Scale hierarchies in particle physics and cosmology

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Problem of scales

- o describe high energy (SUSY?) extension of the Standard Model unification of all fundamental interactions
- incorporate Dark Energy

 $simplest case: infinitesimal (tuneable) +ve cosmological constant$

- **•** describe possible accelerated expanding phase of our universe models of inflation (approximate de Sitter)
	- \Rightarrow 3 very different scales besides M_{Planck} :

Problem of scales

- **1** they are independent
- ² possible connections
	- \bullet M_l could be near the EW scale, such as in Higgs inflation

but large non minimal coupling to explain

 \bullet *M*_{Planck} could be emergent from the EW scale in models of low-scale gravity and TeV strings What about M_l ? can it be at the TeV scale? Can we infer M_l from cosmological data?

I.A.-Patil '14 and '15

• connect inflation and SUSY breaking scales

Inflation in supergravity: main problems

• slow-roll conditions: the eta problem \Rightarrow fine-tuning of the potential

 $\eta = V''/V$, $V_F = e^{K}(|DW|^2 - 3|W|^2)$

 K : Kähler potential, W : superpotential canonically normalised field: $K = X\overline{X} \Rightarrow n = 1 + ...$

- **•** trans-Planckian initial conditions \Rightarrow break validity of EFT no-scale type models that avoid the η -problem
- stabilisation of the (pseudo) scalar companion of the inflaton chiral multiplets \Rightarrow complex scalars
- moduli stabilisation, de Sitter vacuum, . . .

Starobinsky model of inflation

$$
\mathcal{L} = \frac{1}{2}R + \alpha R^2
$$

Lagrange multiplier $\phi \Rightarrow \mathcal{L} = \frac{1}{2}(1+2\phi)R - \frac{1}{4\alpha}\phi^2$

Weyl rescaling \Rightarrow equivalent to a scalar field with exponential potential:

$$
\mathcal{L} = \frac{1}{2}R - \frac{1}{2}(\partial\phi)^2 - \frac{M^2}{12}\left(1 - e^{-\sqrt{\frac{2}{3}}\phi}\right)^2 \qquad M^2 = \frac{3}{4\alpha}
$$

Note that the two metrics are not the same

supersymmetric extension:

add D-term ${\cal R}\bar{\cal R}$ because F-term ${\cal R}^2$ does not contain ${\cal R}^2$

 \Rightarrow brings two chiral multiplets

SUSY extension of Starobinsky model

$$
K = -3\ln(T + \bar{T} - C\bar{C}) \quad ; \quad W = MC(T - \frac{1}{2})
$$

- T contains the inflaton: Re $T = e^{\sqrt{\frac{2}{3}}\phi}$
- \circ $C \sim \mathcal{R}$ is unstable during inflation

 \Rightarrow add higher order terms to stabilize it

e.g. $C\overline{C} \rightarrow h(C, \overline{C}) = C\overline{C} - \zeta(C\overline{C})^2$ Kallosh-Linde '13

• SUSY is broken during inflation with C the goldstino superfield

 \rightarrow model independent treatment in the decoupling sgoldstino limit

 \Rightarrow minimal SUSY extension that evades stability problem ϕ

Effective field theory of SUSY breaking at low energies

Analog of non-linear σ -model \Rightarrow constraint superfields

Rocek-Tseytlin '78, Lindstrom-Rocek '79, Komargodski-Seiberg '09

Goldstino: chiral superfield X_{NL} satisfying $X_{NL}^2=0\,\Rightarrow\,$

 Δ

$$
X_{NL}(y) = \frac{\chi^2}{2F} + \sqrt{2}\theta\chi + \theta^2 F \qquad y^{\mu} = x^{\mu} + i\theta\sigma^{\mu}\bar{\theta}
$$

$$
= F\Theta^2 \qquad \Theta = \theta + \frac{\chi}{\sqrt{2}F}
$$

$$
\mathcal{L}_{NL} = \int d^4\theta X_{NL} \bar{X}_{NL} - \frac{1}{\sqrt{2}\kappa} \left\{ \int d^2\theta X_{NL} + h.c. \right\} = \mathcal{L}_{Volkov-Akulov}
$$
R-symmetry with $[\theta]_R = [\chi]_R = 1$ and $[X]_R = 2$ $F = \frac{1}{\sqrt{2}\kappa} + ...$

Non-linear SUSY in supergravity

I.A.-Dudas-Ferrara-Sagnotti '14

$$
K = -3\log(1 - X\bar{X}) \equiv 3X\bar{X} \quad ; \quad W = f X + W_0 \qquad X \equiv X_{NL}
$$

$$
\Rightarrow V = \frac{1}{3}|f|^2 - 3|W_0|^2 \quad ; \quad m_{3/2}^2 = |W_0|^2
$$

- V can have any sign contrary to global NL SUSY
- NL SUSY in flat space \Rightarrow $f = 3 m_{3/2} M_p$
- R-symmetry is broken by W_0
- Dual gravitational formulation: $({\cal R}_\kappa^-\,6$ W $_0)^2=0$ I.A.-Markou '15 \mathbb{R}^2 chiral curvature superfield
- Minimal SUSY extension of R^2 gravity

Non-linear Starobinsky supergravity

$$
K = -3\ln(T + \bar{T} - X\bar{X}) \quad ; \quad W = MXT + fX + W_0 \quad \Rightarrow
$$
\n
$$
\mathcal{L} = \frac{1}{2}R - \frac{1}{2}(\partial\phi)^2 - \frac{M^2}{12}\left(1 - e^{-\sqrt{\frac{2}{3}}\phi}\right)^2 - \frac{1}{2}e^{-2\sqrt{\frac{2}{3}}\phi}(\partial a)^2 - \frac{M^2}{18}e^{-2\sqrt{\frac{2}{3}}\phi}a^2
$$

• axion a much heavier than ϕ during inflation, decouples:

$$
m_{\phi}=\frac{M}{3}e^{-\sqrt{\frac{2}{3}}\phi_0}<
$$

 \bullet inflation scale M independent from NL-SUSY breaking scale f

 \Rightarrow compatible with low energy SUSY

- **•** however inflaton different from goldstino superpartner
- also initial conditions require trans-planckian values for ϕ ($\phi > 1$) [\[15\]](#page-14-0)

Inflation from supersymmetry breaking I.A.-Chatrabhuti-Isono-Knoops '16, '17

Inflaton : goldstino superpartner in the presence of a gauged R-symmetry

I linear superpotential $W = f X \Rightarrow$ no η -problem

$$
V_F = e^{K} (|DW|^2 - 3|W|^2)
$$

= $e^{K} (|1 + K_XX|^2 - 3|X|^2) |f|^2$ $K = X\overline{X}$
= $e^{|X|^2} (1 - |X|^2 + \mathcal{O}(|X|^4) |f|^2 = \mathcal{O}(|X|^4) \Rightarrow \eta = 0 + ...$

- inflation around a maximum of scalar potential (hill-top) \Rightarrow small field no large field initial conditions
- gauge R-symmetry: (pseudo) scalar absorbed by the $U(1)_R$
- vacuum energy at the minimum: tuning between V_F and V_D

Two classes of models

Case 1: R-symmetry is restored during inflation (at the maximum)

• Case 2: R-symmetry is (spontaneously) broken everywhere (and restored at infinity)

example: toy model of SUSY breaking [\[15\]](#page-14-0) [\[24\]](#page-23-0)

Case 1: R-symmetry restored during inflation

$$
\mathcal{K}(X,\bar{X}) = \kappa^{-2} X \bar{X} + \kappa^{-2} A (X \bar{X})^2 \qquad A > 0
$$

\n
$$
W(X) = \kappa^{-3} K \qquad \Rightarrow
$$

\n
$$
f(X) = 1 \qquad (+\beta \ln X \text{ to cancel anomalies but } \beta \text{ very small})
$$

\n
$$
\mathcal{V} = \mathcal{V}_F + \mathcal{V}_D
$$

\n
$$
\mathcal{V}_F = \kappa^{-4} f^2 e^{X \bar{X} (1 + AX \bar{X})} \left[-3X \bar{X} + \frac{(1 + X \bar{X} (1 + 2AX \bar{X}))^2}{1 + 4AX \bar{X}} \right]
$$

\n
$$
\mathcal{V}_D = \kappa^{-4} \frac{q^2}{2} \left[1 + X \bar{X} (1 + 2AX \bar{X}) \right]^2
$$

Assume inflation happens around the maximum $|X| \equiv \rho \simeq 0 \Rightarrow$

Case 1: predictions

slow-roll parameters

$$
\eta = \frac{1}{\kappa^2} \left(\frac{V''}{V} \right) = 2 \left(\frac{-4A + x^2}{2 + x^2} \right) + \mathcal{O}(\rho^2) \qquad q = f \times
$$

$$
\epsilon = \frac{1}{2\kappa^2} \left(\frac{V'}{V} \right)^2 = 4 \left(\frac{-4A + x^2}{2 + x^2} \right)^2 \rho^2 + \mathcal{O}(\rho^4) \simeq \eta^2 \rho^2
$$

 η small: for instance $x \ll 1$ and $A \sim \mathcal{O}(10^{-1})$

inflation starts with an initial condition for $\phi = \phi_*$ near the maximum and ends when $|\eta| = 1$

$$
\Rightarrow \text{ number of e-folds } N = \int_{\text{end}}^{\text{start}} \frac{V}{V'} = \kappa \int \frac{1}{\sqrt{2\epsilon}} \simeq \frac{1}{|\eta_*|} \ln \left(\frac{\rho_{\text{end}}}{\rho_*} \right)
$$

Case 1: predictions

amplitude of density perturbations $A_s = \frac{\kappa^4 V_*}{24\pi^2 s}$ $rac{\kappa^4 V_*}{24\pi^2 \epsilon_*} = \frac{\kappa^2 H_*^2}{8\pi^2 \epsilon_*}$ $rac{1}{8\pi^2 \epsilon_*}$

spectral index $n_s = 1 + 2\eta_* - 6\epsilon_* \simeq 1 + 2\eta_*$

tensor – to – scalar ratio $r = 16\epsilon_*$

Planck '15 data : $\eta \simeq -0.02$, $A_s \simeq 2.2 \times 10^{-9}$, $N \gtrsim 50$

$$
\Rightarrow r \lesssim 10^{-4}, H_* \lesssim 10^{12} \text{ GeV}
$$

Question: can a 'nearby' minimum exist with a tiny $+ve$ vacuum energy? Answer: Yes in a 'weaker' sense: perturbative expansion [\[11\]](#page-10-0) valid for the Kähler potential but not for the slow-roll parameters generic V (not fine-tuned) $\Rightarrow 10^{-9} \lesssim r \lesssim 10^{-4}$, $10^{10} \lesssim H_* \lesssim 10^{12}$ GeV [\[30\]](#page-29-0)

1 SUSY breaking at m_{SUSY} ∼ TeV with an infinitesimal (tuneable) positive cosmological constant Villadoro-Zwirner '05

I.A.-Knoops, I.A.-Ghilencea-Knoops '14, I.A.-Knoops '15

2 Inflation connected or independent? [\[4\]](#page-3-0) [\[7\]](#page-6-0) [\[24\]](#page-23-0)

Content (besides $N = 1$ SUGRA): one vector V and one chiral multiplet S with a shift symmetry $S \rightarrow S - ic\omega \leftarrow$ transformation parameter String theory: compactification modulus or universal dilaton $s = 1/g^2 + ia \leftarrow$ dual to antisymmetric tensor Kähler potential K: function of $S + \overline{S}$ string theory: $K = -p \ln(S + \bar{S})$ Superpotential: constant or single exponential if R-symmetry $W = ae^{bS}$ $\int d^2$ $b < 0 \Rightarrow$ non perturbative can also be described by a generalized linear multiplet $[21]$

Scalar potential

$$
\mathcal{V}_F = a^2 e^{\frac{b}{7}} l^{p-2} \left\{ \frac{1}{p} (pl - b)^2 - 3l^2 \right\} \qquad l = 1/(s + \bar{s})
$$
 Planck units

- $b > 0 \Rightarrow$ SUSY local minimum in AdS space with $l = b/p$
- $b \le 0 \Rightarrow$ no minimum with $l > 0$ ($p \le 3$)

but interesting metastable SUSY breaking vacuum

when R-symmetry is gauged by V allowing a Fayet-Iliopoulos (FI) term:

$$
V_D = c^2 I (pl - b)^2
$$
 for gauge kinetic function $f(S) = S$

- $b > 0$: $V = V_F + V_D$ SUSY AdS minimum remains
- $b = 0$: SUSY breaking minimum in AdS ($p < 3$)
- $b < 0$: SUSY breaking minimum with tuneable cosmological constant Λ

$$
V = a^2(p-3)l^p + c^2p^2l^3
$$

can be obtained for $p = 2$ and l the string dilaton:

- all geometric moduli fixed by fluxes in a SUSY way
- D-term contribution : D-brane potential (uncancelled tension)
- F-term contribution : tree-level potential (away from criticality)

String realisation : framework of magnetised branes

minimisation and spectrum

Minimisation of the potential: $\mathsf{V}'=0,\ \mathsf{V}=\mathsf{\Lambda}$

In the limit $\Lambda \approx 0$ $(p = 2) \Rightarrow$ [\[26\]](#page-25-0)

 $b/l = \rho \approx -0.183268 \Rightarrow \langle l \rangle = b/\rho$

$$
\frac{a^2}{bc^2} = 2 \frac{e^{-\rho}}{\rho} \frac{(2-\rho)^2}{2+4\rho - \rho^2} + \mathcal{O}(\Lambda) \approx -50.6602 \quad \Rightarrow c \propto a
$$

Physical spectrum:

massive dilaton, $U(1)$ gauge field, Majorana fermion, gravitino

All masses of order $m_{3/2}\approx e^{\rho/2}$ la \leftarrow TeV scale

Properties and generalizations

- • Metastability of the ground state: extremely long lived $l \approx 0.02$ (GUT value α _{GUT} /2) $m_{3/2} \sim \mathcal{O}(TeV)$ \Rightarrow decay rate $\Gamma \sim e^{-\mathcal{B}}$ with $B \approx 10^{300}$
- Add visible sector (MSSM) preserving the same vacuum matter fields ϕ neutral under R-symmetry

$$
K = -2\ln(S + \bar{S}) + \phi^{\dagger} \phi \quad ; \quad W = (a + W_{MSSM})e^{bS}
$$

 \Rightarrow soft scalar masses non-tachyonic of order $m_{3/2}$ (gravity mediation)

 \bullet Toy model classically equivalent to $[16]$

 $K = -p \ln(S + \bar{S}) + b(S + \bar{S})$; $W = a$ with V ordinary $U(1)$

Dilaton shift can be identified with $B-L \supset$ matter parity $(-)^{B-L}$

Properties and generalizations

- R-charged fields needed for anomaly cancellation
- A simple (anomaly free) variation: $f = 1$ and $p = 1$ tuning still possible but scalar masses of neutral matter tachyonic possible solution: add a new field Z in the 'hidden' SUSY sector \Rightarrow one extra parameter
- alternatively: add an S-dependent factor in Matter kinetic terms $K = -\ln(S + \bar{S}) + (S + \bar{S})^{-\nu} \sum \Phi \bar{\Phi}$ for $\nu \gtrsim 2.5$

or the $B - L$ unit charge of SM particles \Rightarrow similar phenomenology

- **•** distinct features from other models of SUSY breaking and mediation
- gaugino masses at the quantum level

 \Rightarrow suppressed compared to scalar masses and A-terms

Typical spectrum

The masses of sbottom squark (yellow), stop (black), gluino (red), lightest chargino (green) and lightest neutralino (blue) as a function of the gravitino mass. The mass of the lightest neutralino varies between \sim 40 and 150 GeV $_{[15]}$ $_{[15]}$ $_{[15]}$

Case 2 example: toy model of SUSY breaking I.A.-Chatrabhuti-Isono-Knoops '16

- Can the dilaton be the inflaton in the simple model of SUSY breaking based on a gauged shift symmetry?
- the only physical scalar left over, partner (partly) of the goldstino partly because of a D-term auxiliary component
- Same potential cannot satisfy the slow roll condition $|\eta| = |V''/V| << 1$ with the dilaton rolling towards the Standard Model minimum
- \Rightarrow need to create an appropriate plateau around the maximum of V $_{[20]}$ $_{[20]}$ $_{[20]}$ without destroying the properties of the SM minimum
- \Rightarrow study possible corrections to the Kähler potential

only possibility compatible with the gauged shift symmetry

Extensions of the SUSY breaking model

Parametrize the general correction to the Kähler potential:

$$
K = -p\kappa^{-2} \log \left(s + \bar{s} + \frac{\xi}{b} F(s + \bar{s}) \right) + \kappa^{-2} b(s + \bar{s})
$$

\n
$$
W = \kappa^{-3} a, \quad f(s) = \gamma + \beta s
$$

\n
$$
\mathcal{P} = \kappa^{-2} c \left(b - p \frac{1 + \frac{\xi}{b} F'}{s + \bar{s} + \frac{\xi}{b} F} \right)
$$

Three types of possible corrections:

- perturbative: $F \sim (s + \bar{s})^{-n}$, $n \ge 0$
- non-perturbative D-brane instantons: $F \sim e^{-\delta(s+\bar{s})}$, $\delta > 0$
- non-perturbative NS5-brane instantons: $F \sim e^{-\delta(s+\bar{s})^2}$, $\delta > 0$

Only the last can lead to slow-roll conditions with sufficient inflation

Slow-roll inflation

 ${\cal F}=\xi e^{\alpha b^2\phi^2}$ with $\phi=s+\bar s=1/l\Rightarrow$ two extra parameters $\alpha< 0,\,\xi$ they control the shape of the potential

slow-roll conditions: $\epsilon = 1/2(V'/V)^2 << 1$, $|\eta| = |V''/V| << 1$

 \Rightarrow allowed regions of the parameter space with $|\xi|$ small

additional independant parameters: a, c, b

SM minimum with tuneable cosmological constant $\Lambda: V'=0, V=\Lambda\approx 0$

 $\xi=0 \Rightarrow b\phi_{min}=\rho_0$, $\frac{a^2}{bc^2}=\lambda_0$ with ρ_0,λ_0 calculable constants $_{[19]}$ $_{[19]}$ $_{[19]}$

b controls ϕ_{min} ∼ $1/g_s$ choose it of order 10

tuning determines a in terms of c overall scale of the potential

 $\xi \neq 0 \Rightarrow \rho_0, \lambda_0$ become functions $I(\xi, \alpha), \lambda(\xi, \alpha)$

numerical analysis \Rightarrow mild dependence

Fit Planck '15 data and predictions

 $p = 1$: similar analysis \Rightarrow

 $\phi_* = 64.53, \xi = 0.30, \alpha = -0.78, b = -0.023, c = 10^{-13}$

 ${\sf SM}$ minimum: $\langle \phi \rangle \approx$ 21.53, $\langle m_{3/2} \rangle = 18.36$ TeV, $\langle M_{A_\mu} \rangle =$ 36.18 TeV During inflation:

$$
H_* = \kappa \sqrt{\mathcal{V}_*/3} = 5.09 \text{ TeV}, \, \, m_{3/2}^* = 4.72 \text{ TeV}, \, \, M_{A_\mu}^* = 6.78 \text{ TeV}
$$

Low energy spectrum essentially the same with $\xi = 0$:

$$
m_0^2 = m_{3/2}^2 [-2 + C],
$$
 $A_0 = m_{3/2} C,$ $B_0 = A_0 - m_{3/2}$

 ${\cal C}=1.53$ vs at $\xi=0{:}\,\,{\cal C}_0=1.52,\, m_{3/2}^0=17.27,\,$ although $\langle\phi\rangle_0\approx 9.96$ [\[11\]](#page-10-0)

Challenge of scales: at least three very different (besides M_{Planck}) electroweak, dark energy, inflation, SUSY?

their origins may be connected or independent

 $SUSY$ with infinitesimal (tuneable) $+ve$ cosmological constant

- **•** interesting framework for model building incorporating dark energy
- identify inflaton with goldstino superpartner inflation at the SUSY breaking scale (TeV?)

General class of models with inflation from SUSY breaking:

(gauged) R-symmetry restored (case 1) or broken (case 2) during inflation small field, avoids the η -problem, no (pseudo) scalar companion