

# PDF uncertainties and LHC physics

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## STANDARD MODEL

- There are W/Z 'calibration' measurements: Z/W ratio is the best
- W and Z cross-sections should first test our understanding and then contribute to our knowledge at greater precision
- W asymmetry should bring something new
- Beware that NEW low-x physics could compromise this.

## BEYOND STANDARD MODEL

- There are discovery channels – high ET jets- which could be obscured by PDF uncertainties
- But Jet Energy Scale Uncertainties could be more of a problem
- Be smart - look at ratios  $W+n\text{-jets}/Z+n\text{-jets}$

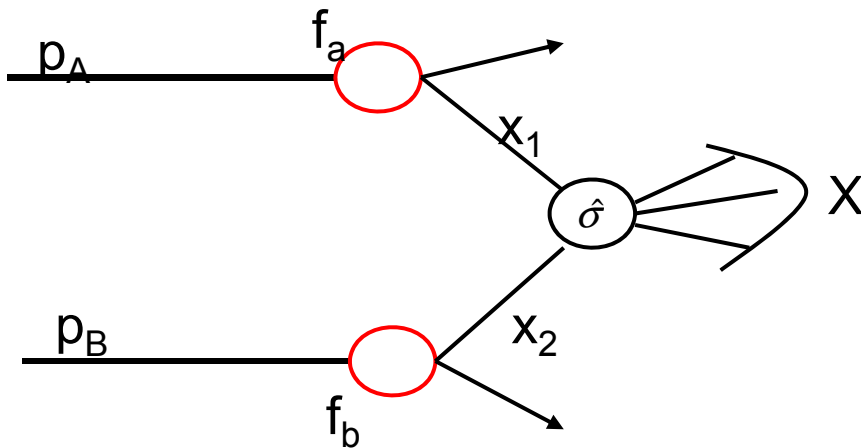
# The Standard Model is not as well known as you might think

In the QCD sector the PDFs limit our knowledge - transport PDFs to hadron-hadron cross-sections using QCD factorization theorem for short-distance **inclusive** processes

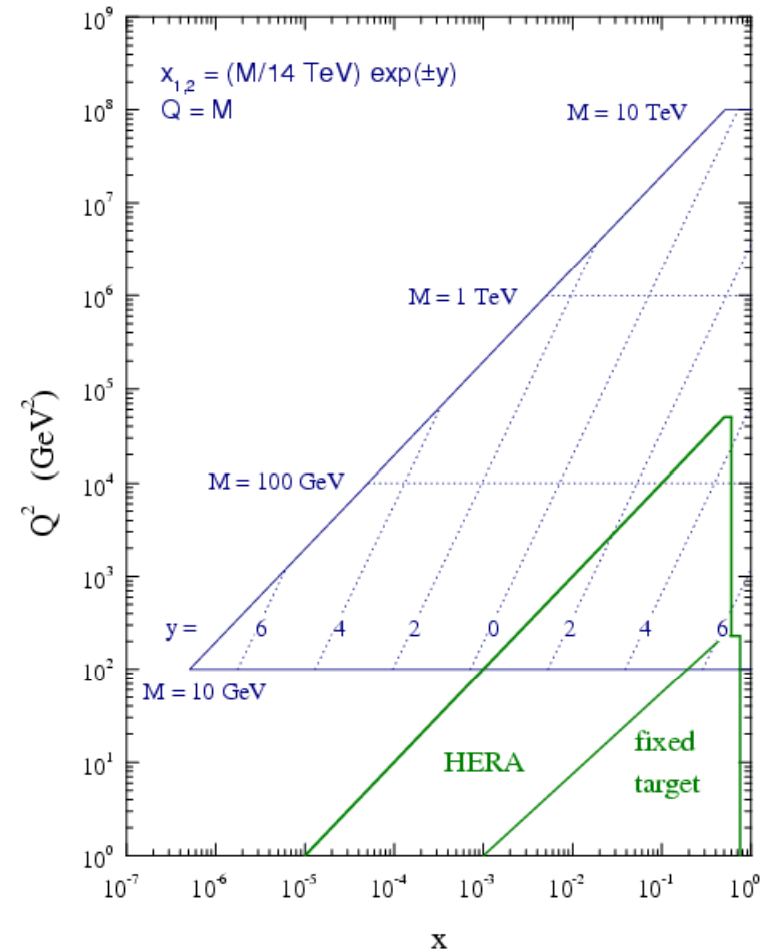
$$\sigma_X = \sum_{a,b} \int_0^1 dx_1 dx_2 f_a(x_1, \mu_F^2) f_b(x_2, \mu_F^2) \times \hat{\sigma}_{ab \rightarrow X} \left( x_1, x_2, \{P_i^\mu\}; \alpha_S(\mu_R^2), \alpha(\mu_R^2), \frac{Q^2}{\mu_R^2}, \frac{Q^2}{\mu_F^2} \right)$$

where  $X=W, Z, D\text{-}Y, H, \text{high-}E_T \text{ jets, prompt-}\gamma$  and  $\hat{\sigma}$  is known

- to some fixed order in pQCD and EW
- in some leading logarithm approximation (LL, NLL, ...) to all orders via resummation



**LHC parton kinematics**



**The central rapidity range for W/Z production AT LHC is at low-x**

**( $6 \times 10^{-4}$  to  $6 \times 10^{-2}$ ) at 14 TeV**

**( $8.5 \times 10^{-4}$  to  $8.5 \times 10^{-2}$ ) at 10 TeV**

The general trend of PDF uncertainties is that

**The u quark is much better known than the d quark**

**The valence quarks are much better known than the gluon/sea at high-x**

**The valence quarks are poorly known at small-x but they are not important for (most) physics in this region (except W asymmetry)**

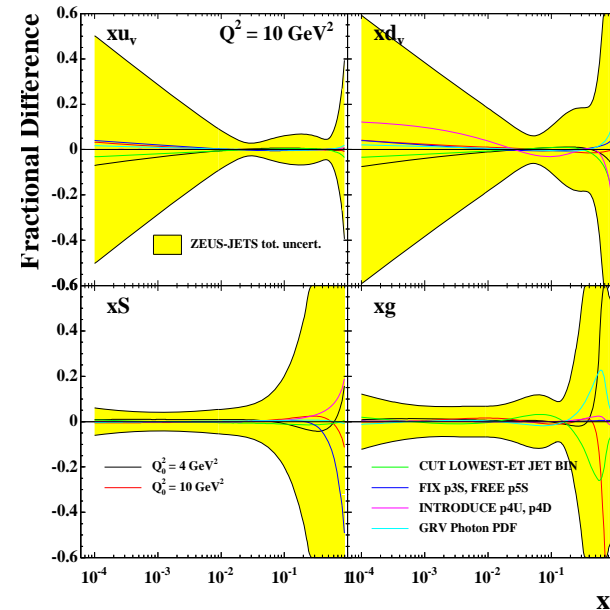
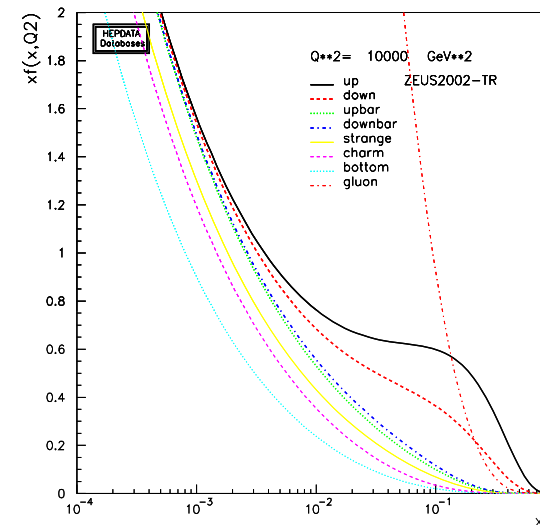
**The sea and the gluon are reasonably well known at low-x- but there is always room for improvement for precision measurements**

**The sea is poorly known at high-x, but the valence quarks are more important in this region**

**The gluon is poorly known at high-x**

**And it can still be very important for physics e.g.– high ET jet xsecn**

**For  $Q^2=10000$  the gluon is the dominant parton until VERY high-x**



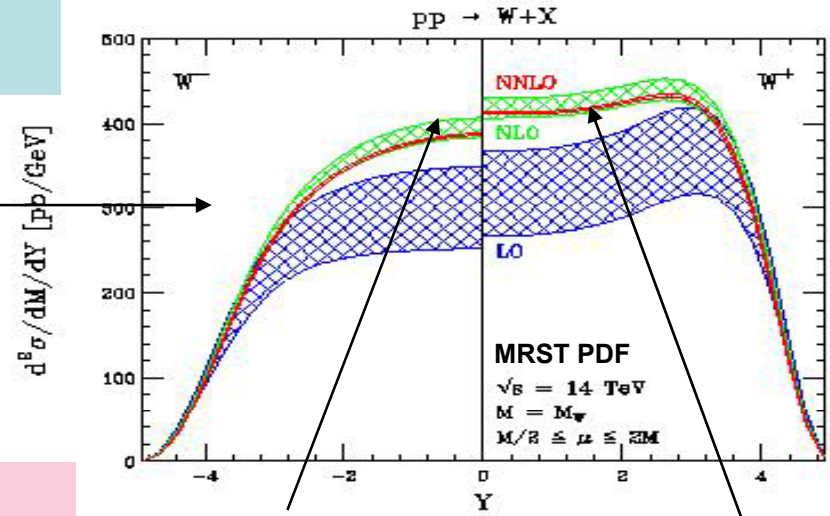
# WHAT DO WE KNOW WELL?

W/Z production have been considered as good standard candle processes with small theoretical uncertainty.

PDF uncertainty is THE dominant contribution and most PDF groups quote (68% uncertainties)  $< \sim 3\%$  (note HERAPDF  $\sim 1\%$ )

Re do at 10 TeV

PDF set	$\sigma_{W^+} B_{W^+ \rightarrow l\nu}$ (nb)	$\sigma_{W^-} B_{W^- \rightarrow l\nu}$ (nb)	$\sigma_Z B_{Z \rightarrow ll}$ (nb)
ZEUS-2005	$8.51 \pm 0.30$	$6.08 \pm 0.20$	$1.36 \pm 0.04$
MSTW08	$8.55 \pm 0.15$	$6.25 \pm 0.12$	$1.38 \pm 0.025$
CTEQ66	$8.77 \pm 0.18$	$6.22 \pm 0.14$	$1.40 \pm 0.027$
<b>HERAPDF</b>	<b><math>8.64 \pm 0.10</math></b>	<b><math>6.27 \pm 0.11</math></b>	<b><math>1.38 \pm 0.02</math></b>
CTEQ61	$8.29 \pm 0.22$	$5.90 \pm 0.17$	$1.32 \pm 0.030$
NNPDF1.0	$11.83 \pm 0.26$	$8.41 \pm 0.20$	$1.95 \pm 0.04$



NNLO corrections small  $\sim$  few%

NNLO residual scale dependence  $< 1\%$

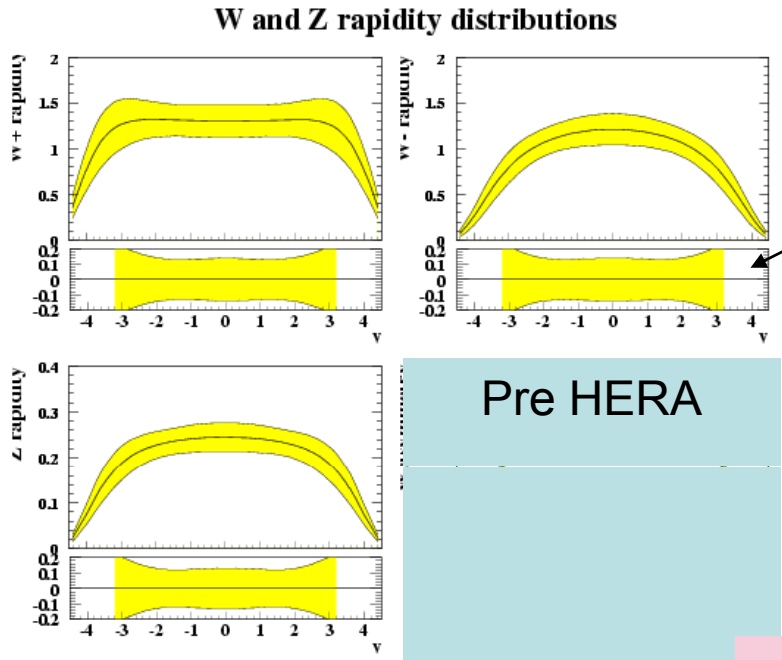
BUT the central values can differ by more than some of the uncertainty estimates  $\rightarrow$  uncertainty  $\sim 5\%$ . **Could be useful as luminosity monitor?**

**Beware Massless heavy quark treatment**

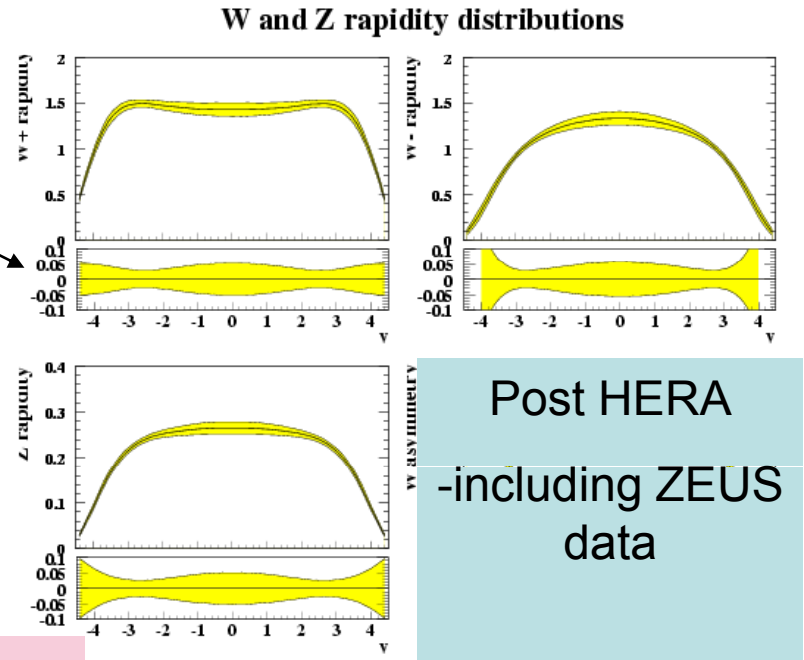
With massive treatment heavy quarks are more suppressed at low-scale so light-quarks increase to compensate when fitting same low-scale data. Consequence is larger W/Z cross-sections at high-scale (CTEQ61 to 66)

# WHY DO WE KNOW IT SO WELL? BECAUSE OF HERA.

Look in detail at predictions for W/Z rapidity distributions: Pre- and Post-HERA



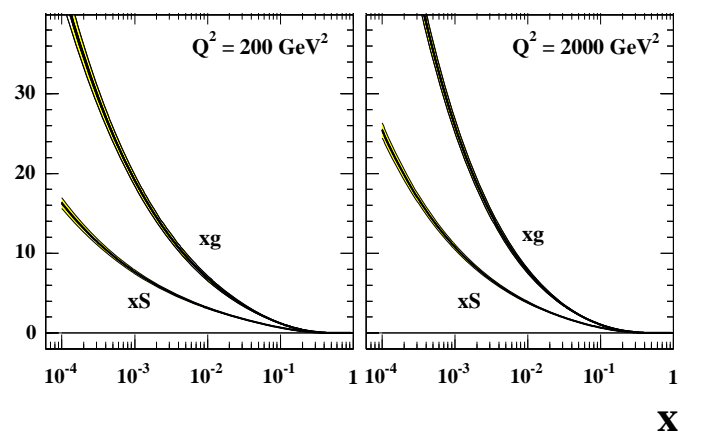
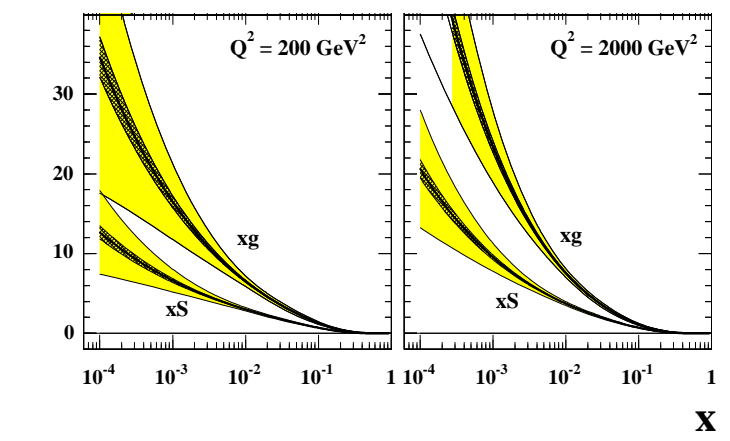
Note difference in scale for fractional errors



Pre HERA

Why such an improvement ?

Post HERA  
-including ZEUS data



It's due to the improvement in the low-x sea and gluon  
At the LHC the q-qbar which make the boson are mostly sea-sea partons  
And at  $Q^2 \sim M_Z^2$  the sea is driven by the gluon

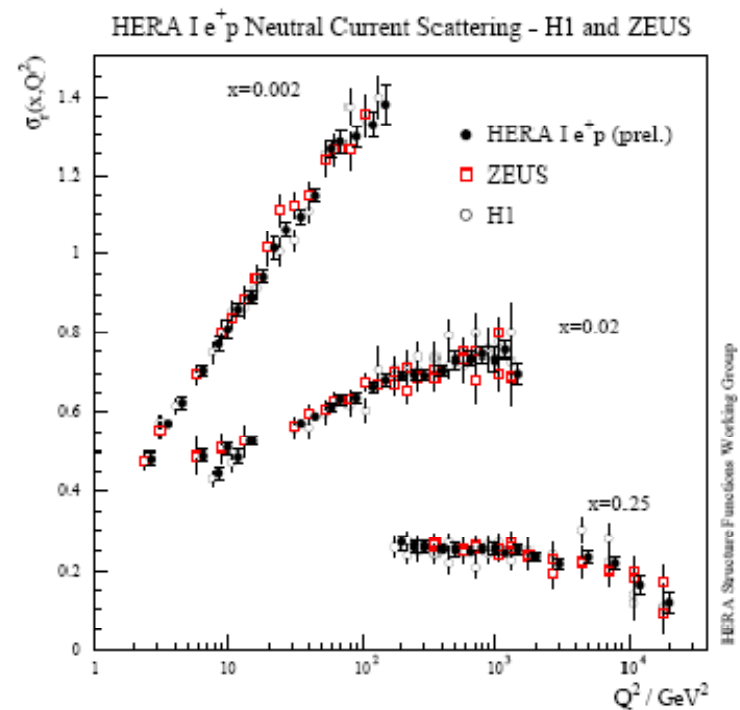
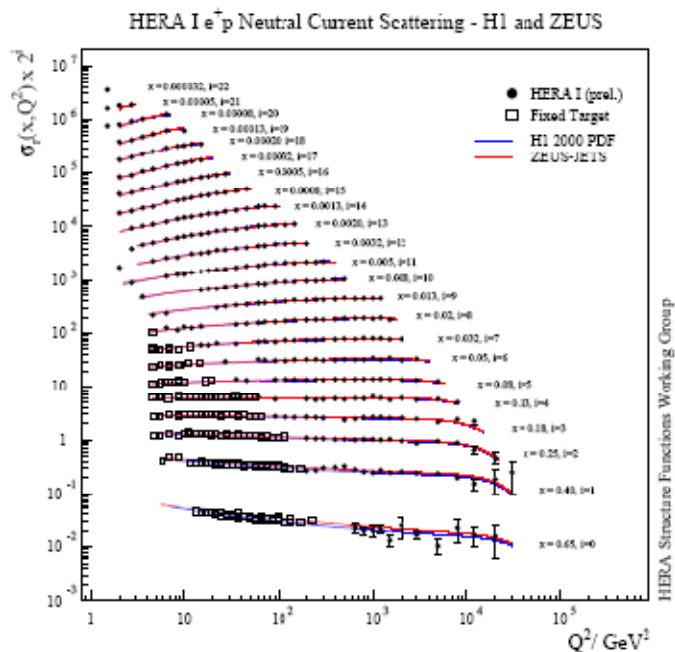
Of course global fits like CTEQ/MSTW include data from BOTH HERA experiments  
 BUT you can do this in a very 'smart' way

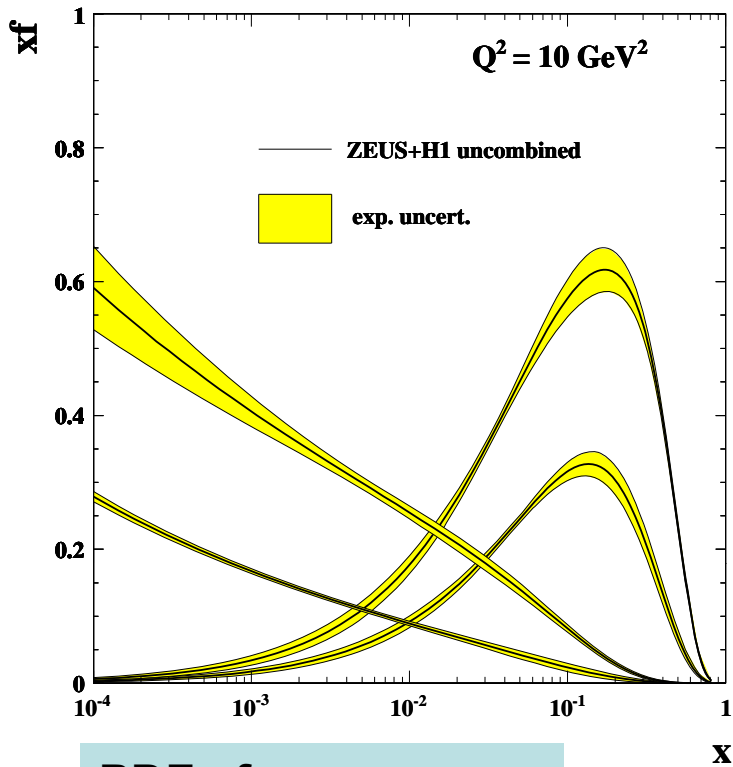
## Recent development: Combining ZEUS and H1 data sets

Not just statistical improvement. Each experiment can be used to calibrate the other since they have rather different sources of experimental systematics

- Before combination the systematic errors are  $\sim 3$  times the statistical for  $Q^2 < 100$
- After combination systematic errors are  $<$  statistical
- $\rightarrow$  very consistent HERA data set can be used as sole input to PDF fits with  $\Delta x^2 = 1$

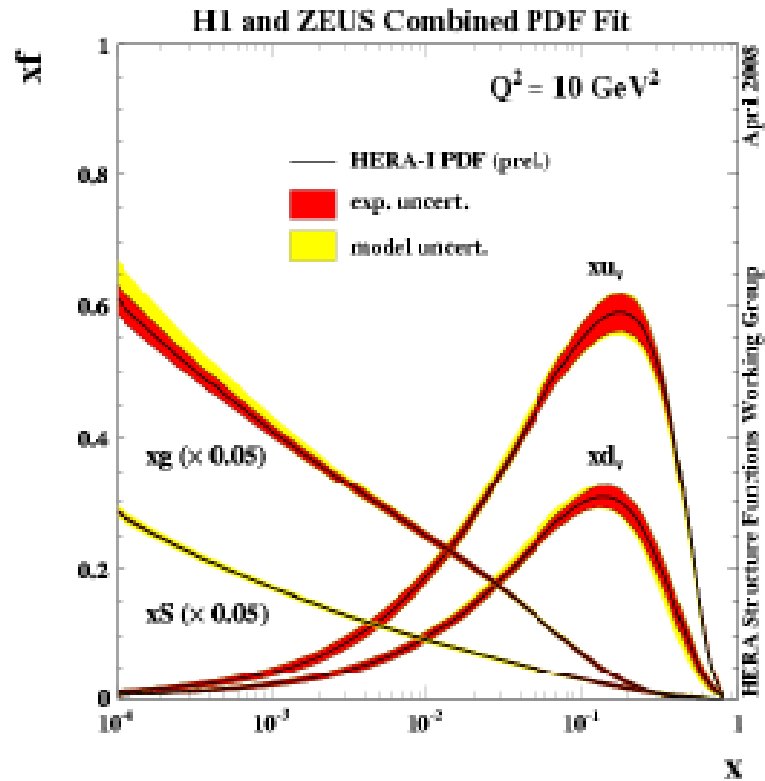
### HERAPDF0.1





PDFs from same QCD analysis of separate ZEUS and H1 data sets - before 'smart' combination

Experimental error only



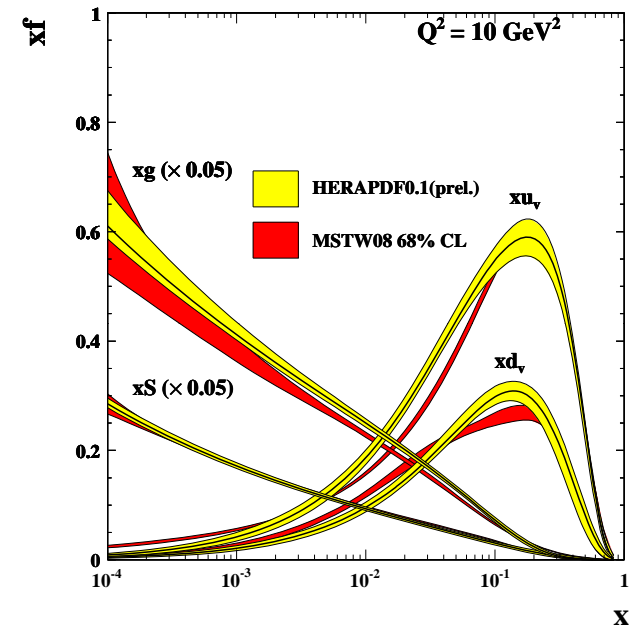
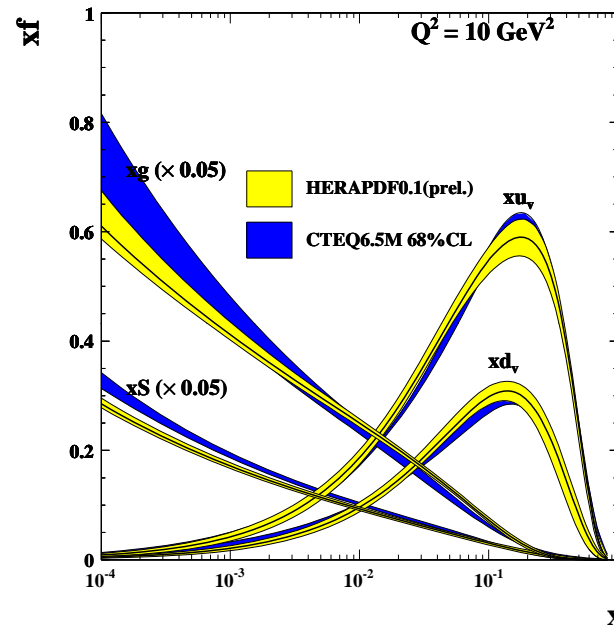
PDFs from same QCD analysis of combined HERA data - after 'smart' combination

HERAPDF0.1 has small experimental errors and modest model errors

## Compare HERAPDF to CTEQ6.5 and MSTW08 PDFs

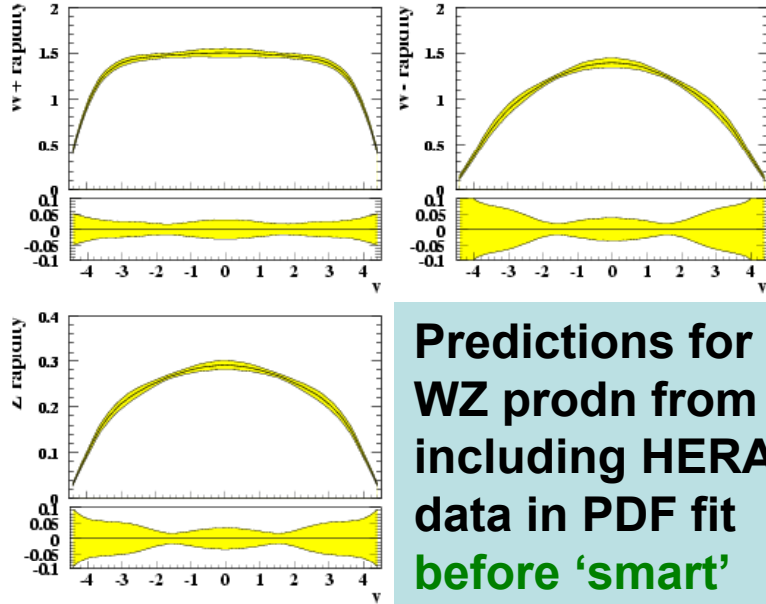
HERAPDF0.1  
experimental errors  
and model errors all  
included in the yellow  
band

CTEQ6.5 and  
MSTW08 uncertainty  
bands are done at  
68%CL for direct  
comparability





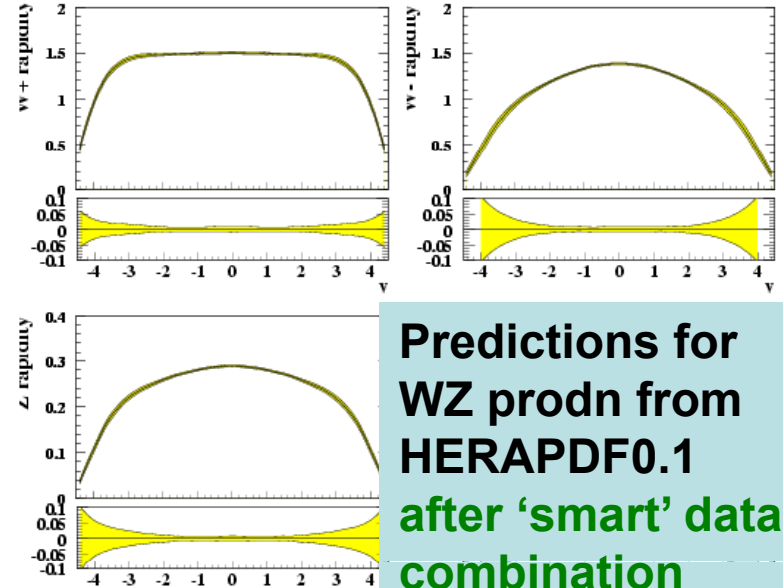
W and Z rapidity distributions



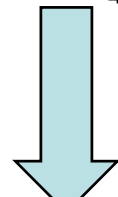
Predictions for WZ prodn from including HERA data in PDF fit before 'smart' data combination



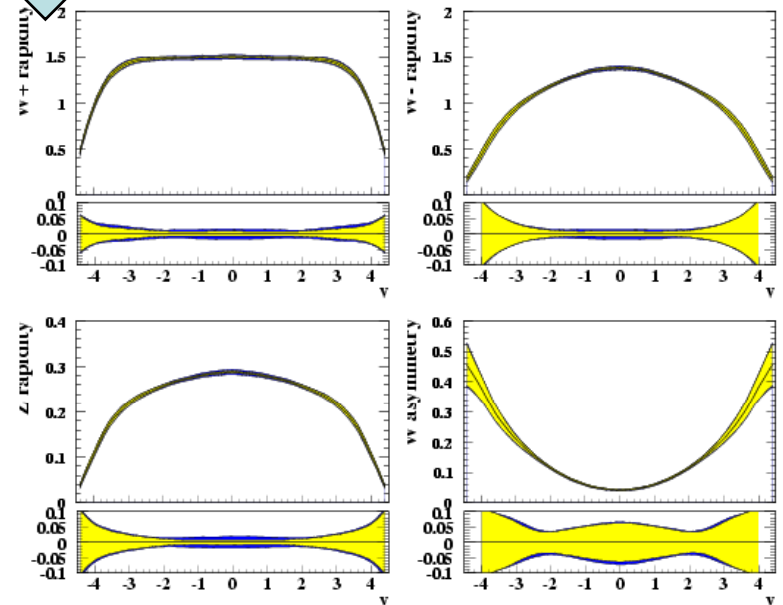
W and Z rapidity distributions



Predictions for WZ prodn from HERAPDF0.1 after 'smart' data combination



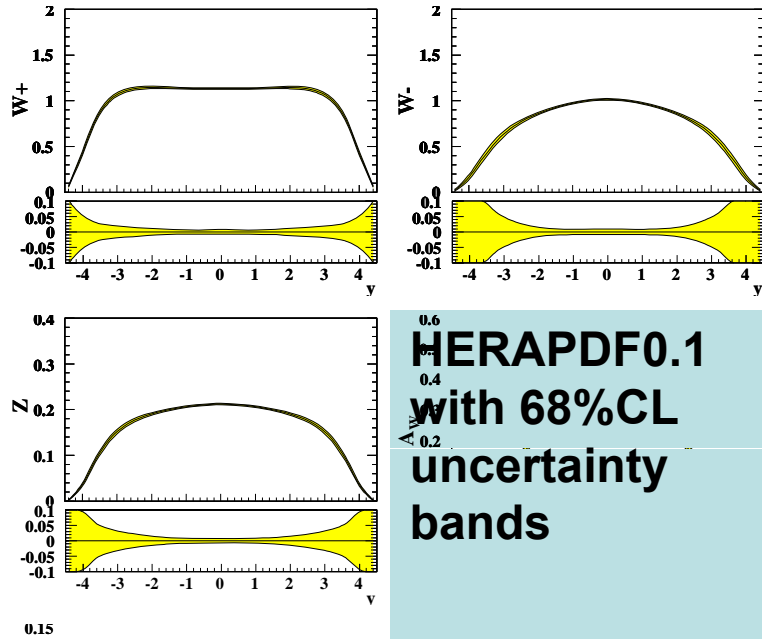
W and Z rapidity distributions



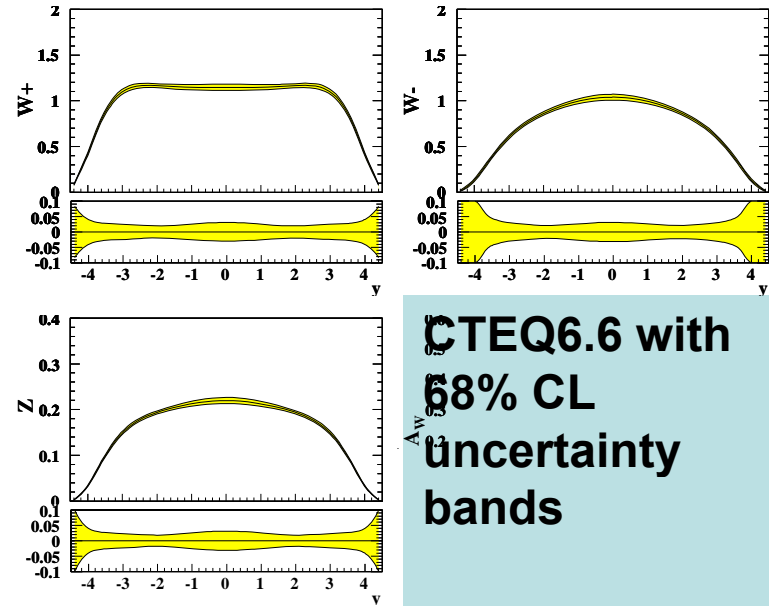
Experimental uncertainties are becoming so small that model dependence assumes greater importance- here add model errors to HERAPDF0.1 from input assumptions to PDF fitting

# Compare HERAPDF to CTEQ6.6 and MSTW08 for W/Z predictions for 10TeV

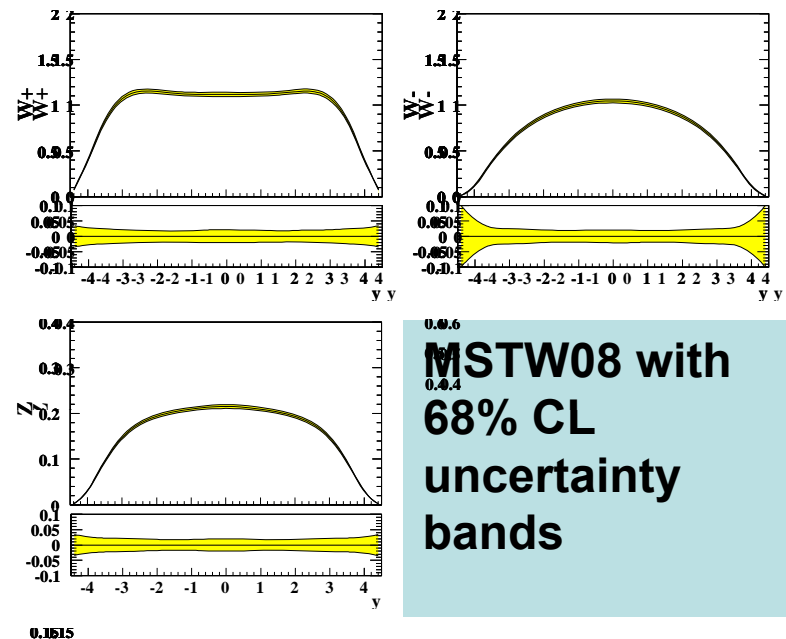
W and Z rapidity distributions



W and Z rapidity distributions



W and Z rapidity distributions



The new HERA combined data reduce the uncertainty in the central region- should be fed into CTEQ/MSTW fits

# Can we improve our knowledge of PDFs using LHC data itself?

## We actually measure the decay lepton spectra

Generate pseudodata at 14TeV corresponding to  $100\text{pb}^{-1}$  using CTEQ6.1M ZEUS\_S MRST2001 PDFs with full uncertainties

At  $y=0$  the total uncertainty is

$\sim \pm 6\%$  from ZEUS

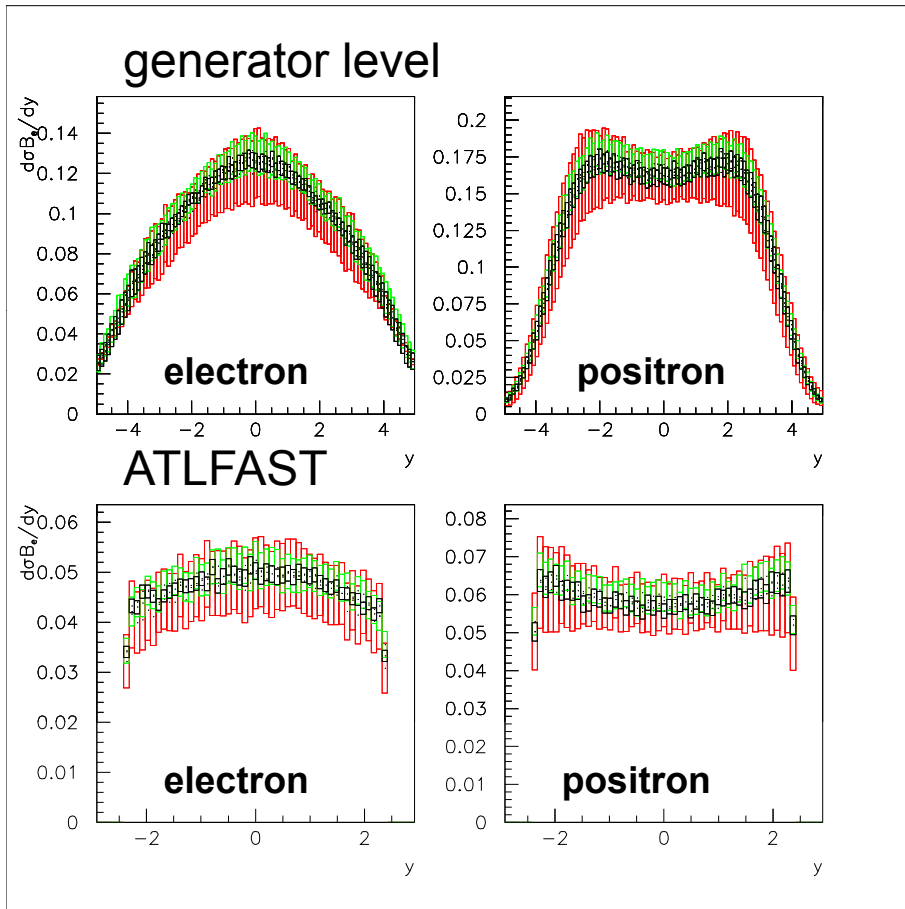
$\sim \pm 4\%$  from MRST01E

$\sim \pm 8\%$  from CTEQ6.1

To improve the situation we NEED to be more accurate than this:  $\sim 4\%$

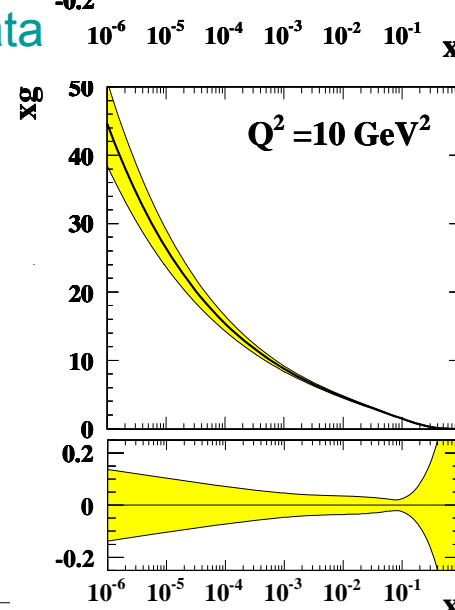
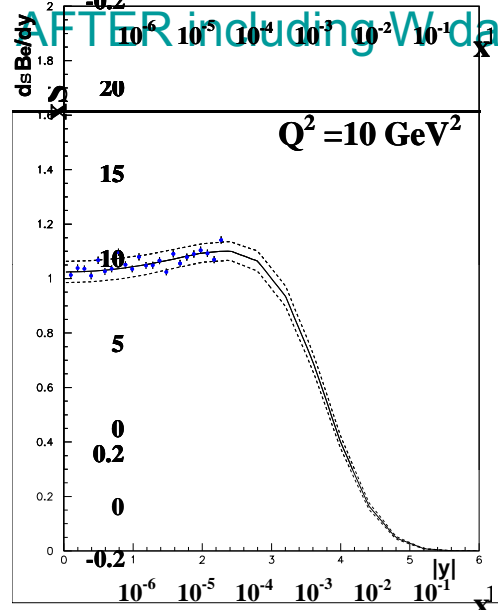
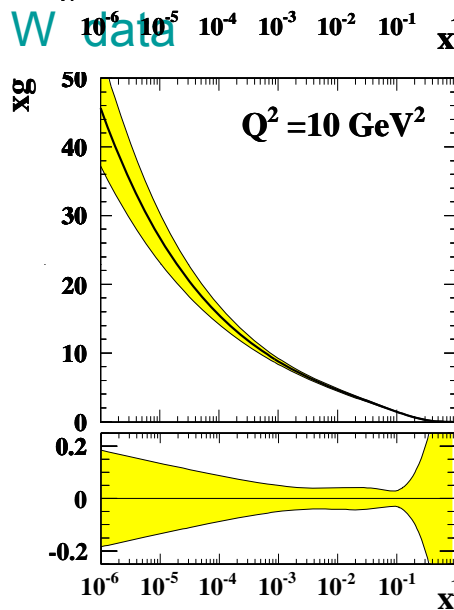
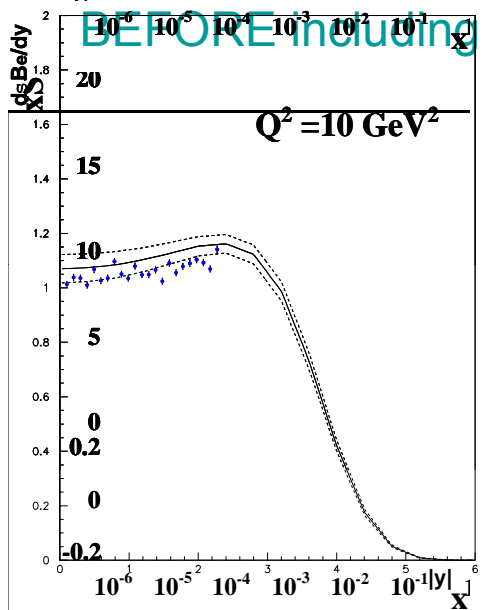
Statistics are no problem there will be millions of W's

We need to control the systematic uncertainty



# Can we improve the situation with early LHC data?

Generate  $W^+/W^-$  data with 4% error using CTEQ6.1 PDF, pass through ATLAS detector simulation and then include this pseudo-data in the global ZEUS PDF fit (actually use the decay lepton spectra) **Central value of prediction shifts and uncertainty is reduced**

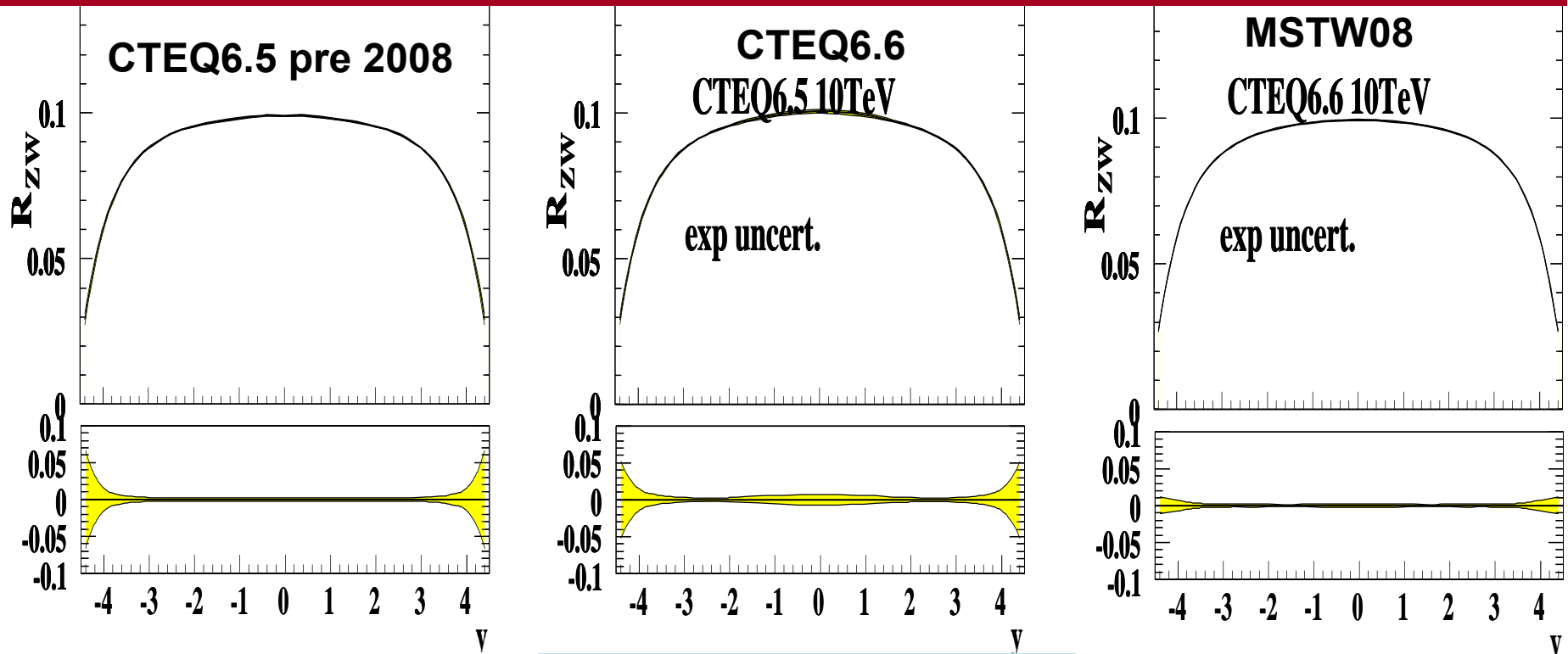


$e^+$  rapidity spectrum and gluon PDF  
BEFORE these data are included in the PDF fit

$e^+$  rapidity spectrum and gluon PDF  
AFTER these pseudodata are included in the PDF fit

**Gluon PDF uncertainties are reduced**

**Now let's look at ratios: Z/W ratio is a golden benchmark measurement - 10TeV**



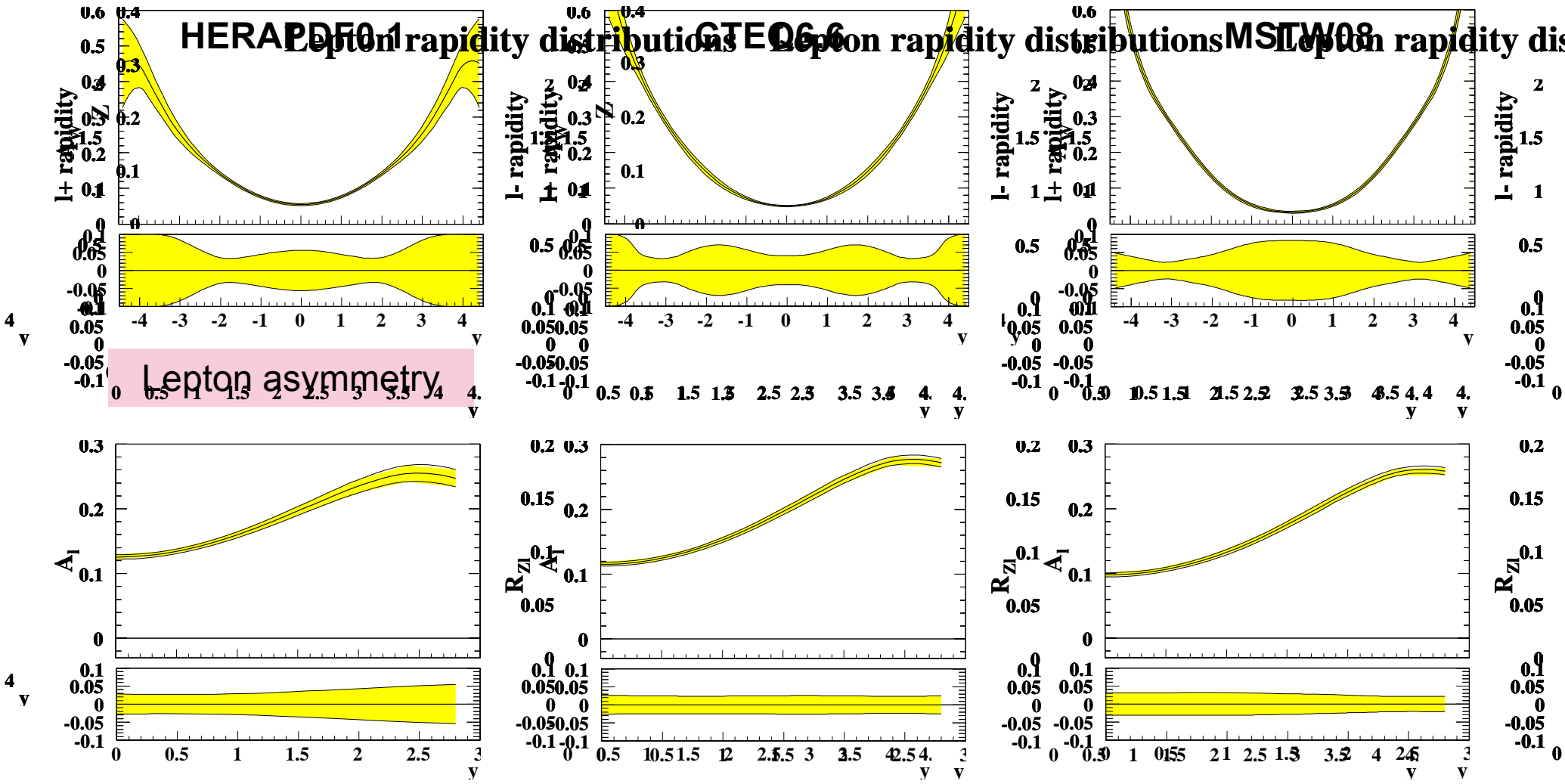
**ZOOM in on Z/W ratio – there is fantastic agreement between PDF providers**  
 PDF uncertainty from the low-x gluon and flavour symmetric sea cancels out- **and so do luminosity errors** BUT there is somewhat more PDF uncertainty than we thought before 2008 (~1.5% rather than <1% in the central region)

There is uncertainty in the strangeness sector that does not cancel out between Z and ( $W^+ + W^-$ )... it was always there we just didn't account for it

$$\frac{Z}{W^+ + W^-} \sim \frac{u\bar{u} + d\bar{d} + s\bar{s} + c\bar{c} + b\bar{b}}{(u\bar{d} + c\bar{s}) + (d\bar{u} + s\bar{c})}$$

YES this does translate to the Z/lepton ratio

But in the W asymmetry – there is NOT fantastic agreement - 10 TeV



Further sources of PDF uncertainty from the valence sector are revealed. And note that when it comes to W asymmetry CTEQ do not have the most conservative errors at central rapidity - MRST/MSTW do

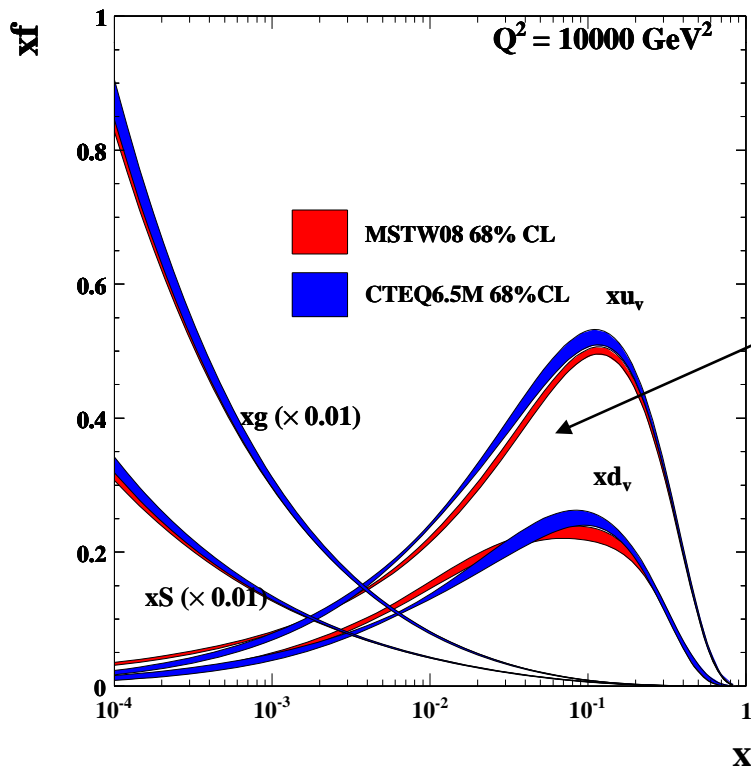
Dominantly, at LO  $A_W = \frac{(u \bar{d} - d \bar{u})}{(u \bar{d} + d \bar{u})}$

Predictions for  $A_W$  are different in the central region- because predictions for valence distributions at small-x are different

And  $\bar{u} \sim \bar{d} \sim \bar{q}$  at small x

So  $A_W \sim \frac{(u - d)}{(u + d)} = \frac{(u_v - d_v)}{(u_v + d_v + 2 \bar{q})}$

Actually this LO approx. is pretty good even quantitatively  
The difference in valence PDFs you see here does explain the difference in  $A_W$  between MRST and CTEQ



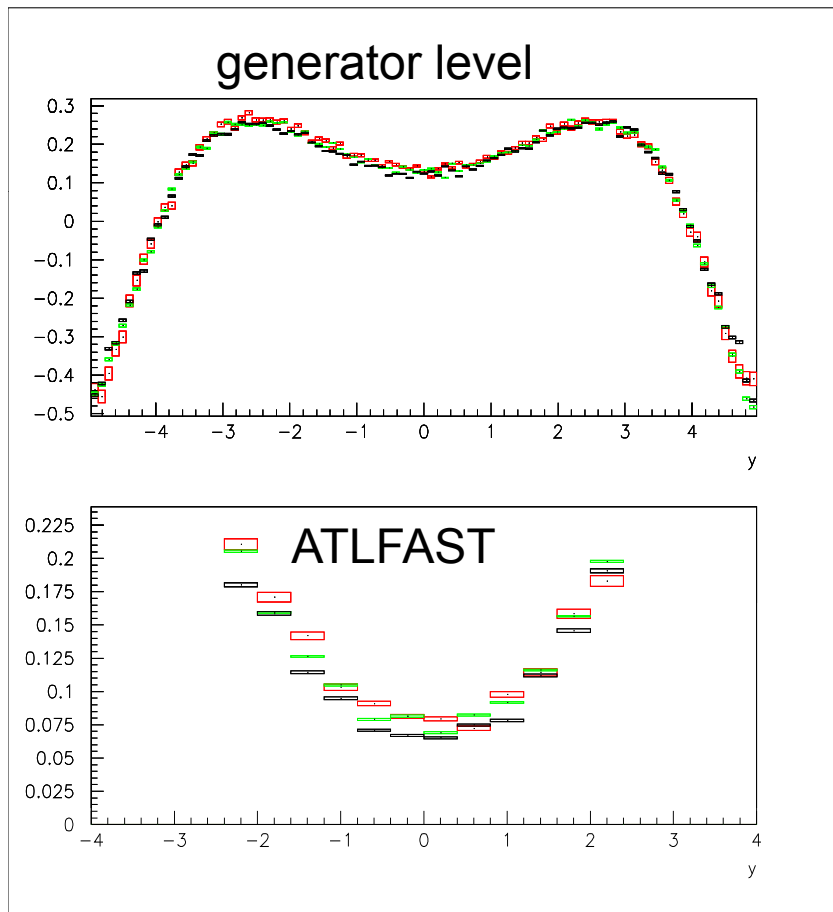
*x*-range affecting  $W$  asymmetry in the measurable rapidity range at ATLAS (10TeV)

# Can we improve our knowledge of PDFs using ATLAS data itself?

**We actually measure the decay lepton spectra**

Generate pseudodata at 14TeV corresponding to  $100\text{pb}^{-1}$  using **CTEQ6.1M** **ZEUS\_S** **MRST2004** PDFs with full uncertainties

Generate data with  $\sim 4\%$  systematic error on the asymmetry



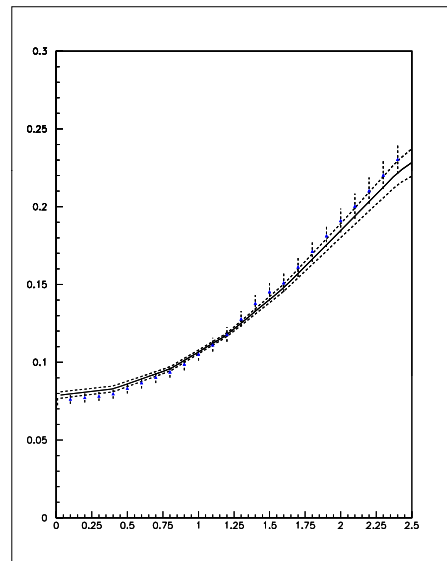
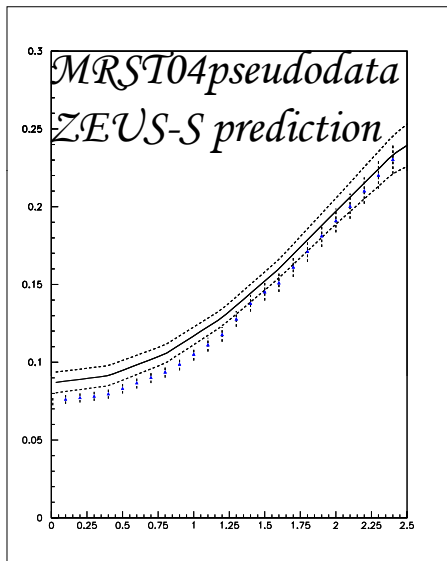


Generate data with 4% error using MRST04 PDF and then include this pseudo-data in the global ZEUS PDF fit (actually use the lepton asymmetry data)

The PDF uncertainty of the valence distributions is improved by the input of such data

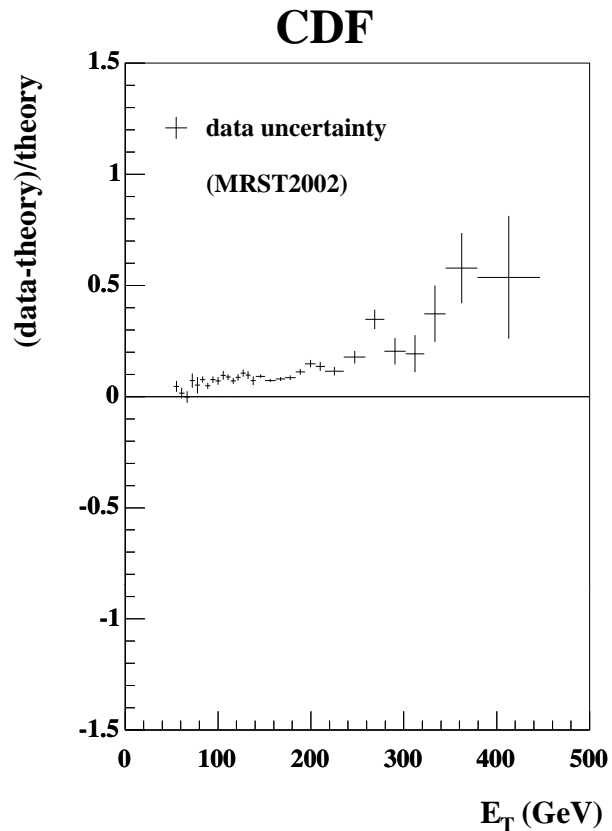
BEFORE including  $A_e$  pseudo-data

AFTER including  $A_e$  pseudo-data

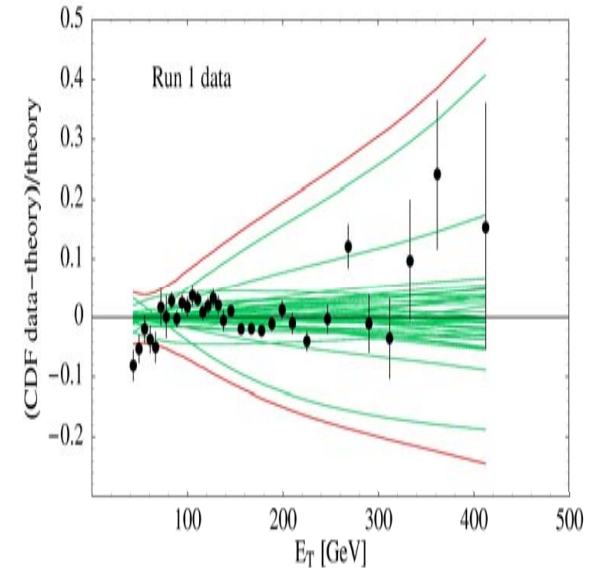


Result is improved accuracy of and change of shape of the valence PDFs

ATLAS/CMS LHC asymmetry data can measure valence distributions at  $x \sim 0.005$



**And what is not well known?**  
 Example of how PDF uncertainties matter for BSM physics— Tevatron jet data were originally taken as evidence for new physics--



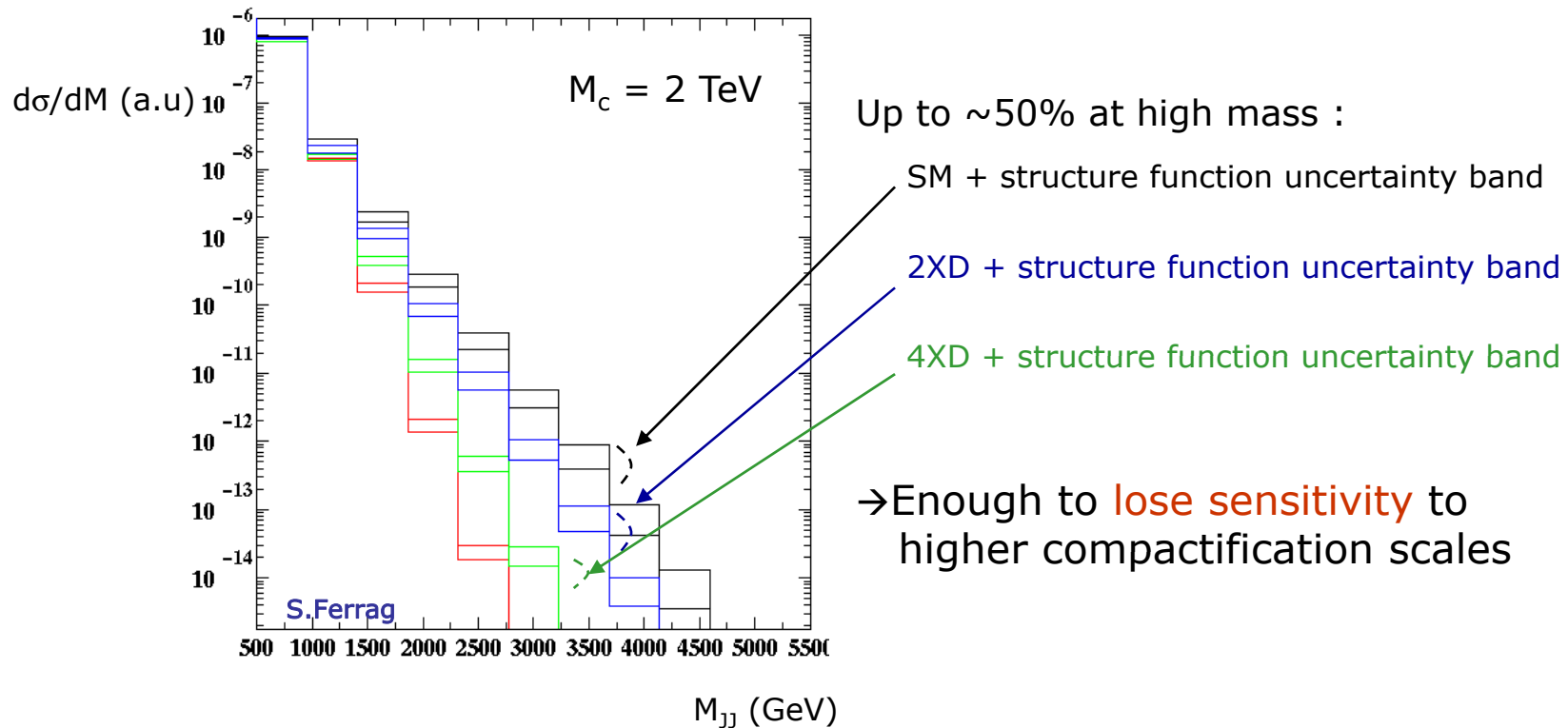
**Theory CTEQ6M**

These figures show inclusive jet cross-sections compared to predictions in the form  $(\text{data} - \text{theory}) / \text{theory}$

Today Tevatron jet data are considered to lie within PDF uncertainties  
 And the largest uncertainty comes from the uncertainty on the high  $x$  gluon

# And what consequences might this have?

Such PDF uncertainties in the jet cross sections compromise the LHC potential for discovery of any new physics which can be written as a contact interaction  
E.G. Dijet cross section has potential sensitivity to compactification scale of extra dimensions ( $M_c$ )

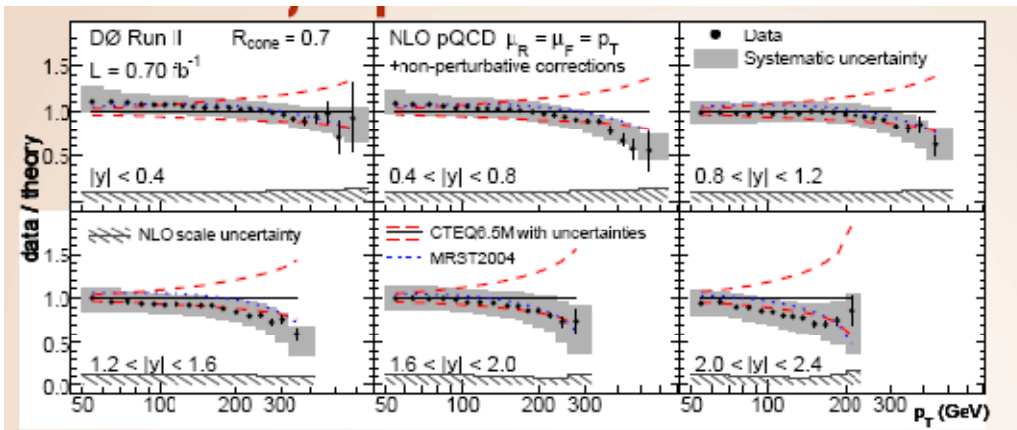
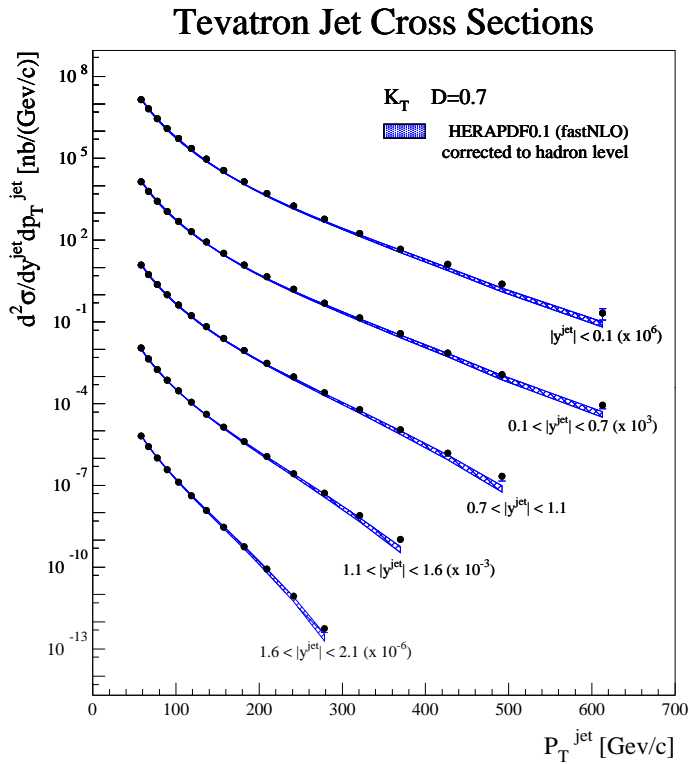


# CDF Run-II jet data compared to HERAPDF0.1

Note there is now new Tevatron Run-II jet data

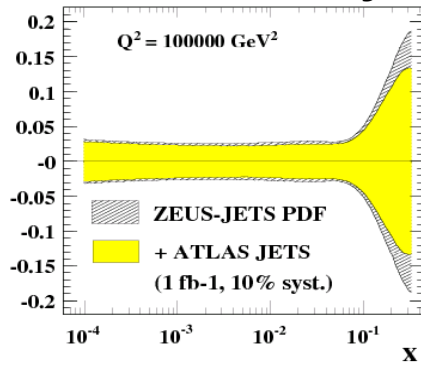
Has been used in MSTW08 PDFs

It does not make MUCH difference to the level of high-x gluon PDF uncertainty

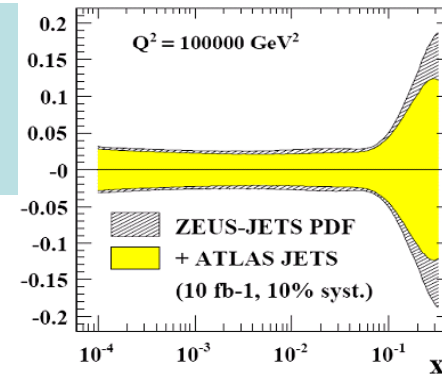


D0 jet data compared to CTEQ6.5 seem to be less hard than Run-I (CTEQ6.5 fitted Run-I)

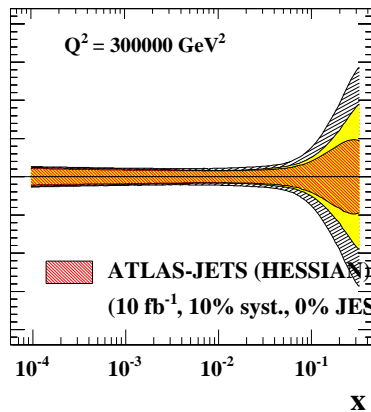
# And will we be able to use LHC data itself to improve the situation?- study of including ATLAS pseudodata in PDF fit



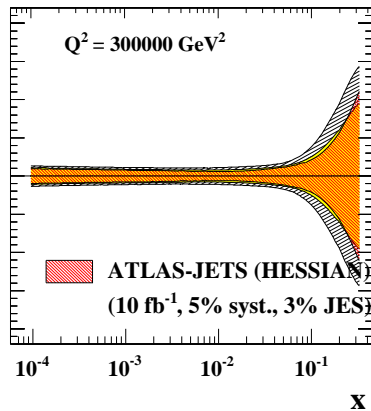
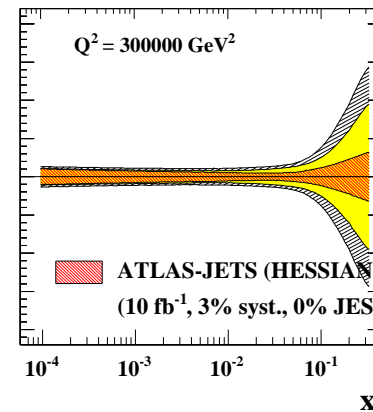
Use data at higher  $\eta > 1$  and lower  $pt < 3\text{TeV}$  to avoid new physics!



Impact of increasing statistics



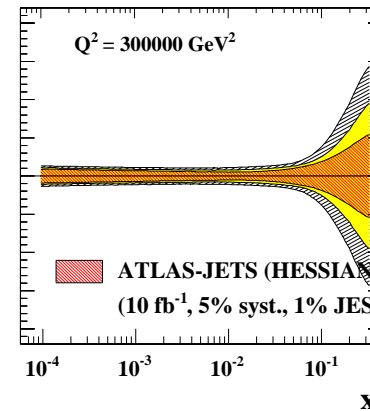
Impact of decreasing experimental systematic uncertainty



Impact of decreasing experimental correlated systematic uncertainty

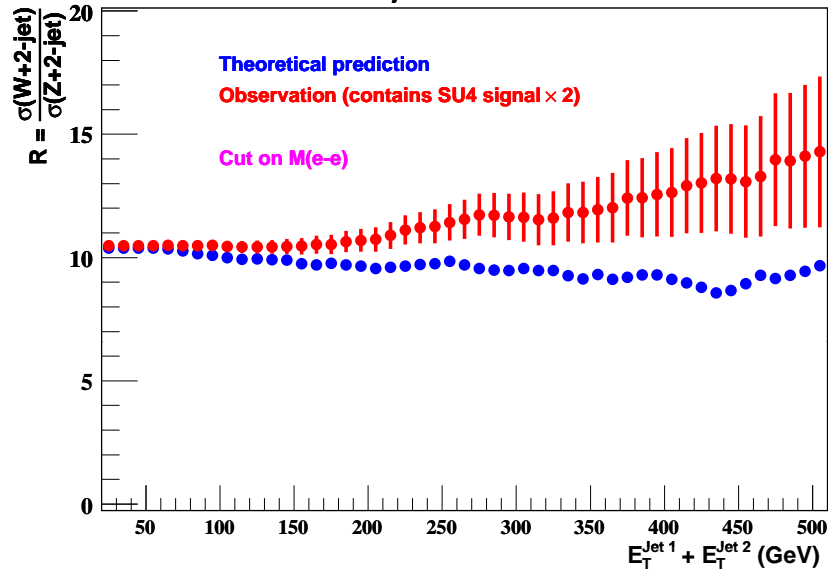
Challenging!

Can we decrease Jet Energy Scale systematic to 1%?

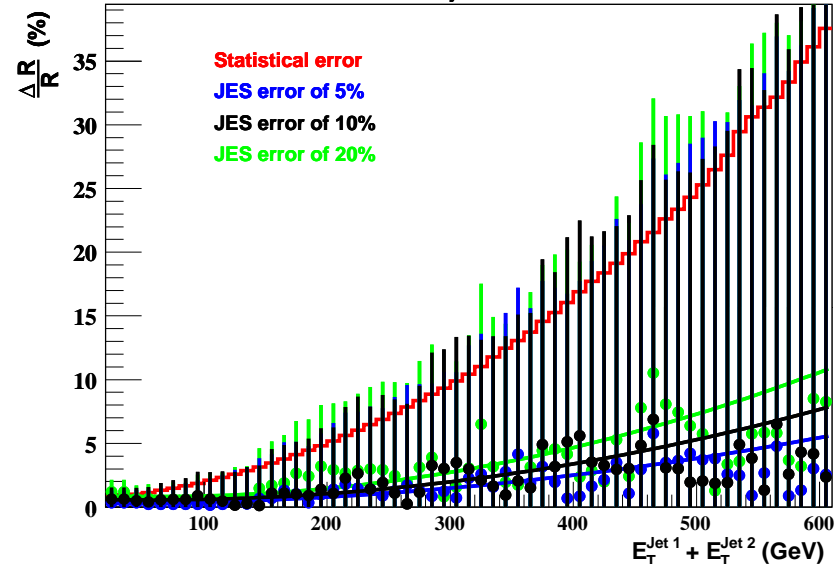


Jet energy scale also a problem in W/Z+jets channel, where SUSY signals may show up – Jet Energy Scale of 5% gives uncertainties 5-12% on the W + (1-6) jet cross-sections. This is larger than the PDF uncertainty (3-8%)

Comparison of measured  $R_{2\text{-jets}}$  with prediction (any lepton signal)



Relative uncertainty on  $R_{2\text{-jets}}$  due to uncertainty on JES



However BSM signals should be more obvious in the  $R=(W+n \text{ jet}) / (Z+n \text{ jet})$  ratio

Illustrated is **MSugra SU(4)** compared to **Standard Model** for  $200\text{pb}^{-1}$  of data in the W/Z +2 jets channel

The jet energy scale is less of a problem in the ratio

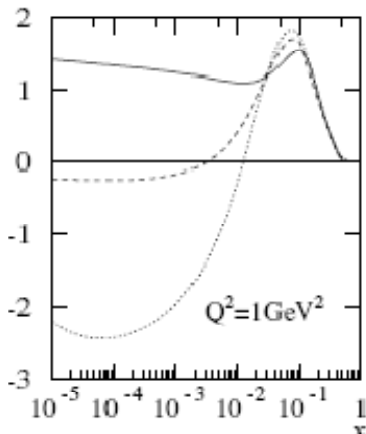
JES of 5% gives < 5% uncertainty on the ratio –very much less than the statistical error

# BEWARE of different sort of 'new physics'

What if low-x behaves very differently?

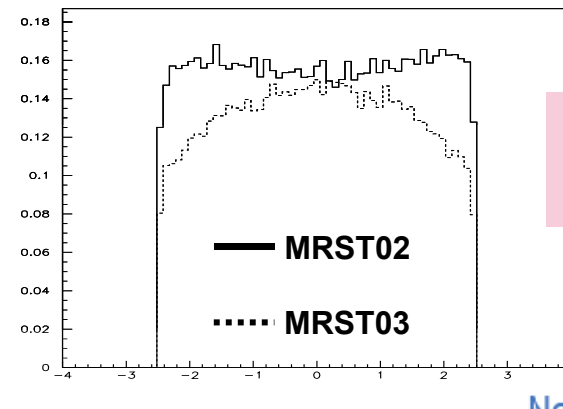
LHC is a low-x machine (at least for the early years of running) **Is NLO (or even NNLO) DGLAP good enough for  $x < 10^{-2}$ . The QCD formalism may need extending at small-x. What is SAFE x?**

•BFKL  $\ln(1/x)$  resummation would change the deduced shape of the gluon



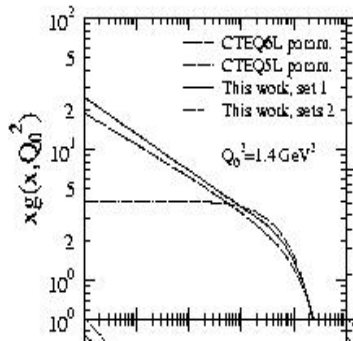
Thorne and White

MRST03 PDFs were a TOY PDF which distrusted all  $x < 10^{-3}$ . This would affect the central region for W production.



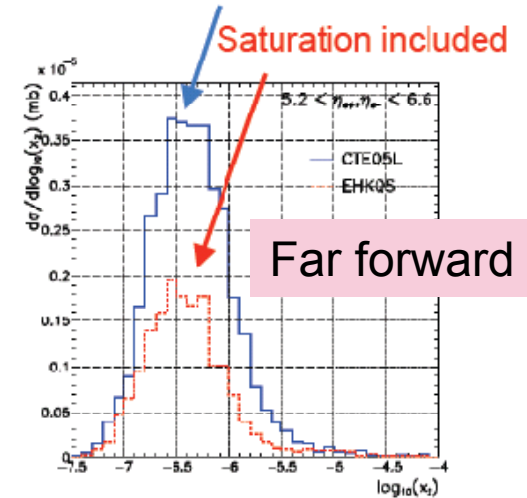
Central rapidity

High density non-linear effects may induce gluon saturation this also affects the deduced shape of the gluon



Eskola et al

Drell-Yan  
 $M(ee) = 4\text{GeV}$

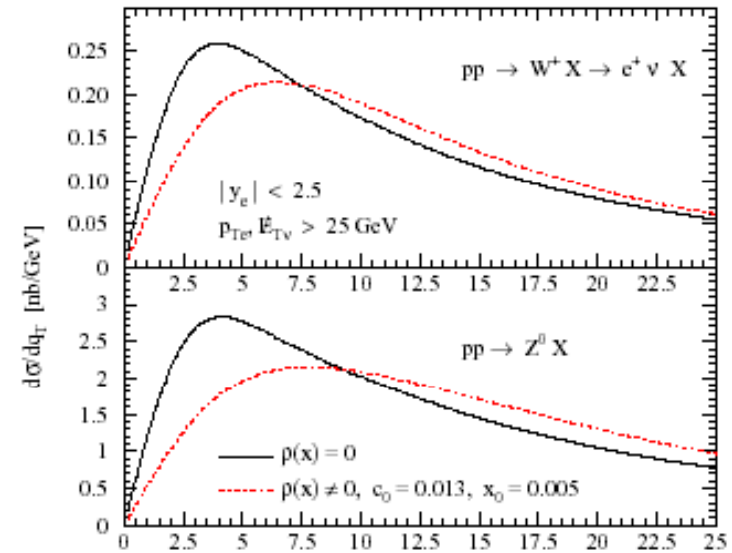


Far forward

But the TOY PDFs are unlikely to be realistic - a better way could be to look at pt spectra for W and Z production

Lack of pt ordering at low-x is a further consequence BFKL resummation AND most non-linear treatments. This would affect the pt spectra for W and Z production at the LHC (See hep-ph/0508215)

And if any of this is true the W/Z cross-sections are very different - cannot be used as a luminosity monitor until we thoroughly understand low-x physics



Conventional  
Unconventional

PDF set	$\sigma_{W^+} B_{W \rightarrow l\nu}$ (nb)	$\sigma_{W^-} B_{W \rightarrow l\nu}$ (nb)	$\sigma_Z B_{Z \rightarrow ll}$ (nb)
MSTW08	$8.55 \pm 0.15$	$6.25 \pm 0.12$	$1.38 \pm 0.025$
MRST03	6.88	5.23	1.18



# Summary

## STANDARD MODEL

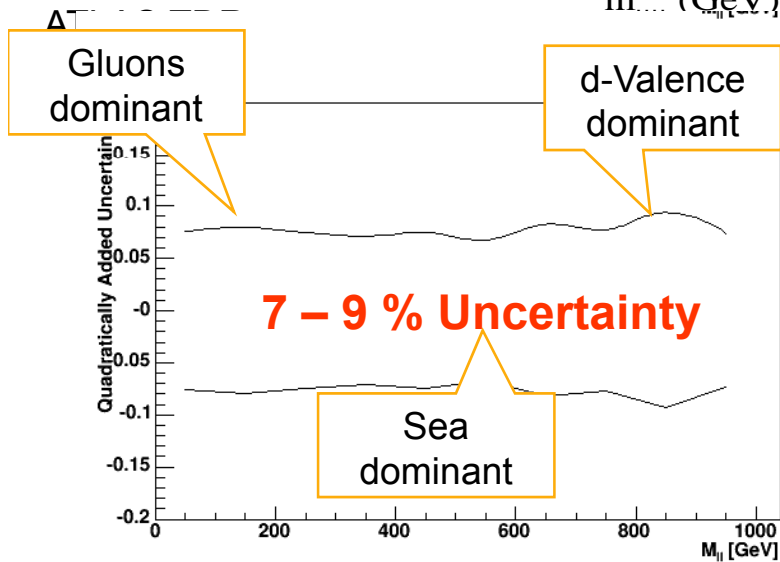
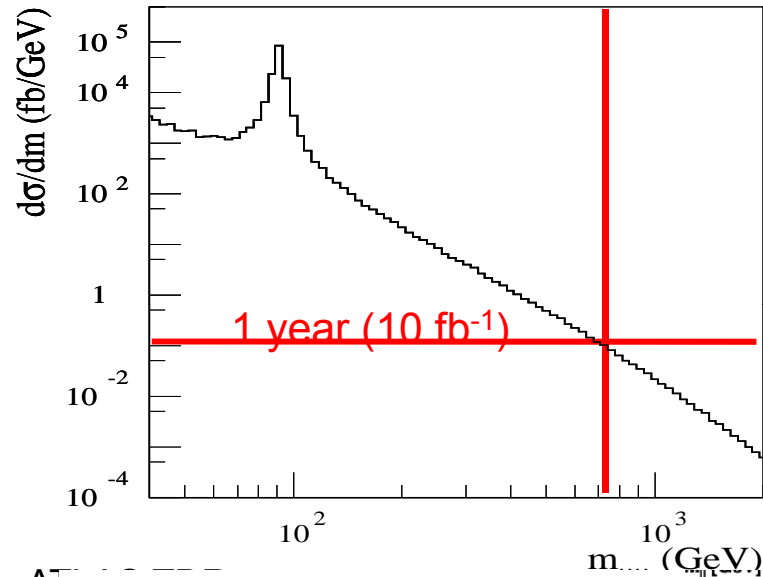
- There are W/Z standard candle measurements: Z/W ratio is the best
- W and Z cross-sections should first test our understanding- then contribute to our knowledge at greater precision
- W asymmetry should bring something new
- Beware that NEW low-x physics could compromise this.

## BEYOND STANDARD MODEL

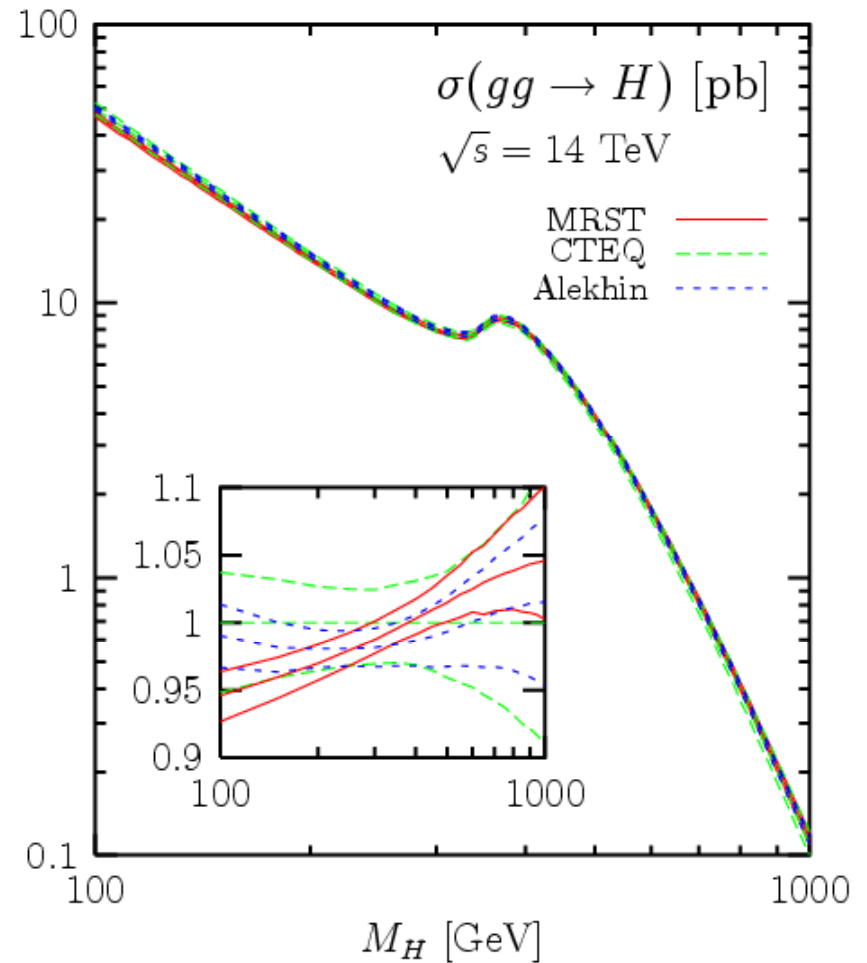
- There are discovery channels – high ET jets- which could be obscured by PDF uncertainties
- But Jet Energy Scale Uncertainties could be more of a problem
- Be smart - look at ratios  $W+n\text{-jets}/Z+n\text{-jets}$

extras

**But not all discovery physics is strongly compromised: e.g PDF Uncertainty in High-mass Drell-Yan won't stop us seeing Zprimes**

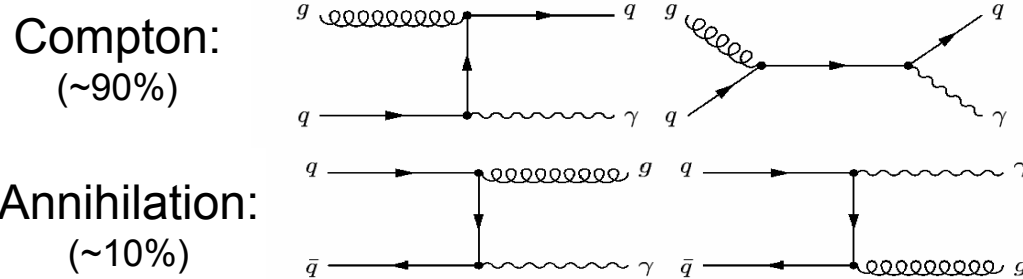


and PDF uncertainties don't affect the Higgs discovery potential too badly



# What other processes will be useful?

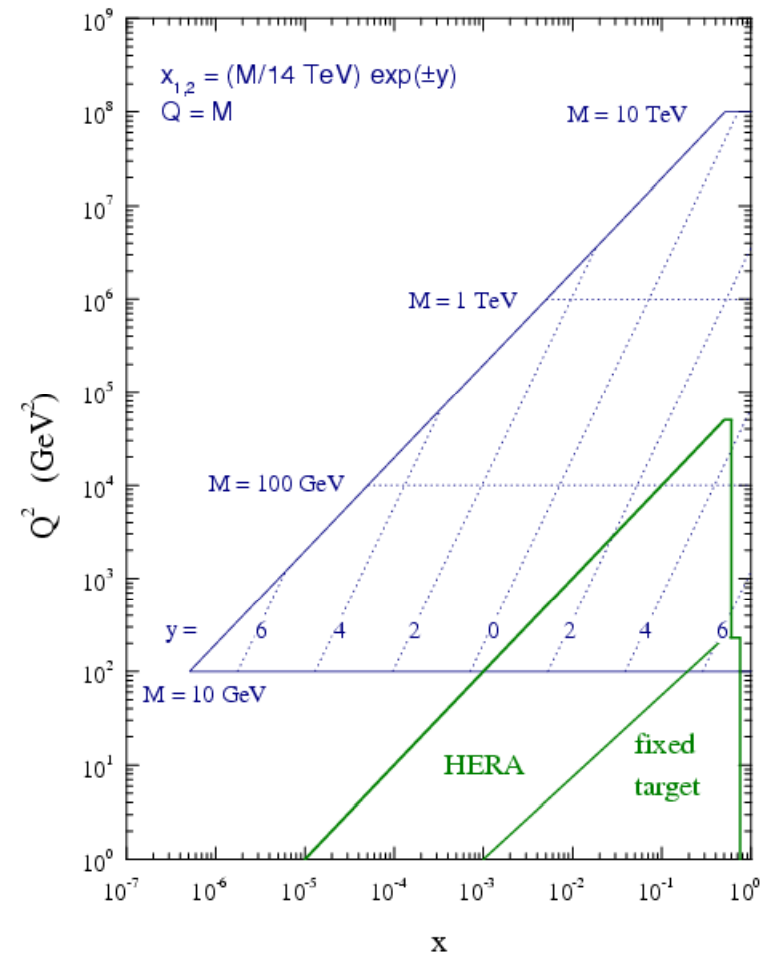
## Direct photon production for the high-x gluon



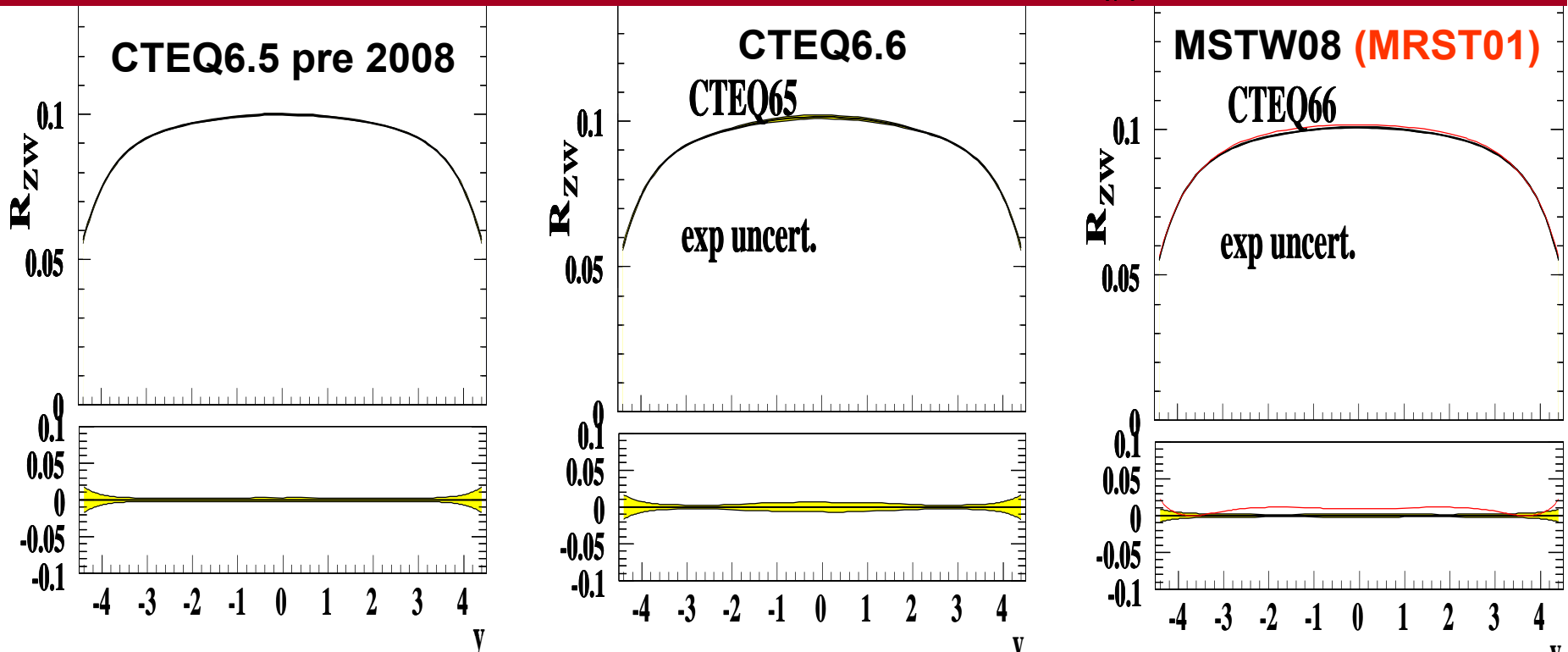
- **Z+ b-jet** for Measurement of the b-quark PDF

Low-mass Drell-Yan will probe low-x partons but also low-x calculations – **LHCb can look at this**

LHC parton kinematics



**Now let's look at ratios: Z/W ratio is a golden benchmark measurement – 14TeV**



**ZOOM in on Z/W ratio – there is fantastic agreement between PDF providers PDF uncertainty from the low-x gluon/ flavour symmetric sea cancels out- and so do luminosity errors BUT there is somewhat more PDF uncertainty than we thought before 2008 (~2% rather than 1% in the central region)**

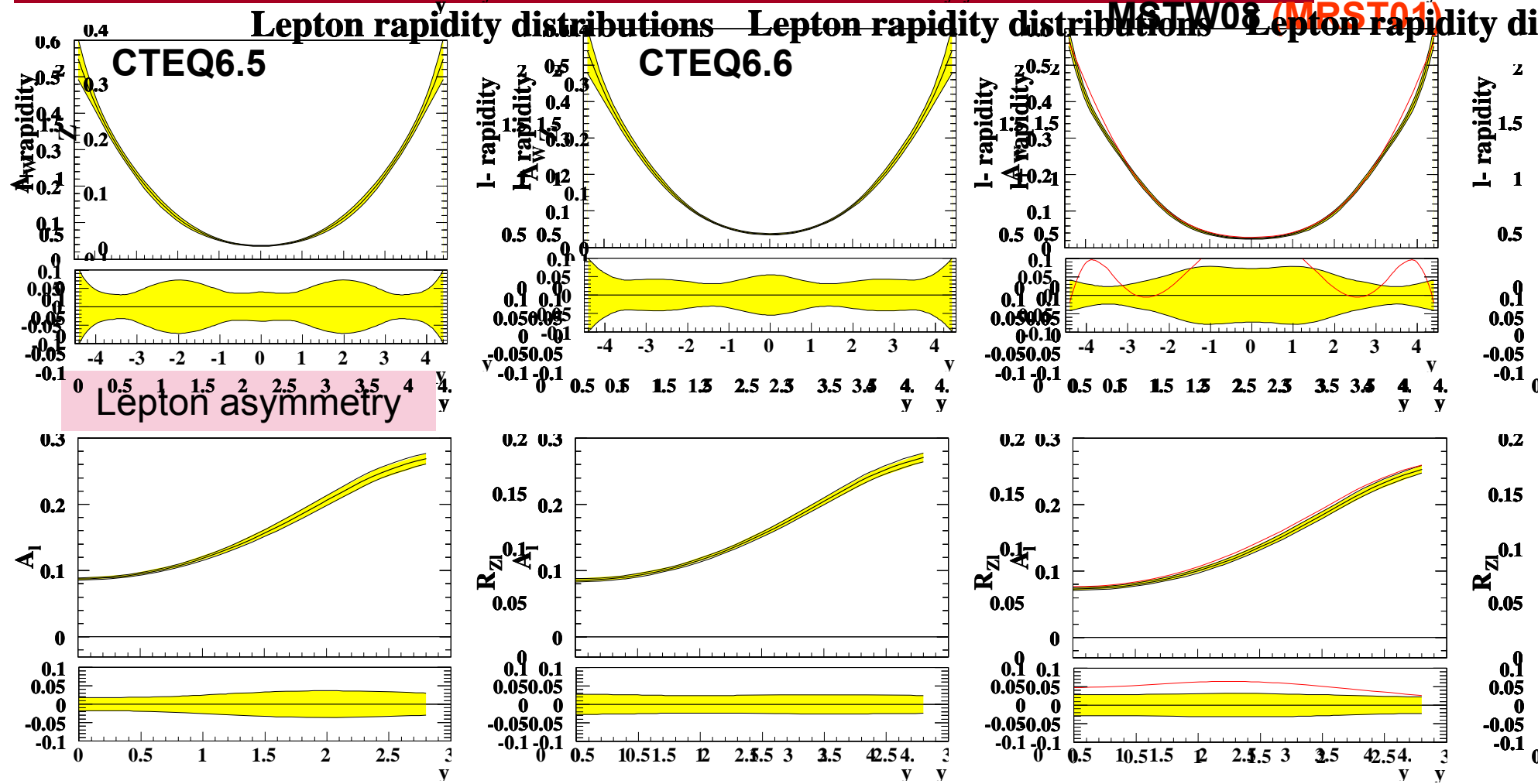
**There is uncertainty in the strangeness sector that does not cancel out between Z and ( $W^+ + W^-$ )... it was always there we just didn't account for it**

$$\frac{Z}{W^+ + W^-} \sim \frac{u\bar{u} + d\bar{d} + s\bar{s} + c\bar{c} + b\bar{b}}{(u\bar{d} + c\bar{s}) + (d\bar{u} + s\bar{c})}$$

YES this does translate to the Z/lepton ratio

But in the W asymmetry - there is NOT fantastic agreement 14TeV

MSTW08 (MRST01)



Further sources of PDF uncertainty from the valence sector are revealed. And note that when it comes to W asymmetry CTEQ do not have the most conservative errors at central rapidity - MRST/MSTW do

# But what about valence PDFs at high-x?

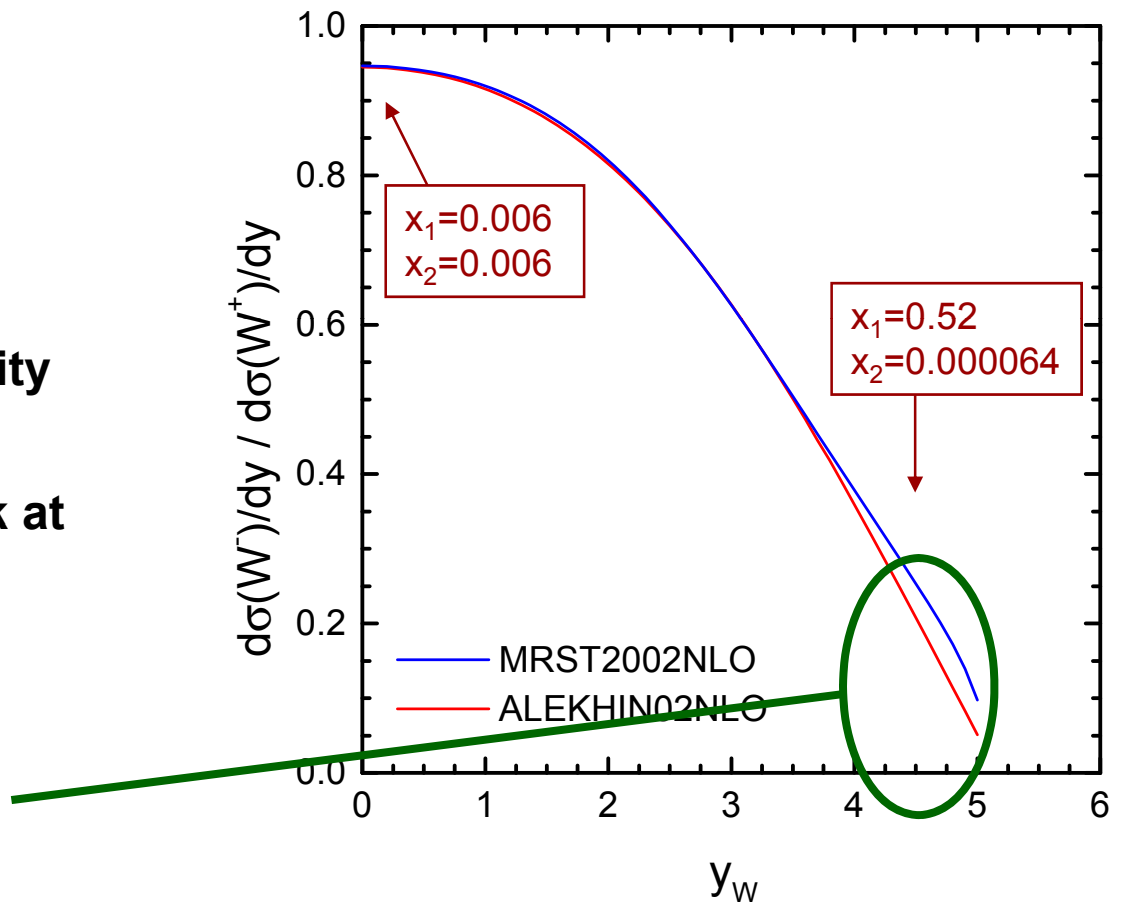
Look at  $W^-/W^+$  ratio at large rapidity

$$\frac{W^-}{W^+} = \frac{u \bar{d}}{d \bar{u}}$$

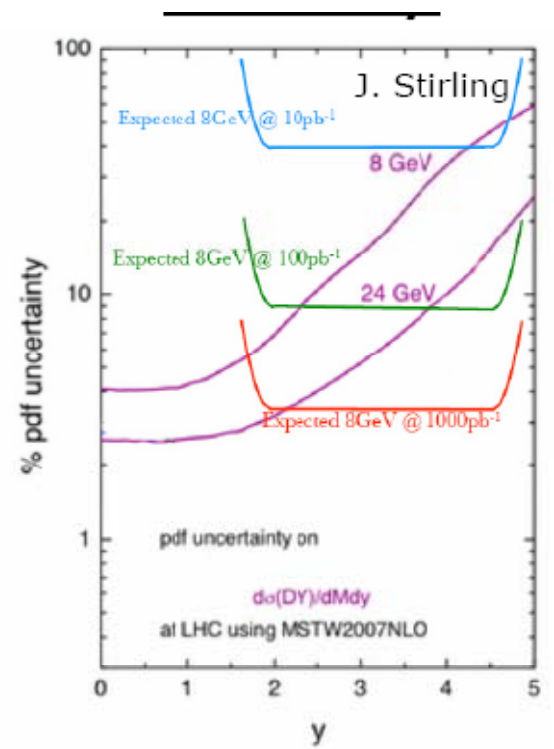
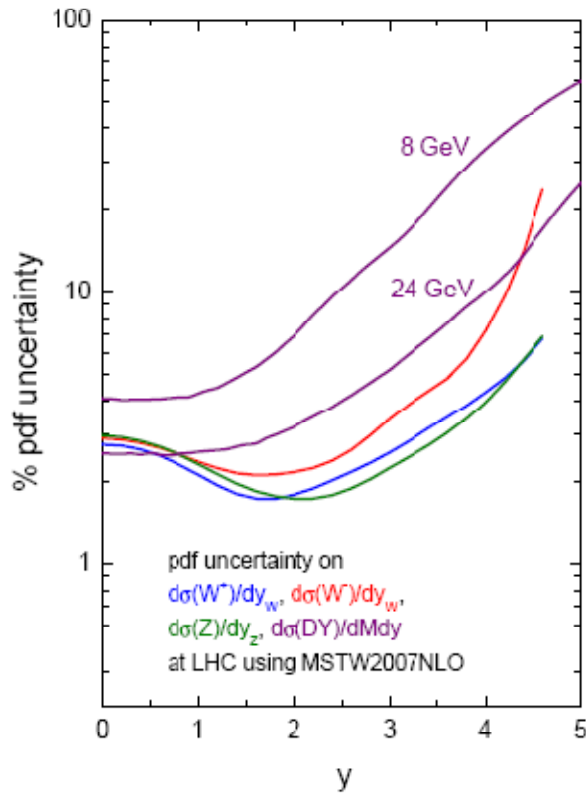
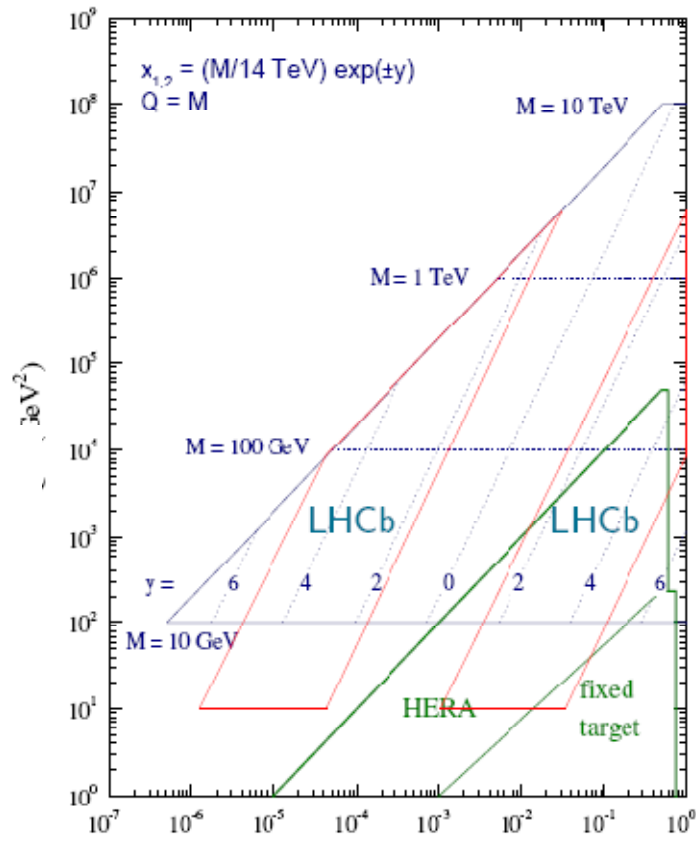
Not possible for main LHC detectors BUT LHCb rapidity range 1.9 to 4.9

There is a proposal to look at this in LHCb

sensitive to large-x  $d/u$



### LHC parton kinematics





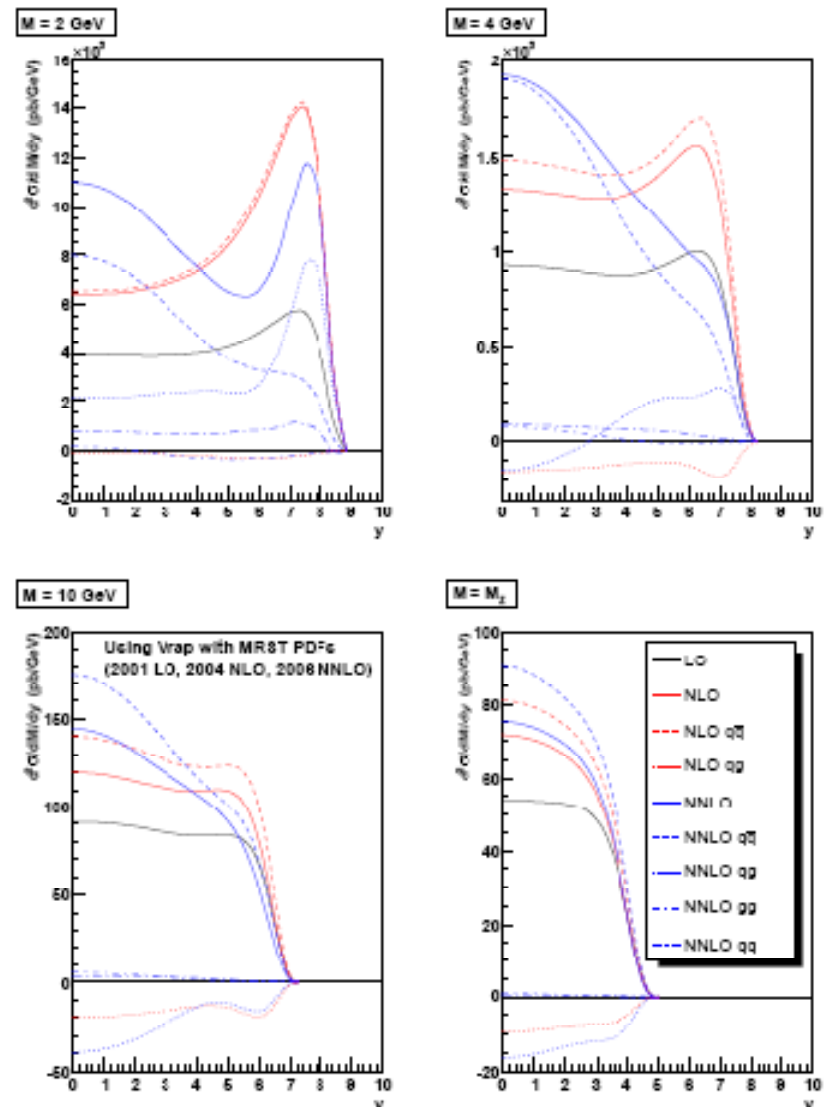
However, this assumes perturbative prediction of Drell-Yan production is reliable.

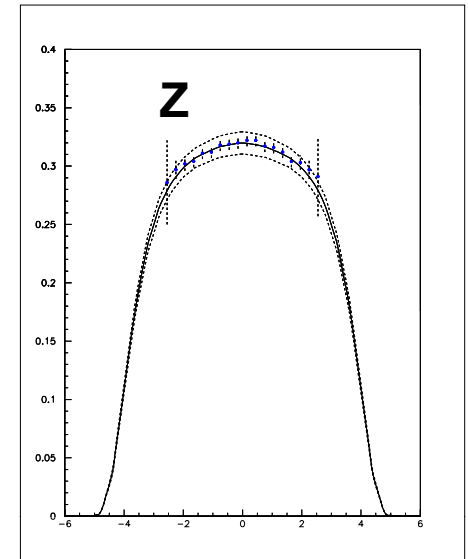
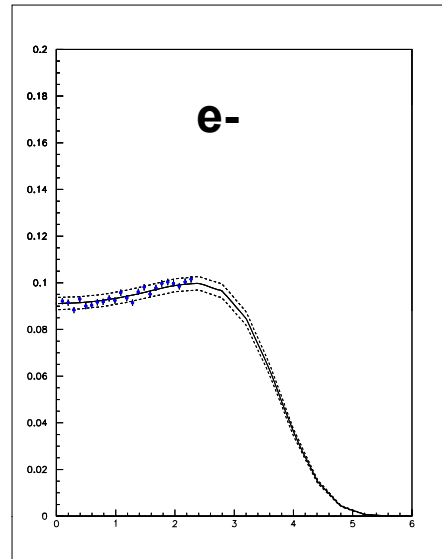
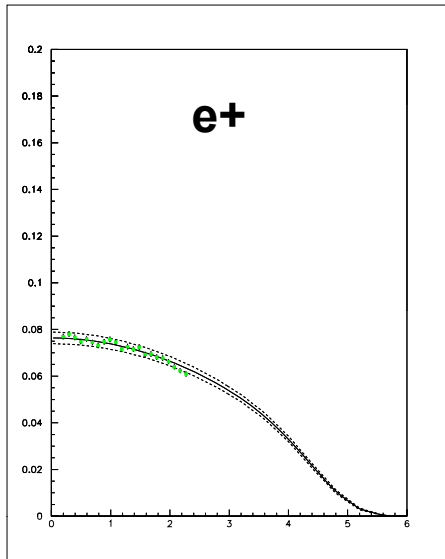
As seen very large change in prediction from order to order, particularly for low  $M$  and high  $y$ .

Problem with perturbative stability. Is this due to partons or cross-sections?

Cross-section may be sensitive to resummations (high and low  $z$ ) at lowest  $M$  and highest  $y$ . In region where measurements can be made?

### $\gamma^*/Z$ rapidity distributions at LHC





**In fact I have included  $e^+/e^-$  from  $W^+/W^-$  decay as well as the Z data in the fit**

**The Z is from CSC muons whereas the  $e^+/e^-$  are from the earlier ATLFast study (for now).**

**The plots show only statistical/uncorrelated errors:  $\sim 4\%$  for  $W^+/W^-$**

**$\sim 1\%$  for Z BUT there is**

**also a correlated systematic 4% for the Z data**

If you are looking at this in detail beware that the normalisation of the  $e^+/e^-$  plots have a bin width included

# W+jets: PDF vs JES Uncertainty

PDF vs Jet Scale Uncertainty ( $\Delta$  JS)  
with 10% (5%) jet energy miscal.

(Note: results with tight EF cuts samples)

2.9% <  $\Delta$  PDF < 7.3%  
5.8% <  $\Delta$  JS (10%) < 23.6%  
3.6% <  $\Delta$  JS (5%) < 11.9%



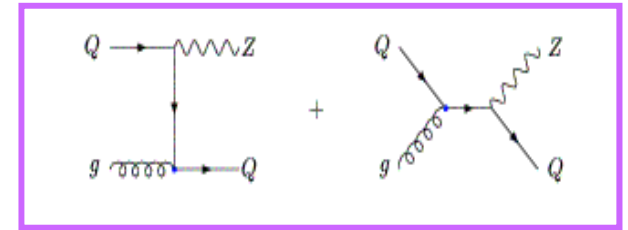
**PDF Uncert < Expt. Syst. Uncert**

Next: When is JES < PDF Unc?  
Try with 1,2,3% jet energy miscal.

Multipl	$\Delta+$ PDF (%)	$\Delta-$ PDF (%)	$\Delta+$ JS (%)	$\Delta-$ JS (%)
W+ $\geq$ 1 jets	3.2	2.9	10.7 (5.2)	10.7 (5.2)
W+ $\geq$ 2 jets	3.2	2.9	10.2 (5.1)	10.7 (5.2)
W+ $\geq$ 3 jets	3.3	2.9	5.8 (3.6)	9.0 (4.0)
W+ $\geq$ 4 jets	5.0	3.9	14.7 (7.8)	15.6 (7.0)
W+ $\geq$ 5 jets	5.9	4.8	20.8 (9.5)	20.5 (10.7)
W+ $\geq$ 6 jets	7.3	5.9	22.2 (10.4)	23.6 (11.9)

- **Also studying Z+ b-jet**

- Measurement of the b-quark PDF
  - Process sensitive to b content of the proton

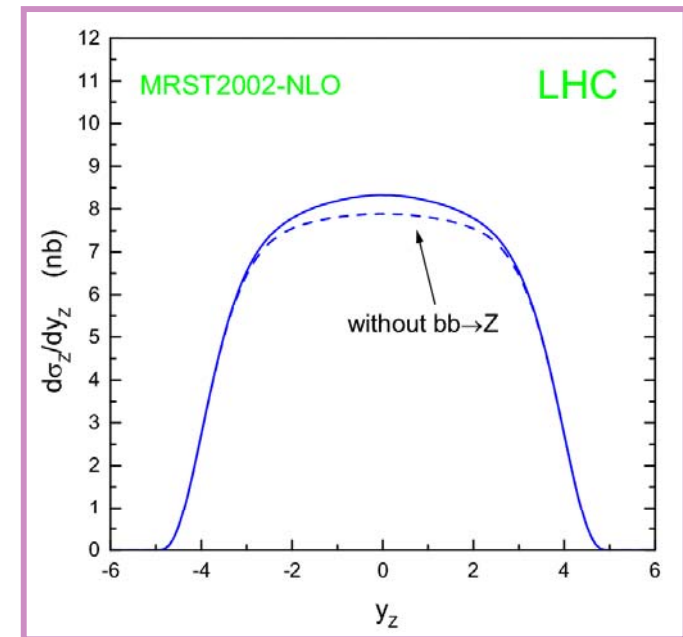


- Differences in total Z+b cross-section from current PDFs are of the order of 5%

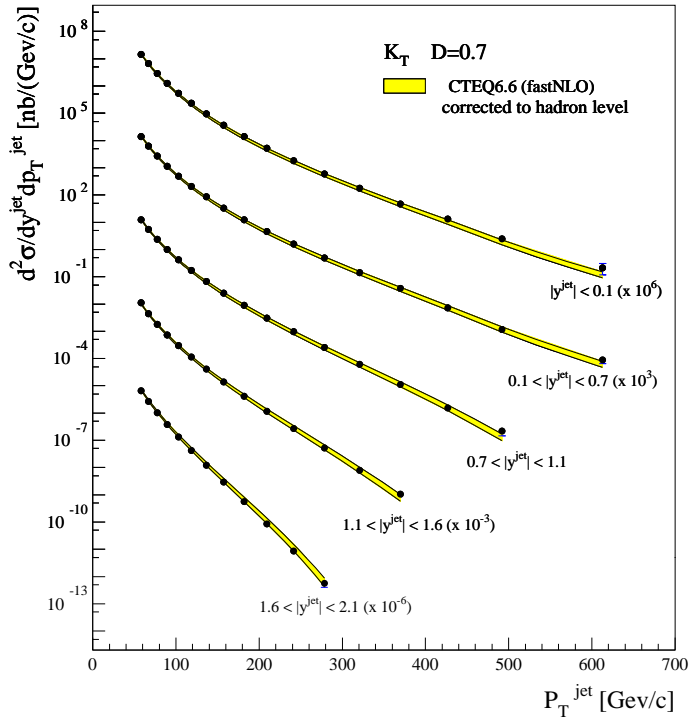
The measurement of Z+b should be more interesting at LHC than at Tevatron:  
 Signal cross-section larger (x80), and more luminosity  
 Relative background contribution smaller (x5)

$bb \rightarrow Z$  @ LHC is ~5% of entire Z production  $\rightarrow$  Knowing  $\sigma_Z$  to about 1% requires a b-pdf precision of the order of 20%

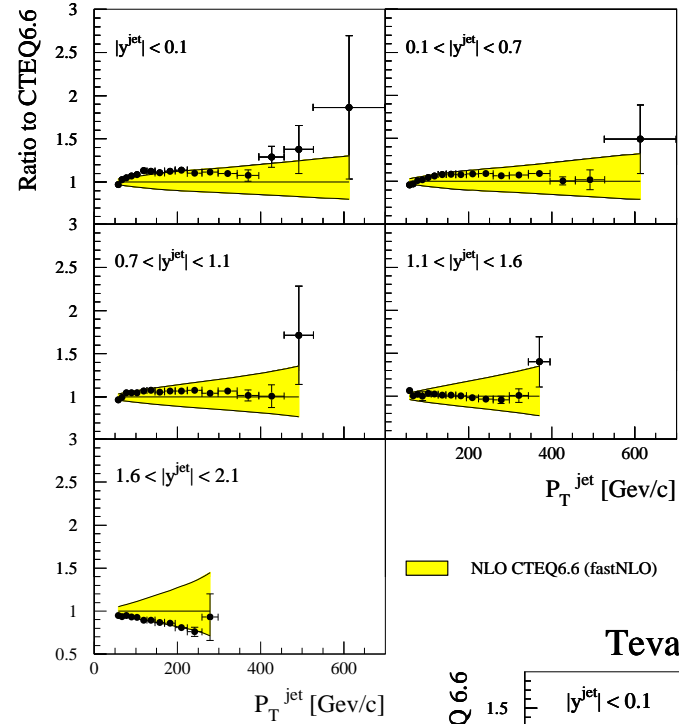
**Z+b** measurement in ATLAS will be possible with **high statistics** and **good purity** of the selected samples with two independent **b-tagging methods**:



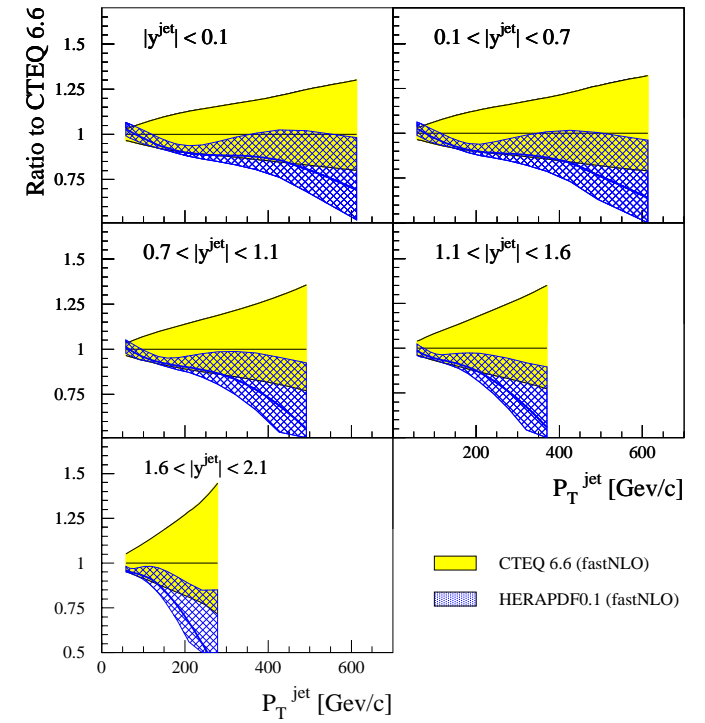
### Tevatron Jet Cross Sections



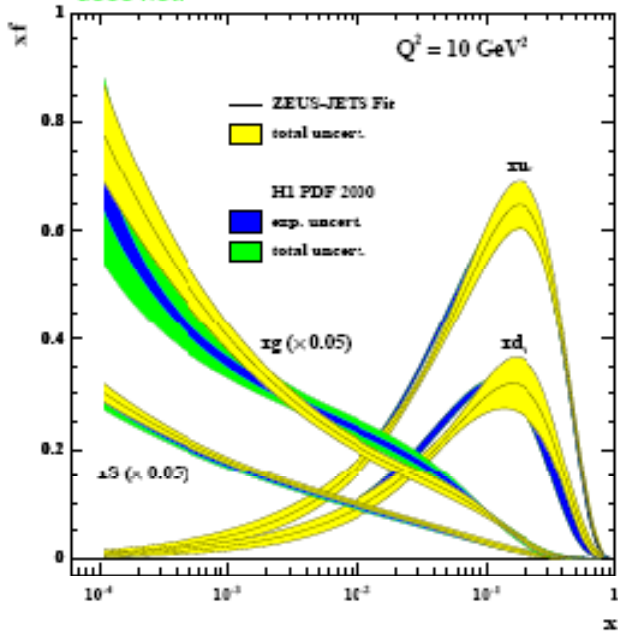
### Tevatron Jet Cross Sections



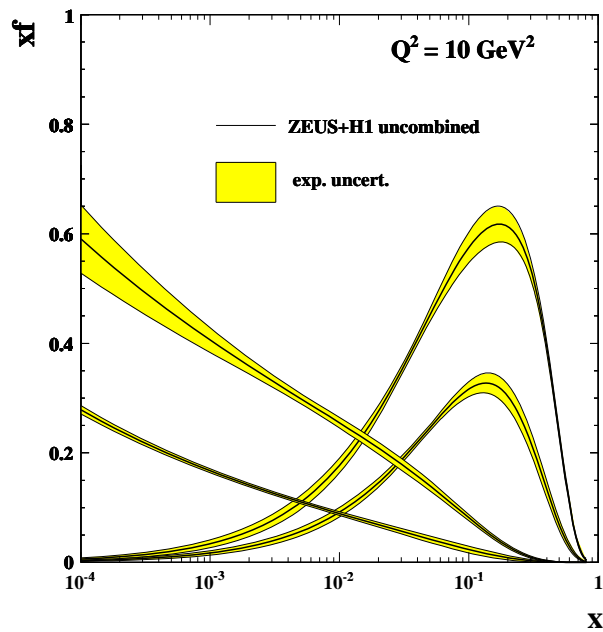
### Tevatron Jet Cross Sections



variation introduced in model error, ZEUS does not.

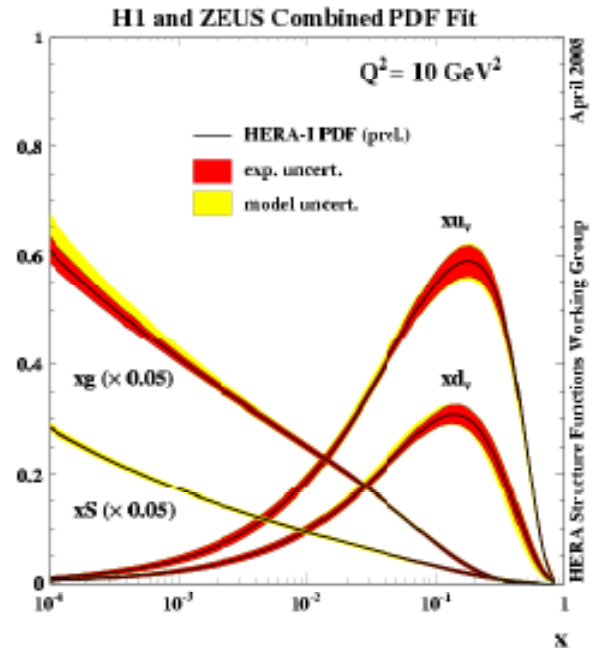


PDFs from separate QCD analyses of separate ZEUS and H1 data



PDFs from same QCD analysis of separate ZEUS and H1 data sets - before 'smart' combination

Experimental error only

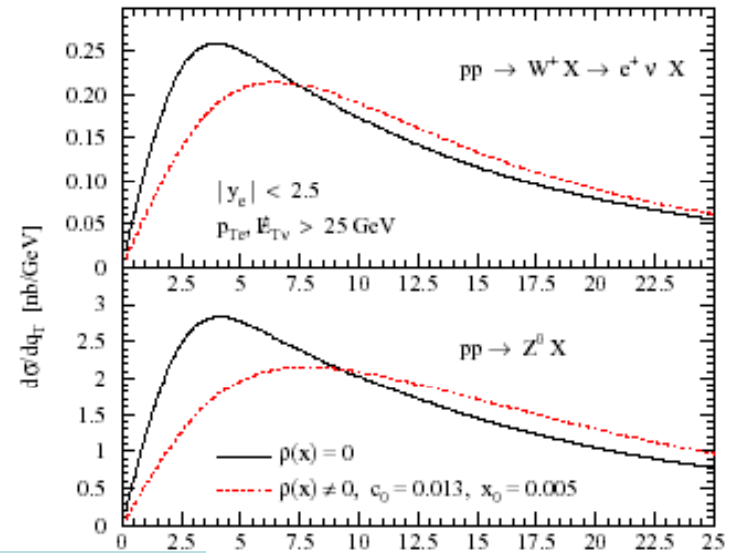


PDFs from same QCD analysis of combined HERA data - after 'smart' combination

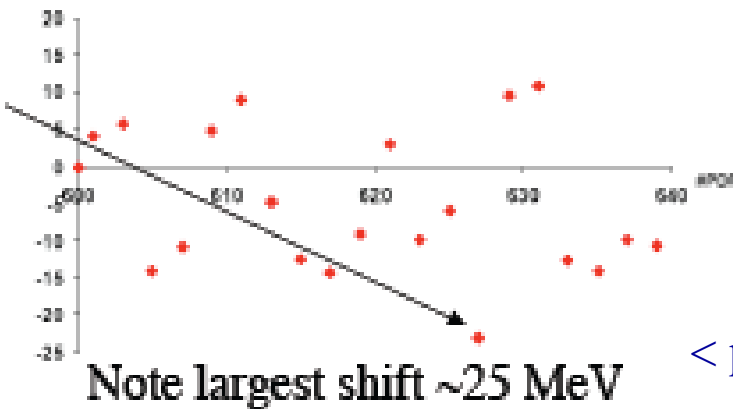
HERAPDF0.1 has small experimental errors and modest model errors

But the TOY PDFs are unlikely to be realistic - a better way could be to look at pt spectra for W and Z production

Lack of pt ordering at low-x is a further consequence BFKL resummation AND most non-linear treatments. This would affect the pt spectra for W and Z production at the LHC (See hep-ph/0508215)



Pt spectra are also used to measure  $M_W$  --  $\delta M_W$  from PDF uncertainties, using  $p_T(e)$ , is  $\sim 20$  MeV

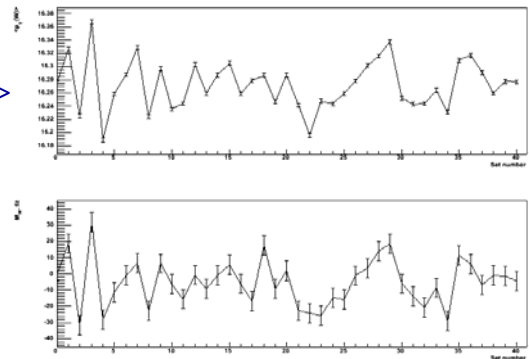


So we'd better be sure we've got the calculations for Pt spectra right

Conventional  
Unconventional

$\langle p_T(W) \rangle$

$\delta M_W(\text{fit})$



Same pattern