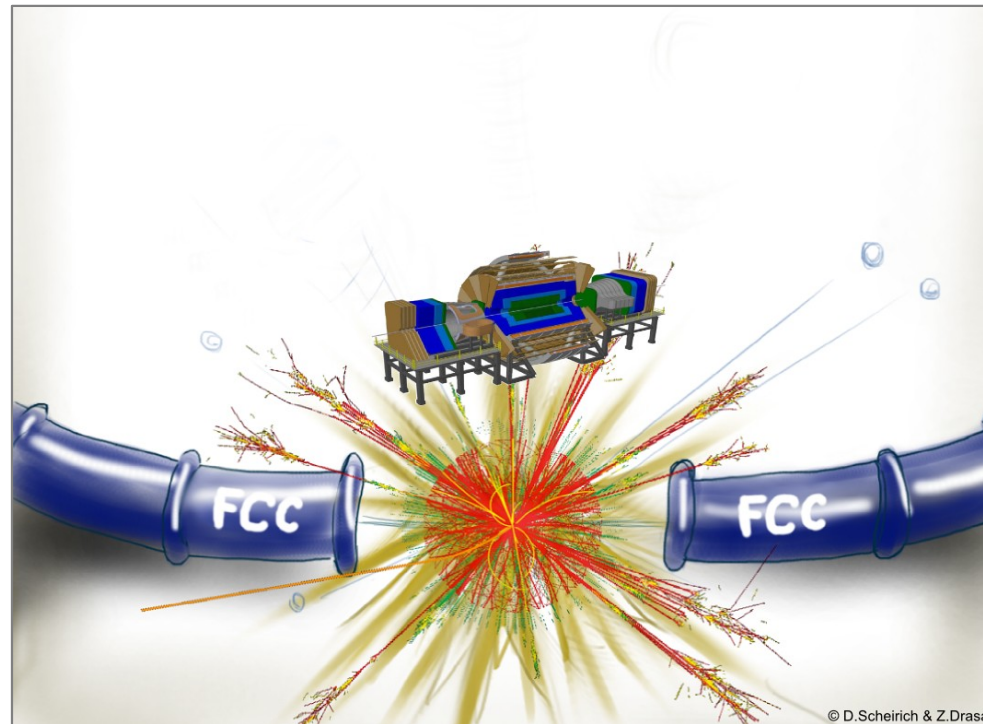


Pattern Recognition & Tracker with Tilted Layout



Zbyněk Drásal
CERN



With many thanks to: G. Hugo & S. Mersi (CMS)



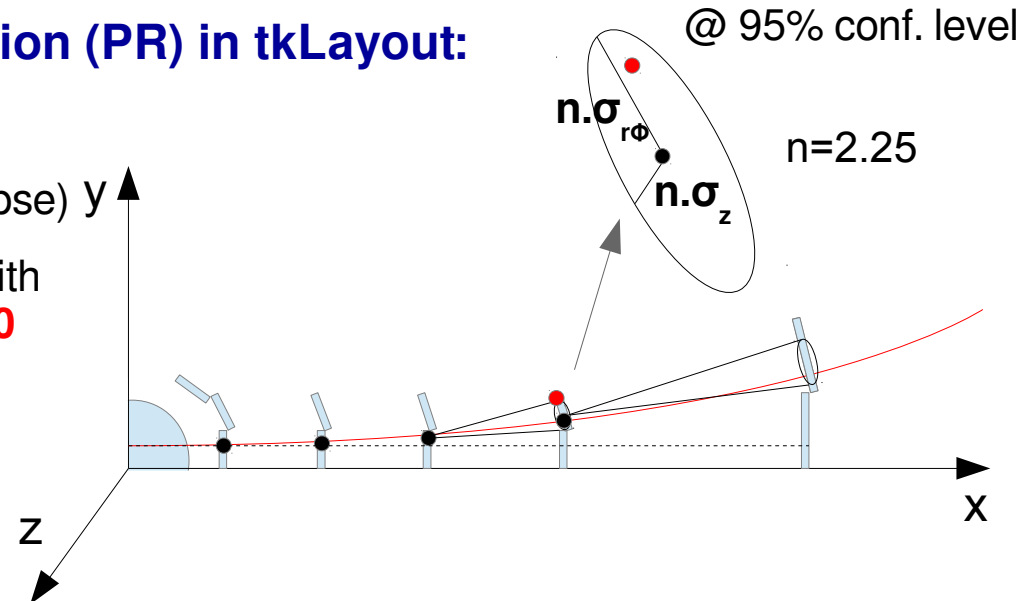
Overview

- **Mathematical concept of tkLayout pattern recognition in a nutshell**
 - Short recap of math. technique introduced 2 months ago
 - Interpretation of method results → comparison with CMS Ph2 tracker layout
- **Non-tilted layout & pattern recognition capabilities**
 - Drawbacks & solution
 - Details on individual layout parameters affecting particle propagation & pattern recognition
- **First proposal of tilted layout**
 - Study of pattern recognition performance
 - Improvement in track parameters resolution
- **Summary & Outlook**

TkLayout Pattern Recognition in a Nutshell

- **Mathematical concept of pattern recognition (PR) in tkLayout:**

- Start with a triplet assuming **perfect seeding**
- Propagate $\sigma_{r\phi}$, σ_z to the **i-th layer** (use error ellipse) y
- Calculate probability p to mis-match a **real hit** with a **bkg hit** @ 95% confidence level → **in PU=1000**



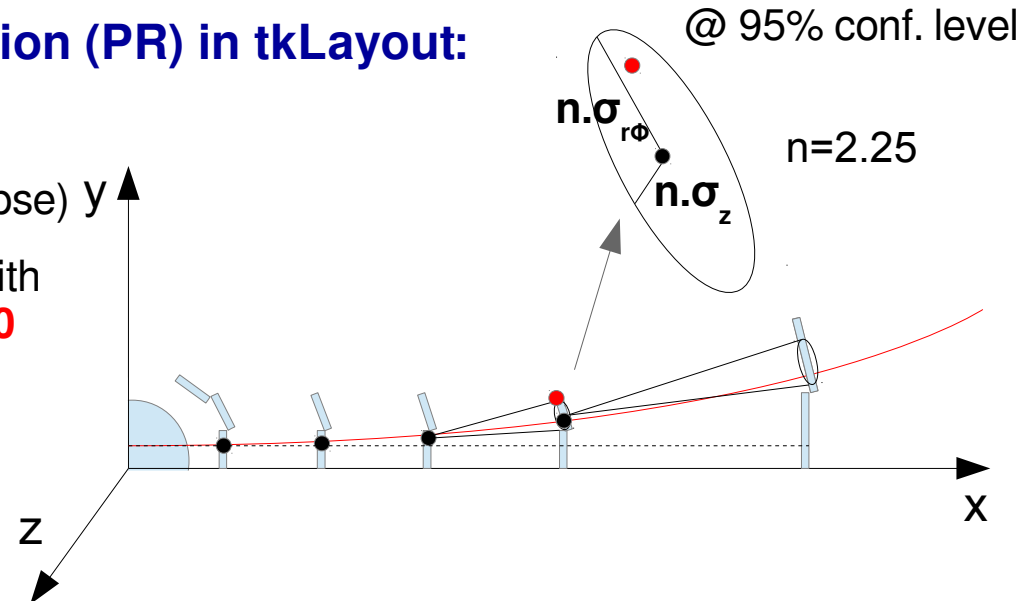
- **To quantitatively evaluate the overall tracker performance**, calculate a probability that the track has been found with any ambiguity:

$$p = 1 - \prod_{i=4}^N (1 - p_{\text{bkg}95\%}^i)$$

TkLayout Pattern Recognition in a Nutshell

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- **To quantitatively evaluate the overall tracker performance**, calculate a probability that the track has been found with any ambiguity:

$$p = 1 - \prod_{i=4}^N (1 - p_{\text{bkg}95\%}^i)$$

- **Strategy: Check “weak” spots in geometry & optimize:**

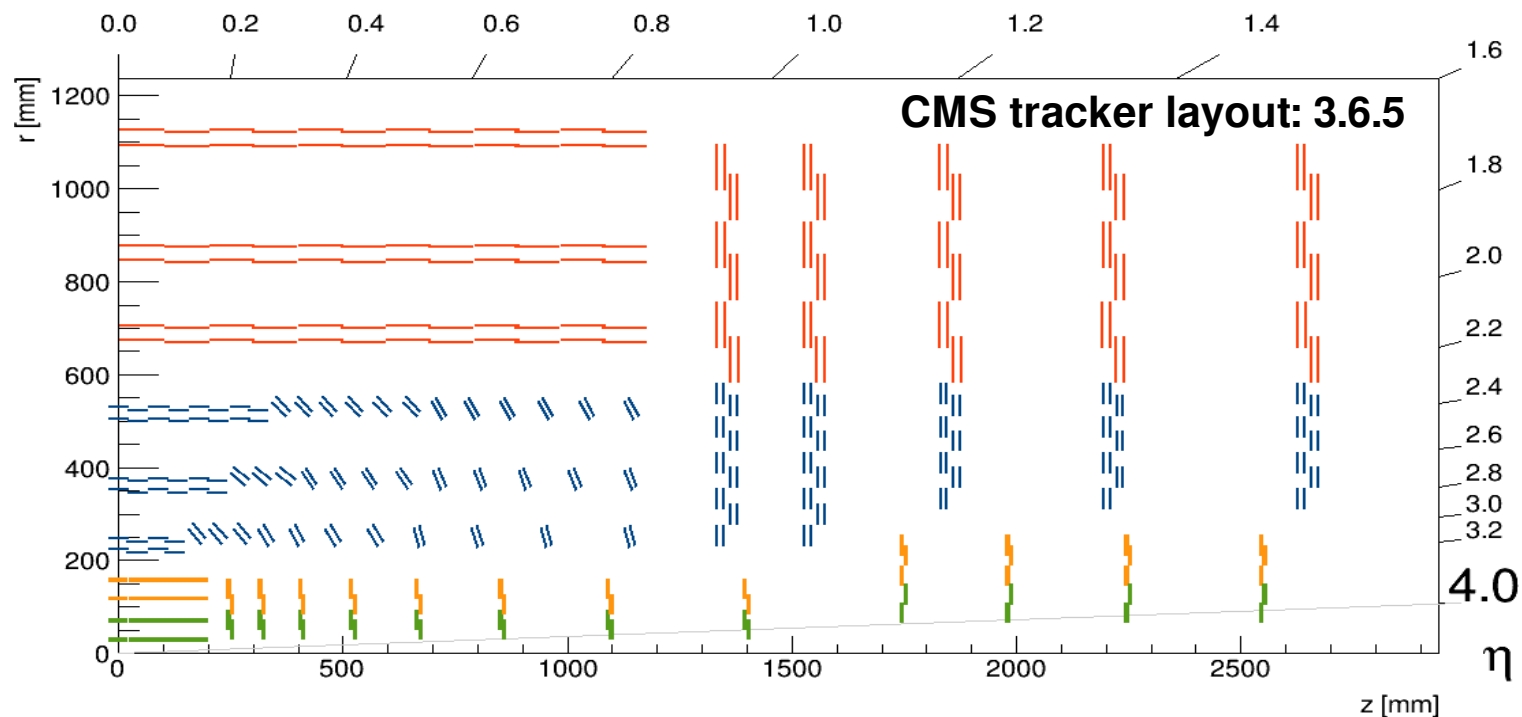
- Module(s) resolution: $\sigma_{r\phi}$, σ_z
- Module(s) tilt (min. material budget) & layer-to-layer distance → limit Multiple scattering effect

Interpretation of tkLayout PR Results?

- **Natural question:** How results from such a technique relates to **real tracker pattern recognition capabilities?** Is there a way to “**evaluate**” that & **interpret the results?**
 - **Only by full simulations**, which is **NOT POSSIBLE** at the moment for FCC-hh tracker, **but...**

Interpretation of tkLayout PR Results?

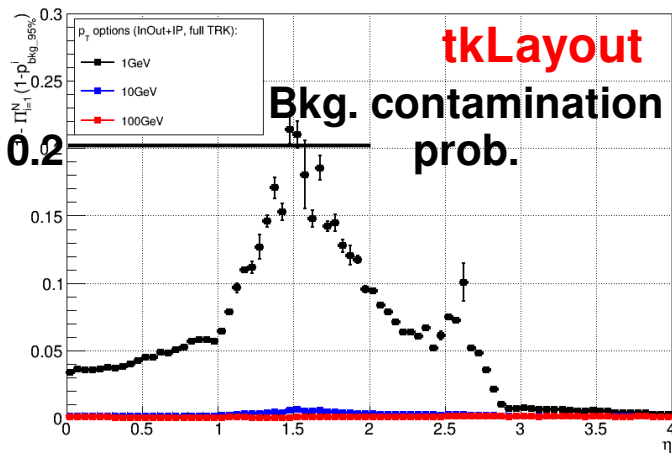
- **Natural question:** How results from such a technique relates to **real tracker pattern recognition capabilities?** Is there a way to “**evaluate**” that & **interpret the results?**
 - **Only by full simulations**, which is **NOT POSSIBLE** at the moment for FCC-hh tracker, **but...**
 - **We may apply the same technique to CMS Phase 2 upgrade tracker layout & “qualitatively” compare with CMSSW full simulation tracking performance** (see results by **E. Brondolin** for CMS collab.: **CMS DP-2017/010**)



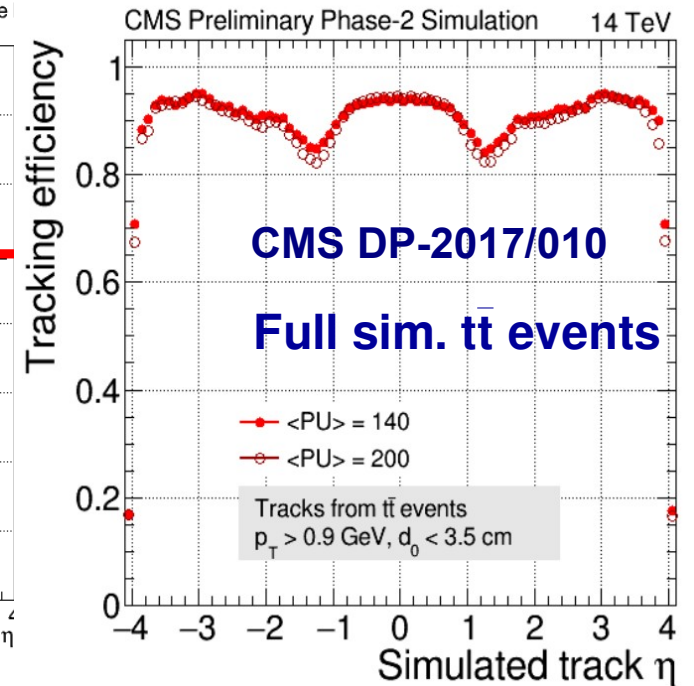
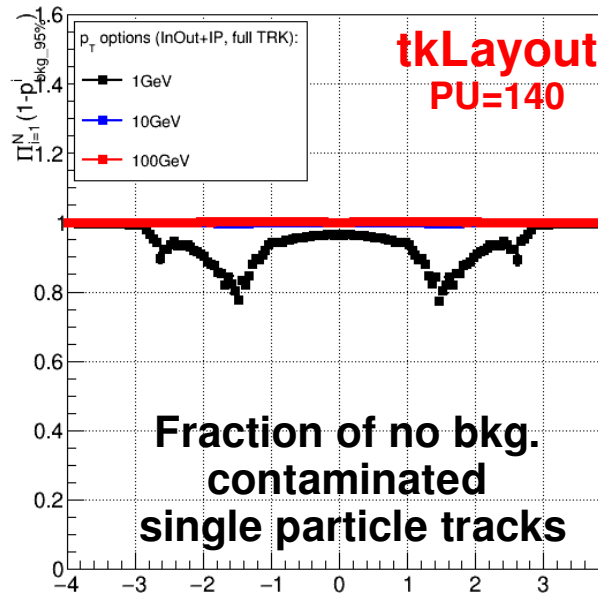
Interpretation of tkLayout PR Results?

→ Qualitative comparison of single particle study (tkLayout) versus full sim. $t\bar{t}$ events study (CMS DP-2017/010) to cross-check, whether the technique “sees” the same weak spots in geometry layout → **Follow the shape of tracking efficiency only!**

In-Out: Bkg contamination prob. in 95% area of 2D error ellipse accumulated across N layers



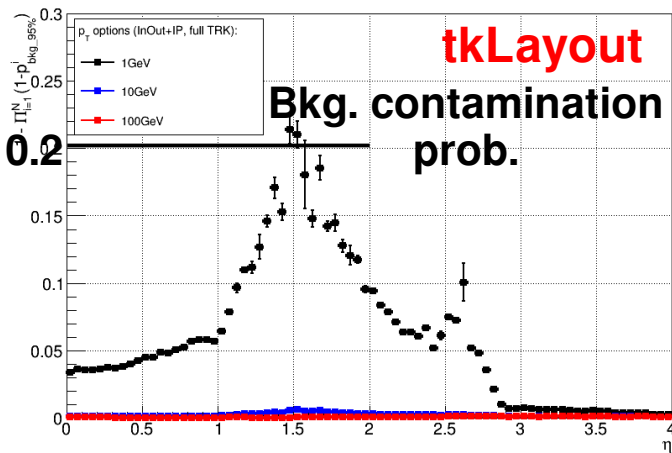
In-Out, PU=140: No bkg contamination prob. (@ 95% confidence)



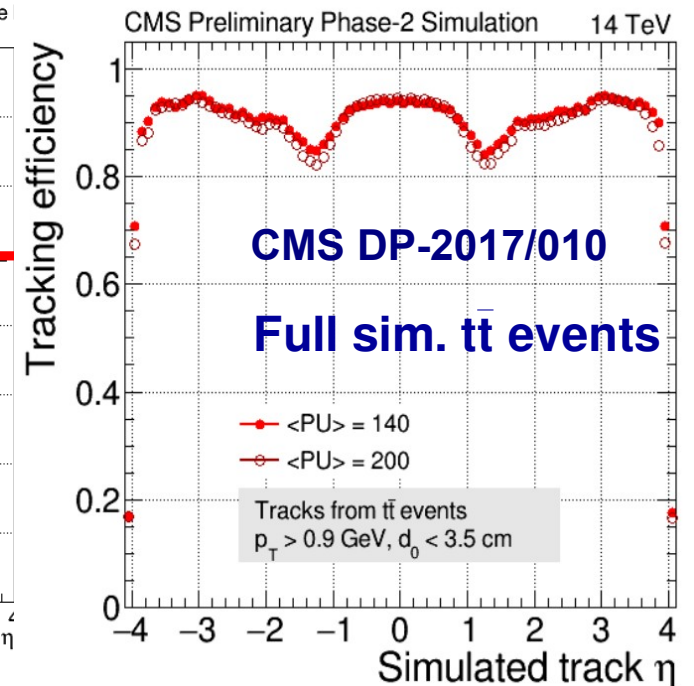
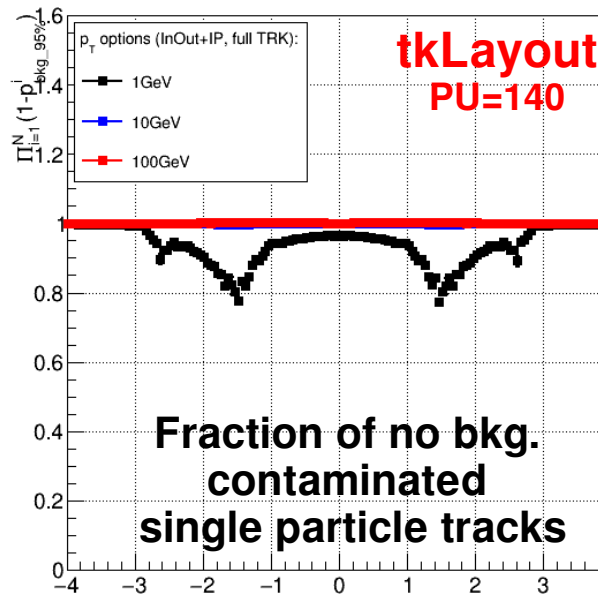
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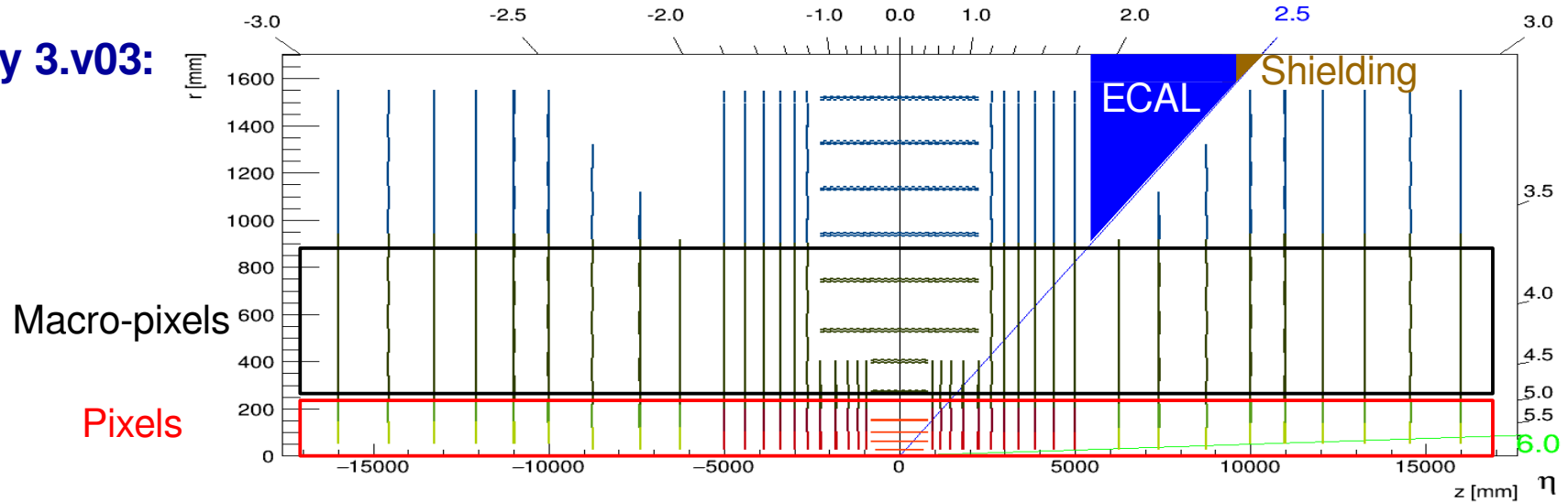


• Conclusion:

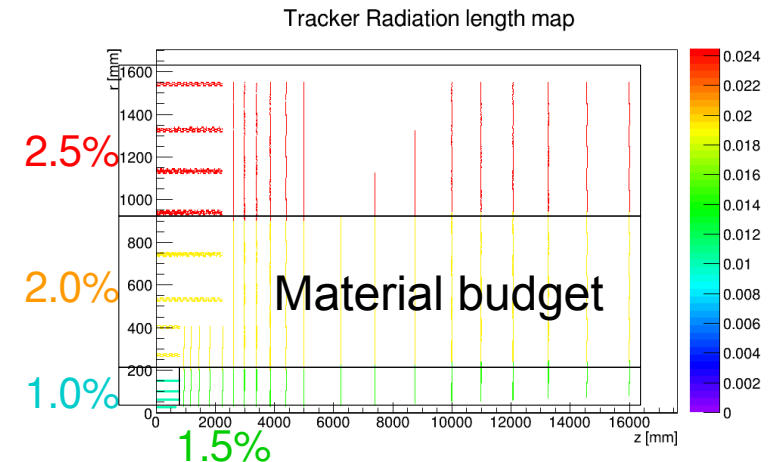
- The method provides first quick insight into layout pattern recognition capabilities, **addressing qualitatively the same layout weak “spots” as full simulation analysis!**
- In order to keep similar performance @ **PU=1000**, let's set the **bkg. prob. contamination @ ~0.2** and drive the layout optimization by that limit! **Cross-check by full. sim. in future necessary!!!**

Non-tilted Layout & Pattern Recognition

- **Geometry 3.v03:**



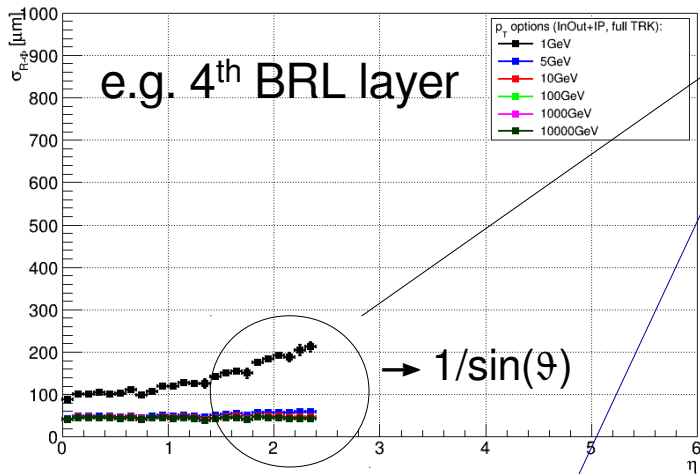
- **Pixels (pitch):** $25 \times 50 \mu\text{m}^2$ (1-4th BRL layers, EC R1), $100/3 \times 100 \mu\text{m}^2$ (R2), $100/3 \times 400 \mu\text{m}^2$ (R3,R4)
- **Macro-pixels (pitch):** $100/3 \times 400 \mu\text{m}^2$
- **Strips (pitch):** $100/3 \mu\text{m} \times 50 \text{mm}$ (BRL), $100/3 \mu\text{m} \times 10 \text{mm}$ (EC)



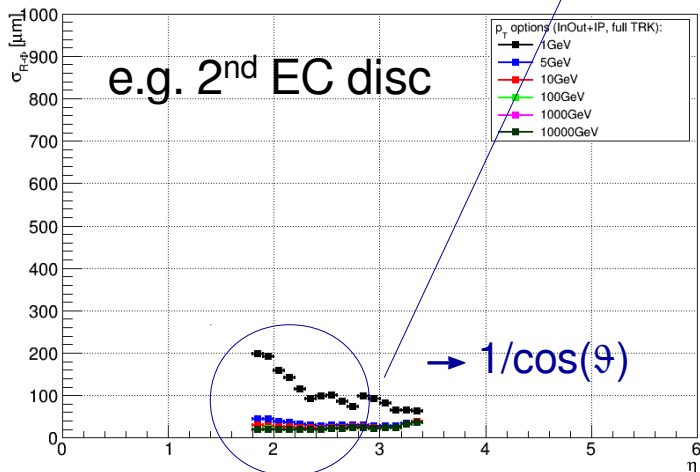
R- Φ : Understanding Pattern Recognition

- Recapitulation of propagator in R- Φ (illustration of typical examples):

Inner_BRL_0_L_4 In-Out approach: an extrapolated $\sigma_{R,\Phi}$ from previous layers/discs



Inner_ECAP_D_2 In-Out approach: an extrapolated $\sigma_{R,\Phi}$ from previous layers/discs



BRL: Why propagation **degrades** with higher η ?

EC: Why propagation **improves** with higher η ?

- σ_d depends on radial distance Δr only \rightarrow **const. effect**, but...
- Multiple scattering** depends on **material & module tilt α** !
 - $\rightarrow \alpha = 0$ for BRL
 - $\rightarrow \alpha = \pi/2$ for EC

$$\sigma_{MS}^2 \approx \langle \vartheta_{pT}^2 \rangle \frac{d/X_0}{\sin(\vartheta + \alpha)} f_L$$

$$\langle \vartheta_{pT}^2 \rangle = \left(\frac{13.6 \text{ MeV}}{\beta p_T c} \right)^2 \left(1 + 0.038 \ln \frac{d/X_0}{\sin(\vartheta + \alpha)} \right)^2$$

$$f_L = \left(\frac{\Delta R}{1} \right)^2 \text{ proj. in } R\Phi$$

- EC** modules \rightarrow res. in R- Φ given by combination of R & Φ :

$$\sigma_{R\Phi} = \sqrt{\sigma_{R\Phi_{loc}}^2 + (A/\sqrt{1-A^2} \sin \alpha)^2 \sigma_{Z_{loc}}^2}$$

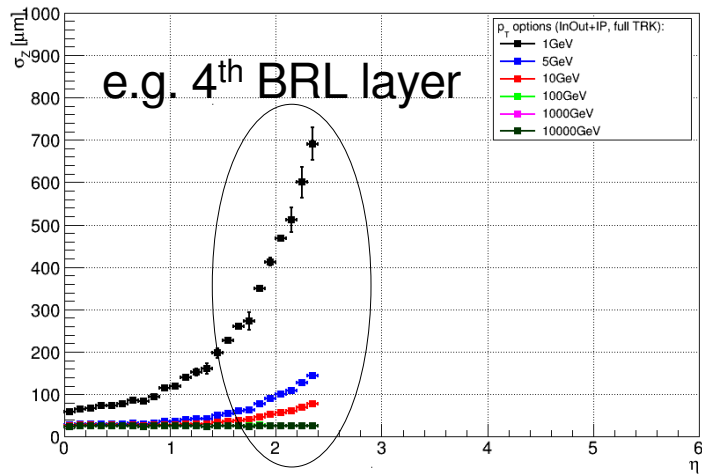
$$A = \Delta r / 2R$$

Problem:
"long" strips

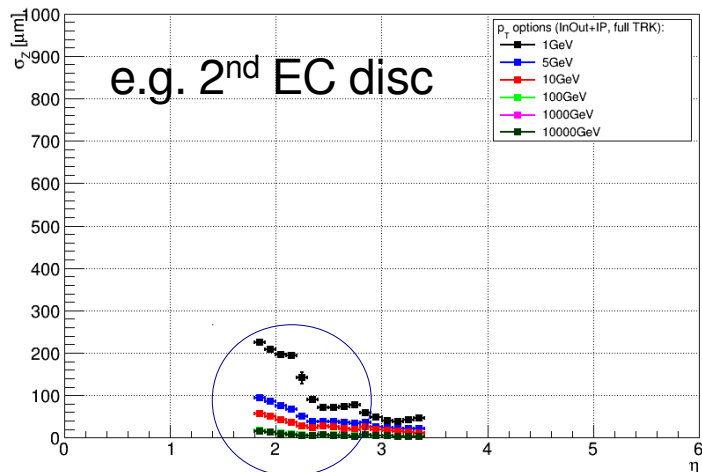
Z: Understanding Pattern Recognition

- Recapitulation of propagator in Z (illustration of typical examples):

Inner_BRL_0_L_4 In-Out approach: an extrapolated σ_z from previous layers/discs



Inner_ECAP_D_2 In-Out approach: an extrapolated σ_z from previous layers/discs



- σ_z depends on radial distance Δr only, but **projection necessary** $\rightarrow \sim 1/\sin^2(\vartheta)$ factor for BRL
- Multiple scattering** depends on **material & module tilt α** !
 - $\rightarrow \alpha = 0$ for BRL
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$$\sigma_{\text{MS}}^2 \approx \langle \vartheta_{p_T}^2 \rangle \frac{d/X_0}{\sin(\vartheta + \alpha)} f_L$$

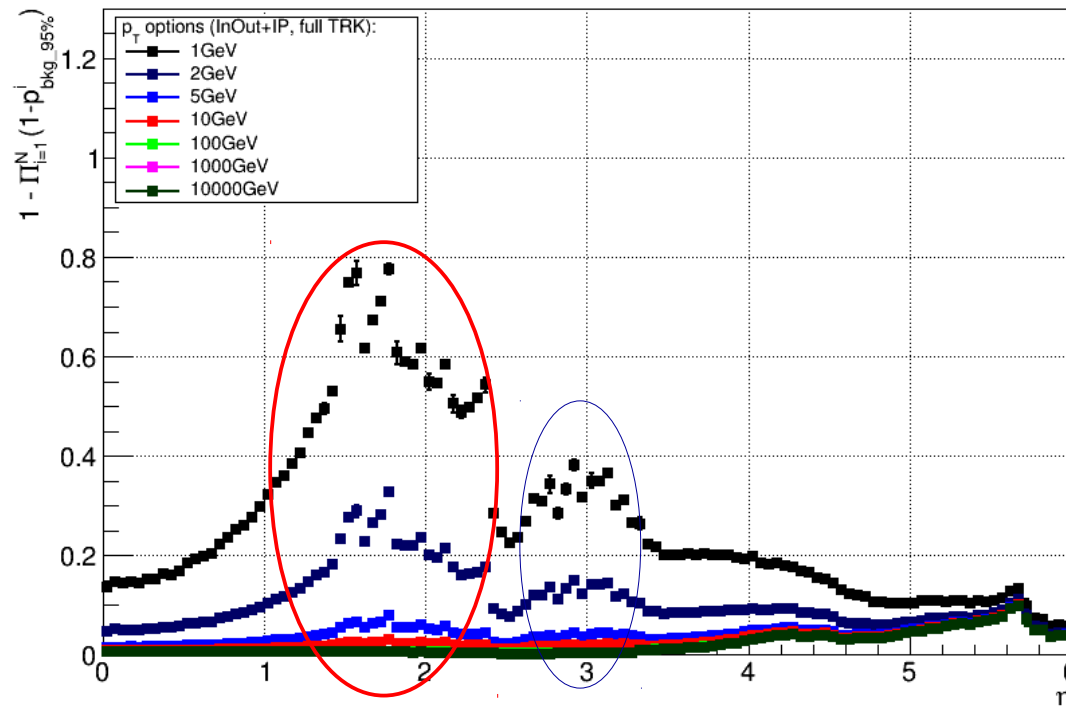
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Non-tilted Layout & Pattern Recognition

- **Geometry 3.v03** → Results on pattern recognition:

In-Out: Bkg contamination prob. in 95% area of 2D error ellipse accumulated across N layers

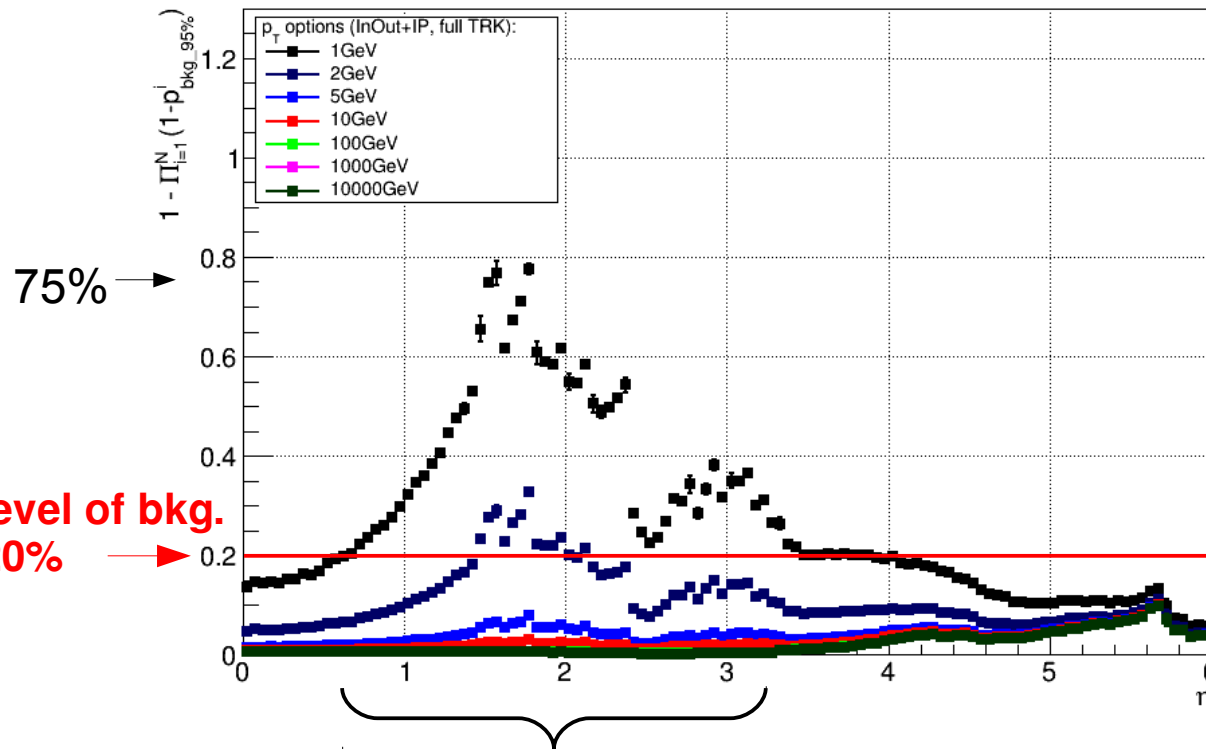


- **EC: Effect of “long” strips along R** → R-φ measurement given by precise φ & radial pos. measur.
- **Effect of barrel modules tilt & material:** Non-tilted modules increase it's material & “projection” effect with increasing eta! (Namely important for BRL & high occupancy region)

Non-tilted Layout & Pattern Recognition

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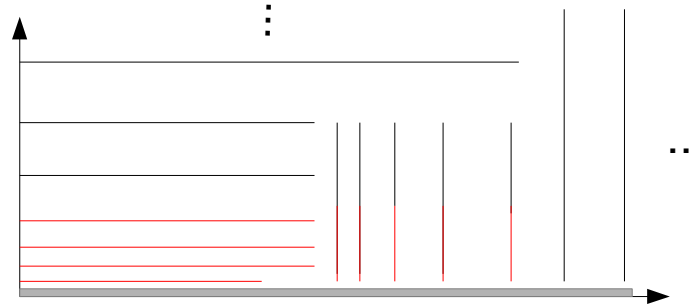
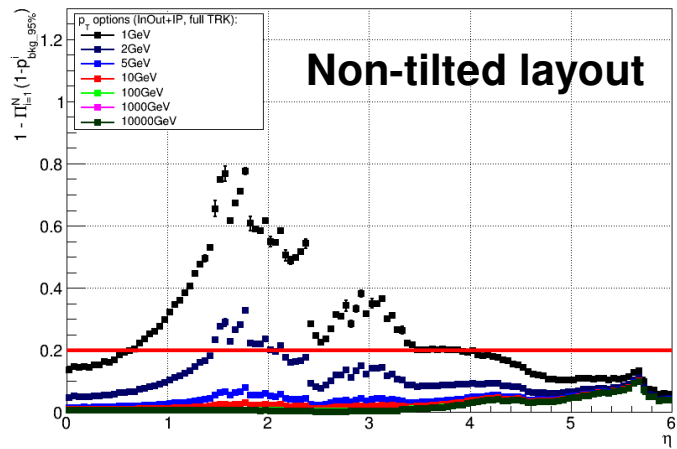
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Critical eta region: 0.5-2.5 (3.5) → transition area between BRL & EC

Non-tilted Layout x Tilted Layout

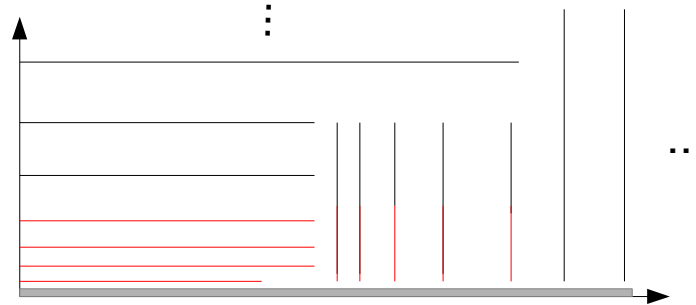
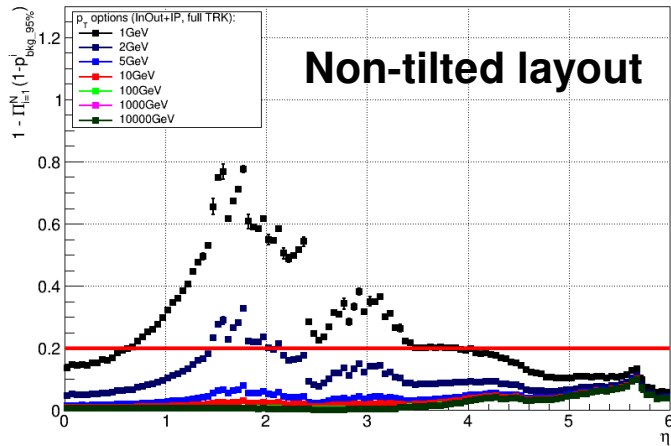
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Solution?

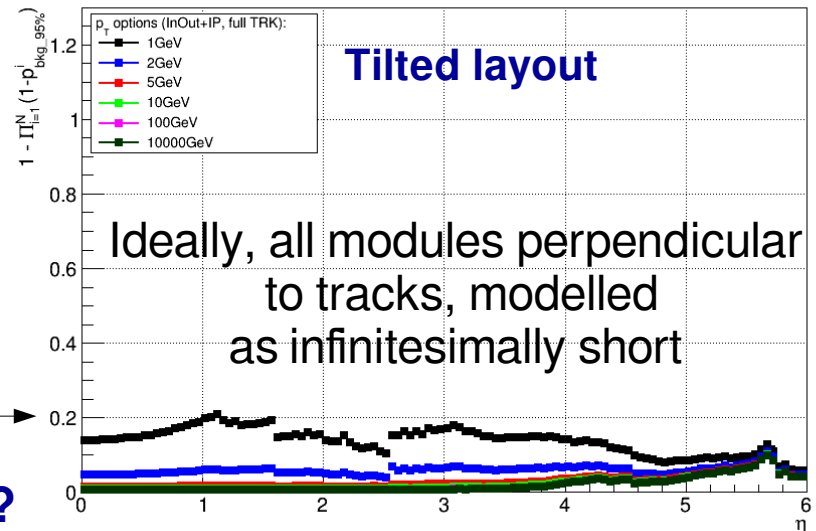
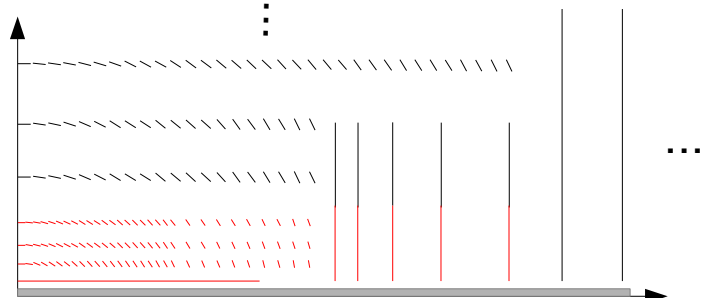
Non-tilted Layout x Tilted Layout

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In-Out: Bkg contamination prob. in 95% area of 2D error ellipse accumulated across N layers

Solution? Go for tilted layout



OK, but how to design tilted layout realistically?

Tilted Layout: Design Principles

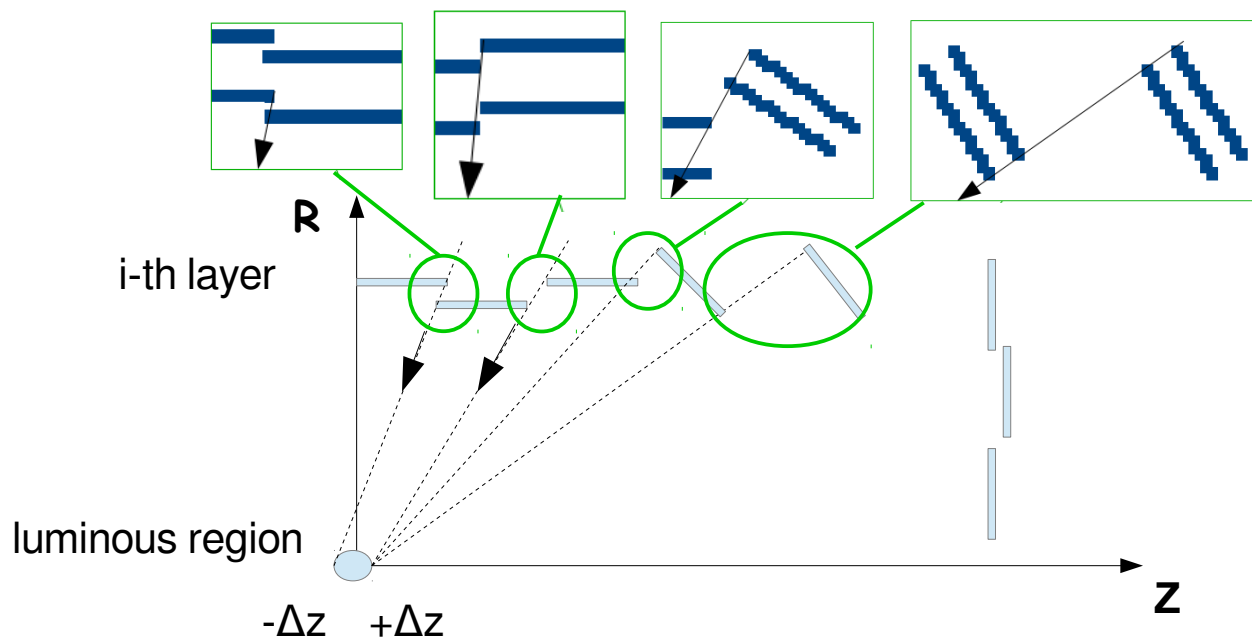
- **Design principles:**

- **Install tilted modules in barrel part only** (no tilting necessary in EC part)
 - Non-tilted (**flat**) part arranged in rods, up-to $\eta \approx 0.5$
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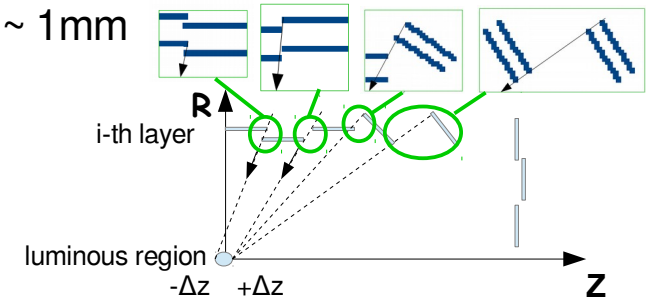
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 - Modules positioned in a way to cover hermetically high energy tracks from the whole luminous region, i.e. $\pm 75\text{mm}$) → defines $z\text{Overlap}$; $r\text{PhiOverlap}$ required $\sim 1\text{mm}$



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- **Last barrel layer kept non-tilted** → **keep max available lever-arm $\sim 1550\text{mm}$!**
 - Module(s) tilting in uppermost layer has no effect on in-out PR + zig-zag structure affects lever-arm

Tilted Layout: Design Principles

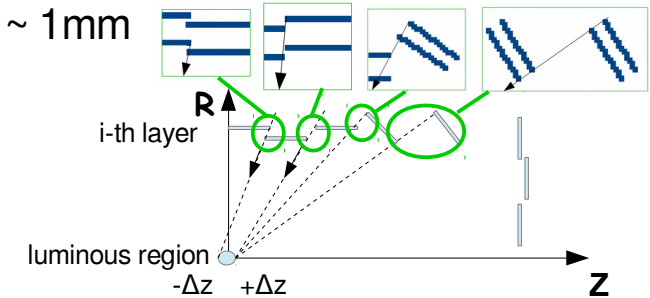
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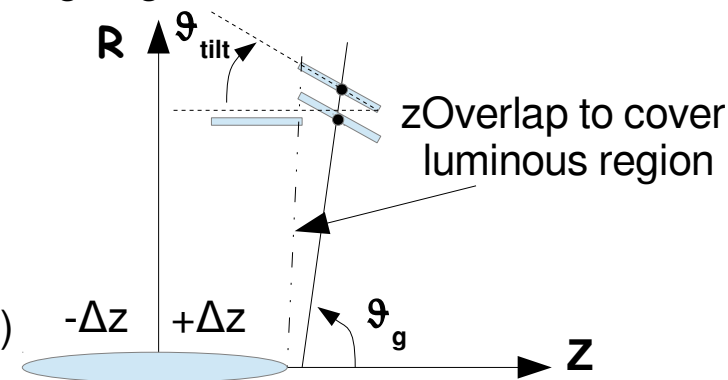
- Module(s) tilting in uppermost layer has no effect on in-out PR + zig-zag structure affects lever-arm

- **Modules tilted geometry:**

- Algorithm kindly provided by CMS Ph2 Tracker group, (special thanks to **G.Hugo & S.Mersi**)

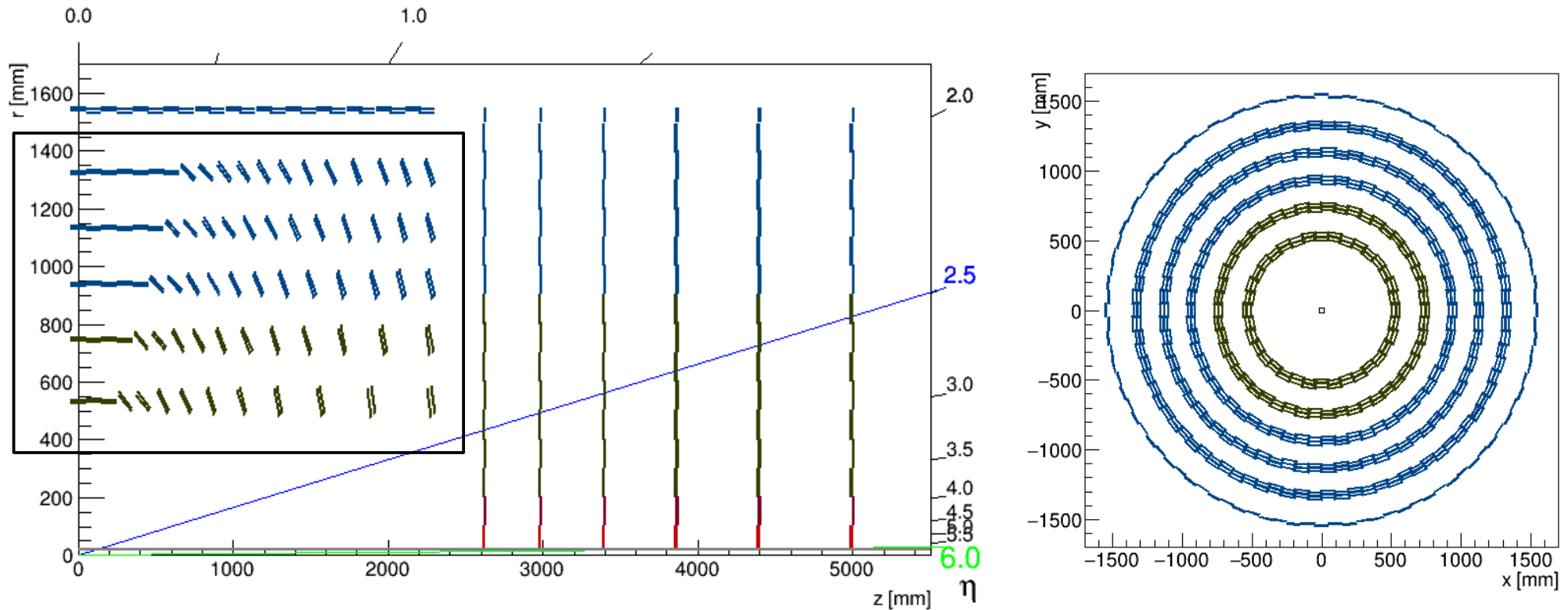
- **Main parameters affecting geometry:** ϑ_{tilt} , ϑ_g , $z\text{Overlap}$

- Same tilt used for a group of 2 rings (higher cls size & practical)



Tilted Geometry: Design Proposal

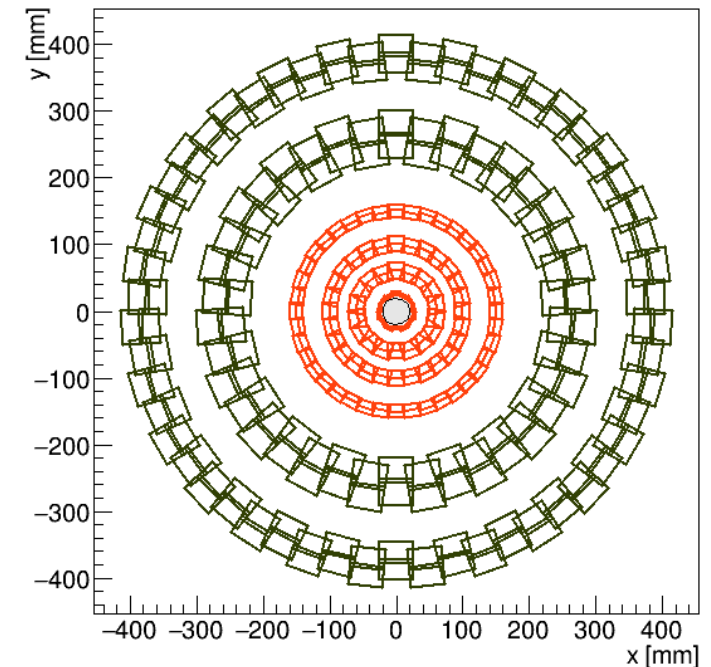
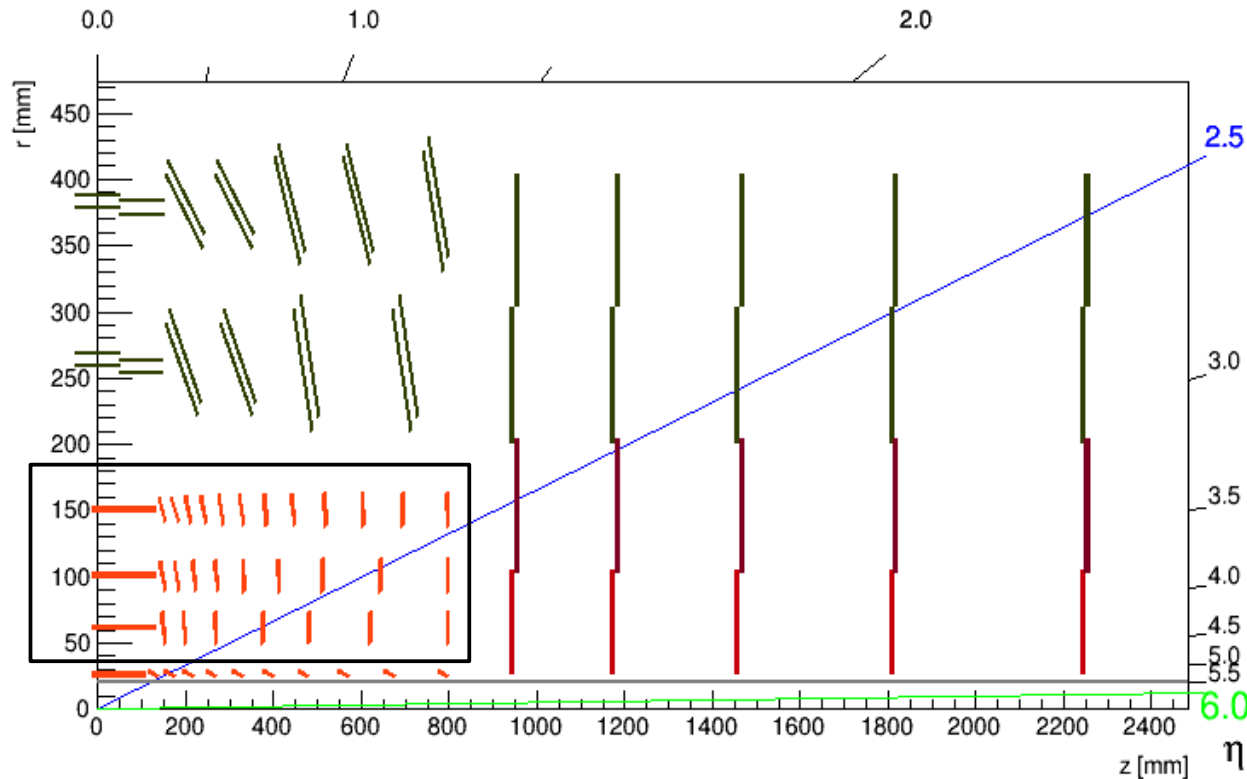
- **Geometry 4.v01 (tilted layout) → outer tracker**



- Drawback of tilted layout versus flat barrel geometry: res. in $R-\Phi$ given by combination of R & Φ → **long Z strips (50mm) not usable (res. ~ 14.4 mm) → Z res. set to 500 μ m (up-to 1mm OK)**
- To achieve 0.2 bkg. contamination level Z res. of EC strips set to 500 μ m too

Tilted Geometry: Design Proposal

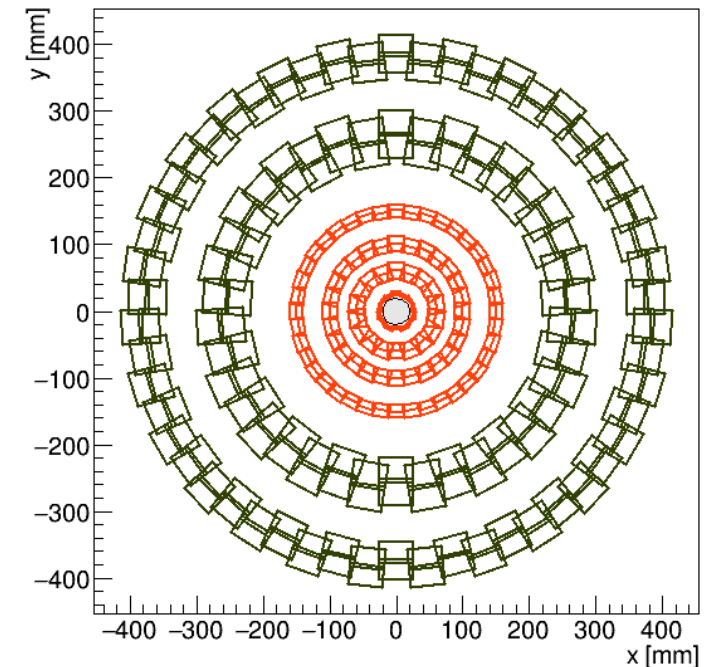
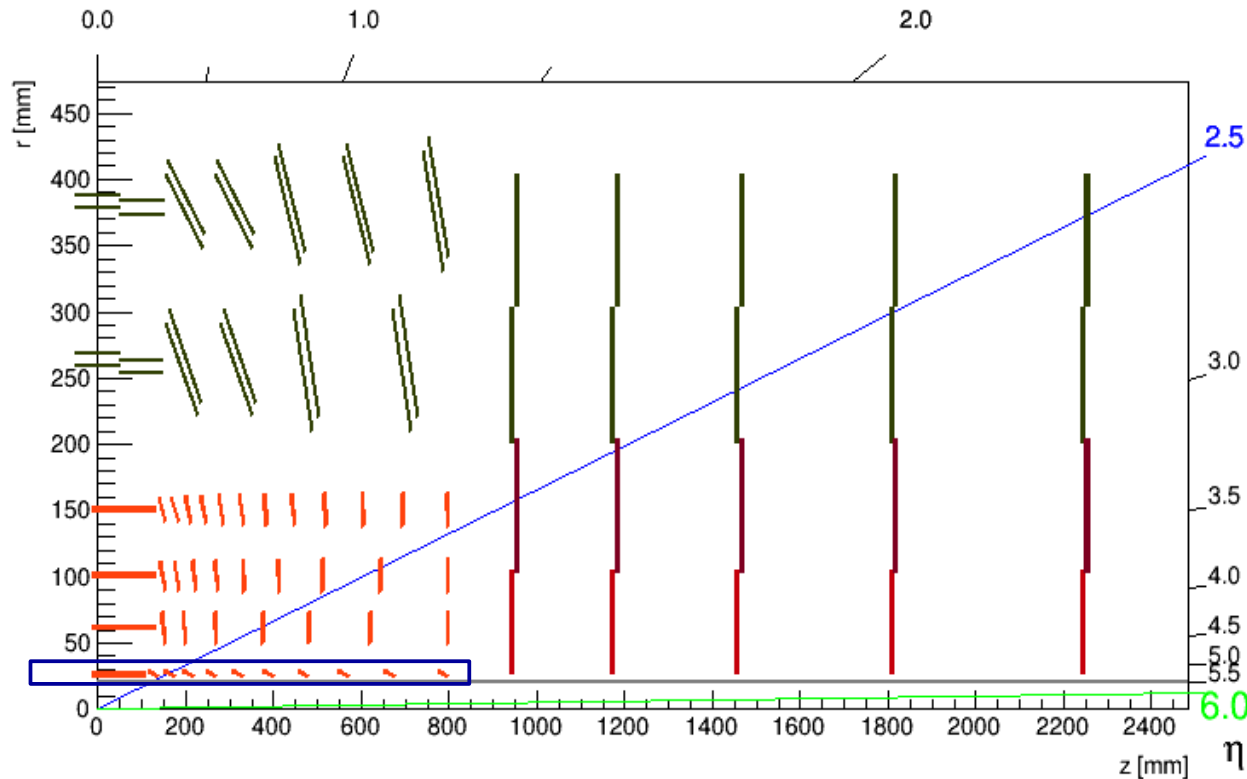
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→ Tilted layout of vertex detector not directly driven by Pattern recognition (used for seeding), **but it improves Z_0 resolution**, visible improvement in correct primary vertex assignment @ high pile-up

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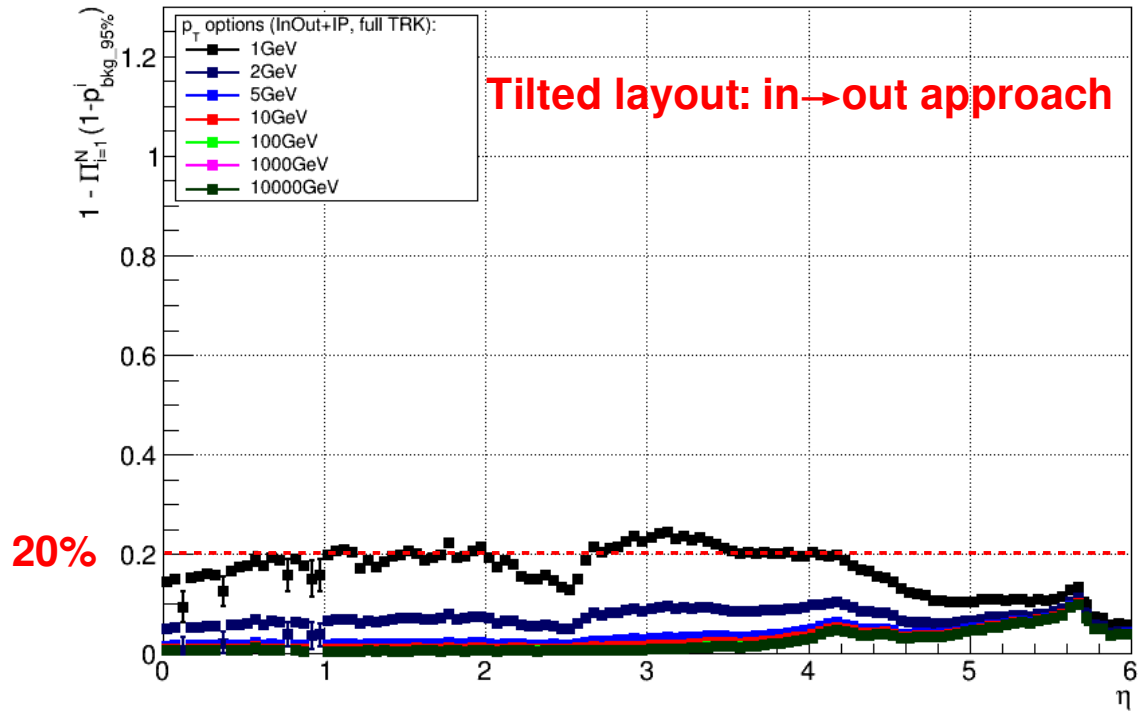
- **Geometry 4.v01 (tilted layout) → inner tracker**



- Tilted layout of vertex detector not directly driven by Pattern recognition (used for seeding), **but it improves Z_0 resolution**, visible improvement in correct primary vertex assignment @ high pile-up
- Tilt angle of first layer is given by compromise between **low material budget & higher radial pos. due to tilt** → set $\vartheta_{\text{tilt}} \approx 10^\circ$

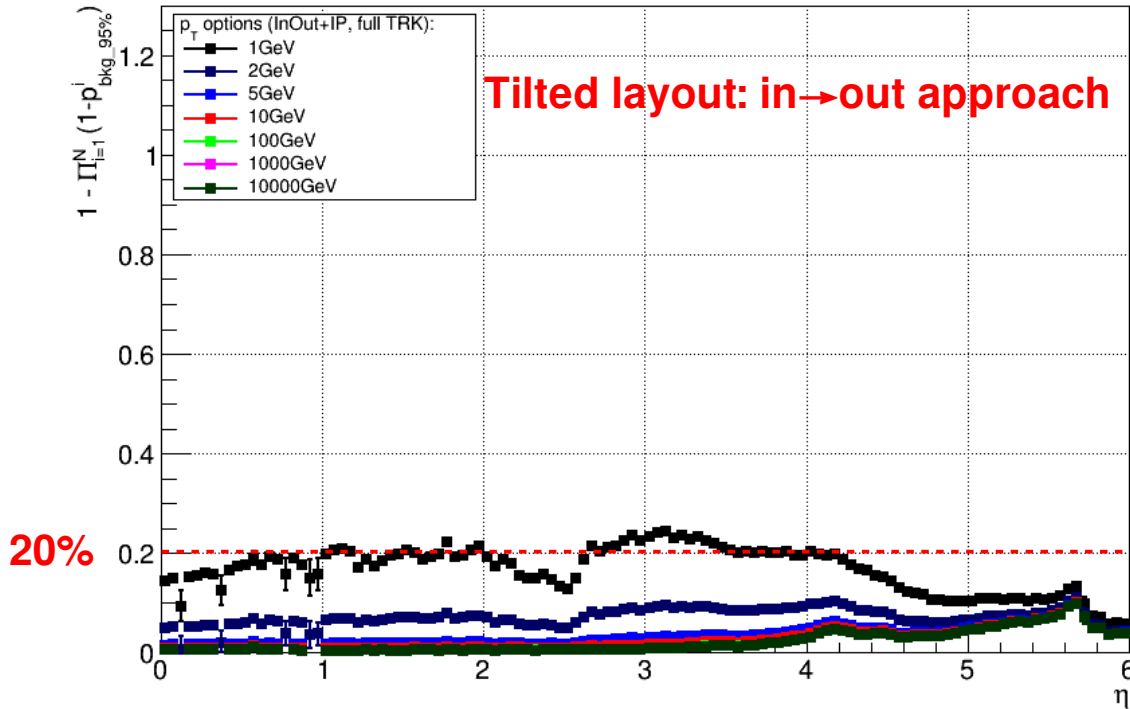
Tilted Layout & Pattern Recognition

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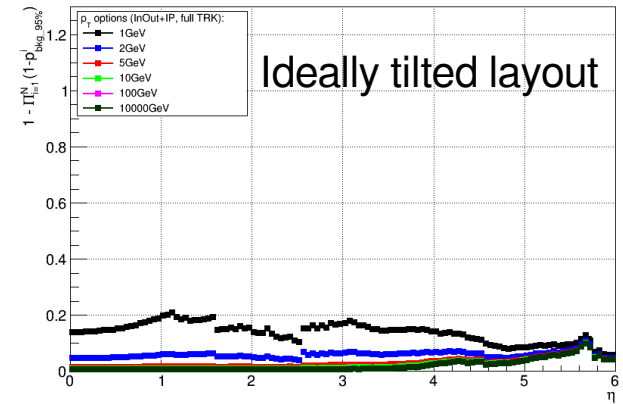


Tilted Layout & Pattern Recognition

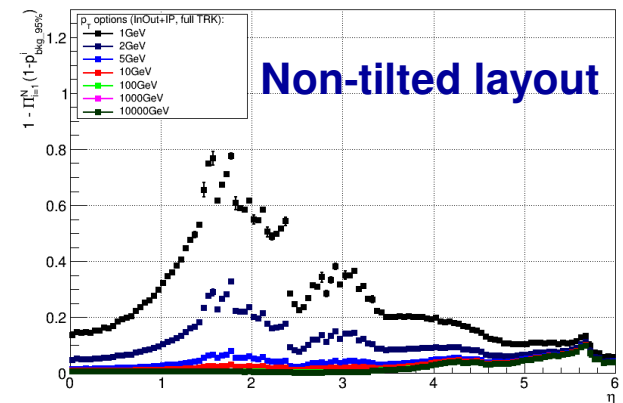
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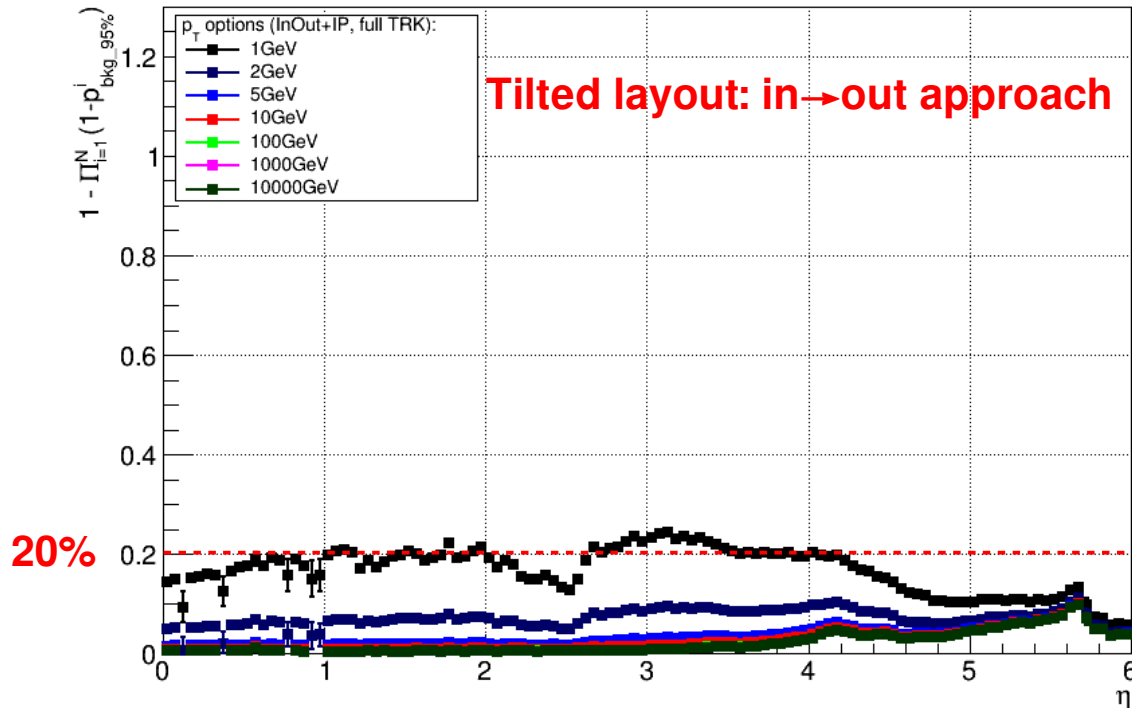


- Conclusion:**

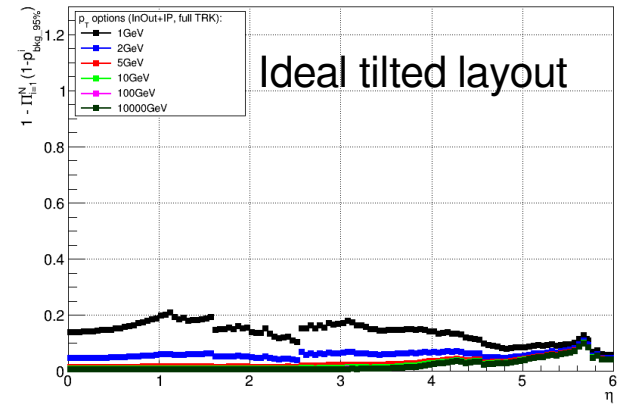
→ Bkg. Contamination level @ 20% for $p_T=1\text{GeV}/c$ (limit driven by CMS Phase 2 upgrade tracker @ PU=140) possibly achievable with tilted geometry @ PU=1000, but...

Tilted Layout & Pattern Recognition

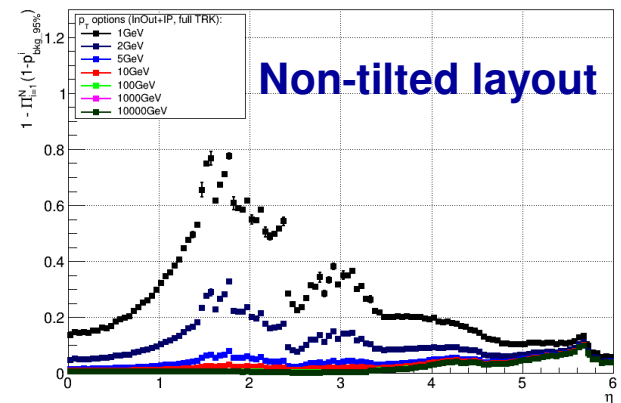
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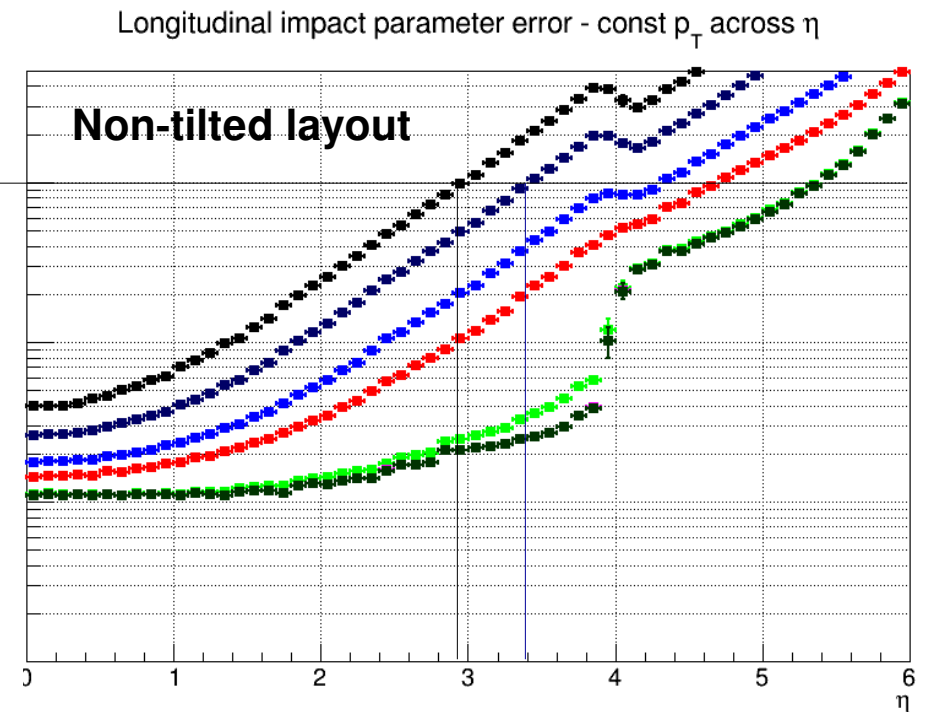
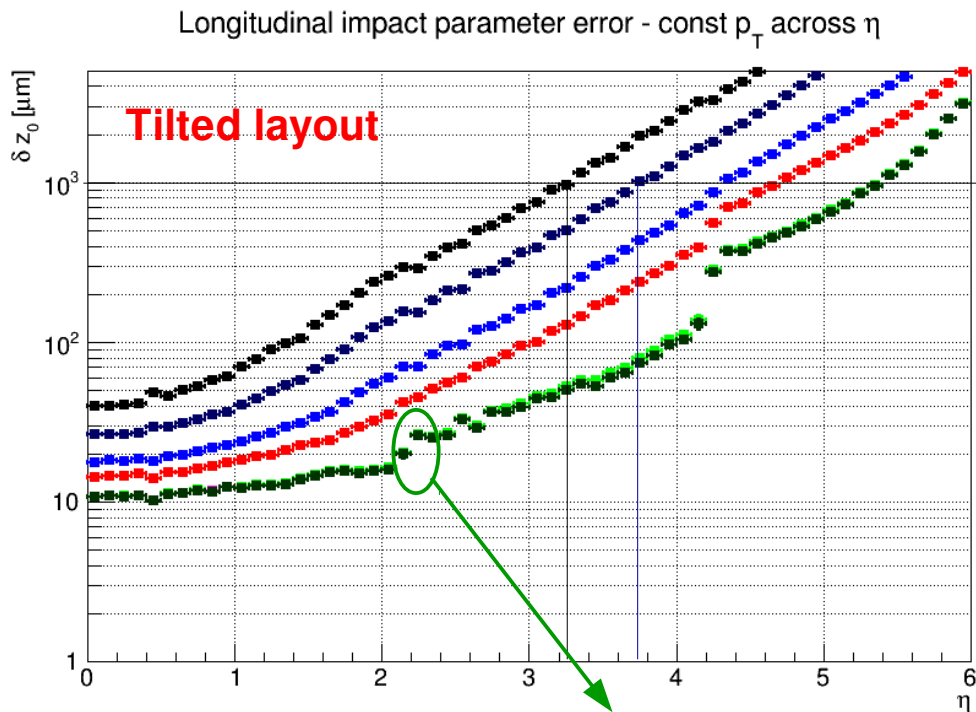


- Conclusion:**

- Bkg. Contamination level @ 20% for $p_T=1\text{GeV}/c$ (limit driven by CMS Phase 2 upgrade tracker @ PU=140) possibly achievable with tilted geometry @ PU=1000, but...
- Up-to now, mat. budget assumed per module → NOT fully realistic for tilted layout, missing services & support structure!

Tilted Layout & Tracking Performance

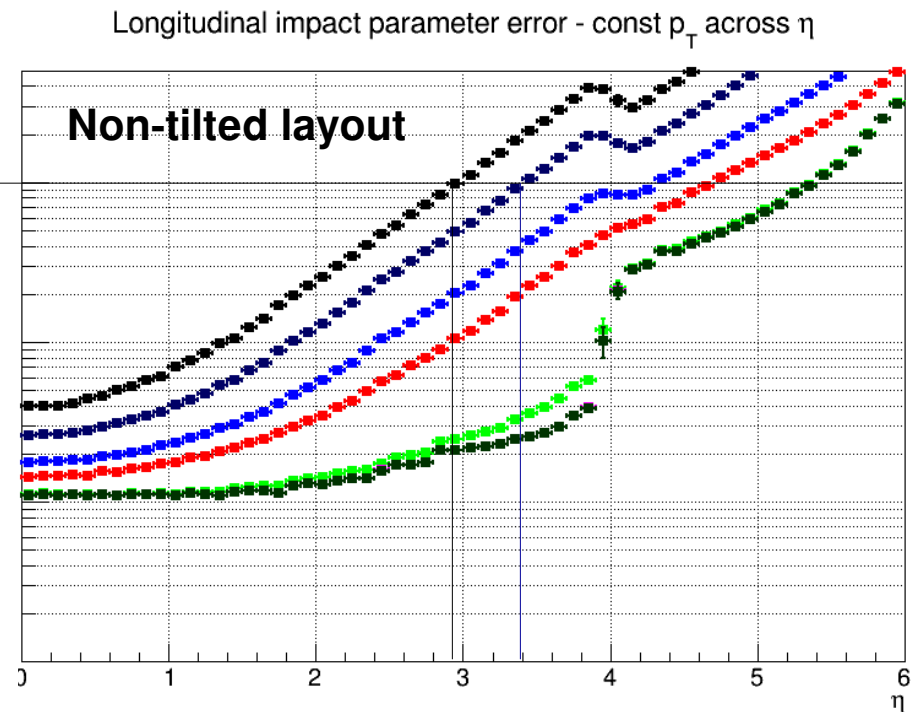
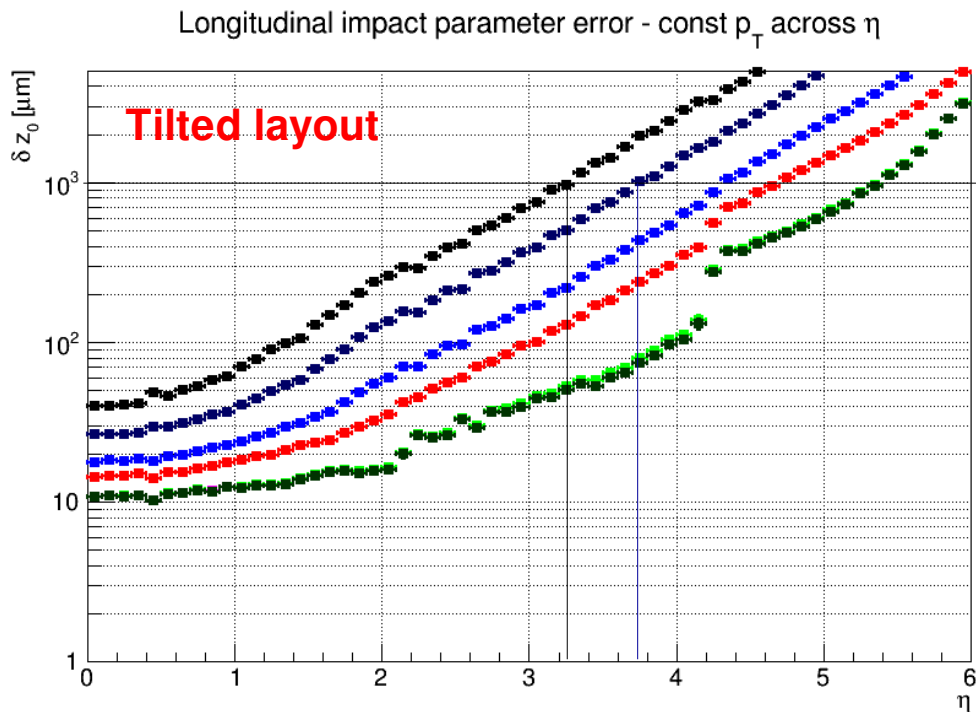
- Resolution of all track parameters remain similar, **except Z0 res.** → **important for primary vertex finding algorithm in high pile-up!**



First layer "tilting" starts @ $\eta \approx 2.2$

Tilted Layout & Tracking Performance

- Resolution of all track parameters remain similar, **except Z0 res.** → **important for primary vertex finding algorithm in high pile-up!**



- Conclusion:** The remaining limiting factor for tilted layout is material budget of beam-pipe! Solution? Combine measurement with timing information?

Summary & Outlook

- **Presented first tracker layout (tilted geometry) “optimized” by pattern recognition capabilities in high pile-up environment ~ 1000**
 - modules tilt introduced in **critical eta region: 0.5-3.0 (transition area between BRL & EC)**
 - **uppermost BRL layer designed untilted** to keep max available lever-arm @ 1550mm
 - **first BRL vertex layer tilt optimized to $\vartheta_{\text{tilt}} \simeq 10^\circ$** to minimize mat. budget, but improve Z0 res

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- **An optimized tilted layout provides an overall improvement by factor of 3-4 in track finding purity & helps improving Z0 res.** (important for primary vertex finding in high PU)

Summary & Outlook

- **Presented first tracker layout (tilted geometry) “optimized” by pattern recognition capabilities in high pile-up environment ~ 1000**
 - modules tilt introduced in critical eta region: 0.5-3.0 (transition area between BRL & EC)
 - uppermost BRL layer designed untilted to keep max available lever-arm @ 1500mm
 - first BRL vertex layer tilt optimized to $\vartheta_{\text{tilt}} \approx 10^\circ$ to minimize mat. budget, but improve Z0 res.
- **An optimized tilted layout provides an overall improvement by factor of 3-4 in track finding purity & helps improving Z0 res.** (important for primary vertex finding in high PU)
- **Key features & limits:**
 - + **An analytical solution to estimate the weak “spots” in geom. layout in a view of pattern recognition** (Algorithms fully implemented in tkLayout SW)
 - + **Implemented algorithms to design tracker with tilted layout in tkLayout SW** (G. Hugo & S. Mersi, CMS Ph2 upgrade tracker group)
 - **Current tracker design with tilted layout still lacks true services & supports, which need to be implemented!** On the other hand, tilted layout is very “transparent” for services, so one may achieve better performance versus material budget compared to “classical” design