

# Threshold effects in hadron spectrum: a new spectroscopy?

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VNiVERSiDAD E SALAMANCA



# Outline

1 Motivation

2 The model

3 Results

4 Conclusions



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1 Motivation

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# Quark model

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PHYSICS LETTERS



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## A SCHEMATIC MODEL OF BARYONS AND MESONS \*

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Received 4 January 1964

If we assume that the strong interactions of baryons and mesons are correctly described in terms of the broken "eightfold way" [1-3], we are tempted to look for some fundamental explanation of the situation. A highly promised approach is the purely dy-

bar  $n_t - n_{\bar{t}}$  would be zero for all known baryons and mesons. The most interesting example of such a model is one in which the triplet has spin  $\frac{1}{2}$  and  $z = -1$ , so that the four particles  $d^-$ ,  $s^-$ ,  $u^0$  and  $b^0$  exhibit a parallel with the leptons.

A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon  $b$  if we assign to the triplet  $t$  the following properties: spin  $\frac{1}{2}$ ,  $z = -\frac{1}{3}$ , and baryon number  $\frac{1}{3}$ . We then refer to the members  $u^{\frac{1}{3}}$ ,  $d^{-\frac{1}{3}}$ , and  $s^{-\frac{1}{3}}$  of the triplet as "quarks" [6] and the members of the anti-triplet as anti-quarks  $\bar{q}$ . Baryons can now be constructed from quarks by using the combinations  $(qqq)$ ,  $(qq\bar{q}\bar{q})$ , etc., while mesons are made out of  $(q\bar{q})$ ,  $(q\bar{q}\bar{q}\bar{q})$ , etc. It is assuming that the lowest baryon configuration  $(qqq)$  gives just the representations **1**, **8**, and **10** that have been observed, while the lowest meson configuration  $(q\bar{q})$  similarly give just **1** and **8**.

$$3 \times 3 = 9,$$

$$3 \times 3 \times 3 = 27, \dots$$

$$3 \otimes \overline{3} = 8 \oplus 1,$$

$$3 \otimes 3 \otimes 3 = 10 \oplus 8 \oplus 8 \oplus 1$$



Murray Gell-Mann, 10-year-old, New York, 1939. Now, 25 years later, Caltech





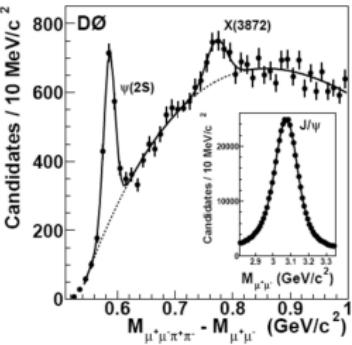
# Discoveries at $B$ -factories

- Exotic Mesons:  $X(3872)$ ,  $D_{s0}^*(2317)$ ,  $D_{s1}(2460)$ ,  $X(4140)$ , ...
- Exotic Baryons:  $\Lambda_c(2940)$ ,  $P_c(4380)$ ,  $P_c(4450)$ , ...

Signals of exotic structures? Standard  $q\bar{q}$  or  $qqq$ ? Threshold cusps?



- Possibility to study the coupling with higher Fock spaces.
- Some of them may be naive  $q\bar{q}$  or  $qqq$  structures.
- Others are more elusive:  $X(3872) \rightarrow$





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1 Motivation

2 The model

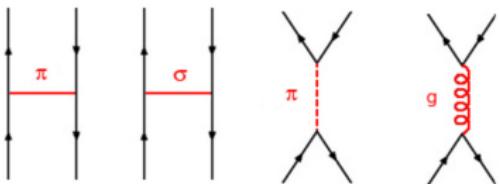
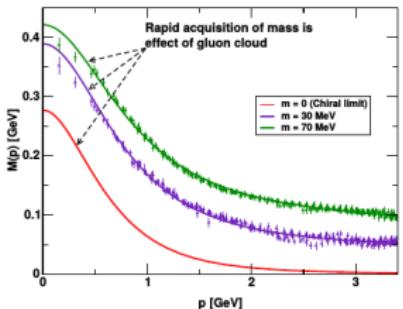
3 Results

4 Conclusions

# Ingredients of constituent quark model

The model includes:

- Spontaneous breaking of chiral symmetry  $\rightarrow$  Constituent mass and Pseudo-Goldstone bosons.



C. D. Roberts, arxiv:1109.6325v1 [nucl-th]

- QCD perturbative effects  $\rightarrow$  Gluon exchange.
- Confinement  $\rightarrow$  Screened potential.
- All parameters constrained from low-lying meson and baryon spectra.



# Constituent quark model

- Nucleon-Nucleon interaction:

- D. R. Entem, F. Fernández, A. Valcarce, **PRC62**, 034002 (2000).
- A. Valcarce, A. Faessler, F. Fernández, **PLB345**, 367 (1995).
- F. Fernández, A. Valcarce, U. Straub, A. Faessler, **JPG19**, 2013 (1993).

- Baryon spectrum:

- A. Valcarce, H. Garcilazo, and J. Vijande, **PRC72**, 025206 (2005).
- H. Garcilazo, A. Valcarce, F. Fernández, **PRC64**, 058201 (2001).

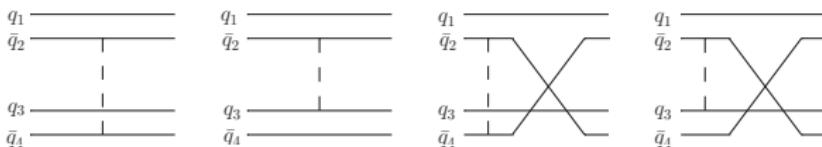
- Meson spectrum:

- J. Vijande, F. Fernández y A. Valcarce, **JPG31**, 481 (2005).
- J. Segovia, A. M. Yasser, D. R. Entem, F. Fernández, **PRD78**, 114033 (2008).
- J. Segovia, P. G. Ortega, D. R. Entem, F. Fernández, **PRD90**, 074027 (2016).



# Solving the two body problem

- We want to explore meson-meson and meson-baryon interactions.
- Meson wave function  $\rightarrow$  Gaussian Expansion Method:
  - $\psi_{lm}(\vec{p}) = \sum_{n=1}^{n_{max}} C_{nl} Y_{lm}(\hat{p}) \phi_{nl}(p)$ , with  $\phi_{nl}(p) = (-i)^l \frac{N_{nl}}{(2\eta_n)^{l+3/2}} p^l e^{-\frac{p^2}{4\eta_n}}$
  - GEM free parameters:  $\{n_{max}, r_1, a\}$
  - Rayleigh-Ritz variational principle:
$$\sum_{n'=1}^{n_{max}} \left[ (T_{nn'}^\alpha - EN_{nn'}^\alpha) c_{n'l}^\alpha + \sum_{\alpha'}^{n^0 chnl} V_{nn'}^{\alpha\alpha'} c_{n'l}^{\alpha'} \right] = 0$$
- Baryon wave functions  $\rightarrow$  Gaussian with scaled range.
- Resonating Group Method:
  - Interaction at quark level  $\rightarrow$  Interaction between clusters
  - Direct and exchange potentials:

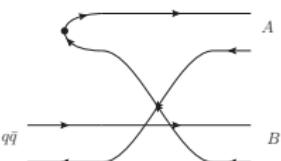




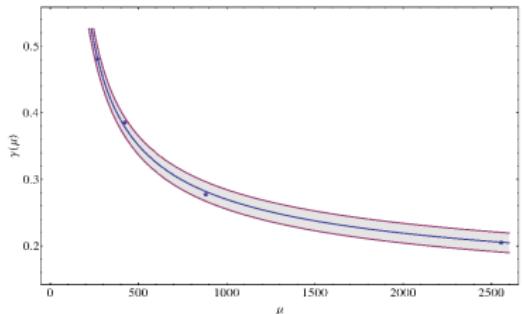
# $^3P_0$ interaction

- $^3P_0$  model used as coupling mechanism.
- Pair creation hamiltonian:

$$\mathcal{H} = g \int d^3x \bar{\psi}(x) \psi(x)$$



- Non relativistic reduction:  
 $T = -3\sqrt{2}\gamma' \sum_{\mu} \int d^3p d^3p' \delta^{(3)}(p + p') \left[ \mathcal{Y}_1 \left( \frac{p-p'}{2} \right) b_{\mu}^{\dagger}(p) d_{\nu}^{\dagger}(p') \right] C=1, I=0, S=1, J=0$   
with  $\gamma' = 2^{5/2} \pi^{1/2} \gamma$  and  $\gamma = \frac{g}{2m}$
- Running of the  $^3P_0$  strength  $\gamma \rightarrow$  [J. Segovia et al., arXiv:1205.2215](#)



$$\gamma(\mu) = \frac{\gamma_0}{\log(\mu/\mu_\gamma)}$$

- $\gamma_0 = 0.81 \pm 0.02$
- $\mu_\gamma = 49.84 \pm 2.58$  MeV
- Solid line is the fit
- Shaded area  $\rightarrow$  90% C.L.

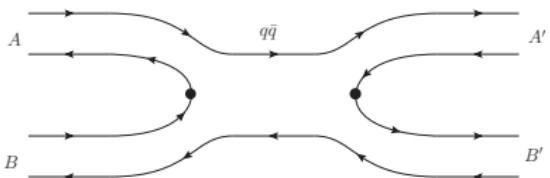


# Coupling between $q\bar{q}$ and $q\bar{q} - q\bar{q}$ sectors

- Effect of  $q\bar{q}$  on meson-meson states  $\rightarrow$  Molecular states, mass-shifts, threshold cusps, . . .
- Mixed states:  $|\Psi\rangle = \sum_{\alpha} c_{\alpha} |\psi\rangle + \sum_{\beta} \chi_{\beta}(P) |\phi_{M1}\phi_{M2}\beta\rangle$
- Solving the coupling with the  $q\bar{q}$  meson spectrum  $\rightarrow$  Schrödinger-type equation:

$$\sum_{\beta} \int \left( H_{\beta'\beta}^{M_1 M_2}(P', P) + V_{\beta'\beta}^{\text{eff}}(E; P', P) \right) \chi_{\beta}(P) P^2 dP = E \chi_{\beta'}(P')$$

with  $V_{\beta'\beta}^{\text{eff}}(E; P', P)$ :





# Coupling formalism with $T$ matrix

- Resonances  $\rightarrow$  Poles of the Scattering Matrix:

$$S_\alpha^{\alpha'} = 1 - 2\pi i \sqrt{\mu_\alpha \mu_{\alpha'} k_\alpha k_{\alpha'}} T_\alpha^{\alpha'}(E + i0; k_{\alpha'}, k_\alpha)$$

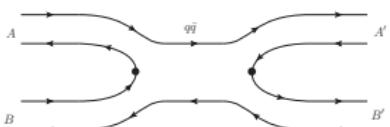
- $T$  matrix obtained with Lippmann-Schwinger:

$$T^{\beta'\beta}(E; P', P) = V_T^{\beta'\beta}(P', P) + \sum_{\beta''} \int dP'' P''^2 V_T^{\beta'\beta''}(P', P'') \frac{1}{E - E_{\beta''}(P'')} T^{\beta''\beta}(E; P'', P)$$

- With  $V_T^{\beta'\beta}(P', P) = V^{\beta'\beta}(P', P) + V_{\text{eff}}^{\beta'\beta}(P', P)$

where

$$V_{\text{eff}}^{\beta'\beta}(P', P) = \sum_\alpha \frac{h_{\beta'\alpha}(P') h_{\alpha\beta}(P)}{E - M_\alpha}$$



The complete  $T$  matrix factorizes like  $V_T$ :

$$T^{\beta'\beta}(E; P', P) = T_V^{\beta'\beta}(E; P', P) + \sum_{\alpha, \alpha'} \phi^{\beta'\alpha'}(E; P') \Delta_{\alpha'\alpha}(E)^{-1} \bar{\phi}^{\alpha\beta}(E; P)$$



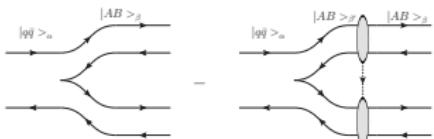
# Coupling elements

From  $T^{\beta'\beta}(E; P', P) = T_V^{\beta'\beta}(E; P', P) + \sum_{\alpha, \alpha'} \phi^{\beta'\alpha'}(E; P') \Delta_{\alpha'\alpha}(E)^{-1} \bar{\phi}^{\alpha\beta}(E; P)$ :

- Modified vertex:

$$\phi^{\alpha\beta'}(E; P) = h_{\alpha\beta'}(P) - \sum_{\beta} \int \frac{T_V^{\beta'\beta}(E; P, q) h_{\alpha\beta}(q)}{q^2/2\mu - E} q^2 dq,$$

$$\bar{\phi}^{\alpha\beta}(E; P) = h_{\alpha\beta}(P) - \sum_{\beta'} \int \frac{h_{\alpha\beta'}(q) T_V^{\beta'\beta}(q, P, E)}{q^2/2\mu - E} q^2 dq$$

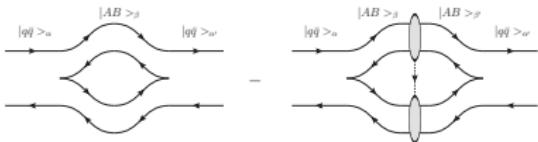


- Complete propagator:

$$\Delta^{\alpha'\alpha}(E) = \left\{ (E - M_{\alpha}) \delta^{\alpha'\alpha} + \mathcal{G}^{\alpha'\alpha}(E) \right\}$$

- Exact mass-shift of the state:

$$\mathcal{G}^{\alpha'\alpha}(E) = \sum_{\beta} \int dq q^2 \frac{\phi^{\alpha\beta}(q, E) h_{\beta\alpha'}(q)}{q^2/2\mu - E}$$





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# $X(3872)$ state

- Quantum numbers:  $J^{PC} = 1^{++}$
- Width :  $\Gamma < 1.2$  (90% C.L.)
- Mass :  $M_X = 3871.69 \pm 0.17 \text{ MeV}/c^2 \rightarrow$   
Close & slightly below  $D^0\bar{D}^{*0}$  threshold.
- $R_1 = \frac{\mathcal{B}(X \rightarrow J/\psi \pi^+ \pi^- \pi^0)}{\mathcal{B}(X \rightarrow J/\psi \pi^+ \pi^-)} = \begin{cases} 1.0 \pm 0.4 \pm 0.3 & (\text{Belle}) \\ 0.8 \pm 0.3 & (\text{BaBar}) \end{cases},$
- $R_2 = \frac{\mathcal{B}(X \rightarrow J/\psi \gamma)}{\mathcal{B}(X \rightarrow J/\psi \pi^+ \pi^-)} = \begin{cases} 0.33 \pm 0.12 & (\text{BaBar}) \\ 0.14 \pm 0.05 & (\text{Belle}) \end{cases},$
- $R_3 = \frac{\mathcal{B}(X \rightarrow \psi(2S) \gamma)}{\mathcal{B}(X \rightarrow J/\psi \gamma)} = 2.6 \pm 0.6$  (LHCb).

Experimental data suggest a loosely-bound  $D^0 D^{*0}$  molecule coupled to  $2P$   $c\bar{c}$  states.

P. G. Ortega *et al.*, PRD 81, 054023 (2010).



# Results for the $X(3872)$ coupled calculation

- $D^0 D^{*0}$  and  $D^\pm D^{*\mp}$  meson-meson channels are included
- Coupled to  $c\bar{c}(2^3P_1)$  meson state  $\rightarrow$  Theoretical bare mass = 3947.4 MeV
- Inclusion of  $J/\psi\rho$  y  $J/\psi\omega$  channels, needed for describing the strong decays  $\rightarrow$  Rearrangement diagrams  
Small contribution to the mass
- The value of  $\gamma$  is fine-tuned to obtain the  $X(3872)$  experimental mass

$\gamma$	$E_{bind}$	$c\bar{c}(2^3P_1)$	$D^0 D^{*0}$	$D^\pm D^{*\mp}$	$J/\psi\rho$	$J/\psi\omega$
0.231	-0.60	12.40	79.24	7.46	0.49	0.40
0.226	-0.25	8.00	86.61	4.58	0.53	0.29



# $X(3872)$ strong and radiative decay results

- Experimental results

$$\begin{aligned} R_1 &= \frac{\mathcal{B}(X \rightarrow J/\psi \pi^+ \pi^- \pi^0)}{\mathcal{B}(X \rightarrow J/\psi \pi^+ \pi^-)} &= & \begin{cases} 1.0 \pm 0.4 \pm 0.3 \\ 0.8 \pm 0.3 \end{cases}, \\ R_2 &= \frac{\mathcal{B}(X \rightarrow J/\psi \gamma)}{\mathcal{B}(X \rightarrow J/\psi \pi^+ \pi^-)} &= & \begin{cases} 0.33 \pm 0.12 \\ 0.14 \pm 0.05 \end{cases}, \\ R_3 &= \frac{\mathcal{B}(X \rightarrow \psi(2S) \gamma)}{\mathcal{B}(X \rightarrow J/\psi \gamma)} &= & 2.6 \pm 0.6 \end{aligned}$$

- Theoretical decays [keV]:

$E_{bind}$	$\Gamma_{\pi^+ \pi^- J/\psi}$	$\Gamma_{\pi^+ \pi^- \pi^0 J/\psi}$	$\Gamma_{J/\psi \gamma}^M$	$\Gamma_{J/\psi \gamma}^{c\bar{c}}$	$\Gamma_{\Psi(2S) \gamma}^{c\bar{c}}$
-0.60	27.61	14.40	0.070	8.15	9.80
-0.25	24.18	10.64	0.056	5.25	6.31

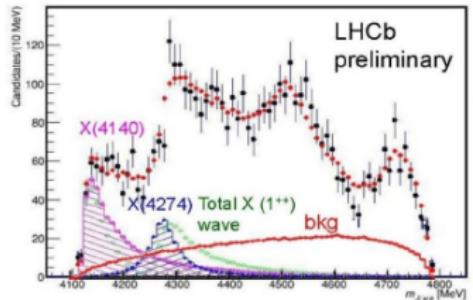
- Theoretical ratios:

$E_{bind}$	$R_1$	$R_2$	$R_3$
-0.60	0.52	0.30	1.20
-0.25	0.44	0.22	1.20



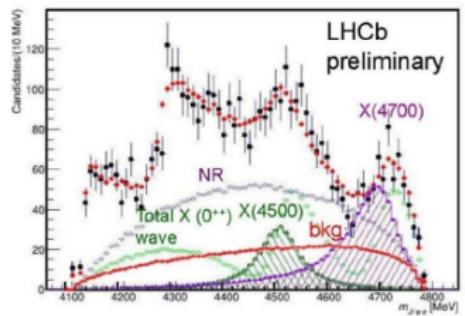
# LHCb Resonances

**X(1<sup>++</sup>)**



Contri- bution	sign. or Ref.	$M_0$ MeV	$\Gamma_0$ MeV	Fit results F.F. %
All $X(1^+)$				$16 \pm 3 \pm 6$
$X(4140)$	$8.4\sigma$	$4146.5 \pm 4.5 \pm 4.6$	$83 \pm 21 \pm 21$	$13 \pm 3.2 \pm 4.8$
ave.		$4146.9 \pm 2.3$	$17.8 \pm 6.8$	
$X(4274)$	$6.0\sigma$	$4273.3 \pm 8.3 \pm 17.2$	$56 \pm 11 \pm 8$	$7.1 \pm 2.5 \pm 3.5$
CDF		$4274.4 \pm 8.4 \pm 3.6$	$32 \pm 22 \pm 8$	
CMS		$4313.8 \pm 5.3 \pm 7.3$	$38 \pm 9 \pm 16$	

**X(0<sup>++</sup>)**



Contri- bution	sign.	$M_0$ MeV	$\Gamma_0$ MeV	Fit results F.F. %
All $X(0^+)$				$28 \pm 5 \pm 7$
NR $_{J/\psi\phi}$	$6.4\sigma$			$46 \pm 11 \pm 11$
$X(4500)$	$6.1\sigma$	$4506 \pm 11 \pm 12$	$92 \pm 21 \pm 21$	$6.6 \pm 2.4 \pm 3.5$
$X(4700)$	$5.6\sigma$	$4704 \pm 10 \pm 14$	$120 \pm 31 \pm 42$	$12 \pm 5 \pm 9$



# LHCb Resonances: $X(4274)$ , $X(4500)$ and $X(4700)$

- States fit naive QM predictions!  $\rightarrow$  non- $q\bar{q}$  part not important.
- Quark model predictions:

State	$J^{PC}$	$nL$	Mass (MeV/ $c^2$ )	Width (MeV)	Exp. (MeV/ $c^2$ )
$\chi_{c0}$	0 <sup>++</sup>	3P	4261.7		
		4P	4497.7	115.40	$4506 \pm 11^{+12}_{-15}$
		5P	4697.6	112.02	$4704 \pm 10^{+14}_{-24}$
		6P	4855.6		
$\chi_{c1}$	1 <sup>++</sup>	3P	4271.5	29.80	$4273.3 \pm 8.3$
		4P	4520.8		

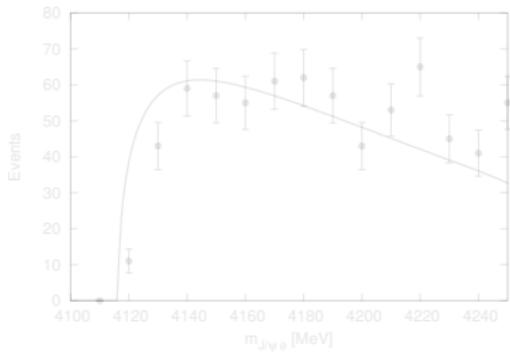
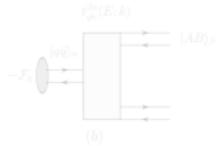
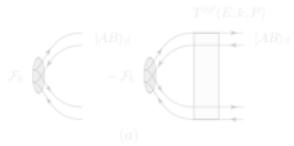
- LHCb results:

Contri- bution	sign. or Ref.	$M_0$ MeV	$\Gamma_0$ MeV	Contri- bution	sign.	$M_0$ MeV	$\Gamma_0$ MeV
All $X(1^+)$				All $X(0^+)$			
$X(4140)$	$8.4\sigma$	$4146.5 \pm 4.5^{+1.6}_{-2.8}$	$83 \pm 21^{+21}_{-14}$	$NR_{J/\psi\phi}$	$6.4\sigma$		
ave.		$4146.9 \pm 2.3$	$17.8 \pm 6.8$	$X(4500)$	$6.1\sigma$	$4506 \pm 11^{+12}_{-15}$	$92 \pm 21^{+21}_{-20}$
$X(4274)$	$6.0\sigma$	$4273.3 \pm 8.3^{+17.2}_{-3.6}$	$56 \pm 11^{+8}_{-11}$	$X(4700)$	$5.6\sigma$	$4704 \pm 10^{+14}_{-24}$	$120 \pm 31^{+42}_{-33}$
CDF		$4274.4^{+8.2}_{-6.7} \pm 1.9$	$32^{+25}_{-15} \pm 8$				
CMS		$4313.8 \pm 5.3 \pm 7.3$	$38^{+30}_{-15} \pm 16$				



# LHCb Resonances: Searching for $X(4140)$

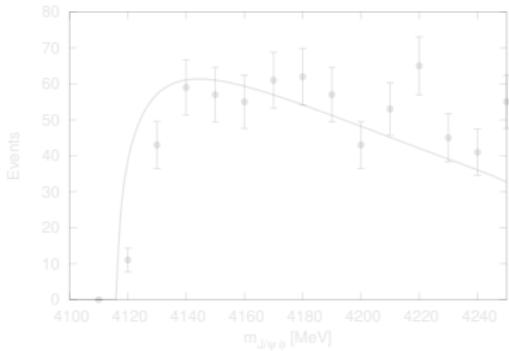
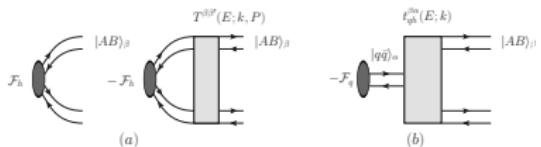
- Coupling channel calculation for the  $J^{PC} = 1^{++}$  sector:  $D_s^{(*)} D_s^{(*)}$  and  $J/\psi \phi$  channels.
- Any signal of  $X(4140)$  neither bound nor virtual





# LHCb Resonances: Searching for $X(4140)$

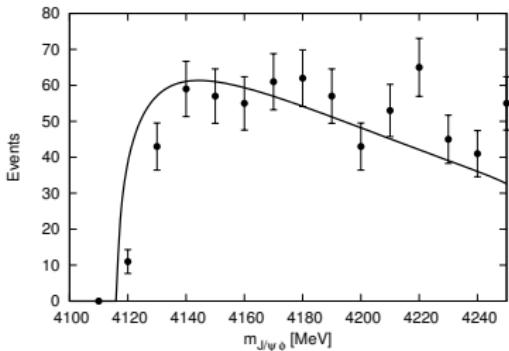
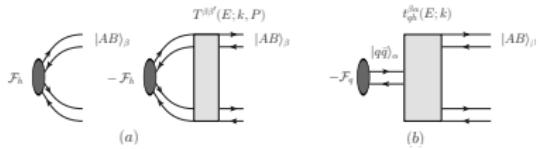
- Coupling channel calculation for the  $J^{PC} = 1^{++}$  sector:  $D_s^{(*)}D_s^{(*)}$  and  $J/\psi\phi$  channels.
- Any signal of  $X(4140)$  neither bound nor virtual  $\rightarrow$  Analysis of line shapes of  $J/\psi\phi$  channel





# LHCb Resonances: Searching for $X(4140)$

- Coupling channel calculation for the  $J^{PC} = 1^{++}$  sector:  $D_s^{(*)}D_s^{(*)}$  and  $J/\psi\phi$  channels.
- Any signal of  $X(4140)$  neither bound nor virtual  $\rightarrow$  Analysis of line shapes of  $J/\psi\phi$  channel



- The  $X(4140)$  appears as a threshold cusp



# LHCb Resonances: Searching for $X(4140)$

- Coupling channel calculation for the  $J^{PC} = 1^{++}$  sector:  $D_s^{(*)} D_s^{(*)}$  and  $J/\psi \phi$  channels.
- Any signal of  $X(4140)$  neither bound nor virtual

More details at:

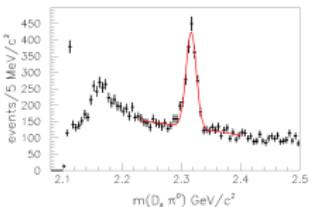
P. G. Ortega *et al.*, PRD 94, 114018 (2016) -- arxiv:1608.01325



# $D_{s0}^*(2317)$ and $D_{s1}(2460)$ open-charm mesons

- $D_{s0}^*(2317)$   $[0^+]$  ↪ Discovered in 2003 in  $D_s^+\pi^0$  by CLEO.
- $D_{s1}(2460)$   $[1^+]$  ↪ Discovered in 2003 in  $D_s^{*+}\pi^0$  by BaBar.
- Very narrow states below the  $D^{(*)}K$  thresholds.
- States far from naive quark models and heavy quark symmetry expectations ↪  $\sim 100$  MeV above thresholds
- $D_{s1}(2536)$   $[1^+]$  width:  $0.92 \pm 0.05$  MeV ↪  $j_q = \frac{3}{2}$  HQS state?

- $c\bar{s}$  system ↪ Heavy Quark Symmetry
- $D^{(*)}K$  molecular states? Renormalized  $c\bar{s}$ ?

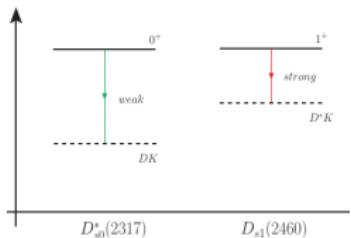


Good agreement with experiments when  $DK$  operators are included.

D. Mohler *et al.* PRL 111, 222001; C. B. Lang *et al.* PRD90, 034510; G. S. Bali *et al.* arXiv:1706.01247.

# $D_{s0}^*(2317)$ and $D_{s1}(2460)$ open-charm mesons

- Potential mass shift depend only on energy difference between  $c\bar{s}$  state and the open-flavored threshold.



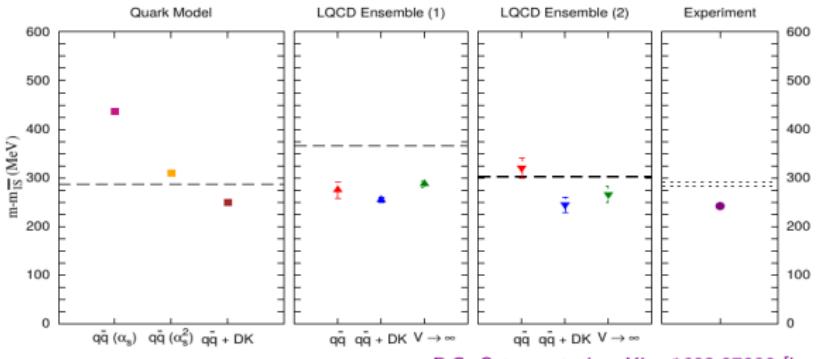
- Similar dynamics for  $0^+$  and  $1^+$   $\rightarrow j_q^P = 1/2^+$  HQS doublet.
- The states should be degenerated.
- They should couple equally to  $DK$  and  $D^*K$ .

- Addition of the one-loop QCD correction to the spin-dependent term of the potential. S.N. Gupta and S.F. Radford, PRD24, 2309 (1981).
- There is a spin-dependent term which affects only to mesons with different flavor quarks. O. Lakhina and E.S. Swanson, PLB650, 159 (2007).
- The  $0^+$  is more sensitive to the inclusion of the one-loop corrections.

	$j_q^P = 1/2^-$		$j_q^P = 1/2^+$		$j_q^P = 3/2^+$	
This work ( $\alpha_s$ )	0 <sup>-</sup> 1984	1 <sup>-</sup> 2110	0 <sup>+</sup> 2510	1 <sup>+</sup> 2593	1 <sup>+</sup> 2554	2 <sup>+</sup> 2591
This work ( $\alpha_s^2$ )	1984	2104	2383	2570	2560	2609
Exp.	$1969.0 \pm 1.4$	$2112.3 \pm 0.5$	$2318.0 \pm 1.0$	$2459.6 \pm 0.9$	$2535.12 \pm 0.25$	$2572.6 \pm 0.9$



# The $D_{s0}^*(2317)$ meson



P.G. Ortega et al., arXiv: 1603.07000 [hep-ph]

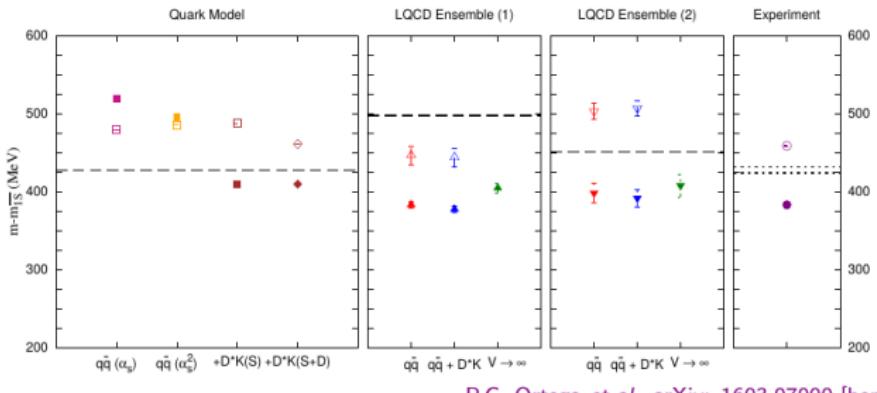
LQCD data: C. B. Lang et al. PRD90, 034510 (2014).

- **Input:** Bare  $c\bar{s}$  ( $1^3P_0$ ) state +  $DK$  threshold.
- Mass much higher using naive quark model and no 1-loop correction.
- Mass due to  $\alpha_s^2$ -corrections allows the  $0^+$  to be closer to  $DK$  threshold  $\rightarrow$   $DK$  coupling becomes a relevant dynamic mechanism.
- When we couple the  $0^+$   $c\bar{s}$  ground state with the  $DK$  threshold the mass is in good agreement with experiment.

State	Mass	$\mathcal{P}[q\bar{q}(^3P_0)]$	$\mathcal{P}[DK(S-\text{wave})]$
$D_{s0}^*(2317)$	2323.7	66.3%	33.7%



# The $D_{s1}(2460)$ and $D_{s1}(2536)$ mesons (I)



P.G. Ortega *et al.*, arXiv: 1603.07000 [hep-ph]

LQCD data: C. B. Lang *et al.* PRD90, 034510 (2014).

- **Input:** Bare  $c\bar{s}$  ( $1^1P_1$ ) and ( $1^3P_1$ ) states +  $D^*K$  threshold (S & D waves).
- Naive quark model predicts states **almost degenerated**, with masses close to the experimentally observed mass of the  $D_{s1}(2536)$ .
- The inclusion of the 1-loop corrections to the OGE potential does not improve the situation, making the **splitting between the two states even smaller**.



# The $D_{s1}(2460)$ and $D_{s1}(2536)$ mesons (II)

State	Mass	Width	$\mathcal{P}[q\bar{q}({}^1P_1)]$	$\mathcal{P}[q\bar{q}({}^3P_1)]$	$\mathcal{P}[D^*K(S)]$	$\mathcal{P}[D^*K(D)]$
$D_{s1}(2460)$	2484.0	0.00	12.9%	32.8%	54.3%	-
$D_{s1}(2536)$	2562.1	0.22	34.4%	15.8%	49.8%	-
$D_{s1}(2460)$	2484.0	0.00	12.1%	33.6%	54.1%	0.2%
$D_{s1}(2536)$	2535.2	0.56	31.9%	14.5%	16.8%	36.8%

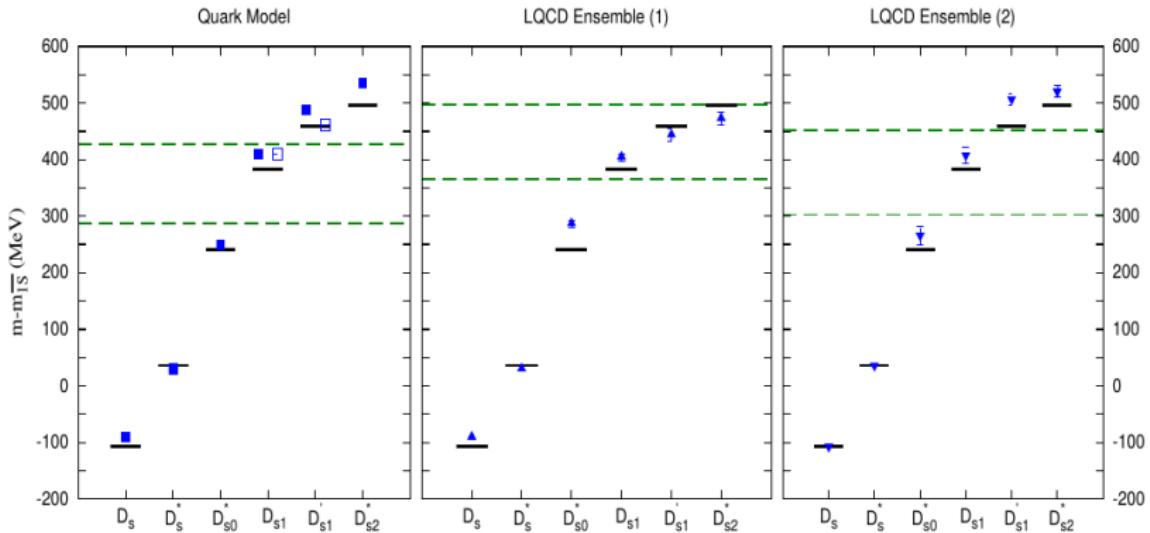
The  $q\bar{q}$  component in the wave function of the  $D_{s1}(2536)$  meson holds quite well the  ${}^1P_1$  and  ${}^3P_1$  composition predicted by HQS  $\rightarrow j_q^P = 3/2^+$  doublet.

Crucial in order to have a very narrow state and describe well its decays.

$$\begin{aligned}
 R_1 &= \frac{\Gamma(D_{s1}(2536)^+ \rightarrow D^{*0} K^+)}{\Gamma(D_{s1}(2536)^+ \rightarrow D^{*+} K^0)}, & \text{This work} && \text{Experiment} \\
 R_2 &= \frac{\Gamma_s(D_{s1}(2536)^+ \rightarrow D^{*+} K^0)}{\Gamma(D_{s1}(2536)^+ \rightarrow D^{*+} K^0)}, & \Gamma [\text{MeV}] & 0.56 & 0.92 \pm 0.03 \pm 0.04 \\
 R_3 &= \frac{\Gamma(D_{s1}(2536)^+ \rightarrow D^+ \pi^- K^+)}{\Gamma(D_{s1}(2536)^+ \rightarrow D^{*+} K^0)}, & R_1 & 1.15 & 1.18 \pm 0.16 \\
 & & R_2 & 0.52 & 0.72 \pm 0.05 \pm 0.01 \\
 & & R_3 [\%] & 14.5 & 3.27 \pm 0.18 \pm 0.37
 \end{aligned}$$

# Low-lying charmed-strange mesons

Overall agreement between quark model, lattice QCD and experimental data



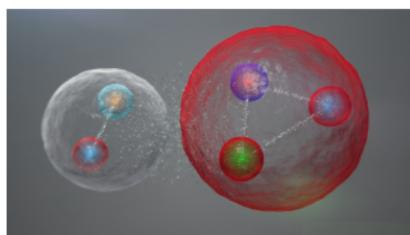
Theoretical results on  $D_{s1}^*(2700)$ ,  $D_{sJ}^*(2860)$  and  $D_{sJ}(3040)$  in PRD91, 094020 (2015).

P. G. Ortega *et al.*, PRD94, 074037 (2016) -- arxiv:1603.07000



# $\Lambda_c(2940)^+$ baryon

- Discovered in  $D^0 p$  and  $\Sigma_c(2455)^{0,++} \pi^\pm$  channels
- Mass:  $2939.8 \pm 1.3 \pm 1.0 \text{ MeV}/c^2$  Width:  $17.5 \pm 5.2 \pm 5.9 \text{ MeV}$  (BaBar)
- Mass:  $2938.0 \pm 1.3^{+2.0}_{-4.0} \text{ MeV}/c^2$  Width:  $13^{+8+27}_{-5-7} \text{ MeV}$  (Belle)
- Mass:  $2944.8 \pm 0.4^{+3.5}_{-2.5} \text{ MeV}/c^2$  Width:  $27.7 \pm 0.9^{+8.2}_{-6.0} \text{ MeV}$  (LHCb)
- $D^*{}^0 p$  molecule in  $S$ -wave?  $\rightarrow$  Possible quantum numbers:



$J^P$	$^{2S+1}L_J$		
$\frac{1}{2}^-$	$^2S_{\frac{1}{2}}$	$^4D_{\frac{1}{2}}$	
$\frac{1}{2}^+$	$^2P_{\frac{1}{2}}$	$^4P_{\frac{1}{2}}$	
$\frac{3}{2}^-$	$^4S_{\frac{3}{2}}$	$^2D_{\frac{3}{2}}$	$^4D_{\frac{3}{2}}$
$\frac{3}{2}^+$	$^2P_{\frac{3}{2}}$	$^4P_{\frac{3}{2}}$	$^4F_{\frac{3}{2}}$

- $J^P = \frac{3}{2}^-$  Similar scenario as the  $X(3872)$  state



# $\Lambda_c(2940)^+$ baryon: $D^*N$ in $J^P = \frac{3}{2}^-$ sector

- Only quark-quark interaction  $\rightarrow$  Pure  $D^*-N$  interaction
- $D^*N$  molecule in  $S$ -wave with  $J^P = \frac{3}{2}^-$
- Results including charged molecular states:

Mass	$\mathcal{P}_{4S_{3/2}}$	$\mathcal{P}_{2D_{3/2}}$	$\mathcal{P}_{4D_{3/2}}$	$\mathcal{P}_{D^{0*}p}$	$\mathcal{P}_{D^{+*}n}$	$\mathcal{P}_{I=0}$	$\mathcal{P}_{I=1}$
2938.80	96.22	0.86	2.92	63.93	36.07	97.52	2.48

- Decays:

Decay channel	Width (MeV)	decay channel	Width (keV)
$\Lambda_c^+ \rightarrow D^0 p$	9.42	$\Lambda_c^+ \rightarrow \Sigma_c^{++} \pi^-$	4.19
$\Lambda_c^+ \rightarrow D^+ n$	10.74	$\Lambda_c^+ \rightarrow \Sigma_c^+ \pi^0$	4.35
		$\Lambda_c^+ \rightarrow \Sigma_c^0 \pi^+$	4.51

- Total width:  $\Gamma = 20.2$  MeV
- Experimental width:  $\Gamma = 17^{+8}_{-6}$  MeV



# $\Lambda_c(2940)^+$ baryon: $D^*N$ in $J^P = \frac{3}{2}^-$ sector

- Only quark-quark interaction  $\rightarrow$  Pure  $D^*-N$  interaction
- $D^*N$  molecule in  $S$ -wave with  $J^P = \frac{3}{2}^- \rightarrow$  favoured by recent LHCb analysis!
- Results including charged molecular states:

Mass	$\mathcal{P}_{4S_{3/2}}$	$\mathcal{P}_{2D_{3/2}}$	$\mathcal{P}_{4D_{3/2}}$	$\mathcal{P}_{D^{0*}p}$	$\mathcal{P}_{D^{+*}n}$	$\mathcal{P}_{I=0}$	$\mathcal{P}_{I=1}$
2938.80	96.22	0.86	2.92	63.93	36.07	97.52	2.48

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- Total width:  $\Gamma = 20.2$  MeV
- Experimental width:  $\Gamma = 17^{+8}_{-6}$  MeV



# Partner in $b$ sector: $\Lambda_b(6248)^0$

- Possibility existence of a partner of  $\Lambda_b(2940)^+$  in  $b$  sector
- Description as a  $B^*N$  molecule in  $J^P = \frac{3}{2}^-$  sector.
- Results including charged molecular states:

$M$ (MeV)	$\mathcal{P}_{4S_{3/2}}$	$\mathcal{P}_{2D_{3/2}}$	$\mathcal{P}_{4D_{3/2}}$	$\mathcal{P}_{B^*-p}$	$\mathcal{P}_{B^{*0}n}$	$\mathcal{P}_{I=0}$	$\mathcal{P}_{I=1}$
6248.34	95.15	1.08	3.77	52.56	47.44	99.91	0.09

- Decays:

Decay channel	Width (MeV)	Decay channel	Width (keV)
$\Lambda_b^0 \rightarrow B^- p$	3.69	$\Lambda_b^0 \rightarrow \Sigma_b^+ \pi^-$	6.30
$\Lambda_b^0 \rightarrow B^0 n$	3.75	$\Lambda_b^0 \rightarrow \Sigma_b^0 \pi^0$	6.34
		$\Lambda_b^0 \rightarrow \Sigma_b^- \pi^+$	6.38

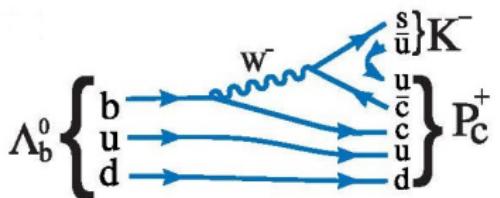
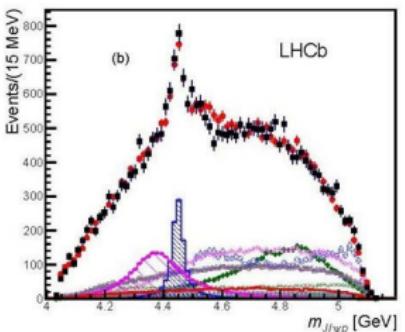
More details at:

P. G. Ortega et al., Physics Letters B 718, 1381-1384 (2013)

# LHCb Pentaquarks: $P_c(4380)$ and $P_c(4450)$

R. Aaij et al, *Phys. Rev. Lett.* **115**, 072001 (2015).

- Discovered in 2015 in  $\Lambda_b^0 \rightarrow J/\psi K^- p$  decay.
- Preferred quantum numbers:  $(\frac{3}{2}^\mp, \frac{5}{2}^\pm)$
- But other combinations such as  $(\frac{3}{2}^-, \frac{3}{2}^-)$  not excluded (L. Roca, arxiv:1602.06791)
- Masses close to  $D\Sigma_c^*$  and  $D^*\Sigma_c$  channel thresholds.



$$\begin{aligned}
 M_{P_c(4380)} &= 4380 \pm 8 \pm 29 \text{ MeV}, \\
 M_{P_c(4450)} &= 4449.8 \pm 1.7 \pm 2.5 \text{ MeV}, \\
 \Gamma_{P_c(4380)} &= 205 \pm 18 \pm 86 \text{ MeV}, \\
 \Gamma_{P_c(4450)} &= 39 \pm 5 \pm 19 \text{ MeV}.
 \end{aligned}$$



# LHCb pentaquarks: $P_c(4380)$ and $P_c(4450)$

- $\bar{D}^{(*)}\Sigma_c^{(*)}$  molecules in  $S$ -wave and  $P$ -wave.
- We obtain the following candidates:

$M_{P_c(4380)}$	$= 4380 \pm 8 \pm 29 \text{ MeV},$
$M_{P_c(4450)}$	$= 4449.8 \pm 1.7 \pm 2.5 \text{ MeV},$
$\Gamma_{P_c(4380)}$	$= 205 \pm 18 \pm 86 \text{ MeV},$
$\Gamma_{P_c(4450)}$	$= 39 \pm 5 \pm 19 \text{ MeV}.$

Molecule	$J^P$	$I$	Mass(MeV/ $c^2$ )	$B_E(\text{MeV}/c^2)$	Width $J/\psi p$	Width $\bar{D}^*\Lambda_c$
$\bar{D}\Sigma_c$	$\frac{1}{2}^-$	$\frac{1}{2}$	4320.8	0.8	2.4	1.1
$\bar{D}\Sigma_c^*$	$\frac{3}{2}^-$	$\frac{1}{2}$	4385.0	1.0	10.0	14.7
$\bar{D}^*\Sigma_c$	$\frac{1}{2}^-$	$\frac{1}{2}$	4458.9	3.8	5.3	63.6
$\bar{D}^*\Sigma_c$	$\frac{3}{2}^-$	$\frac{1}{2}$	4461.3	1.4	0.8	21.2
$\bar{D}^*\Sigma_c$	$\frac{3}{2}^+$	$\frac{1}{2}$	4462.7	0.01	0.2	6.3
$\bar{D}^*\Sigma_c^*$	$\frac{1}{2}^-$	$\frac{1}{2}$	4519.8	7.3	0.9	9.9
$\bar{D}^*\Sigma_c^*$	$\frac{3}{2}^-$	$\frac{1}{2}$	4523.3	3.9	22.9	4.0
$\bar{D}^*\Sigma_c^*$	$\frac{5}{2}^-$	$\frac{1}{2}$	4524.5	2.6	0.05	3.0
$\bar{D}^*\Sigma_c^*$	$\frac{5}{2}^+$	$\frac{1}{2}$	4526.2	1.0	0.05	0.8



# Outline

1 Motivation

2 The model

3 Results

4 Conclusions



# Conclusions

- Heavy quark sector shows a rich phenomenology, including four and five quark structures depending on the dynamics.
- The effect of nearby thresholds may generate non-trivial states (molecules) and structures (mass-shifts, threshold cusps) which modifies naive QM predictions, so they must be incorporated to the models.
- Use of Constituent Quark Model plus a coupled channels calculation can account for this phenomenology in an unified way from naive meson and baryon spectrum to the recently pentaquark signals (and beyond).



# Further details for results presented here...

- **X(3872):**
  - *Coupled channel approach to the structure of the X(3872) – PRD 81 (2010) 054023.*
  - *Molecular Structures in Charmonium Spectrum: The XYZ Puzzle – JPG 40 (2013) 065107.*
  - *Partners of the X(3872) and HQSS breaking – arXiv:1601.03901.*
  - *Counting states and the Hadron Resonance Gas: Does X(3872) count? – arXiv:1707.01915.*
- **XYZ in charmonium and bottomonium sector:**
  - *Canonical description of the new LHCb resonances – PRD 94 (2016), 114018.*
  - *Charmonium resonances in the 3.9 GeV/c<sup>2</sup> energy region and the X(3915)/X(3930) puzzle – arXiv:1706.02639.*
- **XYZ in open-charm and open-bottom meson spectra:**
  - *Molecular components in P-wave charmed-strange mesons – PRD 94 (2016), 074037.*
  - *Threshold effects in P-wave bottom-strange mesons – PRD 95 (2017), 034010.*
- **XYZ in baryon spectra:**
  - *Quark model description of the  $\Lambda_c(2940)^+$  as a molecular  $D^* N$  state and the possible existence of the  $\Lambda_b(6248)$  – PLB 718 (2013) 1381-1384.*
  - *LHCb pentaquarks in constituent quark models – PLB 764 (2017) 207-211.*
  - *Hadronic molecules in the open charm and open bottom baryon spectrum – PRD 90 (2014), 114013.*
  - *$D^* \Delta$  molecular interpretation for the  $X_c(3250)$  – PLB 729 (2014) 24-26.*



# Thanks for your attention.

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Acknowledgements:





# $X(3915)/X(3930)$ controversy

- $X(3915)$  seen in  $\gamma\gamma \rightarrow \omega J/\psi$  process
- Consistent with  $0^{++} \rightarrow$  assigned to  $\chi_{c0}(2P)$ .
- But...  $J^{PC} = 0^{++}$  assignment challenged by Guo and Meissner [arxiv:1208.1134] and Olsen [arxiv:1410.6534] because:
  - $X(3915) \rightarrow \omega J/\psi$  too large for OZI-suppressed decay.
  - No signal for  $X(3915) \rightarrow D\bar{D}$  decay.
  - If  $X(3930)$  is  $\chi_{c2}(2P)$ ,  $\chi_{c2}(2P) - \chi_{c0}(2P)$  mass splitting too small.
- Z.-Y. Zhou [arxiv:1501.00879] points to a  $J^P = 2^+$  assignment!  $\rightarrow$  Implies  $X(3915)$  might not be a pure  $c\bar{c}$  state.
- Besides,  $X(3860)$ , decaying to  $D\bar{D}$ , reported by Belle
- Mass:  $3862^{+26+40}_{-32-13}$  MeV/ $c^2$ , Width:  $201^{+154+88}_{-67-82}$  MeV
- $J^{PC} = 0^{++}$  option is favored over the  $2^{++}$  hypothesis.  $\rightarrow$  Is this the  $\chi_{c0}(2P)$ ?



# $X(3915)/X(3930)$ controversy

- Aim: Analyze if the  $0^{++}$  assignment for  $X(3915)$  is reasonable.
- Effect of the thresholds over the theoretical bare state?
- Two calculations for  $J^{PC} = 0^{++}$  and  $J^{PC} = 2^{++}$  sectors.
- Closest  $c\bar{c}$  states and thresholds (mass in MeV in parenthesis):
  - $J^{PC} = 0^{++}$ :  $2^3P_0$   $c\bar{c}$  (3909),  $D\bar{D}$  (3734),  $\omega J/\psi$  (3880),  $D_s D_s$  (3937) and  $D^* \bar{D}^*$  (4017)
  - $J^{PC} = 2^{++}$ :  $2^3P_2$   $c\bar{c}$  (3969),  $D\bar{D}$ ,  $\omega J/\psi$ ,  $D_s D_s$ ,  $D\bar{D}^*$  (3877) and  $D^* \bar{D}^*$



# Results for $J^{PC} = 0^{++} - 2^{++}$ (I)

- Mass and decay width, in MeV, and probabilities of the different Fock components.

$J^{PC}$	Mass	Width	$\mathcal{P}[c\bar{c}]$	$\mathcal{P}[D\bar{D}]$	$\mathcal{P}[D\bar{D}^*]$	$\mathcal{P}[\omega J/\psi]$	$\mathcal{P}[D_s\bar{D}_s]$	$\mathcal{P}[D^*\bar{D}^*]$
$0^{++}$	3890.3	6.7	44.1%	21.6%	—	28.4%	2.6%	3.3%
$0^{++}$	3927.4	229.8	19.2%	66.3%	—	5.3%	3.7%	5.5%
$2^{++}$	3925.6	19.0	42.2%	11.3%	37.0%	4.0%	0.4%	5.1%

- Mass and width of the  $2^{++}$  state compatible with the  $X(3930)$ .
- The  $0^{++}$  resonances - First guess:
  - Mass of first  $0^{++}$  compatible with  $X(3860)$ , but width smaller → Position of node in  $2^3P_0$  bare wave function?
  - Mass of second  $0^{++}$  state → Elusive  $Y(3940)$  resonance? But width far from experimental value, and controversial state.



# Results for $J^{PC} = 0^{++} - 2^{++}$ (I)

- Mass and decay width, in MeV, and probabilities of the different Fock components.

$J^{PC}$	Mass	Width	$\mathcal{P}[c\bar{c}]$	$\mathcal{P}[D\bar{D}]$	$\mathcal{P}[D\bar{D}^*]$	$\mathcal{P}[\omega J/\psi]$	$\mathcal{P}[D_s\bar{D}_s]$	$\mathcal{P}[D^*\bar{D}^*]$
$0^{++}$	3890.3	6.7	44.1%	21.6%	—	28.4%	2.6%	3.3%
$0^{++}$	3927.4	229.8	19.2%	66.3%	—	5.3%	3.7%	5.5%
$2^{++}$	3925.6	19.0	42.2%	11.3%	37.0%	4.0%	0.4%	5.1%

- Mass and width of the  $2^{++}$  state compatible with the  $X(3930)$ .
- The  $0^{++}$  resonances - Second guess:
  - First  $0^{++} \rightarrow$  Too narrow to be observed? Or  $X(3915)$ ?
  - Second  $0^{++}$  state  $\rightarrow X(3860)$  resonance. Width OK, but mass a bit high.



# Results for $J^{PC} = 0^{++} - 2^{++}$ (II)

- Now, if  $X(3915)$  is  $0^{++}$ ,  $\omega J/\psi$  branching far from experiments.
- Let's calculate for the  $J^{PC} = 2^{++}$  state the product of the two-photon decay width and the branching fraction to  $\omega J/\psi$  and  $D\bar{D}$  channels (in eV), assuming the  $X(3915)$  and  $X(3930)$  are the same  $2^{++}$  resonance.

	Belle	BaBar	model A
$\Gamma_{\gamma\gamma} \times \mathcal{B}(2^{++} \rightarrow \omega J/\psi)$	$18 \pm 5 \pm 2$	$10.5 \pm 1.9 \pm 0.6$	20.9
$\Gamma_{\gamma\gamma} \times \mathcal{B}(2^{++} \rightarrow D\bar{D})$	$180 \pm 50 \pm 30$	$249 \pm 50 \pm 40$	75.4
$\Gamma_{\gamma\gamma} \times \mathcal{B}(2^{++} \rightarrow D\bar{D}^*)$	-	-	196.0

- Results not far from the experimental data.
- $DD$  branching ratio a bit small, but crossed contribution from  $DD^*$  not considered.
- This suggest that the  $X(3915)/X(3930)$  resonances are the same  $2^{++}$  state.

More details at:

P. G. Ortega *et al.*, arxiv:1706.02639



## Results for the $X(3940)$ coupled calculation

- $X(3940) \rightarrow$  Seen on the  $J/\psi$  invariant mass spectrum
- Mass:  $3943 \pm 6 \pm 6 \text{ MeV}$       Width:  $52 \text{ MeV}$  to  $90\% C.L.$
- Decays to  $DD^*$  channel  $\rightarrow$  Good candidate for  $\chi_{c1}(2P)$
- Masses and probabilities:

$\gamma$	Masa	$\Gamma$	$c\bar{c}(2^3P_1)$	$D^0 D^{*0}$	$D^\pm D^{*\mp}$	$J/\psi\rho$	$J/\psi\omega$
0.231	3942.5	93.8	61.02	18.57	16.86	0.01	3.54
0.226	3941.8	89.9	61.09	18.53	16.85	0.01	3.52

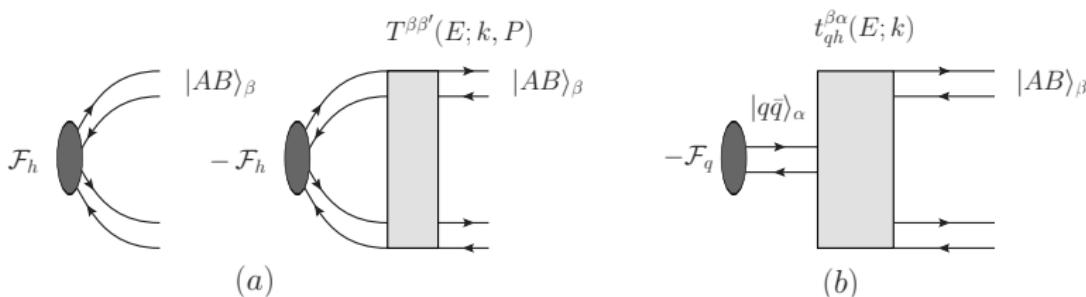
- Partial widths

$\gamma$	$D^0 D^{*0}$	$D^\pm D^{*\mp}$	$J/\psi\rho$	$J/\psi\omega$
0.231	41.82	41.91	0.04	10.01
0.226	40.15	40.28	0.03	9.45



# Lineshapes

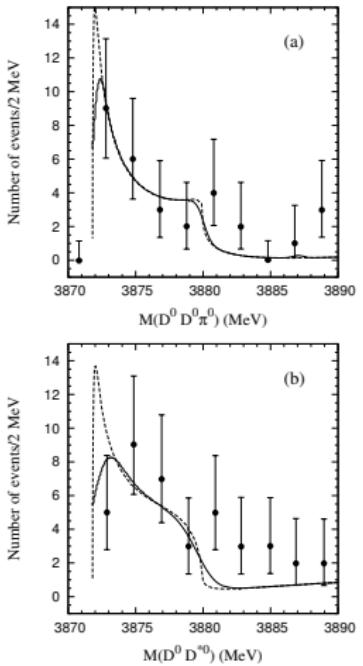
- Molecular contribution  $\rightarrow \frac{dB_{rh}((AB)^\beta)}{dE} = \text{const} \times k |\mathcal{M}_h^\beta(E)|^2 \Theta(E)$   
with  $\mathcal{M}_h^\beta(E) = \mathcal{F}_h \left( 1 - \sum_{\beta'} \int dP T^{\beta\beta'}(E; k_\beta, P) \frac{2\mu_{\beta'} P^2}{P^2 - k_{\beta'}^2} \right)_{\text{on shell}}$
- Mesonic contribution  $\rightarrow \frac{dB_{rq}((AB)^\beta)}{dE} = \text{const} \times k |\mathcal{M}_q^\beta(E)|^2 \Theta(E)$   
with  $\mathcal{M}_q^\beta = -\mathcal{F}_q \sum_{\alpha, \alpha'} \phi_{\alpha'\beta}(E; k) \Delta_{\alpha'\alpha}(E)^{-1}$



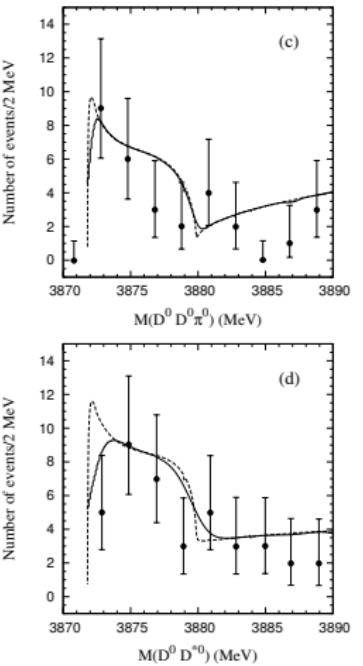


# Lineshapes for $X(3872)$ with $E_b = -0.25\text{ MeV}$

$c\bar{c}$  Production



$D\bar{D}^*$  Production



Belle  
 $B \rightarrow K D^0 \bar{D}^0 \pi^0$

BaBar  
 $B \rightarrow K D^0 \bar{D}^{*0}$