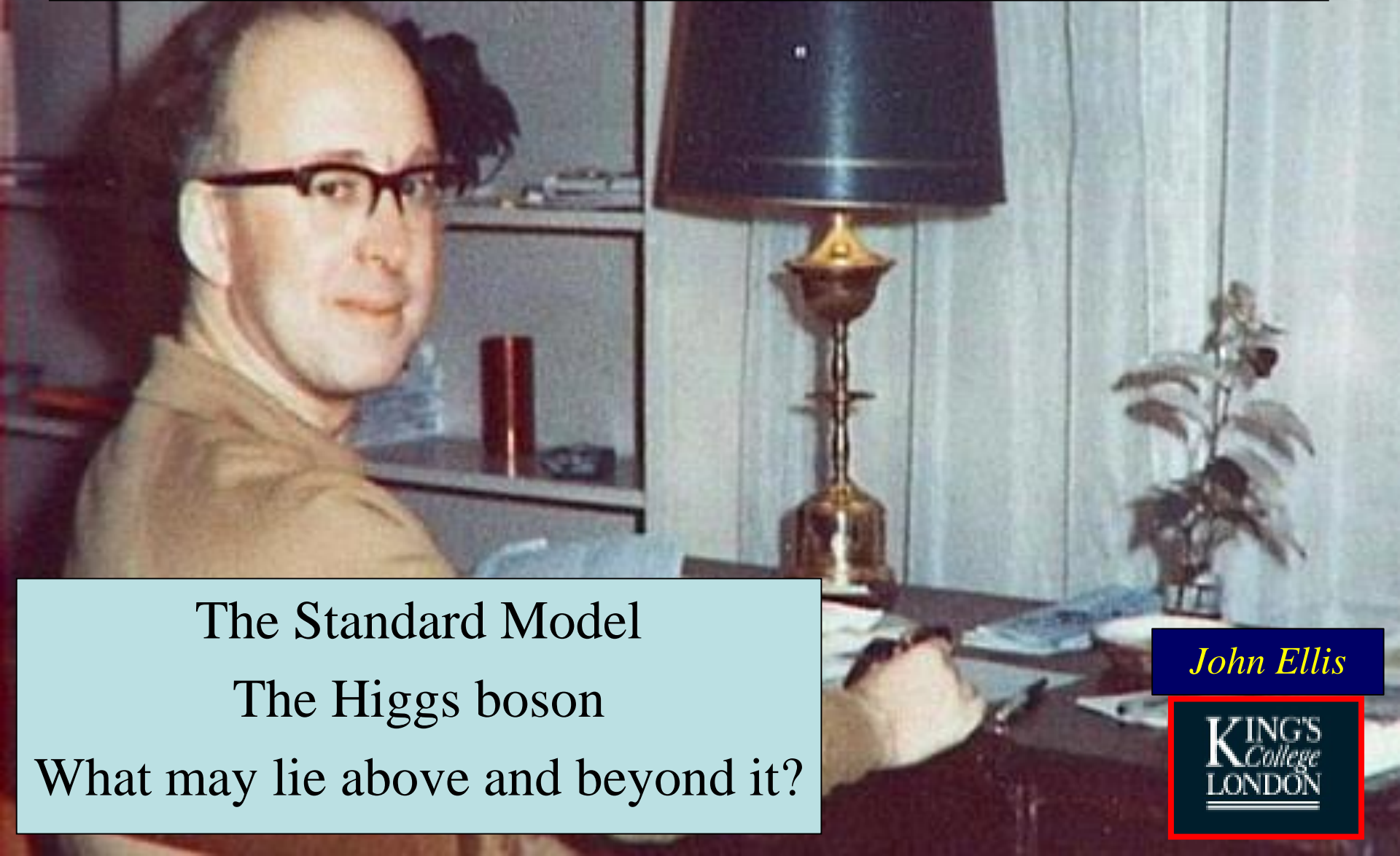


Introduction to Higgs & Beyond



The Standard Model

The Higgs boson

What may lie above and beyond it?

John Ellis

KING'S
College
LONDON

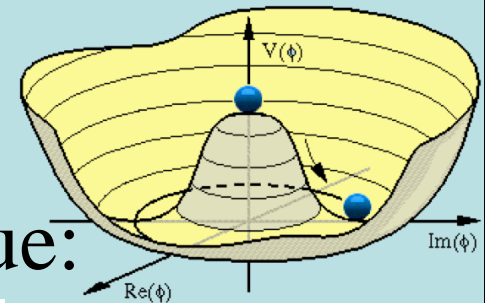
The Brout-Englert- Higgs Mechanism

- Postulated effective potential:

$$V[\phi] = -\mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2$$

- Minimum energy at non-zero value:

$$\phi_0 = \langle 0 | \phi | 0 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ +v \end{pmatrix} \quad v = \sqrt{\frac{-\mu^2}{\lambda}}$$



- Components of Higgs field: $\phi(x) = \frac{1}{\sqrt{2}}(v + \sigma(x))e^{i\pi(x)}$

- π massless, σ massive: $m_H^2 = 2\mu^2 = 2\lambda v$ **Higgs boson**

- After gauging: $M_W = \frac{g v}{2}$ **Massive gauge boson**

- Couple to fermions: non-zero masses: $M_f = y_f \frac{v}{\sqrt{2}}$

Summary of the Standard Model

- Particles and $SU(3) \times SU(2) \times U(1)$ quantum numbers:

L_L E_R	$\begin{pmatrix} \nu_e \\ e^- \end{pmatrix}_L, \begin{pmatrix} \nu_\mu \\ \mu^- \end{pmatrix}_L, \begin{pmatrix} \nu_\tau \\ \tau^- \end{pmatrix}_L$ e_R^-, μ_R^-, τ_R^-	$(1,2,-1)$ $(1,1,-2)$
Q_L U_R D_R	$\begin{pmatrix} u \\ d \end{pmatrix}_L, \begin{pmatrix} c \\ s \end{pmatrix}_L, \begin{pmatrix} t \\ b \end{pmatrix}_L$ u_R, c_R, t_R d_R, s_R, b_R	$(3,2,+1/3)$ $(3,1,+4/3)$ $(3,1,-2/3)$

- Lagrangian: $\mathcal{L} = -\frac{1}{4} F_{\mu\nu}^a F^{a\ \mu\nu}$ gauge interactions
 $+ i\bar{\psi} \not{D}\psi + h.c.$ matter fermions
 $+ \psi_i y_{ij} \psi_j \phi + h.c.$ Yukawa interactions
 $+ |D_\mu \phi|^2 - V(\phi)$ Higgs potential

Untested
before 2012

1975

A Phenomenological Profile of the Higgs Boson

- First attempt at systematic survey

A PHENOMENOLOGICAL PROFILE OF THE HIGGS BOSON

John ELLIS, Mary K. GAILLARD * and D.V. NANOPOULOS **
CERN, Geneva

Received 7 November 1975

A discussion is given of the production, decay and observability of the scalar Higgs boson H expected in gauge theories of the weak and electromagnetic interactions such as the Weinberg-Salam model. After reviewing previous experimental limits on the mass of

We should perhaps finish with an apology and a caution. We apologize to experimentalists for having no idea what is the mass of the Higgs boson, unlike the case with charm [3,4] and for not being sure of its couplings to other particles, except that they are probably all very small. For these reasons we do not want to encourage big experimental searches for the Higgs boson, but we do feel that people performing experiments vulnerable to the Higgs boson should know how it may turn up.

1984

A Preview of the Higgs Boson @ LHC

- Prepared for LHC Lausanne workshop 1984

DEUTSCHES ELEKTRONEN-SYNCHROTRON DESY

DESY 84-071
August 1984
CERN-TH-3943/84

NEW PARTICLES AND THEIR EXPERIMENTAL SIGNATURES

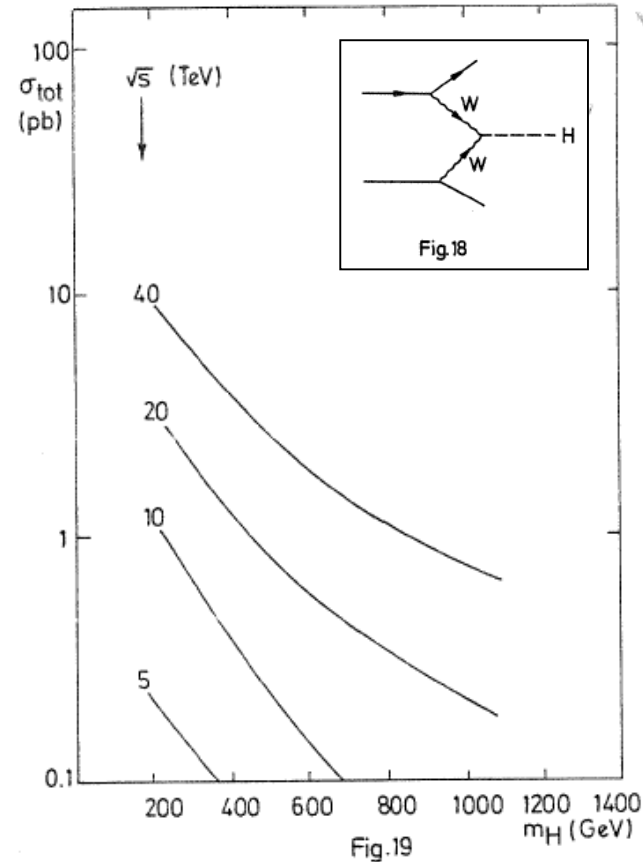
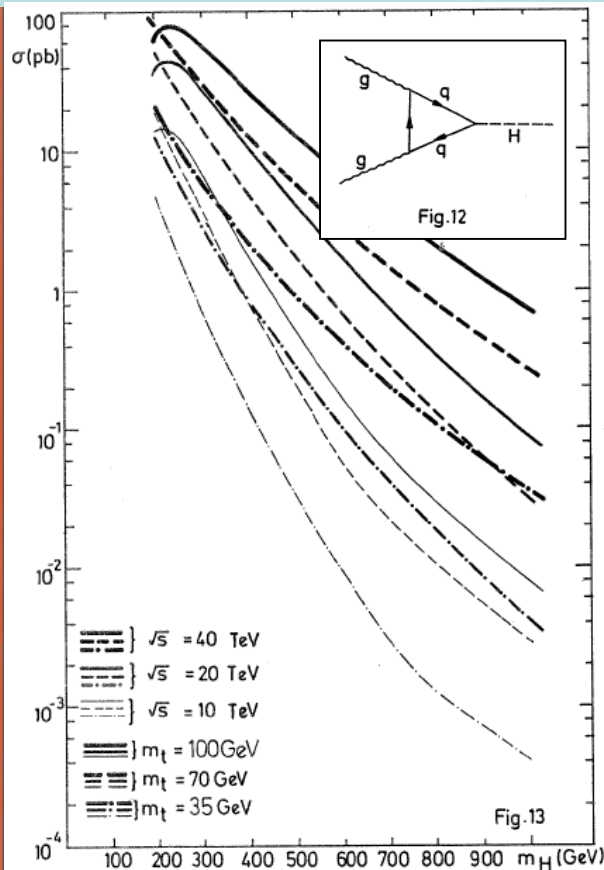
by

J. Ellis and G. Gelmini
CERN, Geneva

H. Kowalski
Deutsches Elektronen-Synchrotron DESY, Hamburg

ISSN 0418-9833

NOTKESTRASSE 85 · 2 HAMBURG 52



Constraints on Higgs Mass

- Electroweak observables sensitive via quantum loop corrections:

$$m_W^2 \sin^2 \theta_W = m_Z^2 \cos^2 \theta_W \sin^2 \theta_W = \frac{\pi\alpha}{\sqrt{2}G_F}(1 + \Delta r)$$

- Sensitivity to top, Higgs masses:

$$\frac{3G_F}{8\pi^2\sqrt{2}}m_t^2$$

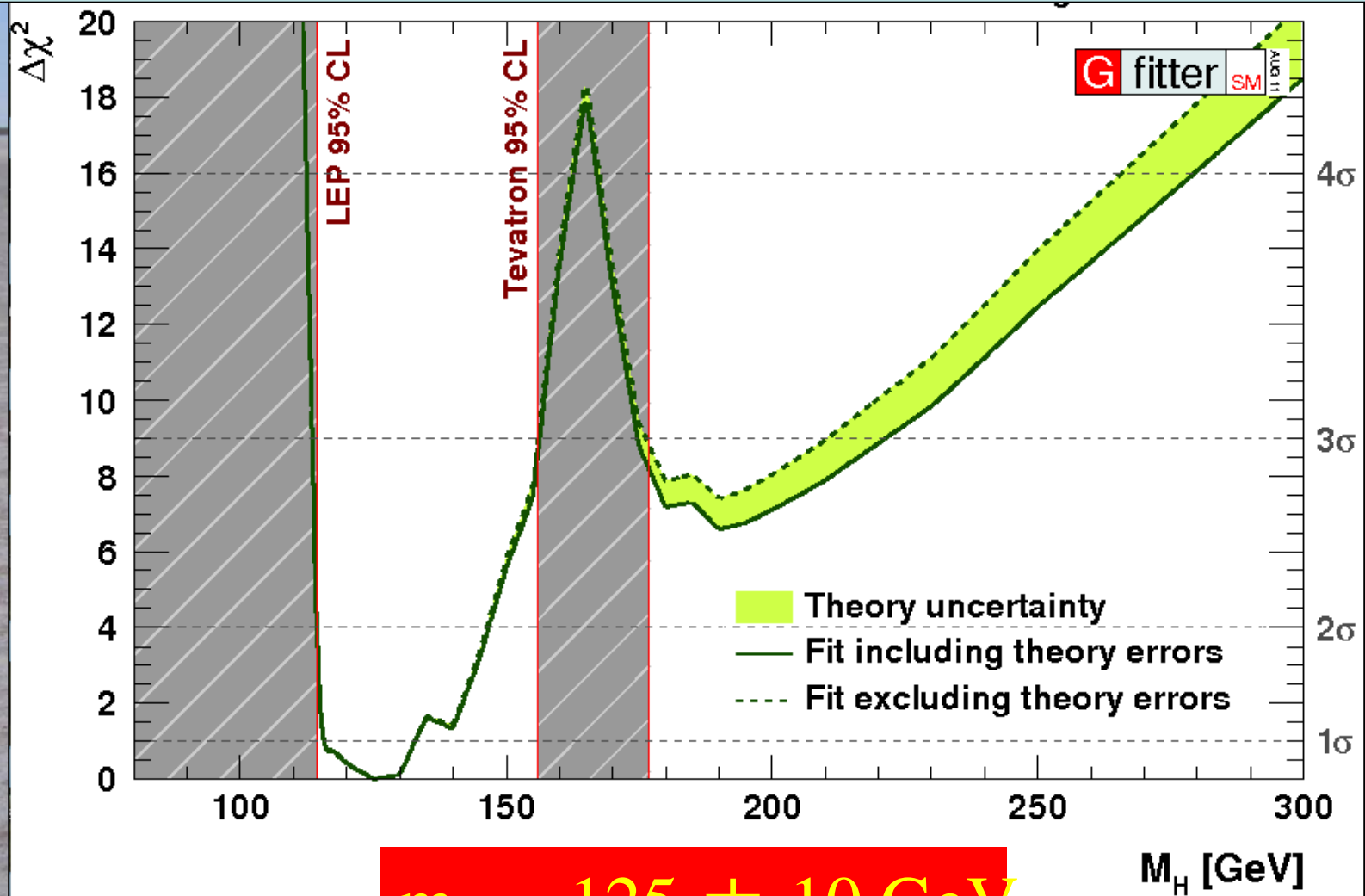
$$\frac{\sqrt{2}G_F}{16\pi^2}m_W^2\left(\frac{11}{3}\ln\frac{M_H^2}{m_Z^2} + \dots\right), M_H \gg m_W$$

- Preferred Higgs mass: **$m_H \sim 100 \pm 30 \text{ GeV}$**
- Compare with lower limit from direct search at LEP:

$$\mathbf{m_H > 114 \text{ GeV}}$$

and exclusion around **(160, 170 GeV)** at TeVatron

2011: Combining Information from Previous Direct Searches and Indirect Data

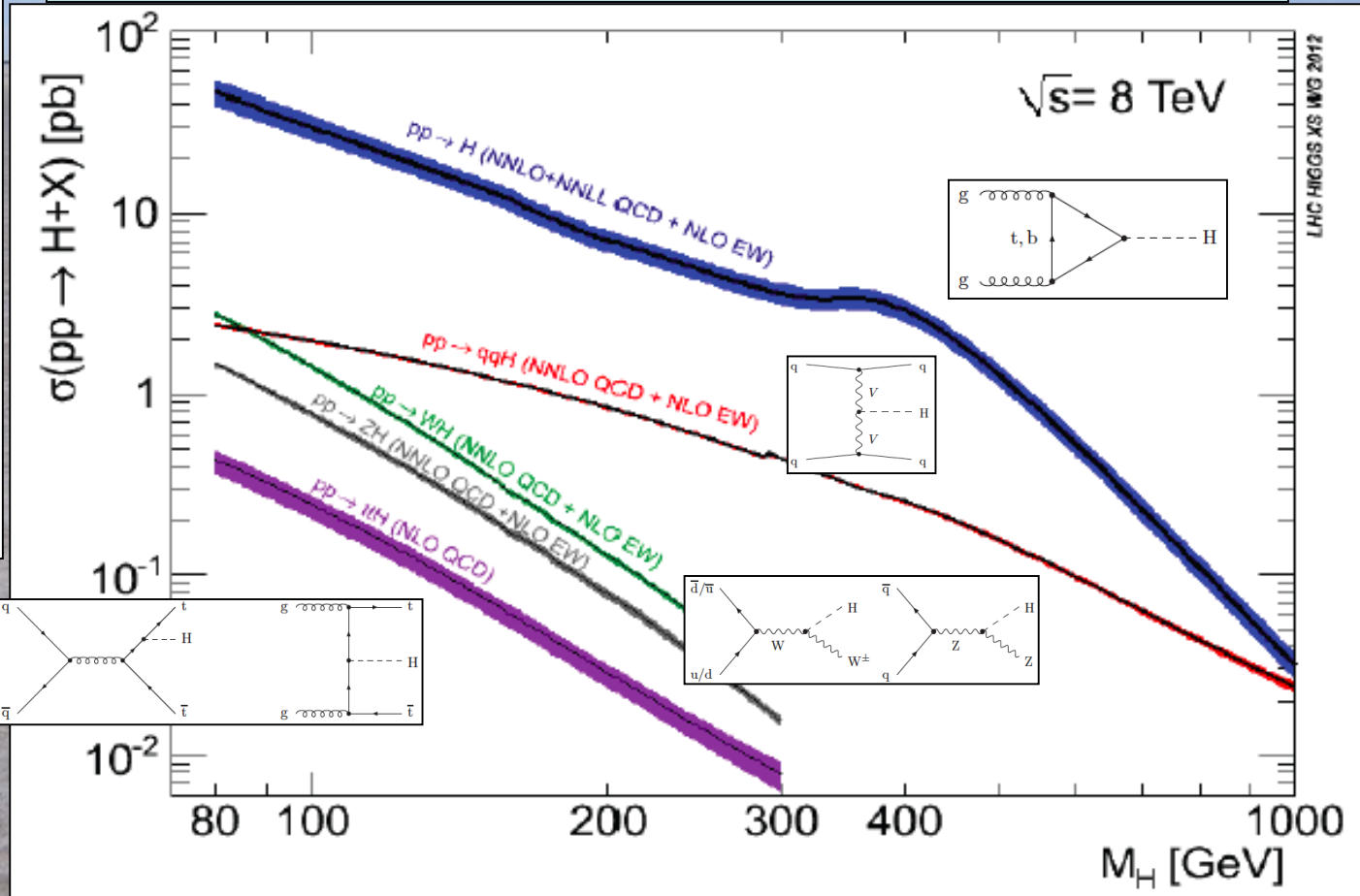
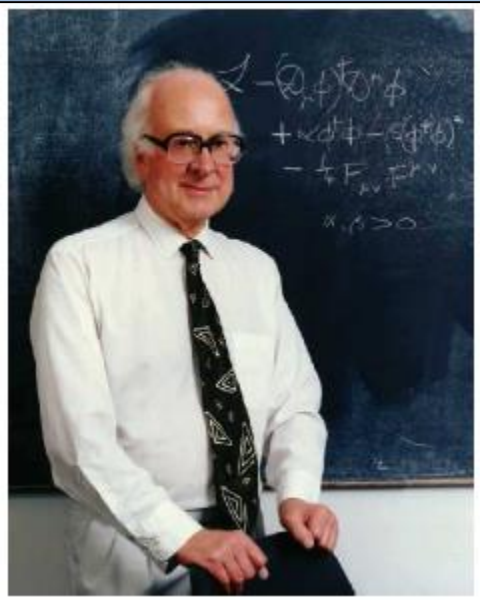


$m_H = 125 \pm 10 \text{ GeV}$

Gfitter collaboration

A la recherche
du
Higgs perdu ...

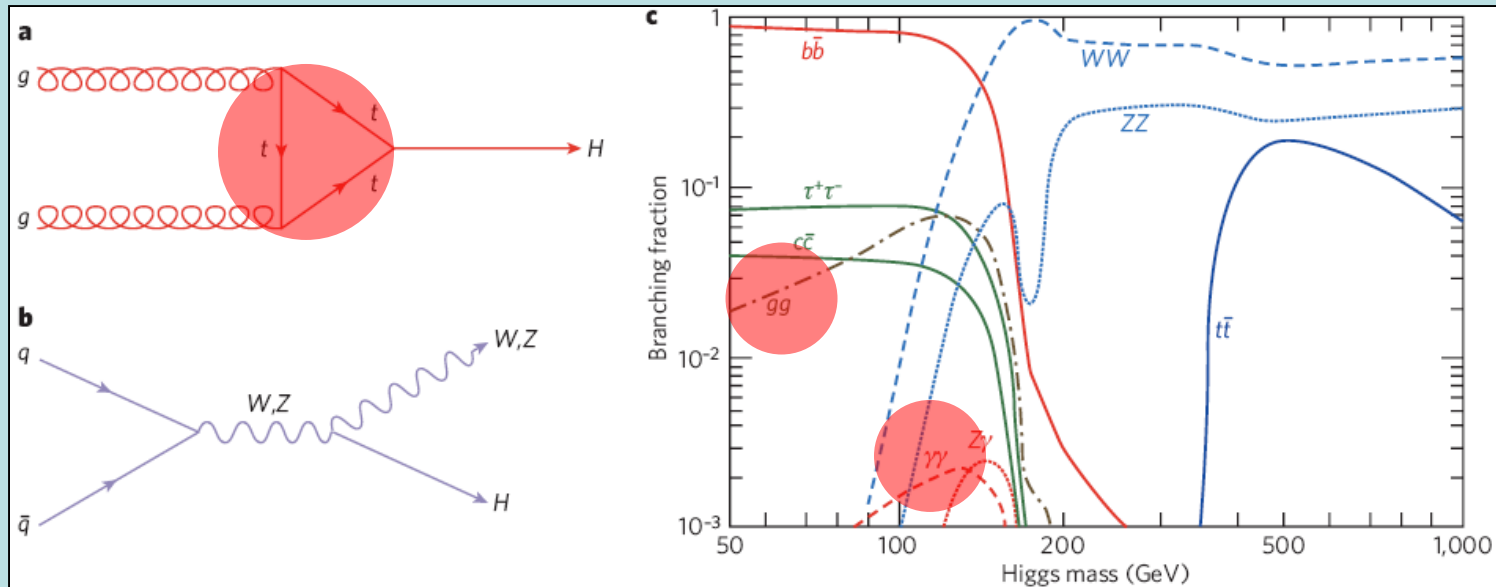
Higgs Production at the LHC



Many production modes measurable if $M_h \sim 125 \text{ GeV}$

Higgs Decay Branching Ratios

- Couplings proportional to masses (?)

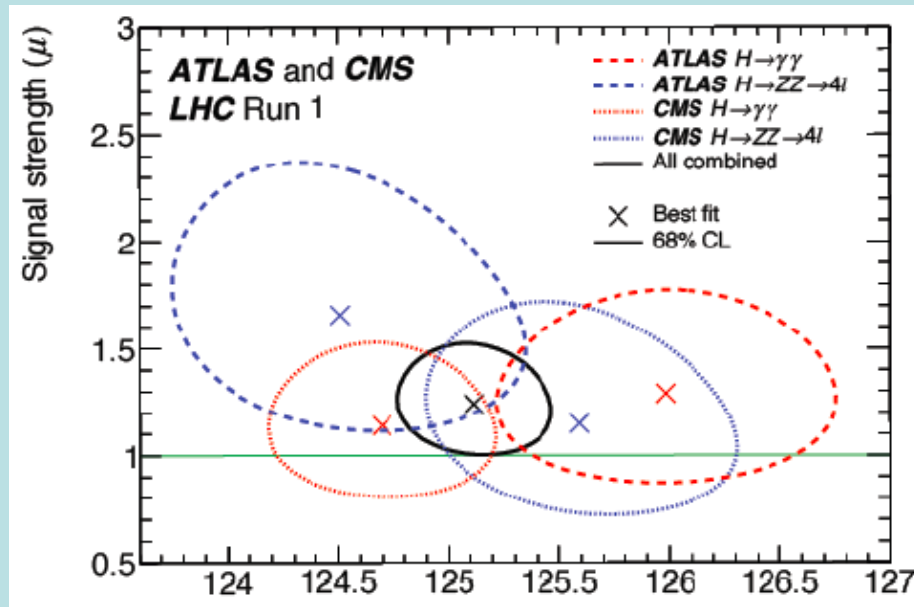


- Important couplings through loops:
 - gluon + gluon \rightarrow Higgs \rightarrow $\gamma\gamma$

Many decay modes measurable if $M_h \sim 125$ GeV

Higgs Mass Measurements

- ATLAS + CMS ZZ^* and $\gamma\gamma$ final states



125.09 ± 0.21 (stat) ± 0.11 (syst)

- Statistical uncertainties dominate
- Allows precision tests
- **Crucial for stability of electroweak vacuum**

The Particle Higgsaw Puzzle

The background of the slide is a blue gradient with a pattern of interlocking puzzle pieces. In the center, one puzzle piece is missing, revealing a white surface underneath. The missing piece is highlighted by a bright blue beam of light that originates from the top of the slide and points down towards the gap.

Did LHC find the missing piece?

Is it the right shape?

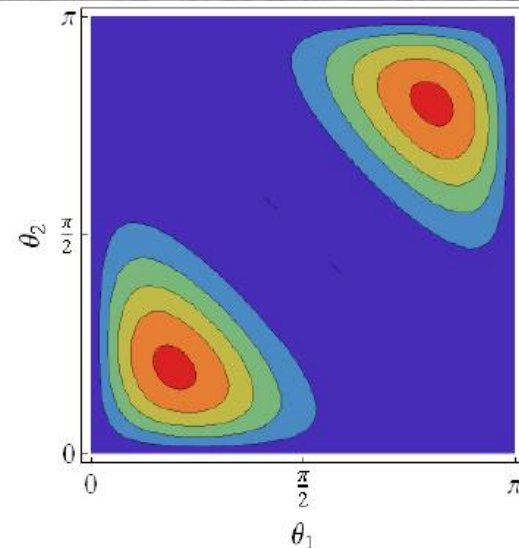
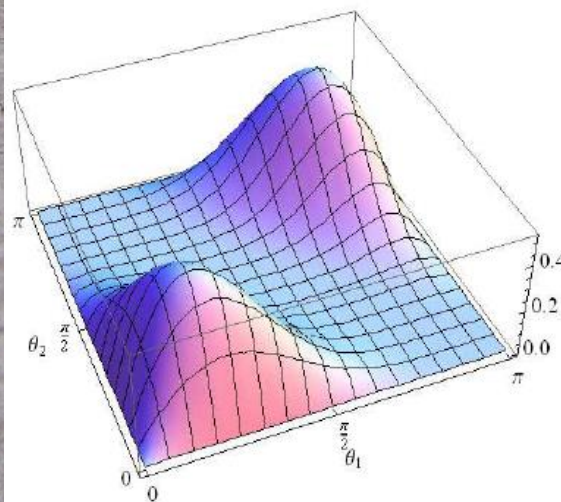
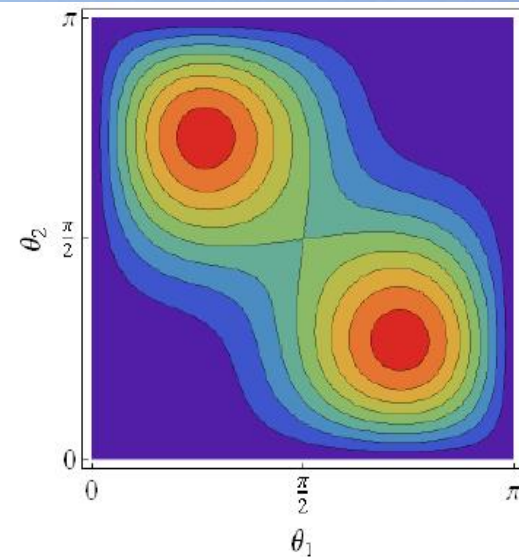
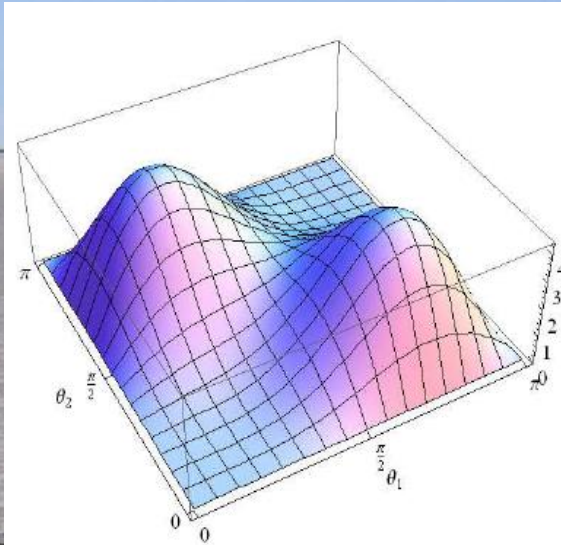
Is it the right size?

What is it ?

- Does it have spin 0 or 2?
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- Quantum (loop) corrections?
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Does the 'Higgs' have Spin Zero ?

- Polar angle distribution for $X_2 \rightarrow W^+W^-$
- Polar angle distribution for $X_0 \rightarrow W^+W^-$
(for $\varphi = \pi$)



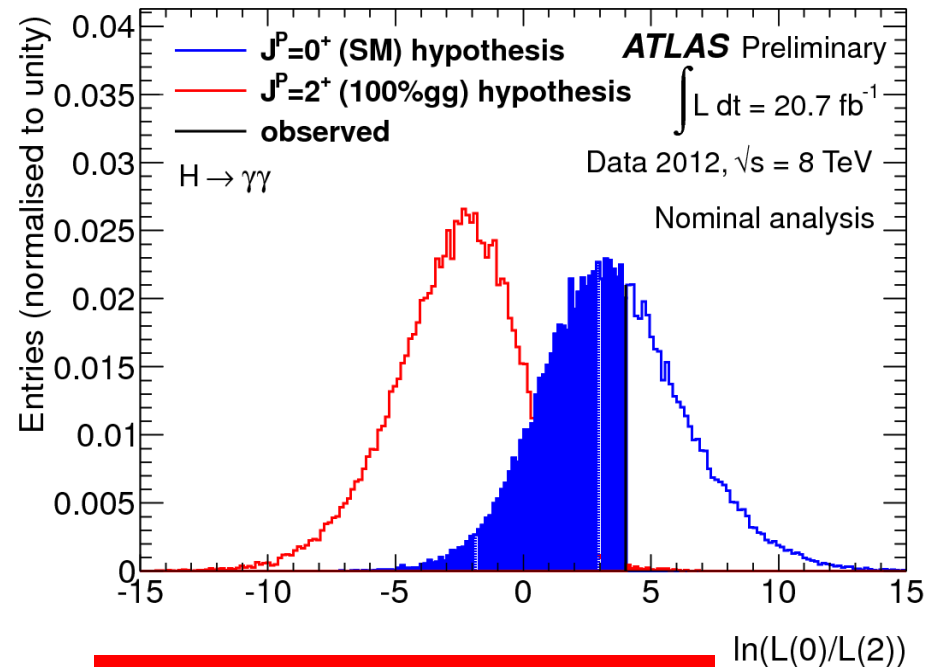
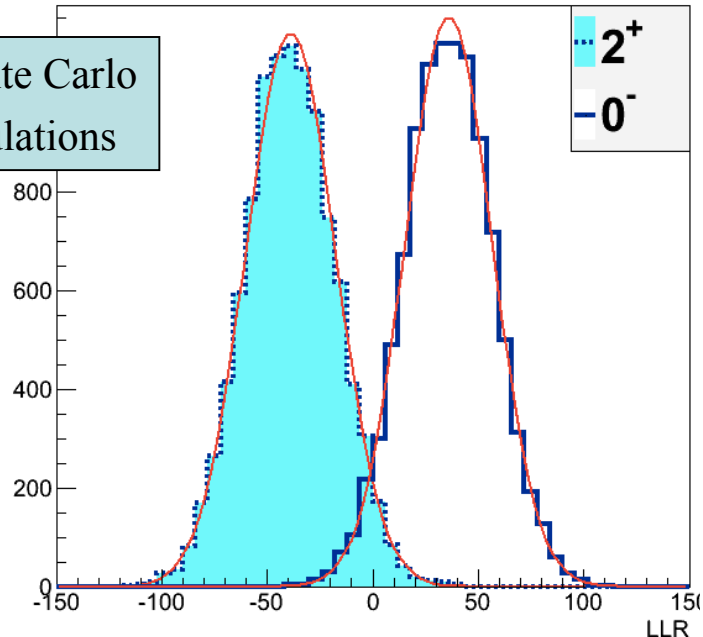
Does the 'Higgs' have Spin Two ?

- Discriminate spin 2 vs spin 0 via angular distribution of decays into $\gamma\gamma$

JE & Hwang: arXiv:1202.6660

$N_{\text{sig}}=160$, High S/B

Monte Carlo simulations

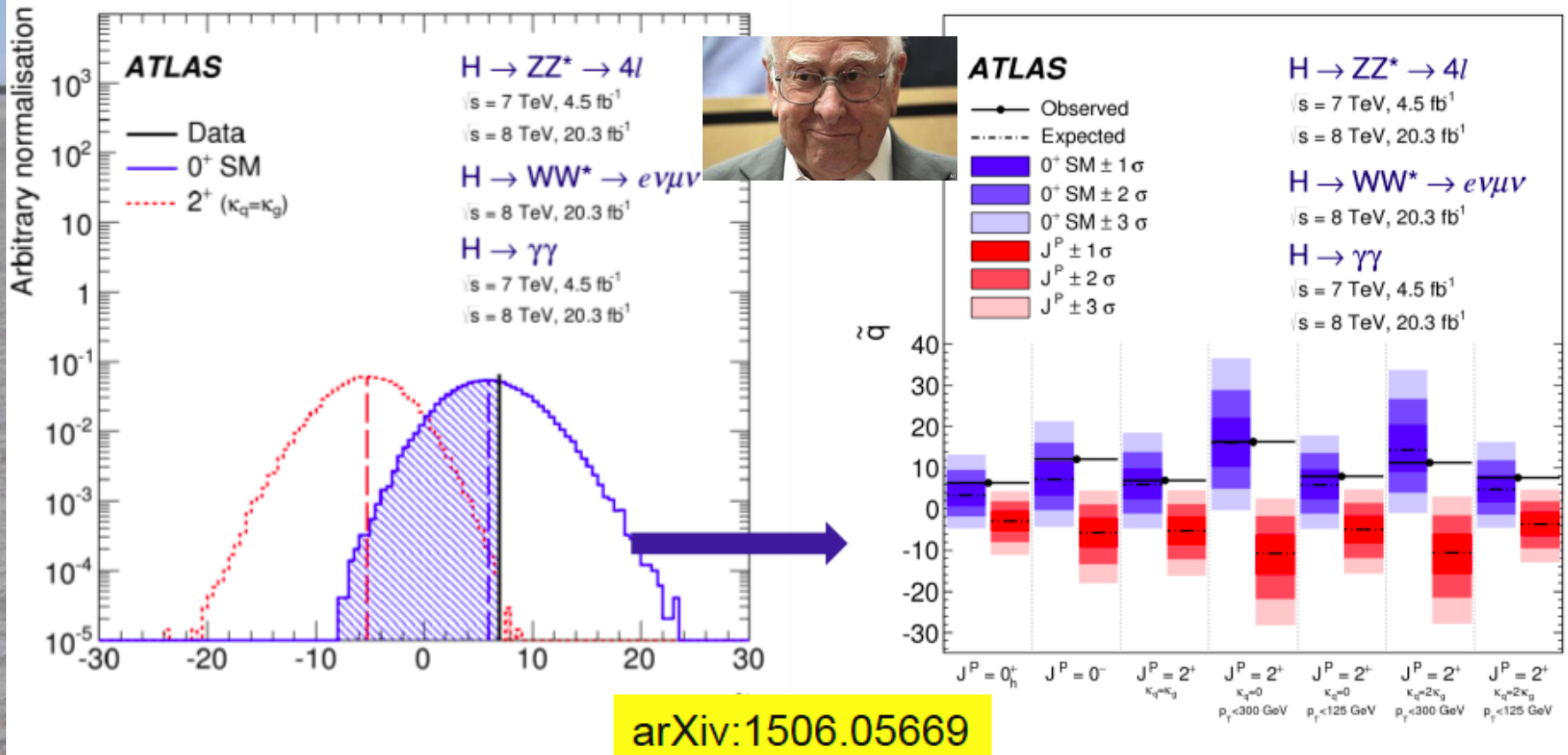


JE, Fok, Hwang, Sanz & You: arXiv:1210.5229

2^+ disfavoured @

99%

H Spin-Parity Tests: 0^+ AOK



- Alternative spin-parities disfavoured $> 99.9\%$

What is it ?

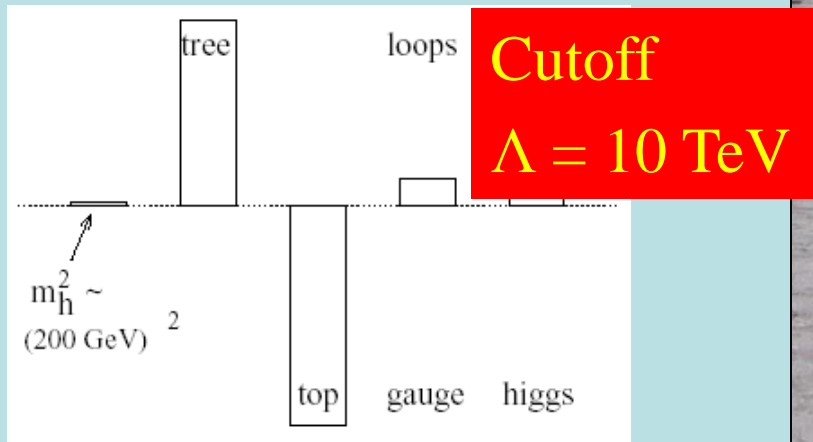
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Elementary Higgs or Composite?

- Higgs field:

$$\langle 0|H|0\rangle \neq 0$$

- Quantum loop problems



Cut-off $\Lambda \sim 1 \text{ TeV}$ with
Supersymmetry?

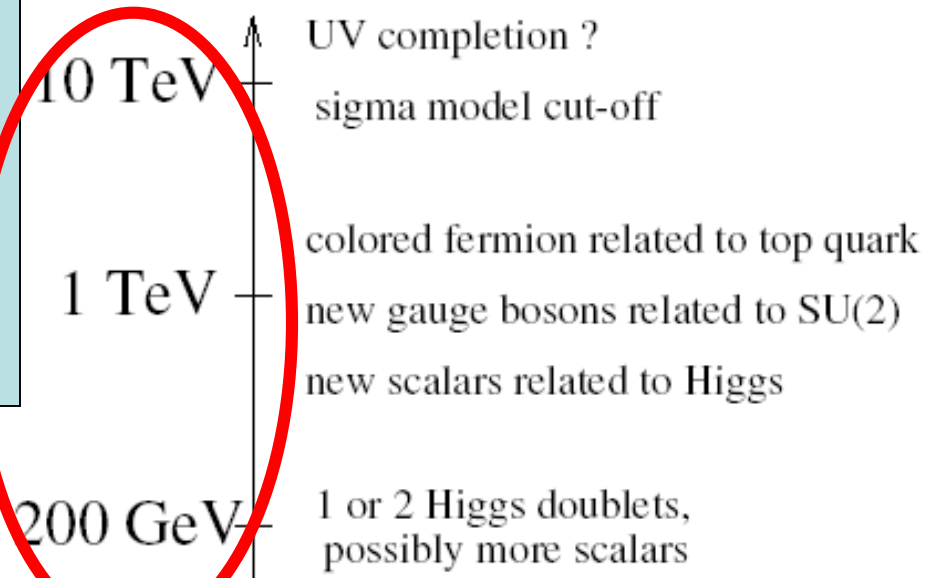
- Fermion-antifermion condensate
- Just like QCD, BCS superconductivity
- Top-antitop condensate? needed $m_t > 200 \text{ GeV}$

New technicolour force?

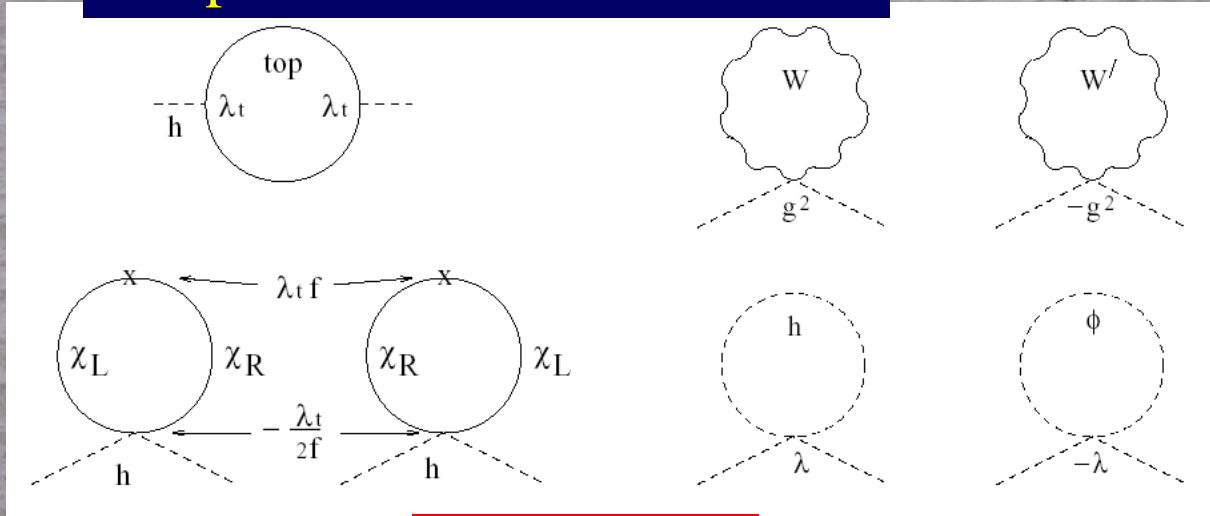
- Heavy scalar resonance?
- Inconsistent with precision electroweak data?

Higgs as a Pseudo-Goldstone Boson

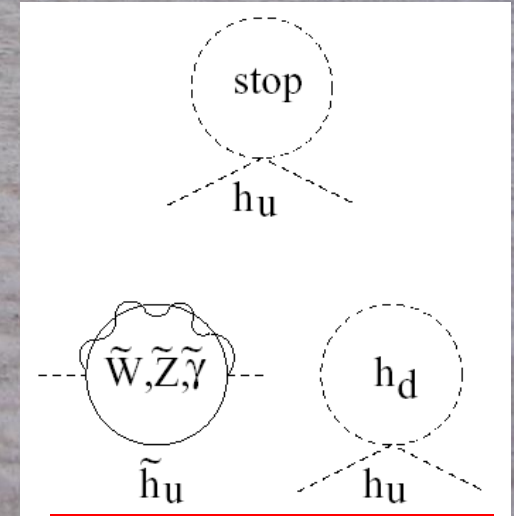
‘Little Higgs’ models
(breakdown of larger symmetry)



Loop cancellation mechanism



Little Higgs



Supersymmetry

Phenomenological Framework

- Assume custodial symmetry:

$$SU(2) \times SU(2) \rightarrow SU(2)_V \quad (\rho \equiv M_W/M_Z \cos \theta_w \sim 1)$$

- Parameterize gauge bosons by 2×2 matrix Σ :

$$\begin{aligned} \mathcal{L} = & \frac{v^2}{4} \text{Tr} D_\mu \Sigma^\dagger D^\mu \Sigma \left(1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} + \dots \right) - m_i \bar{\psi}_L^i \Sigma \left(1 + c \frac{h}{v} + \dots \right) \psi_R^i + \text{h.c.} \\ & + \frac{1}{2} (\partial_\mu h)^2 + \frac{1}{2} m_h^2 h^2 + d_3 \frac{1}{6} \left(\frac{3m_h^2}{v} \right) h^3 + d_4 \frac{1}{24} \left(\frac{3m_h^2}{v^2} \right) h^4 + \dots \quad , \end{aligned}$$

$$\Sigma = \exp \left(i \frac{\sigma^a \pi^a}{v} \right) \quad \mathcal{L}_\Delta = - \left[\frac{\alpha_s}{8\pi} b_s G_{a\mu\nu} G_a^{\mu\nu} + \frac{\alpha_{em}}{8\pi} b_{em} F_{\mu\nu} F^{\mu\nu} \right] \left(\frac{h}{V} \right)$$

- Coefficients $a = c = 1$ in Standard Model

Examples of Higgs as Pseudo-Goldstone Boson

- Sample models:
- Dependences of couplings on model parameters:
- **To be measured!**
- Translation to experimental parameters:

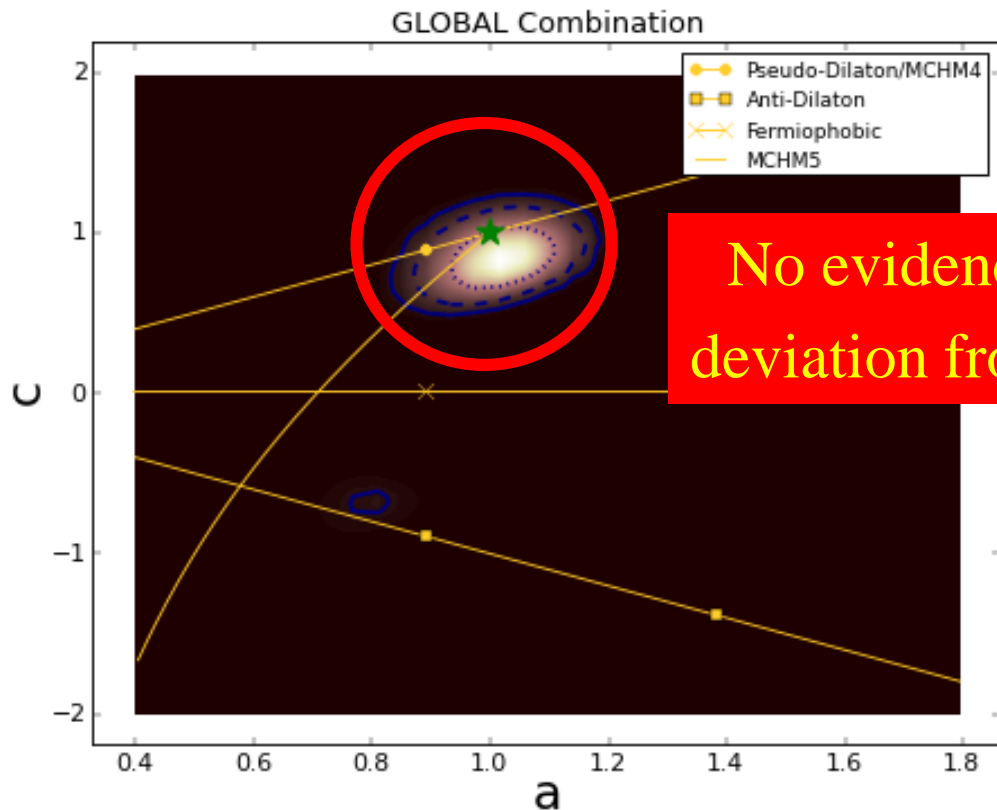
$$a = \kappa_V, \quad c = \kappa_F$$

Model	Symmetry Pattern	Goldstones	
SM	SO(4)/SO(3)	W_L, Z_L	
—	SU(3)/SU(2)×U(1)	W_L, Z_L, h	
MCHM	SO(5)/SO(4)×U(1)	W_L, Z_L, h	
NMCHM	SO(6)/SO(5)×U(1)	W_L, Z_L, h, a	
MCTHM	SO(6)/SO(4)×SO(2)×U(1)	W_L, Z_L, h, H, H^\pm, a	
Parameters	SILH	MCHM4	MCHM5
a	$1 - c_H \xi / 2$	$\sqrt{1 - \xi}$	$\sqrt{1 - \xi}$
b	$1 - 2c_H \xi$	$1 - 2\xi$	$1 - 2\xi$
b_3	$-\frac{4}{3}\xi$	$-\frac{4}{3}\xi \sqrt{1 - \xi}$	$-\frac{4}{3}\xi \sqrt{1 - \xi}$
c	$1 - (c_H/2 + c_y)\xi$	$\sqrt{1 - \xi}$	$\frac{1 - 2\xi}{\sqrt{1 - \xi}}$
c_2	$-(c_H + 3c_y)\xi/2$	$-\xi/2$	-2ξ
d_3	$1 + (c_6 - 3c_H/2)\xi$	$\sqrt{1 - \xi}$	$\frac{1 - 2\xi}{\sqrt{1 - \xi}}$
d_4	$1 + (6c_6 - 25c_H/3)\xi$	$1 - 7\xi/3$	$\frac{1 - 28\xi(1 - \xi)/3}{1 - \xi}$

Global Analysis of Higgs-like Models

- Rescale couplings: to bosons by a , to fermions by c

Global

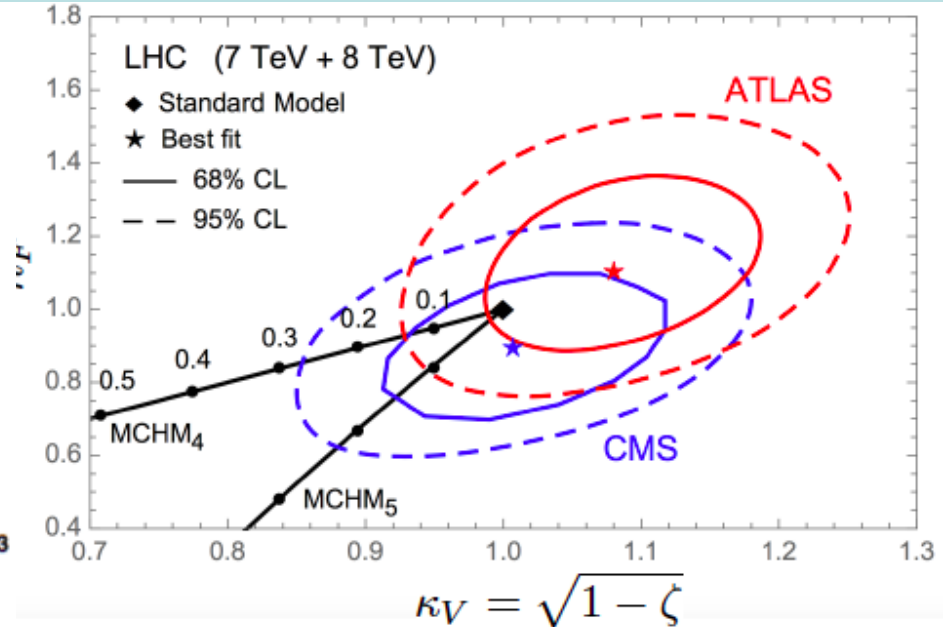
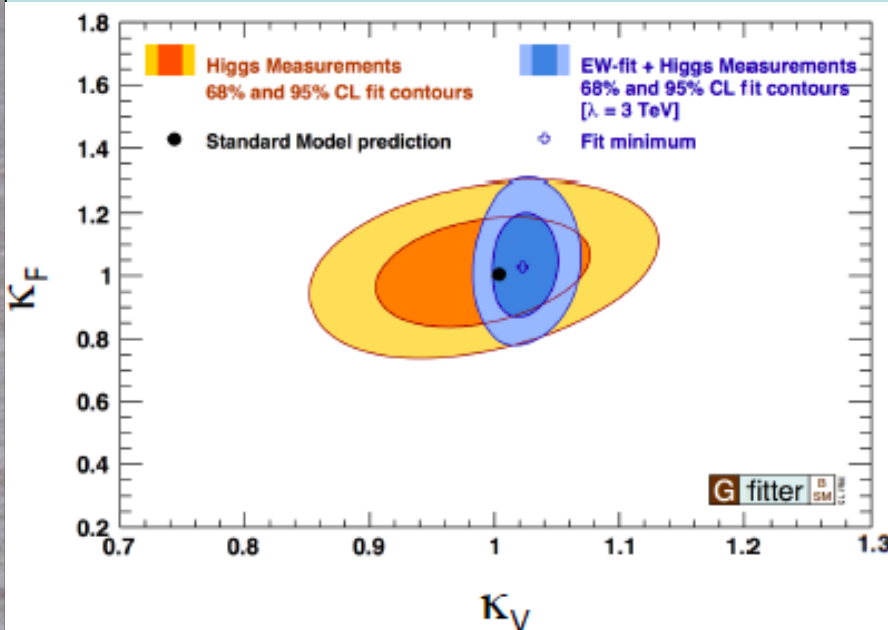


No evidence for deviation from SM

- Standard Model: $a = c = 1$

Global Analysis of Higgs-like Models

- Rescale couplings: to bosons by κ_V , to fermions by κ_f
- Standard Model: $\kappa_V = \kappa_f = 1$



- Consistency between Higgs and EW measurements
- **Must tune composite models to look like SM**

What is it ?

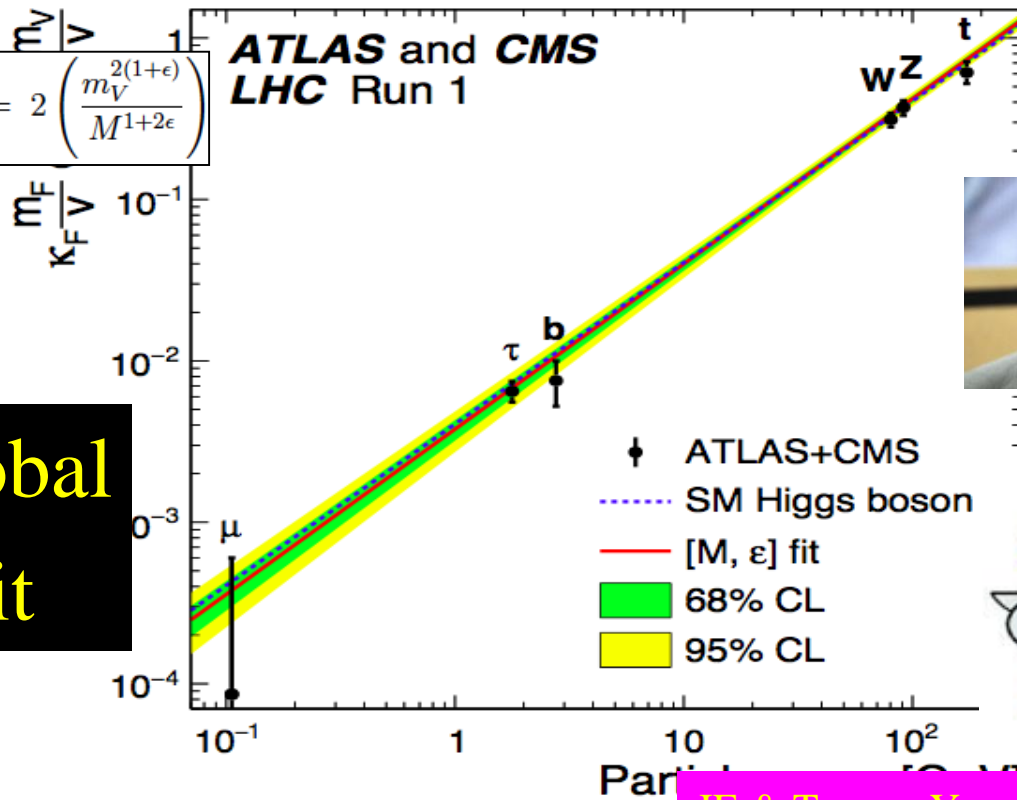
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- What are its self-couplings?

It Walks and Quacks like a Higgs

- Do couplings scale \sim mass? With scale = v ?

$$\lambda_f = \sqrt{2} \left(\frac{m_f}{M} \right)^{1+\epsilon}, \quad g_V = 2 \left(\frac{m_V^{2(1+\epsilon)}}{M^{1+2\epsilon}} \right)$$

**Global
fit**

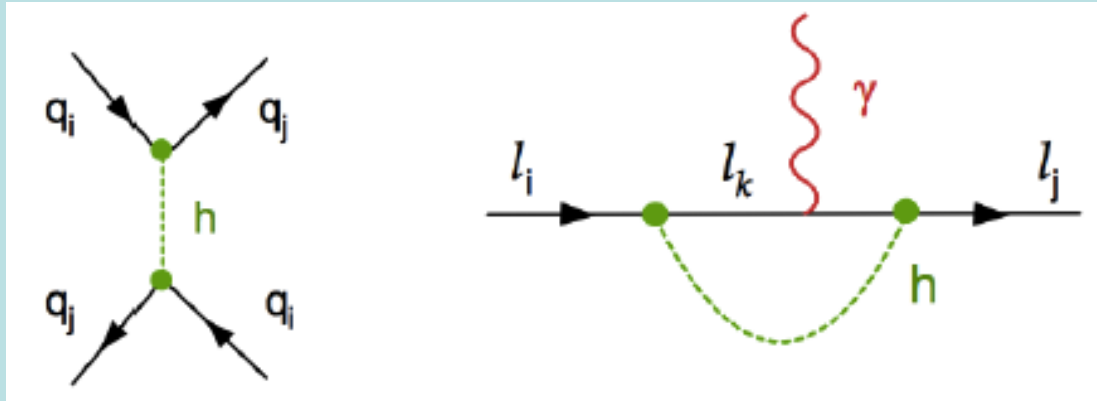


JE & Tevong You

- **Blue** dashed line = Standard Model

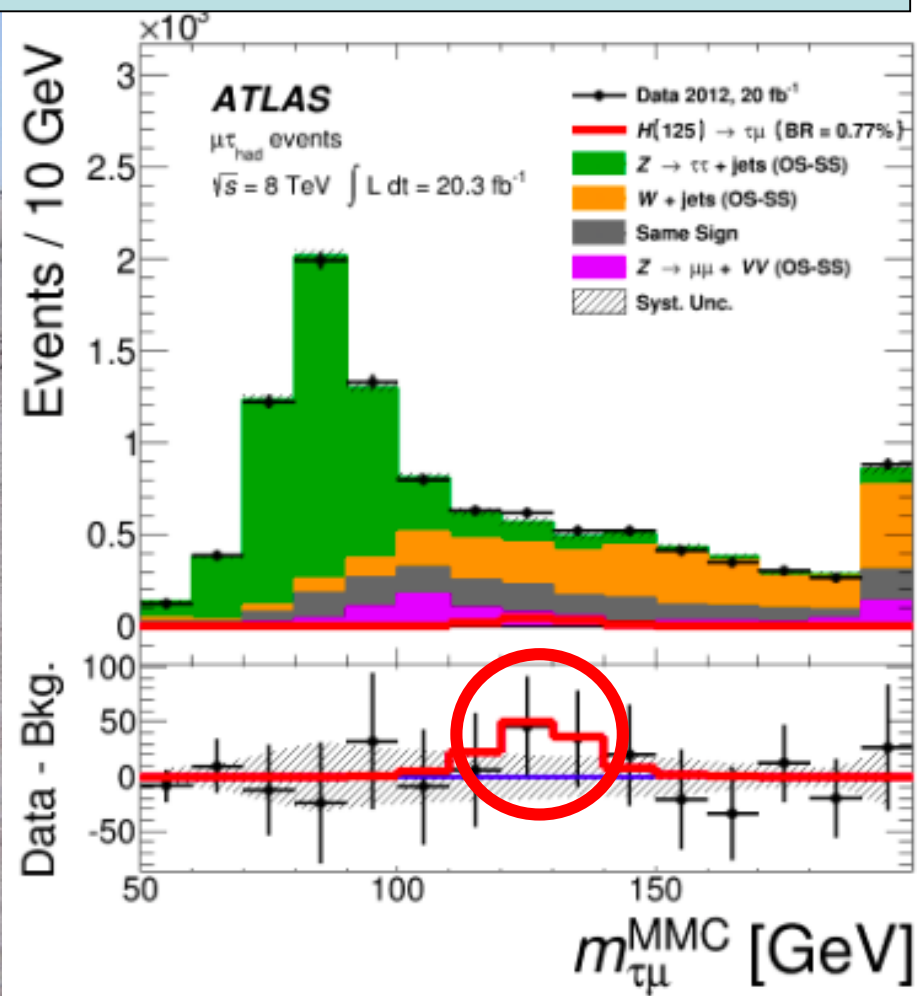
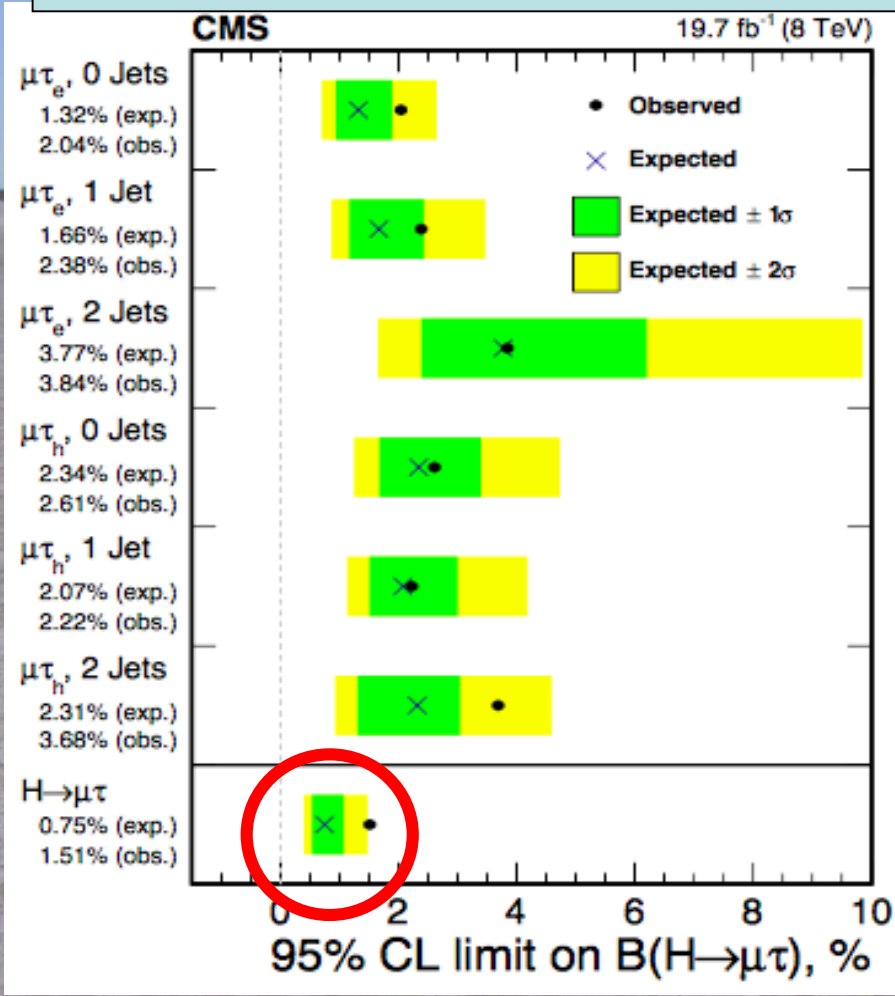
Flavour-Changing Couplings?

- Upper limits from FCNC, EDMs, ...



- Quark FCNC bounds exclude observability of quark-flavour-violating h decays
- Lepton-flavour-violating h decays could be large:
 $BR(\tau\mu)$ or $BR(\tau e)$ could be $O(10)\%$

Flavour-Changing Higgs Coupling?

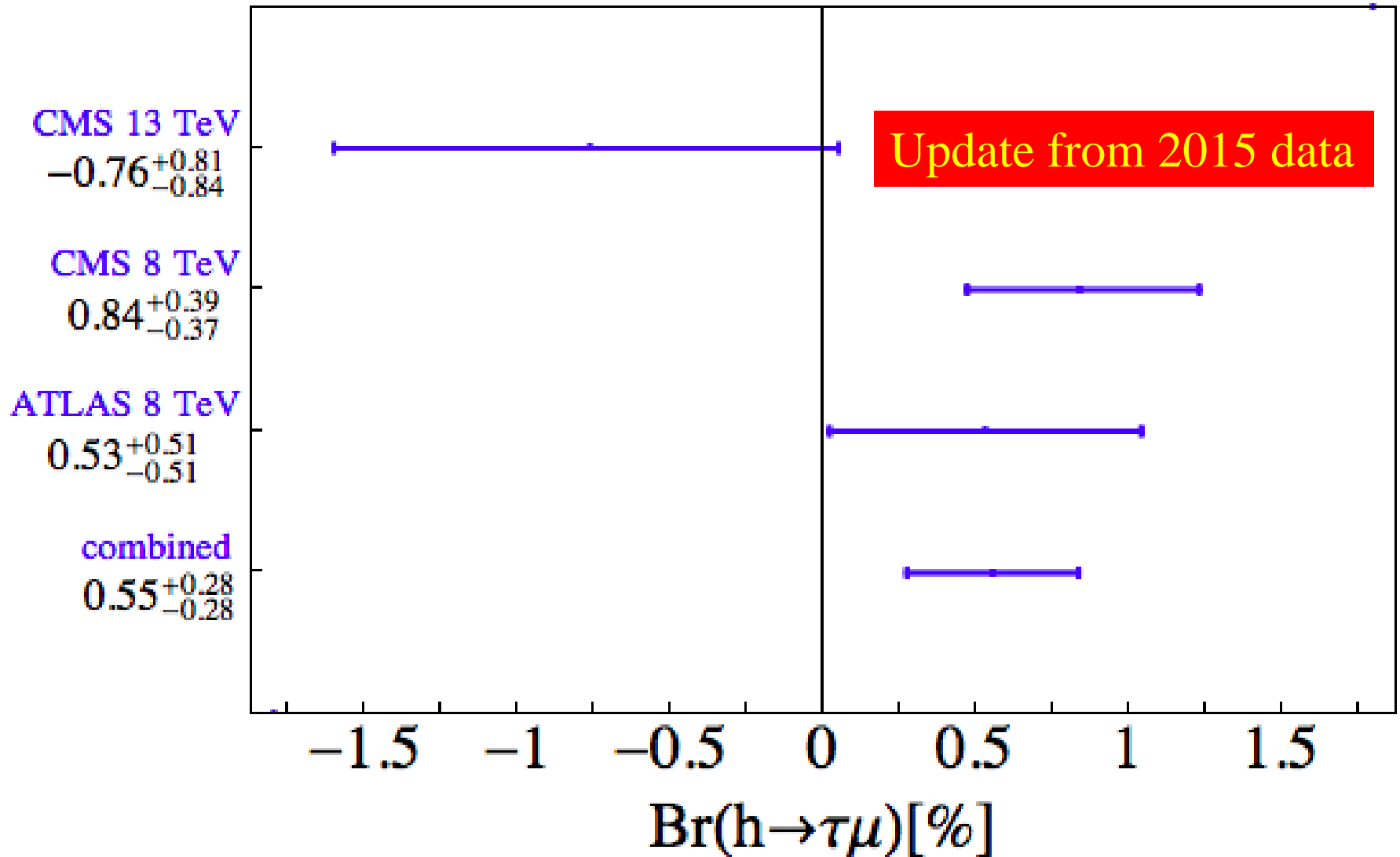


$$B(H \rightarrow \mu\tau) = (0.84^{+0.39}_{-0.37})\%$$

$$Br(H \rightarrow \mu\tau) = (0.77 \pm 0.62)\%$$

Also: $BR(e\tau) < 0.69\%$, $BR(e\mu) < 0.036\%$

Flavour-Changing Higgs Coupling?



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 - ***Prima facie* evidence that it does**
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- What are its self-couplings?

Triangle Diagrams for $gg \rightarrow \text{Spin-0} \rightarrow \gamma\gamma$

- Effective vertices:
$$\mathcal{L}_{\text{eff}}^H = \frac{e}{v} c_{H\gamma\gamma} H F_{\mu\nu} F^{\mu\nu} + \frac{g_s}{v} c_{Hgg} H G_{\mu\nu} G^{\mu\nu}$$
$$\mathcal{L}_{\text{eff}}^A = \frac{e}{v} c_{A\gamma\gamma} A F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{g_s}{v} c_{Agg} A G_{\mu\nu} \tilde{G}^{\mu\nu},$$

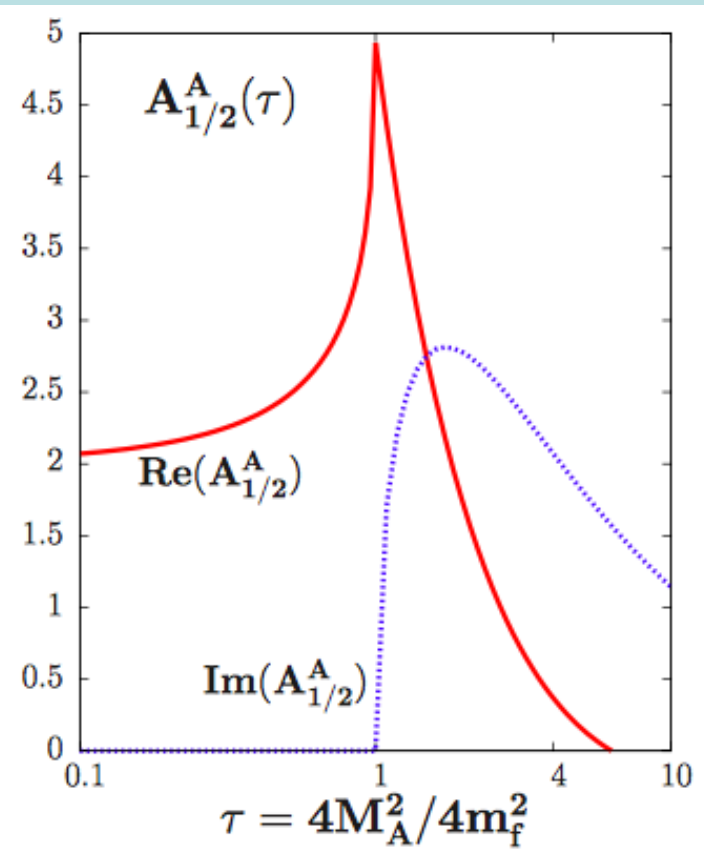
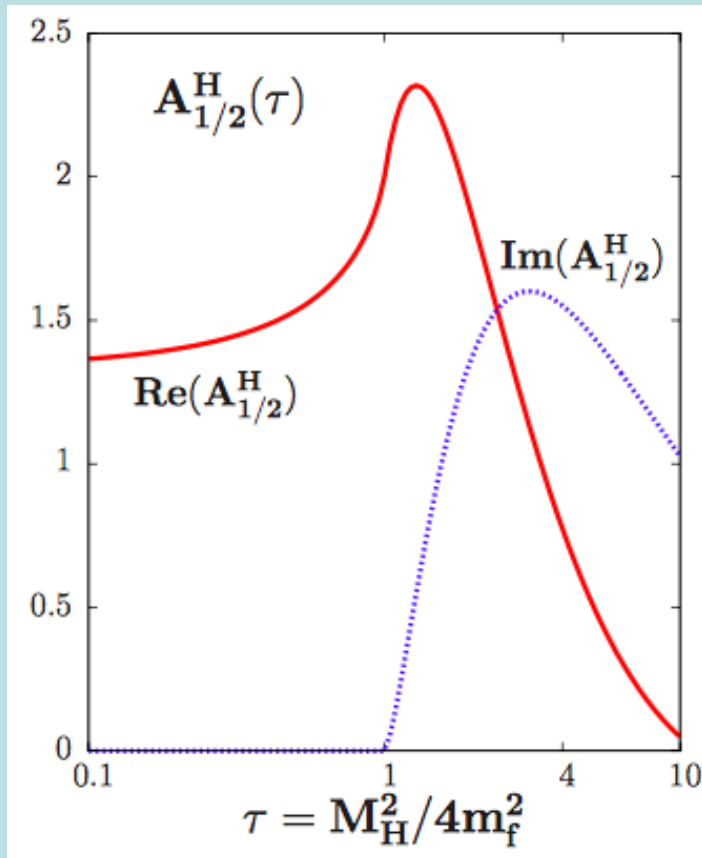
- Decay rates:
$$\Gamma(\Phi \rightarrow gg) = \frac{G_\mu \alpha_s^2 M_\Phi^3}{64\sqrt{2}\pi^3} \left| \sum_Q \hat{g}_{\Phi QQ} A_{1/2}^\Phi(\tau_Q) \right|^2,$$
$$\Gamma(\Phi \rightarrow \gamma\gamma) = \frac{G_\mu \alpha^2 M_\Phi^3}{128\sqrt{2}\pi^3} \left| \sum_F \hat{g}_{\Phi FF} N_c e_F^2 A_{1/2}^\Phi(\tau_F) \right|^2$$

- Vertex form factors:
$$A_{1/2}^H(\tau) = 2 [\tau + (\tau - 1)f(\tau)] \tau^{-2}, \quad A_{1/2}^A(\tau) = 2\tau^{-1} f(\tau)$$
$$f(\tau) = \begin{cases} \arcsin^2 \sqrt{\tau} & \text{for } \tau \leq 1, \\ -\frac{1}{4} \left[\log \frac{1 + \sqrt{1 - \tau^{-1}}}{1 - \sqrt{1 - \tau^{-1}}} - i\pi \right]^2 & \text{for } \tau > 1. \end{cases}$$

- Vanish for fermion mass \ll spin-0 mass

Triangle Diagrams for $gg \rightarrow \text{Spin-0} \rightarrow \gamma\gamma$

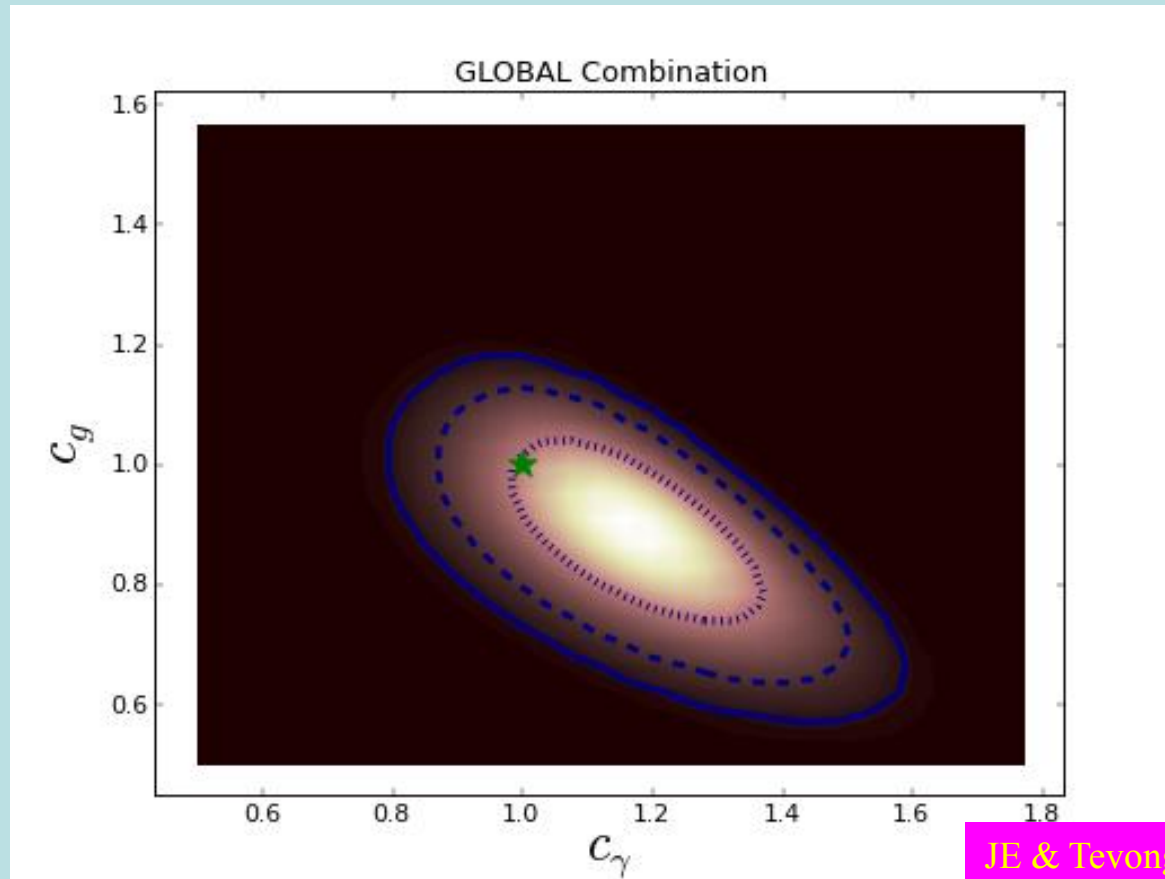
- Form factors for triangle diagrams



- Vanish for fermion mass \ll spin-0 mass

Loop Corrections ?

- Combination of data on $\gamma\gamma$, gluon-gluon couplings



JE & Tevong You, arXiv:1303.3879

- Loop diagrams ~ Standard Model?

What is it ?

H^0

$J = 0$

Mass $m = 125.09 \pm 0.24$ GeV

H^0 Signal Strengths in Different Channels

See Listings for the latest unpublished results.

Combined Final States = 1.17 ± 0.17 (S = 1.2)

$W W^* = 0.81 \pm 0.16$

$Z Z^* = 1.15^{+0.27}_{-0.23}$ (S = 1.2)

$\gamma\gamma = 1.17^{+0.19}_{-0.17}$

$b\bar{b} = 0.85 \pm 0.29$

$\mu^+ \mu^- < 7.0$, CL = 95%

$\tau^+ \tau^- = 0.79 \pm 0.26$

$Z\gamma < 9.5$, CL = 95%

$t\bar{t}H^0$ Production = $2.5^{+0.9}_{-0.8}$

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 - **Prima facie evidence that it does**
- Quantum (loop) corrections?
 - **$\gamma\gamma$, gg couplings \sim Standard Model**
- What are its self-couplings?

Dixit Swedish Academy



Today we believe that “Beyond any reasonable doubt, it is a Higgs boson.” [1]

http://www.nobelprize.org/nobel_prizes/physics/laureates/2013/advanced-physicsprize2013.pdf

[1] = JE & Tevong You, arXiv:1303.3879

Standard Model Effective Field Theory

- Higher-dimensional operators as relics of higher-energy physics, e.g., dimension 6:

$$\mathcal{L}_{\text{eff}} = \sum_n \frac{f_n}{\Lambda^2} \mathcal{O}_n$$

- Operators constrained by $SU(2) \times U(1)$ symmetry:

$$\begin{aligned} \mathcal{L} \supset & \frac{\bar{c}_H}{2v^2} \partial^\mu [\Phi^\dagger \Phi] \partial_\mu [\Phi^\dagger \Phi] + \frac{g'^2 \bar{c}_\gamma}{m_W^2} \Phi^\dagger \Phi B_{\mu\nu} B^{\mu\nu} + \frac{g_s^2 \bar{c}_g}{m_W^2} \Phi^\dagger \Phi G_{\mu\nu}^a G_a^{\mu\nu} \\ & + \frac{2ig \bar{c}_{HW}}{m_W^2} [D^\mu \Phi^\dagger T_{2k} D^\nu \Phi] W_{\mu\nu}^k + \frac{ig' \bar{c}_{HB}}{m_W^2} [D^\mu \Phi^\dagger D^\nu \Phi] B_{\mu\nu} \\ & + \frac{ig \bar{c}_W}{m_W^2} [\Phi^\dagger T_{2k} \overleftrightarrow{D}^\mu \Phi] D^\nu W_{\mu\nu}^k + \frac{ig' \bar{c}_B}{2m_W^2} [\Phi^\dagger \overleftrightarrow{D}^\mu \Phi] \partial^\nu B_{\mu\nu} \\ & + \frac{\bar{c}_t}{v^2} y_t \Phi^\dagger \Phi \Phi^\dagger \cdot \bar{Q}_L t_R + \frac{\bar{c}_b}{v^2} y_b \Phi^\dagger \Phi \Phi \cdot \bar{Q}_L b_R + \frac{\bar{c}_\tau}{v^2} y_\tau \Phi^\dagger \Phi \Phi \cdot \bar{L}_L \tau_R \end{aligned}$$

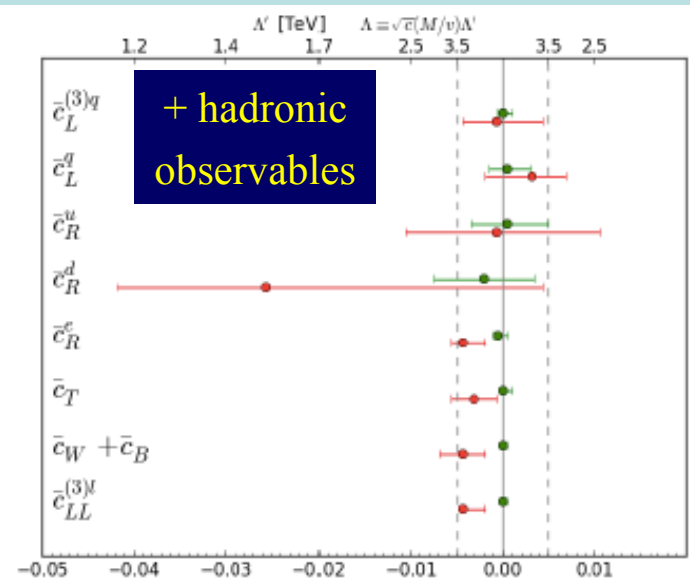
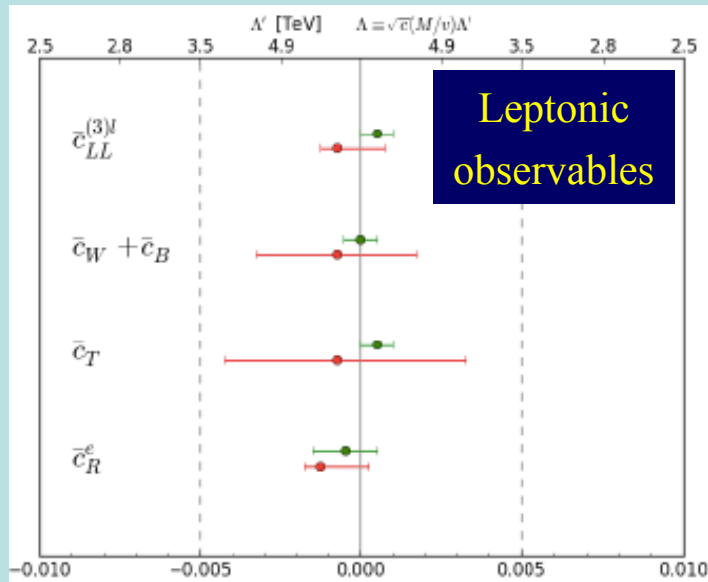
- Constrain with precision EW, Higgs data, TGCs ...

Electroweak Precision Data

- Operators affecting oblique parameters

$$\mathcal{L}_{\text{dim-6}} \subset \frac{\bar{c}_{WB}}{m_W^2} \mathcal{O}_{WB} + \frac{\bar{c}_W}{m_W^2} \mathcal{O}_W + \frac{\bar{c}_B}{m_W^2} \mathcal{O}_B + \frac{\bar{c}_T}{v^2} \mathcal{O}_T + \frac{\bar{c}_{2W}}{m_W^2} \mathcal{O}_{2W} + \frac{\bar{c}_{2B}}{m_W^2} \mathcal{O}_{2B}$$

- Also other electroweak tests
- Constraints from LEP et al. data



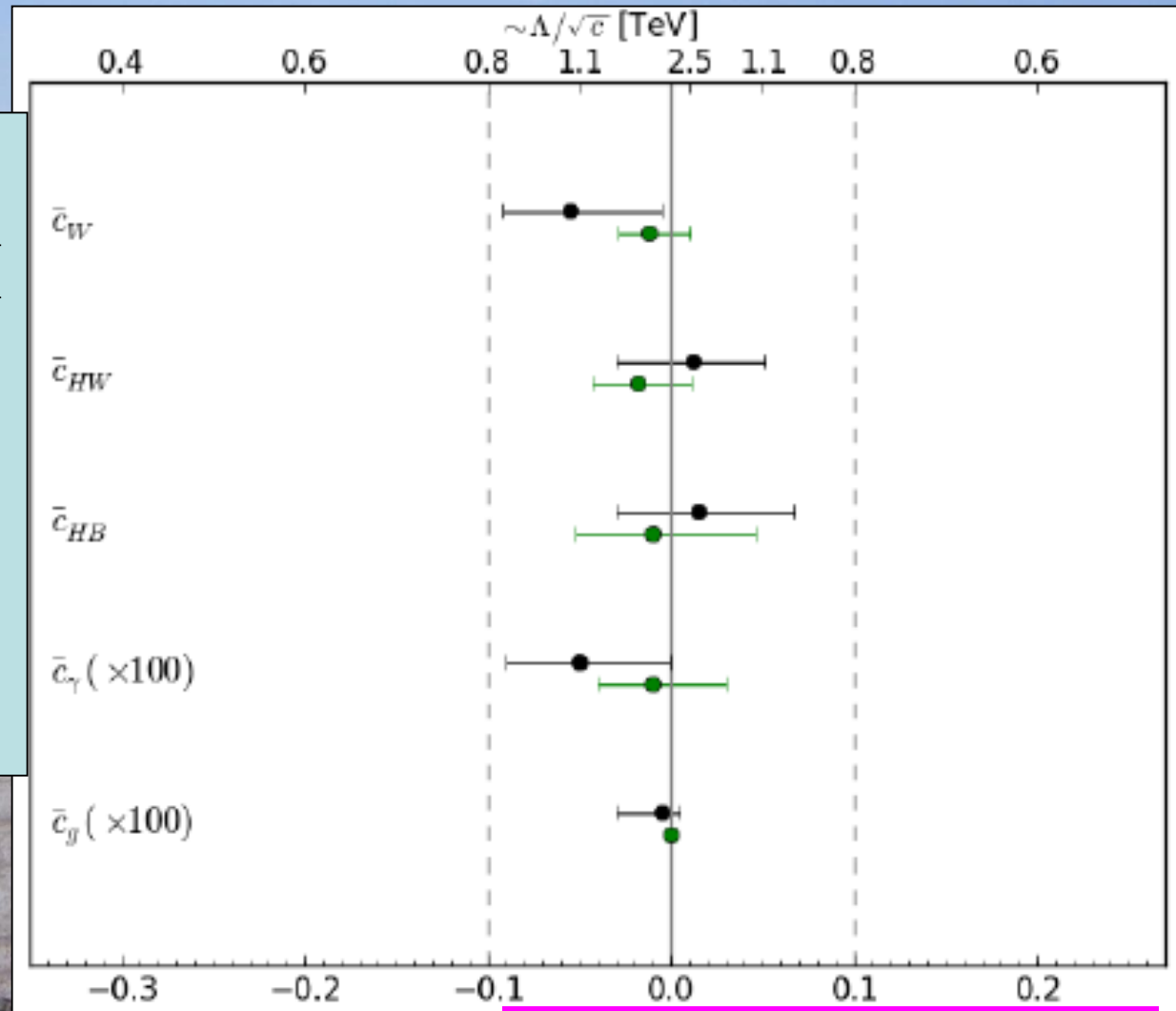
Fits to individual dimension-6 operators

Global fit to dimension-6 operators

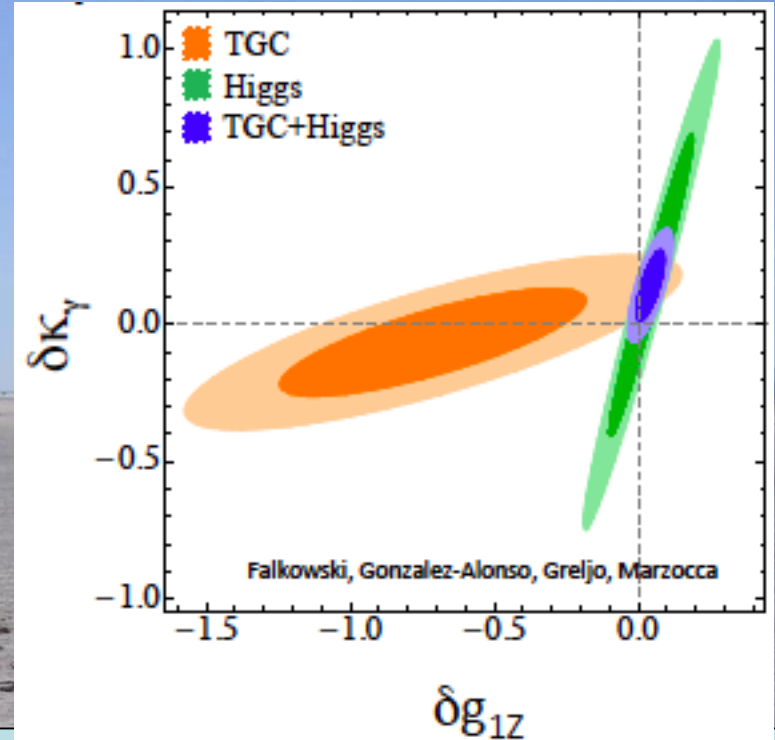
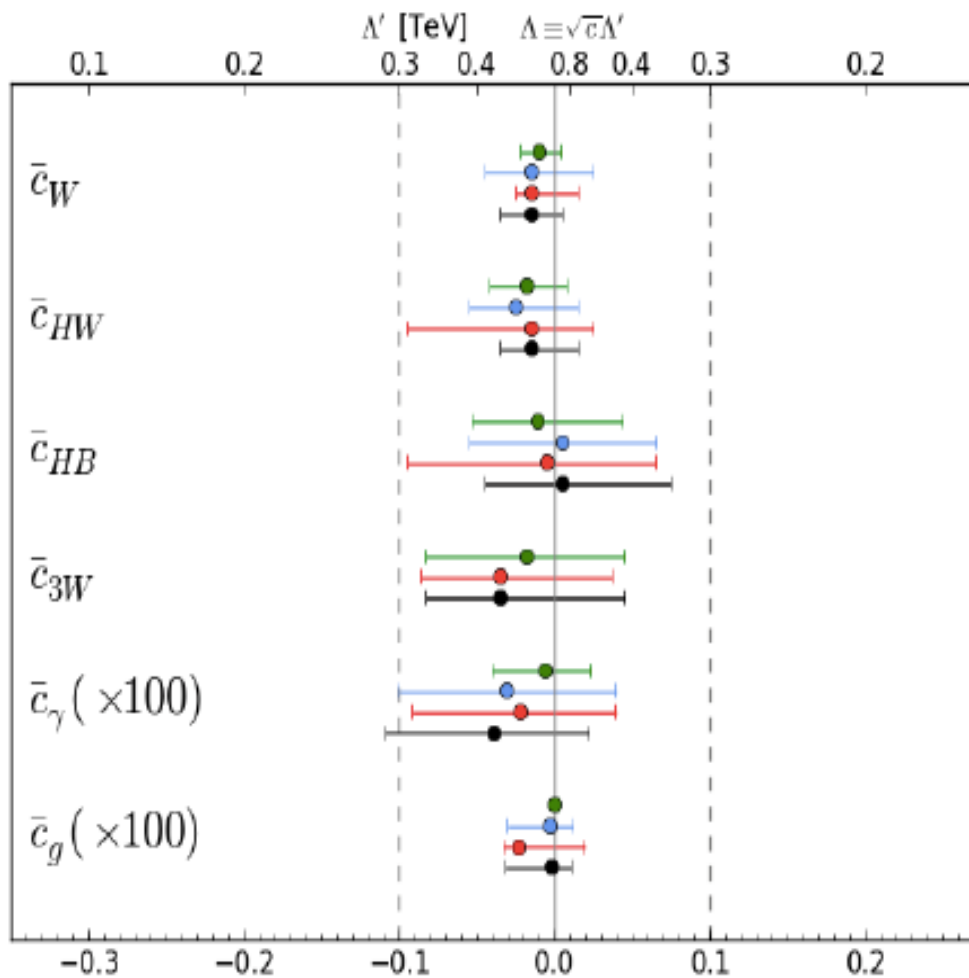
JE, Sanz & Tevong You, arXiv:1410.7703

Fits including Higgs Production

- Using signal strengths & VH kinematics in global fit
- **Single-parameter fits**



Global Fits including LHC TGCs



- Associated production
- LHC Triple-gauge couplings
- Global combination
- Individual operators

Standard Model Particles: Years from Proposal to Discovery

Electron

Photon

Muon

Electron neutrino

Muon neutrino

Down

Strange

Up

Charm

Tau

Bottom

Gluon

W boson

Z boson

Top

Tau neutrino

HIGGS BOSON

Lovers of physics
Beyond the SM:
be patient!





- « Empty » space is unstable
- Dark matter
- Origin of matter
- Masses of neutrinos
- Hierarchy problem
- Inflation
- Quantum gravity
- ...

SUSY

SUSY

SUSY

SUSY

SUSY

SUSY

The Standard Model

THE WORLD IS NOT ENOUGH
007[™]

ALBERT R. BROCCOLI'S SON PRODUCTIONS PRESENTS PIERCE BRUSHMAN IN IAN FLEMING'S JAMES BOND 007[™]
"THE WORLD IS NOT ENOUGH" SOPHIE MARCEAU ROBERT CAROLLE DENISE RICHARDS BRIGIDE COULBRADE AND JUDY DENCH
MUSIC BY LINDY HEARINGS COSTUME DESIGNER DAVID ARNOLD EDITOR JIM CLARK EXECUTIVE PRODUCERS ANDREW ADRIAN BOULE AND ANDREW PETER LAMANI
PRODUCED BY ANTHONY WARE DIRECTED BY NEAL PURVIS & ROBERT WADDE PRODUCED BY NEAL PURVIS & ROBERT WADDE EXECUTIVE PRODUCERS BRUCE FERRISSEN
PRODUCED BY MICHAEL E. WILSON AND BARBARA BROCCOLI PRODUCED BY MICHAEL APPEL
CASTING BY JUDITH GARBAGE
COURTESY OF PETER JACOBSON
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What lies beyond the Standard Model?

Supersymmetry

New motivations
From LHC Run 1

- **Stabilize electroweak vacuum**
- **Successful prediction for Higgs mass**
 - Should be < 130 GeV in simple models
- **Successful predictions for couplings**
 - Should be within few % of SM values
- Naturalness, GUTs, string, ..., **dark matter**

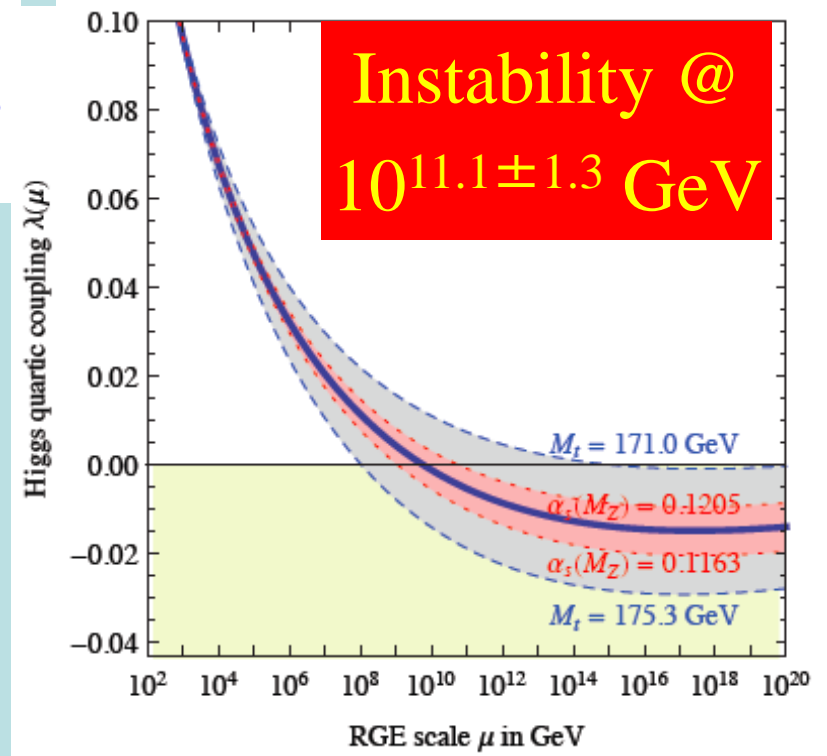
Theoretical Constraints on Higgs Mass

- Large $M_h \rightarrow$ large self-coupling \rightarrow blow up at

$$\lambda(Q) = \lambda(v) - \frac{3m_t^4}{2\pi^2 v^4} \log \frac{Q}{v}$$

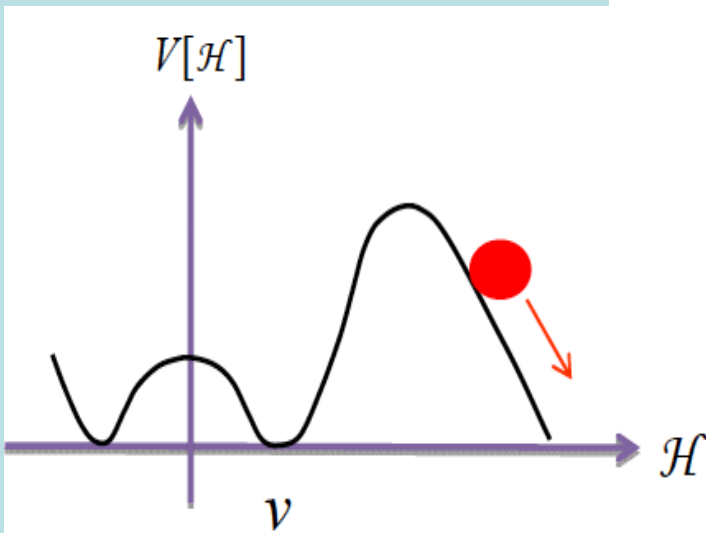
- Small: renormalization due to t quark drives quartic coupling < 0 at some scale Λ
 \rightarrow vacuum unstable

- Vacuum could be stabilized by **Supersymmetry**



Vacuum Instability in the Standard Model

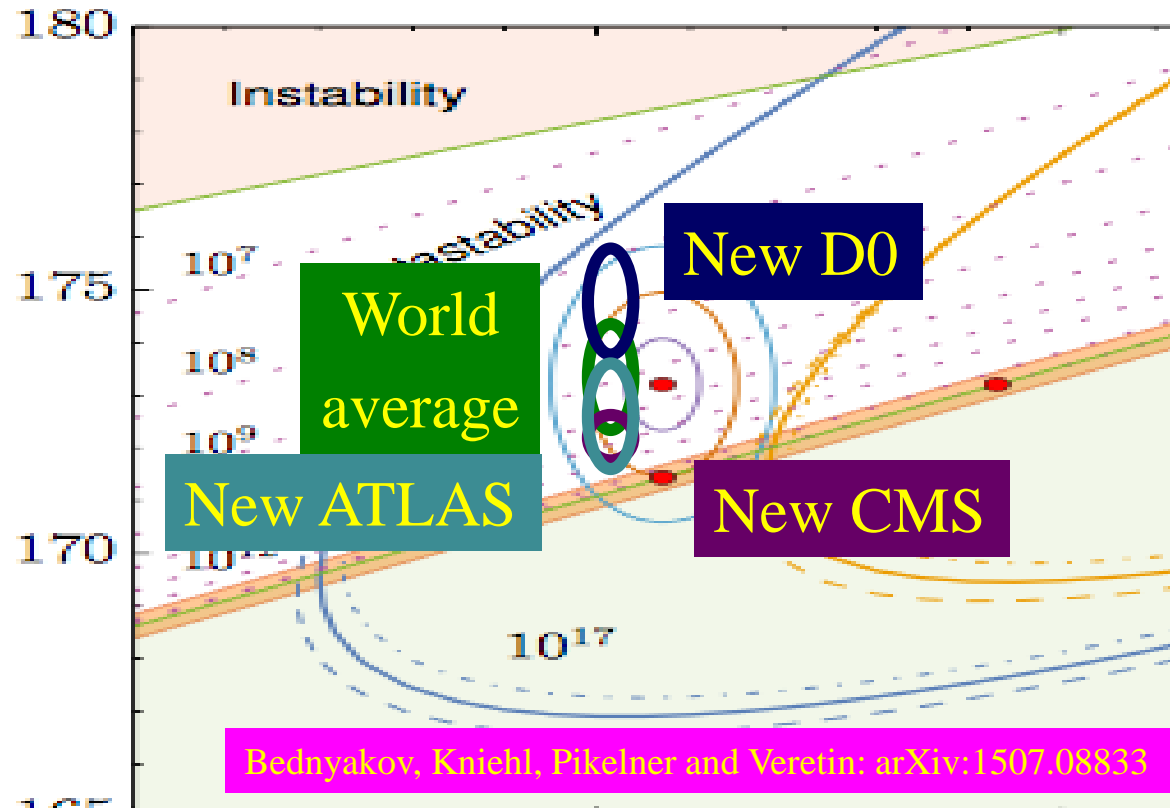
- Very sensitive to



- Instability scale

$$\log_{10} \frac{\Lambda_I}{\text{GeV}} = 11.3 + 1.0 \left(\frac{M_h}{\text{GeV}} - 125.66 \right) - 1.2 \left(\frac{M_t}{\text{GeV}} - 173.10 \right) + 0.4 \frac{\alpha_3(M_Z) - 0.1184}{0.0007}$$

$$m_t = 173.3 \pm 1.0 \text{ GeV} \rightarrow \log_{10}(\Lambda/\text{GeV}) = 11.1 \pm 1.3$$



Bednyakov, Kniehl, Pikelner and Veretin: arXiv:1507.08833

Buttazzo, Degrandi, Giardino, Giudice, Sala, Salvio & Strumia, arXiv:1307.3536

Hard QCD: the Top Mass

- Basic parameter of SM; **stability of EW vacuum?**

- World average:

$$m_t = 173.34 \pm 0.76 \text{ GeV}$$

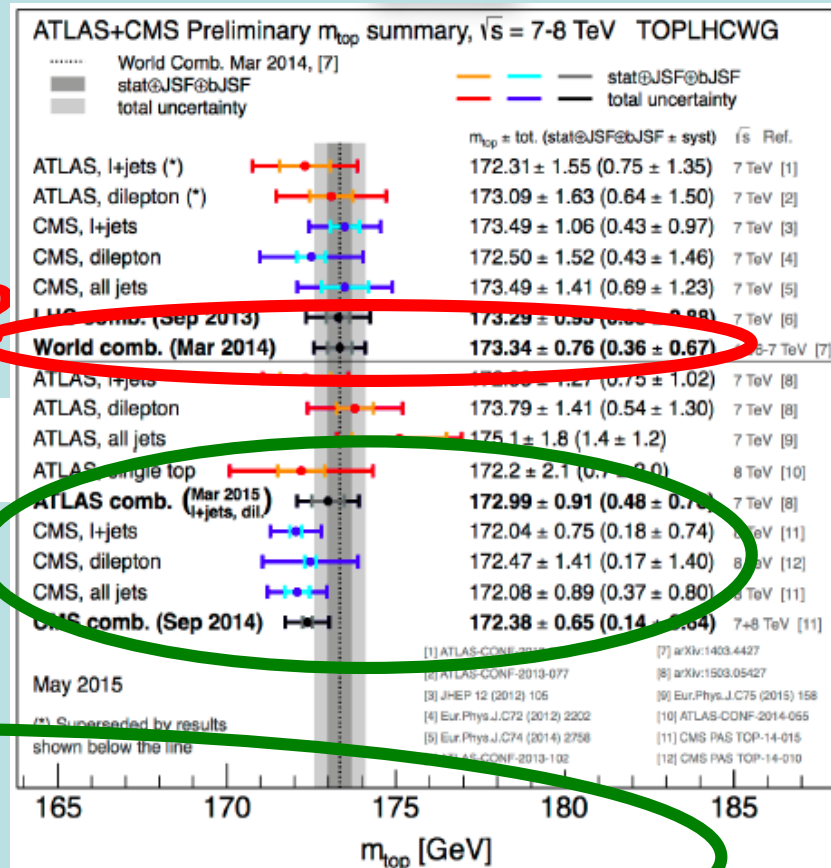
- **Running \rightarrow pole mass OK?**

$$+ 7.557 + 1.617 + 0.501 + 0.195)$$

- Monte Carlo mass \checkmark ?
- New measurements:

$$\text{ATLAS: } 172.99 \pm 0.91 \text{ GeV}$$

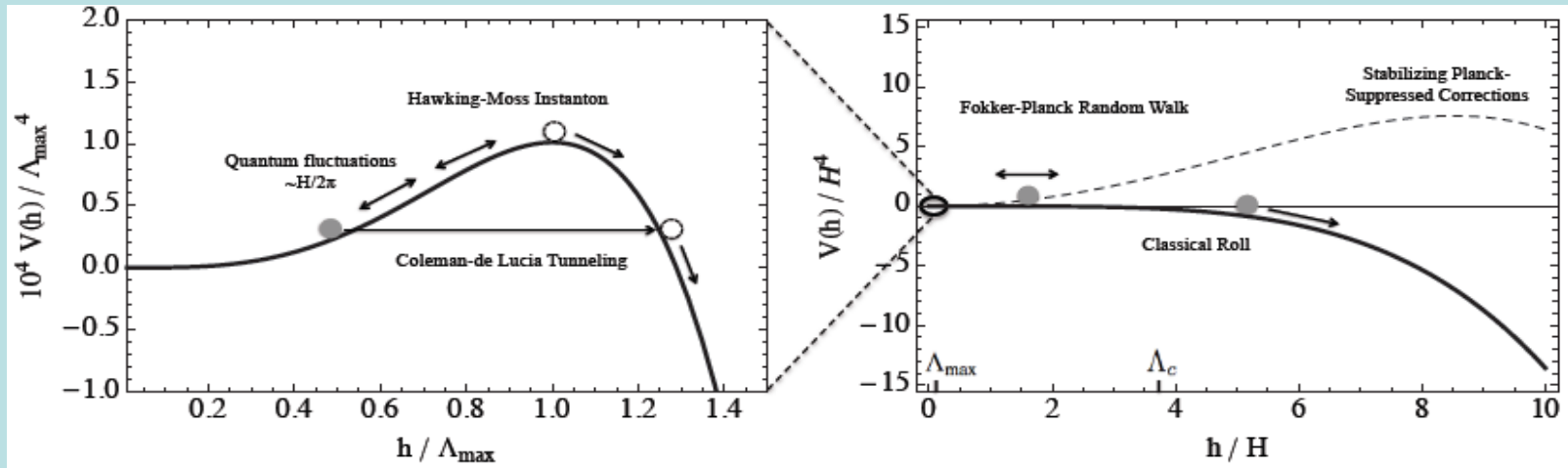
$$\text{CMS: } 172.38 \pm 0.65, \text{ D0: } 174.98 \pm 0.58 \pm 0.49 \text{ GeV}$$



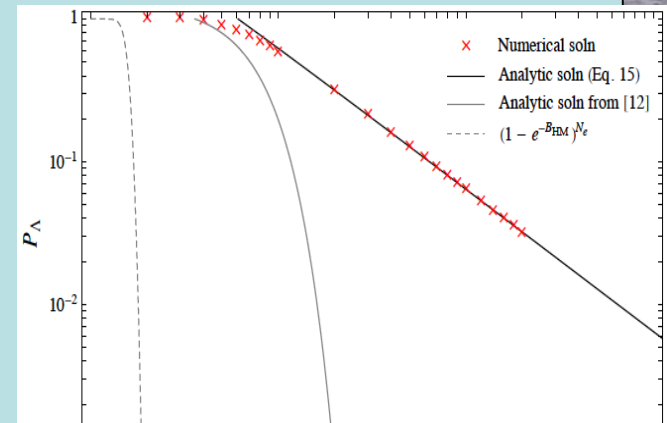
Instability during Inflation?

Hook, Kearns, Shakya & Zurek: arXiv:1404.5953

- Do inflation fluctuations drive us over the hill?



- Then Fokker-Planck evolution
- Do AdS regions eat us?
 - Disaster if so
 - If not, OK if more inflation



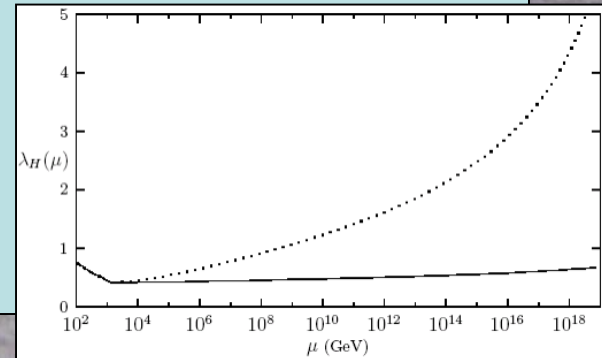
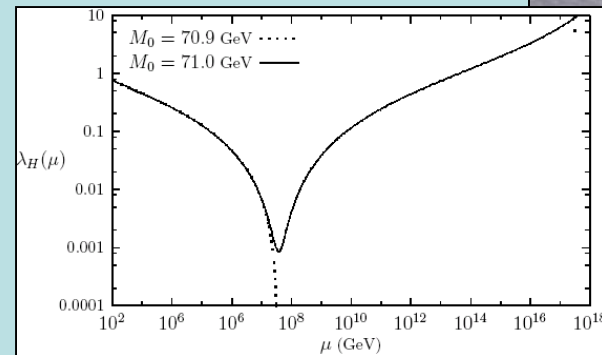
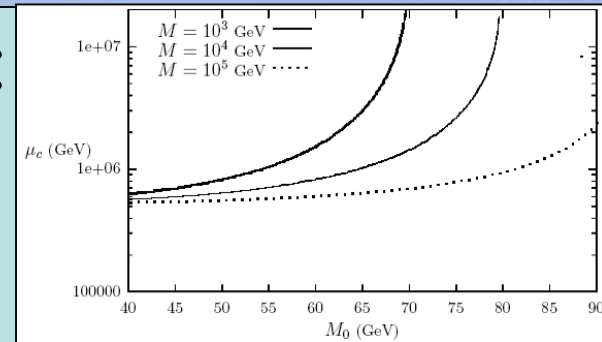
Stabilize vacuum with some physics beyond the SM?

How to Stabilize a Light Higgs Boson?

- Top quark destabilizes potential:
introduce stop-like scalar:

$$\mathcal{L} \supset M^2 |\phi|^2 + \frac{M_0}{v^2} |H|^2 |\phi|^2$$

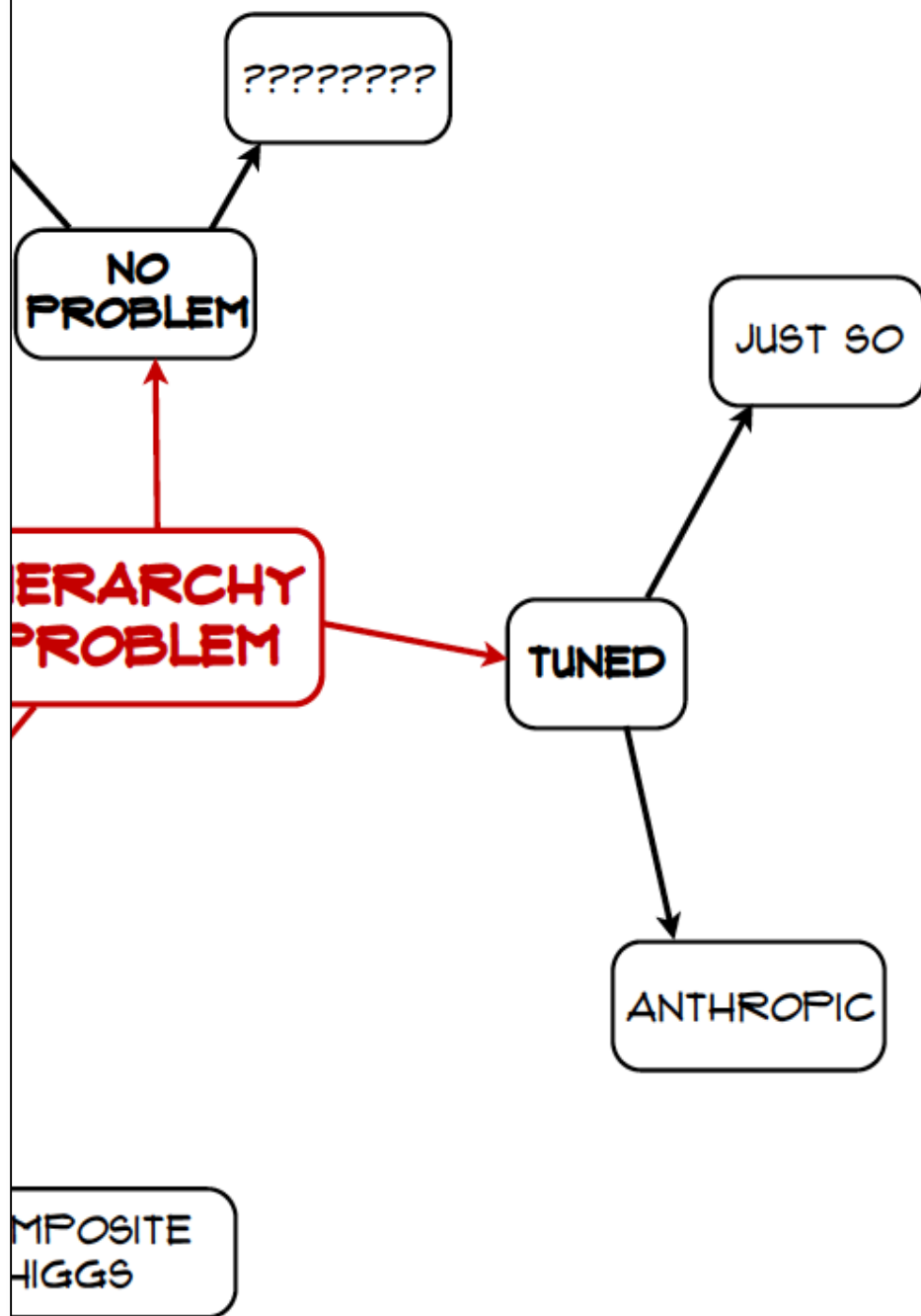
- Can delay collapse of potential:
- But new coupling must be fine-tuned to avoid blow-up:
- Stabilize with new fermions:
 - just like Higgsinos
- Very like **Supersymmetry!**





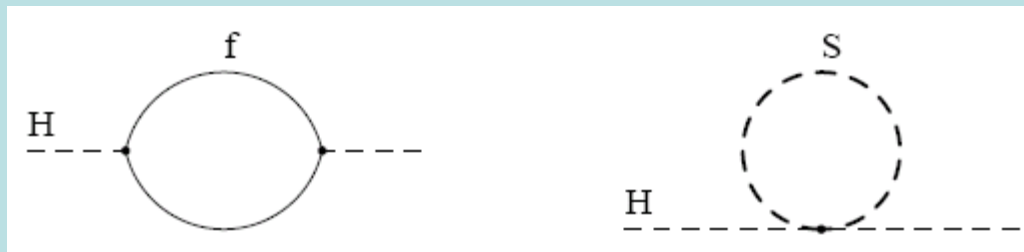
By courtesy of the "Department"

"WELL, IF YOU KNOWS OF A BETTER 'OLE, GO TO IT!"



Loop Corrections to Higgs Mass²

- Consider generic fermion and boson loops:



- Each is quadratically divergent: $\int^{\Lambda} d^4k/k^2$

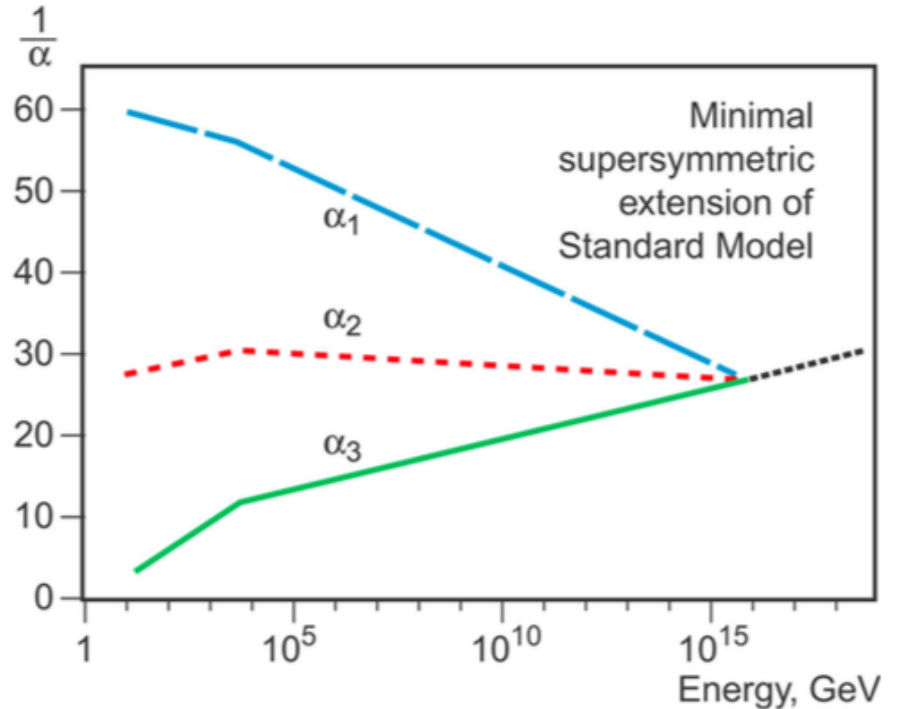
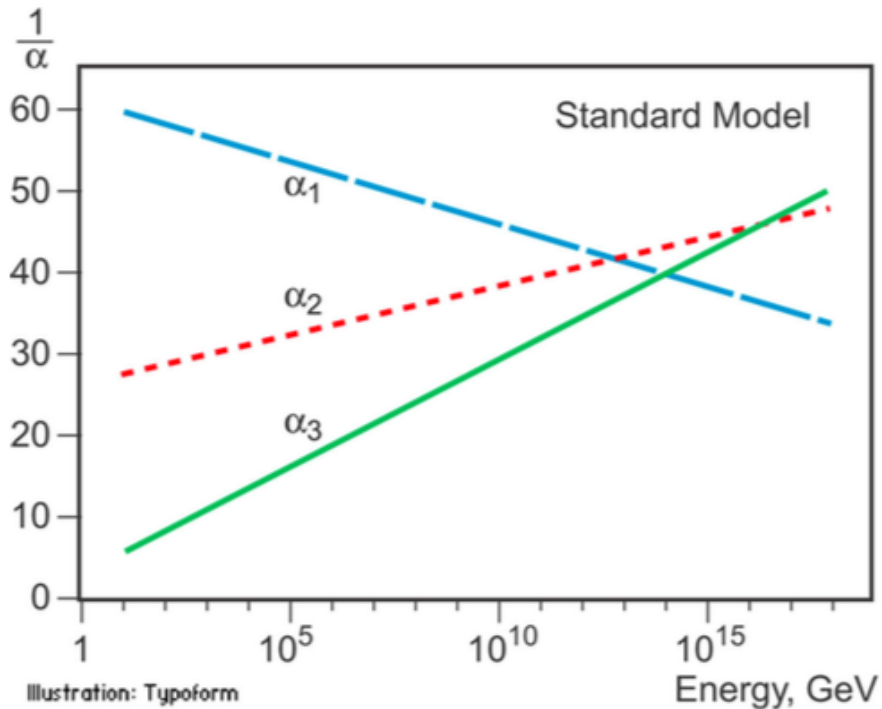
$$\Delta m_H^2 = -\frac{y_f^2}{16\pi^2} [2\Lambda^2 + 6m_f^2 \ln(\Lambda/m_f) + \dots]$$

$$\Delta m_H^2 = \frac{\lambda_S}{16\pi^2} [\Lambda^2 - 2m_S^2 \ln(\Lambda/m_S) + \dots]$$

- Leading divergence cancelled if

$$\lambda_S = y_f^2 \times 2 \quad \text{Supersymmetry!}$$

Unification of Gauge Couplings



- **Impressive!**
- **Over-ambitious? Hubristic?**

Minimal Supersymmetric Extension of Standard Model (MSSM)

- Double up the known particles:

$$\begin{pmatrix} \frac{1}{2} \\ 0 \end{pmatrix} \text{ e.g., } \begin{pmatrix} \ell \text{ (lepton)} \\ \tilde{\ell} \text{ (slepton)} \end{pmatrix} \text{ or } \begin{pmatrix} q \text{ (quark)} \\ \tilde{q} \text{ (squark)} \end{pmatrix}$$

$$\begin{pmatrix} 1 \\ \frac{1}{2} \end{pmatrix} \text{ e.g., } \begin{pmatrix} \gamma \text{ (photon)} \\ \tilde{\gamma} \text{ (photino)} \end{pmatrix} \text{ or } \begin{pmatrix} g \text{ (gluon)} \\ \tilde{g} \text{ (gluino)} \end{pmatrix}$$

- Two Higgs doublets
 - 5 physical Higgs bosons:
 - 3 neutral, 2 charged
- Lightest neutral supersymmetric Higgs looks like the single Higgs in the Standard Model

Higgs Bosons in Supersymmetry

- Need 2 complex Higgs doublets
(cancel anomalies, form of SUSY couplings)
- $8 - 3 = 5$ physical Higgs bosons
Scalars h, H ; pseudoscalar A ; charged H^\pm
- Lightest Higgs $< M_Z$ at tree level:

$$M_{H,h}^2 = \frac{1}{2} \left[M_A^2 + M_Z^2 \pm \sqrt{(M_A^2 + M_Z^2)^2 - 4M_Z^2 M_A^2 \cos^2 2\beta} \right]$$

- Important radiative corrections to mass:

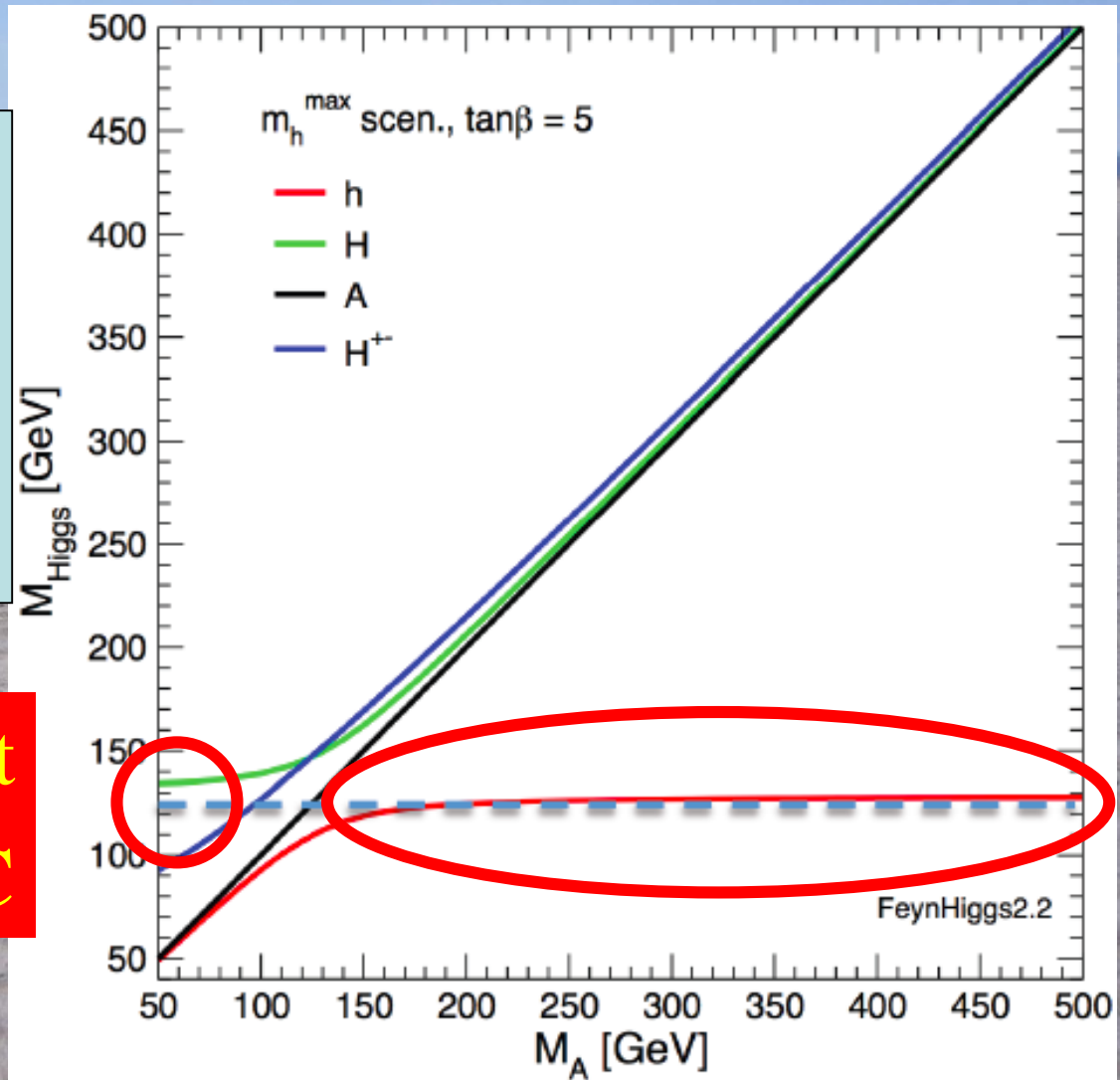
$$G_\mu m_t^4 \ln \left(\frac{m_{\tilde{t}_1} m_{\tilde{t}_2}}{m_t^2} \right) \Delta M_{H|_{TH}} \sim 1.5 \text{ GeV}$$

MSSM Higgs Masses & Couplings

Lightest Higgs mass
up to ~ 130 GeV
Heavy Higgs masses

750? quite close

Consistent
With LHC



Lightest Supersymmetric Particle

- Stable in many models because of conservation of R parity:

$$\mathbf{R = (-1)^{2S - L + 3B}}$$

where S = spin, L = lepton #, B = baryon #

- Particles have $R = +1$, sparticles $R = -1$:

Sparticles produced in pairs

Heavier sparticles \rightarrow lighter sparticles

- **Lightest supersymmetric particle (LSP) stable**

Lightest Sparticle as Dark Matter?

- No strong or electromagnetic interactions

Otherwise would bind to matter

Detectable as anomalous heavy nucleus

- Possible weakly-interacting scandidates

Sneutrino

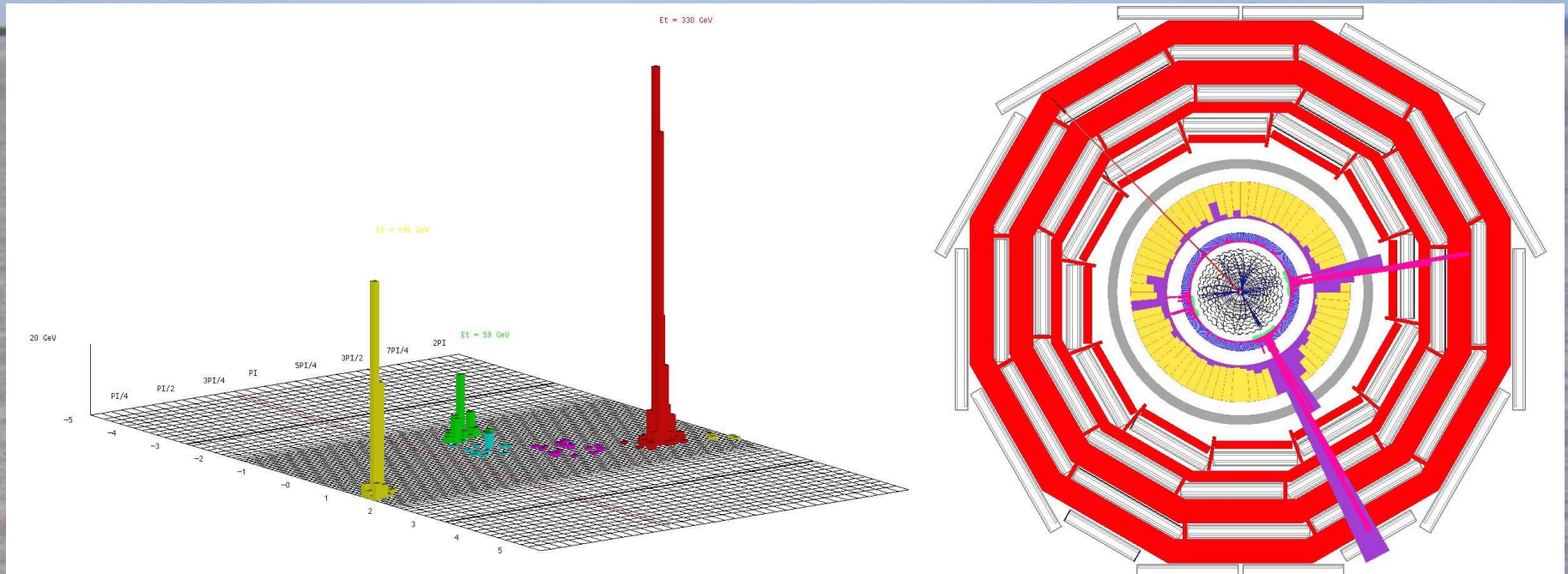
(Excluded by LEP, direct searches)

Lightest neutralino χ (partner of Z, H, γ)

Gravitino

(nightmare for detection)

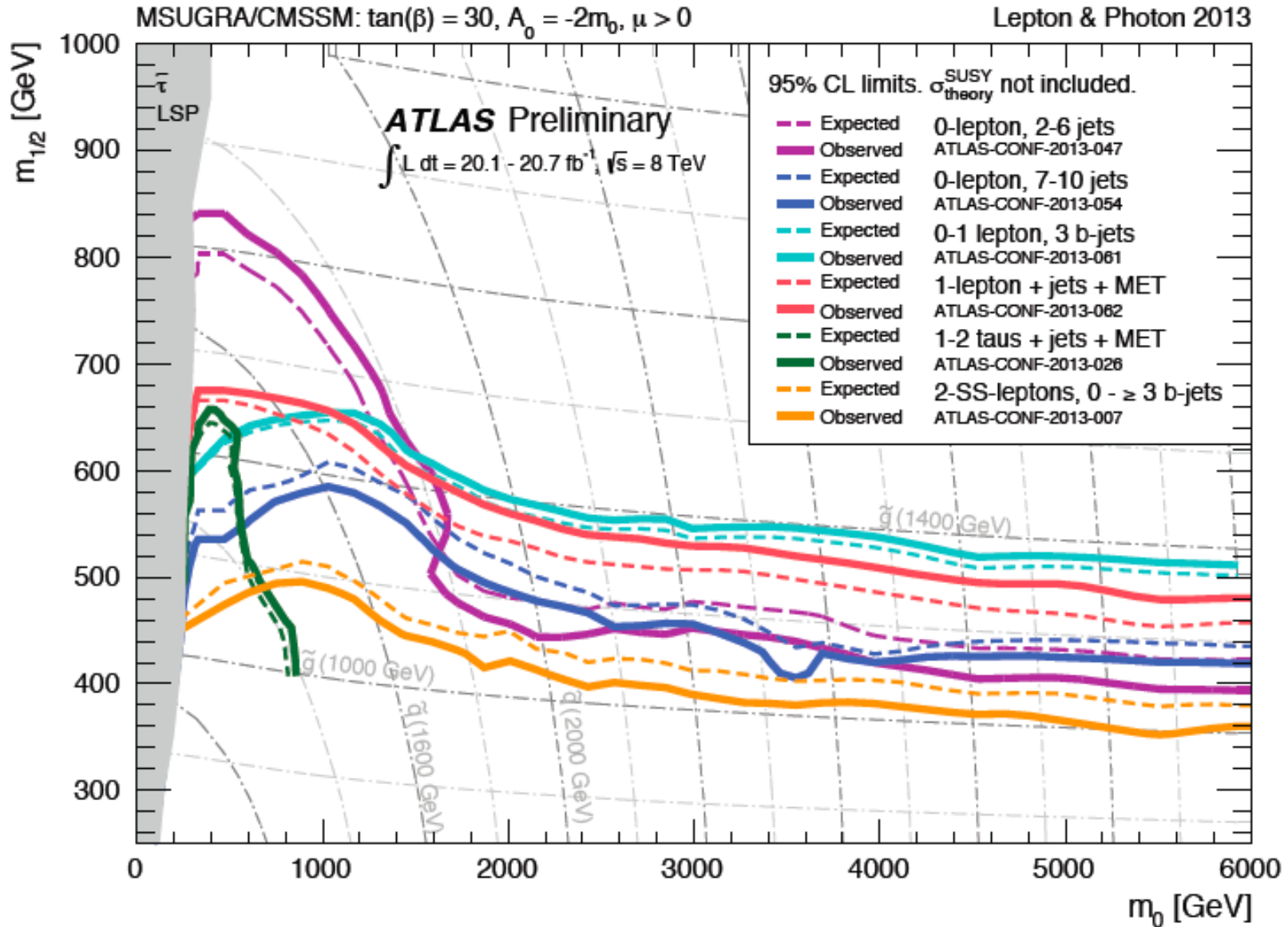
Classic Dark Matter Signature

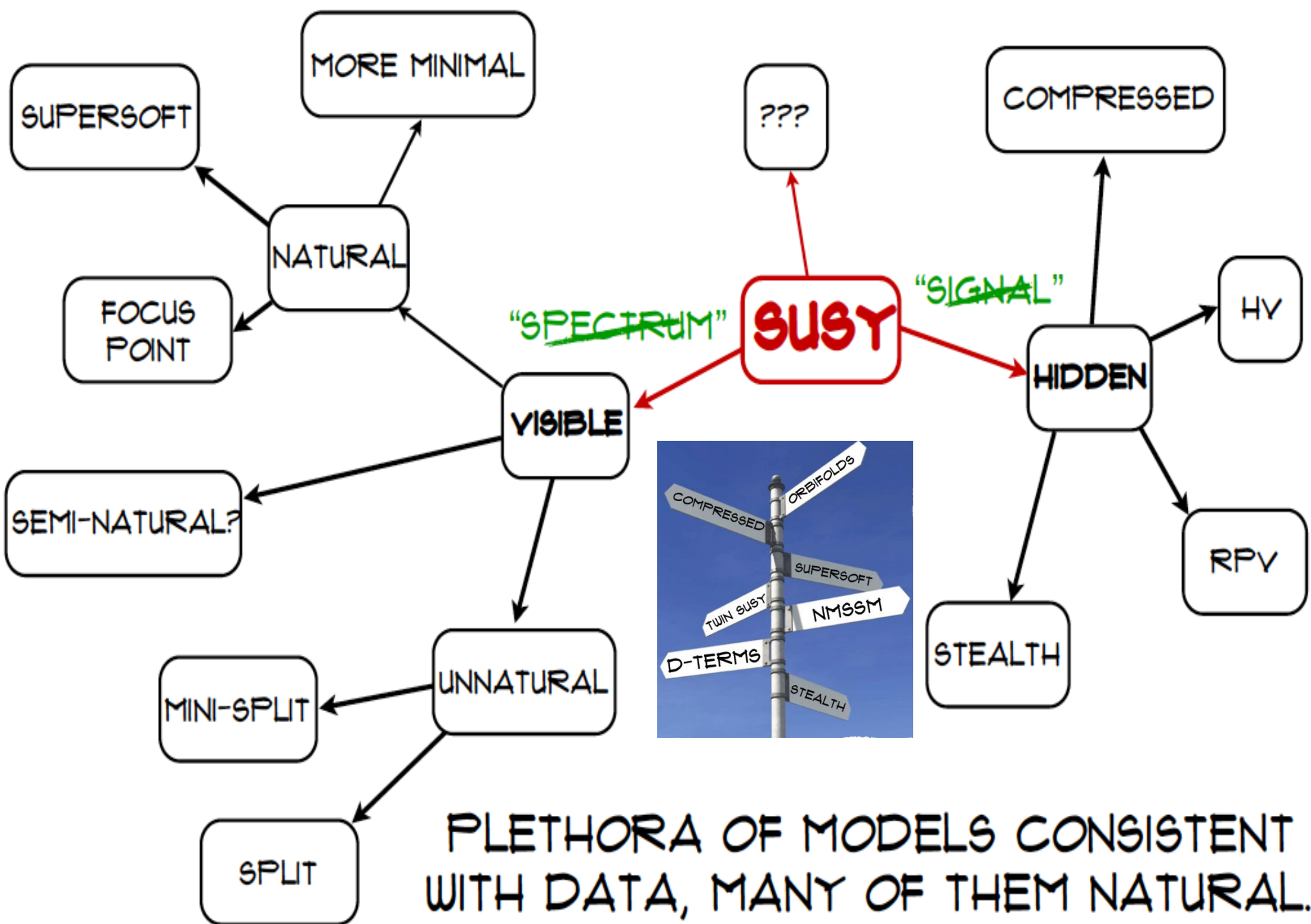


Missing transverse energy
carried away by dark matter particles

Searches with $\sim 20/\text{fb}$ @ 8 TeV

Lepton & Photon 2013





PLETHORA OF MODELS CONSISTENT WITH DATA, MANY OF THEM NATURAL. WHERE DOES THE DATA POINT US?

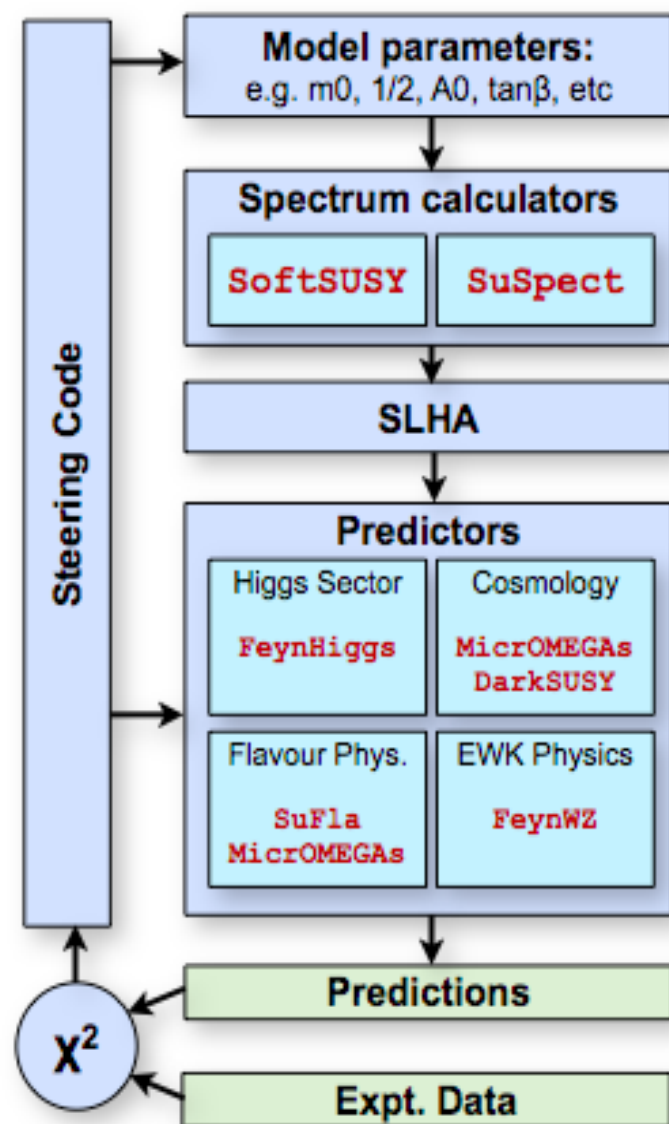
(Non-)Universal Scalar Masses?

- Different sfermions with same quantum #s?
e.g., d, s squarks?
disfavoured by upper limits on flavour-changing neutral interactions
- Squarks with different #s, squarks and sleptons?
disfavoured in various GUT models
e.g., $d_R = e_L$, $d_L = u_L = u_R = e_R$ in $SU(5)$, all in $SO(10)$
- Non-universal susy-breaking masses for Higgses?
No reason why not! NUHM

Sample Supersymmetric Models

- Universal soft supersymmetry breaking at input GUT scale?
 - For gauginos and all scalars: CMSSM
 - Non-universal Higgs masses: NUHM1,2
- **Strong pressure from LHC ($p \sim 0.1$)**
- Treat soft supersymmetry-breaking masses as phenomenological inputs at EW scale
 - pMSSM $_n$ (n parameters)
 - With universality motivated by upper limits on flavour-changing neutral interactions: pMSSM $_{10}$
- **Less strongly constrained by LHC ($p \sim 0.3$)**

- **Combines diverse set of tools**
 - **different codes** : all state-of-the-art
 - Electroweak Precision (**FeynWZ**)
 - Flavour (**SuFla**, **micrOMEGAs**)
 - Cold Dark Matter (**DarkSUSY**, **micrOMEGAs**)
 - Other low energy (**FeynHiggs**)
 - Higgs (**FeynHiggs**)
 - **different precisions** (one-loop, two-loop, etc)
 - **different languages** (Fortran, C++, English, German, Italian, etc)
 - **different people** (theorists, experimentalists)
- **Compatibility is crucial! Ensured by**
 - close collaboration of tools authors
 - standard interfaces



Data

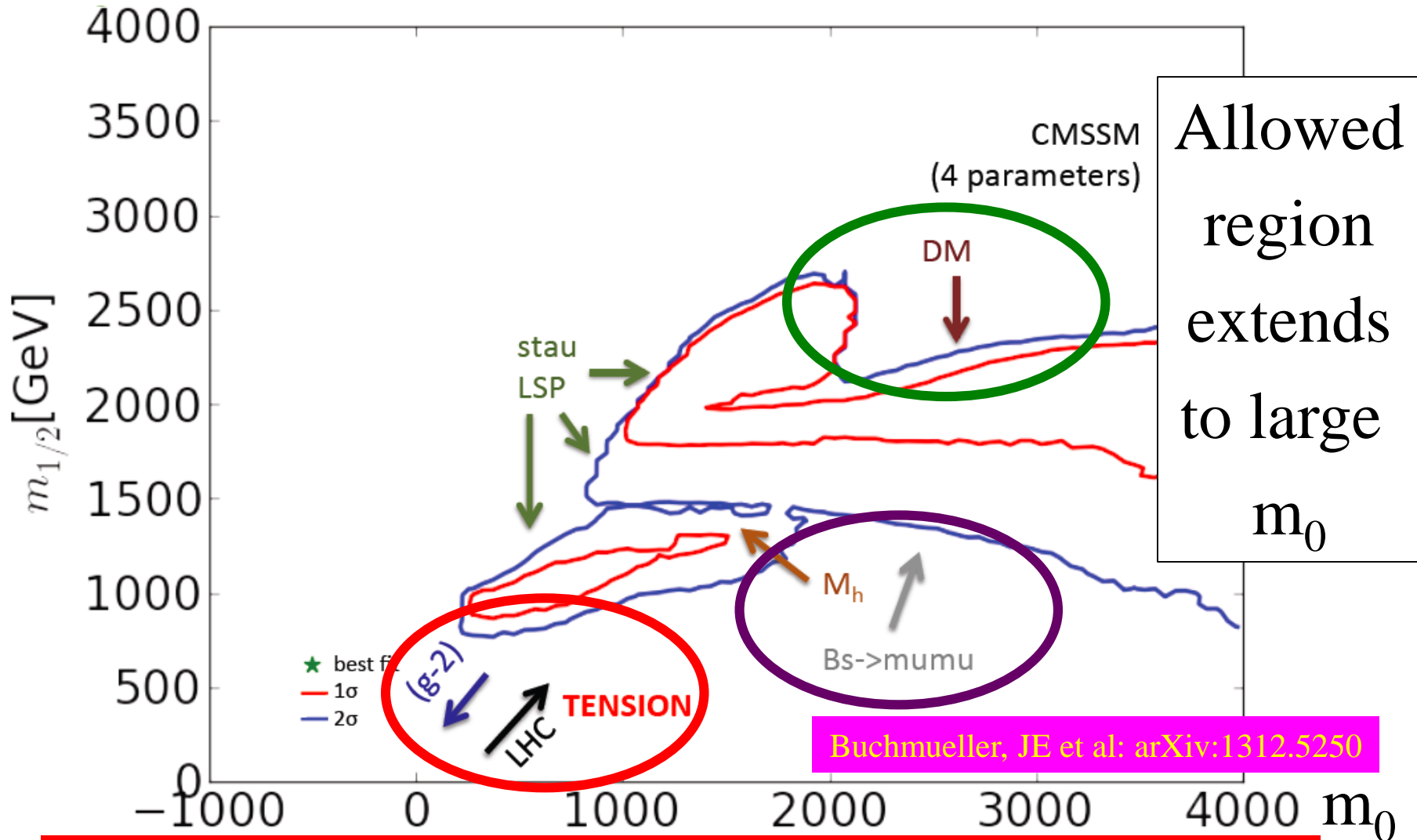
- Electroweak precision observables
- Flavour physics observables
- $g_\mu - 2$
- Higgs mass
- Dark matter
- LHC

Deviation from Standard Model:
Supersymmetry at low scale, or ...?

Observable	Source Th./Ex.	Constraint
m_t [GeV]	[39]	173.2 ± 0.90
$\Delta\alpha_{\text{had}}^{(5)}(m_Z)$	[38]	0.02749 ± 0.00010
M_Z [GeV]	[40]	91.1875 ± 0.0021
Γ_Z [GeV]	[24] / [40]	$2.4952 \pm 0.0023 \pm 0.001_{\text{SUSY}}$
σ_{had}^0 [nb]	[24] / [40]	41.540 ± 0.037
R_t	[24] / [40]	20.767 ± 0.025
$A_{\text{fb}}(\ell)$	[24] / [40]	0.01714 ± 0.00095
$A_\ell(P_\tau)$	[24] / [40]	0.1465 ± 0.0032
R_b	[24] / [40]	0.21629 ± 0.00066
R_c	[24] / [40]	0.1721 ± 0.0030
$A_{\text{fb}}(b)$	[24] / [40]	0.0992 ± 0.0016
$A_{\text{fb}}(c)$	[24] / [40]	0.0707 ± 0.0035
A_b	[24] / [40]	0.923 ± 0.020
A_c	[24] / [40]	0.670 ± 0.027
$A_\ell(\text{SLD})$	[24] / [40]	0.1513 ± 0.0021
$\sin^2 \theta_w^{\text{eff}}(Q_{\text{fb}})$	[24] / [40]	0.2324 ± 0.0012
M_W [GeV]	[24] / [40]	$80.399 \pm 0.023 \pm 0.010_{\text{SUSY}}$
$\text{BR}_{b \rightarrow s\gamma}^{\text{EXP}} / \text{BR}_{b \rightarrow s\gamma}^{\text{SM}}$	[41] / [42]	$1.117 \pm 0.076_{\text{EXP}} \pm 0.082_{\text{SM}} \pm 0.050_{\text{SUSY}}$
	[27] / [37]	$(< 1.08 \pm 0.02_{\text{SUSY}}) \times 10^{-8}$
	[27] / [42]	$1.43 \pm 0.43_{\text{EXP+TH}}$
	[27] / [42]	$< (4.6 \pm 0.01_{\text{SUSY}}) \times 10^{-9}$
	[43] / [42]	0.99 ± 0.32
	[27] / [44]	$1.008 \pm 0.014_{\text{EXP+TH}}$
$\text{BR}_{K \rightarrow \mu\nu}^{\text{EXP}} / \text{BR}_{K \rightarrow \mu\nu}^{\text{SM}}$	[45] / [46]	< 4.5
$\Delta M_{B_s}^{\text{EXP}} / \Delta M_{B_s}^{\text{SM}}$	[45] / [47, 48]	$0.97 \pm 0.01_{\text{EXP}} \pm 0.27_{\text{SM}}$
$(\Delta M_{B_s}^{\text{EXP}} / \Delta M_{B_s}^{\text{SM}}) / (\Delta M_{B_d}^{\text{EXP}} / \Delta M_{B_d}^{\text{SM}})$	[27] / [42, 47, 48]	$1.00 \pm 0.01_{\text{EXP}} \pm 0.13_{\text{SM}}$
$\Delta\epsilon_K^{\text{EXP}} / \Delta\epsilon_K^{\text{SM}}$	[45] / [47, 48]	$1.08 \pm 0.14_{\text{EXP+TH}}$
$\sigma_p^{\text{EXP}} / \sigma_p^{\text{SM}}$	[49] / [38, 50]	$(30.2 + 8.8 + 2.0_{\text{SUSY}}) \times 10^{-10}$
M_H	[17, 18]	$125.09 \pm 0.21 \pm 0.11 \text{ GeV}$
	[17, 18]	$\pm 0.017_{\text{SUSY}}$
σ_p	[23]	$(m_{\text{eff}}^{\text{SI}} / p)$ plane
jets + \cancel{E}_T	[16, 18]	$(m_0, m_{1/2})$ plane
$H/A, H^\pm$	[19]	$(M_A, \tan\beta)$ plane

Fit to Constrained MSSM (CMSSM)

2012 ATLAS + CMS with 20/fb of LHC Data



p-value of simple models $\sim 10\%$ (also SM)

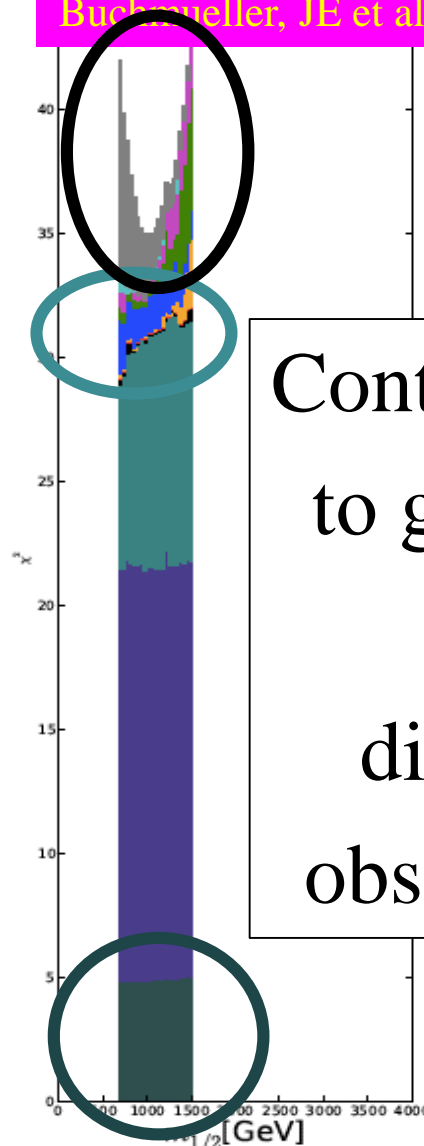
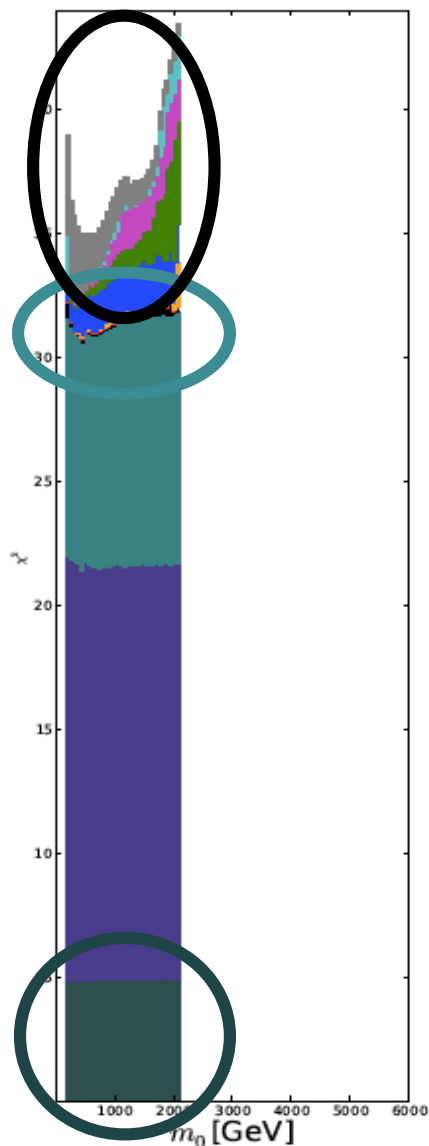
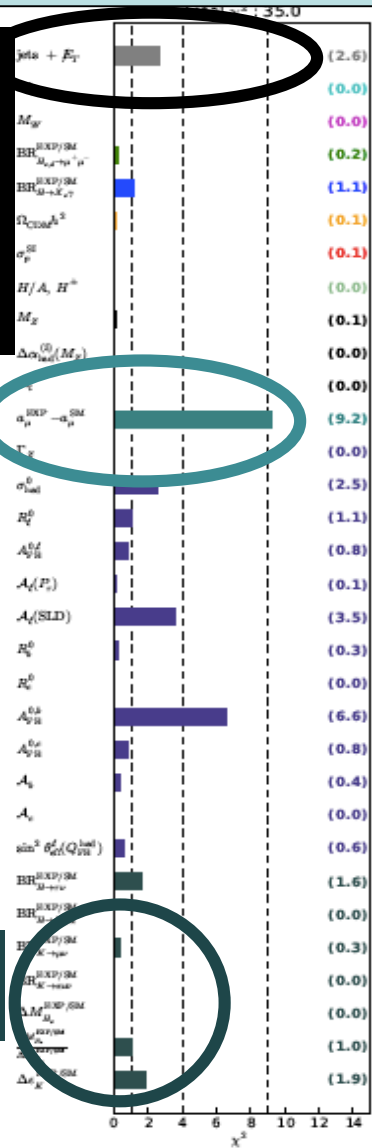
Constrained MSSM (CMSSM)

Buchmüller, JE et al: arXiv:1312.5250

LHC
MET
searches

$g_\mu - 2$

Flavour



Contributions
to global χ^2
from
different
observables



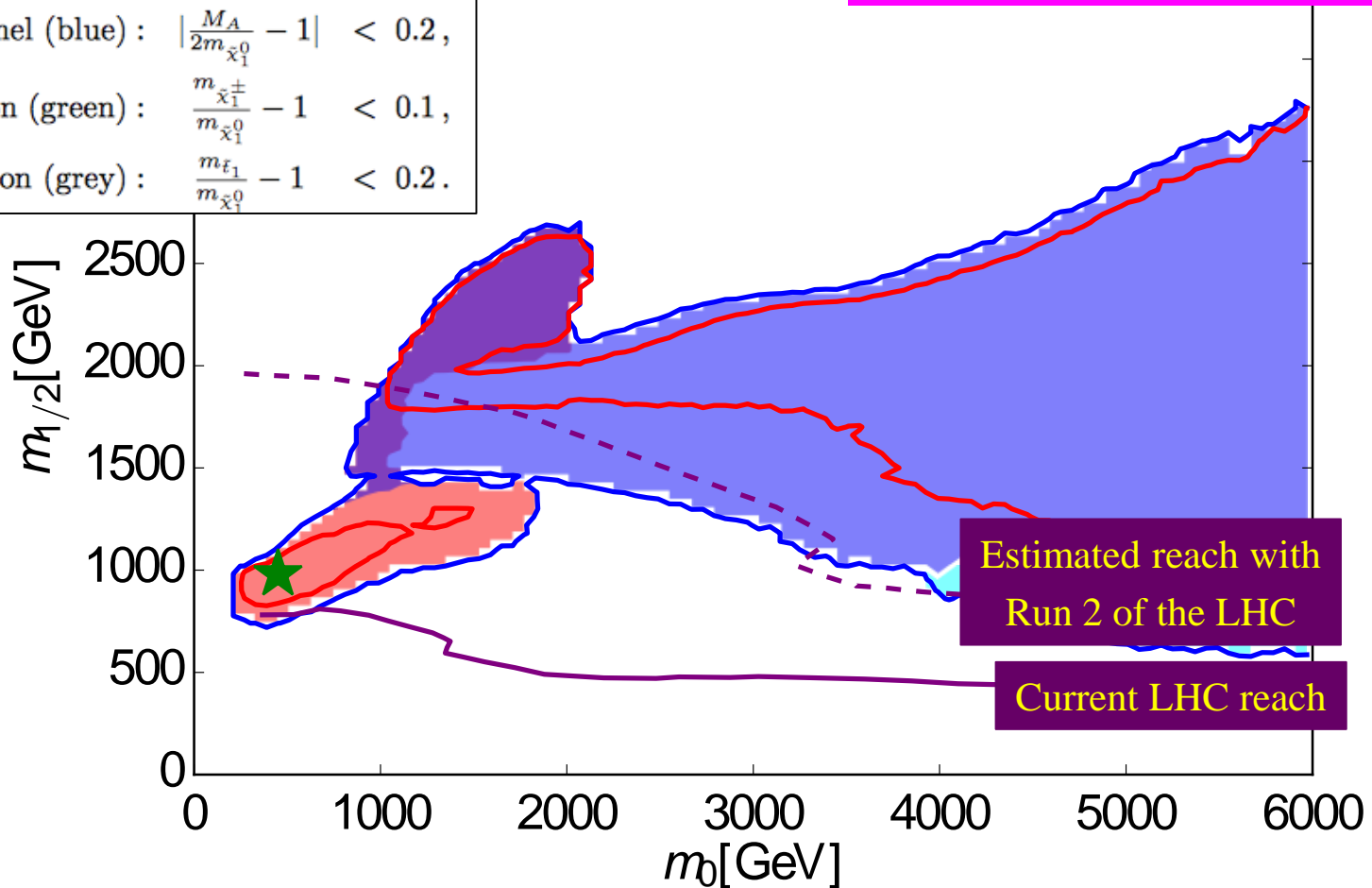
Dark Matter Density Mechanisms

2012 ATLAS + CMS with 20/fb of LHC Data

★ ——— CMSSM: best fit, 1σ, 2σ

$\tilde{\tau}_1$ coannihilation (pink) :	$\frac{m_{\tilde{\tau}_1} - 1}{m_{\tilde{\chi}_1^0}} < 0.15,$
A/H funnel (blue) :	$ \frac{M_A}{2m_{\tilde{\chi}_1^0}} - 1 < 0.2,$
$\tilde{\chi}_1^\pm$ coannihilation (green) :	$\frac{m_{\tilde{\chi}_1^\pm} - 1}{m_{\tilde{\chi}_1^0}} < 0.1,$
\tilde{t}_1 coannihilation (grey) :	$\frac{m_{\tilde{t}_1} - 1}{m_{\tilde{\chi}_1^0}} < 0.2.$

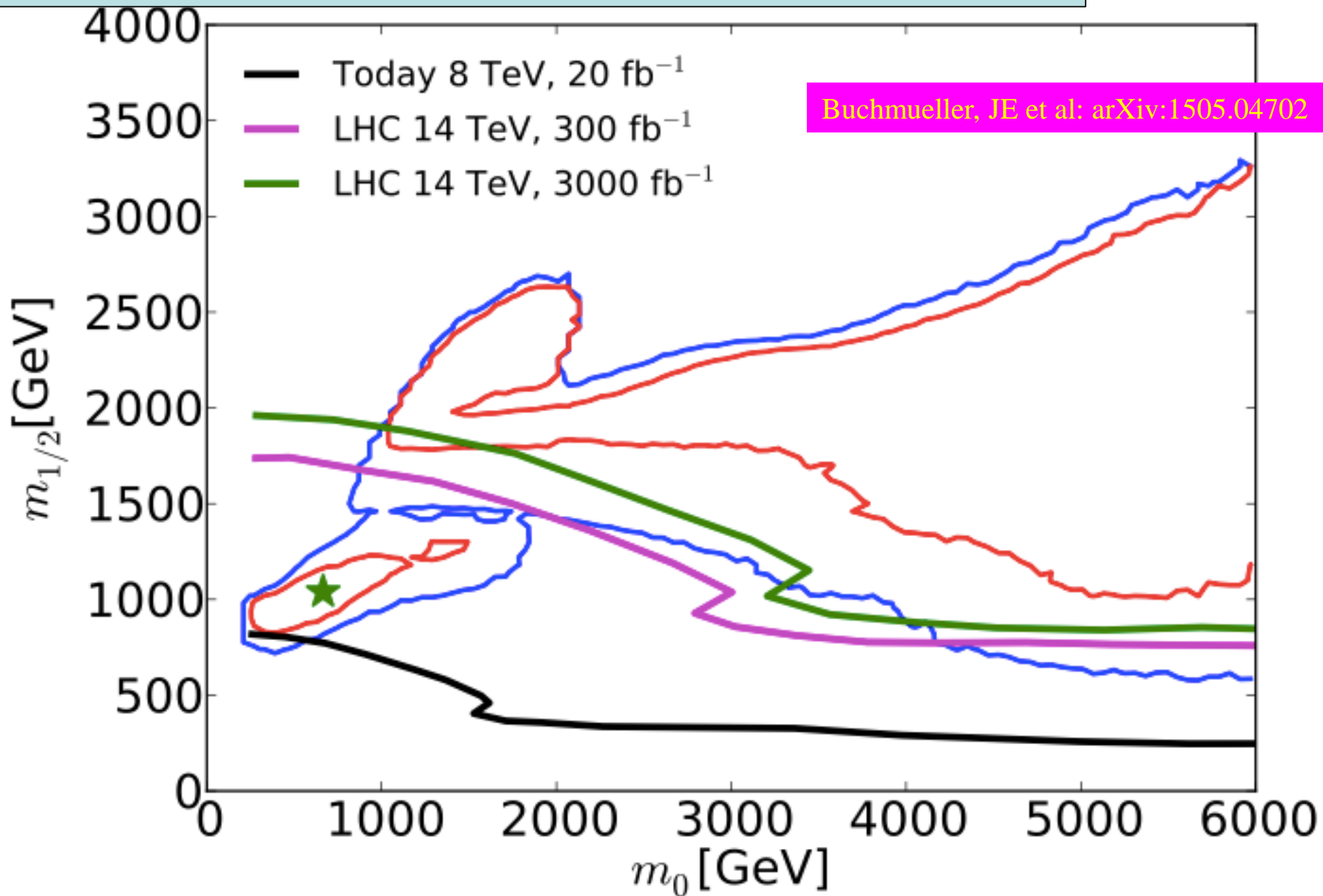
Buchmueller, JE et al: arXiv:1312.5250



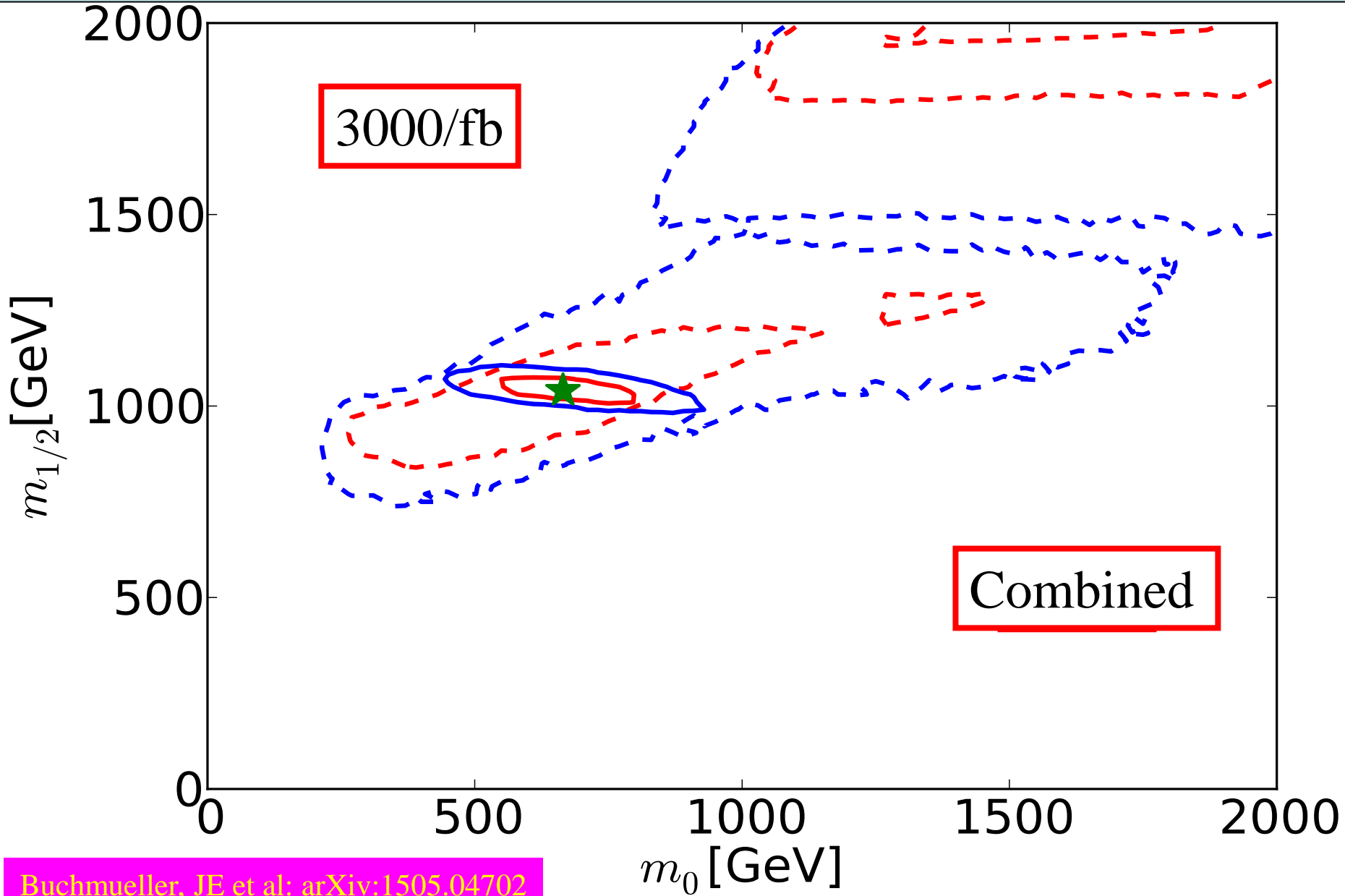
Estimated reach with Run 2 of the LHC

Current LHC reach

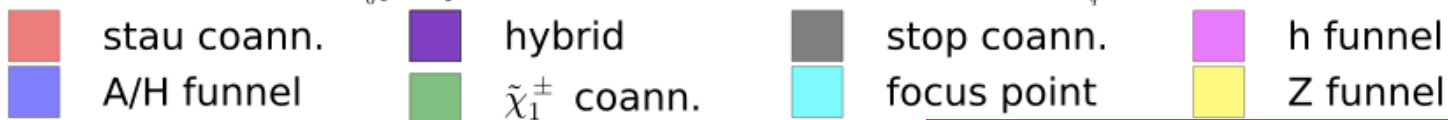
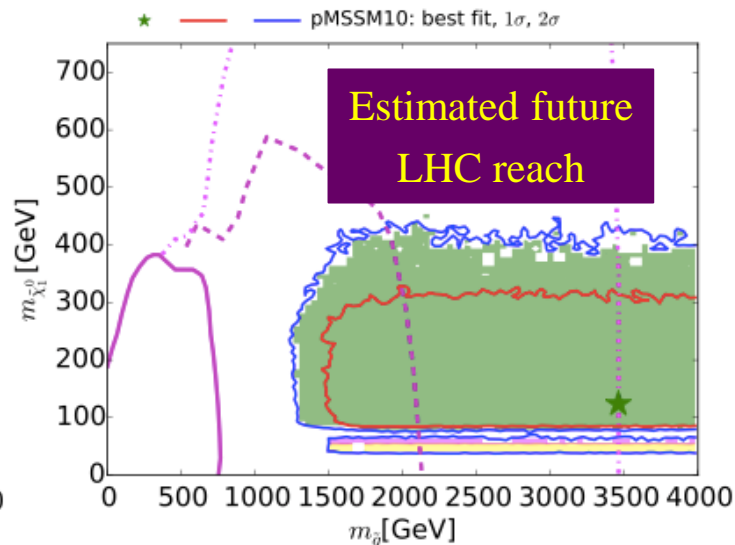
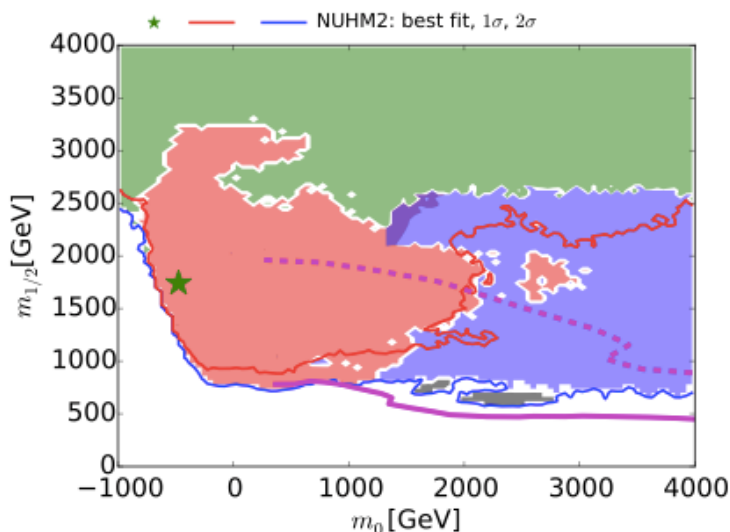
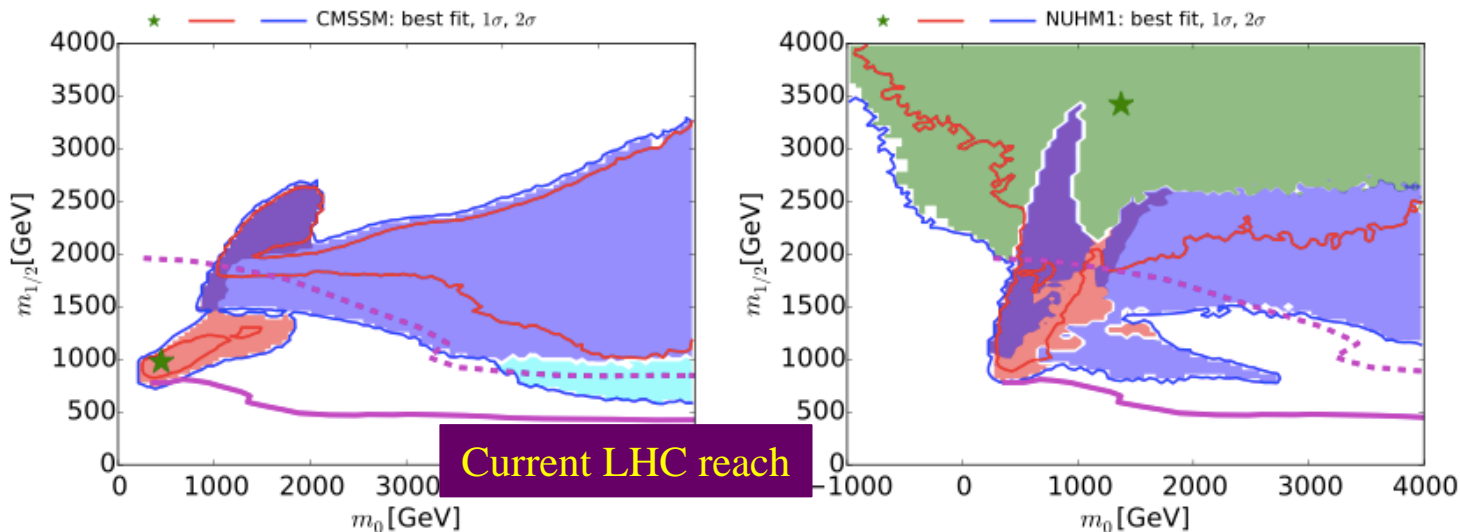
Probing the CMSSM with the LHC



Measuring the CMSSM with the LHC



Dark Matter in CMSSM, NUHM1/2, pMSSM10



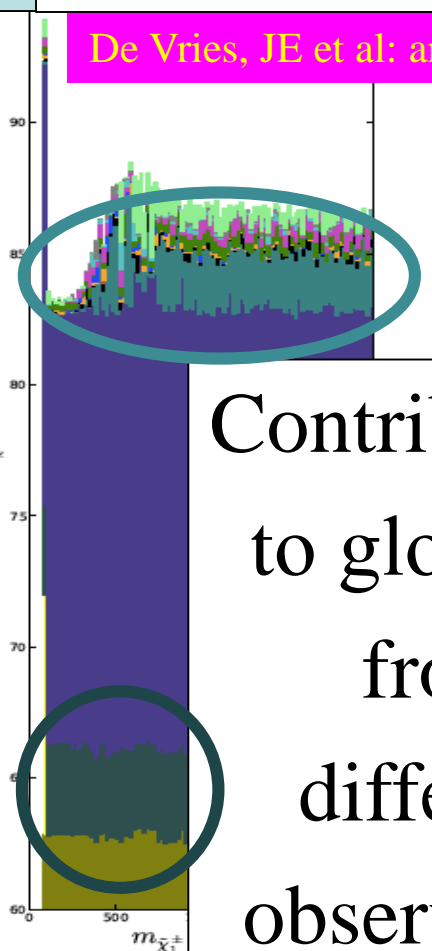
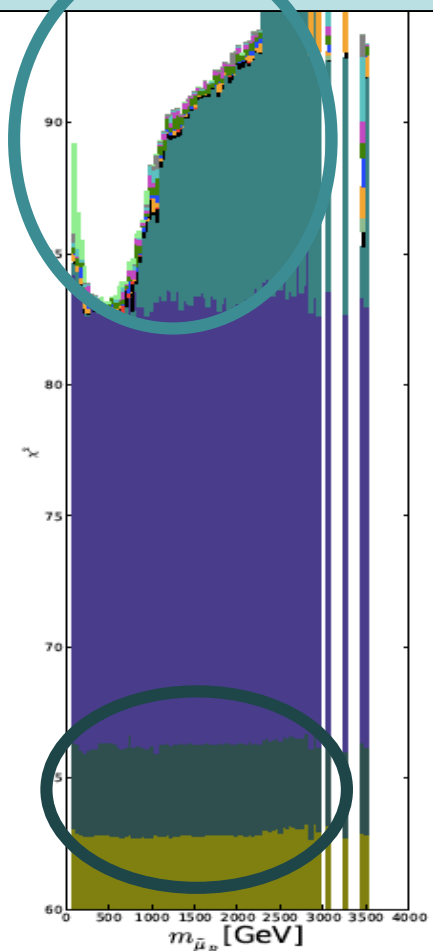
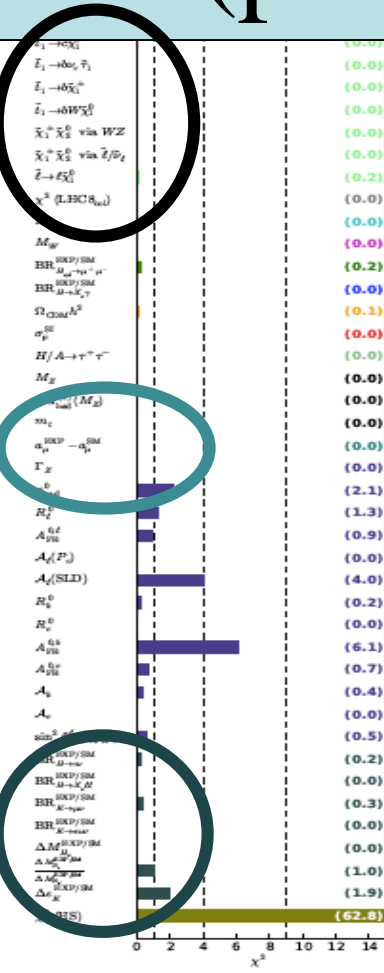
Phenomenological MSSM (pMSSM10)

- 3 gaugino masses : $M_{1,2,3}$,
- 2 squark masses : $m_{\tilde{q}_1} = m_{\tilde{q}_2} \neq m_{\tilde{q}_3}$,
- 1 slepton mass : $m_{\tilde{l}}$,
- 1 trilinear coupling : A ,
- Higgs mixing parameter : μ ,
- Pseudoscalar Higgs mass : M_A ,
- Ratio of vevs : $\tan \beta$.

LHC
MET
searches

$g_\mu - 2$

Flavour



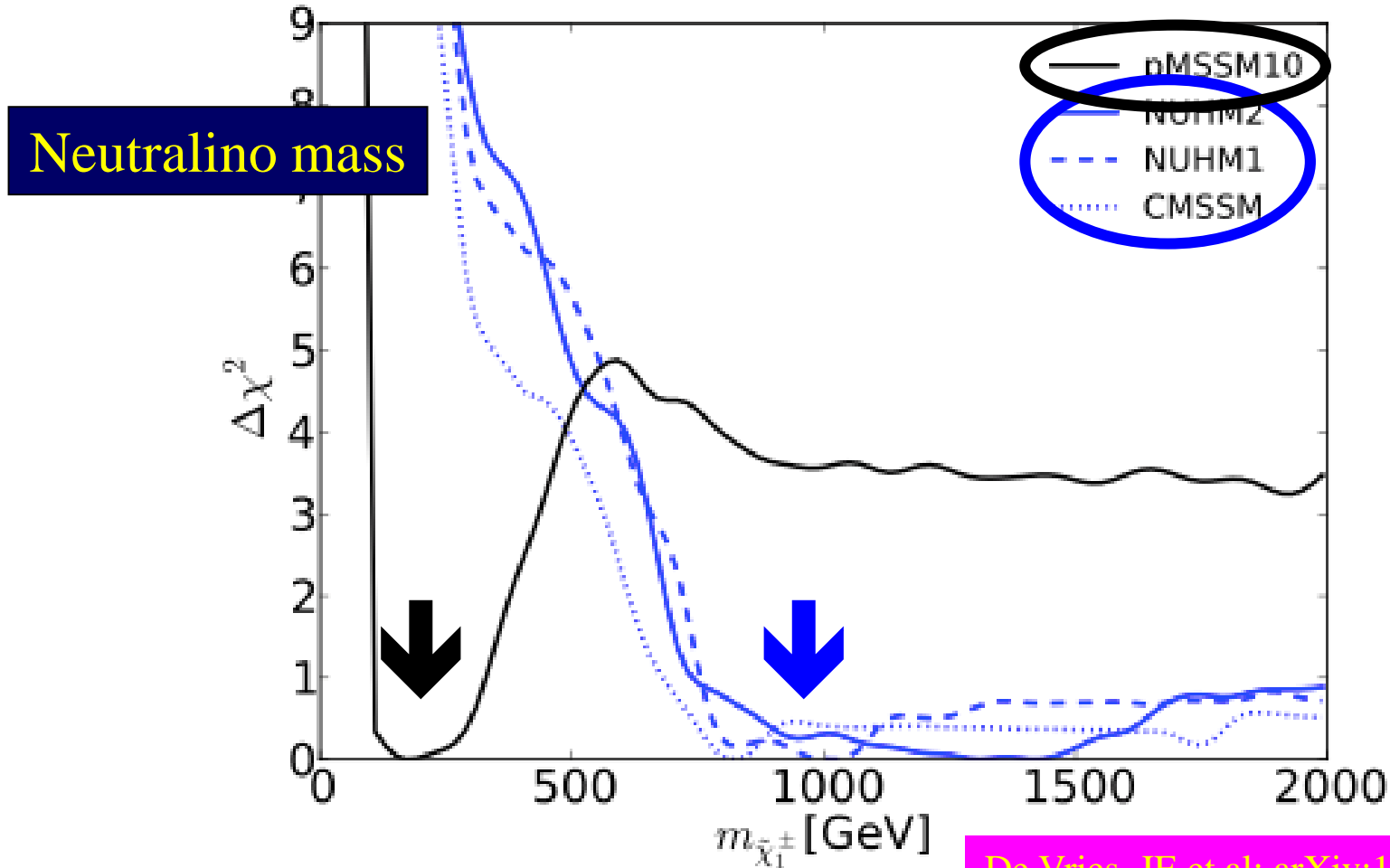
De Vries, JE et al: arXiv:1504.03260

Contributions
to global χ^2
from
different
observables



Possible Dark Matter Particle Mass

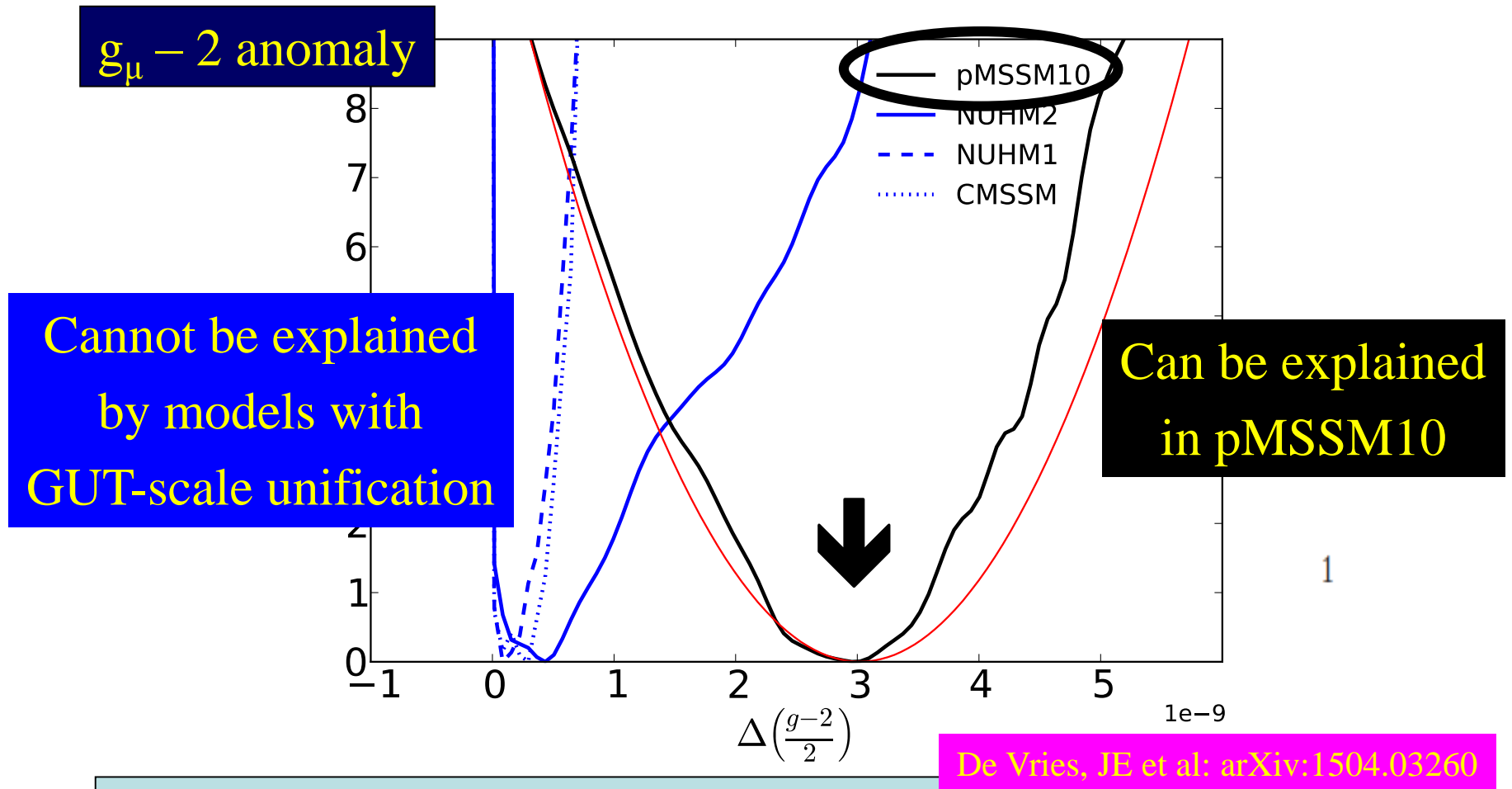
2012 ATLAS + CMS with 20/fb of LHC Data



pMSSM10 favours smaller masses than in models with GUT-scale unification

Anomalous Magnetic Moment of Muon

2012 ATLAS + CMS with 20/fb of LHC Data



pMSSM10 can explain experimental measurements of $g_\mu - 2$

Long-Lived Stau in CMSSM, NUHM?

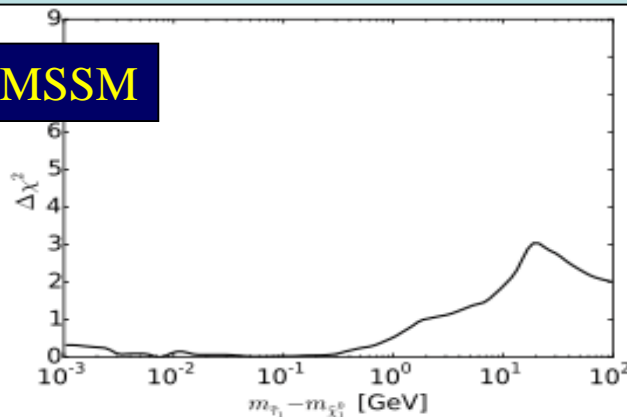
Possible if $m_{\text{stau}} - m_{\text{LSP}} < m_{\tau}$

Generic possibility in CMSSM, NUHM1, NUHM2

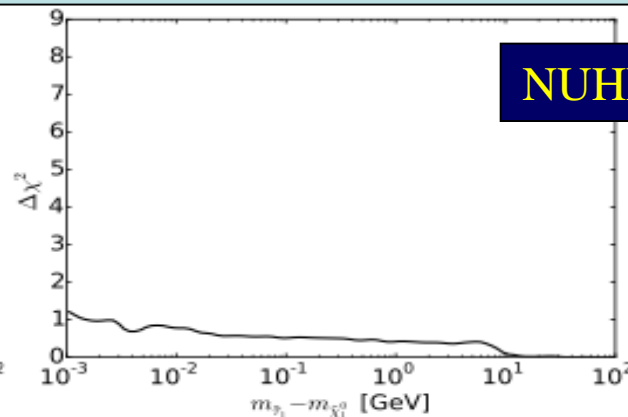
(stau coannihilation region)

Bagnaschi, JE et al: arXiv:1508.01173

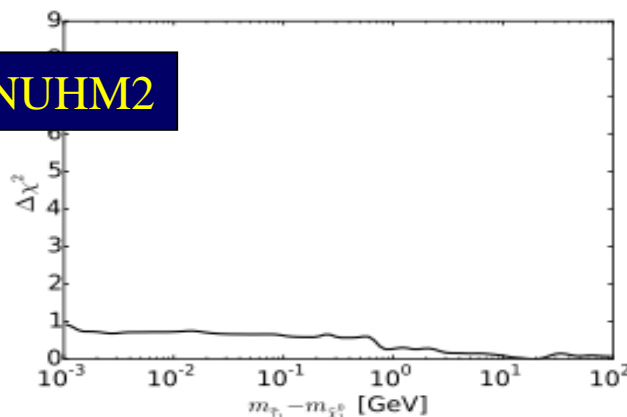
CMSSM



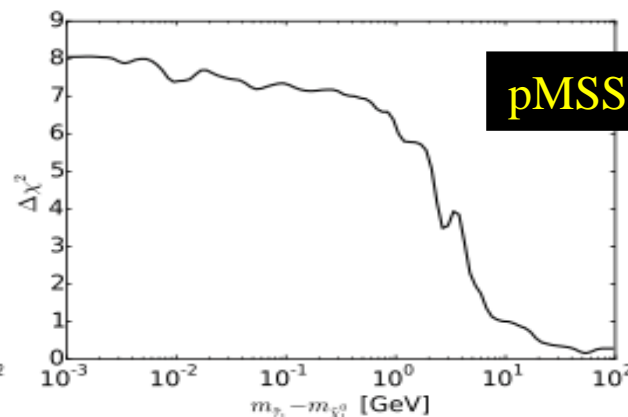
NUHM1



NUHM2



pMSSM10



$\tau_{\text{stau}} > 10^3$ s gives problems with nucleosynthesis

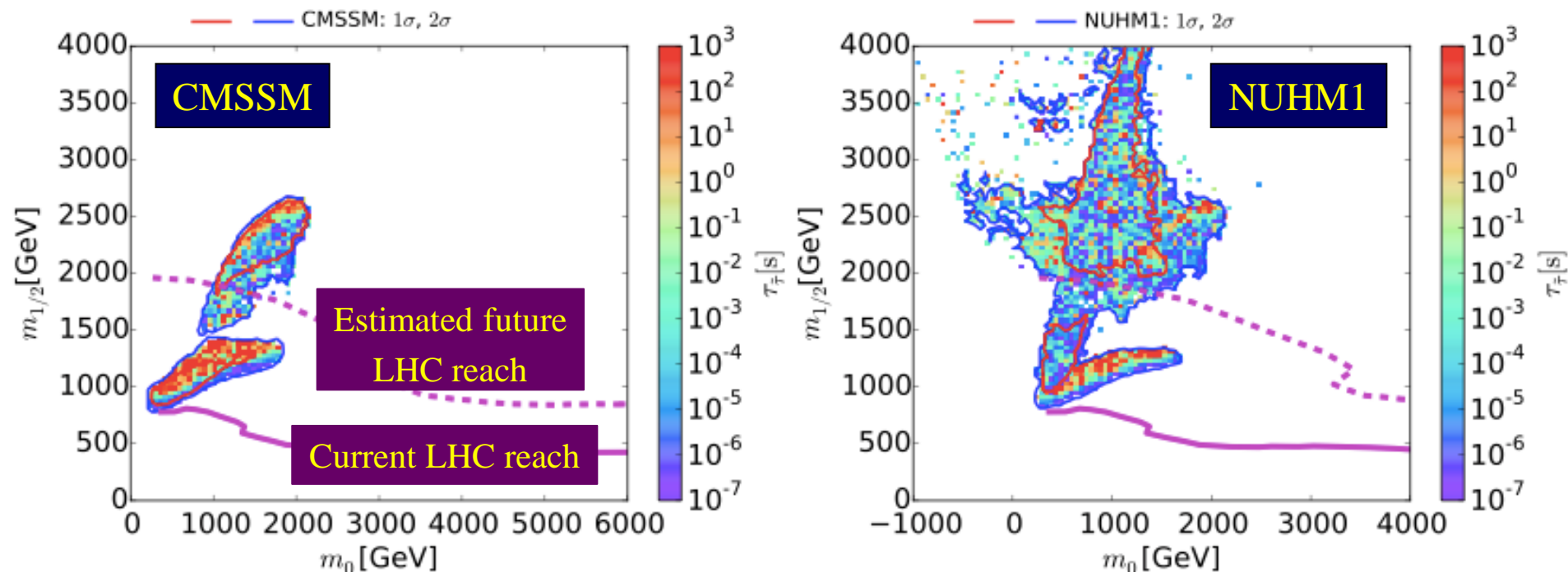
$\tau_{\text{stau}} > 10^{-7}$ s gives separated vertex signature

Long-Lived Stau in CMSSM, NUHM?

Possible if $m_{\text{stau}} - m_{\text{LSP}} < m_{\tau}$

Generic possibility in CMSSM, NUHM

(stau coannihilation region)

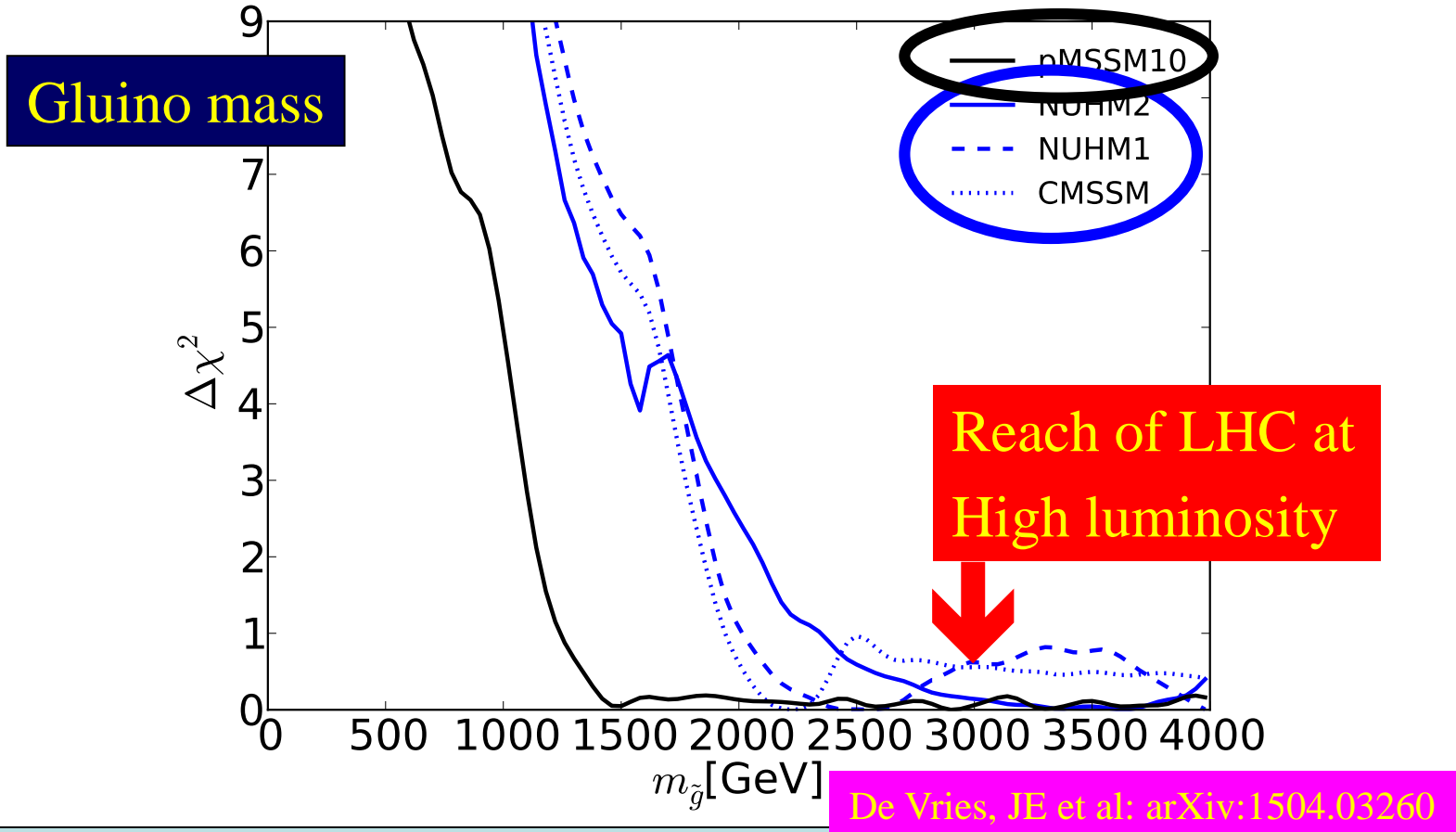


$\tau_{\text{stau}} > 10^3$ s gives problems with nucleosynthesis

$\tau_{\text{stau}} > 10^{-7}$ s gives separated vertex signature **for τ -like decays**

Fits to Supersymmetric Models

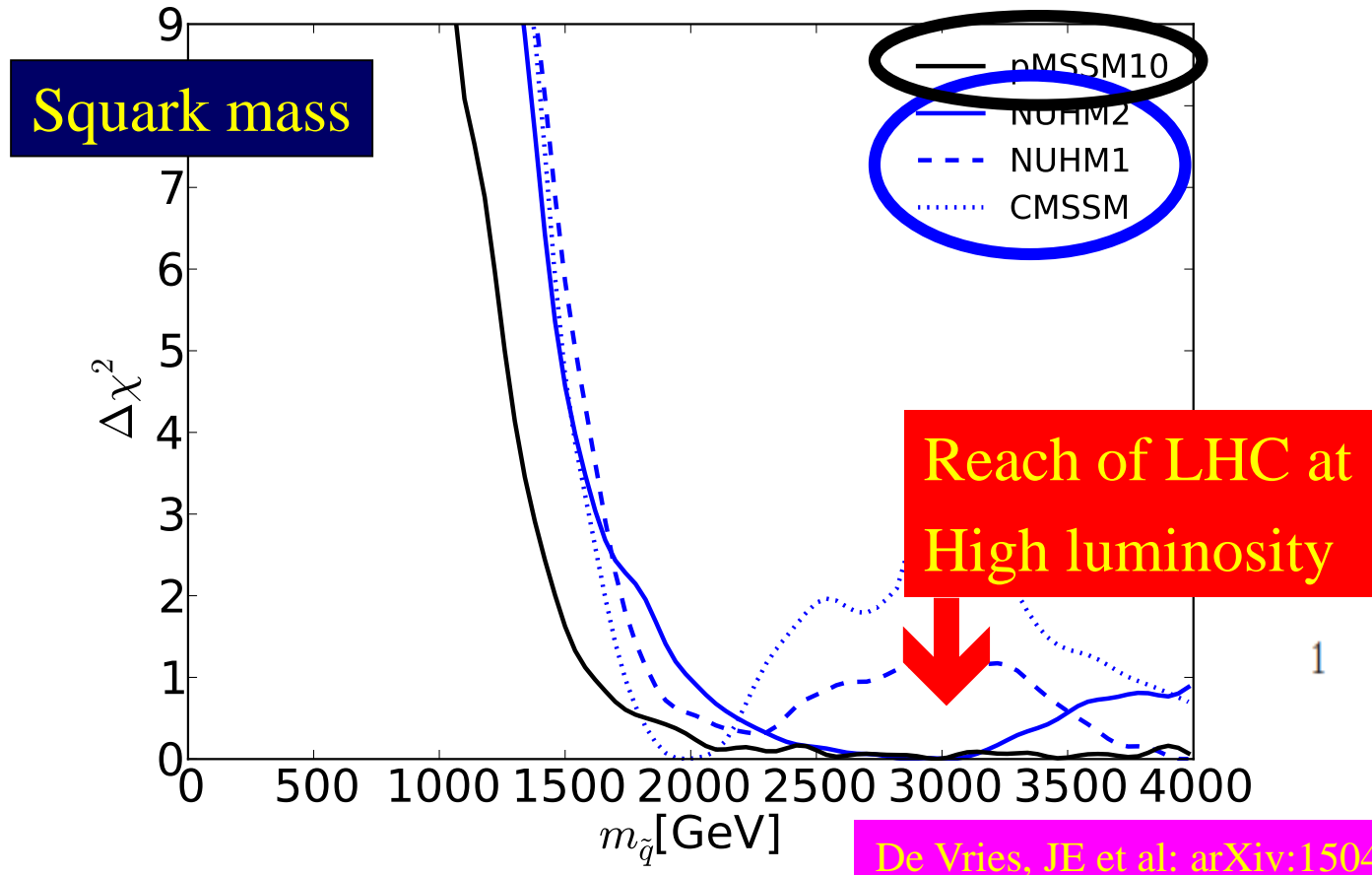
2012 ATLAS + CMS with 20/fb of LHC Data



Favoured values of gluino mass also significantly above pre-LHC, > 1.2 TeV

Fits to Supersymmetric Models

2012 ATLAS + CMS with 20/fb of LHC Data

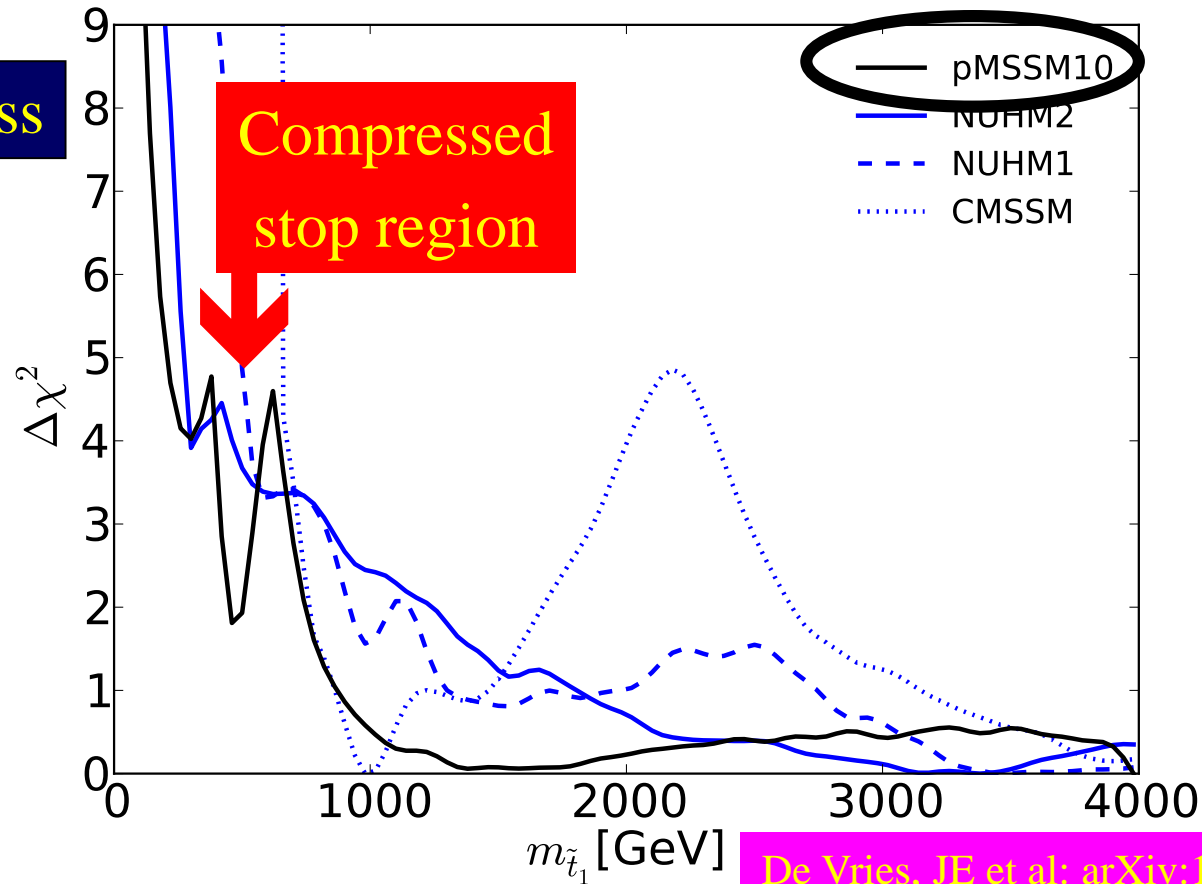


Favoured values of squark mass significantly above pre-LHC, ~ 1.5 TeV or more

Fits to Supersymmetric Models

2012 ATLAS + CMS with 20/fb of LHC Data

Stop mass



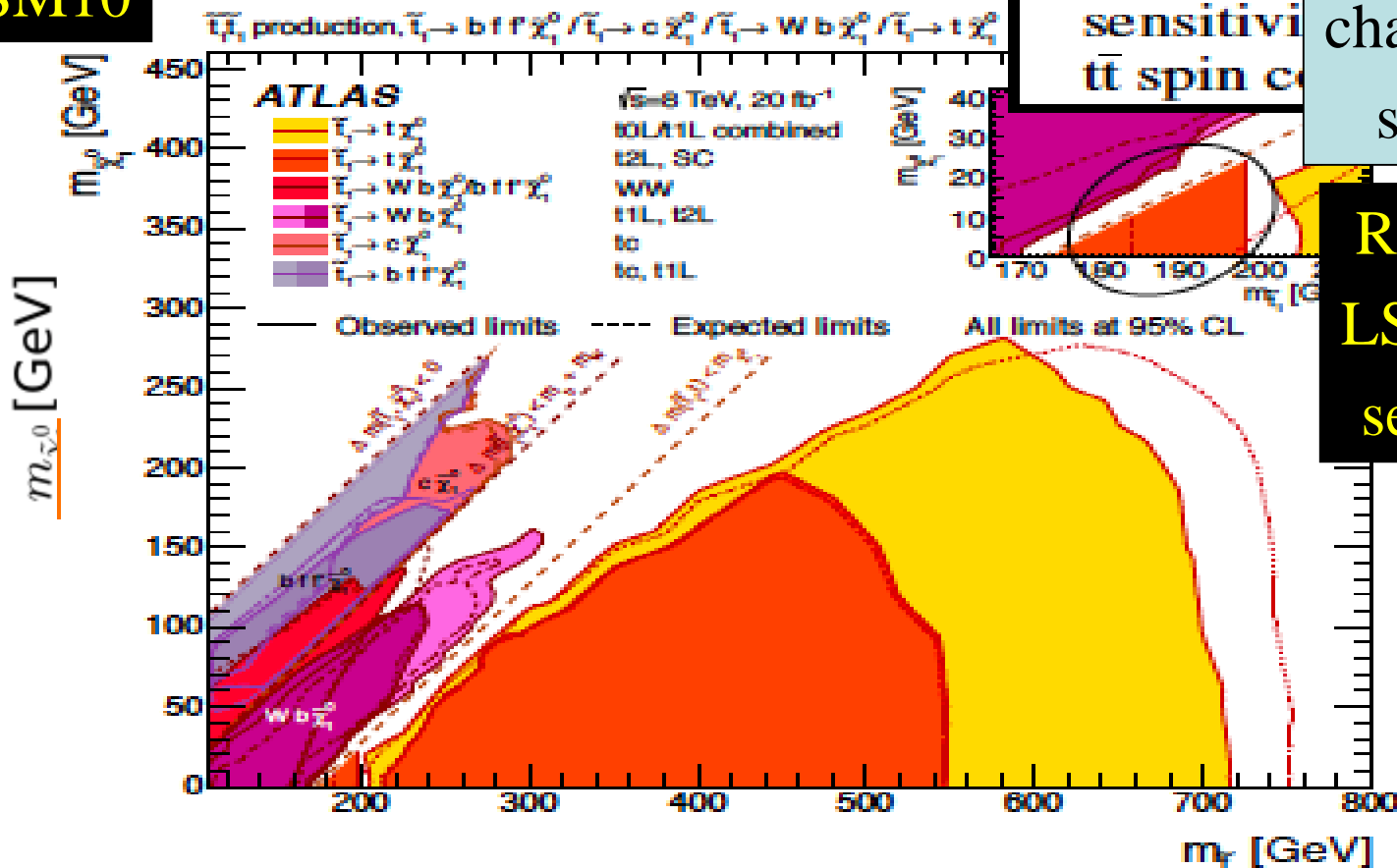
Remaining possibility of a light “natural” stop
weighing ~ 400 GeV

Exploring Light Stops @ Run 2



2012 ATLAS + CMS with 20/fb of LHC Data

pMSSM10



Reach of chargino + b searches

Reach of LSP + top searches

De Vries, JE et al: arXiv:1504.03260

Part of region of light “natural” stop weighing
 ~ 400 GeV can be covered

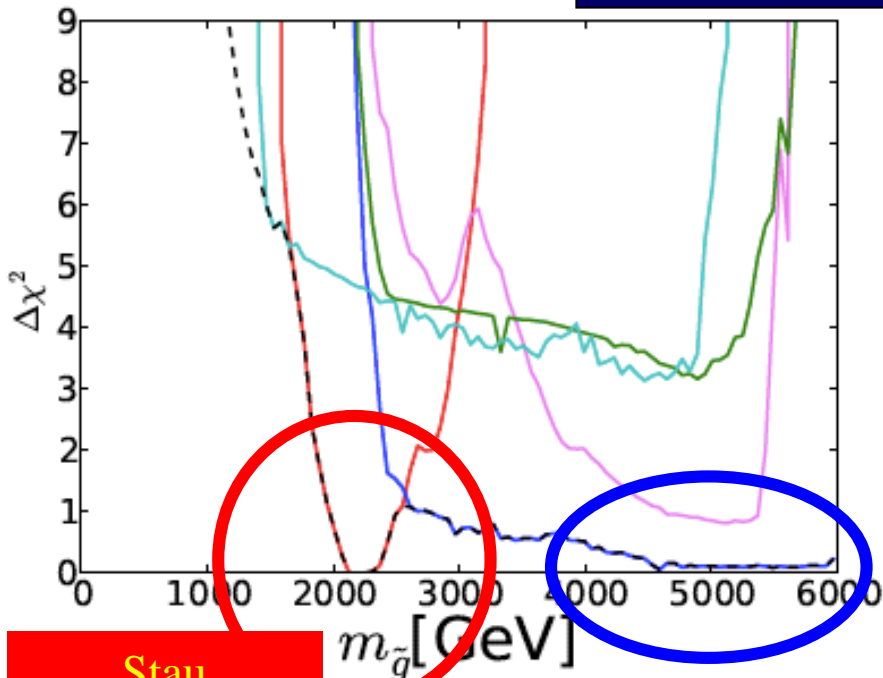
Fits to Supersymmetric Models



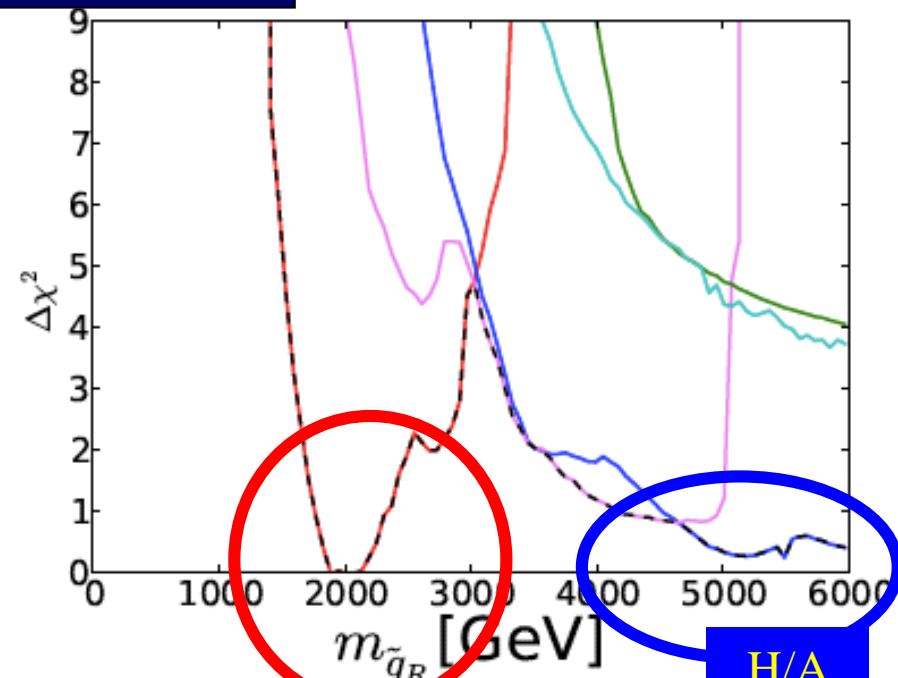
2012 ATLAS + CMS with 20/fb of LHC Data

Buchmueller, JE et al: arXiv:1312.5250

Glino and squark masses



Stau
coannihilation

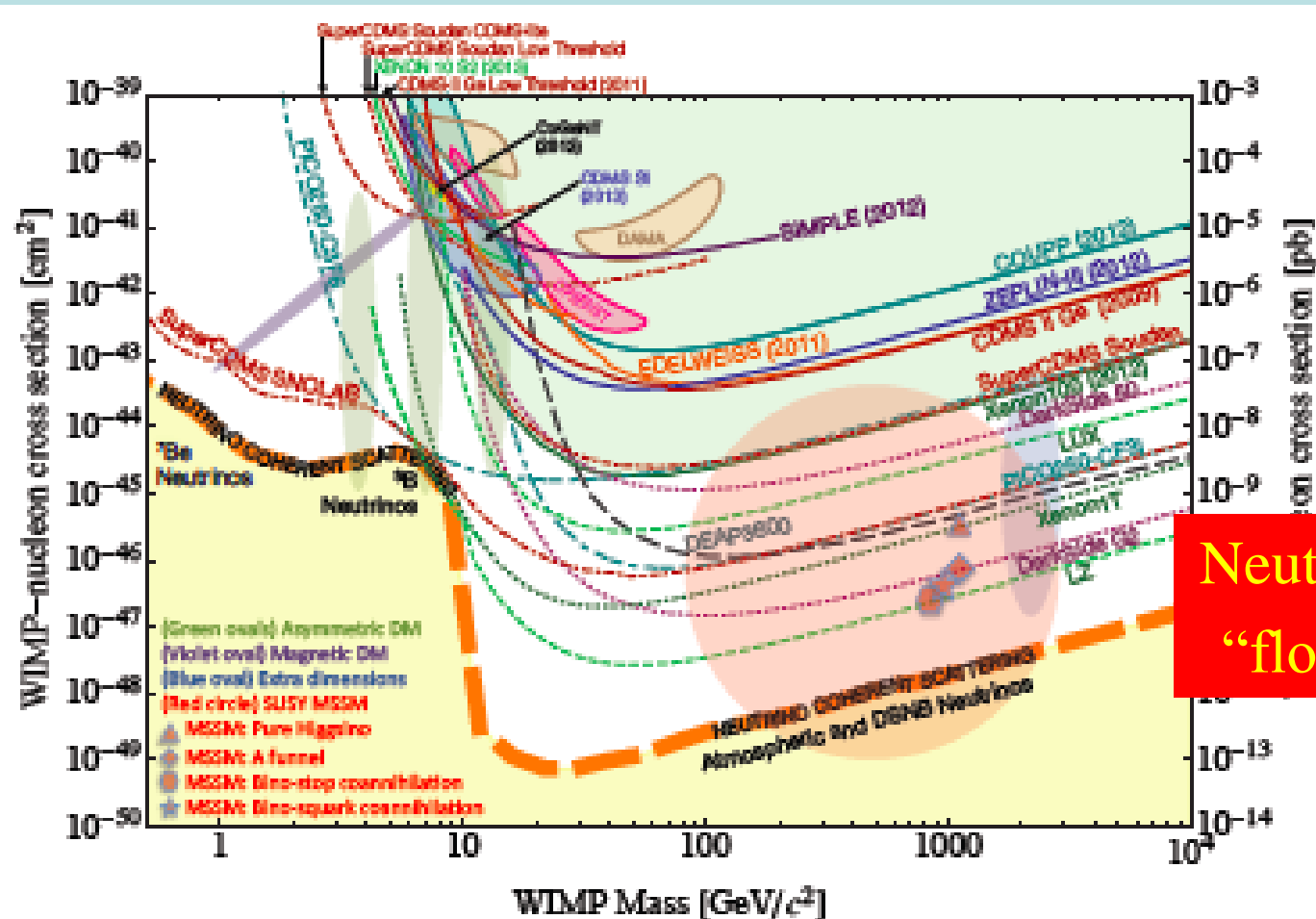


H/A
funnel

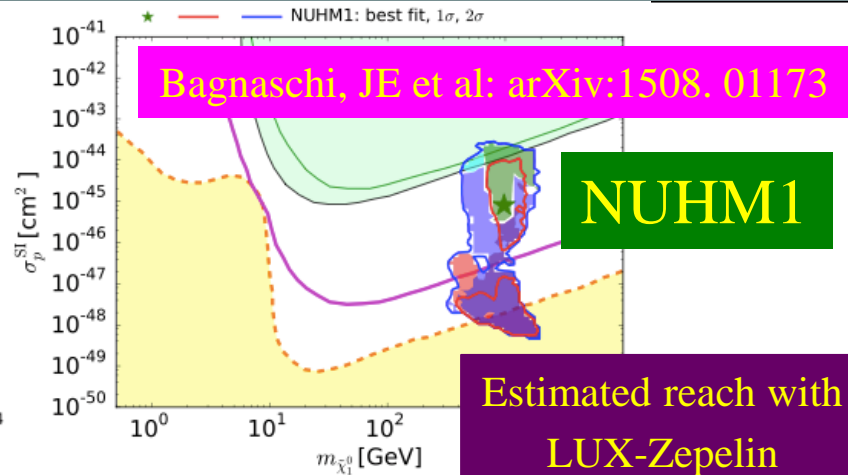
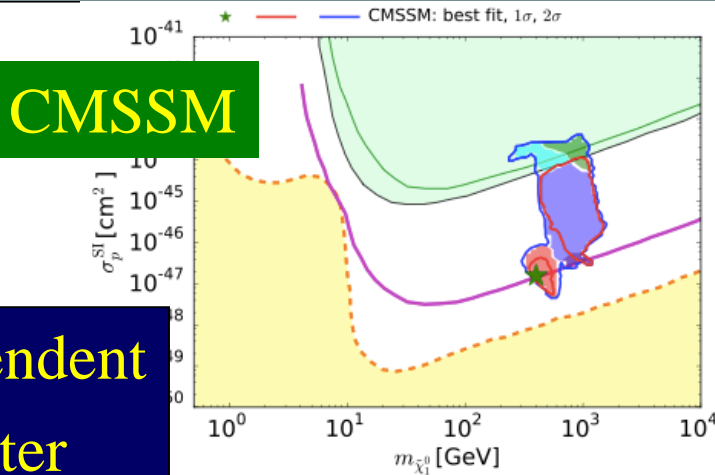
Favoured values of gluino and squark masses significantly above pre-LHC, ~ 2 TeV or more

Direct Dark Matter Searches

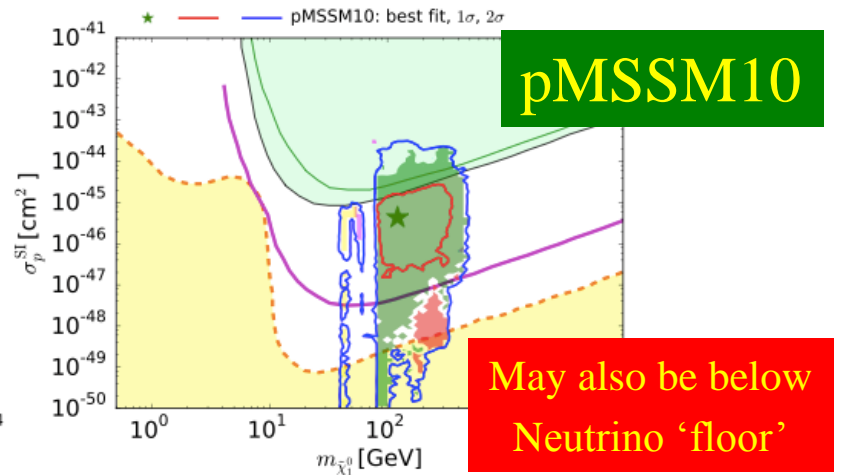
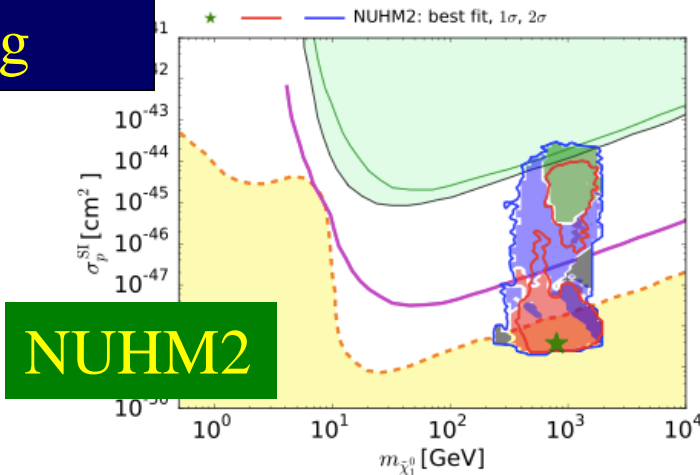
- Compilation of present and future sensitivities



Direct Dark Matter Search



Spin-independent dark matter scattering



- | | | | |
|--|--|--|---|
| stau coann. | hybrid | stop coann. | h funnel |
| A/H funnel | $\tilde{\chi}_1^\pm$ coann. | focus point | Z funnel |

Direct scattering cross-section may be very close to LUX upper limit, accessible to LZ experiment

Prospects for SUSY Searches

- Different models, various dark matter mechanisms

DM mechanism	Exp't	Models			
		CMSSM	NUHM1	NUHM2	pMSSM10
$\tilde{\tau}_1$ coann.	LHC DM	$\checkmark \cancel{E}_T, \checkmark LL$ (\checkmark)	($\checkmark \cancel{E}_T, \checkmark LL$) (\checkmark)	($\checkmark \cancel{E}_T, \checkmark LL$) \times	($\checkmark \cancel{E}_T$), $\times LL$ \times
$\tilde{\chi}_1^\pm$ coann.	LHC DM	– –	\times \checkmark	\times \checkmark	($\checkmark \cancel{E}_T$) (\checkmark)
\tilde{t}_1 coann.	LHC DM	– –	– –	$\checkmark \cancel{E}_T$ \times	– –
A/H funnel	LHC DM	$\checkmark A/H$ \checkmark	($\checkmark A/H$) \checkmark	($\checkmark A/H$) (\checkmark)	– –
Focus point	LHC DM	($\checkmark \cancel{E}_T$) \checkmark	– –	– –	– –
h, Z funnels	LHC DM	– –	– –	– –	($\checkmark \cancel{E}_T$) (\checkmark)

- No guarantees, but good prospects