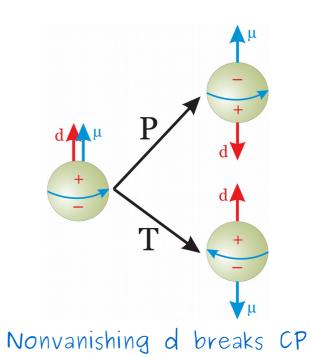
# EFT approach for the electron EDM at two loops

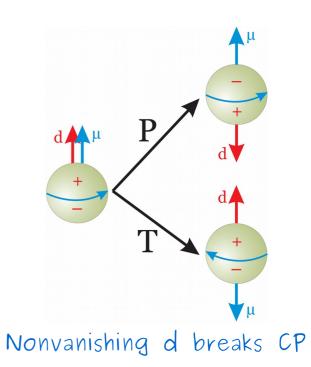
Marc Riembau Université de Genève

NPKI, May 2019

Based on 1810.09413, with Giuliano Panico and Alex Pomarol



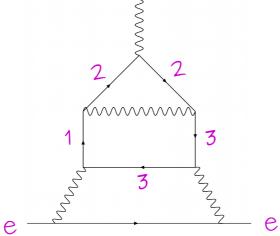
$$\begin{split} H &= -\mu \, \vec{B} \cdot \frac{\vec{S}}{S} \, - \, d \, \vec{E} \cdot \frac{\vec{S}}{S} \\ & \downarrow \quad \text{relativistic limit} \\ \mathcal{L}_{dipole} &= -\frac{\mu}{2} \bar{\Psi} \sigma^{\mu\nu} F_{\mu\nu} \Psi - \frac{d}{2} \bar{\Psi} \sigma^{\mu\nu} i \gamma^5 F_{\mu\nu} \Psi \\ & \downarrow \quad \text{SM} \\ \mathcal{L} \supset \frac{c_W^e}{\Lambda^2} y_e g \, \bar{\ell}_L \sigma_{\mu\nu} e_R \sigma^a H W_{\mu\nu}^a + \frac{c_B^e}{\Lambda^2} y_e g' \, \bar{\ell}_L \sigma_{\mu\nu} e_R H B_{\mu\nu} + h.c. \\ \hline d_e(\mu) &= \frac{\sqrt{2}v}{\Lambda^2} \text{Im} \left[ s_{\theta_W} \, C_{eW}(\mu) - c_{\theta_W} \, C_{eB}(\mu) \right] \end{split}$$



$$3 \rightarrow d_e/e \sim 10^{-40} \ cm$$

SM contribution is ridiculously small, EDM is a clear sign of New Phisics

SM prediction:



3

#### Larger Higgs-Boson-Exchange Terms in the Neutron Electric Dipole Moment

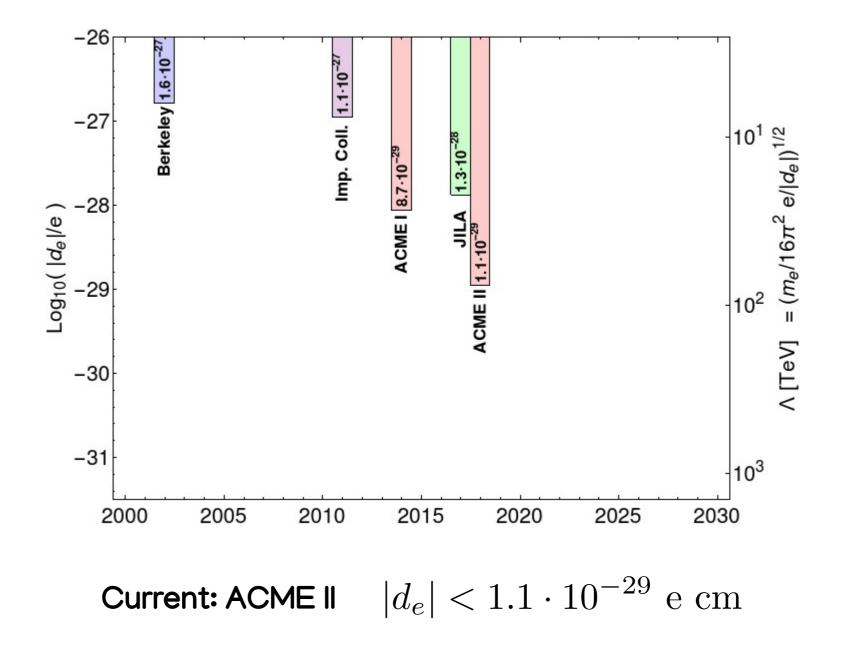
Steven Weinberg

Theory Group, Department of Physics, University of Texas, Austin, Texas 78712 (Received 25 August 1989)

The neutron electric dipole moment  $(d_n)$  due to Higgs-boson exchange is reconsidered, now without assuming that Higgs-boson exchange is solely responsible for  $K_L^0 \rightarrow 2\pi$ . The dominant contribution to  $d_n$  arises from a three-gluon operator, produced in integrating out top quarks and neutral Higgs bosons. The estimated result together with current experimental bounds on  $d_n$  show, even for the largest plausible Higgs-boson masses, that *CP* is not maximally violated in neutral-Higgs-boson exchange.

This is very large compared with other contributions, and potentially in conflict with the experimental results for  $d_n$ ,  $(-14\pm 6)\times 10^{-26} e \text{ cm}$  from Leningrad<sup>20</sup> and  $(-3\pm 5)\times 10^{-26} e \text{ cm}$  from Grenoble.<sup>21</sup> We do not know  $m_H$  or  $m_t$ , but the experimental lower bound on  $m_t$ is rapidly increasing, and it is hard to imagine that  $m_H$ could be larger than  $10m_t$ . This gives<sup>15</sup> h > 0.015. The experimental bound<sup>21</sup>  $|d_n| < 1.2 \times 10^{-25} e \text{ cm}$  thus requires that  $|\text{Im}Z_2| < 8 \times 10^{-5}$ . Our conclusion is that *CP* is not maximally violated in the neutral Higgs sector.<sup>14</sup> The only way that I can see for this to be natural is for the Higgs sector to be very simple: no more than two doublets, and with two doublets, no mixing with any scalar singlets.

# **Evolution of electron EDM constraints**



Translation of ACME constraints to particle physics:

$$\frac{d_e}{e} \sim \frac{1}{(16\pi^2)^2} \frac{m_e}{\Lambda^2} \longrightarrow \Lambda > 3 \,\mathrm{TeV}$$

Relevant constraints even at two loops.

We want to characterize all effects that enter with

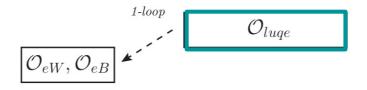
Two loops

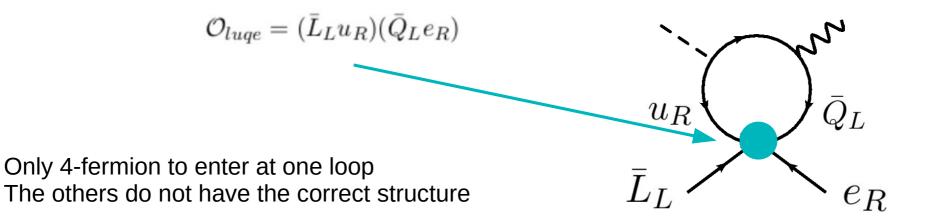
Chirality flip

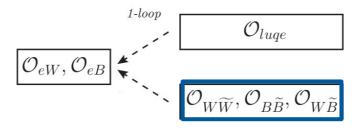


This is the key to help organize the contributions









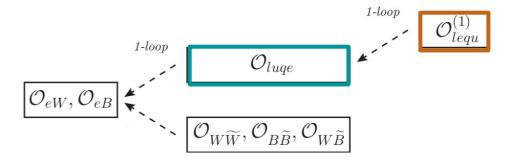
$$\frac{d}{d\ln\mu} \operatorname{Im} \begin{pmatrix} C_{eB} \\ C_{eW} \end{pmatrix} = -\frac{y_e g}{16\pi^2} \begin{pmatrix} 0 & 2t_{\theta_W}(Y_L + Y_e) & \frac{3}{2} \\ 1 & 0 & t_{\theta_W}(Y_L + Y_e) \end{pmatrix} \begin{pmatrix} C_{W\widetilde{W}} \\ C_{B\widetilde{B}} \\ C_{W\widetilde{B}} \end{pmatrix}$$

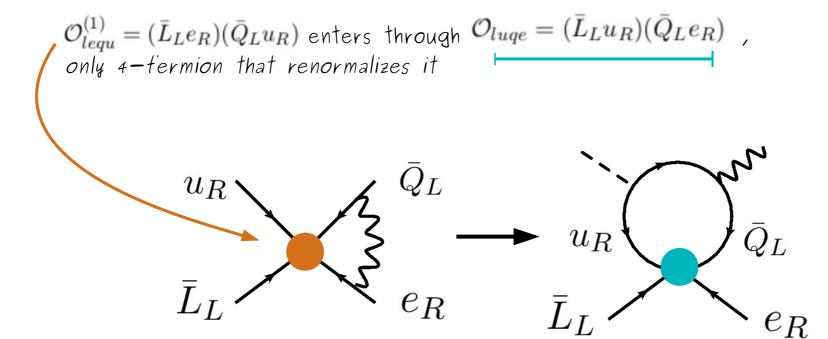
$$\downarrow \quad \text{It is useful to write the parameters} \quad \text{in a more physical way}$$

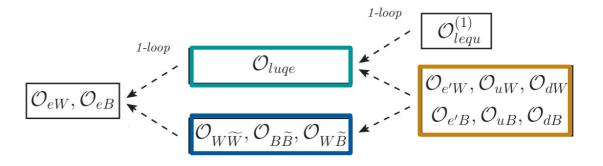
$$\frac{vh}{\Lambda^2} \left( \tilde{\kappa}_{\gamma\gamma} F_{\mu\nu} \widetilde{F}^{\mu\nu} + 2\tilde{\kappa}_{\gamma Z} F_{\mu\nu} \widetilde{Z}^{\mu\nu} \right) + ie\delta \tilde{\kappa}_{\gamma} W^+_{\mu} W^-_{\nu} \widetilde{F}^{\mu\nu}$$

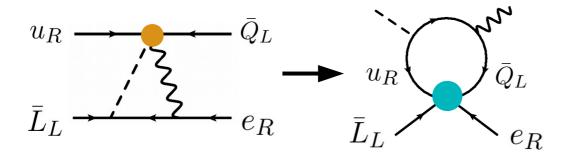
$$\frac{d}{d\ln\mu} d_e(\mu) = \frac{e}{8\pi^2} \frac{m_e}{\Lambda^2} \left[ 4Q_e \tilde{\kappa}_{\gamma\gamma} - \frac{4}{s_{2\theta_W}} \left( \frac{1}{2} + 2Q_e s^2_{\theta_W} \right) \tilde{\kappa}_{\gamma Z} + \frac{\Lambda^2}{v^2} \delta \tilde{\kappa}_{\gamma} \right] \quad \overline{L} \qquad e_R$$

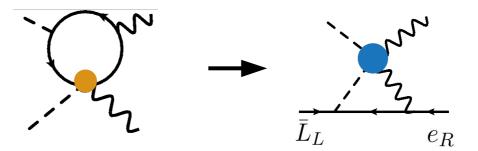
Due to approximate accidental cancellation, 1/2+2 Qe sin<sup>2</sup> ~ 0.04, Z boson contribution negligible.

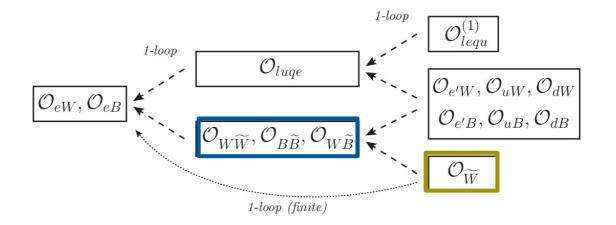




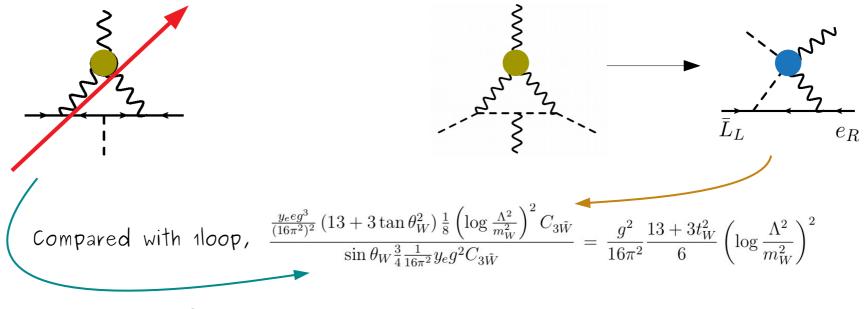




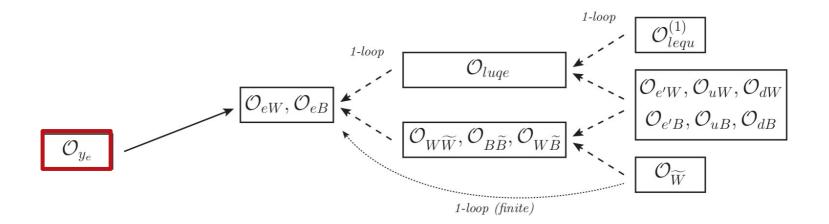




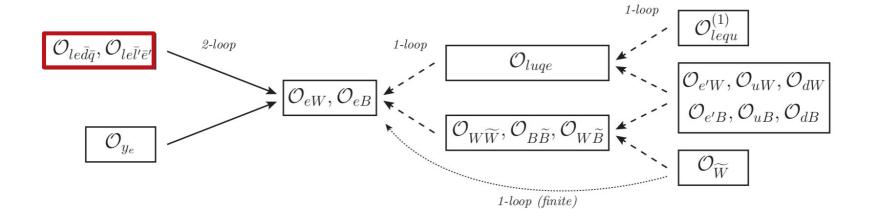
This one is interesting, since a two loop, log<sup>2</sup> contribution competes with the single loop, no log contribution



which is O(1) for  $\Lambda \sim$  5TeV



Accidental cancellation makes it smaller and only hypercharge contributes to EDM



$$\frac{d}{d\ln\mu} \operatorname{Im} \begin{pmatrix} C_{eB} \\ C_{eW} \end{pmatrix} = \frac{y_d g^3}{(16\pi^2)^2} \frac{N_c}{4} \begin{pmatrix} 3t_{\theta_W} Y_Q + 4t_{\theta_W}^3 (Y_L + Y_e) (Y_Q^2 + Y_d^2) \\ \frac{1}{2} + 2t_{\theta_W}^2 (Y_L + Y_e) Y_Q \end{pmatrix} C_{le\bar{d}\bar{q}} \qquad \qquad H \qquad \qquad V_\mu$$

$$\frac{d}{d\ln\mu} \operatorname{Im} \begin{pmatrix} C_{eB} \\ C_{eW} \end{pmatrix} = \frac{y_{e'} g^3}{(16\pi^2)^2} \frac{1}{4} \begin{pmatrix} 3t_{\theta_W} Y_L + 4t_{\theta_W}^3 (Y_L + Y_e) (Y_L^2 + Y_e^2) \\ \frac{1}{2} + 2t_{\theta_W}^2 (Y_L + Y_e) Y_L \end{pmatrix} C_{le\bar{e'}\bar{l'}} \cdot L_L \qquad \qquad E_R$$

The other 4-fermions enter only at 2 loops, single log Again, a cancellation for ledg:  $\sim g^2 \rightarrow \frac{g'^2}{8}$  14

# Impact on BSM

# Impact on BSM



Fix  $\Lambda = 10~TeV$ 

tree-level	
$C_{eW}$	$5.5 \times 10^{-5} y_e g$
$C_{eB}$	$5.5 \times 10^{-5} y_e g'$
one-loop	
Cluqe	$1.0 \times 10^{-3} y_e y_t$
$C_{W\widetilde{W}}$	$4.7 \times 10^{-3} g^2$
$C_{B\widetilde{B}}$	$5.2  imes 10^{-3}  g'^{2}$
$C_{W\widetilde{B}}$	$2.4\times 10^{-3}gg'$
$C_{\widetilde{W}}$	$6.4 \times 10^{-2} g^3$

$$\begin{array}{|c|c|c|c|c|} two-loops \\\hline C_{lequ} & 3.8 \times 10^{-2} \, y_e y_t \\ C_{\tau W} & 260 \, y_{\tau} g \\ C_{\tau B} & 380 \, y_{\tau} g' \\ C_{tW} & 6.9 \times 10^{-3} \, y_t g \\ C_{tB} & 1.2 \times 10^{-2} \, y_t g' \\ C_{bW} & 64 \, y_b g \\ C_{bB} & 47 \, y_b g' \\ C_{le\bar{d}\bar{q}} & 10 \, y_e y_t (y_t/y_b) \\ C_{le\bar{e}'\bar{l}'} & 0.63 \, y_e y_t (y_t/y_{\tau}) \\ \end{array}$$

two-loops finite
$$C_{y_e}$$
 $14 y_e \lambda_h$  $C_{y_t}$  $14 y_t \lambda_h$  $C_{y_b}$  $2.9 \times 10^3 y_b \lambda_h$  $C_{y_{\tau}}$  $3.1 \times 10^4 y_{\tau} \lambda_h$ 

# Leptoquarks

EDM sets strong constraints to leptoquarks that couple to both left and right leptons

$$\begin{aligned} & (\mathbf{3}, \mathbf{2}, \mathbf{7/6}) \\ \mathcal{L} &= -y_2^{RL} \overline{t}_R R^a \varepsilon^{ab} L_{L_1}^b + y_2^{LR} \overline{e}_R R^{a*} Q_{L_3}^a + \text{h.c.}, \\ \mathcal{L}_{eff}^{R_2} &= \frac{y_2^{LR*} y_2^{RL*}}{m_{R_2}^2} \mathcal{O}_{luqe} \\ & (\overline{\mathbf{3}}, \mathbf{1}, \mathbf{1/3}) \\ \mathcal{L} &= y_1^{LL} \overline{Q}_{L_3}^{Ca} S_1 \varepsilon^{ab} L_{L_1}^b + y_1^{RR} \overline{t}_R S_1 e_R + \text{h.c.} \\ \mathcal{L}_{eff}^{S_1} &= \frac{y_1^{LL*} y_1^{RR}}{m_{S_1}^2} \left[ \mathcal{O}_{luqe} + \mathcal{O}_{lequ}^{(1)} \right] \\ \end{array}$$

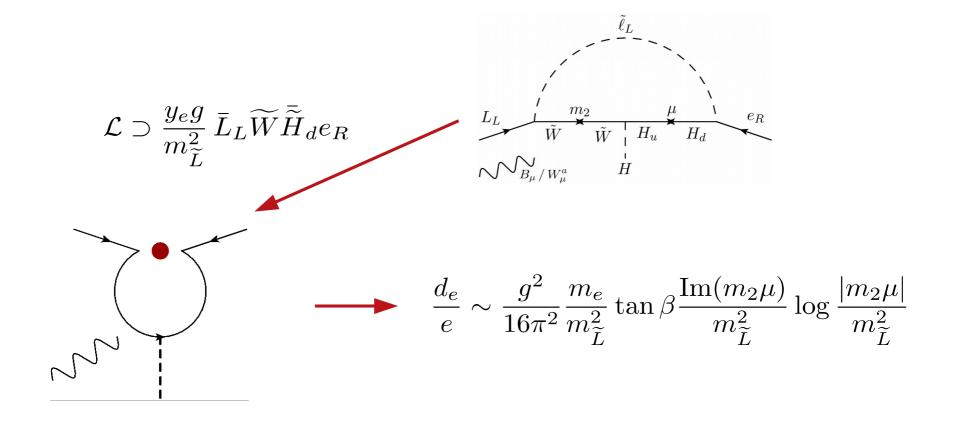
$$(\overline{\mathbf{3}}, \mathbf{2}, \mathbf{5/6}) \\ \mathcal{L} &= x_2^{RL} \overline{b}_R^C \gamma^{\mu} V_{2,\mu}^a \varepsilon^{ab} L_{L_1}^b + x_2^{LR} \overline{Q}_{L_3}^{Ca} \gamma^{\mu} \varepsilon^{ab} V_{2,\mu}^b e_R \\ m_{V_2} &\gtrsim 5.5 \,\text{TeV} \, \sqrt{\frac{\text{Im}(x_2^{LR} x_2^{RL*})}{y_e y_b}} \\ \end{aligned}$$

$$(\overline{\mathbf{3}}, \mathbf{2}, \mathbf{5/6}) \\ m_{V_2} &\gtrsim 5.5 \,\text{TeV} \, \sqrt{\frac{\text{Im}(x_2^{LR} x_2^{RL*})}{y_e y_b}} \\ \end{aligned}$$

# Supersymmetry: 1 loop + tree

One loop EDMs are very important in SUSY.

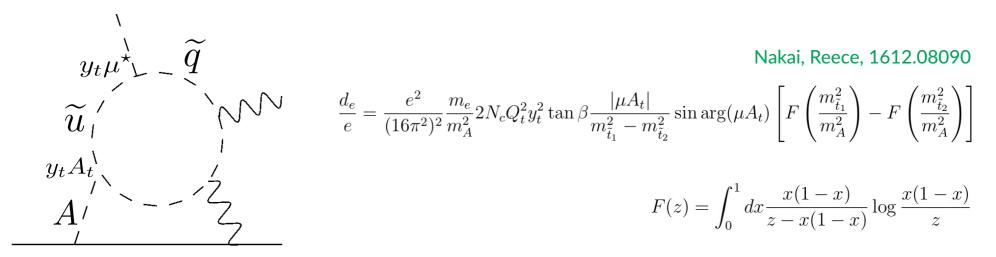
Exact expressions are very complicated, but now we know superpartners are heavy.



$$m_{\tilde{L}_L} \gtrsim 25\,(50) \text{ TeV} \quad \text{for } m_{\tilde{L}_L} = M_2 = \mu \ (m_{\tilde{L}_L} \gg \mu = M_2)$$

#### Supersymmetry: 2 loop + tree

At two loops, a Barr-Zee diagram gives sensitivity to stops.



Also understood via RGE of AFF to dipole. After integrating out the stops,

 $\mathcal{L} \sim y_u^2 (H_u H_d A_u \mu^* + H_u^* H_d^* A_u^* \mu) F_{\mu\nu} F_{\mu\nu} \sim y_u^2 (s_\beta v_u + c_\beta v_d) \mathrm{Im}(A_u \mu^*) A^0 F_{\mu\nu} F_{\mu\nu}$ 

$$\frac{d_e}{e} \sim \frac{e}{16\pi^2} \frac{4}{9} \frac{m_e}{m_A^2} \tan\beta \frac{|\mu A_t|}{m_{\tilde{t}}^2} \sin\arg(\mu A_t) \log\frac{m_{\tilde{t}}^2}{m_A^2}$$

 $\blacktriangleright \quad m_{\tilde{t}} > 5 \text{TeV for } \tan \beta \sim \sin \arg A_t \mu \sim 1, m_A \sim \mu \sim A_t \sim 1 \text{TeV}$ 

# Supersymmetry: 1 loop + 1loop, HHFF

Since the decoupling 1/scalars^4, EDM via HHFF relevant in split SUSY

$$\begin{split} C_{W\widetilde{W}} &= C_{loop} \, \frac{-8 + 27\rho - 24\rho^2 + 5\rho^3 + 6\rho^2 \ln\rho}{16(\rho - 1)^3} \,, \\ C_{B\widetilde{B}} &= t_{\theta_W}^2 C_{loop} \, \frac{\rho(11 - 16\rho + 5\rho^2 - 2(\rho - 4)\ln\rho)}{16(\rho - 1)^3} \,, \\ C_{W\widetilde{B}} &= t_{\theta_W} C_{loop} \, \frac{\rho(7 - 8\rho + \rho^2 + 2(\rho + 2)\ln\rho)}{8(\rho - 1)^3} \,, \end{split}$$

$$\begin{array}{c}
H \\ & \tilde{H}_{u} \\
 & \tilde{H}_{u} \\
 & \tilde{H}_{d} \\
 & \tilde{$$

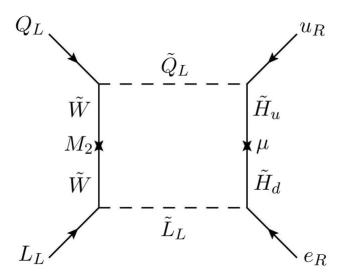
$$C_{loop} \equiv \frac{g^4 \sin 2\beta \sin \varphi}{16\pi^2 |M_2\mu|} , \quad \varphi = \operatorname{Arg}[m_{12}^2 \mu^* M_2^*] \qquad \rho \equiv |M_2/\mu|^2$$

For tan beta ~ CP phases ~ O(1)

$$\sqrt{|M_2\mu|} \gtrsim 4 \,\mathrm{TeV}$$

# Supersymmetry: 1 loop + 1loop, luqe

Contribution to luge via squark-gauginos loop



$$\operatorname{Im} C_{luqe} = -y_e y_u \frac{3g^2 \operatorname{Im}[\mu M_2]}{16\pi^2 \sin 2\beta} F(m_i^2) \quad \text{with} \quad F(m_i^2) = -\sum_i \frac{m_i^2 \ln m_i^2}{\prod_{i \neq j} (m_i^2 - m_j^2)}$$

For degenerate superpartner masses,

 $m_i \gtrsim 7.5 \,\mathrm{TeV}$ 

EDM sets very strong constraints to naive anarchic compositeness for leptons

There are ways to avoid this, e.g. by O(2) symmetries or mass generation by bilinears

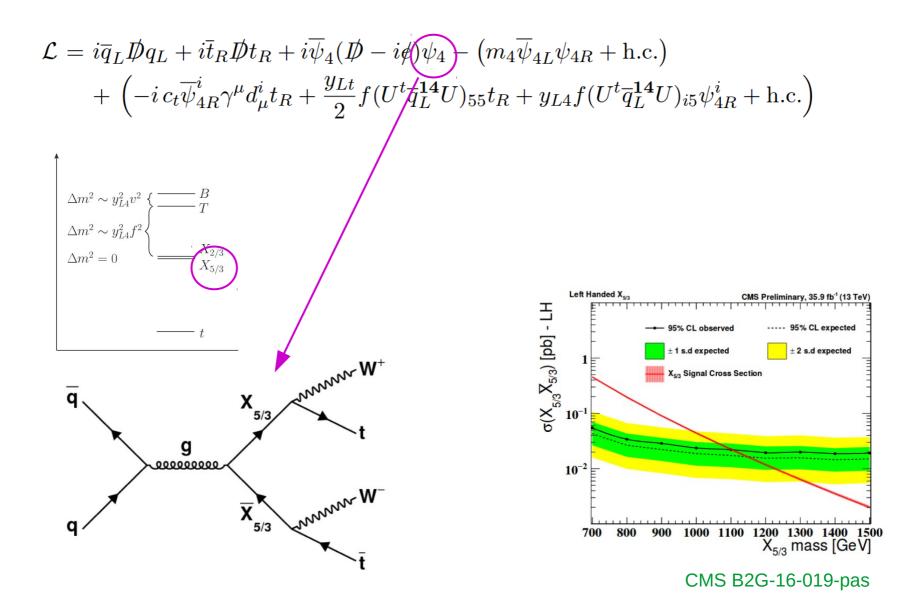
#### Panico, Pomarol, 1603.06609

Decoupling scale  $\Lambda_u$   $\Lambda_u$   $\Lambda_d$   $\Lambda_d$   $\Omega_{u_R}$   $\Omega_{d_R}, \mathcal{O}_{Q_{L1}}$   $\Lambda_s$   $\Omega_{s_R}$   $\Lambda_c$   $\Lambda_b$   $\Omega_{c_R}, \mathcal{O}_{Q_{L2}}$   $\Lambda_b$   $\Omega_{t_R}, \mathcal{O}_{Q_{L2}}$   $\Lambda_b$   $\Omega_{t_R}, \mathcal{O}_{Q_{L3}}$   $\mathcal{L}_{bil} = \frac{1}{\Lambda_i^{d_H-1}} (\epsilon_i f_i) \mathcal{O}_H (\epsilon_j f_j)$   $\mathcal{L}_{bil} = \frac{1}{\Lambda_i^{d_H-1}} (\epsilon_j f_j) \mathcal{O}_H (\epsilon_j f_j)$   $\mathcal{L}_{bil} = \frac{1}{\Lambda_i^{d_H-1}} (\epsilon_j f_j) \mathcal{O}_H (\epsilon_j f_j)$  $\mathcal{L}_{bi$ 

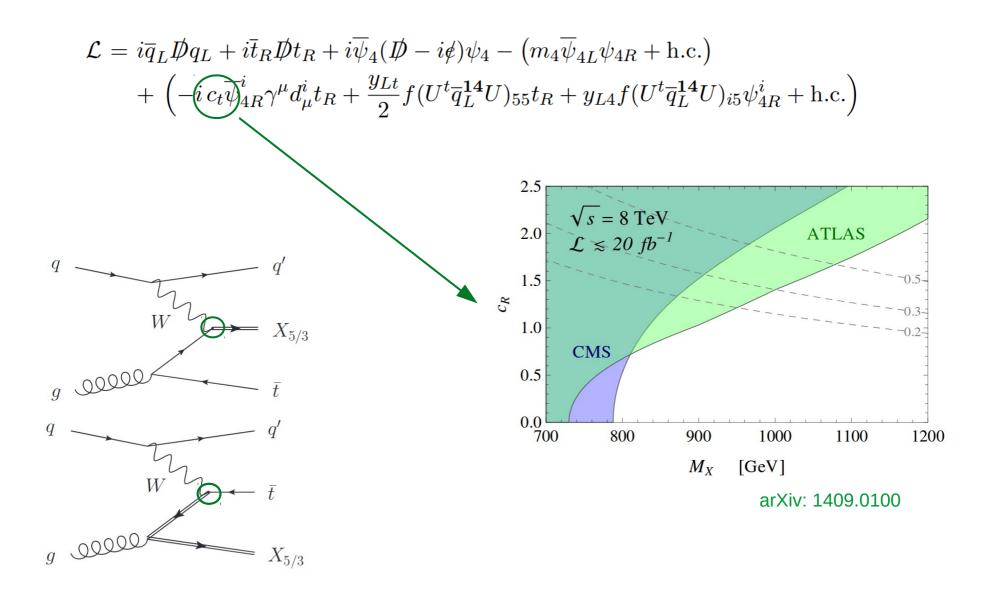
We assume that somehow this is solved.

We focus on the EDM generated by top partners

#### Take SO(5)/SO(4):



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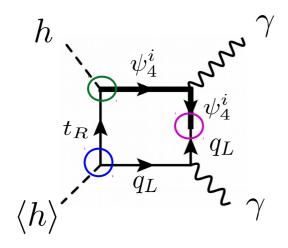
Take SO(5)/SO(4):

e

$$\mathcal{L} = i\overline{q}_{L} \not D q_{L} + i\overline{t}_{R} \not D t_{R} + i\overline{\psi}_{4} (\not D - i\phi)\psi_{4} - (m_{4}\overline{\psi}_{4L}\psi_{4R} + \text{h.c.}) + \left(-ic_{t}\overline{\psi}_{4R}^{i}\gamma^{\mu}d_{\mu}^{i}t_{R} + \frac{y_{Lt}}{2}f(U^{t}\overline{q}_{L}^{14}U)_{55}t_{R} + y_{L4}f(U^{t}\overline{q}_{L}^{14}U)_{i5}\psi_{4R}^{i} + \text{h.c.}) - ic_{t}\overline{\psi}_{4R}^{i}\gamma^{\mu}d_{\mu}^{i}t_{R} + \text{h.c.} \supset i\frac{c_{t}}{f}\partial_{\mu}h\left(\overline{\hat{X}}_{2/3R}\gamma^{\mu}t_{R} - \overline{\hat{T}}_{R}\gamma^{\mu}t_{R}\right) + \text{h.c.}$$

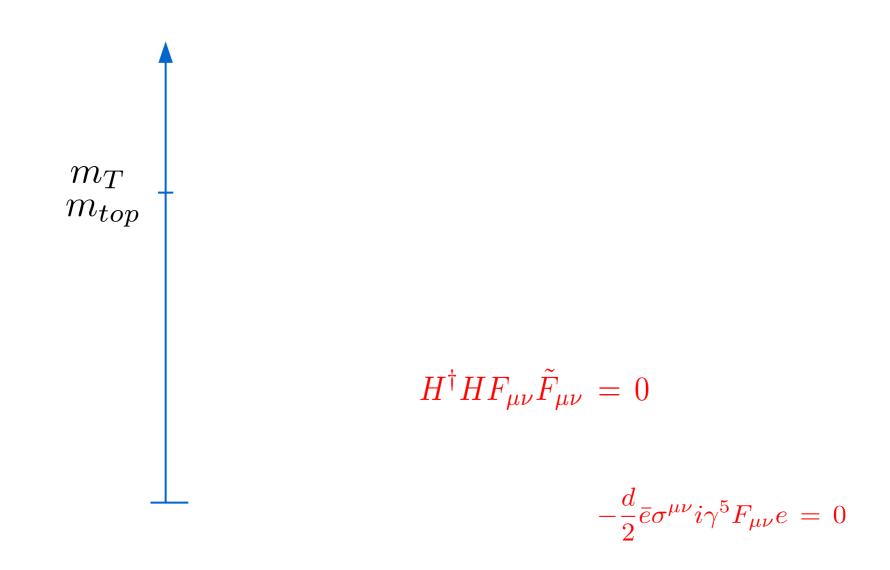
$$\int \gamma de e = -\frac{e^{2}}{48\pi^{4}}\frac{y_{e}}{\sqrt{2}}\text{Im} c_{t}\frac{2y_{L4}}{\sqrt{m_{4}^{2} + y_{L4}^{2}f^{2}}}\frac{m_{top}}{m_{T}}\log\frac{m_{T}^{2}}{m_{top}^{2}}$$

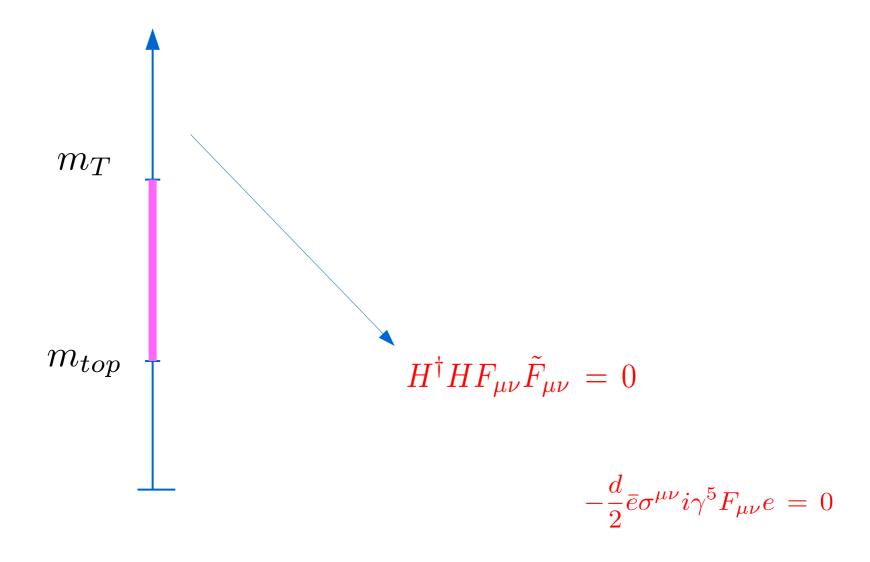
$$\mathcal{L} = i\overline{q}_L \not{D} q_L + i\overline{t}_R \not{D} t_R + i\overline{\psi}_4 (\not{D} - i\not{e})\psi_4 - \left(m_4 \overline{\psi}_{4L} \psi_{4R} + \text{h.c.}\right) \\ + \left(-ic_t \overline{\psi}_{4R}^i \gamma^\mu d^i_\mu t_R + \underbrace{\cancel{\mathcal{Y}}_{Lt}}_2 f(U^t \overline{q}_L^{\mathbf{14}} U)_{55} t_R + \underbrace{y_{L4}}_4 f(U^t \overline{q}_L^{\mathbf{14}} U)_{i5} \psi^i_{4R} + \text{h.c.}\right)$$

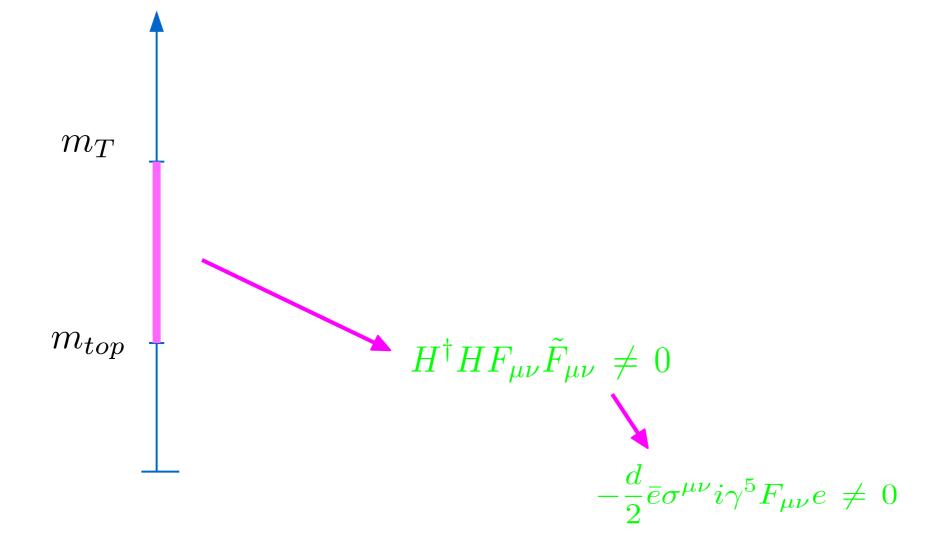


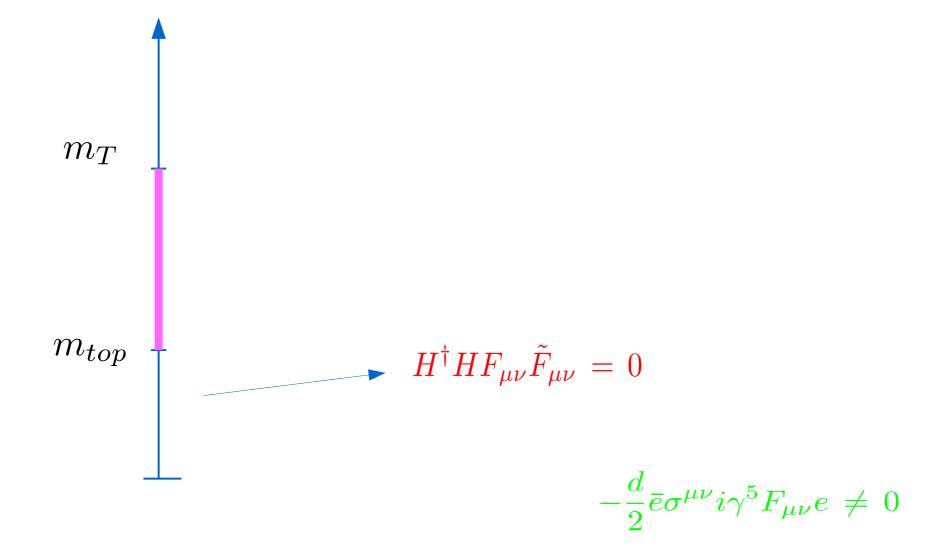
CPV controled by  $c_t y_{Lt}^* y_{L4}$ 

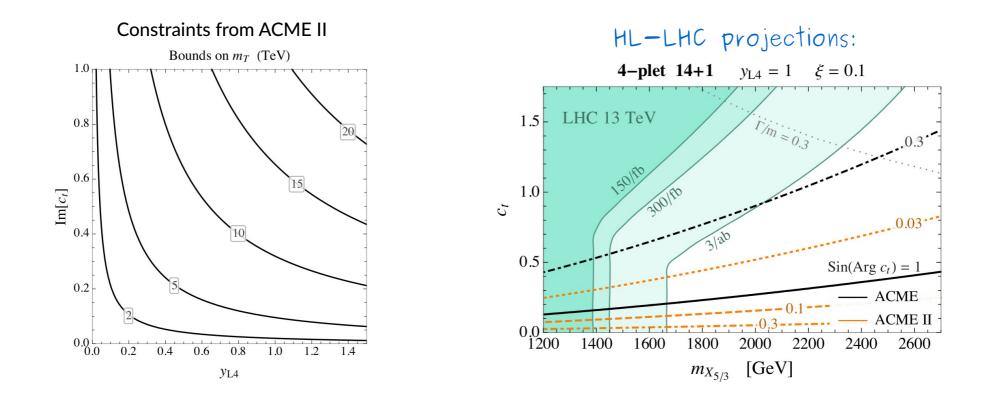
For complete, degenerate multiplets the diagram is proportional to  $tr c_t \sim tr T^a \sim 0$ 







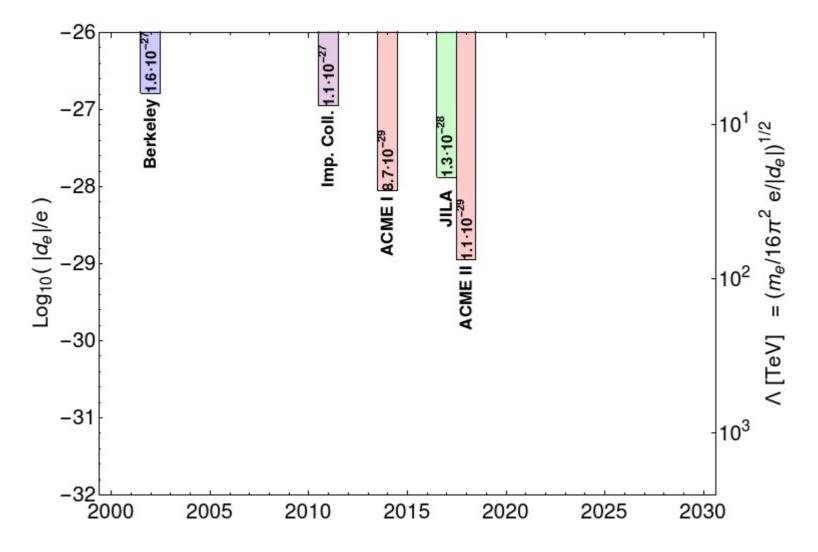




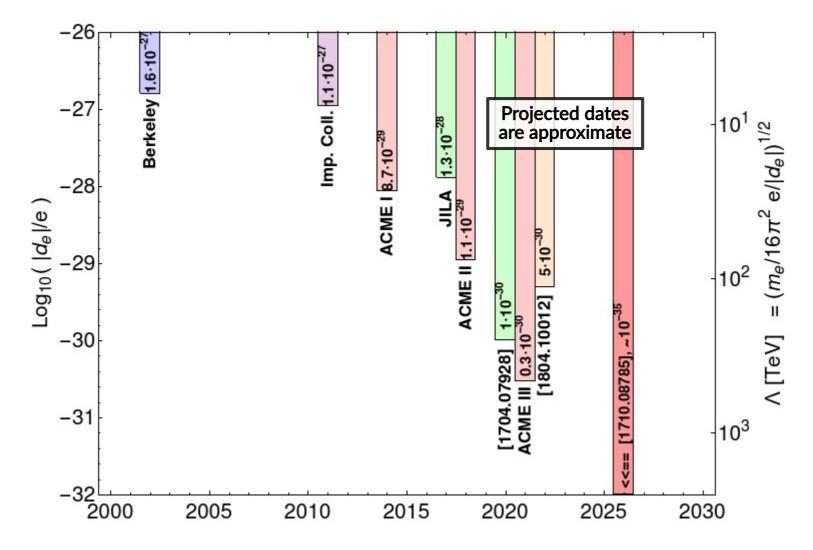
Im(ct) has to be of order 0.01 if we want to be within LHC reach

The future of the electron EDM

# **Evolution of electron EDM constraints**



### **Evolution of electron EDM constraints**



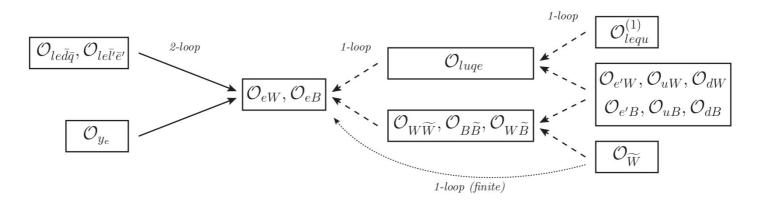
- After some time of promises of improvements with nothing happening, it seems that there will be further progress in a short time scale. - If there is a positive signal, we'll have confirmation very quickly.

- There are some proposals for a total breakthrough.

# Conclusions

## Conclusions

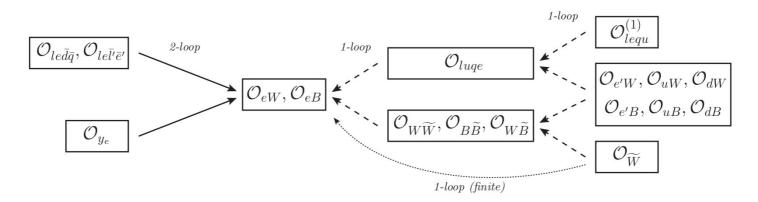
- Map of the most relevant effects at two loops:



- CPV in Higgs sector pushed way outside any current or future collider reach
- Bounds of 1-100TeV for generic theories of leptoquarks
- Characterization of relevant constraints for the MSSM
- In composite models, CPV from top sector important. Top partners pushed outside LHC range, unless they have CP preserving couplings
- Unless there is a reason why, contrary to SM, BSM sector respects CP, ACME result makes these theories much less natural

# Conclusions

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# Thanks!