



## Second Lecture

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# 3. SINGLE TOP PRODUCTION



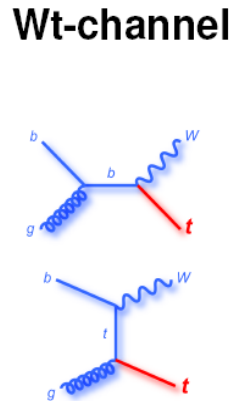
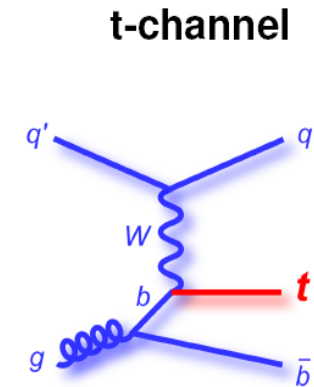
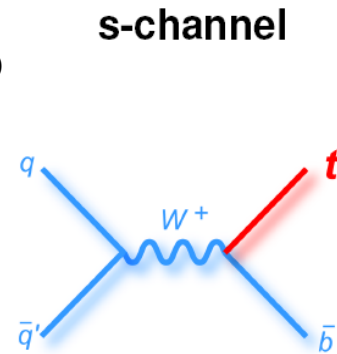
# 3.1 Cross Section, Couplings

Observation of single top production:

- cross section  $\propto V_{tb}^2$
- study top-polarization and EWK top interaction

Test of non-SM phenomena:

- 4th generation
- FCNC couplings
- $W'$ ,  $H^\pm$
- anomalous  $W_{tb}$  couplings



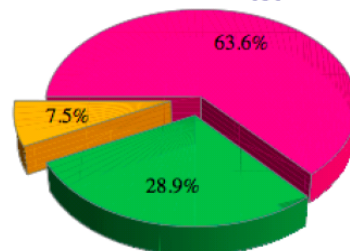
Main backgrounds:

- s-channel: Top pair,  $W$  + (HF) jets, QCD
- t-channel: Top pair,  $W$  + (HF) jets, QCD
- Wt-channel: Top pair,  $Z$  + (HF) jets, QCD

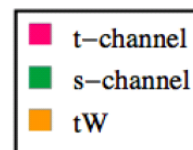
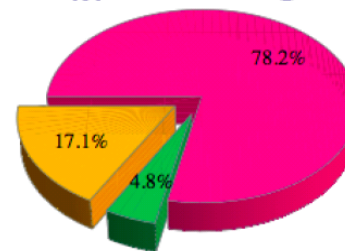
Signal – background discrimination:

- Tevatron: multivariate methods (neural networks, boosted decision trees, matrix element method)
- LHC: cut-based or multivariate method

**Tevatron:  $\sigma_{tot} = 3 \text{ pb}$**



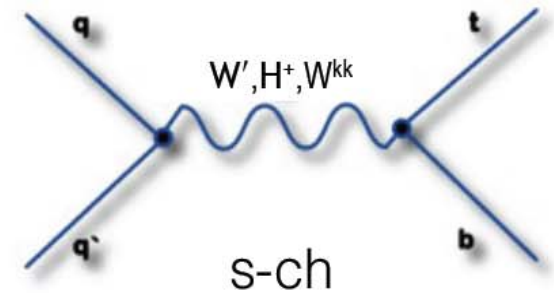
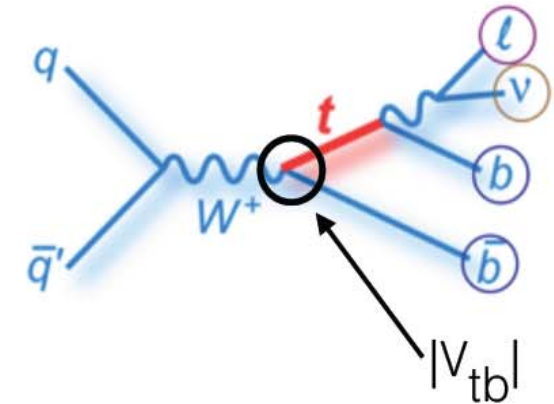
**LHC:  $\sigma_{tot} = 114 \text{ pb @ 8 TeV}$**



$$\sigma_{\text{single top}} \propto |V_{tb}|^2$$

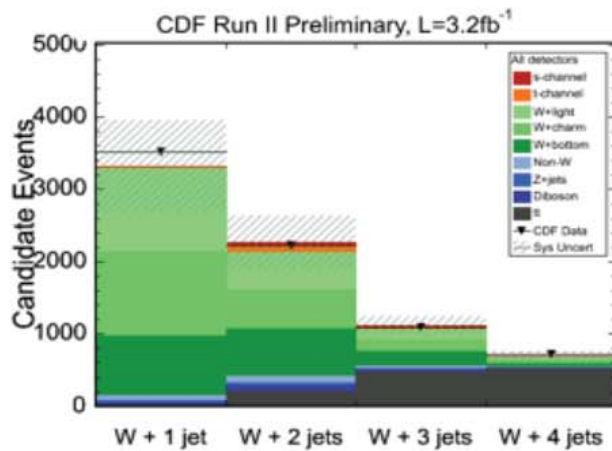
- Direct measurement of  $|V_{tb}|$  CKM matrix element;
- Does unitarity holds?  $|V_{ub}|^2 + |V_{cb}|^2 + |V_{tb}|^2 = 1$

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} & V_{uX?} \\ V_{cd} & V_{cs} & V_{cb} & V_{cX?} \\ V_{td} & V_{ts} & V_{tb} & V_{tX?} \\ V_{Yd?} & V_{Ys?} & V_{Yt?} & V_{YX?} \end{pmatrix}$$



### Sensitivity to new physics

- t-ch: FCNC
- s-ch: heavy  $W'$ , Top pion



### The Challenge

Single top quark production with decay into  $W + 2 \text{ Jets}$  (dominated by  $W + \text{jets}$ ):

final state hidden behind **large backgrounds** with large uncertainties (i.e.  $W + \text{HF}$  uncertainty  $\sim 30\%$ )

→ MVA using Multiple variables combined into a single more powerful discriminant to separate S from B

## Electroweak/Top: Single Top, ttbar, diboson

- modeled by Monte Carlo (MC)
  - single top: **POWHEG** (CDF), **COMPHEP** (DØ)
  - ttbar: **PYTHIA** (CDF), **ALPGEN** (DØ)
  - diboson, WH: **PYTHIA**
- normalized to theoretical cross section

## W+jets:

- modeled by **ALPGEN+PYTHIA** Monte Carlo (MC)
- normalisation and flavour composition from data

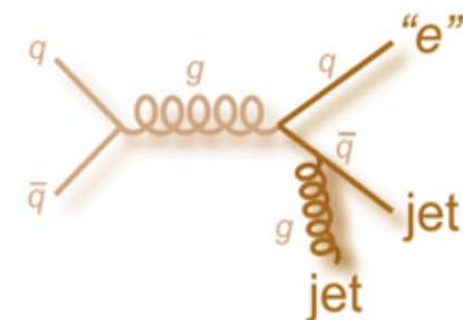
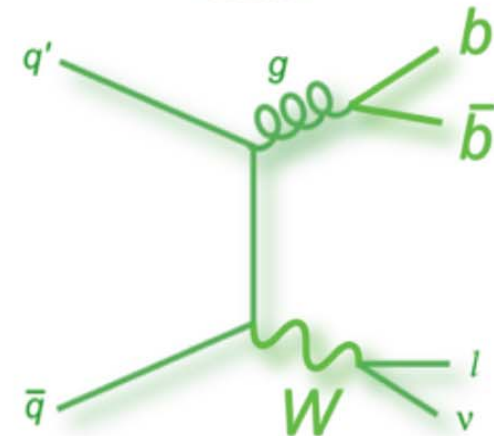
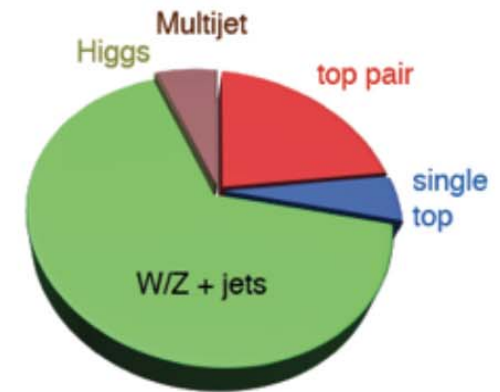
## Mistags:

- falsely tagged light quark or gluon jet
- mistag probability from data

**Z+jets:** modeled by **ALPGEN+PYTHIA** MC

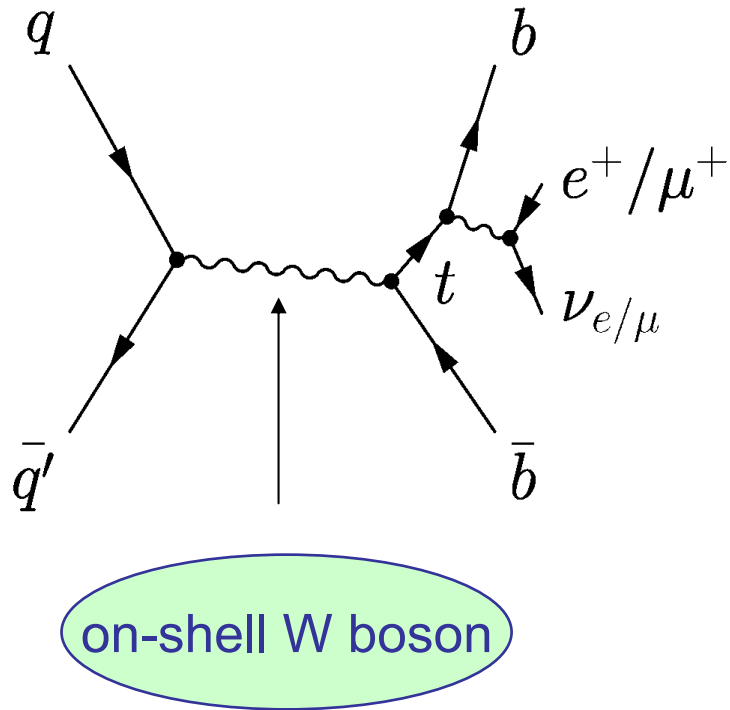
## Multijet:

- Normalisation and shape from data-driven model



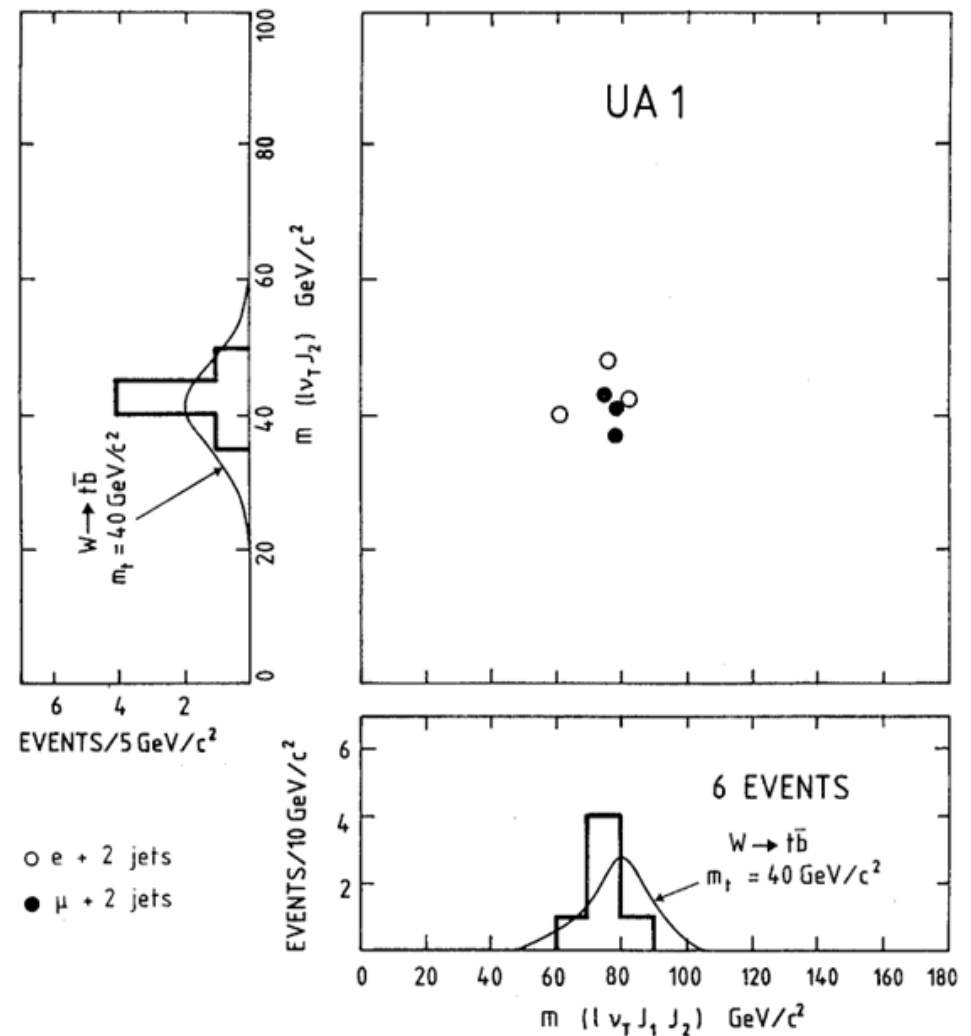


# First "Observation" of Single Top



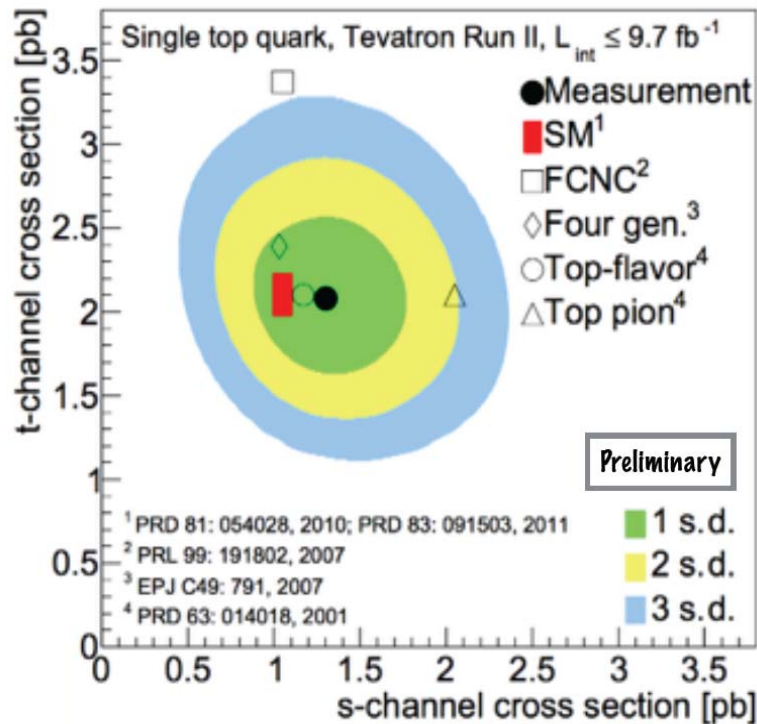
... by UA1 at CERN Sp $\bar{p}$ S

- excess in  $M_{lvb}$  vs.  $M_{lvbb}$  scatter plot
- compatible with  $m_t = 40 \pm 10$  GeV
- later improved background estimate



**Phys. Lett. B 147, 493 (1984)**

Combined CDF, D0  
Legacy Measurement  
From the Tevatron!



Fermilab-CONF-14-370-E

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

- Consistent with NLO+NNLL prediction
- Measure  $V_{tb}$  directly (no assumption on CKM unitarity) →
- Precisely measure s and t channels

$$\begin{aligned} |V_{tb}| &= 1.12^{+0.09}_{-0.08} \quad (\text{D0}) \\ |V_{tb}| &= 0.95 \pm 0.09 \quad (\text{CDF}) \end{aligned}$$

Gregorio Bernardi / I.PNHE-Paris

$$|V_{tb,meas}|^2 = \frac{\sigma_{meas}}{\sigma_{SM}} \cdot |V_{tb,SM}|^2$$

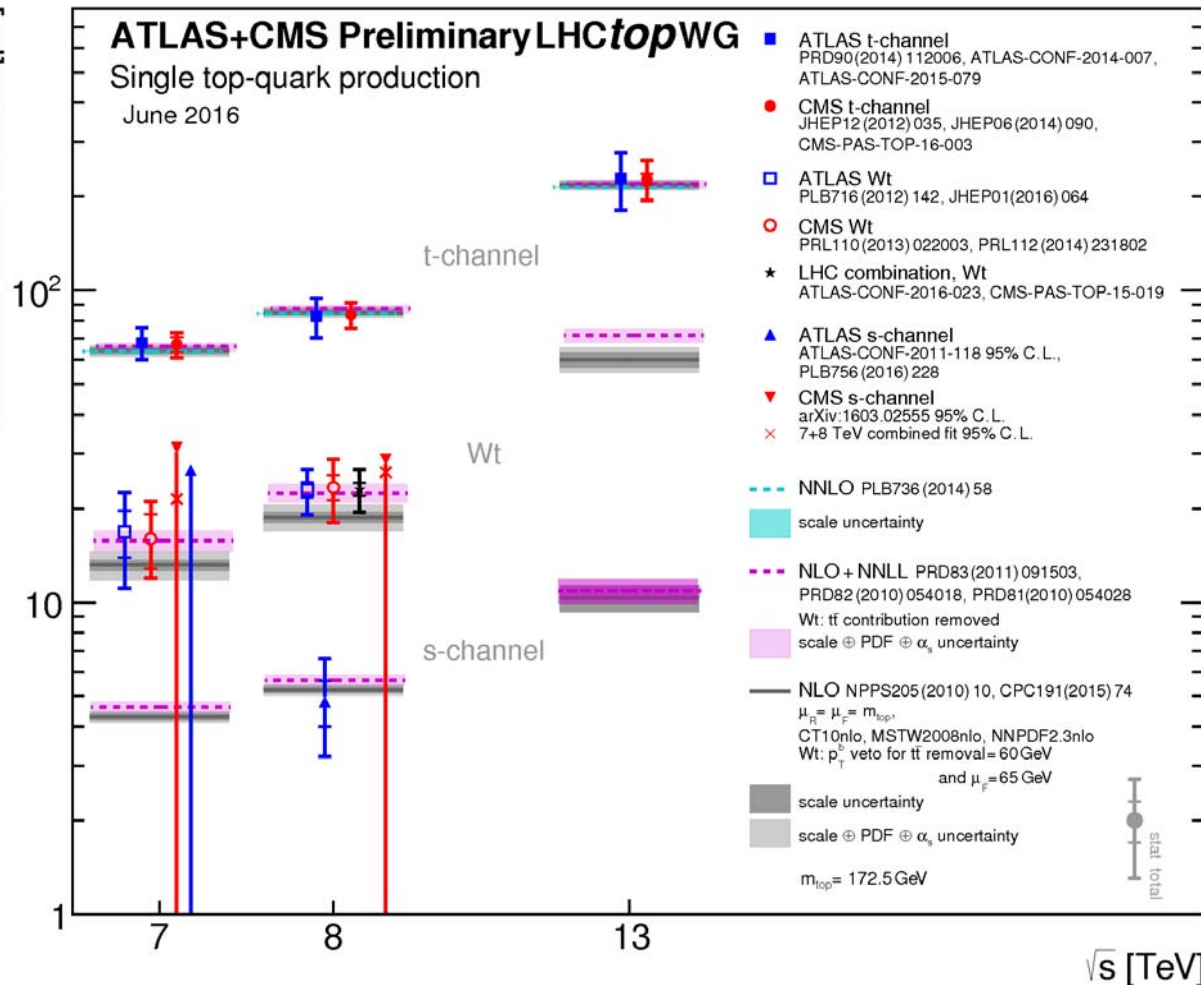
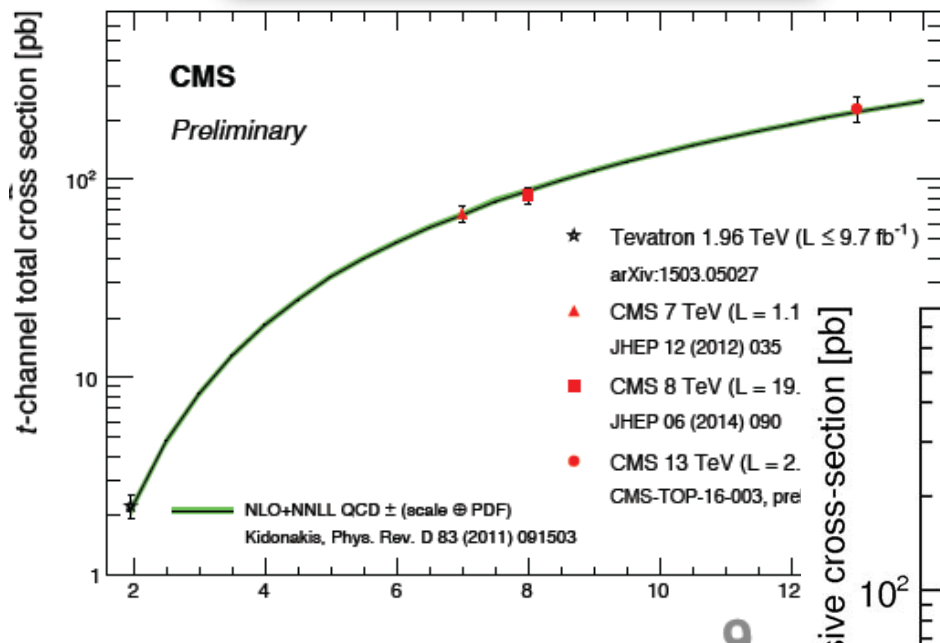
- No assumption about number of generations
- Assumption:  $|V_{ts}|^2 + |V_{td}|^2 \ll |V_{tb}|^2$



# Single Top at the LHC



## CMS PAS TOP-16-003



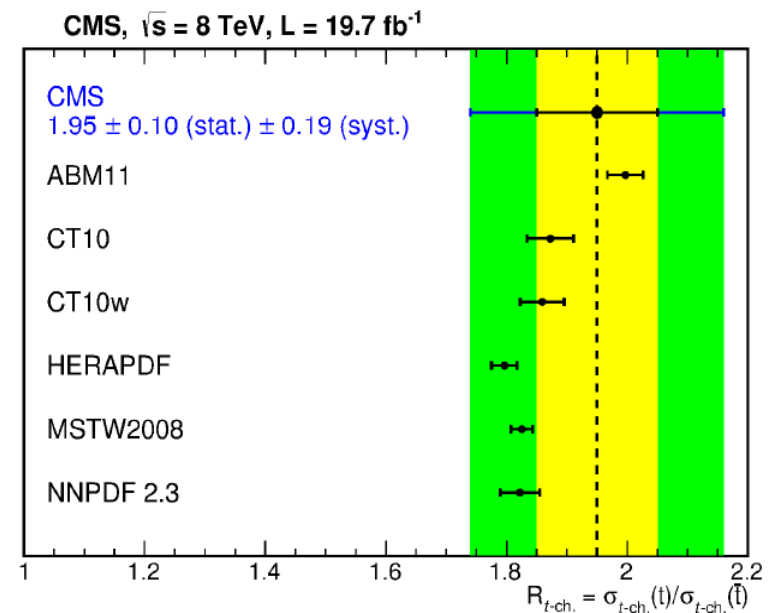


# Ratio $R_t = \sigma_t / \sigma_{\bar{t}}$

- $R_t$  is sensitive to the u/d PDFs; naïve expectation  $R_t = 2$
- Measurement of  $\sigma_t$  using binned max. likelihood fit to NN output in 2-jets and 3-jets data split according to charge of lepton
- The measured ratio of single t to  $\bar{t}$  production cross sections at  $\sqrt{s} = 8$  TeV:

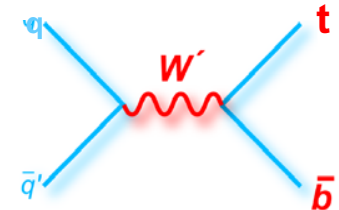
$$R_{t\text{-ch.}} = \sigma_{t\text{-ch.}}(t) / \sigma_{t\text{-ch.}}(\bar{t}) = 1.95 \pm 0.10 \text{ (stat.)} \pm 0.19 \text{ (syst.)}$$

The measurement is in agreement with the predictions based on various global PDF sets that range from 1.86 to 2.07.



Wajid Khan, PhD Thesis.

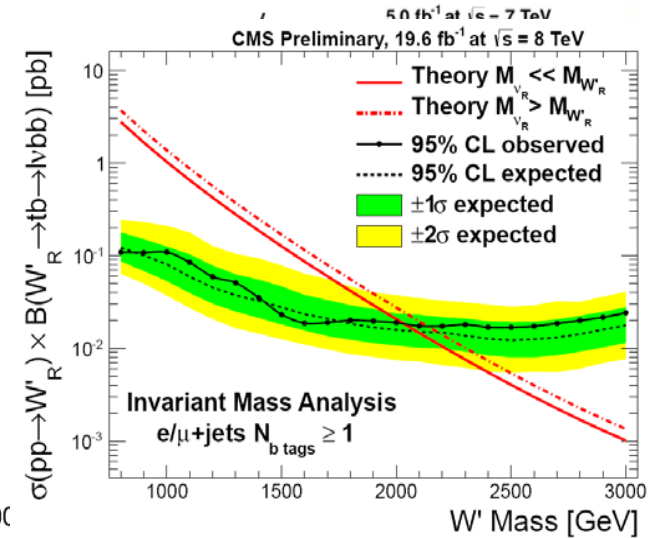
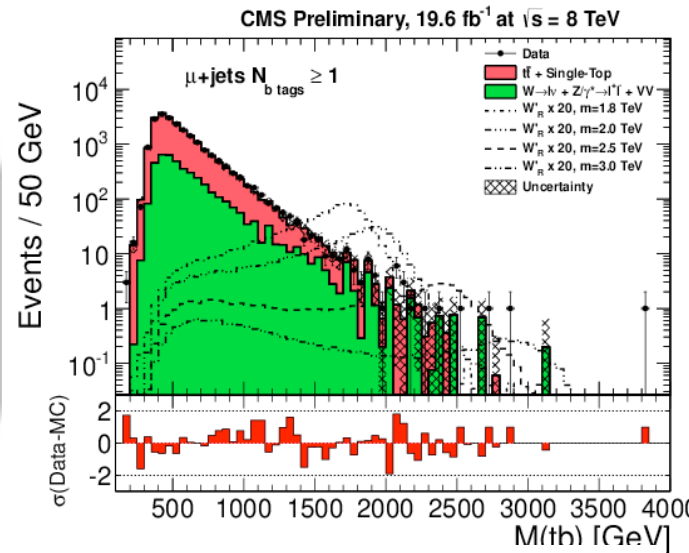
- Right-handed  $W'_R$  with SM-like couplings chosen as benchmark model
- Similar signature as single top s-channel (1 lepton, MET, 2 jets and at least 1  $b$  tag)



**CMS-PAS-B2G-12-010**

**CMS**

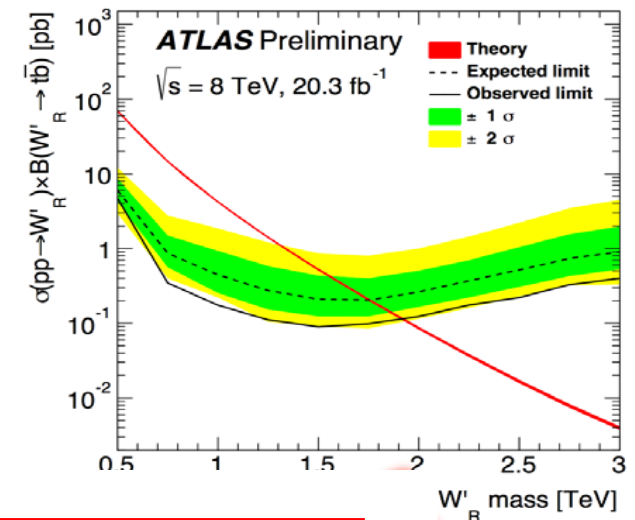
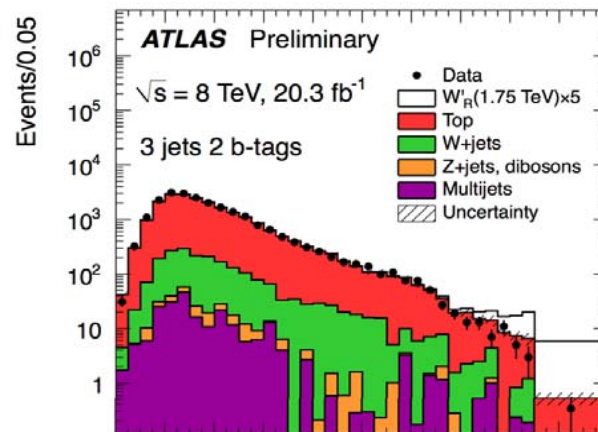
- BDT used to discriminate signal from background



<http://arxiv.org/abs/1205.1016>

**ATLAS**

- Invariant mass of  $tb$  system used as discriminating variable



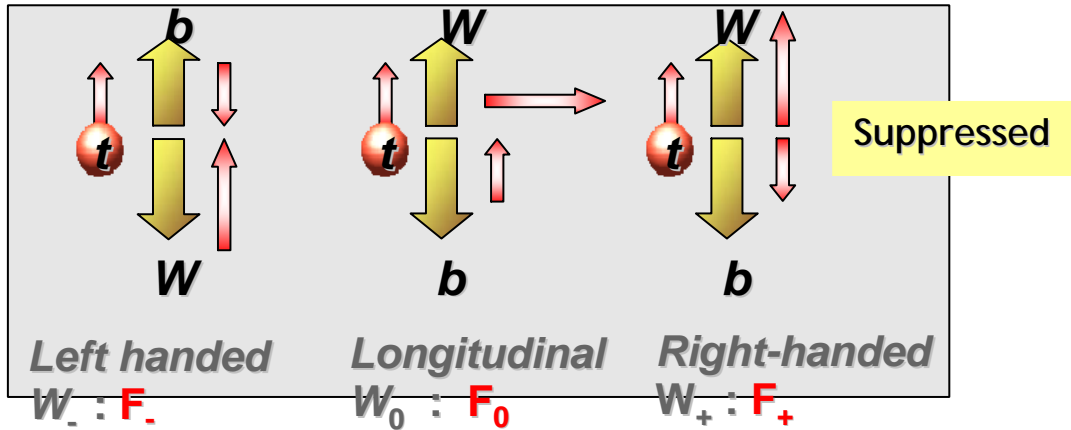
Observed limits (ATLAS, CMS):  $m_{W'_R} > 1.8/ 2.0$  TeV

# 4. DECAY PHYSICS: W HELICITY

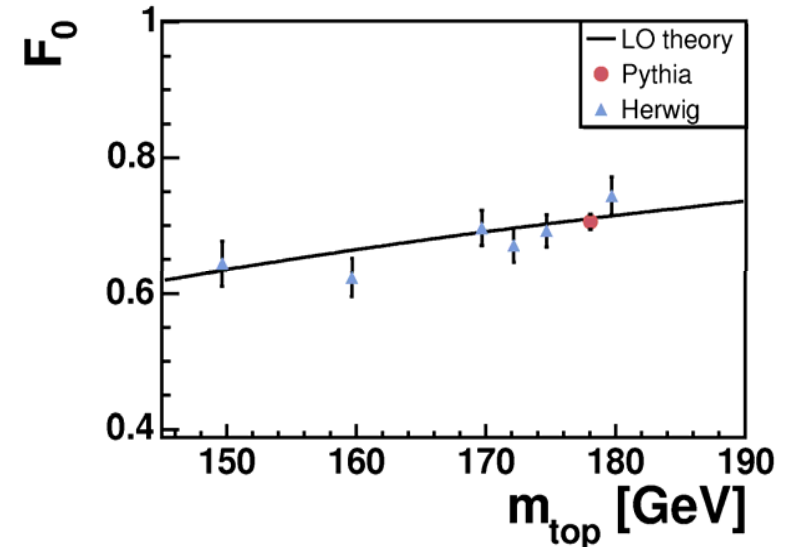
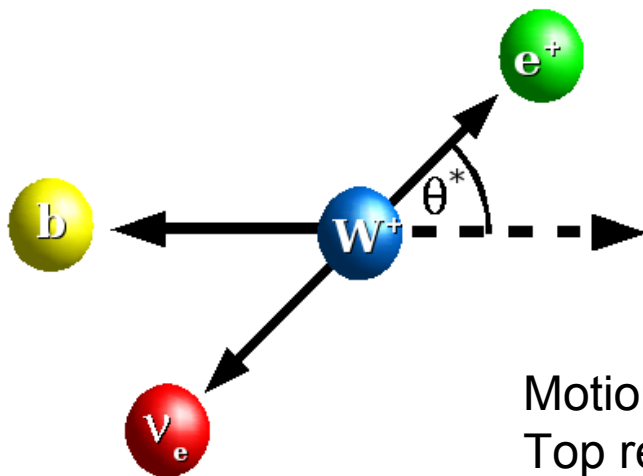


# 4.1 W-Helicity

Three possible helicities:



$$F_0 = \frac{m_t^2}{2M_W^2 + m_t^2}$$



Distribution of Angle  $\theta^*$  between charged lepton in W system and W-Boson in Top-Quark system:

$$\frac{dN_{h_W=-1}}{d(\cos\theta^*)} \sim \frac{3}{8}(1 - \cos\theta^*)^2$$

SM:  
 $F_- = 0.31$

$$\frac{dN_{h_W=0}}{d(\cos\theta^*)} \sim \frac{3}{4}(1 - \cos^2\theta^*)$$

$F_0 = 0.69$

$$\frac{dN_{h_W=+1}}{d(\cos\theta^*)} \sim \frac{3}{8}(1 + \cos\theta^*)^2$$

$F_+ = 0.001$

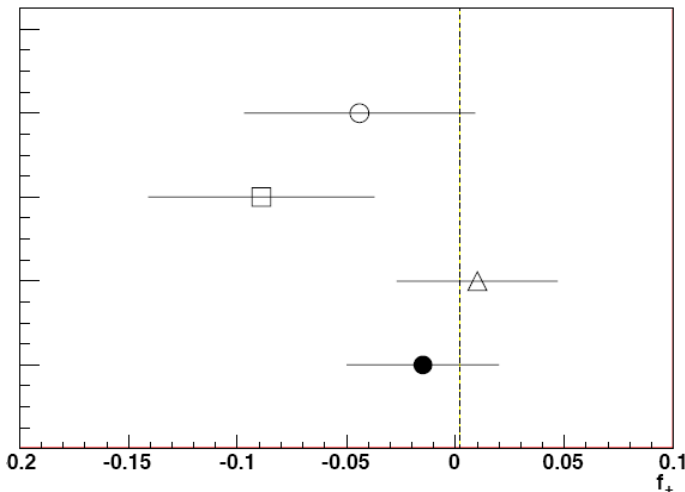
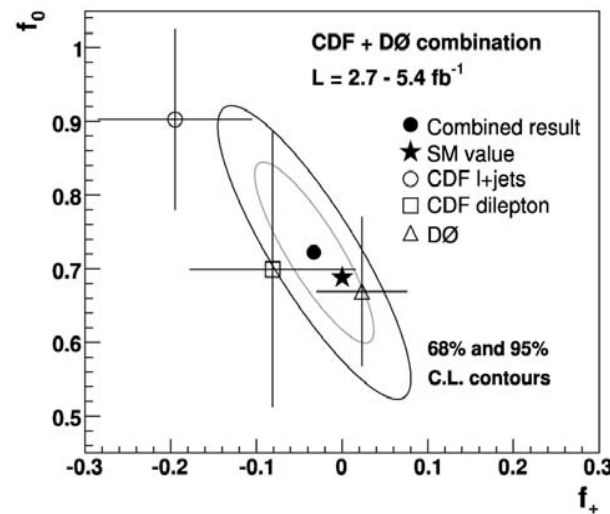
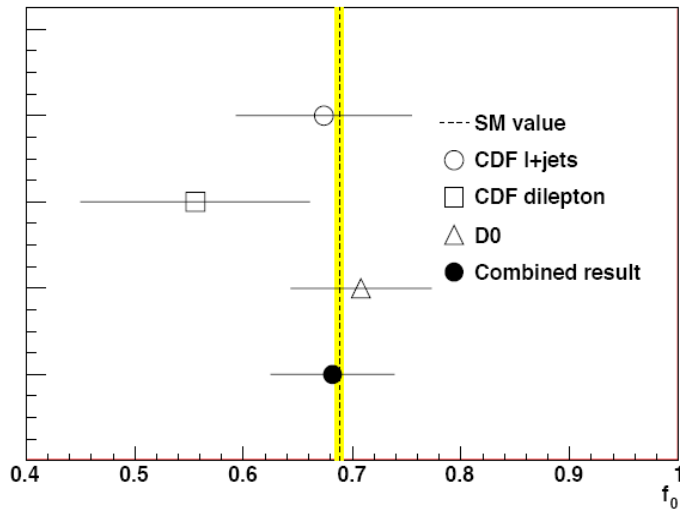
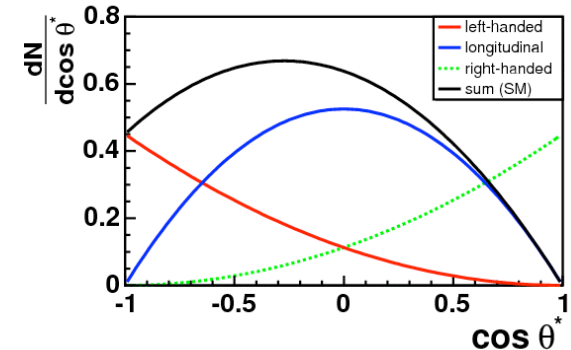
A. Czarnecki, J. G. Körner, J. H. Piclum, Phys. Rev. D 81, 111503

(2010)



With three helicity fractions, there are two independent quantities to measure (3rd fraction is fixed since  $\Sigma f = 1$ )

- We choose to measure  $f_0$  and  $f_+$
- Can either measure both fractions simultaneously (2D fit)
- or fix one fraction to its SM value and measure the other (1D fit)



Tevatron Combo

$$\begin{aligned}
 2D: f_0 &= 0.722 \pm 0.062 \pm 0.052 \\
 f_+ &= -0.033 \pm 0.034 \pm 0.031 \\
 1D: f_0 &= 0.682 \pm 0.035 \pm 0.046 \\
 f_+ &= -0.015 \pm 0.018 \pm 0.030
 \end{aligned}$$

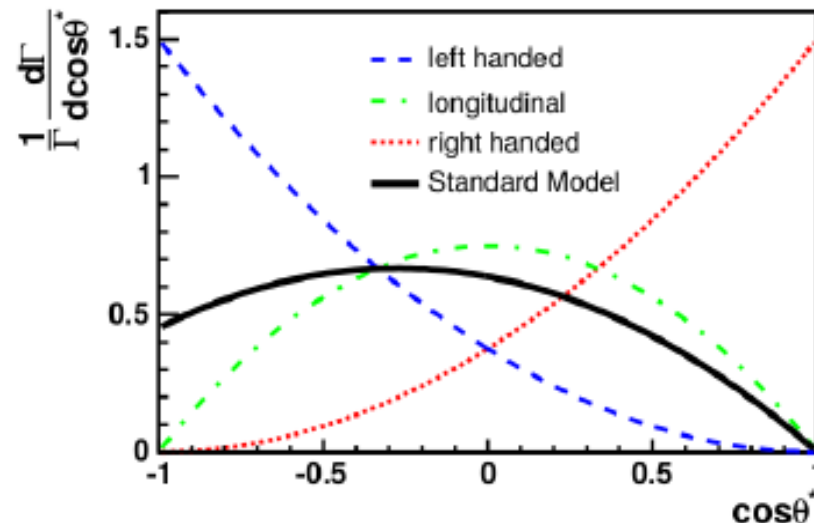
**PRD85, 071106 (2012)**



$$\frac{1}{\Gamma} \frac{d\Gamma}{d\cos\theta^*} = F_0 \cdot \frac{3}{4}(1 - \cos^2\theta^*) + F_- \cdot \frac{3}{8}(1 - \cos\theta^*)^2 + F_+ \cdot \frac{3}{8}(1 + \cos\theta^*)^2$$

$$(SM: F_0 = 0.69 \quad F_- = 0.31 \quad F_+ \sim 0)$$

- **$\mu$ +jets** channel
- Reconstruct top quark kinematics
- Fit to the  **$\cos\theta^*$**  distribution
- Results are based on  **$19.6\text{fb}^{-1}$**



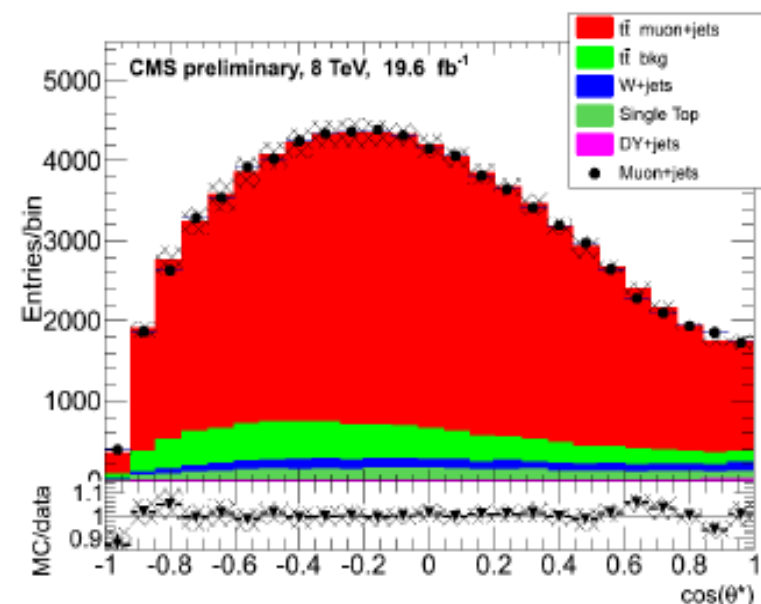
$$F_0 = 0.659 \pm 0.015(\text{stat.}) \pm 0.023(\text{syst.})$$

$$F_L = 0.350 \pm 0.010(\text{stat.}) \pm 0.024(\text{syst.})$$

From  $F_0 + F_L + F_R = 1$ :

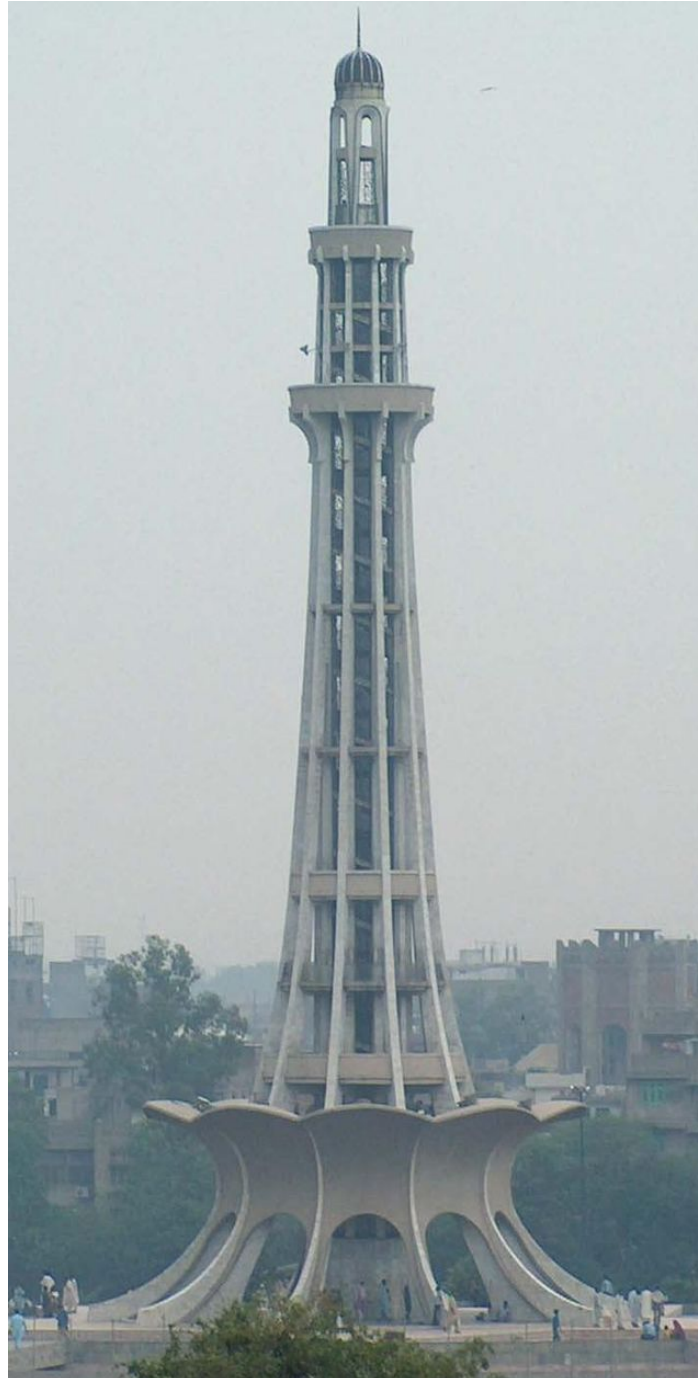
$$F_R = -0.009 \pm 0.006(\text{stat.}) \pm 0.020(\text{syst.})$$

Good agreement with SM-predictions!



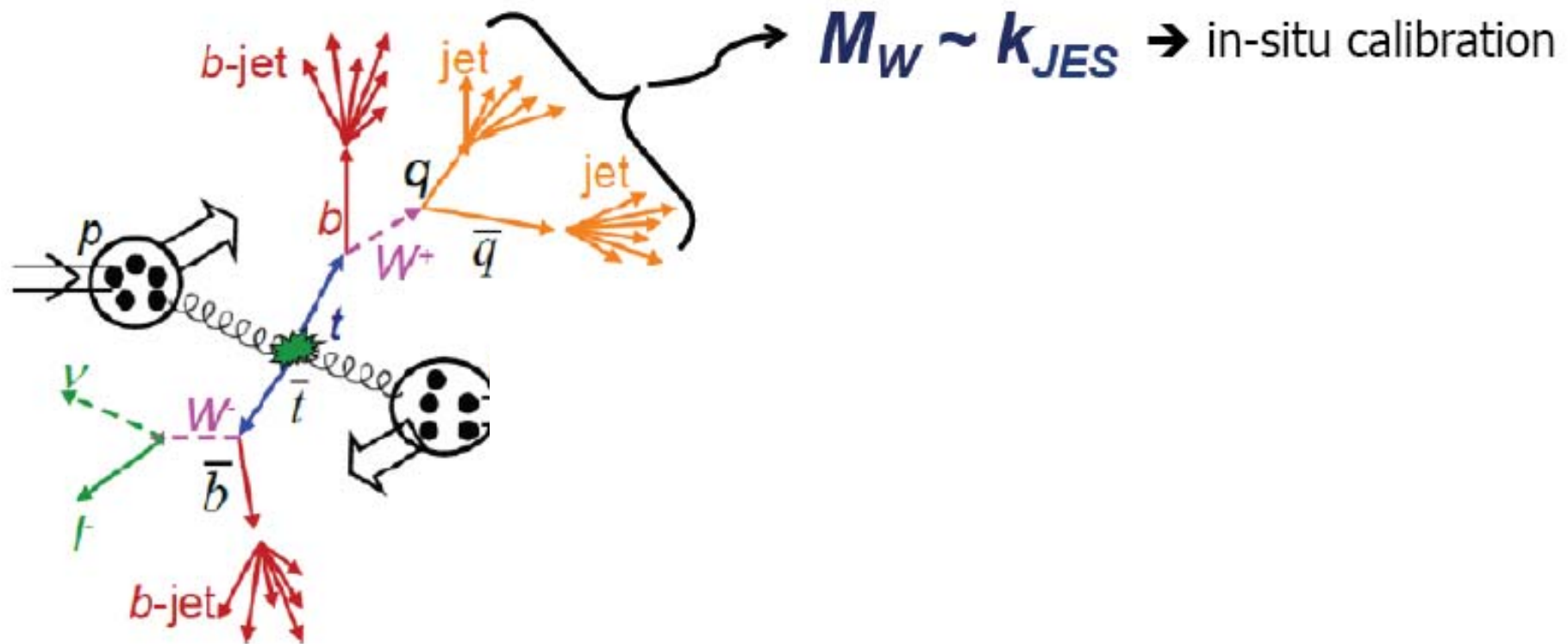
PAS-TOP-13-008

# 5. TOP QUARK PROPERTIES



# 5.1 Top Mass Measurements

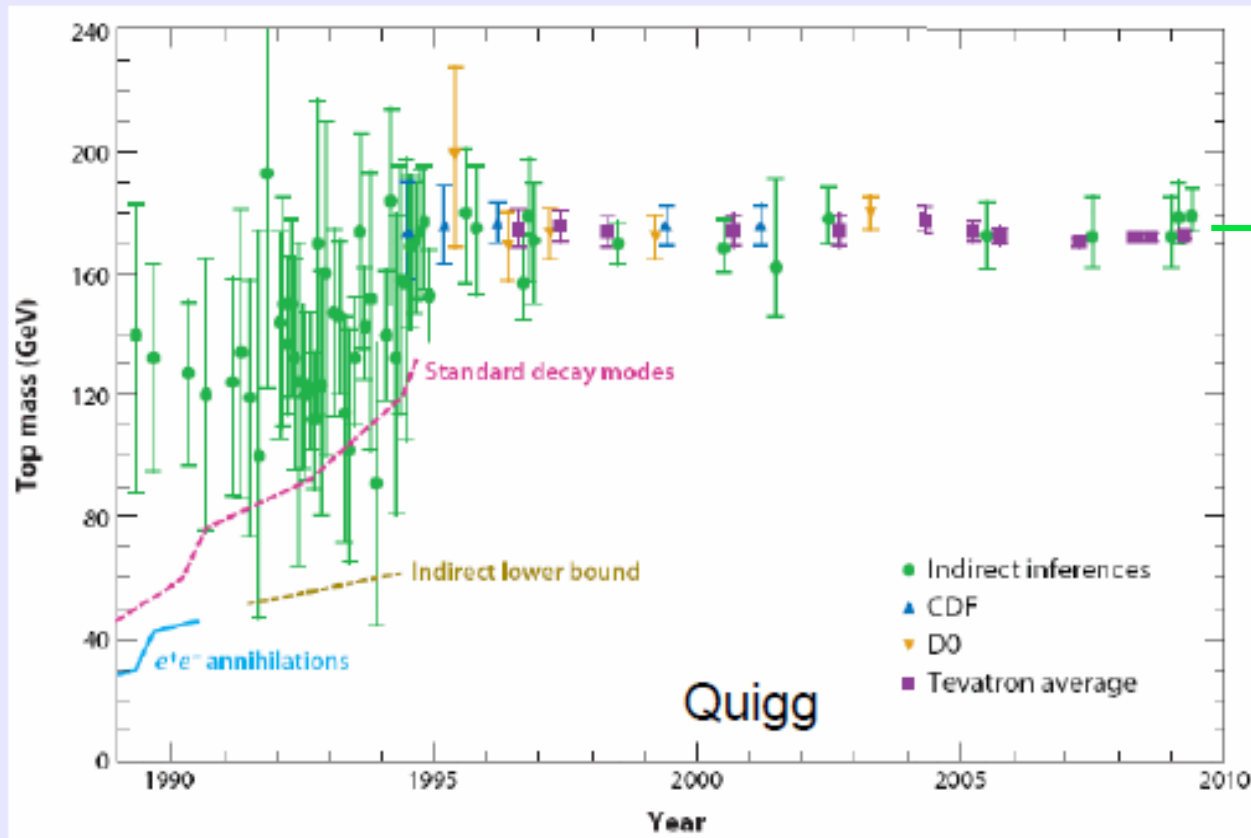
Start with calibration...



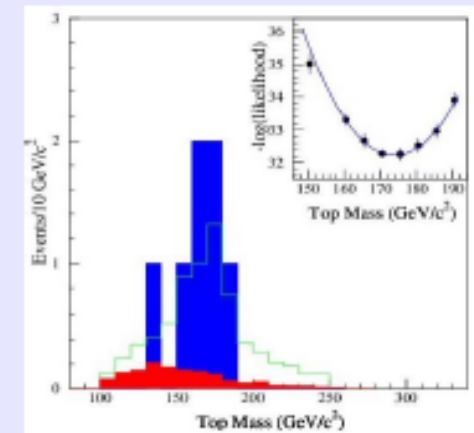
# Evolution of Top Quark Mass Determination

Measurement uncertainty on  $M_T$  has improved since 1994, but mass value has not changed much

$$M_{\text{top}} = 173.1 \pm 1.3 \text{ GeV}$$

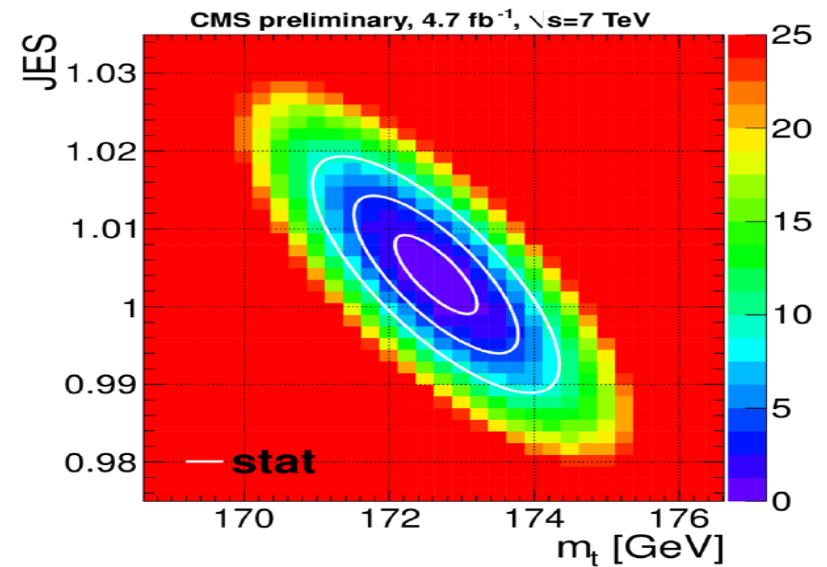
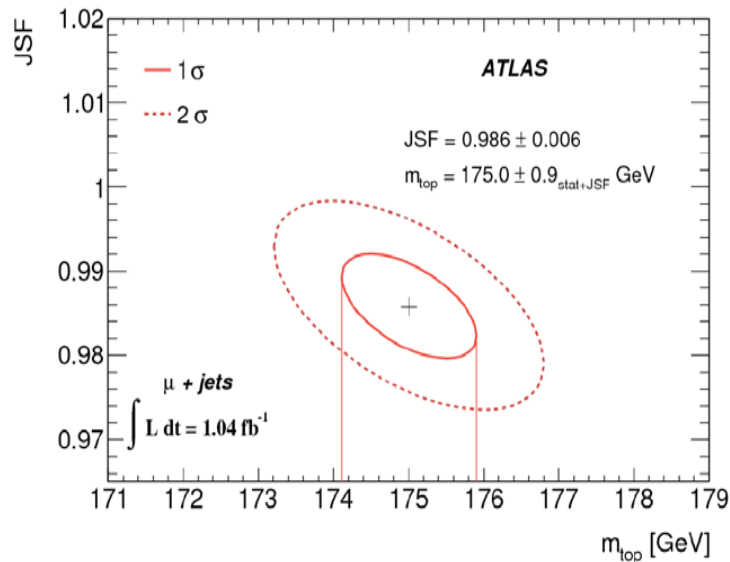
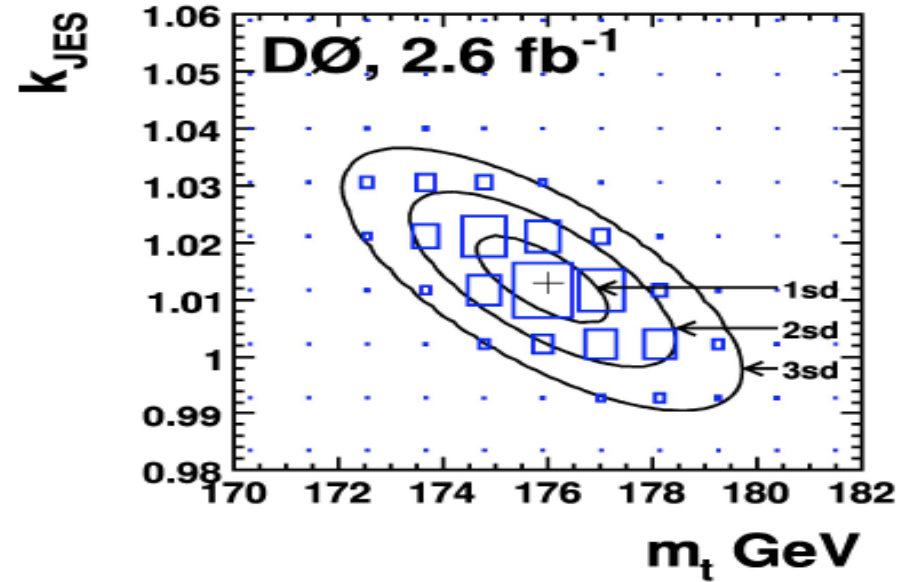
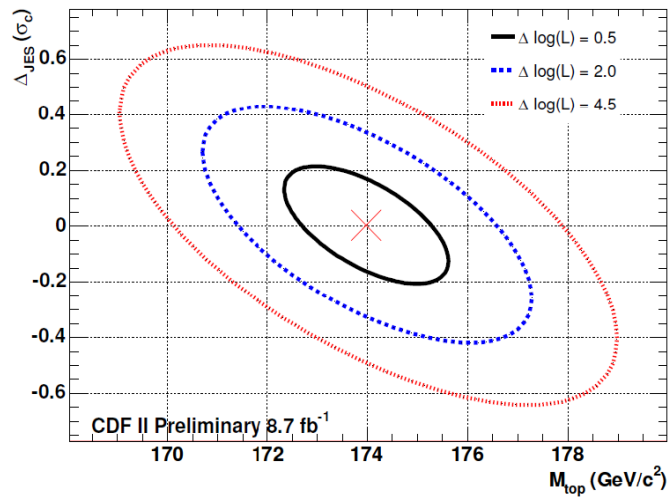


First measurement  
7 events (1.4 background)  
CDF, PRD **50**, 2966 (1994)



$$M_{\text{top}} = 174 \pm 10 \begin{matrix} +13 \\ -12 \end{matrix} \text{ GeV}$$

# JES vs $M_{\text{top}}$ in all four experiments

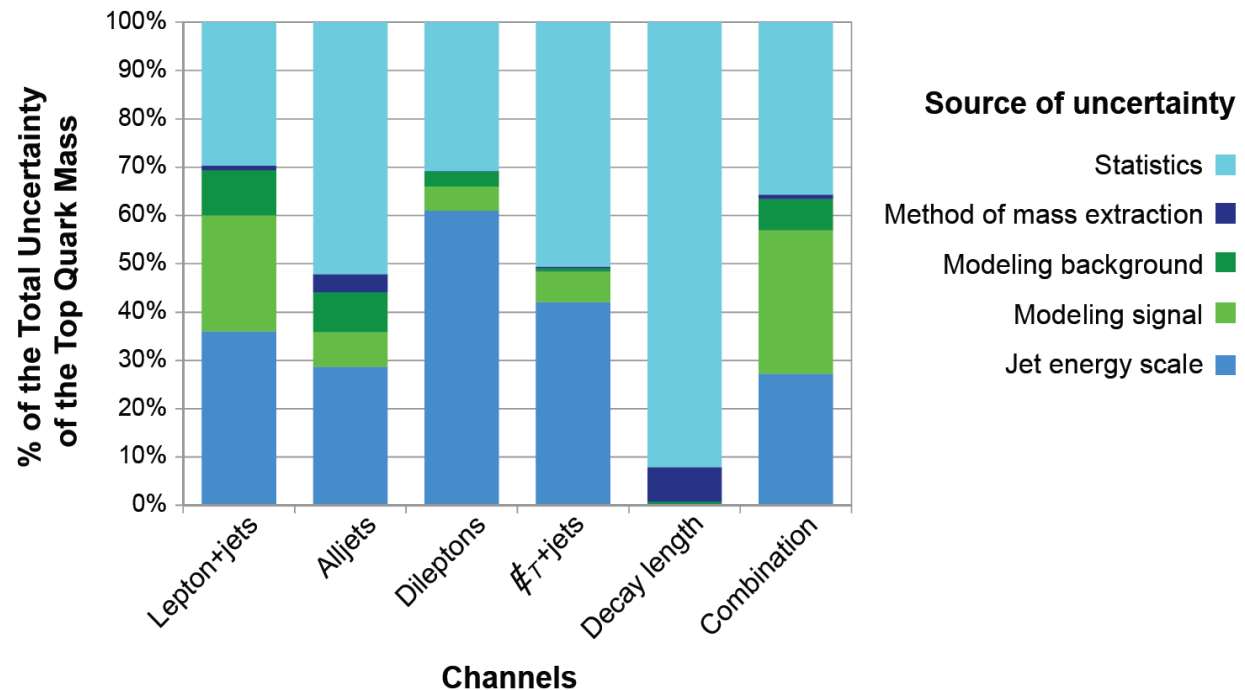
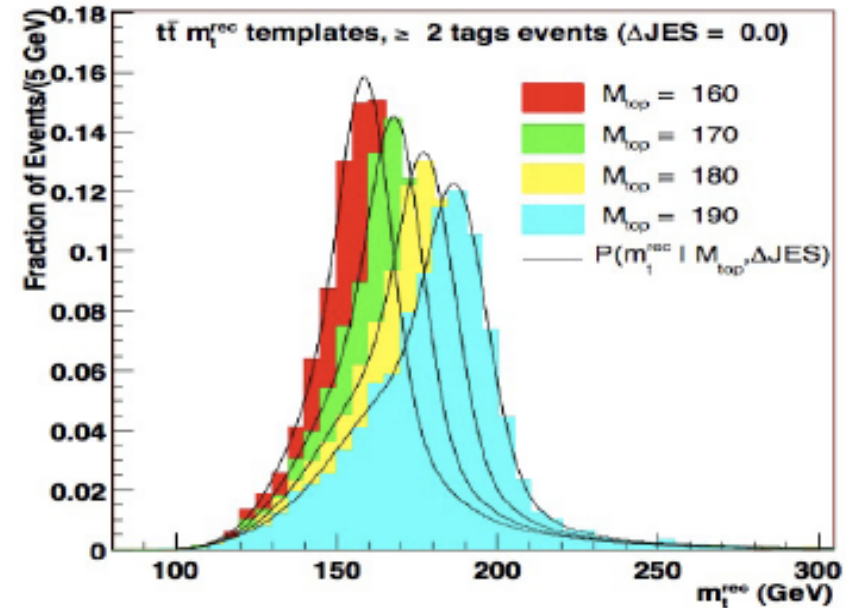




# Mass Fitting

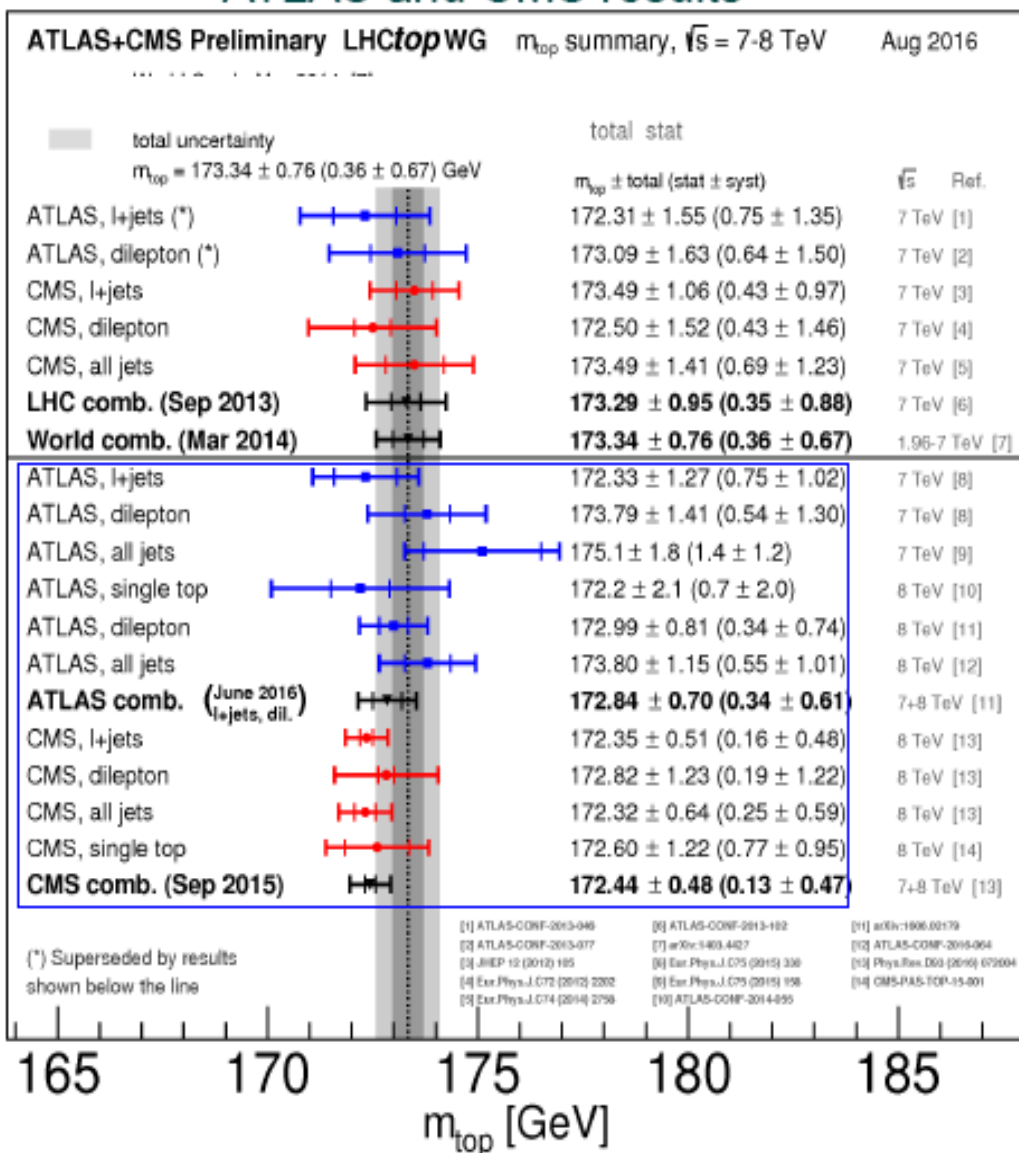
- Template method:  
fit MC generated distributions assuming different  $M_{top}$  to data
- Matrix element method:  
probability based on LO  $t\bar{t}$  matrix element using full kinematics of the event
- Ideogram method  
event likelihood computed as a convolution of a Gaussian resolution function with a Breit-Wigner (signal)
- Calibration curve method  
di-lepton channel using  $m_{t2}$
- b quark lifetime method  
boost proportional to  $M_{top}$ ;  
use of decay length of b jet

Example: sources of uncertainties at Tevatron

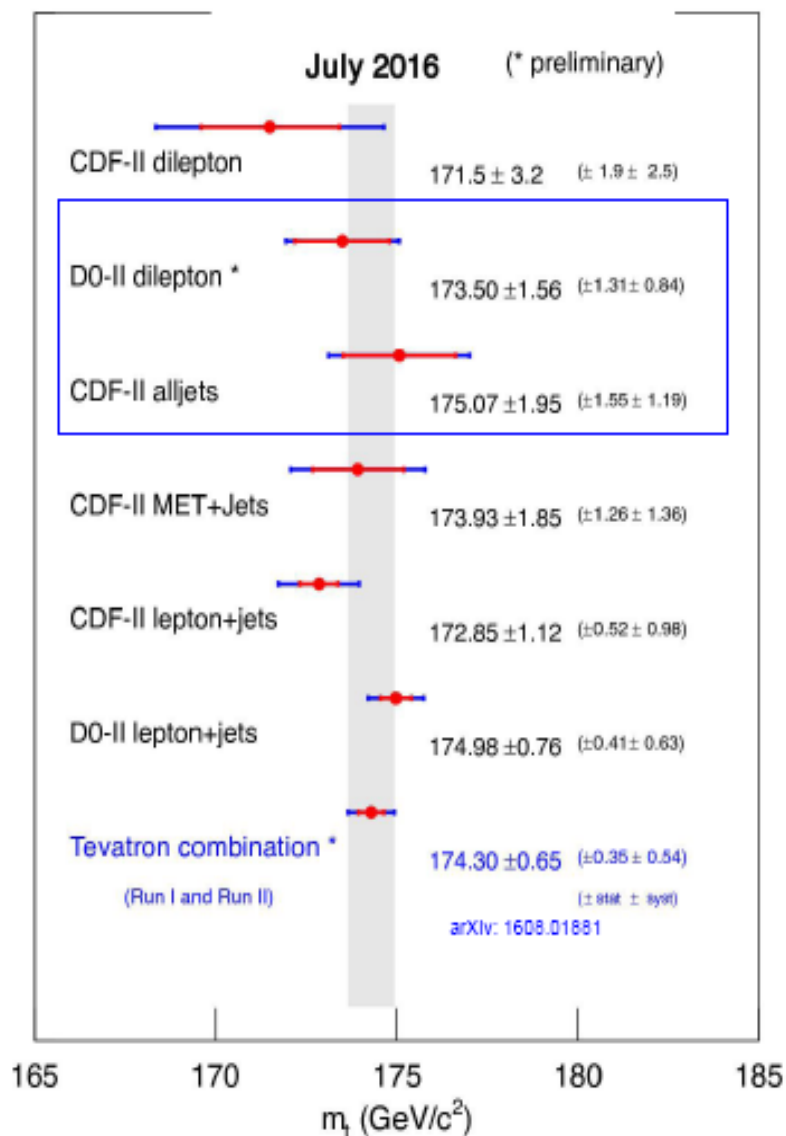


# Top Quark Mass Combinations

## ATLAS and CMS results



## CDF and D0 results



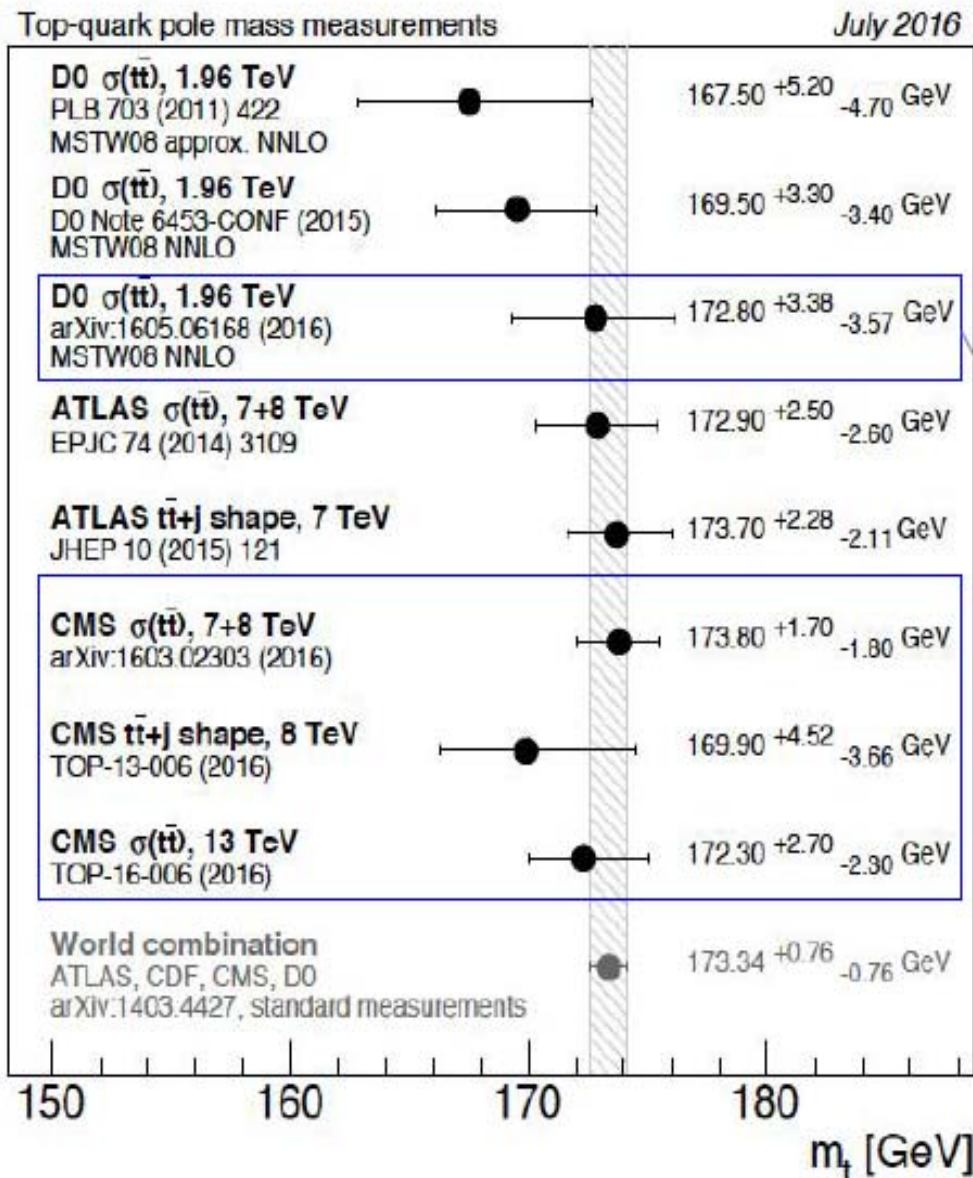
LHC and Tevatron results with nearly comparable precision of 3-4 permille (0.5 GeV)

LHC top mass systematically limited: MC modelling, (b)JES

Template/Matrix element methods  $\rightarrow$  Monte Carlo top mass parameter

# Top Quark Mass Determination from fits and from $\sigma_{tt}$

## Pole mass vs Monte-Carlo mass measurements



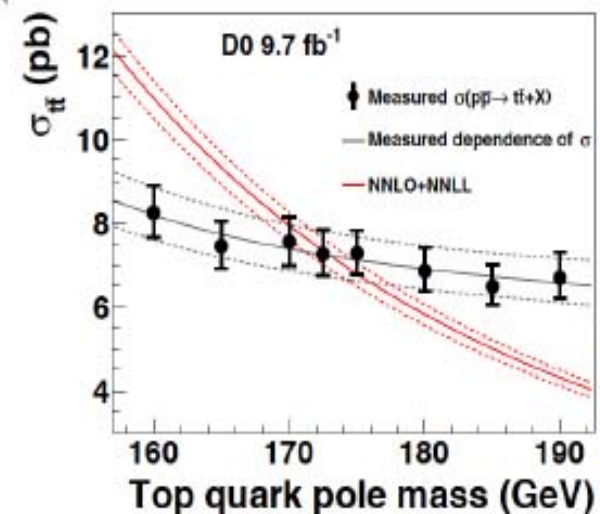
Direct top mass measurements:

- Monte-Carlo mass  $m_t^{MC}$
- precision 0.5 GeV

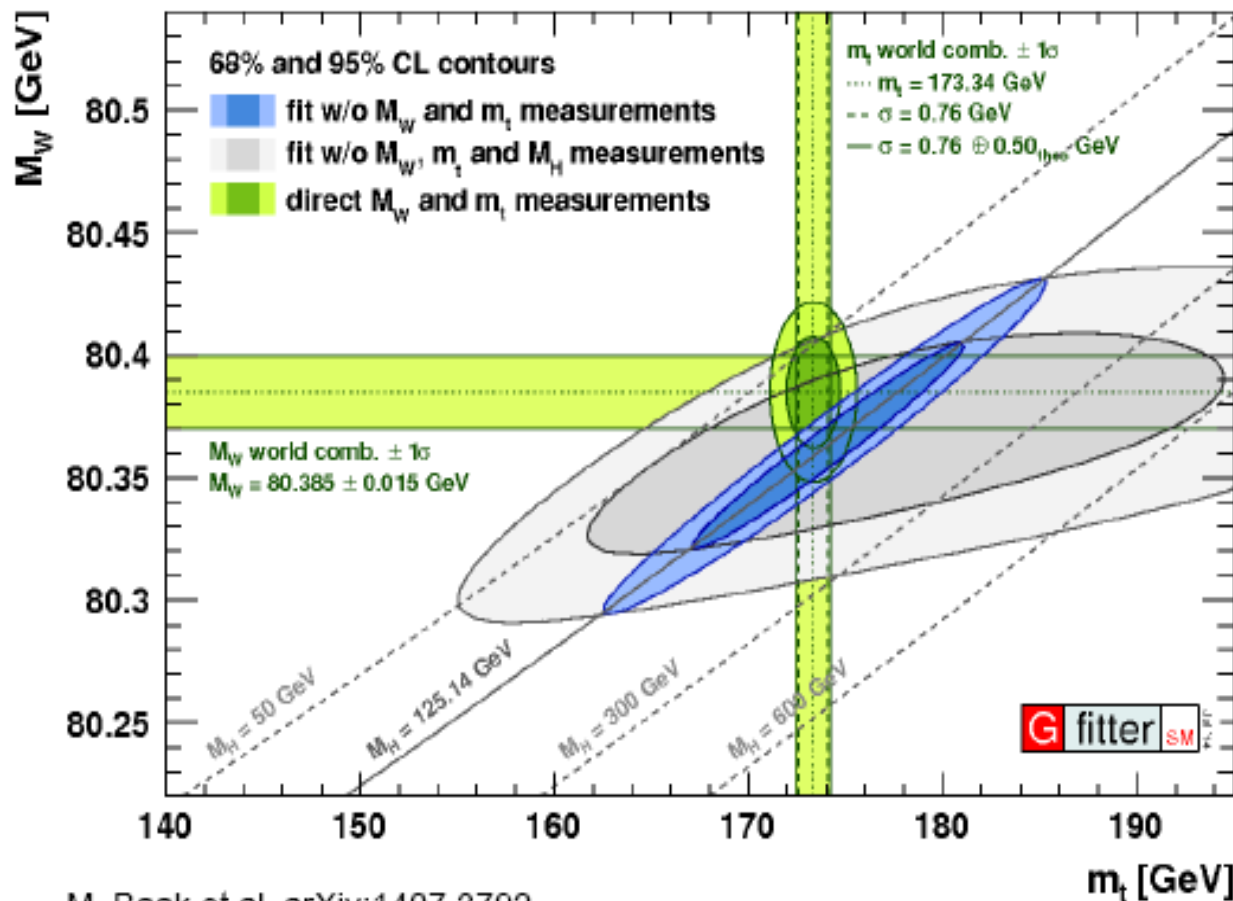
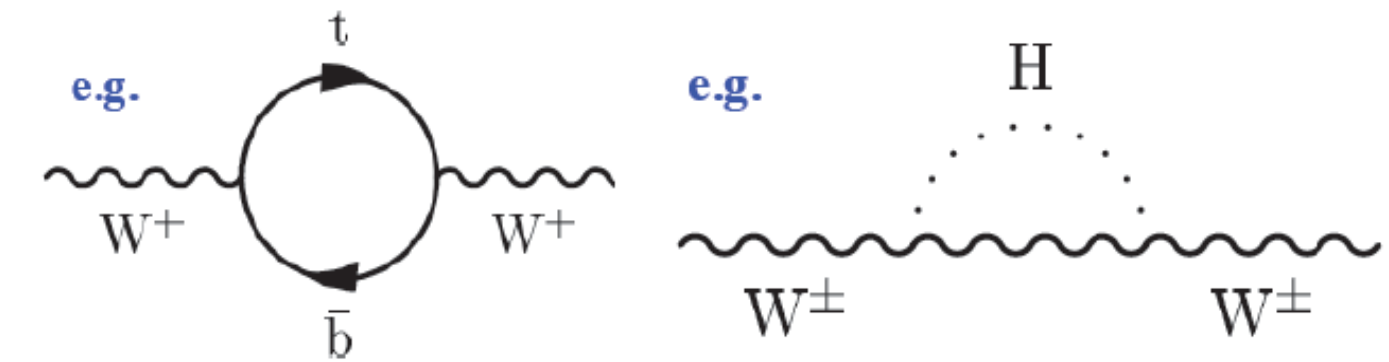
Expect  $m_t^{MC} - m_t^{pole} \sim 1$  GeV

→ Calibrate  $m_t^{MC}$

→ Indirect measurements of  $m_t^{pole}$ :  
compatible with measured  $m_t^{MC}$   
within precision of  $\pm 2$  GeV



# Masses in EWK Theory



M. Baak et al, arXiv:1407.3792

<http://project-gfitter.web.cern.ch/project-gfitter/>



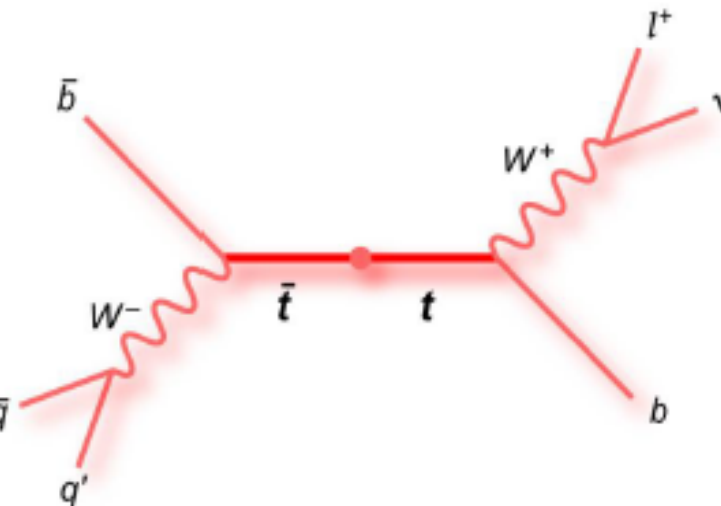
## 5.2 $t \bar{t}$ Mass Difference

- CPT theorem predicts masses of particles and antiparticles to be equal
  - Top-quark only particle with color charge to test this invariance

- Analysis Principle:

Hadronic branch:

Reconstruct top-quark  $\bar{q}$   
to determine mass



Leptonic branch:

Using lepton charge to tag  
top- or antitop-quark

- Analysis of  $\mu$ +jets events

- 1 isolated muon, 4 high- $p_T$  jets
- Kinematic event reconstruction of 12 permutations
- Measurement of top- and antitop-quark masses with Ideogram method
  - Taking b-tagging information into account to reduce background events (mainly  $W$ +jets)



Test CPT invariance in the top sector

$$\Delta M_t = M_{\text{top}} - M_{\overline{\text{top}}}$$

- Reconstruction of the hadronic side: compare  $\ell^+$ +jets and  $\ell^-$ +jets events
- Use kinematic fit, and event-per-event likelihood for  $\ell^-$  and  $\ell^+$  separately

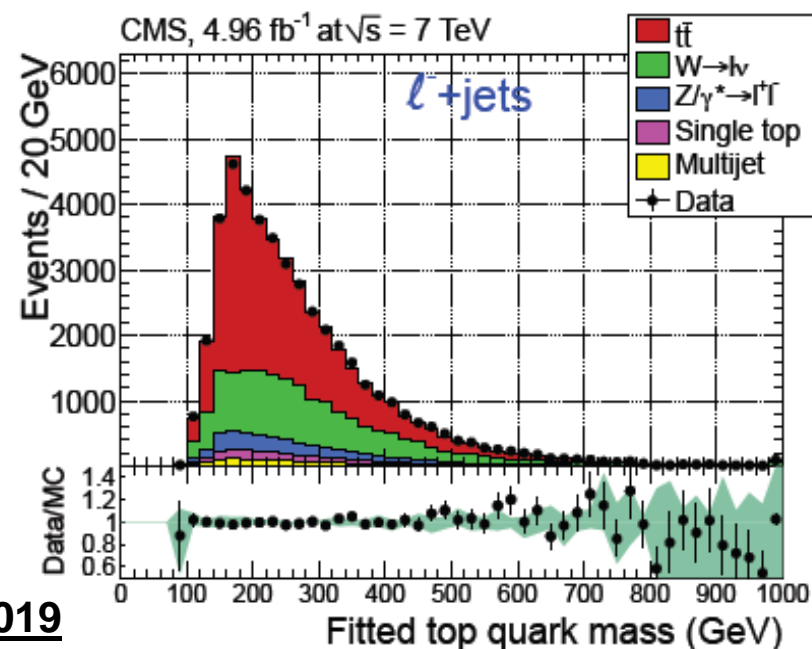
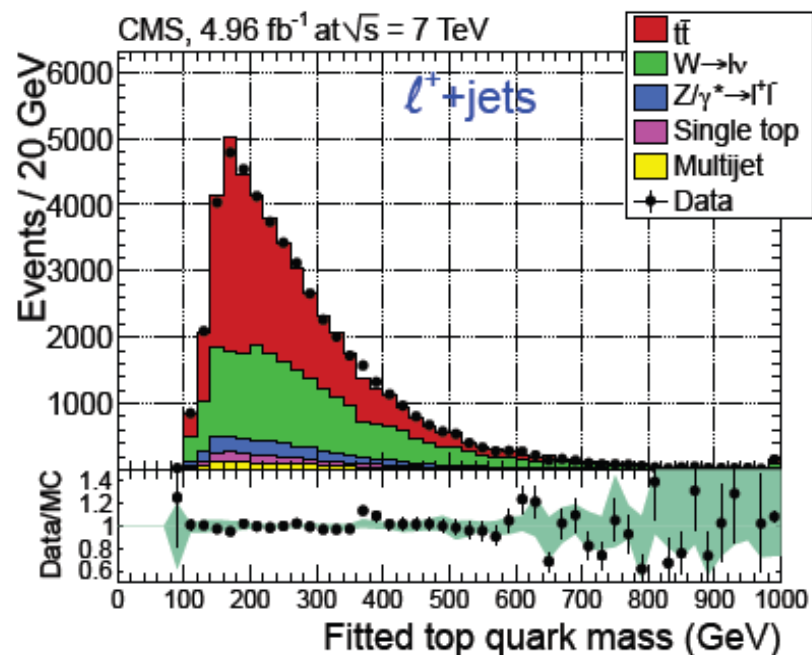
$$\Delta m_t = -0.44 \pm 0.46 \text{ (stat.)} \pm 0.27 \text{ (syst.) GeV}$$

Most systematic effects cancel out !  
 → the measurement is stat. limited

World's best so far

Consistent with SM,  
 Consistent between e and  $\mu$

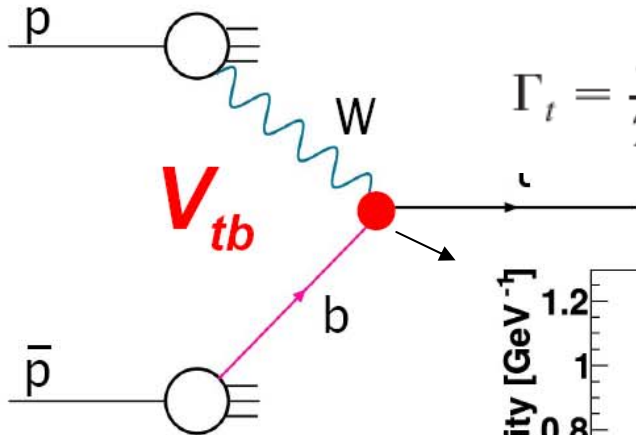
**CMS-TOP-11-019**



## t-channel cross section:

$$\sigma(pp \rightarrow tqb + X) = 2.90 \pm 0.59 \text{ pb}$$

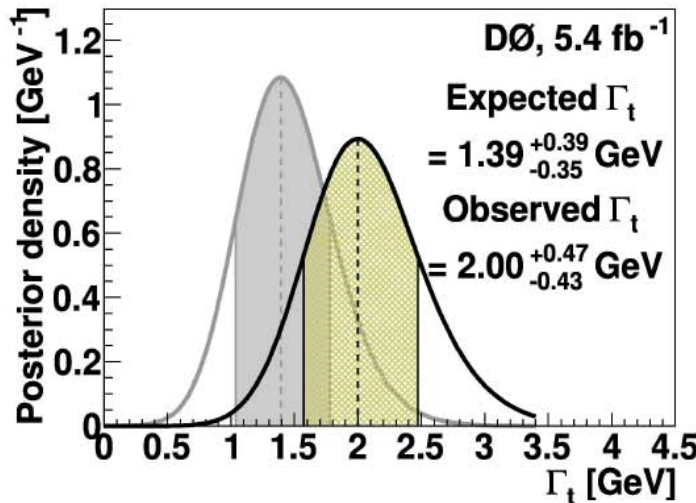
$$m_t = 172.5 \text{ GeV}$$



$$\Gamma_t = \frac{\sigma(t\text{-channel})\Gamma(t \rightarrow Wb)_{SM}}{\mathcal{B}(t \rightarrow Wb)\sigma(t\text{-channel})_{SM}}$$

## partial decay width:

$$R = 0.90 \pm 0.04 \text{ (stat+syst)}$$



$$\tau_{\text{top}} \propto \left(\frac{M_W}{M_{\text{top}}}\right)^3$$

$$\tau_{\text{top}} \approx 4.7 \cdot 10^{-25} \text{ s}$$

Phys. Rev. D84 012008 (2011)

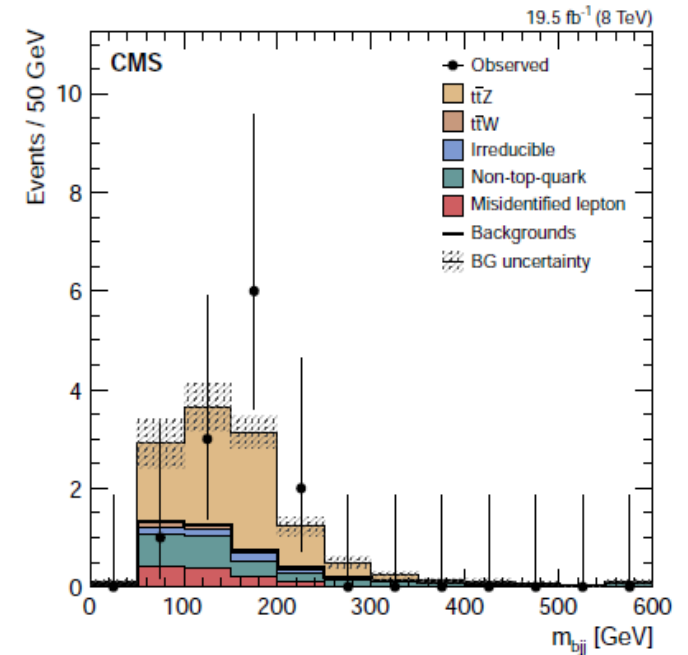
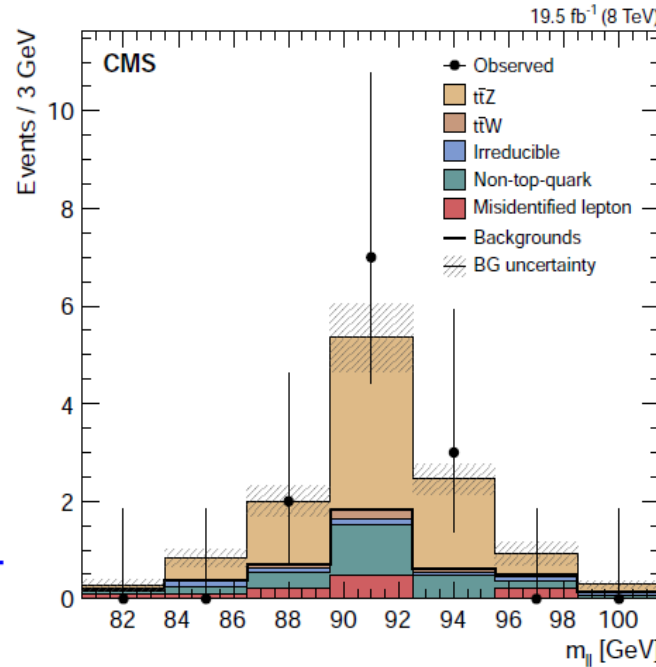
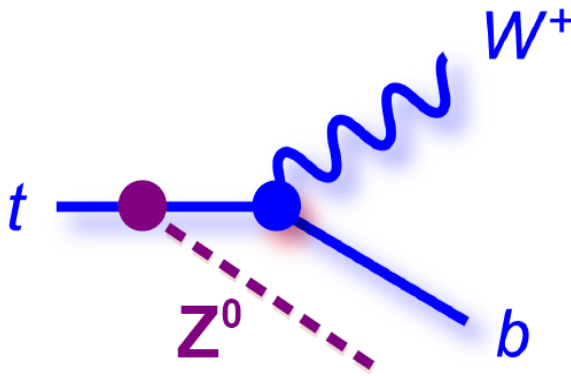
$$\Gamma_t = 2.00^{+0.47}_{-0.43} \text{ GeV}$$

$$\tau_t = (3.29^{+0.90}_{-0.63}) \times 10^{-25} \text{ s}$$

⇒ **most precise determination**

Phys. Rev. D 85, 091104(2012)

# 5.4 $t\bar{t}+V$ Production

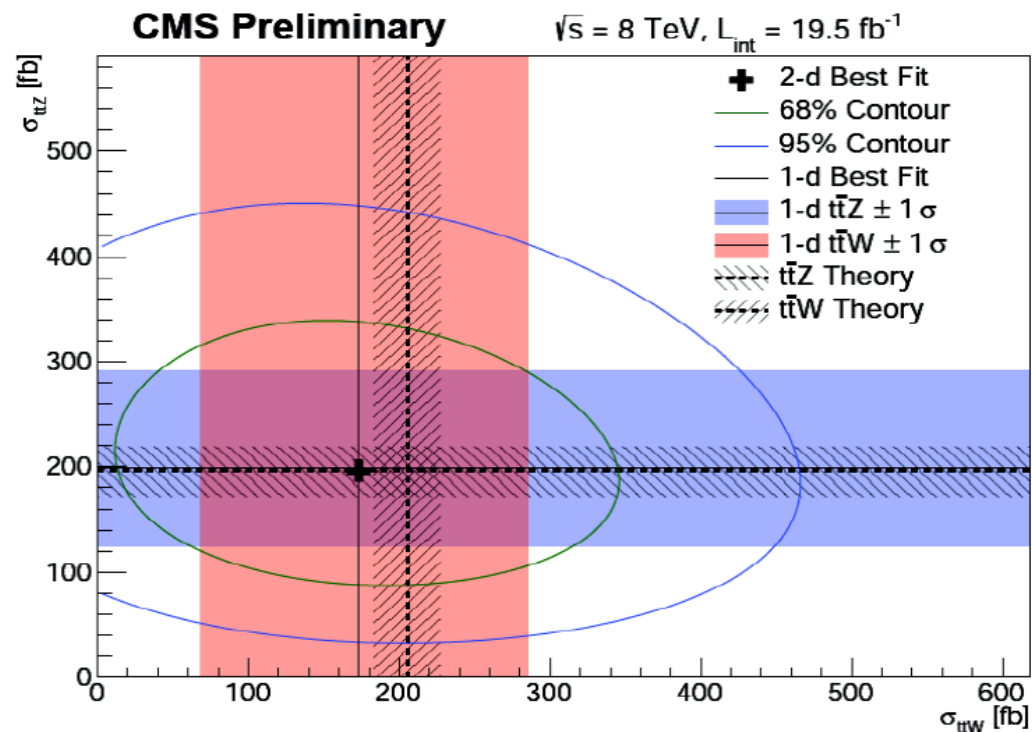
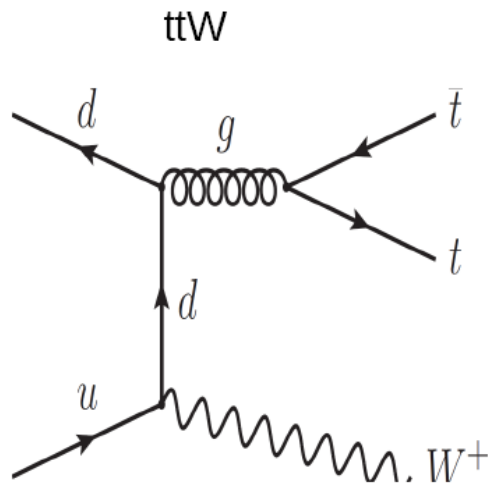
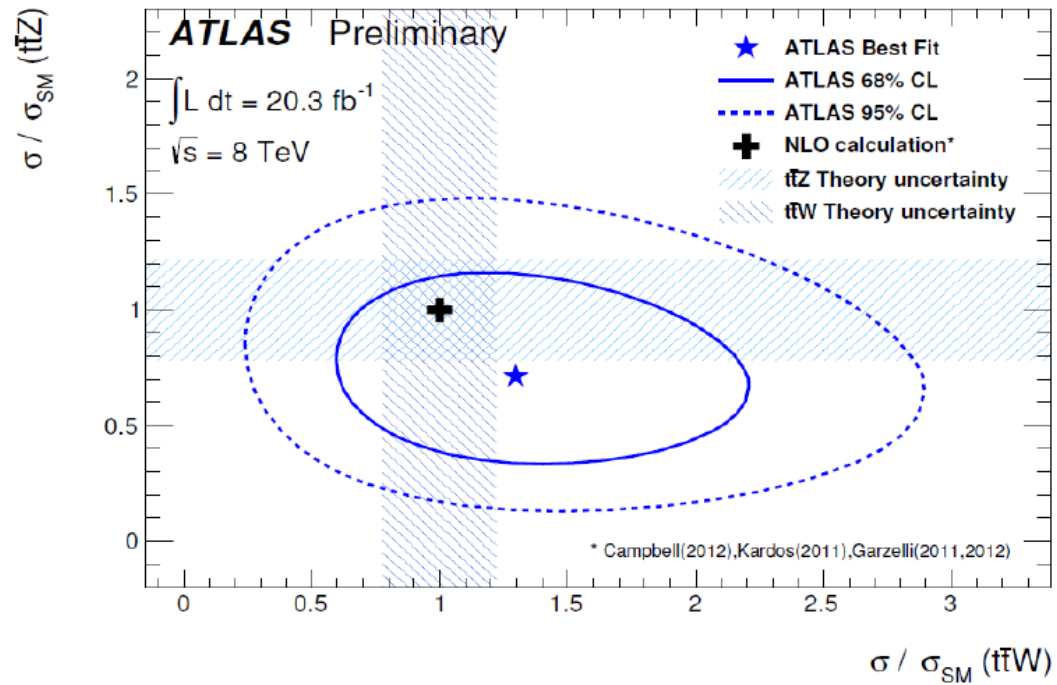
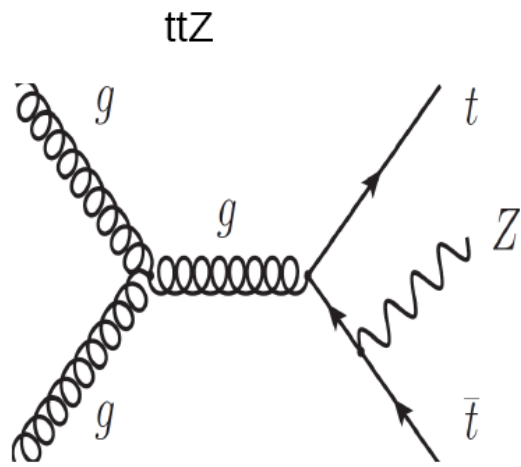


CMS 7 TeV [PRL 110 \(2013\) 172002](#)

Channels used	Process	Cross section	Significance
$2l$	$t\bar{t}V$	$430^{+170}_{-150}$ (stat.) $\pm 90$ (syst.) fb	3.0
$3l$	$t\bar{t}Z$	$280^{+140}_{-110}$ (stat.) $^{+60}_{-30}$ (syst.) fb	3.3

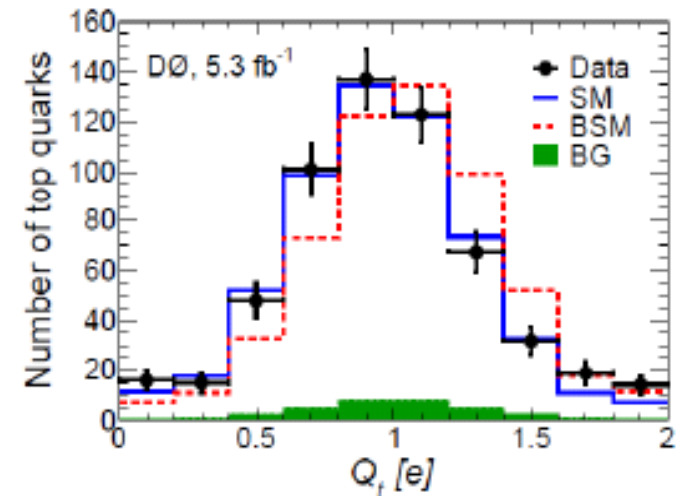
CMS 8 TeV [arXiv:1406.7830](#)

Channels used	Process	Cross section	Significance
$2l$	$t\bar{t}W$	$170^{+90}_{-80}$ (stat) $\pm 70$ (syst) fb	1.6
$3l+4l$	$t\bar{t}Z$	$200^{+80}_{-70}$ (stat) $^{+40}_{-30}$ (syst) fb	3.1
$2l+3l+4l$	$t\bar{t}W + t\bar{t}Z$	$380^{+100}_{-90}$ (stat) $^{+80}_{-70}$ (syst) fb	3.7



- **Charge:**

- Using  $5.3 \text{ fb}^{-1}$ , DØ excludes top quark charge of  $Q = -4/3e$  at  $> 5 \sigma$  level
- Upper limit of 0.46 on the fraction of such quarks in an admixture with SM top quark ( $Q = +2/3 e$ ) @ 95% C.L.

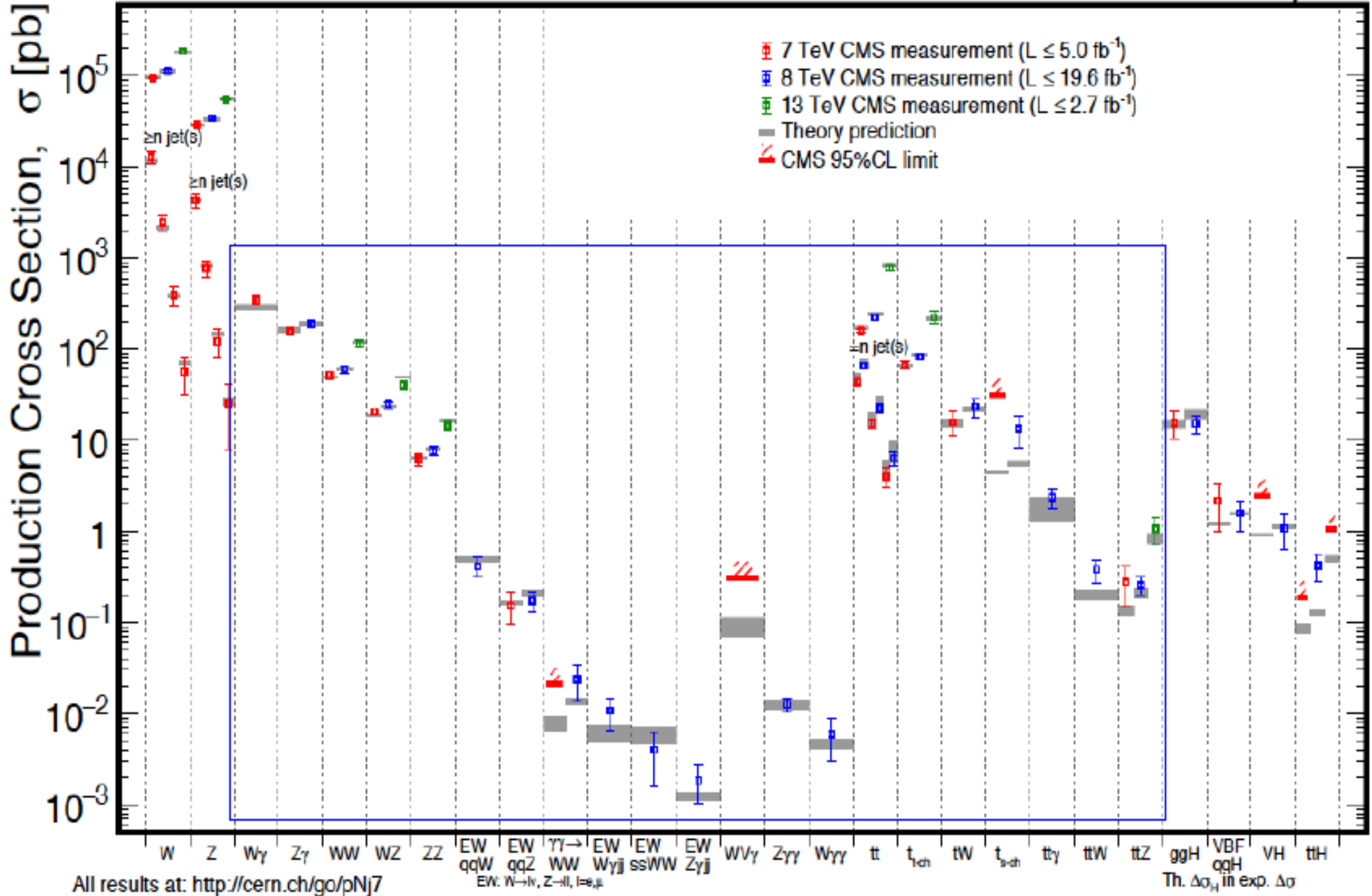




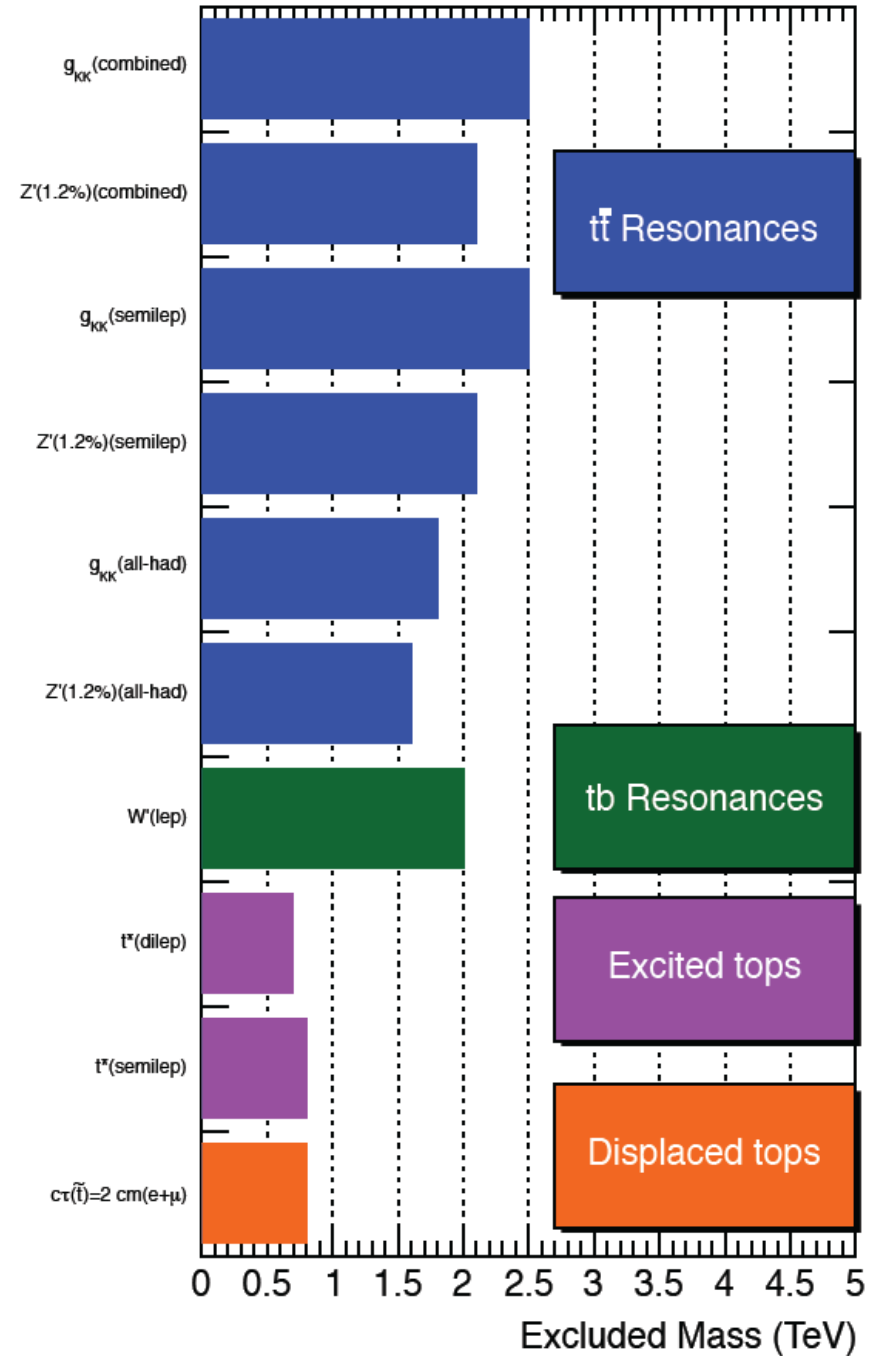
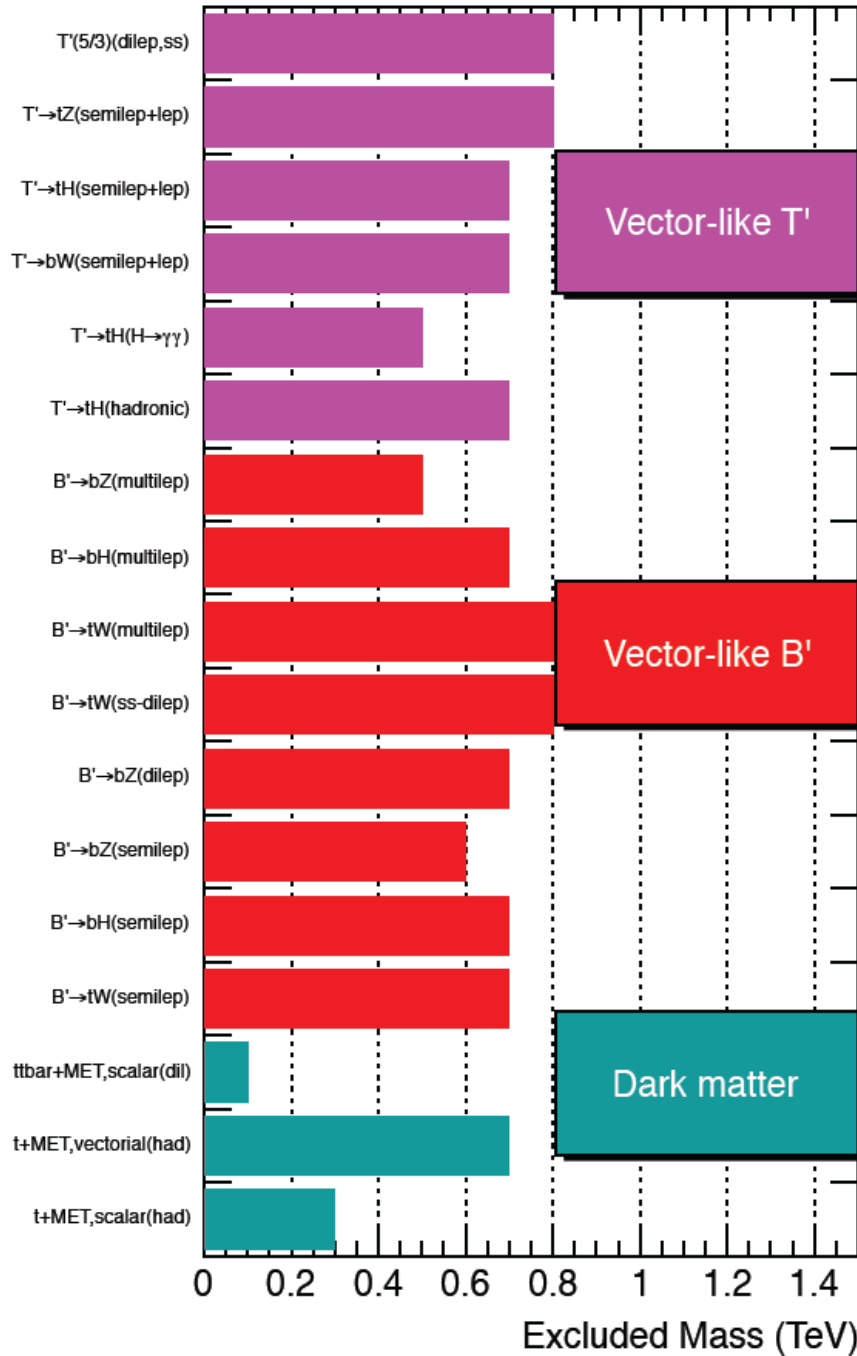
# 5.6 Measurements of the Standard Model

June 2016

CMS Preliminary



# Searches for New Physics Beyond 2 Generations



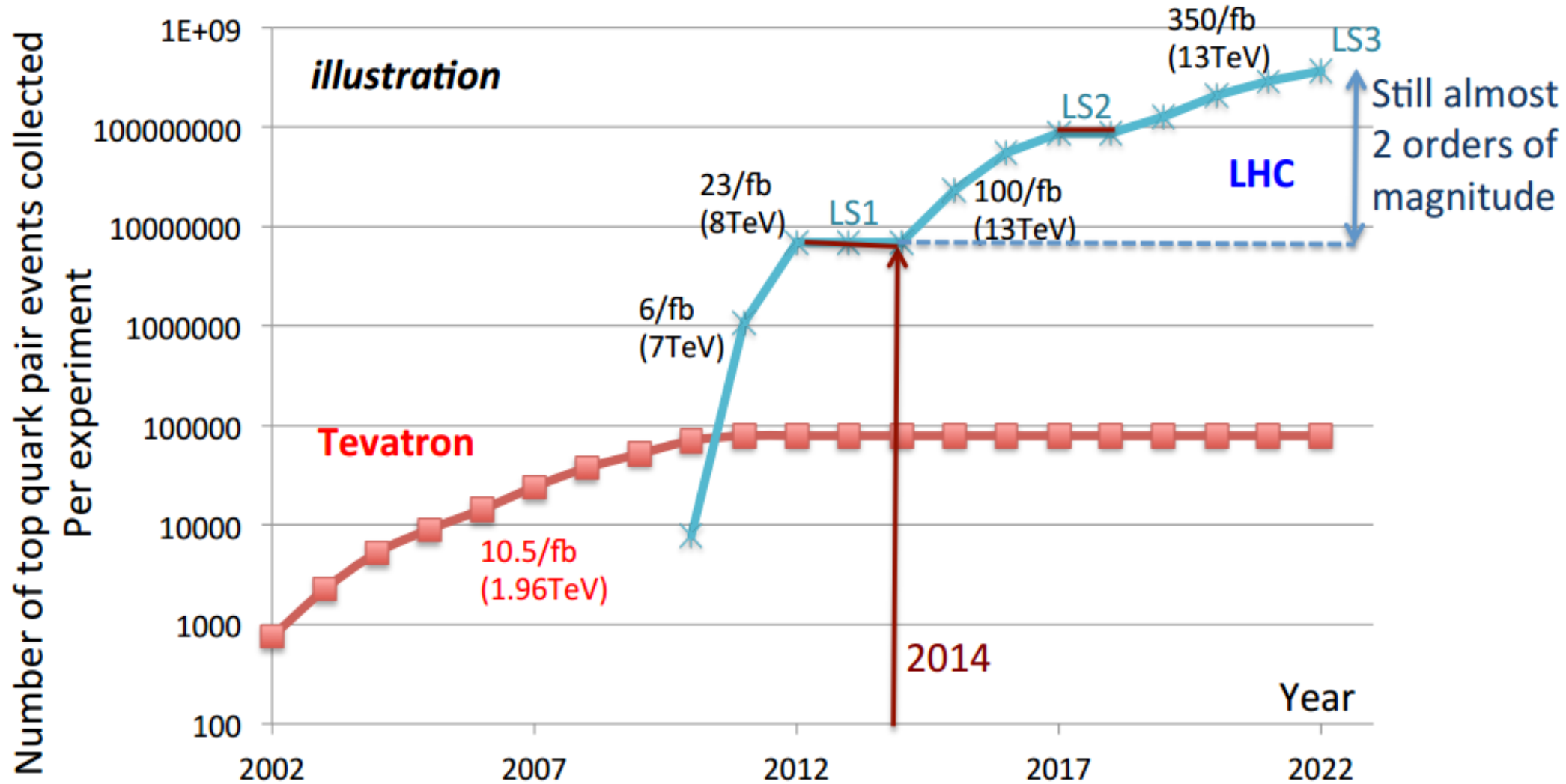
**In all cases, the Standard Model holds firmly!**

# 6. The Future



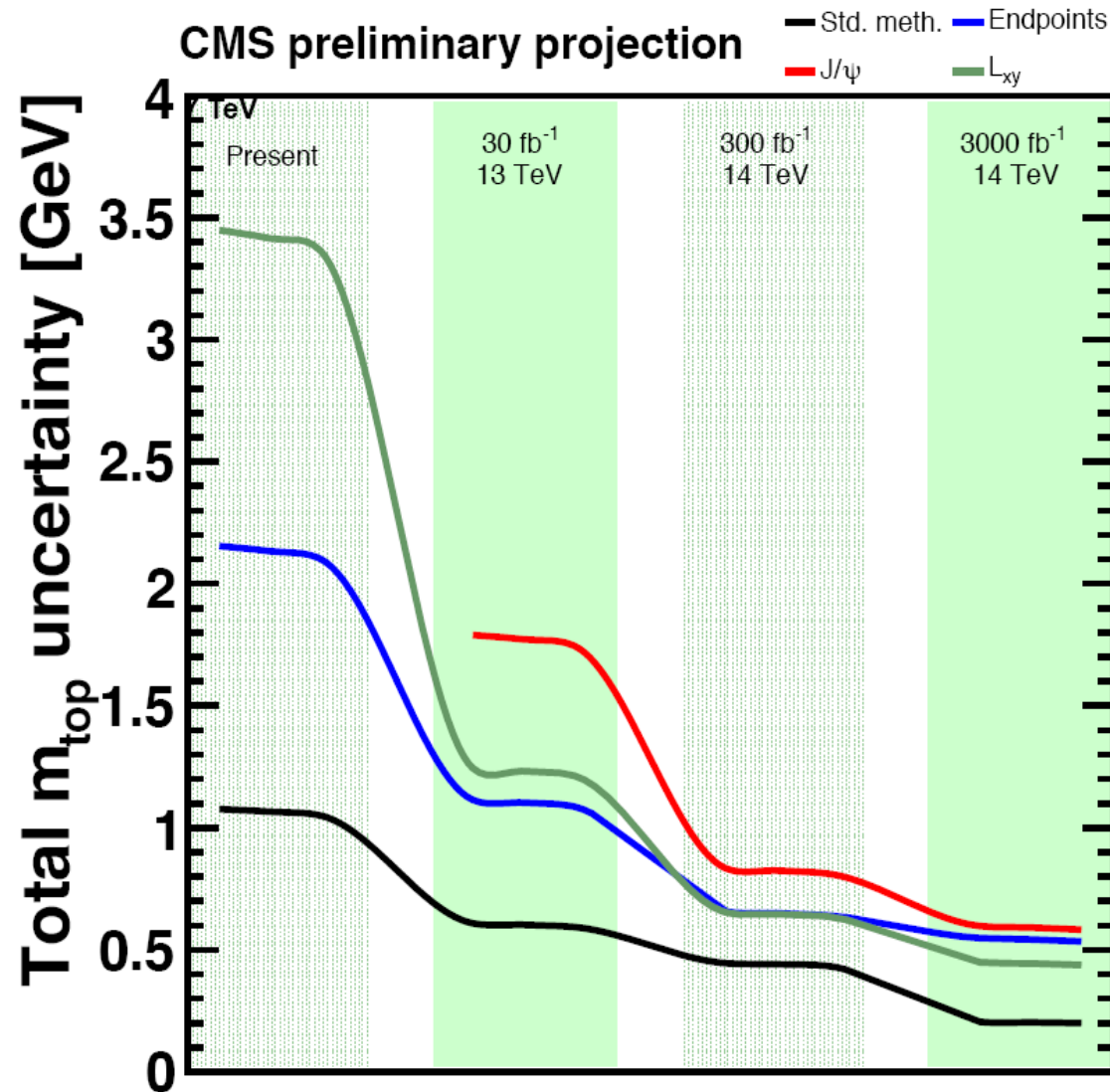
# The Growth of the Number of Top-Antitop-Events

20 years for almost 6 orders of magnitude → the Top Quark era



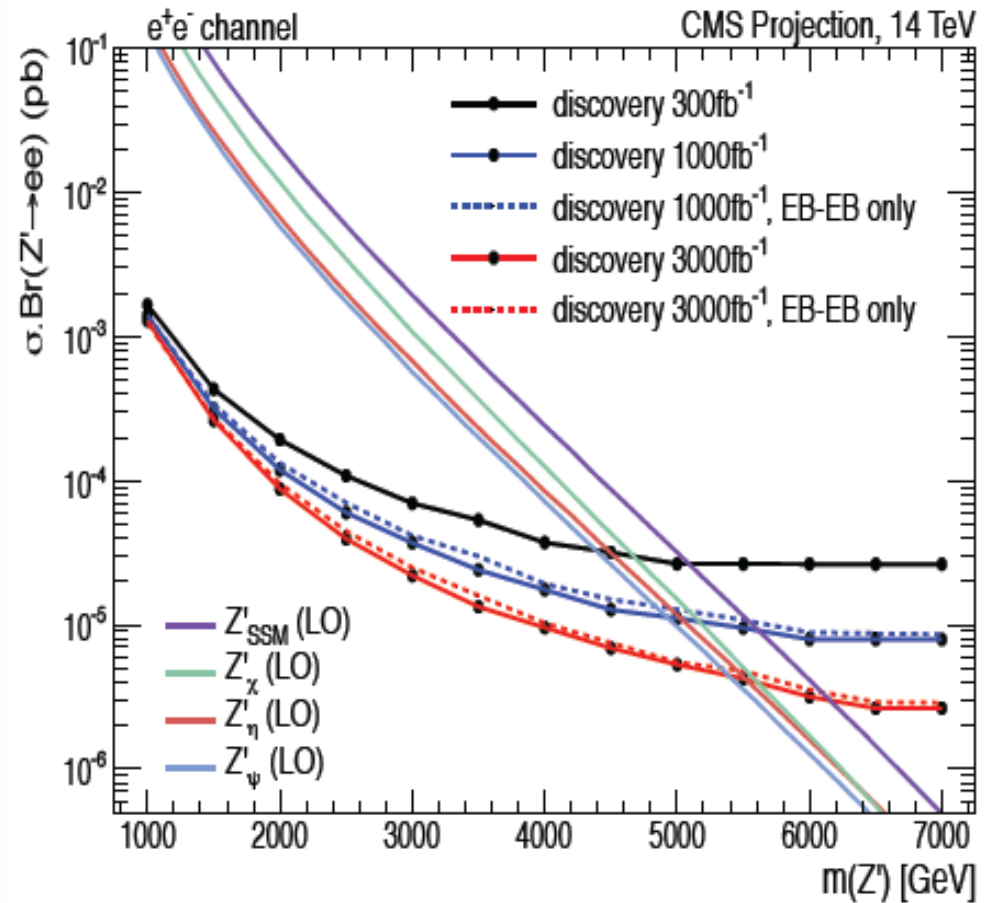
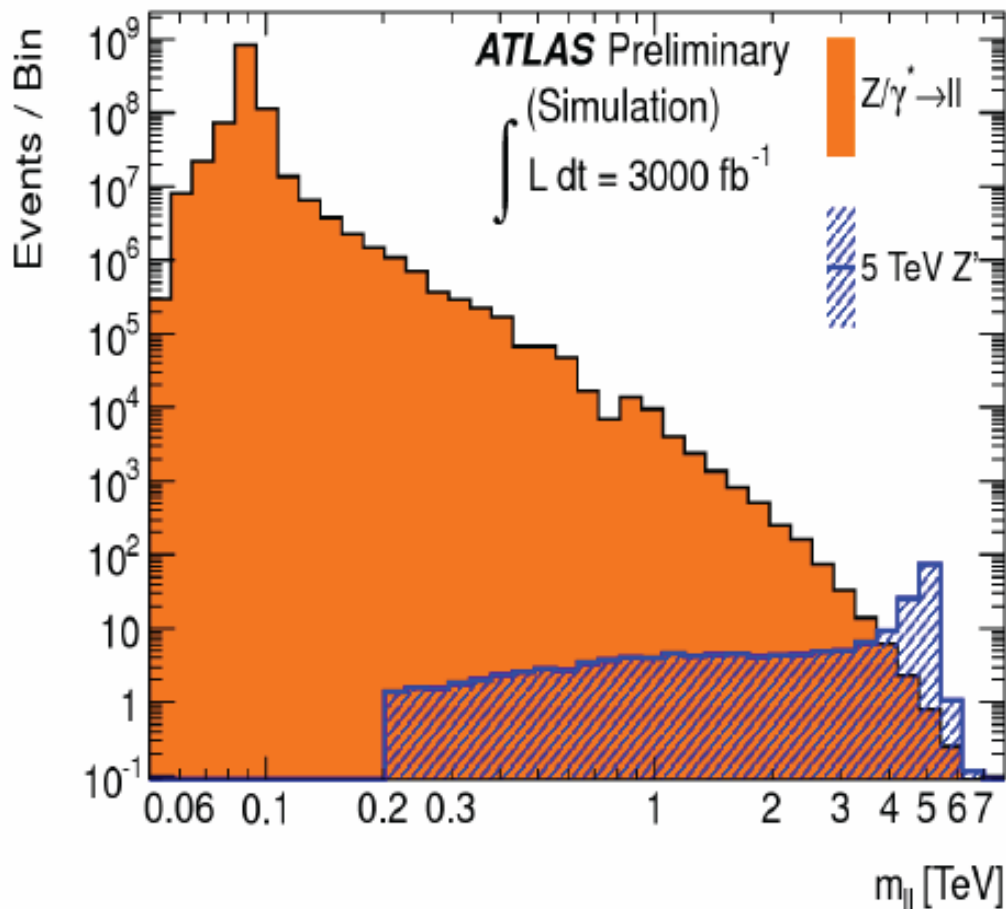
D'Hondt, Talk 2014

# Perspectives for the Top Quark Mass

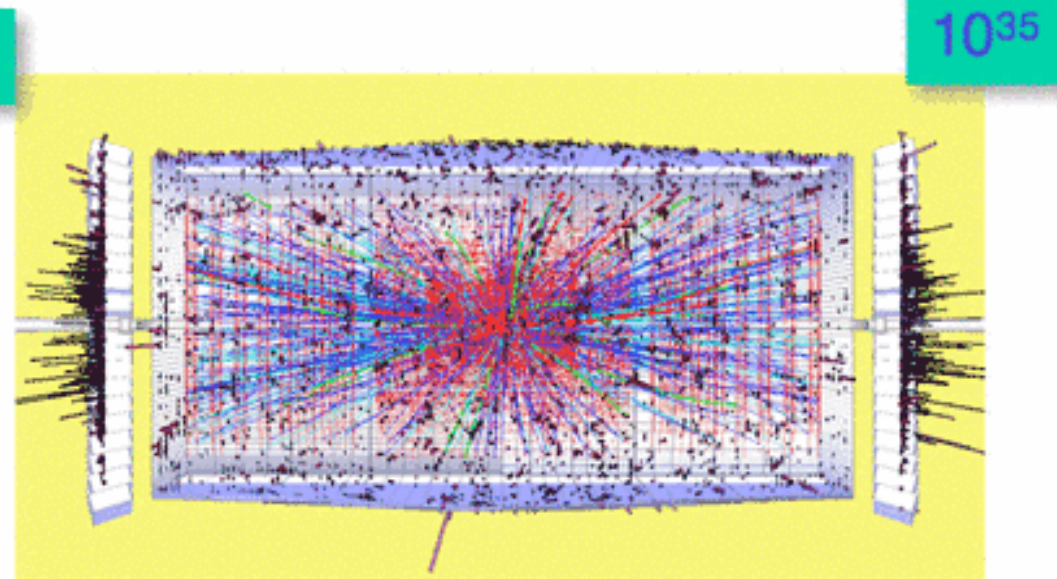
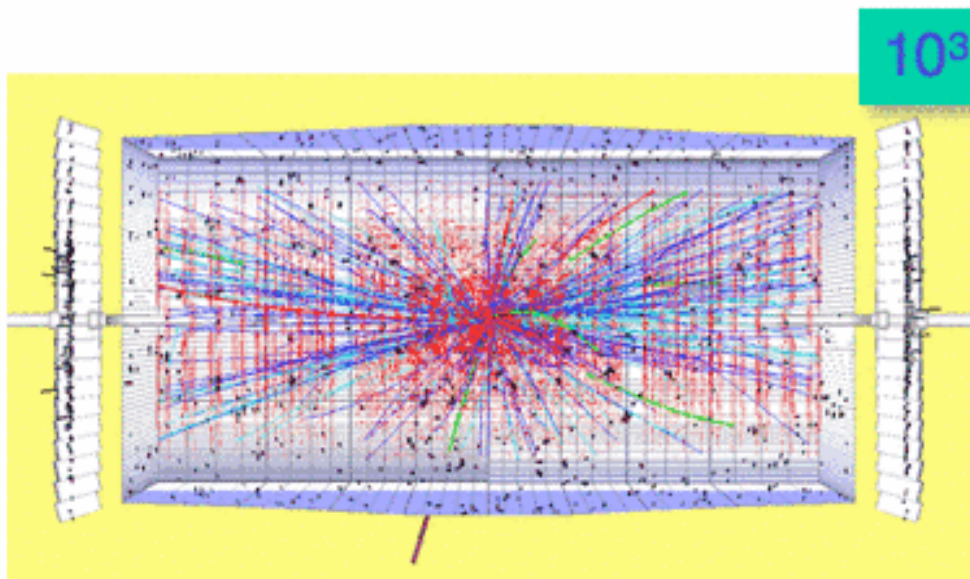
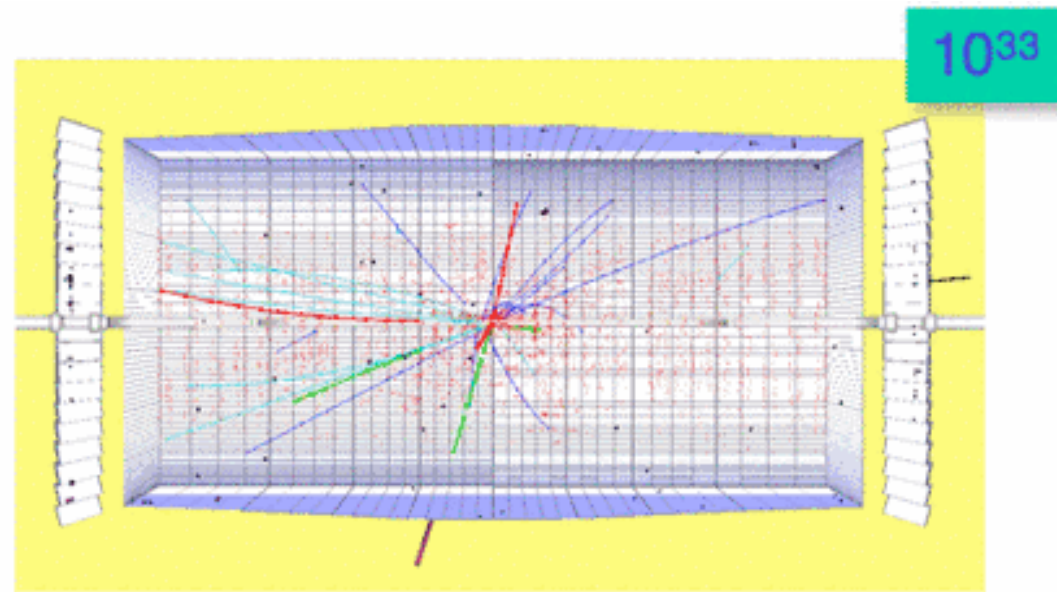
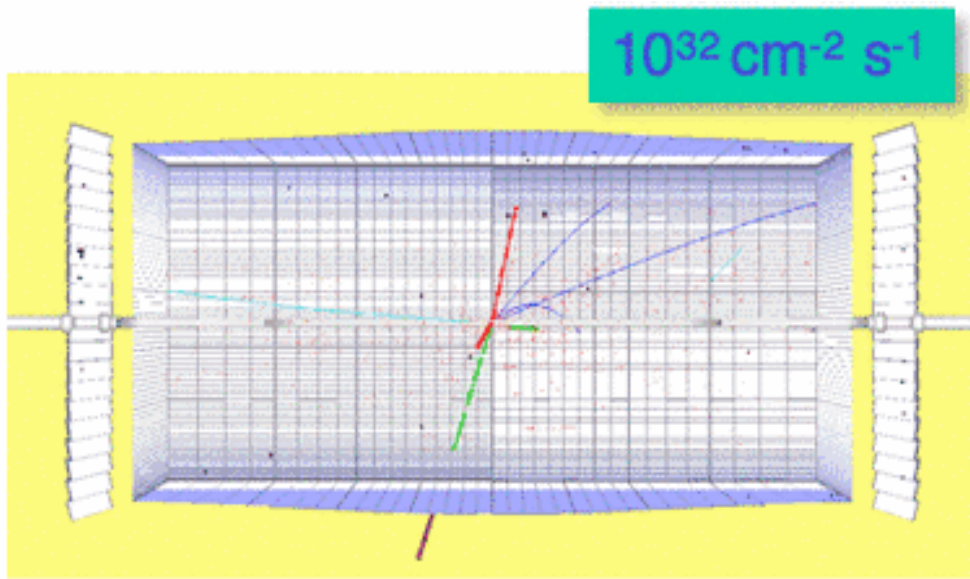




# ... and for new Bosons



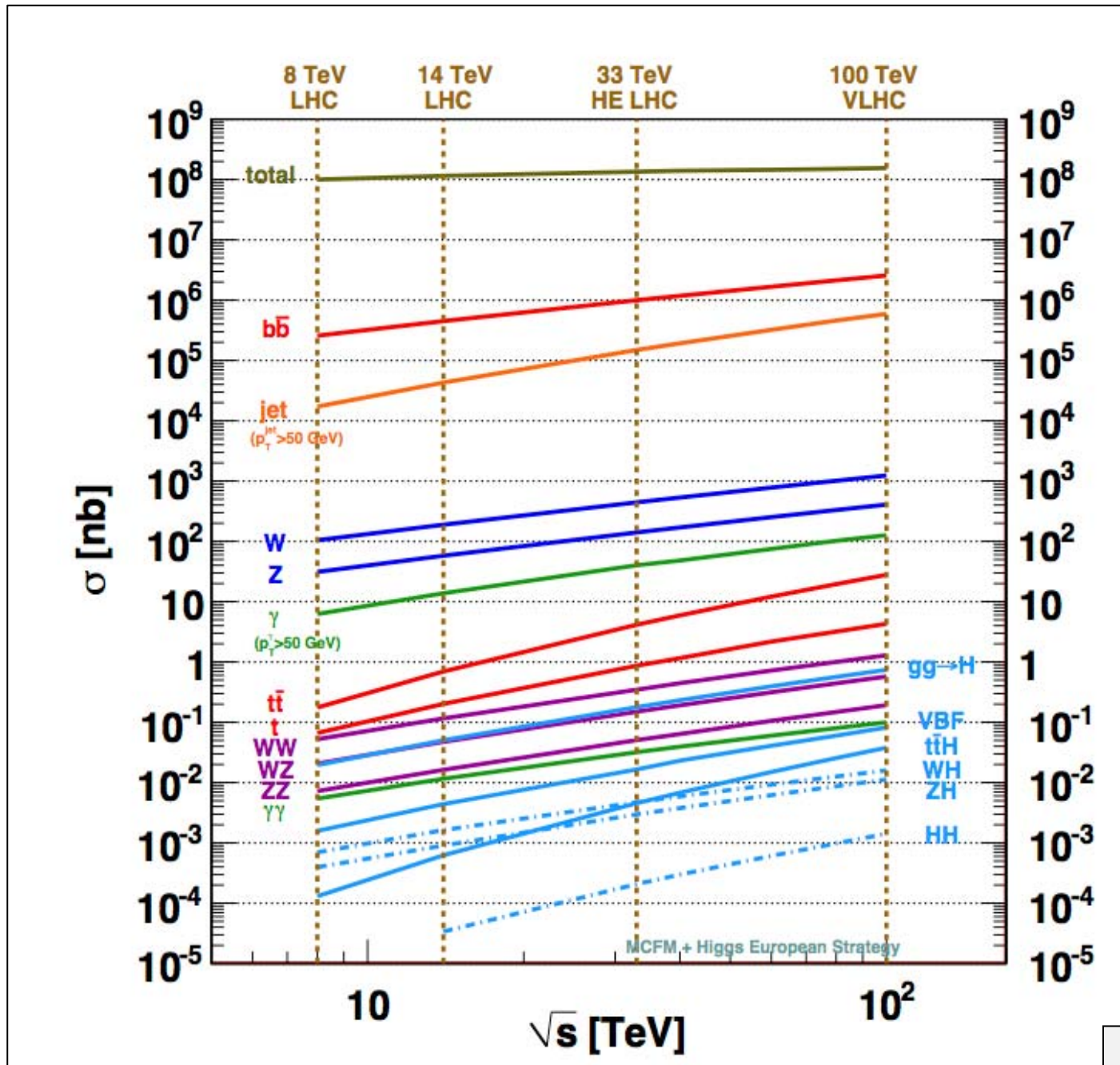
# The Cost of High Luminosities: Pile-Up



**For this we need to rebuild the detector !**

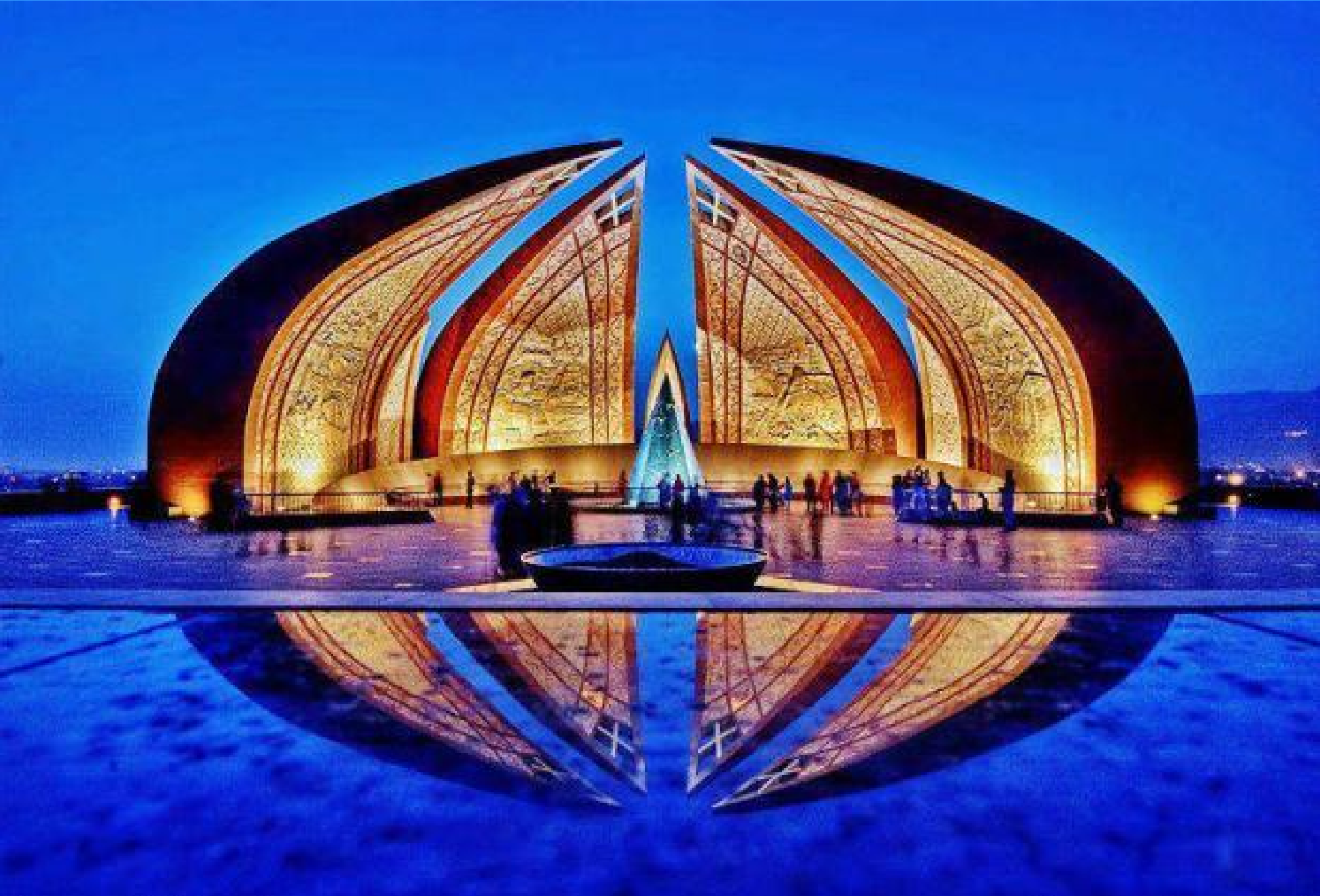


# Our dreams for the Longterm Future



Snowmass report:  
arXiv:1310.5189

# CONCLUSIONS



Twentytwo years after first evidence, top quark physics is a fundamental column in particle physics.

The Tevatron has left a legacy in precision measurements, analysis methods and searches at the energy frontier.

The LHC has become a top factory and outperformed the Tevatron in most aspects.

Theory has been accompanying us in this exciting programme, being a match in terms of precision and paving the way in predicting new phenomena.

So far, agreement with SM predictions is astounding.

**But still: exciting times are awaiting us !**

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Großgeräte  
der physikalischen  
Grundlagenforschung