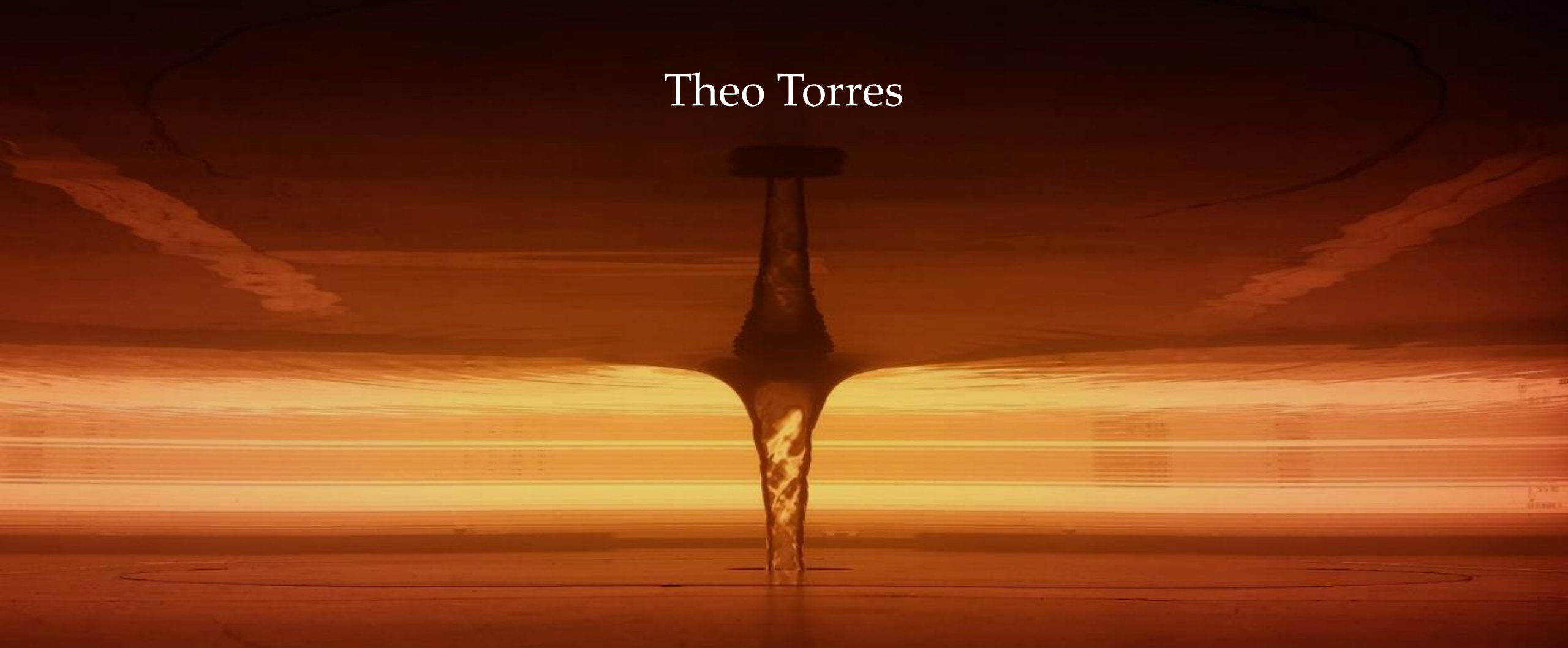


# Observing superradiance in a vortex flow

Theo Torres





The University of  
**Nottingham**

UNITED KINGDOM • CHINA • MALAYSIA



**Quantum Gravity**  
LABORATORY



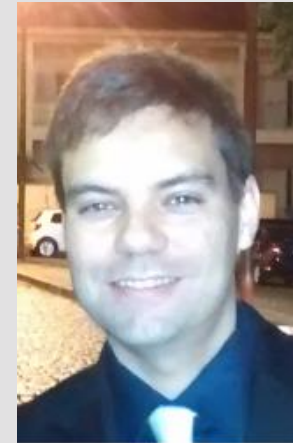
S. Patrick



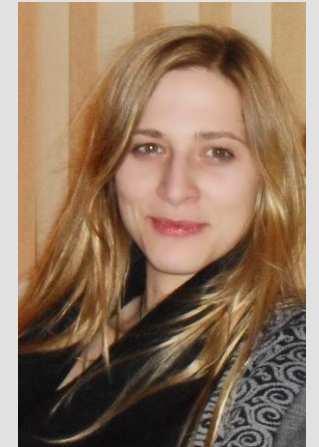
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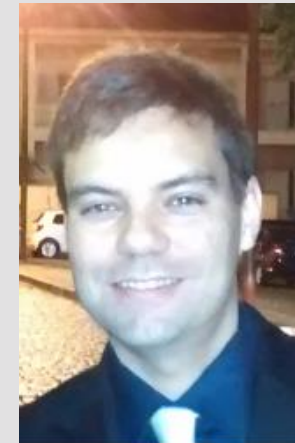
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*Rotational superradiant scattering in a vortex flow*, T.T. *et al*  
Nature Physics (June 2017), doi : 10.1038/nphys4151

# Introduction

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Use a hydrodynamic system to mimic gravity effect

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Analogue gravity

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Use a hydrodynamic system to mimic gravity effect



Good review

Barcelo *et al*, arXiv :  
gr-qc 0505065

Analogue gravity

- BEC
- Fluids of Light
- Water



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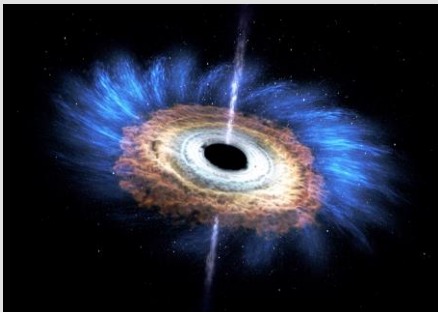
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Black holes



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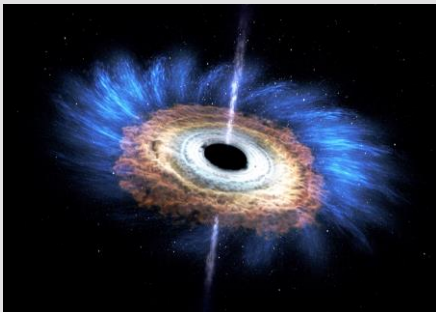
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Black holes



How do black holes lose  
their energy ?

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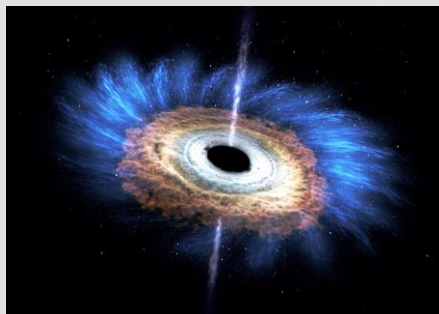
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Hawking  
Radiation

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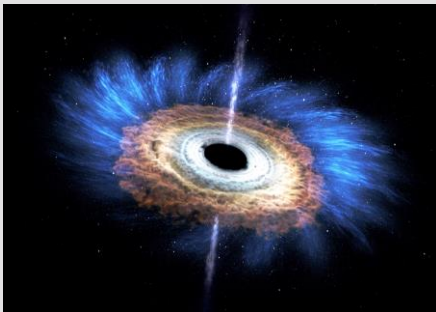
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Superradiance



Hawking  
Radiation

# Superradiance

---

# Superradiance

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- Zel'Dovich (1971)
- Rotating Black Holes
- Many other systems

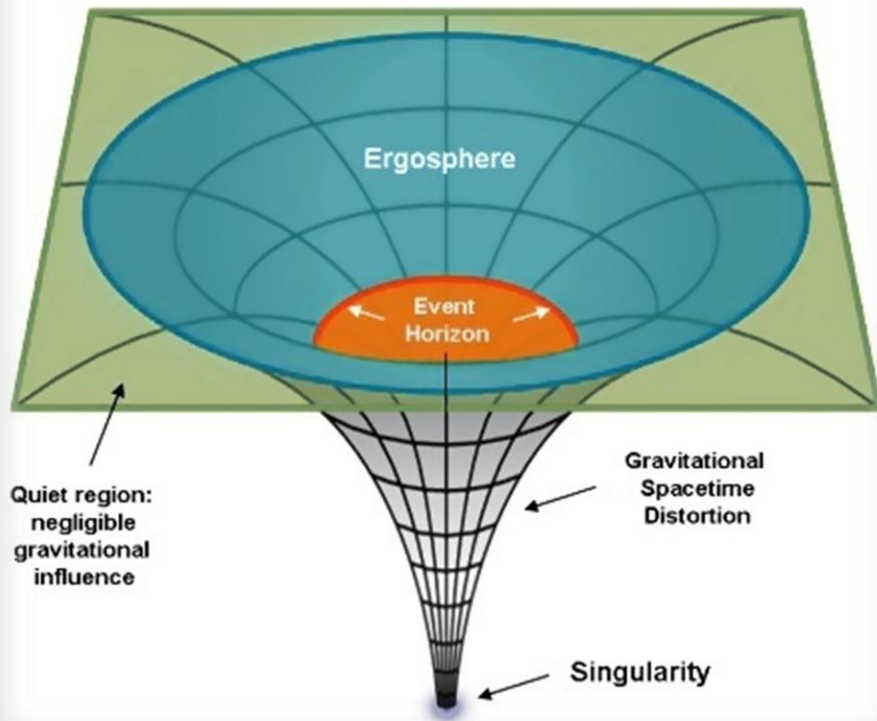
Review : Brito *et al*,  
Superradiance. Lect. Notes Phys.,  
906:pp.1-237,2015.

# Superradiance

---

## Rotating Black Holes

### Black Hole Regions





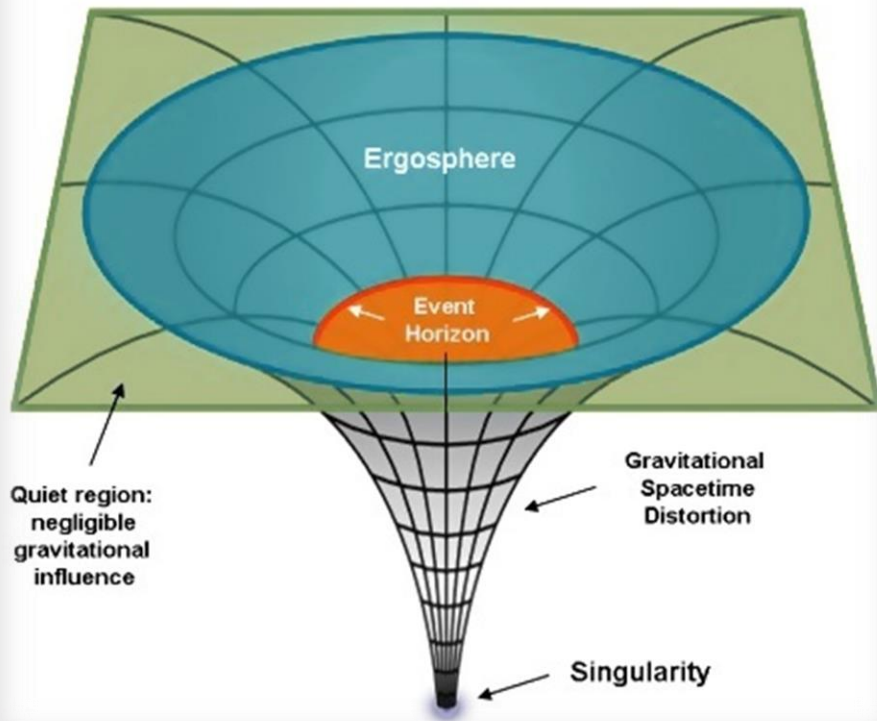
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Rotating Black Holes

During 70's : Bekenstein and Hawking  
Black Hole Thermodynamics

**Black Hole Regions**

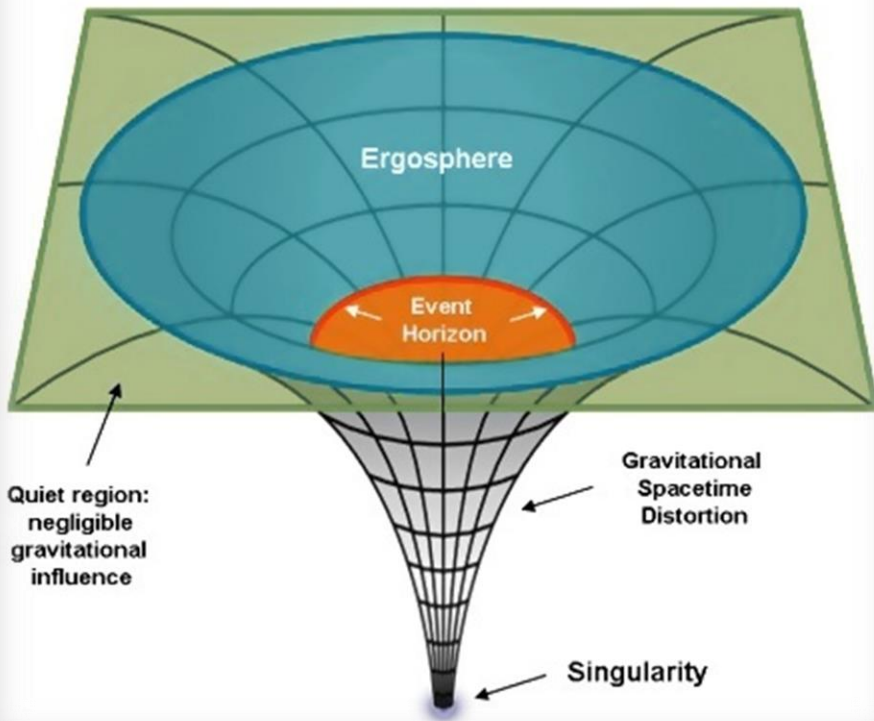


# Superradiance

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## Rotating Black Holes

### Black Hole Regions



During 70's : Bekenstein and Hawking  
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$$S_{BH} = \frac{k_B A}{4l_P^2}$$

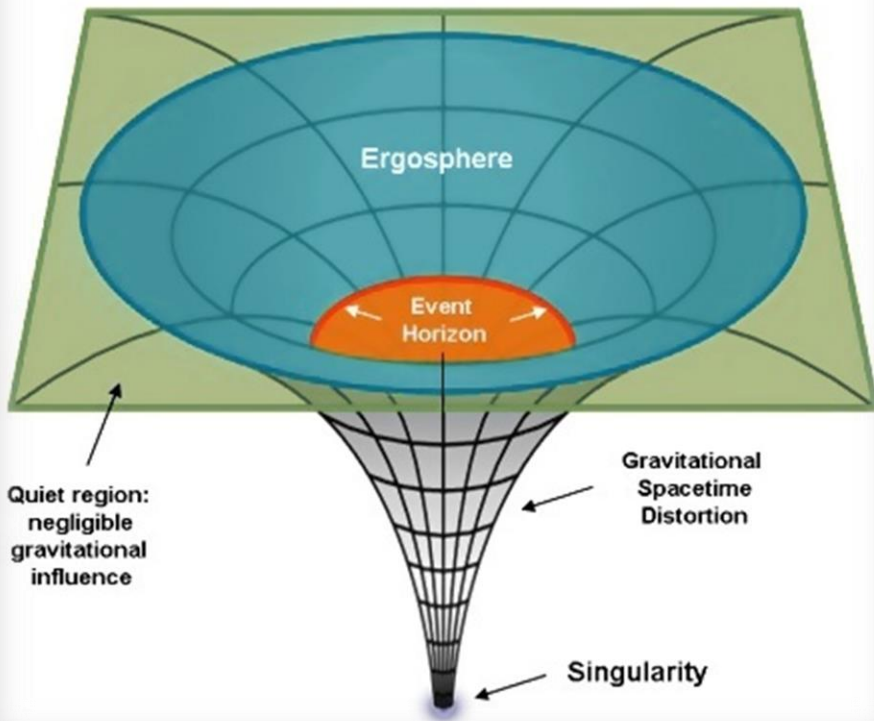
$$\text{First law : } \delta M = \frac{\kappa}{8\pi} \delta A + \Omega_H \delta J$$

$$\text{Second law : } \delta A \geq 0$$

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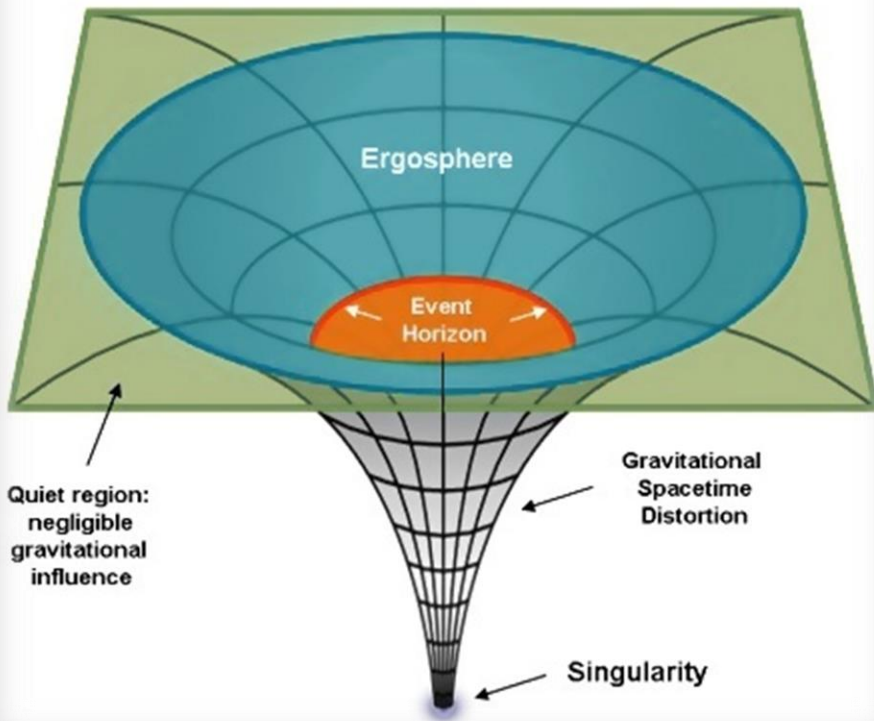
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Superradiance : Radiance enhancement process

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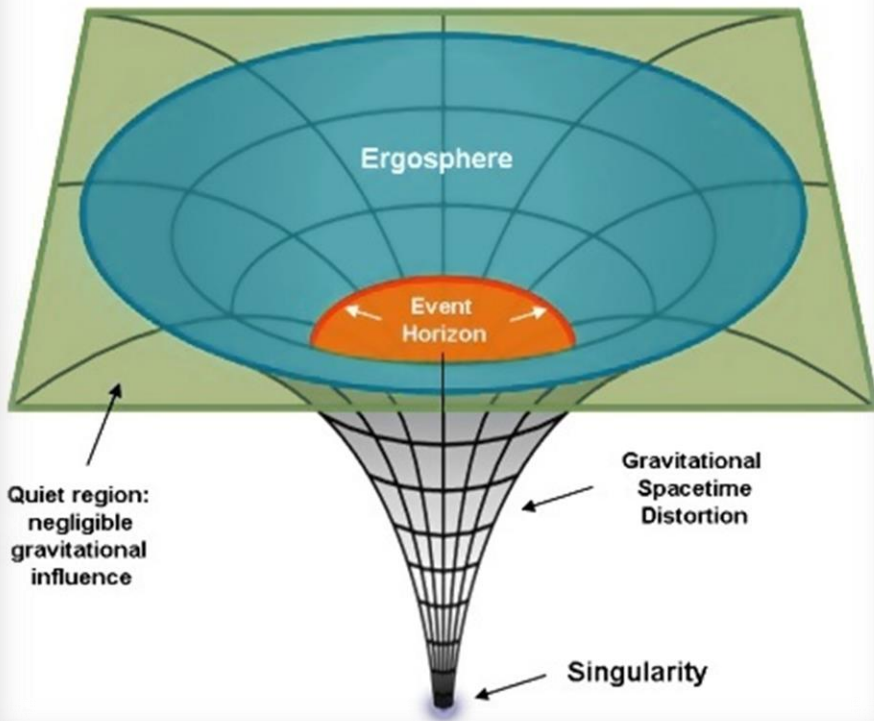
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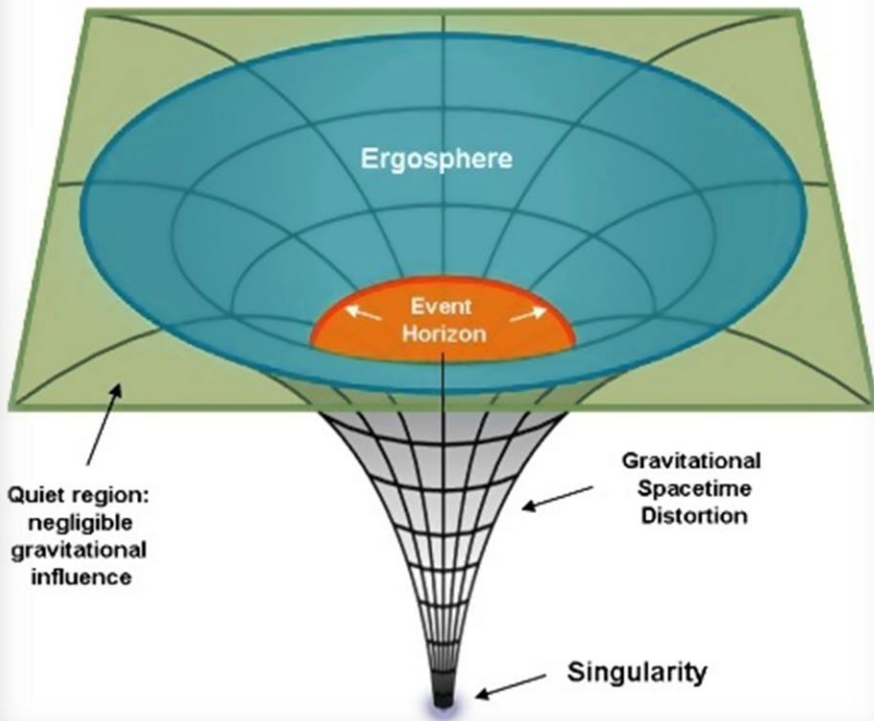
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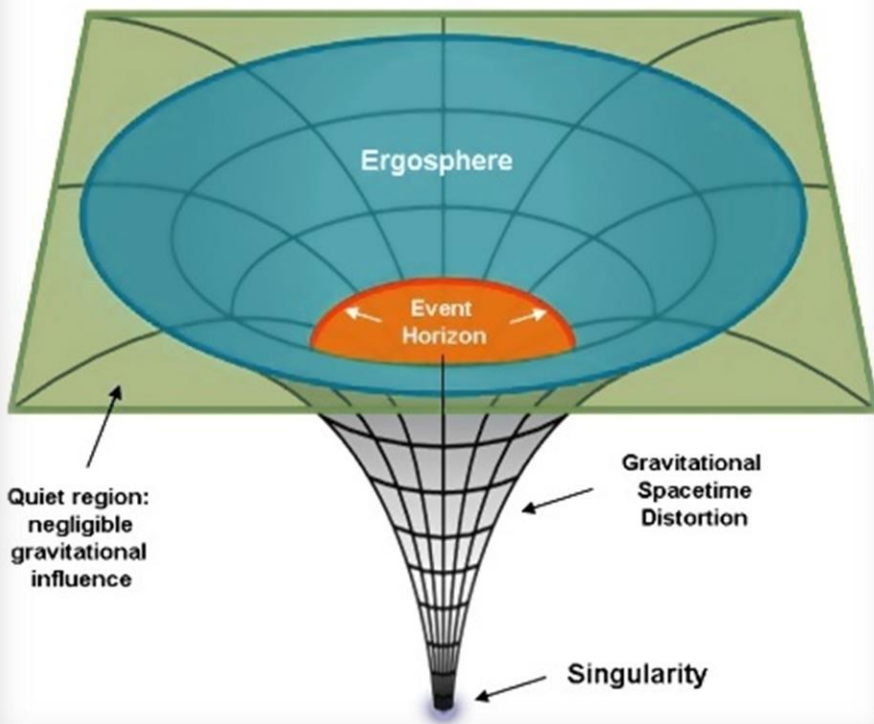
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# Superradiance

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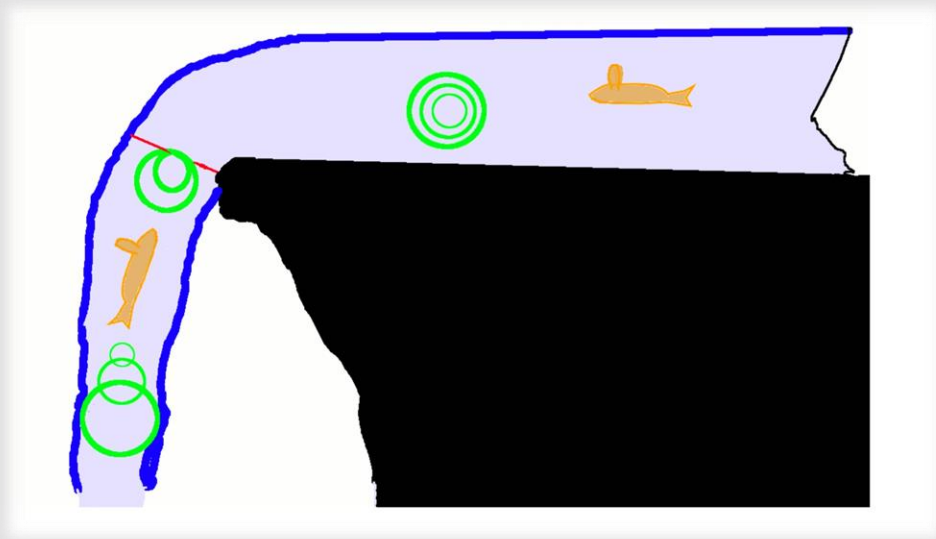
# Analogue gravity

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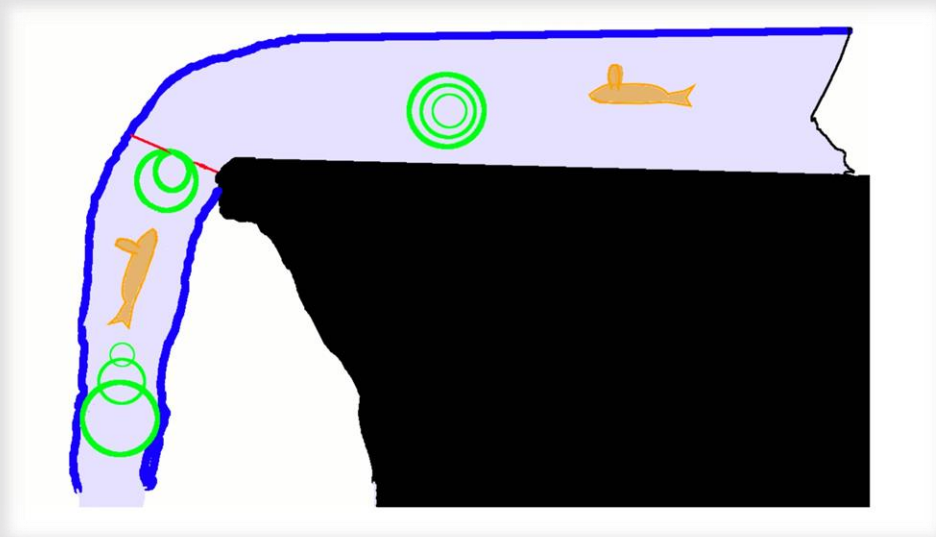
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Credits : W. Unruh

# Analogue gravity

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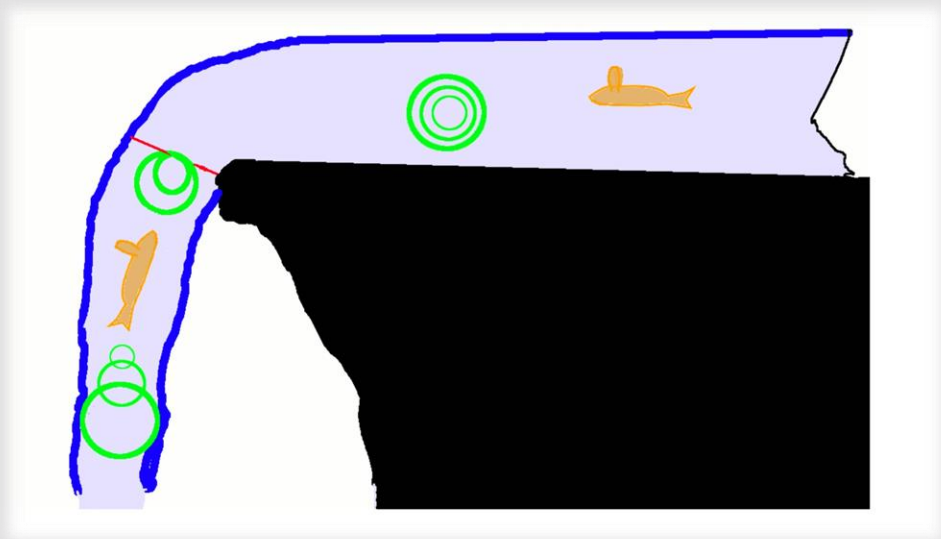


Credits : W. Unruh

When  $c_{Flow} < c_{wave}$  : can propagate  
in all direction

# Analogue gravity

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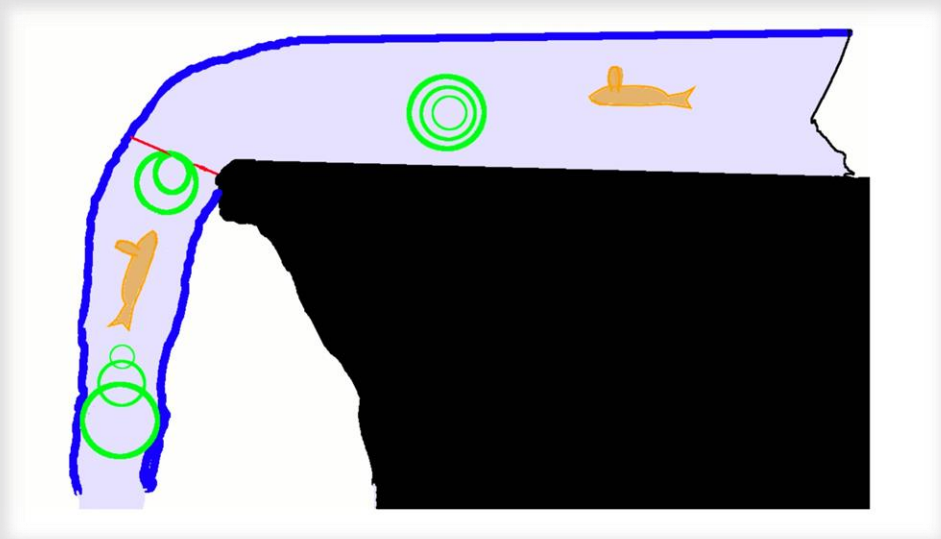
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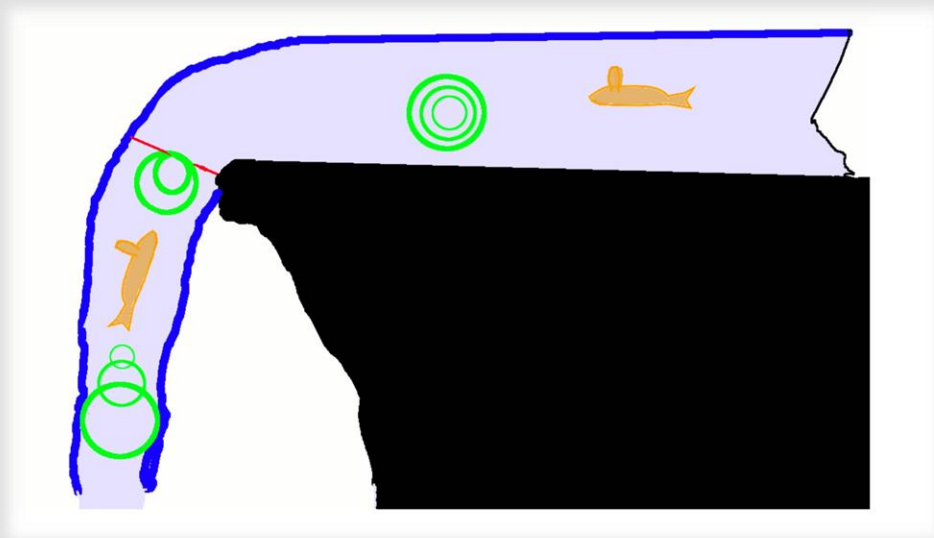
Analogue horizon

# Analogue gravity

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Mathematically equivalent !

R.Schützhold and W.G. Unruh.  
Gravity wave analogues of black holes.  
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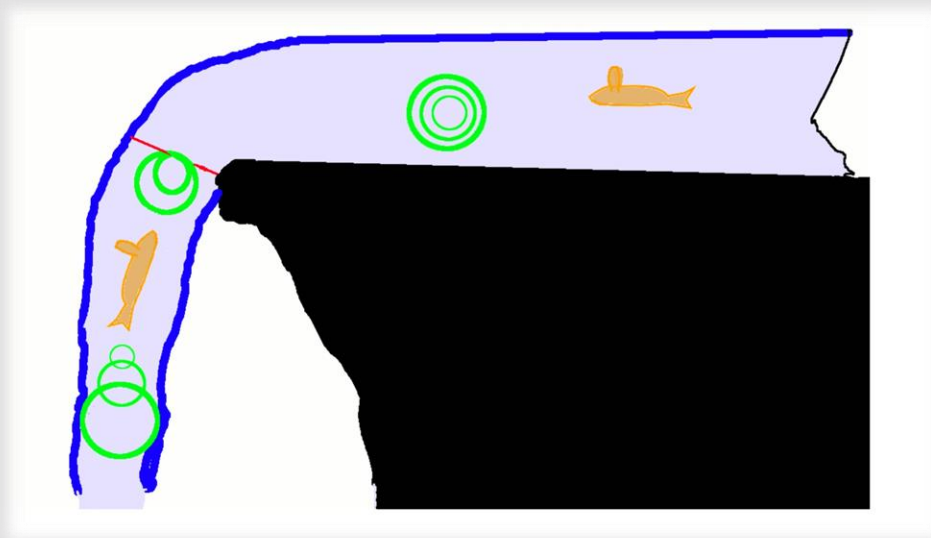
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Navier-Stokes + Continuity + Boundary conditions



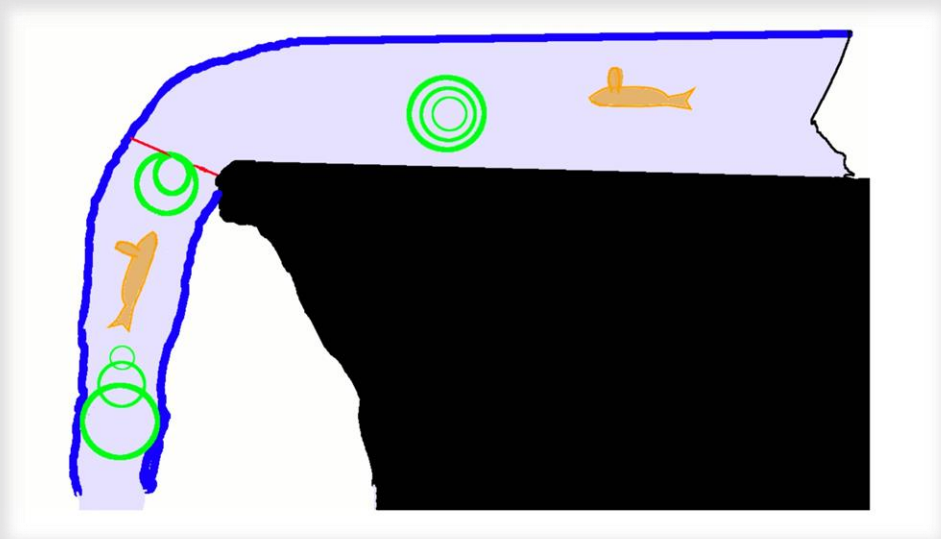
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Flow : Inviscid fluid, Incompressible, Irrotational  
Waves : Small amplitude, Shallow water waves

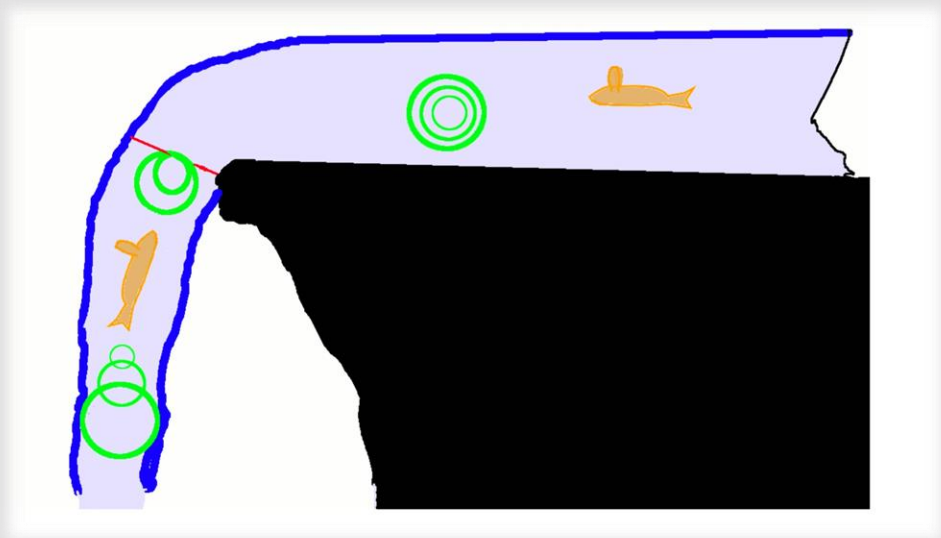
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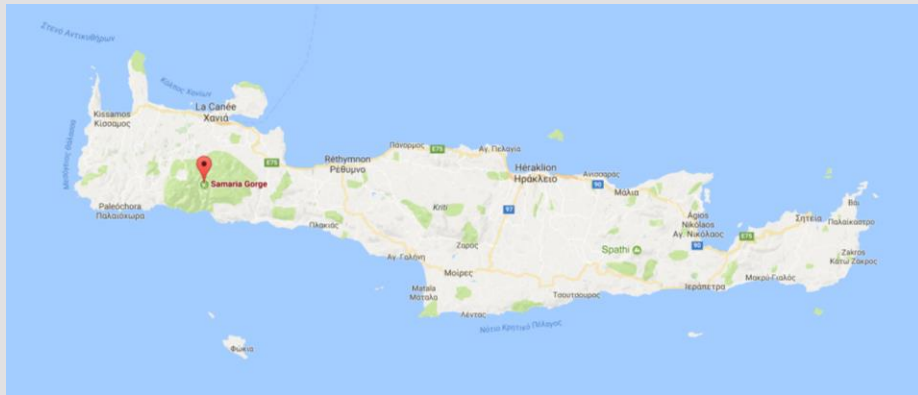
Scalar field  
propagating on  
an effective metric

$$g^{\mu\nu} = \begin{pmatrix} 1 & \vec{v}_B \\ \vec{v}_B^T & \vec{v}_B \times \vec{v}_B - gh_B \cdot Id \end{pmatrix}$$



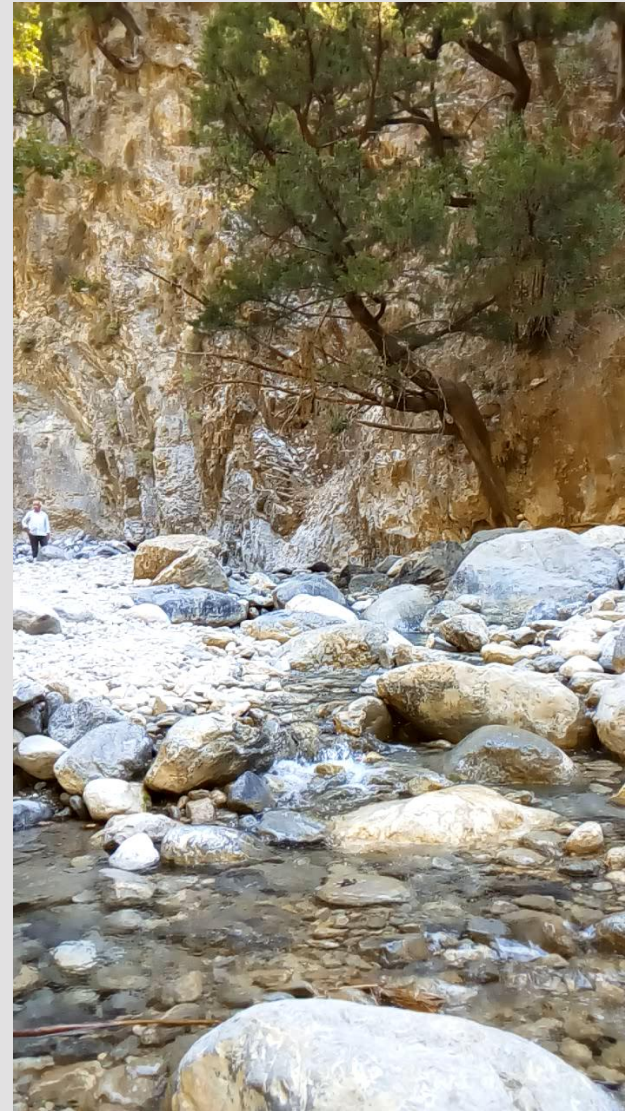
# Analogue gravity

## Example in Samaria Gorges



Scalar field  
propagating on  
an effective metric

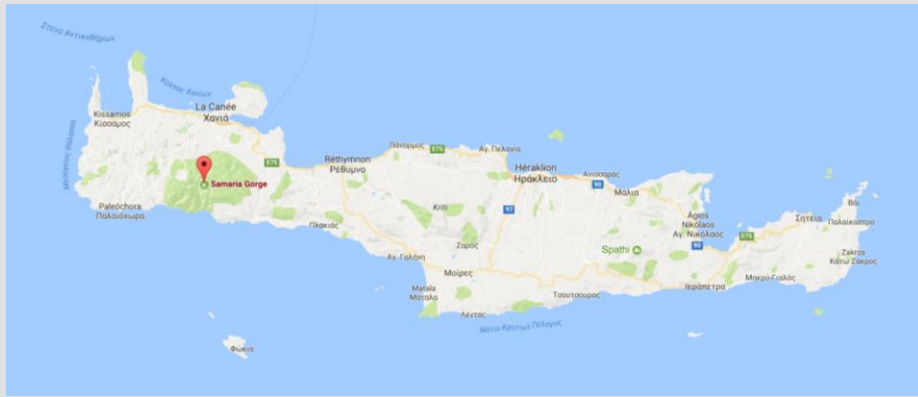
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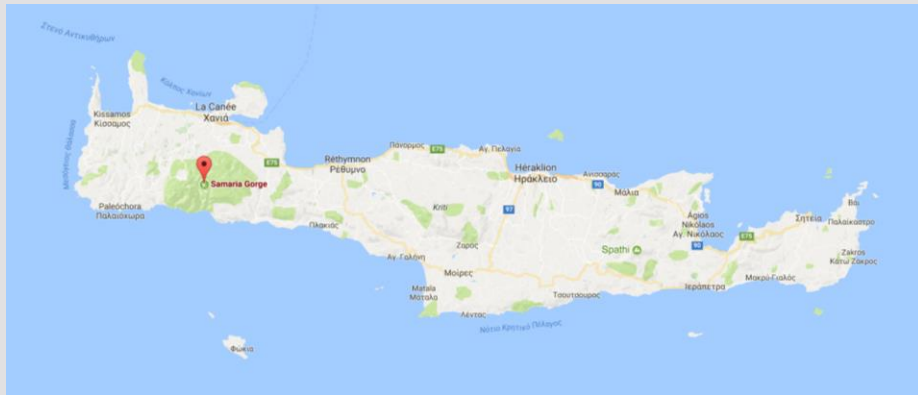
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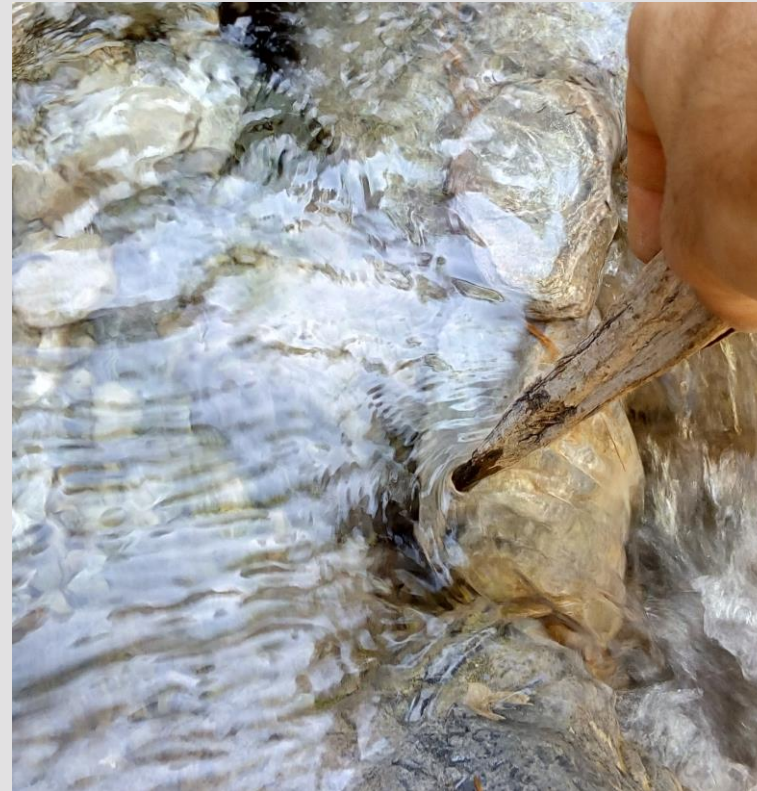
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Try to propagate  
against the flow  
(blue shift)



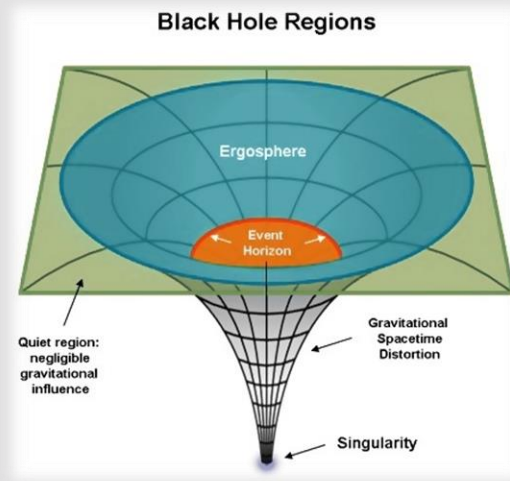
Analogue horizon

# Creating the analogue BH

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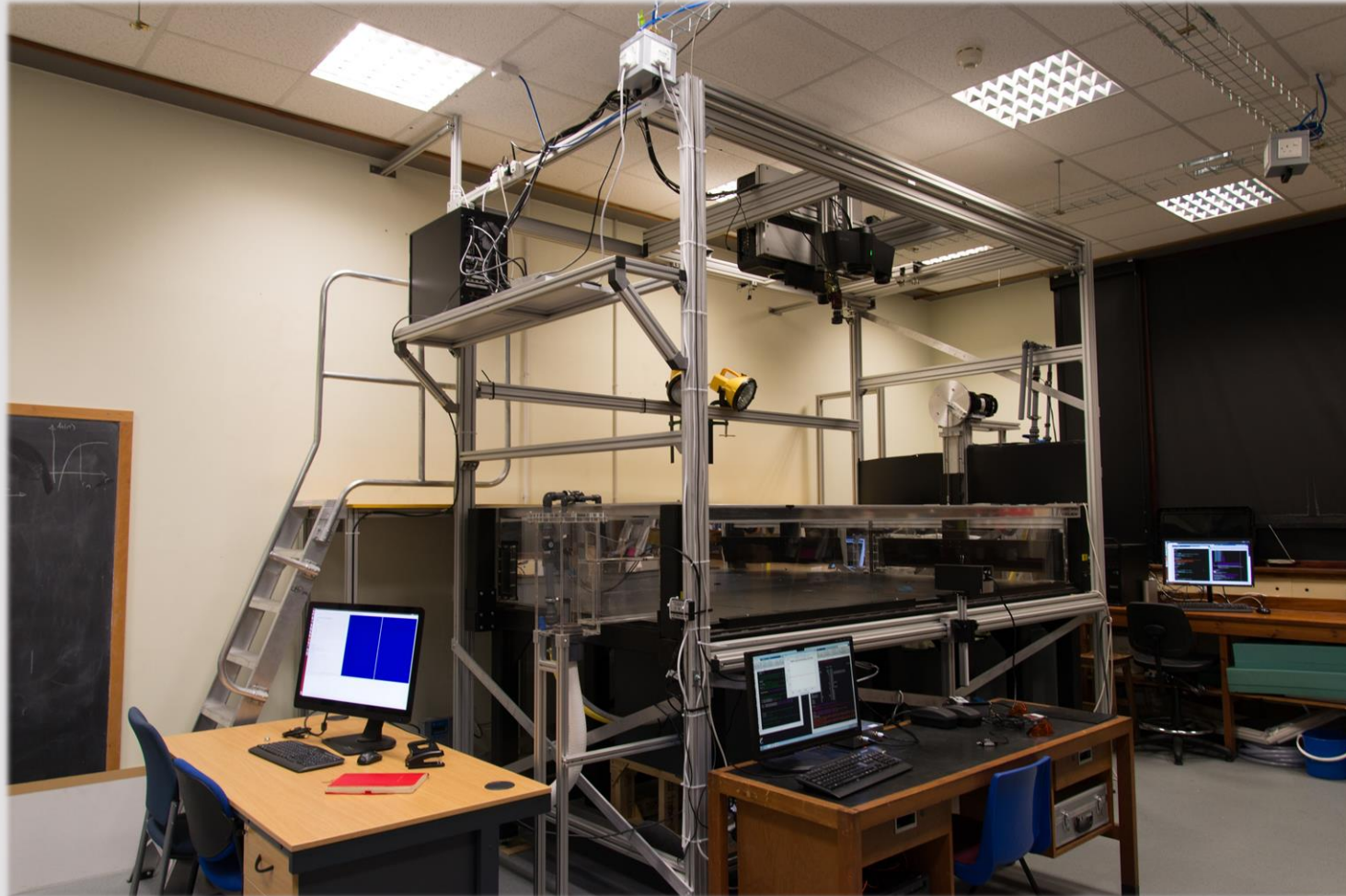
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# Creating the analogue BH

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# Creating the analogue BH

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Irrotational

Axisymmetric

Stationary

# Creating the analogue BH

---



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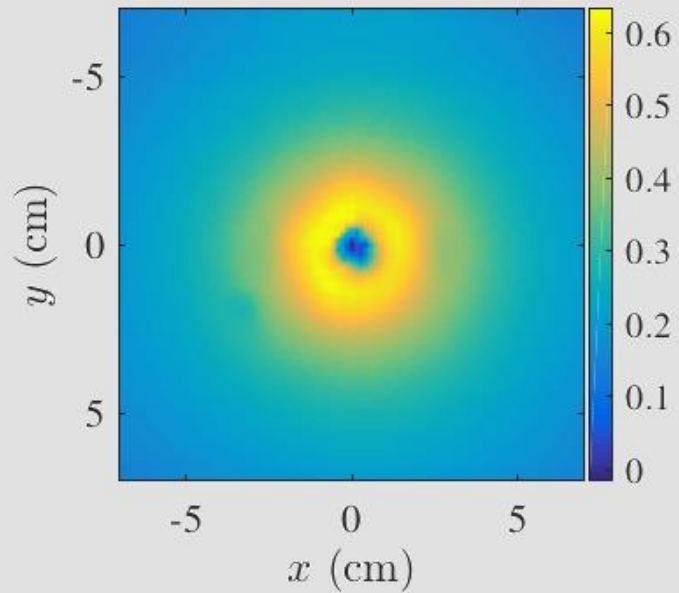
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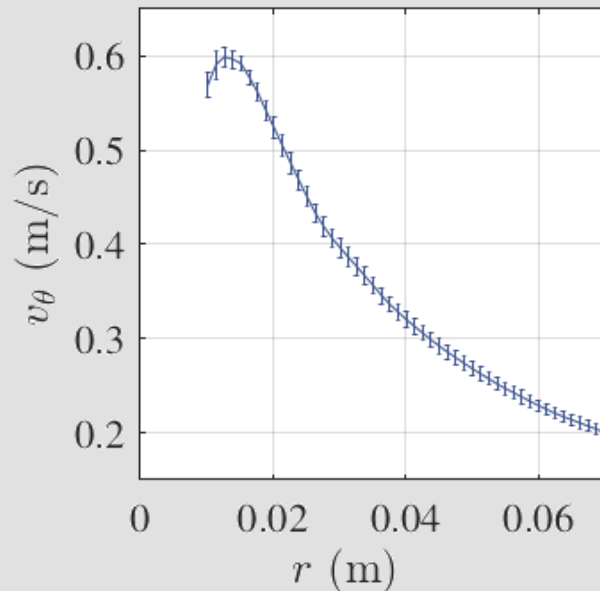
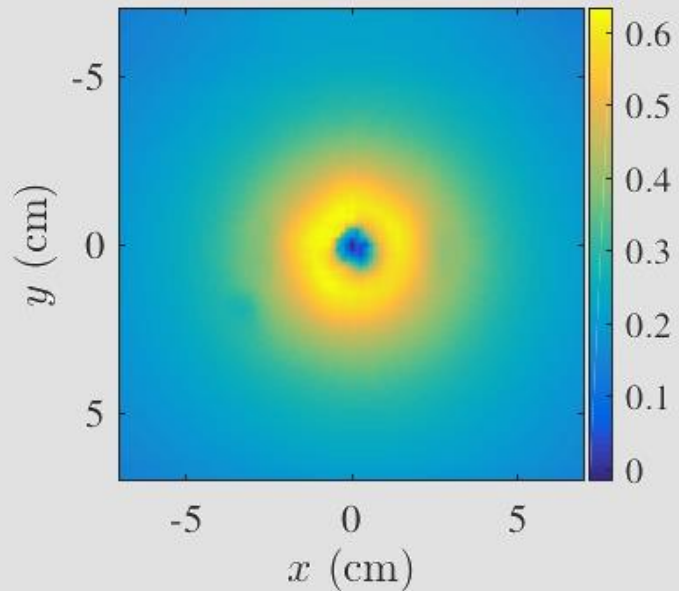
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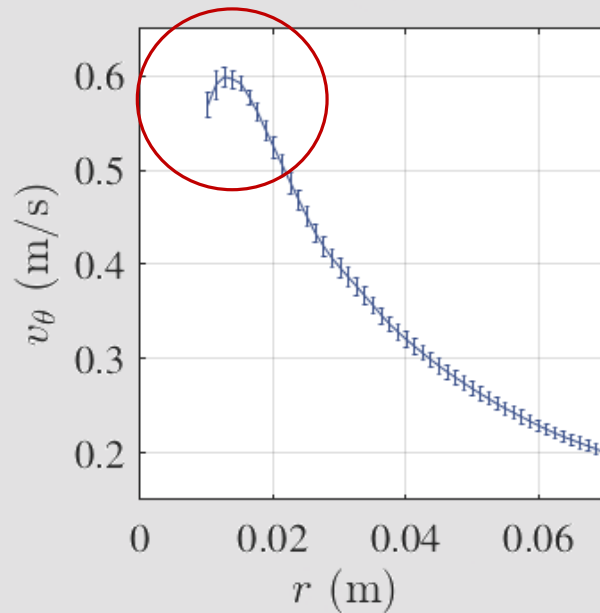
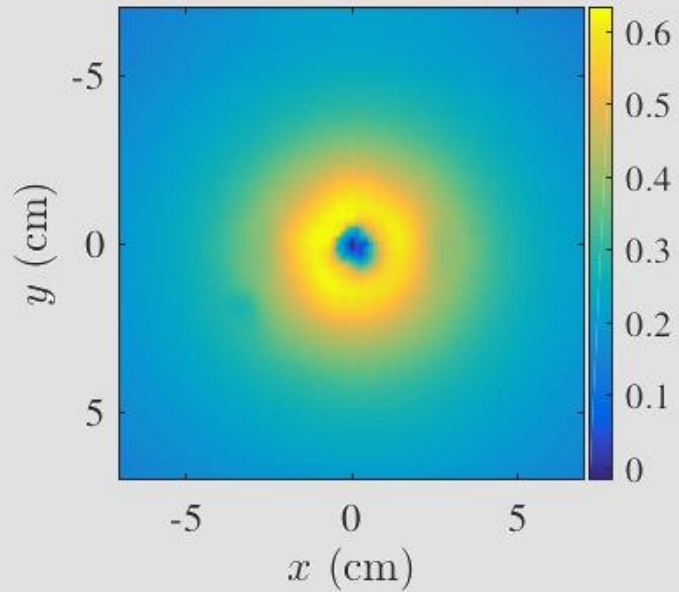
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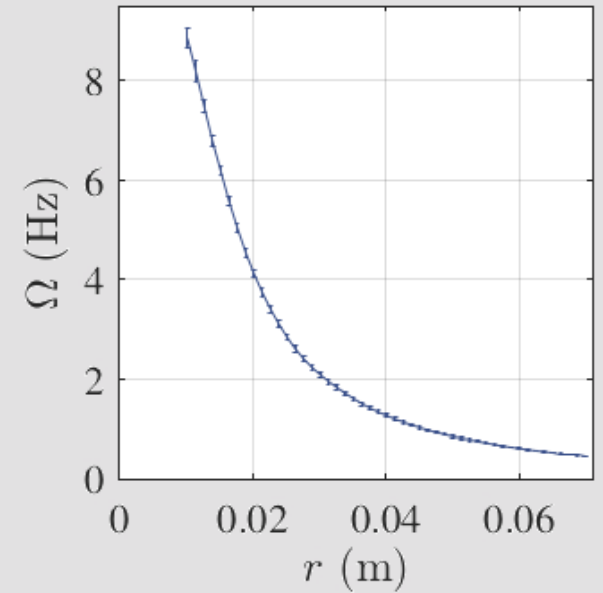
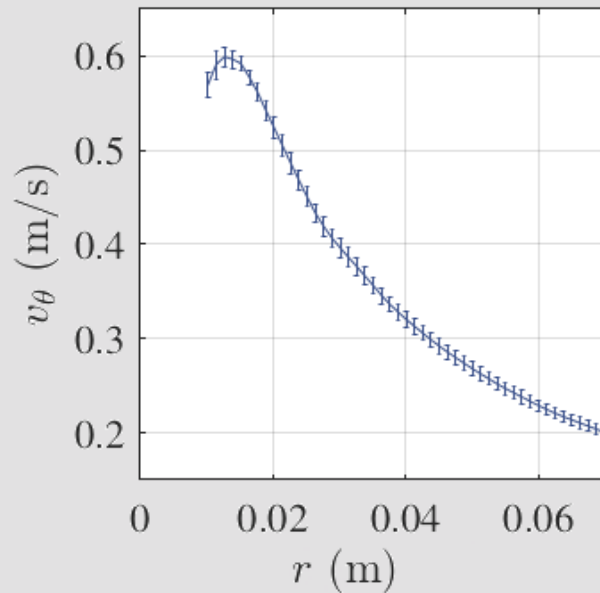
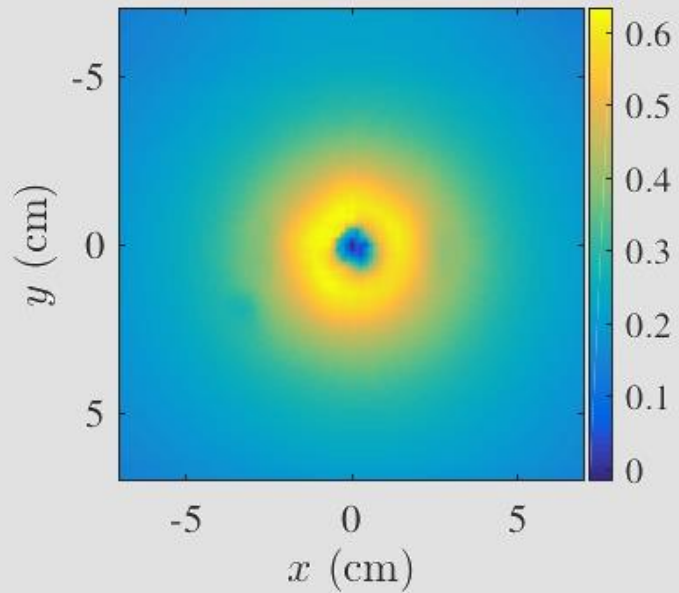
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Irrotational

Axisymmetric

Stationary



# Excitation of waves

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---

Condition of superradiance :  $\omega - m\Omega < 0$

Azimuthal number



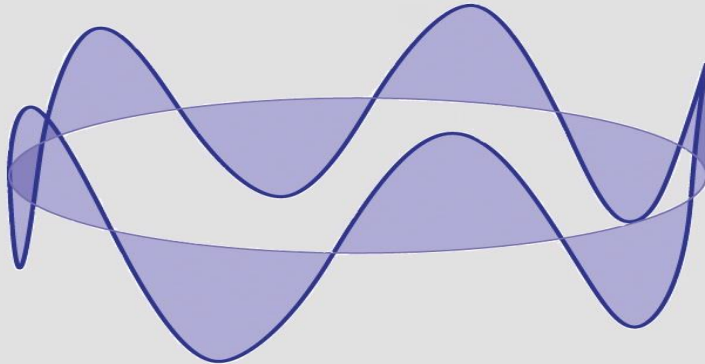


# Excitation of waves

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Condition of superradiance :  $\omega - m\Omega < 0$

We want to excite azimuthal waves

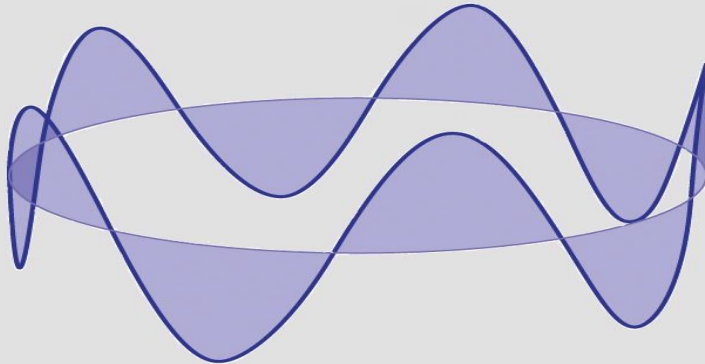


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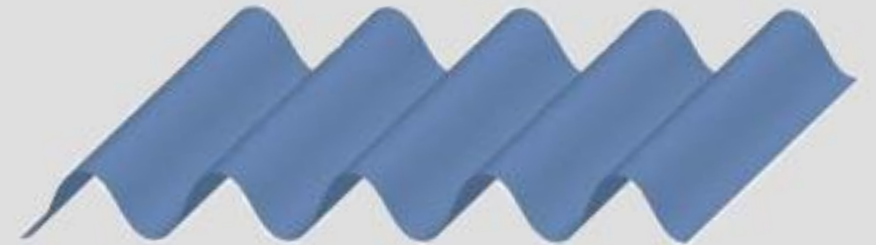
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Instead we excite plane waves

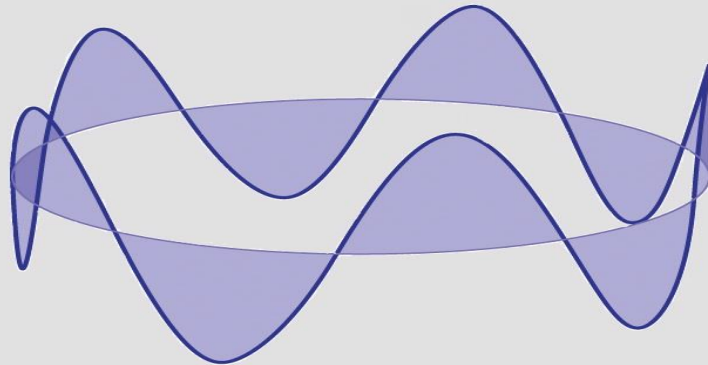


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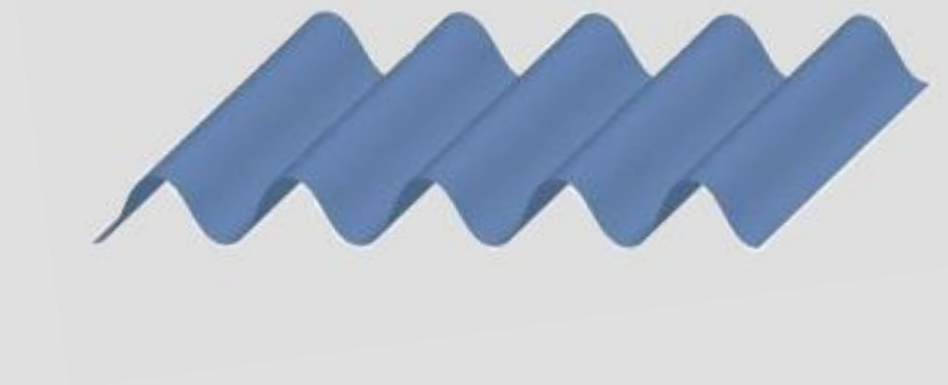
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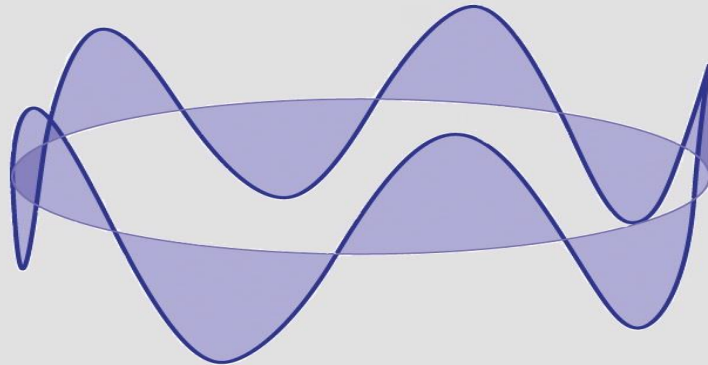
$$e^{i\vec{k}\cdot\vec{r}} = \sum_{m=-\infty}^{\infty} i^m J_m(kr) e^{im\theta}$$

# Excitation of waves

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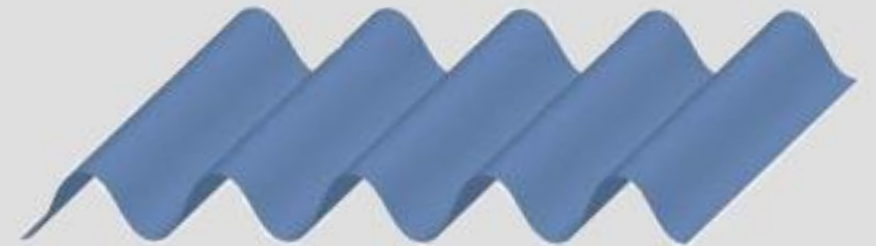
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Data analysis procedure :

- Excite plane waves
- Extract different azimuthal component
- Compare in/out part of the different m's

# Detection method

---

# Detection method

---

Shallow water regime:  $\lambda \gg h_B$

# Detection method

---

Shallow water regime:  $\lambda \gg h_B$

Small amplitude:  $A \ll h_B$

# Detection method

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# Detection method

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Shallow water regime :  $\lambda \gg h_B$

Small amplitude :  $A \ll h_B$



Pattern projector

# Detection method

---

Shallow water regime :  $\lambda \gg h_B$

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Pattern projector

Two cameras

# Detection method

---

Shallow water regime :  $\lambda \gg h_B$

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Pattern projector

Two cameras



Stereo-photogrammetry

# Detection method

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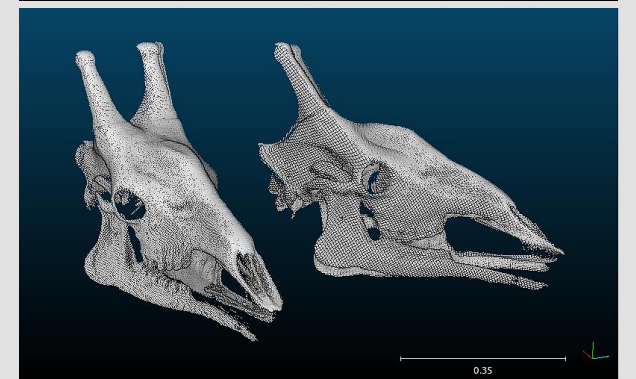


Pattern projector

Two cameras



Stereo-photogrammetry

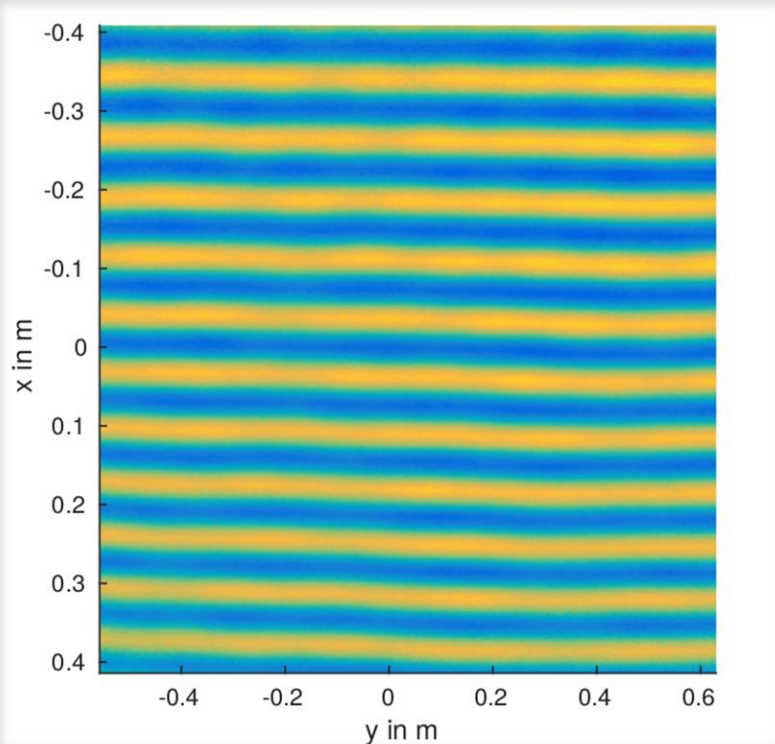


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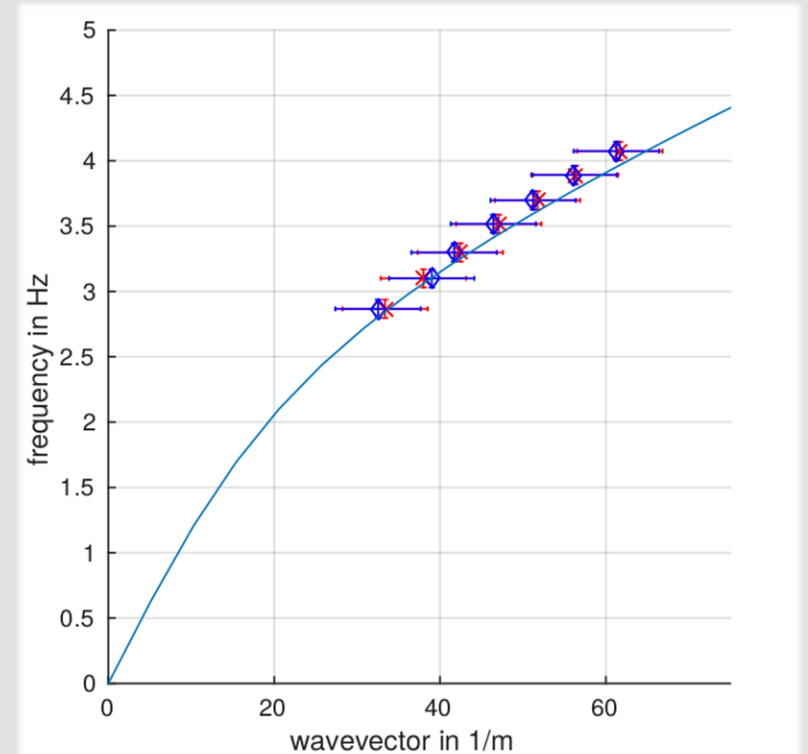
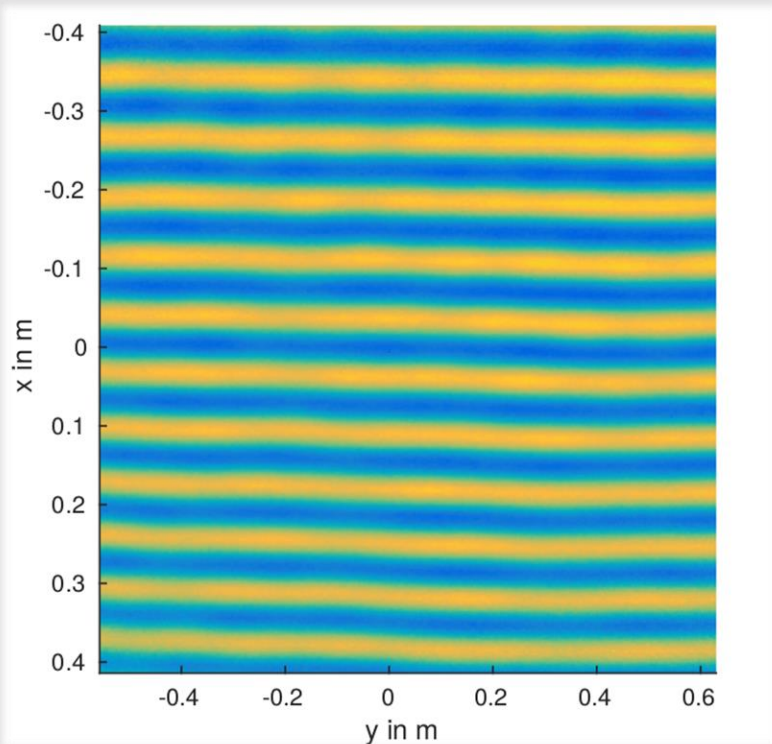
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# Detection method

Shallow water regime:  $\lambda \gg h_B$

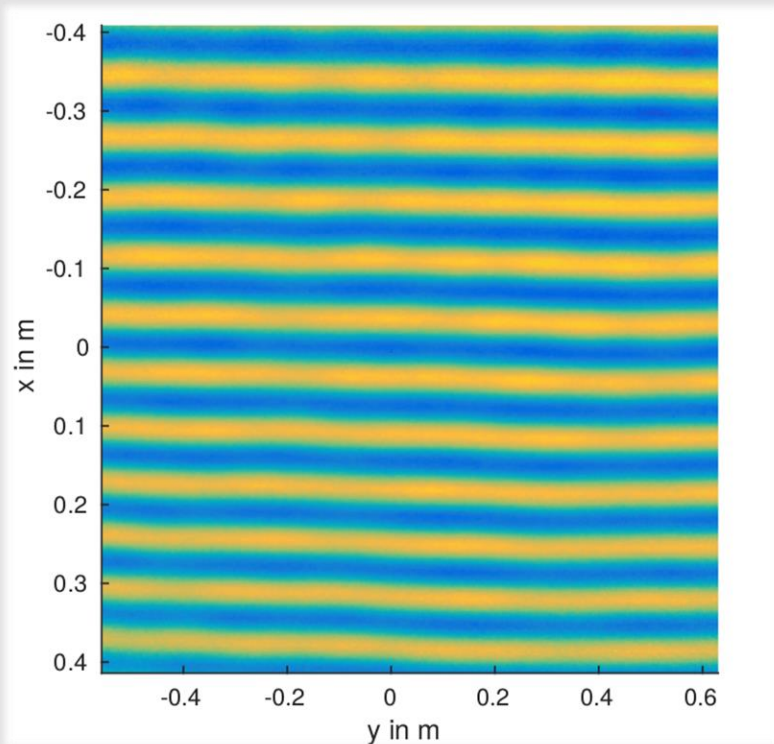
Small amplitude:  $A \ll h_B$



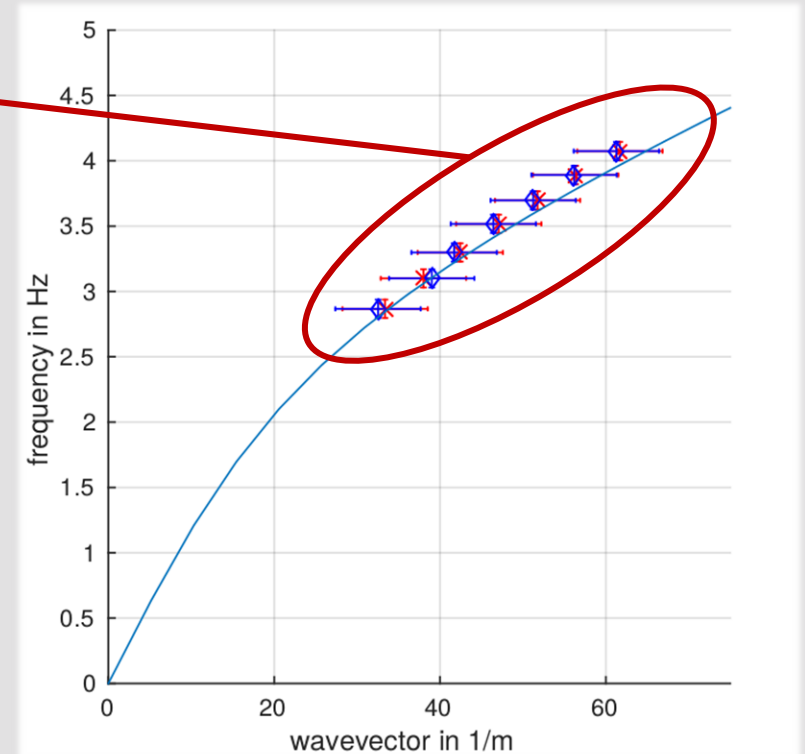
# Detection method

Shallow water regime:  $\lambda \gg h_B$

Small amplitude:  $A \ll h_B$



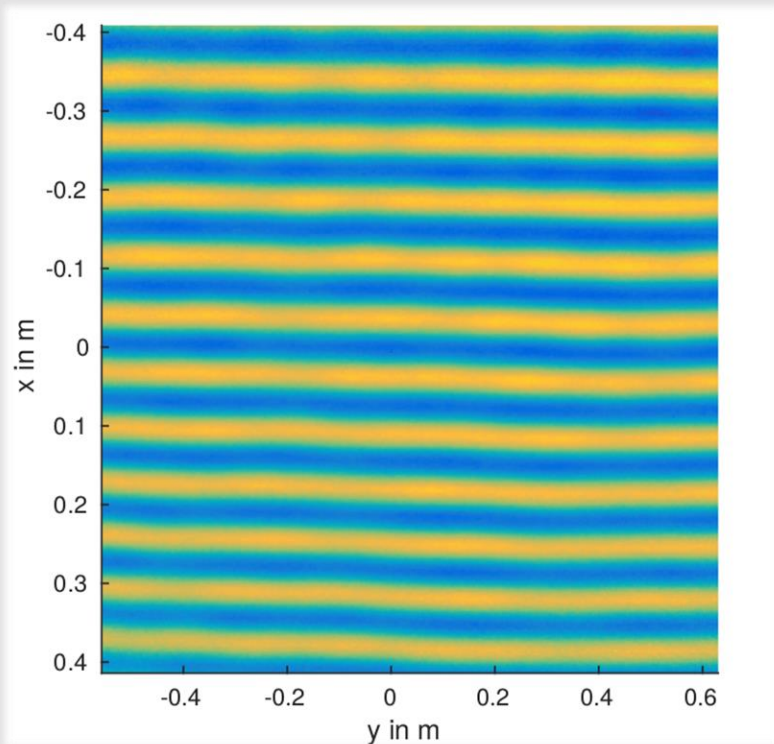
Dispersion –  $c(\lambda)$



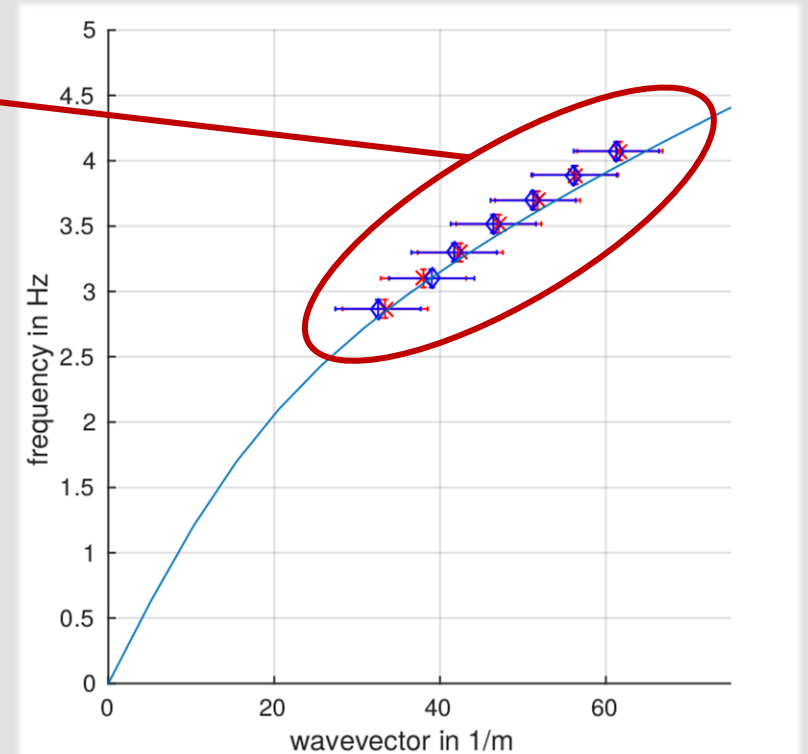
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# Experimental realisation

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## Analogue Black Hole :

- Irrotational
- Stationary
- Axisymmetric

## Waves :

- Shallow water
- Small Amplitude

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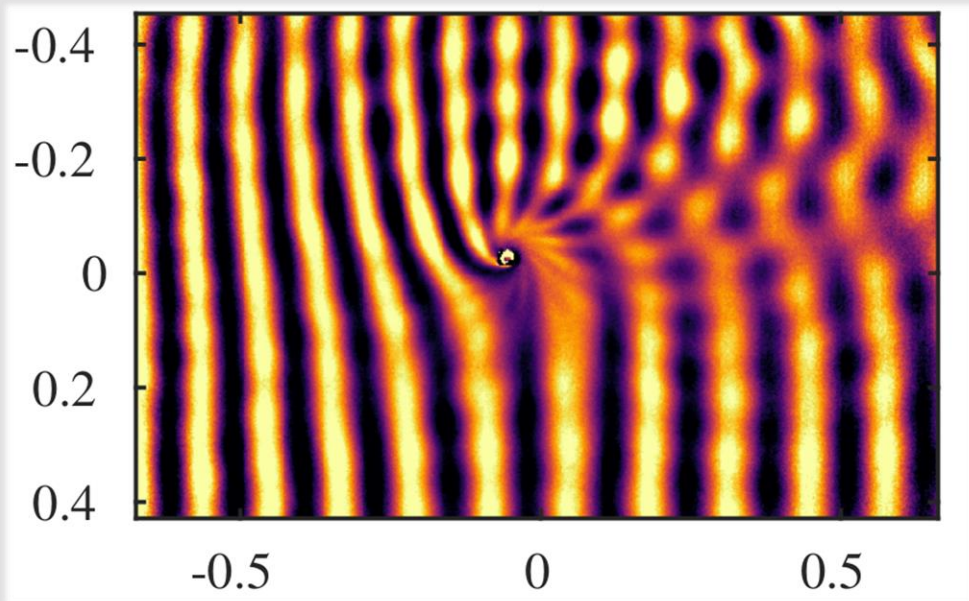
---

## Analogue Black Hole :

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## Waves :

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Free surface at 3.70 Hz

# Experimental realisation

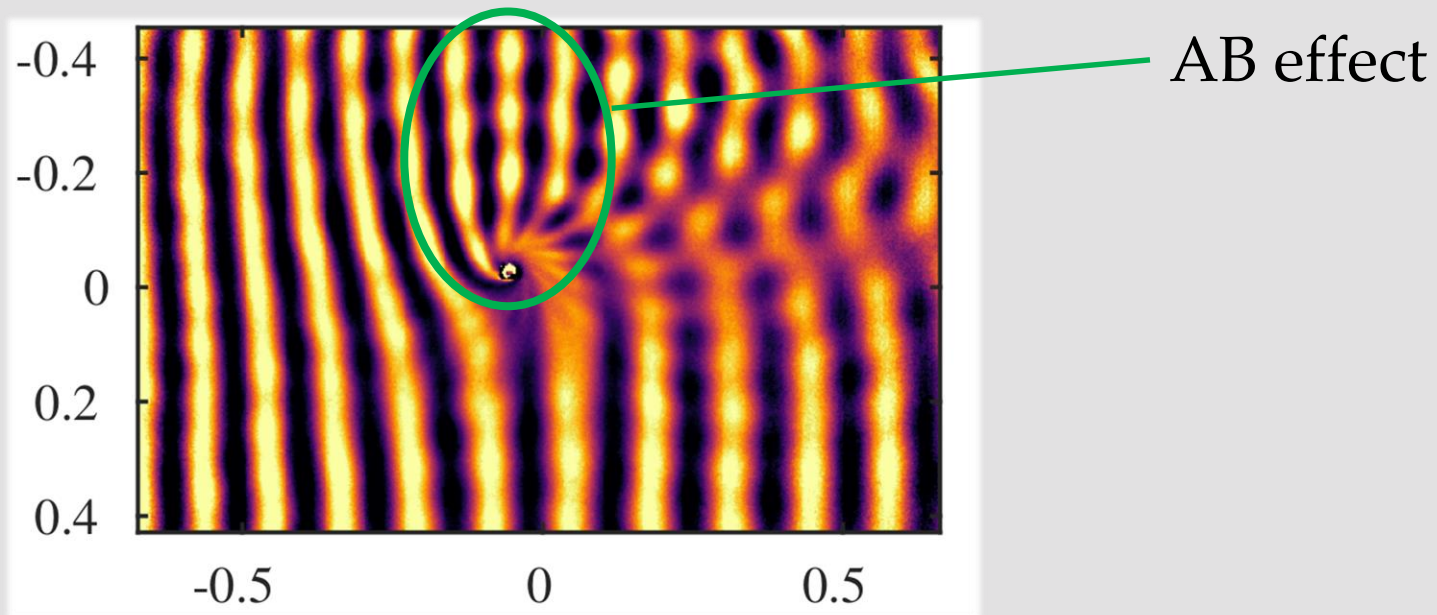
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# Experimental realisation

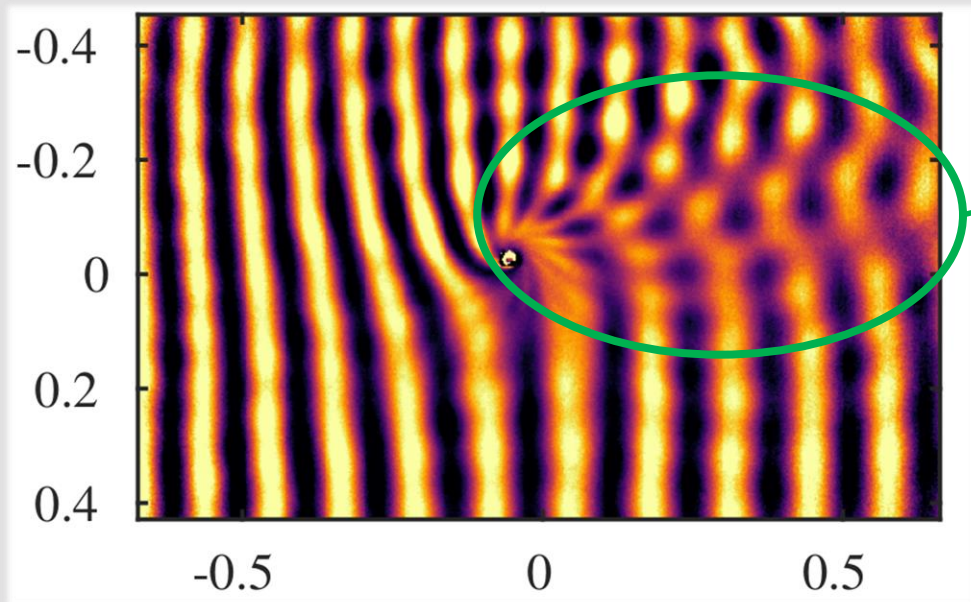
---

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AB effect

Scattering

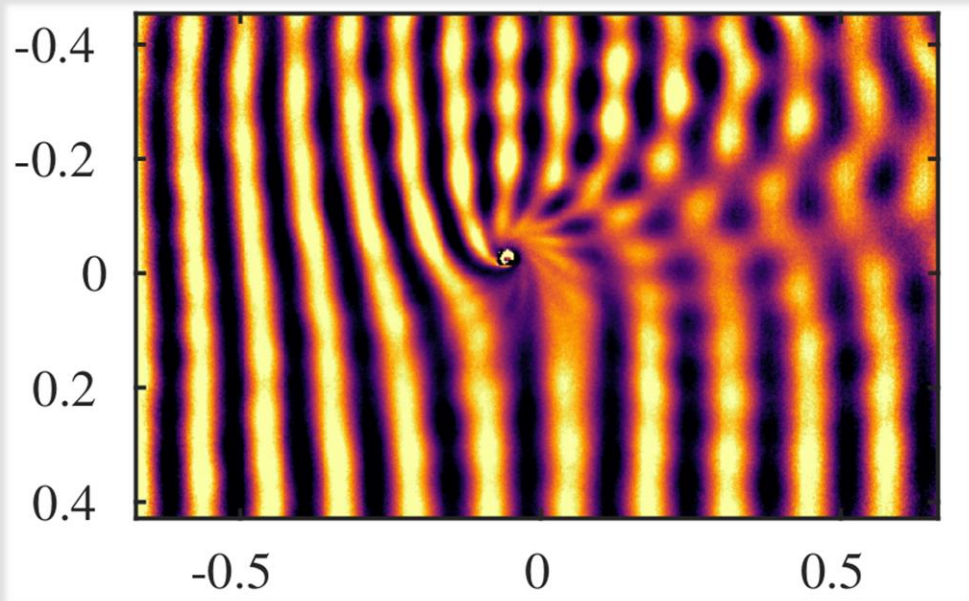
Free surface at 3.70 Hz

# Experimental realisation

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## Analogue Black Hole :

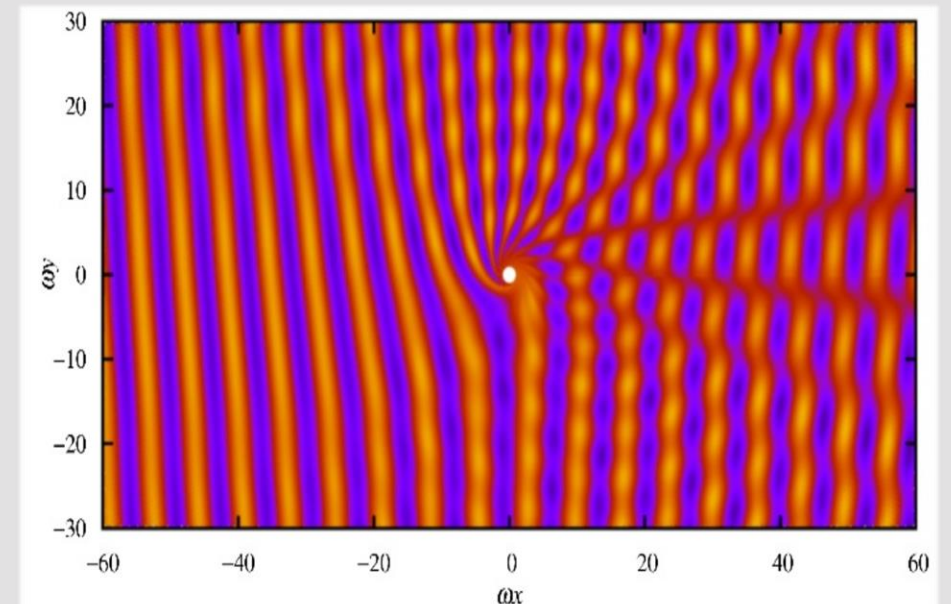
- Irrotational
- Stationary
- Axisymmetric



Free surface at 3.70 Hz

## Waves :

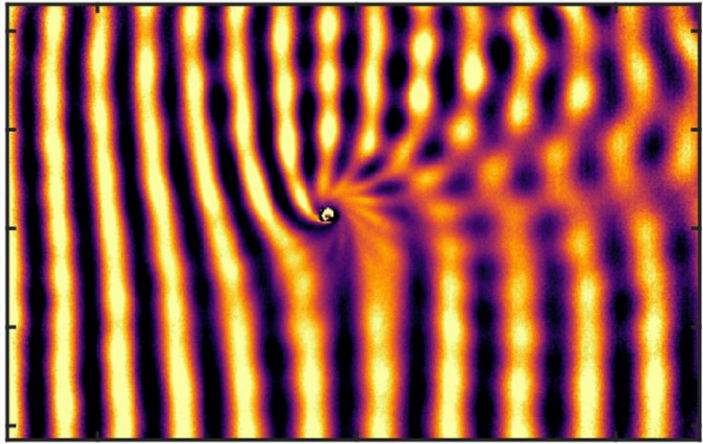
- Shallow water
- Small Amplitude



Numerical simulation by Dolan, S. & Oliveira, E.  
PRD87, 124038 (2013).

# Experimental realisation

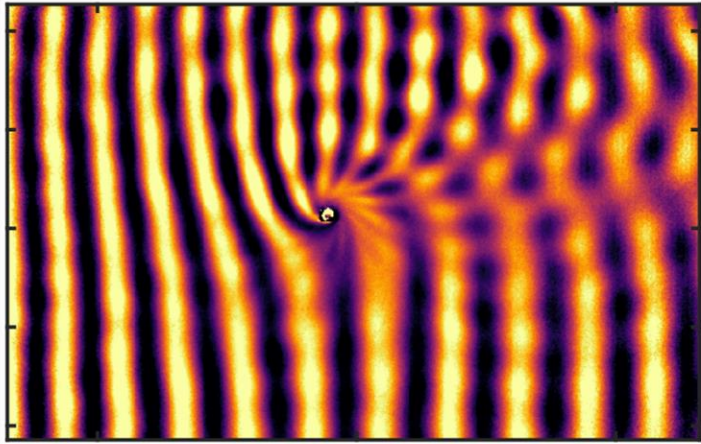
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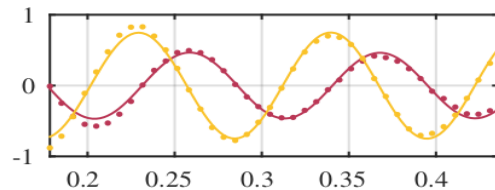


# Experimental realisation

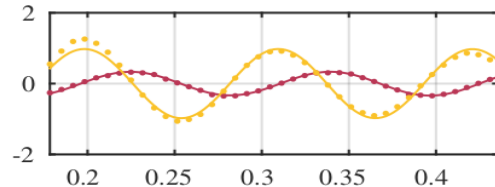
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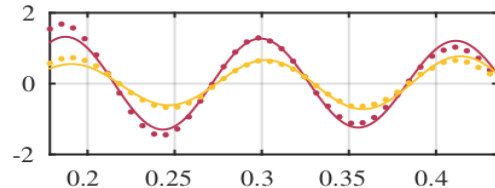
$m = -1$



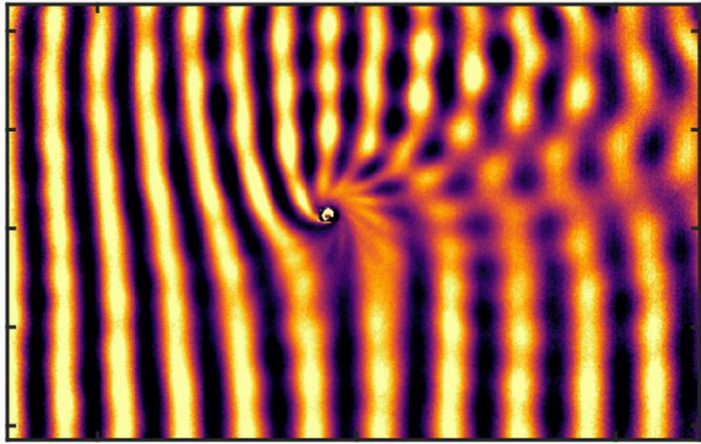
$m = 0$



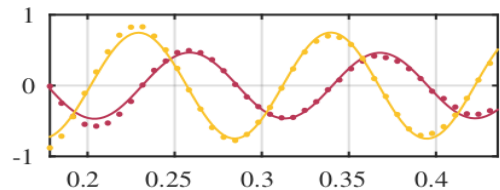
$m = 1$



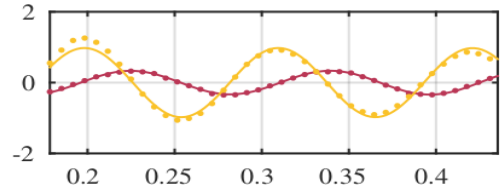
# Experimental realisation



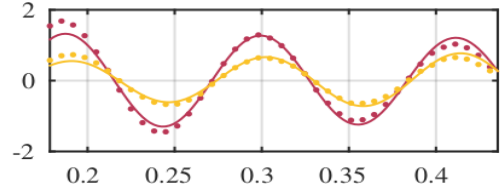
$m = -1$



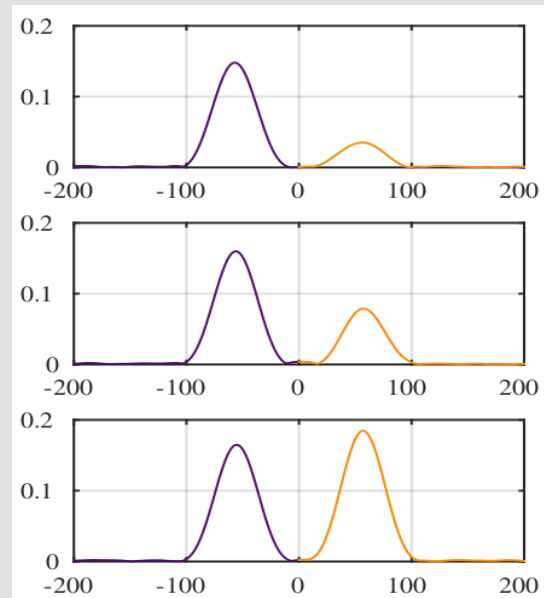
$m = 0$



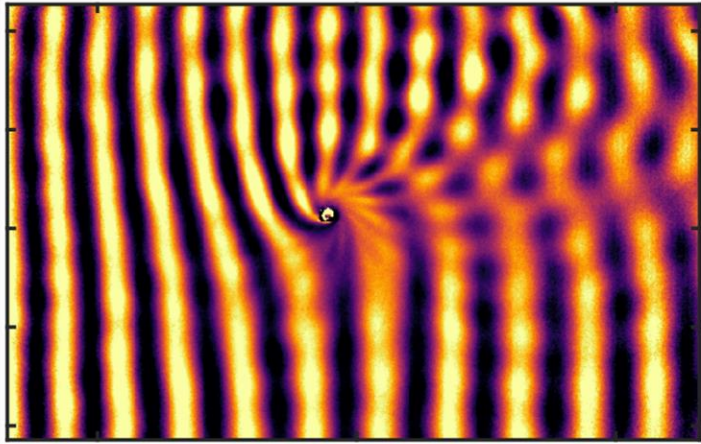
$m = 1$



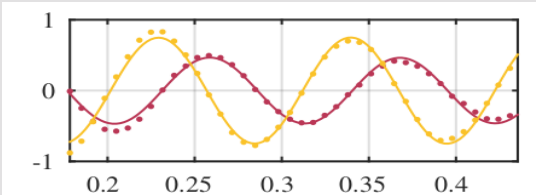
IN OUT



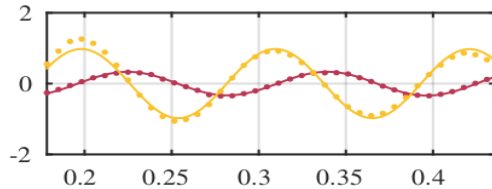
# Experimental realisation



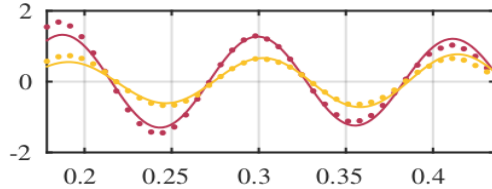
$m = -1$



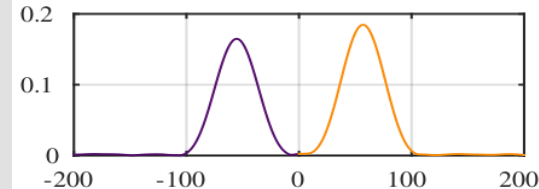
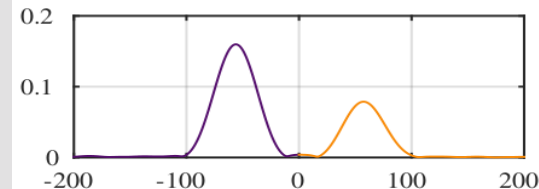
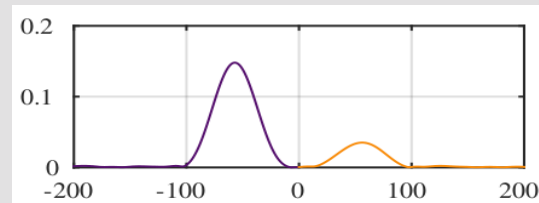
$m = 0$



$m = 1$

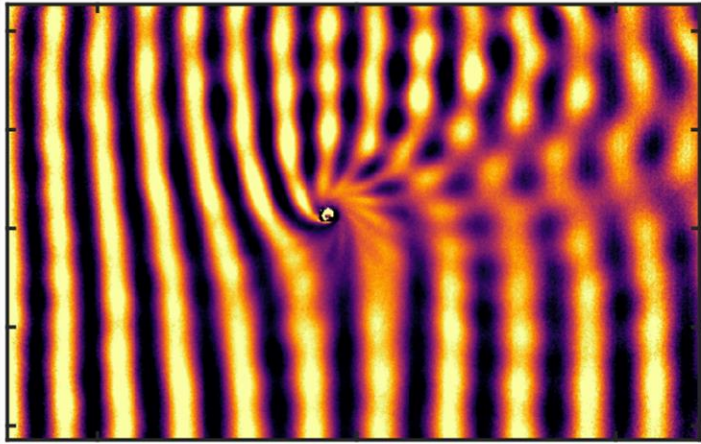


IN OUT

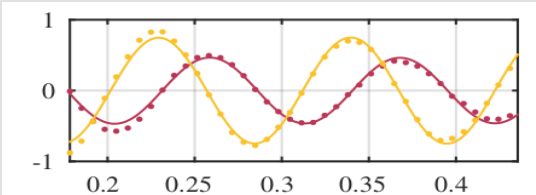


Absorption

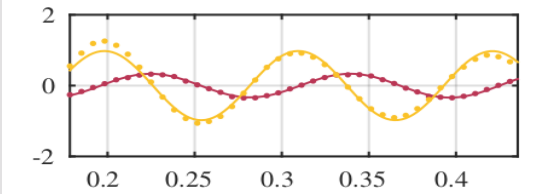
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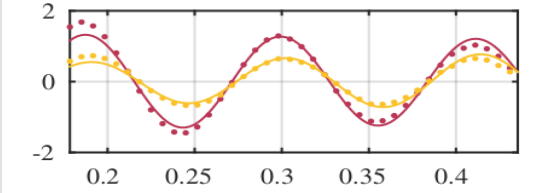
$m = -1$



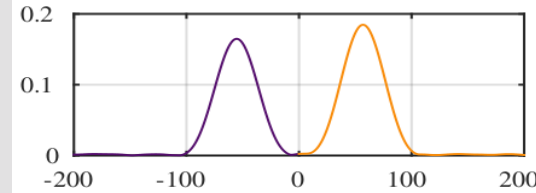
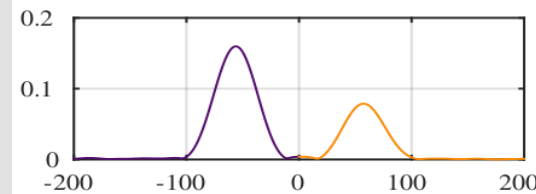
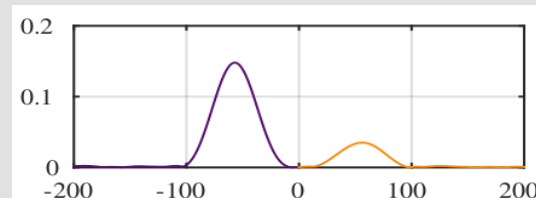
$m = 0$



$m = 1$



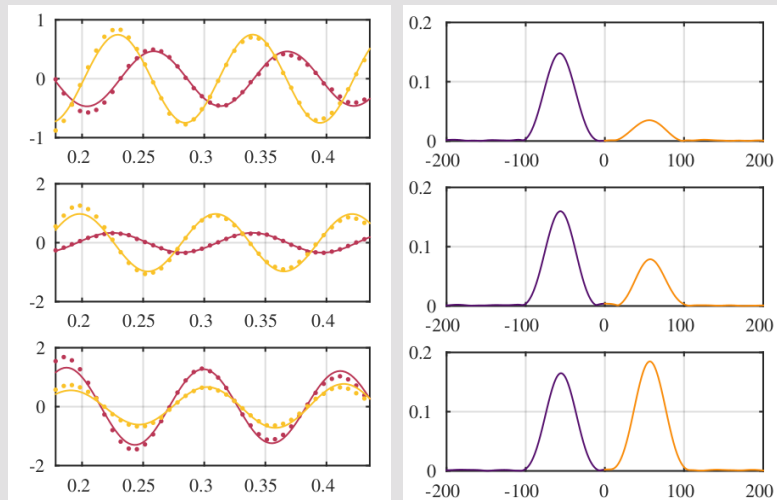
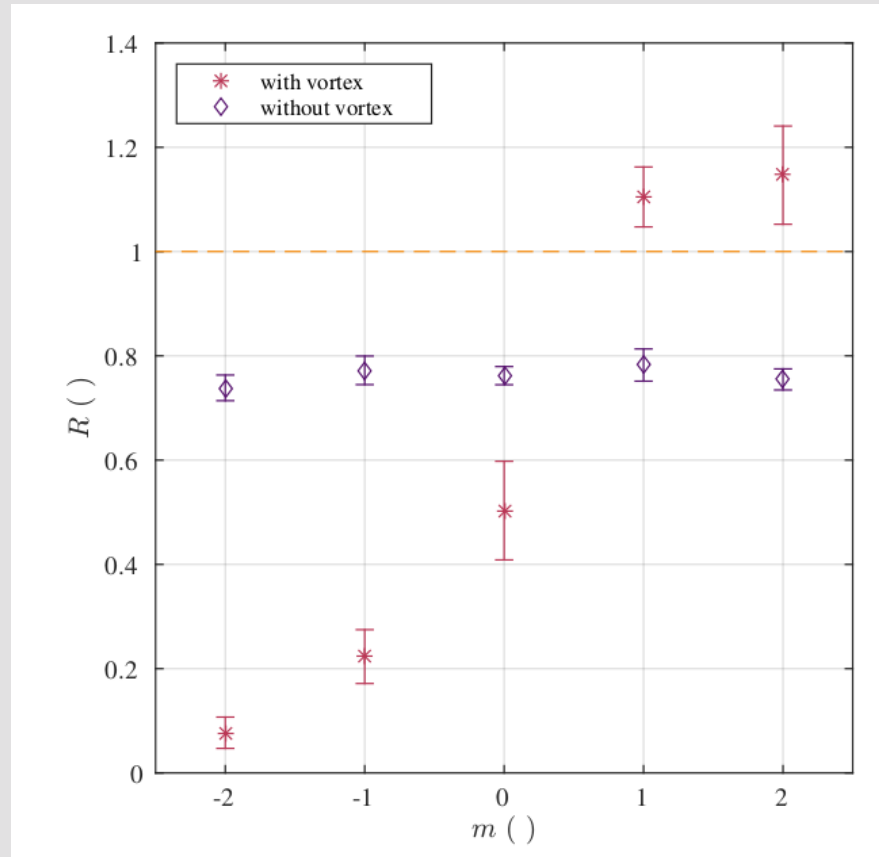
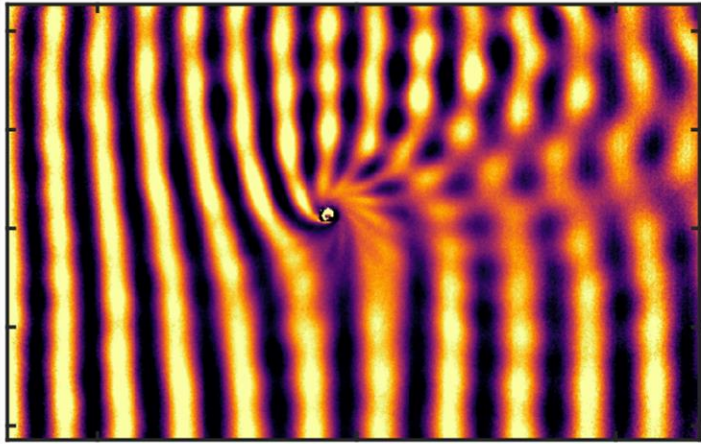
IN OUT



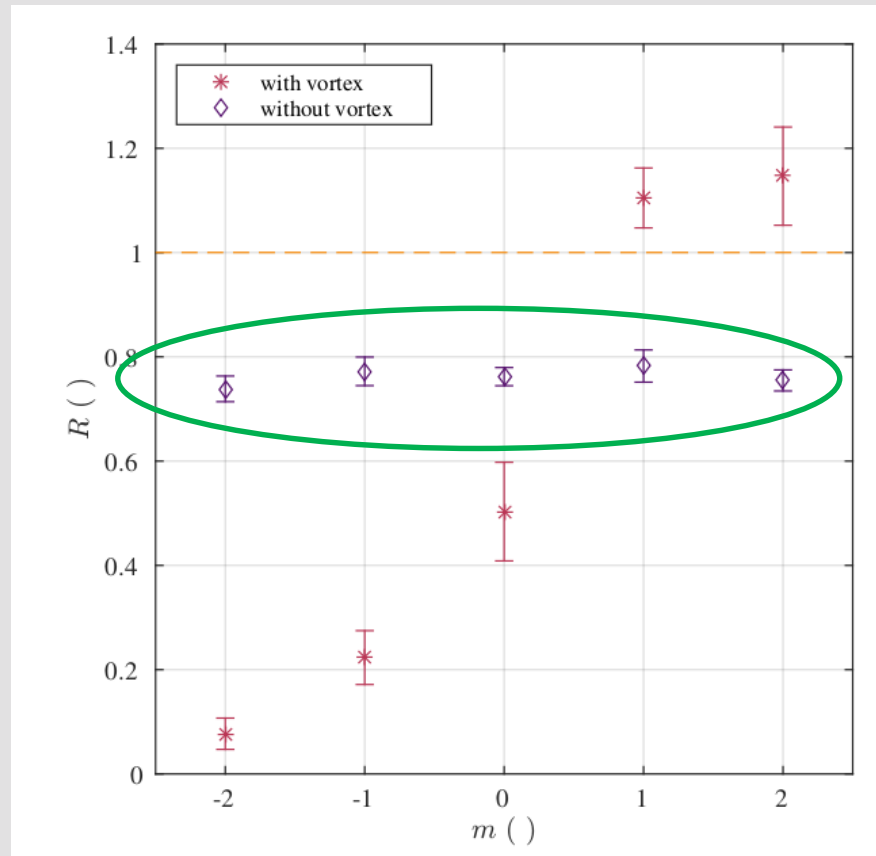
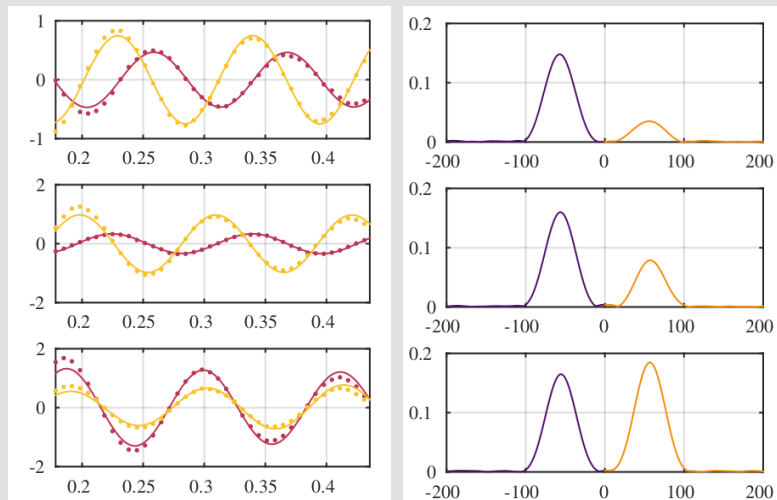
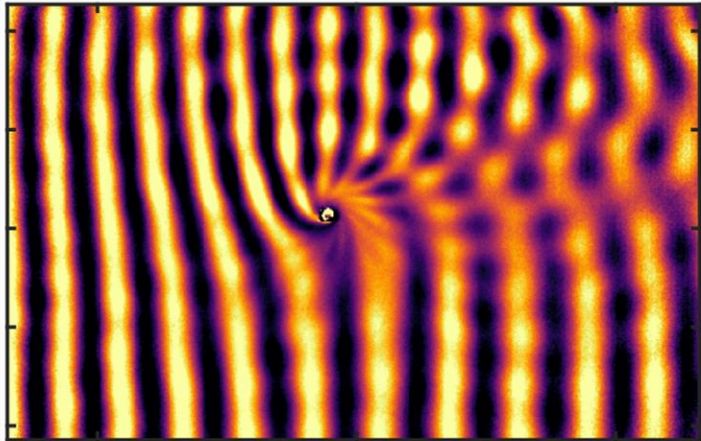
} Absorption

→ Amplification !

# Experimental realisation

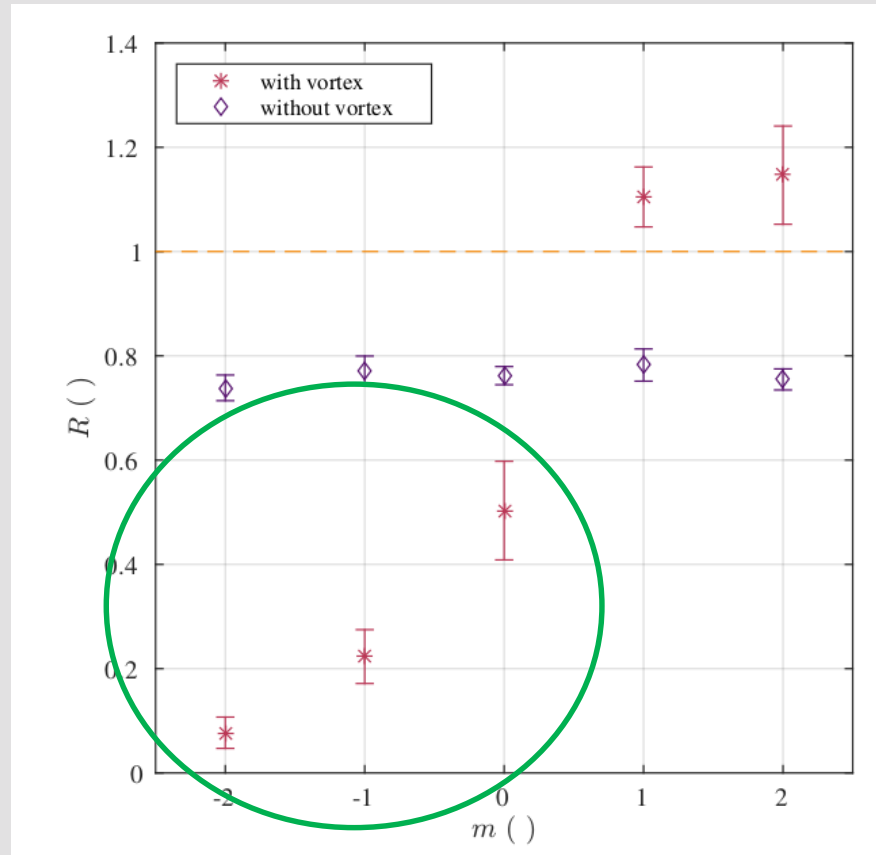
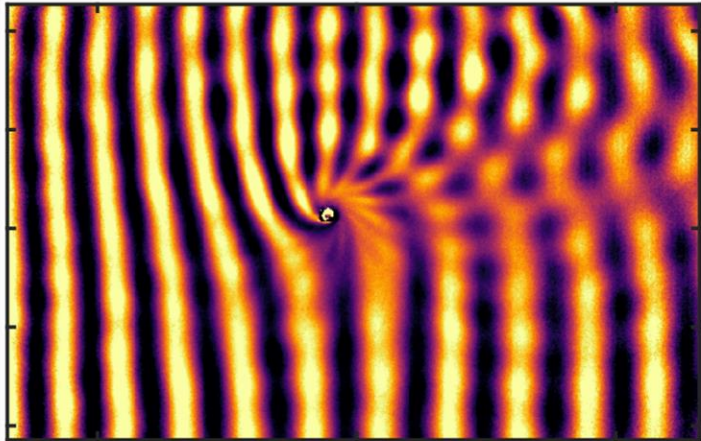


# Experimental realisation



Plane wave absorbed symmetrically

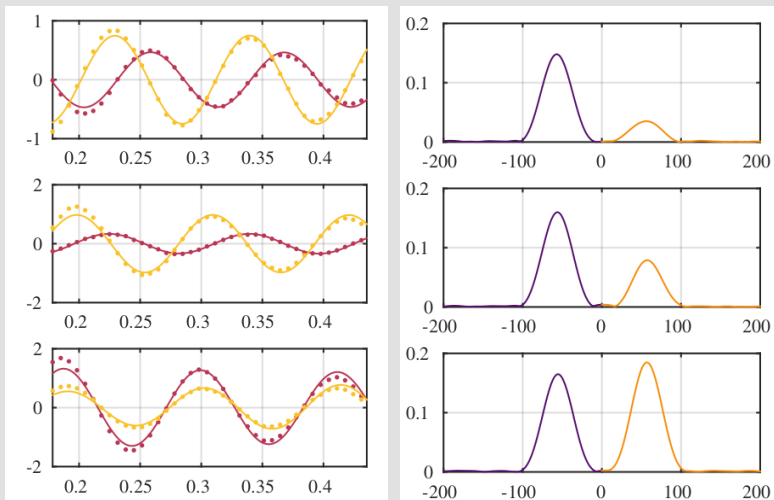
# Experimental realisation



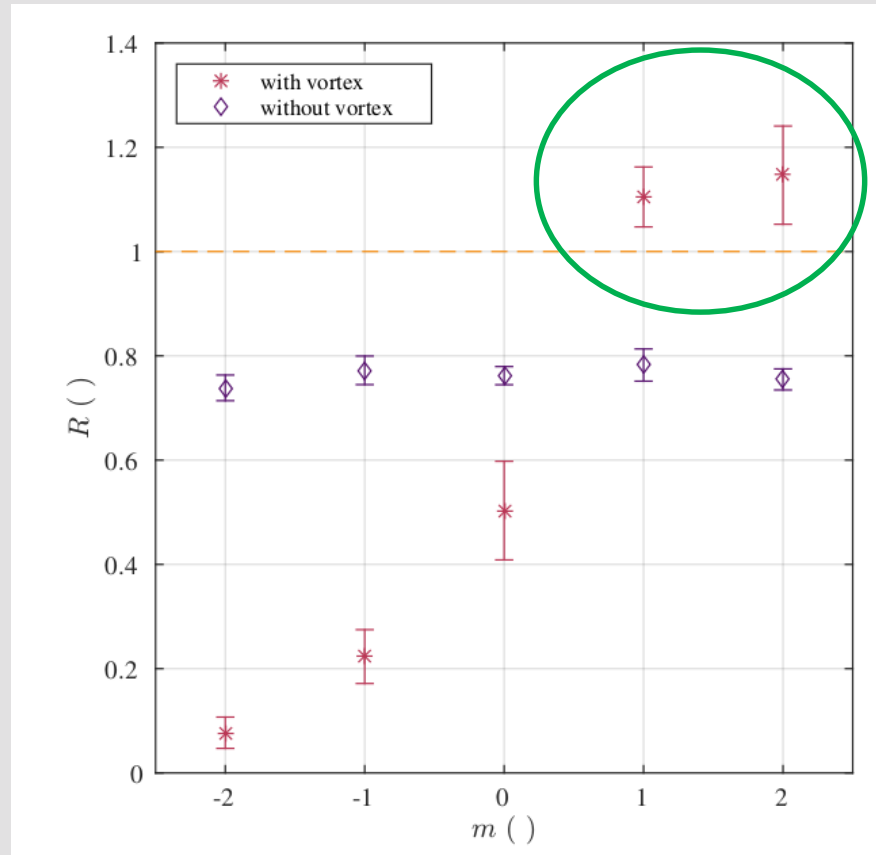
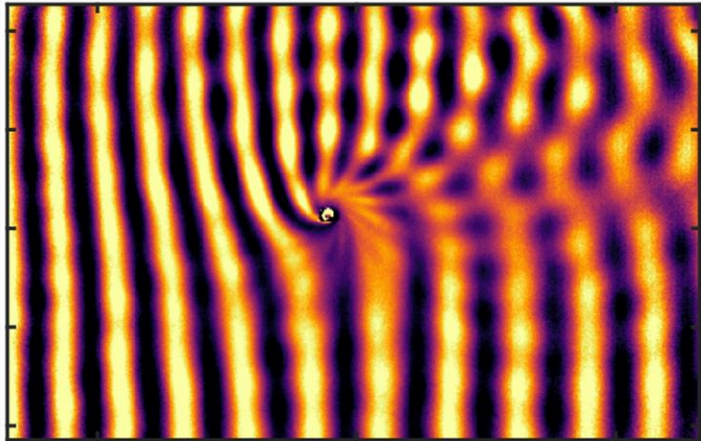
Plane wave absorbed  
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VORTEX

Negative  $m$ 's are  
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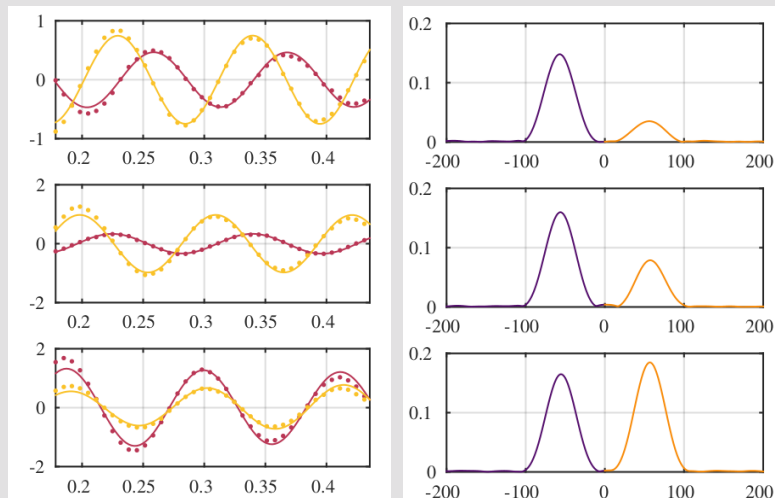


Plane wave absorbed symmetrically

VORTEX

Negative  $m$ 's are absorbed

Positive  $m$ 's are amplified ~ 10 - 15%

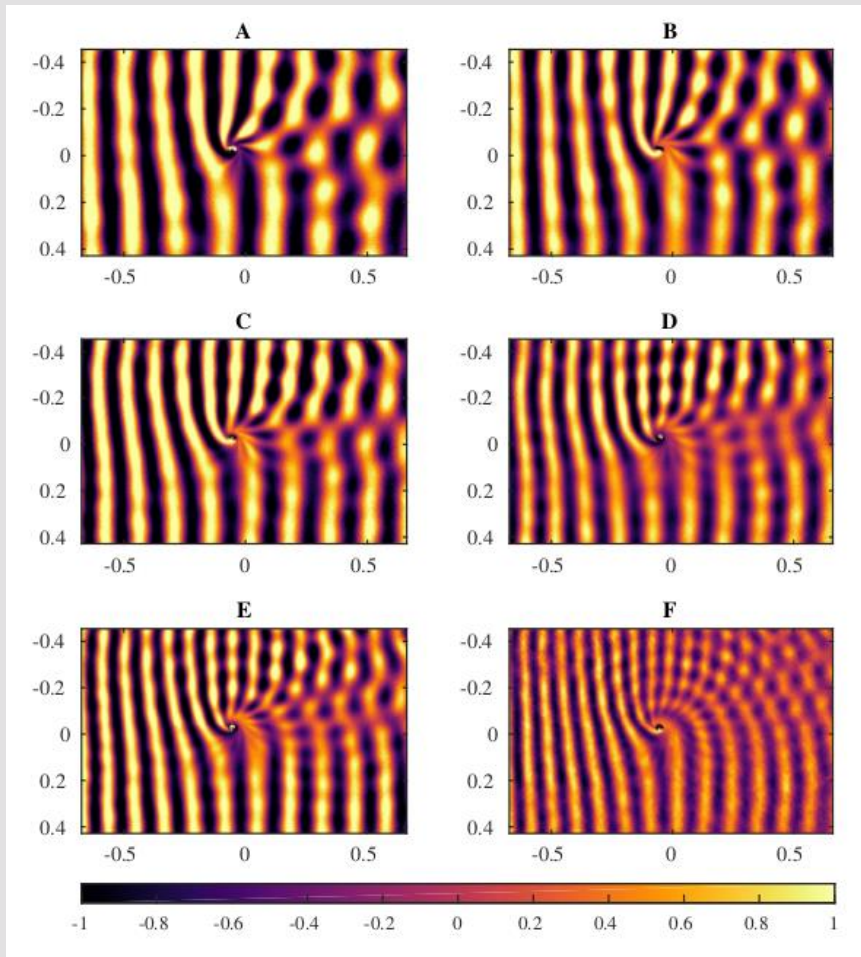




# Results

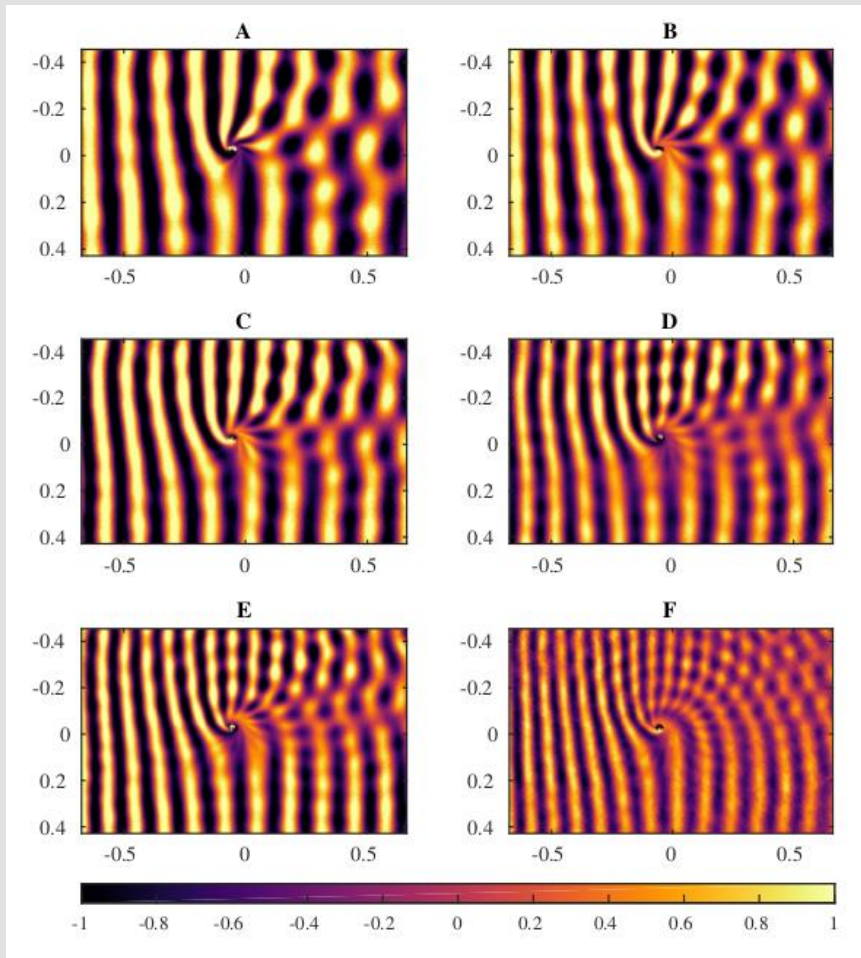
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# Results

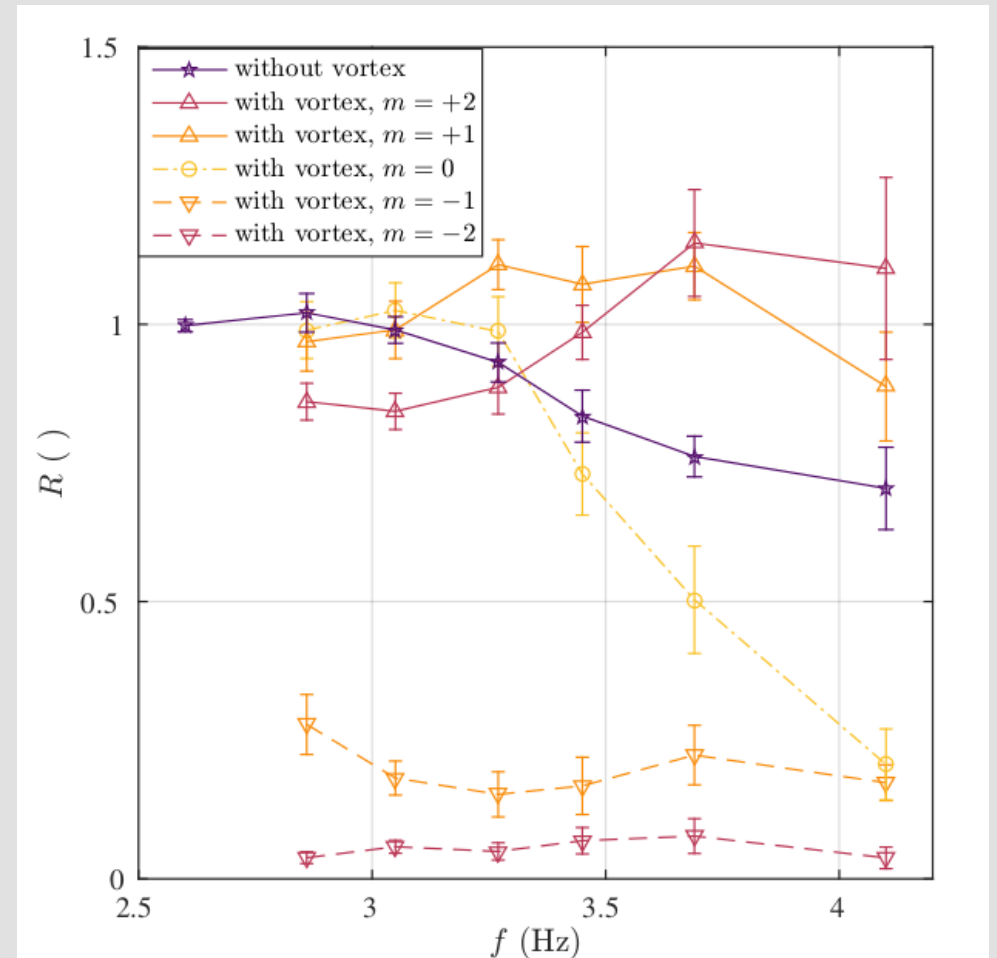


Free surface at various frequency  $\omega$   
( 2.87, 3.04, 3.27, 3.45, 3.70, 4.11 Hz)

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# Conclusion

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The superradiance conditions are fulfilled and we were able to make the first detection of this effect in this system !

↳ *Rotational superradiant scattering in a vortex flow*, Nature Physics  
(June 2017), doi : 10.1038/nphys4151

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Theoretical work :

Dispersion (T.T. in preparation)

Rotationnal flow (S. Patrick in preparation)

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New ideas on  
gravity... ?

Thank you !



