Scales for DM searches: V+jet pT-ratios

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Taming Unphysical Scales for Physical Predictions, Cambridge, 31.03.2016

V+jets backgrounds in monojet/MET/X + jets searches

12.9 fb⁻¹ (13 TeV)



irreducible backgrounds:

 $pp \rightarrow Z(\rightarrow v\overline{v}) + jets \implies MET + jets$

 $pp \rightarrow W(\rightarrow |v) + jets \implies MET + jets$ (lepton lost)



Determine V+jets backgrounds



- very precise at low pT
- but: limited statistics at large pT

• systematics from transfer factors

Goal of the ongoing study

 Combination of state-of-the-art predictions: (N)NLO QCD+(N)NLO EW in order to match (future) experimental sensitivities (1-10% accuracy in the few hundred GeV-TeV range)

$$\frac{\mathrm{d}}{\mathrm{d}x}\frac{\mathrm{d}}{\mathrm{d}\vec{y}}\sigma^{(V)}(\vec{\varepsilon}_{\mathrm{MC}},\vec{\varepsilon}_{\mathrm{TH}}) \coloneqq \frac{\mathrm{d}}{\mathrm{d}x}\frac{\mathrm{d}}{\mathrm{d}\vec{y}}\sigma^{(V)}_{\mathrm{MC}}(\vec{\varepsilon}_{\mathrm{MC}}) \begin{bmatrix} \frac{\mathrm{d}}{\mathrm{d}x}\sigma^{(V)}_{\mathrm{TH}}(\vec{\varepsilon}_{\mathrm{TH}}) \\ \frac{\mathrm{d}}{\mathrm{d}x}\sigma^{(V)}_{\mathrm{MC}}(\vec{\varepsilon}_{\mathrm{MC}}) \end{bmatrix}$$
one-dimensional reweighting of MC samples in $x = p_{\mathrm{T}}^{(V)}$

with
$$\frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{TH}}^{(V)} = \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{QCD}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{mix}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\Delta\sigma_{\mathrm{EW}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\gamma-\mathrm{ind.}}^{(V)}$$

- Robust **uncertainty estimates** including
 - Pure QCD uncertainties
 - Pure EW uncertainties
 - Mixed QCD-EW uncertainties

- Prescription for **correlation** of these uncertainties
 - ▶ within a process (between low-pT and high-pT)
 - ► across processes

QCD effects: scale issues

QCD effects: scale issues

 $\frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{QCD}}^{(V)} = \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{LO\,QCD}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{NLO\,QCD}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{NNLO\,QCD}}^{(V)}$



$$\mu_0 = \frac{1}{2} \left(\sqrt{p_{\mathrm{T},\ell^+\ell^-}^2 + m_{\ell^+\ell^-}^2} + \sum_{i \in \{q,g,\gamma\}} |p_{\mathrm{T},i}| \right)$$

this is a 'good' scale for V+jets

- at large pTV: HT'/2 \approx pTV
- modest higher-order corrections
- sufficient convergence

scale uncertainties due to 7-pt variations

 $\mu_{\rm R,F} = \xi_{\rm R,F} \mu_0$

 $(\xi_{\rm R},\xi_{\rm F}) = (2,2), (2,1), (1,2), (1,1), (1,0.5), (0.5,1), (0.5,0.5)$

yields

O(20%) uncertainties at LO O(10%) uncertainties at NLO O(5%) uncertainties at NNLO



consider Z+jet / W+jet p_{T,V}-ratio @ LO

uncorrelated treatment yields O(40%) uncertainties



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uncorrelated treatment yields O(40%) uncertainties

correlated treatment yields tiny O(< 1%) uncertainties

check against NLO QCD!



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NLO QCD corrections remarkably flat
in Z+jet / W+jet ratio!
→ supports correlated treatment of uncertainties!



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NLO QCD corrections remarkably flat in Z+jet / W+jet ratio!

→ supports correlated treatment of uncertainties!

Also holds for higher jet-multiplicities → indication of correlation also in higher-order corrections beyond NLO!

QCD uncertainties



$$\frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{N}^{k}\mathrm{LO}\,\mathrm{QCD}}^{(V)}(\vec{\varepsilon}_{\mathrm{QCD}}) = \begin{bmatrix} K_{\mathrm{N}^{k}\mathrm{LO}}^{(V)}(x) + \sum_{i=1}^{3}\varepsilon_{\mathrm{QCD},i}\,\delta^{(i)}K_{\mathrm{N}^{k}\mathrm{LO}}^{(V)}(x) \end{bmatrix} \\ \times \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{LO}\,\mathrm{QCD}}^{(V)}(\vec{\mu}_{0}).$$

$$\epsilon_{\mathrm{QCD},i}^{(Z)} = \epsilon_{\mathrm{QCD},i}^{(W^{\pm})} = \epsilon_{\mathrm{QCD},i}^{(\gamma)} = \epsilon_{\mathrm{QCD},i}$$
nuisance parameters:
interpreted as $|\mathbf{\sigma}$ Gaussian
• correlated across pT bins

•
$$\delta^{(1)} K_{N^k LO}^{(V)}(x) = \frac{1}{2} \left[K_{N^k LO}^{(V, \max)}(x) - K_{N^k LO}^{(V, \min)}(x) \right]$$

•
$$\delta^{(2)} K_{N^k LO}^{(V)}(x) = \omega_{shape}(x) \, \delta^{(1)} K_{N^k LO}^{(V)}(x)$$

with $\omega_{shape}(x) = \frac{p_T^2 - p_{T,0}^2}{p_T^2 + p_{T,0}^2}$

•
$$\delta^{(3)} K_{N^k LO}^{(V)}(x) = \Delta K_{N^k LO}^{(V)}(x) - \Delta K_{N^k LO}^{(Z)}(x)$$

 $\Delta K_{N^k LO}^{(V)}(x) = K_{N^k LO}^{(V)}(x) / K_{N^{k-1} LO}^{(V)}(x) - 1$

this modelling of process correlations assumes a close similarity of QCD effects between different V+jets processes

QCD uncertainties in pT-ratios



this modelling of process correlations assumes a close similarity of QCD effects between all V+jets processes

- apart from PDF effects it is the case for W+jets vs. Z+jets
- at large pT is is also the case for \mathbf{y} +jets vs. Z+jets. In particular with dynamical cone $R_{dyn}(E_{T,\gamma},\varepsilon_0) = \frac{M_Z}{E_{T,\gamma}\sqrt{\varepsilon_0}}$





EW corrections become sizeable at large $p_{\text{T,V}}$

Origin: virtual EW Sudakov logarithms

Note: real EW Sudakov logarithms included as separate VV(+jets) backgrounds

How to estimate corresponding pure EW uncertainties of relative $\mathcal{O}(\alpha^2)$?



Large EW corrections dominated by Sudakov logs Uncertainty estimate of NLO EW from naive exponentiation x 2: $\delta^{(1)}\kappa^{(V)}_{\rm EW}(x) = \delta\kappa^{(V)}_{\rm NLO EW}(x) = \frac{2}{2} \left[\kappa^{(V)}_{\rm NLO EW}(x)\right]^2$



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Large EW corrections dominated by Sudakov logs \downarrow Uncertainty estimate of NLO EW from naive exponentiation × 2: $\delta^{(1)}\kappa^{(V)}_{\rm EW}(x) = \delta\kappa^{(V)}_{\rm NLO EW}(x) = \frac{2}{2} \left[\kappa^{(V)}_{\rm NLO EW}(x)\right]^2$

check against two-loop Sudakov logs [Kühn, Kulesza, Pozzorini, Schulze; 05-07]

QCD and EW corrections for V+jets as backgrounds in DM searches



Large EW corrections dominated by Sudakov logs Uncertainty estimate of NLO EW from naive exponentiation x 2: $\delta^{(1)}\kappa_{\rm EW}^{(V)}(x) = \delta\kappa_{\rm NLO EW}^{(V)}(x) = \frac{2}{2} \left[\kappa_{\rm NLO EW}^{(V)}(x)\right]^2$

check against two-loop Sudakov logs [Kühn, Kulesza, Pozzorini, Schulze; 05-07]

Uncertainty estimate of NNLO EW:

$$\delta^{(1)}\kappa^{(V)}_{\rm EW}(x) = \frac{2}{3}\kappa^{(V)}_{\rm NLO\,EW}(x)\,\kappa^{(V)}_{\rm NNLO\,Sud}(x)$$

QCD and EW corrections for V+jets as backgrounds in DM searches





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mixed QCD-EW effects

Mixed QCD-EW uncertainties

Other issues

Photon-induced production

QED corrections to quark PDFs

- small percent-level QED effects on qg/qq luminosities (included via LUXqed)
- 1.5-5% PDF uncertainties

Conclusions & Outlook

- monojet / MET+jets searches soon limited by V+jets background systematics
- MC reweighting allows to promote V + jet to NNLO QCD+(N)NLO EW:
 - inclusion of EW corrections *crucial* due to large Sudakov logs
- ▶ Perturbative systematics in pTV under control at the level of 1-10% up to the TeV
- Outlook: investigate/interpret post-fit nominal predictions and ratios

Illuminating standard candles at the LHC - V+jets

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This informal, brainstorming work Particle Physics Phenomenology a measurements of vector boson + to enhance our understanding of constrain higher order QCD and e Starts 25 Apr 2017 10:00 Ends 26 Apr 2017 14:00	kshop held in conjunction with the IPPP (Institute for at Durham) will focus on the Standard Model jets processes that we can perform in Run 2 of the LHC the high transverse momentum phase space and electroweak corrections.
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https://indico.cern.ch/event/624982

Putting everything together

$$\frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{TH}}^{(V)}(\vec{\mu}) = K_{\mathrm{TH}}^{(V)}(x,\vec{\mu}) \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{LO}\,\mathrm{QCD}}^{(V)}(\vec{\mu}_0) + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\gamma-\mathrm{ind.}}^{(V)}(x,\vec{\mu})$$

$$\begin{split} &K_{\mathrm{TH}}^{(V)}(x,\vec{\varepsilon}_{\mathrm{QCD}},\vec{\varepsilon}_{\mathrm{EW}},\varepsilon_{\mathrm{mix}}) = K_{\mathrm{TH},\otimes}^{(V)}(x,\vec{\varepsilon}_{\mathrm{QCD}},\vec{\varepsilon}_{\mathrm{EW}}) + \varepsilon_{\mathrm{mix}}\,\delta K_{\mathrm{mix}}^{(V)}(x), \\ &= \left[K_{\mathrm{N}^{k}\mathrm{LO}}^{(V)}(x) + \sum_{i=1}^{3} \varepsilon_{\mathrm{QCD},i}\,\delta^{(i)}K_{\mathrm{N}^{k}\mathrm{LO}}^{(V)}(x)\right] \\ &\times \left[1 + \kappa_{\mathrm{EW}}^{(V)}(x) + \sum_{i=1}^{3} \varepsilon_{\mathrm{EW},i}^{(V)}\,\delta^{(i)}\kappa_{\mathrm{EW}}^{(V)}(x)\right] + \varepsilon_{\mathrm{mix}}\,\delta K_{\mathrm{mix}}^{(V)}(x), \end{split}$$

$$\frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{QCD}}^{(V)} = \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{LOQCD}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{NLOQCD}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{NNLOQCD}}^{(V)}$$
$$\frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{EW}}^{(V)} = \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{NLOEW}}^{(V)} + \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{Sudakov\,NNLOEW}}^{(V)}$$

with nuisance parameters $\vec{\varepsilon}_{TH} = (\vec{\varepsilon}_{QCD}, \hat{\varepsilon}, \vec{\varepsilon}_{EW}, \varepsilon_{\gamma})$

Correlation of scale variations: prescription

$$\frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{N}^{k}\mathrm{LO}\,\mathrm{QCD}}^{(V)}(\vec{\varepsilon}_{\mathrm{QCD}}) = \begin{bmatrix} K_{\mathrm{N}^{k}\mathrm{LO}}^{(V)}(x) + \sum_{i=1}^{3}\varepsilon_{\mathrm{QCD},i}\,\delta^{(i)}K_{\mathrm{N}^{k}\mathrm{LO}}^{(V)}(x) \end{bmatrix} \text{ nuisance parameters} \\ \times \frac{\mathrm{d}}{\mathrm{d}x}\sigma_{\mathrm{LO}\,\mathrm{QCD}}^{(V)}(\vec{\mu}_{0}).$$

$$K_{N^{k}LO}^{(V)}(x) = \frac{1}{2} \left[K_{N^{k}LO}^{(V,\max)}(x) + K_{N^{k}LO}^{(V,\min)}(x) \right]$$

$$\delta^{(1)} K_{N^{k}LO}^{(V)}(x) = \frac{1}{2} \left[K_{N^{k}LO}^{(V,\max)}(x) - K_{N^{k}LO}^{(V,\min)}(x) \right]$$

$$\epsilon_{\text{QCD},1}^{(Z)} = \epsilon_{\text{QCD},1}^{(W^{\pm})} = \epsilon_{\text{QCD},1}^{(\gamma)} = \epsilon_{\text{QCD},1}$$

- fully correlated across processes
- correlated across pT bins
- include additional uncertainty based on differences in QCD corrections of the last calculated order:

$$\Delta K_{N^{k}LO}^{(V)}(x) = K_{N^{k}LO}^{(V)}(x) / K_{N^{k-1}LO}^{(V)}(x) - 1$$

$$^{3)}K_{N^{k}LO}^{(V)}(x) = \Delta K_{N^{k}LO}^{(V)}(x) - \Delta K_{N^{k}LO}^{(Z)}(x)$$

$$\epsilon_{QCD,3}^{(Z)} = \epsilon_{QCD,3}^{(W^{\pm})} = \epsilon_{QCD,3}^{(\gamma)} = \epsilon_{QCD,3}^{$$

- this modelling of process correlations assumes a close similarity of QCD effects between all V+jets processes
 - certainly the case for $Z(\rightarrow \nu \overline{\nu})$ +jets vs. $Z(\rightarrow I\overline{I})$ +jets
 - apart from PDF effects it is the case for W+jets vs. Z+jets
 - at large pT is is also the case for γ +jets vs. Z+jets

 $\delta^{(}$

γ +jet: Isolation

$$\implies M_{\gamma j}^2 \simeq E_{\mathrm{T},\gamma} E_{\mathrm{T},j} R_{\gamma j}^2 = \varepsilon_0 E_{\mathrm{T},\gamma}^2 R_{\mathrm{dyn}}^2 = M_Z^2$$

. Using this dynamic smooth isolation mimics the role of the Z- and W -boson masses as regulators of collinear singularities in Z/W +jet production at high pT.

NNLO for Z+jet

[Gehrmann-De Ridder, Gehrmann, Glover, A. Huss, Morgan; '16]

NNLO for W/Z+jet

- unprecedented reduction of scale uncertainties at NNLO: $O(\sim 5\%)$
- we can now check the correlation of the uncertainties going from NLO to NNLO

NNLO for Z/γ +jet

[Campbell, Ellis, Williams; '17]

NNLO/NLO ~ 1 for large pT!

$Z/\gamma + I$ jet: pT-ratio

Overall

mild dependence on the boson pT

QCD corrections

- ▶ 10-15% below 250 GeV
- ► 5% above 350 GeV

EW corrections

- sizeable difference in EW corrections results in 10-15% corrections at several hundred GeV
- ~5% difference between NLO QCD+EW and NLO QCDxEW

Compare against data: Z/γ

Frixione-Isolation with $\begin{aligned} \epsilon &= 0.025\\ \delta_0 &= 0.4 \end{aligned}$

[JHEP10(2015)128]

[Ciulli, Kallweit, JML, Pozzorini, Schönherr for LH'I5]

• remarkable agreement with data at @ NLO QCD+EW!

Combination of NLO QCD and EW & Setup

Two alternatives:

$$\sigma_{\rm QCD+EW}^{\rm NLO} = \sigma^{\rm LO} + \delta \sigma_{\rm QCD}^{\rm NLO} + \delta \sigma_{\rm EW}^{\rm NLO}$$
$$\sigma_{\rm QCD\times EW}^{\rm NLO} = \sigma_{\rm QCD}^{\rm NLO} \left(1 + \frac{\delta \sigma_{\rm EW}^{\rm NLO}}{\sigma^{\rm LO}}\right) = \sigma_{\rm EW}^{\rm NLO} \left(1 + \frac{\delta \sigma_{\rm QCD}^{\rm NLO}}{\sigma^{\rm LO}}\right)$$

Difference between the two approaches indicates uncertainties due to missing two-loop EW-QCD corrections of $\mathcal{O}(\alpha\alpha_s)$

Relative corrections w.rt. NLO QCD:

$$\frac{\sigma_{\rm QCD+EW}^{\rm NLO}}{\sigma_{\rm QCD}^{\rm NLO}} = \left(1 + \frac{\delta \sigma_{\rm EW}^{\rm NLO}}{\sigma_{\rm QCD}^{\rm NLO}}\right) \qquad \text{suppressed by large NLO QCD corrections}$$
$$\frac{\sigma_{\rm QCD\times EW}^{\rm NLO}}{\sigma_{\rm QCD}^{\rm NLO}} = \left(1 + \frac{\delta \sigma_{\rm EW}^{\rm NLO}}{\sigma_{\rm LO}^{\rm NLO}}\right) \qquad \text{``usual'' NLO EW w.r.t. LO}$$

•
$$\alpha = \frac{\sqrt{2}}{\pi} G_{\mu} M_{W}^{2} \left(1 - \frac{M_{W}^{2}}{M_{Z}^{2}} \right)$$
 in G_{μ} -scheme with $G_{\mu} = 1.16637 \times 10^{-5} \text{ GeV}^{-2}$

Virtual EW Sudakov logarithms

Originate from soft/collinear virtual EW bosons coupling to on-shell legs

Universality and factorisation similar as in QCD [Denner, Pozzorini; '01]

$$\delta_{\mathrm{LL+NLL}}^{1-\mathrm{loop}} = \frac{\alpha}{4\pi} \sum_{k=1}^{n} \left\{ \frac{1}{2} \sum_{l \neq k} \sum_{a=\gamma, Z, W^{\pm}} I^{a}(k) I^{\bar{a}}(l) \ln^{2} \frac{s_{kl}}{M^{2}} + \gamma^{\mathrm{ew}}(k) \ln \frac{s}{M^{2}} \right\}$$

- process-independent, simple structure
- 2-loop extension and resummation partially available
- typical size at $\sqrt{\hat{s}} = 1, 5, 10 \text{ TeV}$:

$$\begin{split} \delta_{\rm LL} &\sim -\frac{\alpha}{\pi s_W^2} \log^2 \frac{\hat{s}}{M_W^2} \simeq -28, -76, -104\%, \\ \delta_{\rm NLL} &\sim +\frac{3\alpha}{\pi s_W^4} \log \frac{\hat{s}}{M_W^2} \simeq +16, +28, +32\% \end{split} \Rightarrow \text{large cancellations possible} \end{split}$$

LUXqed

