

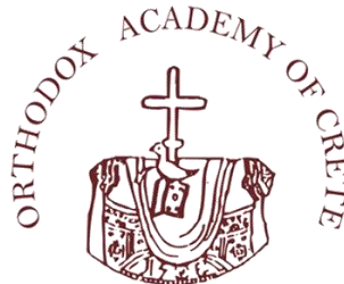
Exotic meson candidates from amplitude analyses of B meson decays

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Syracuse University



Workshop on Exotic Hadrons
ICNFP2017, Κολυμβάρι, Ελλάδα, 21-23 August 2017

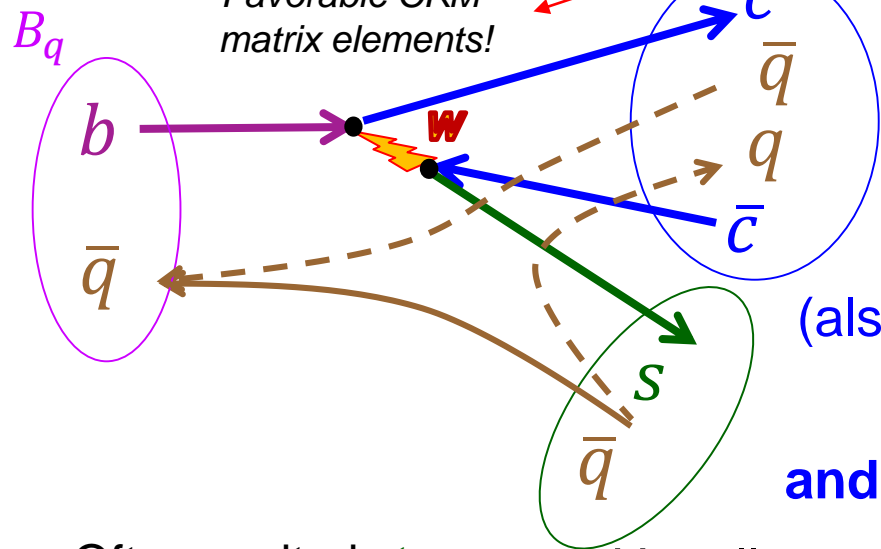


Decays of b hadrons as a source of charmonium(-like) states

Weak decay

→ long lifetime

Favorable CKM matrix elements!



The best trigger gateway at hadronic colliders

Source of charmonium states $c\bar{c}$:
 $\psi(n^3S), \chi_{cJ}(n^3P), \eta_c(n^1S), h_c(n^1P)$

Easiest to detect: $J/\psi, \psi(2S) \rightarrow \mu^+\mu^-, e^+e^-$
 then: $\chi_{c1} \rightarrow \gamma J/\psi$

(also of charmed meson-antimeson pairs $c\bar{q} + \bar{c}q$)

Dominate the decay rate

and of charmonium-like exotics $c\bar{c}q\bar{q}, \{c\bar{c}qqq\}$:

Usually tagged by decays to charmonium ($\rightarrow c\bar{c} + \text{light hadrons}$), while above the open charm threshold ($\rightarrow c\bar{q} + \bar{c}q$)

Smaller contributions

Often-excited strange meson {baryon} decaying to $K \{\Lambda\} + \text{light hadrons}$

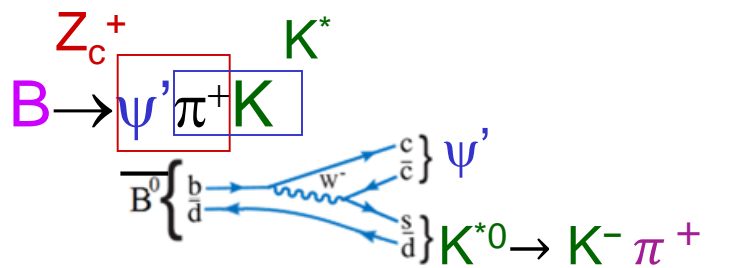
Lead to the same final states:

unless the exotic state is super narrow (*the X(3872) is the only case!*), difficulty in resolving the conventional and the exotic contributions;

a sophisticated amplitude analysis is necessary!

Strangeness in the final state helps background suppression, especially at LHCb

Discovery of Z(4430)⁺



Belle 2008

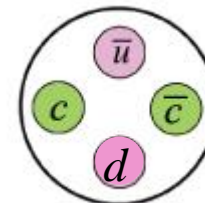
PRL 100, 142001 (2008)

1D $M(\psi' \pi^-)$ mass fit

“K* veto region”: suppress $K^*(892)$ and $K^*_2(1430)$

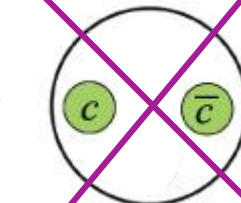
First charged charmonium-like state discovered!

charged

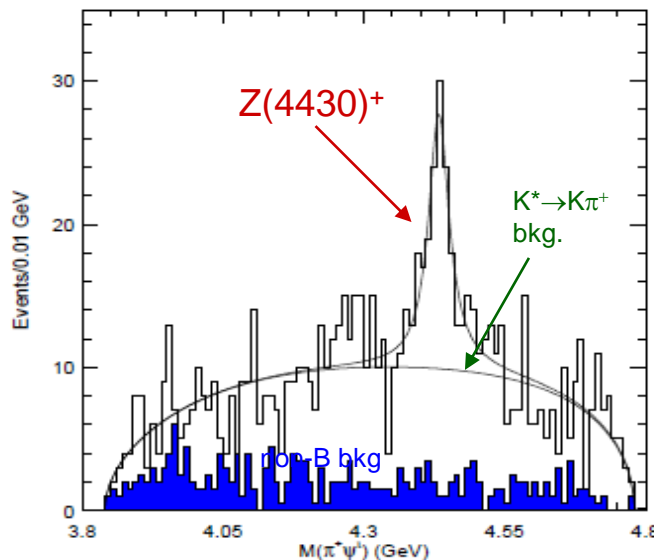
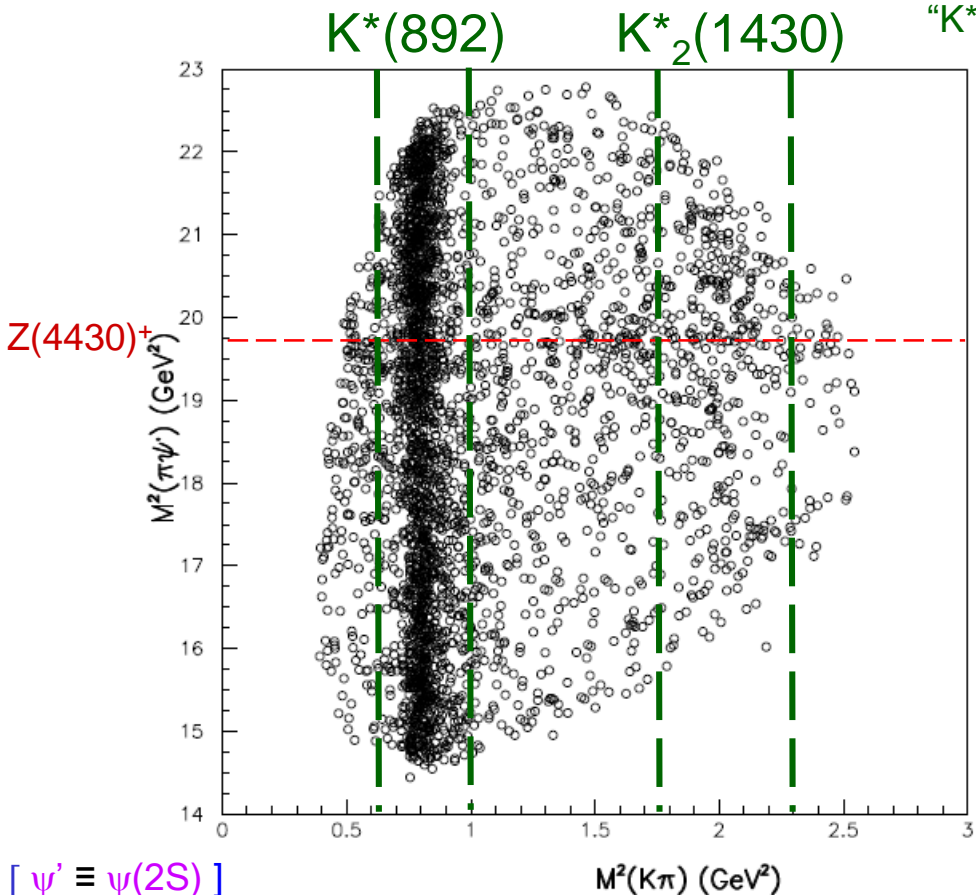


Exotic tetraquark, molecule, ...

neutral



Standard charmonium



$M(Z) = 4433 \pm 4 \pm 2 \text{ MeV}$

$\Gamma(Z) = 45^{+18}_{-13} \text{ MeV}$

significance 6.5σ

Press Release

Belle Discovers a New Type of Meson

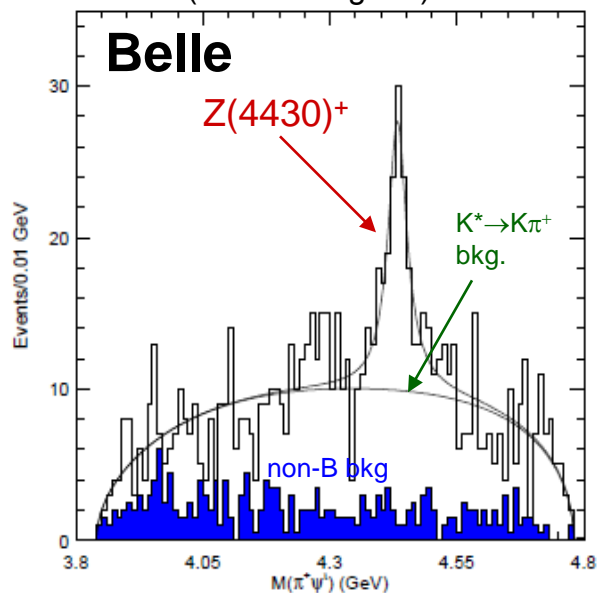
November 13, 2007
High Energy Accelerator Research Organization (KEK)

[$\psi' \equiv \psi(2S)$]

Lesson in importance of doing proper amplitude analysis

2008 1D $M(\psi'\pi^-)$ mass fit

PRL 100, 142001 (2008)
("K* veto region")



$$M(Z) = 4433 \pm 4 \pm 2 \text{ MeV}$$

$$\Gamma(Z) = 45_{-13}^{+18} \text{ MeV}$$

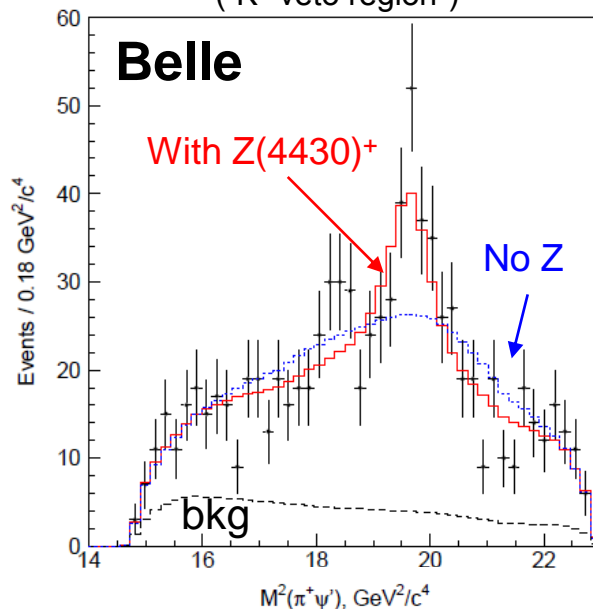
significance 6.5σ

Ad hoc assumption about $K^* \rightarrow K\pi^+$
background shape.

2009 2D amplitude ("Dalitz") fit

(same data)

PRD 80, 031104 (2009)
("K* veto region")



$$M(Z) = 4443_{-12}^{+15} \text{ MeV}$$

$$\Gamma(Z) = 107_{-43}^{+86} \text{ MeV}$$

significance 6.4σ

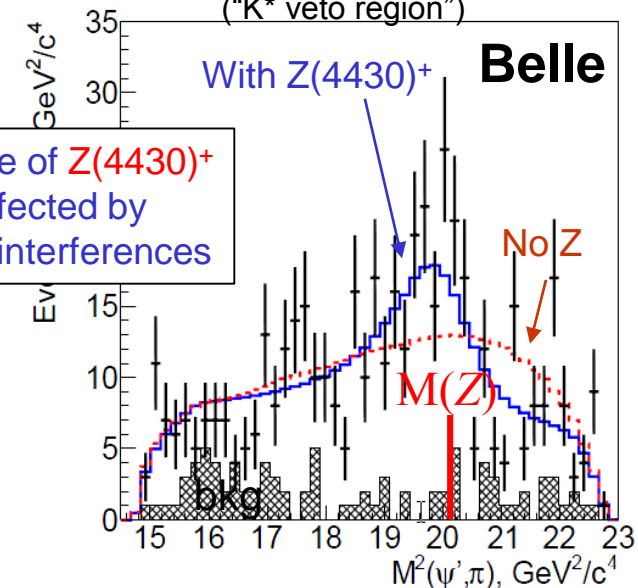
Proper model of $K^* \rightarrow K\pi^+$ resonances.

Neglect interplay of resonance interferences

2013 4D amplitude fit

(subsample with $\psi' \rightarrow l^+l^-$)

PRD 88, 074026 (2013)
 $0.996 \text{ GeV}/c^2 < M(K,\pi) < 1.332 \text{ GeV}/c^2$
("K* veto region")



$$M(Z) = 4485_{-22}^{+22} \text{ MeV}$$

$$\Gamma(Z) = 200_{-46}^{+41} \text{ MeV}$$

significance 6.4σ (5.6σ with sys.)

$J^P=1^+$ preferred by $>3.4\sigma$

Interferences properly implemented

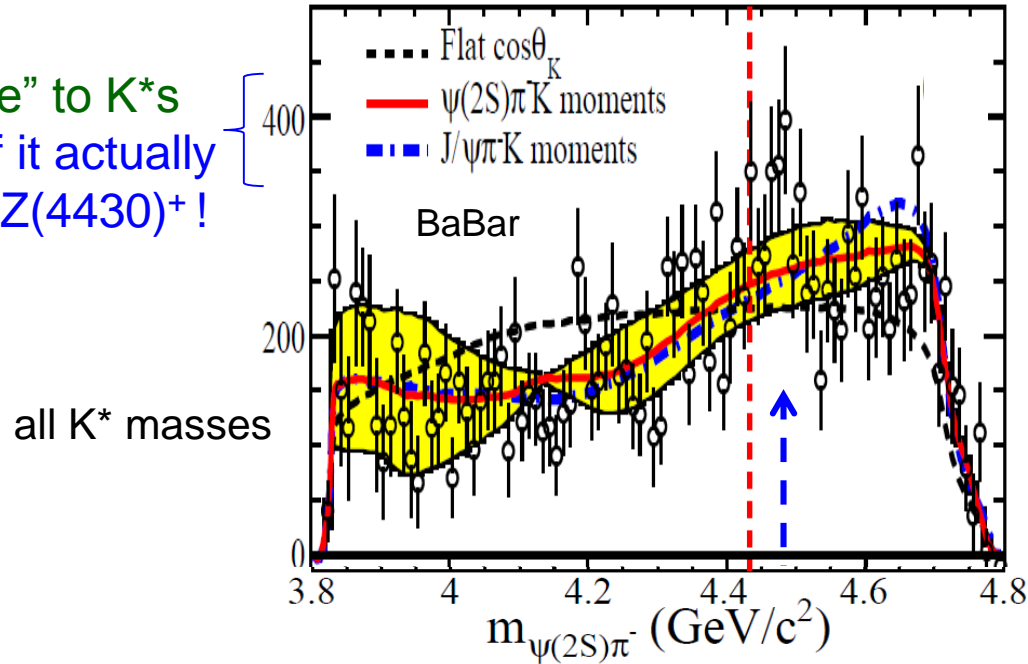
Naïve mass fits can lead to biased central values and severely underestimated errors!

BaBar puts $Z(4430)^+$ in limbo

BaBar PRD 79, 112001 (2009)

Data sample comparable to Belle (18% smaller)

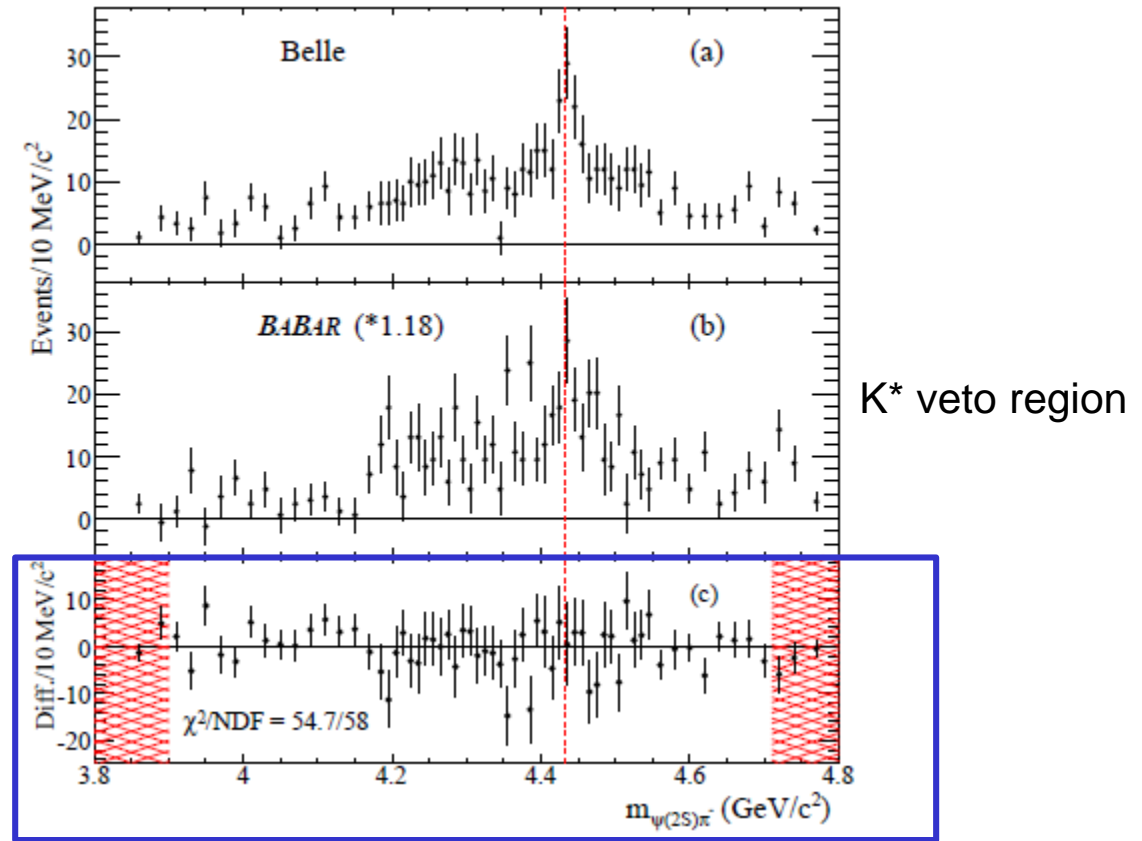
“Attributable” to K^* s
Some part of it actually comes from $Z(4430)^+$!



all K^* masses

$K\pi$ helicity angle moments analysis cannot possibly deal with Z - K^* interferences, thus any upper limits from this method are at best questionable!

2008 Z^+ mass
2013 Z^+ mass



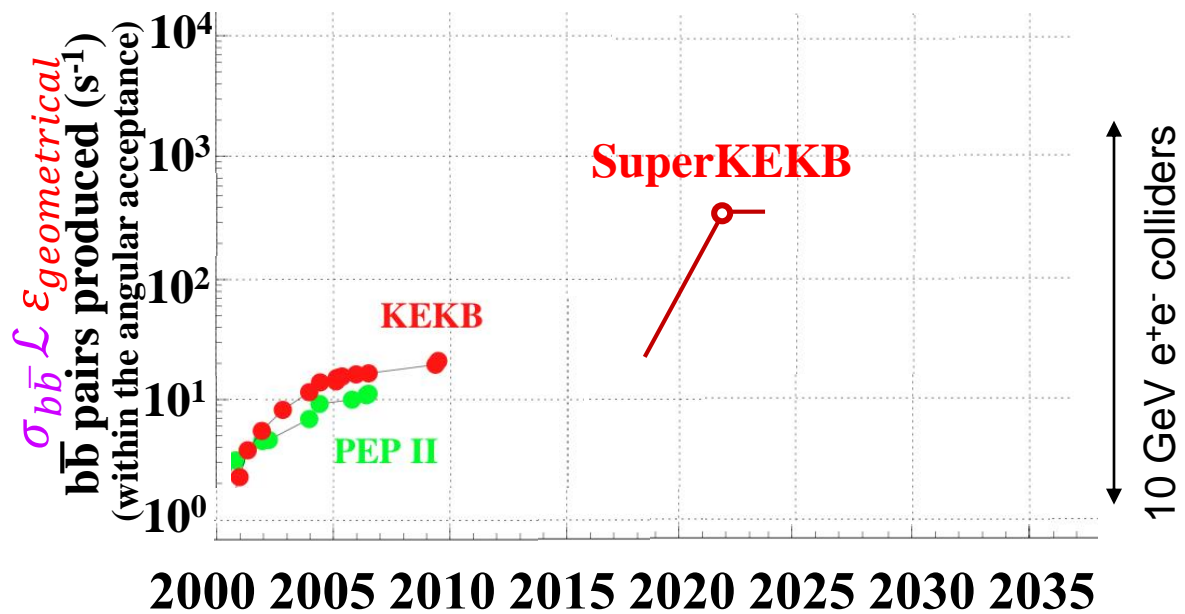
The data samples were fully compatible.

BaBar chose not to perform amplitude analysis...

Both samples have large statistical errors.

We see no significant evidence for a $Z(4430)^-$ signal for any of the processes investigated, neither in the total $J/\psi\pi^-$ or $\psi(2S)\pi^-$ mass distribution, nor in the corresponding distributions for the regions of $K\pi^-$ mass for which observation of the $Z(4430)^-$ signal was reported. We obtain branching-fraction upper limits $\mathcal{B}(B^- \rightarrow Z^- \bar{K}^0, Z^- \rightarrow J/\psi\pi^-) < 1.5 \times 10^{-5}$, $\mathcal{B}(B^0 \rightarrow Z^- K^+, Z^- \rightarrow J/\psi\pi^-) < 0.4 \times 10^{-5}$, $\mathcal{B}(B^- \rightarrow Z^- \bar{K}^0, Z^- \rightarrow \psi(2S)\pi^-) < 4.7 \times 10^{-5}$, and $\mathcal{B}(B^0 \rightarrow Z^- K^+, Z^- \rightarrow \psi(2S)\pi^-) < 3.1 \times 10^{-5}$ at 95% confidence level, where the $Z(4430)^-$ mass and width have been fixed to the reported central values.

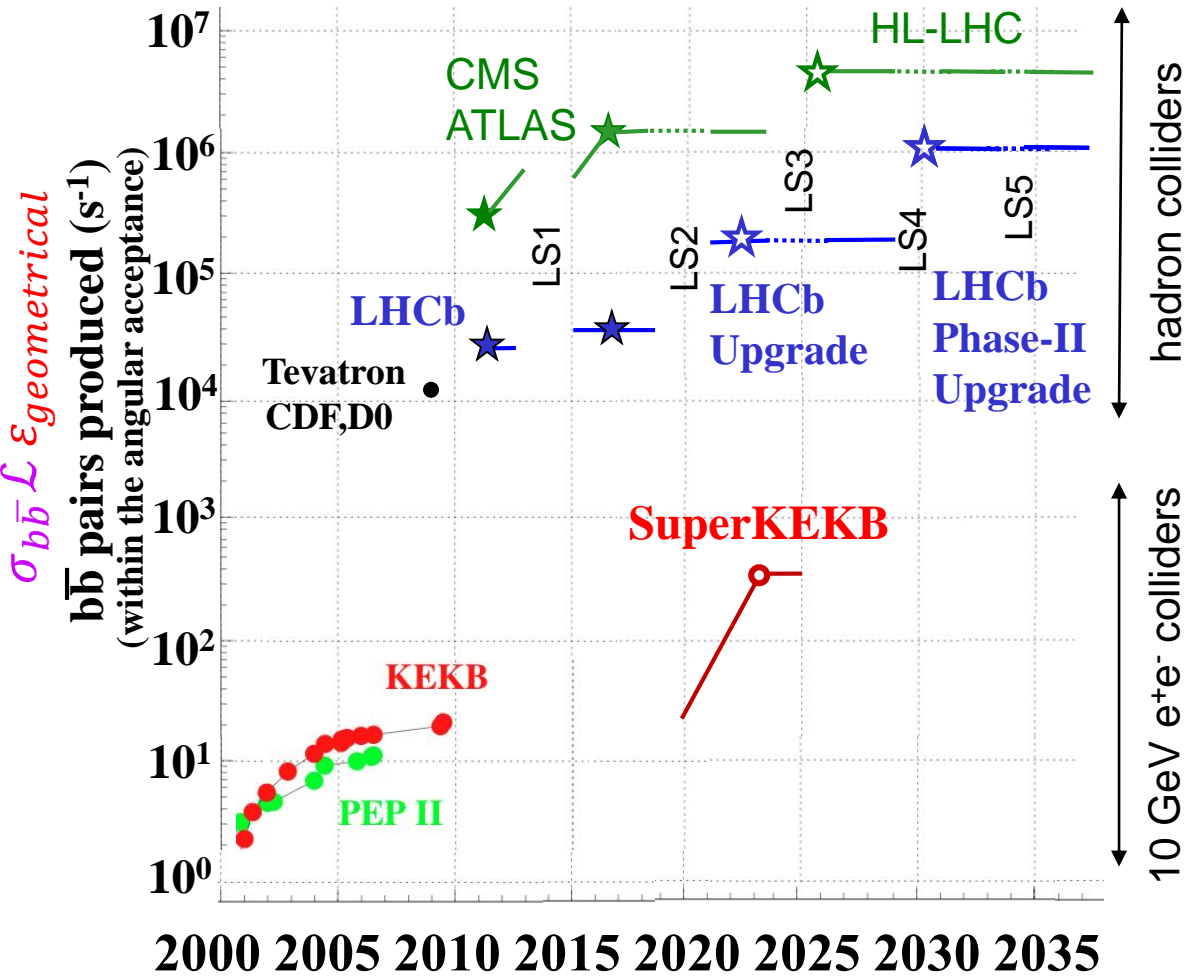
Colliders and $b\bar{b}$ rates



golden age of
10 GeV e^+e^- b-factories
(Belle & BaBar)

under construction
in Japan
(Belle II)

Colliders and $b\bar{b}$ rates



CDF 10 fb⁻¹ , D0 8 fb⁻¹
 LHCb Run I 3 fb⁻¹ Run II 5 fb⁻¹ Run III 50 fb⁻¹ Run IV 300 fb⁻¹ Run V+VI 300 fb⁻¹
 ATLAS,CMS 25 fb⁻¹ 450 fb⁻¹ 3000 fb⁻¹

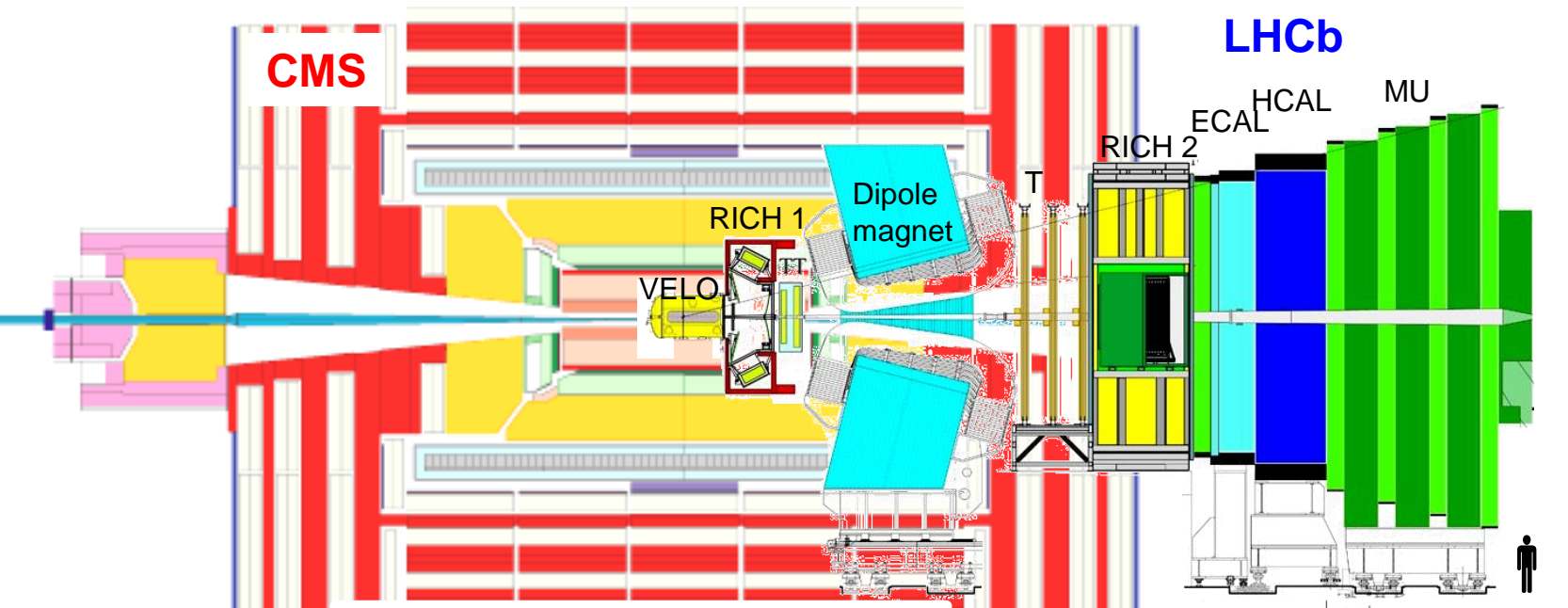
- Tremendous rate potential at hadron colliders
 - physics reach determined by the **detector capabilities** not by the machine
- Collect all b-hadron species at the same time:
 - additional gain by a factor of ~10-100 in integrated B_s rates at hadronic colliders
 - time dependent CPV studies of B_s possible
 - also get Λ_b, B_c which are out of reach of the 10 GeV e⁺e⁻ factories

$$\text{detected events } N = \text{produced events } \sigma_{b\bar{b}} \int \mathcal{L} dt \times \text{detector efficiency } \epsilon$$

$$\epsilon = \epsilon_{\text{geometrical}} \cdot \epsilon_{\text{trigger}} \cdot \epsilon_{\text{rest}}$$

major challenge for b,c physics at hadron colliders

LHCb vs central detectors



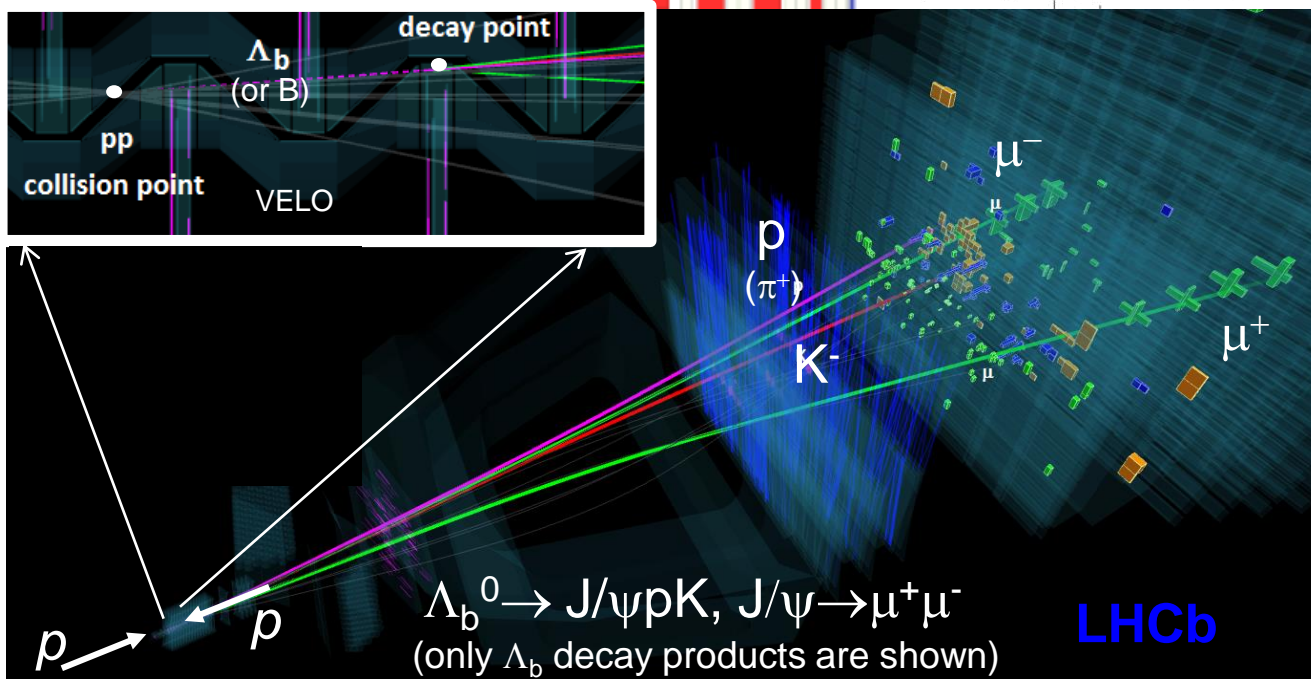
Advantages of LHCb (forward spectrometer):

- comparable b cross-section in much smaller solid angle; smaller number of electronic channels; smaller event size; **much larger trigger bandwidth to tape** (Run I ~ 5 kHz, Run II ~ 12 kHz)
- **b and c physics dominate the trigger bandwidth** (e.g. CMS b -trigger rate ~ 25 Hz; almost 3 orders of magnitude less than LHCb)
- large p for small p_T (in central region $p \sim p_T$); **can identify muons to lower p_T values**
- **large bandwidth important for triggering on purely hadronic final states** (central detectors limited to dimuon trigger)
- **large bandwidth important for collecting very large bottom & charm samples**
- space for RICH detectors: $p/K/\pi$ **separation**; crucial for background suppression in many channels; increased flavor tagging

Limitation of present LHCb detector:

- luminosity limited by the detector readout capabilities (**upgrades of the detector will allow increasing the luminosity**)
- compared to Belle: poor γ (i.e. π^0) and K_s detection (**will be improved in Phase II upgrade**)

Trigger on muons or decay points detached from pp collision point

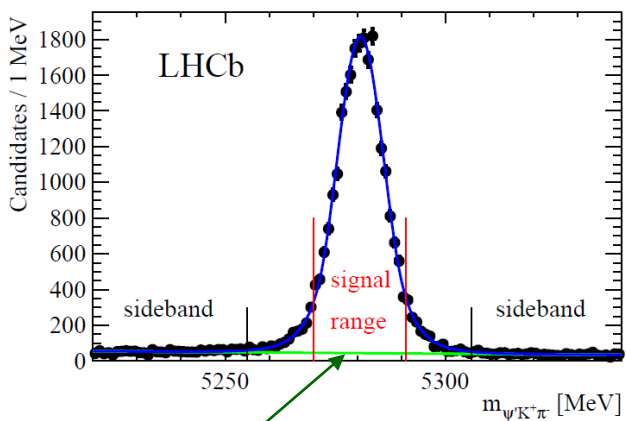


LHCb

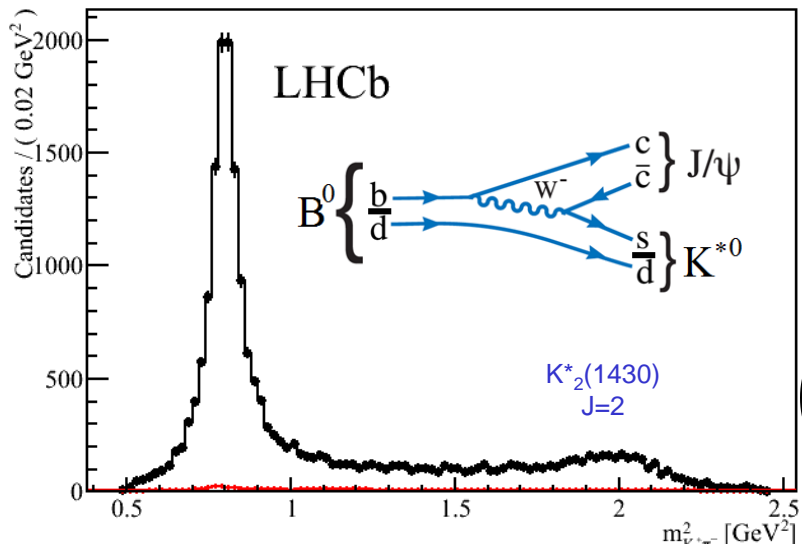
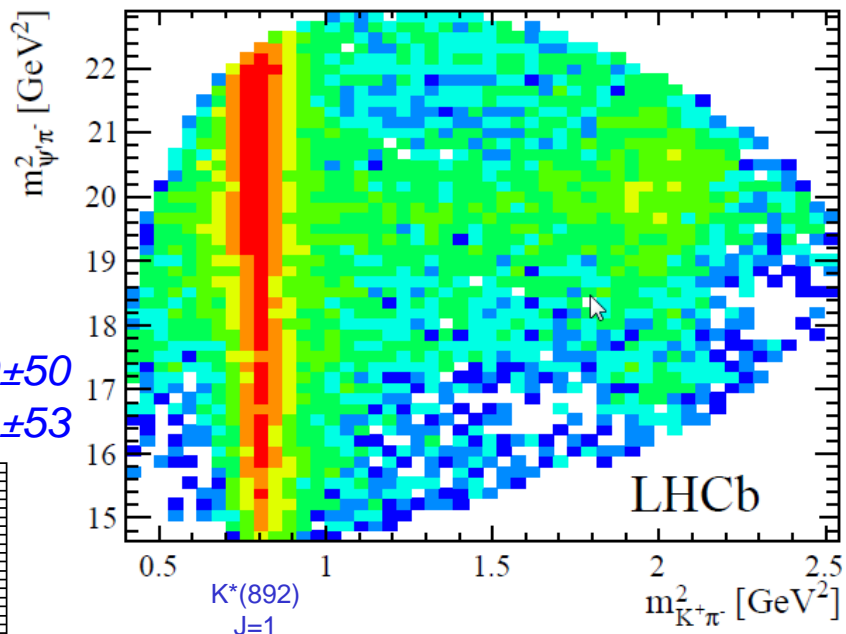
$\bar{B}^0 \rightarrow \psi' \pi^+ K^-$ in LHCb

LHCb PRL 112, 222002 (2014)

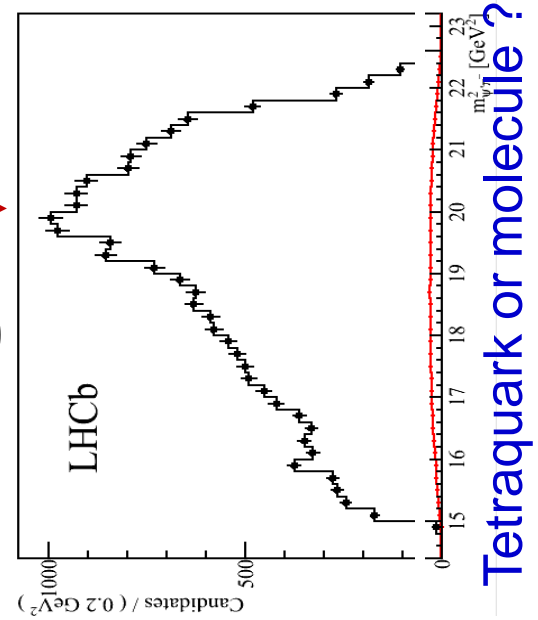
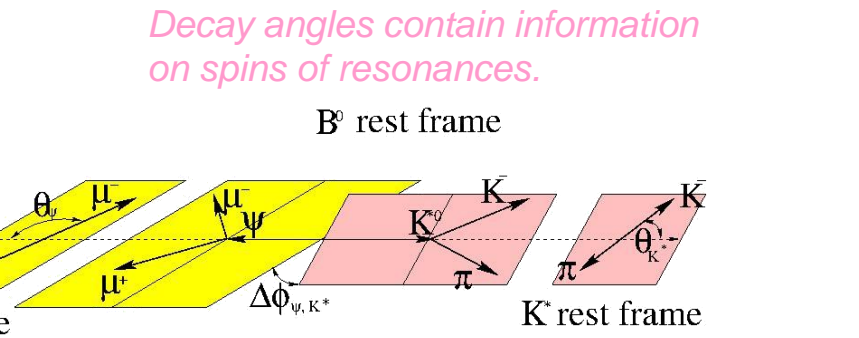
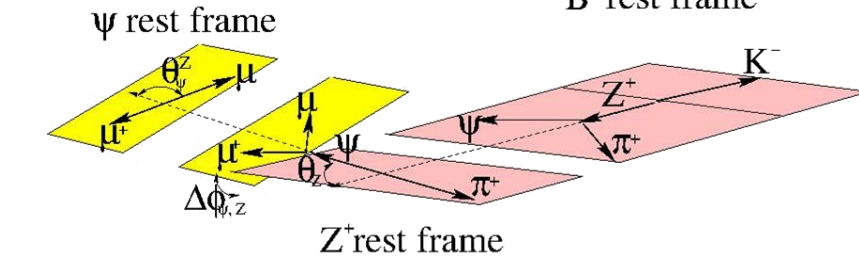
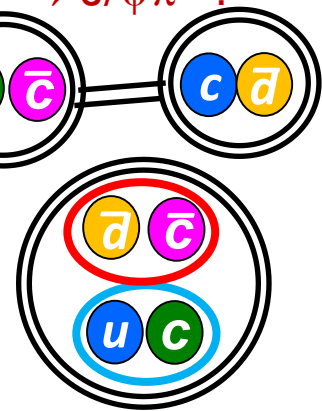
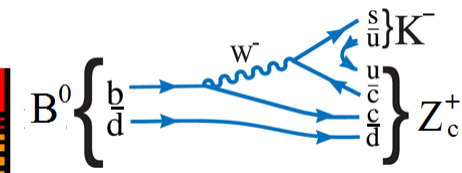
25,176 ± 174 signal events vs Belle: 2,010 ± 50
 BaBar: 2,021 ± 53



bkg (4.1 ± 0.1)% vs. bkg in Belle: 7.8%



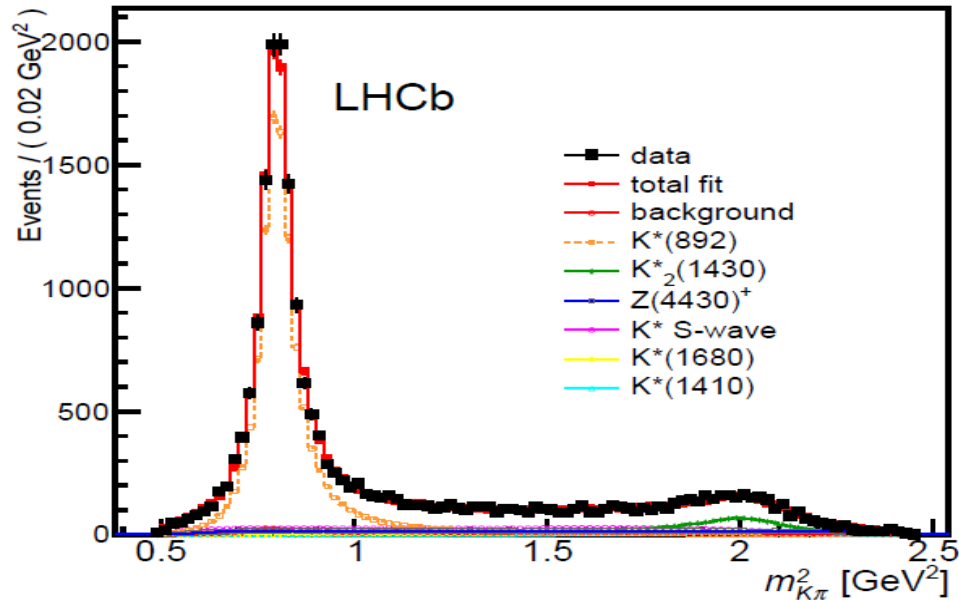
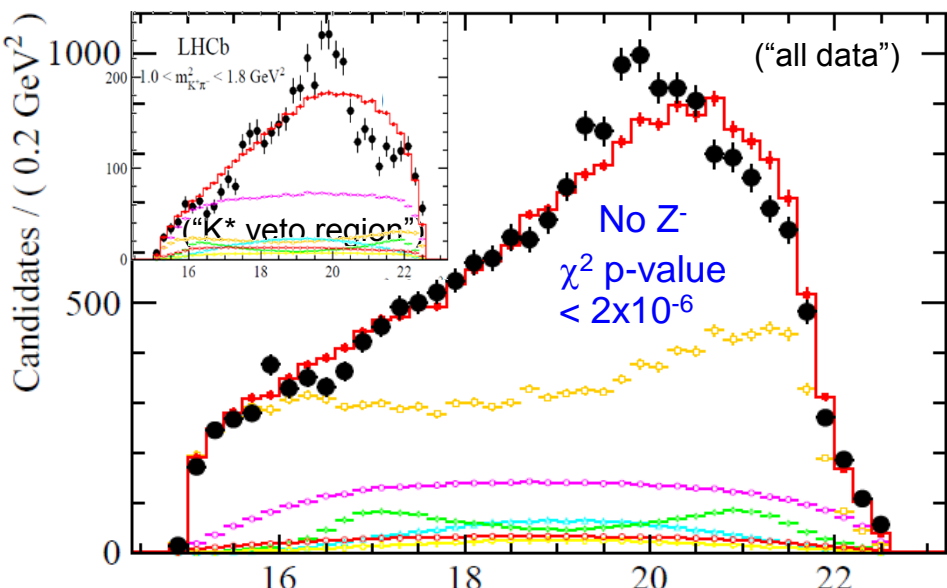
Kaon excitations



Tetraquark or molecule?

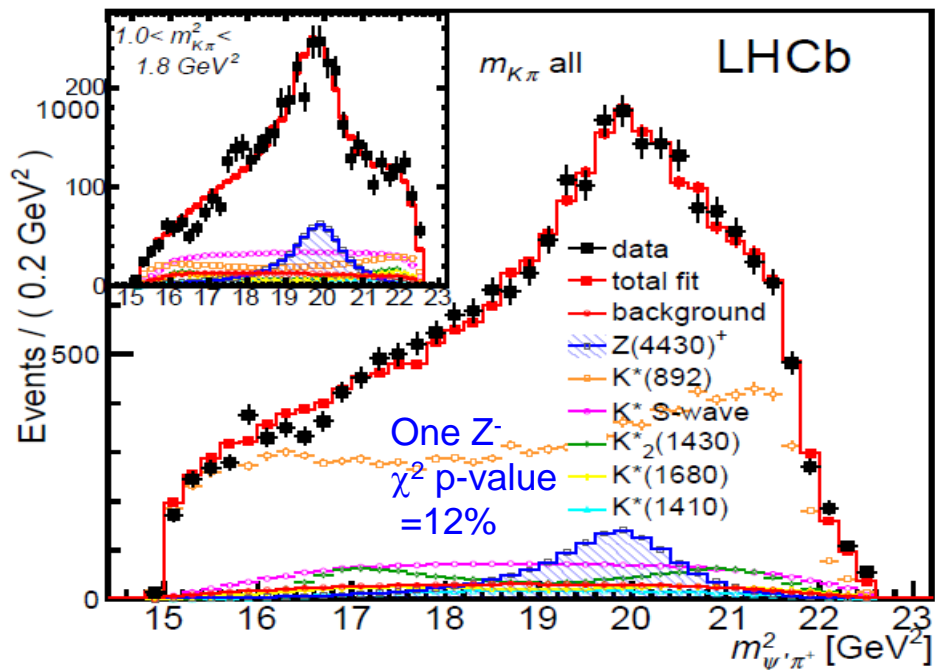
Decay angles contain information on spins of resonances.

Amplitude fits in LHCb: $Z(4430)^+$ confirmed



	Z(4430) ⁻ LHCb	Belle
$M(Z)$ [MeV]	$4475 \pm 7_{-25}^{+15}$	$4485 \pm 22_{-11}^{+28}$
$\Gamma(Z)$ [MeV]	$172 \pm 13_{-34}^{+37}$	200_{-46-35}^{+41+26}
f_Z [%]	$5.9 \pm 0.9_{-3.3}^{+1.5}$	$10.3_{-3.5-2.3}^{+3.0+4.3}$
f_{1-Z} [%]	$16.7 \pm 1.6_{-5.2}^{+2.6}$	
Significance	$> 13.9\sigma$	$> 5.2\sigma$
$J^P=1^+$	9.7σ	3.4σ

Excellent agreement !



2nd Z⁻ at lower mass?

$J^P=0^-$

$$M(Z_0) = 4239 \pm 18_{-10}^{+45} \text{ MeV}$$

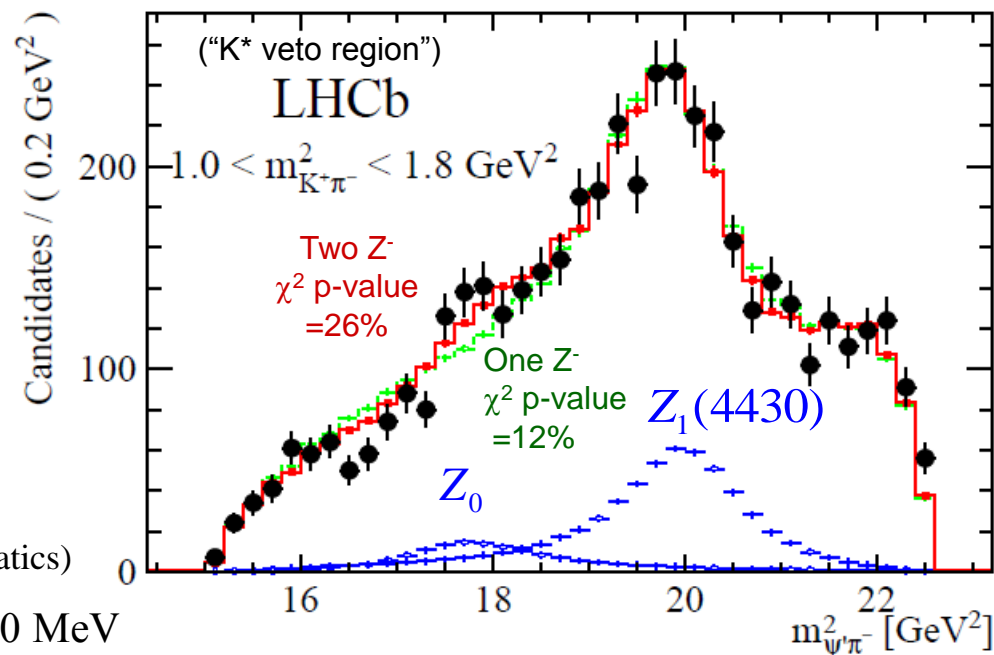
$$\Gamma(Z_0) = 220 \pm 47_{-74}^{+108} \text{ MeV}$$

$$f_{Z_0} = 1.6 \pm 0.5_{-0.4}^{+1.9} \%$$

$$f_{Z_0}^I = 2.4 \pm 1.1_{-0.2}^{+1.7} \%$$

6 σ significance (with systematics)

$J^P=1^+$ also possible $\Gamma=660 \pm 150 \text{ MeV}$

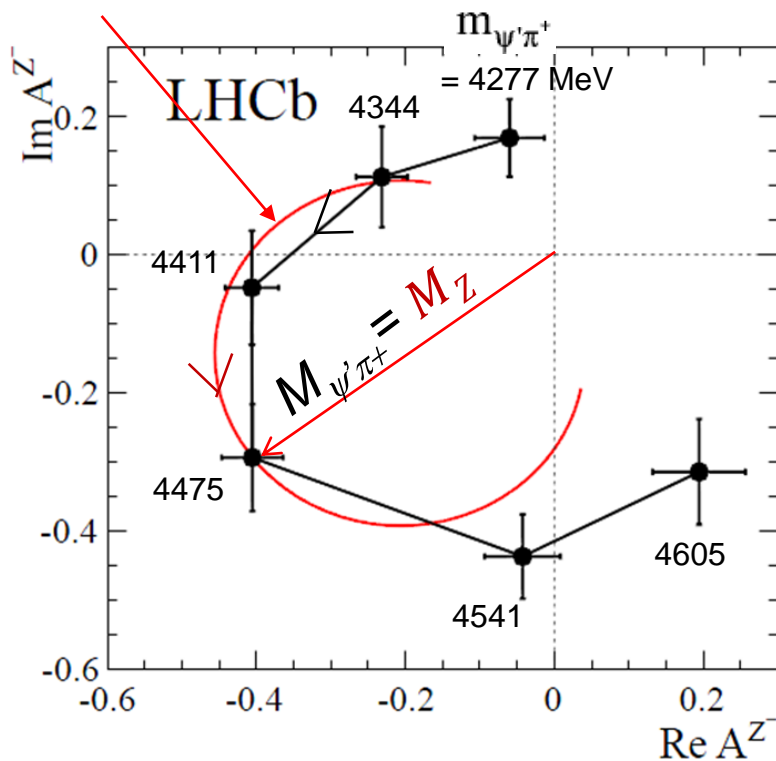


Argand diagram of Z(4430)⁺

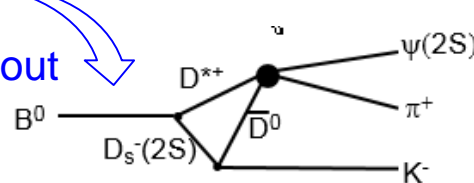
- Thanks to the large data statistics LHCb has been able to extract Argand diagram of Z(4430)⁺ amplitude from its interference with the K^{*} amplitudes:

$$\frac{1}{M_Z^2 - m_{\psi'\pi^+}^2 - i M_Z \Gamma_Z}$$

Breit-Wigner
amplitude

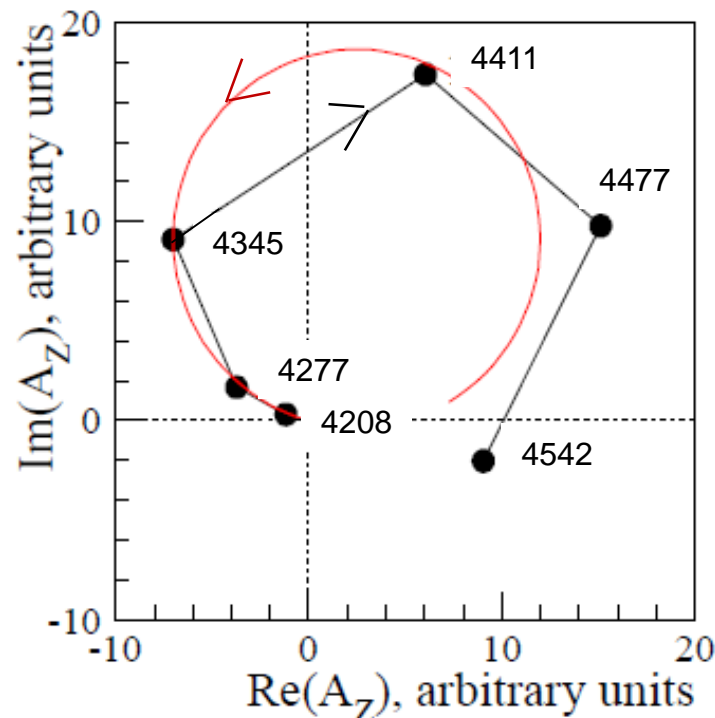


rules out



rescattering
model

P. Pakhlov, T. Ugllov
PL B748, 183 (2015)



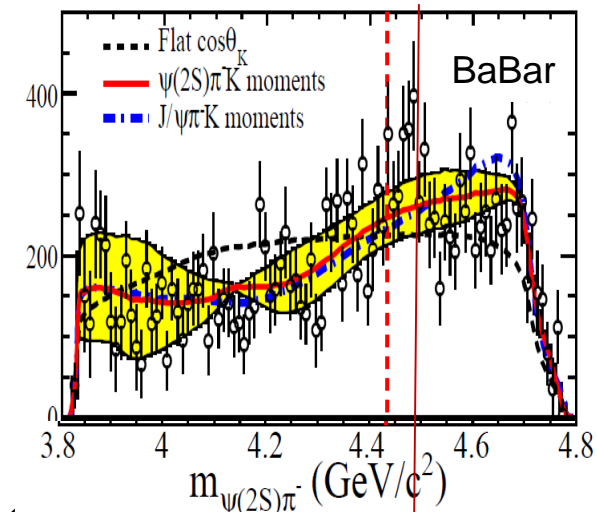
However, the predictions of Pakhlov-Ugllov model do not reflect generic behavior of triangle anomalies, which can generate counterclockwise phase changes – just not as circular as the one from a resonance.

Improving experimental precision of Argand diagram determination is highly desired.

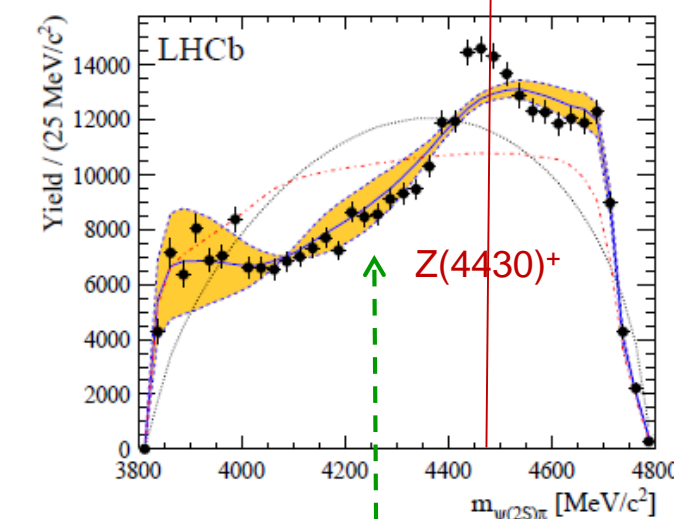
Model independent analysis a la BaBar



BaBar PRD 79, 112001 (2009)

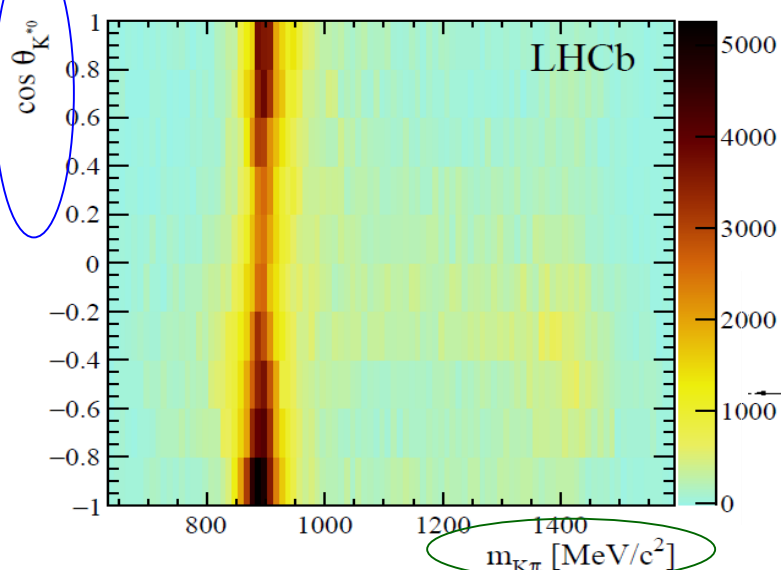


LHCb PRD 92, 112009 (2015)

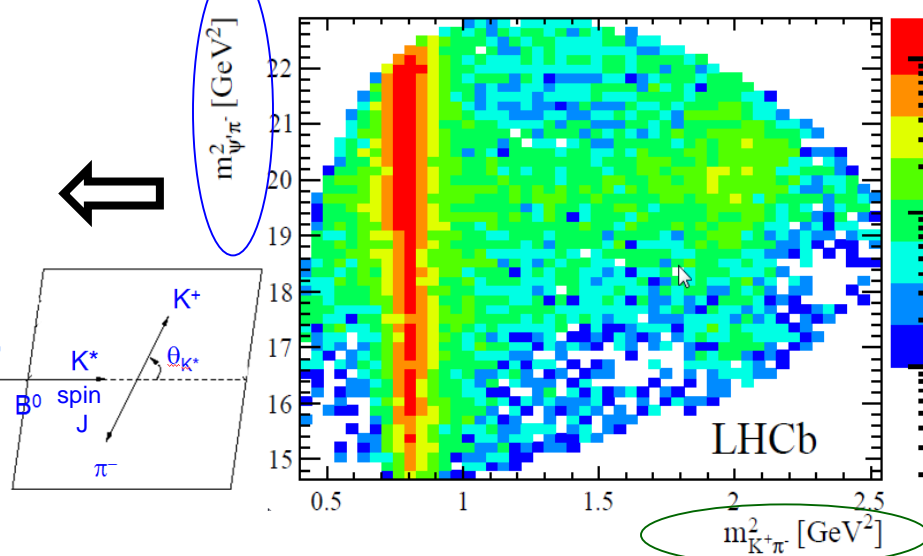


The lack of “access” at 4239 MeV implies nothing. This method is not sensitive to small and broad structures (see PRL, 117, 082002 (2016)).

Efficiency-corrected “rectangular” Dalitz plot



Dalitz plot



Decompose into Legendre moments

$$\langle P_l^U \rangle = \sum_{i=1}^{N_{data}} \frac{1}{\epsilon_i} P_l(\cos \theta_{K^*i})$$

vs. $m_{K+\pi^-}$

Pass only moments with l not more than $l_{max} = J_{max}/2$

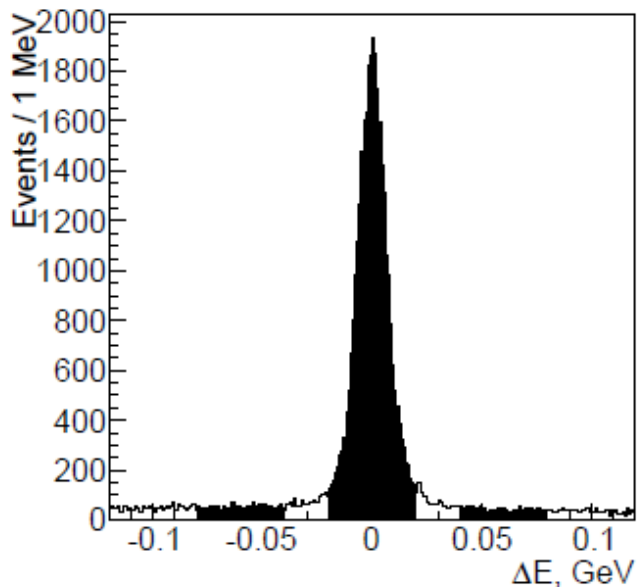
J_{max} limited from QM and scattering experiments

- LHCb data inconsistent with K^* contributions alone ($>8\sigma$)
- BaBar did not have enough statistics to “see” Z(4430) this way.

$\bar{B}^0 \rightarrow J/\psi \pi^+ K^-$ in Belle

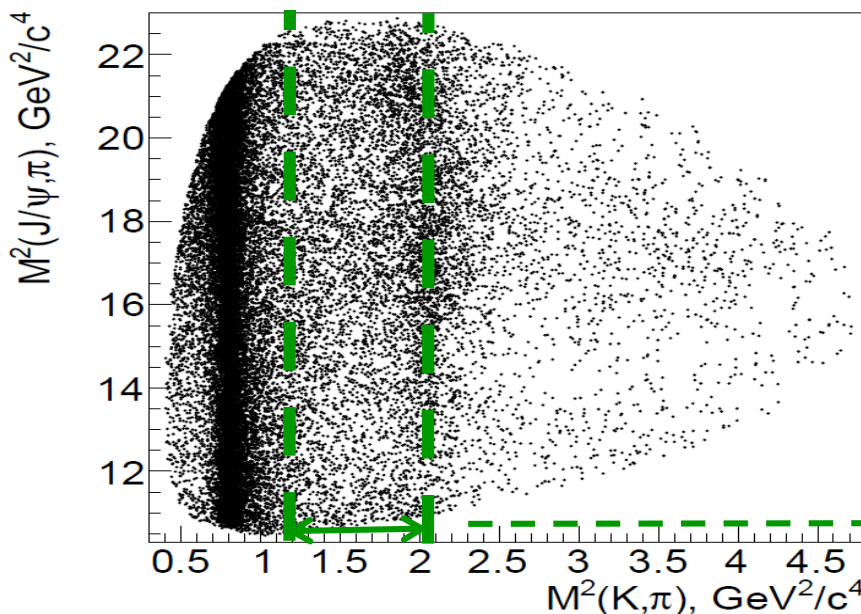
Belle PR D90, 112009 (2014)

29,990 ± 190
signal events

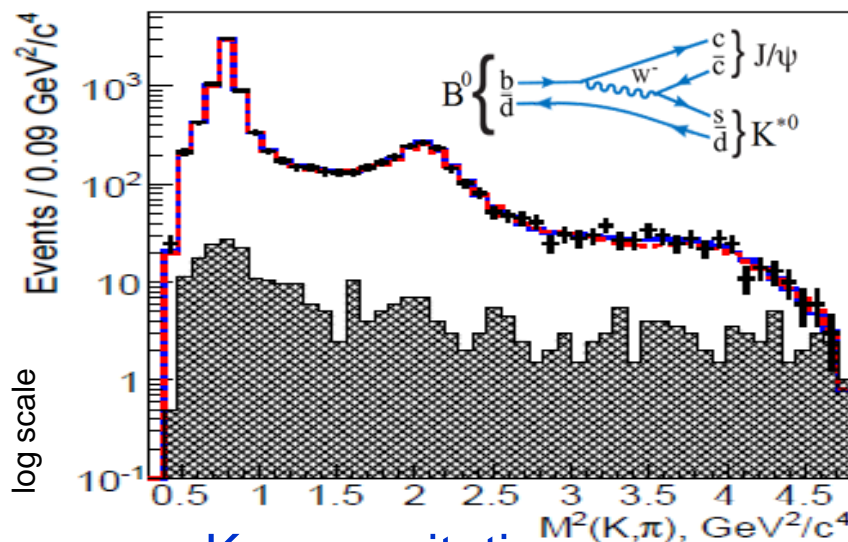


bkg 5.6%

Larger BR → as good a sample as $\bar{B}^0 \rightarrow \psi' \pi^+ K^-$ in LHCb



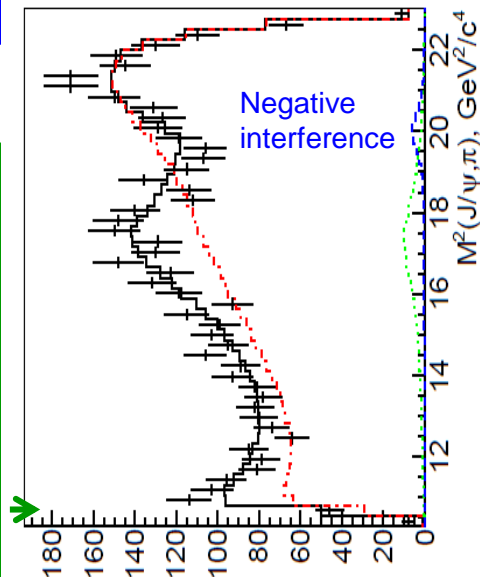
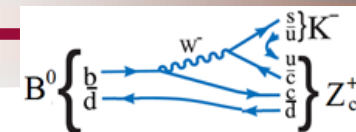
$16 \text{ GeV}^2/c^4 < M^2(J/\psi, \pi) < 19 \text{ GeV}^2/c^4$



Kaon excitations

Significance	5.1σ
f_Z [%]	$(0.5^{+0.4}_{-0.1})\%$
$Z_c(4430)^+ \rightarrow J/\psi \pi^+$	
$Z_c(4200)^+ \rightarrow J/\psi \pi^+$	
$M(Z)$ [MeV]	4196^{+31+17}_{-29-13}
$\Gamma(Z)$ [MeV]	$370^{+70+70}_{-70-132}$
f_Z [%]	$(1.9^{+0.7}_{-0.5})\%$
Significance	6.2σ
$J^P=1^+$	4.4σ

Small fit fractions!



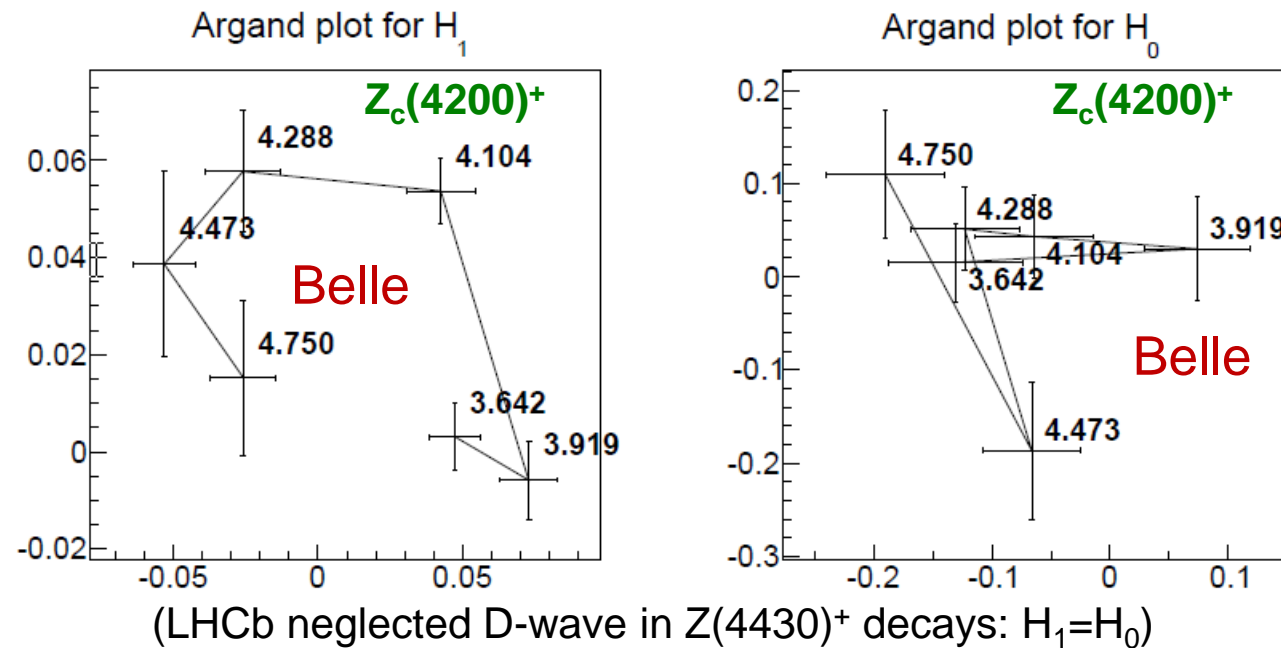
Tetraquark or meson-meson molecule

- The $Z_c(4430)^+$ observed in the 2nd decay mode!
 - However, with the mass and width fixed in the fit; not quite an independent confirmation of the resonance
- A broad but significant 2nd 1⁺ resonances at the lower mass, $Z_c(4200)^+$
 - Possibly the same structure as observed by the LHCb in $\bar{B}^0 \rightarrow \psi' \pi^+ K^-$ (1⁺ was not ruled out by LHCb)

$\bar{B}^0 \rightarrow J/\psi \pi^+ K^-$ in Belle

- Is the $Z_c(4200)^+$ a resonance, given its large width?

Encouraging results; higher data statistics are needed (and available in LHCb!)



Z(4430)⁺, Z(4200)⁺ production and decay rates

Belle PR D88, 074026 (2013)

$$\mathcal{B}(B^0 \rightarrow Z(4430)^- K^+) \times \mathcal{B}(Z(4430)^- \rightarrow \psi' \pi^-) = (6.0_{-2.0}^{+1.7+2.5}) \times 10^{-5},$$

Averaging fit fractions as determined by Belle & LHCb [PRL 112, 222002 (2014)], $(6.6 \pm 1.6)\%$, and using PDG for $\mathcal{B}(B^0 \rightarrow Z(4430)^- K^+)$

$$\mathcal{B}(B^0 \rightarrow Z(4430)^- K^+) \times \mathcal{B}(Z(4430)^- \rightarrow \psi' \pi^-) = (3.8 \pm 1.0) \times 10^{-5}$$

$$\mathcal{B}(Z(4430)^- \rightarrow \psi' \pi^-) / \mathcal{B}(Z(4430)^- \rightarrow J/\psi \pi^-) = 7.0_{-4.4}^{+2.6}$$

Motivates models which can explain the preference for ψ' in spite of the smaller phase-space (a factor of 0.6)

LHCb 0⁻ Z(4239)⁻

$$\mathcal{B}(B^0 \rightarrow Z(4239)^- K^+) \times \mathcal{B}(Z(4239)^- \rightarrow \psi' \pi^-) = (0.9_{-0.4}^{+1.2}) \times 10^{-5}$$

The Z_c^+ states observed in $e^+ e^- \rightarrow \pi^- Z_c^+$ not observed in $\bar{B}^0 \rightarrow Z_c^+ K^-$ and vice versa

BaBar PR D79, 112001 (2009)

$$\mathcal{B}(\bar{B}^0 \rightarrow Z_c(4430)^+ K^-) \times \mathcal{B}(Z_c(4430)^+ \rightarrow J/\psi \pi^+) < 4 \times 10^{-6} \text{ (95\% CL)}$$

However this limit was obtained without amplitude analysis, thus neglected interference effects, which are crucial according to the Belle results:

Belle PR D90, 112009 (2014)

$$\mathcal{B}(\bar{B}^0 \rightarrow Z_c(4430)^+ K^-) \times \mathcal{B}(Z_c(4430)^+ \rightarrow J/\psi \pi^+) = (5.4_{-1.0}^{+4.0+1.1}) \times 10^{-6},$$

Belle 1⁺ Z(4200)⁻

$$\mathcal{B}(\bar{B}^0 \rightarrow Z_c(4200)^+ K^-) \times \mathcal{B}(Z_c(4200)^+ \rightarrow J/\psi \pi^+) = (2.2_{-0.5}^{+0.7+1.1}) \times 10^{-5},$$

$$\mathcal{B}(\bar{B}^0 \rightarrow Z_c(3900)^+ K^-) \times \mathcal{B}(Z_c(3900)^+ \rightarrow J/\psi \pi^+) < 9 \times 10^{-7} \text{ (90\% CL)}.$$

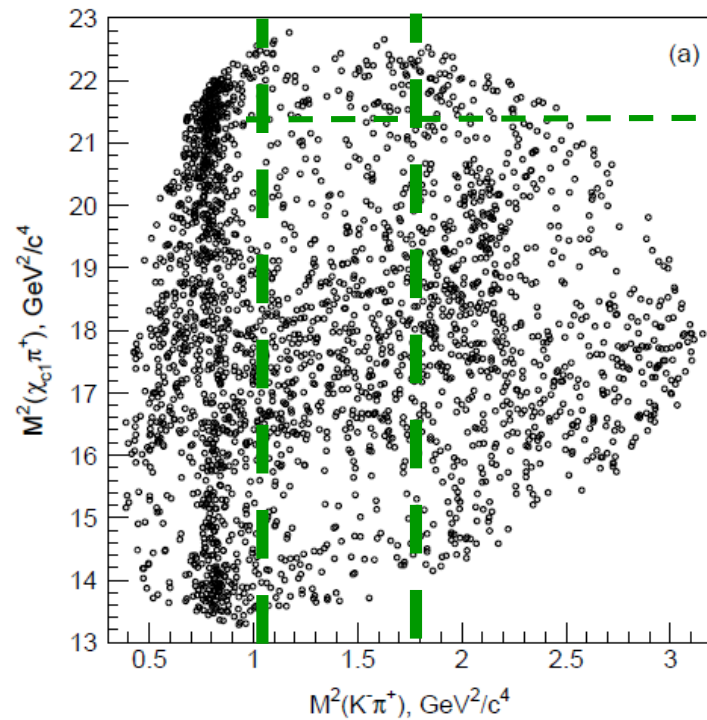
$\bar{B}^0 \rightarrow \chi_{c1} \pi^+ K^-$, $\chi_{c1} \rightarrow \gamma J/\psi$ Belle

Belle PR, D78, 072004 (2008)
2D amplitude analysis

2,126 ± 70 signal events

(non-B bkg. ~20%)

BaBar PRD, 85, 052003 (2012)
Model independent approach
~1,968 signal events

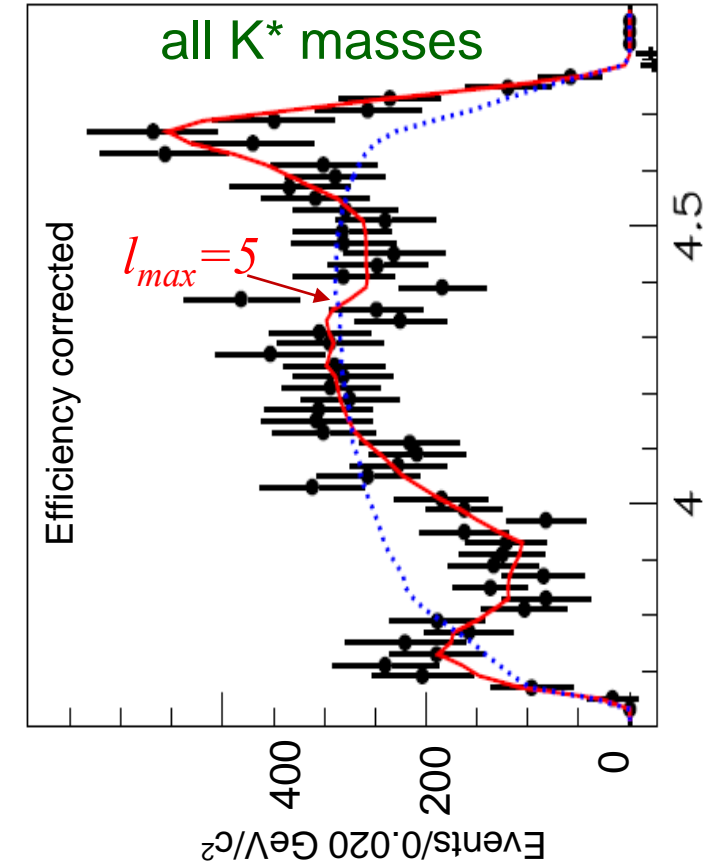
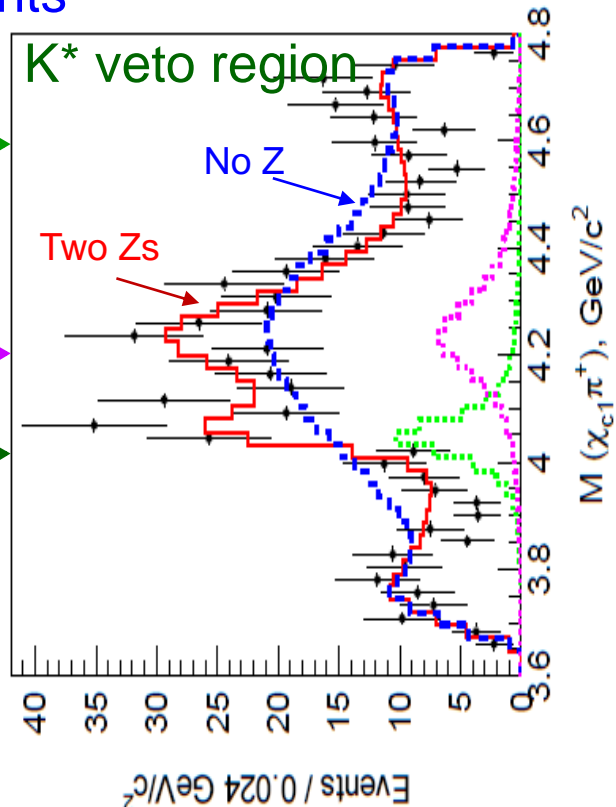


No J^P sensitivity

$M(Z_2) = 4248^{+44}_{-29} {}^{+180}_{-35}$ MeV
 $\Gamma(Z_2) = 177^{+54}_{-39} {}^{+316}_{-61}$ MeV
 $f_Z = 10.4^{+6.1}_{-2.3}$ %
 significance 5σ

$M(Z_1) = 4051^{+14}_{-14} {}^{+20}_{-41}$ MeV
 $\Gamma(Z_1) = 82^{+21}_{-17} {}^{+47}_{-22}$ MeV
 $f_Z = 8.0^{+3.8}_{-2.2}$ %
 significance 5σ

Sizable fit fractions!



One or two states claimed by Belle.

Need confirmation and J^P determination

$$\begin{aligned} \mathcal{B}(\bar{B}^0 \rightarrow K^- Z_1^+) \times \mathcal{B}(Z_1^+ \rightarrow \pi^+ \chi_{c1}) &= (3.0^{+1.5+3.7}_{-0.8-1.6}) \times 10^{-5}, \\ \mathcal{B}(\bar{B}^0 \rightarrow K^- Z_2^+) \times \mathcal{B}(Z_2^+ \rightarrow \pi^+ \chi_{c1}) &= (4.0^{+2.3+19.7}_{-0.9-0.5}) \times 10^{-5}. \end{aligned}$$

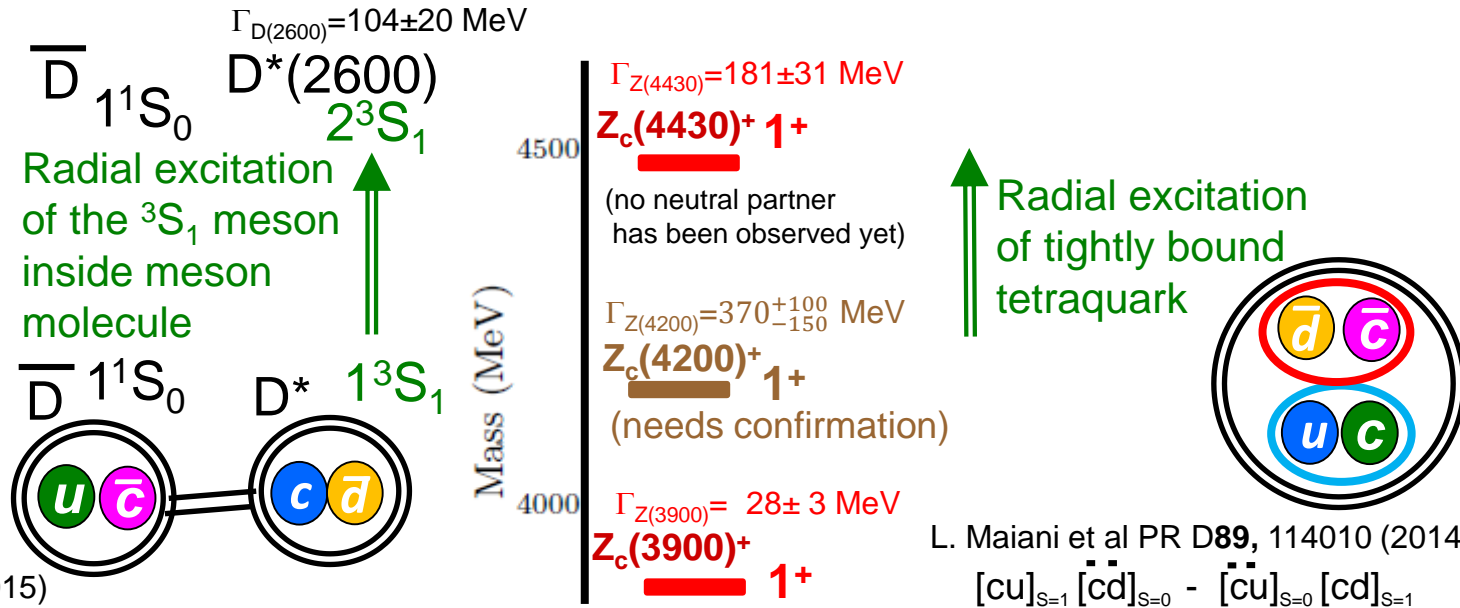
$$\begin{aligned} \mathcal{B}(\bar{B}^0 \rightarrow Z_1(4050)^+ K^-) \times \mathcal{B}(Z_1(4050)^+ \rightarrow \chi_{c1} \pi^+) &< 1.8 \times 10^{-5}, \\ \mathcal{B}(\bar{B}^0 \rightarrow Z_2(4250)^+ K^-) \times \mathcal{B}(Z_2(4250)^+ \rightarrow \chi_{c1} \pi^+) &< 4.0 \times 10^{-5}, \end{aligned}$$

(90% CL)

BaBar did confirm these states, but did not contradict them either

Obtained by neglecting any interference effects and statistical correlations between direct and moments-filtered mass spectra

Interpretations of Z_c^+ states observed in B decays



L. Ma et al PRD 90, 037502 (2014)
 T. Barnes et al, PRD 91, 014004 (2015)

L. Maiani et al PR D89, 114010 (2014)
 $[cu]_{S=1} [\bar{c}\bar{d}]_{S=0} - [\bar{c}u]_{S=0} [c\bar{d}]_{S=1}$

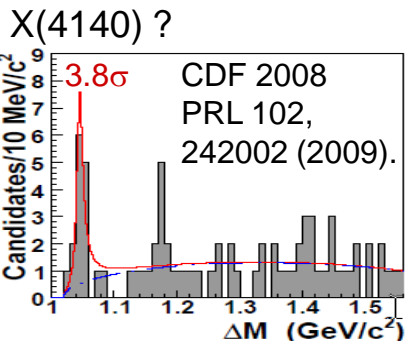
Absence of $Z_c(3900)^+$ in B decays makes it questionable to pair it up with $Z_c(4430)^+$

No molecular thresholds can explain $Z_c(4200)^+$

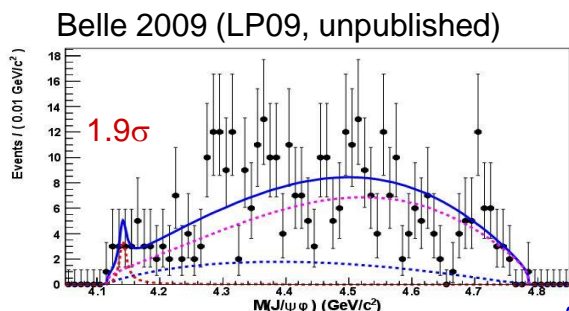
While it has been suggested $Z_c(4200)^+$ is a tetraquark, no tetraquark model can accommodate it together with $Z_c(4430)^+$
 C.Deng et al PR D92, 034027 (2015)

Vivid and confusing history of X(4140)

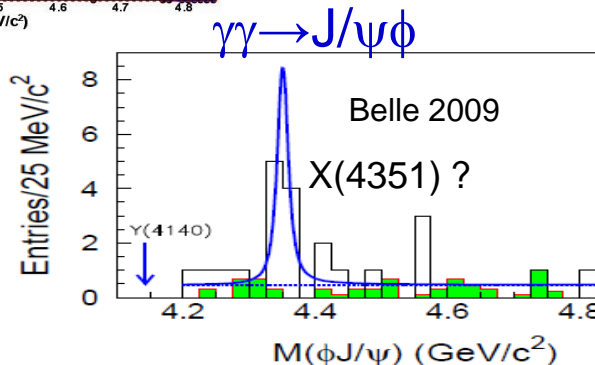
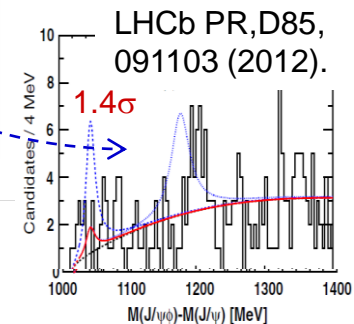
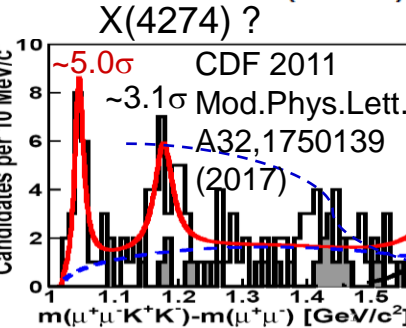
All 1D fits to $m(J/\psi\phi)$ with naïve bkg shapes



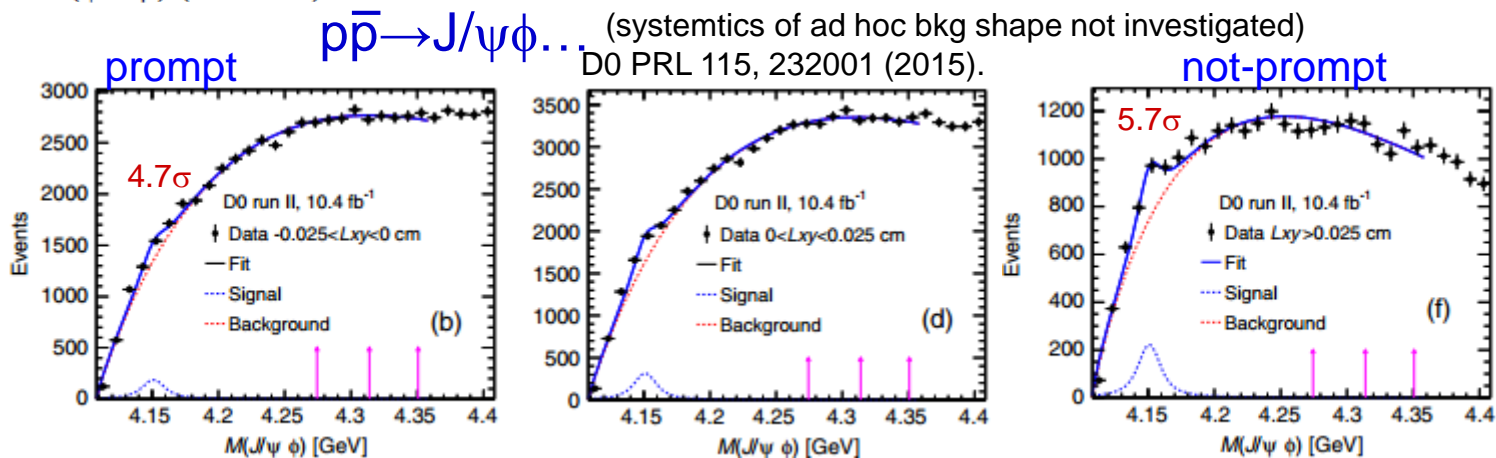
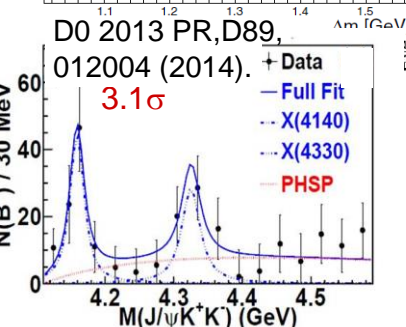
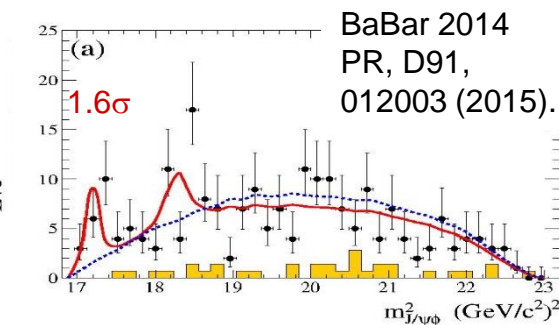
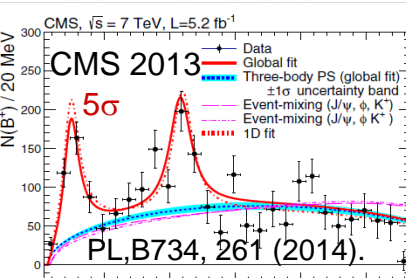
$B \rightarrow J/\psi\phi K$



Year	Experiment luminosity	$B \rightarrow J/\psi\phi K$ yield	Mass (MeV)	X(4140) peak		
				Width (MeV)	Significance	Fraction (%)
2008	CDF 2.7 fb^{-1} [1]	58 ± 10	$4143.0 \pm 2.9 \pm 1.2$	$11.7^{+8.3}_{-5.0} \pm 3.7$	3.8σ	
2009	Belle [22]	325 ± 21	4143.0 fixed	11.7 fixed	1.9σ	
2011	CDF 6.0 fb^{-1} [29]	115 ± 12	$4143.4^{+2.9}_{-3.0} \pm 0.6$	$15.3^{+10.4}_{-6.1} \pm 2.5$	5.0σ	$14.9 \pm 3.9 \pm 2.4$
2011	LHCb 0.37 fb^{-1} [21]	346 ± 20	4143.4 fixed	15.3 fixed	1.4σ	<7 @ 90% CL
2013	CMS 5.2 fb^{-1} [25]	2480 ± 160	$4148.0 \pm 2.4 \pm 6.3$	$28^{+15}_{-11} \pm 19$	5.0σ	10 ± 3 (stat.)
2013	D0 10.4 fb^{-1} [26]	215 ± 37	$4159.0 \pm 4.3 \pm 6.6$	$19.9 \pm 12.6^{+1.0}_{-8.0}$	3.0σ	$21 \pm 8 \pm 4$
2014	BABAR [24]	189 ± 14	4143.4 fixed	15.3 fixed	1.6σ	<13.3 @ 90% CL
2015	D0 10.4 fb^{-1} [27]	$p\bar{p} \rightarrow J/\psi\phi\dots$	$4152.5 \pm 1.7^{+6.2}_{-5.4}$	$16.3 \pm 5.6 \pm 11.4$	4.7σ (5.7σ)	
Average			4147.1 ± 2.4	15.7 ± 6.3		



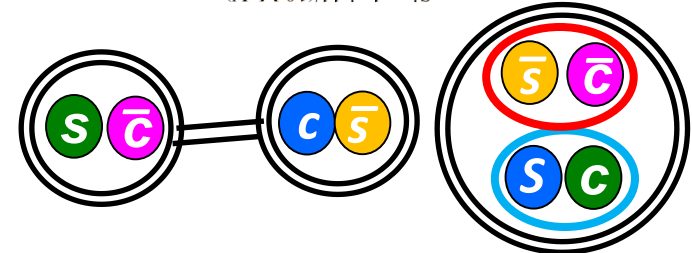
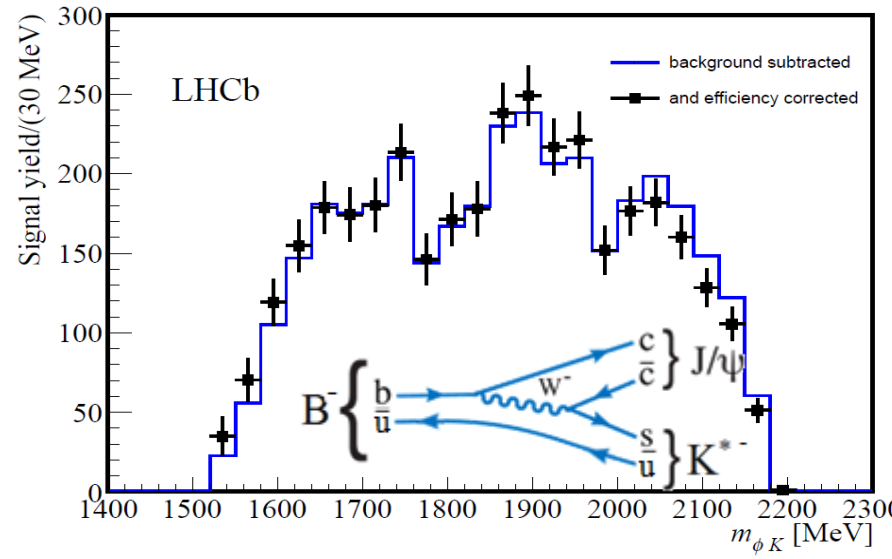
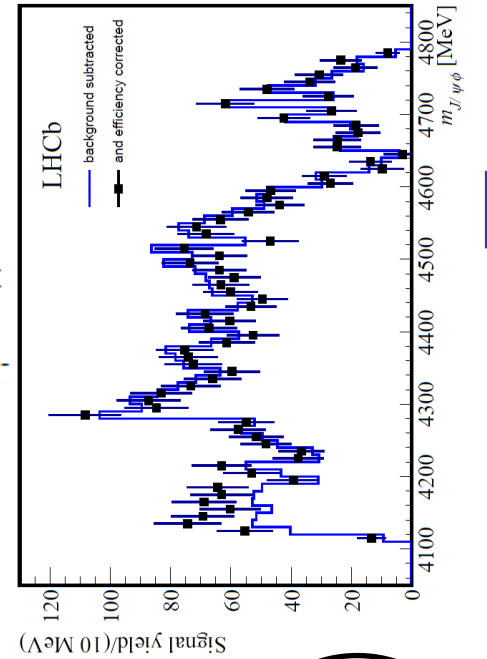
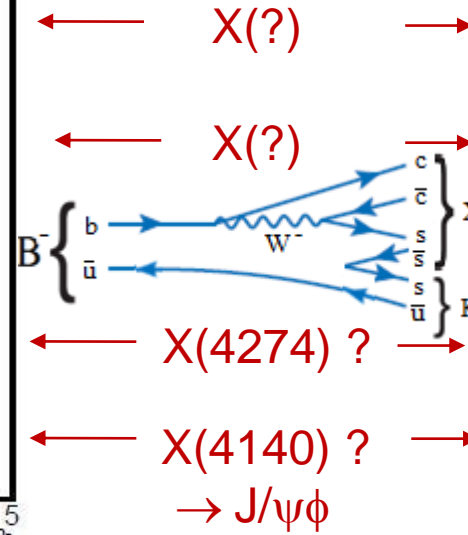
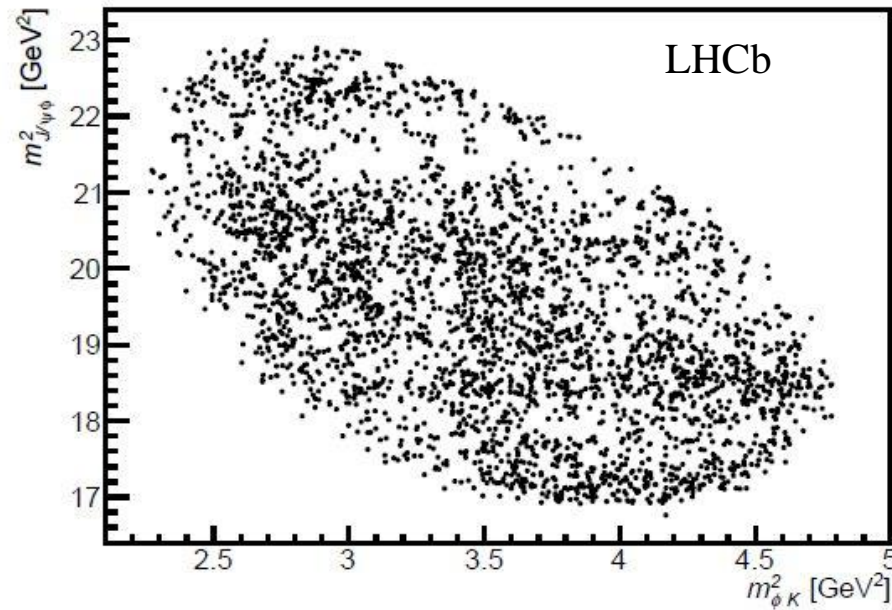
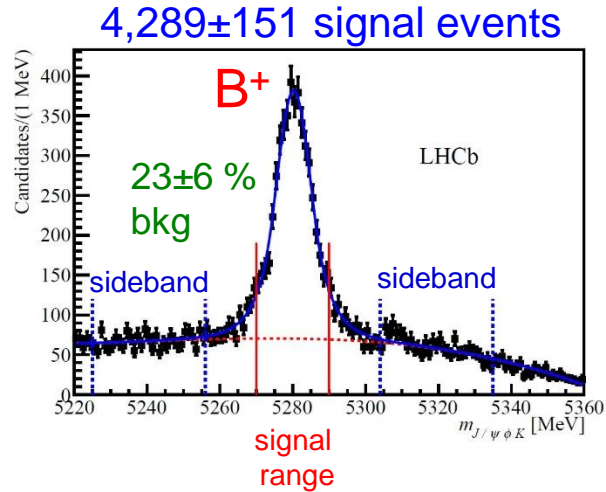
Year	Experiment luminosity	$B \rightarrow J/\psi\phi K$ yield	Mass (MeV)	X(4274–4351) peaks(s)	
				Width (MeV)	Significance
2011	CDF 6.0 fb^{-1} [29]	115 ± 12	$4274.4^{+8.4}_{-6.7} \pm 1.9$	$32.3^{+21.9}_{-15.3} \pm 7.6$	3.1σ
2011	LHCb 0.37 fb^{-1} [21]	346 ± 20	4274.4 fixed	32.3 fixed	
2013	CMS 5.2 fb^{-1} [25]	2480 ± 160	$4313.8 \pm 5.3 \pm 7.3$	$38^{+30}_{-15} \pm 16$	
2013	D0 10.4 fb^{-1} [26]	215 ± 37	4328.5 ± 12.0	30 fixed	
2014	BABAR [24]	189 ± 14	4274.4 fixed	32.3 fixed	1.2σ
2010	Belle [32]	$\gamma\gamma \rightarrow J/\psi\phi$	$4350.6^{+4.6}_{-5.1} \pm 0.7$	$13^{+18}_{-9} \pm 4$	3.2σ



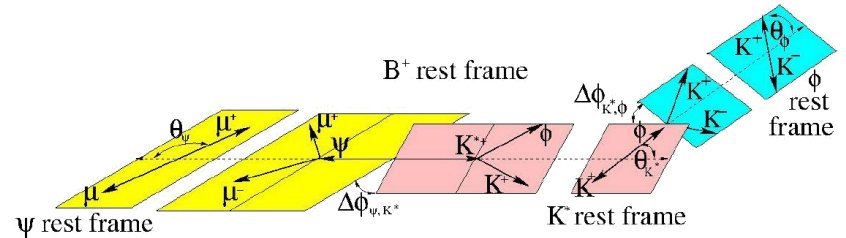
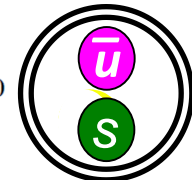
(events dominated by non- ϕ bkg.)

$B^+ \rightarrow J/\psi \phi K^+$

Tetraquarks or $\overline{D}s$ molecules



Perform first amplitude analysis (6D) of $B^+ \rightarrow J/\psi \phi K^+$



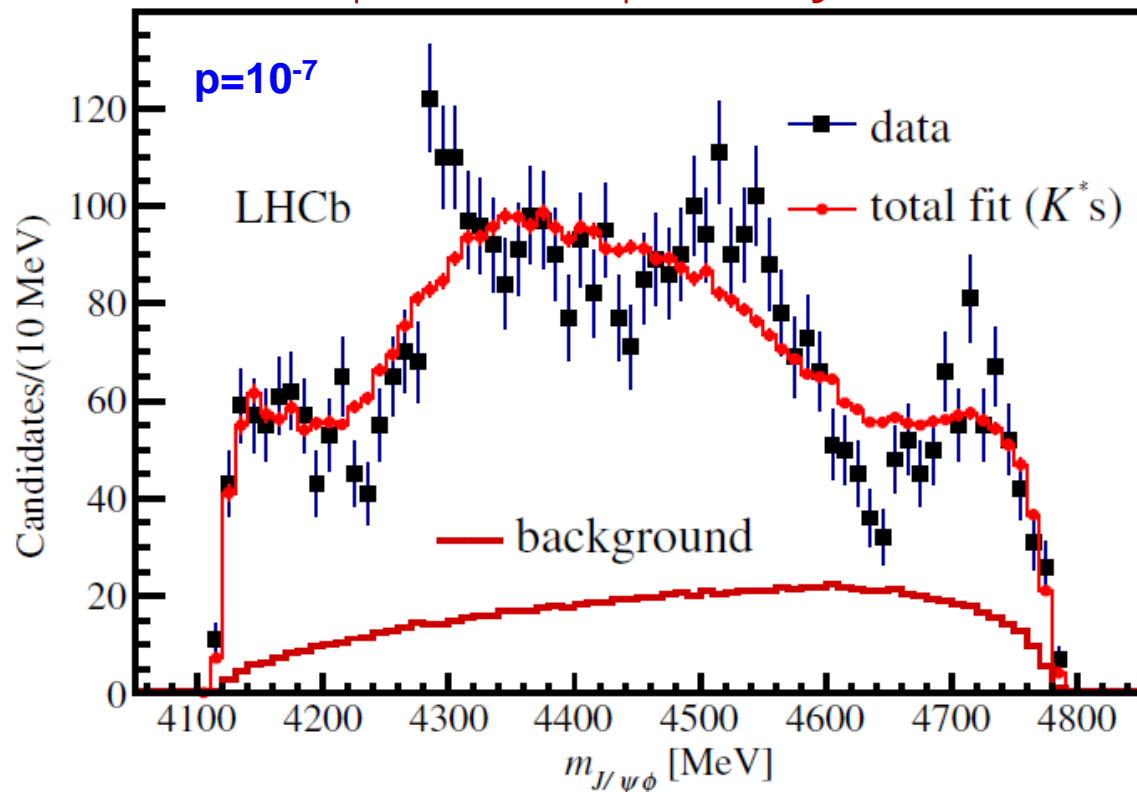
LHCb PRL118, 022003 (2017)
PR, D95, 012002 (2017)

Kaon excitations

Amplitude fit results

LHCb PRL118, 022003 (2017)
PR, D95, 012002 (2017)

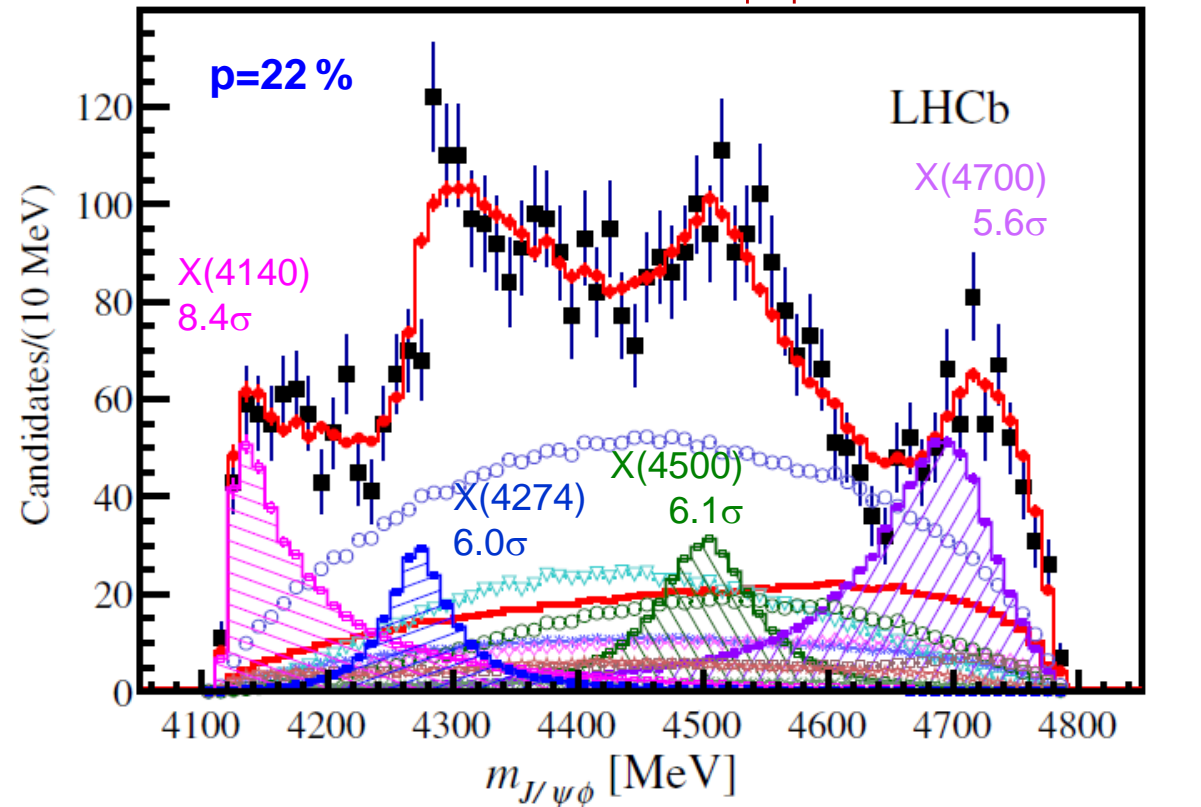
$B^+ \rightarrow J/\psi K^{*+}, K^{*+} \rightarrow \phi K^+$ only



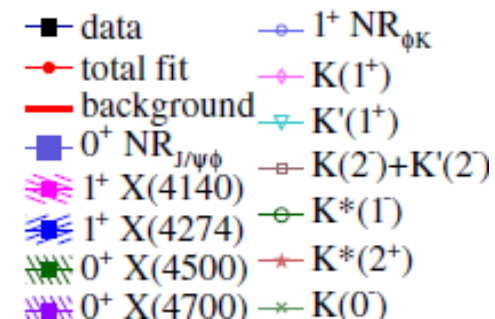
NR $\phi K 1^+$, two $2P_{1^+}$, two $2D_{2^-}$, and one of $1^3F_{3^+}$, $1^3D_{1^-}$, $3^3S_{1^-}$, $3^1S_{0^-}$, $2^3P_{2^+}$, $1^3F_{2^+}$, $1^3D_{3^-}$, $1^3F_{4^+}$. Fit 104 free parameters.

- Unlike in the other amplitude analyses, K^{*+} resonance composition (number, J^P, m, Γ) are not constrained to other experimental results (little is known about high mass kaon excitations)

+ $B^+ \rightarrow X K^+, X \rightarrow J/\psi \phi$



NR $\phi K 1^+$, two $2P_{1^+}$, two $2D_{2^-}$, and one of $1^3D_{1^-}$, $3^1S_{0^-}$, $2^3P_{2^+}$. Two $1^+ X$, Two $0^+ X$, NR $0^+ J/\psi\phi$. Fit 98 free parameters.



Amplitude fit results

LHCb PRL118, 022003 (2017)
PR, D95, 012002 (2017)

Contribution	Significance or Reference	M_0 (MeV)	Γ_0 (MeV)	FF (%)
All $K(1^+)$	8.0σ			$42 \pm 8^{+5}_{-9}$
NR $_{\phi K}$				$16 \pm 13^{+35}_{-6}$
$K(1^+)$	7.6σ	$1793 \pm 59^{+153}_{-101}$	$365 \pm 157^{+138}_{-215}$	$12 \pm 10^{+17}_{-6}$
2^1P_1	[53]	1900		
$K_1(1650)$	[36]	1650 ± 50	150 ± 50	
$K'(1^+)$	1.9σ	$1968 \pm 65^{+70}_{-172}$	$396 \pm 170^{+174}_{-178}$	$23 \pm 20^{+31}_{-29}$
2^3P_1	[53]	1930		
All $K(2^-)$	5.6σ			$11 \pm 3^{+2}_{-5}$
$K(2^-)$	5.0σ	$1777 \pm 35^{+122}_{-77}$	$217 \pm 116^{+221}_{-154}$	
1^1D_2	[53]	1780		
$K_2(1770)$	[36]	1773 ± 8	188 ± 14	
$K'(2^-)$	3.0σ	$1853 \pm 27^{+18}_{-35}$	$167 \pm 58^{+83}_{-72}$	
1^3D_2	[53]	1810		
$K_2(1820)$	[36]	1816 ± 13	276 ± 35	
$K^*(1^-)$	8.5σ	$1722 \pm 20^{+33}_{-109}$	$354 \pm 75^{+140}_{-181}$	$6.7 \pm 1.9^{+3.2}_{-3.9}$
1^3D_1	[53]	1780		
$K^*(1680)$	[36]	1717 ± 27	322 ± 110	
$K^*(2^+)$	5.4σ	$2073 \pm 94^{+245}_{-240}$	$678 \pm 311^{+1153}_{-559}$	$2.9 \pm 0.8^{+1.7}_{-0.7}$
2^3P_2	[53]	1940		
$K_2^*(1980)$	[36]	1973 ± 26	373 ± 69	
$K(0^-)$	3.5σ	$1874 \pm 43^{+59}_{-115}$	$168 \pm 90^{+280}_{-104}$	$2.6 \pm 1.1^{+2.3}_{-1.8}$
3^1S_0	[53]	2020		
$K(1830)$	[36]	~ 1830	~ 250	
All $X(1^+)$				$16 \pm 3^{+6}_{-2}$
$X(4140)$	8.4σ	$4146.5 \pm 4.5^{+4.6}_{-2.8}$	$83 \pm 21^{+21}_{-14}$	$13.0 \pm 3.2^{+4.8}_{-2.0}$
Averages from	Table I	4147.1 ± 2.4	15.7 ± 6.3	
$X(4274)$	6.0σ	$4273.3 \pm 8.3^{+17.2}_{-3.6}$	$56 \pm 11^{+8}_{-11}$	$7.1 \pm 2.5^{+3.5}_{-2.4}$
CDF	[29]	$4274.4^{+8.4}_{-6.7} \pm 1.9$	$32^{+22}_{-15} \pm 8$	
CMS	[25]	$4313.8 \pm 5.3 \pm 7.3$	$38^{+30}_{-15} \pm 16$	
All $X(0^+)$				$28 \pm 5 \pm 7$
NR $_{J/\psi\phi}$	6.4σ			$46 \pm 11^{+11}_{-21}$
$X(4500)$	6.1σ	$4506 \pm 11^{+12}_{-15}$	$92 \pm 21^{+21}_{-20}$	$6.6 \pm 2.4^{+3.5}_{-2.3}$
$X(4700)$	5.6σ	$4704 \pm 10^{+14}_{-24}$	$120 \pm 31^{+42}_{-33}$	$12 \pm 5^{+9}_{-5}$

FF ~ 65%

$B^+ \rightarrow J/\psi K^{*+}, K^{*+} \rightarrow \phi K^+$

- The most sizable contribution of “exotic” part of the amplitude among analyzed B decay channels (related to the smallest Q in the B decay?)

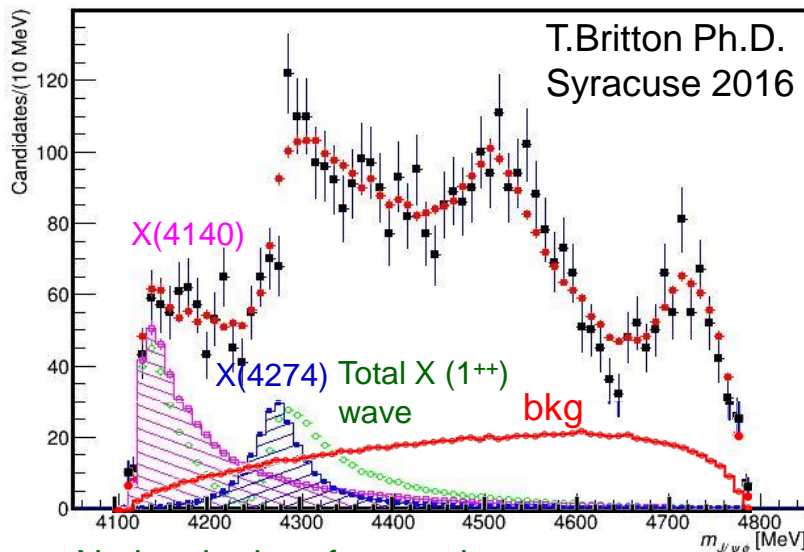
FF ~44%

$B^+ \rightarrow X K^+, X \rightarrow J/\psi \phi$

X(1⁺⁺)

LHCb PRL118, 022003 (2017)
PR, D95, 012002 (2017)

<http://surface.syr.edu/etd/510/>



Notice the interference between the two 1⁺⁺ states!

Contribution	sign. or Ref.	M_0 MeV	Γ_0 MeV	Fit results F.F. %	
All X(1 ⁺)				16 ± 3	
X(4140)	8.4σ	$4146.5 \pm 4.5^{+4.6}_{-2.8}$	$83 \pm 21^{+21}_{-14}$	$13.0 \pm 3.2^{+4.8}_{-2.0}$	Good consistency in mass 2.6 σ tension in width $\Gamma \nearrow$ $\Delta\Gamma \nearrow$
ave.		4147.1 ± 2.4	15.7 ± 6.3		
X(4274)	6.0σ	$4273.3 \pm 8.3^{+17.2}_{-3.6}$	$56 \pm 11^{+8}_{-11}$	$7.1 \pm 2.5^{+3.5}_{-2.4}$	Good consistency
CDF		$4274.4^{+8.4}_{-6.7} \pm 1.9$	$32^{+22}_{-15} \pm 8$		
CMS		$4313.8 \pm 5.3 \pm 7.3$	$38^{+30}_{-15} \pm 16$		3.2 σ disagreement in mass

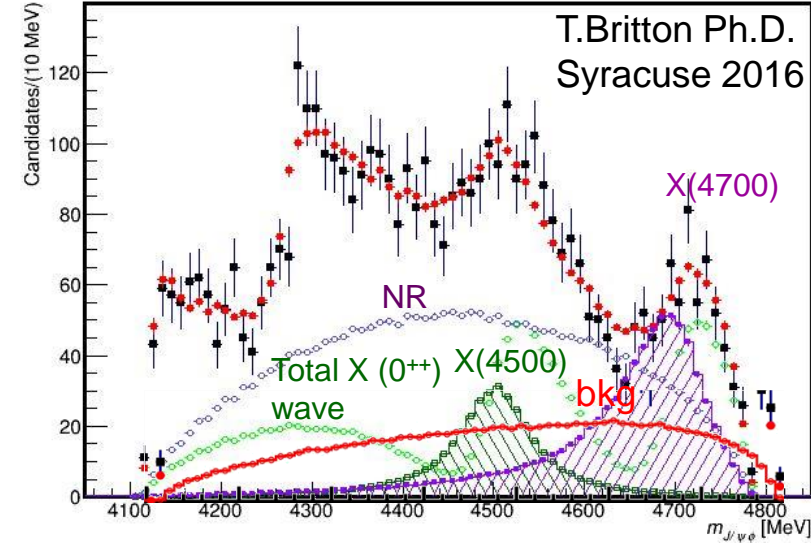
- Significant X(4140) 8.4σ ,
 - mass consistent with the previous measurements, but the width substantially larger (2.6 σ “tension” with the previous 1D fits)
 - $J^{PC}=1^{++}$ determined at 5.7σ including systematic errors
- Significant X(4274) 6.0σ ,
 - Consistent with the unpublished CDF results. First significant claim for this structure.
 - $J^{PC}=1^{++}$ determined at 5.8σ including systematic errors

X(0⁺⁺)

<http://surface.syr.edu/etd/510/>

First observations

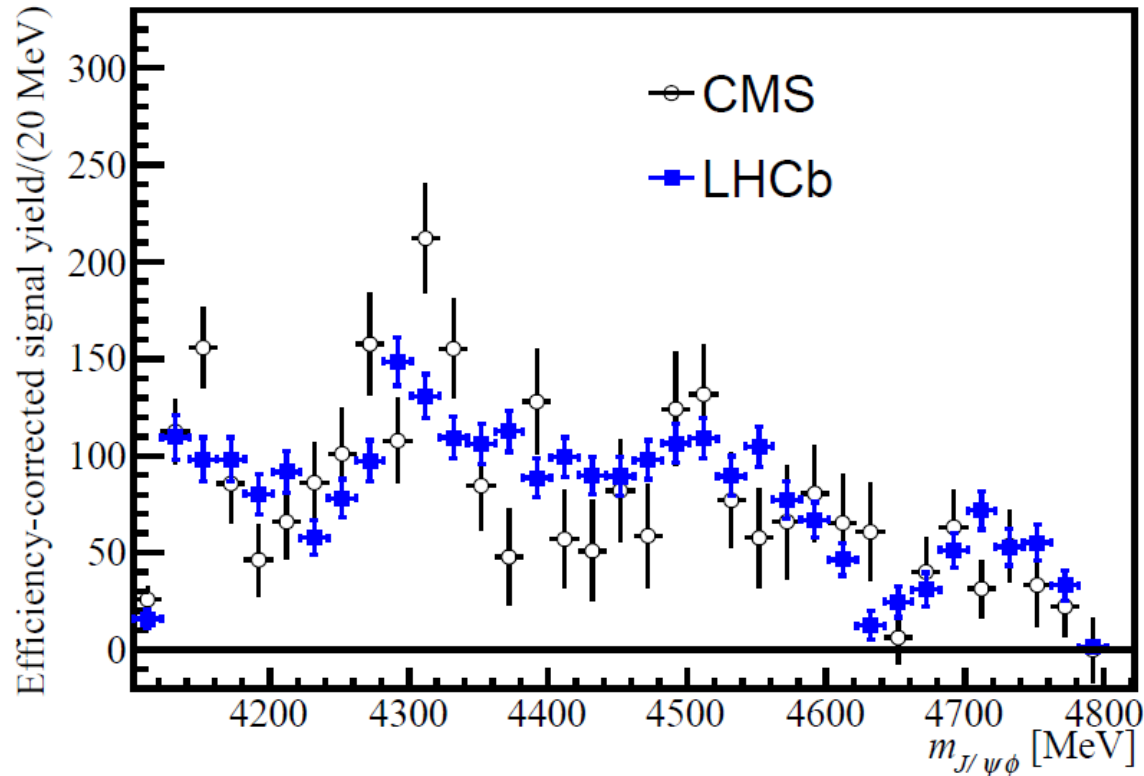
Contribution	sign.	Fit results		
		M_0 MeV	Γ_0 MeV	F.F. %
All X(0 ⁺)				$28 \pm 5^{+7}_{-7}$
NR _{J/ψφ}	6.4σ			$46 \pm 11^{+11}_{-21}$
X(4500)	6.1σ	$4506 \pm 11^{+12}_{-15}$	$92 \pm 21^{+21}_{-20}$	$6.6 \pm 2.4^{+3.5}_{-2.3}$
X(4700)	5.6σ	$4704 \pm 10^{+14}_{-24}$	$120 \pm 31^{+42}_{-33}$	$12 \pm 5^{+9}_{-5}$



- Significant structures at higher masses, best described by two new 0⁺⁺ resonances X(4500), X(4700):
 - Significances of 6.1σ, 5.6σ
 - J^{PC}=0⁺⁺ determined at 4.0σ, 4.5σ, respectively
 - Hints of these structures can be found in Belle & CMS data (see next)

LHCb vs CMS data

- Compare $m_{J/\psi\phi}$ to the CMS data (the previous best sample).
- Non-B background subtracted, corrected for signal efficiency.



Used publically available CMS background-free distribution and CMS efficiency dependence on $m_{J/\psi\phi}$

LHCb efficiency corrections via 6D parameterization of efficiency in all dimensions of the decay phase-space.

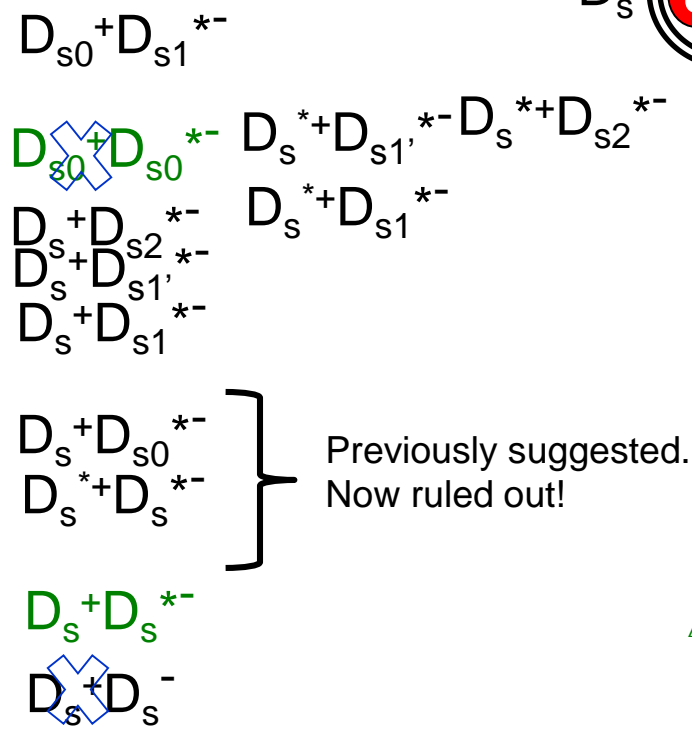
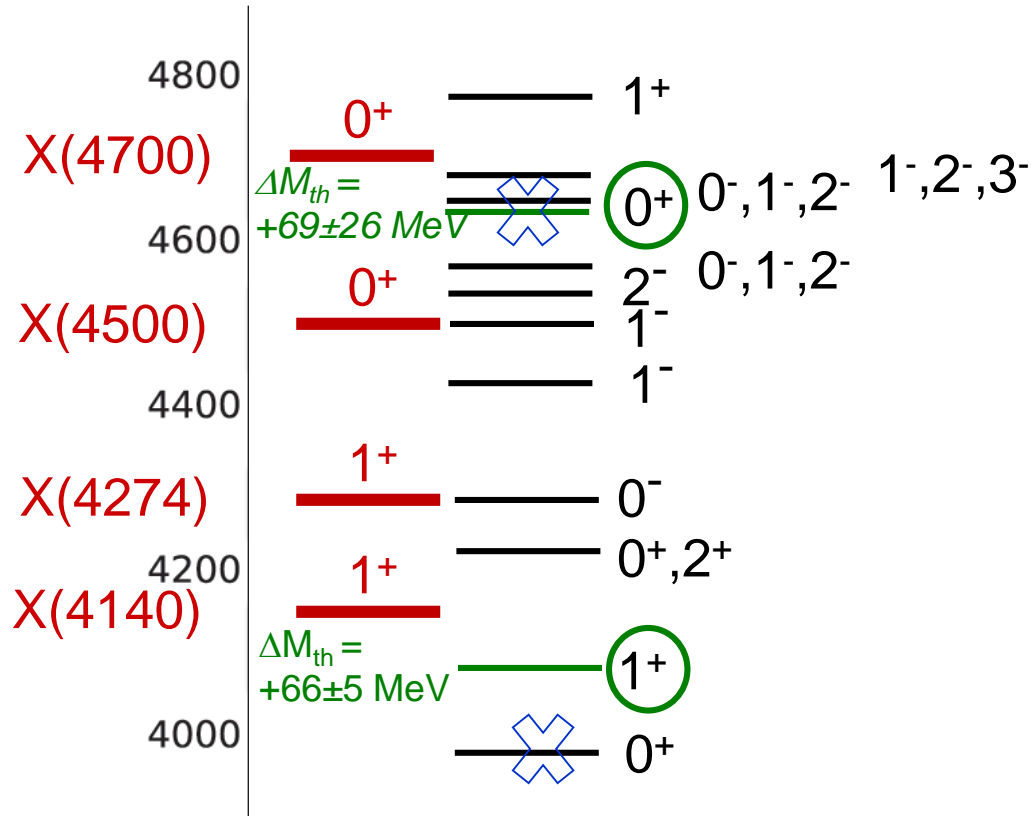
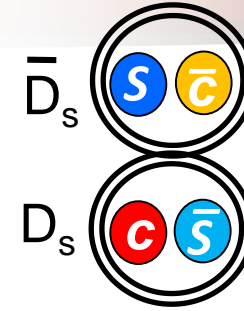
Normalized to the same area.

The vertical scale is arbitrary.

- LHCb data more precise.
- Qualitative agreement over the full mass range.
- Can't rely on naïve 1D mass fits to determine resonant composition.

Interpretation of $J/\psi\phi$ structures?

- A molecule/threshold effect?



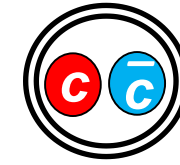
$$\Delta M_{th} = M_{measured} - M_{threshold}$$

No π -exchange forces ($l=0$)!

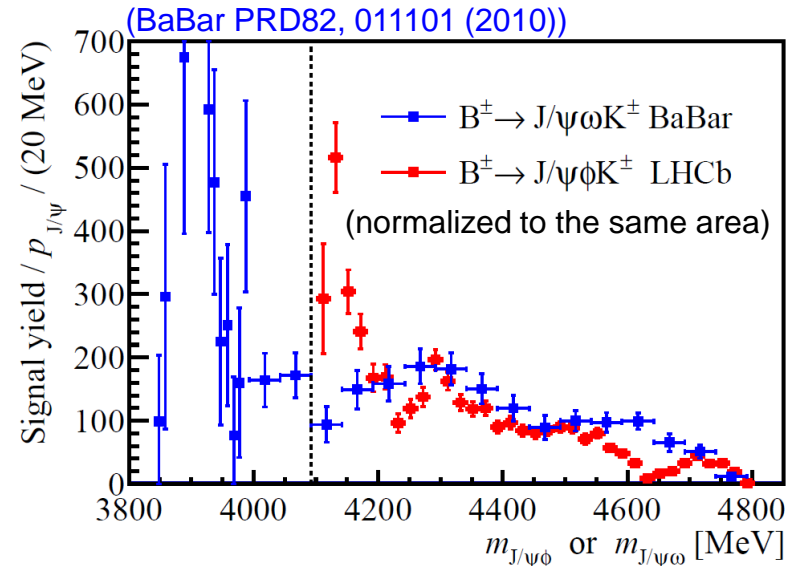
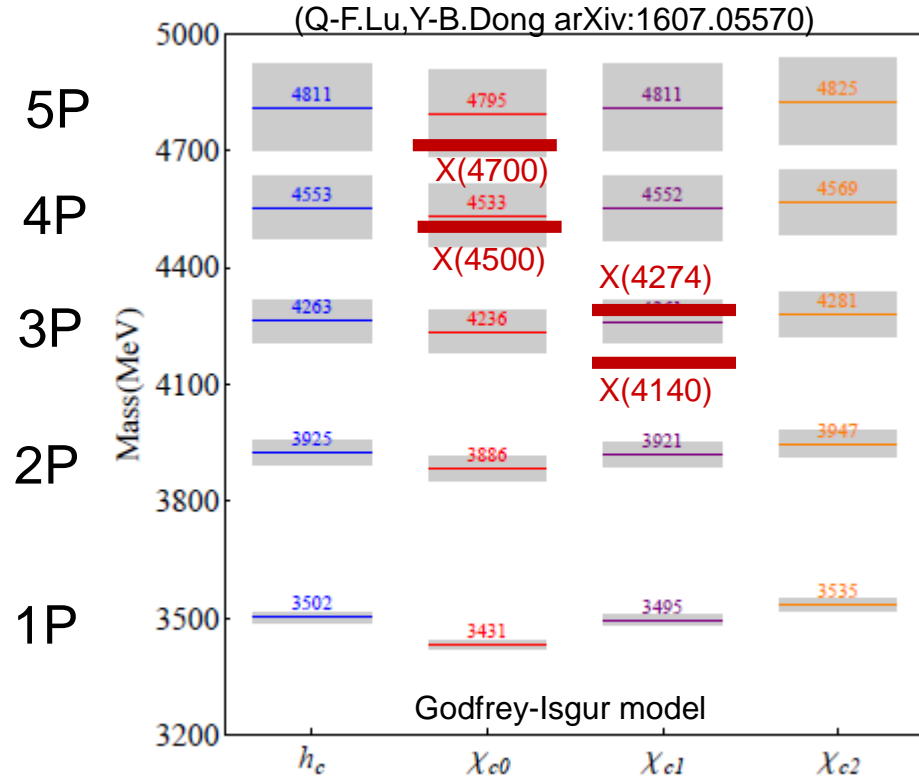
η -exchange possible (unless crossed-over above) (M.Karliner, J.L.Rosner arXiv:1601.00565)

• Except for X(4140) being possibly affected by a $D_s + D_s^{*-}$ threshold, the observed $J/\psi\phi$ structures don't fit the $D_{sJ}^{(*)}$ -pair mass thresholds or their quantum numbers.

Interpretation of $J/\psi\phi$ structures?



- P-wave charmonia?



It is possible to find matching $\chi_{cJ}(nP)$ states but the J^P -mass patterns are different

$\chi_{cJ}(nP)$ states would couple to $J/\psi\phi$ and $J/\psi\omega$ the same way.

The $J/\psi\phi$ structures do not show up in $J/\psi\omega$ spectrum.

- Not a plausible explanation.

Interpretation of $J/\psi\phi$ structures?

- Tetraquarks?



PREDICTION

F. Stancu,
J. Phys. G37 (2010) 075017, arXiv:0906.2485

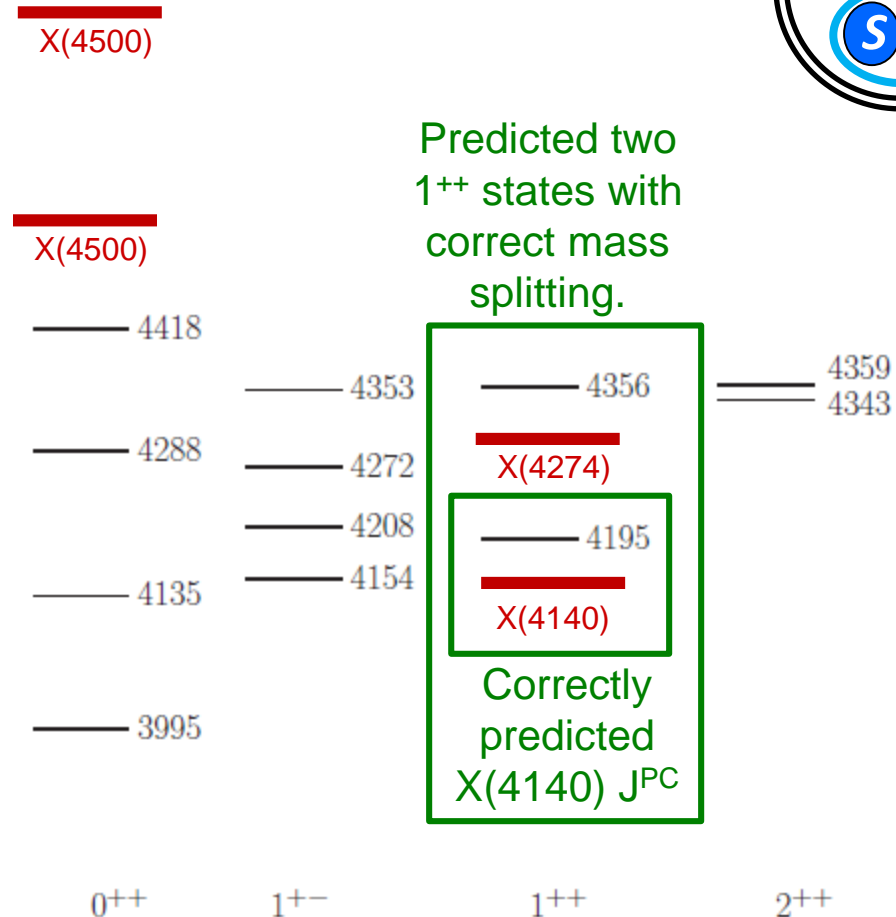
Allow $S=0$ and $S=1$ diquarks.
Allow diquarks in color triplet and sextet configurations.

Calculated $n=0, L=0$ states.

MANY POSTDICTIONS

e.g. L. Maiani, A.D. Polosa, V. Riquer arXiv:1607.02405

Allow diquarks only in color triplet configuration; cuts # of states in half. Only one 1^{++} state.
Describe $X(4500), X(4700)$ 0^{++} states as the radial excitations ($n=1$).



Conclusions - I

- There are a number of very significant $[c\bar{c}u\bar{d}]$ structures observed in $B \rightarrow [(c\bar{c})\pi^+]K$ decays. Interpretations of them is far from clear.
 - Only one, $Z_c(4430)^+ \rightarrow \psi(2S)\pi^+$, was observed by two experiments, but there is no reason to doubt the others, $Z_c(4200)^+ \rightarrow J/\psi\pi^+$ (confirmation needed), at least one $Z_c^+ \rightarrow \chi_{c1}\pi^+$ (confirmation and J^P determination are needed).
 - $Z_c(4430)^+$ was observed in 2nd decay mode ($\rightarrow J/\psi\pi^+$), but a confirmation of this, especially with mass and width free in the fit, will be important. $Z_c(4200)^+$ is also likely present in $\psi(2S)\pi^+$, which requires a clarification. Non-observation in the other decay modes (e.g. in Cabibbo suppressed $B \rightarrow [(c\bar{c})\pi^+]\pi$ decays) needs to be quantified.
 - They are both 1^+ (S wave decay possible) and require $l = 1$ in the parity-violating production in the B decay ($0^- \rightarrow 1^+0^-$), just like πK S wave in $B \rightarrow (J/\psi, \psi(2S))[\pi^+ K]$ ($0^- \rightarrow 1^-0^+$). Dominance of the lowest angular momenta not surprising for any dynamics, but why aren't we seeing other J^P values in $[\psi\pi^+]$ like we do in $[\pi^+ K]$ system? Need 6D amplitude fits to $B \rightarrow \chi_{c1}\pi^+ K$ to verify the claimed $\chi_{c1}\pi^+$ states and determine their quantum numbers .
 - Argand diagrams for $Z_c(4430)^+$ and $Z_c(4200)^+$ are consistent with resonances, but improvements in experimental uncertainties are highly desired.
 - They are not the same as the structures observed in $e^+e^- \rightarrow [J/\psi\pi^+]\pi^-$, $e^+e^- \rightarrow [\psi(2S)\pi^+]\pi^-$, ... Exotic hadron model builders need to take this into account (the current trend is to ignore it).
 - Why aren't we seeing $[c\bar{c}\bar{q}s]$ ($q=u$ or d) exotics?

Conclusions - II

- Low fit fraction signals, e.g. $B \rightarrow [(J/\psi)\pi^+]K$, may be susceptible to the approximations made in matrix element formulation (e.g. sum over Breit-Wigners); ought to explore better approximations.
- Isospin partners in $B \rightarrow [(c\bar{c})\pi^0]K$? Quantitative results from coupled-channels $B \rightarrow [c\bar{u}][\bar{c}d]K$?
- There are four significant $[c\bar{c}\bar{s}s]$ structures observed in $B \rightarrow [J/\psi\phi]K$. Interpretations of them is also unclear.
 - X(4140) is well established. Evolution of its width determination has follow the $Z_c(4430)^+$ path ($\Gamma \nearrow$, $\Delta\Gamma \nearrow$). Results for any resonance with observable decay width should not be trusted without amplitude analysis.
 - X(4274) is also rather well established.
 - Their quantum numbers were determined to be 1^{++} in complex amplitude analysis. They require independent confirmation.
 - Observation of X(4140) in prompt production in high energy $p\bar{p}$ collisions has been claimed. If confirmed this would be the only 2^{nd} exotic hadron candidate observed in B decays and in prompt productions (after X(3872)). Why would X(4140) be produced promptly, but not X(4274)?
 - X(4500), X(4700) 0^+ states, and a significant non-resonant 0^+ $J/\psi\phi$ component were also needed to describe the data well. All require independent confirmation.
 - Studies of coupled-channels $B \rightarrow [c\bar{s}][\bar{c}s]K$ are highly desired.
- Further progress in understanding of exotic meson candidates observed in amplitude analyses of B decays will only be made by more experimental studies:
 - Good prospects for substantially larger data samples in upgraded LHCb, Belle II, ...