

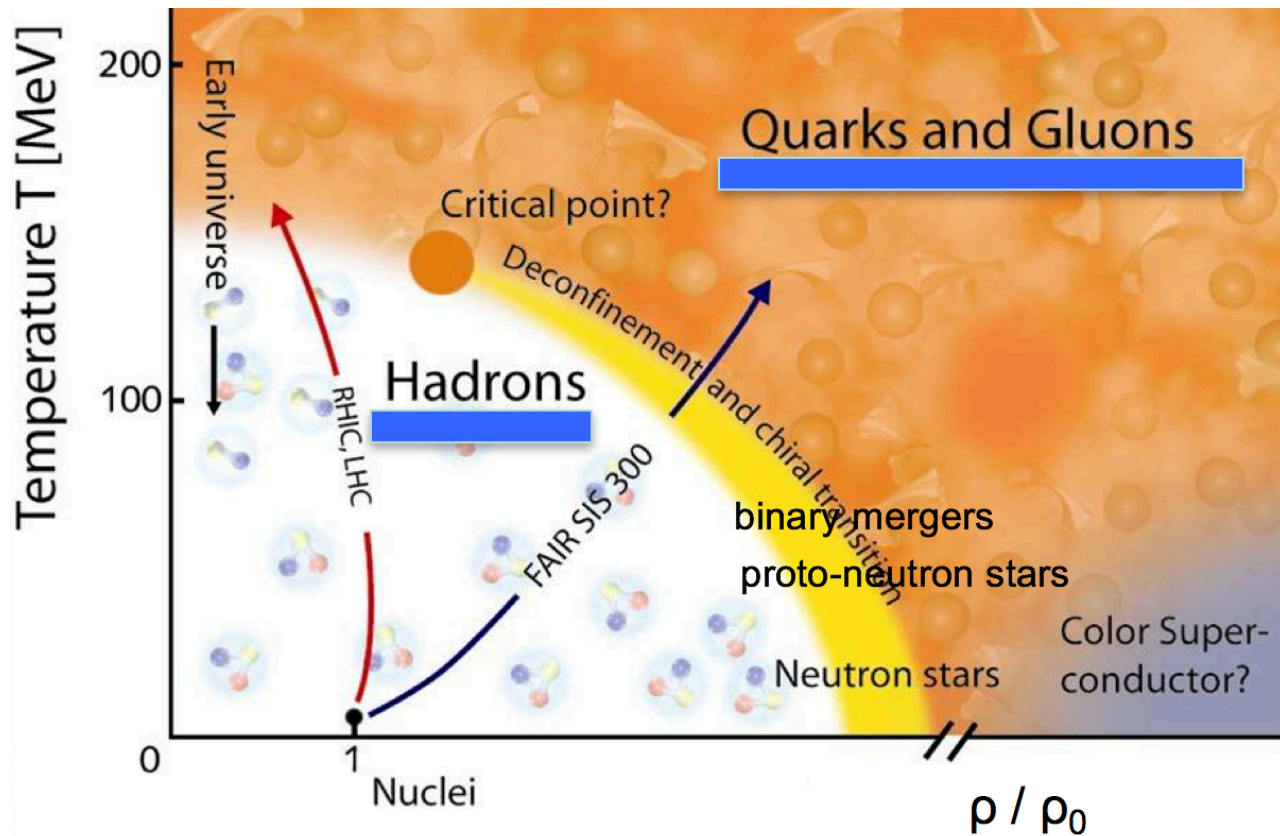
## Exotic Matter in Neutron Stars

### ***OUTLINE***

- basics of neutron stars
- hyperons in the core
- quark matter in the star
- magnetic fields
- meson condensation

*V. Dexheimer, R. Mallick, R. Nandi, R. Negreiros,  
B. Franzon, R. Gomes, A. Mukherjee,, J. Steinheimer, SWS  
FIAS ,Kent State, Rio de Janeiro, Porto Alegre, Bhopal , Mumbai*

*the usual phase diagram (sketch) of strong interactions*



connect both worlds  
in some reasonable way

Practical model useful for heavy-ion simulations and compact star physics

correct asymptotic degrees of freedom

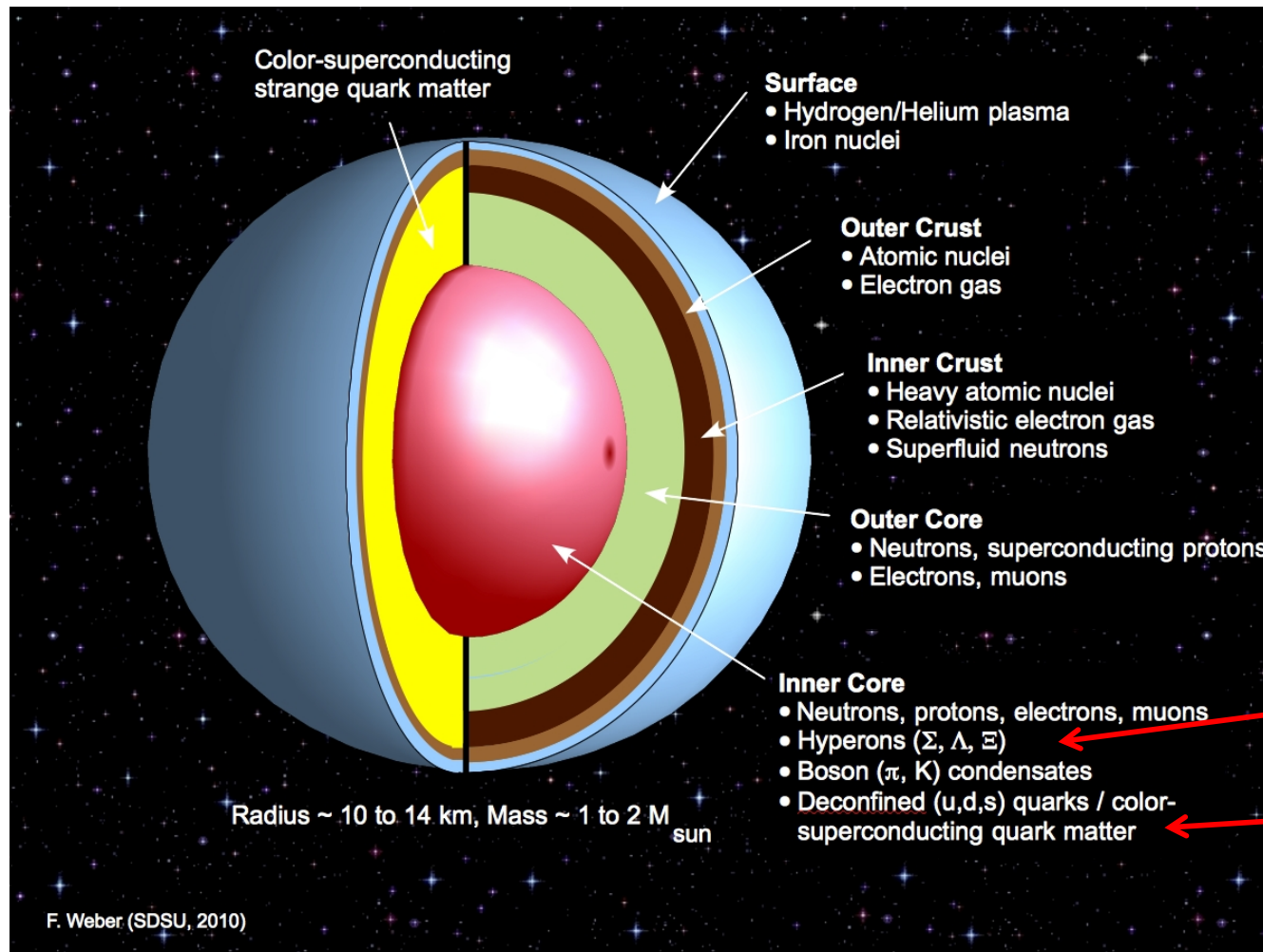
reasonable description on a quantitative level for high  $T$  down to nuclei

possibility of studying first-order as well as cross-over transitions

neutron stars are remnants of Type II supernovae

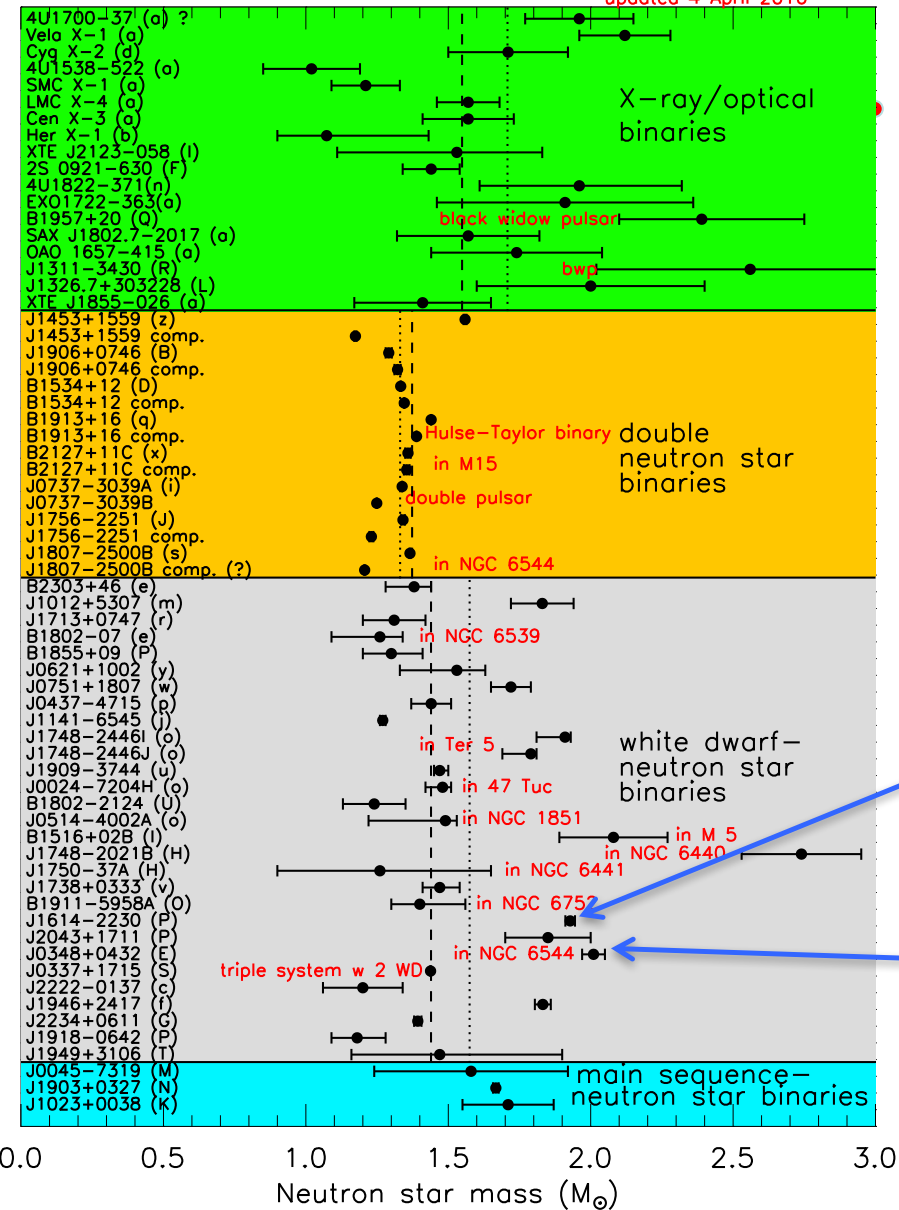
1 to 2 solar masses, radii around 10 - 15 km  
maximum central densities 4 to 10  $\rho_0$

more than 2000 known neutron stars



hyper star

hybrid star



Masses of Neutron Stars

*benchmark for NS models*

$$M = (1.97 \pm .04) M_{\odot}$$

Demorest et al. Nature 467, 1081 (2010)

*new observation PSR J0348+0432*

$$M = (2.01 \pm .04) M_{\odot}$$

Antoniadis et al. Science 340, 448 (2013)

well established - heavy neutron stars

# hadronic SU(3) approach based on non-linear realization of $\sigma\omega$ model

Lowest multiplets

$$B = \{ p, n, \Lambda, \Sigma^{\pm/0}, X^{-/0} \} \quad \text{baryons}$$

$$\text{diag} (V) = \{ (\omega + \rho) / \sqrt{2}, (\omega - \rho) / \sqrt{2}, \phi \} \quad \text{vector mesons}$$

$$\text{diag} (X) = \{ (\sigma + \delta) / \sqrt{2}, (\sigma - \delta) / \sqrt{2}, \zeta \} \quad \text{scalar mesons}$$

Mean fields generate masses, scalar attraction and vector repulsion

SU(3) interaction

$$L_{BW} = - \sqrt{2} g_8^W ( \alpha_W [BOBW]_F + (1 - \alpha_W) [BOBW]_D )$$

$$- g_1^W / \sqrt{3} \text{Tr}(\bar{B}OB) \text{Tr} (W)$$

$$V(M) \quad \langle \sigma \rangle = \sigma_0 \neq 0 \quad \langle \zeta \rangle = \zeta_0 \neq 0$$

$$\sigma \sim \langle \bar{u} u + \bar{d} d \rangle \quad \zeta \sim \langle \bar{s} s \rangle \quad \delta^0 \sim \langle \bar{u} u - \bar{d} d \rangle$$

plus explicit symmetry breaking

## Nuclear Matter and Nuclei

binding energy  $E/A \sim -15.2 \text{ MeV}$       saturation  $(\rho_B)_0 \sim .16/\text{fm}^3$

compressibility  $\sim 223 \text{ MeV}$       asymmetry energy  $\sim 31.9 \text{ MeV}$

parameter fit to known nuclear binding energies and hadron masses

2d calculation of all measured ( $\sim 800$ ) even-even nuclei

error in energy  $\varepsilon (A > 50) \sim 0.17 \%$

$\varepsilon (A > 100) \sim 0.12 \%$

+ correct binding energies of hypernuclei, reasonable charge radii

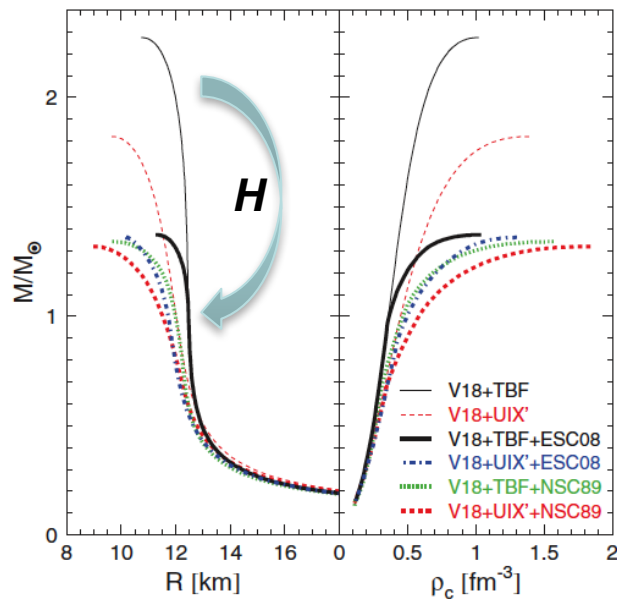
## Neutron Stars with Hyperons

relatively easy to generate heavy stars with nucleonic EOS  $M_{\max} \sim 2.8 M_{\odot}$  (NL3)  
 $\sim 2.2 M_{\odot}$  (APR)

Causal limit beyond  $\rho_c$  - Rhoades, Ruffini (1974):  $M_{\max} < 3.2 M_{\odot}$

additional degrees of freedom soften the equation of state  
 reducing the maximum star mass

**“hyperon puzzle”**



Nijmegen potential

hyper stars tend to have small mass

e.g.

*Vidaña et. al., EPL 94 11002*

*Schulze et. al, PRC 84, 035801*

...

*Schulze, Rijken, PRC 84, 035801 (2011)*

most HN scattering data from the 60's !  
 no corresponding HH data

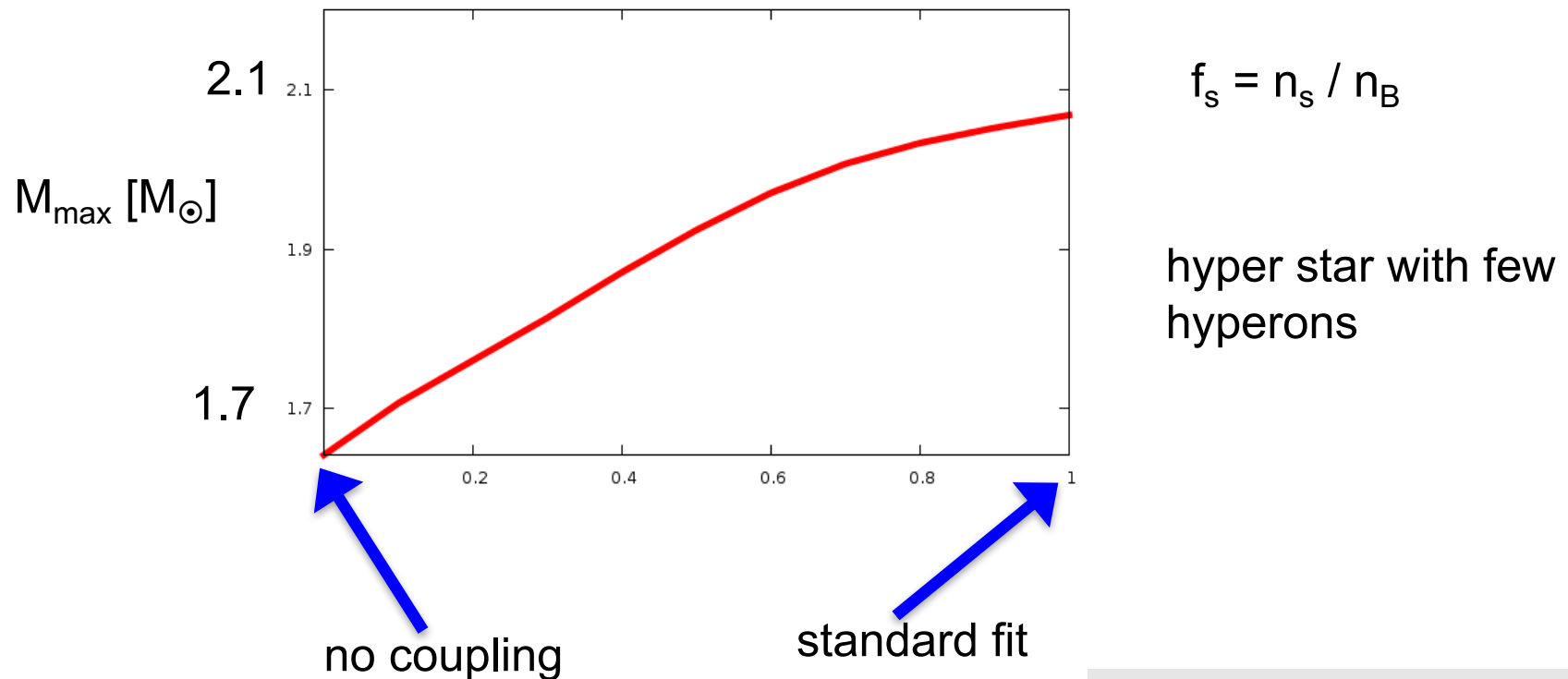
## “Hyperon Puzzle”

many hyperons soften EOS, reduce star masses significantly

hyperon-hyperon repulsion - impact of  $s\bar{s}$  vector field  $\Phi$

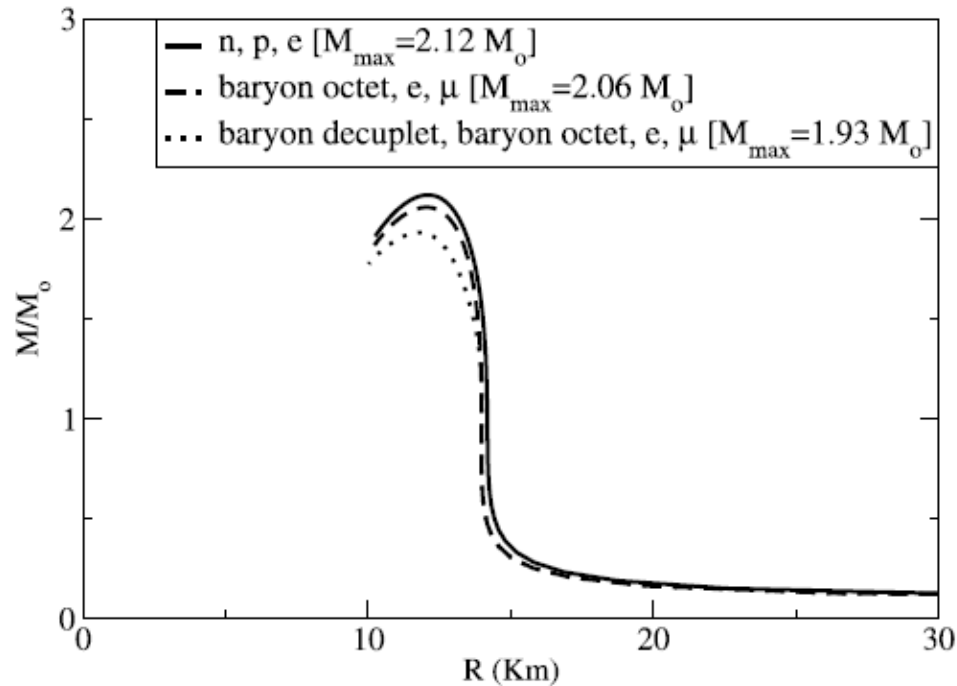
strong nonlinear hyperon-nucleon interaction (Lonardoni et al, PRL 114 092301)

rescale  $g_{B\Phi}$  coupling parameters,  $f_s(\text{core})$  varies between 0.1 and 1





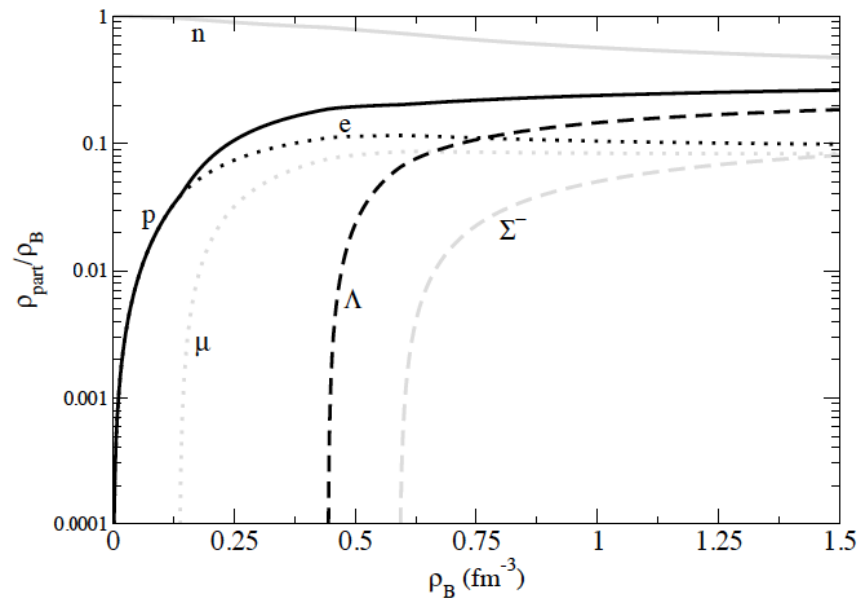
# Neutron star masses including different sets of particles



Tolman-Oppenheimer-Volkov equations, static spherical star

changing masses with degrees of freedom

large star masses even with spin 3/2 resonances



*normalized particle densities*

# Δ baryons in compact stars?

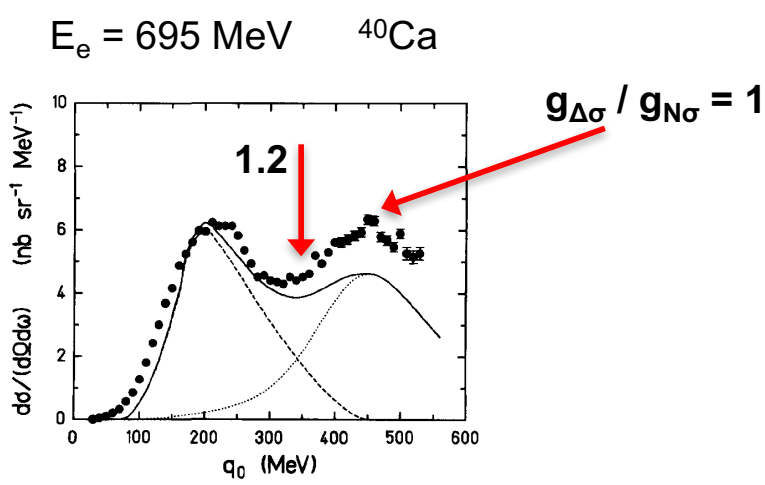
Δ resonances  
 scalar couplings → vacuum masses

vector couplings unclear  
 moderate changes  $r_V = g_{\Delta\omega} / g_{N\omega}$

not far from SU(6)

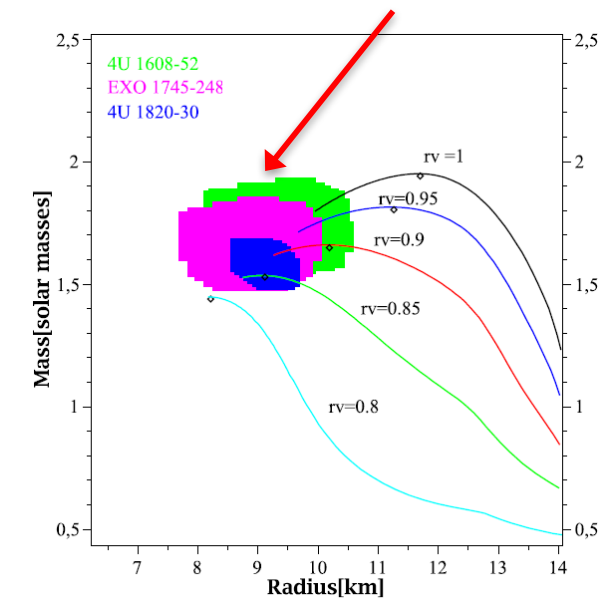
constraints from πA scattering  
 photoabsorbtion

quasielastic eA scattering

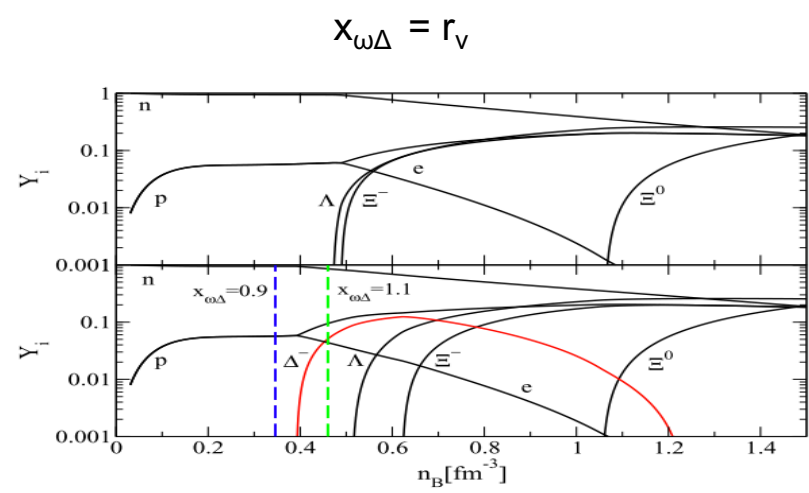


Wehrberger, Phys. Rep. 225, 273 (1993)

Özel et al, Phys.Rev.D82:101301,2010



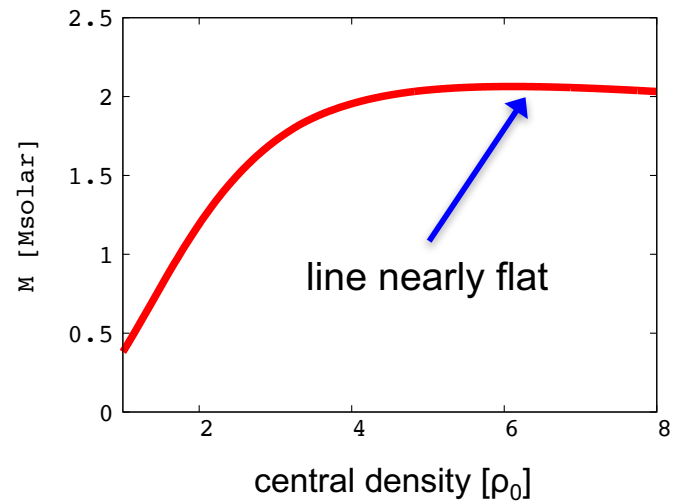
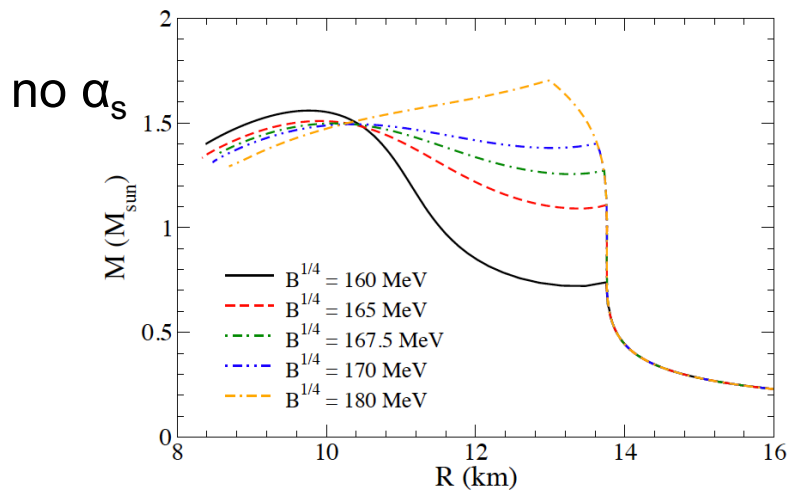
Schürhoff, SWS, Dexheimer, APJL 724 (2010) L74



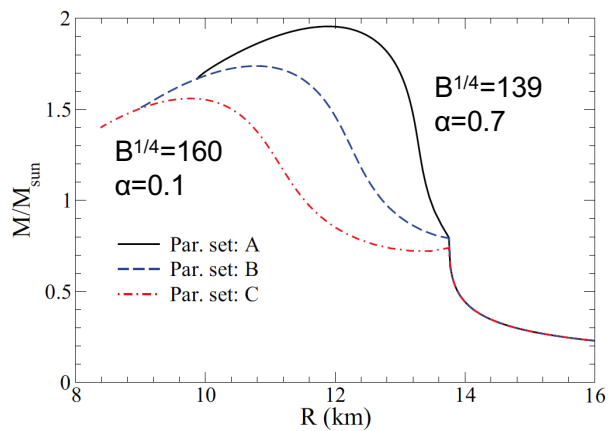
analysis in Drago et al astro-ph:1407.2843:  
 Onset of Δ population at 2 to 3 ρ₀

Quark star and Δ star families

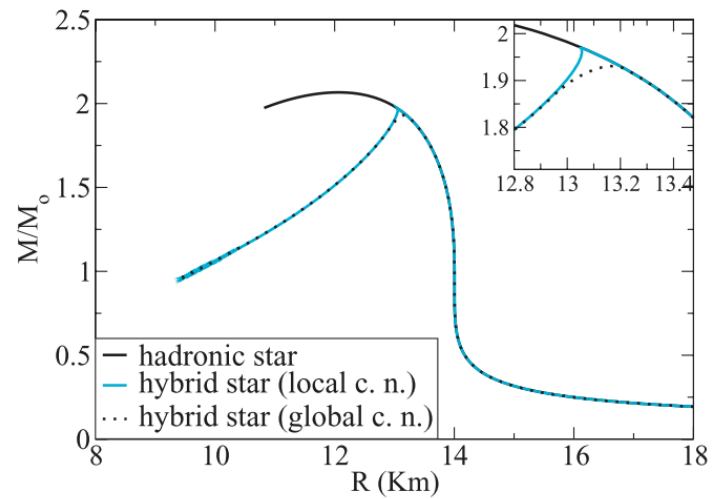
# Hybrid Stars, Quark Interactions



ingredients –  
 Standard baryonic EOS (G300)  
 plus MIT bag model +  $\alpha_s$  corrections



unified hadron-quark model



baryons alone  $M_{\text{max}} \sim 1.8 M_{\text{solar}}$

## hadrons, quarks, Polyakov loop and excluded volume

Include modified distribution functions for quarks/antiquarks

$$\Omega_q = -T \sum_{j \in Q} \frac{\gamma_j}{(2\pi)^3} \int d^3k \ln \left( 1 + \Phi \exp \frac{E_j^* - \mu_j}{T} \right)^* \quad \Phi \quad \text{confinement order parameter}^*$$

Following the parametrization used in PNJL calculations, introduce Polyakov loop potential  $U(\Phi, T)$

*Ratti et al, EPJC49, 213*

The switch between the degrees of freedom is triggered by hadronic excluded volume corrections

*no reconfinement!*

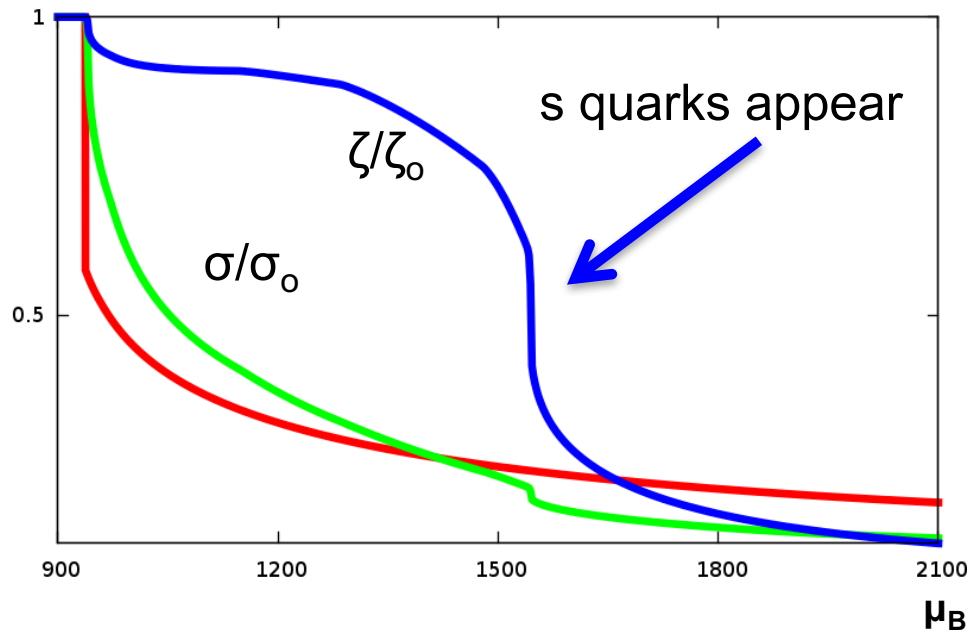
equation of state stays causal!

$$\begin{aligned} V_q &= 0 \\ V_h &= v \\ V_m &= v/8 \end{aligned}$$

$$\tilde{\mu}_i = \mu_i - v_i P$$

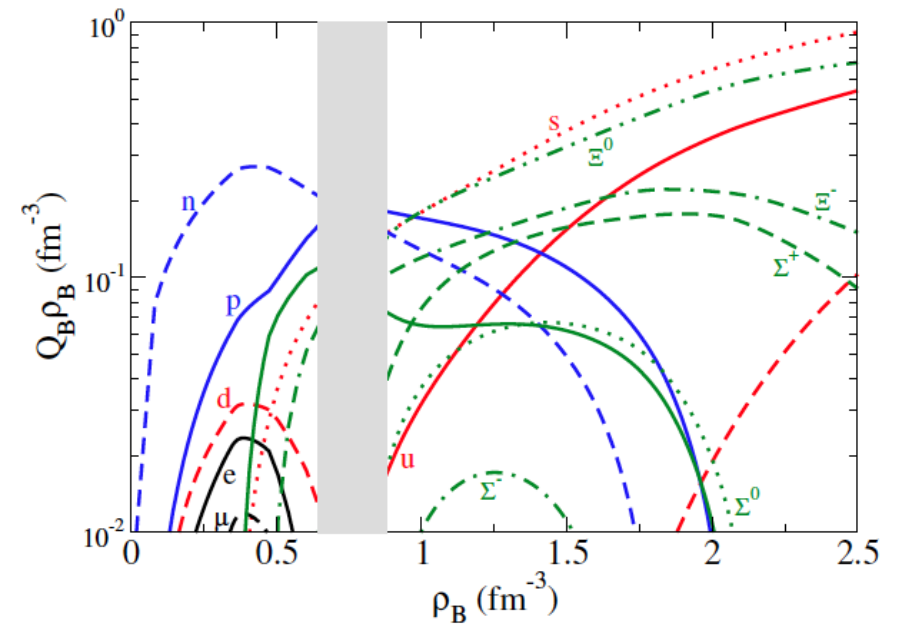
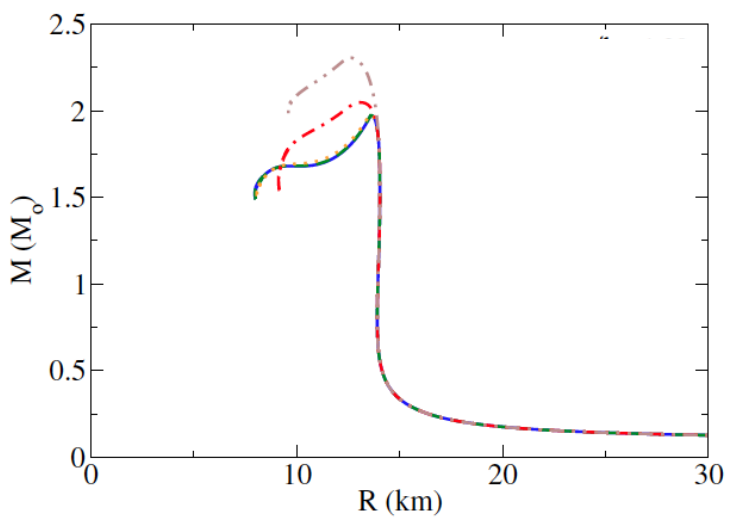
$$e = \tilde{e} / (1 + \sum v_i \tilde{\rho}_i)$$

star matter in beta equilibrium in QH approach



1<sup>st</sup> order phase transition  
in star matter possible  
cross over in symmetric matter  
 $f_s(\text{core})$  jumps to  $\sim 1$   
particle cocktail

star masses M varying quark interactions

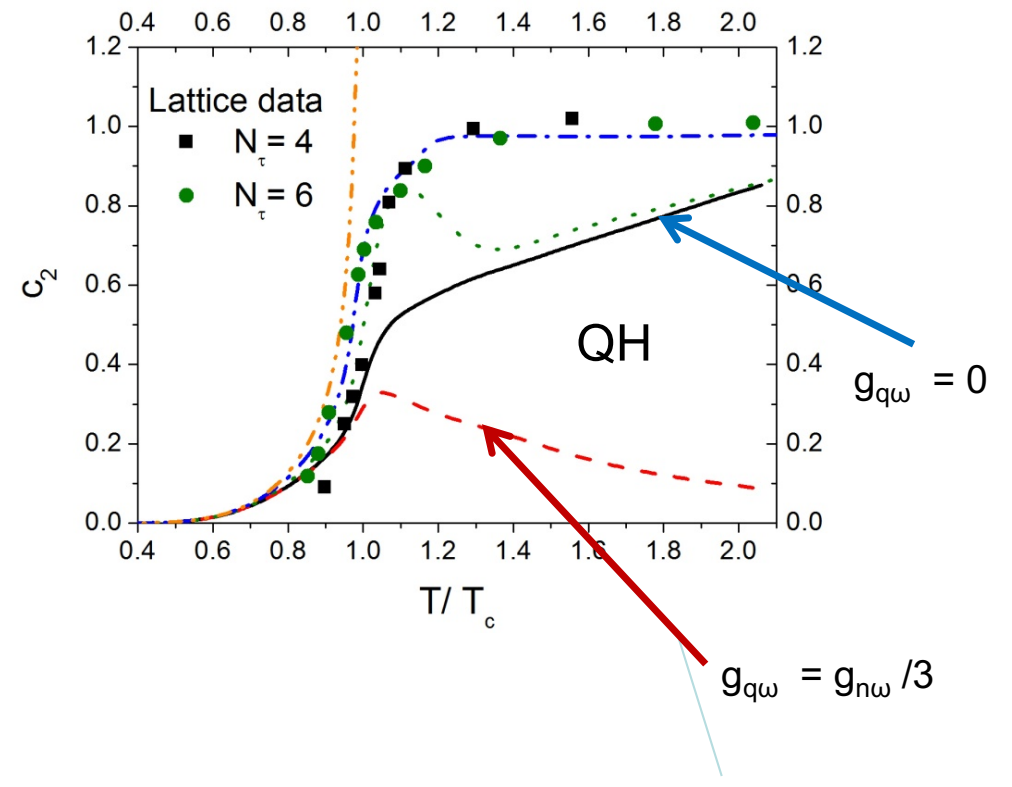
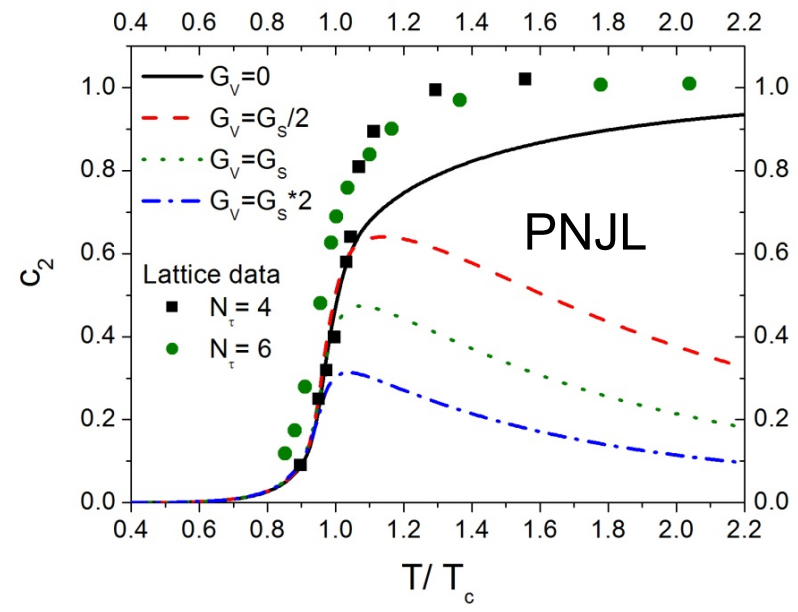


Mass  $\sim 2 - 2.3 M_\odot$  Radius  $\sim 13$  km

# Susceptibility in PNJL and QH model for different quark vector interactions

$$P(T, \mu) = P(T) + c_2(T) \mu^2 T^2 + \dots$$

small quark vector repulsion !!

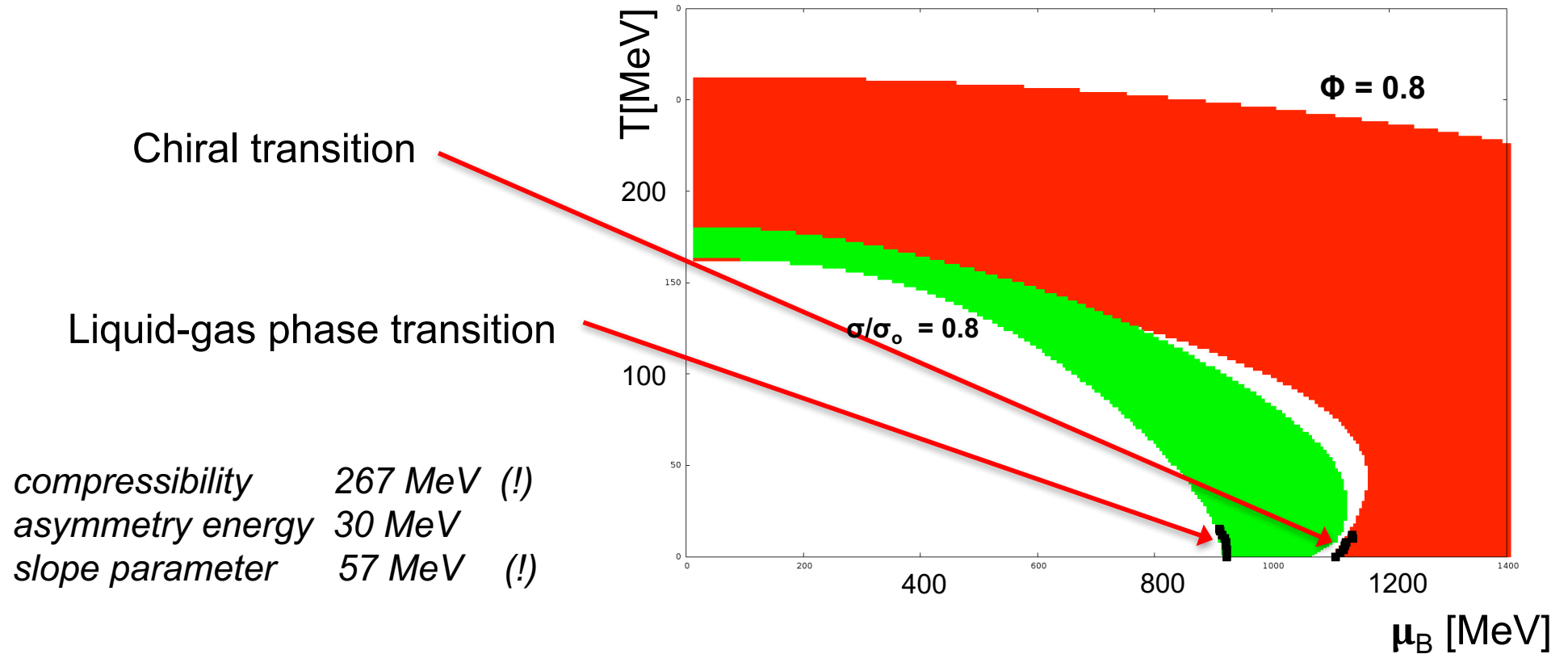


same behavior for strangeness susceptibilities

Steinheimer, SWS, PLB 696, 257  
 Rau et al, Phys.Lett.B733, 176

# Excited quark-hadron matter in the parity-doublet approach

doublet candidates – N(1535),  $\Lambda(1670)$ ,  $\Sigma(1750)$ ,  $\Xi$  (?) overall unclear



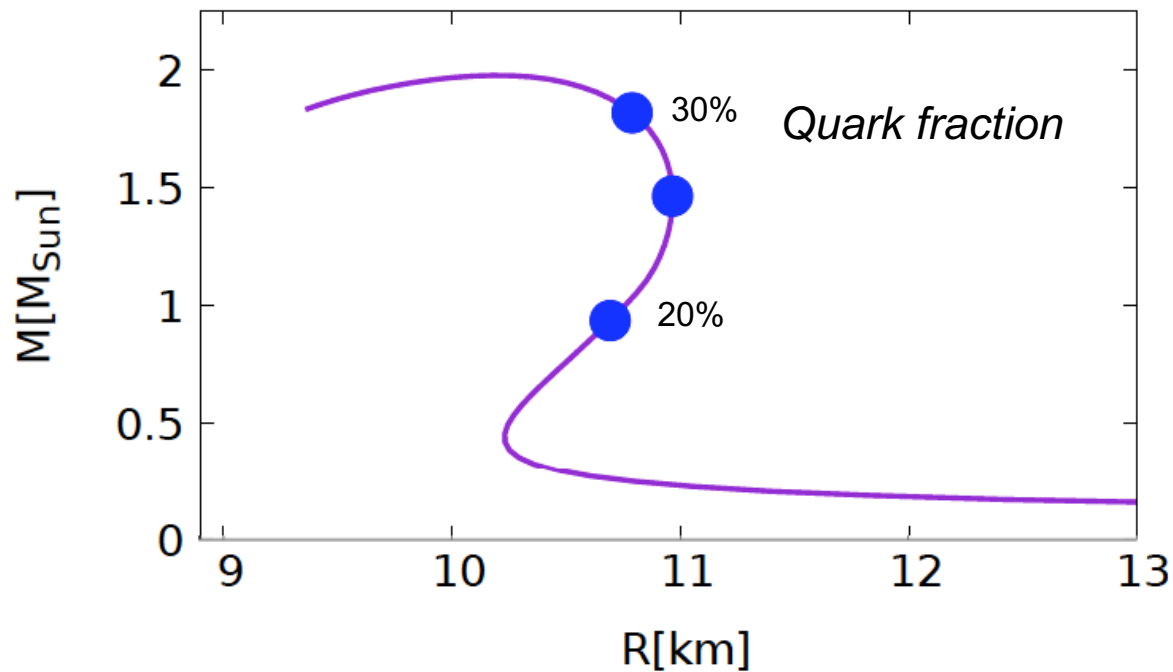
single particle energies

$$E_{\pm} = \sqrt{(g_1 \sigma + g_2 \zeta)^2 + m_0^2} \pm (g'_1 \sigma + g'_2 \zeta)$$

chirally invariant mass term

Mukherjee, SWS, Steinheimer, Dexheimer, arXiv: 1706.09191  
 Steinheimer, SWS, Stöcker, JPhysG 38, 035001  
 Y. Motohiro et al. PRC 92, 025201

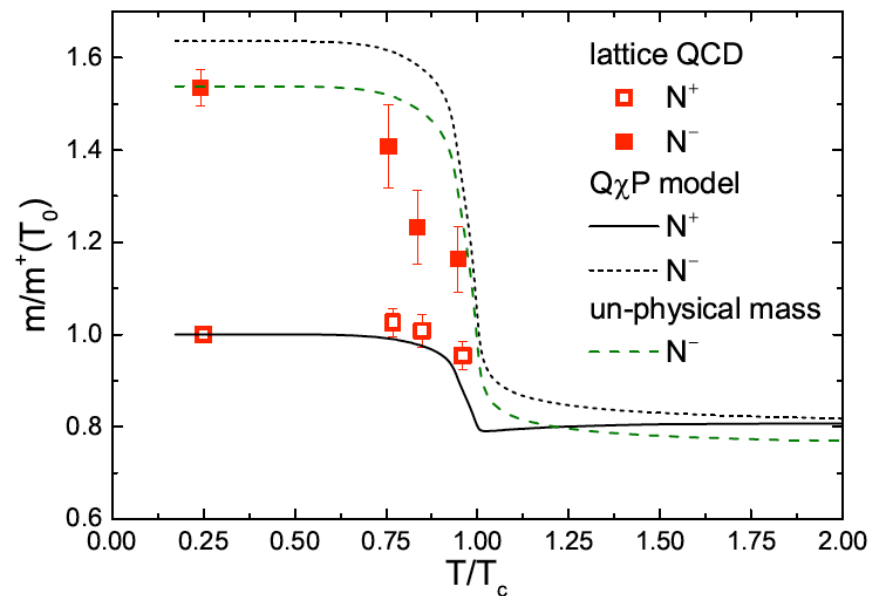
## Mass radius diagram for hybrid star



A number of observations (LMXB binary systems) point to a small radius of 9 - 11 km of typical neutron star

*e.g. Guillot et al. APJ 772, 7*

negative parity state on the lattice and in the model



*lattice data from Aarts et al, arXiv:1703.09246 [hep-lat]*



## Condensation of charged higher spin particles?

Heavy-ion collisions can generate very large B fields

W boson condensation at LHC? *Ambjørn, Olesen, PLB257, 201 (1991)*

*however, see SWS, Müller, A. Schramm, PLB 277, 512 (1992)*

$\rho$  mesons? Simple estimate requires  $B \sim 10^{20}$  G

*SWS, Müller, A. Schramm MPLA 7, 9773 (1992)*

heavy-ion collisions – bind away the whole mass of the particle

*Chernodub, Phys. Rev. Lett. 106, 142003*

*Hidaka, Yamamoto PRD87, 094502*

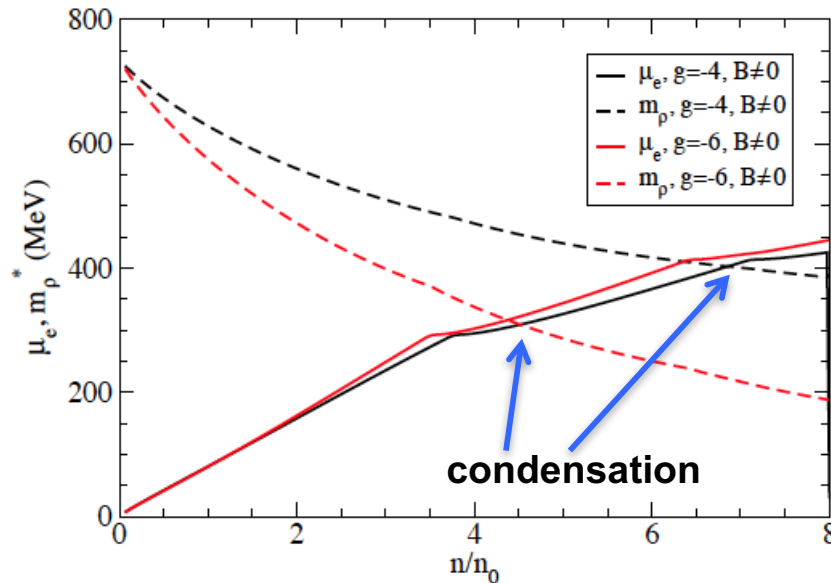
Advantage: high spin – strong interaction with magnetic field

Landau levels of the rho meson

$$E_{n,S_z}^2 = p^2 + m^2 + (2n - 2S_z + 1)eB$$

$$m_{\rho^-}^{2*} = m_{\rho^-}^2 - eB.$$

# charge chemical potential and effective rho mass as function of density



magnetars with surface fields up to  $10^{15}$  G

Use standard hadronic model GM3 parameterization

B value:  $7 \times 10^{18}$  G

slight change of star masses  
faster cooling

density dependence of rho mass ?

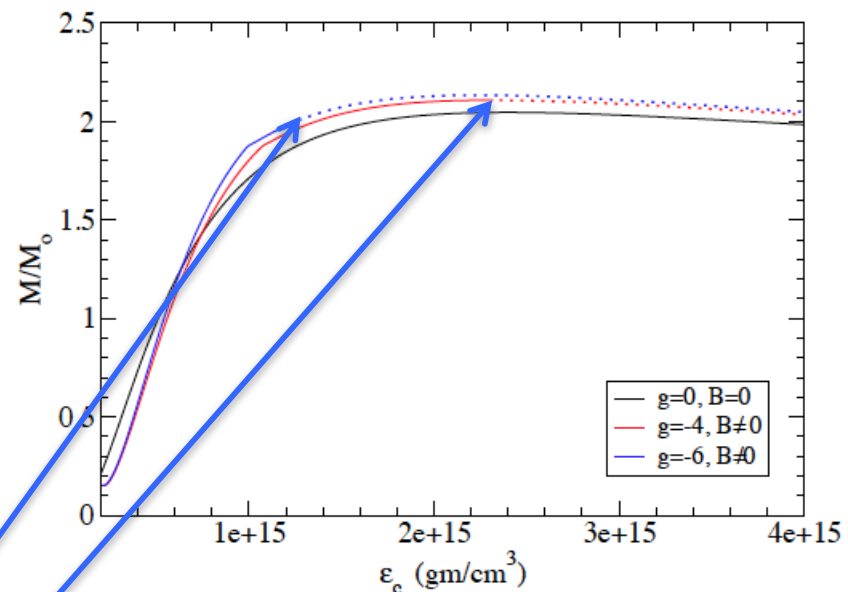
simple estimate  $m_\rho^* = m_\rho - g \sigma$

readjust  $g_{N\rho}$  to correct  
asymmetry energy  $a_{\text{sym}}$

range of g limited by slope of  $a_{\text{sym}}(\rho)$

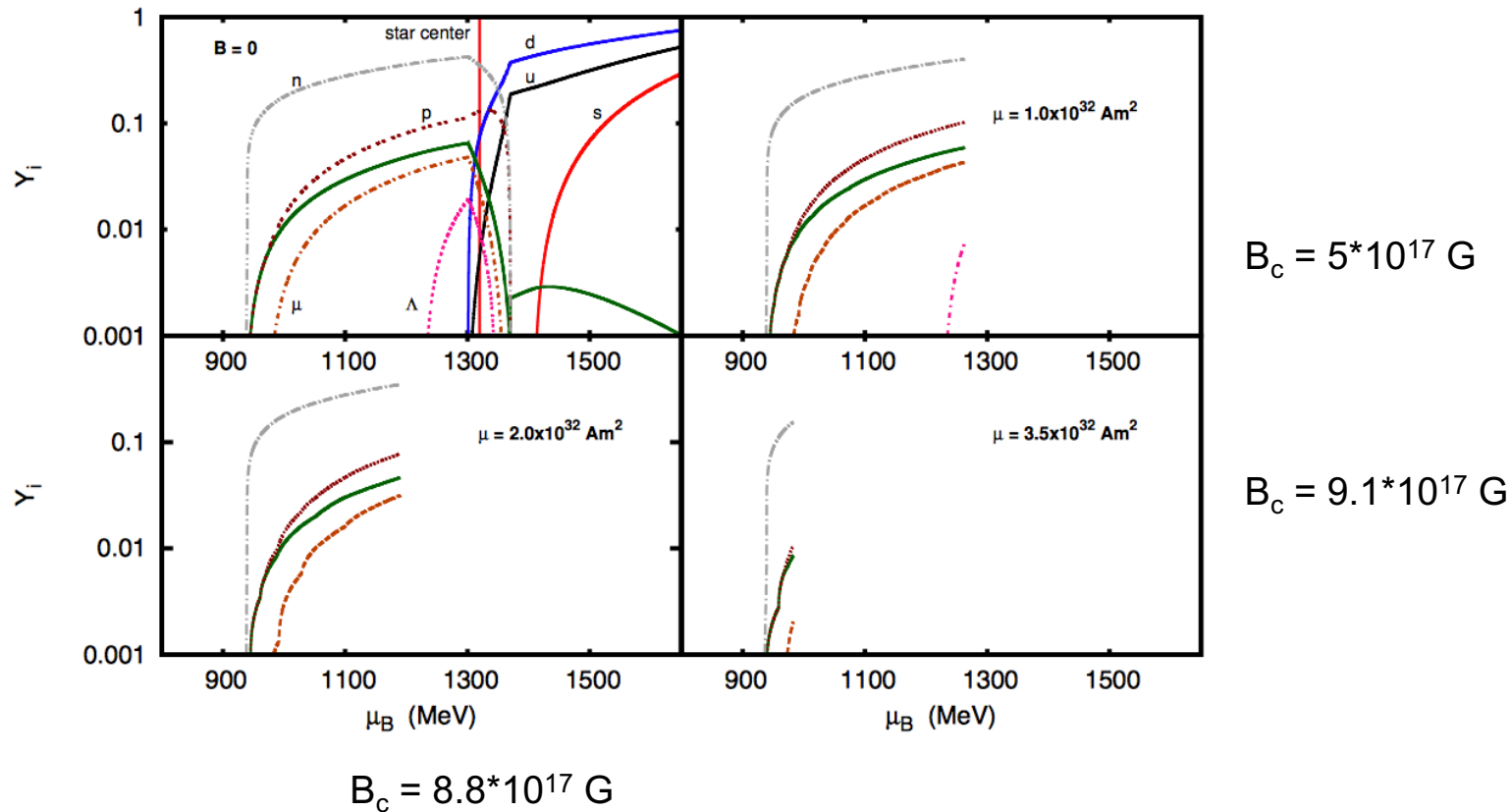
Mallick, Dexheimer, SWS, Bhattacharyya,  
MNRAS (2015)

first: Voskresensky PLB 1997  
Kolomeitsev, Voskresensky NPA 2005



onset of condensation

effect of strong magnetic fields on hybrid star



equation of state not strongly affected by B fields,  
but the population is!

possible backbending/spin-up for slow rotation

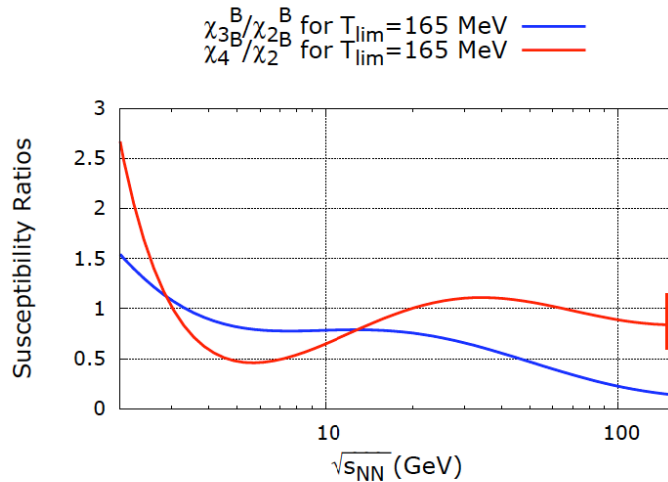
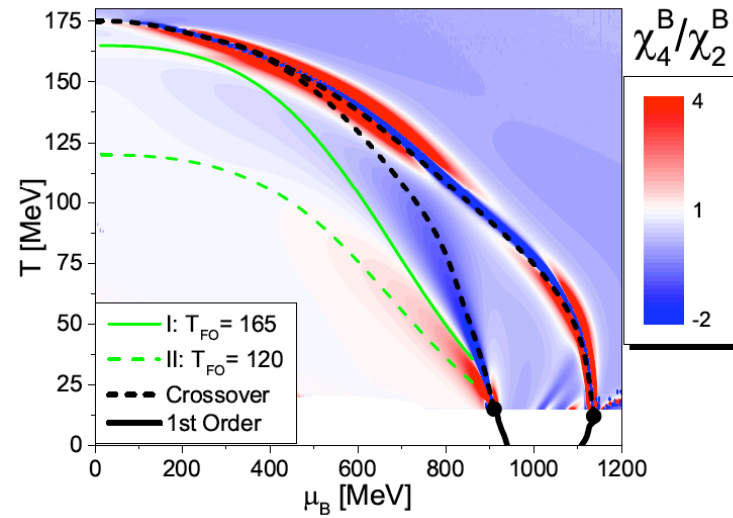
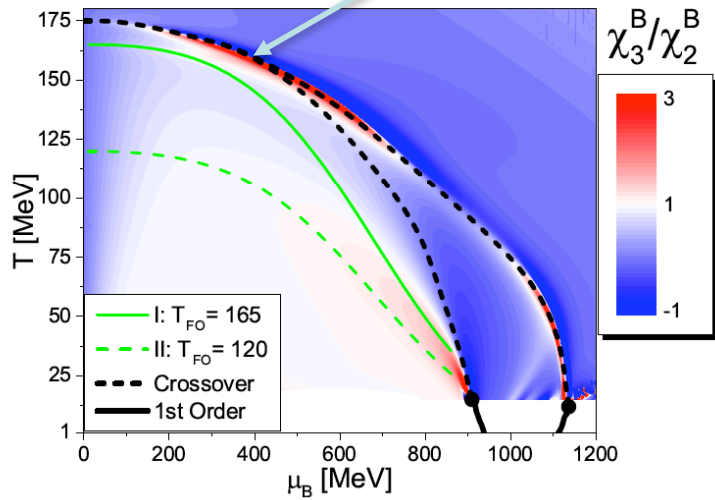
# Conclusions, Outlook

- coherent phenomenological model including reasonable asymptotic degrees of freedom
- heavy compact stars / hyper stars - little strangeness
- hybrid stars: stiff equation of state for quarks ? lattice susceptibilities
- large mixed phase in hybrid star
- rho meson condensate (just) possible
- magnetic fields remove quark core
- *comprehensive equation of state for a wide range of densities/temperatures (supernovae, mergers)*
- *consistent crust simulations*
- *couple hydro and kinetic equations for fields*

# fluctuations in heavy-ion collisions

susceptibilities  $\chi_n^B$  as marker of interesting phase structures

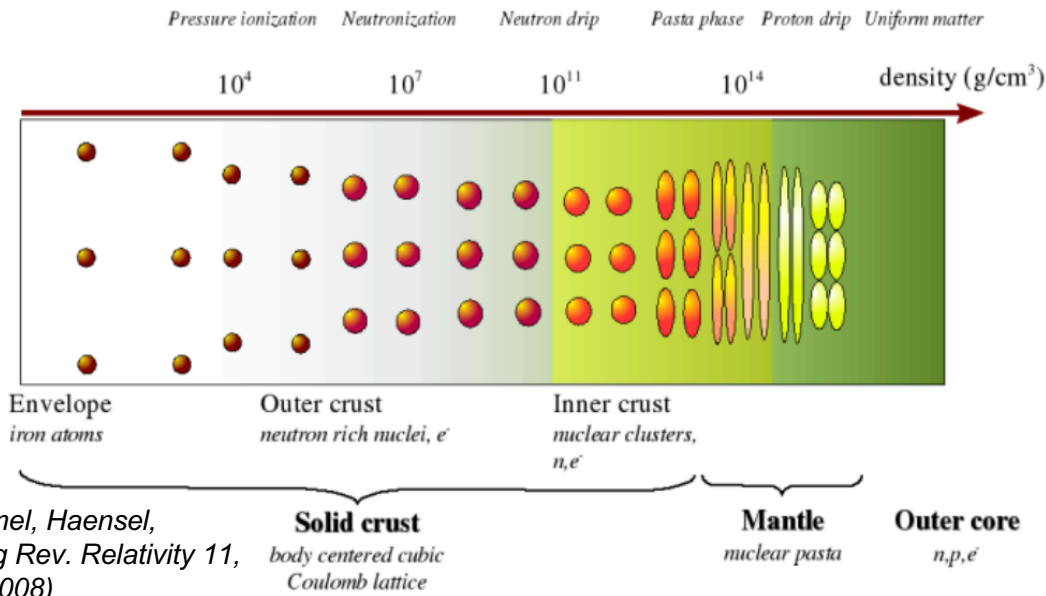
importance of liquid-gas transition



$$\chi_n^B \sim n! c_n^B$$

susceptibilities along freeze-out line  
(temperatures rescaled)

# structure of the crust



Chamel, Haensel,  
Living Rev. Relativity 11,  
10 (2008)

non-accreting crust

(BPS)     $\rho$  [g/cm<sup>3</sup>]

<sup>56</sup>Fe    8.1 × 10<sup>6</sup>

<sup>62</sup>Ni    2.7 × 10<sup>8</sup>

<sup>64</sup>Ni    1.2 × 10<sup>9</sup>

<sup>84</sup>Se    8.1 × 10<sup>9</sup>

<sup>82</sup>Ge    2.2 × 10<sup>10</sup>

<sup>80</sup>Zn    4.9 × 10<sup>10</sup>

<sup>78</sup>Ni    1.6 × 10<sup>11</sup>

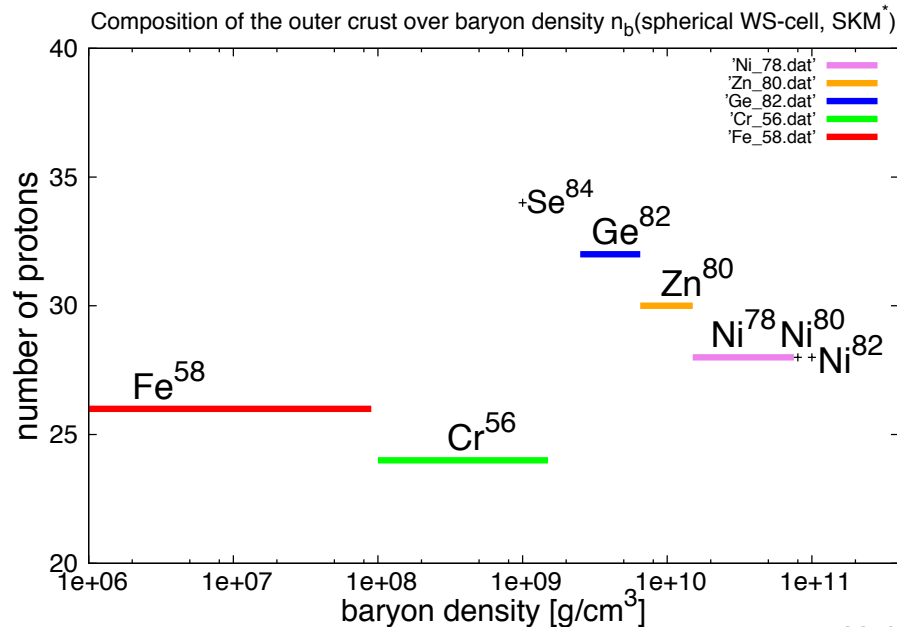
<sup>76</sup>Fe    1.8 × 10<sup>11</sup>

<sup>124</sup>Mo    1.9 × 10<sup>11</sup>

<sup>122</sup>Zr    2.7 × 10<sup>11</sup>

<sup>120</sup>Sr    3.7 × 10<sup>11</sup>

<sup>118</sup>Kr    4.3 × 10<sup>11</sup>

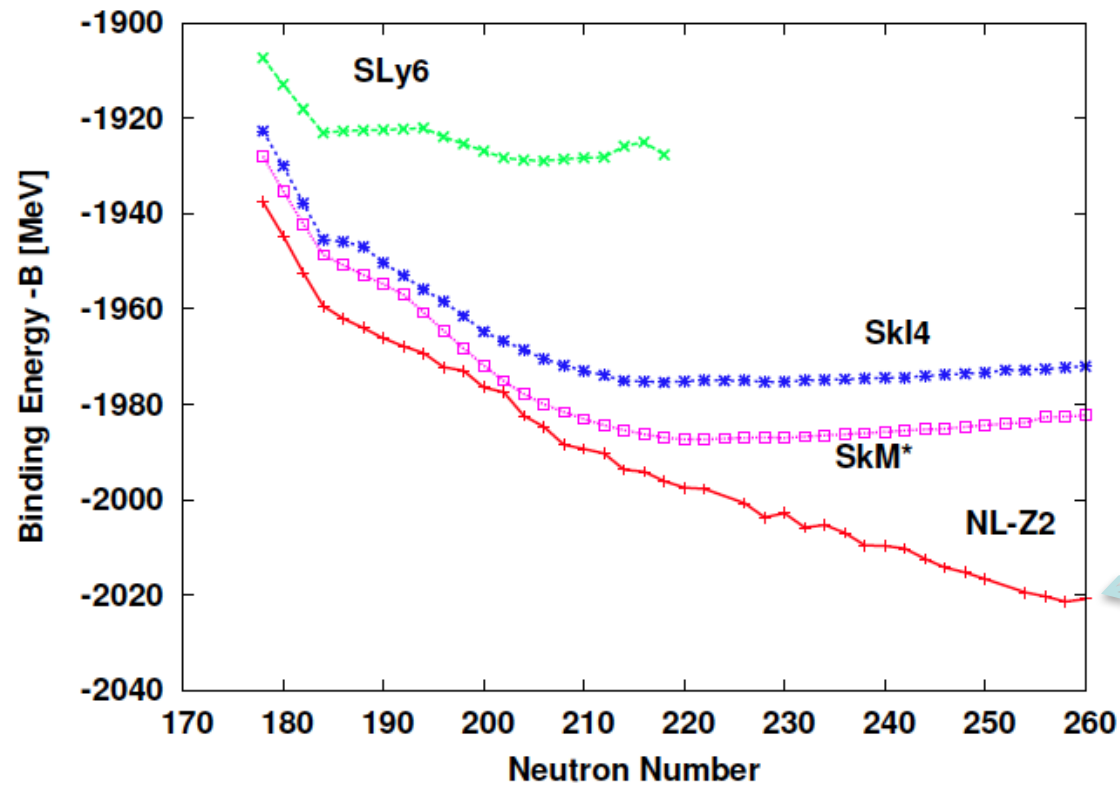


results can be very model-dependent

see e.g. Ruster et al, PRC 73, 035804 (2006)

extreme example - total binding energy  $-B$  (MeV) for Uranium Isotopes

side remark - drip line for heavy nuclei highly uncertain (far beyond crust conditions)



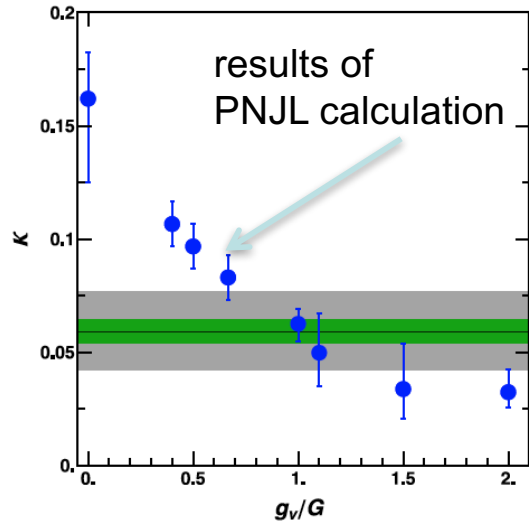
*more parameter sets  
behave similarly*

# signs of vector repulsion in $T_c(\mu)$ behavior

phase transition line very flat,  $T_c$  changes slowly with  $\mu$

curvature  $\kappa = -T_c \left. \frac{dT_c(\mu)}{d\mu^2} \right|_{\mu=0}$

plot taken from  
Bratovic et al, PLB 719, 131 (2013)



Lattice results Kacmarek et al  
PRD 83, 014504 (2011)

large quark vector repulsion?

turn on/off repulsion  
of quarks and baryons

quark interaction should be small  
in the hadron sector either heavy  
baryons and/or repulsion (liquid-gas,  
nuclei)

scalar field as function of  $\mu$   
for fixed  $T = 140$  MeV

