

CMS Measurements of Single Top Quark Production Cross Section

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Outline

- Motivation to Study the Single Top Quark
- Experimental Setup
- Selected CMS measurements of single top quark
 - S-channel cross section at 8 TeV
 - T-channel cross section (inclusive) at 13 TeV
 - TW-channel cross section at 8 TeV
 - Differential cross section for t-channel at 13 TeV

Top Quark Pair Production

- Top quark was discovered by CDF and D0 experiments in 1995.

Phys.Rev.Lett. 74 (1995) 2626–2631

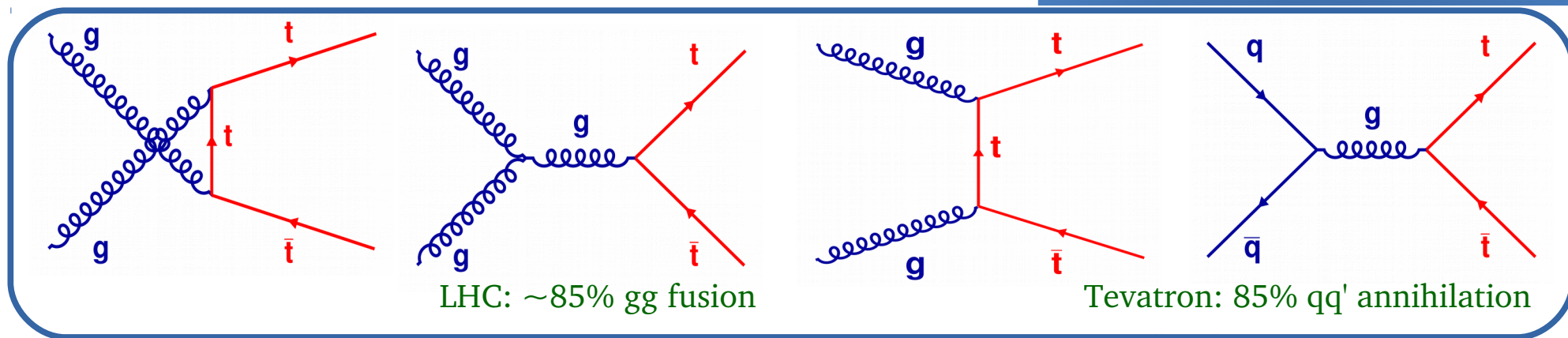
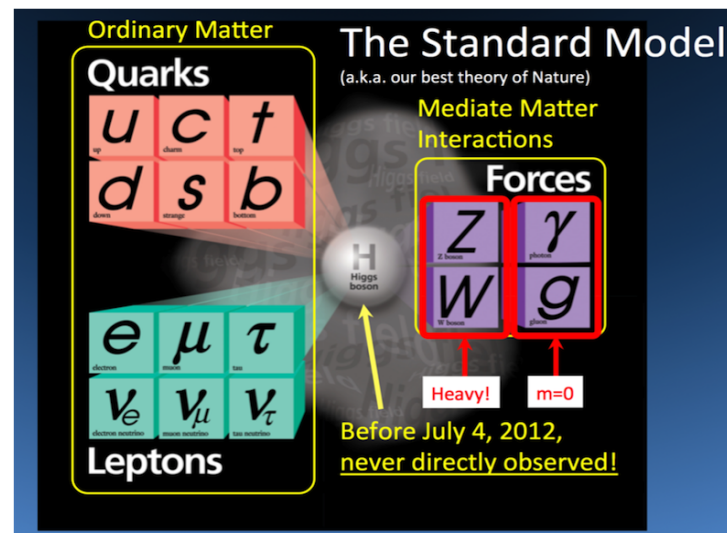
Phys.Rev.Lett. 74 (1995) 2632–2637

- Top mass measurement : 173.34 ± 0.76 GeV.

- Top decay width is large $\Gamma_t \propto m_t^3$:

$$\Gamma_t = 1.3 \text{ GeV} > \Lambda_{\text{QCD}} = 200 \text{ MeV} \rightarrow$$

Decay before hadronization \rightarrow bare quark

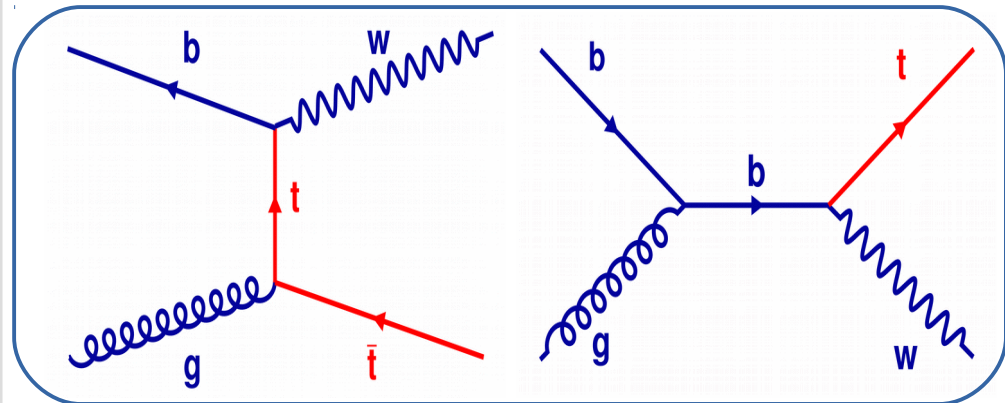
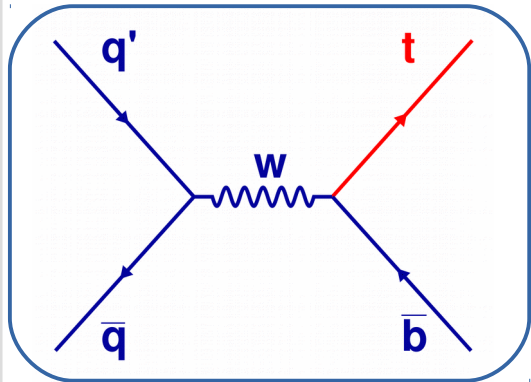
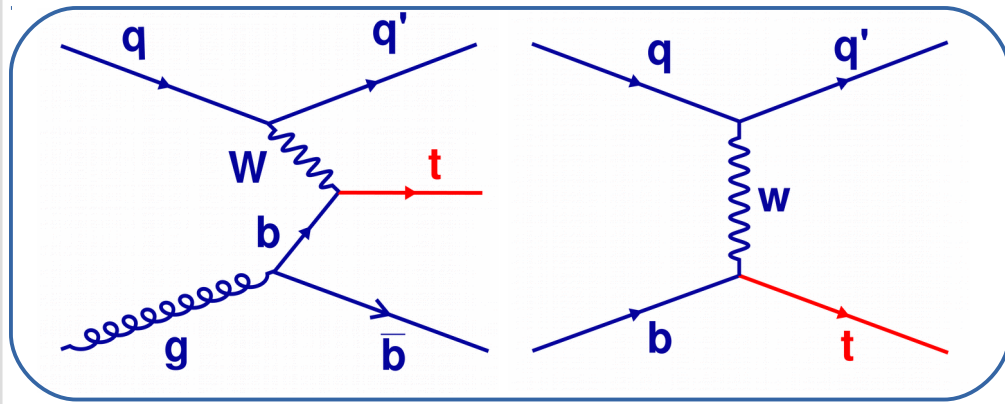


$$\sigma_{t\bar{t}} = 245.8 \pm 9.7 \text{ pb} \quad \text{LHC} \quad 8 \text{ TeV}$$

$$\sigma_{t\bar{t}} = 7.164 \pm 0.21 \text{ pb} \quad \text{Tevatron} \quad 1.96 \text{ TeV}$$



Single Top Quark Production



	collider	total[pb]
<i>t</i> -channel	LHC 7 TeV	$65.9^{+2.1}_{-0.7} \begin{smallmatrix} +1.5 \\ -1.7 \end{smallmatrix}$
	LHC 8 TeV	$87.2^{+2.8}_{-1.0} \begin{smallmatrix} +2.0 \\ -2.2 \end{smallmatrix}$
	LHC 13 TeV	$216.99^{+6.62}_{-4.64} \pm 6.16$
	Tevatron 1.96 TeV	$2.08^{+0.00}_{-0.03} \pm 0.08$
<i>s</i> -channel	LHC 7 TeV	$4.56 \pm 0.07^{+0.18}_{-0.17}$
	LHC 8 TeV	$5.55 \pm 0.08 \pm 0.21$
	LHC 13 TeV	$10.32^{+0.29}_{-0.24} \pm 0.27$
	Tevatron 1.96 TeV	$1.046^{+0.001}_{-0.007} \begin{smallmatrix} +0.042 \\ -0.039 \end{smallmatrix}$
<i>tW</i> -channel	LHC 7 TeV	$15.6 \pm 0.03^{+0.7}_{-0.8}$
	LHC 8 TeV	$22.2 \pm 0.4 \pm 1.0$
	LHC 13 TeV	$60.20^{+3.03}_{-3.62} \pm 4.59$
	Tevatron 1.96 TeV	$0.14 \pm 0.02^{+0.01}_{-0.02} \pm 0.02$

What are s channel, t channel?

In two particles scattering, where p_1 and p_2 are the **four-momenta** of the incoming particles and p_3 and p_4 are the four-momenta of the outgoing particles:

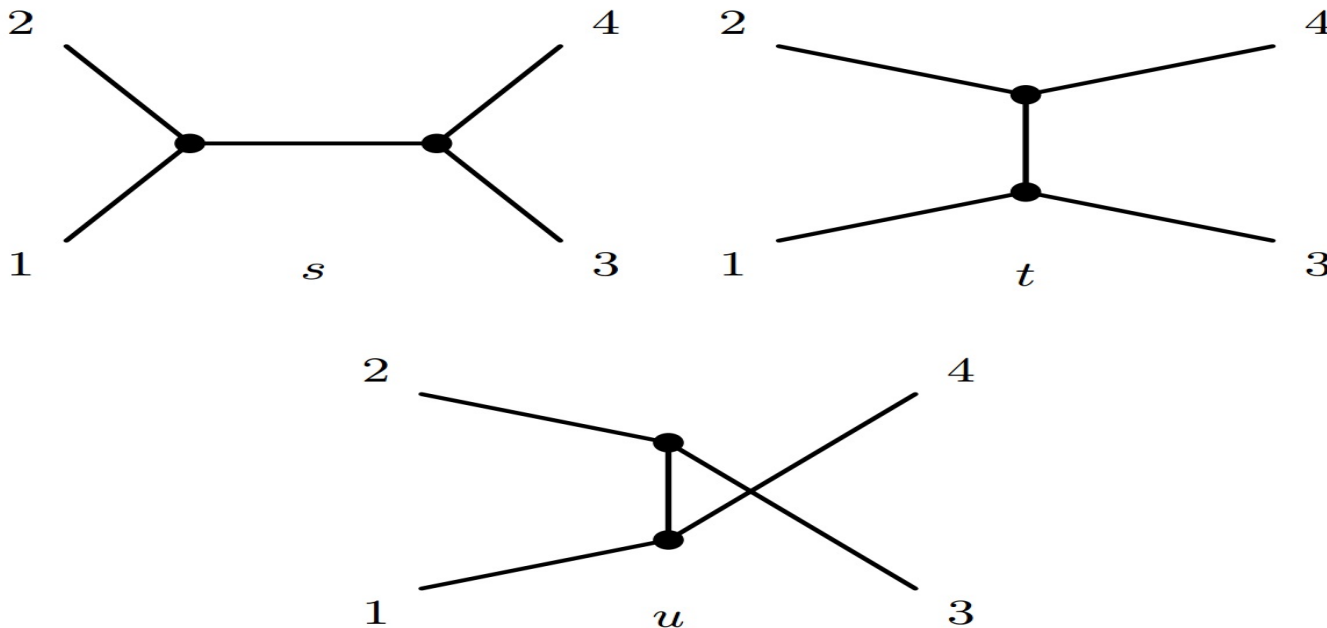
Mandelstam Variables

$$s=(p_1+p_2)^2=(p_3+p_4)^2$$

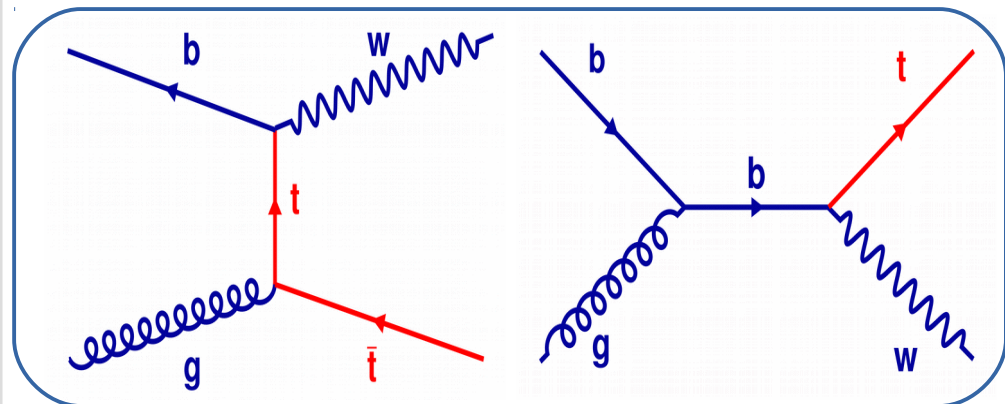
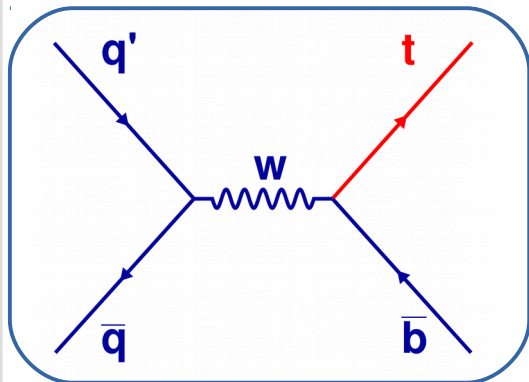
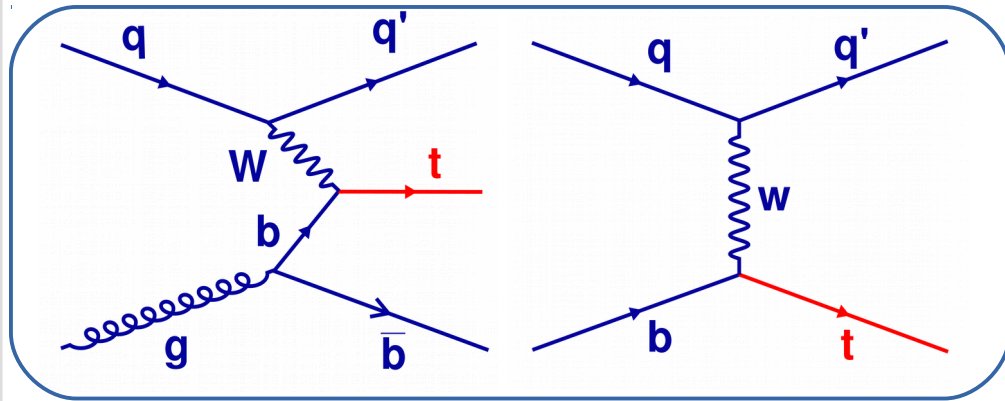
$$t=(p_1-p_3)^2=(p_2-p_4)^2$$

$$u=(p_1-p_4)^2=(p_2-p_3)^2$$

Four-momentum square of the mediator is the reference for the names of different feynman diagrams

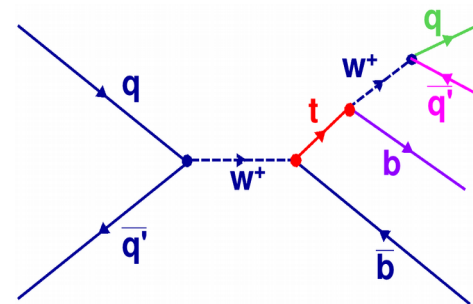


Single Top Quark Production

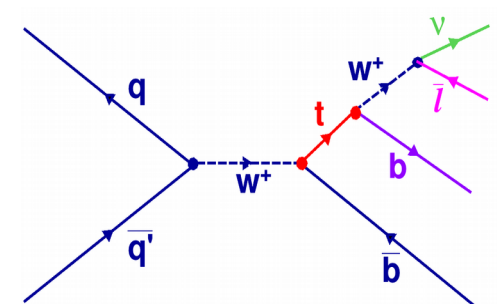


Top Quark Decay

- Top quark decays almost exclusively into a **b quark** and a **W boson**.
- **W boson** decays into **quarks** (in $\sim 67\%$ of cases) or into **leptons** (in $\sim 33\%$ of cases).



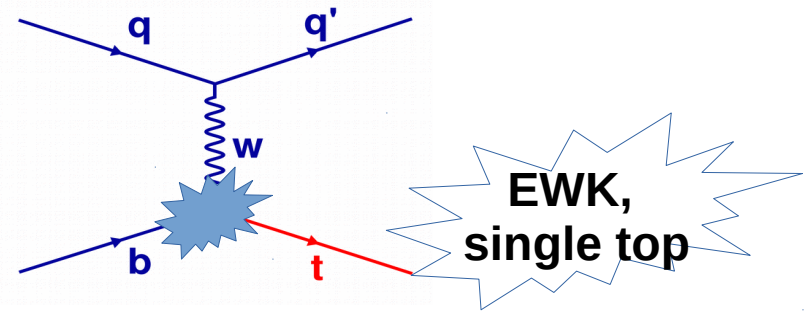
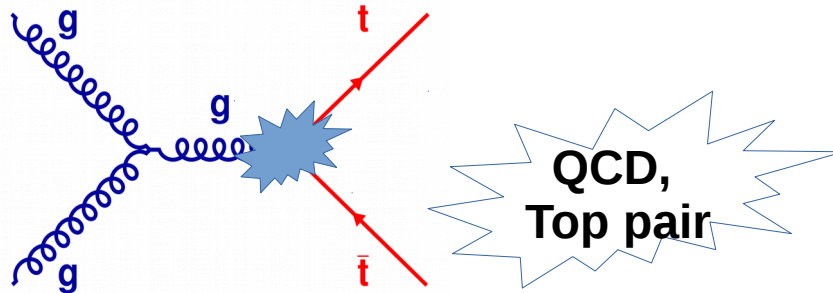
Hadronic decay



Leptonic decay

Why Single Top ?

Motivation



- Validates the electroweak in the SM
- Direct measurement of the CKM matrix element $|V_{tb}|$, W_{tb} vertex introduces
$$\frac{-ig}{2\sqrt{2}}V_{tb}\gamma^\mu(1 - \gamma^5)$$
- Measuring the top quark properties, measurement of the top spin polarization in the single top sample
- Cross check of the CPT symmetry, by measuring the difference in the top and anti-top production rate
- Probe the PDFs

Why Single Top ?

Motivation

- Any deviation from SM prediction in the top properties is a hint for models beyond the SM
- Test anomalous Wtb couplings in the production rates of top and antitop quarks
- Search for FCNC interactions
- Sensitive to new physics that includes new mediators like charged higgs.

Compact Muon Solenoid(CMS)

CMS Detector

Pixels
 Tracker
 ECAL
 HCAL
 Solenoid
 Steel Yoke
 Muons

SILICON TRACKER
 Pixels (100 x 150 μm^2)
 ~1m² ~66M channels
 Microstrips (80-180 μm)
 ~200m² ~9.6M channels

CRYSTAL ELECTROMAGNETIC CALORIMETER (ECAL)
 ~76k scintillating PbWO₄ crystals

PRESHOWER
 Silicon strips
 ~16m² ~137k channels

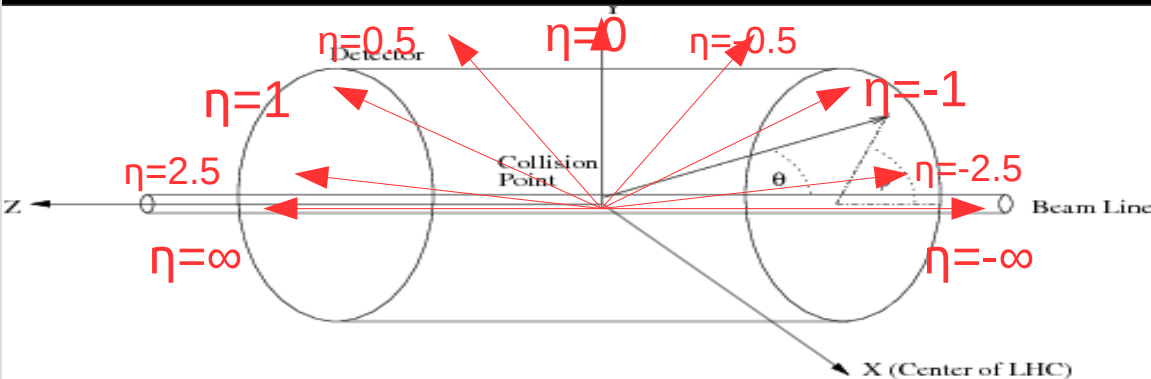
STEEL RETURN YOKE
 ~13000 tonnes

SUPERCONDUCTING SOLENOID
 Niobium-titanium coil
 carrying ~18000 A

HADRON CALORIMETER (HCAL)
 Brass + plastic scintillator
 ~7k channels

MUON CHAMBERS
 Barrel: 250 Drift Tube & 480 Resistive Plate Chambers
 Endcaps: 473 Cathode Strip & 432 Resistive Plate Chambers

Total weight : 14000 tonnes
 Overall diameter : 15.0 m
 Overall length : 28.7 m
 Magnetic field : 3.8 T



CMS Coordination

$$\eta = -\ln(\tan \theta/2), \quad \theta: \text{polar angle}$$

Compact Muon Solenoid(CMS)

CMS Detector

Pixels
 Tracker
 ECAL
 HCAL
 Solenoid
 Steel Yoke
 Muons

SILICON TRACKER
 Pixels (100 x 150 μm^2)
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CRYSTAL ELECTROMAGNETIC CALORIMETER (ECAL)
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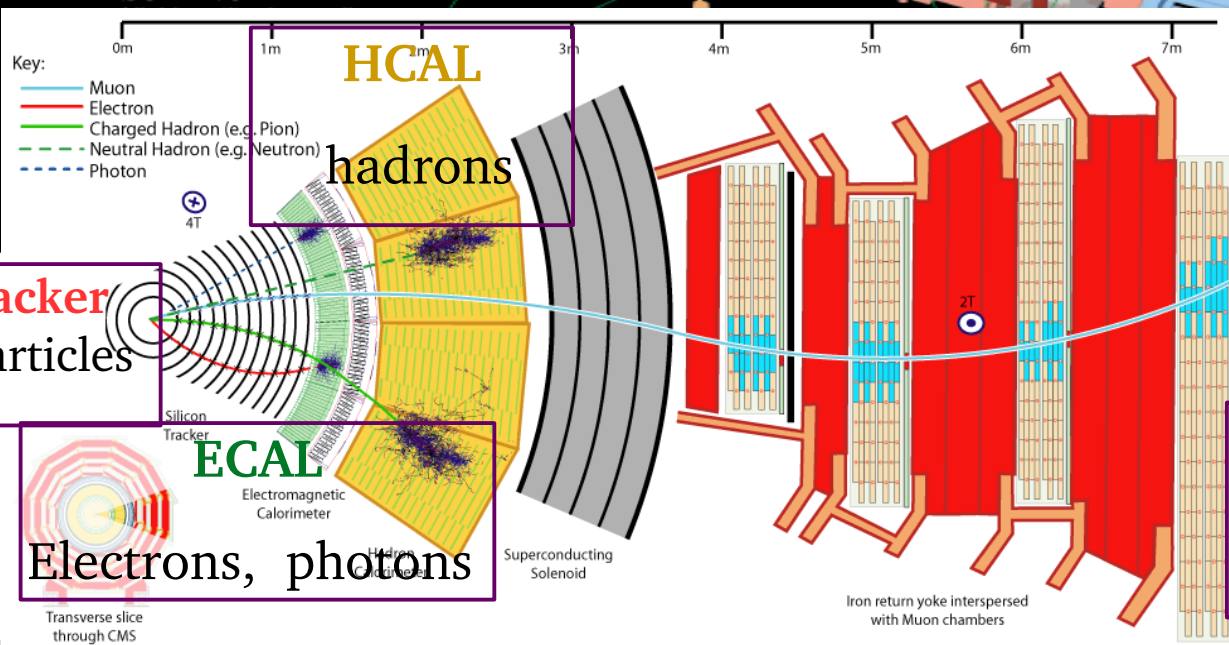
PRESHOWER
 Silicon strips
 ~16m² ~137k channels

STEEL RETURN YOKE
 ~13000 tonnes

SUPERCONDUCTING SOLENOID

FORWARD CALORIMETER
 Steel + quartz fibres
 ~2k channels

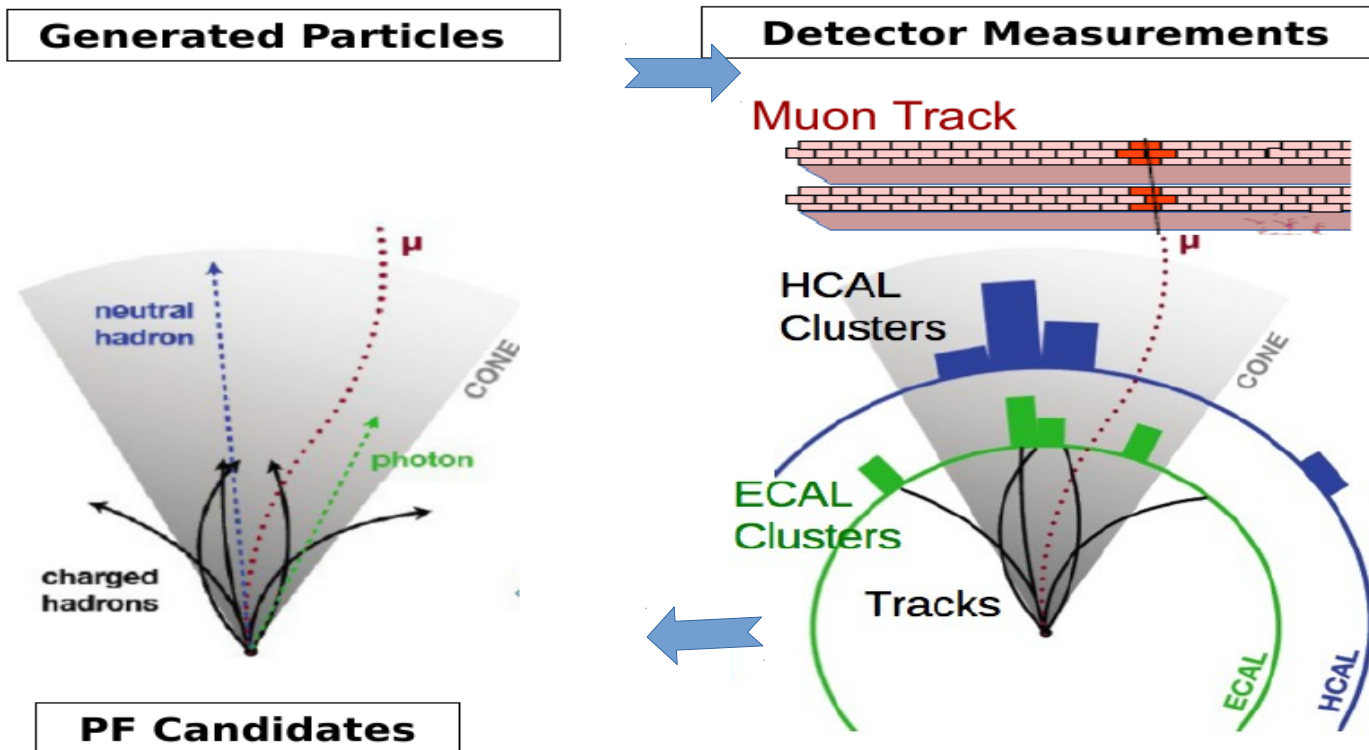
Total weight
 Overall diameter
 Overall length
 Magnetic field



Inner tracker
 charged particles

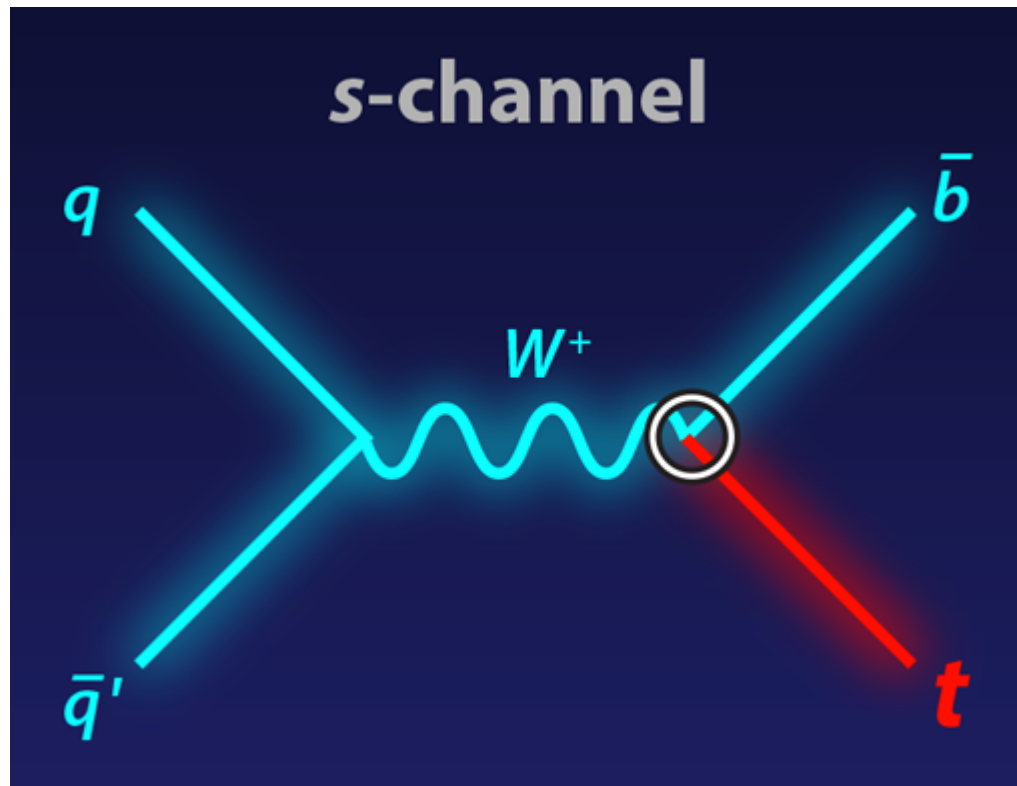
Muon System
 muons

Physics Object Reconstruction



- In **Reconstruction**: CMS sub-detectors signals are translated to physics objects.
- CMS uses information from its sub-detectors in the **Particle Flow** algorithm.
- PF algorithm aims to reconstruct objects back to the particle level.

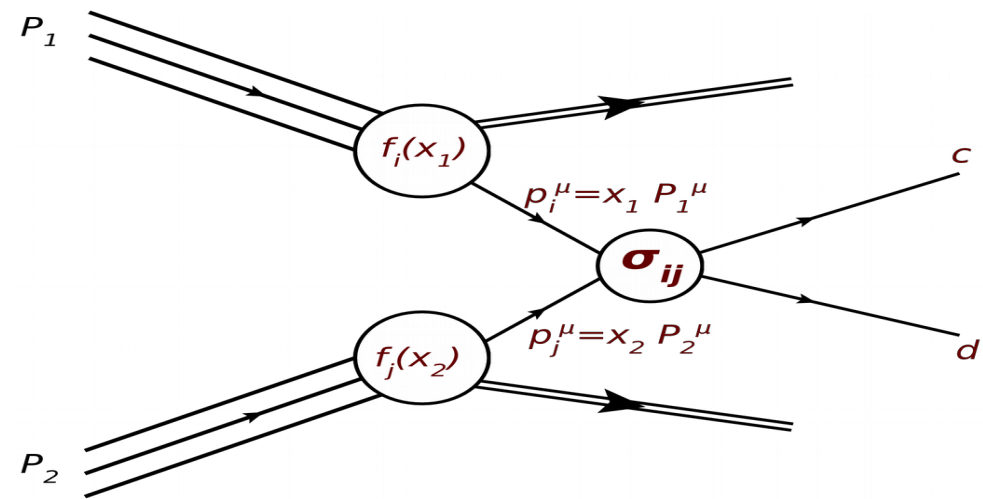
CMS measurement (8TeV): Single Top in s-channel



Why single top s-channel has such small cross section?

t-channel	LHC 7 TeV	$65.9^{+2.1}_{-0.7} \text{ } ^{+1.5}_{-1.7}$
	LHC 8 TeV	$87.2^{+2.8}_{-1.0} \text{ } ^{+2.0}_{-2.2}$
	LHC 13 TeV	$216.99^{+6.62}_{-4.64} \pm 6.16$
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<hr/>		
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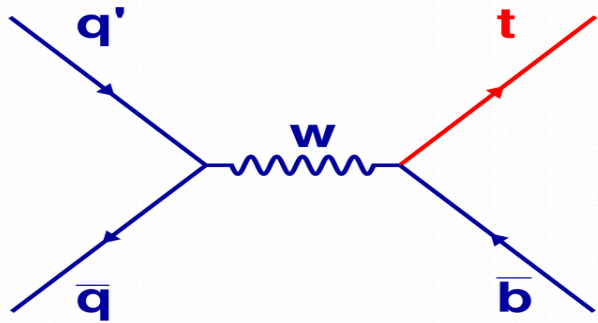
hard scattering in hadron-hadron collisions
QCD FACTORISATION THEOREM:



PDF is defined as the probability density for finding a particle with a certain longitudinal momentum fraction x at resolution scale Q^2 .

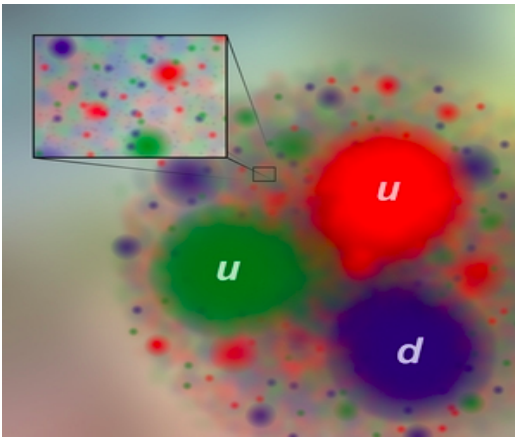
$$\sigma_{ab \rightarrow t\bar{t}} = \sum_{ij} \int dx_i dx_j f_i^{(a)}(x_i, \mu_F^2) f_j^{(b)}(x_j, \mu_F^2) \hat{\sigma}_{ij \rightarrow t\bar{t}}(\hat{s}, m_t, \mu_F, \mu_r, \alpha_s).$$

Why s-channel has such small cross section?

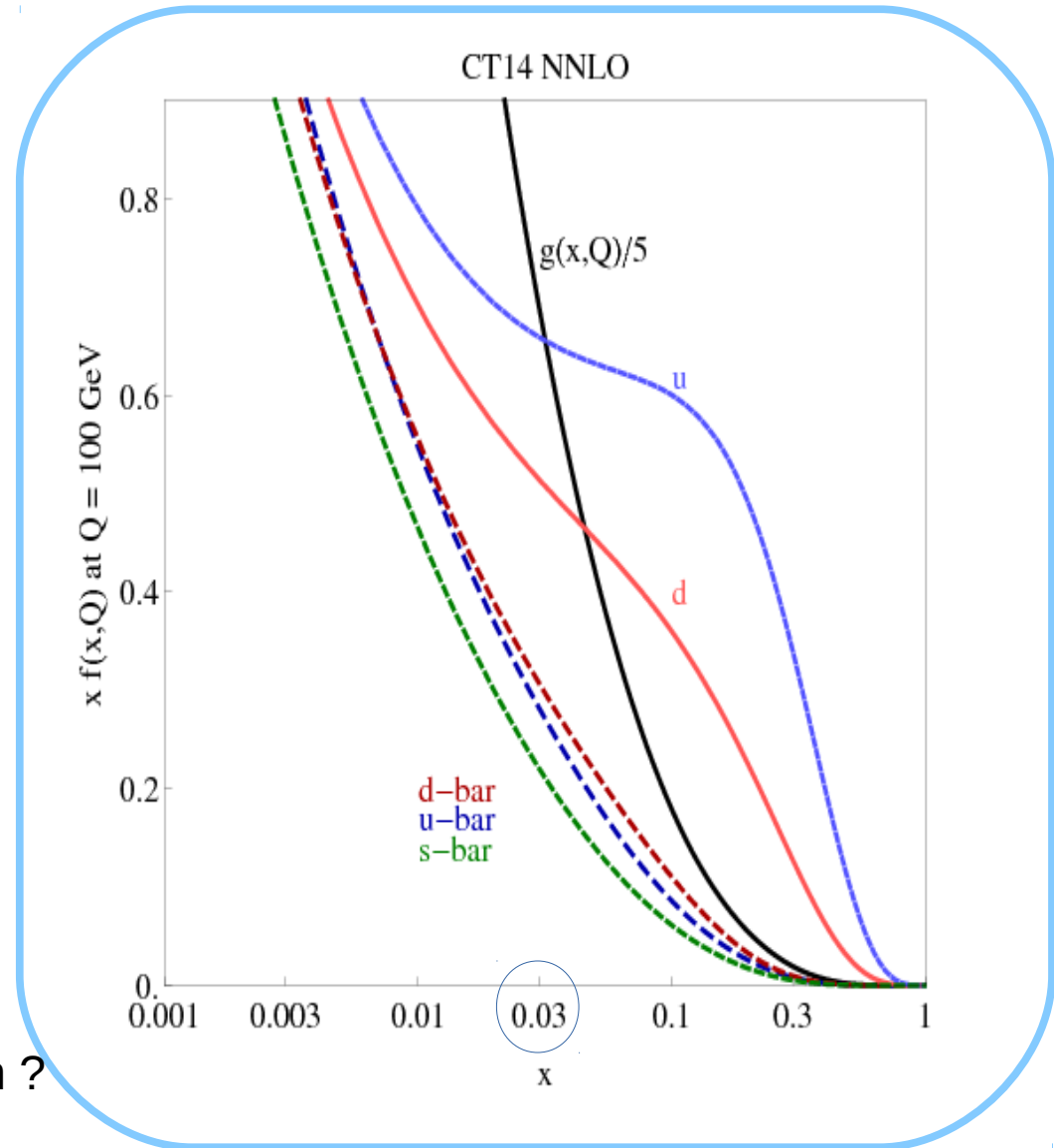


need a quark and an anti quark

pdf of antiquarks in proton?

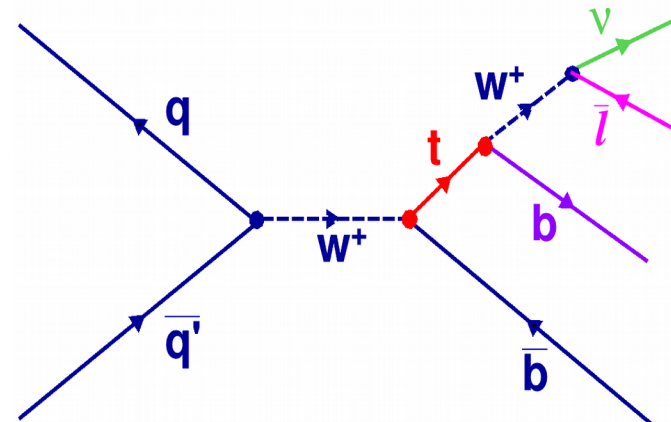


Charge asymmetry in top/anti top production ?



Signal Definition

- Single top produced in s channel and decay leptonically to electron is considered as signal : $pp \rightarrow t b \rightarrow W b b \rightarrow e \nu b b$



- Signal final state topology :

- one isolated electron ---> directly reconstructed in detector
- two b quarks, represented by two jets in the event signature, tagged as two b jet
- one neutrino, escapes undetected, the transverse momentum is taken from MET, longitudinal component is extracted from the W boson mass constraint

- Cascade decay $W \rightarrow \tau \nu \rightarrow e \nu \nu$ is considered as signal

**Jet? Bjet?
Next to next slide**

Background Modeling

Backgrounds:

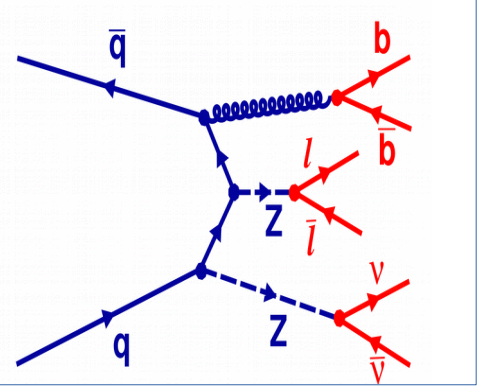
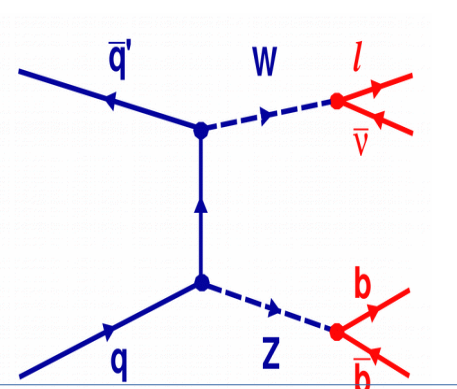
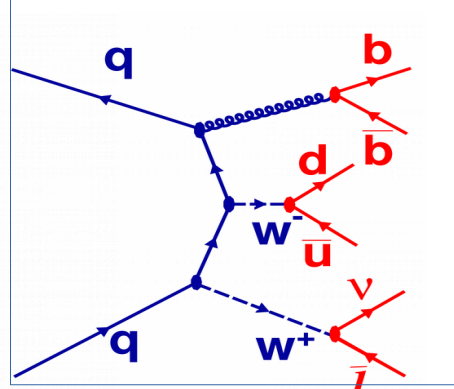
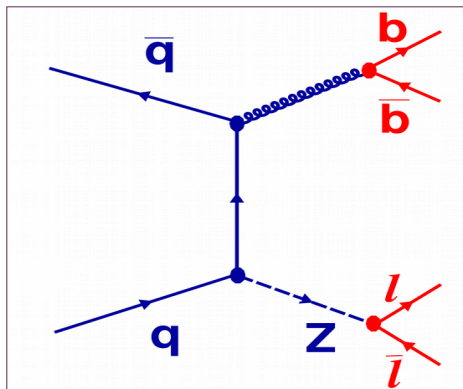
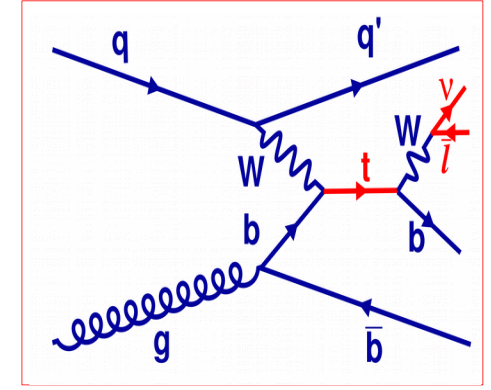
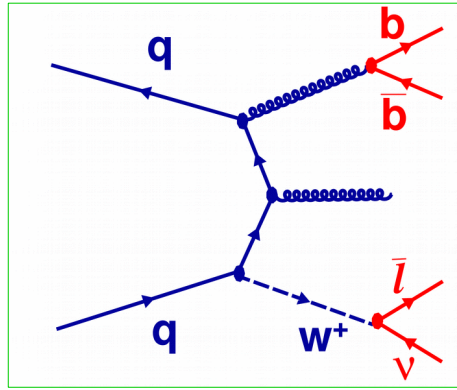
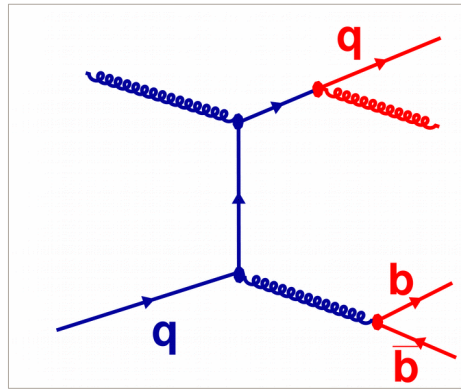
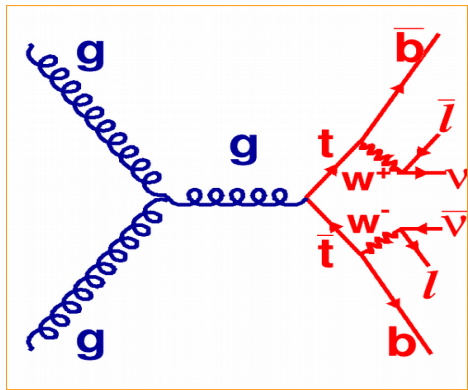
physics processes produce fake signal signature

Having similar objects in the final states



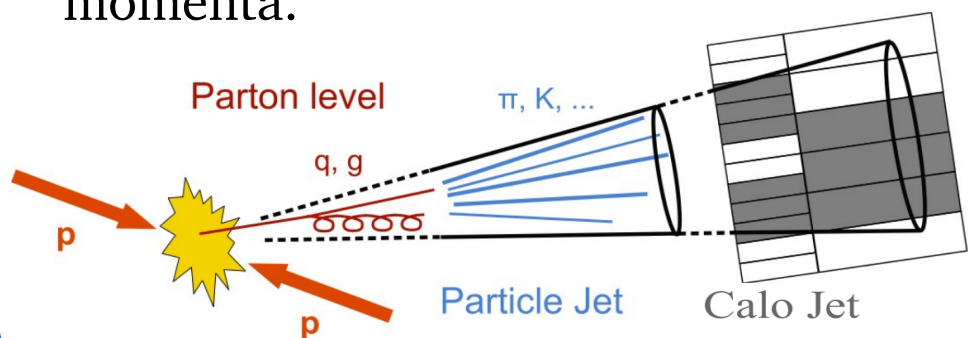
Instrumental effects

Main backgrounds: top quark pair, QCD, W + jets, other single top, Z + jets, diboson



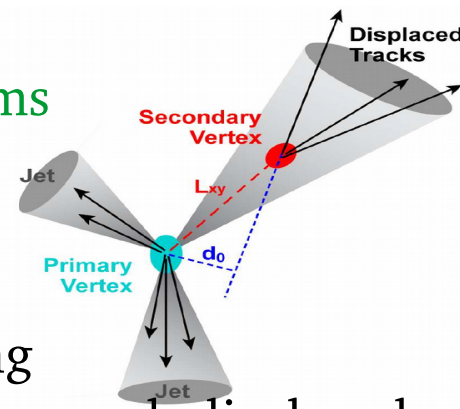
Jet Reconstruction

- PF particles are clustered into jet using Anti-kT clustering algorithm.
- PF particles four-momenta are summed to construct the jet four-momenta.



Heavy-flavor jet tagging

- A jet originating from the hadronization of a b quark referred to as b jet.
- **B-tagging algorithms** use relatively large masses long lifetime of B hadrons, resulting in a secondary vertex and displaced tracks.



- Jet four-momenta in detector-level \neq jet four-momenta of the generated-jet.
- Jet Energy Corrections (JEC) and Jet Energy Resolution (JER) scale factors are used.



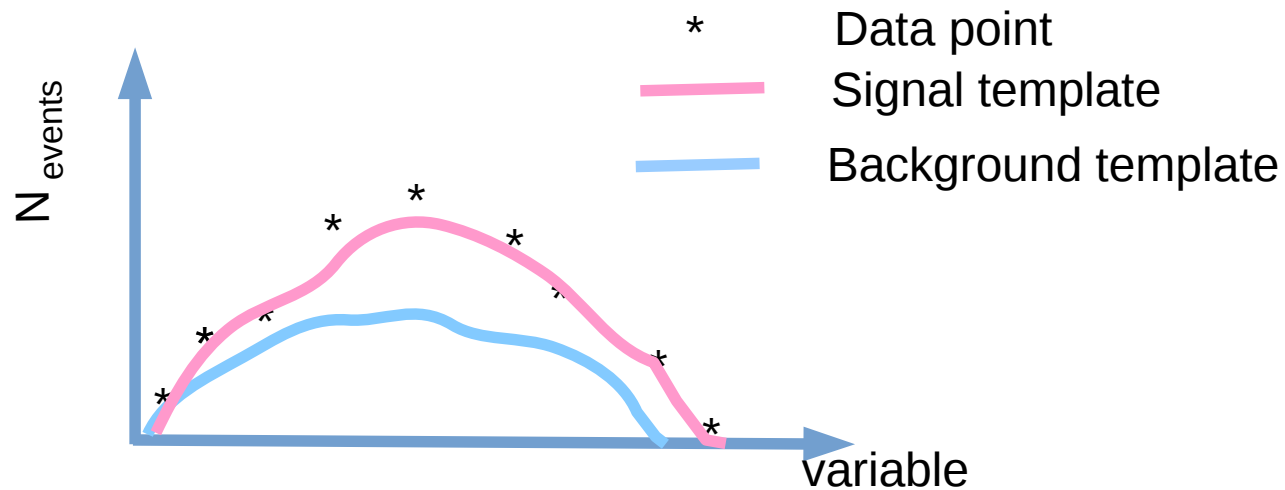
Cross section measurement methods

Templates Fit

Reconstruct
Discriminating
variable(ex. HT)

Form signal and
Background
templates

Perform a likelihood fit
Between data and
templates



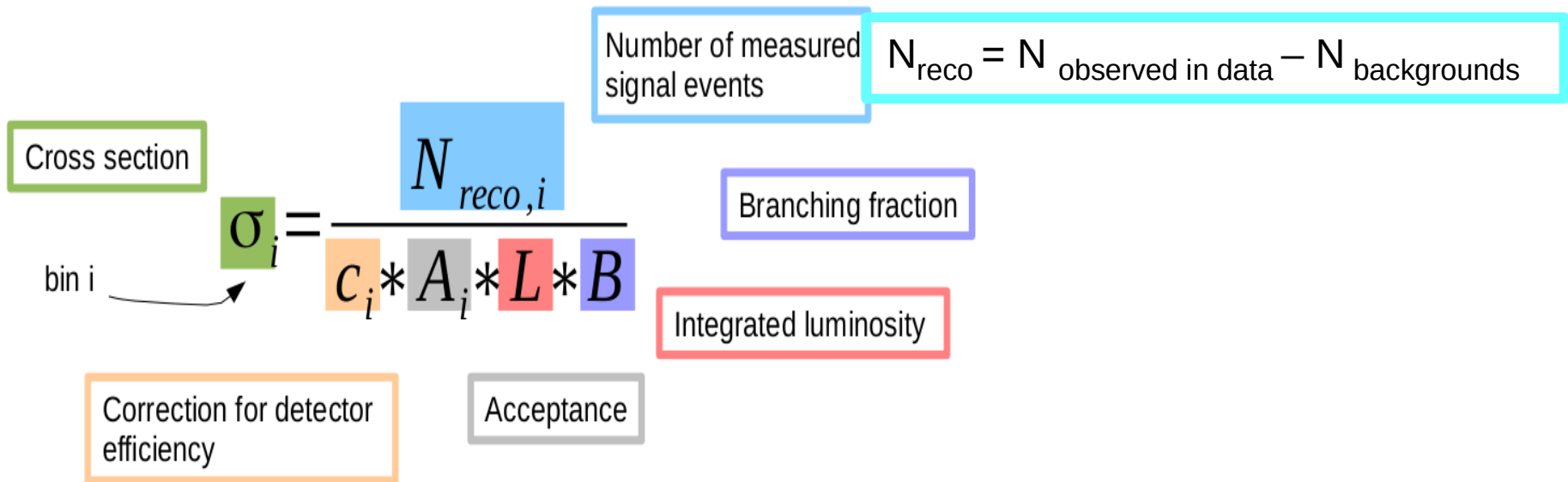
Cross section measurement methods

Cut and Count

Establish selection,
Estimate expected BKG

Find number of data
events

$N_{\text{obs.}} - \text{BKG} / \epsilon \cdot \text{Lumi.}$



Data Set

- The main analysis is based on the full data set of the proton proton collisions at 8 TeV recorded in 2012 by the CMS detector corresponding to an integrated luminosity of 19.7 fb^{-1} .

Official CMS Software (CMSSW) :
CMSSW_5_3_11

Detector conditions and object calibrations
Global Tag : FT53-V21A-AN6::All

Primary Dataset : SingleElectron

High Level Trigger (HLT) path : HLT_Ele27_WP80 with 80% trigger efficiency

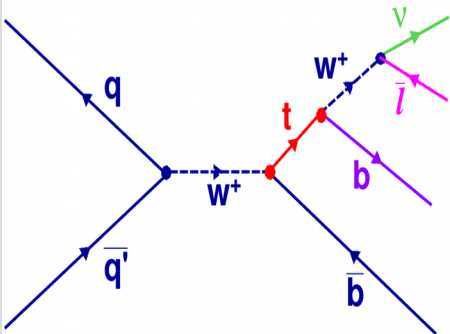
DataSet	Run Range	Integrated Luminosity	Global Tag
/SingleElectron/Run2012A-22Jan2013-v1/AOD	190450-193621	889.3 pb^{-1}	FT53-V21A-AN6::All
/SingleElectron/Run2012B-22Jan2013-v1/AOD	193833-196531	4423.1 pb^{-1}	FT53-V21A-AN6::All
/SingleElectron/Run2012D-22Jan2013-v1/AOD	198022-203742	7146.6 pb^{-1}	FT53-V21A-AN6::All
/SingleElectron/Run2012D-22Jan2013-v1/AOD	203777-208686	7319.0 pb^{-1}	FT53-V21A-AN6::All

Monte Carlo Samples

- Simulated events pass through the CMS full simulation implemented in the Geant4 software.
- Detector conditions and object calibrations, Global Tag : START53_V27::All

Process	$\sigma [pb]$
single top, <i>s</i> channel, top (leptonic decay)(*)	1.228(NLLL)[44]
single top, <i>s</i> channel, anti-top (leptonic decay)(*)	0.570(NLLL)[44]
single top, <i>t</i> channel, top (leptonic decay)(*)	17.496(NLLL)[44]
single top, <i>t</i> channel, anti-top (leptonic decay)(*)	9.947(NLLL)[44]
single top, <i>tW</i> channel, top	11.1(NNLL)[44]
single top, <i>tW</i> channel, anti-top	11.1(NNLL)[44]
<i>tt</i>	245.8(NNLL)[141]
<i>W</i> ($\rightarrow l\nu$)+1 jet(**)	5,000
<i>W</i> ($\rightarrow l\nu$)+2 jets(**)	1,750
<i>W</i> ($\rightarrow l\nu$)+3 jets(**)	519
<i>W</i> ($\rightarrow l\nu$)+4 jets(**)	214
<i>Z</i> / γ^* ($\rightarrow l^+l^-$) + jets (***)	3,500(NNLO)
<i>WW</i>	57
<i>WZ</i>	32
<i>ZZ</i>	8.3
EM-enriched QCD, $20 < \hat{p}_T < 30\text{GeV}$	2454400(LO)
EM-enriched QCD, $30 < \hat{p}_T < 80\text{GeV}$	4615893(LO)
EM-enriched QCD, $80 < \hat{p}_T < 170\text{GeV}$	183,294.9(LO)
EM-enriched QCD, $170 < \hat{p}_T < 250\text{GeV}$	4,586.5(LO)

Event Selection in Signal Sample



- **One isolated lepton**, events with additional lepton are rejected

- PF electron, $E_T > 30$ GeV, $|\eta| < 2.5$
- PF lepton relative isolation: $relIso < 0.1$
- electron MVA ID > 0.9
- electron veto: $p_T > 20$ GeV, $relIso < 0.15$,
- muon veto: $p_T > 10$ GeV, $relIso < 0.2$

suppress dilepton events from $t\bar{t}$ or Drell-Yan processes

- **Two b tagged jets**

- AK5 PF Jets
- $p_T > 40$ GeV
- Jet $|\eta| < 5$
- Jet ID quality cuts
- CSV tight threshold: discriminator > 0.898

suppress $t\bar{t}$ and QCD multijets events

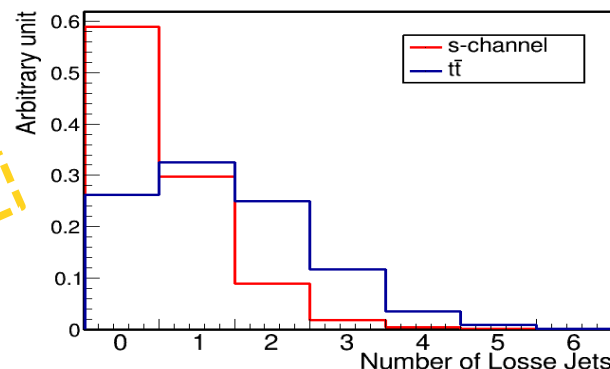
- **Missing transverse energy**
- no explicit requirement

In notation "n-jets m-tags",
Signal sample : 2-jets 2-tags

- **events with more than one loose jets are rejected**

- usual jet selection, $20 < p_T < 40$ GeV

suppress $t\bar{t}$ events



Event Selection in Control Samples

- The primary goal of the control samples is either **to study the modeling of the various background processes** or **to estimate and to constrain their contributions**.
- Events divided in various categories based on jet and b jet multiplicity. Definition of selected objects are similar to signal sample.

**signal sample: 2 -jets 2-tags
s-channel enriched**

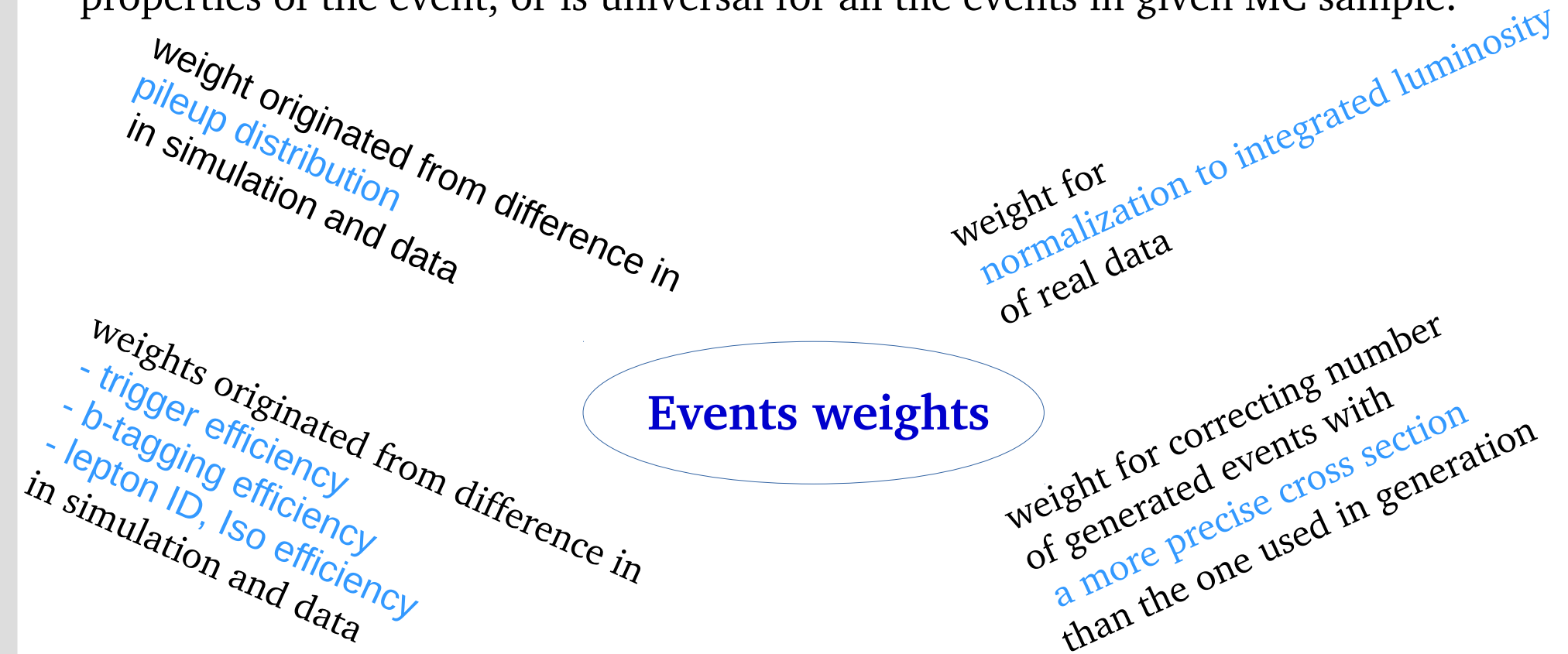
**s channel
analysis**

**control sample: 2-jets 1-tag
W+jets and t-channel
enriched**

**control sample: 3-jets 2-tags
top pair enriched**

Simulated Events Weights

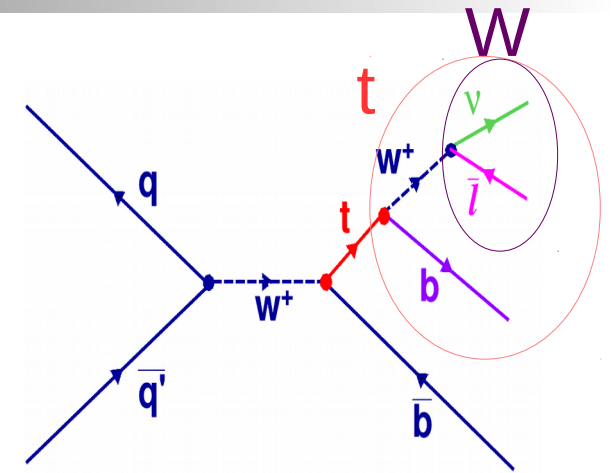
- Each simulated event gets a weight which either is determined from the specific properties of the event, or is universal for all the events in given MC sample.



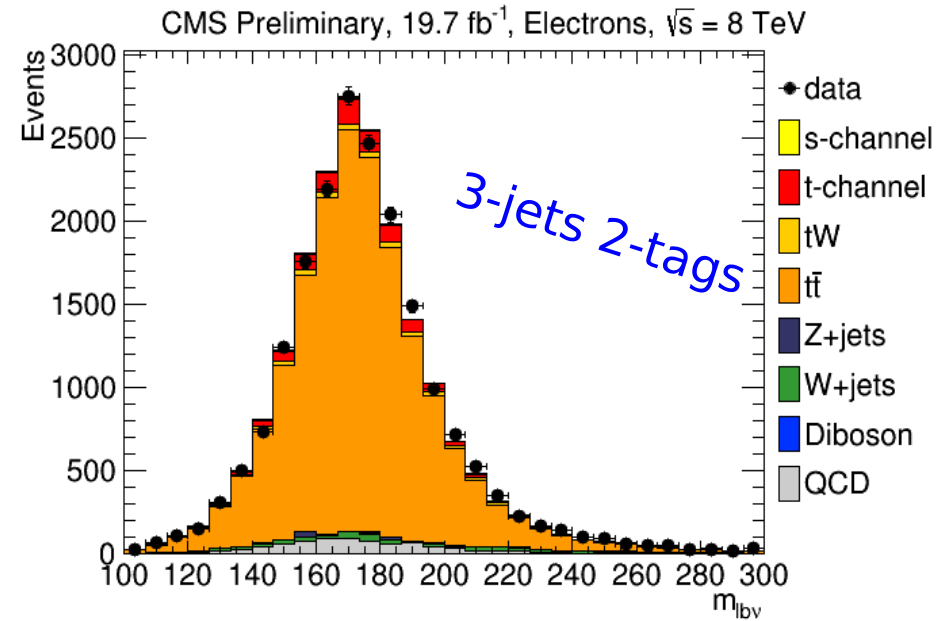
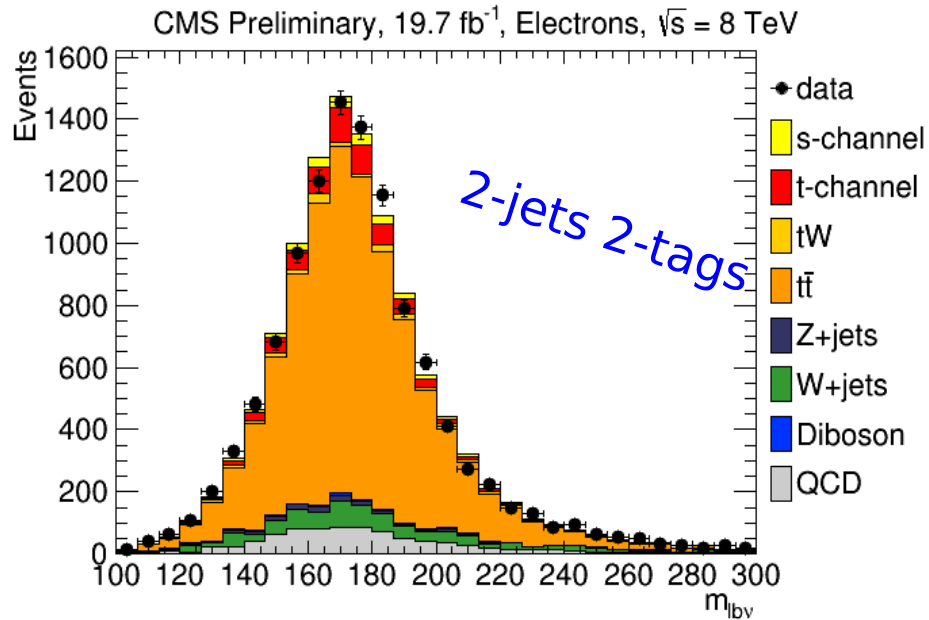
- JER and JES corrections are applied and propagated to MET.
- Uncertainty on the events weights introduces uncertainty on the measurement.

Top Reconstruction

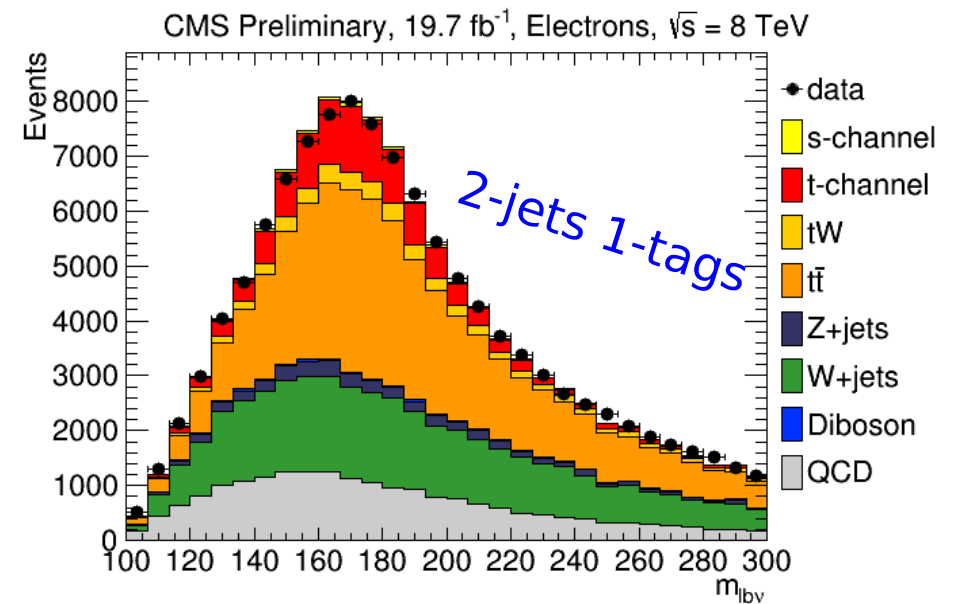
- ◆ $M_{lb\nu}$ invariant mass of the top quark candidate
- ◆ Lepton is reconstructed in detector
- ◆ Neutrino reconstruction:
 - ◆ $MET_x = p_{x,\nu}$
 - ◆ $MET_y = p_{y,\nu}$
 - ◆ **W-boson** mass constraint \rightarrow quadratic equation for $p_{z,\nu}$
 - \rightarrow In case of two real solutions: choose the one with the smaller $|p_{z,\nu}|$
 - \rightarrow In case of complex solutions: modify $p_{x,\nu}$ and $p_{y,\nu}$ to have $m_{T,W} = m_W$,
Recalculate the $p_{z,\nu}$
- ◆ b-jet assignment
 - In 2tag samples: “best-mass-top” method
 - In 1tag sample : b-tagged jet



Reconstructed Top Mass in Signal and Control Samples



QCD extracted by a data-driven procedure.



Background Modeling and Estimation

- The shape and the rate of background processes are taken from the simulation with two exceptions: **QCD multijets** in all samples and **W+jets** yields in the 2-jets 1-tag sample.
- **W+jets** global normalization scale factor of 1.6 is used in 2-jets 1-tag.
- **QCD multijets** process is not well modeled by the MC simulation, its contribution is not reliable.
 - QCD shape is taken from **anti-isolated sample** in data and normalization from a **fit to the BDT distributions**.
 - “anti-iso” selection** = standard selection with lepton relative isolation $I_{rel} > 0.1$ OR MVA ID < 0.9.

QCD Estimation Strategy

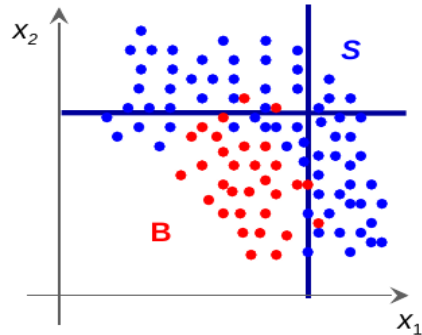
- Three anti-QCD **boosted decision trees** are trained in the 2-jets 2-tags, 2-jets 1-tag and 3-jets 2-tags categories.

What is Multivariate analysis? Why?

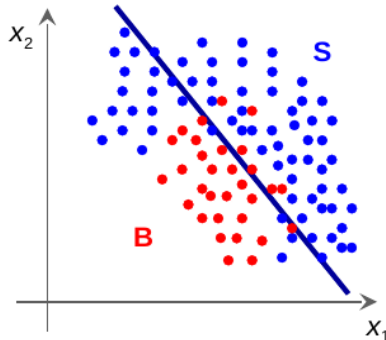
What is BDT?

Multivariate Analysis

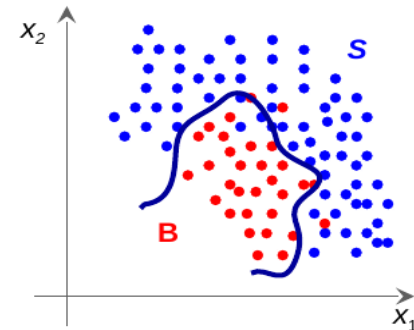
Multivariate Analysis (MVA)



Rectangular cuts



Linear

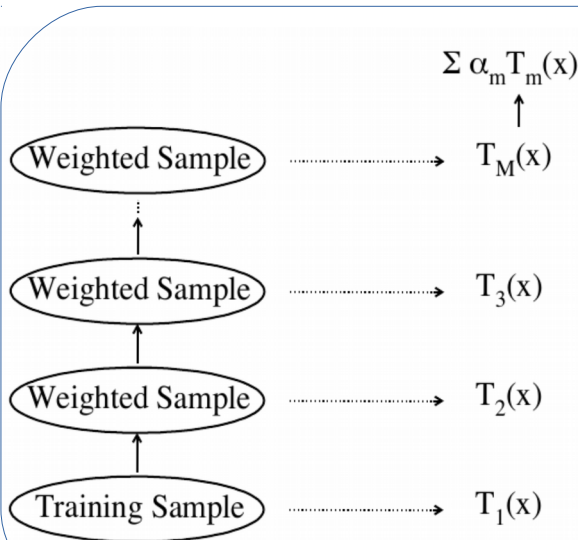
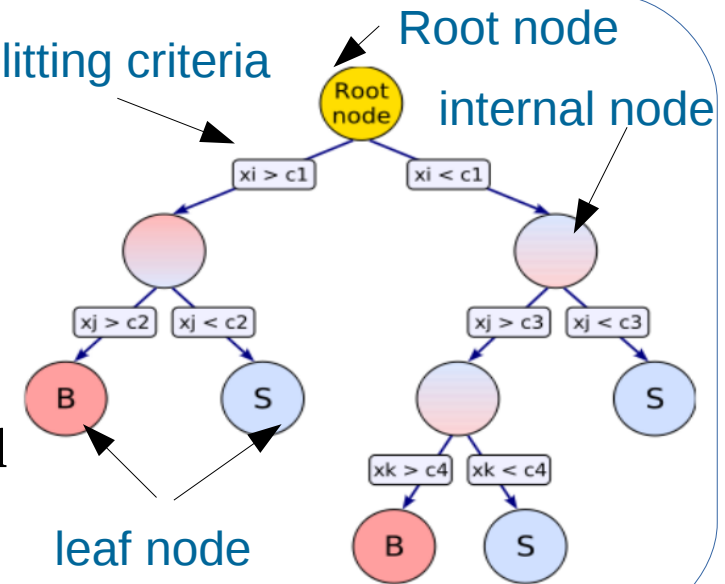


Non-linear (BDT,...)

- MVA is based on **machine learning** methods.
- An MVA analysis consists of two separate phases: the **learning phase** where the multivariate method is trained, tested and evaluated, and the **application phase** where the chosen method is applied on the problem that it has been trained for.
- In a classification multivariate analysis, the machine is learned to separate a given signal from backgrounds, given already known results on a training sample.

Boosted Decision Trees (BDT)

- **Decision Trees** is an example of MVA, in which a binary tree structure (a series of yes/no decisions) is built to classify events.
- Training a decision tree: process that defines the **splitting criteria** for each node.
- Depending on the majority of signal and background events in leaf nodes, the events inside that node are labeled as **signal (+1)** or **background (-1)**.



To stabilize Decision Tree performance, one can use different techniques: e.g. **Boosting**.

Boosting : sequentially apply the DT algorithm to reweighted (boosted) version of training sample, and produce a forest.

The idea behind the boosting is that misclassified events, are given a higher event weight and hence higher importance in the training of the next tree.

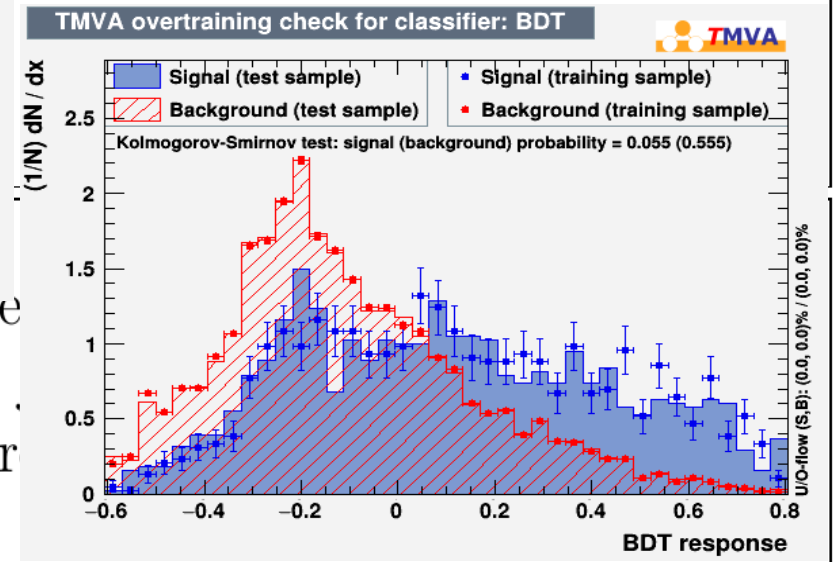
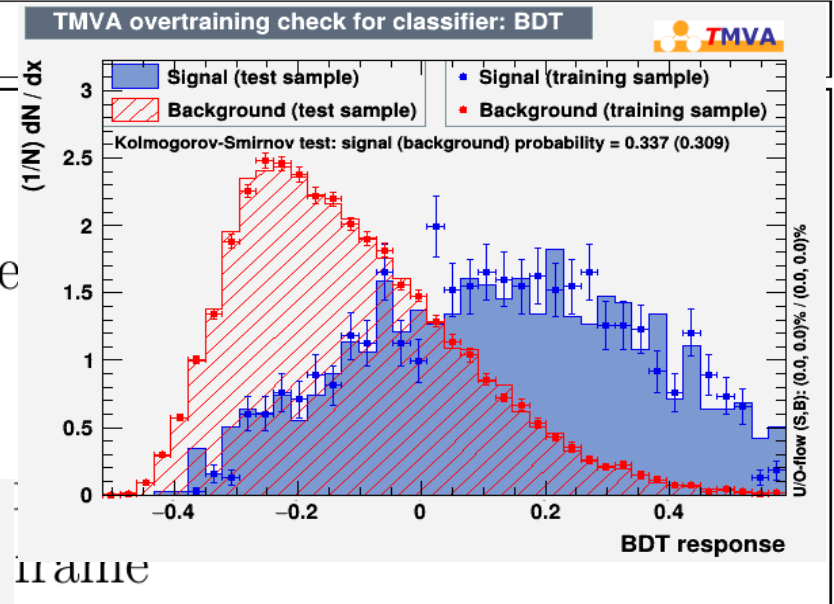
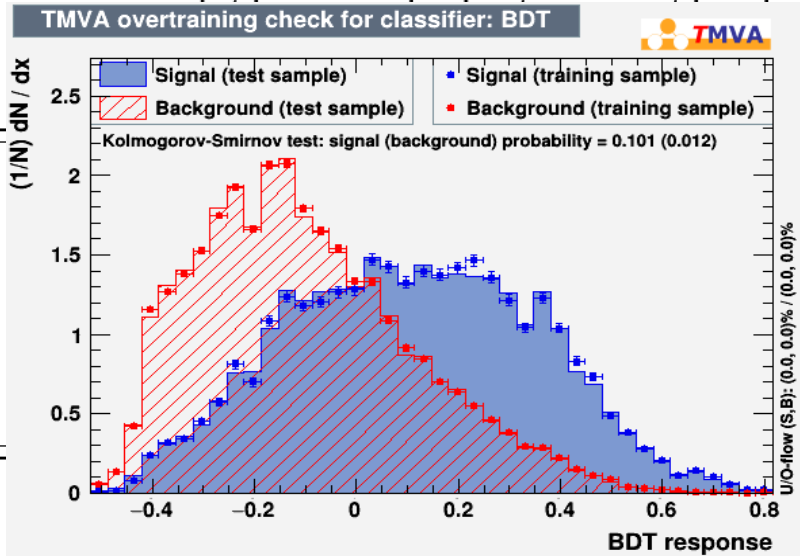
QCD Estimation Strategy

- Three anti-QCD **boosted decision trees** are trained in the 2-jets 2-tags, 2-jets 1-tag and 3-jets 2-tags categories.
 - **Signal**: QCD, taken from data with “anti-iso” selection
 - **Backgrounds**: top pair, W/Z+jets and single top

	Variable	Description
2-jets 2-tags	η_e m_T $\Delta R_{b',\ell}(*)$ H_T $\cos \theta^*$	pseudorapidity of lepton transverse W boson mass angular separation of the b-tagged jet with lower b discriminator and the lepton scalar sum of p_T of all jets cosine of the angle between the lepton and the b-tagged jet recoiled against top-quark in the top rest frame
2-jets 1-tag	η_e H_T $\Delta \Phi_{\cancel{E}_T,\ell}$	pseudorapidity of lepton scalar sum of p_T of all jets distance in azimuthal angle ($\Delta \Phi$) between $\vec{\cancel{E}}_T$ and lepton
3-jets 2-tags	η_e \cancel{E}_T $\Delta R_{j1,j3}$ $p_T^{lb\nu}$	pseudorapidity of lepton missing transverse energy in the event angular separation of the leading jet and the least energetic jet transverse momentum of the top reconstructed with the best-mass-top method

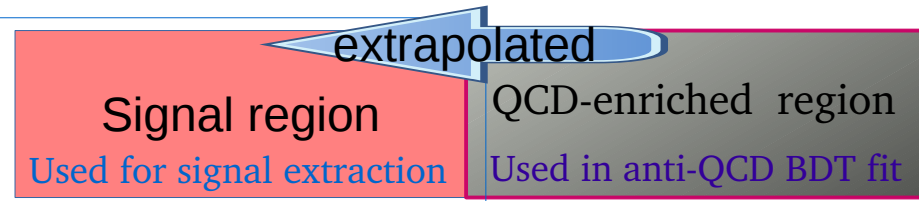
QCD Estimation Strategy ...

	Variable	Description
2-jets 2-tags	η_ℓ	pseudorapidity of lepton
	m_T	transverse W boson mass
	$\Delta R_{b',\ell}(\ast)$	angular separation of the b-tagged and the lepton
	H_T	scalar sum of p_T of all jets
	$\cos \theta^\ast$	
2-jets 1-tag	η_ℓ	
	H_T	
	$\Delta\Phi_{\cancel{E}_T,\ell}$	
3-jets 2-tags	η_ℓ	
	\cancel{E}_T	missing transverse energy in the e
	$\Delta R_{j1,j3}$	angular separation of the leading
	$p_T^{lb\nu}$	transverse momentum of the top r
		top method



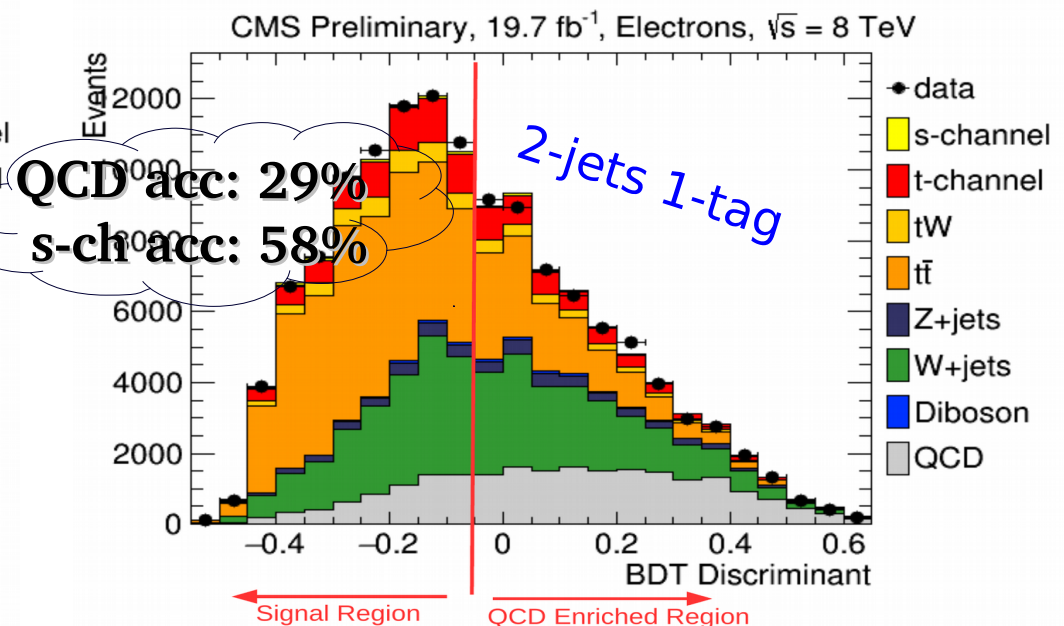
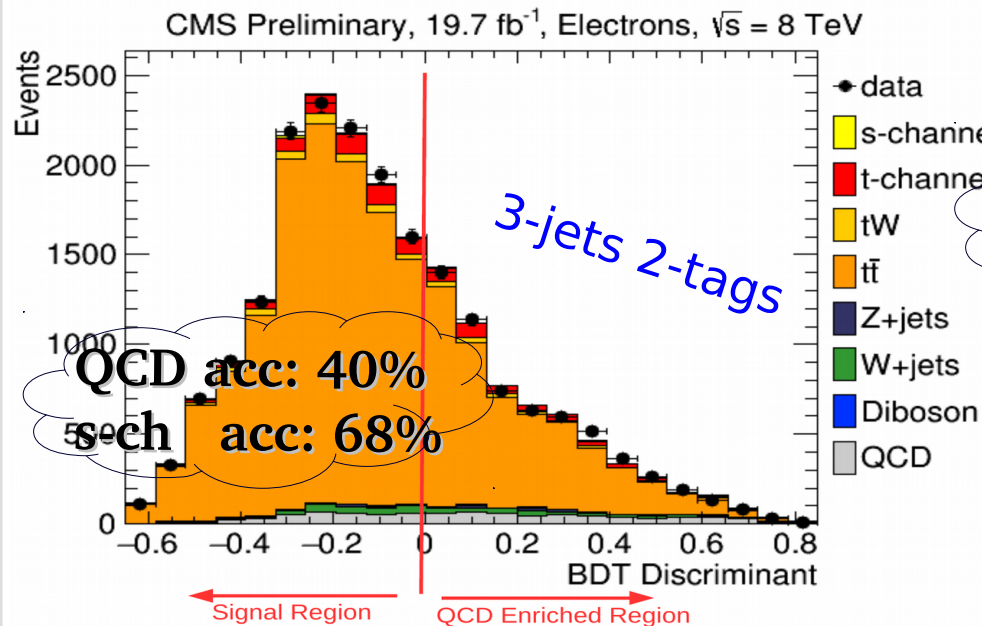
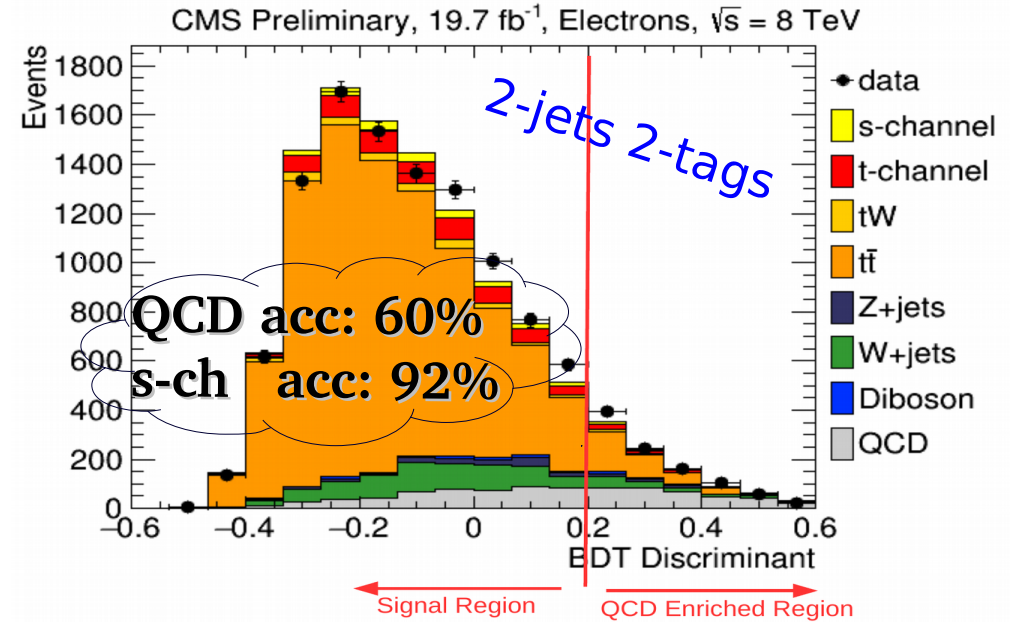
QCD Estimation Strategy ...

- Divide the sample in two regions: QCD-enriched and signal region



BDT cut point

- Events in the QCD-enriched region are eliminated from the analysis



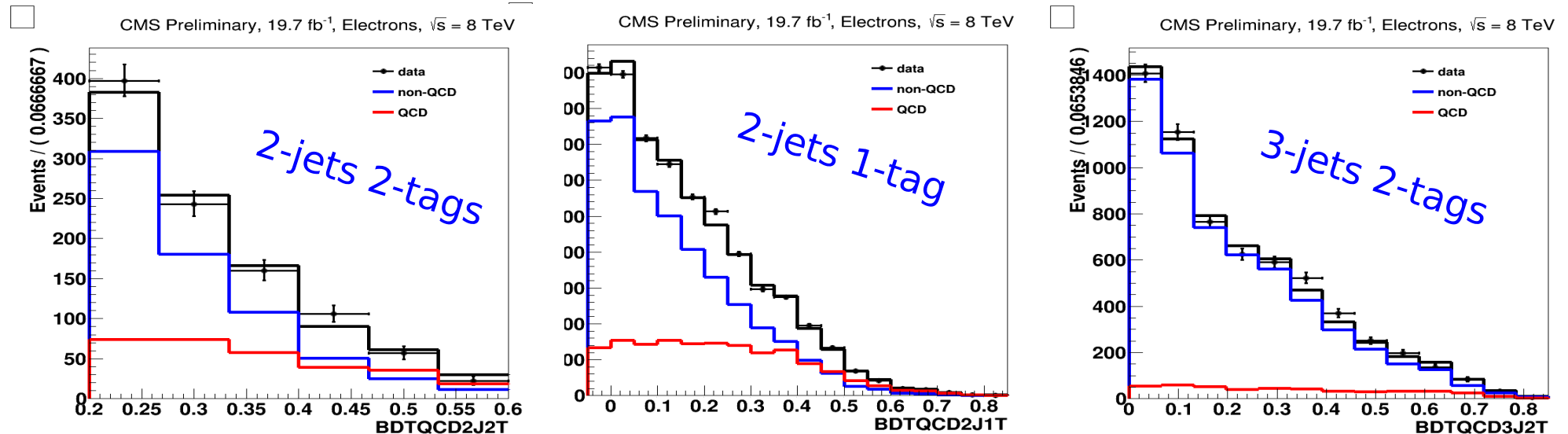
Fit in QCD-Enriched Region

- The maximum likelihood fit to BDT distribution in QCD-enriched region

$$F(\text{BDT}) = s \cdot S(\text{BDT}) + b \cdot B(\text{BDT})$$

$B(\text{BDT})$: template for non-QCD events, obtained from simulation

$S(\text{BDT})$: template for QCD events, obtained from anti-isolated sample in collisions data, $\Delta R_{\text{lepton,jet}} > 0.3$



Sample	$N_{\text{QCD}}^{\text{fit}}$	$N_{\text{QCD}}^{\text{SR}}$	QCD uncertainty
2-jets 2-tags	296.7	439.4	17%
2-jets 1-tag	15250.0	6081.3	2.6%
3-jets 2-tags	463.0	313.5	24%

Event Yields

Event yields after selections and background estimation in signal and control samples.

Process	3-jets 2-tags	2-jets 1-tag	2-jets 2-tags
$t\bar{t}$	10838	34373	3943
$W + jets$	201	17443	530
$Z + jets$	32	1732	88
Diboson	17	331	45
QCD	313	6081	291
tW	280	3198	108
t channel	528	6800	374
s channel	48	429	171
Total MC	12254	70387	5550
Data	13512	73895	6301

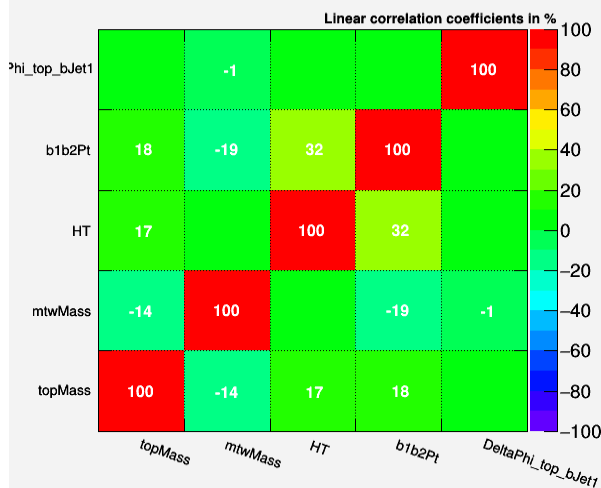
signal /background=0.033

Signal Extraction, s-channel Enriched Region

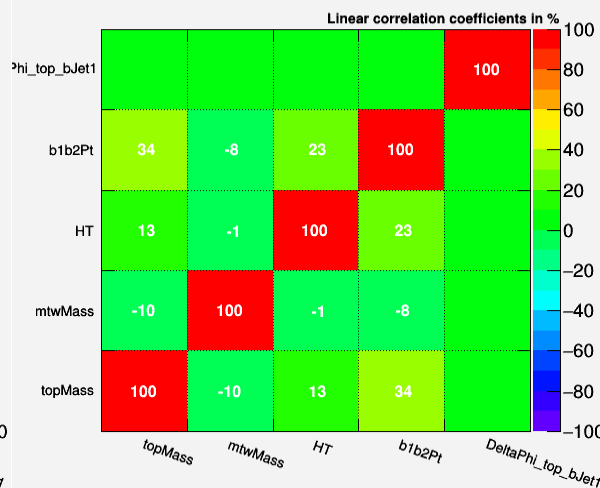
- A boosted decision trees is trained in 2-jets 2-tags sample.
- In BDT framework: **Signal: s-channel** **Background: rest of physics process involved**

Variable	Description
$\Delta\Phi_{top,b1}$	difference in azimuthal angle between top and leading jet
p_T^{bb}	vector sum of p_T of the two b-tagged jets
m_T	transverse W boson mass
H_T	scalar sum of p_T of all jets
$m_{\ell b\nu best}$	invariant mass of lepton, neutrino and one of the b-tagged jets reconstructed with the best-mass-top method

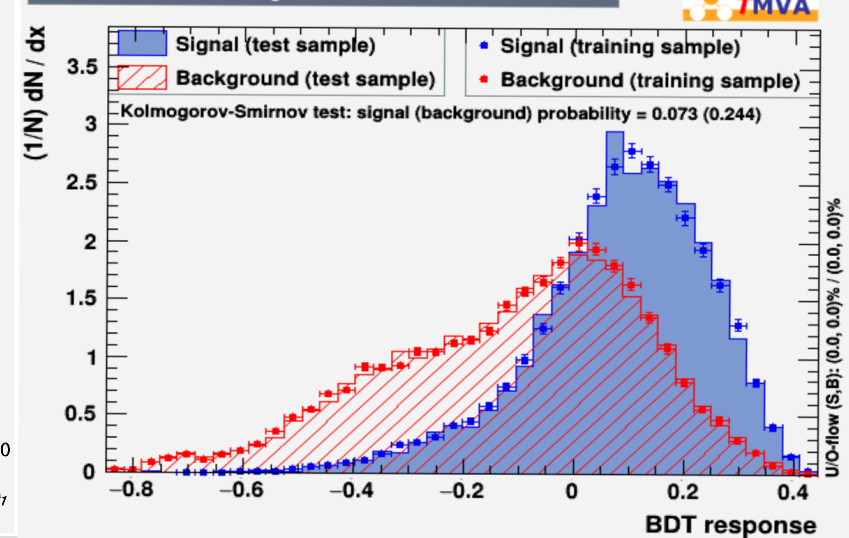
Correlation Matrix (signal)



Correlation Matrix (background)



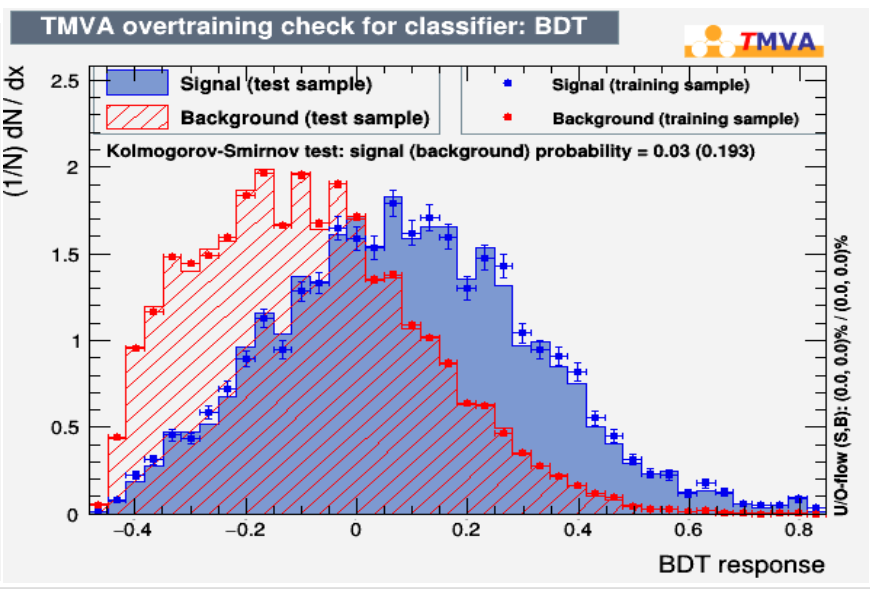
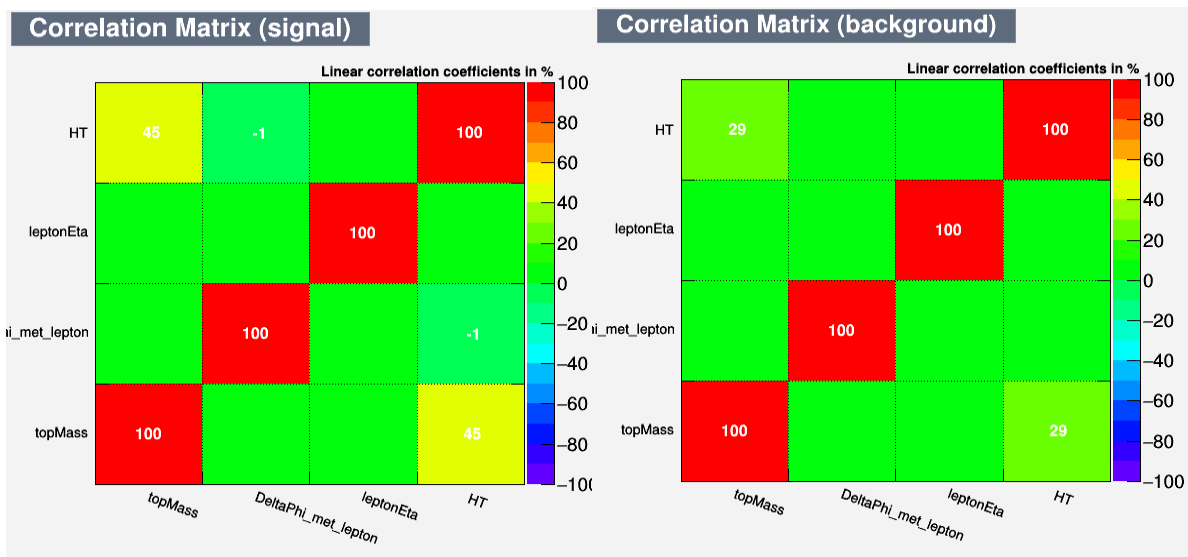
TMVA overtraining check for classifier: BDT



Signal Extraction, W+jets and t-channel Enriched Region

- A boosted decision trees is trained in the 2-jets 1-tag sample.
- In BDT framework: **Signal: W+jets** **Background: rest of physics process involved.**

Variable	Description
$m_{\ell b\nu \text{ best}}$	invariant mass of lepton, neutrino and one of the b-tagged jets reconstructed with the best-mass-top method
H_T	scalar sum of p_T of all jets
η_ℓ	pseudorapidity of lepton
$\Delta\Phi_{\vec{E}_T, \ell}$	difference in azimuthal angle between \vec{E}_T and lepton

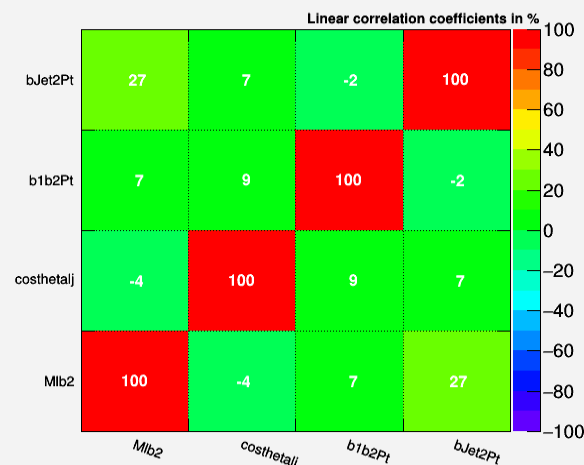


Signal Extraction, Top Pair Enriched Region

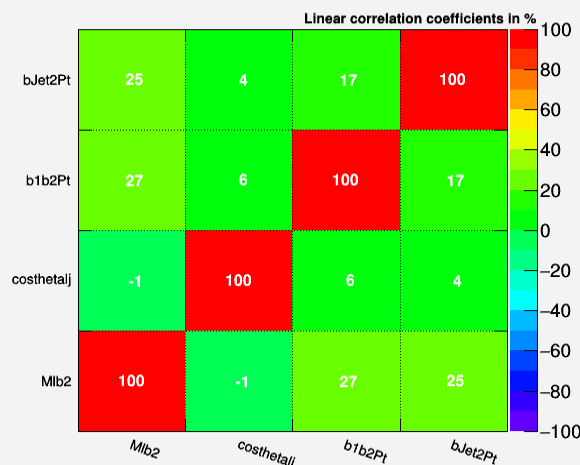
- A boosted decision trees is trained in the 3-jets 2-tags sample.
- In BDT framework **Signal: top pair**, **Background : rest of physics process involved**.

Variable	Description
$\cos \theta^*$	cosine of the angle between the lepton and the b-tagged jet recoiled against top quark in the top rest frame
M_{lb2}	invariant mass of the lepton and the second b-tagged jet
p_T^{b2}	p_T of the second b-tagged jets
p_T^{bb}	vector sum of p_T of the two b-tagged jets

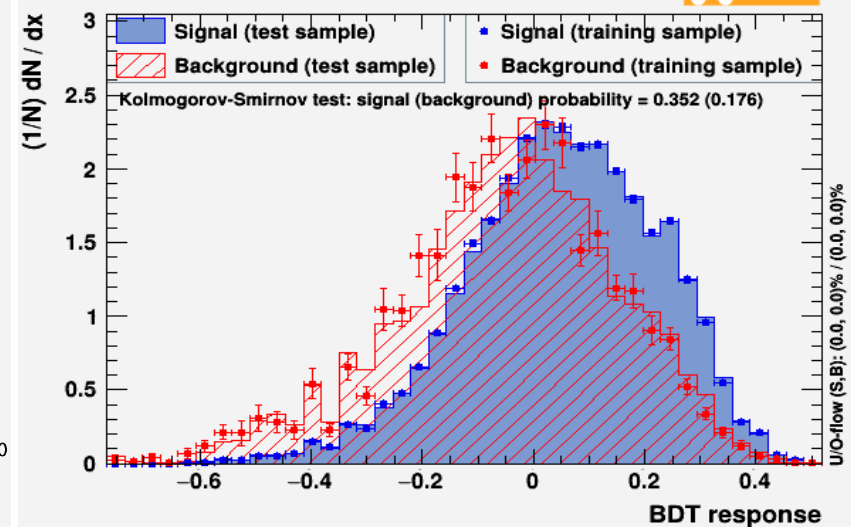
Correlation Matrix (signal)



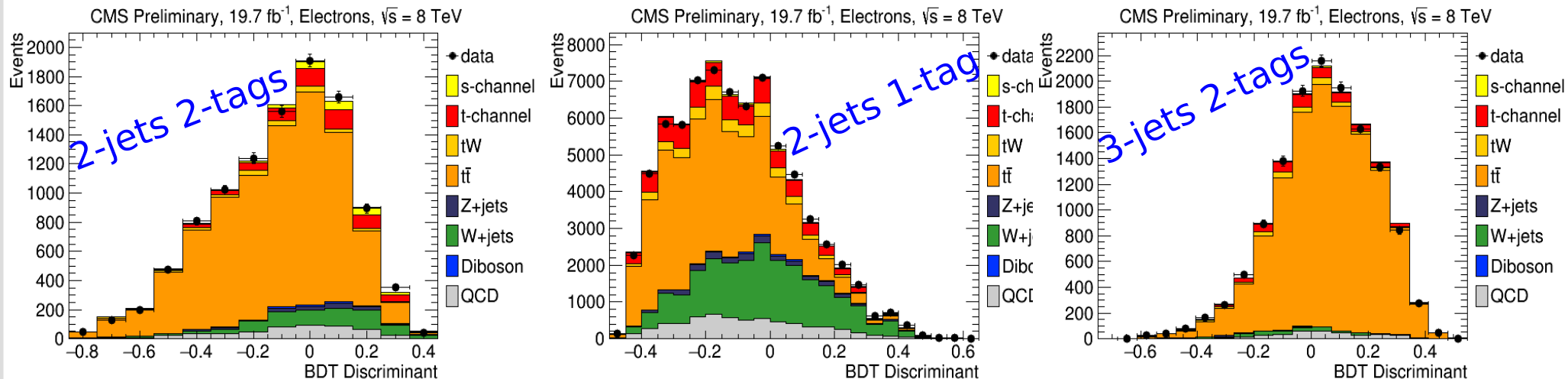
Correlation Matrix (background)



TMVA overtraining check for classifier: BDT



Signal Extraction Strategy



- A **simultaneous maximum likelihood fit** is performed in BDT distributions in 2-jets 2-tags, 3-jets 2-tags and 2-jets 1-tag bins.
- The statistical evaluation is made using the software **THETA**.
- Assuming n_i and λ_i as the number of observed and expected events in i^{th} bin, the

likelihood function is:

$$L(\theta, \beta | n) = \prod_{i=1}^N \frac{\lambda_i^{n_i} e^{-\lambda_i}}{n_i!} \prod_{u=1}^{N_u} \pi(\theta_u)$$

$$\lambda = B + \beta S.$$

→ signal
→ Background

- **Signal strength modifier β** is defined as the ratio of measured cross section and the SM prediction. β is the parameter of interest in the fit.

Systematic Uncertainties

- The individual quantities used to estimate the cross section are not perfectly known, and the obtained measurement is limited by the systematic uncertainties.

Theoretical origin:

PDF

Top p_T reweighting

ME and PS
Matching thresholds

Factorization and
renormalization scales

Simulation statistics

Background normalization:

top pair	10%
T-channel	10%
tW channel	15%
W+jets	20%
Z+jets	20%
Dibosons	30%
QCD	estimation uncertainty

Instrumental origin:

Unclustered
 $E_{T,miss}$

Luminosity

Lepton trigger,
reconstruction

Jet energy
resolution

b-tagging
mis-tagging

Jet energy
scale

Pile up

Systematic Uncertainties ...

- Background normalization uncertainties are added in the likelihood model as nuisance parameters.
- Simulation statistics is evaluated using “Barlow-Beeston light” * method by introducing new nuisance parameters in each bin.
- All the other instrumental and theoretical uncertainties are externalised due to:
 - theoretical motivation for theoretical uncertainties.
 - fit instability (fit not converging, asymmetric uncertainties in results).

Therefore, impact evaluation involves pseudo-data corresponding to $\pm 1\sigma$ shifts for each source, the difference between the fitted value for signal strength in $\pm 1\sigma$ scenarios and the nominal one is taken as the systematic uncertainty.

- **Total uncertainty:** uncertainties combined together with Barlow method**, which is the proper way for combining asymmetric systematic errors.

* Fitting using finite Monte Carlo samples”, Comput. Phys. Commun. 77 (1993) 219.

** R. Barlow, “Asymmetric Systematic Errors”, arXiv:physics/0306138.

Results: Significance, Upper Limit and Cross Section

- ▶ The significance of the s-channel excess over the background is measured:

Expected Significance	Observed Significance
0.6	2.2

- ▶ Observed and expected upper limits (UL) is measured:

	Expected UL	Observed UL
UL on cross section	23.8 [18.3, 33.3] pb	28.8 pb
UL on Cross section/SM prediction	4.3 [3.3, 6.0]	6.8

- ▶ The single top cross section in the s-channel is measured to be:

$$\sigma_{\text{s-ch.}} = 16.8^{+8.9}_{-9.3} \text{ pb} = 16.8 \pm 9.1 \text{ (stat + syst) pb}$$

$$\sigma_{\text{SM}} = 5.55 \pm 0.22 \text{ 8TeV}$$

which is equivalent to an scale factor with respect to the standard model prediction

$$\beta = 3.0 \pm 1.6$$

Relative Impact of Systematic Uncertainties

The uncertainty is shown to be extensively systematic dominant

Uncertainty source	up (%)	down (%)
Statistical	$\pm 14\%$	
$t\bar{t}$ and single top quark rate	-12.8	14.0
W/Z+jets, diboson rate	-13.8	11.7
QCD rate	4.7	-4.3
* Lepton efficiency	2.2	-1.8
Luminosity	5.3	-5.7
*JER	-9.0	8.7
*JES	-24.5	30.6
*b-tagging	13.9	-13.7
*mis-tag	0.14	-0.6
*Pileup	-6.9	6.5
*Unclustered E_T	0.8	-2.8
* μ_R, μ_F scales	-36	26
* Matching thresholds	-12.1	-11.1
* PDF	6.7	-7.3
*Top quark p_T reweighting	6.8	-7.5
Total uncertainty	$\pm 54.4\%$	

Combining Electron and Muon Channels Analyses at 8TeV



Muon Analysis, 8TeV

- In order to improve the precision of measurement, a combination of electron and muon results is also studied.
- **Event selection is generally similar to electron channel.**
 - HLT path : **IsoMu24_eta2p1**
 - Muon selection: PF muon and Global muon
 - $p_T > 26 \text{ GeV}$, $|\eta| < 2.1$
 - PF lepton relative isolation: $\text{relIso} < 0.12$
 - muon veto: $p_T > 10 \text{ GeV}$, $\text{relIso} < 0.2$
 - Jet selection similar to electron channel
 - Signal and control samples: **2-jets 2-tags, 3-jets 2-tags, 2-jets 1-tag**
- **Same strategy for QCD estimation and signal extraction.**

Combined Results: Muon+Electron Channels at 8TeV

- ◆ The significance of the s-channel excess over the background is measured:

	Expected Significance	Observed Significance
8 TeV, electron	0.6	2.2
8 TeV, muon	0.8	1.7
8 TeV, muon +electron	0.8	2.3

- ◆ The single top cross section in the s-channel is measured to be:

$$\begin{array}{lll} \sigma_{s\text{-ch.}} = 16.8 \pm 9.1 \text{ pb}, & \beta_{\text{signal}} = 3.0 \pm 1.6 & \text{electron channel, 8TeV,} \\ \sigma_{s\text{-ch.}} = 11.7 \pm 7.5 \text{ pb}, & \beta_{\text{signal}} = 2.1 \pm 1.2 & \text{muon channel, 8TeV,} \\ \sigma_{s\text{-ch.}} = 13.4 \pm 7.3 \text{ pb}, & \beta_{\text{signal}} = 2.4 \pm 1.3 & \text{combined, 8TeV.} \end{array}$$

Combining the 8TeV and 7TeV Analyses



Muon Analysis, 7TeV

- SM prediction at 7TeV: $\sigma_{s\text{-channel}} = 4.56 \pm 0.07^{+0.18}_{-0.17} \text{ pb}$
- The measurement is based on the full 2011 single muon dataset at 7TeV corresponding to an integrated luminosity of 5.1 fb^{-1}
- Event selection:
 - HLT Path:
 - HLT_IsoMu17_v* in first period of data taking
 - HLT_IsoMu17_CentralJet30_BtagIP_v* in second period of data taking
 - HLT_IsoMu17_eta2p1_CentralJet30_BtagIP_v*,
 - Muon selection: PF muon, IsGlobal muon and IsTrackerMuon
 - $p_T > 20 \text{ GeV}$, $|\eta| < 2.1$ - PF relIso < 0.15
 - muon veto: $p_T > 10 \text{ GeV}$, relIso < 0.2
 - Jet selection is similar to 8TeV
 - B-tagging: Track Counting High Purity
- Strategy for the QCD estimation: fit to the m_T distribution (not enough statistics to train BDT)

Combined Results: 7+8TeV

- The **significance** of the s-channel excess over the background is measured:

	Expected Significance	Observed Significance
8 TeV, muon +electron	0.8	2.3
7 TeV, muon	0.5	0.9
7 + 8 TeV	1.1	2.5

- Observed and expected **upper limits (UL)** on cross section is measured:

	Expected UL	Observed UL
8 TeV, muon +electron	20.5 [13.4, 26.7] pb	28.8 pb
7 TeV, muon	25.4 [19.0, 36.6] pb	31.4 pb
7 + 8 TeV	3.1 [2.1, 4.0]	4.7

last row: the upper limits on the rate relative to the SM expectation is given.

- The single top **cross section** in the s-channel is measured to be

$$\begin{aligned}
 \sigma_{\text{s-ch.}} &= 13.4 \pm 7.3 \text{ pb}, & \beta_{\text{signal}} &= 2.4 \pm 1.3 & \text{combined, 8TeV,} \\
 \sigma_{\text{s-ch.}} &= 7.1 \pm 8.1 \text{ pb}, & \beta_{\text{signal}} &= 1.5 \pm 1.8 & \text{muon channel 7TeV,} \\
 & & \beta_{\text{signal}} &= 2.0 \pm 0.9 & \text{combined, 7+8TeV}
 \end{aligned}$$

Relative Impact of Systematic Uncertainties

- ◆ The measurement is limited with the systematics uncertainty.

Source	Uncertainty (%)				
	$\mu, 7 \text{ TeV}$	$\mu, 8 \text{ TeV}$	$e, 8 \text{ TeV}$	$\mu + e, 8 \text{ TeV}$	$7 + 8 \text{ TeV}$
Statistical	34	15	14	10	11
$t\bar{t}$, single top quark rate	29	15	14	12	14
W/Z+jets, diboson rate	23	11	13	12	12
multijet rate	9	3	5	2	2
Lepton efficiency	14	1	2	1	3
Hadronic trigger	5	-	-	-	1
Luminosity	10	5	6	4	6
JER & JES	66	39	29	34	18
b tagging & mistag	34	15	14	14	16
Pileup	6	11	7	9	7
Unclustered \cancel{E}_T	5	8	2	6	5
μ_R, μ_F scales	54	34	31	30	28
Matching thresholds	43	11	12	7	17
PDF	12	8	7	7	9
Top quark p_T reweighting	3	5	7	6	6
Total uncertainty	115	64	54	55	47

Conclusion

- ✓ The observed significance of the combined measurement is 2.5 standard deviations with 1.1 standard deviations expected.
- ✓ The observed and expected upper limits on the combined signal strength at 95% confidence level are found to be 4.7 and 3.1, respectively.