

# Tracking in the Triggering System

the use of Associative Memory  
from CDF to the HL-LHC

*Luciano Ristori - October 19, 2016*

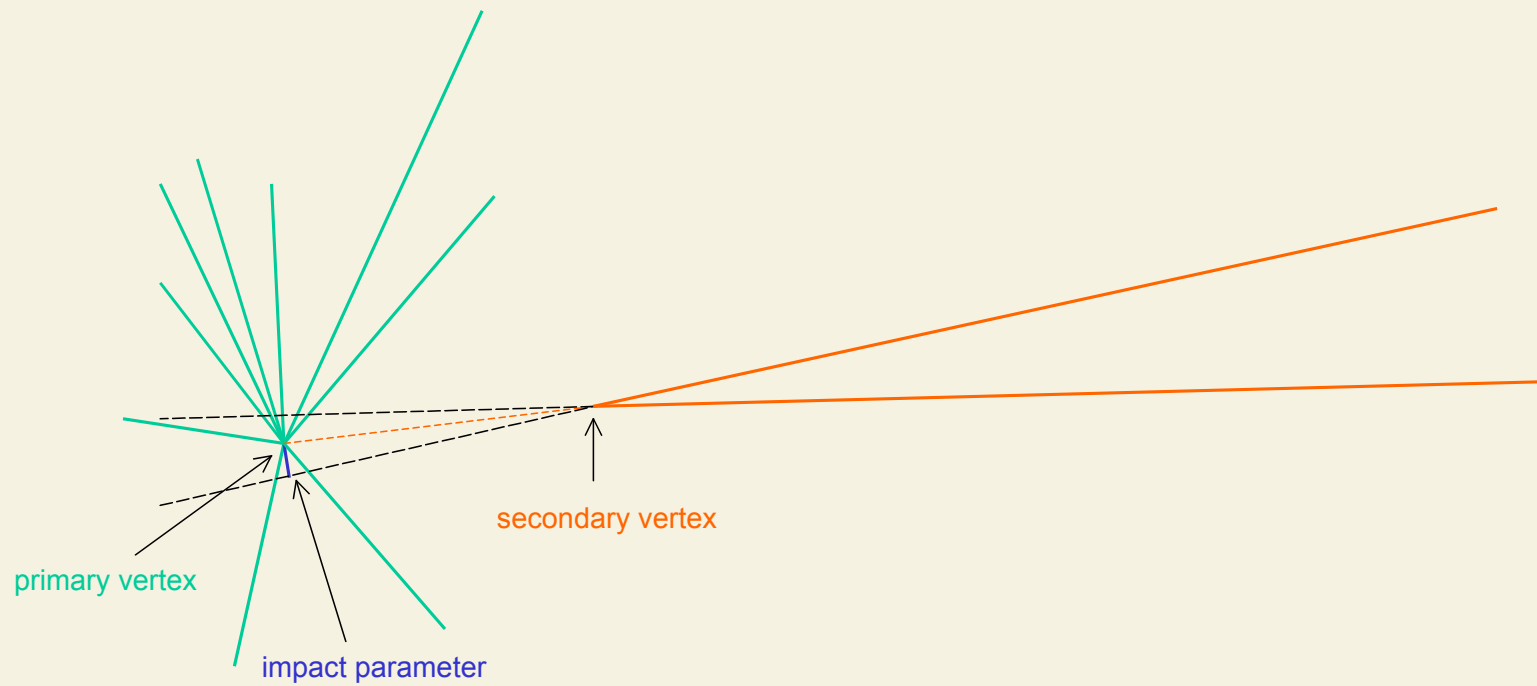
# The Associative Memory

- The idea
- How does it work?
- A little history
- Recent optimizations
- Possible future developments

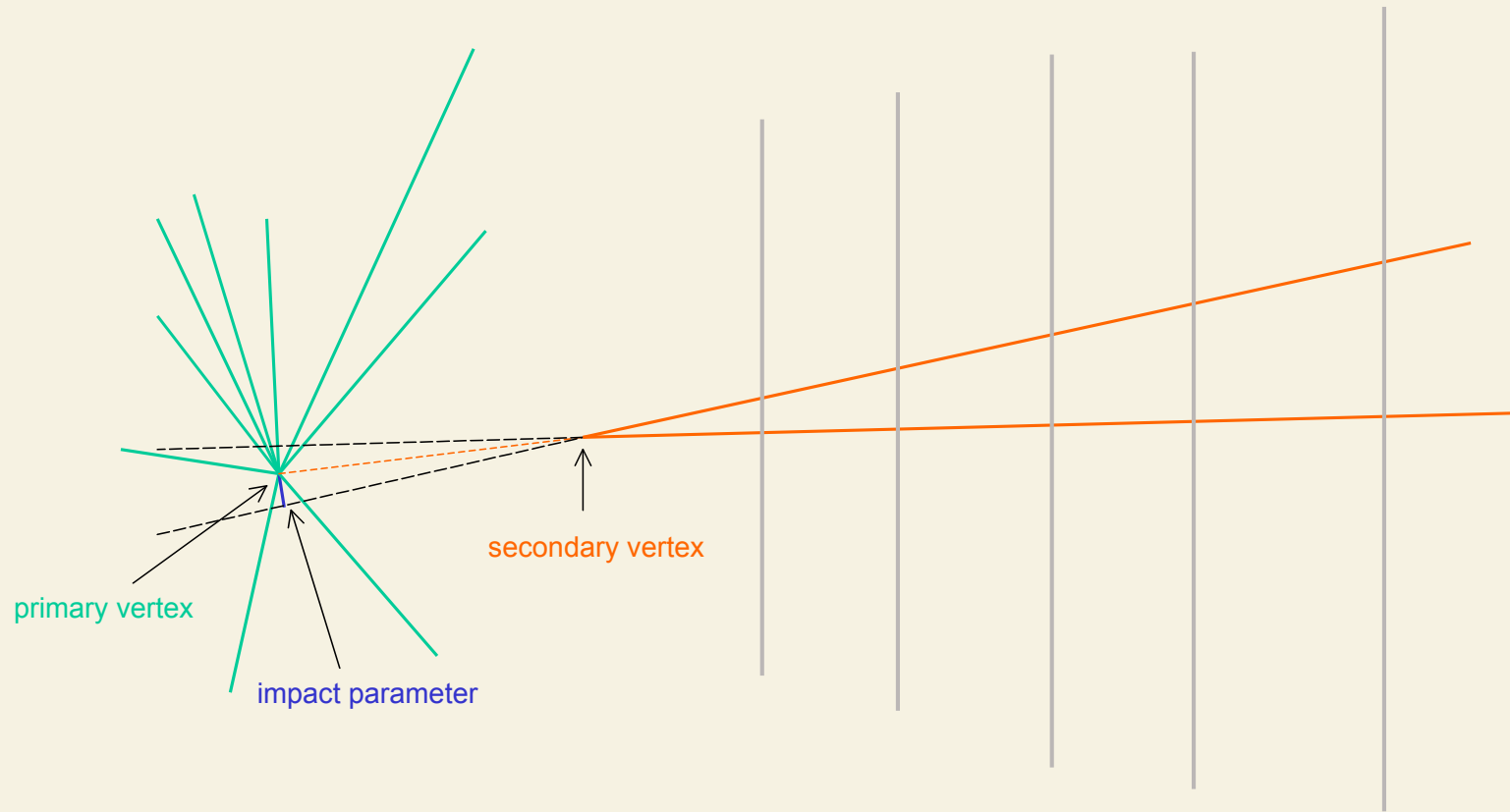


# The idea

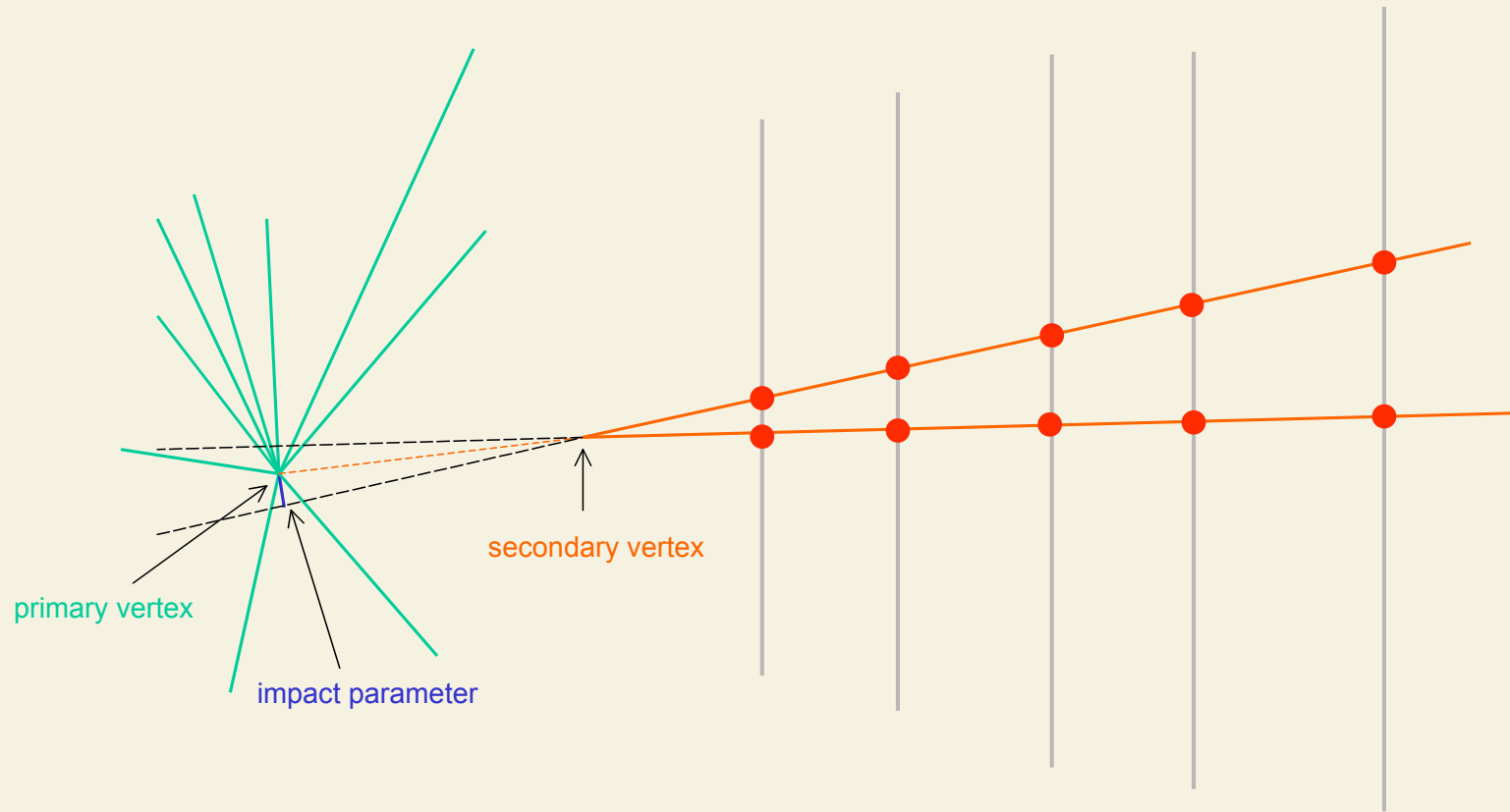
# *pattern recognition*



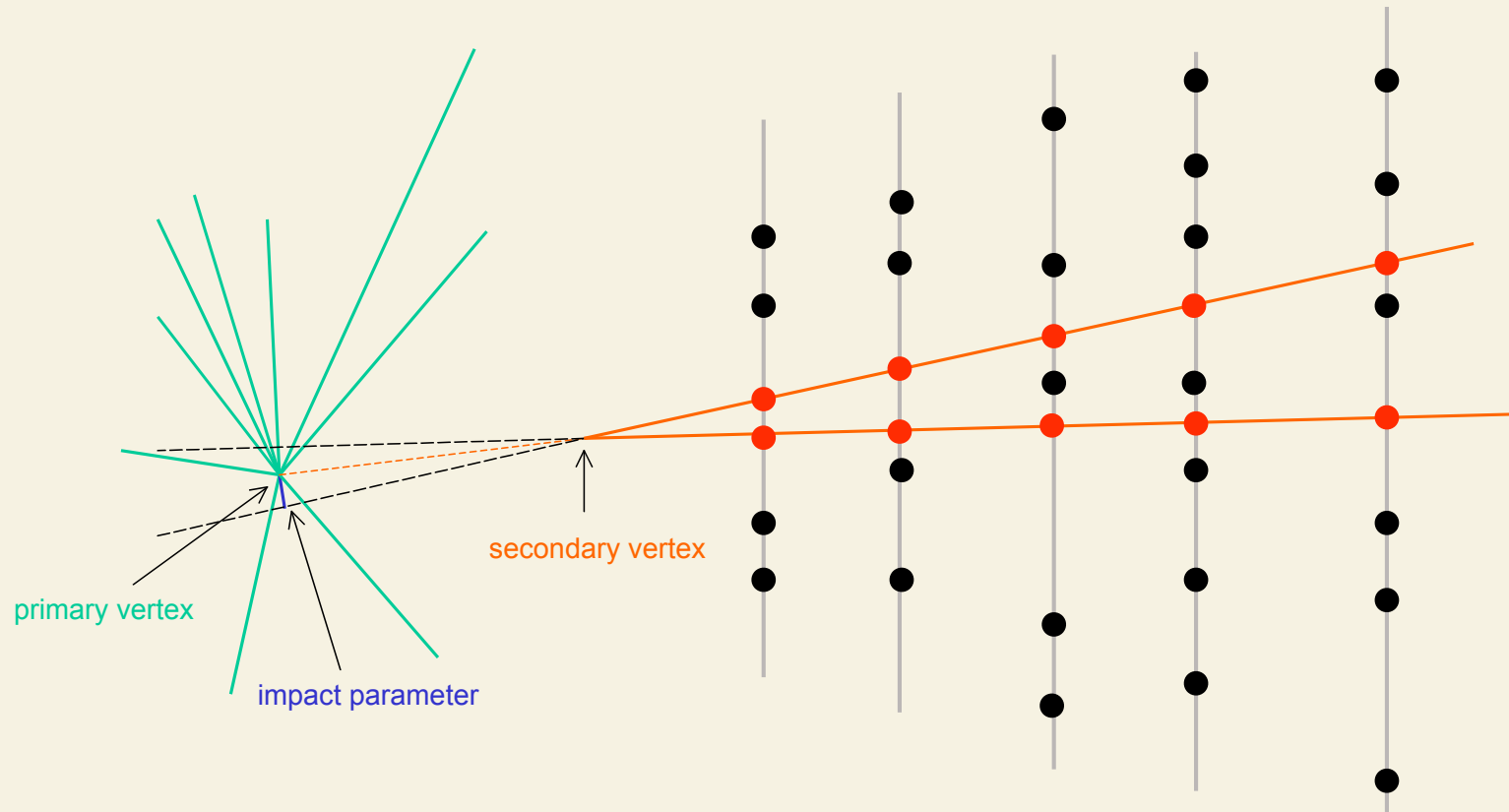
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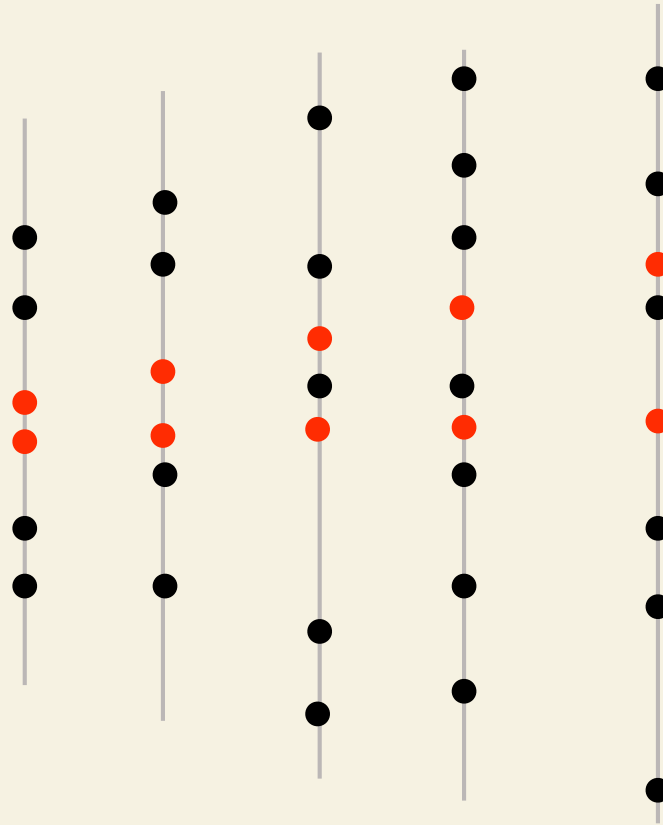
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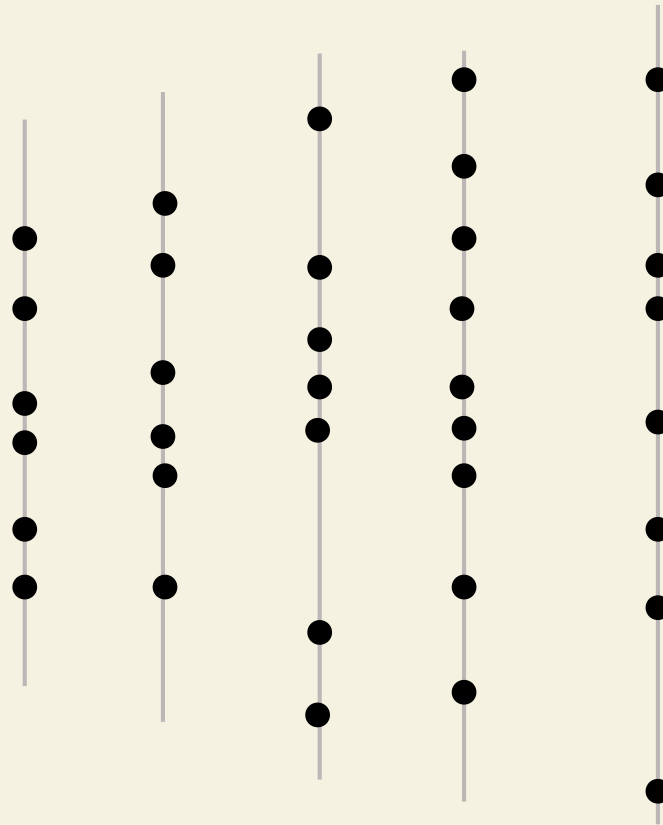
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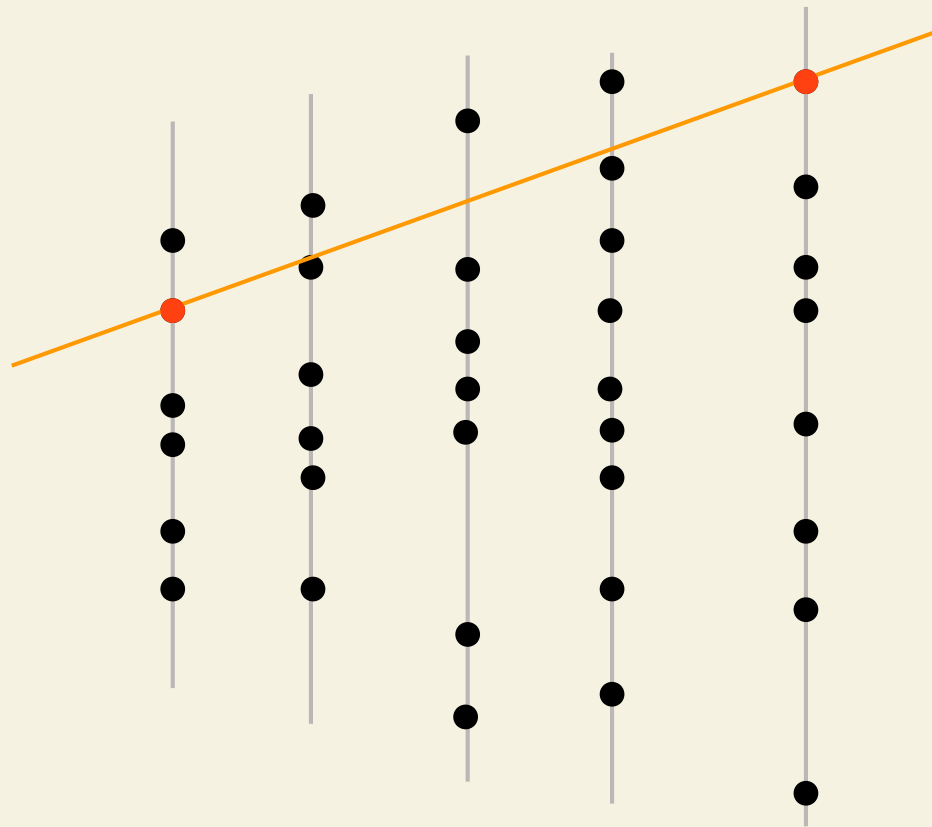
# *pattern recognition*



looking for the right combination of hits

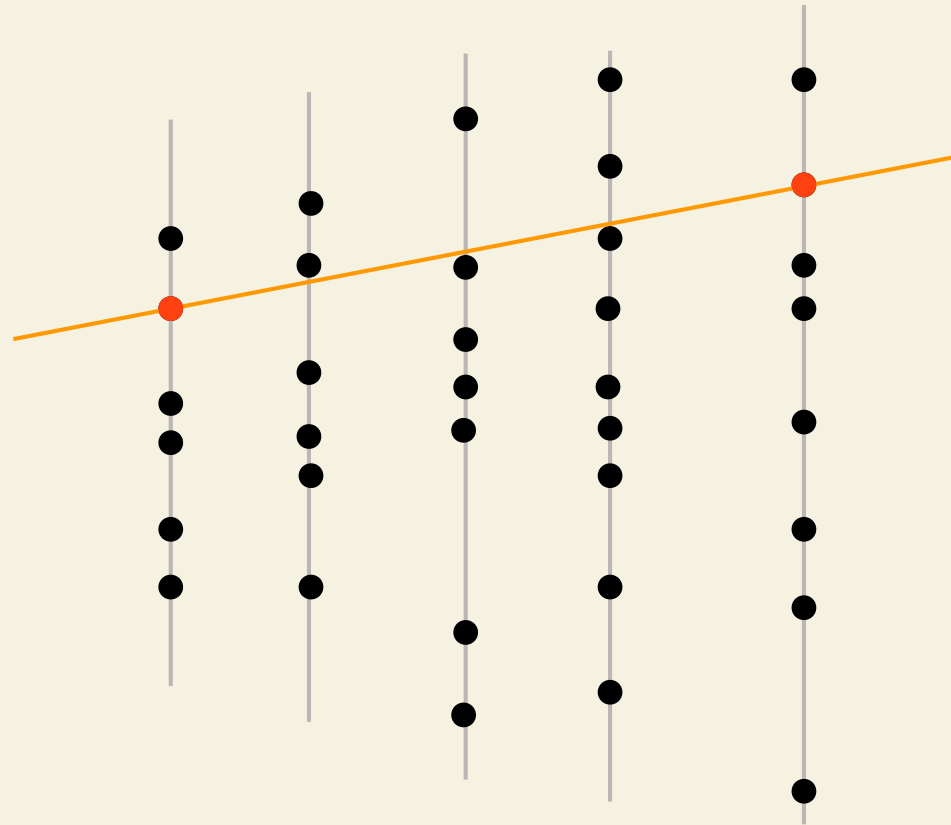


# looking for the right combination of hits

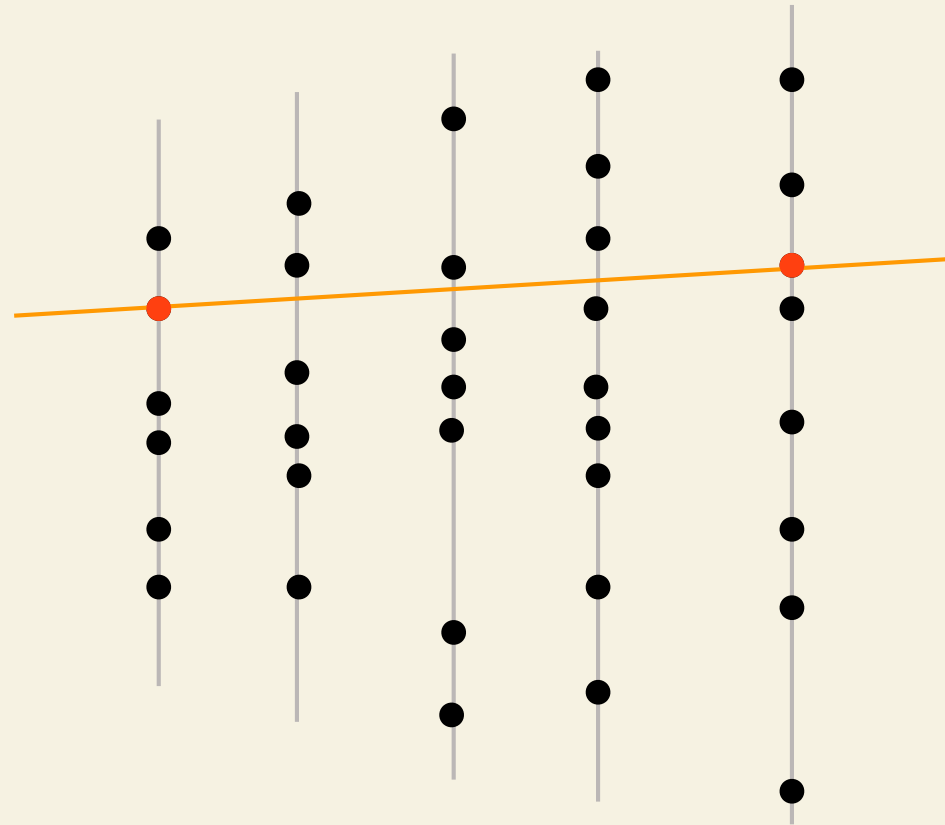




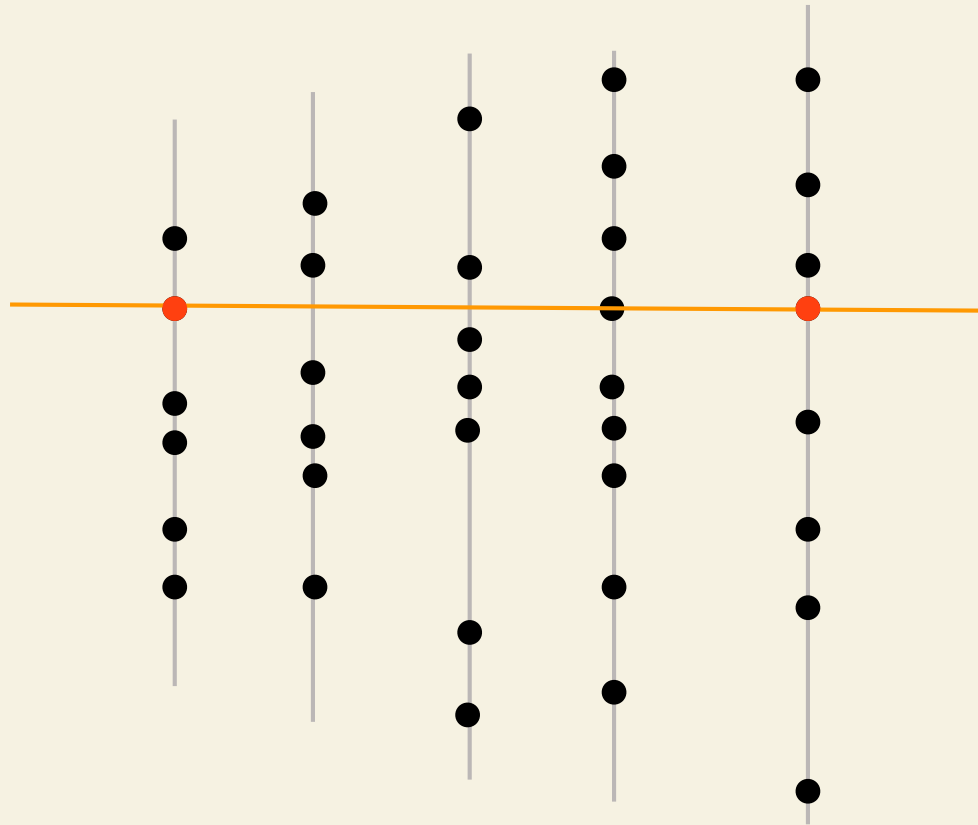
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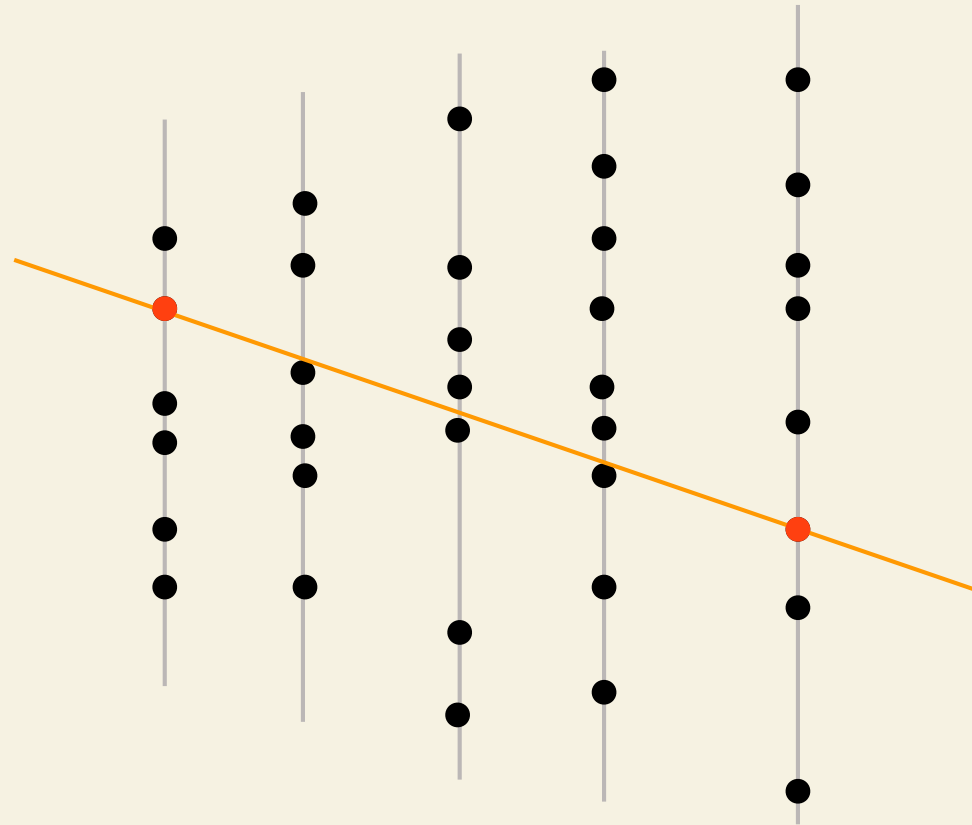


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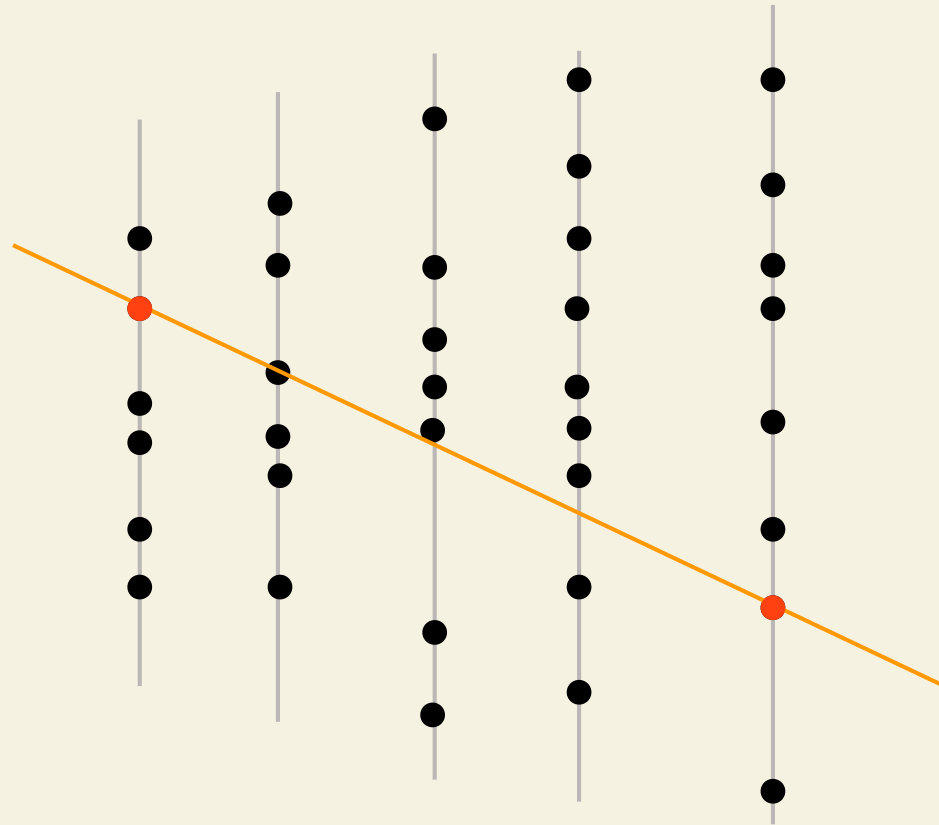




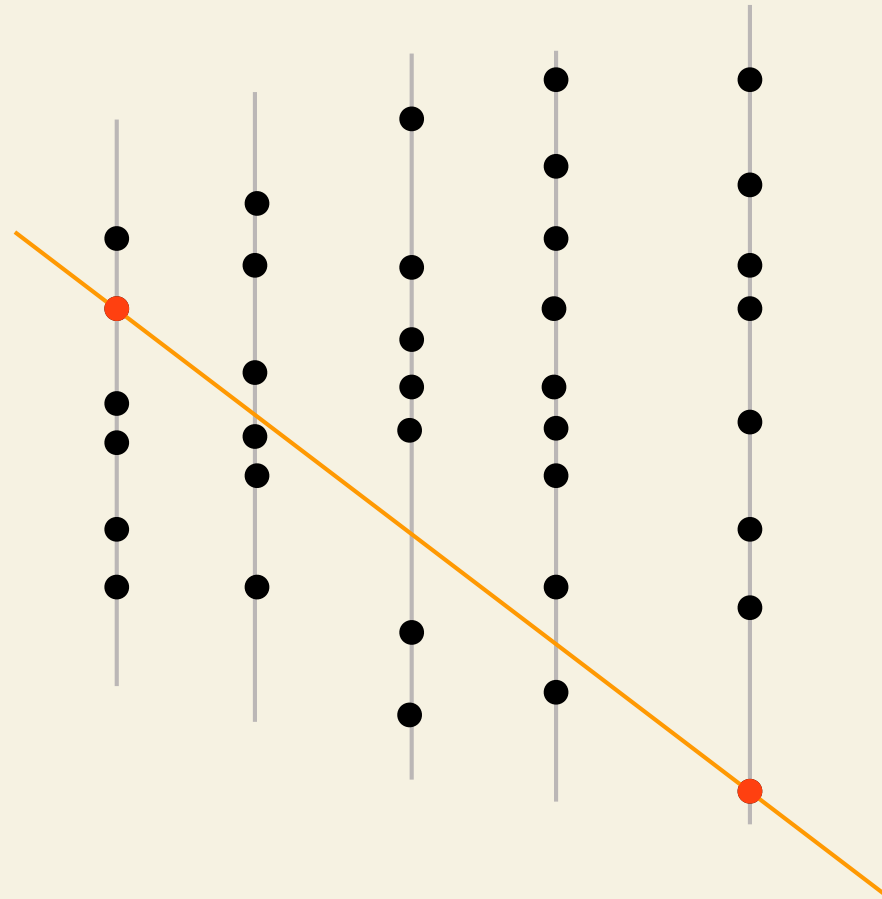
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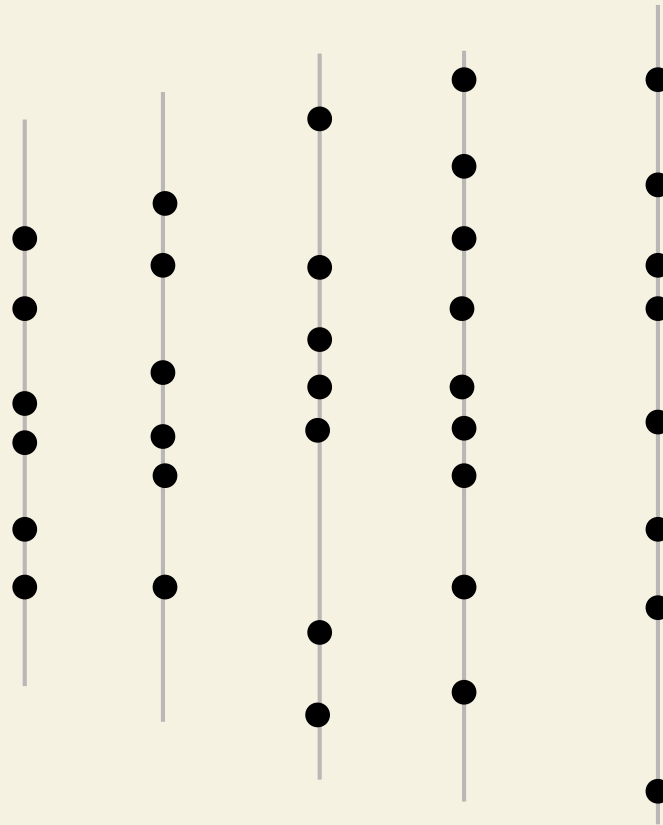
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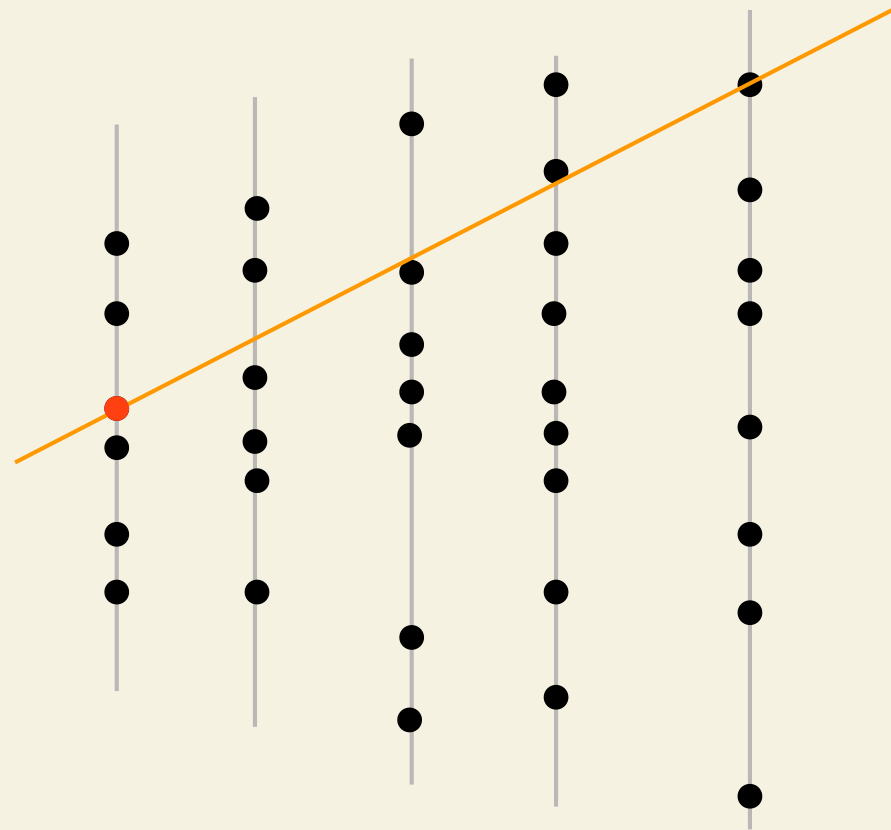


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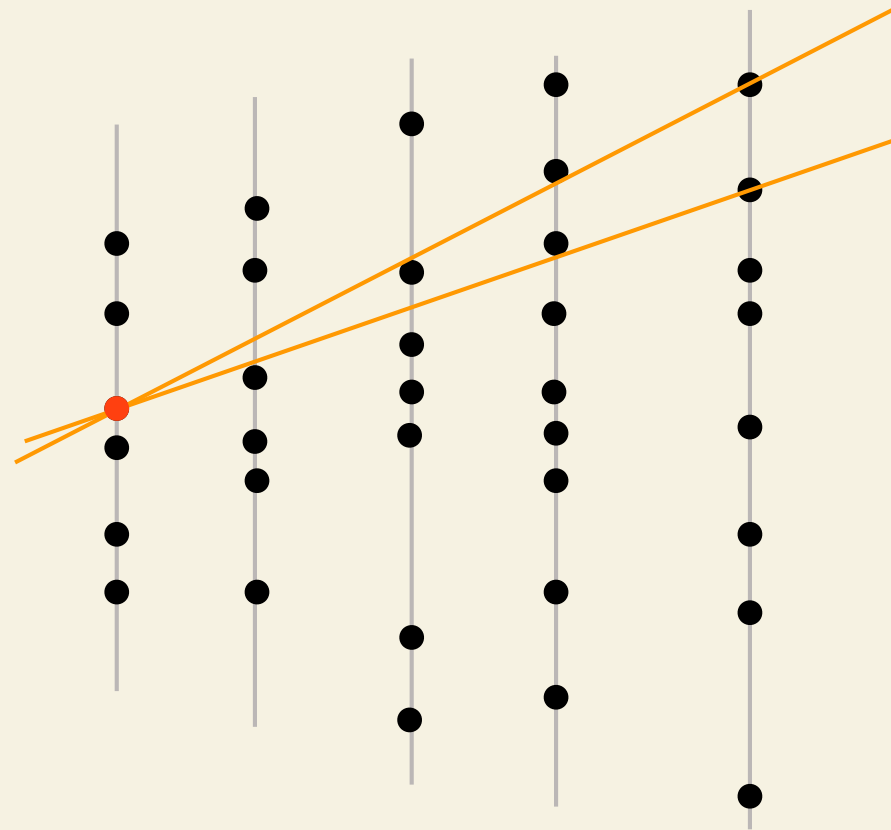




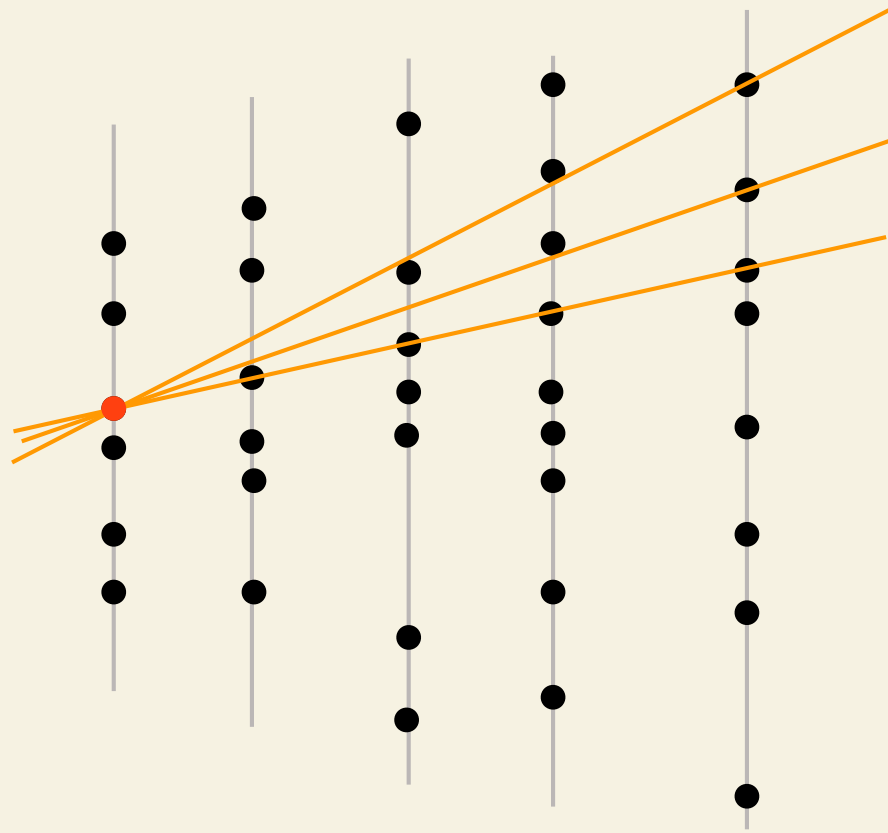
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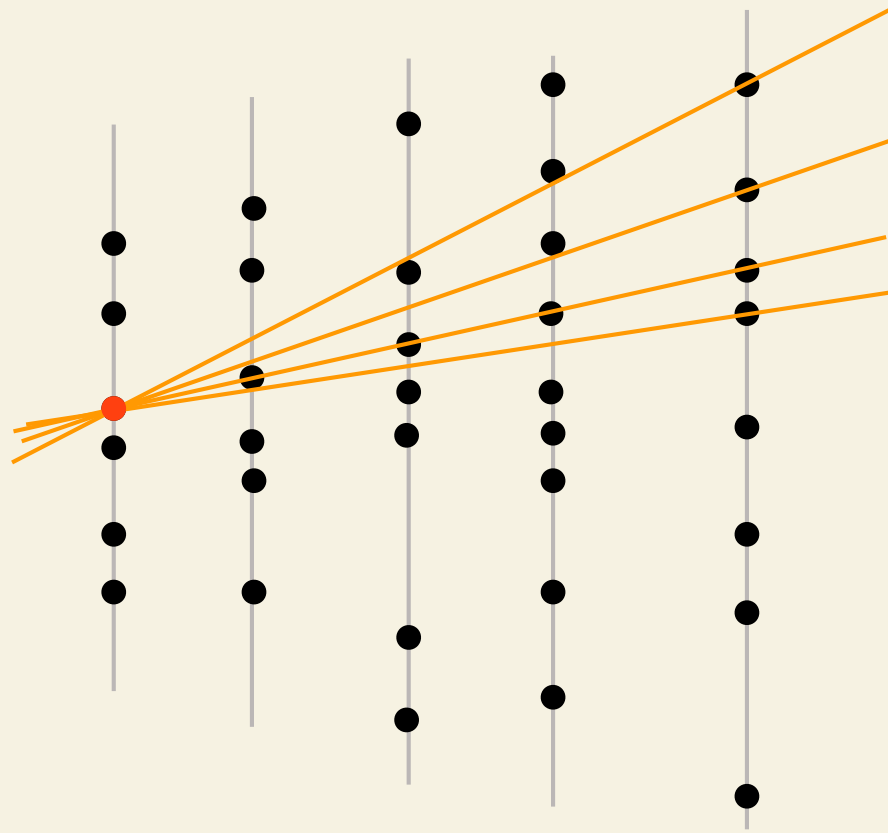
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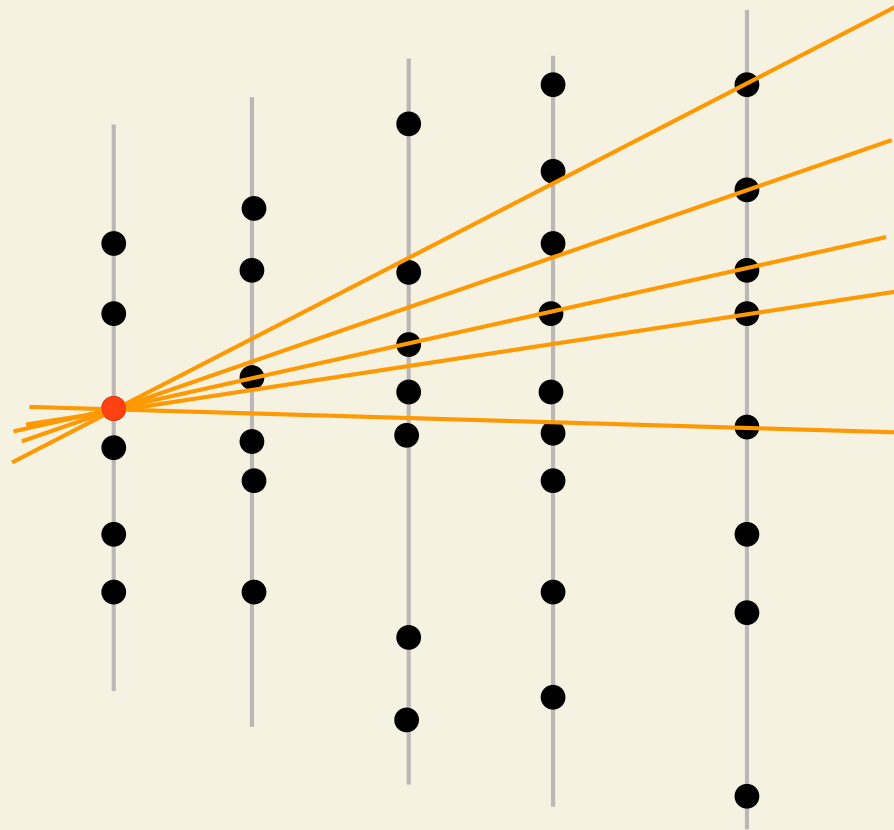
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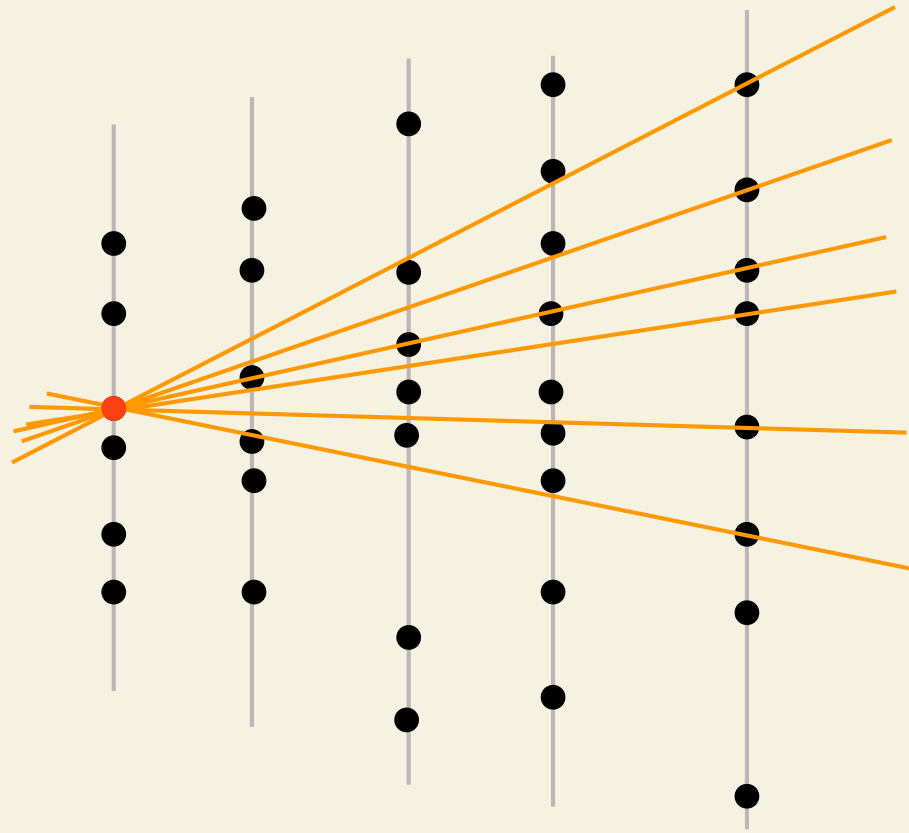
looking for the right combination of hits



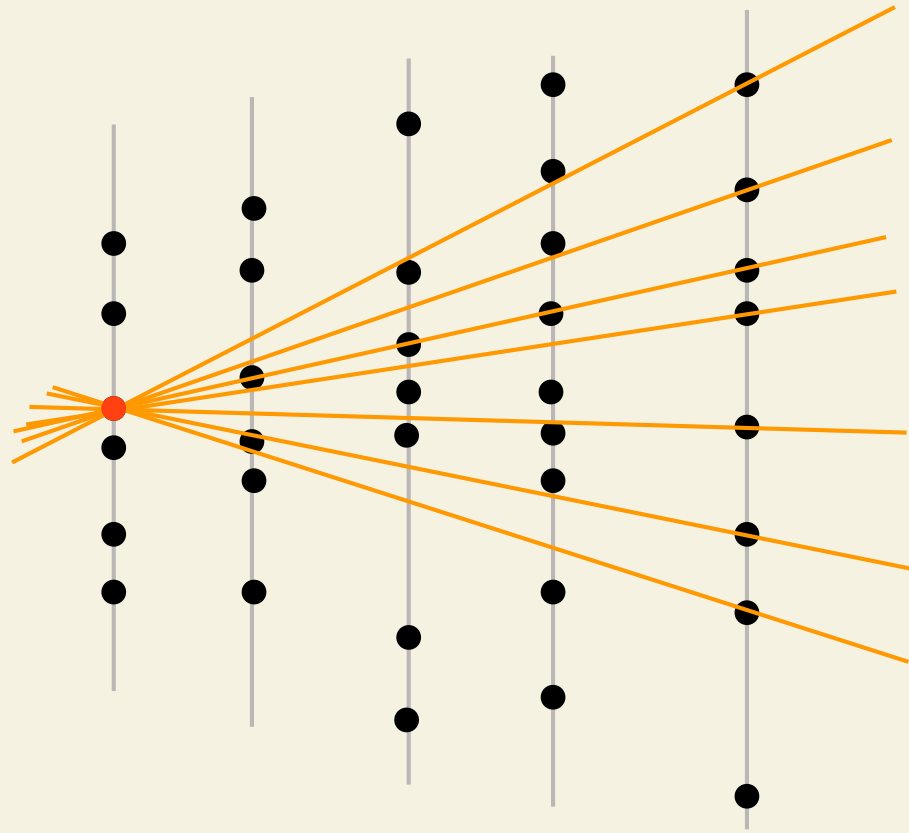
looking for the right combination of hits



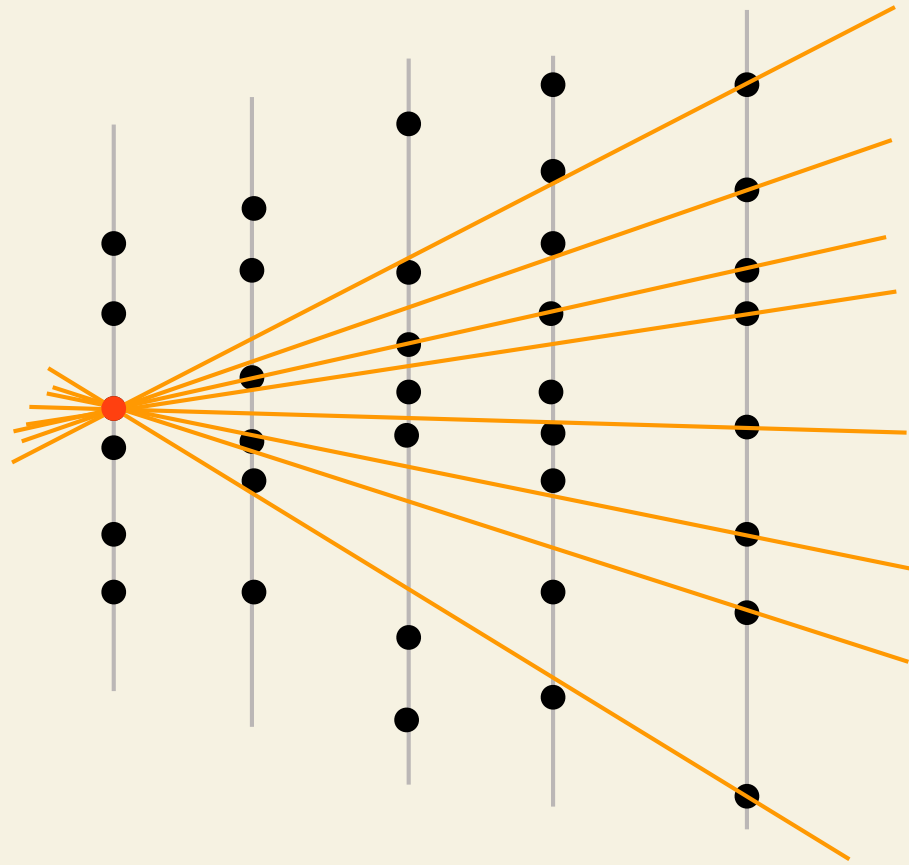
looking for the right combination of hits



looking for the right combination of hits

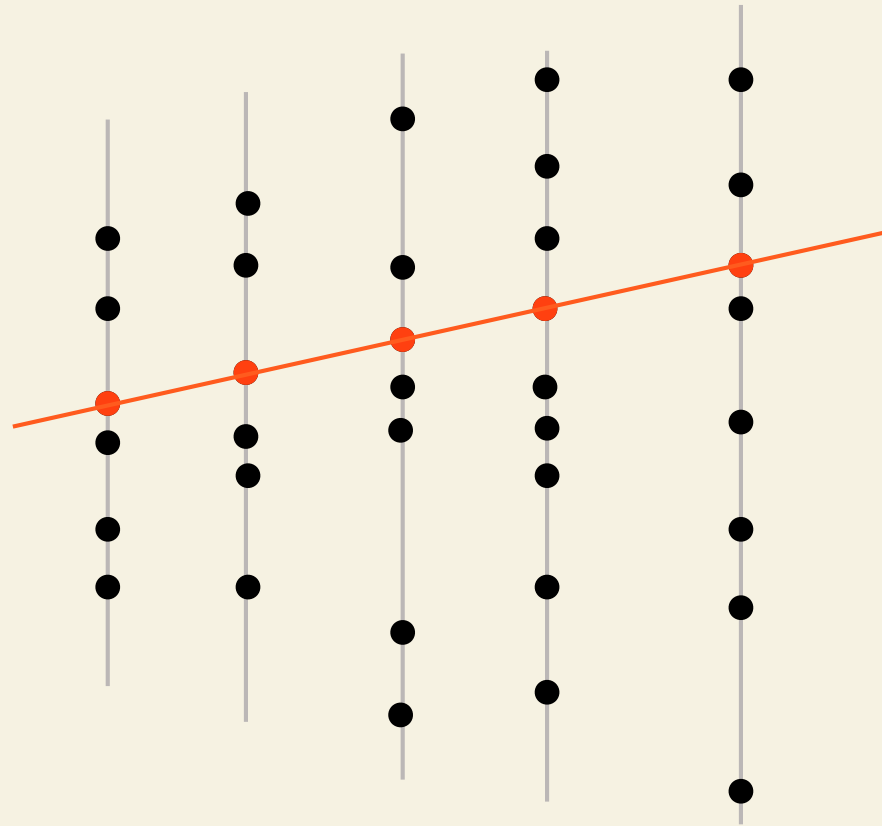


looking for the right combination of hits

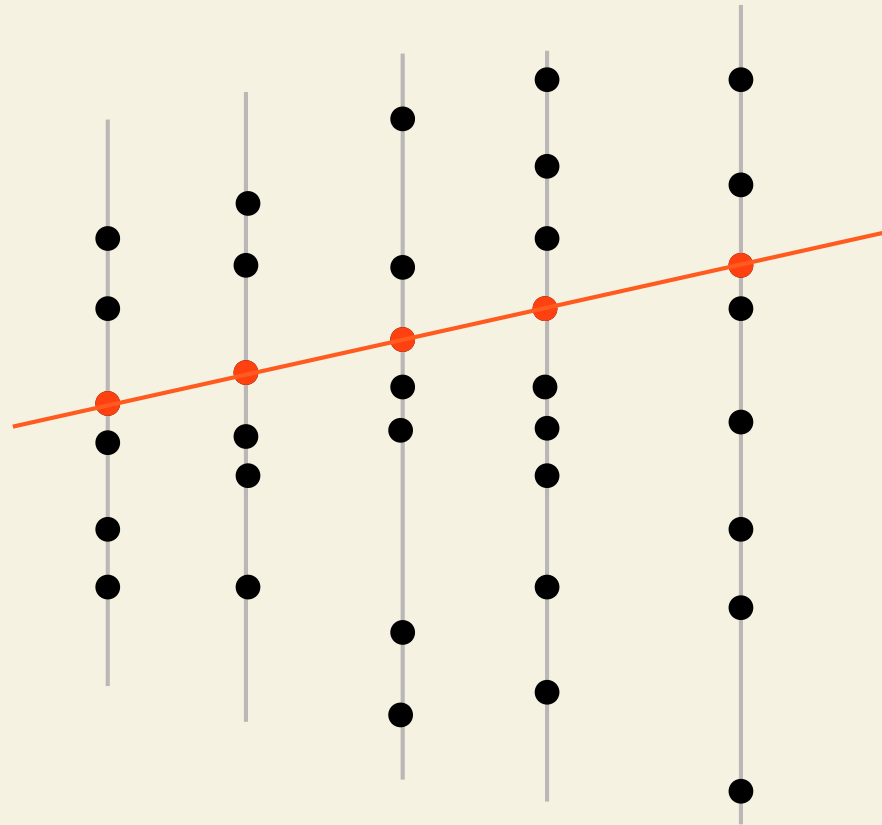




looking for the right combination of hits

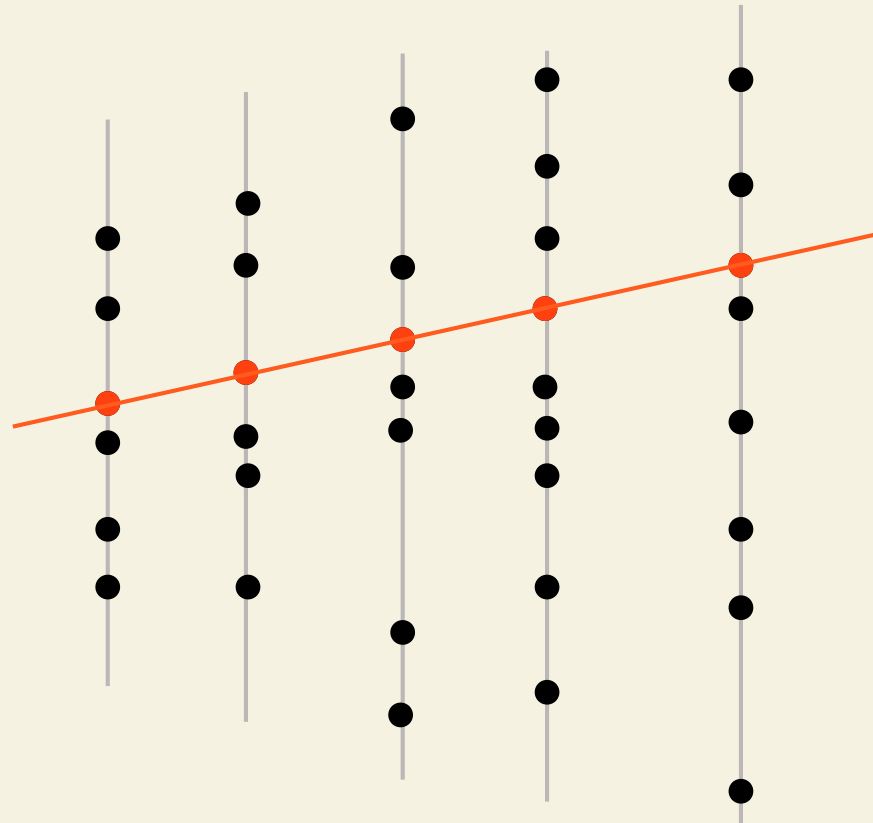


## looking for the right combination of hits



number of trials  $\propto$  (number of hits)<sup>3</sup>

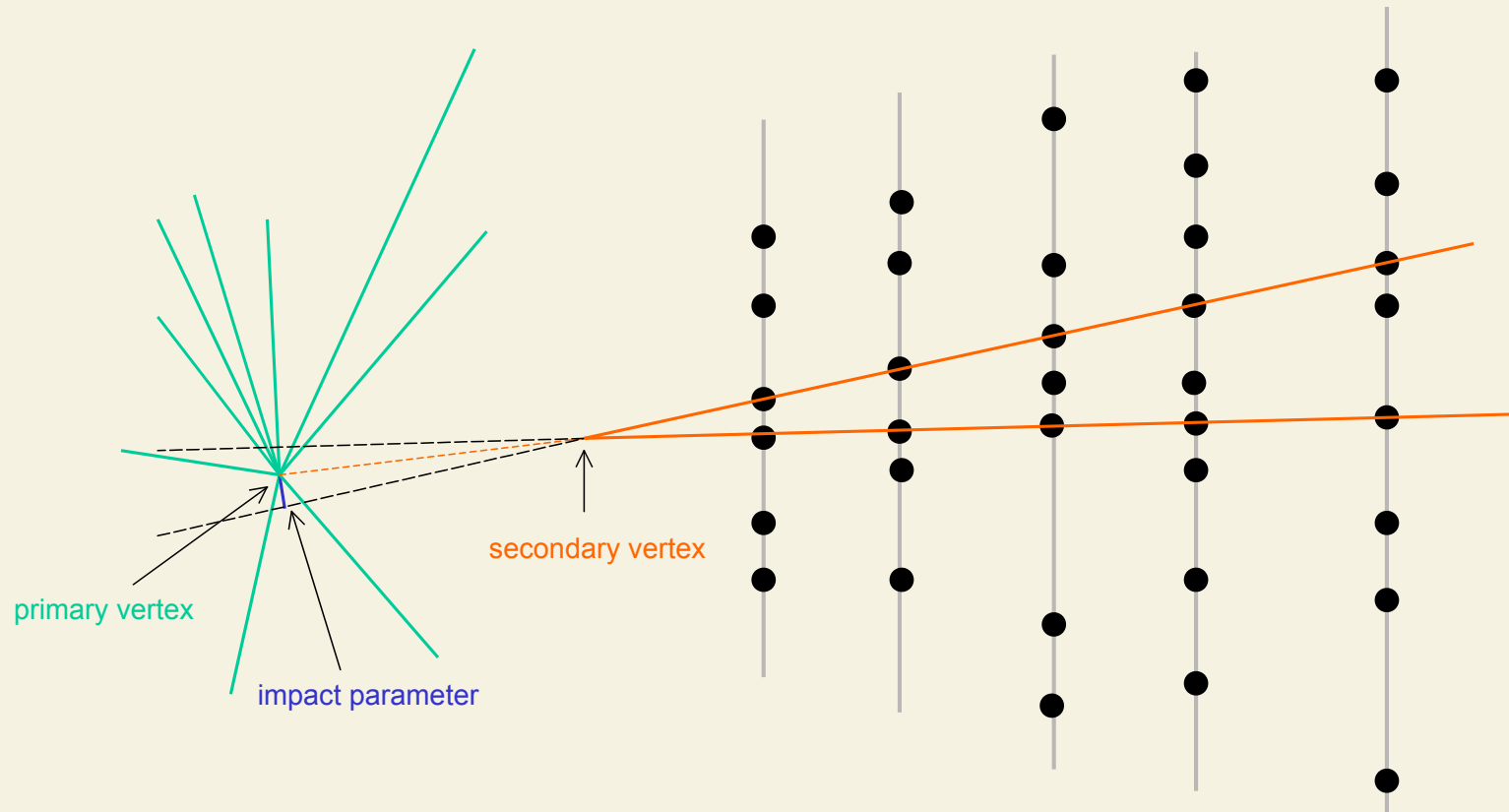
## looking for the right combination of hits



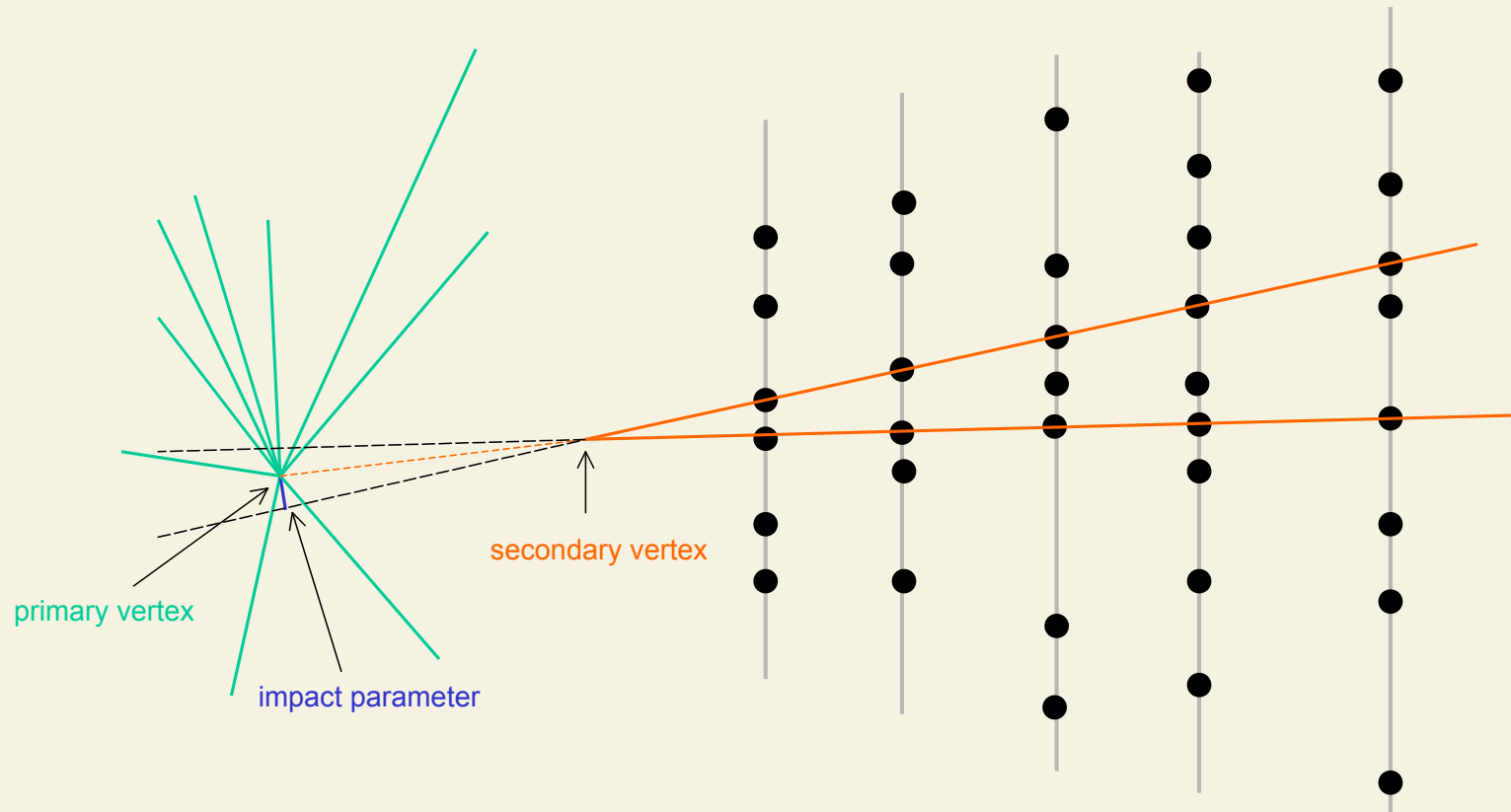
number of trials  $\propto$  (number of hits)<sup>3</sup>

straight line = 2 degrees of freedom

# *pattern recognition*



# *pattern recognition*



*computationally intensive*

*typically solved by trial and error*

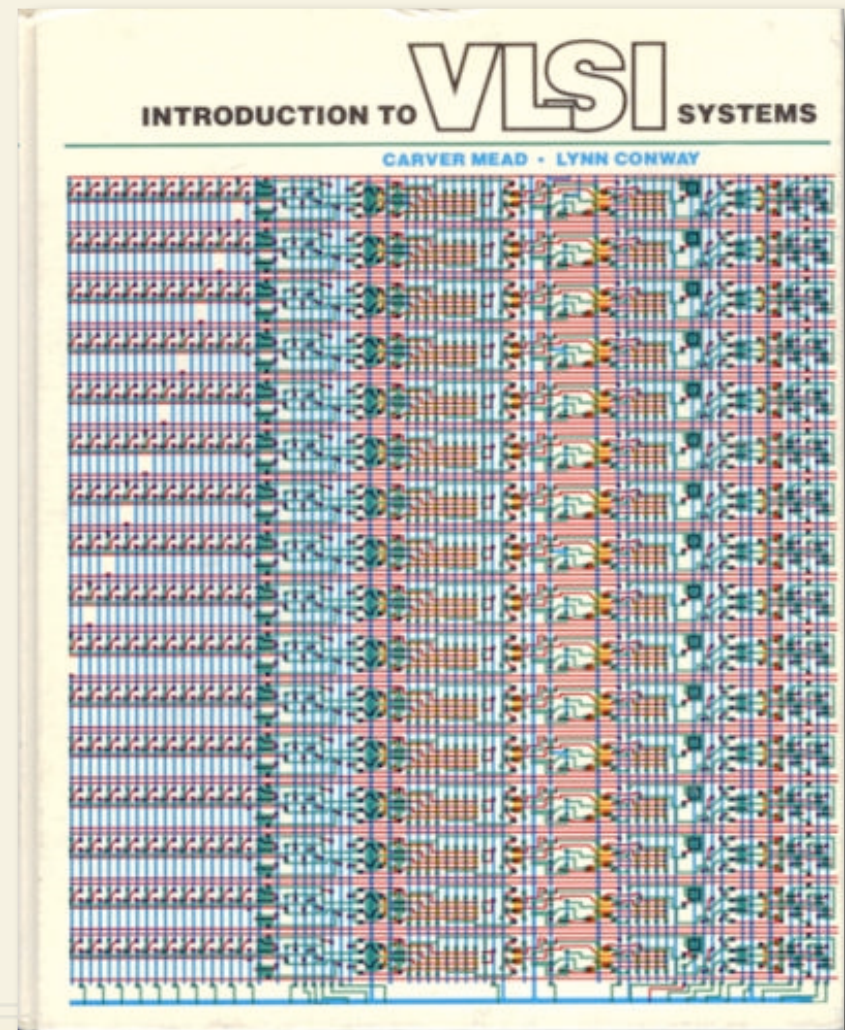
*execution time typically goes as 3rd or 4th power of occupancy*

**It all started around 1986**

# Very Large Scale Integration the revolution

Carver Mead & Lynn Conway

in the '80s the technology of  
VLSI design becomes  
available to the universities  
and to small research  
projects

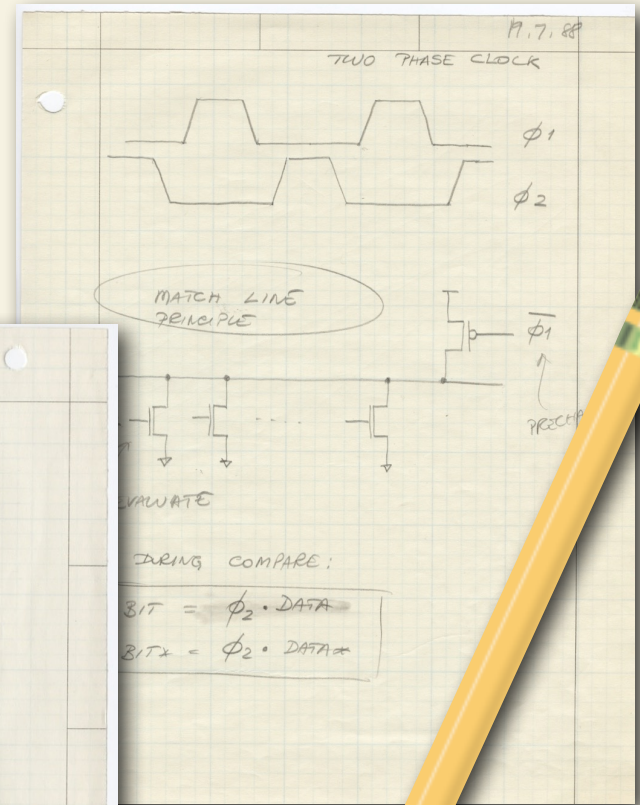
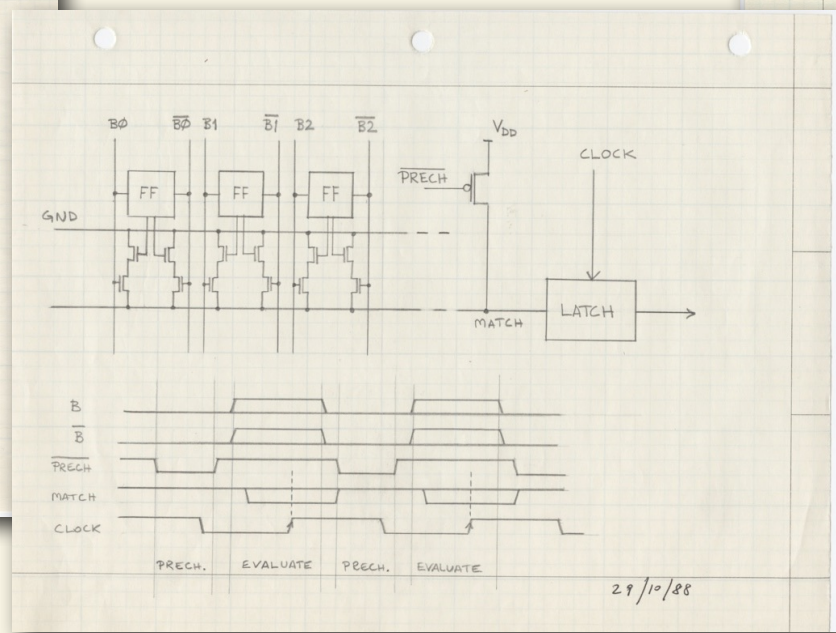
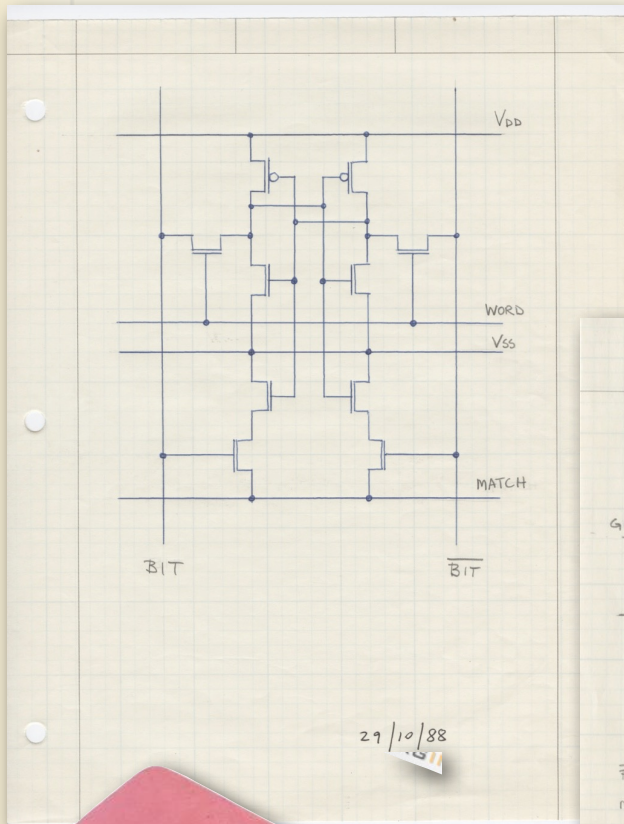


# need for speed

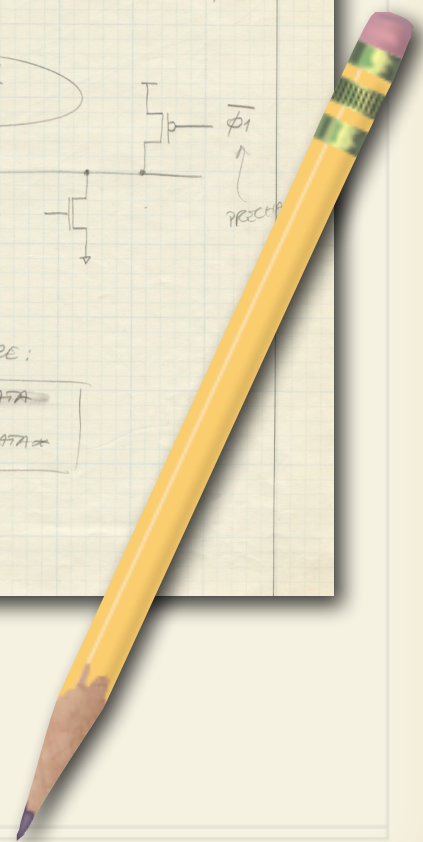
- ~ Our main goal is speed
- ~ Many hit combinations to be examined in sequence
  - ~ → long execution time
- ~ In principle **all combinations can be examined in parallel**
  - ~ many processing unit each one checking a single combination (a very simple task)
  - ~ not **all** combinations, only **valid** combinations
- ~ For finite detector resolution the number of valid hit combinations is finite. Is it tractable?
  - ~ processors are **very simple**
  - ~ basically an AND circuit



it is at this point in time that we came up with the idea to use VLSI technology to solve the pattern recognition problem and reconstruct tracks in the detector in a very short time



DURING COMPARE:  
 $BIT = \phi_2 \cdot DATA$   
 $BITx = \phi_2 \cdot DATAx$



October 1988: paper, pencil, eraser....

# the Associative Memory

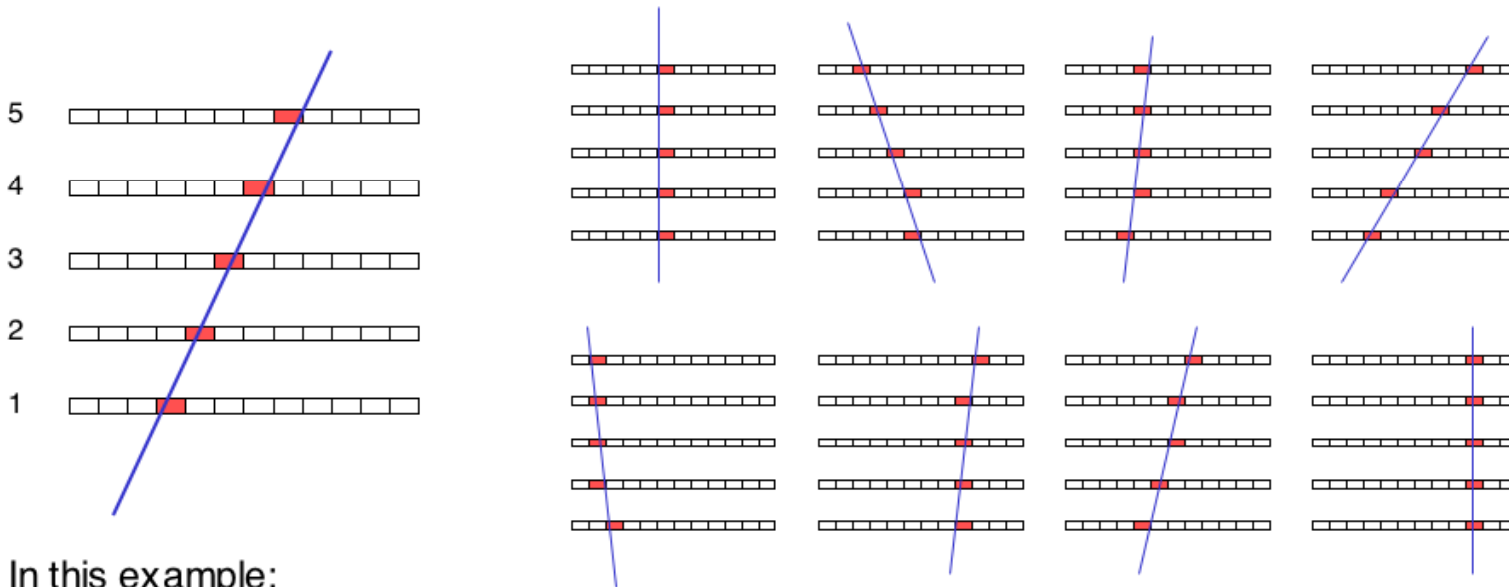


## Building the “Pattern Bank”

SVT

Instead of looking for hit combinations such that  $f(x_1, x_2, x_3, \dots) = 0$

1. Build a database with all patterns corresponding to “good” tracks
2. Compare hits in each event with all patterns to find track candidates



In this example:  
Straight lines, 5 layers, 12 bins/layer

⇒ Total number of patterns  $\sim (12)^2 \cdot (5-1) = 576$

October 24, 1988

VLSI STRUCTURES FOR TRACK FINDING

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Received 24 October 1988

We discuss the architecture of a device based on the concept of *associative memory* designed to solve the track finding problem, typical of high energy physics experiments, in a time span of a few microseconds even for very high multiplicity events. This "machine" is implemented as a large array of custom VLSI chips. All the chips are equal and each of them stores a number of "patterns". All the patterns in all the chips are compared in parallel to the data coming from the detector while the detector is being read out.

1. Introduction

The quality of results from present and future high energy physics experiments depends to some extent on the implementation of fast and efficient track finding algorithms. The detection of *heavy flavor* production, for example, depends on the reconstruction of secondary vertices generated by the decay of long lived particles, which in turn requires the reconstruction of the majority of the tracks in every event.

Particularly appealing is the possibility of having detailed tracking information available at trigger level even for high multiplicity events. This information could be used to select events based on impact parameter or secondary vertices. If we could do this in a sufficiently short time we would significantly enrich the sample of events containing heavy flavors.

Typical events feature up to several tens of tracks each of them traversing a few position sensitive detector layers. Each layer detects many hits and we must correctly correlate hits belonging to the same track on different layers before we can compute the parameters of the track. This task is typically time consuming, it is

2. The detector

In this discussion we will assume that our detector consists of a number of layers, each layer being segmented into a number of *bins*. When charged particles cross the detector they *hit* one bin per layer. No particular assumption is made on the shape of trajectories: they could be straight or curved. Also the detector layers need not be parallel nor flat. This abstraction is meant to represent a whole class of real detectors (drift chambers, silicon microstrip detectors etc.). In the real world the coordinate of each hit will actually be the result of some computation performed on "raw" data: it could be the center of gravity of a cluster or a charge division interpolation or a drift-time to space conversion depending on the particular class of detector we are considering. We assume that all these operations are performed upstream and that the resulting coordinates are "binned" in some way before being transmitted to our device.

3. The pattern bank

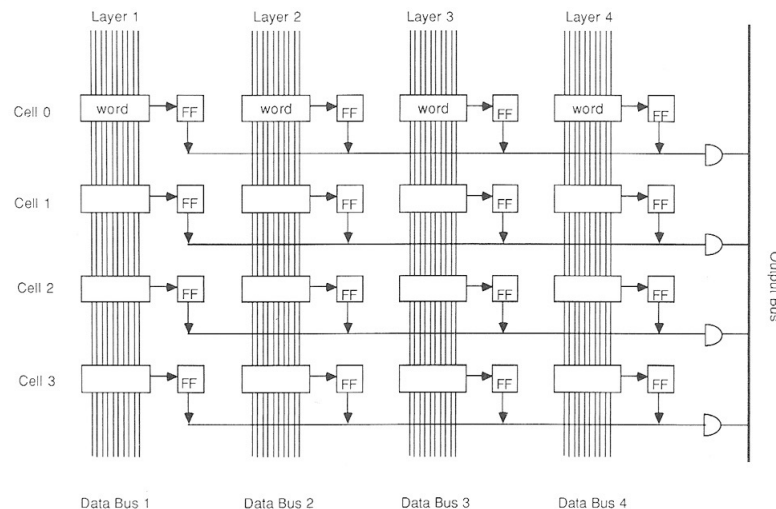


Fig. 3. Associative memory architecture.

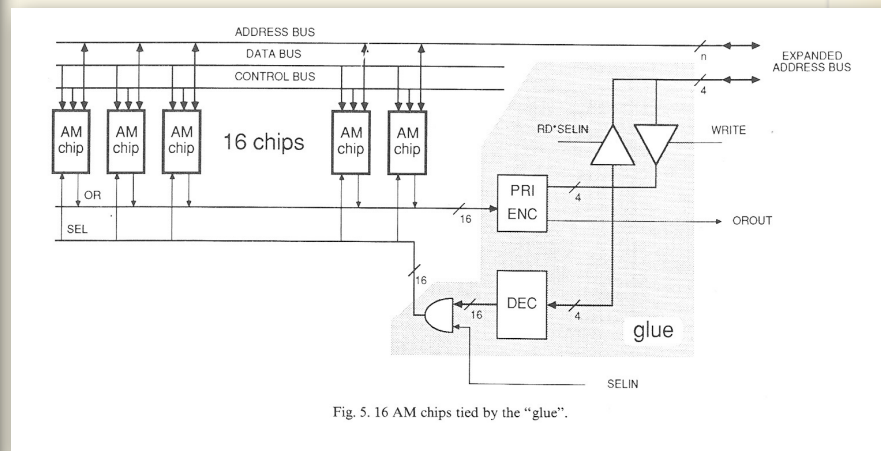


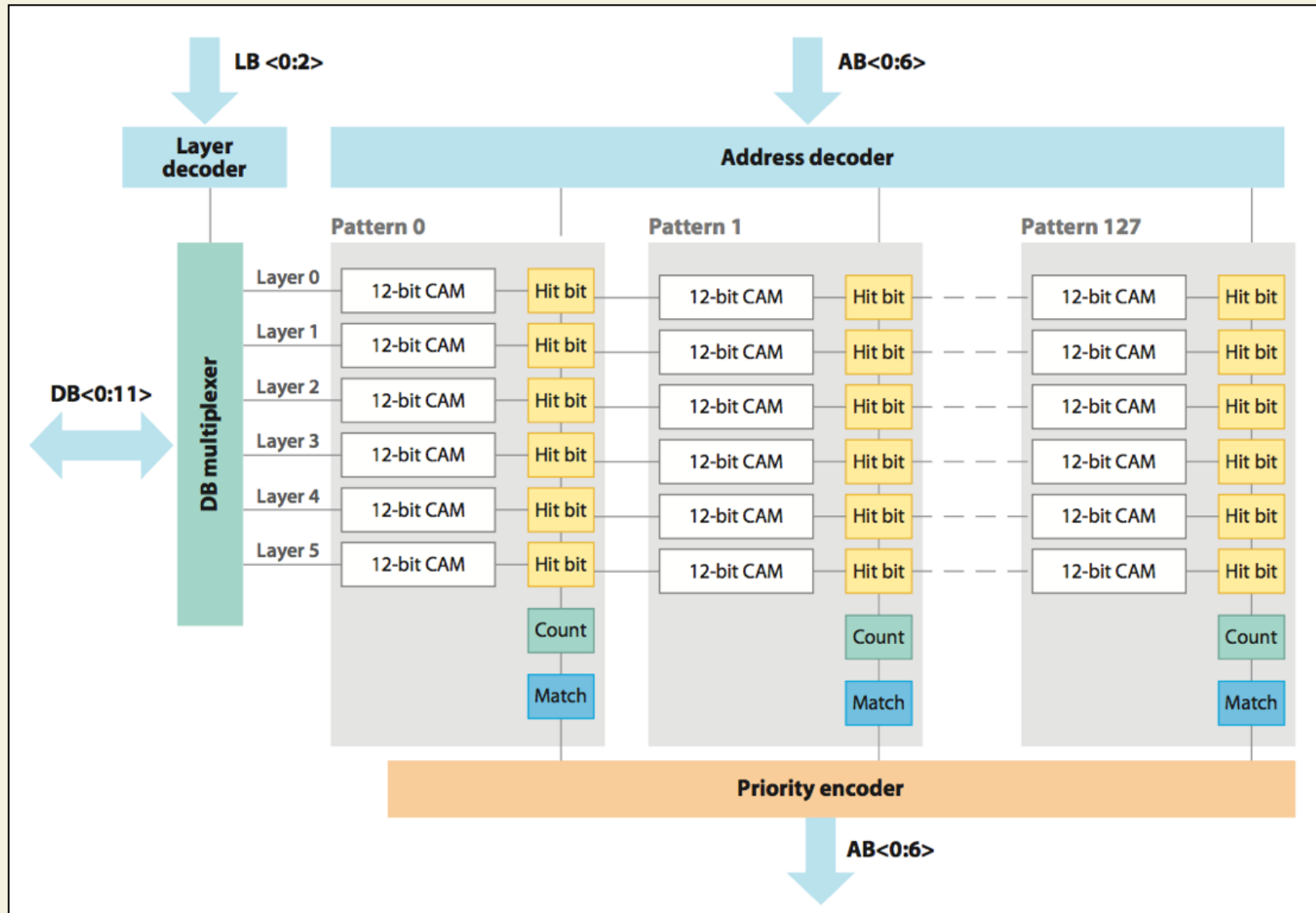
Fig. 5. 16 AM chips tied by the "glue".

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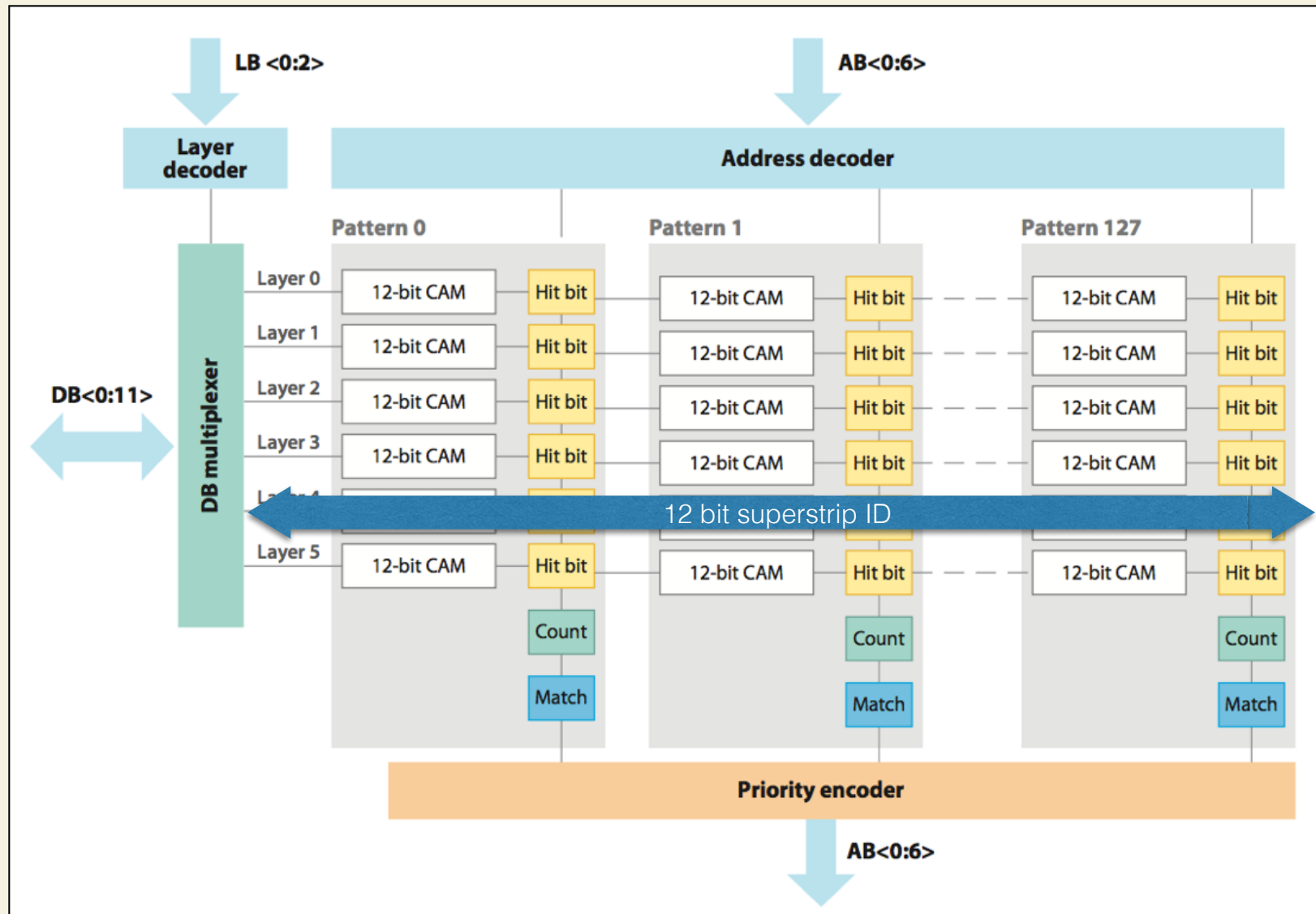
**How does it work?**



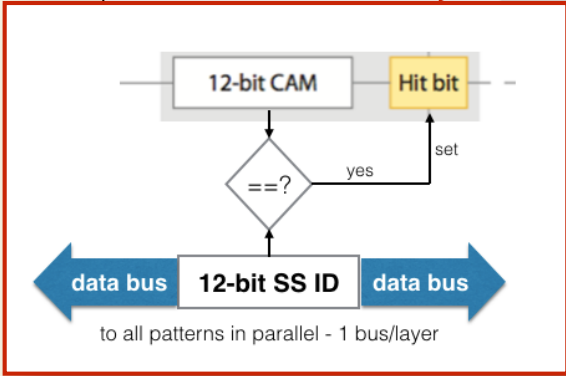
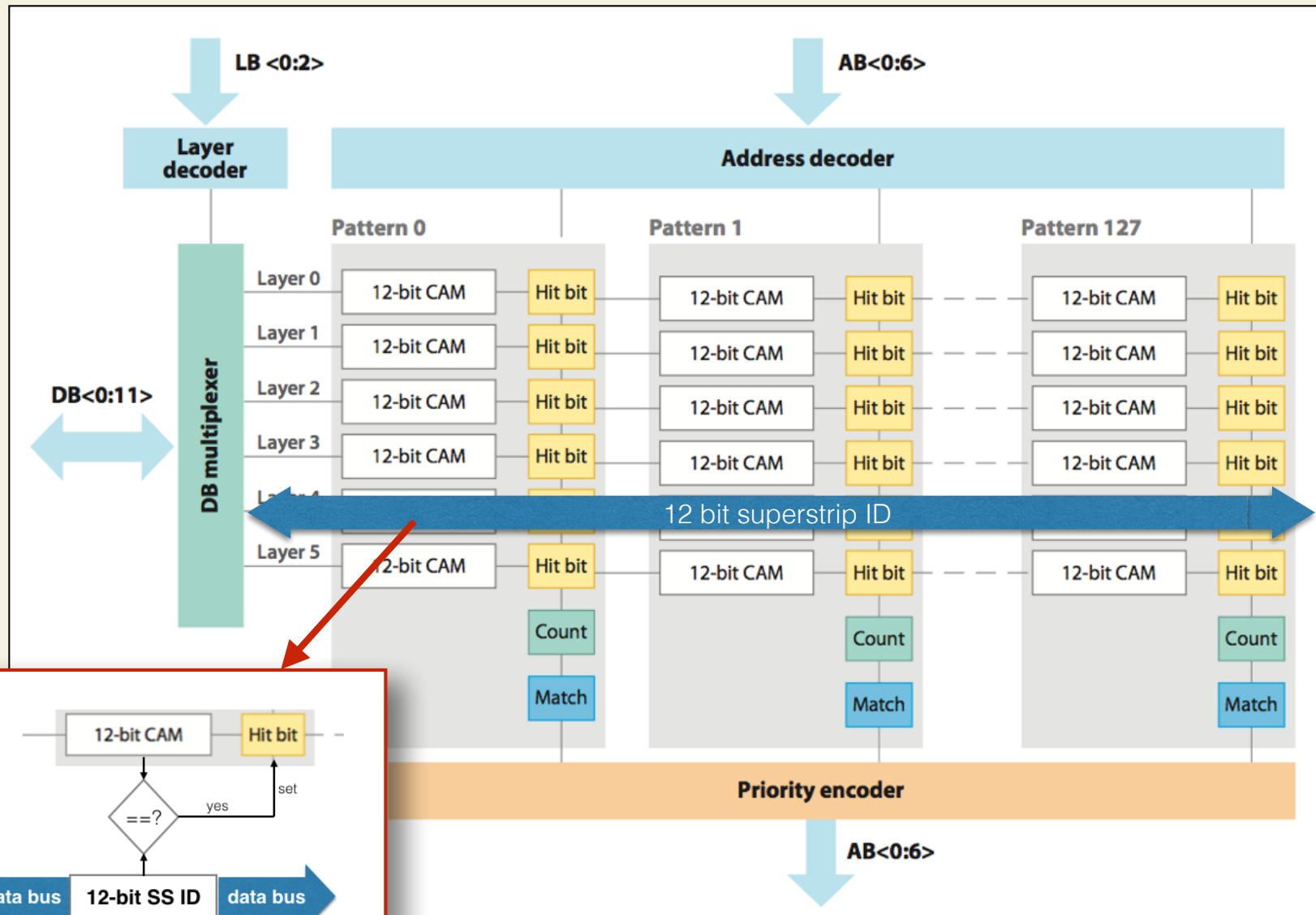
# AM internal structure



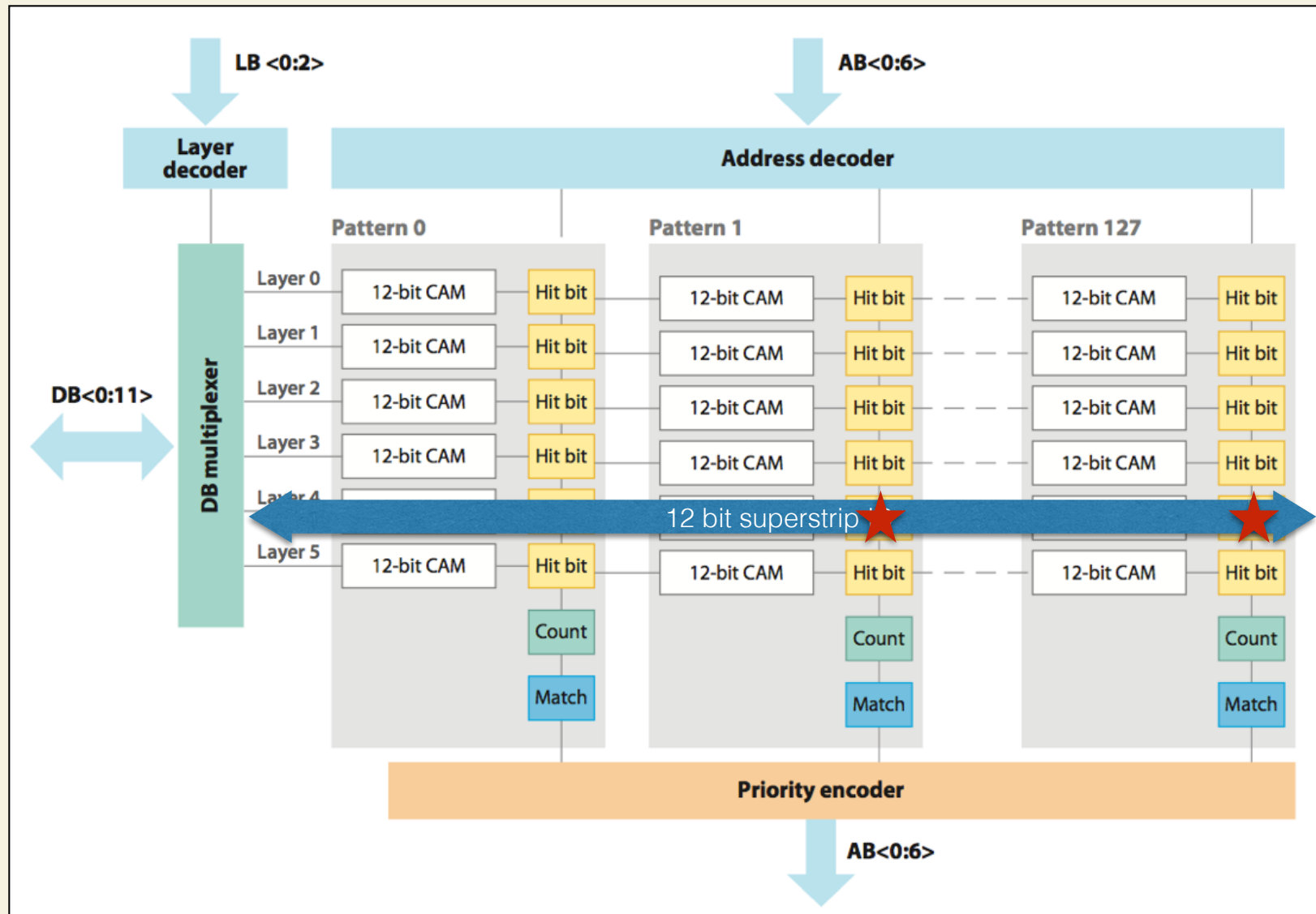
# AM internal structure



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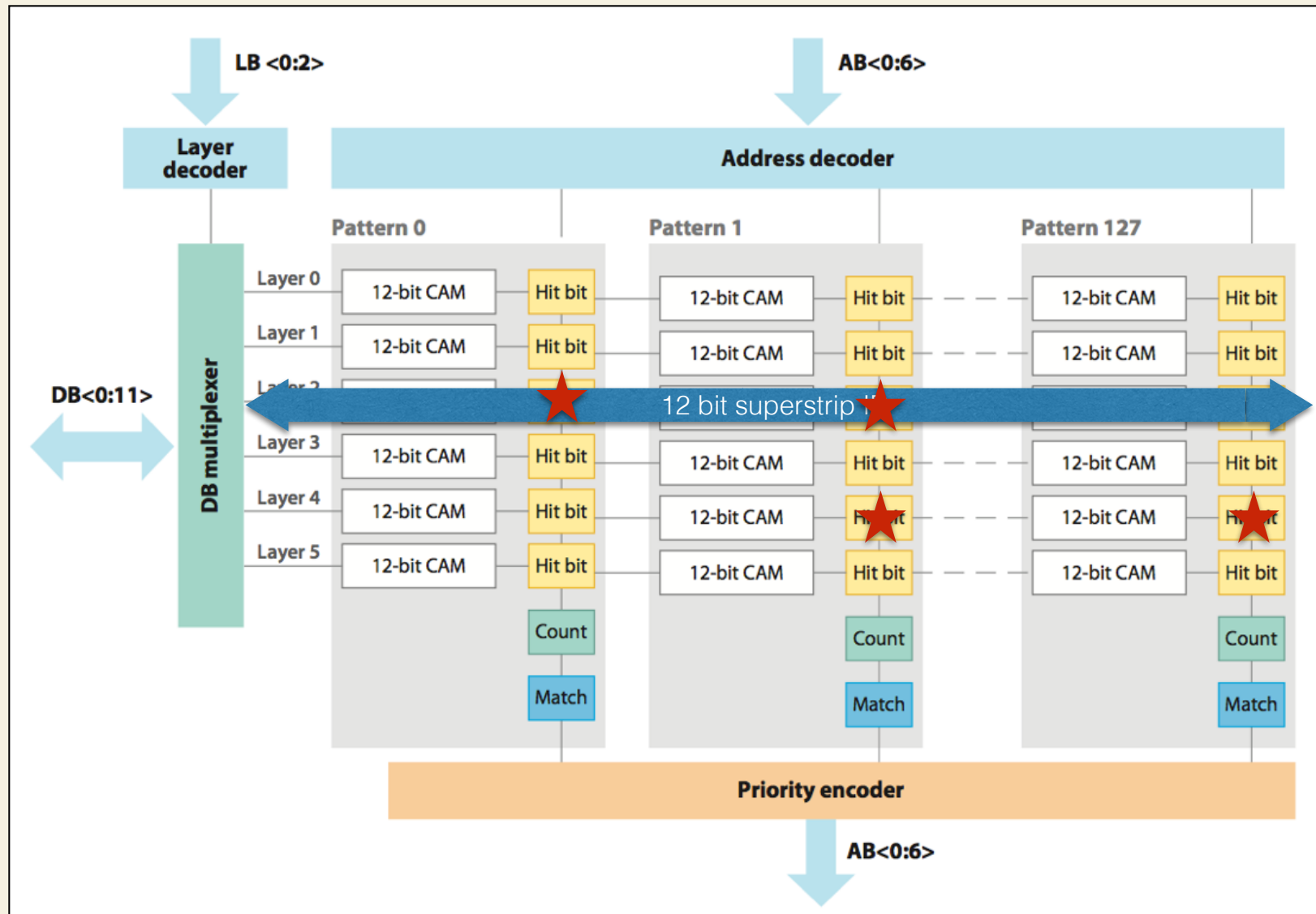


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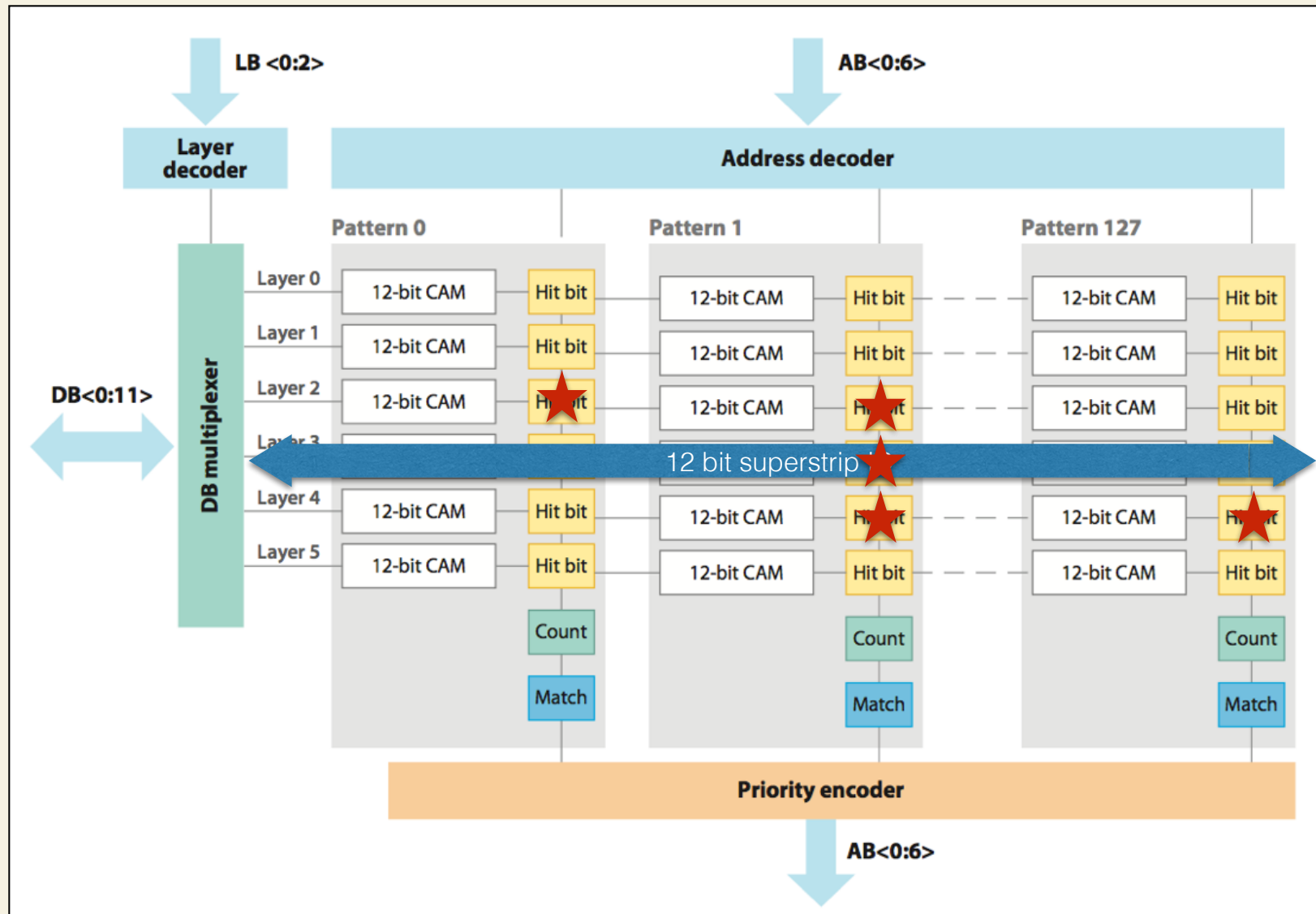




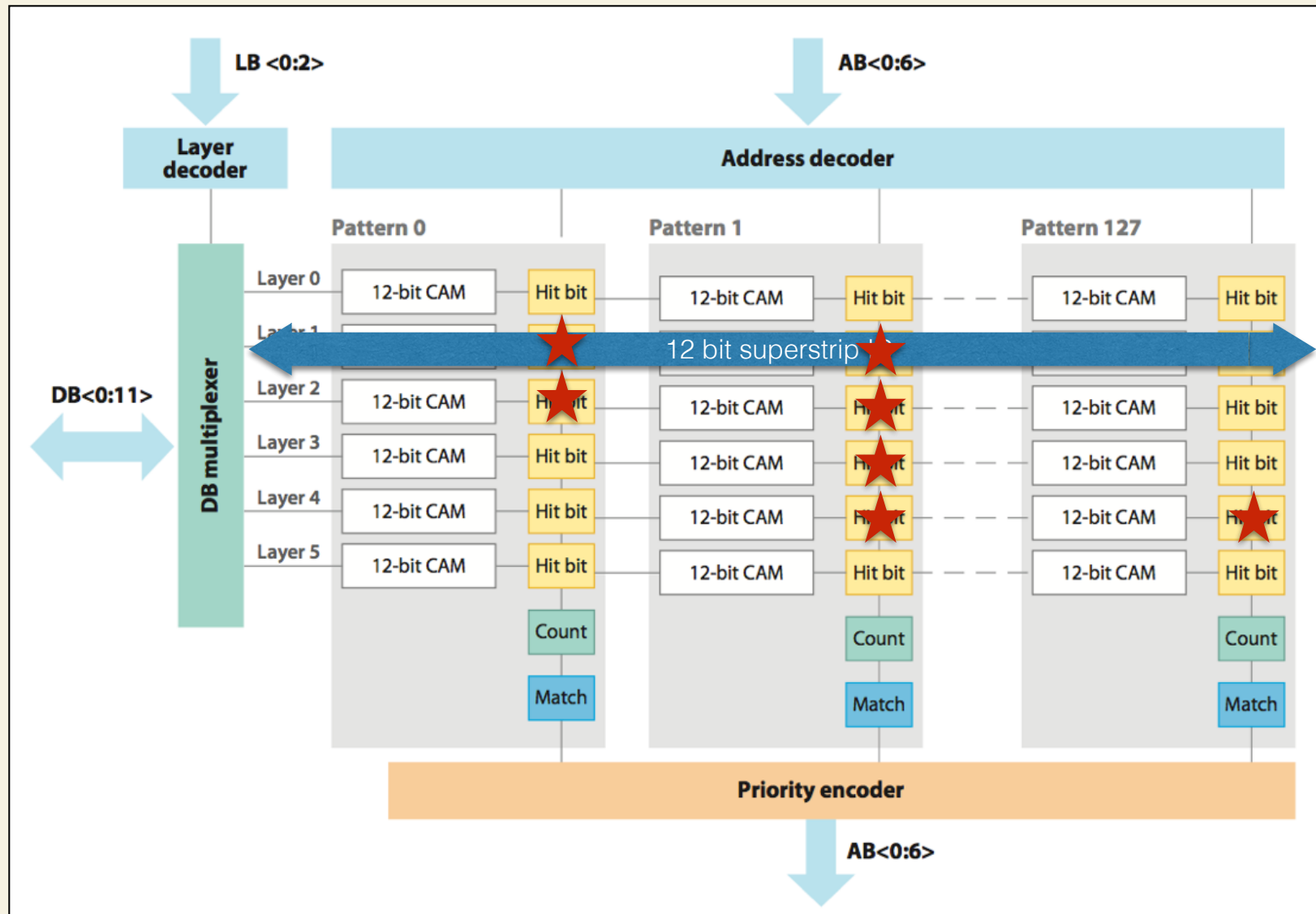
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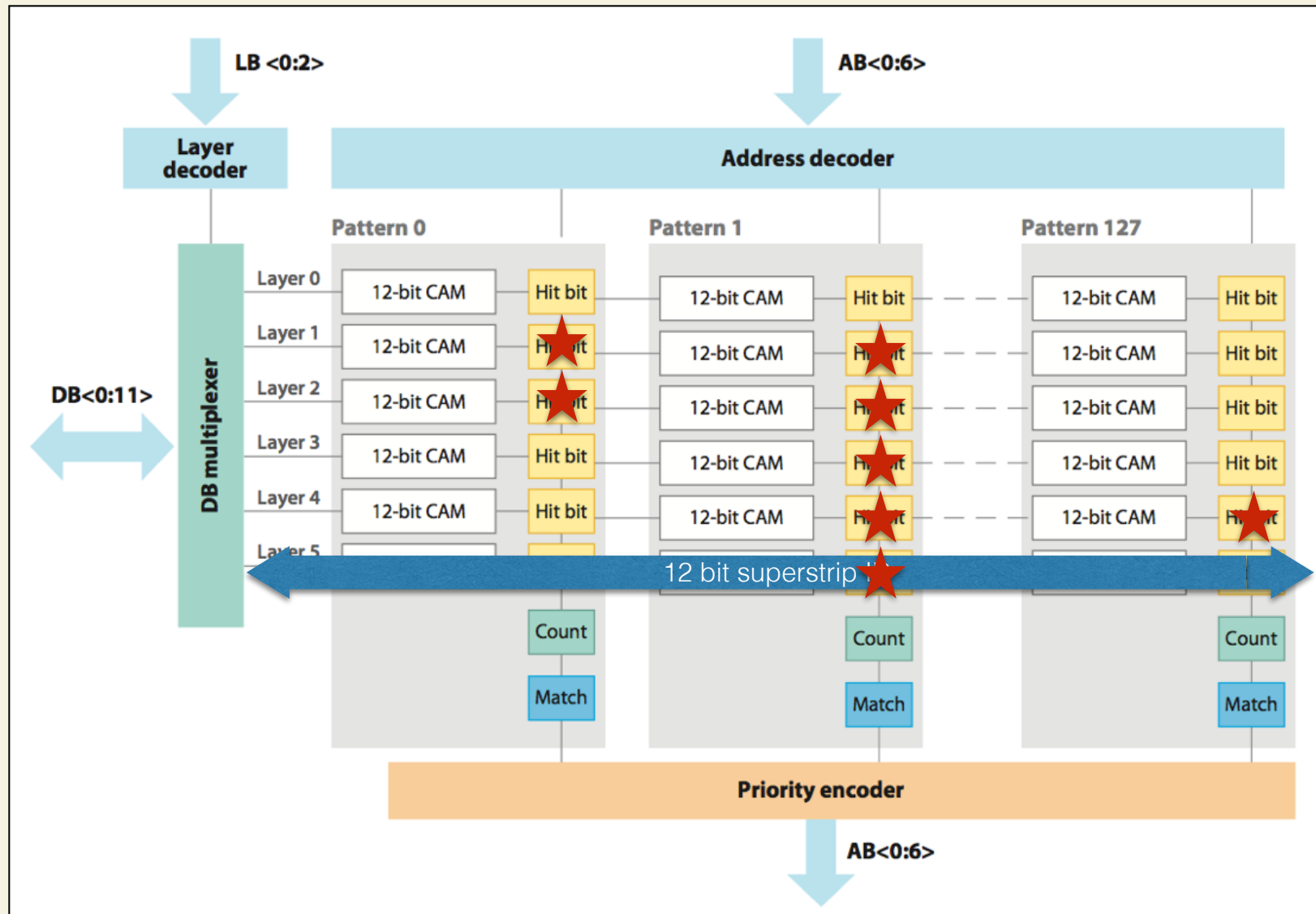
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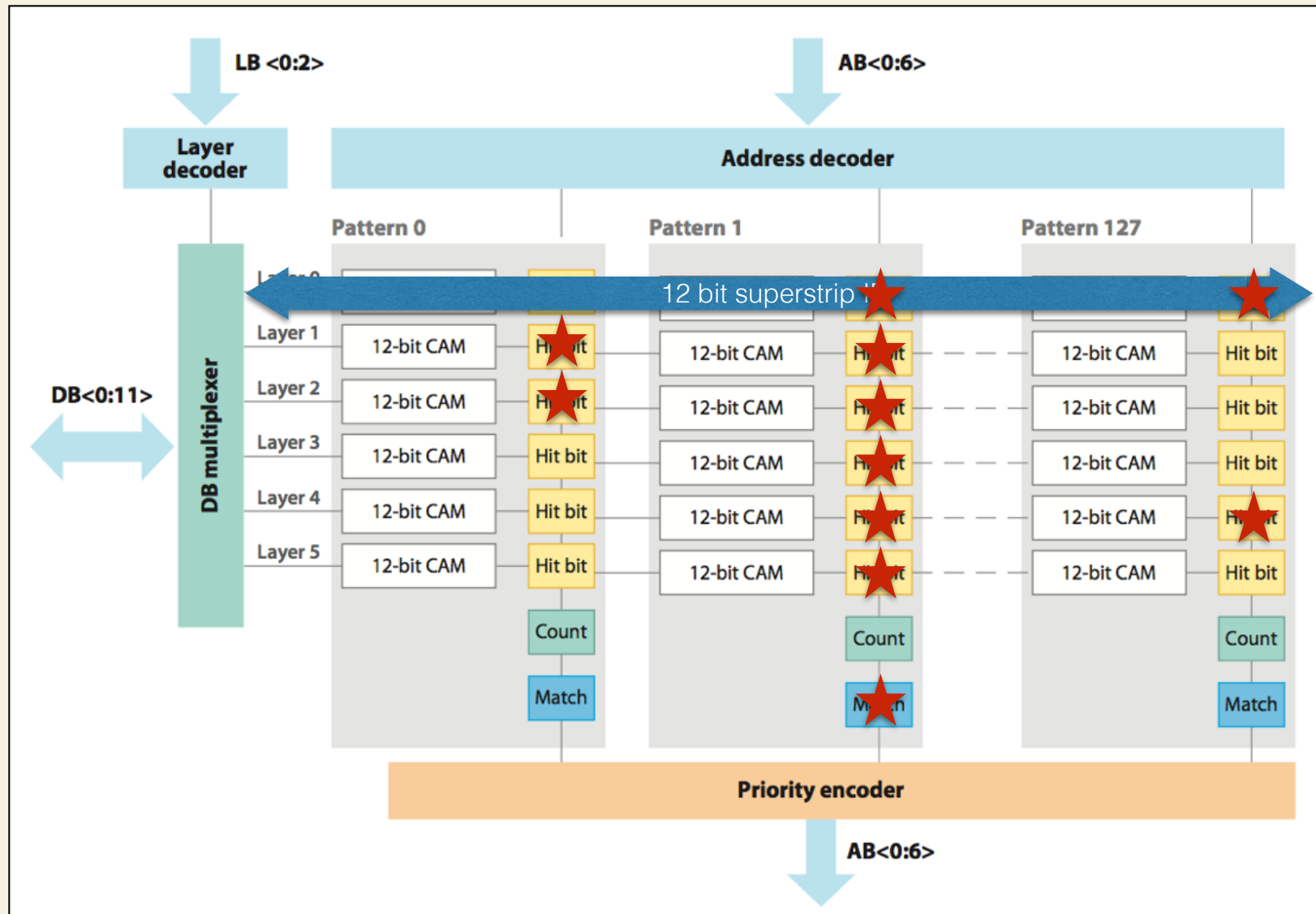
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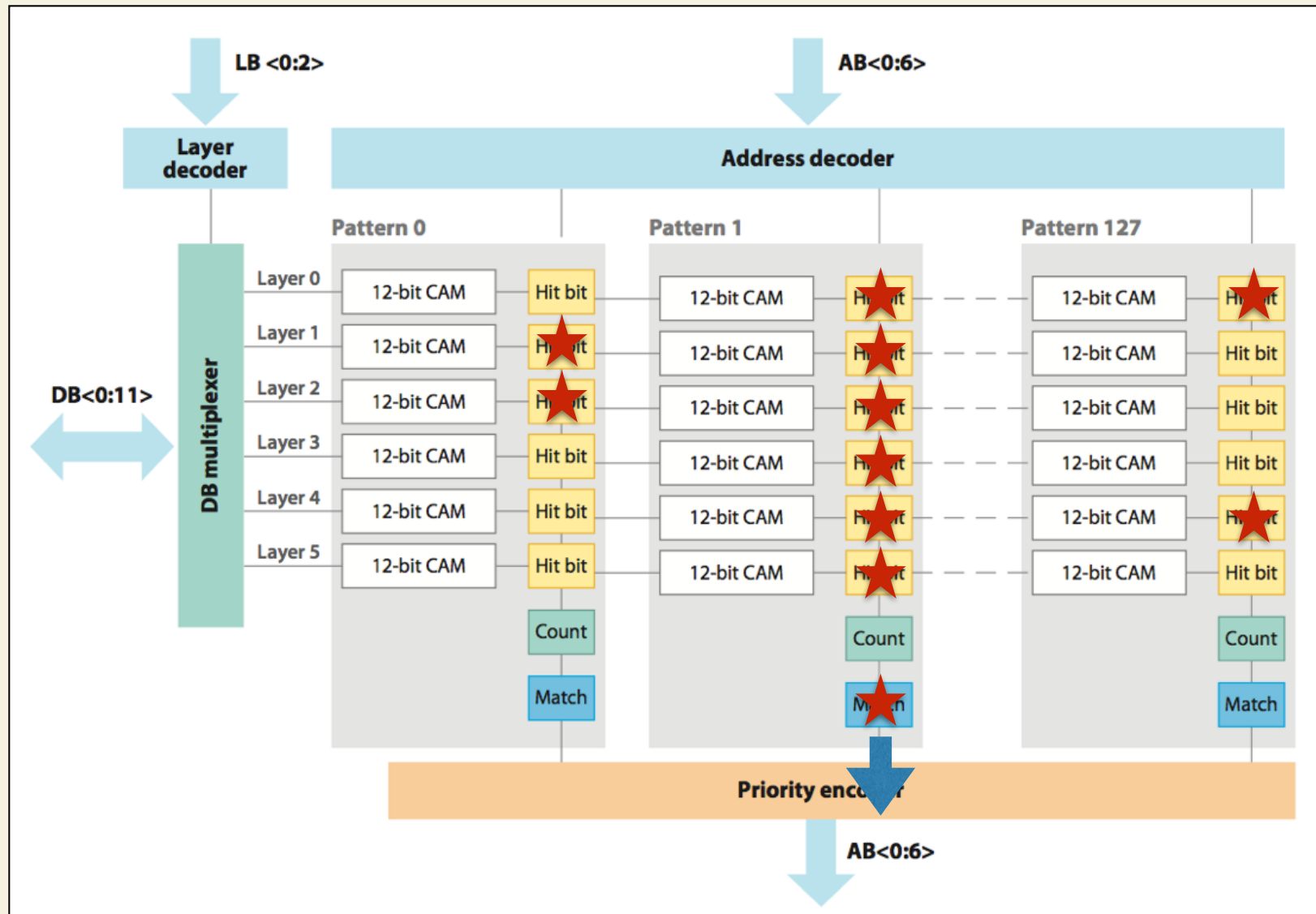
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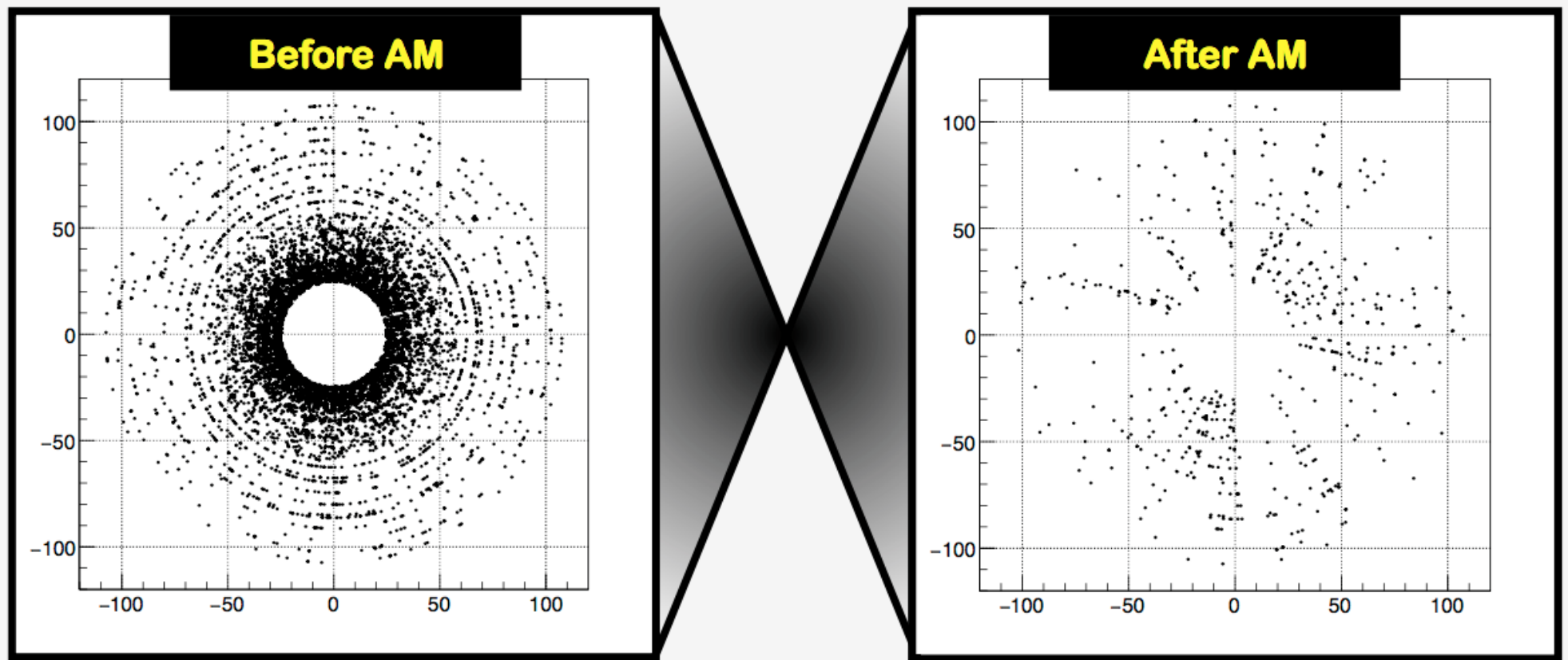
# AM internal structure



as soon as all the hits have been read out from the detector into the AM, the first matched pattern is available immediately and all the others are coming out in a continuous stream, one per clock cycle

in this sense, pattern recognition, in the AM, takes very little time since it is mostly hidden behind the readout time

# The Associative Memory does a lot in a very short time



Simulated beam crossing at the HL-LHC  
(drawing courtesy of Seb Viret)

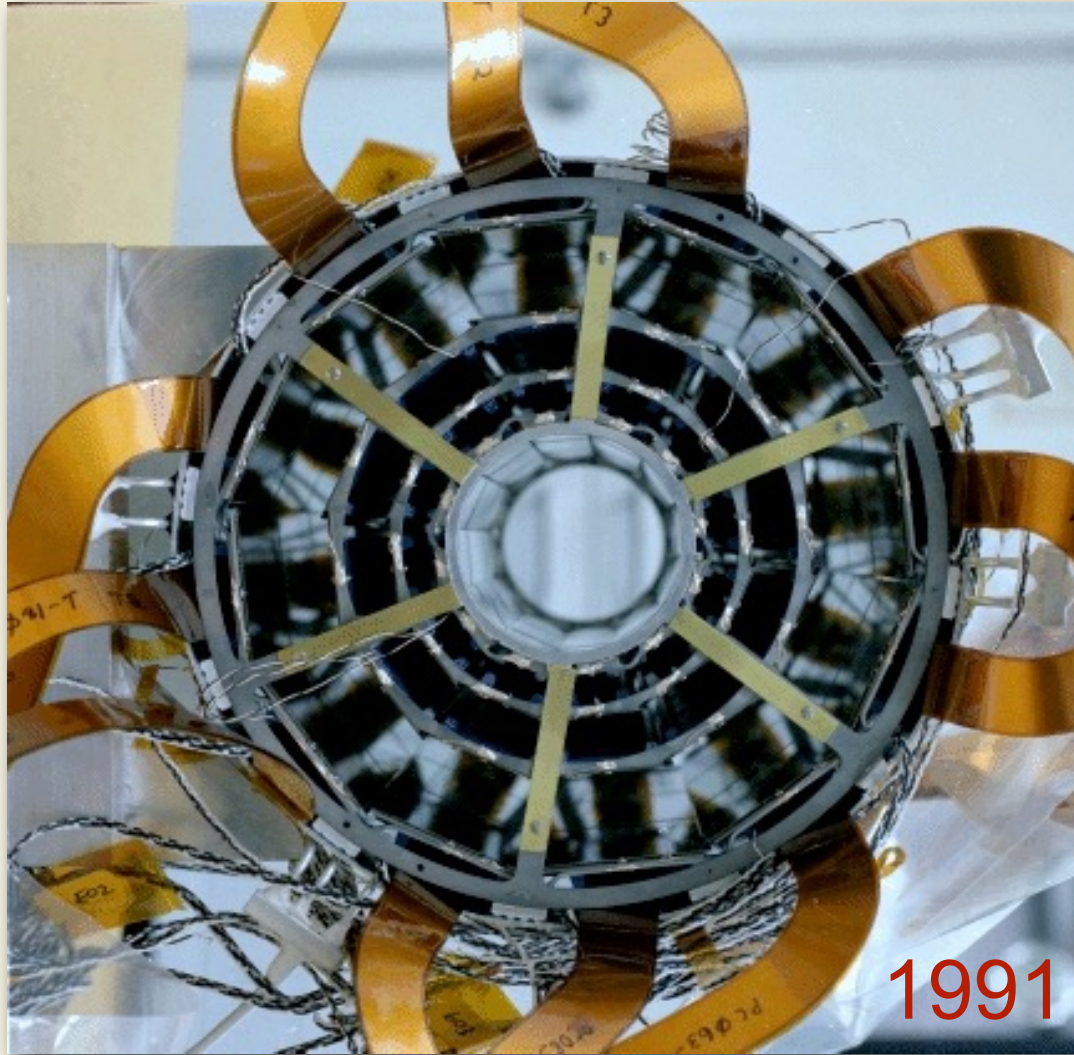


but let's go back again to the beginning...

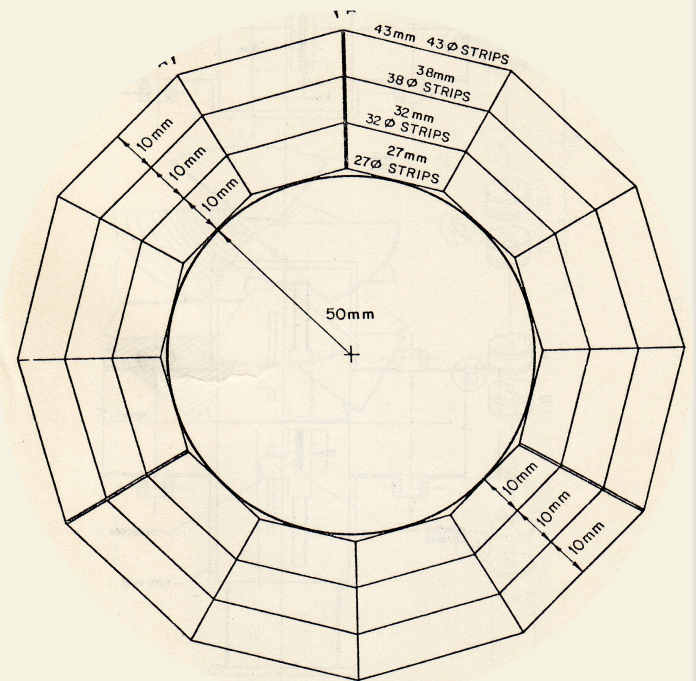
# CDF and the SVX

# SVX: the first CDF micro vertex detector

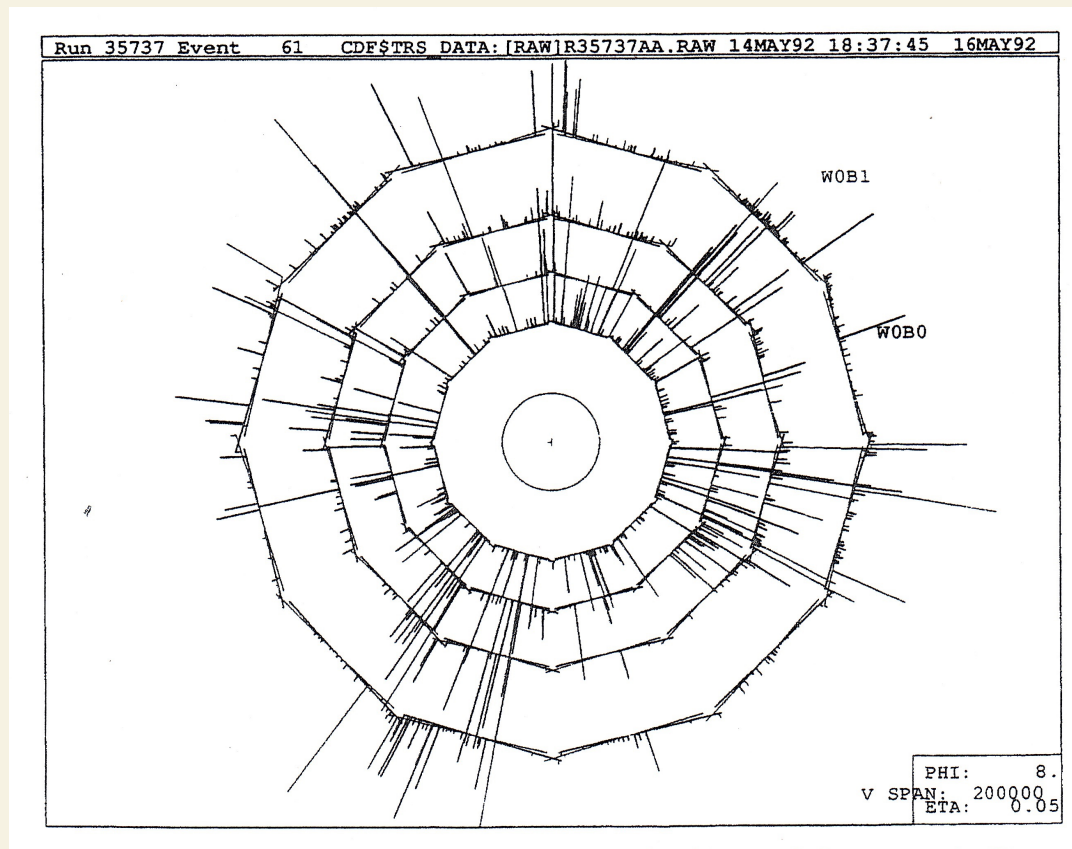
finished in 1991



1981



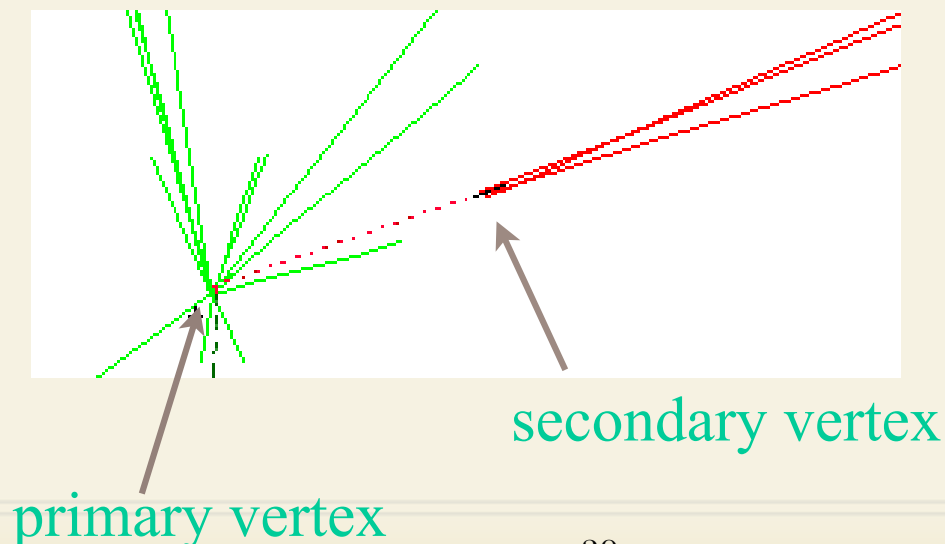
# 1992: particles from collisions are recorded by SVX



will be of crucial importance for the discovery of the Top quark in 1995

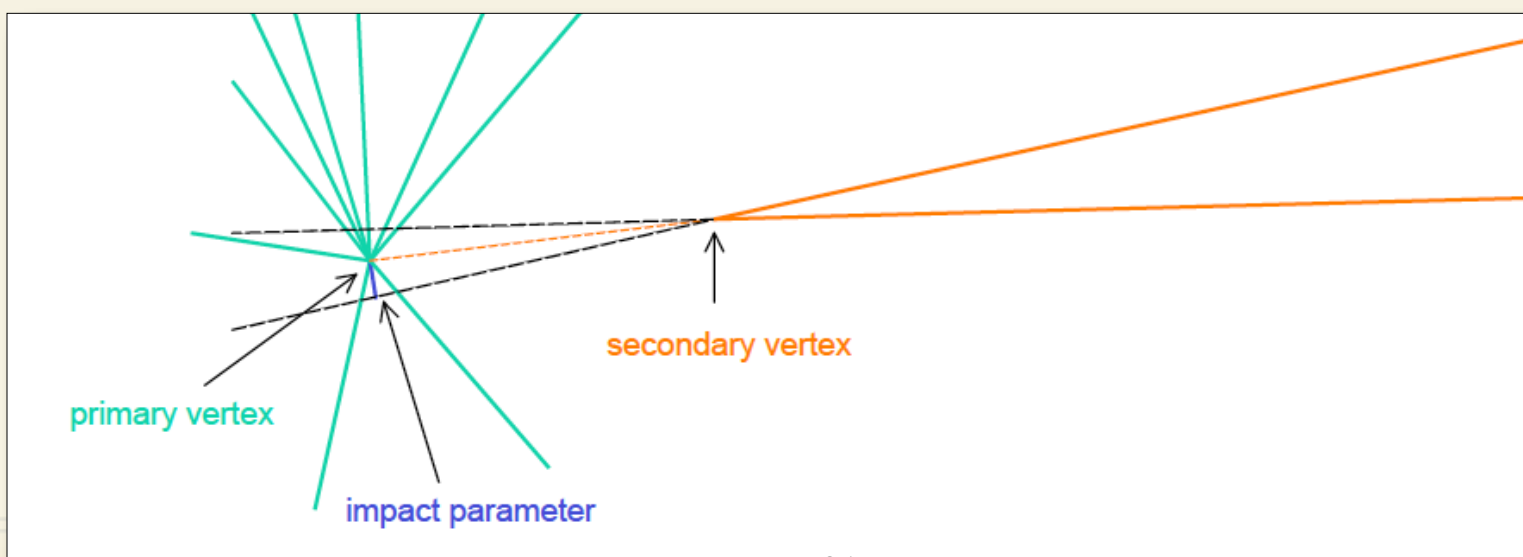
# Heavy Flavor Physics

- ~ at the start of CDF, at the end of the '80s, the first priority was the search for the *Top* quark but...
- ~ quarks with *Charm* and *Beauty* are produced abundantly at the Tevatron and turn out to be extremely interesting too, but they are hard to identify being produced mostly at relatively low transverse momentum
- ~ their main characteristic is a relatively long lifetime which creates *secondary vertices* at distances of the order of millimeters from the collision point



## to trigger on secondary vertices you need to:

- ~ perform **pattern recognition** and sort hits into tracks
- ~ fit all tracks to extract relevant parameters ( $P_T$ ,  $\phi$ ,  $d$ )
- ~ do all this with
  - ~ sufficient **speed** to be used at trigger level ( $\sim 20\mu\text{s}$ )
  - ~ sufficient impact parameter **precision** ( $\sim 40\mu\text{m}$ )





May 1st 1991

CDF/DOC/TRIGGER/PUBLIC/1421

## SVT THE SILICON VERTEX TRACKER

Luciano Ristori

May 1, 1991

### INTRODUCTION

This note describes the architecture of a device we believe we can build to reconstruct tracks in the Silicon Vertex Detector (SVX) with enough speed and accuracy to be used at trigger level 2 to select events containing secondary vertices originated by B decay. We name such a device *Silicon Vertex Tracker* (SVT).

The use of SVT as part of the CDF trigger would allow us to collect a large sample of B's ( $> 10^7$  events) in a  $100 \text{ pb}^{-1}$  run.

B production at 2 TeV in the c.m. is abundant: Isajet predicts that, in the central region, 6.5% of two-jet events with  $P_t > 20 \text{ GeV}/c$  contain a B pair. Thus we need a trigger with a relatively modest rejection factor ( $10 \div 20$ ) not necessarily requiring the presence of very high  $P_T$  tracks.

It turns out that the simple requirement of a single track with an impact parameter greater than a given threshold might do the job.

The possibility to use the output of SVT to actually reconstruct secondary vertices is left open and it's not discussed here.

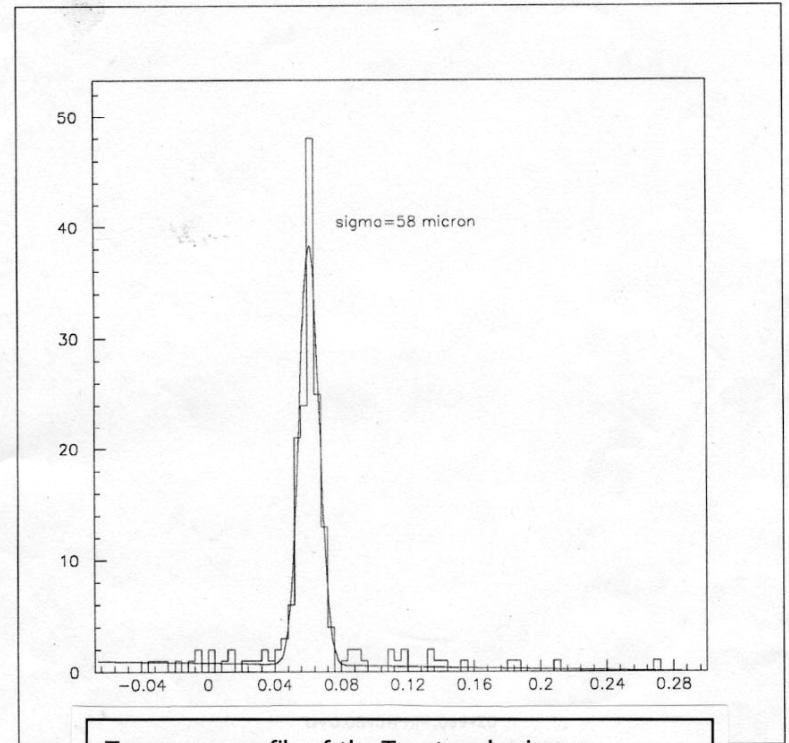
In Section 1 we report the results of some simple simulations we have done to show the efficacy of the impact parameter cut, in Section 2 we overview the overall architecture of SVT, in Section 3 we describe the different parts SVT is made of and how they relate to the different stages the track finding process goes through.

### 1. SIMULATION RESULTS

#### 1.1 Impact Parameter Cut

The impact parameter  $s$  of each track is defined as the minimum

real data + SVT simulation



Transverse profile of the Tevatron luminous region obtained feeding real data from SVX into the simulation of SVT. The sigma of this curve ( $58 \mu\text{m}$ ) is the result of the folding of spot size with impact parameter resolution.

Nov 17, 1992

WEDGE 2

May 1st 1991

CDF/DOC/TRIGGER/PUBLIC/1421

# SVT THE SILICON VERTEX TRACKER

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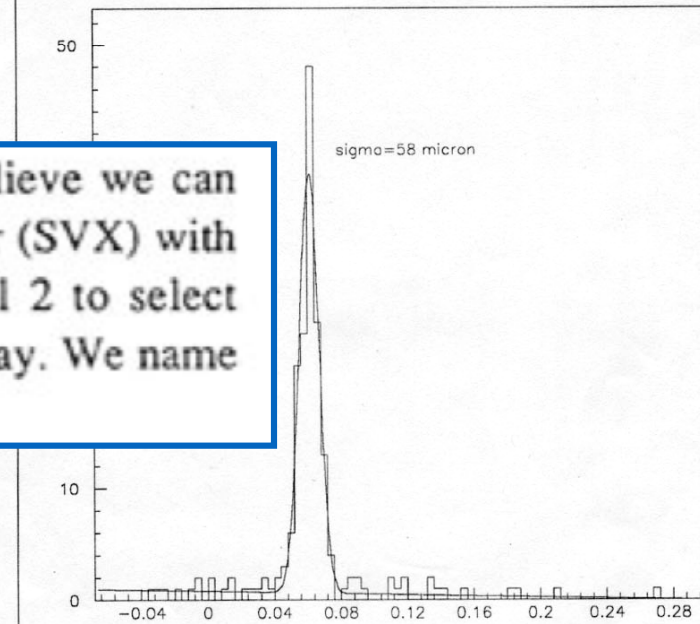
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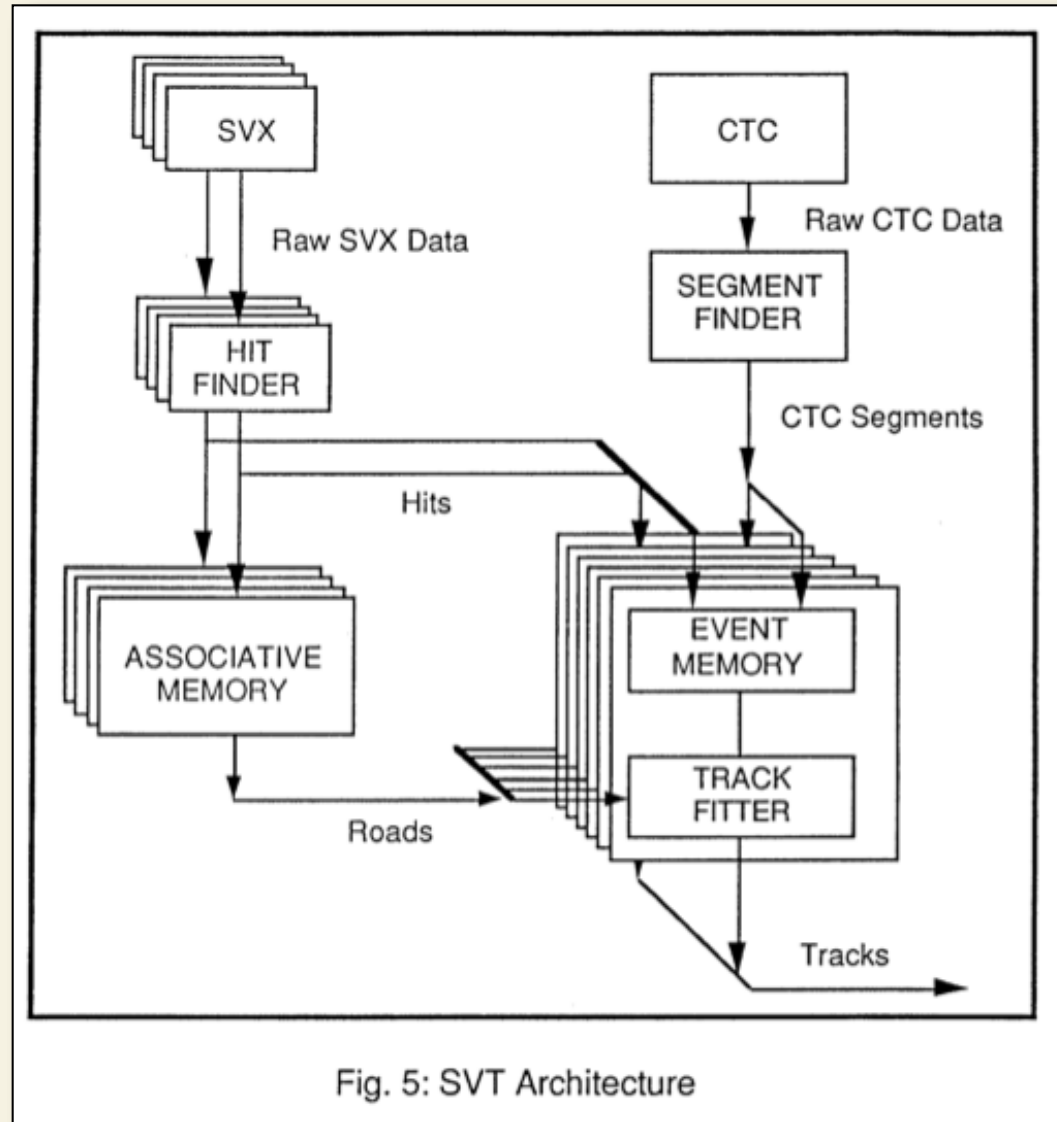


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Nov 17, 1992

WEDGE 2

May 1st 1991





6 coordinates:  $x_1, x_2, x_3, x_4, x_5 (P_T), x_6 (\phi)$

3 parameters to fit:  $P_T, \phi, d$

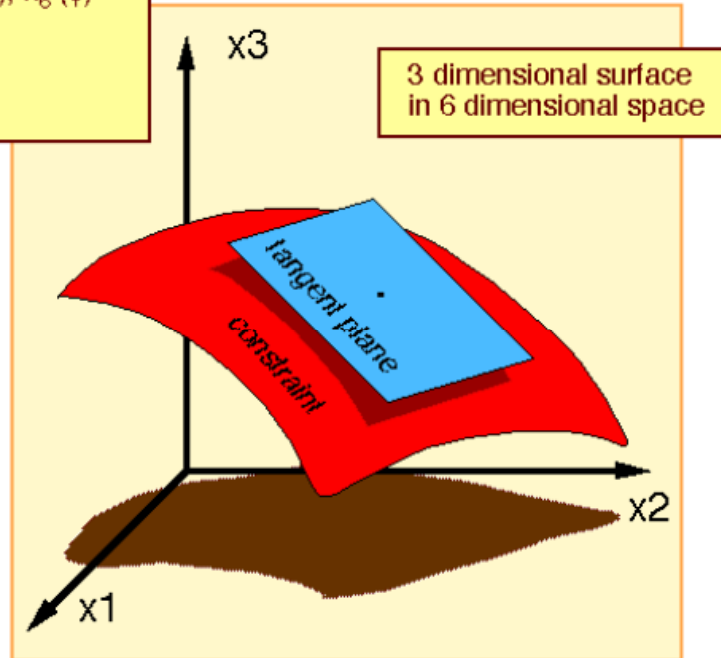
3 constraints

tangent plane:

$$\sum_1^6 a_i x_i = b$$

track parameters:

$$d \approx c_0 + \sum_1^6 c_i x_i$$



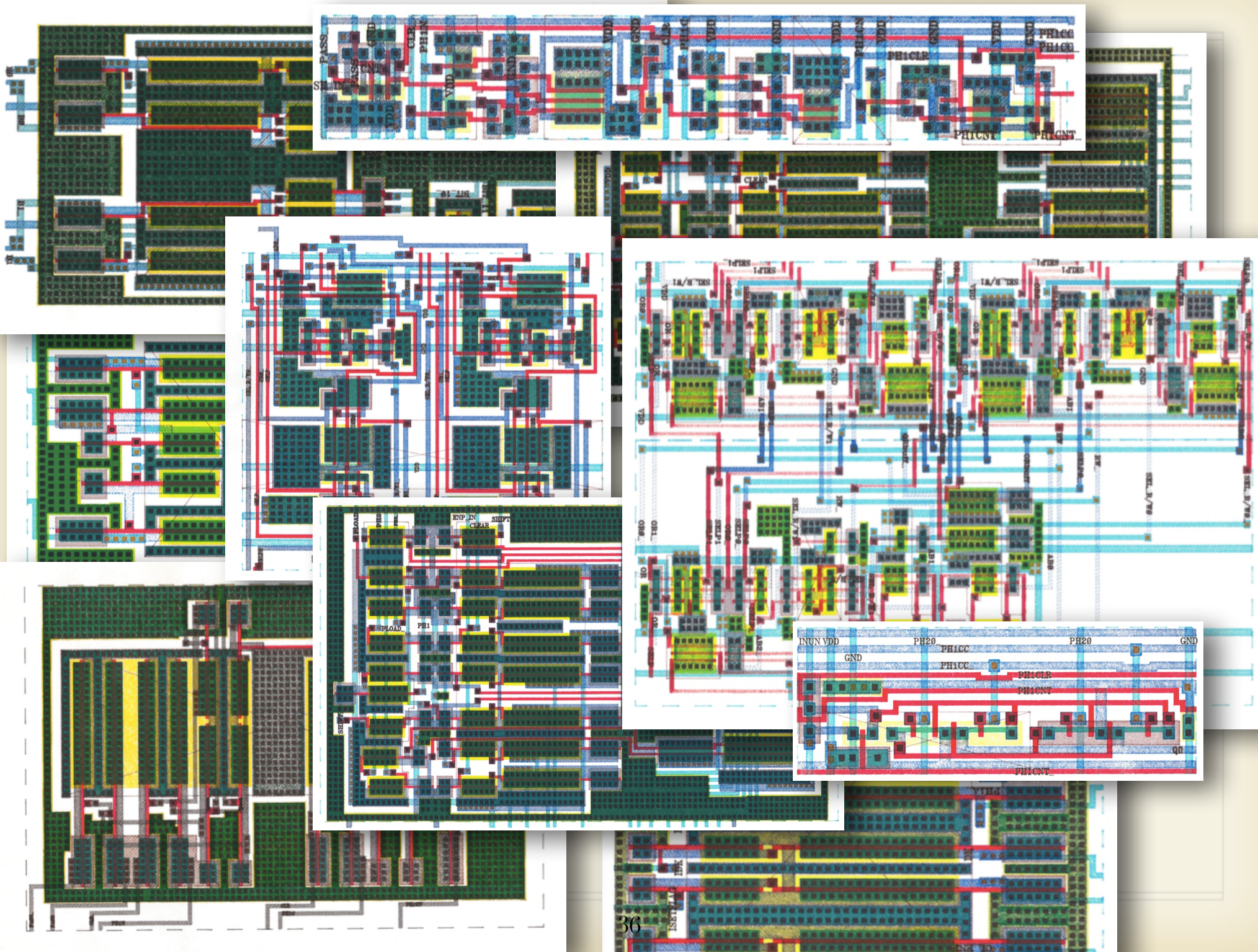
Linear approximation is so good that a single set of constants is sufficient for a whole detector wedge (  $30^\circ$  in  $\phi$  )

linear transformation  
hit coordinates  $\rightarrow$  track parameters

single AM pattern = small volume in phase space

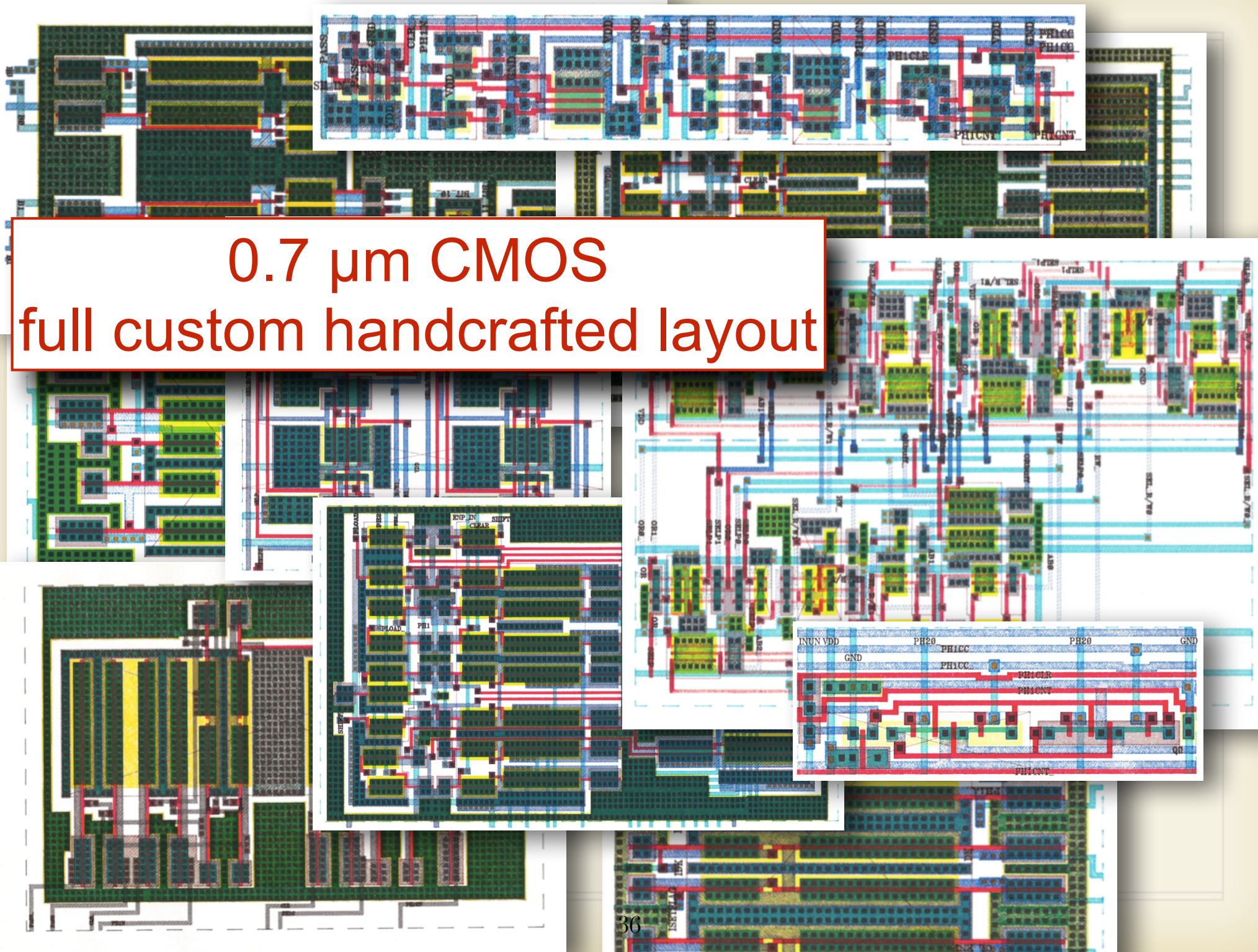
# The AM chip







0.7  $\mu\text{m}$  CMOS  
full custom handcrafted layout







0.7  $\mu\text{m}$  CMOS  
full custom handcrafted layout

150K transistors





0.7  $\mu\text{m}$  CMOS  
full custom handcrafted layout

150K transistors

~10 years development time  
1990-2000



0.7  $\mu\text{m}$  CMOS  
full custom handcrafted layout

150K transistors

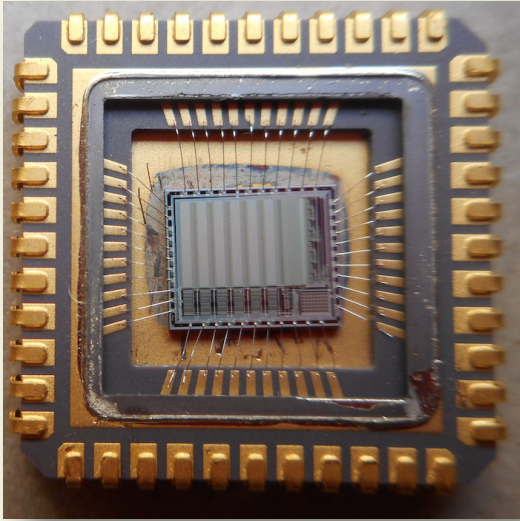


Fabio Morsani

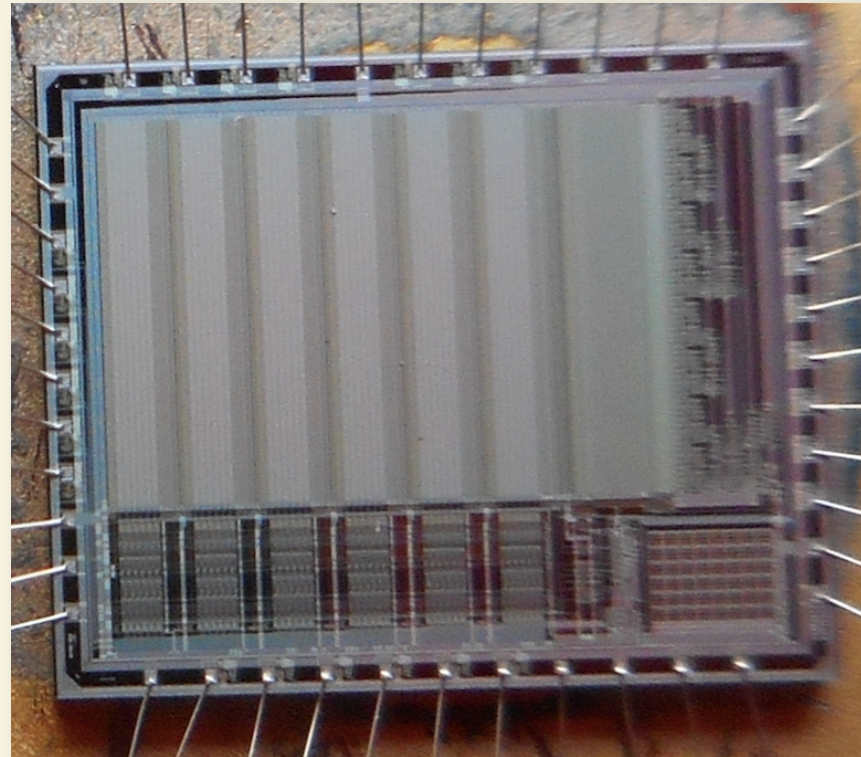
~10 years development time  
1990-2000



First production prototype  
end of 1998

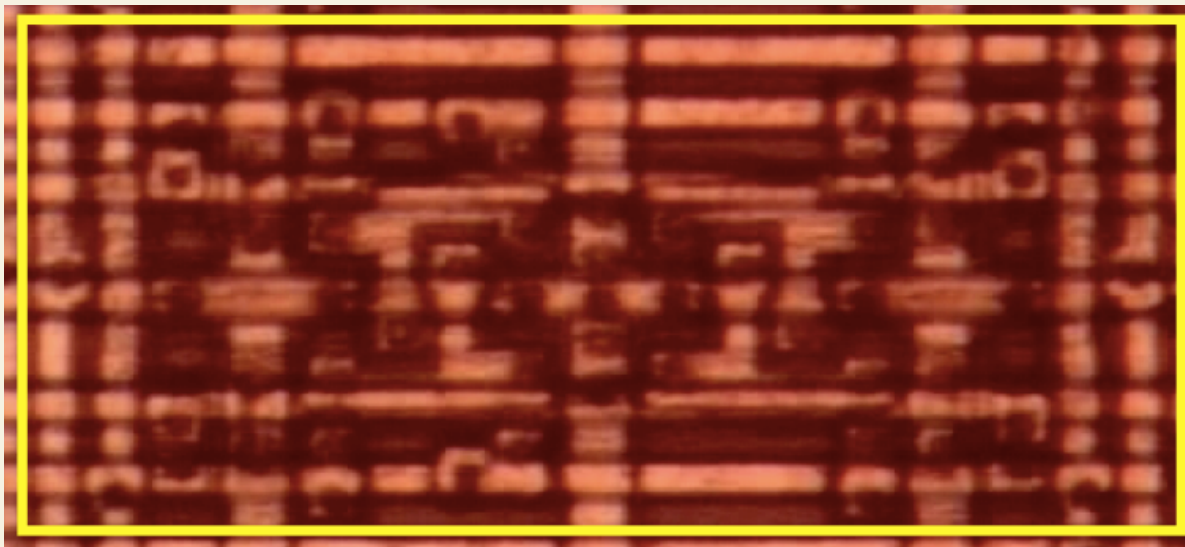
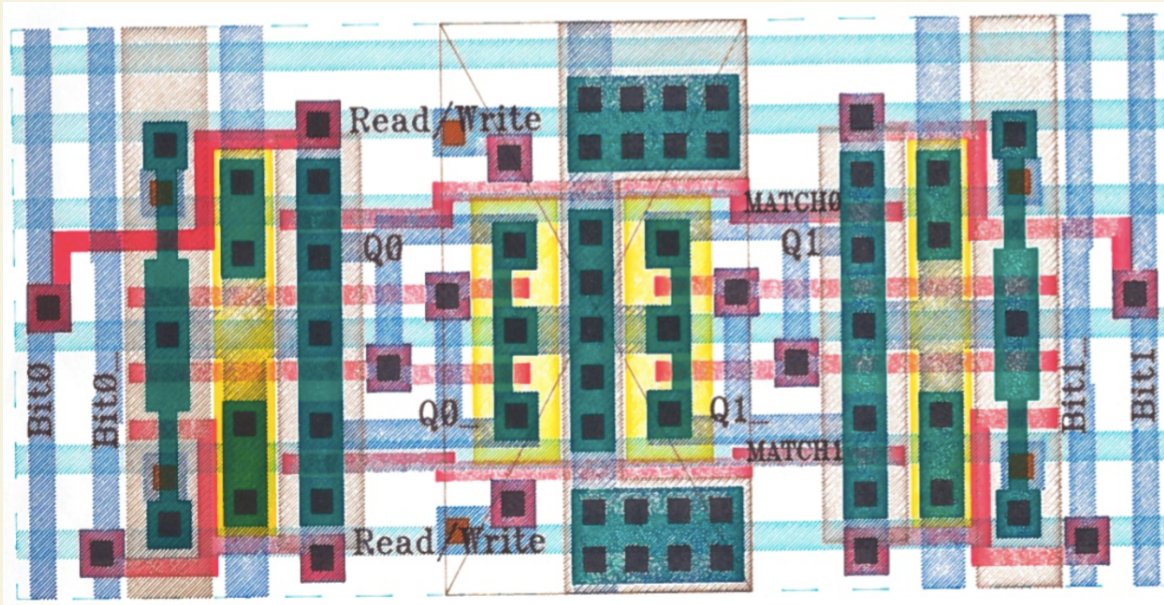


35 mm<sup>2</sup>  
150K transistors

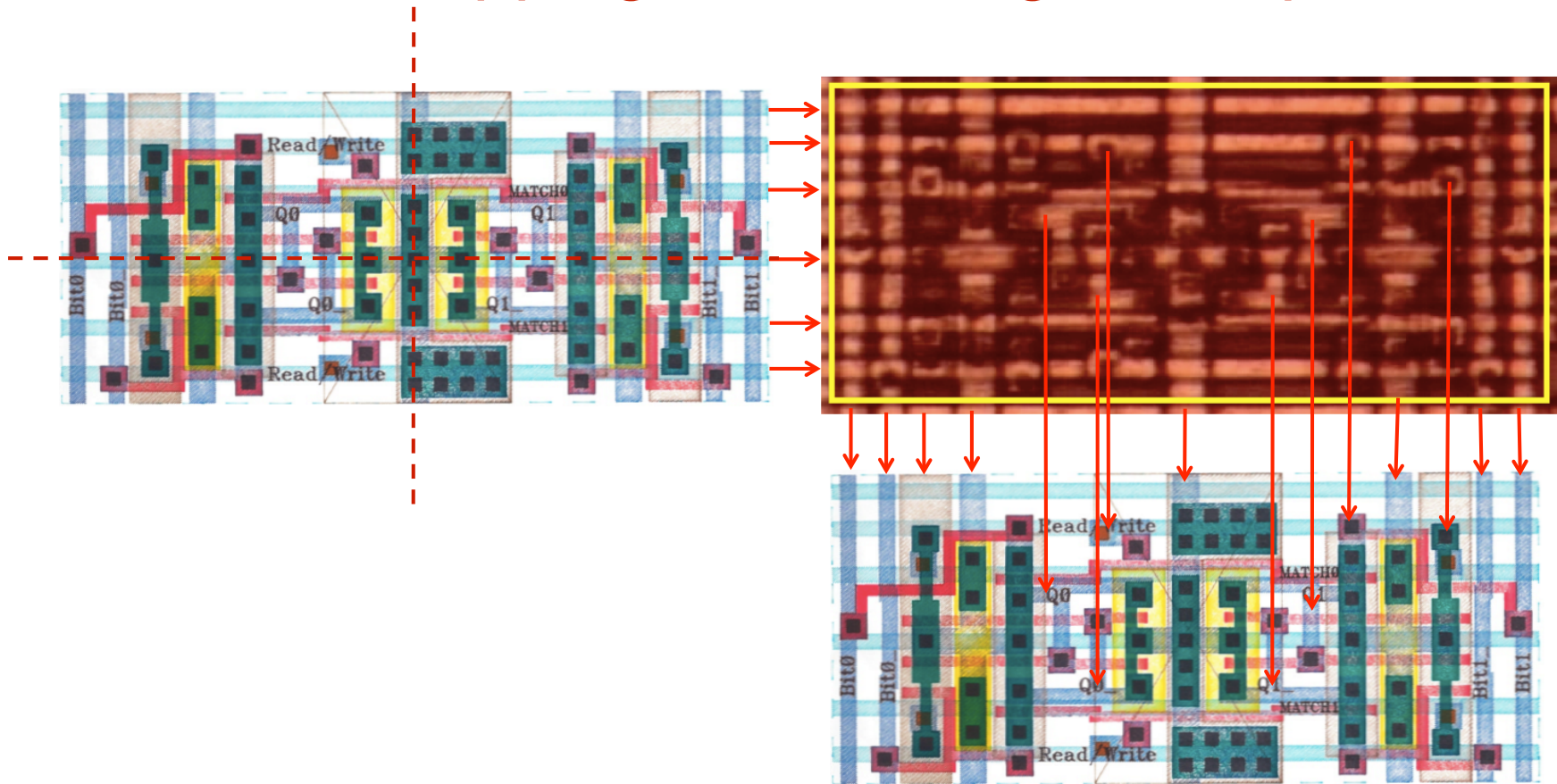




# AM cell: pen plotter drawing and microscope photo



# AM cell: mapping the drawing to the photo







Luciano

Giovanni

Alexei

Fabio

AM board

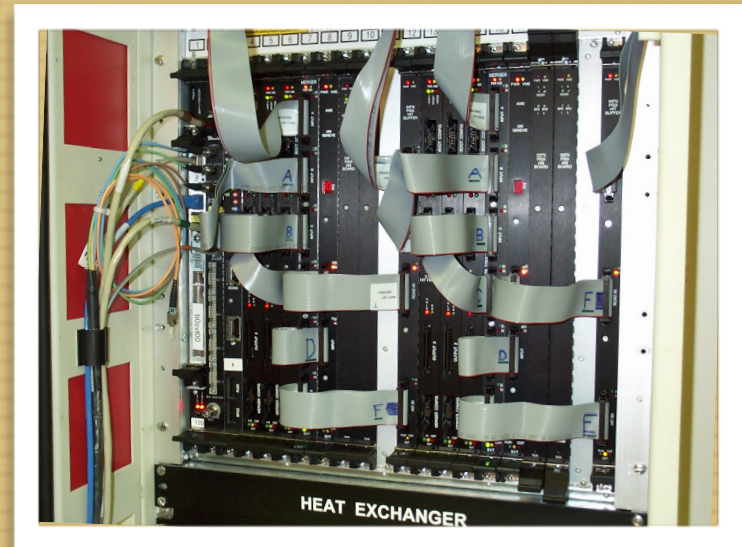
AM chips





August 2000

All SVT boards  
installed in the CDF  
trigger room





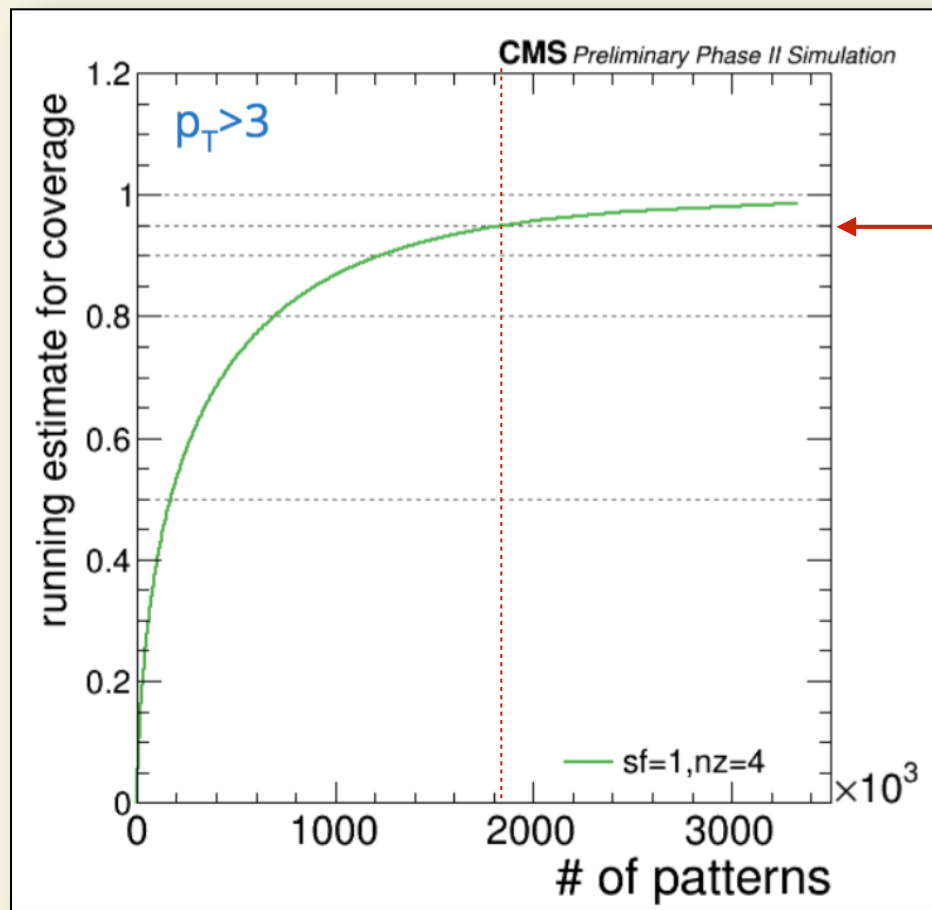
# The Pattern Bank

what do we load in the AM ?

# Building the pattern bank

1. Define superstrips
2. Simulate single tracks from appropriate parameter region
3. Collect all patterns
4. Stop at target **coverage**

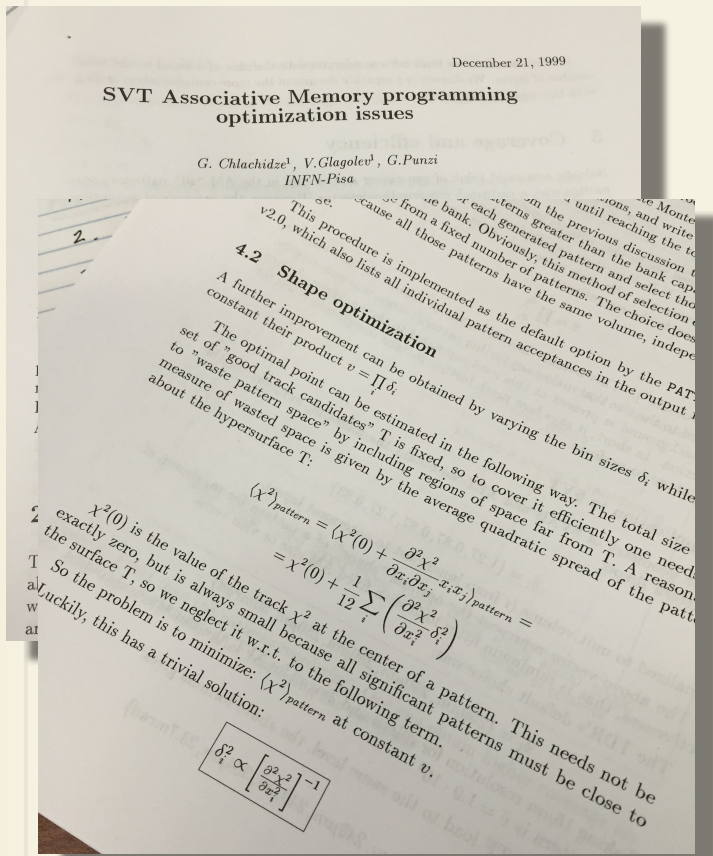
**coverage:**  
fraction of tracks which  
fire a pattern already  
included in the AM





# Superstrip size optimization

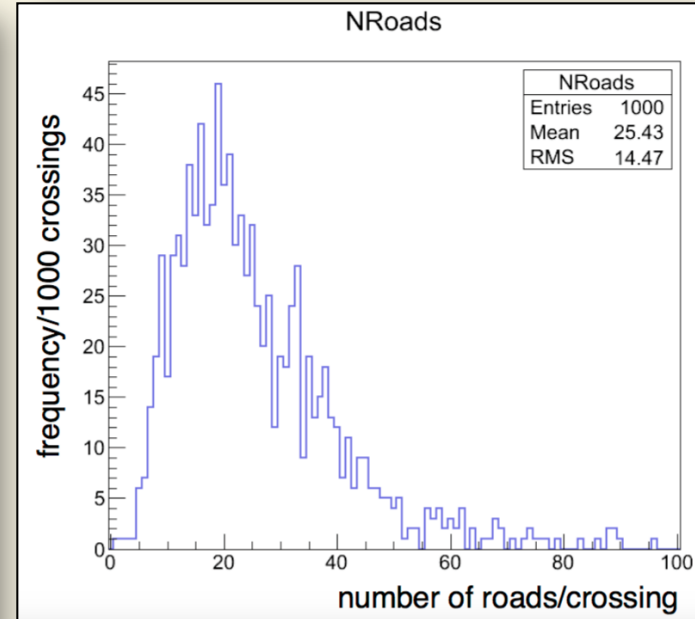
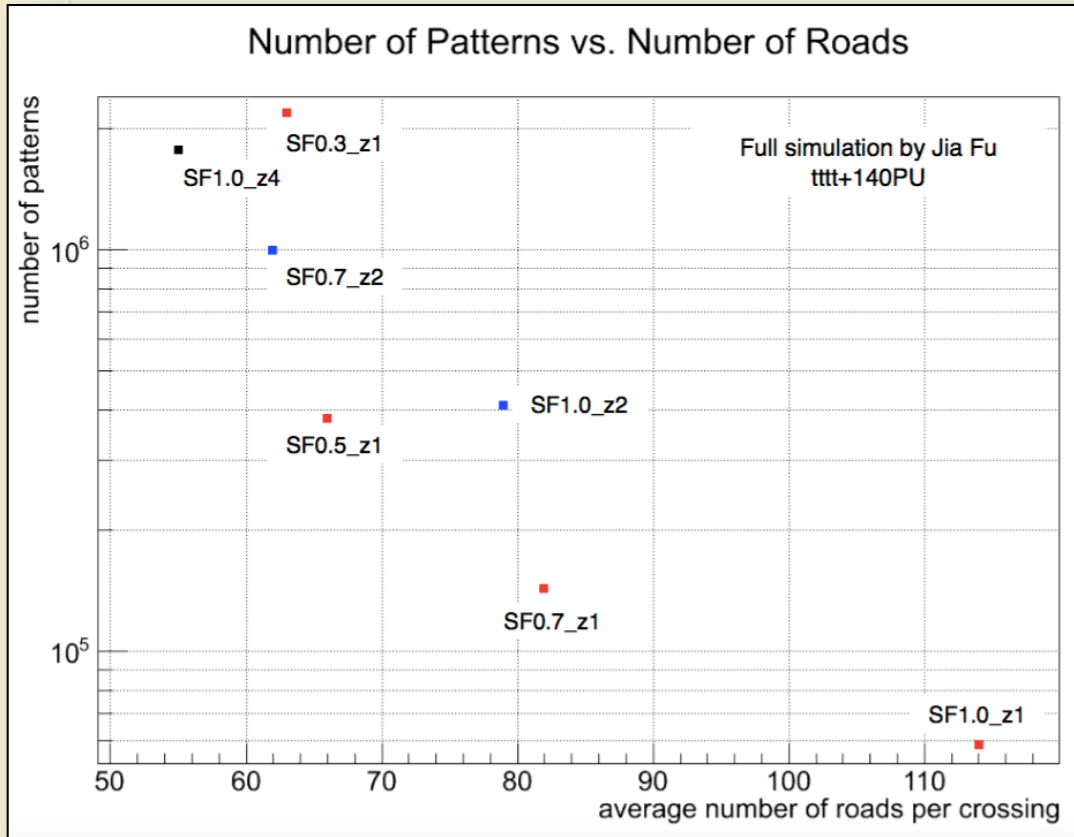
- Goals
  - Maximize coverage
  - Minimize number of patterns
  - Minimize number of roads
- Rules of thumb
  - small occupancy
  - uniform occupancy
  - larger than resolution
- Optimal working point is searched by **trial and error guided by intuition**
- Interesting approximate theory exists but **no exact solution**



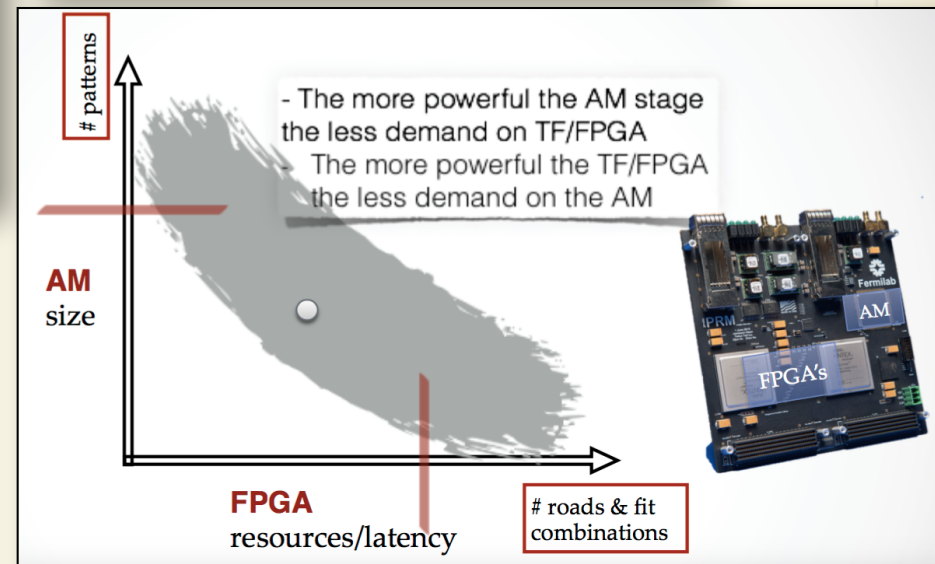
CDF\_5201



# #patterns vs. #roads



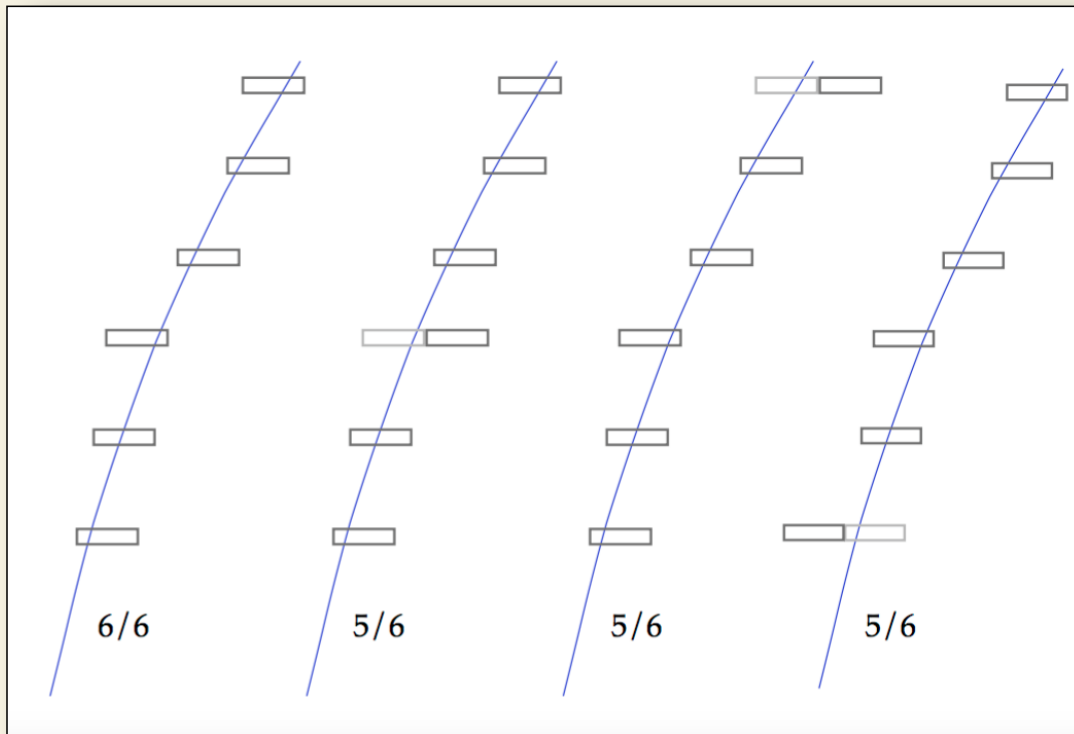
sharing the load



# Majority Logic

allow for missing hits:  
e.g. fire patterns with 5 hits out of 6

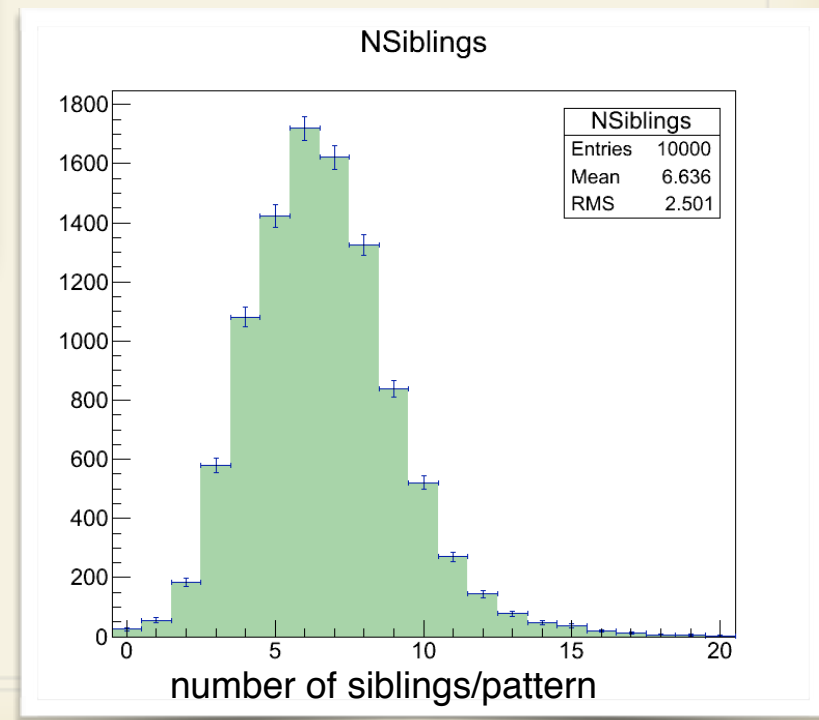
# Siblings and road proliferation



one good 6/6 track also fires several 5/6 patterns

“sibling” = each of two or more patterns differing only in one layer

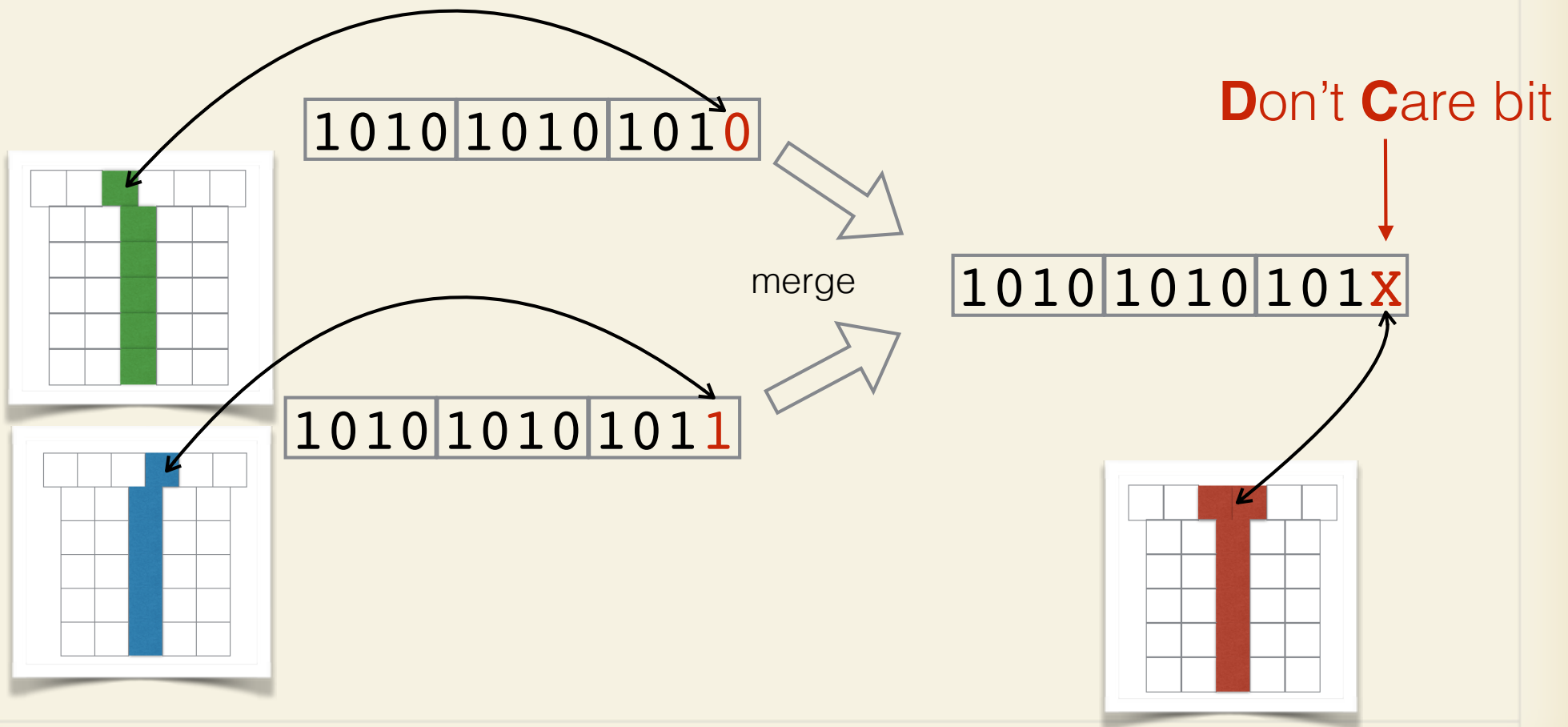
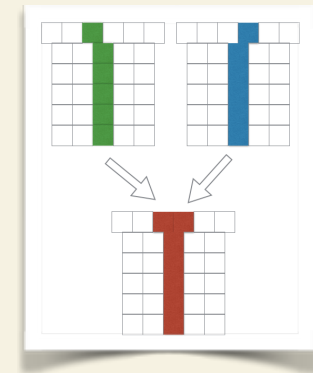
Major cause  
of road proliferation



# Sibling Removal?

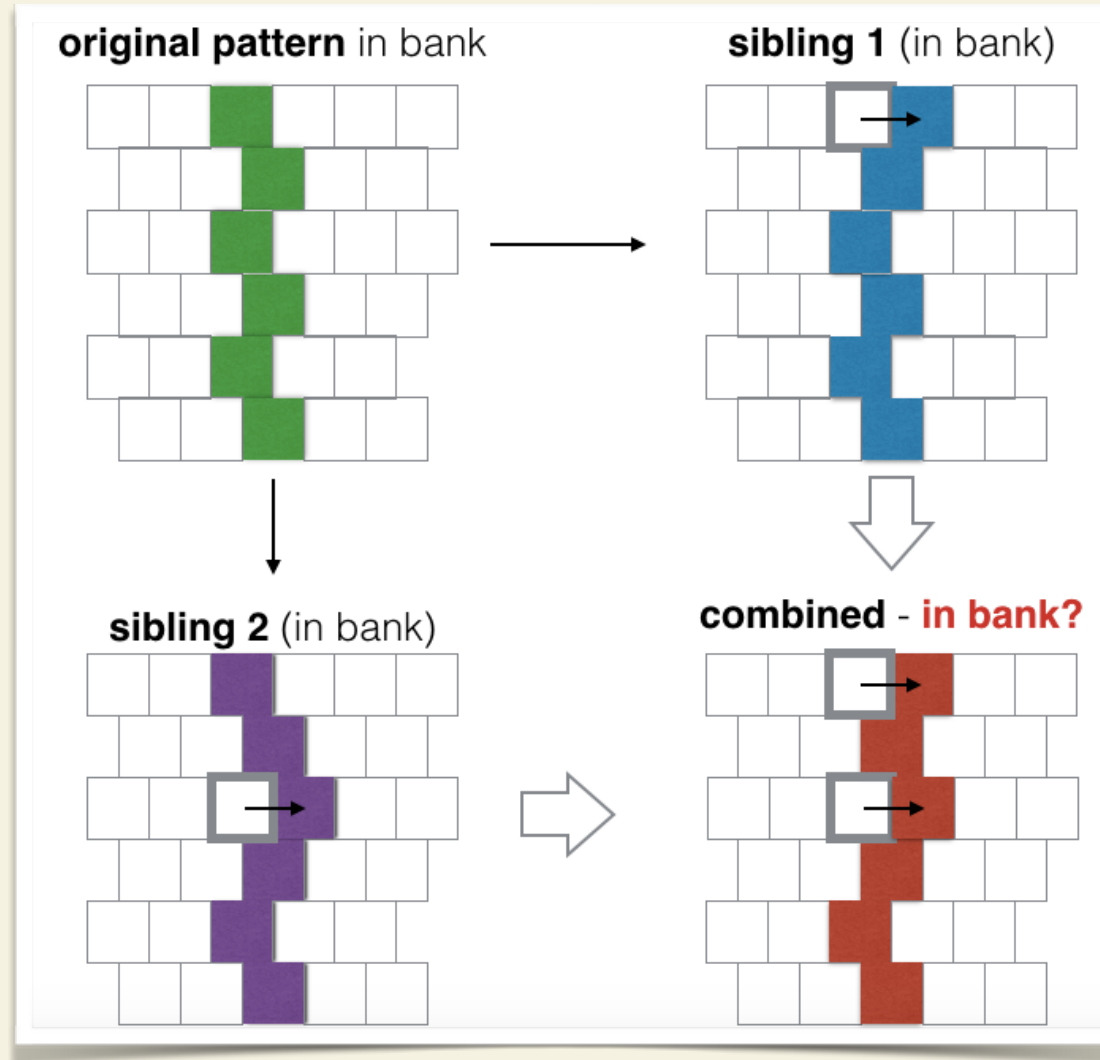
# Merging two siblings

(DC bits introduced in the AM by Atlas-FTK)



# Merge x 4

two siblings in two different layers

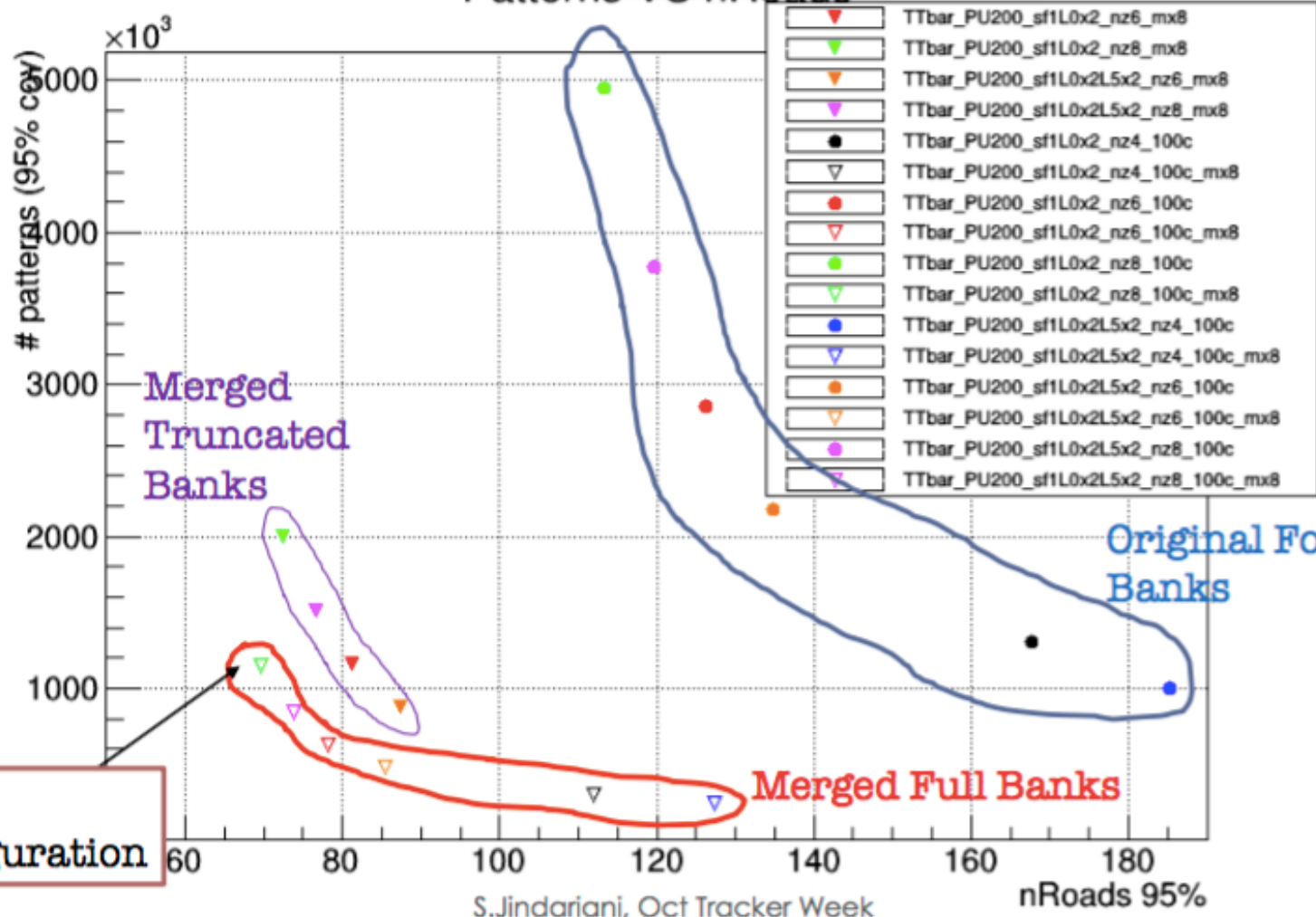


not a sibling  
of the original pattern

# SS Optimization: Patterns VS Roads

TTbar+PU200

↑ Fixed SS banks ↑



Demo Configuration

10/12/16

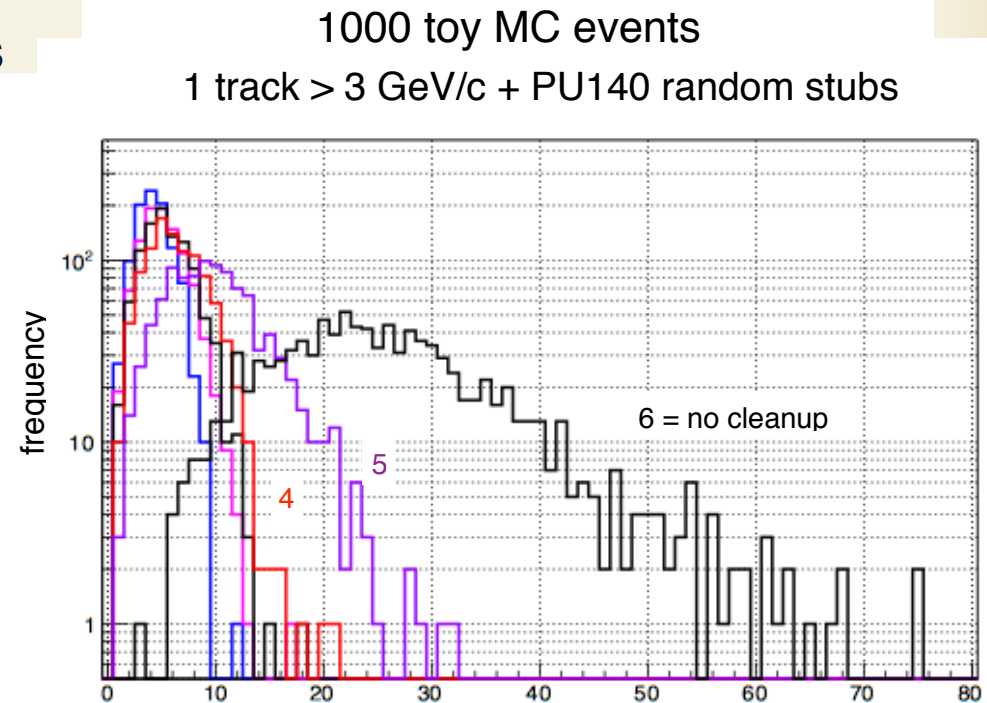
S.Jindariani, Oct Tracker Week

44

# Road Cleanup Algorithm

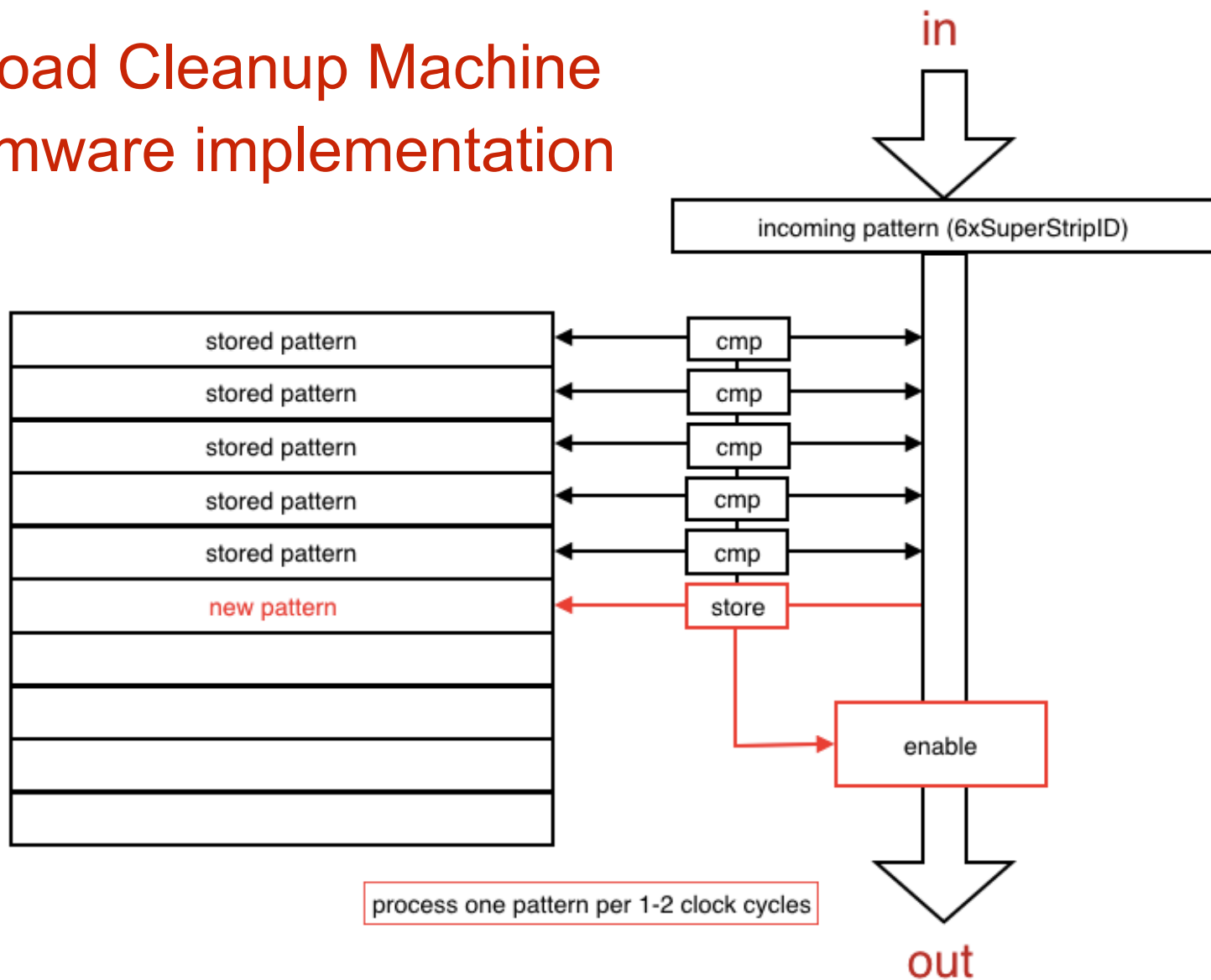
1. Sort roads 6/6 first
2. Output first road and store it in the list of good roads
3. Examine each incoming road sequentially one at a time, compare it to all stored good roads to find if any one has  $n$  or more superstrips in common with this road
4. if yes, just ignore this road
5. if no, output this road and append it to the good road list
6. at end-of-event clear the list of good roads

optimal  $n$  found through simulation





# Road Cleanup Machine firmware implementation

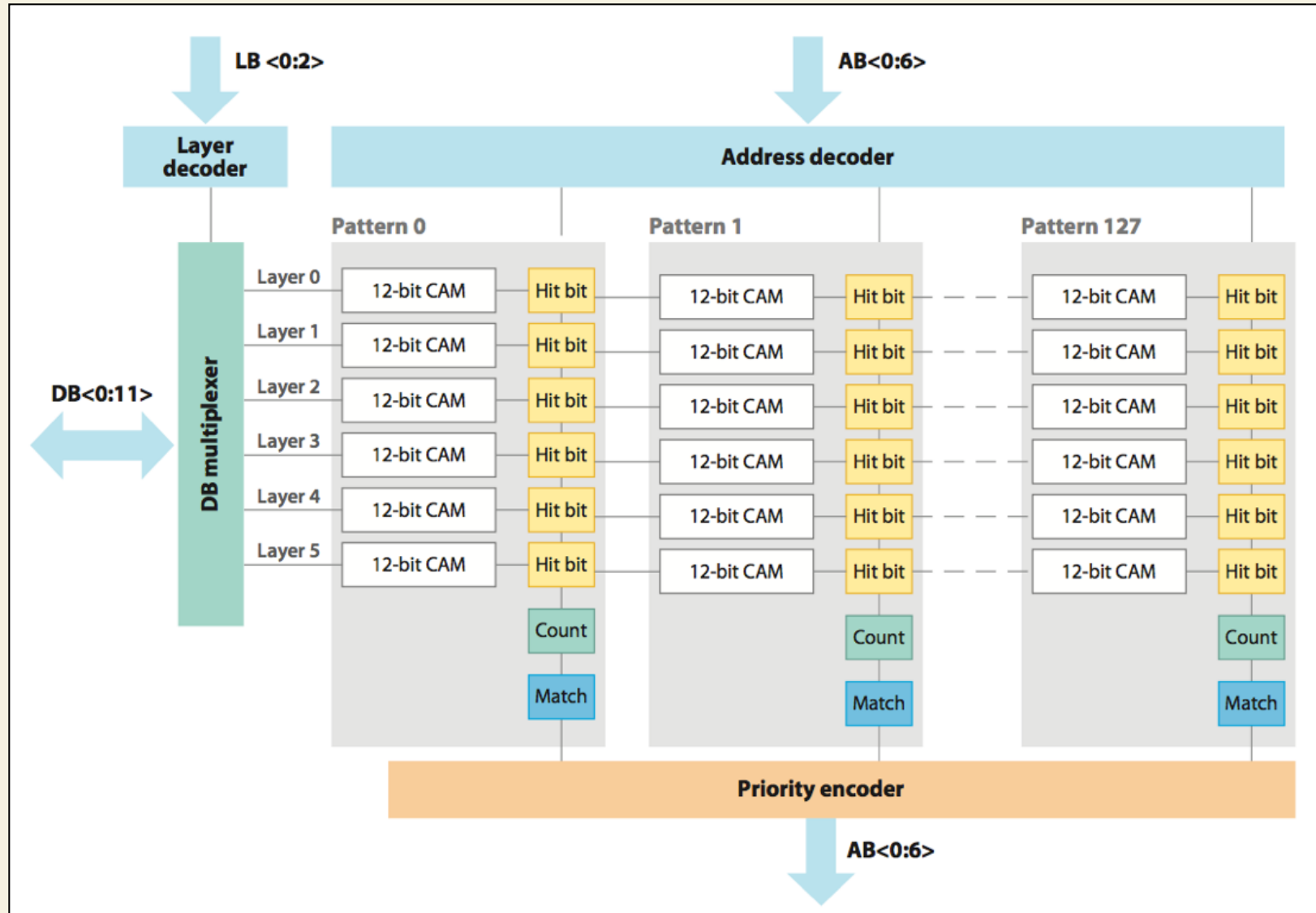


still there might be a better way.....

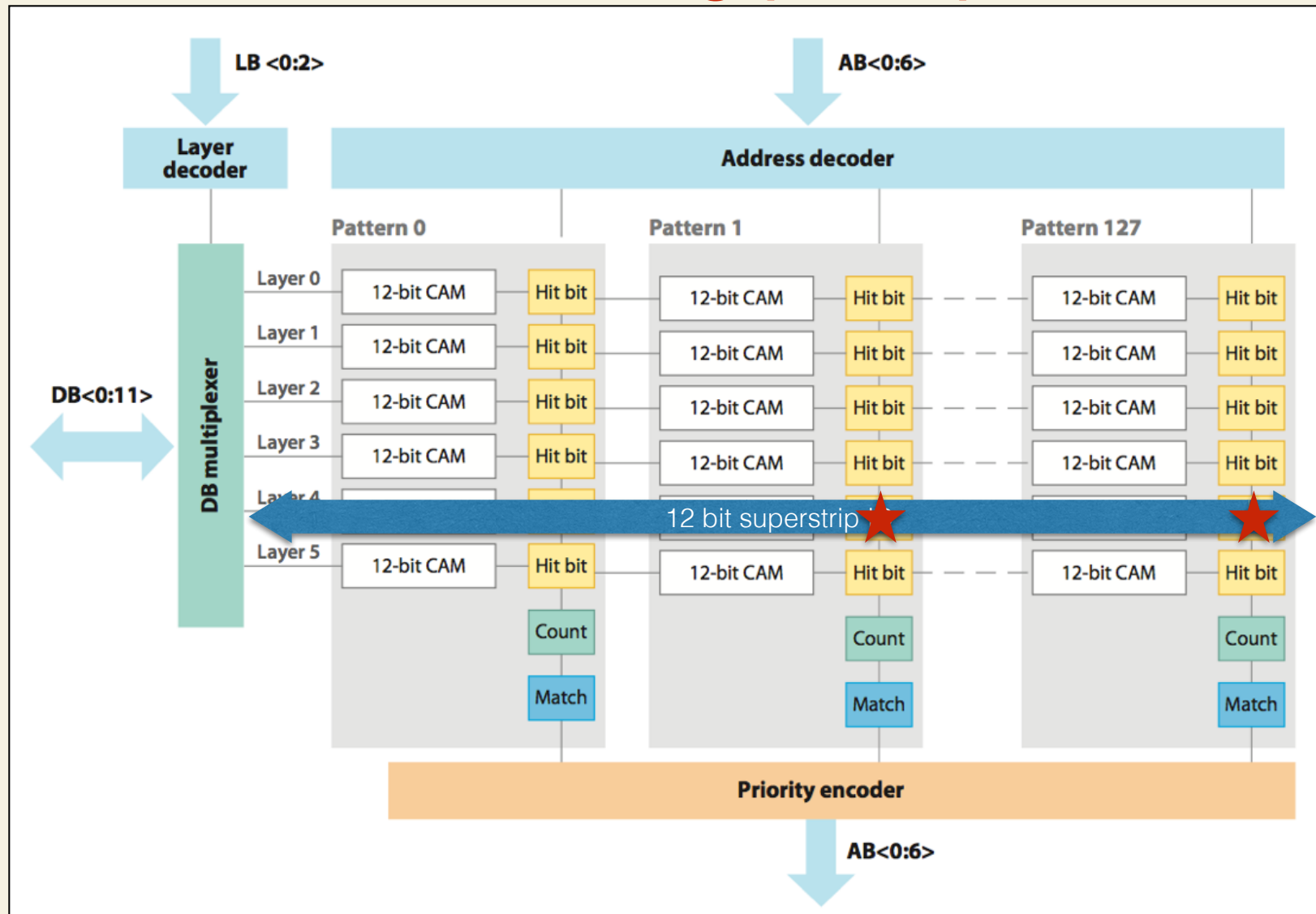
# AM+

a possible solution to  
the road proliferation problem

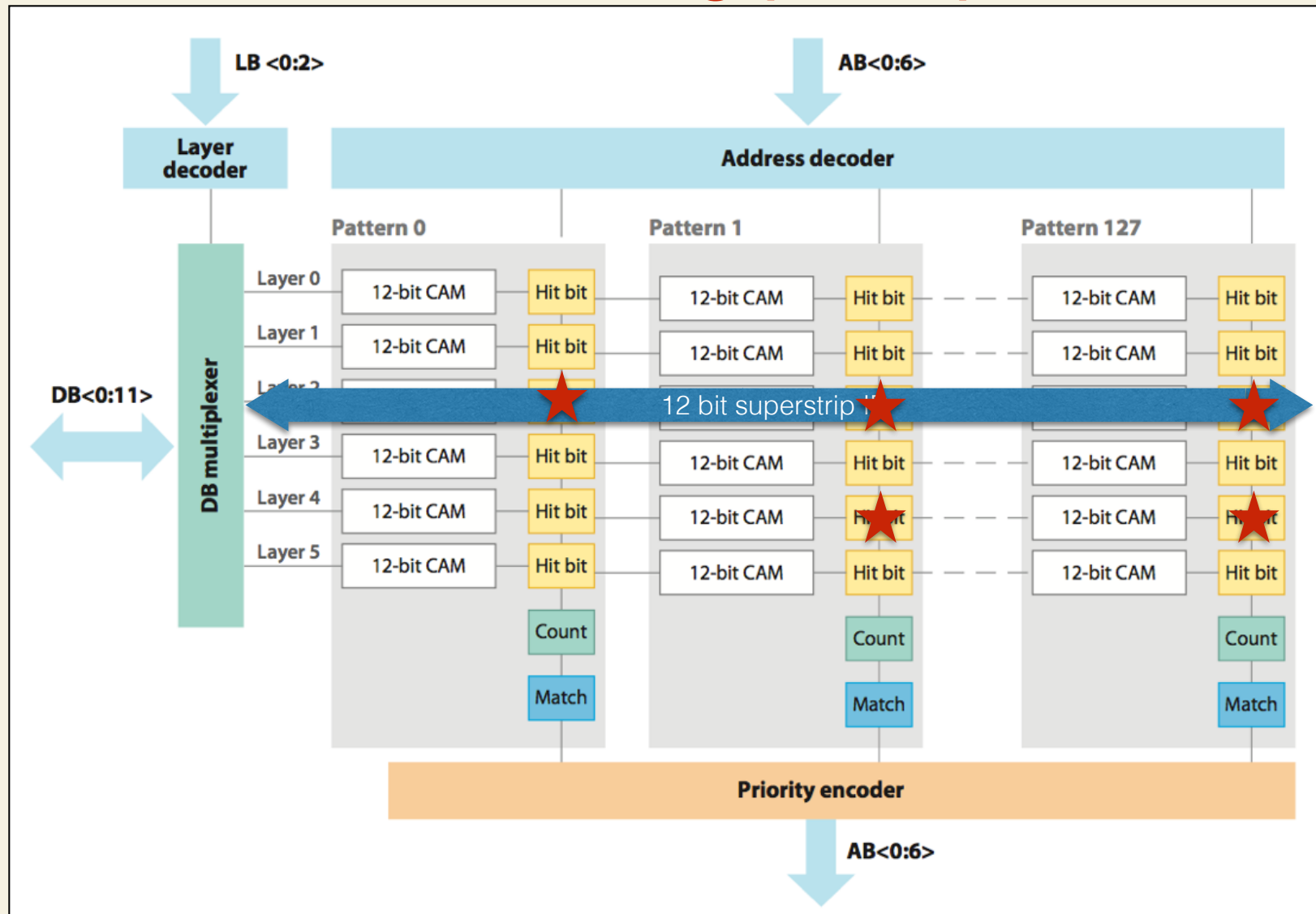
# AM+ working principle



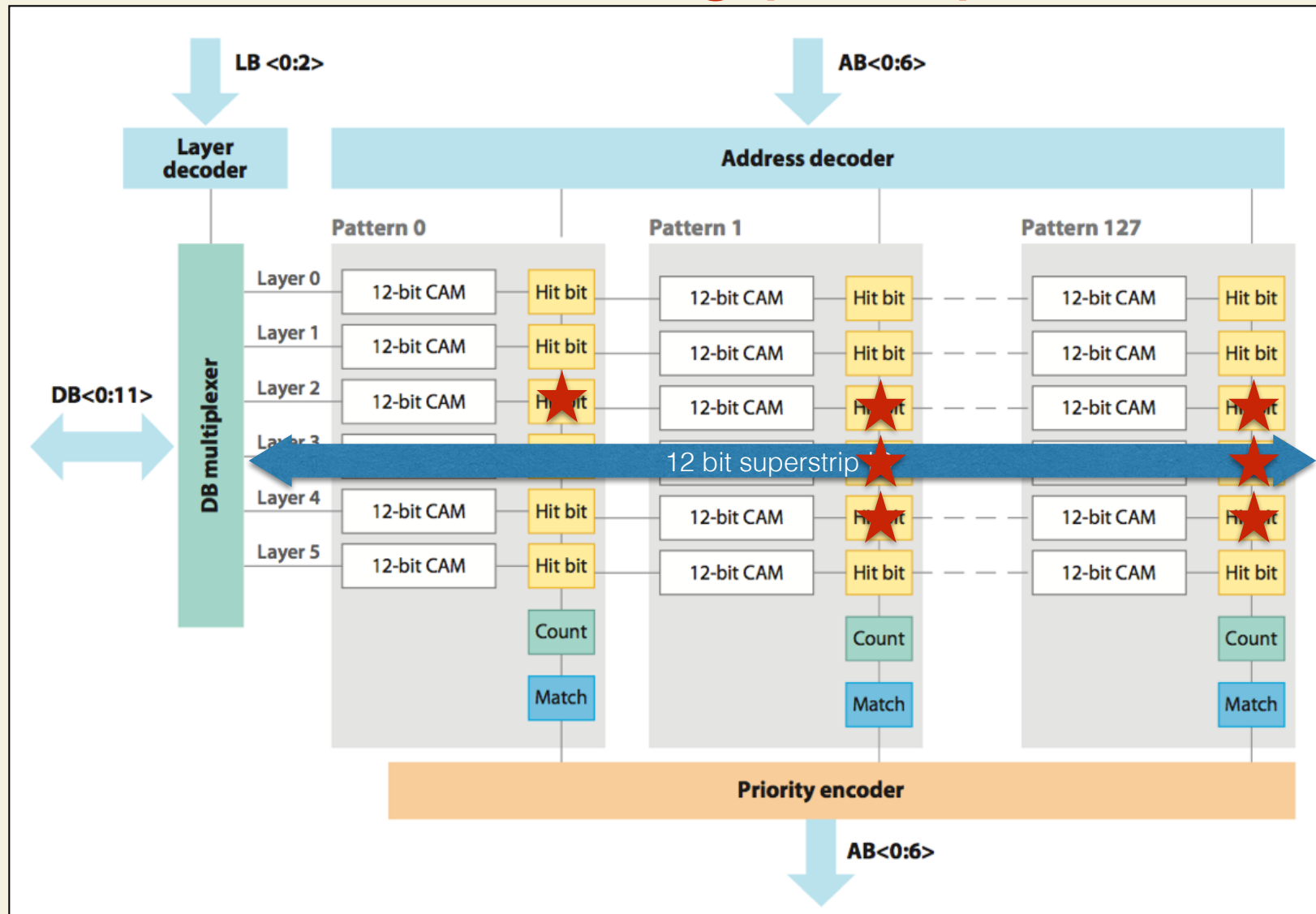
# AM+ working principle



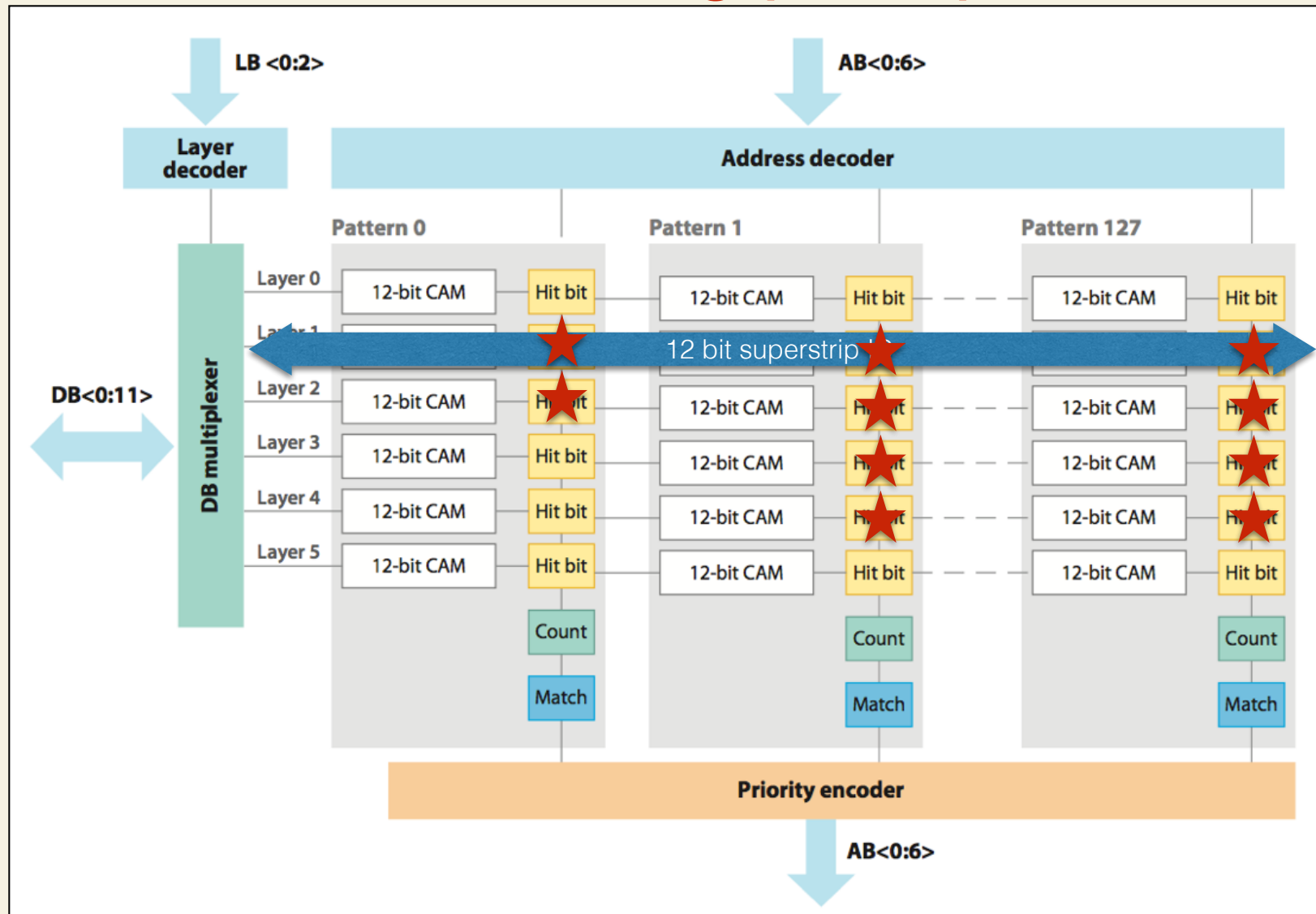
# AM+ working principle



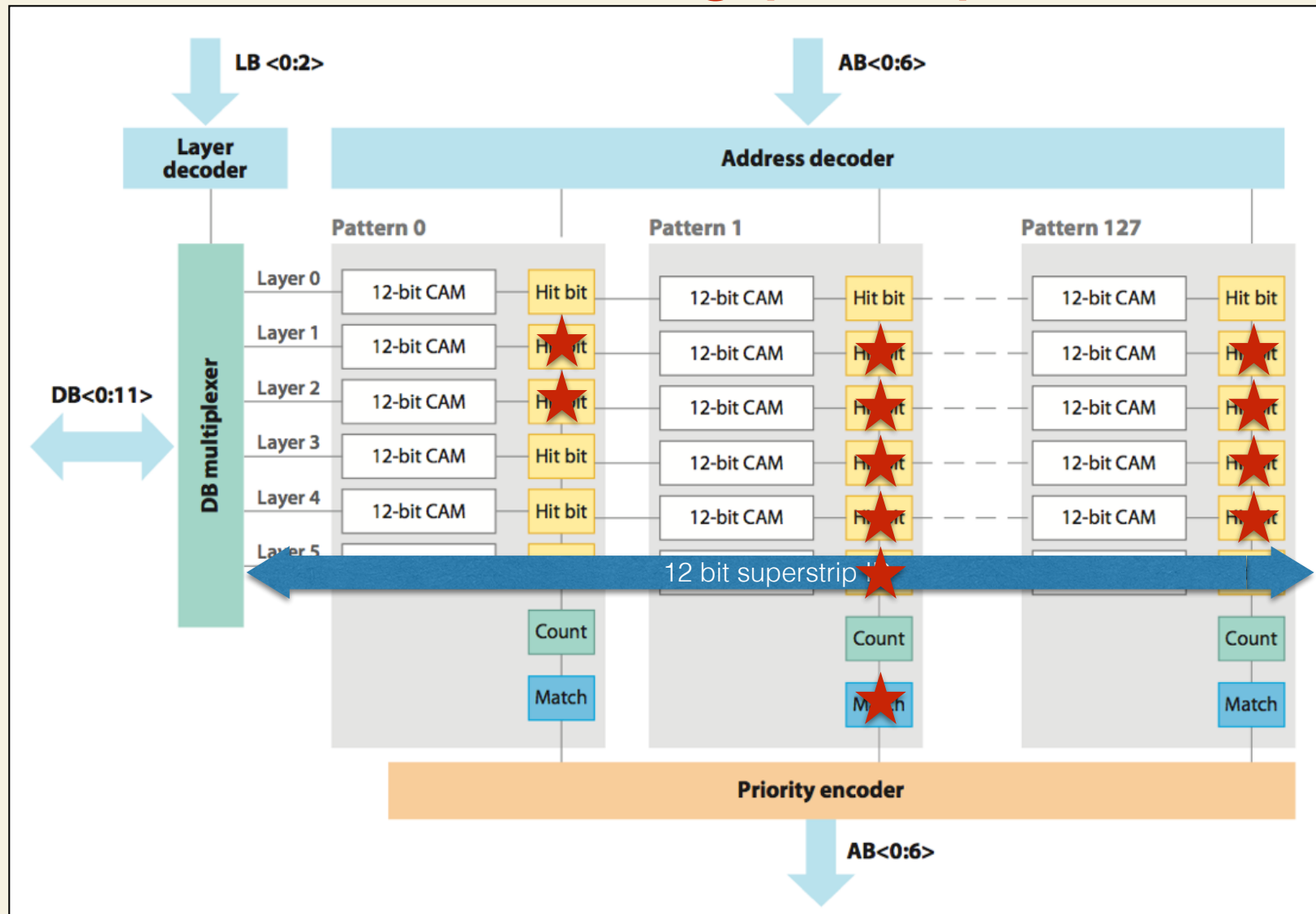
# AM+ working principle



# AM+ working principle

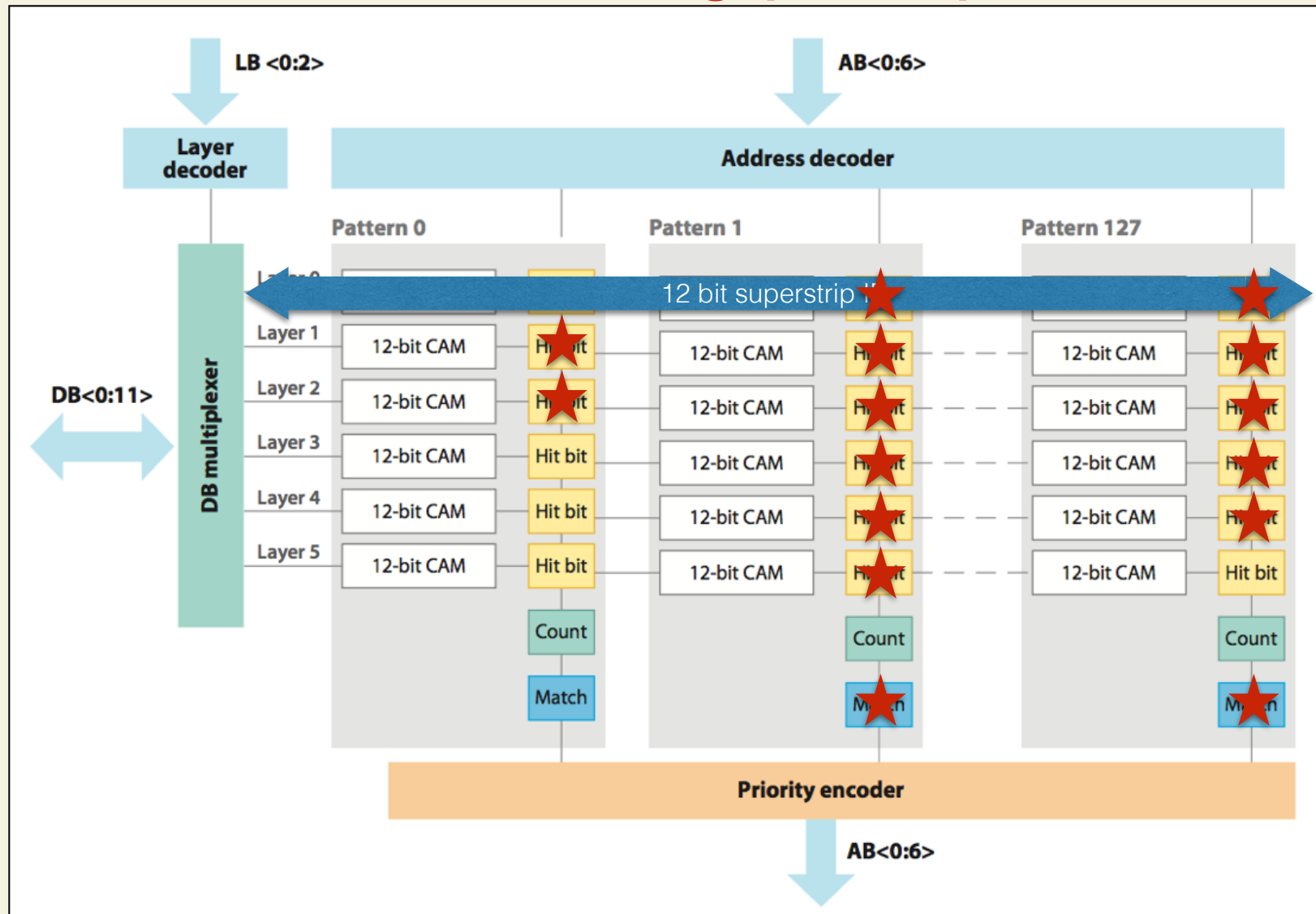


# AM+ working principle

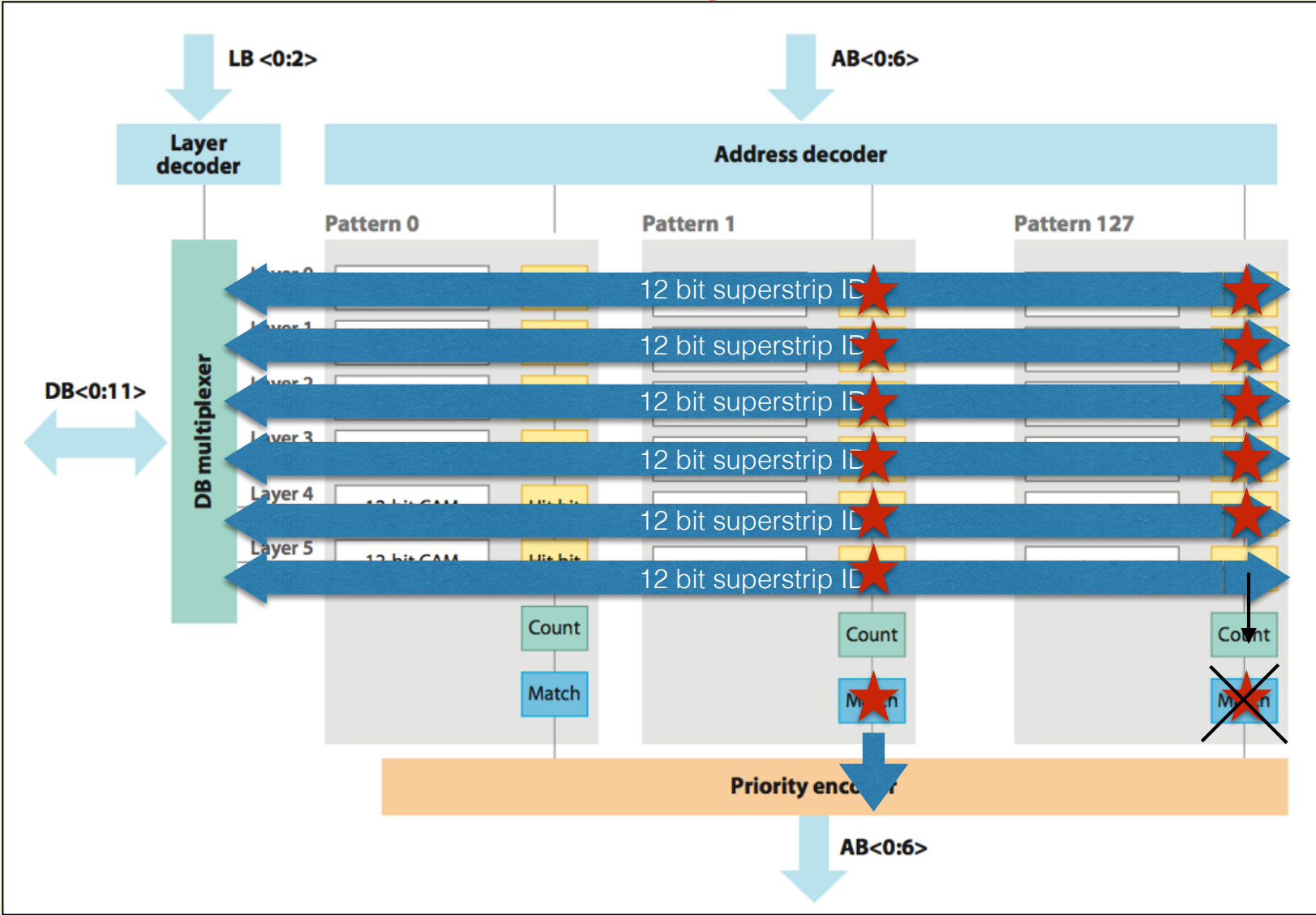




# AM+ working principle



# AM+ working principle



# AM+

- The AM+ can potentially stop the problem of road proliferation due to siblings before it even starts
- 5/6 siblings of a 6/6 track are not even output by the AM saving many precious clock cycles
- Most of the logic needed is already in the current version of the AM
- Simulations indicate that loss in efficiency should be small
- Seems like an interesting possible future development

**That is all  
Thanks for listening**