

# Optics Development for HE-LHC

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- Introduction
- Simplified model of injection lattice with basic IRs without dipoles
  - Three models with  $60^\circ$  and  $90^\circ$  arc cells
- Injection lattice with  $60^\circ$  arcs and realistic IR layout
- Dynamic aperture
- Impact of systematic dipole field errors
- Conclusion and outlook

HE-LHC: 26.659 km ring fitting LHC tunnel, but higher collision beam energy  $\rightarrow$  13.5 TeV

## ❑ Requires stronger magnets

- Present LHC magnets  $\rightarrow$  8.33 T dipole, 223 T/m arc quadrupole, 4430 T/m<sup>2</sup> sextupole, 56 mm aperture
- For HE-LHC  $\rightarrow$  assume “baseline” FCC magnet technology: 16 T dipole, 400 T/m quadrupole, 7800 T/m<sup>2</sup> sextupole, 50 mm aperture
- Dipole field must increase with energy to fit the ring  $\rightarrow$  ~16 T
- Scaling LHC optics to 13.5 TeV: arc quadrupoles would slightly exceed 400 T/m; sextupoles at 7800 T/m<sup>2</sup> may be limiting collision  $\beta^*$  (M.P. Crouch)

## ➤ Study lattices with reduced quadrupole and sextupole strengths

❑ Field quality of dipoles for the HE-LHC energy range is not yet defined  $\rightarrow$  assume pessimistic scenario with larger errors, particularly at injection energy  $\rightarrow$  affects dynamic aperture, depends on injection energy (1.3 TeV proposed for HE-LHC)

## ➤ Design lattice with reduced sensitivity to field errors

## ❑ This study:

### ➤ Investigate lattice designs having

- Low quadrupole and sextupole strengths
- Reduced sensitivity to field errors

### ➤ As a first step, study injection type lattice (expected worse field quality than at collision energy)

### ➤ Focus on arcs design; not yet a detail IR study

### ➤ Use a simplified IR model for general study; verify one model with a realistic IR optics based on SLHCV3.1a layout

### ➤ Compare with LHC lattice layout V6.503

# Proposal – part 1



SLAC

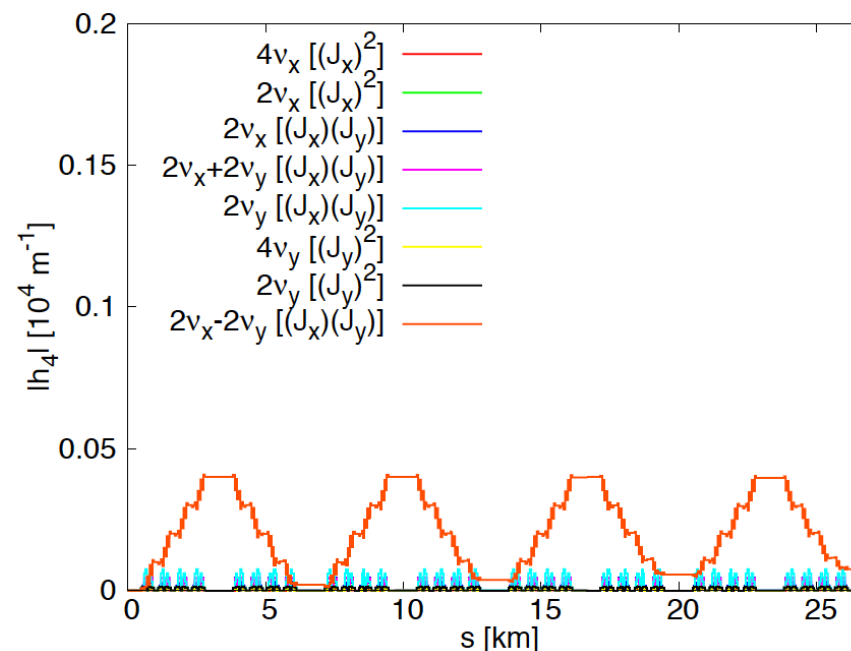
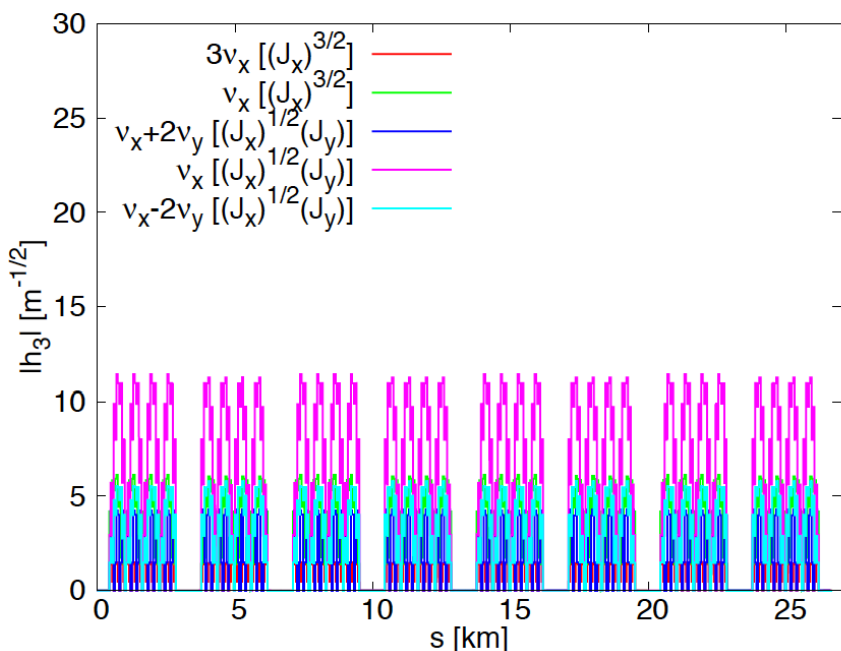
Reduce arc FODO cell phase advance  $\mu$  and / or increase cell length  $L_c$

90 deg $\rightarrow$ 60 deg	Longer cell $L_c$
Weaker quads $\rightarrow$ factor of $\sqrt{2}$ ( $\sim \sin(\mu/2)$ )	Weaker quads $\sim 1/L_c$
Weaker sextupoles $\rightarrow$ factor of 3 (for arcs correction)	Weaker sextupoles $\sim 1/L_c^3$
Lower cell chromaticity $\rightarrow$ factor of $\sqrt{3}$ ( $\sim \tan(\mu/2)$ )	Same cell chromaticity
Similar peak $\beta$ -functions	Larger peak $\beta \sim L_c$
Larger dispersion $\rightarrow$ factor of 2	Larger dispersion $\sim L_c^2$

# Proposal – part 2

## Design arc lattice with reduced sensitivity to systematic non-linear field

- Choose cell phase advance and number of cells  $N_c$  per arc such that  $N_c \mu_c = 2\pi k$ 
  - $\mu_c = 60 \text{ deg} \rightarrow N_c = 24, 18, \dots$  ;  $\mu_c = 90 \text{ deg} \rightarrow N_c = 24, 20, \dots$
- Cancellation of many non-linear resonances from systematic non-linear field in periodic arc (*A. Verdier, PAC'99; Y. Cai, NIM, A645:168–174, 2011*)
  - Potential improvement of dynamic aperture



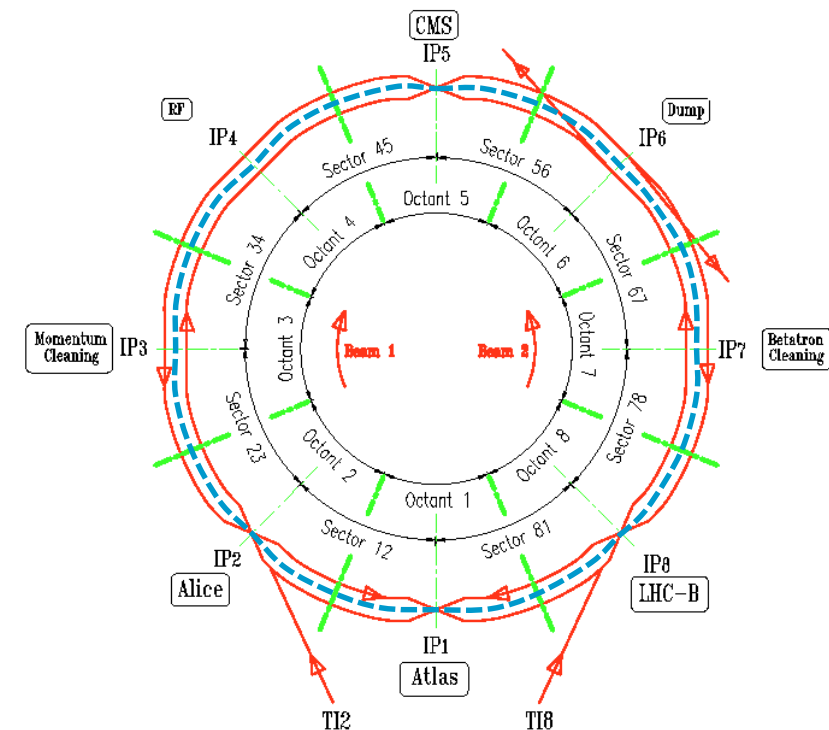
3<sup>rd</sup> and 4<sup>th</sup> order RDT from sextupoles in 60° arcs

Details in talk by D. Zhou

# Lattice model

## Simplified model for injection study

- $C = 26658.8832$  m – same as in LHC
- Same quad and sextupole lengths and same magnet-to-magnet distances as in LHC cell
- Same dispersion suppressors as in LHC
- Odd and even arcs with opposite quad polarity – same as in LHC
- Arc length = average of LHC longer & shorter arcs
- Simple IR straight with anti-symmetric optics without dipoles  
→ 4-fold ring periodicity
- Same fractional tune (.28 / .31) as in LHC injection lattice
- Later → implement realistic IRs from SLHCV3.1a layout with separation dipoles and longer & shorter arcs



Schematic of ring layout:

- Red – two LHC rings with long & short arcs
- Blue dash – sketch of simple model with average length arcs and straight IRs (w/o dipoles)

# Arc configurations studied

Nominal LHC arc has 23 cells with  $90^\circ$  phase advance

- $L_C = 106.9$  m,  $L_B = 14.3$  m,  $N_B = 6$

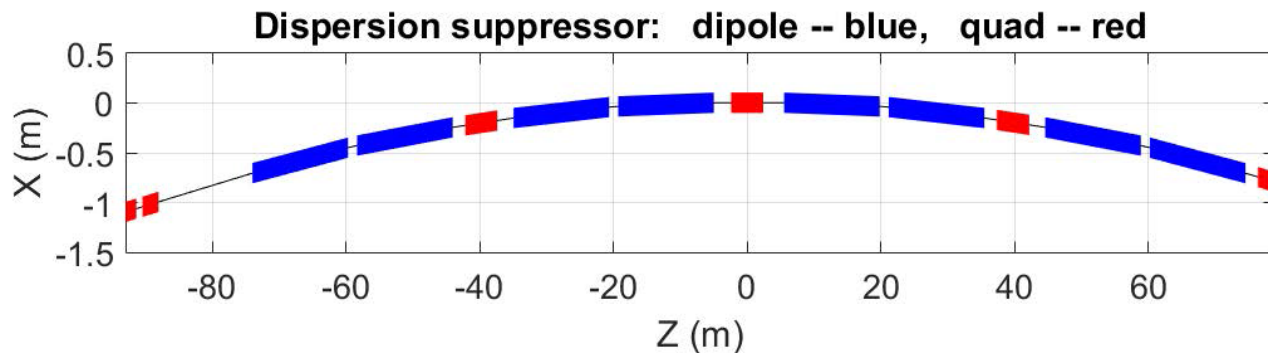
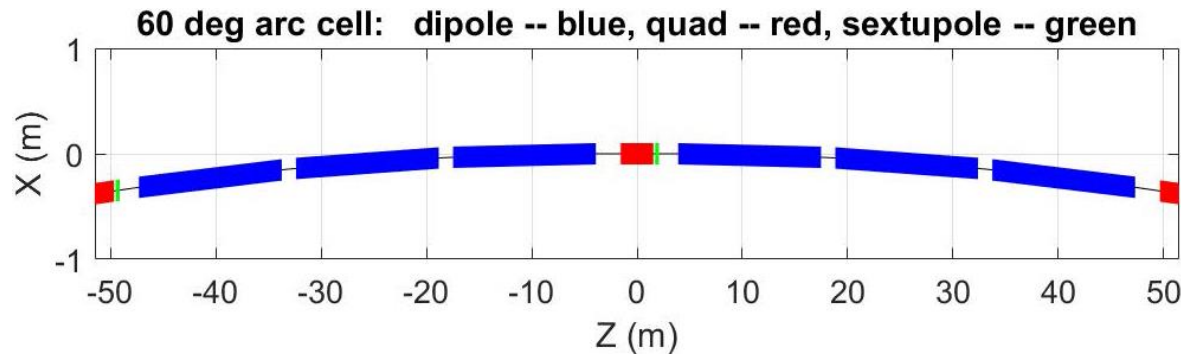
## Three model arcs:

- **24 cells with  $60^\circ$  phase advance**
  - $L_C = 102.446$  m,  $L_B = 13.56$  m,  $N_B = 6$ , fill factor = 0.794
- **18 cells with  $60^\circ$  phase advance**
  - $L_C = 136.594$  m,  $L_B = 14.10$  m,  $N_B = 8$ , fill factor = 0.826 → **lowest dipole field**
- **20 cells with  $90^\circ$  phase advance**
  - $L_C = 122.935$  m,  $L_B = 12.39$  m,  $N_B = 8$ , fill factor = 0.806
- Dispersion suppressors in the simple model are kept identical to the LHC design (for geometry) with eight **14.3 m dipoles in DS** → 2 types of dipoles (arc and DS)
- In a more realistic design (24 x  $60^\circ$  + SLHCV3.1a IRs), 2 types of dipoles are changed to one type dipole in the arc and DS, and geometry is rematched

# Geometry

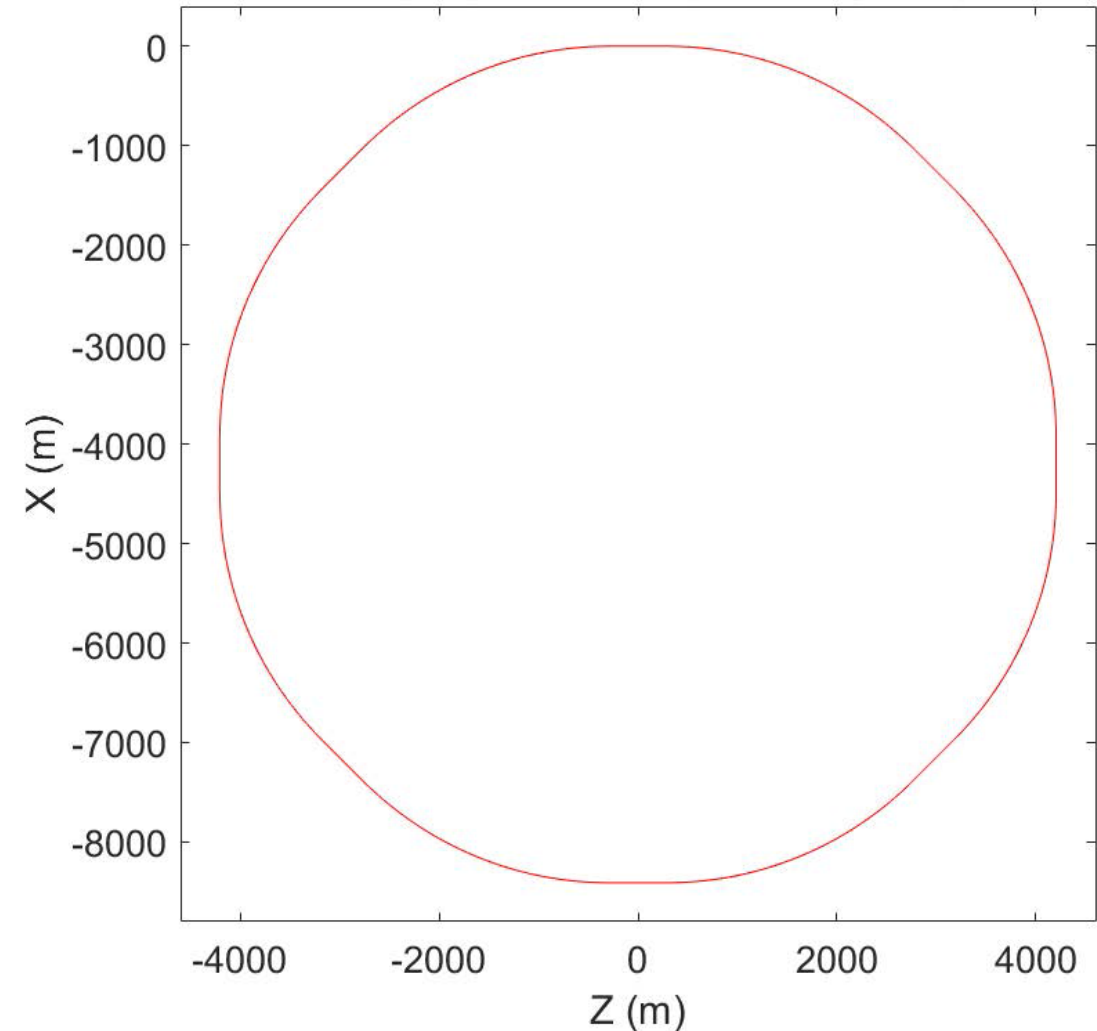
Geometry of the model ring is matched reasonably close to the LHC ring (some deviations of cm level)

One cell of 24-cell arc design



Dispersion suppressors are attached to either F or D arc quadrupole → two types of optics match

LHC (red) and 60 deg model (black)



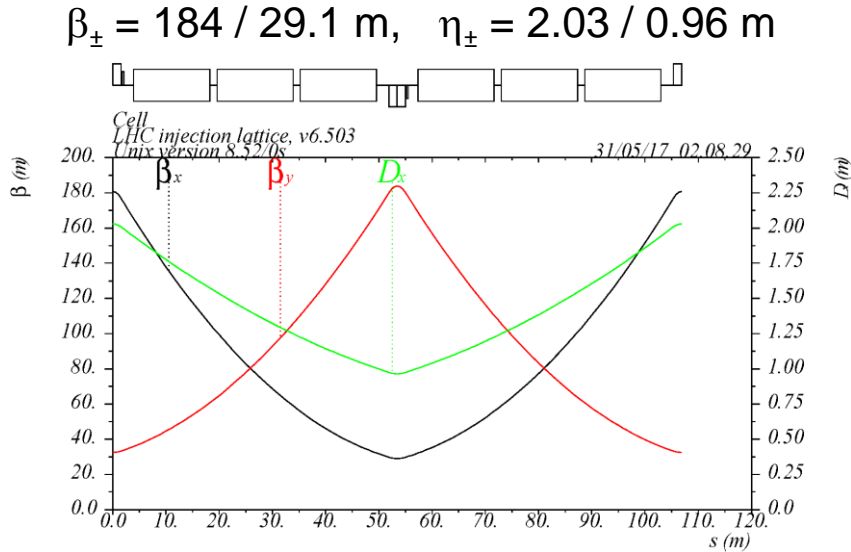


# Arc cells: LHC and 3 models

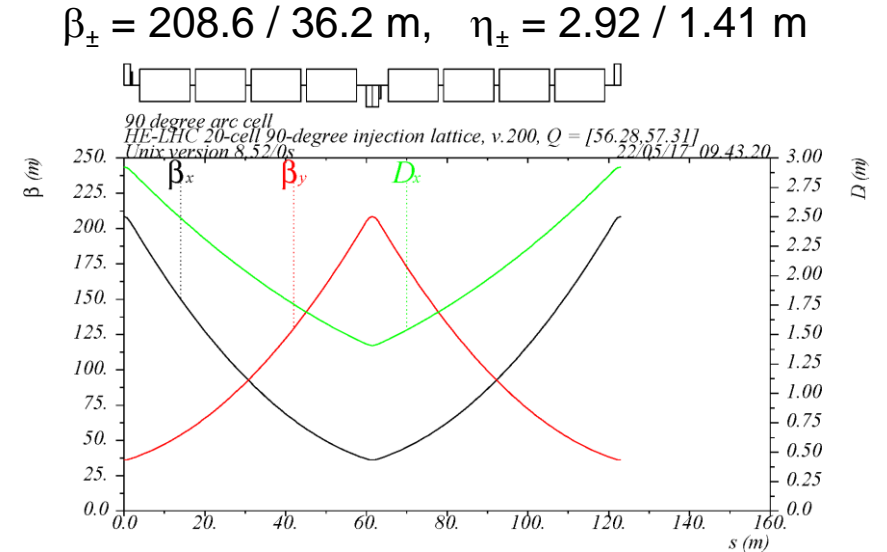


SLAC

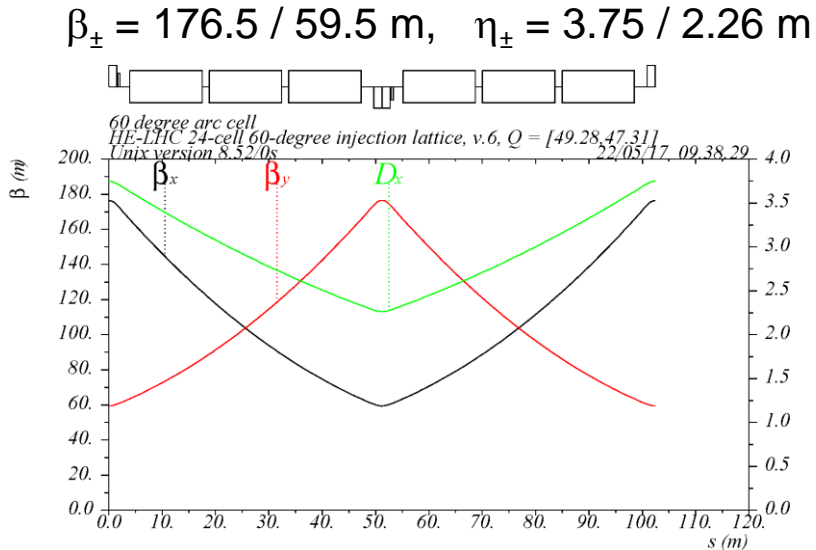
LHC V6.503  
23 x 90° arc  
 $L_c = 106.9$  m



Model  
20 x 90° arc  
 $L_c = 122.94$  m

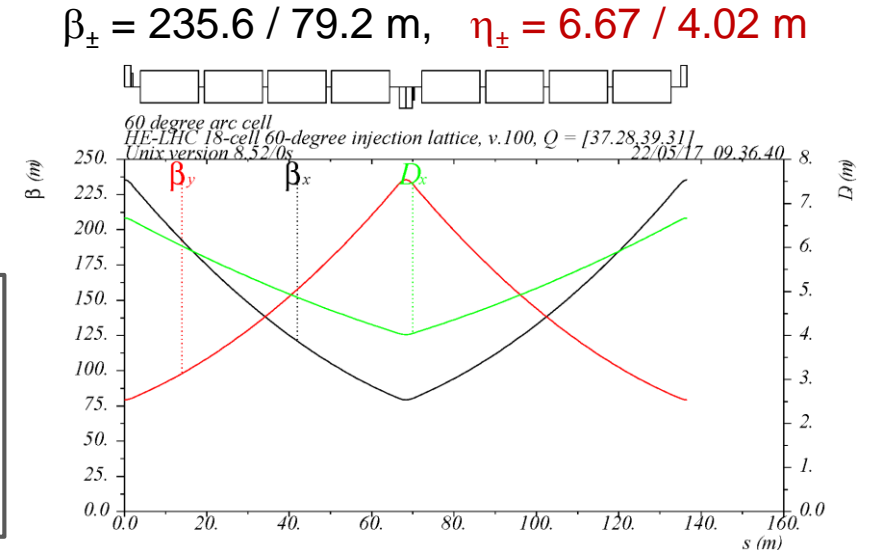


Model  
24 x 60° arc  
 $L_c = 102.45$  m



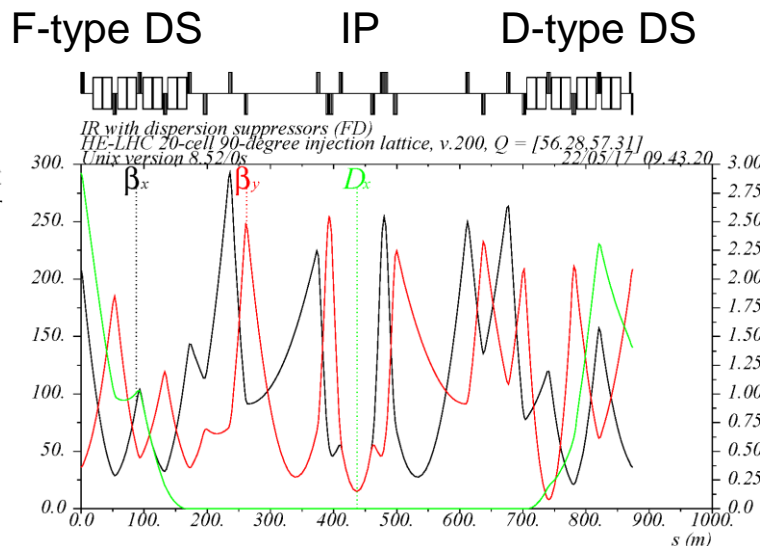
Model  
18 x 60° arc  
 $L_c = 136.59$  m

Large  $\beta$  &  $\eta \rightarrow$   
For collimation  
>1 TeV injection  
energy  
(F. Zimmermann)

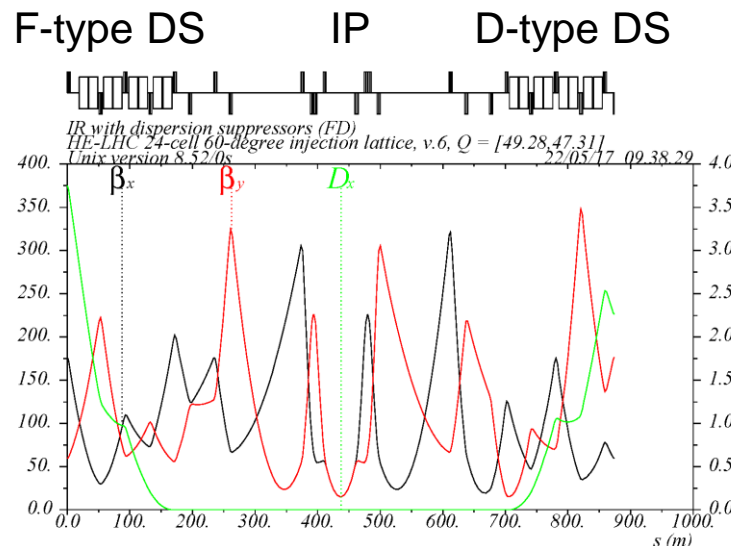


# IR straight and dispersion suppressors

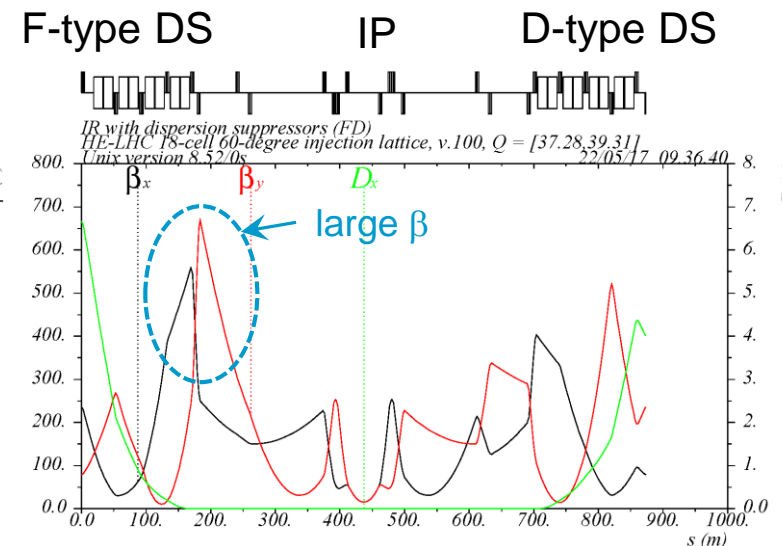
- LHC-type dispersion suppressor made of 2 FODO cells with eight 14.3 m dipoles
- Two types of DS optics (attached to F or D arc quad); IR dispersion is exactly cancelled
- Simple IR model with IP triplets and matching quads; no IR dipoles; small injection-type  $\beta$
- Findings:
  - LHC-type DS matches better to 90° arcs, less optimal for 60° arcs, especially for a longer cell (18 x 60°); the match could be improved by adjustment of the adjacent 1-2 arc quads (small adjustments are preferred to minimize impact on non-linear field cancellation properties in the arc)



IR + 2 DS  
20 x 90° arc



IR + 2 DS  
24 x 60° arc

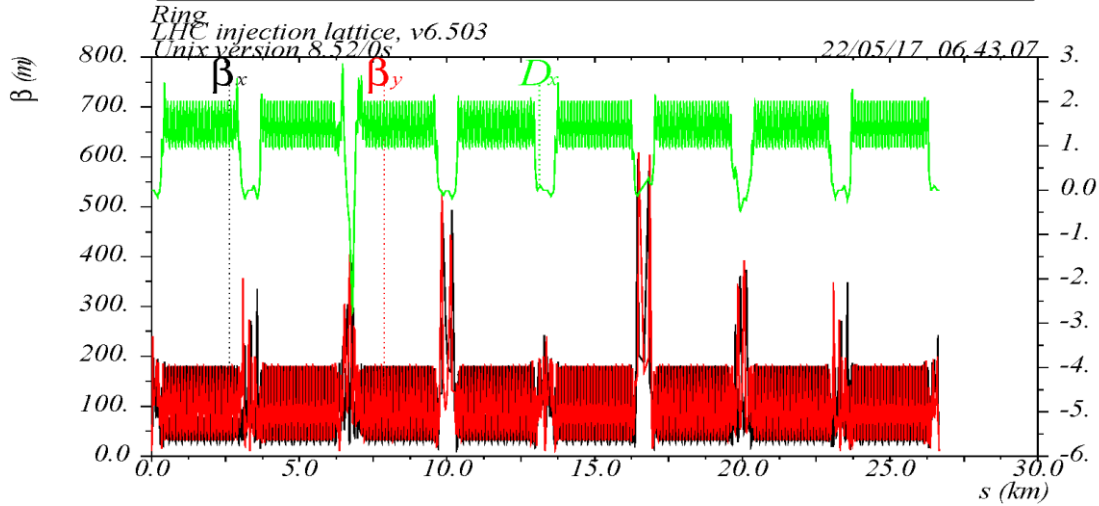


IR + 2 DS  
18 x 60° arc

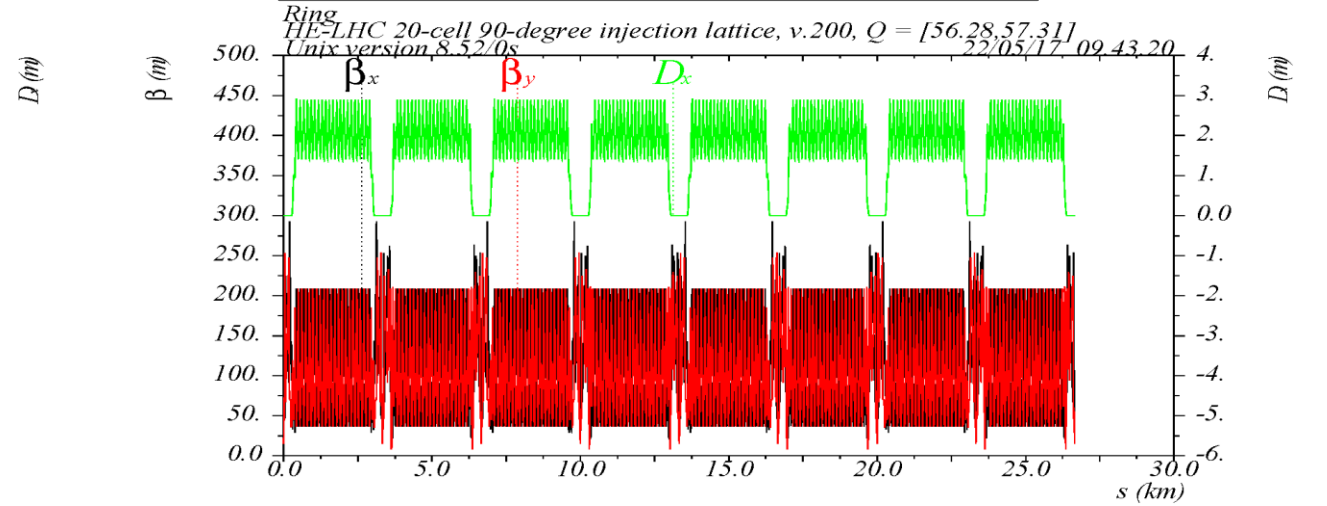
# Complete ring: LHC and 3 models



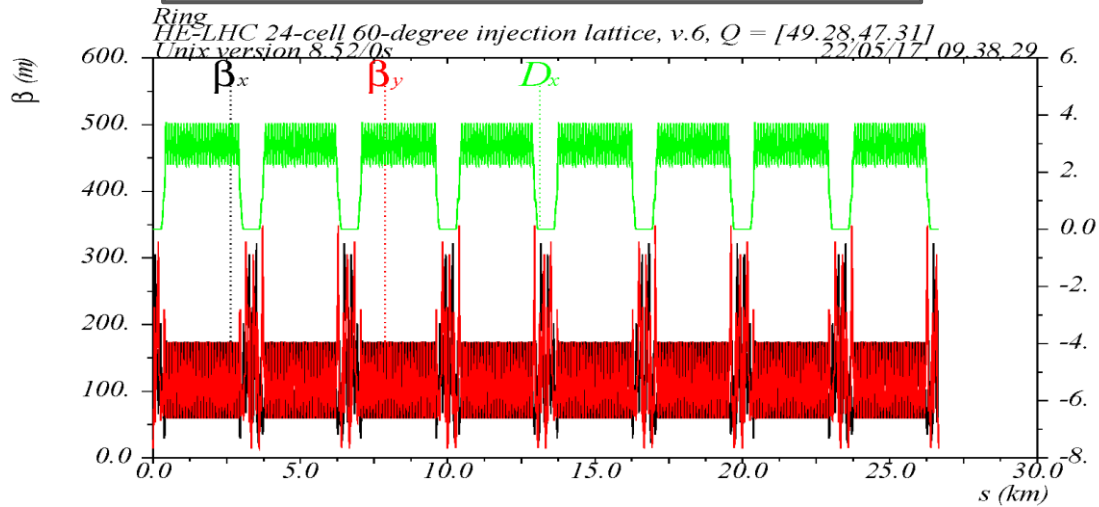
LHC V6.503, 23 x 90° arc, Q = 64.28, 59.31



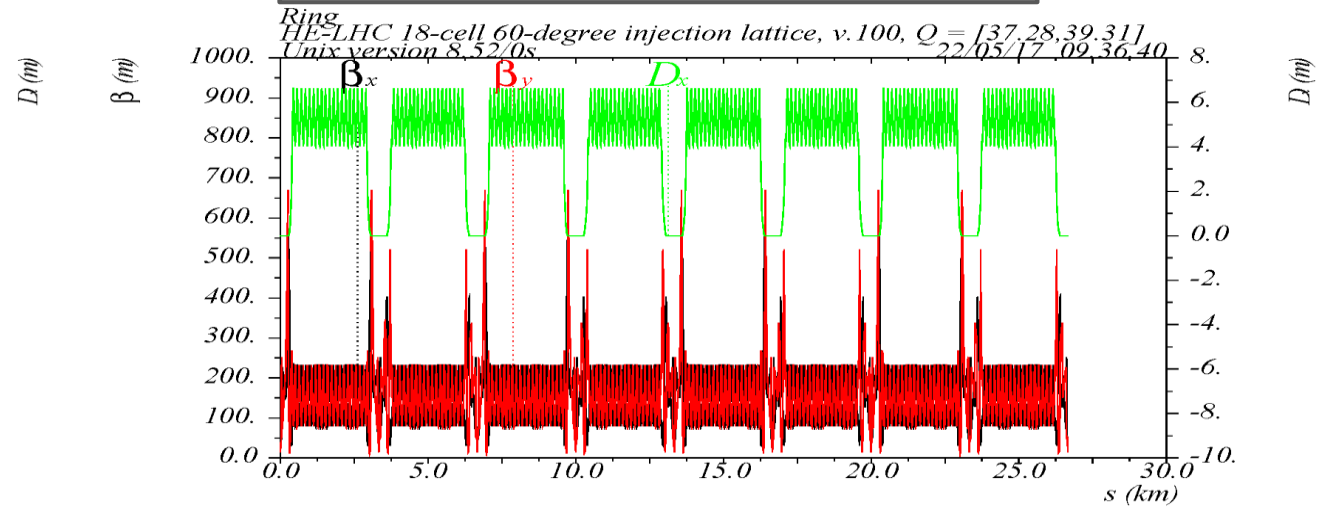
Model, 20 x 90° arc, Q = 56.28, 57.31



Model, 24 x 60° arc, Q = 49.28, 47.31

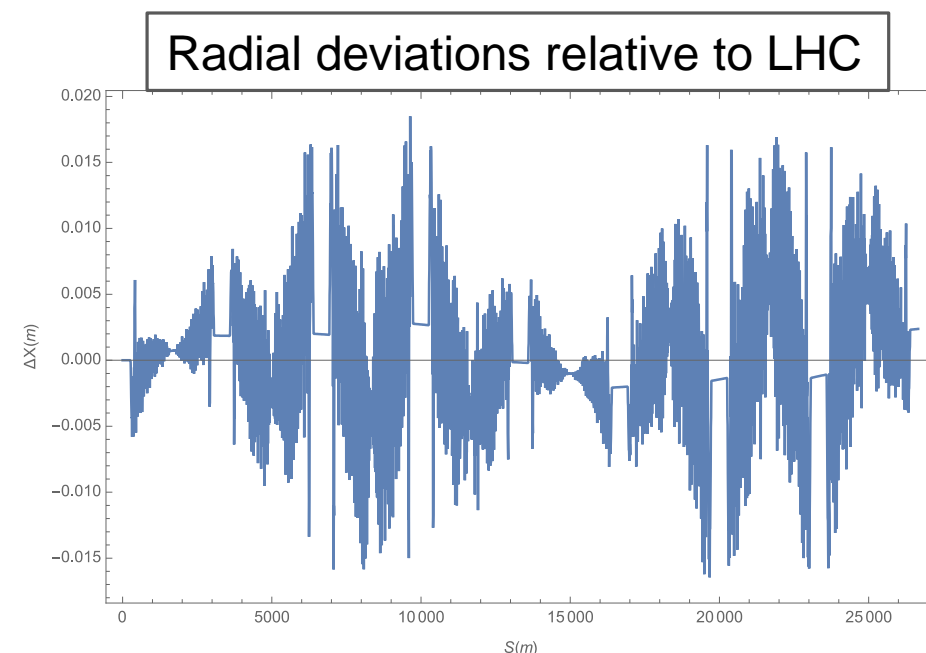


Model, 18 x 60° arc, Q = 37.28, 39.31



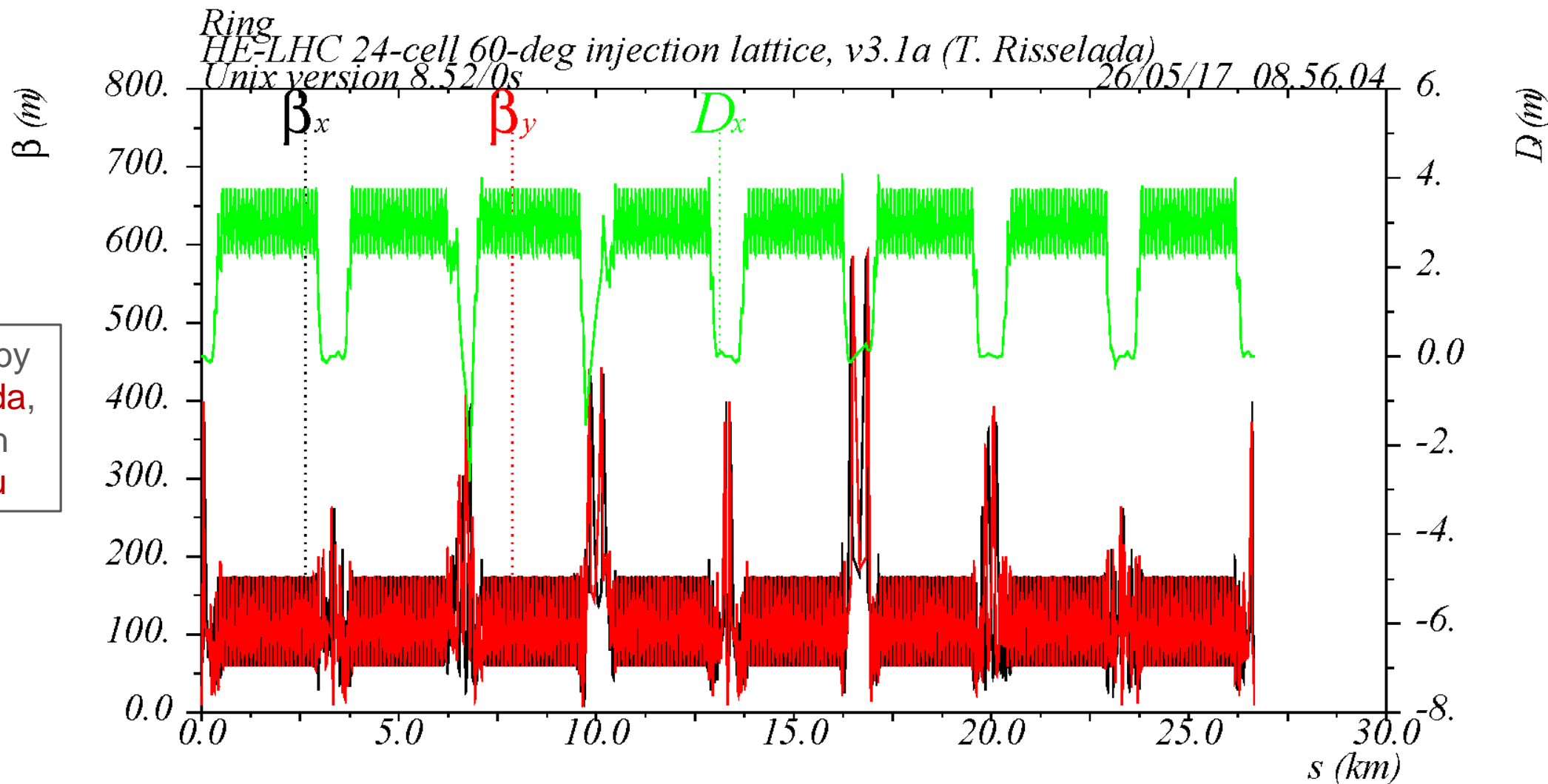
## 24 x 60° model + realistic IRs (T. Risselada)

- Arcs with 24 x 60° cells are combined with IRs from **SLHCV3.1a layout** (differs from LHC only in IR1, 5) as suggested by S. Fartoukh
- Separation dipoles included for a realistic layout for the clock-wise beam
- **One type of dipole** (13.56 m) is used in the arcs and DS
- Small adjustments to length of arc cell and DS for geometry match (radial deviations within ~cm level compared to LHC)
- Improvement to optics match from arcs to DS to IR using 1-2 quad adjustments in the last arc cell
- Strong SC separation dipoles due to increased separation (250 mm used) and reduced distance (specifications per D. Shoerling):
  - 12 T D1, D2; 8T D3, D4 (IR4)
- 1.8 T for NC dipoles D3, D4 → preliminary layout of IR3, 7 → should be carefully reviewed



# Complete ring with 24 x 60° arcs and SLHCV3.1a IRs

Optics files available at official repository [/afs/cern.ch/eng/lhc/optics/HELHC](https://afs.cern.ch/eng/lhc/optics/HELHC)



# Injection lattice parameters at 13.5 TeV

	LHC V6.503 23 x 90 deg	Model 24 x 60 deg	Model 18 x 60 deg	Model 20 x 90 deg	SLHCV3.1a 24 x 60 deg
Cell length, m	106.90	102.45	136.59	122.94	102.89
Dipole length, m	14.3	13.56 <sup>(1)</sup>	14.1 <sup>(1)</sup>	12.39 <sup>(1)</sup>	13.56
Number of dipoles	1232	1280	1280	1424 <sup>(2)</sup>	1280
Dipole B, T	16.06	16.30 <sup>(1)</sup>	15.68 <sup>(1)</sup>	16.04 <sup>(1)</sup>	16.30
Cell quad B', T/m	404.8	289.5	215.9	340.0	288.2
Sextupole B'', T/m <sup>2</sup> <sup>(3)</sup>	4883	2057	1103	3366	1891
Max/Min arc $\beta$ , m	184 / 29	177 / 60	236 / 79	209 / 36	178 / 60
Max/Min arc $\eta$ , m	2.03 / 0.96	3.75 / 2.26	6.67 / 4.02	2.92 / 1.41	3.78 / 2.28
Tune, x/y	64.28 / 59.31	49.28 / 47.31	37.28 / 39.31	56.28 / 57.31	46.28 / 45.31
Momentum compaction	3.22 10 <sup>-4</sup>	6.41 10 <sup>-4</sup>	1.13 10 <sup>-3</sup>	4.57 10 <sup>-4</sup>	6.50 10 <sup>-4</sup>
Natural chromaticity	-86 / -82	-63 / -63	-53 / -63	-78 / -80	-58 / -59

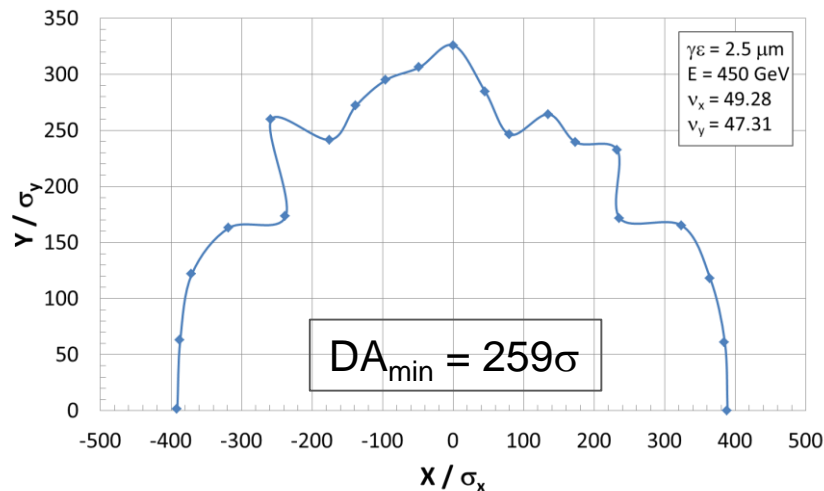
- (1) Extrapolating to one type of dipole in arcs and DS (2) Assuming additional dipole in each DS in 20 x 90 deg model  
 (3) For injection optics chromaticity **FCC baseline target: 16 T dipole, 400 T/m quad, 7800 T/m<sup>2</sup> sextupole**

## Dynamic aperture studies

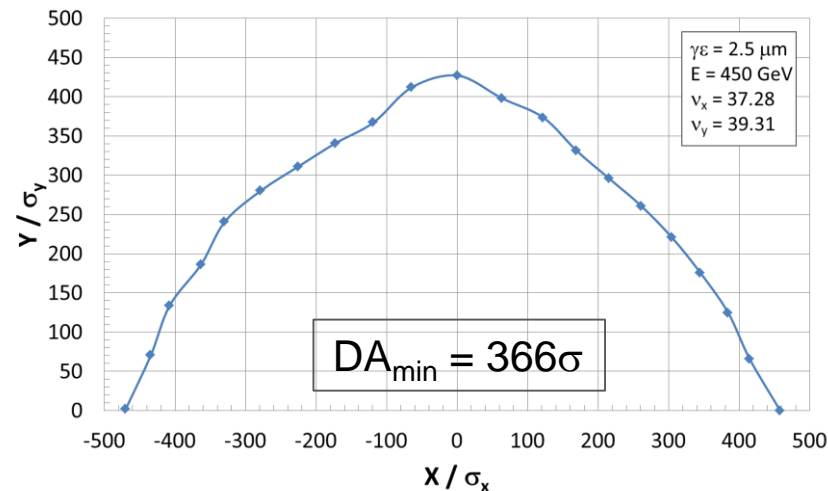
- Tracking using LEGO code (*Y. Cai, SLAC-PUB-7642, 1997*)
- DA is calculated at IP ( $\beta = 15$  m in model lattice)
- DA is shown in number of beam  $\sigma$  at 450 GeV
  - 1.7 times more sigma's at 1.3 TeV injection energy proposed for HE-LHC
- Normalized emittance = 2.5  $\mu\text{m-rad}$
- Chromaticity corrected to +3 using SF, SD arc sextupoles
- 21 angles in x-y space
- Nominally 1024 turns tracking, but also tested at  $10^4$  turns  $\rightarrow$  5-10% underestimate
- Initial  $dp/p = 7.5 \cdot 10^{-4}$

# Dynamic aperture without errors

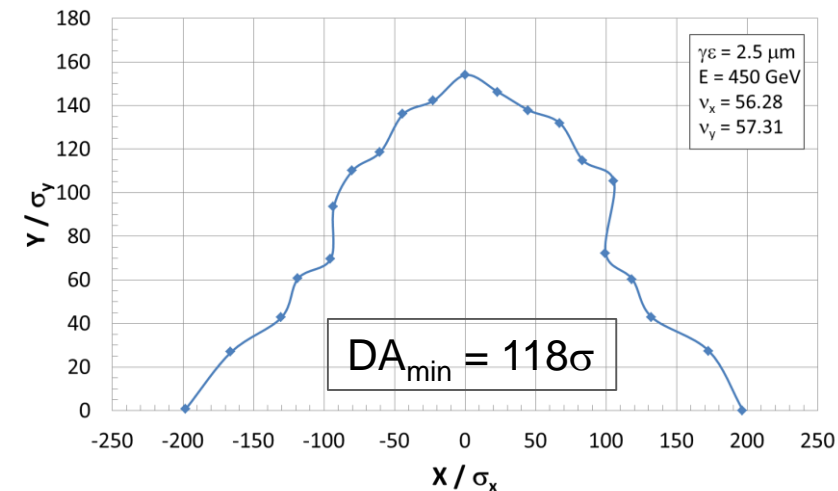
24 x 60-degree arc cells and basic IRs; no errors



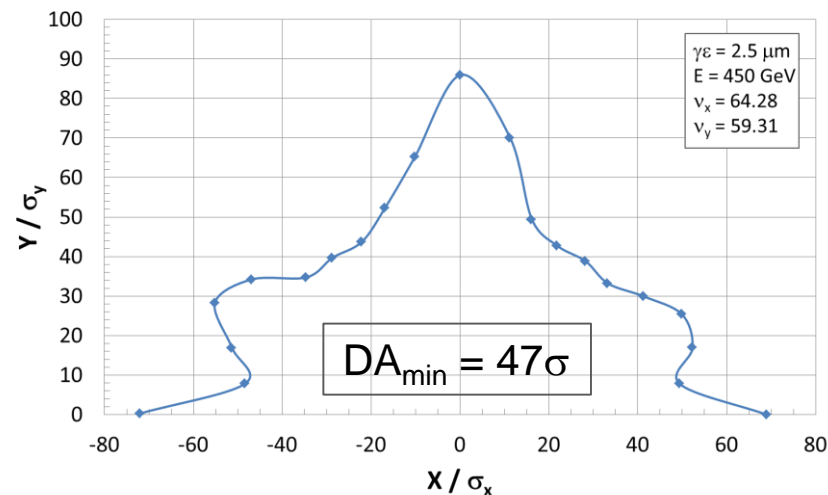
18 x 60-degree arc cells and basic IRs; no errors



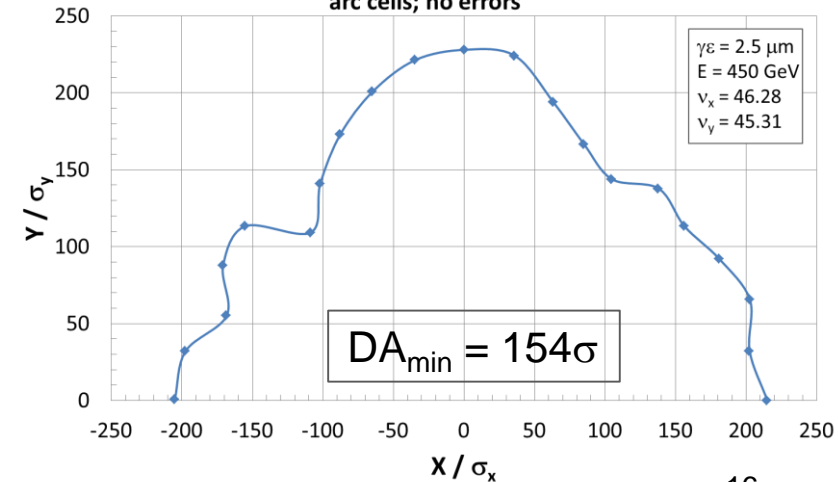
20 x 90-degree arc cells and basic IRs; no errors



LHC V6.503 injection lattice, 23 x 90-degree arc cells; no errors



LHC V3.1a injection lattice modified to include 24 x 60-degree arc cells; no errors



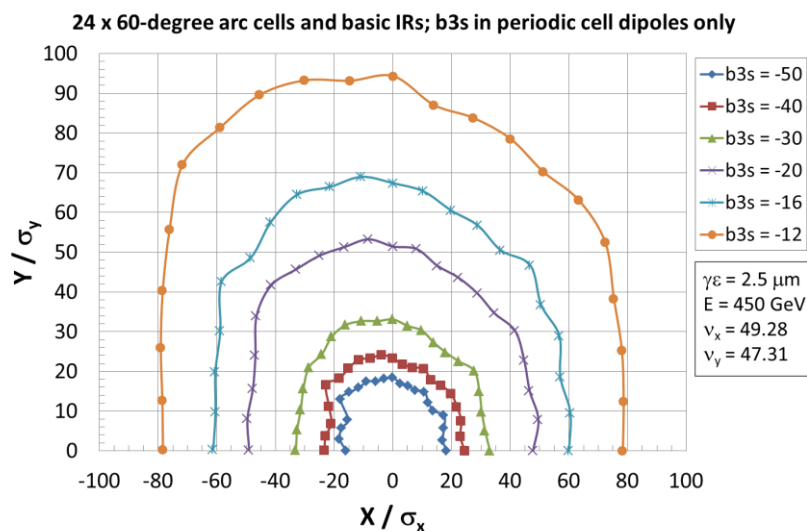
- Huge DA for model lattices due to built-in arc non-linear compensation (cancellation of sextupole effects), but also due to 4-fold periodicity
- Larger DA of SLHCV3.1a model compared to LHC V6.503, due to 60° arcs with weaker sextupoles, but arc compensation may not be perfect due to quad adjustments at arc ends

→ May not be a completely fair comparison, but indicates that non-linear field compensation works

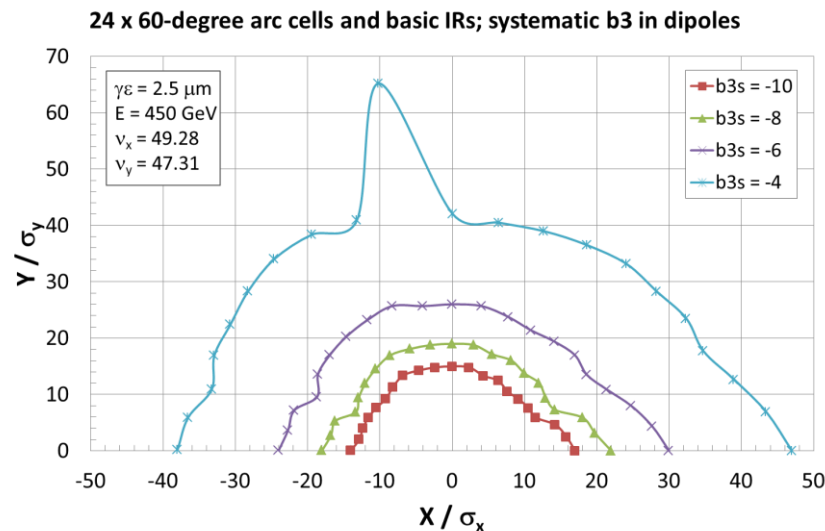


# 24 x 60 deg model with systematic b3s in dipoles

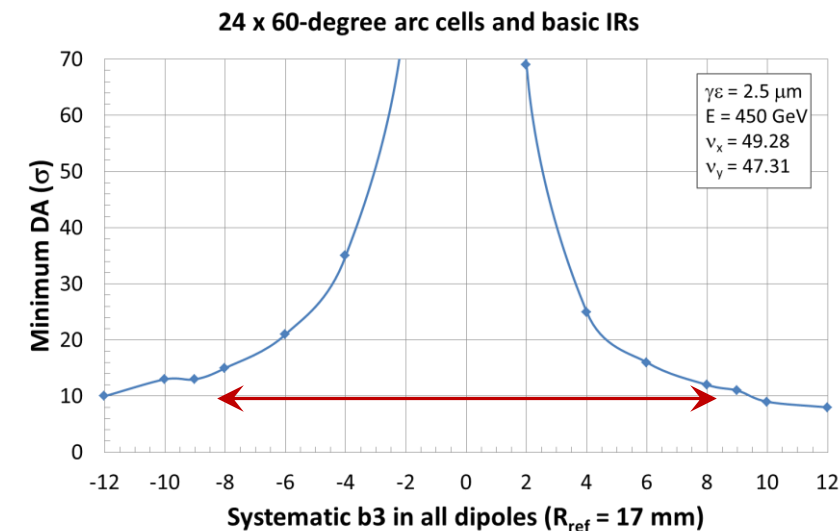
- Dipole FQ for HE-LHC is not yet defined. Estimates for FCC suggest  $b_{3s} = 6$ ,  $b_{5s} = -1$ ,  $b_{3r} < 1$ ,  $b_{5r} < 0.1$  for FCC injection ( $R_{ref} = 17$  mm) (*E. Todesco, FCC Week 2016*)
- Observe very large acceptable  $b_{3s}$  range (50 units) if  $b_{3s}$  is only in periodic cell dipoles  $\rightarrow$  confirms arc compensation properties
- If  $b_{3s}$  is in both arc cells and DS dipoles, the range is  $\sim 8$  units (but without other errors)
- Large chromaticity from  $b_{3s}$  is corrected by arc sextupoles. Using dipole  $b_3$  correctors (as in LHC) may help improving the DA (the correctors not included in this study).



$b_{3s}$  in periodic cell dipoles only

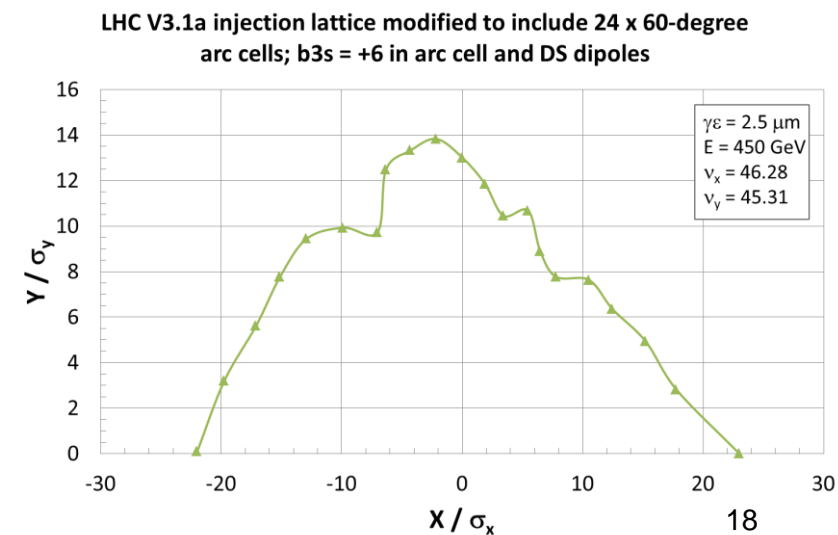
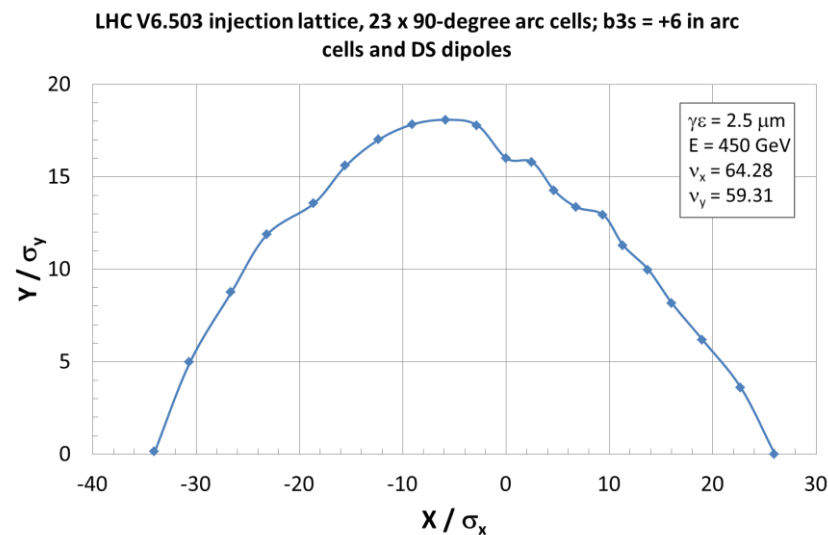
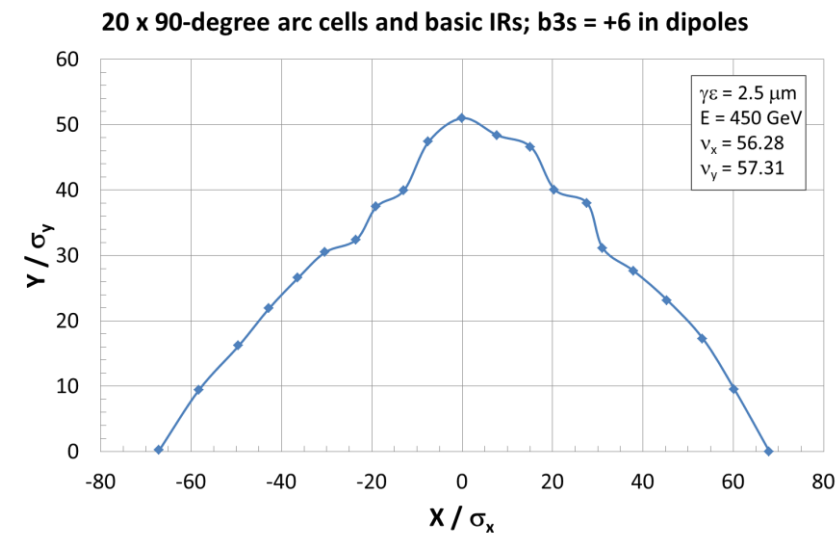
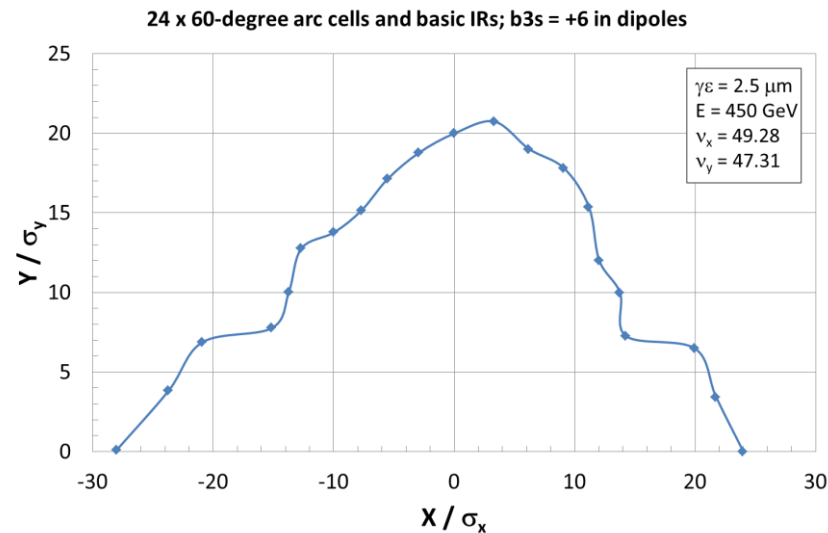


$b_{3s}$  in arc and DS dipoles



# DA for $b_{3s} = +6$ in dipoles

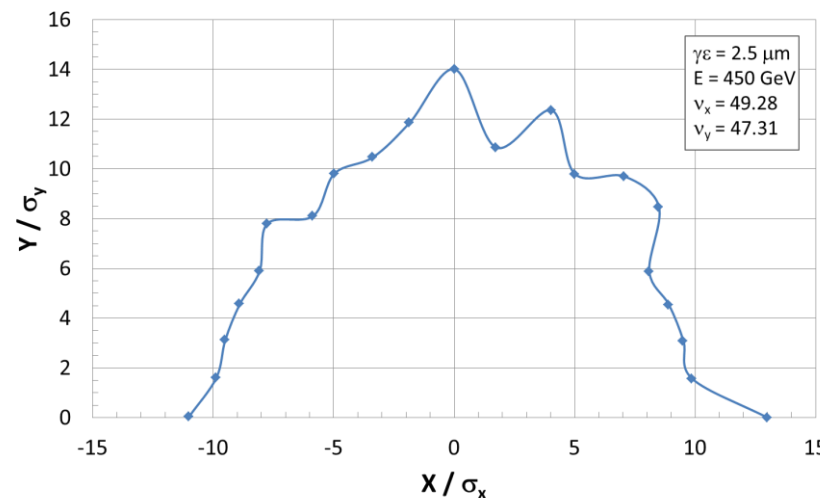
- Try  $b_{3s} = +6$  as estimated for FCC (E. Todesco)
- Sufficient DA for all lattices except 18 x 60° model
- **Largest aperture for 20 x 90° model**
- **Small DA for 18 x 60° model** (not shown), possibly due to large beta functions at dipoles in dispersion suppressors. Should investigate if the DA can be increased by improving the match with adjustment of 1-2 quads in the adjacent to DS arc cell.



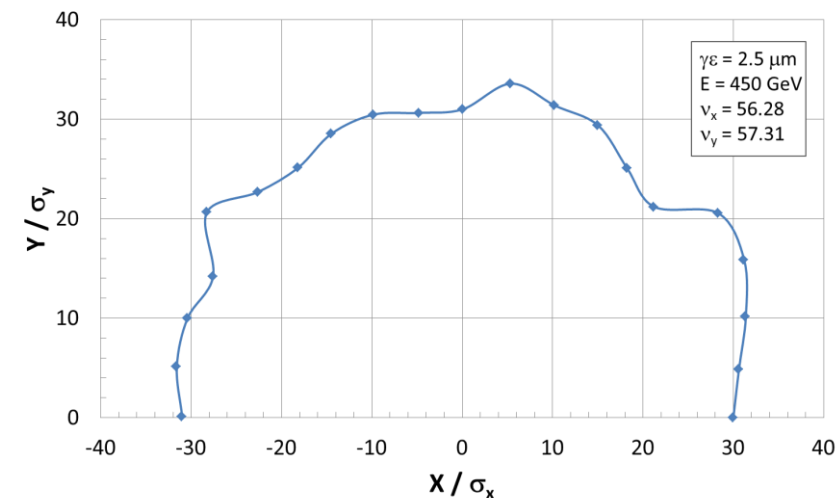
# DA for b3s = +6 and b5s = -1 in dipoles

- Comfortably large aperture for 20 x 90° model
- Stronger b5 impact on 24 x 60° model and modified SLHCV3.1a. DA is near 10σ at 450 GeV → acceptable at 1.3 TeV injection energy (σ is 1.7 times smaller)
- Sufficient DA of LHC V6.503 lattice
- Small DA for 18 x 60° model (not shown) due to impact of b3s → improvements are needed
- Some of the b5 impact could be due to Qx-4Qy resonance being within ~0.01 near the injection working point
- Including b5 correctors for dipoles may help improving the DA

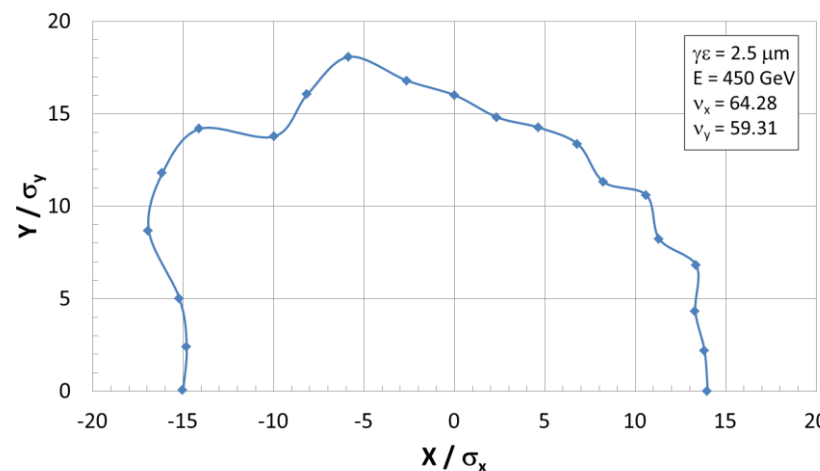
24 x 60-degree arc cells and basic IRs; b3s = 6, b5s = -1 in dipoles



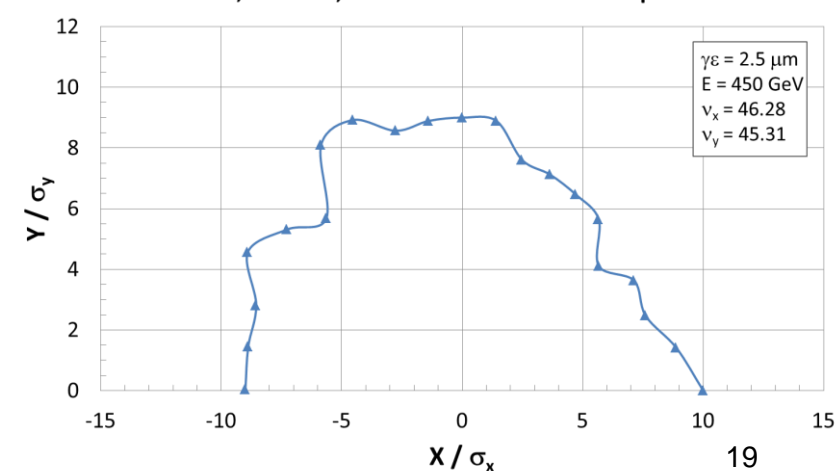
20 x 90-degree arc cells and basic IRs; b3s = +6, b5s = -1 in dipoles



LHC V6.503 injection lattice, 23 x 90-degree arc cells; b3s = +6, b5s = -1 in arc cell and DS dipoles



LHC V3.1a injection lattice modified to include 24 x 60-degree arc cells; b3s = +6, b5s = -1 in arc cell and DS dipoles

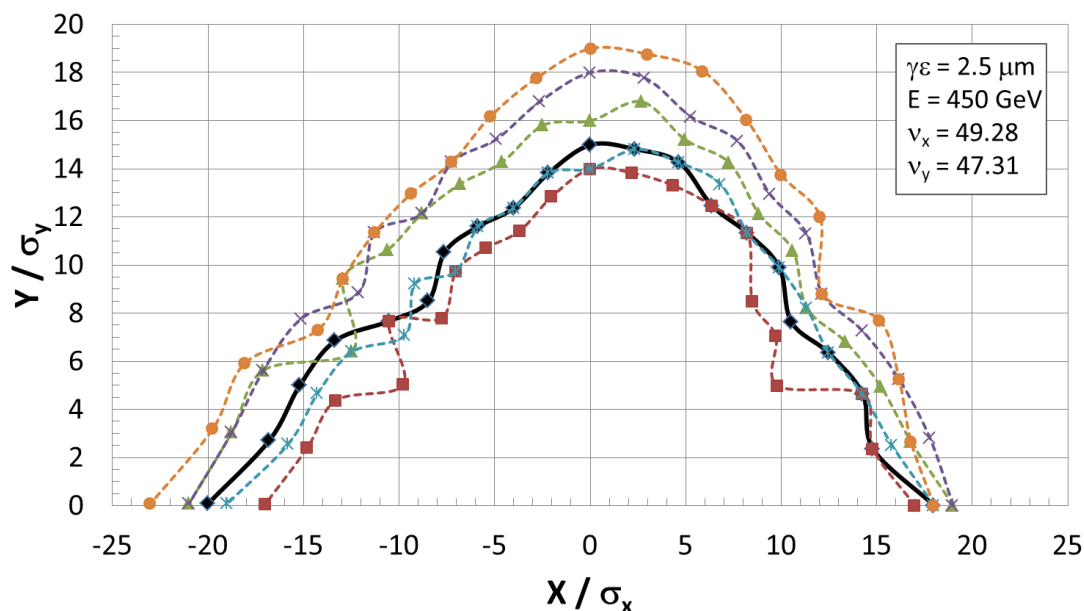


# Systematic and random b3, b5 in dipoles

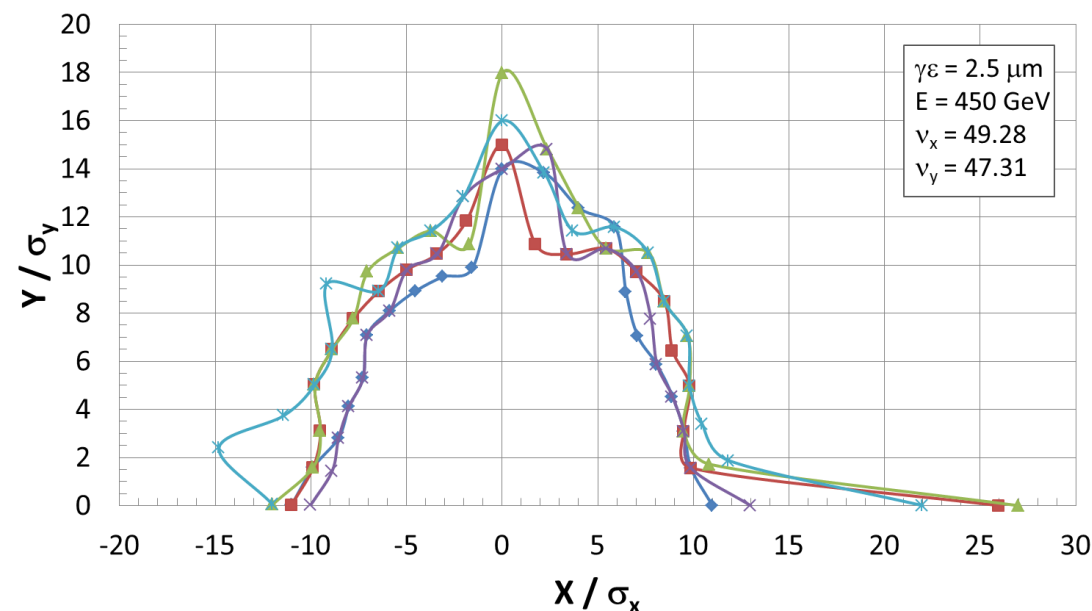
Limited study of random error effects for 24 x 60° simple model

- $b_{3s} = +8$ ,  $b_{3r} = 1$ , 5 random seeds  $\rightarrow$  moderate DA reduction due to random b3
- $b_{3s} = +6$ ,  $b_{3r} = 1$ ,  $b_{5s} = -1$ ,  $b_{5r} = 0.1$   $\rightarrow$  not significant impact from b3r, b5r compared to systematic error only (shown on previous page)

24 x 60-degree arc cells and basic IRs;  $b_{3s} = +8$  in dipoles with  $b_{3r} = 0$  (solid black) and  $b_{3r} = 1$  (dash lines -- 5 seeds)



24 x 60-degree arc cells and basic IRs;  $b_{3s} = +6$ ,  $b_{3r} = 1$ ,  $b_{5s} = -1$ ,  $b_{5r} = 0.1$  in dipoles (5 seeds)



# Conclusions and Outlook

- HE-LHC injection lattice models with reduced quad and sextupole strengths and compensation of systematic non-linear field in arcs have been studied, including a realistic design based on SLHCV3.1a IRs
- The 18-cell 60° model has the lowest magnet strengths with dipole field <math><15.7\text{ T}</math>. But the present optics needs improvements to satisfy acceptable DA with dipole errors.
- The 20-cell 90° model may satisfy the 16 T target with some adjustments. It provides the largest DA (so far), but requires stronger quads and sextupoles than 60° models.
- The 24-cell 60° lattices have acceptable DA, but the dipole field is 0.3 T above the target

**A lot of more work to be done**

- The 18-cell x 60° lattice requires optimization to improve the DA
- A detailed look at realistic IR designs such as separation layout, dipole requirements, layout of injection and extraction systems, collimation scheme, etc...
- More comprehensive tracking simulations



**SLAC**

Thank you for your attention!