G. Isidori – PO in Higgs Physics



Pseudo Observables in Higgs Physics

[a concise status report in view of YR4]

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▶ Introduction [*What are and why we need Higgs PO*]

- ▶ PO in Higgs decays
- ▶ PO in Higgs EW production  $[\rightarrow more in the next talk]$
- ▶ PO vs. EFT, parameter counting & symmetry limits

▶ Outlook [*YR4 and beyond*]

So far, possible non-standard properties of the Higgs boson (in process with a leading SM amplitude) have been analyzed from the experimental point of view using the so-called "kappa-formalism":

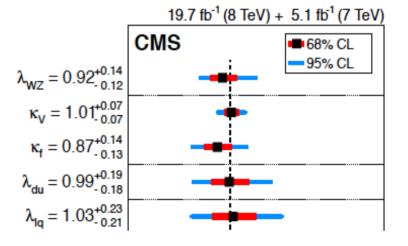
$$\sigma(ii \to h+X) \times BR(h \to ff) = \sigma_{ii} \frac{\Gamma_{ff}}{\Gamma_{h}} = \frac{\kappa_{ii}^2 \kappa_{ff}^2}{\kappa_{h}^2} \sigma_{SM} \times BR_{SM}$$

Main virtues:

- Clean SM limit [best up-to-date TH predictions recovered for  $\kappa_i \rightarrow 1$ ]
- Well-defined both on TH and EXP sides
- (almost) Model independent

Main problem:

• <u>Loss of information</u> on possible NP effects modifying the kinematical distributions



N.B.: *easy to conceive NP effects showing up mainly in kin. effects rather than in total rates* (e.g. CPV)

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Main problem:

• <u>Loss of information</u> on possible NP effects modifying the kinematical distributions We need to identify a <u>larger</u> <u>set</u> of <u>"pseudo-observables"</u> able to characterize NP in the Higgs sector in general terms

- The goal of the PO is to provide a general encoding of the exp. results in terms of a limited number of "simplified" (idealized) observables of easy th. interpretation [*old idea heavily used and developed at LEP times*]
- The experimental determination of an appropriate set of PO will "help" and not "replace" any explicit NP approach to Higgs physics (*including the EFT*)



Experimental data

Pseudo Observables

Lagrangian parameters

The PO can be <u>computed</u> in terms of Lagrangian parameters in any specific th. framework (SM, SM-EFT, SUSY, ...)

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- The PO should be defined from kinematical properties of <u>on-shell processes</u> (*no problems of renormalization, scale dependence,...*)
- The theory corrections applied to extract them should be universally accepted as "NP-free" (*soft QCD and QED radiation*)

There are two main categories of PO:

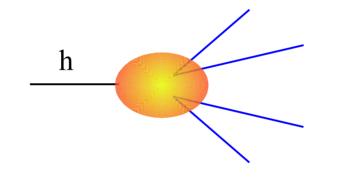
A) "Ideal observables"

 $M_W$ , Γ(Z→*ll*), ...  $M_h$ , Γ(h→γγ), Γ(h→4μ), ... but also dσ(pp→hZ)/dm<sub>hZ</sub> ...

B) "Effective on-shell couplings"

 $g_{Z}^{f}, g_{W}^{f}, ...$ 

- Both categories are useful (*there is redundancy having both, but that's not an issue*...).
- For B) one can write an effective Feynman rule, not to be used beyond tree-level (its just a practical way to re-write, *and code in existing tools*, an on-shell amplitude).





Multi-body modes e.g.  $h \rightarrow 4\ell, \ell\ell\gamma, ...$ 

There is more to extract from data other than the  $\kappa_i$ 

# Two-body (on-shell) decays

[no polarization properties of the final state accessible]

e.g.  $h \rightarrow \gamma \gamma, \mu \mu, \tau \tau, bb$ 

*The*  $\kappa_i (\leftrightarrow \Gamma_i)$  *is* <u>all what</u> <u>one can extract</u> from data

[+ one more parameter if the polarization is accessible]

Multi-body modes  
e.g. 
$$h \rightarrow 4\ell, \, \ell\ell\gamma, \dots$$
  
 $\downarrow$   
Form factors  $\rightarrow f_i(s)$  [E.g.:  $s = m_{\ell\ell}^2$ 

# Two-body (on-shell) decays

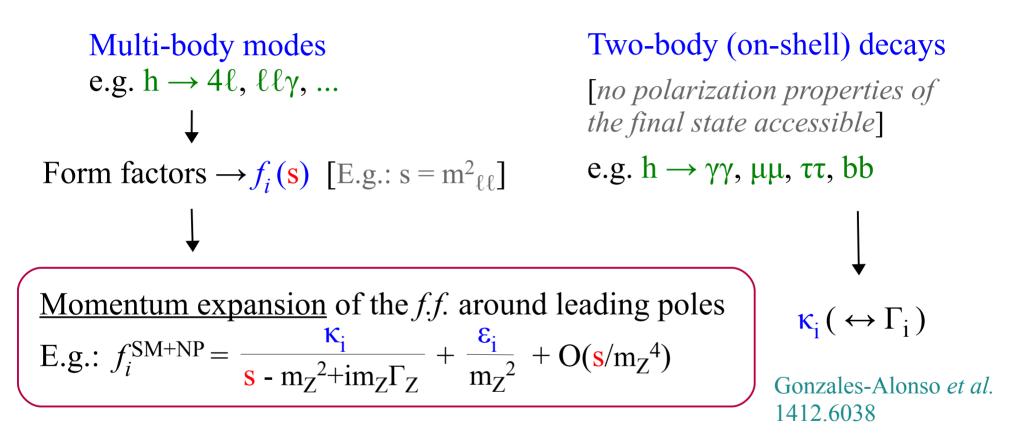
[no polarization properties of the final state accessible]

e.g.  $h \rightarrow \gamma \gamma$ ,  $\mu \mu$ ,  $\tau \tau$ , bb

E.g.: 
$$\mathscr{A}(h \to Z ee) \sim$$
  
 $\epsilon_{\mu}^{Z} J_{\mu}^{e_{L}} [f_{1}^{Ze_{L}}(q^{2})g^{\mu\nu} + f_{3}^{Ze_{L}}(q^{2})(pq g^{\mu\nu} - q^{\mu} p^{\nu}) + ...]$ 

N.B.: There is noting "wrong" or "dangerous" in using *f.f.*, provided

- → they are defined from on-shell amplitudes [*ill-defined for*  $h \rightarrow WW^*$ , ZZ\* *but perfectly ok for*  $h \rightarrow 4\ell$ ]
- no model-dependent assumptions are made on their functional form

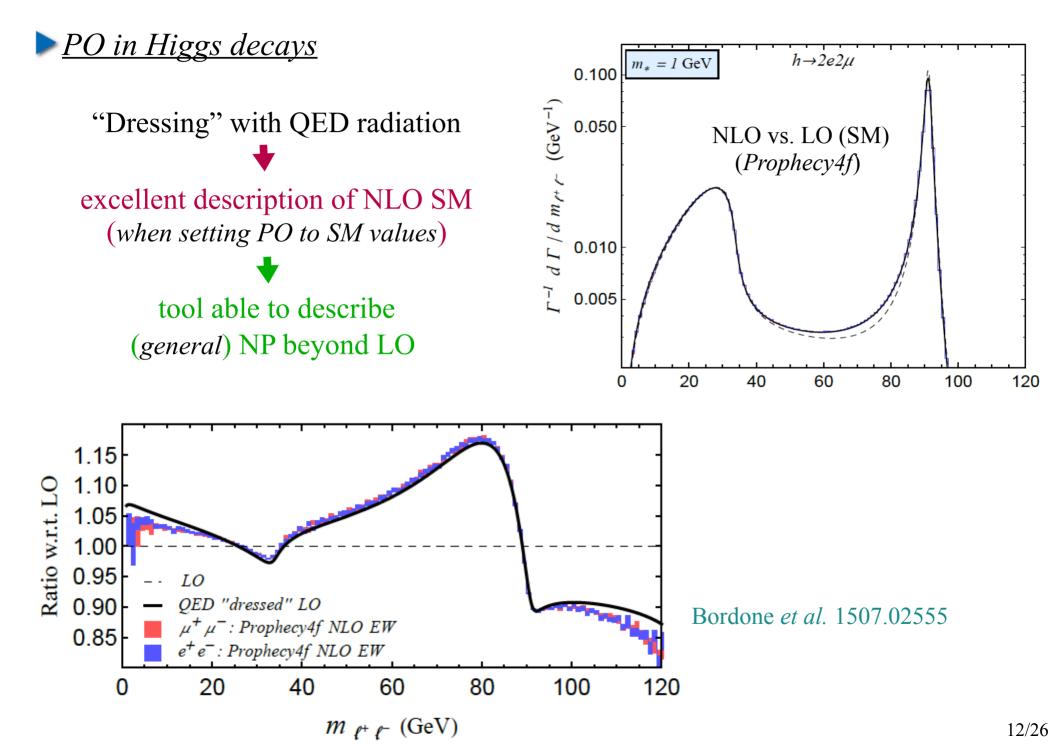


- No need to specify any detail about the EFT, but for the absence of light new particles → momentum expansion <u>very well justified</u> by the Higgs kinematic
- The  $\{\kappa_i, \epsilon_i\}$  thus defined are well-defined PO  $\rightarrow$  systematic inclusion of higherorder QED and QCD (soft) corrections possible (and necessary...)

#### $\blacktriangleright$ <u>PO in Higgs decays</u> [e.g.: the $h \rightarrow$ 4f case]

$$\begin{split} \mathcal{A} = & i \frac{2m_Z^2}{v_F} \sum_{e=e_L,e_R} \sum_{\mu=\mu_L,\mu_R} (\bar{e}\gamma_{\alpha}e)(\bar{\mu}\gamma_{\beta}\mu) \times & \epsilon_{Z\gamma}^{\text{SM-1L}} \simeq 3.8 \times 10^{-3} \\ & \left[ \left( \kappa_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \frac{\epsilon_{Ze}}{m_Z^2} \frac{g_Z^\mu}{P_Z(q_2^2)} + \frac{\epsilon_{Z\mu}}{m_Z^2} \frac{g_Z^e}{P_Z(q_1^2)} \right) g^{\alpha\beta} + \\ & + \left( \epsilon_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \kappa_{Z\gamma} \epsilon_{Z\gamma}^{\text{SM-1L}} \left( \frac{eQ_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{eQ_e g_Z^\mu}{q_1^2 P_Z(q_2^2)} \right) + \kappa_{\gamma\gamma} \epsilon_{\gamma\gamma}^{\text{SM-1L}} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} \right) \frac{q_1 \cdot q_2 \ g^{\alpha\beta} - q_2^\alpha q_1^\beta}{m_Z^2} + \\ & + \left( \epsilon_{ZZ}^{\text{CP}} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \epsilon_{Z\gamma}^{\text{CP}} \left( \frac{eQ_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{eQ_e g_Z^\mu}{q_1^2 P_Z(q_2^2)} \right) + \epsilon_{\gamma\gamma}^{\text{CP}} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} \right) \frac{\epsilon^{\alpha\beta\rho\sigma} q_{2\rho} q_{1\sigma}}{m_Z^2} \right] \end{split}$$

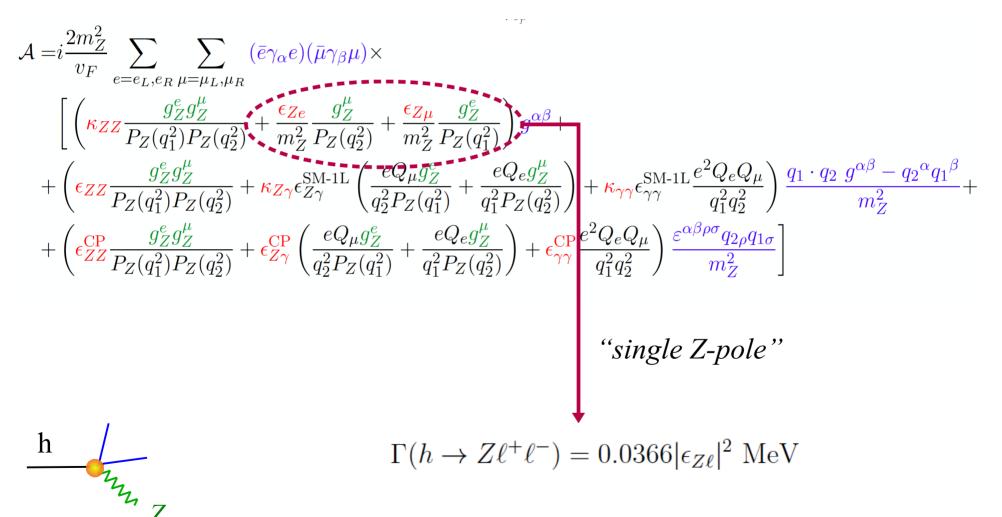
- The  $\{\kappa_i, \epsilon_i\}$  are defined from the residues of the amplitude on the physical poles  $\rightarrow$  well-defined PO that can be extracted from data and computed to desired accuracy in a given BSM framework (including the SMEFT)
- By construction, the  $g_Z^{f}$  are the PO from Z-pole measurements
- $\kappa_{\gamma\gamma}$  and  $\kappa_{Z\gamma}$  are the standard "kappas" from <u>on-shell</u>  $h \to \gamma\gamma$  and  $h \to Z\gamma$ , the  $\varepsilon_i$  are sub-leading terms in the SM: SM recovered for  $\kappa_i \to 1$ ,  $\varepsilon_i = O(10^{-3}) \to 0$
- To this amplitude we must apply a "<u>radiation function</u>" to take into account QED radiation → excellent description of SM (and NP) beyond the tree level.



The "physical meaning" of the parameters appearing in this decomposition is not obvious at first sight, but it is actually quite simple  $[\rightarrow physical PO]$ :

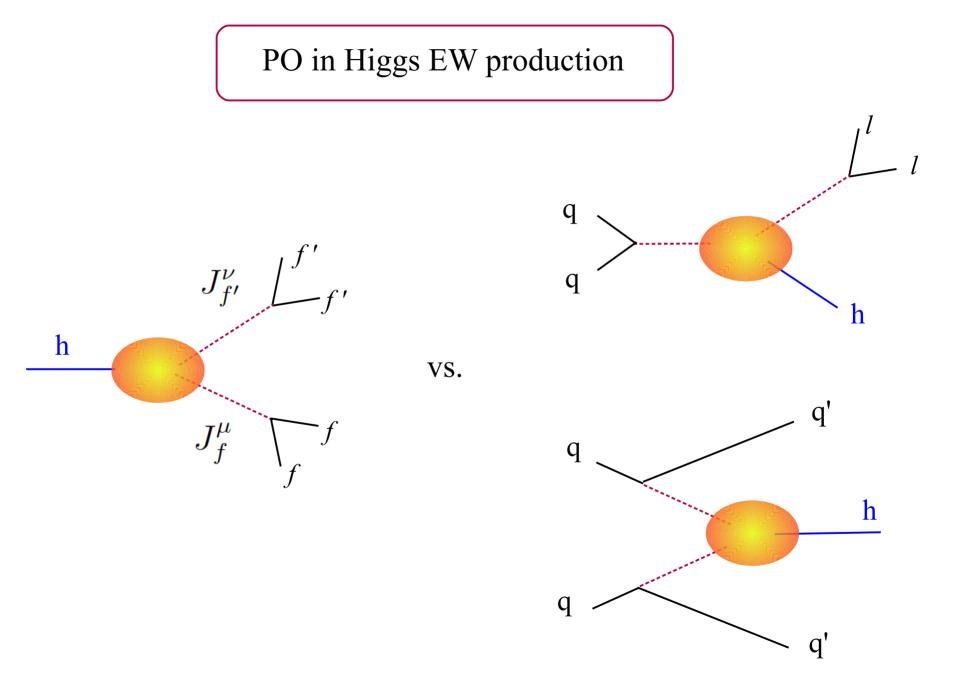
$$\mathcal{A} = i \frac{2m_Z^2}{v_F} \sum_{e=e_L,e_R} \sum_{\mu=\mu_L,\mu_R} (\bar{e}\gamma_{\alpha} e) (\bar{\mu}\gamma_{\beta} \mu) \times \begin{bmatrix} \left(\kappa_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \frac{\epsilon_{Ze}}{m_Z^2} \frac{g_Z^\mu}{P_Z(q_2^2)} + \frac{\epsilon_{Z\mu}}{m_Z^2} \frac{g_Z^e}{P_Z(q_1^2)} \right) g^{\alpha\beta} + \\ + \left(\epsilon_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \kappa_{Z\gamma} \epsilon_{Z\gamma}^{SM-1L} \left(\frac{eQ_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{eQ_e g_Z^\mu}{q_1^2 P_Z(q_2^2)}\right) + \kappa_{\gamma\gamma} \epsilon_{\gamma\gamma}^{SM-1L} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} \right) \frac{g_1 \cdot q_2 \ g^{\alpha\beta} - q_2^\alpha q_1^\beta}{m_Z^2} + \\ + \left(\epsilon_{ZZ}^{CP} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \epsilon_{Z\gamma}^{CP} \left(\frac{eQ_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{eQ_e g_Z^\mu}{q_1^2 P_Z(q_2^2)}\right) + \epsilon_{\gamma\gamma}^{CP} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} \right) \frac{e^{\alpha\beta\rho\sigma} q_{2\rho}q_{1\sigma}}{m_Z^2} \end{bmatrix} \\ \xrightarrow{\mathbf{M}} \frac{\mathbf{M}}{\mathbf{M}} \frac{\mathbf$$

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PO	Physical PO	Relation to the eff. coupl.
$\kappa_f, \; \lambda_f^{ m CP}$	$\Gamma(h \to f\bar{f})$	$= \Gamma(h \to f\bar{f})^{(\mathrm{SM})}[(\kappa_f)^2 + (\lambda_f^{\mathrm{CP}})^2]$
$\kappa_{\gamma\gamma}, \; \lambda^{ m CP}_{\gamma\gamma}$	$\Gamma(h \to \gamma \gamma)$	$= \Gamma(h \to \gamma \gamma)^{(\mathrm{SM})} [(\kappa_{\gamma \gamma})^2 + (\lambda_{\gamma \gamma}^{\mathrm{CP}})^2]$
$\kappa_{Z\gamma}, \; \lambda^{ m CP}_{Z\gamma}$	$\Gamma(h \to Z\gamma)$	$= \Gamma(h \to Z\gamma)^{(\mathrm{SM})}[(\kappa_{Z\gamma})^2 + (\lambda_{Z\gamma}^{\mathrm{CP}})^2]$
$\kappa_{ZZ}$	$\Gamma(h \to Z_L Z_L)$	$= (0.209 \text{ MeV}) \times  \kappa_{ZZ} ^2$
$\epsilon_{ZZ}$	$\Gamma(h \to Z_T Z_T)$	$= (1.9 \times 10^{-2} \text{ MeV}) \times  \epsilon_{ZZ} ^2$
$\epsilon^{ m CP}_{ZZ}$	$\Gamma^{\rm CPV}(h \to Z_T Z_T)$	$= (8.0 \times 10^{-3} \text{ MeV}) \times  \epsilon_{ZZ}^{CP} ^2$
$\epsilon_{Zf}$	$\Gamma(h \to Z f \bar{f})$	$= (3.7 \times 10^{-2} \text{ MeV}) \times N_c^f  \epsilon_{Zf} ^2$
$\kappa_{WW}$	$\Gamma(h \to W_L W_L)$	$= (0.84 \text{ MeV}) \times  \kappa_{WW} ^2$
$\epsilon_{WW}$	$\Gamma(h \to W_T W_T)$	$= (0.16 \text{ MeV}) \times  \epsilon_{WW} ^2$
$\epsilon^{ m CP}_{WW}$	$\Gamma^{\rm CPV}(h \to W_T W_T)$	$= (6.8 \times 10^{-2} \text{ MeV}) \times  \epsilon_{WW}^{CP} ^2$
$\epsilon_{Wf}$	$\Gamma(h \to W f \bar{f'})$	$= (0.14 \text{ MeV}) \times N_c^f  \epsilon_{Wf} ^2$



*Greljo et al. 1512.06135* 

conceptually

trivial

delicate

### *PO in Higgs EW production*

The same Green Function controlling  $h \rightarrow 4f$  decays is accessible also in  $pp \rightarrow hV$ and  $pp \rightarrow h$  via VBF, i.e. the two leading EW-type Higgs production processes (*N.B.: this follows from "plain QFT" no need to invoke any EFT...*)

 $\langle 0 | \mathcal{T} \left\{ J_f^{\mu}(x), J_{f'}^{\nu}(y), h(0) \right\} | 0 \rangle$ 

Same approach as in  $h \rightarrow 4f$  (and, to some extent, same PO) but for three important differences:

• different flavor composition  $(q \leftrightarrow \ell) \rightarrow$  new param. associated to the physical PO  $\Gamma(h \rightarrow Zqq) \& \Gamma(h \rightarrow Wud)$ 

large impact of (facotrizable) QCD corrections

 different kinematical regime: <u>momentum exp. not always justified</u> (*large momentum transfer*)

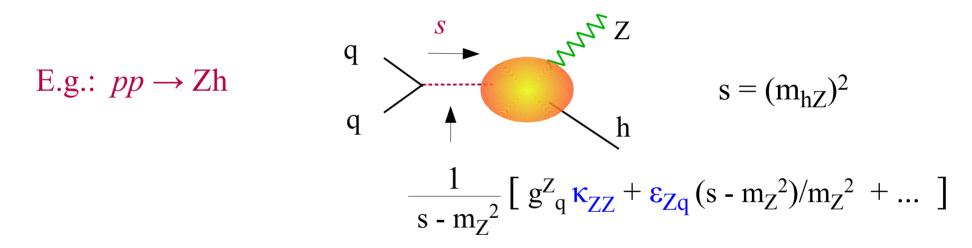


### PO in Higgs EW production

Twofold problem:

I. identify which are the "dangerous" kinematical variables (and how to access them when not directly measurable  $\rightarrow p_T^{jet}$  in VBF,  $p_T^Z$  in Zh [ $\rightarrow$  see next talk])

II. how to control the validity of the expansion



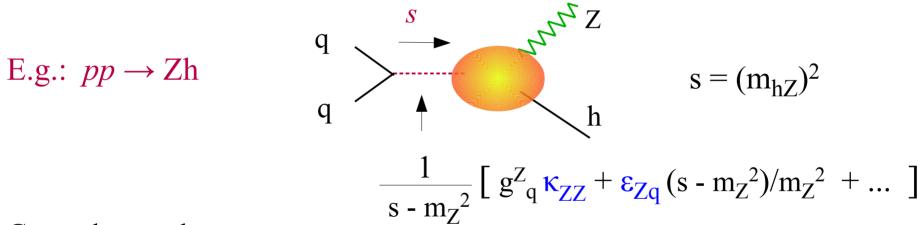
Key point: since we expand on a measurable kinematical variable, the validity of the expansion can be directly checked/validated by data

## *PO in Higgs EW production*

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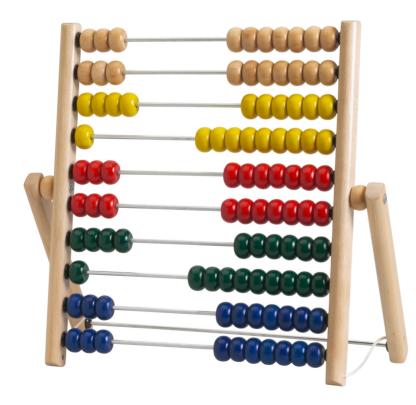
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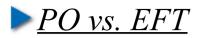


General procedure:

- Measure the PO setting close to the threshold region, setting a cut on the "dangerous" kinematical variable [→ a-posteriori data-driven check of the validity of the momentum expansion = definition of threshold region]
- → Report the cross-section as a function of the kinematical variable in the highmomentum region [→ natural link/merging with template cross-section]

# PO vs. EFT, parameter counting & symmetry limits





PO and couplings in EFT Lagrangians are *intimately related but are not the same thing* (on-shell amplitudes vs. Lagrangians parameters)  $\rightarrow$  <u>full complementarity</u>

- The PO are calculable in any EFT approach (*linear, non-linear, LO, NLO*...)
  - In the limit where we work at the <u>tree-level in the EFT</u> there is a simple linear relation between PO and EFT couplings: each PO represent a unique linear combination of couplings of the <u>most general Higgs EFT</u>.
  - <u>This does not hold beyond the tree-level</u> (the PO do not change, but their relation to EFT couplings is more involved....)

### ▶ <u>PO vs. EFT</u>

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  - <u>This does not hold beyond the tree-level</u> (the PO do not change, but their relation to EFT couplings is more involved....)
- For Higgs production also the PO involve an expansion in momenta; however, this is different that the operator expansion employed within the EFT
  - To define the PO we expand only on a <u>measurable kinematical variables</u>, this is why the validity of the *expansion can be checked directly by data* (on the same process used to determine the PO)
- In each process the <u>PO are the maximum number of independent observables</u> that can be extracted by that process only → naturally optimized for data analyses 22/26

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#### Parameter counting & symmetry limits

Number of independent PO for EW Higgs decays  $[h \rightarrow 4\ell \ (\ell = e, \mu, \nu) + \ell \ell \gamma + \gamma \gamma]$ :

EW decay modes	flavor +CP symm.	flavor non univ.	CP violation
$\begin{array}{c} h \rightarrow \gamma \gamma, 2e\gamma, 2\mu \gamma \\ 4e, 4\mu, 2e2\mu \end{array}$	$ \begin{pmatrix} \kappa_{ZZ}, \kappa_{Z\gamma}, \kappa_{\gamma\gamma} \\ \epsilon_{ZZ}, \epsilon_{Ze_L}, \epsilon_{Ze_R} \end{pmatrix} (6) $	$\epsilon_{Z\mu_L}, \epsilon_{Z\mu_R}$ (2)	$\epsilon_{ZZ}^{CP}, \epsilon_{Z\gamma}^{CP}, \epsilon_{\gamma\gamma}^{CP}$ (3)
$h \rightarrow 2e2\nu, 2\mu 2\nu, e\nu\mu\nu$	$\begin{array}{c} \kappa_{WW}  (4) \\ \epsilon_{WW},  \epsilon_{Z\nu_e},  \operatorname{Re}(\epsilon_{We_L}) \end{array}$	$\epsilon_{Z\nu_{\mu}}, \operatorname{Re}(\epsilon_{W\mu_{L}})$ Im $(\epsilon_{W})$	$\epsilon_{WW}^{CP}, \operatorname{Im}(\epsilon_{We_L})$ $\epsilon_{\mu_L}$ (5)
all EW decay modes with custodial symmetry	$ \begin{array}{c} \kappa_{ZZ}, \kappa_{Z\gamma}, \kappa_{\gamma\gamma} \\ \epsilon_{ZZ}, \epsilon_{Ze_L}, \epsilon_{Ze_R} \\ \operatorname{Re}(\epsilon_{We_L}) \end{array} (7) $	$\epsilon_{Z\mu_L}, \epsilon_{Z\mu_R}$	$\epsilon^{CP}_{ZZ}, \epsilon^{CP}_{Z\gamma}, \epsilon^{CP}_{\gamma\gamma}$

20 (no symmetries)  $\rightarrow$  7 (CP + Lepton Univ + Custodial)

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#### *Parameter counting & symmetry limits*

Number of independent PO for EW Higgs decays + EW production + Yukawa modes (h  $\rightarrow$  ff):

	PO with maximal symmetry [CP + Lepton Univ + Custodial]:		
Production & decays EW decays only EW productions only	$\kappa_{ZZ}, \kappa_{Z\gamma}, \epsilon_{ZZ}$ $\kappa_{\gamma\gamma}, \epsilon_{Ze_L}, \epsilon_{Ze_R}, \operatorname{Re}(\epsilon_{We_L})$ $\epsilon_{Zu_L}, \epsilon_{Zu_R}, \epsilon_{Zd_L}, \epsilon_{Zd_R}$		
	(11) $[\rightarrow 32 \text{ with no symm.}]$		
Yukawa modes	$\kappa_b, \kappa_c, \kappa_{\tau}, \kappa_{\mu}$ (4) [ $\rightarrow$ 8 with no symm.] (as in the original $\kappa$ -formalism)		



- A first automated public tool (*UFO model* for MG5\_aMC@NLO or Sherpa) is now
  - <u>fully available for decays</u> (*QED corrections fully accounted by standard shower algorithms, as verified by the comparison with Profecy4f*)
  - will soon be available also for EW production, with inclusion of NLO QCD corrections (*work in prog....* → *see next talk*)



http://www.physik.uzh.ch/data/HiggsPO



- The PO represent a general tool for the exploration of Higgs properties (in view of high-statistics data), with minimum loss of information and minimum theoretical bias → *full complementary to EFT* (and explicit BSM)
- The formalism is now fully developed and the corresponding note for YR4 is well in progress [incomplete version available as additional material to this talk, 1<sup>st</sup> complete version expected next week → will be circulated within WG2 for comments/feedback]
- But there is still a lot of work to be done, especially from the tool/implementation side → worth to conceive a dedicated subgroup within the HXSWG, beyond YR4 (*if sufficient interest shown by the exp. collab....*).