



University of
Zurich^{UZH}

Pseudo Observables in Higgs Physics
[status report & future plans]

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- ▶ Introduction [*Why PO?*]
- ▶ PO in Higgs decays
- ▶ PO in Higgs EW production
- ▶ PO vs. EFT, parameter counting & symmetry limits
- ▶ Tools & Work in Progress
- ▶ Conclusions

► Introduction [*Why PO?*]

The Higgs-PO are a natural generalization (*in my opinion the only natural...*) of the “kappa-formalism”

$$\sigma(in \rightarrow \mathbf{h}+X) \times \text{BR}(\mathbf{h} \rightarrow fin) = \sigma_{ii} \frac{\Gamma_{ff}}{\Gamma_h} = \frac{\kappa_{in}^2 \kappa_{fin}^2}{\kappa_h^2} \sigma_{\text{SM}} \times \text{BR}_{\text{SM}}$$

Main virtues of the κ 's:

- **Clean SM limit** [best up-to-date TH predictions recovered for $\kappa_i \rightarrow 1$]
- **Well-defined both on TH and EXP sides**
- **(almost) Model independent**

Main problem:

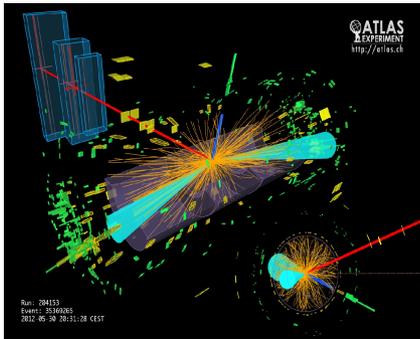
- **Loss of information** on possible NP effects modifying the **kinematical distributions**

When aiming at high precision, in observables with non-trivial kinematics, we need a larger set of “pseudo-observables”

The “old” κ 's are nothing but a subset of the Higgs PO

► Introduction [*Why PO?*]

- The goal of the PO is to provide a general encoding of the exp. results in terms of a limited number of “simplified” (idealized) observables of easy th. interpretation [*old idea - heavily used and developed at LEP times*]
- The experimental determination of an appropriate set of PO will “help” and not “replace” any explicit NP approach to Higgs physics (*including the EFT*)



$$\begin{aligned} \mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i\bar{\psi}\not{D}\psi + \text{h.c.} \\ & + \chi_i y_{ij} \chi_j \phi + \text{h.c.} \\ & + |D_\mu \phi|^2 - V(\phi) \end{aligned}$$

Experimental data

Pseudo Observables

Lagrangian parameters

The PO can be computed in terms of Lagrangian parameters in any specific th. framework (SM, SM-EFT, SUSY, ...)

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- The PO should be defined from kinematical properties of on-shell processes (*no problems of renormalization, scale dependence, ...*)
- The theory corrections applied to extract them should be universally accepted as “NP-free” (*soft QCD and QED radiation*)

► Introduction [*Why PO?*]

Some people ask the following question:

Why do we need to measure PO, given we can go to a “more fundamental level” and directly extract the Wilson coefficients of the EFT from data?

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Answer (I):

What is “more fundamental”?

- A) The combination [$c_W(\mu) + c_{HW}(\mu) + \tan(\theta_W)(c_B(\mu) + c_{HW}(\mu))$],
- defined assuming a *linear realization of the EWSB* & employing the *SILH basis* for the EFT Lagrangian
 - extracted computing amplitudes at *LO in the EFT expansion*, setting the *renormalization scale $\mu=1$ TeV* (and assuming that at that scale *NLO-EW effects are negligible*)
- B) The partial width $\Gamma(h \rightarrow W_L W_L)$

► Introduction [*Why PO?*]

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Why do we need to measure PO, given we can go to a “more fundamental level” and directly extract the Wilson coefficients of the EFT from data?

Answer (II):

There is no reason to consider Wilson coefficients and, more generally, Lagrangian parameters “more fundamental” than on-shell physical amplitudes (or the elements of the S matrix). Actually it is the opposite.

Lagrangians are nothing but tools...

Extracting their parameters requires a series of additional assumptions, that we may change in the future with more data and/or better understanding of the underlying (BSM) physics theory.

...the “physics” is in the scattering amplitudes, hence in the PO.

► Introduction

There are two main categories of PO:

A) “Ideal observables”

$M_W, \Gamma(Z \rightarrow ll), \dots$

$M_h, \Gamma(h \rightarrow \gamma\gamma), \Gamma(h \rightarrow 4\mu), \dots$

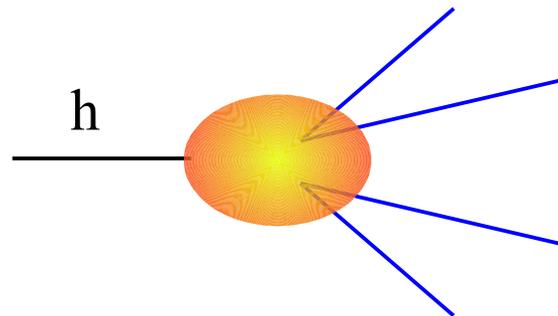
but also $d\sigma(pp \rightarrow hZ)/dm_{hZ} \dots$

B) “Effective on-shell couplings”

g_Z^f, g_W^f, \dots

- Both categories are useful
(*there is redundancy having both, but that's not an issue...*).
- For B) one can write an effective Feynman rule, not to be used beyond tree-level
(its just a practical way to re-write, *and code in existing tools*, an on-shell amplitude).

PO in Higgs decays



► PO in Higgs decays

Multi-body modes

e.g. $h \rightarrow 4\ell, \ell\ell\gamma, \dots$



There is more to extract from data other than the κ_i

Two-body (on-shell) decays

[no polarization properties of the final state accessible]

e.g. $h \rightarrow \gamma\gamma, \mu\mu, \tau\tau, bb$



The κ_i ($\leftrightarrow \Gamma_i$) is all what one can extract from data

[+ one more parameter if the polarization is accessible]

► PO in Higgs decays

Multi-body modes

e.g. $h \rightarrow 4\ell, \ell\ell\gamma, \dots$



Form factors $\rightarrow f_i(\mathbf{s})$ [E.g.: $s = m_{\ell\ell}^2$]



Momentum expansion of the $f.f.$ around leading poles

$$\text{E.g.: } f_i^{\text{SM+NP}} = \frac{\kappa_i}{s - m_Z^2 + im_Z\Gamma_Z} + \frac{\epsilon_i}{m_Z^2} + \mathcal{O}(s/m_Z^4)$$

Two-body (on-shell) decays

[no polarization properties of the final state accessible]

e.g. $h \rightarrow \gamma\gamma, \mu\mu, \tau\tau, bb$



κ_i ($\leftrightarrow \Gamma_i$)

Gonzales-Alonso *et al.*
1412.6038

- No need to specify any detail about the EFT, but for the absence of light new particles \rightarrow momentum expansion very well justified by the Higgs kinematic
- The $\{\kappa_i, \epsilon_i\}$ thus defined are well-defined **PO** \rightarrow systematic inclusion of higher-order QED and QCD (soft) corrections possible (and necessary...)

► PO in Higgs decays [e.g.: $h \rightarrow 4l$]

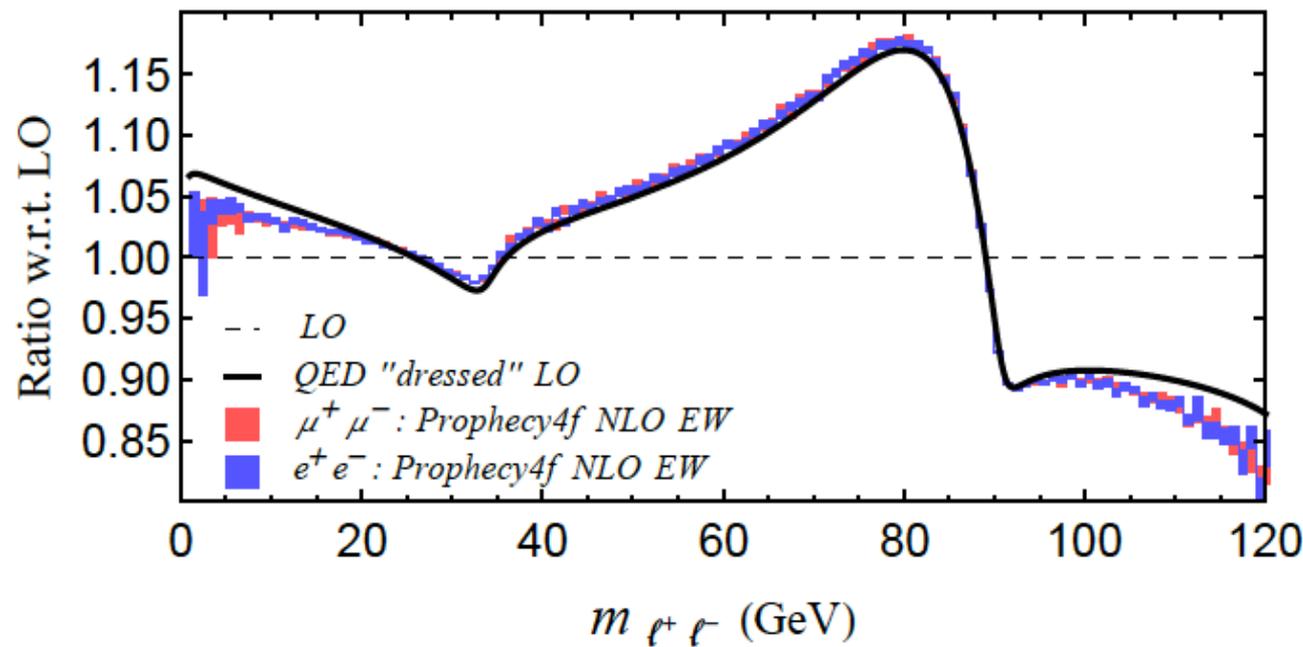
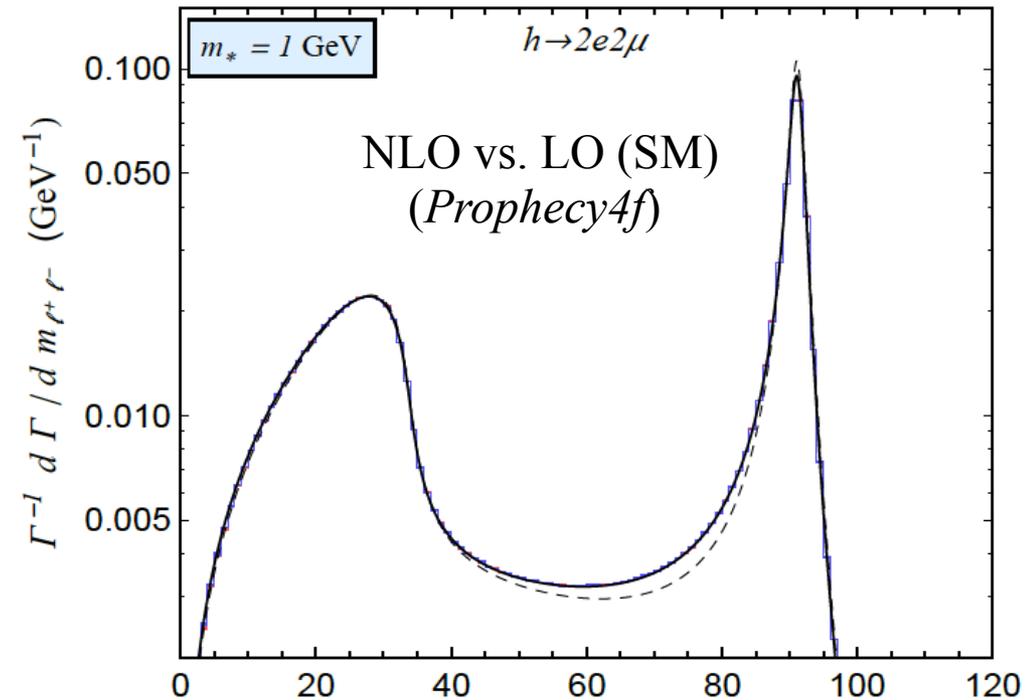
“Dressing” with QED radiation



excellent description of NLO SM
(when setting PO to SM values)



tool able to describe
(general) NP beyond LO



Bordone et al. 1507.02555

► PO in Higgs decays

The “physical meaning” of the parameters appearing in the $\{\kappa_i, \epsilon_i\}$ decomposition is not obvious at first sight, but it is actually quite simple [\rightarrow *physical PO*]:

$$\mathcal{A} = i \frac{2m_Z^2}{v_F} \sum_{e=e_L, e_R} \sum_{\mu=\mu_L, \mu_R} (\bar{e} \gamma_\alpha e) (\bar{\mu} \gamma_\beta \mu) \times$$

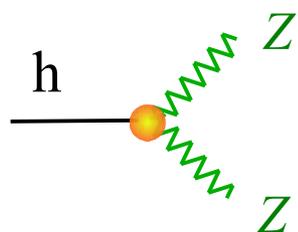
$$\left[\left(\kappa_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \frac{\epsilon_{Ze}}{m_Z^2} \frac{g_Z^\mu}{P_Z(q_2^2)} + \frac{\epsilon_{Z\mu}}{m_Z^2} \frac{g_Z^e}{P_Z(q_1^2)} \right) g^{\alpha\beta} + \right.$$

$$\left. + \left(\epsilon_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \kappa_{Z\gamma} \epsilon_{Z\gamma}^{\text{SM-1L}} \left(\frac{e Q_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{e Q_e g_Z^\mu}{q_1^2 P_Z(q_2^2)} \right) + \kappa_{\gamma\gamma} \epsilon_{\gamma\gamma}^{\text{SM-1L}} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} \right) \frac{q_1 \cdot q_2 g^{\alpha\beta} - q_2^\alpha q_1^\beta}{m_Z^2} + \right.$$

$$\left. + \left(\epsilon_{ZZ}^{\text{CP}} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \epsilon_{Z\gamma}^{\text{CP}} \left(\frac{e Q_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{e Q_e g_Z^\mu}{q_1^2 P_Z(q_2^2)} \right) + \epsilon_{\gamma\gamma}^{\text{CP}} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} \right) \frac{\epsilon^{\alpha\beta\rho\sigma} q_{2\rho} q_{1\sigma}}{m_Z^2} \right]$$

\rightarrow PO note in YR4

“double Z-pole”



$$\Gamma(h \rightarrow Z_L Z_L) \equiv \frac{\Gamma(h \rightarrow 2e2\mu) [\kappa_{ZZ}]}{\mathcal{B}(Z \rightarrow 2e) \mathcal{B}(Z \rightarrow 2\mu)} = 0.209 |\kappa_{ZZ}|^2 \text{ MeV}$$

$$\Gamma(h \rightarrow Z_T Z_T) \equiv \frac{\Gamma(h \rightarrow 2e2\mu) [\epsilon_{ZZ}]}{\mathcal{B}(Z \rightarrow 2e) \mathcal{B}(Z \rightarrow 2\mu)} = 0.0189 |\epsilon_{ZZ}|^2 \text{ MeV}$$

$$\Gamma^{\text{CPV}}(h \rightarrow Z_T Z_T) \equiv \frac{\Gamma(h \rightarrow 2e2\mu) [\epsilon_{ZZ}^{\text{CP}}]}{\mathcal{B}(Z \rightarrow 2e) \mathcal{B}(Z \rightarrow 2\mu)} = 0.00799 |\epsilon_{ZZ}^{\text{CP}}|^2 \text{ MeV}$$

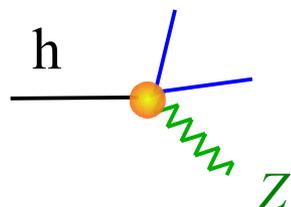
► PO in Higgs decays

The “physical meaning” of the parameters appearing in the $\{\kappa_i, \epsilon_i\}$ decomposition is not obvious at first sight, but it is actually quite simple [\rightarrow *physical PO*]:

$$\begin{aligned}
 \mathcal{A} = & i \frac{2m_Z^2}{v_F} \sum_{e=e_L, e_R} \sum_{\mu=\mu_L, \mu_R} (\bar{e} \gamma_\alpha e) (\bar{\mu} \gamma_\beta \mu) \times \\
 & \left[\left(\kappa_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \frac{\epsilon_{Ze}}{m_Z^2} \frac{g_Z^\mu}{P_Z(q_2^2)} + \frac{\epsilon_{Z\mu}}{m_Z^2} \frac{g_Z^e}{P_Z(q_1^2)} \right) g^{\alpha\beta} + \right. \\
 & + \left(\epsilon_{ZZ} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \kappa_{Z\gamma} \epsilon_{Z\gamma}^{\text{SM-1L}} \left(\frac{e Q_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{e Q_e g_Z^\mu}{q_1^2 P_Z(q_2^2)} \right) + \kappa_{\gamma\gamma} \epsilon_{\gamma\gamma}^{\text{SM-1L}} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} \right) \frac{q_1 \cdot q_2 g^{\alpha\beta} - q_2^\alpha q_1^\beta}{m_Z^2} + \\
 & \left. + \left(\epsilon_{ZZ}^{\text{CP}} \frac{g_Z^e g_Z^\mu}{P_Z(q_1^2) P_Z(q_2^2)} + \epsilon_{Z\gamma}^{\text{CP}} \left(\frac{e Q_\mu g_Z^e}{q_2^2 P_Z(q_1^2)} + \frac{e Q_e g_Z^\mu}{q_1^2 P_Z(q_2^2)} \right) + \epsilon_{\gamma\gamma}^{\text{CP}} \frac{e^2 Q_e Q_\mu}{q_1^2 q_2^2} \right) \frac{\epsilon^{\alpha\beta\rho\sigma} q_{2\rho} q_{1\sigma}}{m_Z^2} \right]
 \end{aligned}$$

\rightarrow PO note in YR4

“single Z-pole”



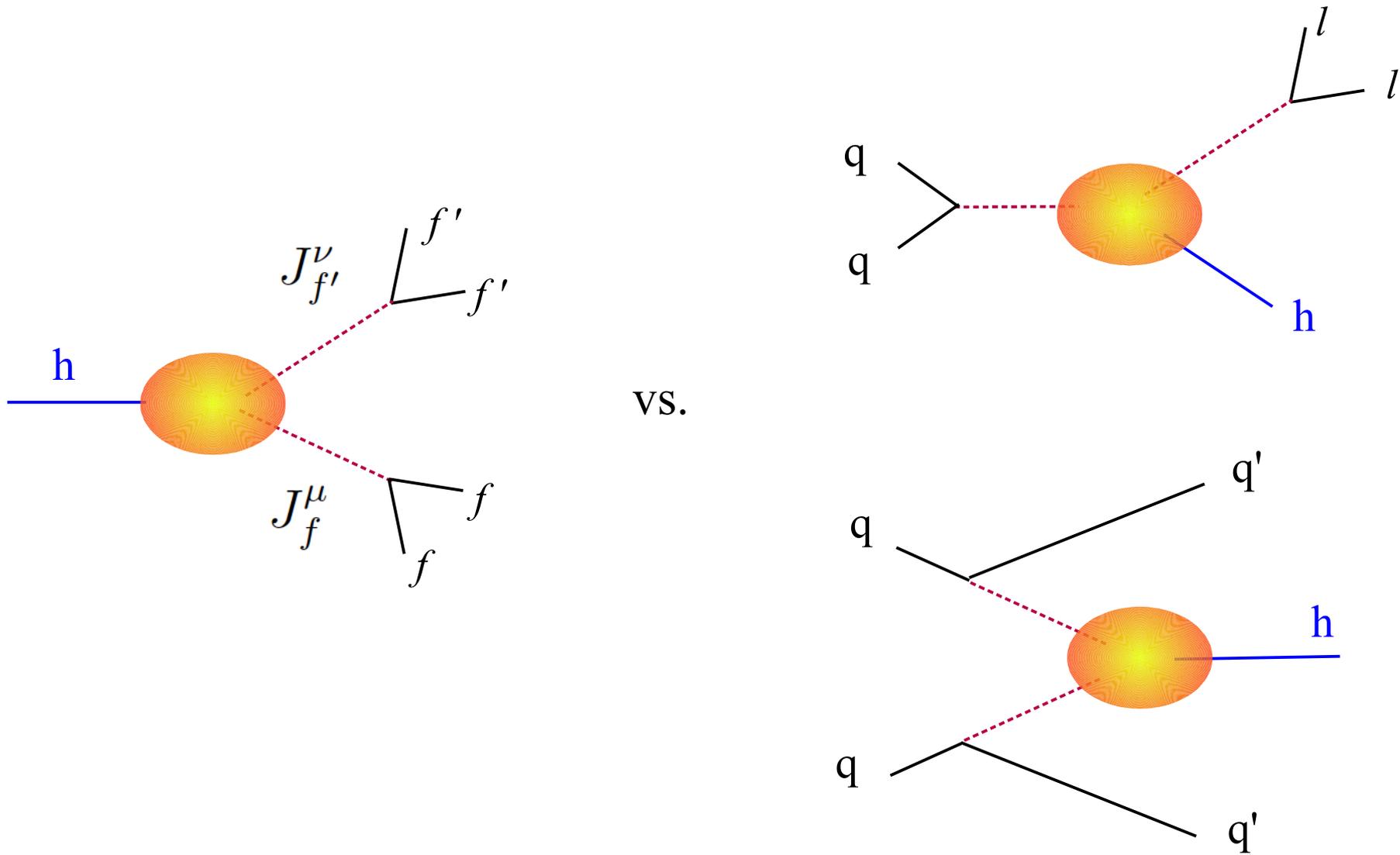
$$\Gamma(h \rightarrow Z \ell^+ \ell^-) = 0.0366 |\epsilon_{Ze}|^2 \text{ MeV}$$

► PO in Higgs decays

The “physical meaning” of the parameters appearing in the $\{\kappa_i, \epsilon_i\}$ decomposition is not obvious at first sight, but it is actually quite simple [\rightarrow *physical PO*]:

PO	Physical PO	Relation to the eff. coupl.
$\kappa_f, \lambda_f^{\text{CP}}$	$\Gamma(h \rightarrow f\bar{f})$	$= \Gamma(h \rightarrow f\bar{f})^{(\text{SM})} [(\kappa_f)^2 + (\lambda_f^{\text{CP}})^2]$
$\kappa_{\gamma\gamma}, \lambda_{\gamma\gamma}^{\text{CP}}$	$\Gamma(h \rightarrow \gamma\gamma)$	$= \Gamma(h \rightarrow \gamma\gamma)^{(\text{SM})} [(\kappa_{\gamma\gamma})^2 + (\lambda_{\gamma\gamma}^{\text{CP}})^2]$
$\kappa_{Z\gamma}, \lambda_{Z\gamma}^{\text{CP}}$	$\Gamma(h \rightarrow Z\gamma)$	$= \Gamma(h \rightarrow Z\gamma)^{(\text{SM})} [(\kappa_{Z\gamma})^2 + (\lambda_{Z\gamma}^{\text{CP}})^2]$
κ_{ZZ}	$\Gamma(h \rightarrow Z_L Z_L)$	$= (0.209 \text{ MeV}) \times \kappa_{ZZ} ^2$
ϵ_{ZZ}	$\Gamma(h \rightarrow Z_T Z_T)$	$= (1.9 \times 10^{-2} \text{ MeV}) \times \epsilon_{ZZ} ^2$
$\epsilon_{ZZ}^{\text{CP}}$	$\Gamma^{\text{CPV}}(h \rightarrow Z_T Z_T)$	$= (8.0 \times 10^{-3} \text{ MeV}) \times \epsilon_{ZZ}^{\text{CP}} ^2$
ϵ_{Zf}	$\Gamma(h \rightarrow Z f\bar{f})$	$= (3.7 \times 10^{-2} \text{ MeV}) \times N_c^f \epsilon_{Zf} ^2$
κ_{WW}	$\Gamma(h \rightarrow W_L W_L)$	$= (0.84 \text{ MeV}) \times \kappa_{WW} ^2$
ϵ_{WW}	$\Gamma(h \rightarrow W_T W_T)$	$= (0.16 \text{ MeV}) \times \epsilon_{WW} ^2$
$\epsilon_{WW}^{\text{CP}}$	$\Gamma^{\text{CPV}}(h \rightarrow W_T W_T)$	$= (6.8 \times 10^{-2} \text{ MeV}) \times \epsilon_{WW}^{\text{CP}} ^2$
ϵ_{Wf}	$\Gamma(h \rightarrow W f\bar{f}')$	$= (0.14 \text{ MeV}) \times N_c^f \epsilon_{Wf} ^2$

PO in Higgs EW production



► PO in Higgs EW production

The same Green Function controlling $h \rightarrow 4f$ decays is accessible also in $pp \rightarrow hV$ and $pp \rightarrow h$ via VBF, i.e. the two leading EW-type Higgs production processes (N.B.: this follows from “plain QFT” no need to invoke any EFT...)

$$\langle 0 | \mathcal{T} \{ J_f^\mu(x), J_{f'}^\nu(y), h(0) \} | 0 \rangle$$

Same approach as in $h \rightarrow 4f$ (and, to some extent, same PO) but for three important differences:

Greljo et al. 1512.06135

- different flavor composition ($q \leftrightarrow \ell$) \rightarrow new param. associated to the physical PO $\Gamma(h \rightarrow Zqq)$ & $\Gamma(h \rightarrow Wud)$
- large impact of (factorizable) QCD corrections
- different kinematical regime: momentum exp. not always justified (*large momentum transfer*)

trivial

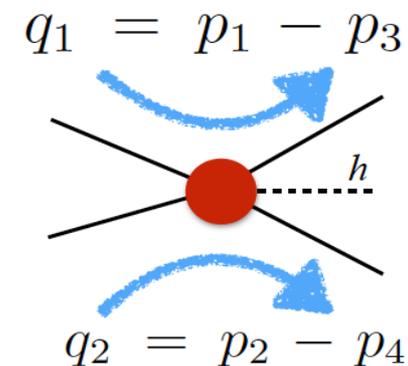
conceptually
easy

delicate
point

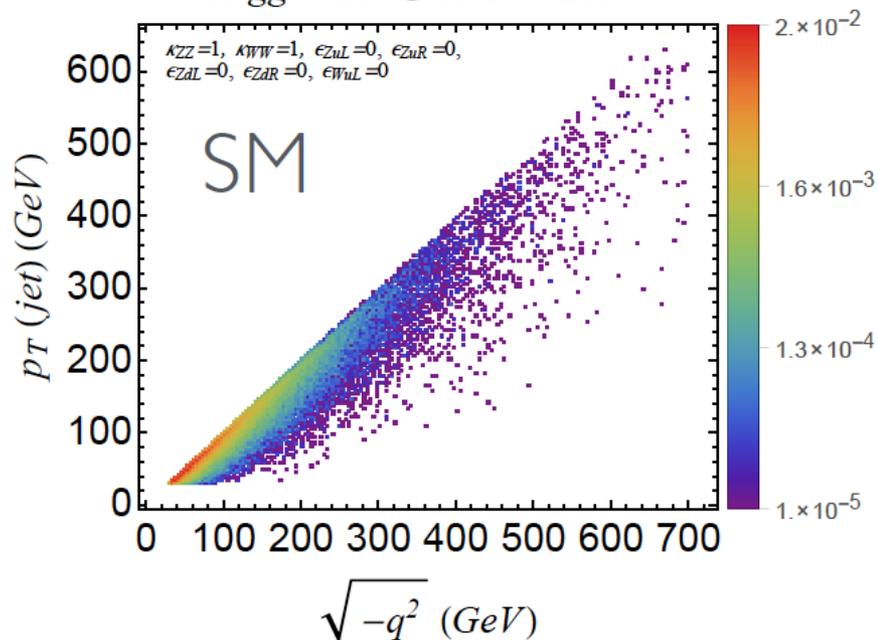
► PO in VBF [slides by J. Lindert]

Practical problem:

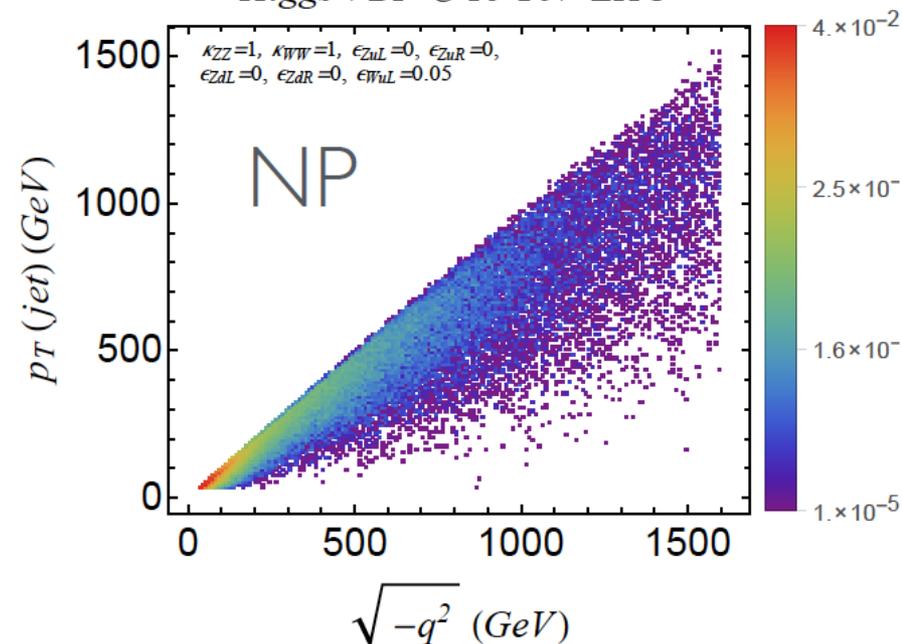
- $F_X(q_1^2, q_2^2)$, $G_X(q_1^2, q_2^2)$ not directly measurable
- not even q_1^2, q_2^2 measurable (in particular not in $H \rightarrow WW$)
- construct proxy:



Higgs VBF @ 13 TeV LHC



Higgs VBF @ 13 TeV LHC

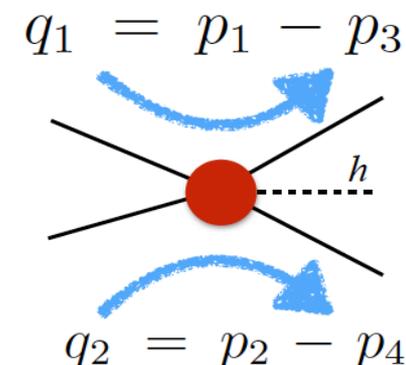


$$\Rightarrow q_i^2 \approx -p_{T,i}^2 \quad (\text{for Higgs produced near threshold})$$

► PO in VBF [slides by J. Lindert]

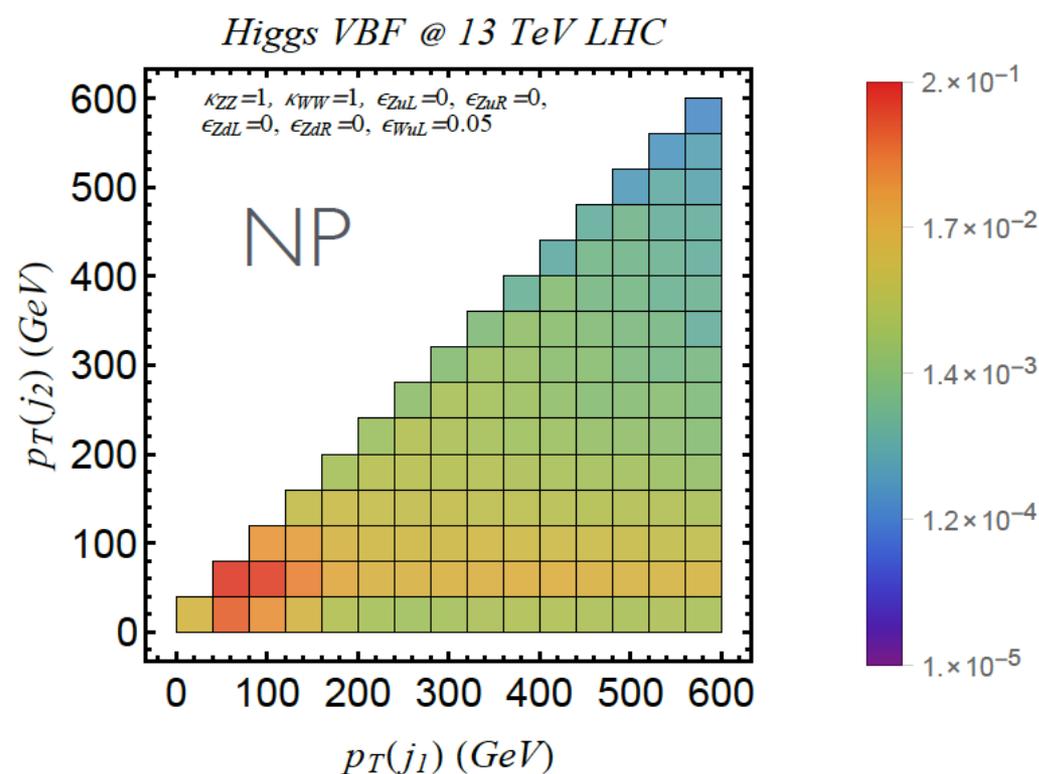
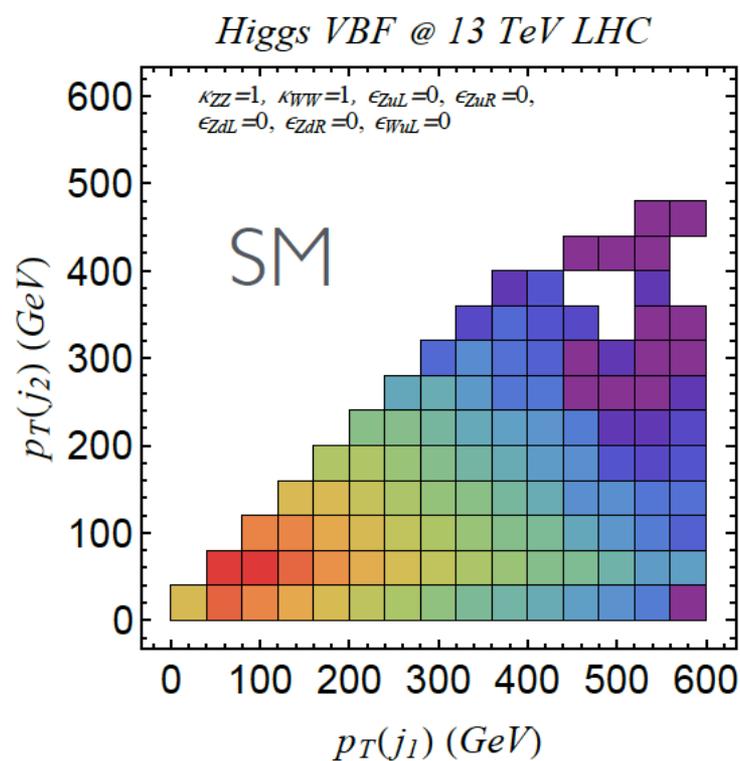
- Crucial measurement:
double differential cross section in jet p_T 's
(order by p_T and/or $\Delta\eta_{ij}$)

$$\frac{d^2\sigma}{dp_{T,j_1} dp_{T,j_2}}$$



- allows for extraction/fit of PO!

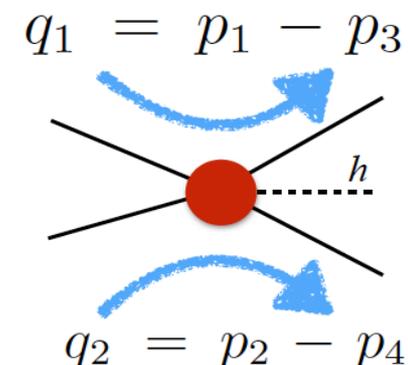
$$F(q_1^2, q_2^2) \rightarrow \tilde{F}(p_{T1}^2, p_{T2}^2)$$



► PO in VBF [slides by J. Lindert]

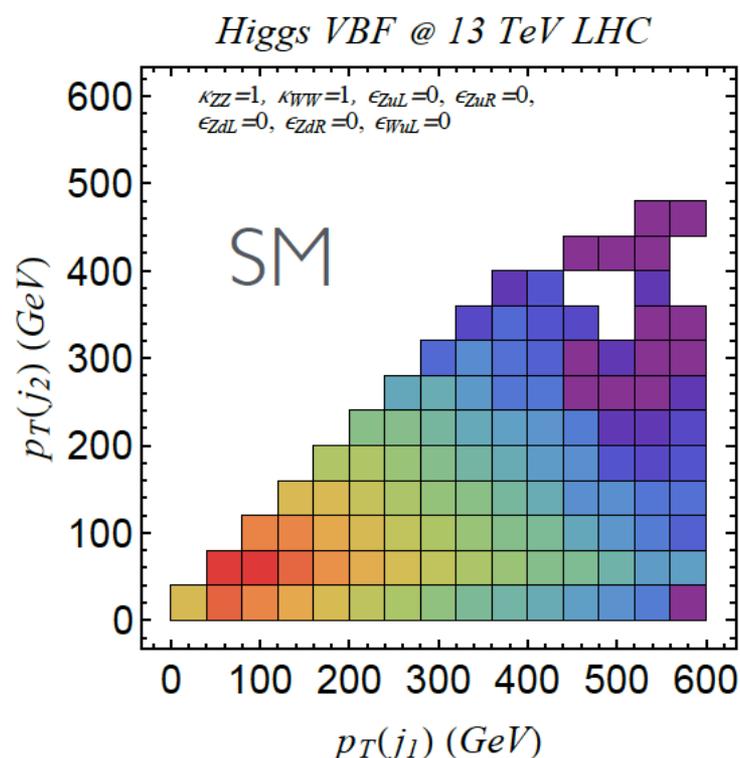
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General procedure:

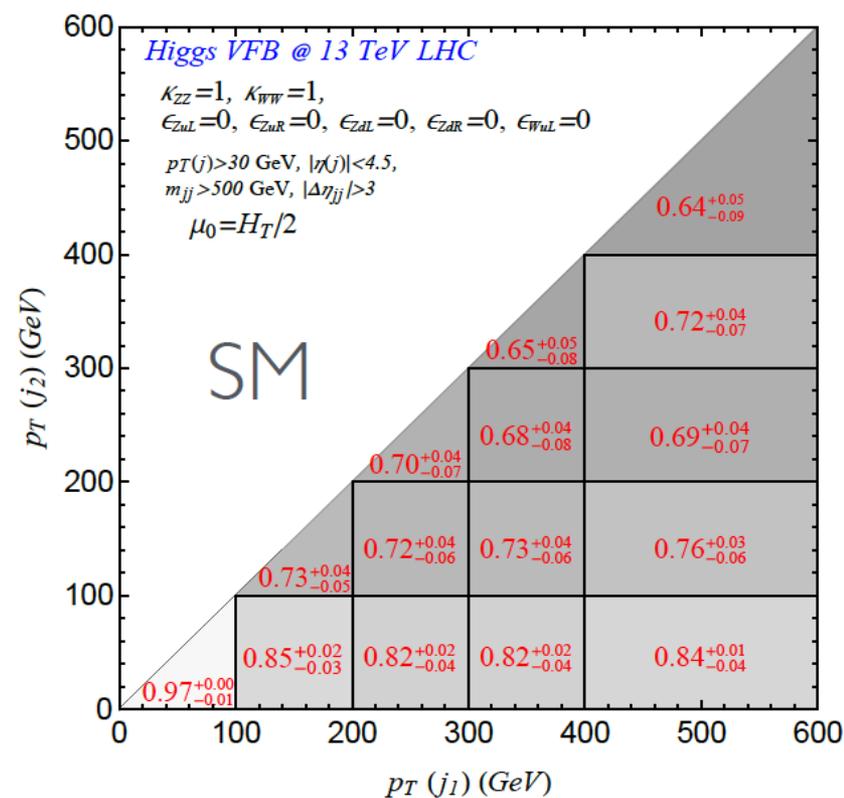
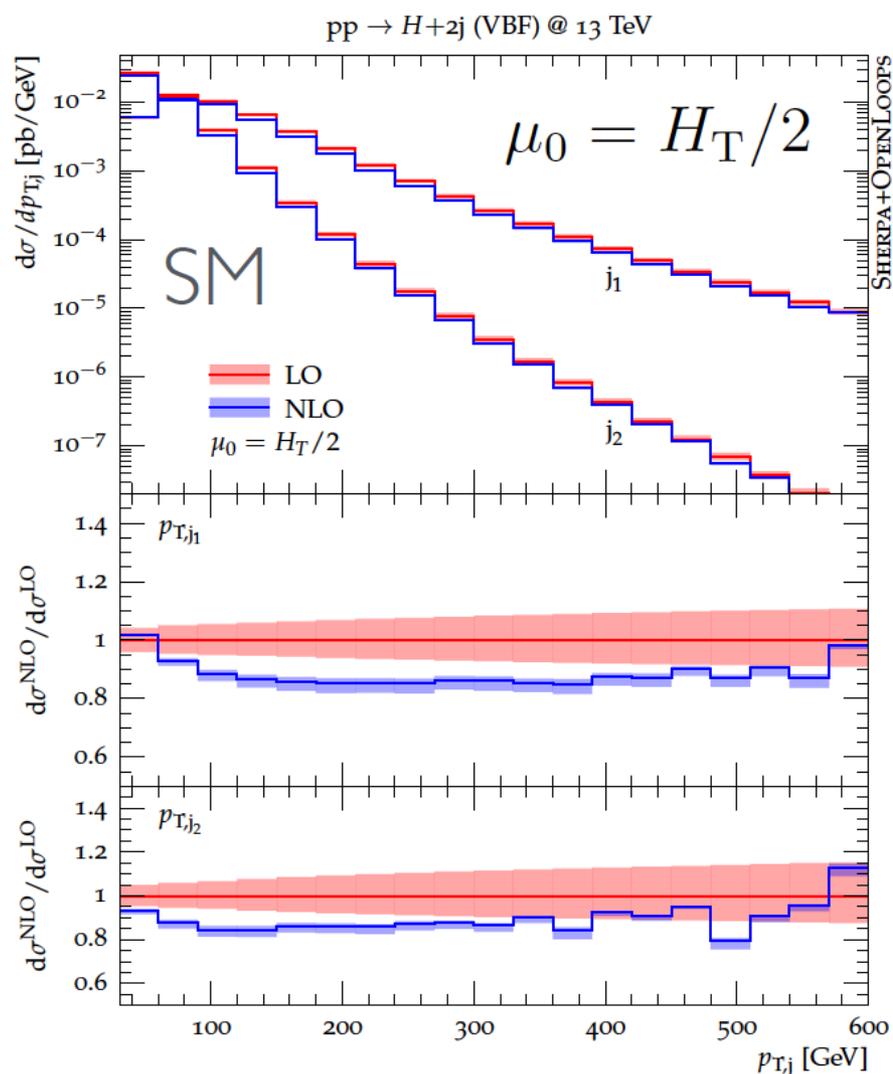
- Measure the PO setting close to the threshold region, setting a cut on the “dangerous” kinematical variable [→ a-posteriori data-driven check of the validity of the momentum expansion ↔ definition of threshold region]
- Report the cross-section as a function of the kinematical variable in the high-momentum region [→ natural link/merging with template cross-section]

► PO in VBF [slides by J. Lindert]

NLO QCD corrections

$$p_{T,j_{1,2}} > 30 \text{ GeV}, \quad |\eta_{j_{1,2}}| < 4.5, \quad \text{and} \quad m_{j_1 j_2} > 500 \text{ GeV}$$

$$\Delta\eta_{j_1 j_2} > 3$$

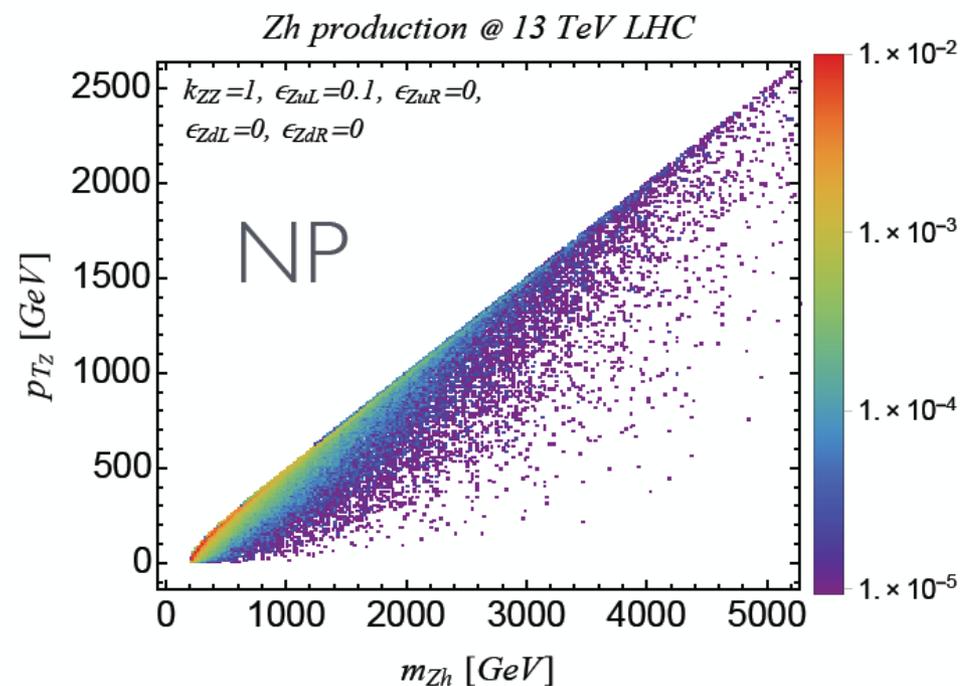
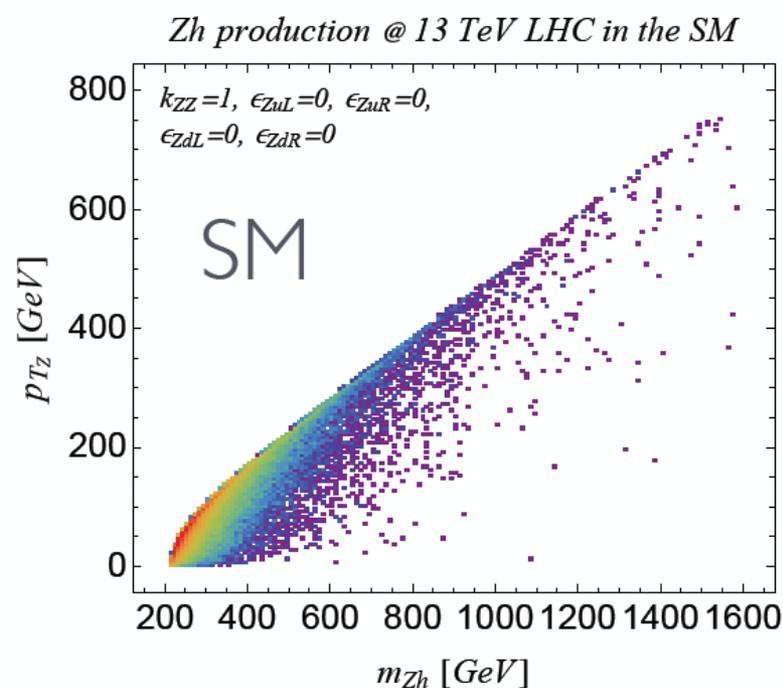
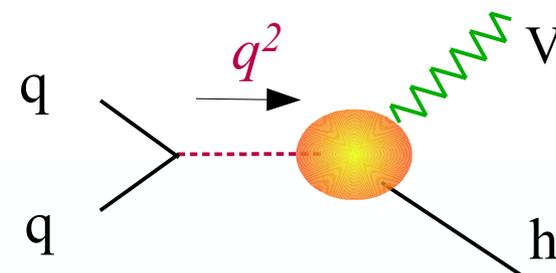


- NLO QCD corrections: max ~ 15-35%
- NNLO ~ 10% shape effects
- NLO EW ~ 10-15% shape effects

► PO in VH [slides by J. Lindert]

Practical problem:

- process governed by $q^2 = m_{Vh}^2$
- not measurable in all decay modes ($V=W$ or $H \rightarrow WW$)

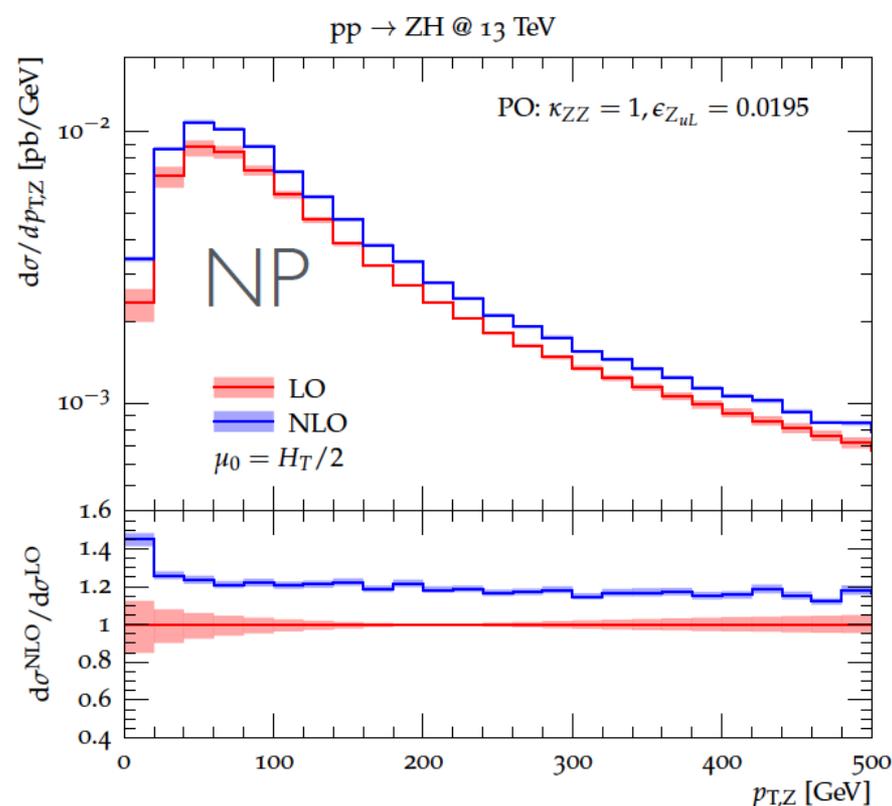
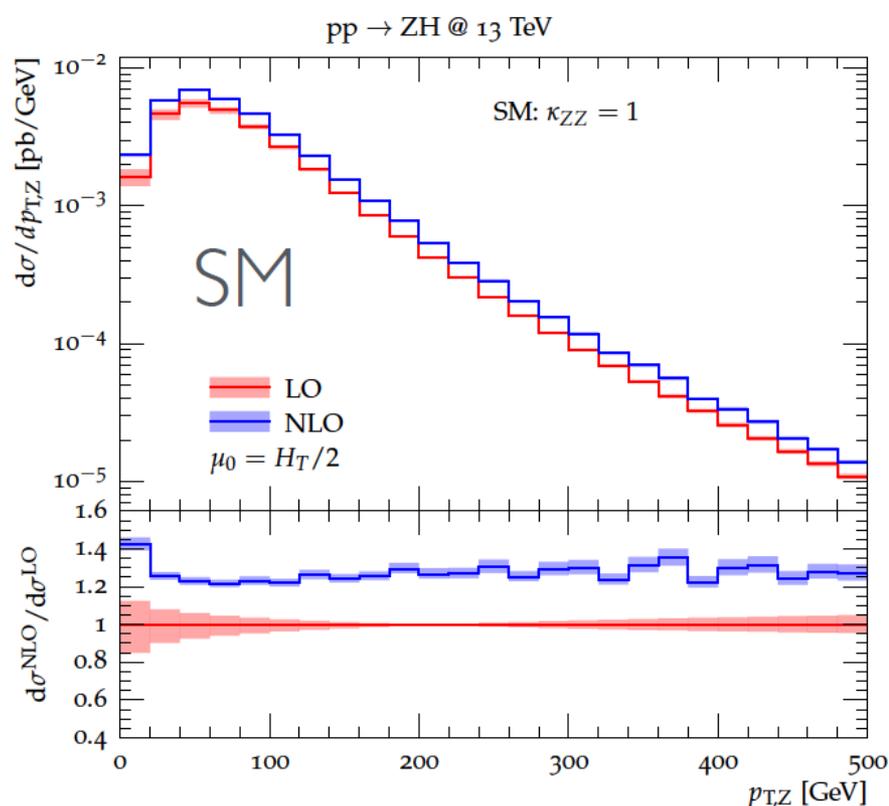


$$m_{Vh}^2 \rightarrow 4p_T^2 \quad \text{for} \quad |p_T| \rightarrow \infty$$

► PO in VH [slides by J. Lindert]

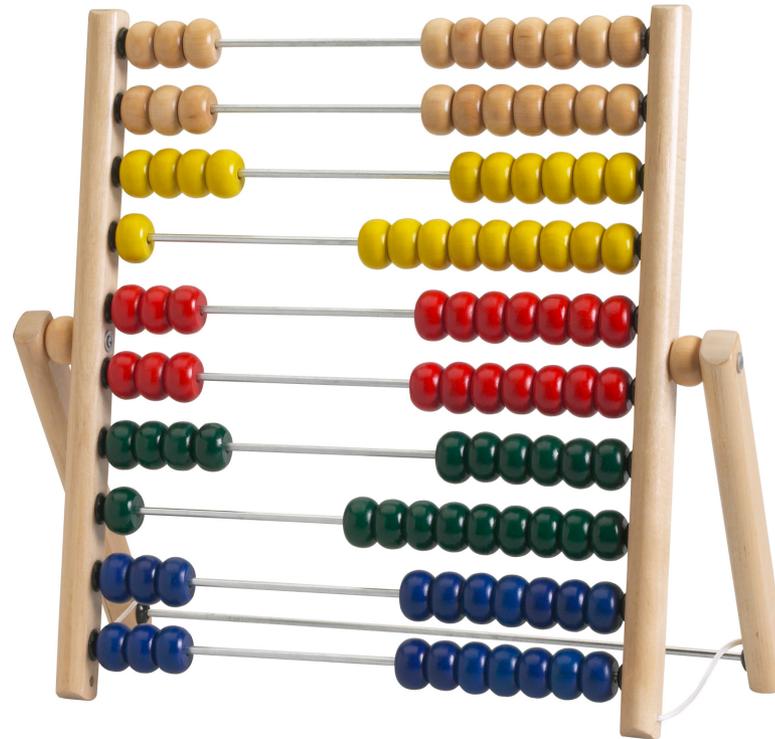
NLO QCD corrections in PO

- process independent implementation of **Higgs PO @ NLO QCD** in Sherpa+OpenLoops
- via Sherpa's UFO functionality (1412.6478)



- NP shapes largely unaffected by QCD corrections
- detailed study @ NLO+PS in preparation

PO vs. EFT,
parameter counting & symmetry limits



► PO vs. EFT

PO and couplings in EFT Lagrangians are *intimately related but are not the same thing* (on-shell amplitudes vs. Lagrangians parameters) → full complementarity

- The PO **are calculable in any EFT** approach (*linear, non-linear, LO, NLO...*)
 - In the limit where we work at the tree-level in the EFT there is a simple linear relation between PO and EFT couplings: each PO represent a unique linear combination of couplings of the most general Higgs EFT.
 - This does not hold beyond the tree-level (the PO do not change, but their relation to EFT couplings is more involved....)

→ PO note in YR4

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 - ➔ This does not hold beyond the tree-level (the PO do not change, but their relation to EFT couplings is more involved....)
- For Higgs production also the PO involve an **expansion in momenta**; however, this is different than the operator expansion employed within the EFT
 - ➔ To define the PO we expand only on a measurable kinematical variables, this is why the validity of the *expansion can be checked directly by data* (on the same process used to determine the PO)
- In each process the PO are the maximum number of independent observables that can be extracted by that process only → **naturally optimized for data analyses**

► Parameter counting & symmetry limits

Number of independent PO for **EW Higgs decays** + **EW production** + **Yukawa modes** ($h \rightarrow ff$):

PO set with maximal symmetry [CP + Lepton Univ]:

	<i>Minimal set:</i>		<i>Without custodial symm.:</i>
Prod. & decays	$\kappa_{ZZ}, \kappa_{Z\gamma}, \epsilon_{ZZ}$		$\kappa_{WW}, \epsilon_{WW}$
EW decays only	$\kappa_{\gamma\gamma}, \epsilon_{Ze_L}, \epsilon_{Ze_R}, \epsilon_{We_L}$		$\epsilon_{Z\nu_\mu}$
EW prod. only	$\epsilon_{Zu_L}, \epsilon_{Zu_R}, \epsilon_{Zd_L}, \epsilon_{Zd_R}$		ϵ_{Wu_L}
		15 (11)	[→ 32 with no symm.]
Yukawa modes	$\kappa_b, \kappa_\tau, \kappa_c, \kappa_\mu$	4	[→ 8 with no symm.]
<i>(as in the original κ-formalism)</i>			
gg→h & ttH	κ_g, κ_t	2	[→ 4 with no symm.]

► Tools

A first automated public tool (*UFO model* for **MG5_aMC@NLO** or **Sherpa**) is now

- ♦ [fully available for decays](#) (*QED corrections fully accounted by standard shower algorithms, as verified by the comparison with Profecy4f*)
- ♦ [will soon be available also for EW production](#), with inclusion of NLO QCD corrections (*work in prog....*)



Higgs PO

DESCRIPTION

DOWNLOAD

CONTACTS

<http://www.physik.uzh.ch/data/HiggsPO>

► Tools & Work in Progress

A first automated public tool (*UFO model* for **MG5_aMC@NLO** or **Sherpa**) is now

- ♦ fully available for decays (*QED corrections fully accounted by standard shower algorithms, as verified by the comparison with Profecy4f*)
- ♦ will soon be available also for EW production, with inclusion of NLO QCD corrections (*work in prog....*)

Beside the activity on the tools (for NLO QCD corrections), more-theoretical on-going (post YR4...) activities includes:

- ♦ Inclusion of NLO EW corrections in production (VBF & VH)
- ♦ Development of the PO formalism for ttH beyond κ_t (*non-trivial kin. effects*)
- ♦ Extraction of EFT couplings @ NLO

Conclusions

- The **PO** represent a general tool for the exploration of Higgs properties (in view of high-statistics data), with minimum loss of information and minimum theoretical bias → *full complementary to EFT* (and explicit BSM)
- The formalism is now fully developed for Higgs decays and Higgs EW productions [→ *see PO section in YR4*]
- NLO tools are ready for all relevant Higgs decay channels and (almost) ready for EW production (VBF+VH)
- On-going (beyond YR4) activity on NLO EW corrections & ttH.