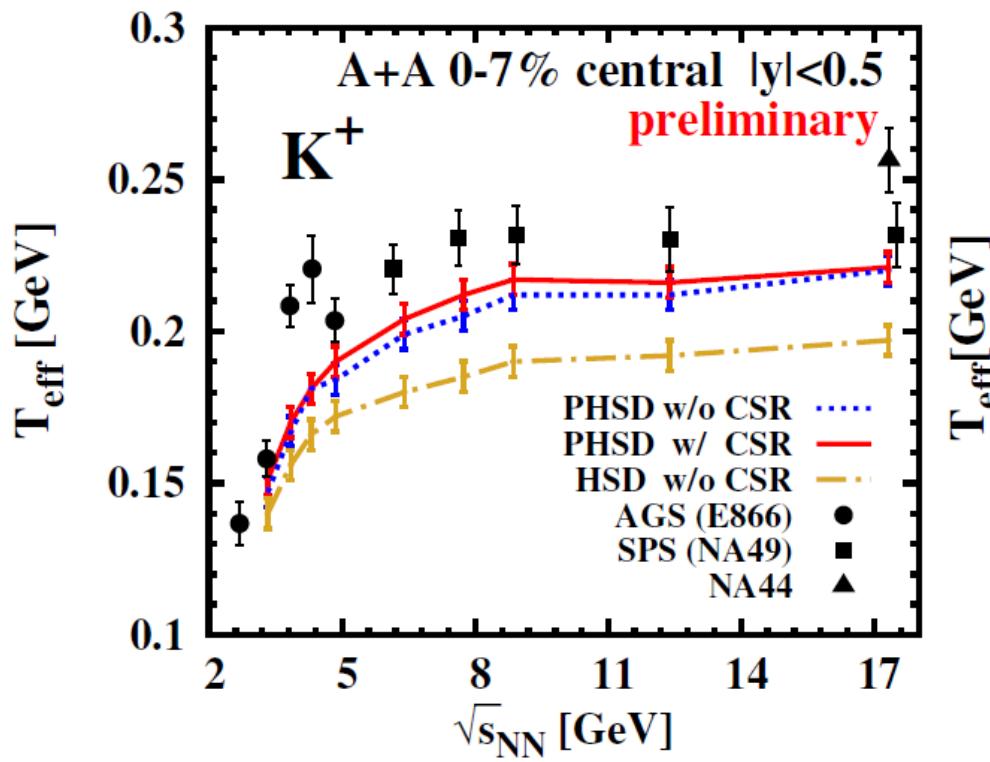


# $m_T$ spectra of pions and $K^{+/-}$ at SPS energies



# Excitation function of $T_{\text{eff}}$

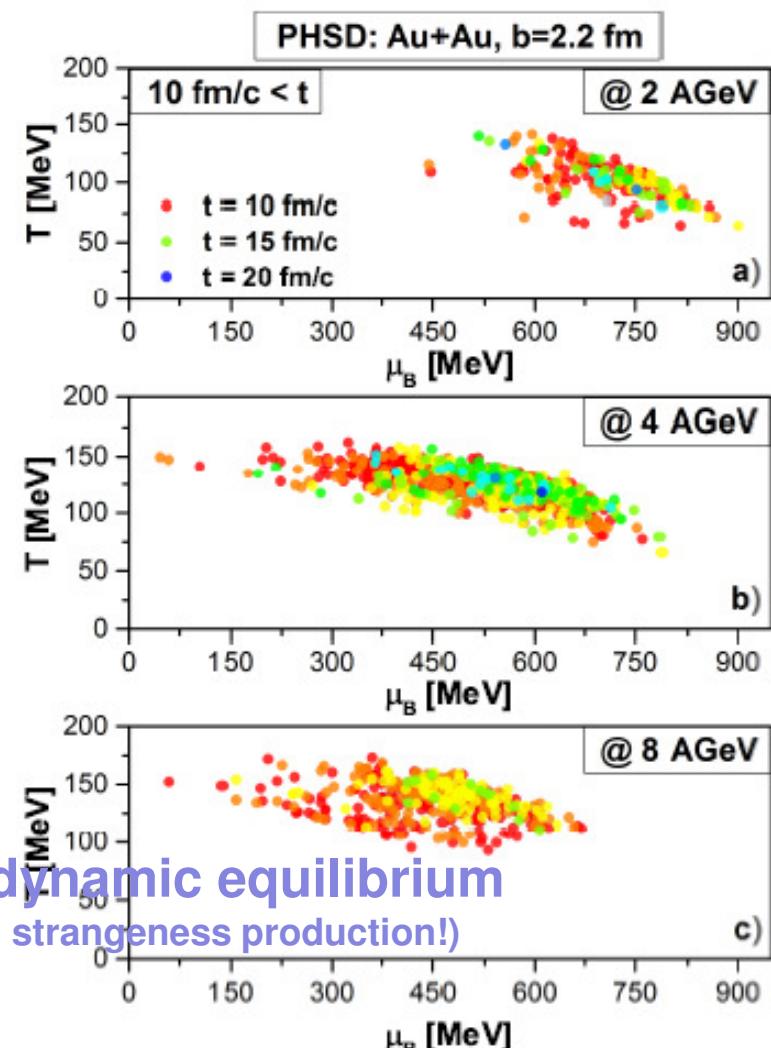
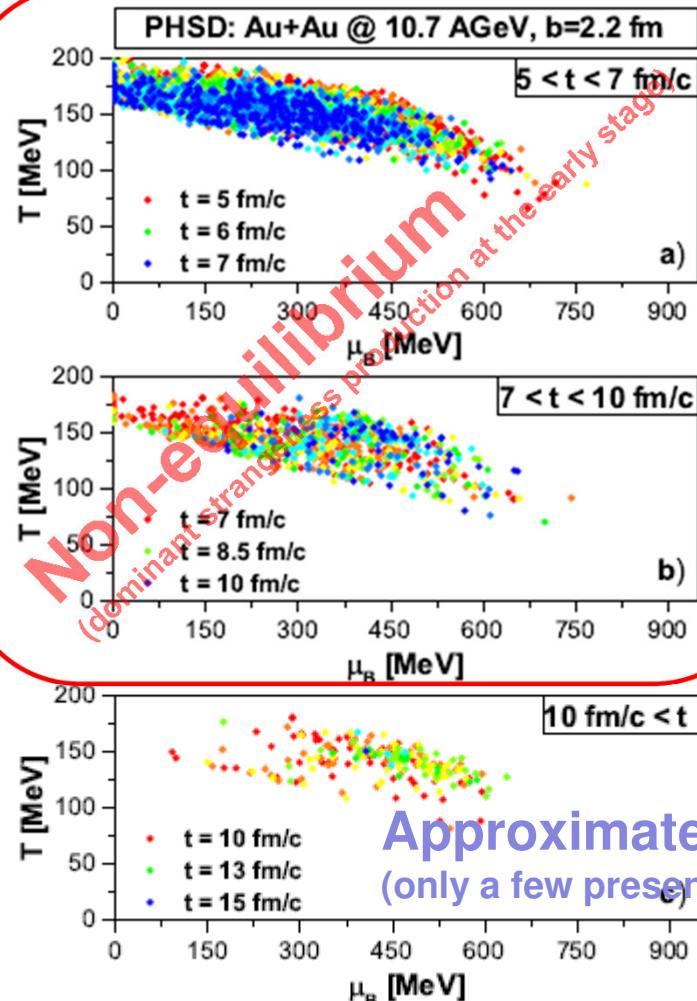
Alessia Palmese



- Increase of slope  $T_{\text{eff}}$  due to the QGP
- Small effect of chiral symmetry restoration on slope  $T_{\text{eff}}$

# Thermodynamics of strangeness in HIC

Which parts of the phase diagram in the  $(T, \mu_B)$ -plane are probed by heavy-ion collisions via the strangeness production?



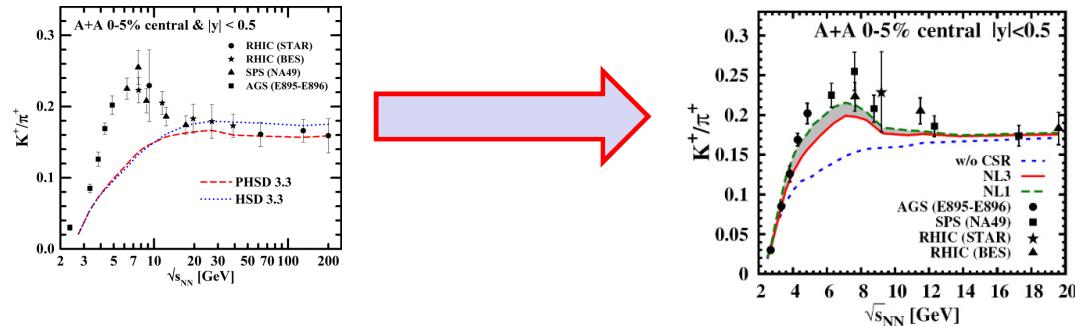
Approximate thermodynamic equilibrium  
(only a few present of the total strangeness production!)

\* T here corresponds to the pion, nucleon gas,  
i.e. a real T is smaller!

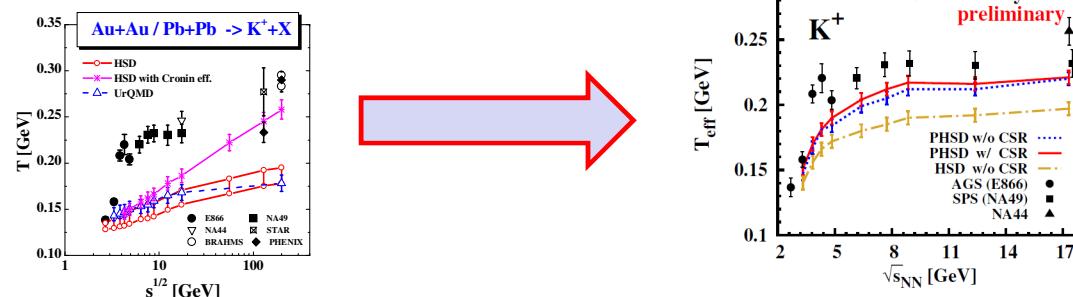
→ the spread in T and  $\mu_B$  is very large !



# Summary



- The **strangeness ‘enhancement’ (‘horn’)** seen experimentally by NA49 and STAR at a bombarding energy  $\sim$ 20-30 A GeV (FAIR/NICA energies!) cannot be attributed to deconfinement
- Including essential aspects of **chiral symmetry restoration** in the hadronic phase, we observe a **rise in the  $K^+/\pi^+$  ratio** at low  $\sqrt{s_{NN}}$  and then a **drop** due to the appearance of a deconfined partonic medium  $\rightarrow$  a ‘**horn**’ emerges
- Hardening of  $m_T$  spectra due to the **QGP**



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# PHSD group

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Elena Bratkovskaya  
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Thorsten Steinert  
Alessia Palmese  
Eduard Seifert  
Olena Linnyk



## External Collaborations

SUBATECH, Nantes University:

Jörg Aichelin  
Christoph Hartnack  
Pol-Bernard Gossiaux  
Marlene Nahrgang

Texas A&M University:

Che-Ming Ko

JINR, Dubna:

Viacheslav Toneev  
Vadim Voronyuk

Valencia University:

Daniel Cabrera

Barcelona University:

Laura Tolos  
Angel Ramos

Duke University:

Steffen Bass

