

Single Higgs production at LHC as a probe for an anomalous Higgs self coupling

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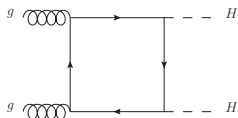
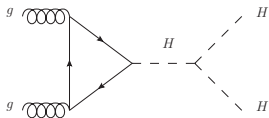


Based mainly on: G. Degrassi, PPG, F. Maltoni, D. Pagani [arXiv:1607.04251](https://arxiv.org/abs/1607.04251)

and G. Degrassi, M. Fedele, PPG [arXiv:1702.01737](https://arxiv.org/abs/1702.01737)

Outline

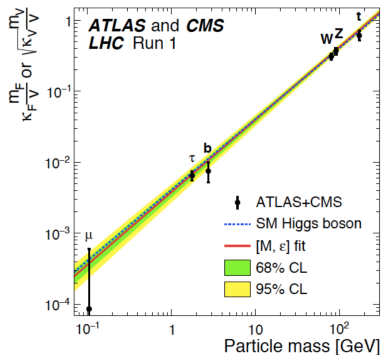
$$V(h) = \frac{1}{2}M_h^2 h^2 + \frac{M_h^2}{2v} h^3 + \frac{M_h^2}{8v^2} h^4$$



- 1 Introduction
- 2 Direct approach
 - Higgs Pair Production
 - κ_λ vs. EFT
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 - Precision Physics

A Standard Higgs

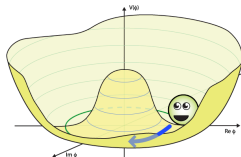
JHEP 1608 (2016) 045



- The Higgs still appears to be quite "Standard".
- The couplings with the vector bosons are compatible with the SM within a $\sim 10\%$ uncertainty,
- for the couplings to fermions the compatibility is within $\sim 15 - 20\%$ uncertainty.

But the situation with the Higgs self couplings is quite different.

The SM Higgs Potential



quantumdiaries.com

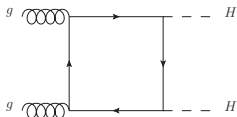
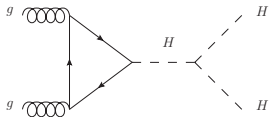
$$V(\phi) = -\mu^2(\phi^\dagger\phi) + \lambda(\phi^\dagger\phi)^2$$

$$V(h) = \frac{1}{2}M_h^2 h^2 + \frac{M_h^2}{2v} h^3 + \frac{M_h^2}{8v^2} h^4$$

- The self couplings are fixed once the Higgs mass and the vev are known.
- Trilinear coupling can be investigated at LHC from Higgs Pair Production.
- The quartic coupling will not be measured at LHC (or at ILC/CLIC).

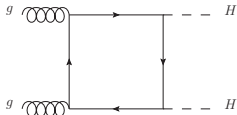
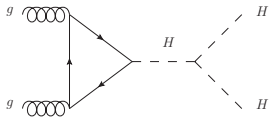
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$$V(h) = \frac{1}{2}M_h^2 h^2 + \frac{M_h^2}{2v} h^3 + \frac{M_h^2}{8v^2} h^4$$



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Higgs pair production



One vs. Two at 13 TeV

$gg \rightarrow H \sim 40 \text{ pb}$

$gg \rightarrow HH \sim 30 \text{ fb}$

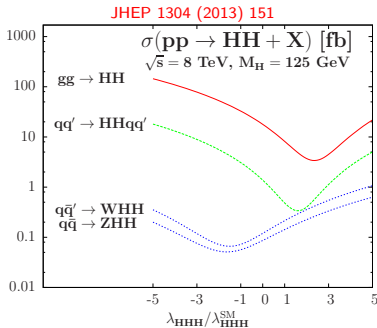
Very small Cross Section.

- Heavier final state.
- Additional weak coupling.
- Destructive interference.

Higgs pair production

The situation might change if we assume

$$V_{H^3} = \lambda_3 v H^3 \equiv \kappa_\lambda \lambda_3^{\text{SM}} v H^3.$$



One vs. Two at 13 TeV

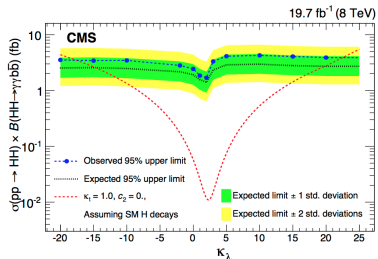
$gg \rightarrow H \sim 40 \text{ pb}$

$gg \rightarrow \text{HH} \sim 30 \text{ fb}$

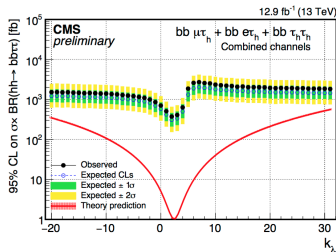
Very small Cross Section.

- Heavier final state.
- Additional weak coupling.
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Bounds on the anomalous trilinear



arxiv:1603.06896



PAS-HIG-16-028

Assuming no change in the other Higgs couplings at 8 TeV,

ATLAS and CMS constraints λ_3
 in the region

$$\mathcal{O}(\pm(15 - 20)\lambda_3^{\text{SM}})$$

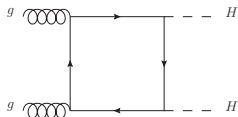
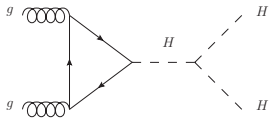
arXiv:1509.0467; arXiv:1506.0028; arXiv:1603.0689; ATLAS-CONF-2016-049

At 3000 fb⁻¹ λ_3 is constraint in the region $(-1.3, 8.7)\lambda_3^{\text{SM}}$

ATL-PHYS-PUB-2014-019; ATL-PHYS-PUB-2015-046

Outline

$$V(h) = \frac{1}{2}M_h^2 h^2 + \frac{M_h^2}{2v} h^3 + \frac{M_h^2}{8v^2} h^4$$



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The dimension 6 operator

$$V^{\dim-6}(\Phi) = V^{\text{SM}}(\Phi) + \frac{c_6}{v^2}(\Phi^\dagger\Phi)^3, \text{ with } \Phi = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi^+ \\ v + H + i\phi^0 \end{pmatrix}$$

$$\text{From the conditions } \left| \frac{dV^{\dim-6}(\Phi)}{d\Phi} \right|_{|\Phi|=v/\sqrt{2}} = 0,$$

$$\kappa_\lambda = 1 + \frac{2c_6 v^2}{m_H^2}$$

We need to impose that $\Phi = \frac{v}{\sqrt{2}}$ is still a global minimum.

$$V^{\dim-6}(v/\sqrt{2}) = \frac{c_6 v^4 - m_H^2 v^2}{8} < 0 = V^{\dim-6}(0) \rightarrow \kappa_\lambda < 3$$

C. Grojean, G. Servant and J. D. Wells; *Phys. Rev. D*71 (2005) 036001

P. Huang, A. Joglekar, B. Li and C. E. M. Wagner; *Phys. Rev. D*93 (2016) 055049

EFT vs. κ_λ

$\kappa_\lambda < 3$ is not very interesting for present phenomenology

More in general one can write $V^{NP} = \sum_{n=1}^N c_{2n} (\Phi^\dagger \Phi)^n$.

We ask the series to be convergent but we do not impose other conditions on c_{2n} .

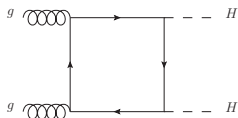
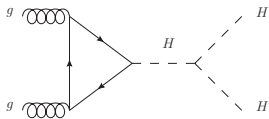
Expanding up to ϕ^4 ($\xi = \phi^+ \phi^- + \frac{1}{2} \phi_2^2$)

$$\begin{aligned} V_{4\phi}^{NP} &= \frac{m_H^2}{2v^2} \xi^2 + \left(\frac{m_H^2}{2v^2} + d\lambda_4 \right) \frac{1}{4} \phi_1^4 + \left(\frac{m_H^2}{2v^2} + 3d\lambda_3 \right) \xi \phi_1^2 \\ &\quad + \left(\frac{m_H^2}{2v} + d\lambda_3 \right) \phi_1^3 + \frac{m_H^2}{v} \xi \phi_1 + \frac{1}{2} m_H^2 \phi_1^2. \end{aligned}$$

$V_{4\phi}^{NP}$ gives the same results of the anomalous coupling, since contributions due to $d\lambda_4$ are zero at the order of our calculations.

Outline

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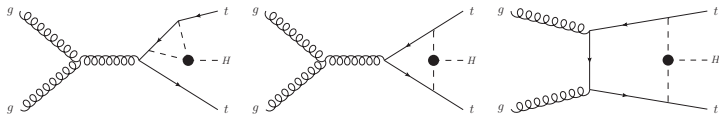


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Single Higgs at NLO

The trilinear appears at NLO in Single Higgs processes.

Due to the presence of different Loop structures these contributions cannot be captured by a local rescaling.



For similar ideas: [M. McCullough Phys. Rev. D90 \(2014\), no. 1 015001,](#)

[M. Gorbahn and U. Haisch, arXiv:1607.03773 \[hep-ph\]](#)

Calculation

Processes at NLO

$$\Sigma_{NLO} = Z_H \Sigma_{LO} (1 + \kappa_\lambda C_1)$$

- Σ_{LO} contains QCD corrections.
- C_1 depends on the process.
- Z_H is Higgs wave function renormalization,
- $Z_H = \frac{1}{1 - \kappa_\lambda^2 \delta Z_H}$

The range of validity of our calculation is $|\kappa_\lambda| \lesssim 20$

In general an Observable O can be written as

$$O = O^{\text{SM}} [1 + (\kappa_\lambda - 1) C_1 + (\kappa_\lambda^2 - 1) C_2]$$

Calculation

In general an observable O can be written as

$$O = O^{\text{SM}}[1 + (\kappa_\lambda - 1)C_1 + (\kappa_\lambda^2 - 1)C_2]$$

C_1 depend on the specific observable, \sqrt{s} , p_t cuts...

$$C_1 = \frac{\int 2\Re(\mathcal{M}^{0*} \mathcal{M}_{\lambda_3^{\text{SM}}}^1)}{\int |\mathcal{M}^0|^2}$$

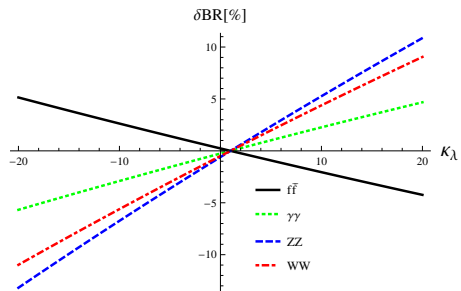
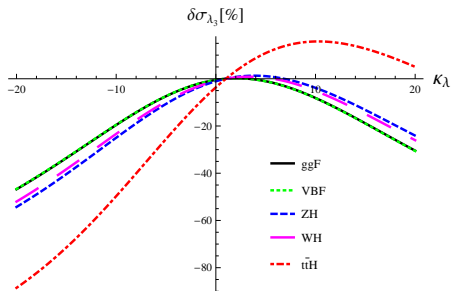
Amplitudes generated by FeynArts, computed by FormCalc interfaced to Loop-Tools,
checked with FeynCalc.

C_2 is calculated from δZ_H and does not depend on the observable.

C_1 coefficients

C_1^σ [%]	ggF	VBF	WH	ZH	$t\bar{t}H$
8 TeV	0.66	0.65	1.05	1.22	3.78
14 TeV	0.66	0.64	1.03	1.18	3.47

C_1^Γ [%]	$\gamma\gamma$	ZZ	WW	$f\bar{f}$	gg
on-shell H	0.49	0.83	0.73	0	0.66



Differential Information

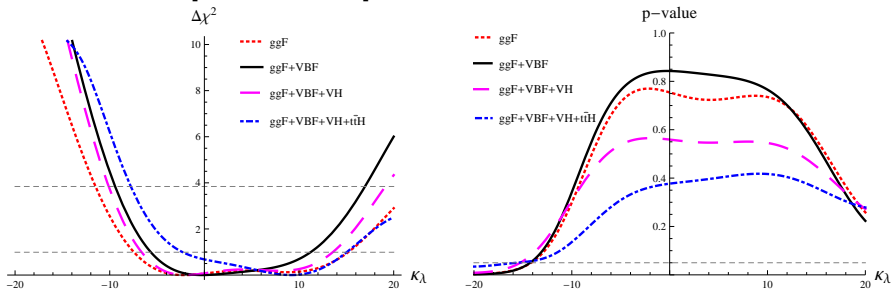
Further information can be in principle obtained from the kinematical dependence of the C_1 coefficients.

C_1^σ [%]	25 GeV	50 GeV	100 GeV	200 GeV	500 GeV
WH	1.71	1.56	1.29	1.09	1.03
ZH	2.00	1.83	1.50	1.26	1.19
$t\bar{t}H$	5.44	5.14	4.66	3.95	3.54

Table: C_1^σ at 13 TeV obtained by imposing the cut $p_T(H) < p_{T,\text{cut}}$, for several values of $p_{T,\text{cut}}$.

Present

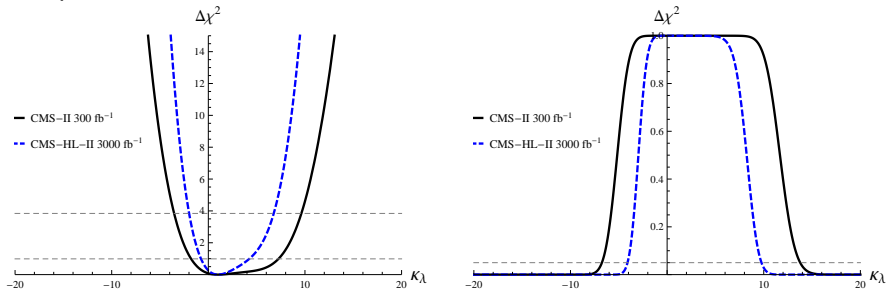
Fit on different "scenarios". Data from ATLAS-CMS 8 TeV data combination [JHEP 1608 (2016) 045]



- For ggF+VBF: $\kappa_\lambda^{\text{best}} = -0.24$, $\kappa_\lambda^{1\sigma} = [-5.7, 11.2]$, $\kappa_\lambda^{2\sigma} = [-9.4, 17.0]$.
- Requiring $p > 0.05$, we exclude at more than 2σ $\kappa_\lambda < -14.3$

Future

Using the uncertainties presented in [arXiv:1312.4974](https://arxiv.org/abs/1312.4974), and assuming that LHC will measure SM, we can estimate the future capabilities of LHC.

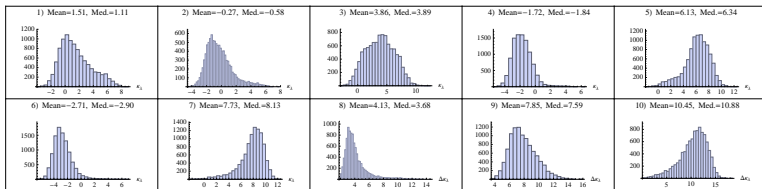


For CMS-HL-II 3000 fb⁻¹: $\kappa_\lambda^{1\sigma} = [-0.8, 4.2]$, $\kappa_\lambda^{2\sigma} = [-2.0, 6.8]$,
 $\kappa_\lambda^{p > 0.05} = [-4.1, 9.8]$.

Future

A more reliable approach is to consider central values compatible with SM.

We produce a collection of pseudo-measurements randomly generated with a gaussian distribution around the SM.



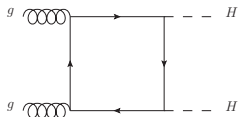
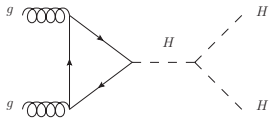
- 1) best values, 2) 1σ region lower limit, 3) 1σ region upper limit, 4) 2σ region lower limit, 5) 2σ region upper limit, 6) $p > 0.05$ region lower limit, 7) $p > 0.05$ region upper limit, 8) 1σ region width, 9) 2σ region width, 10) $p > 0.05$ region width.

$$\kappa_\lambda^{p>0.05} = [-2.8, 7.9]$$

$$\text{For ATLAS } 3000 \text{ fb}^{-1} \kappa_\lambda^{p>0.05} = [-1.3, 8.7]$$

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λ_3 -dependent contributions in m_W and $\sin^2 \theta_{\text{eff}}^{\text{lep}}$

Precision physics can also give informations on the trilinear.¹
The theoretical predictions of m_W and $\sin^2 \theta_{\text{eff}}^{\text{lep}}$ can be expressed in terms of physical quantities:

$$m_W^2 = \frac{\hat{\rho} m_Z^2}{2} \left\{ 1 + \left[1 - \frac{4\hat{A}^2}{m_Z^2 \hat{\rho}} (1 + \Delta \hat{r}_W) \right]^{1/2} \right\}$$

with $\hat{A} = (\pi \hat{\alpha}(m_Z) / (\sqrt{2} G_\mu))^{1/2}$.

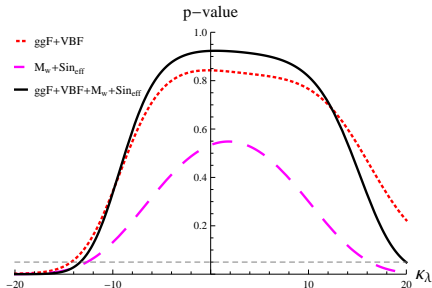
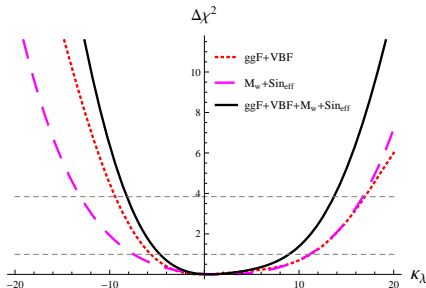
$\hat{\rho}$ and $\Delta \hat{r}_W$ are related to the Peskin-Takeuchi parameters T and S.

$$O = O^{\text{SM}} [1 + (\kappa_\lambda - 1) C_1 + (\kappa_\lambda^2 - 1) C_2]$$

¹ see also Kribs, Maier, Rzehak, Spannowsky, Waite arXiv:1702.07678

Results

	C_1	C_2
m_W	6.27×10^{-6}	-1.72×10^{-6}
$\sin^2 \theta_{\text{eff}}^{\text{lep}}$	-1.56×10^{-5}	4.55×10^{-6}



- $\kappa_\lambda^{\text{best}} = 0.5$, $\kappa_\lambda^{1\sigma} = [-4.7, 8.9]$, $\kappa_\lambda^{2\sigma} = [-8.2, 13.7]$.
- Requiring $p > 0.05$ we exclude at more than 2σ $\kappa_\lambda < -13.3$ and $\kappa_\lambda > 20.0$

FAQ

- In our fit we vary only the trilinear coupling. Is this a necessity? (e.g. arXiv: 1704.01953).
- We can have $k_\lambda \simeq 20$. Is this allowed by unitarity conditions? (Falkowski and Rattazzi private note: theory with only self-coupling modifications valid up to few TeV for $k_\lambda \lesssim 10$)
- Are there concrete models with k_λ so large? (arXiv: 1704.02311, arXiv: 1704.01953).

Conclusions

- No direct measurement of the Higgs self couplings. In particular of the trilinear.
- The Higgs trilinear coupling can be investigated from single Higgs processes.
- Compared to Higgs pair production, the bounds obtained are competitive and complementary.
- Precision physics can help further constraints the allowed region.