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LHC Higgs XS WG – 11th Workshop

15 January 2016

- Chiral Lagrangian and power counting
- Linear vs. nonlinear
- Higgs couplings
- Section outline

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# LHCHXSWG – Yellow Report 4

## Working Group 2 – Nonlinear EFT

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# Leading-order Lagrangian

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$$\begin{aligned}\mathcal{L}_{LO} = & -\frac{1}{2}\langle G_{\mu\nu}G^{\mu\nu}\rangle - \frac{1}{2}\langle W_{\mu\nu}W^{\mu\nu}\rangle - \frac{1}{4}B_{\mu\nu}B^{\mu\nu} + \bar{\psi}i\not{D}\psi \\ & + \frac{v^2}{4}\langle D_\mu U^\dagger D^\mu U\rangle (1 + F_U(h/v)) + \frac{1}{2}\partial_\mu h\partial^\mu h - V(h) \\ & - v \left[ \sum_{n=0}^{\infty} \bar{q}\hat{Y}_u^{(n)}UP_{+r} \left(\frac{h}{v}\right)^n + \text{h.c.} + \dots \right]\end{aligned}$$

- $U = \exp(2i\varphi^a T^a / v)$ ,  $F_U(h/v) = \sum_{n=1}^{\infty} f_n (h/v)^n$ , etc.
- SM:  $f_1 = 2$ ,  $f_2 = 1$ ,  $f_{n>2} = 0$ , etc.
- deviations  $\sim \xi \equiv \frac{v^2}{f^2}$ ;  $\xi \sim 10\%$  still allowed
- $\mathcal{L}_{LO}$  non-renormalizable, cut-off  $\Lambda = 4\pi f \rightarrow \text{EW}\chi\text{L}$

- **particle content** of SM, mass gap  
gauge bosons and fermions weakly coupled to Higgs dynamics
- **symmetries**: SM gauge symmetries  
conservation of lepton and baryon number  
conservation *at lowest order* of custodial symmetry,  
CP invariance in the Higgs sector, (fermion flavour).
- **power counting** by chiral dimensions  $\Leftrightarrow$  loop expansion

# Loop counting $\equiv$ chiral counting

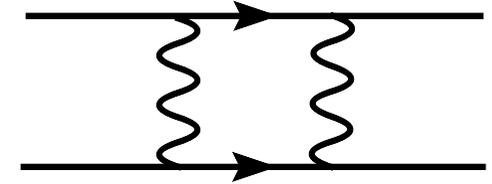
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*Urech; Nyffeler, Schenk; Hirn, Stern; G.B., Catà, Krause*

chiral dimensions:  $[A_\mu, \varphi, h]_c = 0, \quad [\partial_\mu, g, y, \psi\bar{\psi}]_c = 1$

loop order:  $2L + 2 = \Sigma$  (*chiral dim.*)

example:  $4_p - 6_p + 4_g + 2_\psi = 4$



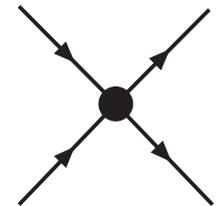
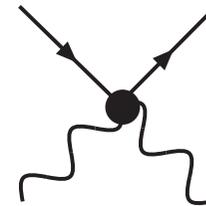
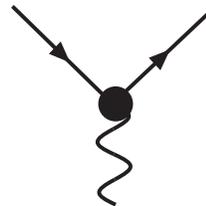
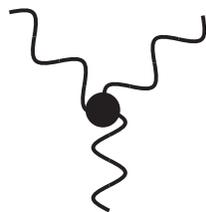
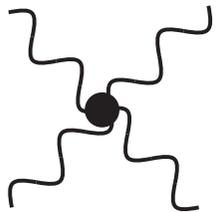
$\Rightarrow [\mathcal{L}_{LO}]_c = 2, \quad [\text{NLO}]_c = 4 \quad (\text{local terms; } D^n, n \geq 0)$

$UhD^4, \quad g^2X^2Uh, \quad gXUhD^2, \quad y^2\psi^2UhD, \quad y\psi^2UhD^2, \quad y^2\psi^4Uh$

- $\bar{\psi}\psi\bar{\psi}\psi, X^2Uh$  not LO

→ classification of NLO operators

$UhD^4$ ,  $X^2Uh$ ,  $XUhD^2$ ,  $\psi^2UhD$ ,  $\psi^2UhD^2$ ,  $\psi^4Uh$



related work:

*Giudice et al., Contino et al., Alonso et al.*

# Loop vs. dimensional counting

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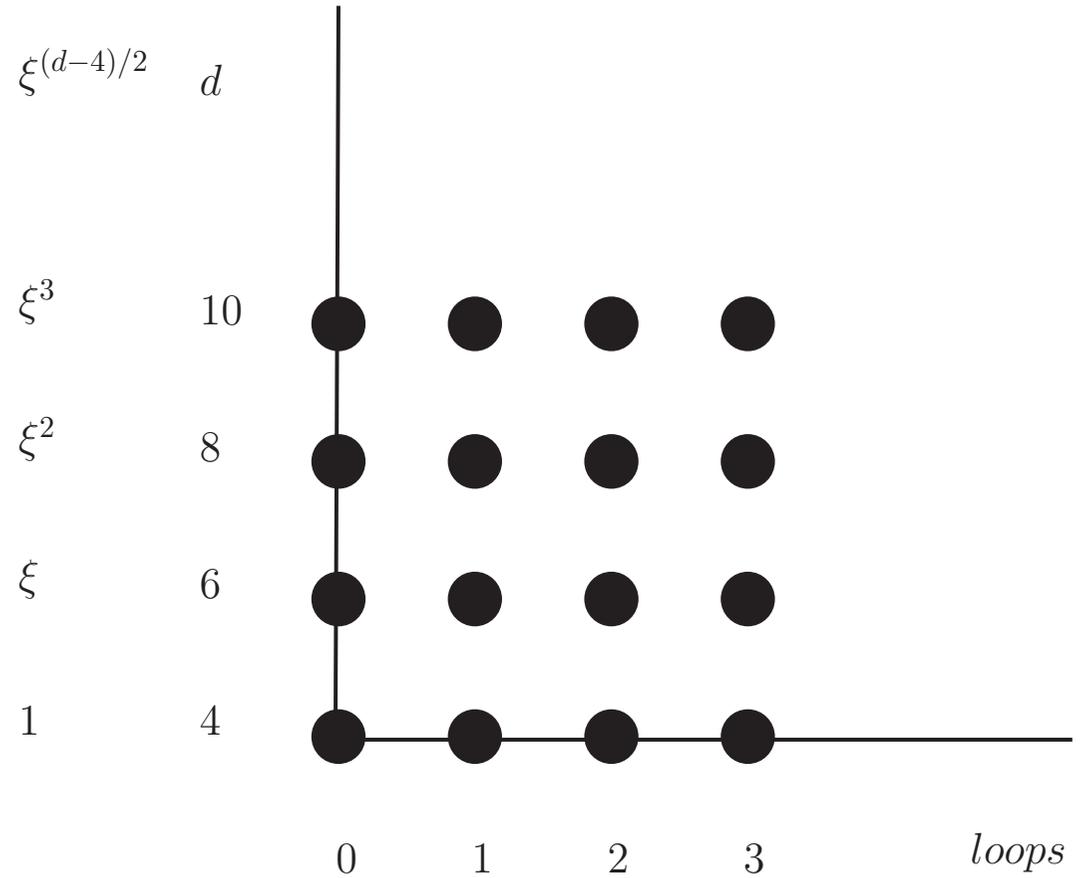
$$\Lambda = 4\pi f$$

$f$

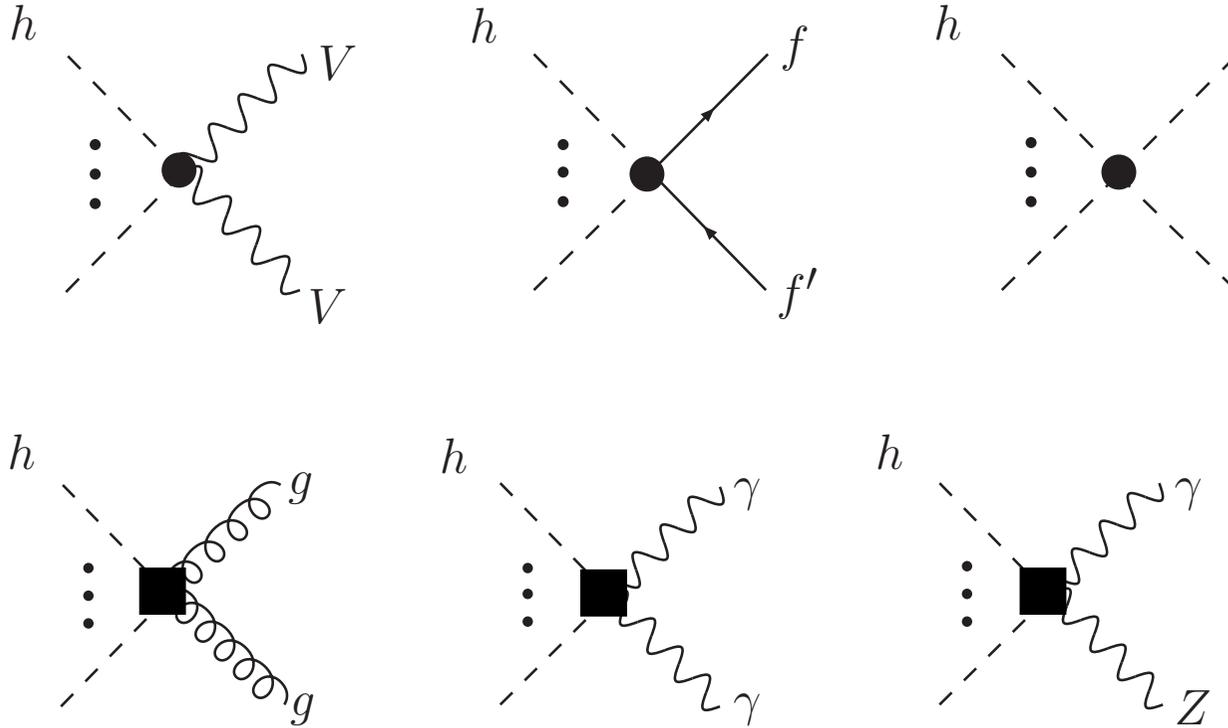
$v$

$$\xi = \frac{v^2}{f^2} \rightarrow \text{dim. exp.}$$

$$\frac{1}{16\pi^2} \approx \frac{f^2}{\Lambda^2} \rightarrow \text{loop exp.}$$



# LO couplings

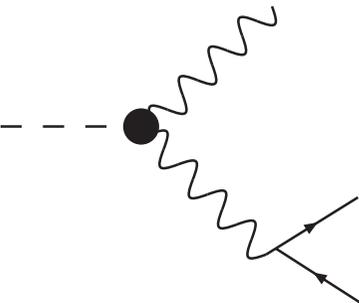


$$\begin{aligned}
 \mathcal{L} = & 2c_V \left( m_W^2 W_\mu^+ W^{-\mu} + \frac{1}{2} m_Z^2 Z_\mu Z^\mu \right) \frac{h}{v} - c_t y_t \bar{t} t h - c_b y_b \bar{b} b h - c_\tau y_\tau \bar{\tau} \tau h \\
 & + \frac{e^2}{16\pi^2} c_{\gamma\gamma} F_{\mu\nu} F^{\mu\nu} \frac{h}{v} + \frac{eg'}{16\pi^2} c_{Z\gamma} Z_{\mu\nu} F^{\mu\nu} \frac{h}{v} + \frac{g_s^2}{16\pi^2} c_{gg} \langle G_{\mu\nu} G^{\mu\nu} \rangle \frac{h}{v}
 \end{aligned}$$

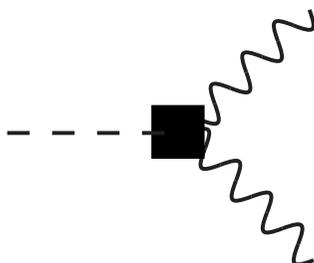
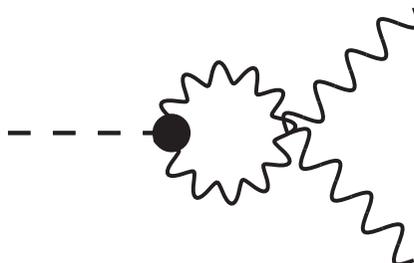
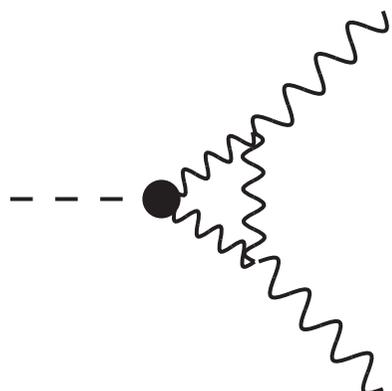
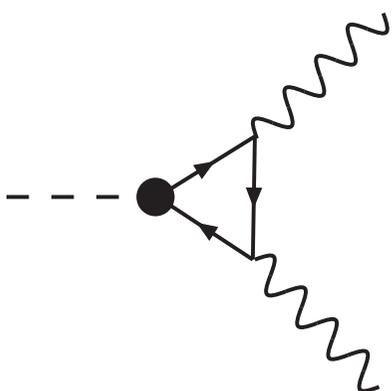
# Sample applications

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$$h \rightarrow Zl^+l^-$$

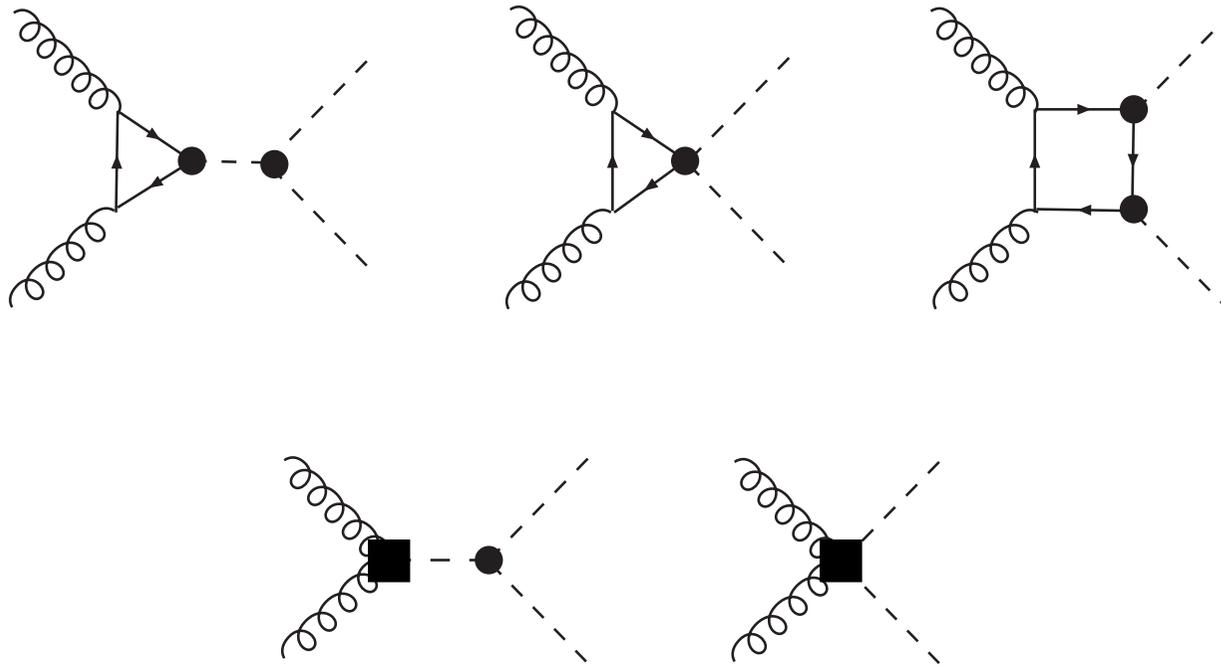


$$h \rightarrow \gamma\gamma$$



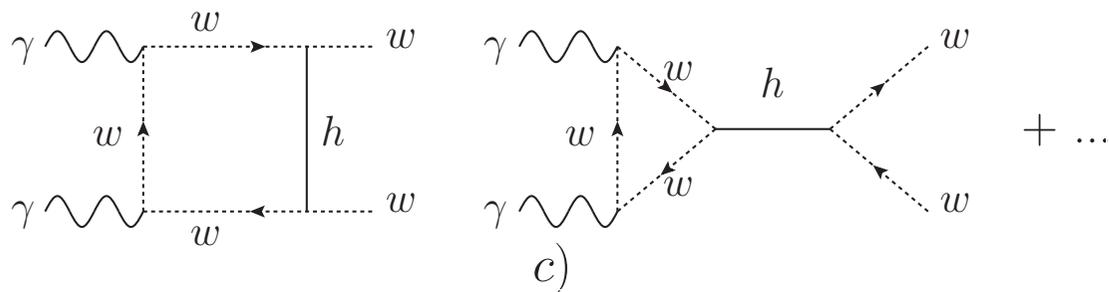
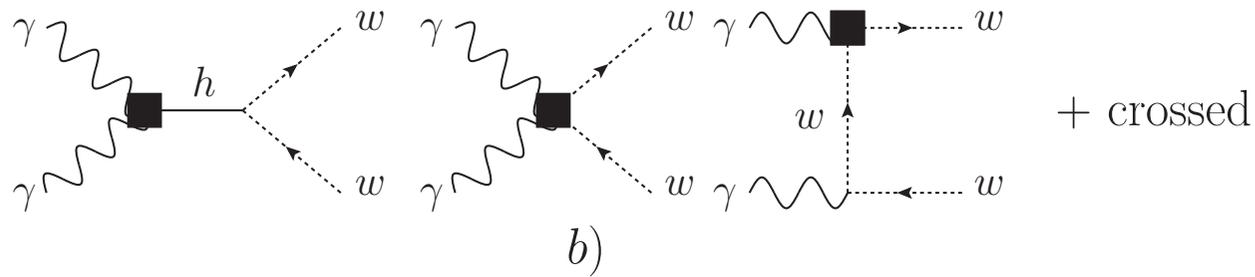
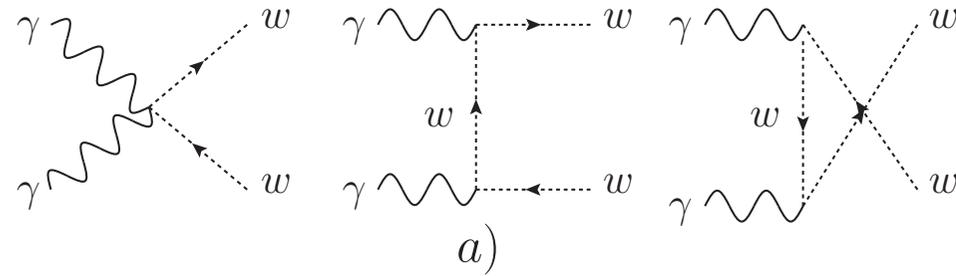
# Higgs-pair production in gluon fusion

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*Gröber, Mühlleitner, Spira, Streicher*

# $\gamma\gamma \rightarrow ww$



*Delgado, Dobado, Herrero, Sanz-Cillero*

1. Motivation and leading-order Lagrangian
2. Renormalization of the chiral Lagrangian
3. Connection of chiral Lagrangian to  $\kappa$ -formalism
4. Linear vs. nonlinear EFT
5. Sample applications
  - $h \rightarrow Zl^+l^-$ ,  $h \rightarrow \gamma\gamma$ ,  $h \rightarrow Z\gamma$
  - Higgs-pair production in gluon fusion
  - $\gamma\gamma$  scattering;  $\gamma^* \rightarrow w^+w^-$ ,  $\gamma^*\gamma^* \rightarrow h$  form factors
  - TeV-scale particle pair production at NLO
6. Concluding remarks

- natural framework for sizable NP in Higgs couplings
- power counting by chiral dimensions
- consistent EFT, systematic improvement possible
- LO description  $\leftrightarrow$   $\kappa$ -formalism