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Higgs Boson Production with Multiple Hard Jets

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SMLHC Workshop - UCL

Overview

How can we reliably estimate multijet final states?

- ▶ Traditional methods for calculating jets.
- ▶ Higgs physics at the LHC.
- ▶ New technique for calculating Higgs + multijets.
- ▶ Example results and outlook.

- ▶ Events at the LHC will be dominated by multijet final states.
- ▶ These arise from QCD radiation.
- ▶ In some processes, measurable properties are sensitive to this radiation. Number of jets? Hard or soft?
- ▶ Need to be able to calculate Feynman diagrams with lots of quark and gluon legs.
- ▶ Let's review existing methods...

Fixed Order Perturbation Theory

Why not just calculate all the Feynman diagrams?

- ▶ In principle, can write down Feynman diagrams at any order of α_S and calculate them.
- ▶ Real and virtual contributions are both singular, but singularities cancel when added together.
- ▶ However, calculational complexity increases stupendously with:
 1. Increasing order in the coupling constant (number of diagrams grows factorially).
 2. Number of external parton legs (number of scales in the problem increases).
- ▶ Only very low orders in α_S are known for most processes...

Parton Shower Techniques

- ▶ Can use parton showers to simulate extra radiation.
- ▶ Based on a known factorisation of matrix elements in the *soft* and *collinear* limit.
- ▶ Shower is applied to each external leg.
- ▶ Get final states with many particles.
- ▶ Can couple to hadronisation / detector simulations etc.
- ▶ Accurate only if jets are soft - can increase accuracy by including higher order tree level matrix elements.

Summary of Methods for Final State Jets

Exact

- ▶ Use standard perturbation theory at LO, NLO...
- ▶ Best thing to do, but very difficult.
- ▶ Limited to small numbers of final state partons and low orders in α_S .

- ▶ We know that parton showers are insufficient in some processes.

→ Can we instead estimate **hard** radiation in the final state?

Approximate

- ▶ Combine tree level matrix elements (e.g. from MADGRAPH) with parton showers.
- ▶ Get more realistic final states.
- ▶ However, only soft / collinear enhanced radiation included (low p_t).

New method

- ▶ Will now introduce our new technique.
- ▶ Aim: estimate hard jets in the matrix element.
- ▶ Will start with a known factorisation formula for hard jet emission (FKL).
- ▶ Can be modified to include known features of the perturbation expansion.
- ▶ Will apply this to Higgs boson production via GGF.
- ▶ Can validate approximate matrix elements by comparing to known results at low orders in α_S .

FKL Factorisation - Overview

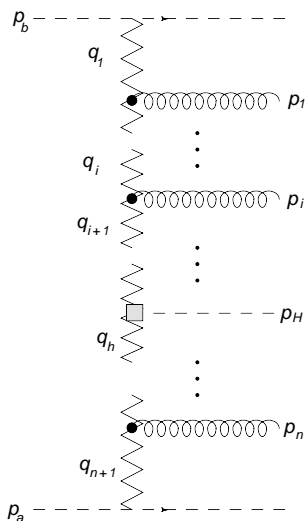
- ▶ In a particular kinematic limit (**MRK**), particular Feynman diagrams dominate the matrix element (**Fadin, Kuraev & Lipatov**).
- ▶ These correspond to the process:

$$\alpha + \beta \rightarrow \alpha + \beta + ng,$$

where $\alpha, \beta \in \{q, \bar{q}, g\}$.

- ▶ The sum of such diagrams gives a factorised expression for the matrix element in terms of:
 1. Impact factors for the incoming jets and additional particles (e.g. Higgs, W bosons).
 2. Modified emission vertices for the outgoing gluons.
 3. Propagators for the (virtual) exchanged gluons.
 4. Leading virtual corrections.
- ▶ Let's look at this for Higgs production...

FKL factorisation



► The FKL formula:

$$\begin{aligned}
 i\mathcal{M}_{\mu_1 \dots \mu_n}^{ab \rightarrow abj_1 \dots j_n} &= 2s(g_s)^{n+2} \\
 &\times \left(\prod_{i=1}^{n_1+1} \frac{1}{q_i^2} \exp[\hat{\alpha}(q_i^2)(y_{i-1} - y_i)] \right) \\
 &\times \left(\prod_{i=1}^{n_1} C_{\mu_i}(q_{i-1}, q_i) \right) C_H(q_{n_1+1}, q_{n_1+2}) \\
 &\times \left(\prod_{i=n_1+2}^{n+1} \frac{1}{q_i^2} \exp[\hat{\alpha}(q_i^2)(y_{i-1} - y_i)] \right) \\
 &\times \left(\prod_{i=n_1+2}^n C_{\mu_i}(q_{i-1}, q_i) \right)
 \end{aligned}$$

FKL - Comments

- ▶ Formally applies only in a certain high energy limit (MRK):

$$y_1 \ll y_2 \ll \dots y_n; \quad k_{1\perp} \sim k_{2\perp} \sim \dots k_{n\perp}.$$

- ▶ Jets strongly ordered in rapidity, but not in transverse momentum (so “hard”).
- ▶ Resums (includes at each order in α_S) leading logarithms in \hat{s}/t .
- ▶ In the traditional implementation of this formula, one replaces the virtual gluon 4 -momenta:

$$q_i \rightarrow q_{i\perp}$$

and ignores any contributions which are subleading in $\ln(\hat{s}/t)$.

- ▶ Can also ignore 4-momentum conservation at LL order.
- ▶ This is known as **BFKL** after **Balitski, Fadin, Kuraev & Lipatov**.
- ▶ Will see later how this performs for Higgs production - description is not good at LHC.

FKL - Comments

Advantages

- ▶ Factorised form - can be applied at any order in α_S .
- ▶ Gives exclusive multijet final states with hard jets.
- ▶ Some virtual corrections built in - collinear singularities cancelled.

- ▶ Solution: Use **FKL** as a starting point. Modify to build in extra features.

Disadvantages

- ▶ Only works in a certain kinematic limit (MRK)
- ▶ Does not approximate matrix element well outside this limit.
- ▶ MRK kinematics not a good approximation for the Tevatron or LHC.

Improved Description

- ▶ We construct approximate matrix elements from the FKL formula with the following prescription:
 1. Impose 4-momentum conservation at emission vertices.
 2. Use full dependence on virtual momenta instead of transverse components.
 3. Impose gauge invariance of Lipatov vertex ($k \cdot C=0$) over all of phase space.

- ▶ These modifications significantly affect the FKL description.

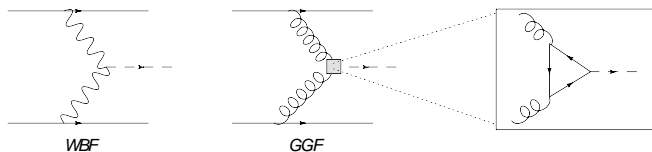
Improved Description - Comments

- ▶ Energy-momentum conservation is an obvious piece of physics, and should be included.
- ▶ Has been considered before, but makes numerical implementation mandatory.
- ▶ Use of full 4-momenta corresponds to including known singularity structure of amplitude, rather than shifting poles outside the MRK limit.
- ▶ Gauge invariance leads to local positivity of the Lipatov vertex ($-C.C > 0$), thus removes spurious negative contributions due to gauge-violating terms.
- ▶ These corrections are not just NLL...

Improved Description - More Comments

- ▶ Conservation of energy implements subleading corrections to FKL, but also phase space of emitted gluons.
- ▶ Thus goes beyond any logarithmic order in \hat{s}/t .
- ▶ Likewise, so does the use of full virtual momenta.
- ▶ Resulting matrix elements are much closer to fixed order perturbation theory than to the original FKL description.
- ▶ Will validate approximation by looking at a particular process (Higgs boson production via gluon-gluon fusion).
- ▶ Let's briefly review some aspects of Higgs physics at the LHC...

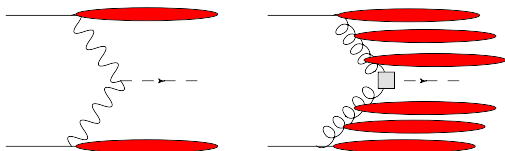
Higgs Production at the LHC



- ▶ Two main production modes - both can be used as a discovery channel.
 - ▶ WBF - measure coupling of h to vector bosons. Is it the SM Higgs?
 - ▶ GGF - measure nature of fermion coupling. CP even or odd?
 - ▶ Can use cuts to separate processes.
- ⇒ Need a detailed understanding of both production modes.

WBF & GGF - Differences

- ▶ No exchange of colour in WBF - QCD radiation limited mainly to incoming partons.
- ▶ Colour octet exchange in GGF - get lots of QCD radiation in central rapidity region.



- ▶ Understanding of jet pattern in GGF crucial for:
 1. Measurement of coupling of h to fermions.
 2. Efficient background reduction of GGF w.r.t WBF.

Implementation

- ▶ Have calculated GGF matrix elements using the modified FKL description.
- ▶ Factorised form - can be efficiently implemented in a numerical code.
- ▶ We produced a Monte Carlo implementation of our technique.
- ▶ Generates events (with any number of final state partons) weighted by the approximated matrix elements.
- ▶ To investigate how good the new approximate matrix elements are, can compare to exact perturbation theory.
- ▶ I.e. expand approximate results order by order in α_S , and compare with known tree level results for hjj and $hjjj$ ([MADGRAPH](#)).

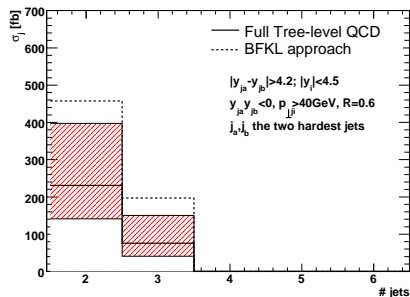
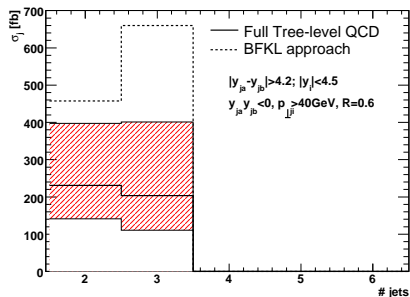
Results

- ▶ Will show results for *WBF cuts*, designed to reduce the GGF process.
- ▶ This has been widely studied in the literature with other techniques ([Zeppenfeld et. al.](#)).

$p_{c\perp}, p_{d\perp}, p_{j\perp}$	$> 40 \text{ GeV}$	$y_c \cdot y_d$	< 0
$ y_j $	< 4.5	$ y_c - y_d $	> 4.2

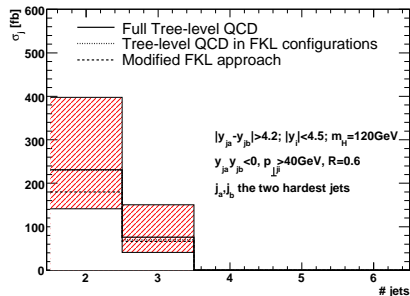
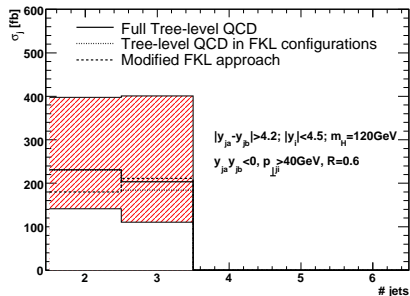
- ▶ But results are representative of those obtained for other cuts.
- ▶ First show traditional BFKL results, before the new approach...

BFKL comparison



- ▶ The BFKL description with 4-momentum conservation is shown.
- ▶ Does not work well.

Improved description

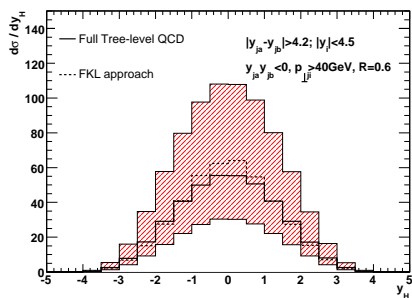
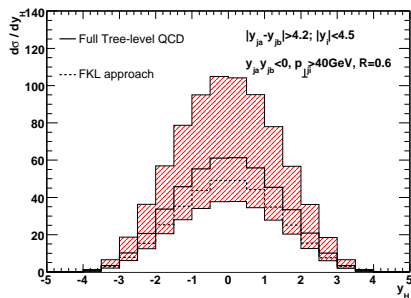


- Approximation is well within scale variation!

Comments

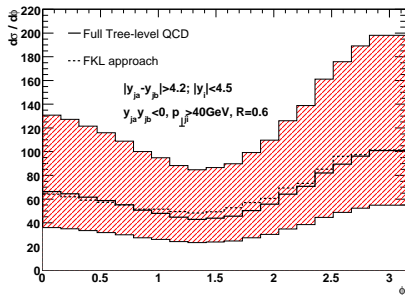
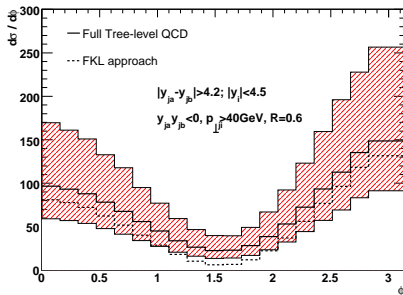
- ▶ Total cross-sections are well estimated by the new technique.
- ▶ However, this is only part of the story.
- ▶ Can also check differential distributions at fixed order...

Rapidity of Higgs boson



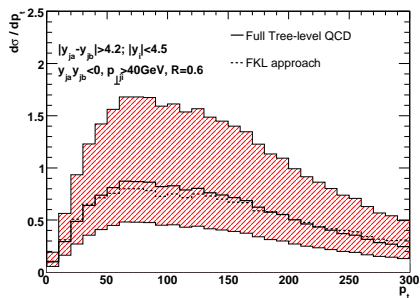
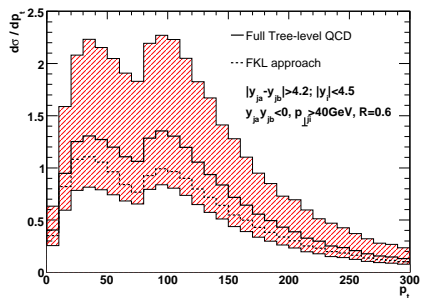
- Shown for hjj (left) and $hj\bar{j}\bar{j}$ (right).

Azimuthal angle between tagging jets

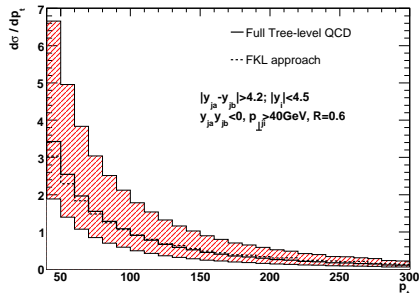
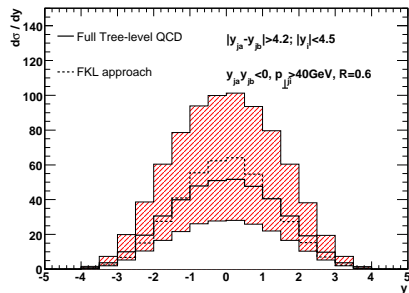


- Intimately related to CP nature of Higgs boson.

Transverse momentum of Higgs boson

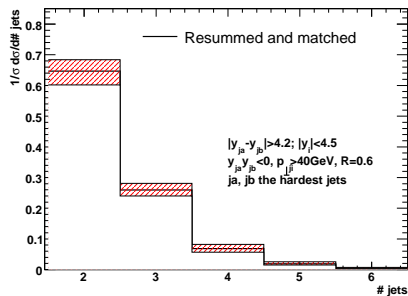
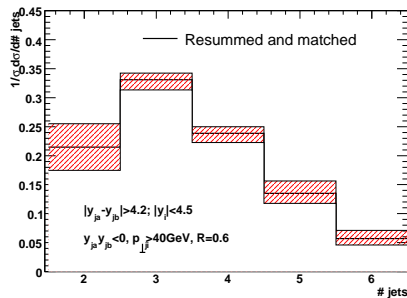


- Shape change due to azimuthal correlation...

Properties of third parton in $hjjj$ 

- ▶ Approximate matrix elements are working well.
- ▶ Can now turn on full resummation i.e. look at effect of multiple hard jets.

Number of hard jets



- ▶ Tagging on hardest jets reduces impact of further radiation.
- ▶ Still significant number of events with many hard partons.

Azimuthal correlation

- ▶ We have already seen that the azimuthal angle distribution has a pronounced shape at fixed order.
- ▶ Related to CP nature of Higgs-fermion coupling.
- ▶ Whether or not it can be measured depends strongly on the extent of QCD radiation.
- ▶ Introduce (Zeppenfeld et. al.):

$$A_\phi = \frac{\sigma(\phi_{j_a j_b} < \pi/4) - \sigma(\pi/4 < \phi_{j_a j_b} < 3\pi/4) + \sigma(\phi_{j_a j_b} > 3\pi/4)}{\sigma(\phi_{j_a j_b} < \pi/4) + \sigma(\pi/4 < \phi_{j_a j_b} < 3\pi/4) + \sigma(\phi_{j_a j_b} > 3\pi/4)}$$

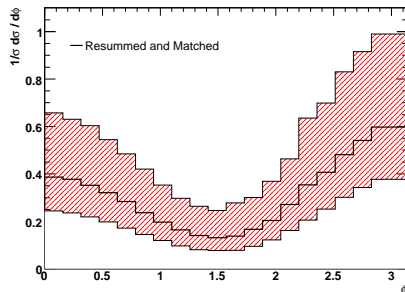
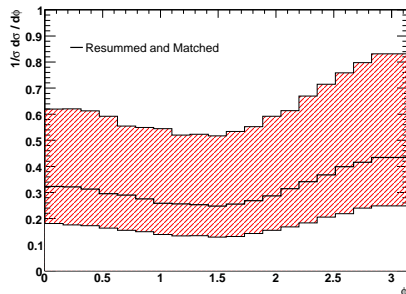
- ▶ $|A_\phi = 0|$ for completely uncorrelated jets, and 1 for completely correlated.
- ▶ $A_\phi \sim 0$ for WBF.
- ▶ In GGF, $A_\phi > 0$ for CP even (scalar) Higgs and < 0 for CP odd (pseudoscalar).

A_ϕ values

Inclusive cuts	A_ϕ	Hardest cuts	A_ϕ
LO 2-jet	0.456	LO 2-jet	0.456
Resummed, = 2-jet	0.444	Resummed, = 2-jet	0.436
LO 3-jet	0.203	LO 3-jet	0.374
Resummed	0.123	Resummed	0.372

- ▶ Cuts can efficiently be used to increase the observed correlation.
- ▶ E.g. jet vetoes, tagging jet choice.

Azimuthal correlation



- Distributions confirm the numbers on the previous slide...

Conclusions

- ▶ Have devised a new technique for approximating matrix elements with multiple final state hard partons.
- ▶ Useful for estimating final state jet **topology**, rather than the jet **substructure** which is better estimated by a parton shower.
- ▶ Uses FKL factorisation as a starting point, with modifications to include known features of perturbation theory.
- ▶ So far applied to Higgs production.
- ▶ Code available for simulating Higgs + multijet events.

Outlook

- ▶ More detailed Higgs phenomenology in progress.
- ▶ Can extend technique to other processes (e.g. $W / Z + \text{jets}$, pure multijet).
- ▶ Underlying approximation (FKL factorisation) can be systematically improved.
- ▶ Interfacing to parton showers for a more complete description of final states.